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Infrared Energy Conversion in Plasmonic Fields at Two-Dimensional Semiconductors

Gregory Thomas Forcherio
University of Arkansas, Fayetteville

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Infrared Energy Conversion in Plasmonic Fields at Two-Dimensional Semiconductors

A dissertation submitted in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy in Microelectronics-Photonics

by

Gregory Thomas Forcherio
Southeast Missouri State University
Bachelor of Science in Engineering Physics and Mathematics, 2012
University of Arkansas
Master of Science in Microelectronics-Photonics, 2014

May 2017
University of Arkansas

This dissertation is approved for recommendation to the Graduate Council.

Dr. D. Keith Roper
Dissertation Director

Dr. Gregory J. Salamo
Committee Member

Dr. Surendra P. Singh
Committee Member

Dr. Hameed A. Naseem
Committee Member

Dr. Rick L. Wise
Ex-Officio Member

The following signatories attest that all software used in this dissertation was legally licensed for use by Mr. Gregory T. Forcherio for research purposes and publication.

Mr. Gregory T. Forcherio
Student

Dr. D. Keith Roper
Dissertation Director

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Dr. Rick L. Wise
Program Director

Dr. D. Keith Roper
Dissertation Director

ABSTRACT

Conversion of infrared energy within plasmonic fields at two-dimensional, semiconductive transition metal dichalcogenides (TMD) through plasmonic hot electron transport and nonlinear frequency mixing has important implications in next-generation optoelectronics. Drude-Lorentz theory and approximate discrete dipole (DDA) solutions to Maxwell's equations guided metal nanoantenna design towards strong infrared localized surface plasmon resonance (LSPR). Excitation and damping dynamics of LSPR in heterostructures of noble metal nanoantennas and molybdenum- or tungsten-disulfide (MoS_2 ; WS_2) monolayers were examined by parallel synthesis of (i) DDA electrodynamic simulations and (ii) near-field electron energy loss (EELS) and far-field optical transmission UV-vis spectroscopic measurements. Susceptibility to second-order nonlinear frequency conversion processes, $\chi^{(2)}$, for monolayer MoS_2 and WS_2 were measured to be $660 \pm 130 \text{ pm V}^{-1}$ and $280 \pm 18 \text{ pm V}^{-1}$, respectively, by Hyper Rayleigh Scattering. Femtosecond conversion of resonant irradiation to injection of plasmonic hot electrons into the TMD were measured in EELS at a maximum of $11 \pm 5\%$ quantum efficiency for an optimized physicochemical Au- WS_2 junction. Measured nonlinear second harmonic generation (SHG) from a ca. $1 \mu\text{m}$ MoS_2 monolayer was enhanced 17-84% by local electric field augmentation from a single 150 nm Au nanoshell to a conversion efficiency of up to $0.023\% \text{ W}^{-1}$. Capacitive coupling between nanoshells arranged into dimers further augmented SHG activity from MoS_2 . New theoretical and experimental insights into energy conversion interactions between coupled plasmonic and excitonic materials spanning the linear and nonlinear optical regimes were established towards their implementation as an optoelectronic platform.

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DEDICATION

I dedicate this dissertation to my precious daughter, Emma, who makes my work more meaningful with each smile.

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LIST OF NOMENCLATURE

Acronyms & Abbreviations

| | |
|--------|--|
| Al | Aluminum |
| Al:ZnO | Aluminum-Doped Zinc Oxide |
| AFM | Atomic Force Microscopy |
| BSE | Bethe-Salpeter Exciton Method |
| BEM | Boundary Element Method |
| CCD | Charge-Coupled Device |
| CVD | Chemical Vapor Deposition |
| CDA | Coupled Dipole Approximation |
| CLR | Coupled Lattice Resonance |
| CMOS | Complementary Metal-Oxide Semiconductor |
| Cu | Copper |
| DFT | Density Functional Theory |
| DMT | Density Matrix Theory |
| DDA | Discrete Dipole Approximation |
| DFG | Difference Frequency Generation |
| DLS | Dynamic Light Scattering |
| EELS | Electron Energy Loss Spectroscopy |
| EFTEM | Energy-Filtered Transmission Electron Microscopy |
| ELDOS | Electromagnetic Local Density of States |
| FFT | Fast-Fourier Transform |
| FDTD | Finite Difference Time Domain |
| FEM | Finite Element Method |
| FWHM | Full Width at Half Maximum |

| | |
|-------------------|---|
| Ga:ZnO | Gallium-Doped Zinc Oxide |
| GIF | GATAN Post-Column Imaging Filter |
| Au | Gold |
| AuCl ₃ | Gold Chloride |
| AuNA | Gold Nanoantenna |
| AuNS | Gold Nanosphere or Nanoshell |
| HAADF | High-Angle Annular Dark-Field |
| HRS | Hyper Rayleigh Scattering |
| InSb | Indium Antimonide |
| InAs | Indium Arsenide |
| ITO | Indium Tin Oxide |
| LSP | Localized Surface Plasmon |
| LSPR | Localized Surface Plasmon Resonance |
| MoS ₂ | Molybdenum Disulfide |
| MoSe ₂ | Molybdenum Diselenide |
| MoO ₃ | Molybdenum Trioxide |
| Nd:YAG | Neodymium-doped Yttrium Aluminum Garnet |
| NiSi | Nickel Silicide |
| 1D | One-Dimensional |
| OR | Optical Rectification |
| pNA | Para-Nitroaniline |
| PL | Photoluminescence |
| PMT | Photomultiplier Tube |
| PVP | Poly(vinylpyrrolidone) |
| SEM | Scanning Electron Microscopy |

| | |
|------------------|---|
| Ag | Silver |
| SFG | Sum Frequency Generation |
| SH | Second Harmonic |
| SHG | Second Harmonic Generation |
| SiO _x | Silica |
| SiO ₂ | Silicon Dioxide |
| STEM | Scanning Transmission Electron Microscopy |
| TiN | Titanium Nitride |
| TiSi | Titanium Silicide |
| TEM | Transmission Electron Microscopy |
| TMD | Transition Metal Dichalcogenide |
| WS ₂ | Tungsten Disulfide |
| WSe ₂ | Tungsten Diselenide |
| 2D | Two-Dimensional |
| UV-vis | Ultraviolet-visible |
| XPS | X-Ray Photoelectron Spectroscopy |
| ZnO | Zinc Oxide |
| ZrN | Zirconium Nitride |

Symbols

| | |
|----------------|---|
| σ_{abs} | Absorption Cross Section [m ²] |
| σ_{TMD} | Beer-Lambert Absorption Correction Factor for TMD [m ³] |
| N | Carrier Concentration [m ⁻³] |
| C | Concentration [m ⁻³] |
| $p^{(n)}$ | Dipole Moment Polarization [C m] |
| A | Dipole-Dipole Interaction Matrix [V m C ⁻¹] |

| | |
|---------------------------------|---|
| \hbar | Dirac Constant [eV s or J s] |
| γ | Drude Damping Rate [eV] |
| m_o | Effective Electron Mass [g] |
| α_{eff} | Effective Polarizability [C m ² V ⁻¹] |
| E | Electric Field [V m ⁻¹] |
| F | Electric Field Enhancement Factor [unitless] |
| ϵ | Electric Permittivity [unitless] |
| $\chi^{(n)}$ | Electric Susceptibility [$n = 1$, unitless; $n = 2$, m V ⁻¹ ; $n = 2$, m ² V ⁻² ...] |
| $q\chi$ | Electron Affinity [eV] |
| e | Electron Charge [C] |
| m | Electron Mass [g] |
| G | Experimental Constant [unitless] |
| σ_{ext} | Extinction Cross Section [m ²] |
| ω & λ | Frequency or Wavelength of Light [m, eV, or s ⁻¹] |
| Γ | Full Width at Half Maximum [m or eV] |
| β | Hyperpolarizability [m ⁴ V ⁻¹ or esu] |
| α_{TMD} & α_{pNA} | Hyper Rayleigh Scattering vs. Species Concentration Slope [a.u. m ³] |
| I | Intensity [W m ⁻² or a.u.] |
| d | Inter-Atomic or Inter-Dipole Separation [m] |
| L | Length of Nonlinear Crystal [m] |
| L_{TMD} | Mean Length [m] |
| N_{TMD} | Mean Layer Number [unitless] |
| X | Measured Second Harmonic Generation Enhancement Factor [unitless] |
| $q\phi$ | Metal Work Function [eV] |
| η_{norm} | Normalized Second Harmonic Conversion Efficiency [W ⁻¹] |
| ϵ_o | Permittivity of Free Space [F m ⁻¹] |
| ω_p | Plasma Frequency [m, eV, or s ⁻¹] |
| α | Polarizability [C m ² V ⁻¹] |
| $P^{(n)}$ | Polarization Density [C m ⁻²] |
| η | Quantum Efficiency of Plasmon Damping Mechanism [unitless] |
| n | Refractive Index [unitless] |
| S | Retarded Dipole Sum [V C ⁻¹ m ⁻²] |

| | |
|------------------|--|
| σ_{sca} | Scattering Cross Section [m^2] |
| $q\phi_{SB}$ | Schottky Barrier [eV] |
| $\eta_{2\omega}$ | Second Harmonic Conversion Efficiency [unitless] |
| c | Speed of Light [m s^{-1}] |
| T_2 | Surface Plasmon Dephasing Time [s] |
| V | Volume of Nanoparticle [m^3] |
| k | Wave Vector [m^{-1}] |

CHAPTER 1

INTRODUCTION

Advancements in solar photovoltaic, wind turbine, geothermal, and biofuel technologies have decreased proportional fossil fuel dependence by 10% over the past half century.¹ Policies enacted by the International Energy Agency aim for a 160 gigatonne reduction in carbon dioxide emissions with 33% capacity increase by 2035 to accommodate a population nearing 9 billion.¹⁻³ Despite progress of alternative energies, nearly 60% of generated energy is lost to heat.^{4,5} Recovery of waste heat potentiates an emission-free 10 terawatt reduction in energy demand,^{5,6} motivating ample research in thermoelectric materials and thermophotovoltaics since the 1950s.⁷⁻¹⁰ However, efficiencies and balance-of-system costs inherent to these methods have limited their implementation to niche markets undeterred by high investment capital.^{4,8,11} Herein, two alternative schemes unique to an emerging class of materials which could allow conversion, and utilization, of radiative waste heat through optical resonances are studied.

1.1 Motivation

In addition to decarbonization of energy resources, the U.S. Department of Energy advocates decreasing device power consumption is essential to a sustainable future.¹ Energy consumption and processing speed of electronic transistors improved with geometric downscaling according to Moore's Law for over 40 years. However, progress today is limited by ohmic heat confined at sub-50 nm transistor nodes.¹² Dissipation traditionally relies on forced convection, conduction, and/or evaporation. Dissipation by radiation could provide additional, parallel rejection processes with rapid dynamics not requiring additional equipment or contact.

Recycling infrared photons radiated by electronic components provides opportunities to enhance heat rejection and integrate electro-optical interconnects into the next-generation of optoelectronic devices. Optical interconnection between electronic transistors avoids ohmic losses at 10^3 x higher data densities while offering additional processing capabilities, such as wavelength-division multiplexing.^{12,13} Interconnects comprise 80% of total microprocessor energy consumption.¹³ Inefficient emission from bulk silicon in the visible to near-infrared spectrum and size of existing optic-electronic transition components has precluded hybrid electronic and optic operations.¹²⁻¹⁴ Concomitant conversion of heat into electrical signals beyond the Seebeck effect⁸ could augment rejection and diversify signal functions. A material with engineered optical resonance characteristics to enable conversion of energy between frequencies or signal modality (i.e., electric or optic) could provide a new optoelectronic material platform.

1.2 Hypothesis

Resonant photon-electron interactions in nanomaterials could support passive infrared energy conversion mechanisms for optoelectronics beyond conventional thermodynamic paths:

- conversion of infrared energy into hot carriers
- nonlinear frequency conversion toward higher energies

1.3 Hot Carrier Generation

Optical resonances of sub-wavelength metal architectures, called nanoantennas, generate energetically hot electrons through plasmon excitation. Incident electromagnetism at the energy which a nanoantenna is intrinsically resonant (determined by structural morphology and elemental composition) induces collective oscillations of its free electrons, known as a localized surface

plasmon resonance (LSPR).^{12,15} Relaxation, or damping, of the LSPR initiates transfer of its energy into hot electron-hole pairs in the metal through Landau damping over 1-100 fs.¹⁶ “Hot” attribution refers to the energy of the carrier exceeding its thermal energy (on order of 10^{-2} eV).

Nonradiative relaxation of plasmonic hot electrons traditionally offers two pathways: (i) phonon scattering into the metal as the carriers fall back to the Fermi level and (ii) interfacial interactions (e.g., entrapment into defects).¹⁷⁻²¹ A semiconductor in near proximity to the metal nanoantenna can serve as an acceptor for hot electrons, thus offering an additional relaxation pathway.^{16,22,23} Figure 1.1 shows an energy band diagram for a metal-semiconductor interface. Conduction band of the semiconductor may accept plasmonic hot electrons when their energy exceeds the metal-semiconductor Schottky barrier, $q\phi_{SB}$.²² The Schottky barrier is equal to the difference between the metal work function, $q\phi$, and semiconductor electron affinity, $q\chi$, viz.²⁴

$$q\phi_{SB} = q\phi - q\chi . \quad (\text{Equation 1.1})$$

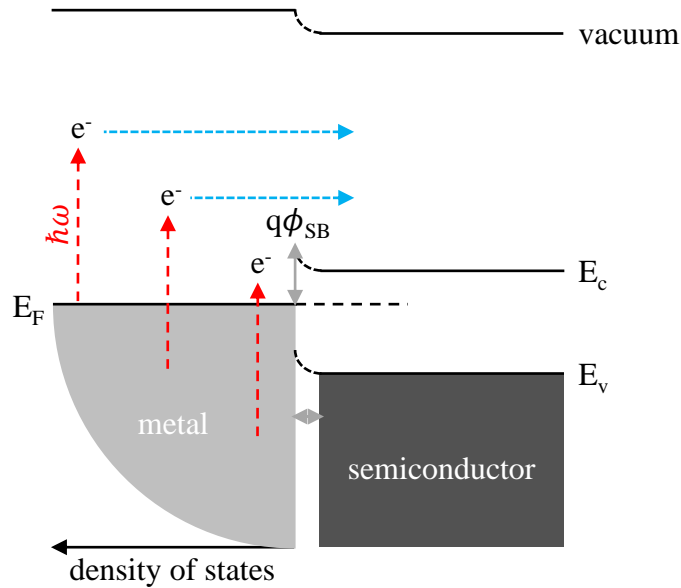


Figure 1.1: Energy band diagram of an unbiased metal-semiconductor junction at thermal equilibrium, signifying contact between a metal nanoantenna and an adjacent semiconductor. Resonant plasmon excitation, of energy $\hbar\omega$, on the metal nanoantenna generates hot electrons, which may transfer into the semiconductor if their energy exceeds the Schottky barrier ($q\phi_{SB}$).

Conversion of infrared energy exceeding the Schottky barrier through transduction into plasmonic hot electrons followed by transport into a semiconductor represents one possible heat rejection mechanism beyond conventional thermodynamic paths. Within the context of optoelectronic devices, radiated waste heat could be converted into electric signals. Reports estimate transport efficiency of plasmonic hot electrons from metals to titanium dioxide, aluminum-doped zinc oxide, or cadmium sulfide at 2-10%.²⁵⁻²⁷ Radiative recombination of hot electrons transported into a semiconductor quantum well has been proposed as an energy upconversion scheme, with theoretical efficiency as high as 25% for 5 nm silver nanocubes.²⁸ In such a scheme, recombination across the semiconductor bandgap allows re-radiation at a higher energy than the initial photon exciting the plasmonic hot electron (energy as low as $q\phi_{SB}$). Photocurrent from plasmonic hot electrons has also been utilized in photodetector schemes²⁹ and catalysis processes, such as the hydrogen evolution reaction.³⁰

1.4 Nonlinear Optical Frequency Mixing

The optical behavior of a material can be described by its polarization in response to an incident electromagnetic field. Macroscopic polarization density, \mathbf{P} , of a material is driven by applied electric fields, \mathbf{E} , with strength given by the product of free space permittivity, ϵ_o and its intrinsic electric susceptibility, χ .³¹ However, a more rigorous description of electric polarization reveals that total polarization is a sum of distinct n^{th} -order polarizations where $n \in \mathbb{N}$, viz.

$$\begin{aligned} \mathbf{P} &= \sum_{n=1}^N \mathbf{P}^{(n)} = \epsilon_o \sum_{n=1}^N \chi^{(n)} \mathbf{E}^n \\ &= \epsilon_o (\chi \mathbf{E} + \chi^{(2)} \mathbf{E}^2 + \chi^{(3)} \mathbf{E}^3 + \dots + \chi^{(N)} \mathbf{E}^N) \end{aligned} \quad (\text{Equation 1.2})$$

and $\chi^{(n)}$ are the n^{th} -order electric susceptibilities,^{32,33} assuming a dispersionless material. Polarization of the first-order (i.e., $n = 1$) is referred to as the linear optical response. Higher order polarizations which do not scale linearly with the applied electric field (i.e., $n \neq 1$) are responsible for nonlinear optical behavior. Time-varying nonlinear polarization of charge creates new frequency components in the radiated electromagnetic field, referred to as frequency mixing.³³ This work focuses on frequency mixing phenomena arising from the 2nd-order nonlinear response as a possible radiative heat rejection mechanism beyond conventional thermodynamic paths.

1.4.1 Electrodynamic Theory

Consider the simplistic case of simultaneous irradiation of a nonlinear material with two different frequencies of light. Time-variant second-order nonlinear polarization in response to the excitation electric fields (given by $\mathbf{E}(t) = E_1 e^{-i\omega_1 t} + E_2 e^{-i\omega_2 t} + c. c.$) takes the form

$$\begin{aligned} \mathbf{P}^{(2)}(t) = \epsilon_0 \chi^{(2)} [& E_1^2 e^{-i2\omega_1 t} + E_2^2 e^{-i2\omega_2 t} + 2E_1 E_2 e^{-i(\omega_1 + \omega_2)t} \\ & + 2E_1 E_2^* e^{-i(\omega_1 - \omega_2)t} + (E_1 E_1^* + E_2 E_2^*) e^0 + c. c.] \end{aligned} \quad (\text{Equation 1.3})$$

with dipole oscillation frequencies at $2\omega_1, 2\omega_2, \omega_1 + \omega_2, \omega_1 - \omega_2$, and 0. Derivation of the wave equation from Faraday's and Ampere's Laws (assuming nonmagnetic material with no free currents) for optically nonlinear materials shows each frequency component in $\mathbf{P}^{(2)}$ acts as a source of electromagnetic radiation, *viz.*³³

$$\nabla^2 \mathbf{E} - \frac{n^2}{c^2} \frac{\partial^2 \mathbf{E}}{\partial t^2} = \frac{1}{\epsilon_0 c^2} \frac{\partial^2 \mathbf{P}^{(2)}}{\partial t^2} \quad (\text{Equation 1.4})$$

where n is the refractive index of the material and c is the speed of light. Larmor's theorem states that electromagnetic radiation emitted from a material originates from accelerated charges polarized within the material,³¹ consistent with the $\partial^2 \mathbf{P}^{(2)} / \partial t^2$ term in Equation 1.4.

Intensity of nonlinear radiation from the excited material is dependent on the collective phase for each oscillating dipole relative to phase of the excitation fields as they propagate through the material.^{32,33} If the excitation fields are given by $\mathbf{E}(t) = E_1 e^{-i(k_1 x - \omega_1 t)} + E_2 e^{-i(k_2 x - \omega_2 t)} + c.c.$ at some point x in the material (along the propagation vector), then observed intensity of the new frequency component ω_3 depends on the phase condition $k_3 = k_1 + k_2$. Intensity of the nonlinearly-generated radiation at ω_3 is directly proportional to the phase coherence Δk via³³

$$I_3 \propto [\chi^{(2)}]^2 I_1 I_2 L^2 \text{sinc}^2 \left(\frac{\Delta k x}{2} \right) \quad (\text{Equation 1.5})$$

where I_1 and I_2 are the excitation intensities. Under this notation, the quantity $2/\Delta k$ is defined as the phase coherence length. After integrating Equation 1.5 over the length of the material, L , the characteristic length for constructive coherence leading to maximum I_3 is given by

$$L_{coh} \equiv \frac{2}{\Delta k} = \frac{2c}{n_1 \omega_1 + n_2 \omega_2 - n_3 \omega_3} . \quad (\text{Equation 1.6})$$

In the case of frequency doubling ($\omega_3 = 2\omega_1$ or $2\omega_2$), the characteristic L_{coh} simplifies to:

$$L_{coh} = \frac{\lambda_\omega}{2\pi(n_\omega - n_{2\omega})} \quad (\text{Equation 1.7})$$

which highlights utilization of nanomaterials for nonlinear optics. Phase matching can be neglected for materials with dimension beneath the wavelength scale, e.g., ca. 1-10 μm for infrared irradiation, since the phase of radiating dipoles are always coherent. In the case of infrared irradiation, L_{coh} is generally on the order of microns.

1.4.2 Second-Order Frequency Conversion Processes

Second-order nonlinear interactions between a material and light intrinsically results in new frequency sources radiated from the material, called frequency mixing. The processes of creating radiation at $2\omega_1$, $2\omega_2$, $\omega_1 + \omega_2$, $\omega_1 - \omega_2$, and 0 frequencies are referred to as nonlinear second harmonic generation (SHG), sum frequency generation (SFG), difference frequency

generation (DFG), and optical rectification (OR), respectively.^{32,33} Each process is shown schematically in Figure 1.2. The energy of two distinct photons combine and re-radiate as a single photon in SHG and SFG. Energy of a single high frequency photon can re-radiate as two photons in DFG with energy-conserved components of (i) the incident lower frequency (referred to as optical parametric amplification of ω_2) and (ii) the difference frequency. A static electric field across the material is created in OR.

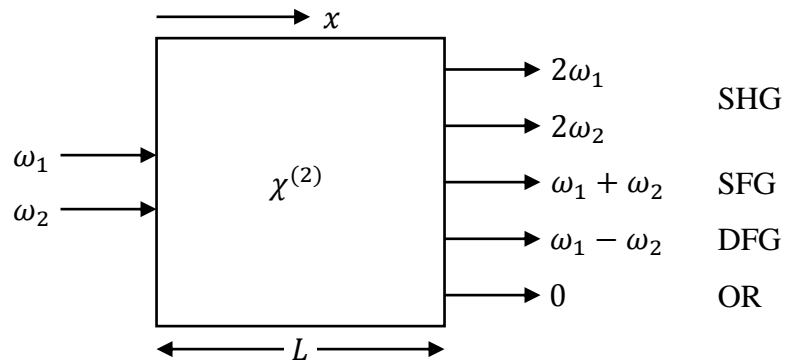


Figure 1.2: Schematic representation of frequency mixing processes arising from second-order nonlinear interaction of a material with two excitation frequencies, ω_1 and ω_2 .

Nonlinear frequency mixing was first observed in 1961 by Franken *et al.* using quartz to generate the second harmonic (SH) of a ruby laser.³⁴ Underlying electrodynamic relations for SHG and other nonlinear processes were developed by Bloembergen *et al.*³⁵ in 1962 following successive discoveries of SFG, DFG, and OR in potassium dihydrogen phosphate crystals.^{36,37} Frequency conversion processes have since become a foundation for fiber-based telecommunication systems, wavelength-tunable lasers,³⁸ materials characterization,³⁹ and advanced microscopy⁴⁰ and tomography⁴¹ techniques for examining biological entities.

Observation of second-order frequency mixing phenomena is limited to materials whose intrinsic crystal structure is non-centrosymmetric; in other words, the time-averaged nonlinear polarization is zero for centrosymmetric materials. Nonlinear atomic polarization $\mathbf{P}^{(2)}$ of a

centrosymmetric crystal generates opposing dipole moments equal in magnitude as the excitation electric field oscillates (i.e., from $+\mathbf{E}$ to $-\mathbf{E}$) with time. Hence,

$$-\mathbf{P}^{(2)} = \epsilon_o \chi^{(2)} [-\mathbf{E}]^2 = \epsilon_o \chi^{(2)} \mathbf{E}^2 \quad (\text{Equation 1.8})$$

which is true only if the material's intrinsic $\chi^{(2)}$ along some i , j , and k crystalline orientation is equal to 0, since $\mathbf{P}^{(2)}$ and \mathbf{E} are finite and ϵ_o is a constant. Therefore, the crystal structure of a material must be non-centrosymmetric to observe second-order nonlinear effects. Conventional nonlinear crystals exhibit a $\chi^{(2)}$ up to ca. 400 pm V⁻¹, but typically less than 10 pm V⁻¹.³³ It is noted however, that a finite nonlinear signal originates from surface contributions in all materials, regardless of crystal structure, where centrosymmetry is broken at interfaces and lattice defects.³⁹

1.5 Research Objective

This work examined conversion of infrared energy from two-dimensional transition metal dichalcogenides (TMD)⁴²⁻⁴⁴ within plasmonic fields of nanoantennas^{12,45,46} via two mechanisms: (i) plasmonic hot electron transport and (ii) enhanced second harmonic generation (SHG). Monolayer TMD were renowned for their extraordinary SHG activity⁴⁷ arising from their reported $\chi^{(2)}$ up to 10⁴ pm V⁻¹.⁴⁸⁻⁵⁴ Nanoantennas augment local electric field 10-100x by confining incident energy into surface plasmons,^{12,55} and thus offered higher power densities for nonlinear phenomena from TMD. Plasmonic hot electron interactions had been inferred in nanoantenna-TMD heterostructure devices,⁵⁶⁻⁵⁸ but remained to be quantified. Overall, little was known about the electromagnetic interplay between TMD and nanoantennas. Rapid experimental progress since initial work in 2013 had outpaced development of descriptive frameworks by which to interpret experimental results. This work provided new insights into the resonant energetics and damping between coupled plasmonic and excitonic materials across the linear and nonlinear optical regimes.

CHAPTER 2

SURFACE PLASMON PHOTONICS

Electromagnetic energy may be concentrated to sub-wavelength scales at augmented field intensities by nanoantennas in the form of coherent electron oscillations, called localized surface plasmons.^{12,15} Nanoantennas are nanoscale architectures whose morphology and arrangement are engineered to manipulate light,^{59,60} sometimes in ways that defy materials found in nature.^{61,62} This chapter surveys the electrodynamical framework, materials, and architectural parameters which guided nanoantenna design for infrared energy conversion processes.

2.1 Surface Plasmon Excitation

Subwavelength structures, called nanoantennas, allow manipulation of electromagnetic energy through their ability to support plasmons.⁴⁶ Plasmons are quasi-particles of electromagnetically-induced coherent oscillations of electron gas in condensed matter. The structural morphology, elemental composition, physical arrangement, and environment of nanoantennas determines their absorption and scattering of electromagnetic energy.

2.1.1 Localized Surface Plasmon Resonance

Coherent electron gas oscillations confined to the surface of a nanoantenna are referred to as localized surface plasmons (LSP).^{15,63} The energy, or frequency, at which a LSP is induced on a given nanoantenna is referred to as the localized surface plasmon resonance (LSPR). Figure 2.1 schematically depicts dipole LSPR excitation on a subwavelength sphere, explored initially by Gustav Mie in the early 20th century.⁶⁴ Expanding the radial dimension of the sphere accommodates excitation of multi-pole LSPR, such as a quadrupole, hexapole, etc. due to phase

retardation across the sphere.⁶⁵ The LSPR is intrinsically a function of size,^{66,67} shape,^{63,66,68,69} and elemental composition^{70–72} of a nanoantenna. The LSPR is extrinsically dependent on dielectric screening in media local to the nanoantenna.^{59,73–75}

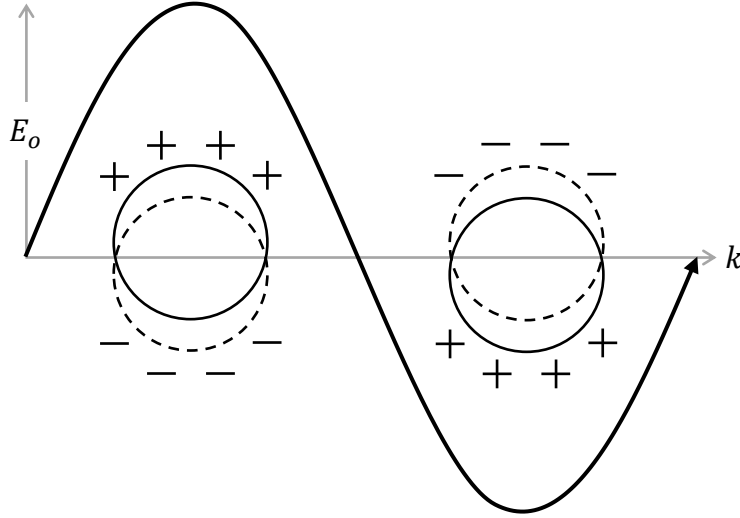


Figure 2.1: Electromagnetic wave propagating in free space inducing a dipolar localized surface plasmon on a subwavelength sphere. E_o is the electric field amplitude and k is the wave vector.

2.1.2 Fano Resonant Diffractive Coupling

Periodically arranging nanoantennas into regular lattices at constants near or above their LSPR wavelength results in Fano resonant coupling between LSP and diffractive modes, causing emergence of a coupled lattice resonance (CLR).^{76–78} In-phase diffractive scattering induces coherent plasmonic oscillation across the lattice with enhanced net electric field strength, provided that the diffraction length falls within the intrinsic polarizability envelope of the nanoantennas.⁷⁹ Figure 2.2 schematically depicts CLR excitation for (a) rectilinear and (b) hexagonal lattice arrangements of nanoantennas. Rectilinear lattices consist of nodes at regular intervals in cardinal directions (d_y and d_x , respectively). Square lattices (i.e., $d_y = d_x$) are a subset of rectilinearity that exhibit an isotropic response to \hat{x} and \hat{y} polarization due to $\pi/2$ rotational symmetry.⁸⁰ Hexagonal lattices exhibiting $\pi/6$ rotational symmetry with an anisotropic polarization response.

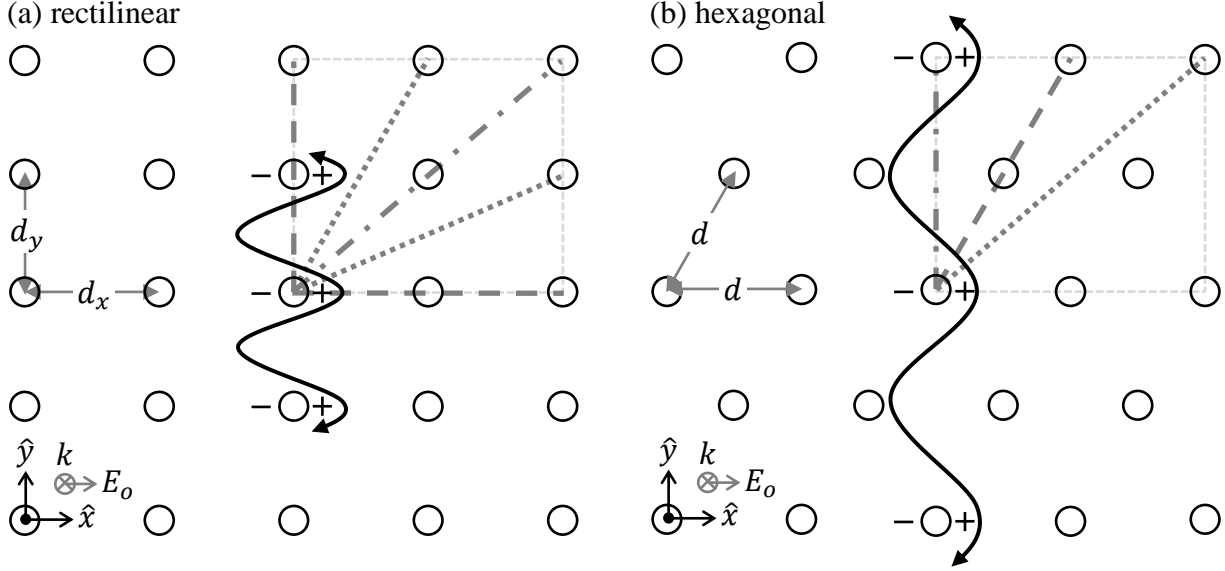


Figure 2.2: Schematic representations of CLR excitation in (a) rectilinear and (b) hexagonal lattices of nanoantennas. Grid in upper right quadrant of each lattice type coordinates inter-node diffraction at the lattice constant (dashed), primary diagonal (dot-dashed), and off-axis positions (dotted) relative to the center node.

Two primary plasmon resonant modes are supported by diffractive-coupling nanoantenna lattices: (i) the dipolar surface plasmon and (ii) the CLR. The higher energy dipolar surface plasmon originates from the LSP, but is blue-shifted by tens of nanometers⁸¹ via destructive Fano interference spanning between the inherent LSPR and lattice constant lengths. Diffractive coupling is intrinsically a function of the lattice constant and incident polarization^{65,80} and extrinsically a function of environment local to the lattice.^{65,75,81,82} Fano resonances based upon near-field interactions between surface plasmons on adjacent, nearby nanoantennas^{77,78,83–86} were not considered in this work.

2.2 Computational Models

Optics of nanoantenna systems may be modeled by finite difference time domain (FDTD),⁸⁷ boundary/finite element methods (BEM/FEM), T-matrix,⁸⁸ and coupled/discrete dipole approximations (CDA/DDA) to Maxwell's equations.^{74,89,90} Discretization of time and space in FDTD, FEM, and T-matrix offer precise numerical solutions to Maxwell's equations at significant

computational expense. Computational memory advantages of BEM are limited to nanoantennas whose volume may be approximated as a one-dimensional (1D) surface contour,⁹¹ e.g., nanodiscs. DDA and CDA together offer reduced computational time,^{92,93} elegant consideration of inhomogenous local environments,⁸² and the unique flexibility to describe fabricated nanoantennas with distorted, complex morphologies.⁹⁴ This section describes utilization of CDA and DDA to guide design and describe optical behavior of nanoantennas.

2.2.1 Coupled Dipole Approximation

The CDA solves Maxwell's equations for two-dimensional (2D) nanoantenna lattices by treating each constituent nanoantenna as a point dipole with polarizability, α , characteristic of its size, morphology, and elemental composition.^{74,95,96} Dipole polarization induced on each nanoantenna, \mathbf{p} , in response to an applied electric excitation field, \mathbf{E}_o , is calculated according to its α , *viz.*

$$\mathbf{p} = \frac{\alpha \mathbf{E}_o}{1 - \alpha S} \quad (\text{Equation 2.1})$$

where S represents the retarded dipole sum, which accounts for near-field and far-field dipole radiation from adjacent nanoantennas comprising the lattice.⁷⁴ At lattice constants comparable to the excitation wavelength, accrued far-field diffraction between lattice nodes dominate S . Optical extinction of an orthogonally incident wavevector, k , arises from the degree to which polarization of the lattice is out of phase with the incident field (i.e., \mathbf{p}/\mathbf{E}_o). Resultant extinction may be expressed by

$$\sigma_{ext} = 4\pi k \Im \left(\frac{1}{1/\alpha - S} \right). \quad (\text{Equation 2.2})$$

The CDA is limited to situations for which analytical descriptions of S for a given lattice and nanoantenna α exist. The rapid, semi-analytical solution for the CDA (rsa-CDA) exploits

rotational symmetry of square lattices to ease computation of S .^{79,95} Analytical dipole α is available for centrosymmetric nanoantennas such as spheres, spheroids, and toroids in homogeneous environments.^{79,97,98} Corrections to sphere α to account for quadrupole interactions⁷⁹ and/or immersion in lossy, multi-layered environments⁹⁹ may be implemented. However, external calculation of α is required for situations involving (i) arbitrary nanoantenna morphologies or (ii) complex dielectric super/sub-strates.

2.2.2 Discrete Dipole Approximation

The DDA solves Maxwell's equations for absorption and scattering of electromagnetic waves by arbitrary, three-dimensional ensembles of polarizable dipoles according to their elemental composition(s) and unique arrangement.^{89,100} A subwavelength target, e.g., a non-symmetric nanoantenna on a substrate, is discretized into a cubic lattice of dipoles with characteristic dielectric functions; α for each dipole comprising the target is calculated according to a Lattice Dispersion Relation.¹⁰¹ Extinction and absorption cross sections of the ensemble are readily deduced from polarization magnitudes at each i^{th} sub-volume of the target, \mathbf{P}_i , in response to its local electric field, *viz.*

$$\mathbf{P}_i = \alpha_i \left(\mathbf{E}_{o,i} - \sum_{j \neq i}^N \mathbf{A}_{ij} \mathbf{P}_j \right) \quad (\text{Equation 2.3})$$

where $\sum_{j \neq i}^N \mathbf{A}_{ij} \mathbf{P}_j$ accounts for interactions between dipoles. Here \mathbf{A}_{ij} is the dipole-dipole interaction matrix including radiative retardation; it is a three-dimensional, more rigorous analog to S in the CDA. Extinction and absorption cross sections are then computed according to Equations 2.4-2.6 after solving for all \mathbf{P}_i in the target.

$$\sigma_{ext} = \frac{4\pi k}{|\mathbf{E}_o|^2} \sum_{j=1}^N \Im(\mathbf{E}_{o,j}^* \cdot \mathbf{P}_j) \quad (\text{Equation 2.4})$$

$$\sigma_{abs} = \frac{4\pi k}{|\mathbf{E}_o|^2} \sum_{j=1}^N \left\{ \Im[\mathbf{P}_j \cdot (\alpha_j^{-1})^* \mathbf{P}_j^*] - \frac{2}{3} k^3 |\mathbf{P}_j|^2 \right\} \quad (\text{Equation 2.5})$$

$$\sigma_{sca} = \sigma_{ext} - \sigma_{abs} \quad (\text{Equation 2.6})$$

Near- and far-field optical responses of arbitrarily shaped nanoantennas interfaced with complex dielectric sub- and/or super-strates, called a target, are described uniquely by the DDA. An example DDA target is shown in Figure 2.3. Electric field-enhancement factors for the target are calculated according to the Clausius-Mossotti relation.¹⁰² Far-field optics of 1D chains and 2D rectilinear lattices of targets are calculated by a generalization of the Mueller scattering matrix.¹⁰³ Detailed electromagnetic data comes at the expense of requiring 10^3 - 10^6 dipoles for computational convergence, thus necessitating DDA simulations execution on high-memory, multi-core processing clusters.

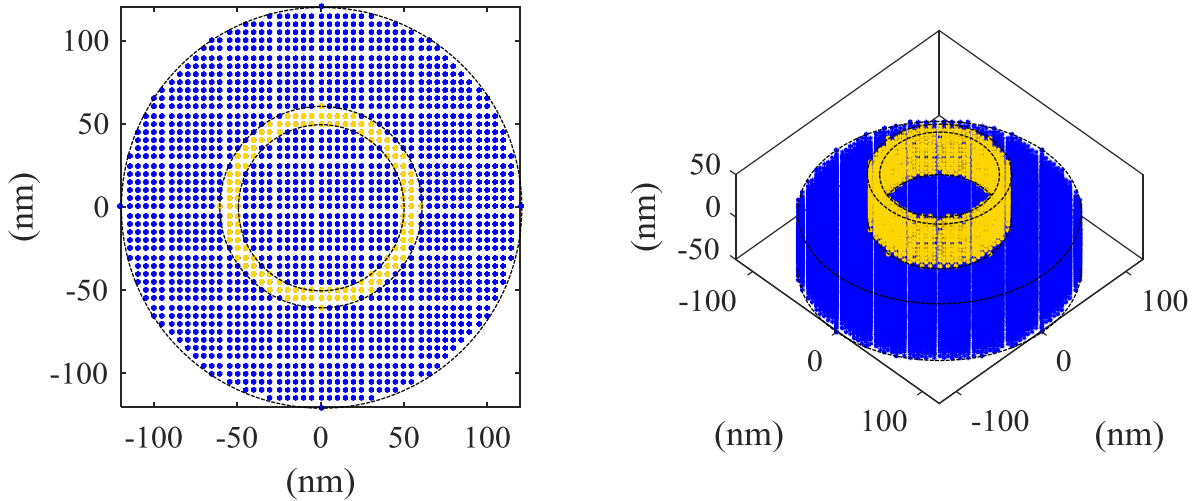


Figure 2.3: Example DDA target comprised of a nanoring supported by a cylindrical substrate discretized into 21,219 dipoles according to a 5 nm inter-dipole spacing. Nanoring dimensions are 60 nm outer radius, 10 nm wall thickness, and 50 nm height. Substrate dimensions are 120 nm radius and 50 nm height. Point dipoles comprising the target are illustrated as spheres; yellow and blue represent the nanoring and substrate, respectively.

The DDA is available as open-source software from Draine and Flatau as DDSCAT.^{100–103} Recent implementations by Masiello and Henrard adapt the DDA algorithm to electron-excitation, called eDDA¹⁰⁴ and DDEELS,¹⁰⁵ respectively. Nanoantenna excitation by an electron uniquely induces resonances not observable under light excitation, deemed “dark” modes. Comprehensive characterization of both bright and dark modes comprising the overall plasmonic mode structure is unique to electron excitation.

2.2.3 Multi-Scale Synthesis of Discrete & Coupled Dipole Approximations

The DDA and CDA was synthesized to rapidly describe far-field optical extinction from lattices composed of arbitrary nanoantenna-dielectric nodes, where DDA calculated an effective α in the absence of analytical descriptions.⁹² Effective α of DDA targets were calculated via

$$\alpha_{eff} = \sum_j \frac{d^3 \mathbf{P}_j}{\mathbf{E}_{o,j}} \quad (\text{Equation 2.7})$$

where d is the inter-dipole spacing of the discretized target. Synthesized DDA-CDA allowed rapid (i) optimization of lattice constant for optimal CLR activity at 40,000x reduced computation time^{75,92} and (ii) interrogation of near-field dielectric screening and energy exchange impacts on coupled nanoantenna interactions in complex dielectric environments.⁸²

Utility of the multi-scale DDA/CDA approach was benchmarked against experimental transmission UV-vis spectra from a 2D square lattice of 160 nm gold (Au) nanospheres lithographed onto indium tin oxide (ITO) covered silica (SiO_x),⁸² which exhibited resonance features unexplainable by the CDA.⁸¹ A scanning electron microscopy (SEM) image of the sample is shown in Figure 2.4(a). The DDA was first used to examine SiO_x- and ITO-dependent dynamics of plasmon excitation and accrued damping for a single 160 nm Au nanosphere embedded 0%, 15%, and 30% by surface area into the substrate.¹⁰⁶ Red-shifts in LSPR scaled with substrate interaction (i.e., embedment). Atomic polarization within the substrate increasingly suppressed

the Coulombic restoring force acting against the plasmon oscillation, thus decreasing net energy required for plasmon excitation.⁶⁵ Enhanced electric near-field plots in Figure 2.4(b) show plasmonic energy transfer and surface plasmon dipole pattern alterations unique to both SiO_x and ITO.⁸² Overall, SiO_x accrued additional radiative scattering losses while ITO improved non-radiative absorption and energy confinement.

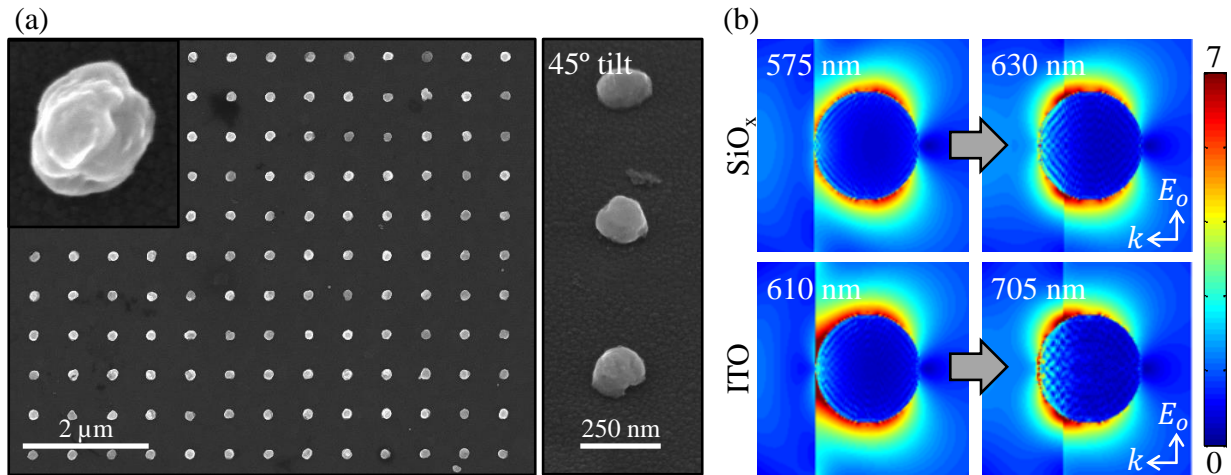


Figure 2.4: (a) SEM micrographs of a 2D square lattice of 160 nm Au nanospheres lithographed onto ITO-covered SiO_x. (b) Electric near-field enhancement (E/E_0) at the LSPR for Au nanospheres embedded 0% (left column) and 30% (right column) by surface area into SiO_x (top row) and ITO (bottom row). Wavelengths of LSPR for each are inset.

Extraction of DDA-calculated α_{eff} for a 160 nm Au nanosphere interacting with SiO_x or ITO into the rsa-CDA showed ITO primarily red-shifted near-field LSPR and glass primarily affected far-field diffractive interactions.⁸² Figure 2.5 shows experimental transmission UV-vis extinction spectra (black) reproduced by superposed theoretical spectral signatures of distinct nanosphere-substrate interaction scenarios (15% dashed; 30% dotted) with SiO_x (blue and cyan) or ITO (red and orange). Symbols label the origin of each spectral feature. Spectral features at 490 nm, 532 nm (dipole surface plasmon of the lattice), and 670 nm (a CLR) were anticipated by the CDA with analytical sphere α and Maxwell Garnett (MG) effective medium theory^{107,108} (black symbols).⁸¹ Expanded bandwidth of the 670 nm feature, presence of secondary shoulders, and

near-infrared resonances 750-800 nm could not be explained using analytical α with MG in the CDA. The multi-scale approach employed herein rapidly characterized *a priori* the bandwidth, relative intensity, and wavelength occurrence for each of these previously unknown resonances.

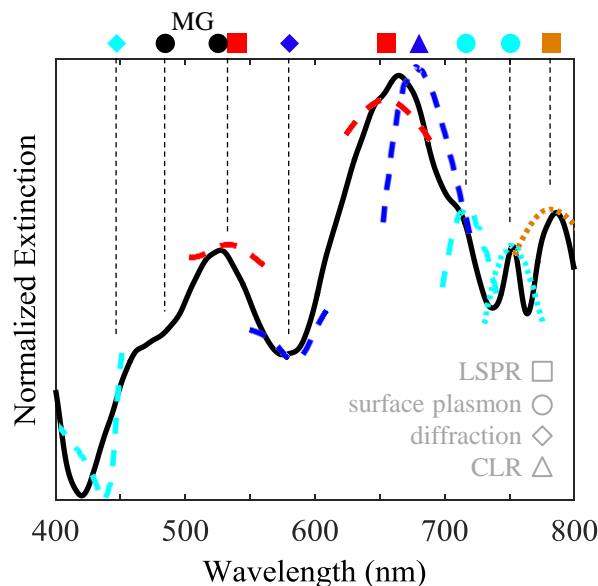


Figure 2.5: Experimental transmission UV-vis extinction spectra (solid black) with superposed theoretical optical extinction signatures (dashed and dotted colored) from single and ordered 160 nm Au nanospheres interacting with SiO_x (blue and cyan) or ITO (red and orange).

2.3 Material Considerations

Utilization of a metal, semiconductor, or ceramic as a plasmonic nanoantenna has direct impacts on its capabilities to resonantly confine, transport, or transduce electromagnetic energy. Research in light-matter interactions has focused on noble metals since Michael Faraday's discovery of stable Au colloids in the mid-19th century.¹⁰⁹ Despite historical significance of metals, research into plasmonically-active semiconductors and ceramics recently accelerated because of their (i) activity near the 1.55 μm telecommunication frequency, (ii) compatibility with CMOS technology, and (iii) lower intrinsic losses.⁷⁰⁻⁷² Design of nanoantennas for operating

within large temperature gradients requires careful survey of a material's intrinsic plasma frequency range and losses, as well as its ability to structurally withstand high temperatures.

Table 2.1 summarizes the intrinsic plasmonic activity of different metal, ceramic, and semiconductive materials according to their underlying Drude-Lorentz dielectric function parameters and respective melting points. Drude-Lorentz dielectric theory expresses $|\mathbf{P}|$ of a material by its intrinsic electric permittivity function, $\epsilon(\omega)$, according to inter- and intra-band optical interactions/losses, *viz.*¹¹⁰

$$\epsilon(\omega) = \epsilon'(\omega) + i\epsilon''(\omega) = \epsilon_b + \sum_j \frac{f_j \omega_{p,j}^2}{\omega_j^2 - \omega^2 - i\omega\gamma_j} \quad (\text{Equation 2.8})$$

where ϵ_b signifies core-electron polarization, $f_j \omega_{p,j}$ is the free-electron intraband plasma frequency strength, ω_j is some resonant interband transition, and γ_j is the total damping rate from electron scattering by electrons, phonons, and lattice defects (e.g., grain boundaries). The real component, $\Re(\epsilon)$, signifies polarization strength. The imaginary component, $\Im(\epsilon)$, signifies losses. Equation 2.9 gives the bulk ω_p from j^{th} resonance-induced carrier concentration (N), electron charge (e), permittivity of free space (ϵ_o), and effective electron mass (m_o).

$$\omega_p^2 = \frac{Ne^2}{\epsilon_o m_o} \quad (\text{Equation 2.9})$$

LSPR for quasistatic nanoantennas is directly related to the bulk ω_p , but occurs at lower energies due to surface damping (increasing γ in Equation 2.8) and screening by the local environment.¹¹¹

Metals exhibit ω_p between 8.7 eV to 12.7 eV, leading to LSPR in the UV to visible spectrum.^{70,71,112–114} Melting points range from 660 °C to 1085 °C.¹¹⁵ High losses at the plasmon frequency from interband transitions [$\Im(\epsilon) \sim 10^0\text{-}10^1$] and at 1.55 μm from intraband transitions make them undesirable for many applications, especially electrical-optical transition circuitry

components.¹¹⁶ Notwithstanding relatively low melting points ranging from 660 °C to 1085 °C precluding use in high temperature applications,¹¹⁵ aluminum (Al), silver (Ag), and copper (Cu) also suffer from oxidation in natural environments which raise additional degradation concerns.^{70,117,118} Relatively high ϵ_b of metals make them the strongest resonators in Table 1 (data not shown). However, complex nanoantenna morphologies^{75,86,119–121} and Fano coupling interactions^{92,122–124} are required to shift LSPR activity into the infrared spectrum, which involves high capital lithography processes with generally low throughput.^{125–127}

Table 2.1: Comparison of common plasmonic materials and their experimentally measured optical characteristics according to Drude-Lorentz dielectric theory.

| material | | resonant spectrum | ω_p [eV] | $\Im(\epsilon)$ at ω_p | $\Im(\epsilon)$ at 1.55 μm | γ_p [eV] | melting point [°C] |
|--|---------------------|-------------------|-----------------|-------------------------------|---------------------------------------|-----------------|--------------------|
| metals [70,71,112-118] | Al | UV-visible | 12.7 | 10^0 | 46 | 0.13 | 660 |
| | Ag | visible | 9.2 | 10^1 | 3-4 | 0.02 | 962 |
| | Au | visible | 8.9 | 10^1 | 11 | 0.07 | 1064 |
| | Cu | visible | 8.7 | - | 15 | 0.07 | 1085 |
| ceramics [†] [70,-72,112,116,128-130] | TiN | visible-NIR | 1.92-2.43 | 3.1-8.2 | 20 | 0.18-0.51 | 2930 |
| | ZrN | visible-NIR | - | 2 | 8-55 | 0.52 | 2980 |
| | Al:ZnO [‡] | NIR | 0.71-2.03 | 0.8-1.6 | 0.1-1.3 | 0.04-0.31 | 660-1975* |
| | Ga:ZnO | NIR | 1.99 | 10^{-1} | 0.59-1.2 | 0.12-0.22 | 30-1975* |
| | ITO | mid-IR | 0.62-1.07 | 0.5-1.4 | 0.2-1.5 | 0.16 | 1526-1926 |
| | NiSi | mid-IR | 4.6-7.4 | - | 12 | 10^{-1} | 993 |
| | TiSi | mid-IR | 4.2 | - | 10 | 10^{-1} | 1470 |
| semicond. [71,130,131] | InAs | mid-IR | 0.12-0.22 | 0.4-0.6 | - | 10^{-1} | 942 |
| | InSb | mid-IR | 0.18 | 2.7 | - | 10^{-1} | 527 |
| | ZnO | long-IR | 0.30 | 1-3 | - | - | 1975 |
| [†] passively tunable according to deposition temperature/environment and dopant concentration [‡] demonstrated active tunability according to electrical bias * cited range of known melting points for subcompounds comprising the alloy | | | | | | | |

Ceramic and semiconductive materials offer (i) intrinsic LSPR throughout the infrared spectrum at lower loss,^{70,71} (ii) generally higher melting points than metals,¹¹⁵ and (iii) compatibility with CMOS fabrication technology.^{71,72} The ϵ of ceramics is passively tunable, unlike metals, according to their deposition temperature and environment (e.g., nitrogen versus argon gases) and dopant concentration.^{112,128} Transparent conducting oxides [aluminum/gallium-doped zinc oxide (Al:ZnO/Ga:ZnO) and ITO]^{70,112,116,128–130} and transition metal nitrides [titanium/zirconium nitride (TiN/ZrN)]^{72,116,128} exhibit ω_p between 0.62 eV and 2.43 eV leading to near- to mid-infrared LSPR. Active ϵ tunability has been demonstrated for Al:ZnO and ITO with electric bias.¹¹⁶ High temperature applications may be best suited for TiN and ZrN, whose melting points exceeding 2900 °C ensure structurally robust nanoantennas. Silicides [nickel/titanium silicide (NiSi/TiSi)] exhibit many metal-like Drude-Lorentz characteristics, but with LSPR in the mid-infrared due to high damping rates.⁷¹ Semiconductive III-V indium arsenide/antimonide (InAS/InSb)⁷¹ and II-VI zinc oxide (ZnO)^{71,130,131} support LSPR in the mid- to long-infrared spectrum, but their understanding as a plasmonic material remains immature.

Overall, Al:ZnO or ITO appeared as ideal candidates for surface plasmon-functionalized energy conversion of infrared radiation in optoelectronics. Both materials exhibit low loss at the plasmon and telecommunication frequencies (ca. 1526 °C to 1975 °C melting points for resistance to high temperature deformation)¹¹⁵ and comparable ϵ_b to metals for intense, broad-band field enhancements.⁷⁰ Compatibility with conventional CMOS processing supports facile integration into current electronic platforms.¹¹⁶ Active and passive LSPR tunability offers on-board tailoring of optical activity to unique thermal environments.¹¹⁶ However, Al:ZnO and ITO plasmonics have remained in the prototyping phase primarily due to lack of: (i) widely disseminated, reproducible data for plasmonic interactions, (ii) availability of infrared-compatible spectroscopic tools to

validate models, and (iii) refined chemical synthesis techniques relative to noble metals. Therefore noble metal, in particular Au, nanoantennas were used herein as prototypes to explore the underlying hypothesis of this dissertation.

2.4 Morphology Influences

Morphological acircularity and annularity influences on the evolution of the electromagnetic local density of states (ELDOS) for plasmonic nanoantennas were characterized using computational electron energy loss spectroscopy (EELS; detailed later in § 5.1) to guide nanoantenna design.⁹⁴ Available plasmonic states of a nanoantenna may be tailored to application-specific energies by engineering its morphology.^{66,75,97,132,133} Concomitantly, LSPR can deviate from design as a consequence of structural aberrations accrued from self-assembly and/or oxidization in natural environments.^{118,132} To date, plasmonic mode structures have been computed for nanodiscs,¹³⁴ nanoellipses,¹³⁵ nanobipyramids,¹³⁶ triangular nanoprisms,^{137–139} nanorods,¹⁴⁰ split-ring resonators,¹⁴¹ and dynamic disc transformations into triangular prisms.¹⁴² Plasmonic mode structures obtained in EELS¹⁴³ only qualitatively describe the ELDOS however.¹⁴⁴ Direct quantitative correlation is precluded by differences in respective electric-field distributions of a photon versus a propagating electron.^{135,145}

Figure 2.6 shows the evolution of plasmon mode structure within the ELDOS of a 60 nm radius Au nanodisc (upper left) as a result of 1.5x aspect radial elongation and annulation.⁹⁴ Au was used because its quasistatic LSPR in the visible spectrum readily allowed facile observation of morphological changes to plasmonic activity across a wide energy range. EELS spectra were computed with eDDA (v2.0).¹⁴⁶ Impact points of the electron beam were the center (blue), half major/minor radius (purple/cyan), and full major/minor radius (red/green).

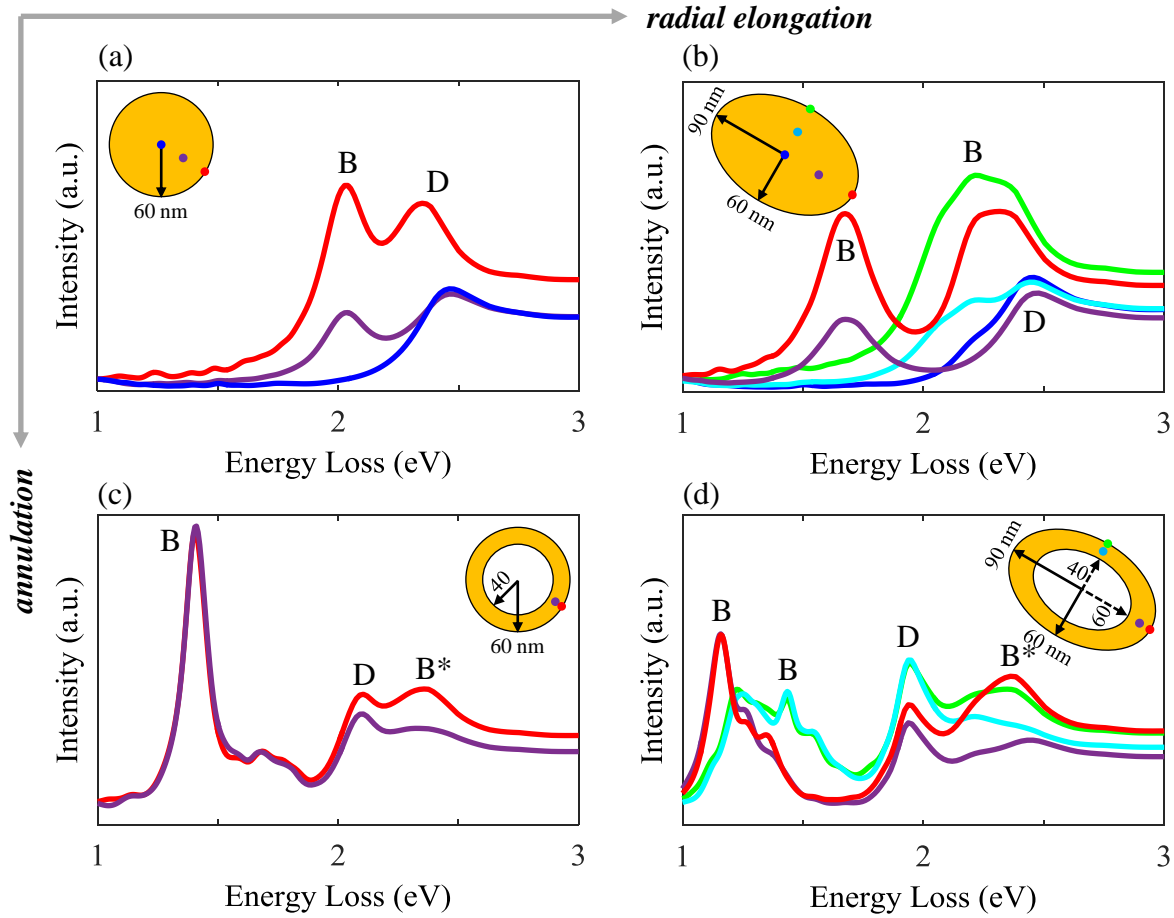


Figure 2.6: Computational EELS spectra for a 60 nm radius (a) Au nanodisc subjected to (b) 1.5x aspect ratio elongation, (c) annulation, and (d) 1.5x aspect ratio elongated annulation. Electron beam impact points were at the nanoantenna center (blue), major axis edge/mid-point (red/purple), and minor axis edge/mid-point (green/cyan). Structure schemes for each nanoantenna are inset. Height was held constant at 20 nm. “B” and “B*” indicate bonding and anti-bonding bright plasmon modes. “D” indicates dark plasmon mode.

Each impact point induced a spatially-unique bright or dark plasmon resonance mode in the ELDOS. Bright plasmon modes (labeled B and B* for bonding and anti-bonding, respectively) are resonances which exhibit a finite net dipole moment ($\sum \vec{p} \neq 0$), thus enabling both photon and electron induction. Electron beams are also capable of exciting dark plasmon modes (labeled D) with net zero dipole moment ($\sum \vec{p} = 0$) which cannot be directly induced by photons. Thus, resonances not observed in light-excitation DDSCAT (v7.3)¹⁰⁰ simulations were classified as dark modes.¹⁴⁷ In the quasistatic limit for Au, the bright and dark modes converge at 2.45 eV where

the real component of its dielectric function crosses zero, i.e., the bulk ω_p .¹⁴⁸ The two modes split and shift upon radial elongation (upper right), annulation (lower left), and concomitant elongation and annulation (lower right) due to phase retardation and inter-surface capacitive coupling.

Centrosymmetric nanoantennas just beyond the quasistatic regime yielded distinct bright and dark plasmon resonances.⁹⁴ Figure 2.6(a) shows bright and dark plasmon resonances at 2.03 eV and 2.45 eV for a 60 nm radius nanodisc. The 2.03 eV bright mode corresponded to a dipole LSP, as previously reported for optical excitation.¹⁴⁹ Expansion of the radial dimension would (i) red-shift the dipole LSP and (ii) accommodate multipole LSP resonances in the ELDOS. Angular rotational symmetry of the nanodisc precluded resonant energy dependence on the angular coordinate. The dark mode at 2.45 eV represents the bulk plasma energy of Au.¹⁵⁰ The bulk mode for Au has been observed for other structures.^{150–152} Though not inducible by photons, an optically excited bright dipole LSP can decay into a dark mode via coupled excitation of an adjacent structure.^{77,86} Corresponding EELS supporting mode-type classifications in Figure 2.6(a) can be found in Refs. 94, 153, and 151.

Radial elongation of the nanodisc to a 1.5x aspect ratio, in Figure 2.6(b), caused a second, lower energy bright mode to emerge due to radial asymmetry.⁹⁴ Nanorods analogously support two bright modes in their ELDOS, observed in polarized optical excitation along transverse (rod diameter) and longitudinal (rod length) axes.¹⁵⁴ Major axis excitation induced a 1.67 eV bright LSP. Minor axis excitation induced a 2.21 eV bright LSP, blue-shifted by 0.17 eV from the initial centrosymmetric disc bright mode. Dipole LSP are known to red-shift from increasing the radial dimension of an axis because of phase retardation, per Mie theory of oblate spheroids.⁶⁴ The 2.45 eV dark “bulk” mode was preserved despite structural asymmetry. Optical excitation of an ellipse can controllably decay into a dark mode on an adjacent ellipse by tuning physical orientation

between the two.¹⁵⁵ Corresponding EELS maps supporting mode-type attribution may be found in Refs. 151 and 152.

Distinct dipole “bonding” and “anti-bonding” bright plasmon resonances arose from annulation of the nanodisc,⁹⁴ caused by capacitive charge interactions between the inner and outer ring walls.^{92,119} Resonances at 1.41 eV, 2.11 eV, and 2.36 eV in Figure 2.6(c) corresponded to bright bonding, dark, and bright anti-bonding plasmon modes,¹⁵⁶ respectively. Corresponding EELS maps corroborating mode-type attribution may be found in Ref. 94. The bright resonances agreed within 0.17 eV to 0.03 eV of experimental and theoretical reports of comparably sized rings.^{75,92,119} High energy anti-bonding exhibits dipole moments on each wall, anticipated to occur near 2.4 eV according to a Drude-type dielectric model.¹¹⁹ Anti-bonding modes were not observed in EELS experiments on smaller nanorings.¹⁵⁷ Low energy bonding exhibits collective negative and positive charge on opposing walls, and was anticipated to occur near 1.2 eV according to a Drude-type dielectric model.¹¹⁹ Charge distributions for each bright mode type are illustrated in Ref. 119. Increasing the ring aspect ratio (wall thickness to radius) converges the bonding resonance to that of a disc LSPR,¹¹⁹ as described earlier. The 2.11 eV dark resonance would create net zero dipole moments ($\sum \vec{p} = 0$) within the ring wall.⁹⁴ Such a charge distribution would not be possible under optical excitation because each subwavelength ring wall experiences a static electric field.¹⁴⁵ Dark modes were not observed in EELS experiment of rings with 7-10 nm wall thicknesses.¹⁵⁷

Simultaneous elongation and annulation hybridized the nanoantennas’ ELDOS between that of a nanoring and a nanoellipse.⁹⁴ Figure 2.6(d) shows 1.16 eV bright minor axis bonding, 1.44 eV bright major axis bonding, 1.94 eV dark plasmon, and 2.42 eV bright anti-bonding resonances. Occurrence of bonding along each axis, emergence of anti-bonding behavior, and a

preservation of a single dark mode are consistent with hybridization of the ring and ellipse plasmonic mode structures. For example, consider the 1.5x aspect ratio nanoellipse in Fig. 1(b) subjected to annulation. Annulation at the considered structure dimensions (i) red-shifted the bright mode by 0.62 eV, (ii) red-shifted the dark mode, and (iii) caused a bright anti-bonding mode to emerge at 2.36 eV. Annulating the nanoellipse [transition from (b) to (d) in Figure 2.6] indeed caused both bonding modes to red-shift, red-shifted to dark mode down to 1.94 eV, and induced a bright anti-bonding mode at 2.42 eV. Bright bonding mode energy for the 0.6x aspect ratio major axis was lower than that of the 0.7x aspect ratio minor axis, consistent with previous optical reports.^{75,92} A parallel analysis could have been performed by elongating the nanoring to a 1.5x aspect ratio to arrive at the same result.

2.5 Summary

Material and structural morphology influences on discrete localized (e.g., LSPR) and coupled (e.g., CLR) surface plasmon resonance modes comprising the ELDOS of nanoantennas were elucidated, enabling their design towards nonlinear infrared frequency conversion processes. Electrodynamic frameworks of the CDA and DDA to describe plasmonic phenomena were described. A survey of Drude-Lorentz theory parameters and melting points across metals, ceramics, and semiconductors indicated Al:ZnO and ITO were well-suited as nanoantenna materials for the proposed hypothesis. However, an immature understanding of their plasmonic properties and available spectroscopic tools limit their implementation over traditional noble metals, such as Au. Excitation by a swift electron in the DDA distinguished emergence and energy-shifting patterns for bright and dark plasmonic modes of a Au nanodisc subjected to elongation and/or annulation. Radial elongation caused a second bright plasmon resonance to

emerge at a lower energy. Annulation split the initial bright mode into discrete higher-energy anti-bonding and lower-energy bonding bright modes. Elliptical annulation hybridized the effects. Overall, the foundational electrodynamic and material frameworks to optimize nanoantennas for infrared functionality were described.

CHAPTER 3

TWO-DIMENSIONAL TRANSITION METAL DICHALCOGENIDES

Monolayer group-VI transition metal dichalcogenides (TMD) exhibit remarkable light-matter interactions arising from their direct bandgap,⁴² presence of van Hove singularities,¹⁵⁸ and lack of crystalline inversion symmetry.⁵⁰ A TMD crystal is comprised of a single transition metal and two chalcogen atoms. Van der Waals bonding between monolayers comprise bulk TMD, which have been studied extensively since the 1960s.^{159–161} The discovery of graphene in 2004¹⁶² renewed interest in TMD materials to exploit the optical, electronic, and physical properties unique to monolayers, most notably, in photocatalysis¹⁶³ and field-effect transistors.¹⁶⁴ Monolayer TMD exhibit extraordinary optoelectronic and nonlinear optical activity,⁵⁰ and thus were chosen as the base material for prototyping energy conversion within plasmonic fields.

3.1 Overview

Group-VI TMD crystals are van der Waals bonded semiconductive monolayers of the formula MX_2 , comprised of a transition metal (M; molybdenum or tungsten) occupying trigonal prismatic sites between two hexagonal chalcogen layers (X; sulfur, selenium, or tellurium).⁴³ Figure 3.1 shows the crystal structure of a single-layer TMD. Different structural polytypes occur based on trigonal or octahedral coordination of the transition metal with the chalcogens: 2H, 3R, or 1T.^{165,166} TMD naturally form the 2H phase, but may be reversibly changed to the “metallic” 1T phase¹⁶⁷ by external optical/electrical stimuli⁵⁶ or elemental doping.¹⁶⁸ TMD are not limited to semiconductive behavior; TMD based on group-V transition metals (e.g., niobium or tantalum)

range from metallic to superconductive.¹⁶⁵ Scope of this work was limited to group-VI TMD monolayers, specifically molybdenum and tungsten disulfide (MoS_2 and WS_2 , respectively).

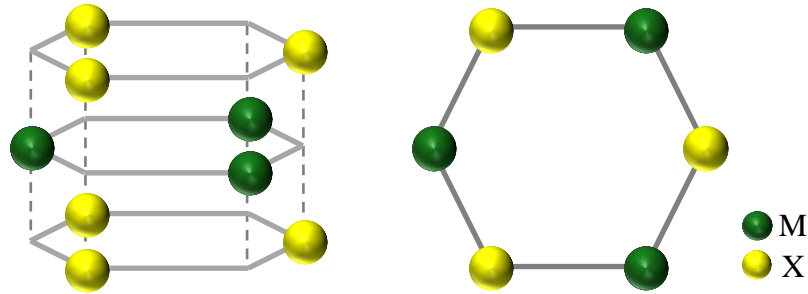


Figure 3.1: Crystal structure of a TMD monolayer with the transition metal atoms (M) in green and chalcogen atoms (X) in yellow.

The optical properties of TMD change with layer number comprising the total thickness.^{42,169} Bulk TMD are indirect-bandgap semiconductors. In the monolayer limit however, quantum confinement alters their electronic band structure to accommodate direct transitions across the K point of the Brillouin zone near 2 eV range and suppresses the bulk-form indirect transition.⁴² The linear optical properties of various TMD are tabulated in Refs. 43 and 44. The fundamental direct bandgap is referred to as the A bandgap and higher-energy direct transitions are referred to as the B, C, etc. bandgaps by convention. The A and B transitions both occur across the K point but are distinct in energy because of spin-split valence bands, accrued from spin-orbital coupling.⁴³ Such interactions enable TMD to be used in spintronics,¹⁷⁰ where the spin state could serve as a degree of freedom for storing data.¹⁷¹ Electrical properties of TMD, e.g., 10^8 on/off ratio¹⁷² and $1000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ carrier mobility¹⁷³ demonstrated in monolayer MoS_2 field-effect transistors, are reviewed in Refs. 44 and 165.

3.2 Fabrication Techniques

Two-dimensional (2D) monolayer TMD may be fabricated naturally or synthetically by exfoliation from bulk crystals or chemical vapor deposition (CVD) growth, respectively. Weak

inter-layer van der Waals forces and strong intra-layer covalent bonds facilitate access to single TMD monolayers from natural bulk crystals from a strategically applied force, called exfoliation. Scaling monolayer TMD crystals to wafer-scale lengths has motivated refinement of synthetic protocols based on gaseous chalcogens reacting with oxidized transition metals at high temperature and vacuum to form monolayers on specific substrates. The MoS₂ and WS₂ samples used herein were fabricated by (i) liquid exfoliation into water or ethanol and (ii) CVD onto silica (SiO_x) atop a silicon (Si) wafer.

Exfoliation of TMD by mechanical,^{42,164} chemical,^{168,174} and liquid¹⁷⁵⁻¹⁷⁷ techniques have been described. Mechanical exfoliation of single-crystalline TMD at 1-10 μm length scales using adhesive tape is suitable for fundamental studies and prototyping, but suffers from low throughput and no control over thickness.^{44,178} Chemical exfoliation produces gram quantities of sub-1 μm TMD monolayers by overcoming van der Waals force between layers with the hydrogen evolution reaction, where water interacts with lithium ions intercalated between TMD layers (via *n*-butyllithium).^{168,174,179} However, the process induces a phase change to the metallic 1T phase and a 300 °C annealing step¹⁶⁸ is required to restore the semiconducting 2H phase desired for optoelectronic applications. Liquid exfoliation techniques span many protocols which bypass chemical oxidation of the bulk materials in favor of some direct strategy,¹⁷⁵⁻¹⁷⁷ most namely the utilization of an ultrasonic probe to shear monolayers from the bulk crystal into a solvent.^{180,181}

Synthetic CVD growth involves strategic placement of chalcogen and transition metal oxide precursors in a pressure- and temperature-controlled tube furnace. The chalcogen powder precursor is vaporized and then reduced with the transition metal onto a substrate.¹⁸²⁻¹⁸⁵ CVD processes form triangular TMD monolayers due to their trigonal crystal structure. Typical sizes range from 1-100 μm length scales depending on purities of precursors, substrate, and

environment.^{185–187} However, recent precursor refinements have advanced the technique to give polycrystalline monolayer films across centimeter scales¹⁸⁸ and even 100 mm wafers.¹⁸⁹

3.2.1 Liquid Phase Exfoliation

Liquid phase exfoliation presents a readily accessible, potentially scalable method for technologies based on few- to mono-layer TMD.^{175–177} Figure 3.2 schematically depicts TMD liquid exfoliation broken down into two stages: ultrasonic exfoliation and iterative centrifugation cascades for size selection. Bulk TMD powder (234842 and 243639; Sigma Aldrich, St. Louis, MO USA) was mixed into aqueous sodium cholate at ca. 25 mg ml⁻¹. Sodium cholate (C1254; Sigma Aldrich, St. Louis, MO USA) provided suspension stability and minimized aggregation.¹⁹⁰ The initial sonication and low-speed centrifugation served as a cleaning/purification step. The primary exfoliation step occurred over a 12 hour duration at 360 W to exfoliate the mixture down to mono- and few-layer TMD crystals. After a low-speed centrifugation to remove aggregates and residual bulk crystallites, an iterative series of centrifugations at increasing speeds from 2 krpm to 10 krpm were performed to size-select TMD.¹⁸¹ Figure 3.3 shows representative scanning transmission electron microscopy (STEM) images of exfoliated (a) MoS₂ and (b) WS₂.

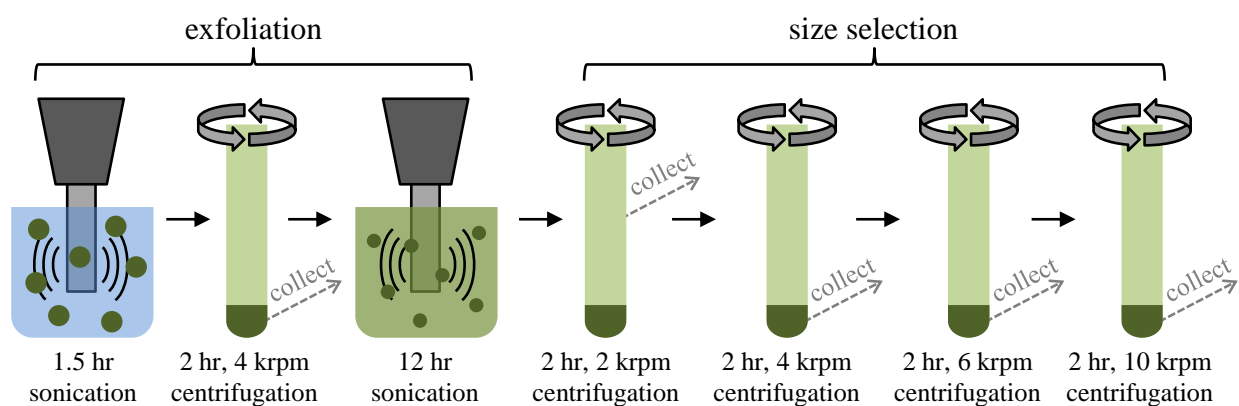


Figure 3.2: Process schematic for liquid phase exfoliation of 2D TMD crystals. Monolayer TMD are obtained from interactive liquid cascade centrifugations after a 12 hr ultrasonic exfoliation.

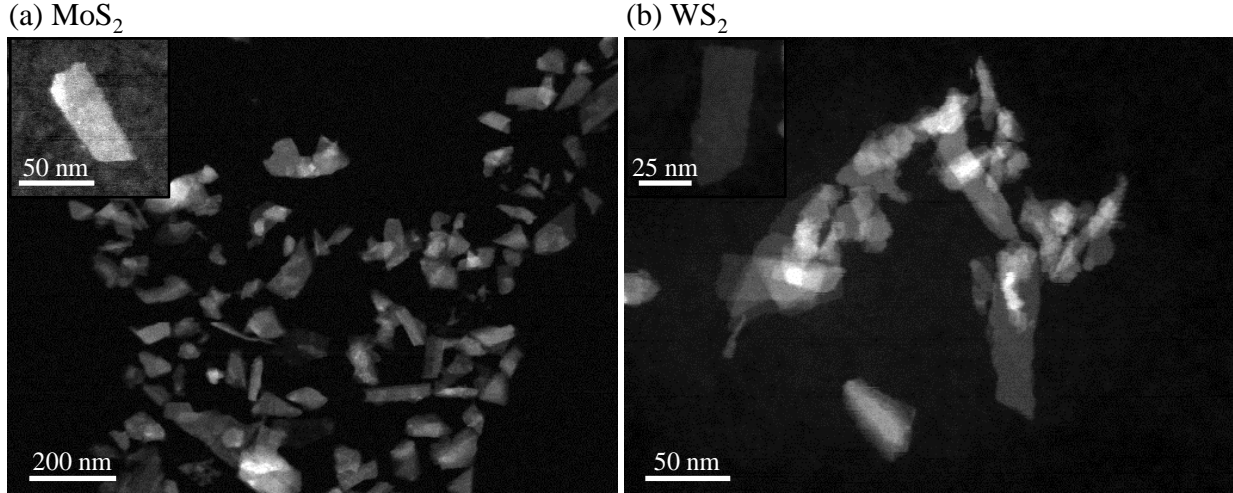


Figure 3.3: High-angular annular dark field STEM (HAADF-STEM) images of liquid exfoliated few- to mono-layer (a) MoS₂ and (b) WS₂ flakes. Accelerating voltage was 200 kV.

Mean size of exfoliated MoS₂ and WS₂ crystals comprising the dispersions were sub-100 nm in length and monolayer in thickness as measured *in situ* by empirical absorbance spectrum metrics.^{180,181} The absorbance spectrum contains size/thickness-dependent signatures of electronic structure changes at the crystal edges and quantum confinement.^{42,180} Quantitative relationships between absorbance spectra features of disulfide TMD and their dimensions were previously determined according to statistical analyses from transmission electron microscopy (TEM) and atomic force microscopy (AFM) with corroboration by dynamic light scattering (DLS).^{181,191} Mean layer quantity per flake, N_{TMD} , was calculated from to the A exciton wavelength, *viz.*^{180,181}

$$N_{TMD} = \begin{cases} 2.3 \times 10^{36} e^{-54,888/\lambda_A}, & \text{MoS}_2 \\ 6.35 \times 10^{-32} e^{\lambda_A/8.51}, & \text{WS}_2 \end{cases}. \quad (\text{Equation 3.1})$$

Mean length, L_{TMD} , was calculated according to the ratio of absorbance intensity (I) at two carefully selected wavelengths which express their size-dependent scattering behavior^{176,192} arising carrier confinement at the crystal edge by Equation 3.2,¹⁸⁰ where intensity at the B exciton and 345 nm were selected for MoS₂ and 235 nm and 290 nm were selected for WS₂.^{180,181} Error in N_{TMD} and L_{TMD} were estimated be less than 10%.¹⁸⁰

$$L_{TMD} = \begin{cases} \frac{3.5 \frac{I_B}{I_{345 \text{ nm}}} - 0.14}{11.5 - \frac{I_B}{I_{345 \text{ nm}}}}, & \text{MoS}_2 \\ \frac{2.3 - \frac{I_{235 \text{ nm}}}{I_{290 \text{ nm}}}}{0.02 \frac{I_{235 \text{ nm}}}{I_{290 \text{ nm}}} - 0.0185}, & \text{WS}_2 \end{cases} \quad (\text{Equation 3.2})$$

3.2.2 Chemical Vapor Deposition

CVD growth of monolayer TMD presents a scalable avenue amenable with existing high-volume microelectronics manufacturing infrastructure. Figure 3.4 schematically depicts a typical CVD procedure to synthesize monolayer TMD onto a Si wafer in a tube furnace. Taking MoS₂ as an example, sulfur powder is vaporized (ca. 650 °C) and carried downstream by an inert gas to partially reduce molybdenum trioxide (MoO₃) into volatile MoO_{3-x} which subsequently adsorbs onto the target substrate and continues reaction with the sulfur to form MoS₂.^{183,193}

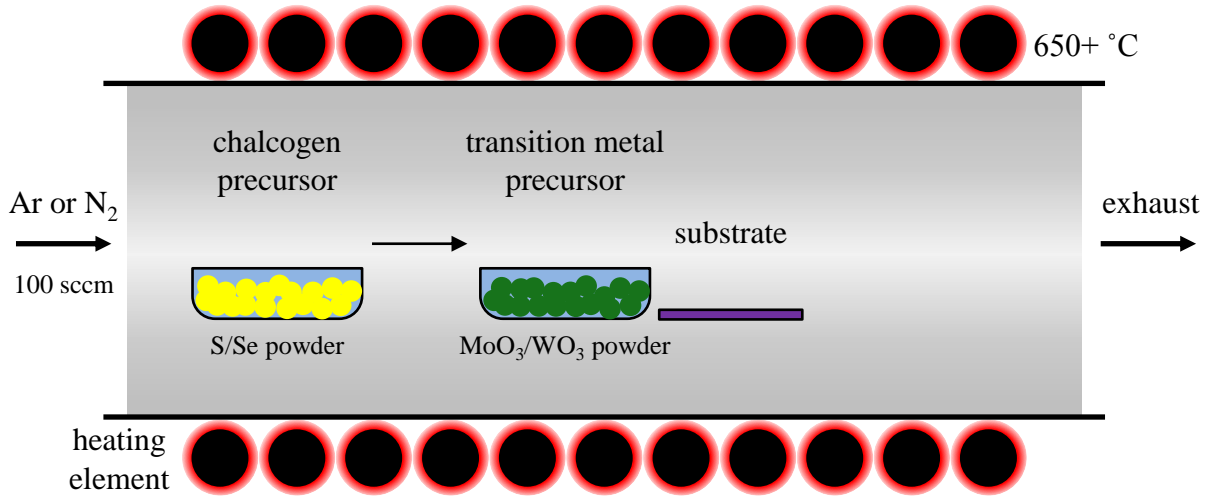


Figure 3.4: Typical process schematic for CVD growth of monolayer group-IV TMD in a tube furnace. Vaporized chalcogen atoms are transported downstream to react with the transition metal trioxides to form monolayer MoS₂, WS₂, MoSe₂, or WSe₂ on the adjacent substrate.

The resultant triangular TMD are predominantly monolayer thickness in the absence of defects or use of secondary seed precursors which promote multi-layer nucleation.¹⁸⁶ Continued growth causes the triangular, single crystalline domains to eventually merge and form

polycrystalline films.¹⁸⁷ Table 3.1 summarizes 13 reported protocols spanning MoS₂,^{183,186–189,194,195} WS₂,^{185,189,193} molybdenum diselenide (MoSe₂),^{184,196} and tungsten diselenide (WSe₂);¹⁹⁷ each are unique to specific furnace configurations. However in the absence of a rigorously tested internal CVD protocol, CVD-synthesized monolayer MoS₂ was sourced externally (CVD-MOS2; 2Dsemiconductors, Scottsdale, AZ USA). Figure 3.5 shows (a) optical bright-field images and (b) scanning electron microscopy (SEM) images of triangular monolayer MoS₂ crystal domains synthesized by CVD.

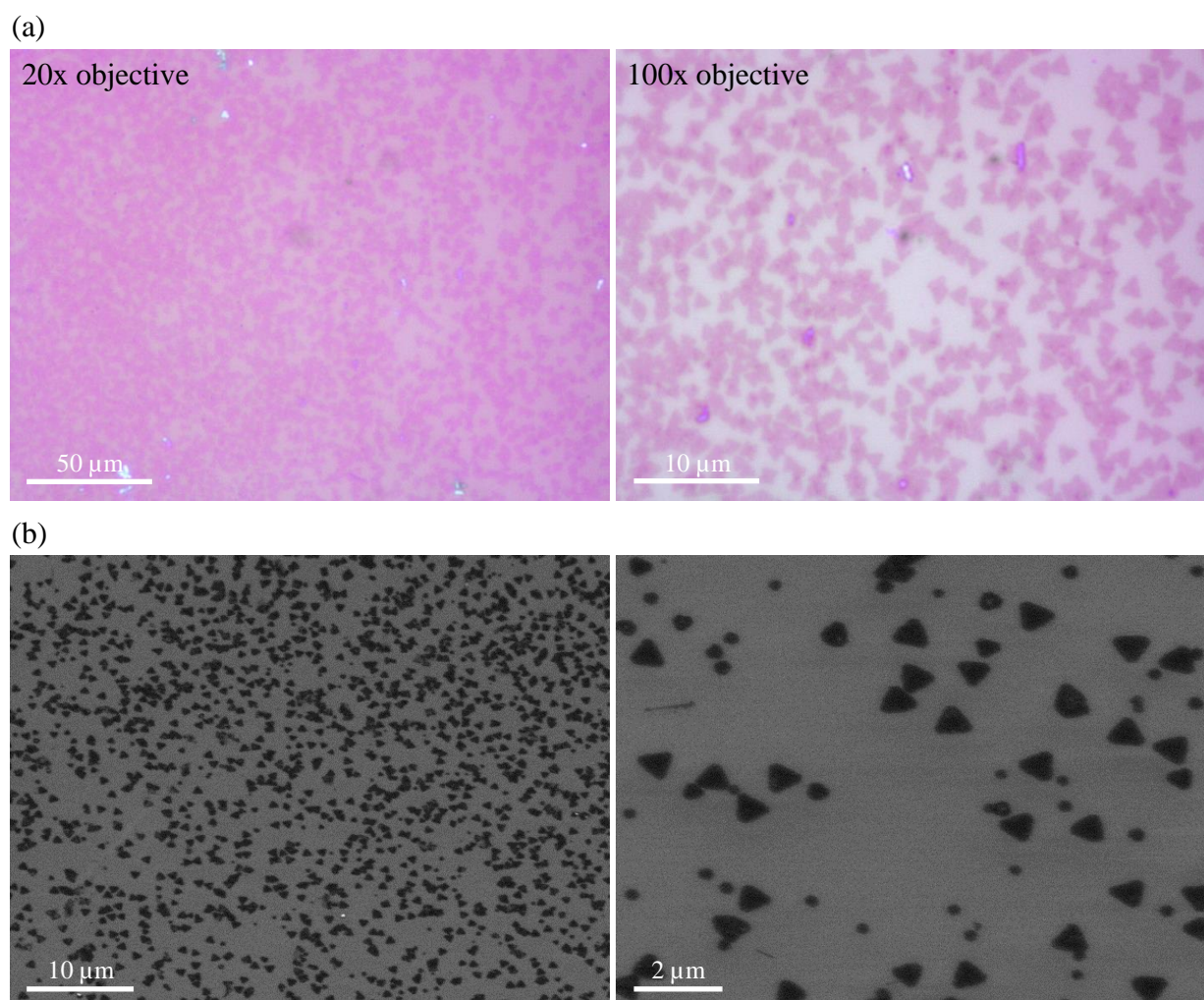


Figure 3.5: (a) Optical 20x and 100x objective bright-field images and (b) SEM images of CVD-synthesized MoS₂ monolayers on a Si wafer. Accelerating voltage was 5 kV.

Table 3.1: Protocol parameters for CVD synthesis of MoS₂, WS₂, MoSe₂, and WSe₂.

| MX ₂ protocol | size order limit | MX ₂ Precursors | | Environment | | | Substrate Locale | Seed | |
|--------------------------|---------------------|----------------------------|---|--------------------------|---------------------|--------|------------------|------------------------|-------------------|
| | | X | M | Gas | Flow [sccm] | T [°C] | | | |
| MoS ₂ | Lee [182] | 1 mm | S powder | MoO ₃ powder | N ₂ | N/A | 650 | above MoO ₃ | GO [†] |
| | Najmaei [185] | 100 μm | S powder | MoO ₃ ribbons | N ₂ | 200 | 850 | away | - |
| | van der Zande [186] | 100 μm | S powder | MoO ₃ powder | N ₂ | 10 | 700 | above MoO ₃ | - |
| | Kim [187] | 1 cm | H ₂ S gas | MoO ₃ powder | Ar | 200 | 600 | away | - |
| | Kang [188] | 1 cm (wafer) | (C ₂ H ₅) ₂ S gas | Mo(CO) ₆ gas | Ar/H ₂ | 150 | 550 | away | - |
| | Liu [193] | 10 μm | S powder | MoO ₃ powder | Ar | 50 | 625 | above MoO ₃ | - |
| | Ling [194] | 10 μm | S powder | MoO ₃ powder | Ar | 5 | 650 | above MoO ₃ | PTAS [‡] |
| WS ₂ | Cong [184] | 100 μm | S powder | WO ₃ powder | Ar | 100 | 750 | above WO ₃ | - |
| | Kang [188] | 1 cm (wafer) | (C ₂ H ₅) ₂ S gas | W(CO) ₆ gas | Ar/H ₂ | 150/5 | 550 | away | - |
| | McCreary [192] | 10 μm | S powder | WO ₃ powder | Ar | 100 | 825 | above WO ₃ | PTAS [‡] |
| MoSe ₂ | Wang [183] | 100 μm | Se pellets | MoO ₃ powder | Ar/H ₂ * | 50 | 750 | above MoO ₃ | - |
| | Chang [195] | 1 μm | Se pellets | MoO ₃ powder | Ar/H ₂ * | 40/10 | 700 | away | - |
| WSe ₂ | Huang [196] | 10 μm | Se powder | WO ₃ powder | Ar/H ₂ * | 80/20 | 925 | away | - |

[†] reduced graphene oxide
^{‡‡} perylene-3,4,9,10-tetracarboxylic acid tetrapotassium salt
^{*} H₂ required to selenize the transition metal trioxide precursor^{183,196}

3.3 Spectroscopic Characterization

Transmission UV-vis absorbance, photoluminescence (PL), and Raman spectroscopies were performed to interrogate the optoelectronic and physical properties of MoS₂ and WS₂. Figure 3.6 shows normalized transmission UV-vis absorbance spectra for (a) MoS₂ and (b) WS₂ liquid exfoliated into water with each exciton transition labeled. The A and B transition occurred at 1.87 eV and 2.06 eV, respectively, for MoS₂. The A and B excitons both correspond to direct transitions across the K point of the Brillouin zone, but differ in energy because of spin-split valence bands.⁴² The C transition occurred at 3.14 eV. The C exciton corresponds to a van Hove singularity where electronic bands are locally parallel between Γ and Λ points (called the “nesting” region), which is responsible for its large bandwidth.^{198,199} The A, B, and C excitons of WS₂ occurred at 2.02 eV, 2.44 eV, and 3.41 eV, respectively. The high energy absorbance maxima beyond the C transition (4.02 eV for MoS₂ and 5.35 eV for WS₂) has not been examined or attributed in the literature, but was ostensibly related to an additional exciton transition.

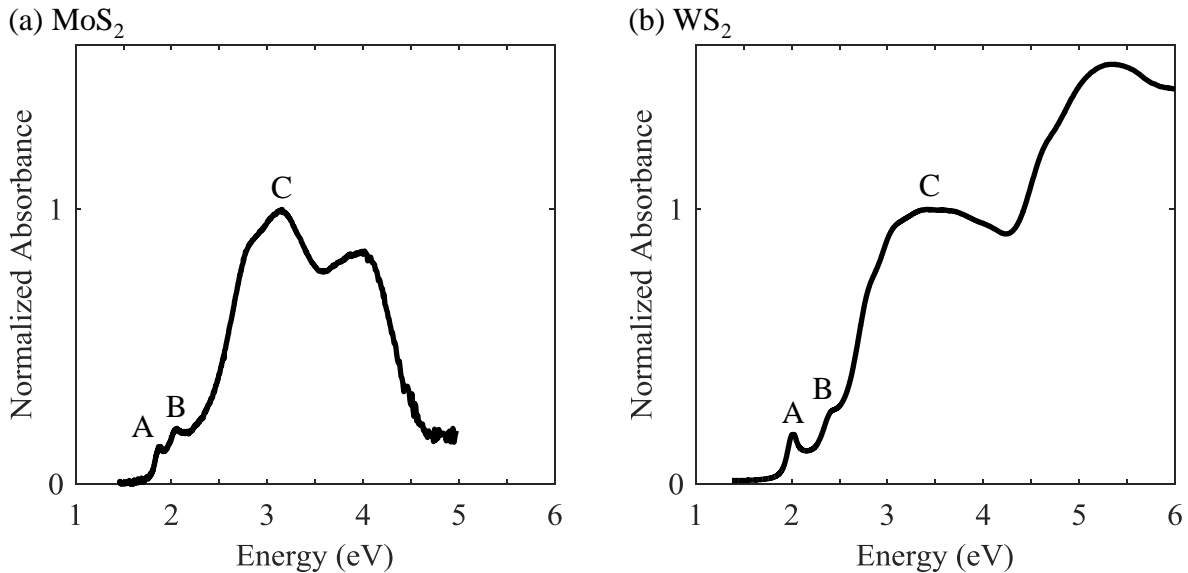


Figure 3.6: Normalized transmission UV-vis spectra of (a) MoS₂ and (b) WS₂ showing the A, B, and C exciton transitions. Spectra were each normalized to the C transition.

To confirm direct bandgap behavior and provide a benchmark for A exciton energy from high-quality monolayer MoS₂, PL was examined from CVD-synthesized MoS₂,²⁰⁰ shown in Figure 3.7. A PL peak at 1.86 eV was observed, corresponding to the A exciton and was consistent with other reports.^{187,201,202} Strong PL emission confirmed direct bandgap behavior. PL is negligible from indirect bandgap semiconductors, where electrons require assistance from phonons to jump from the valence to conduction band and thus preclude efficient radiative recombination.¹¹⁰ A small shoulder occurred around 2 eV which corresponded with the B exciton, whose emission is suppressed in monolayer TMD.⁴² CVD-grown WS₂ was not available for study.

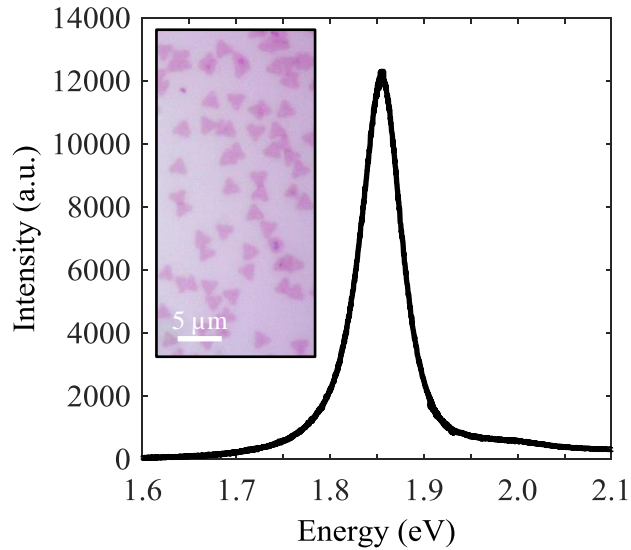


Figure 3.7: PL emission from CVD grown MoS₂ on a Si wafer with maxima at 1.86 eV. Excitation wavelength was 488 nm (2.54 eV).

Layer-dependent changes in the coupling between K electronic transitions and molecular vibrations (i.e., phonons) provided Stoke shift signals as a fingerprint of N_{TMD} . Figure 3.8 shows normalized Raman spectra of the Stoke shift signals from liquid exfoliated (dashed) and CVD-grown (solid) MoS₂,^{200,203} whose E_{2g}^1 and A_{1g} frequencies confirmed monolayer thicknesses for each. The E_{2g}^1 peak corresponds to in-plane vibrations of chalcogens against the transition metal, which are dominated by inter-layer Coulombic screening interactions.^{204,205} The A_{1g} peak

corresponds to out-of-plane opposing vibrations of chalcogens, which are dominated by van der Waals forces between layers.²⁰⁴ Liquid exfoliated MoS₂ exhibited Raman peaks at 384 cm⁻¹ and 408 cm⁻¹ for E_{2g}¹ and A_{1g} modes, respectively. The CVD-synthesized MoS₂ exhibited Raman peaks at 385 cm⁻¹ and 407 cm⁻¹ for E_{2g}¹ and A_{1g} modes, respectively; lower frequency peaks at 350-365 cm⁻¹ were noise arising from the normalization. The E_{2g}¹ and A_{1g} Raman frequencies fell within reported thresholds for monolayers.²⁰⁴ Intensity and width of Raman signatures vary arbitrarily between samples and hold no information.²⁰⁴ CVD-grown WS₂ was not available for benchmarking against liquid exfoliated WS₂.

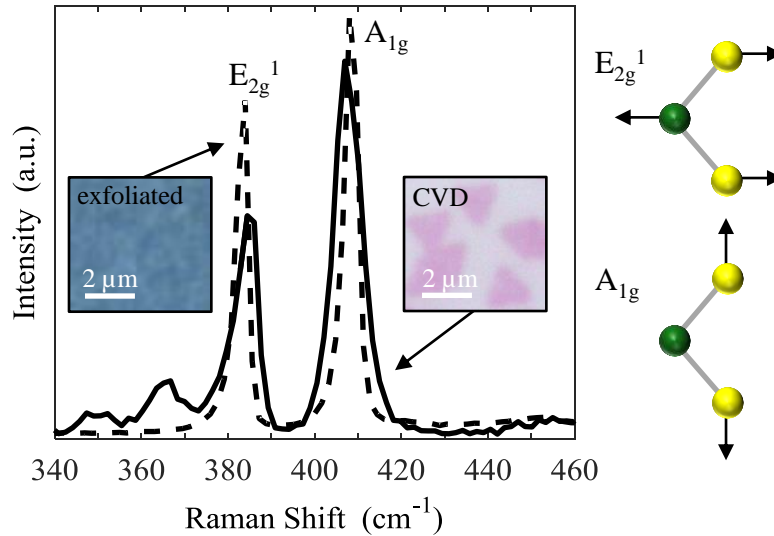


Figure 3.8: Raman spectra of liquid exfoliated (dashed) and CVD-synthesized (solid) MoS₂ on SiO_x. In-plane E_{2g}¹ and out-of-plane A_{1g} vibrational modes are labeled and shown schematically. Optical images from areas which were measured are inset. Excitation wavelength was 488 nm.

3.4 Measurement of $\chi^{(2)}$ for Monolayer Transition Metal Disulfides

Strength of second order nonlinear frequency mixing from material may be quantified by its intrinsic nonlinear susceptibility, $\chi^{(2)}$.³² Measurements of $\chi^{(2)}$ for monolayer MoS₂ and WS₂ to date⁴⁸⁻⁵² vary across 10²-10⁴ pm V⁻¹ because of reliance on indirect classical calculations based

on α -quartz references and/or Green's function, where "bulk" versus "sheet" treatment significantly impacts the calculation.⁴⁹ Models estimate $\chi^{(2)}$ at 10^2 pm V⁻¹ off-resonance and up to 10^3 pm V⁻¹ on-resonance using density functional theory (DFT) with and without a scissors correction,^{49,206} density matrix theory (DMT),⁵⁴ and the Bethe-Salpeter exciton (BSE) method.⁵³ Disagreement in $\chi^{(2)}$ spanning three orders of magnitude motivated independent, direct measurements to circumvent established indirect methods.

Hyper Rayleigh Scattering (HRS) directly measured $\chi^{(2)}$ at 523 nm herein to be 660 ± 130 pm V⁻¹ and 280 ± 18 pm V⁻¹ for liquid exfoliated MoS₂ and WS₂ monolayers, respectively.²⁰⁷ Liquid exfoliated TMD permitted use of HRS, a technique which CVD and mechanically exfoliated crystals (on which previous studies were based) cannot accommodate. HRS was originally developed to study hyperpolarizability, β , of organic molecule solutions,²⁰⁸ and has since been used to study β and $\chi^{(2)}$ of inorganic nanoparticles.^{209,210} Briefly, a polarized, 1 ns pulsed 1064 nm Nd:YAG laser (Wedge HB; Bright Solutions, Cura Carpignano, IT) was focused into a quartz cuvette containing the TMD dispersion and second harmonic (SH) signal at 532 nm was orthogonally collected without an analyzer and measured by a photomultiplier tube (PMT). See Figure 3.9 and Ref. 207 for details.

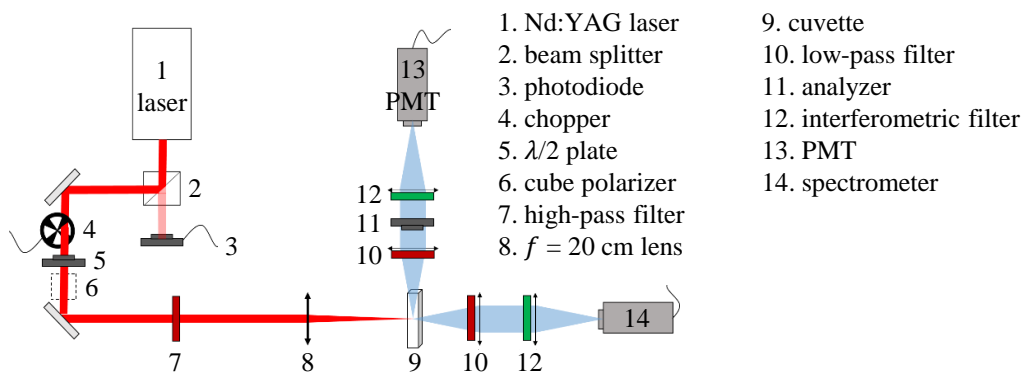


Figure 3.9: Schematic for HRS measurements of MoS₂ and WS₂ by a 1064 Nd:YAG laser.

3.4.1 Hyper Rayleigh Scattering

HRS interrogates the orientation-averaged nonlinear efficiency of nanoparticle suspensions by correlating intensity scattered SH signal with nanoparticle concentration.^{208–210} Intensity of HRS is defined as the incoherent sum of scattered SH frequencies by a composite media:

$$I_{HRS} = I_{\omega}^2 G \sum_i C_i F_i \langle \beta_i^2 \rangle \quad (\text{Equation 3.3})$$

where I_{ω} is the excitation intensity, $\langle \beta \rangle$ is the isotropic second-order hyperpolarizability of material i with concentration C , F is a local field enhancement factor, and G is an experimental constant. Unlike $\chi^{(2)}$ treatment of polarization density ($\mathbf{P}^{(2)}$) in macroscale crystals, β describes the magnitude of an induced second-order dipole moment, $\mathbf{p}_{HRS}^{(2)}$, on a subwavelength molecule driven by the local electric field, $\mathbf{E}_{loc} = F\mathbf{E}_o$, viz.

$$\mathbf{p}_{HRS}^{(2)} = \beta \mathbf{E}_{loc}^2. \quad (\text{Equation 3.4})$$

“Hyper Rayleigh Scattering” is nomenclature convention given to SH scatterers whose size fall within the subwavelength Rayleigh regime. Independent size/spatial characterization of nanoparticles comprising the ensemble permits straightforward conversion of per-nanoparticle β to bulk crystal $\chi^{(2)}$.

Second-order $\langle \beta \rangle$ for exfoliated MoS₂ and WS₂ were measured to be $4.03 \pm 0.78 \times 10^{-24}$ esu and $4.90 \pm 0.30 \times 10^{-25}$ esu,²⁰⁷ respectively, using the HRS external reference protocol with para-nitroaniline (pNA).²¹⁰ Here, I_{HRS} was recorded as a function of TMD concentration, as shown in Figure 3.10(a). To determine $\langle \beta_{TMD} \rangle$, the slope $\alpha_{TMD} = I_{\omega}^2 G F_{TMD} \langle \beta_{TMD}^2 \rangle$ was scaled against the slope for positive-control pNA with a defined $\langle \beta \rangle$, but with addition of a $e^{-\sigma_{TMD}}$ Beer-Lambert correction factor for self-absorbance of the SH by the TMD,^{211,212} viz.

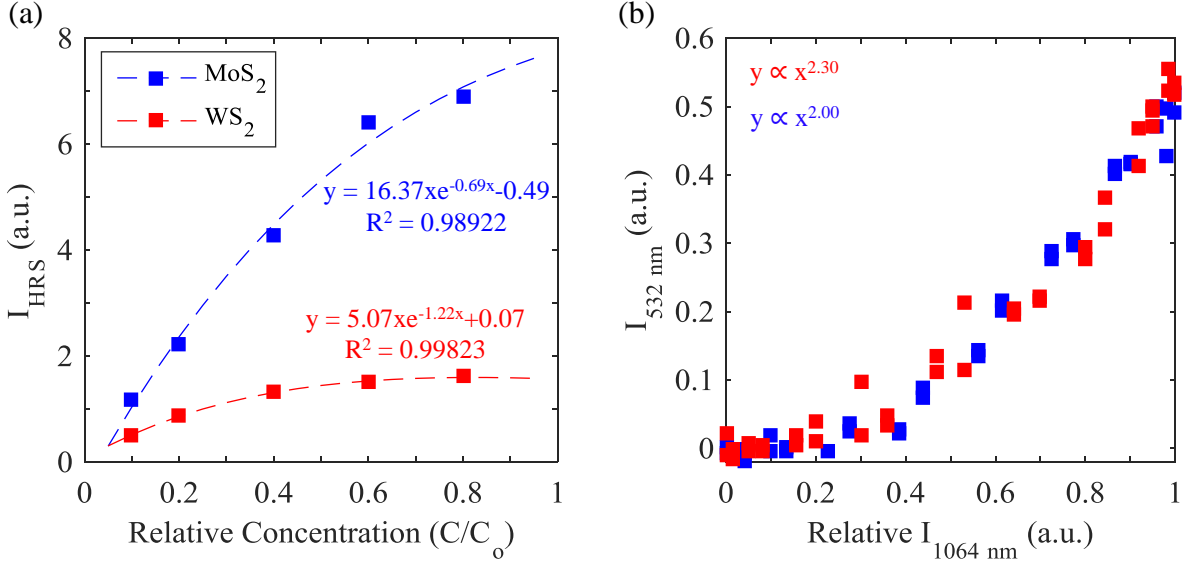


Figure 3.10: (a) HRS intensity as a function of relative MoS₂ (blue) and WS₂ (red) concentration with superposed regressions of the form $I_{HRS} = \alpha_{TMD}(C/C_o)\exp[-\sigma_{TMD}(C/C_o)] + I_{HRS-solvent}$. (b) Representative power dependence of collected signal at C_o for (i) MoS₂ and (ii) WS₂ confirming second-order nonlinear process.

$$\langle \beta_{TMD} \rangle = \sqrt{\frac{\alpha_{TMD} F_{pNA}}{\alpha_{pNA} F_{TMD} e^{-\sigma_{TMD}}} \langle \beta_{pNA} \rangle} \quad (\text{Equation 3.5})$$

The local field correction factor F_{pNA} was calculated *a priori* by the Lorentz-Lorenz correction²⁰⁸ and F_{TMD} was set to 1 since no analytic expression exists for a 2D sheet. Reference $\langle \beta_{pNA} \rangle$ used was $\sqrt{6/35} \beta_{33} = \sqrt{6/35} (25.9 \times 10^{-30} \text{ esu})$,²¹³ where $\sqrt{6/35}$ was the Kleinman weighting factor unique to vertically polarized excitation and unpolarized detection.²⁰⁸ The excitation intensity, I_ω , and experimental proportionality constant, G , (comprising e.g., collection efficiency) were unchanged between respective trials, and thus assumed constant.

Progressive dilution of the stock MoS₂ and WS₂ concentrations, $C_o = 2.7 \times 10^{11} \text{ cm}^{-3}$ and $9.6 \times 10^{12} \text{ cm}^{-3}$, respectively, gave expected linear I_{HRS} behavior at lower relative concentrations with suppressed linearity at higher concentrations by SH (2.3 eV) absorption above the direct TMD bandgap (1.87-2.02 eV). Despite Beer-Lambert absorption at higher concentrations, I_{HRS} scaled

quadratically with excitation power with coefficients ranging from 2.0-2.3 at C_o , thus confirming second-order processes [see Figure 3.10(b)].³³ Highest re-absorption was observed for WS₂ (deviations from linear behavior beginning at about $C/C_o = 0.4$), consistent with its reported higher extinction coefficient than MoS₂.²¹⁴ Linear behavior can be readily recovered, however, by dilution to lower concentrations. Dilution decreases the Beer-Lambert absorption correction $e^{-\sigma_{TMD}(C/C_o)}$ from $e^{-0.05} \approx 0.95$ back up to 1, and thus becomes a negligible factor in I_{HRS} from the TMD.²¹² Higher concentrations were included in this work for further confidence in physical significance of fitted numerical regressions, despite re-absorption of the SH.

Nonlinear regressions of the form $I_{HRS} = \alpha_{TMD}(C/C_o)e^{-\sigma_{TMD}(C/C_o)} + I_{HRS-solvent}$ performed on the MoS₂ and WS₂ HRS data readily provided necessary parameters to calculate $\langle\beta_{TMD}\rangle$. All fitted parameters with error are tabulated in Table 3.2. Common units between α_{TMD} and α_{pNA} are required prior to use of Equation 3.5, and thus each were normalized to their respective C_o (Avogadro's number for α_{pNA}). The y-axis intercept from the origin calculated by the nonlinear regression intrinsically represented the near-zero SH contribution from the solvent (aqueous sodium cholate) and quartz cuvette.

Table 3.2: Summary of parameters extracted for numerical regressions of the form $y = Axe^{-Bx} + C$ for TMD and linear regressions of the form $y = Ax + C$ for pNA. Data for MoS₂ and WS₂ were taken at different powers and thus pNA data at each respective power was recorded.

| | A | | B | C |
|------------------|---------------------------------------|-------------------------------------|-----------------|------------------|
| | relative to C/C_o | relative to C_o | | |
| MoS ₂ | 16.3709 ± 4.3698 | 6.1207 ± 1.6338 × 10 ⁻¹¹ | 0.6853 ± 0.2725 | -0.4905 ± 0.6401 |
| pNA | 2.0380 ± 0.1126 | 3.3840 ± 0.1870 × 10 ⁻²¹ | - | -0.0689 ± 0.0207 |
| WS ₂ | 5.0719 ± 0.4177 | 5.2722 ± 0.0430 × 10 ⁻¹³ | 1.2190 ± 0.0775 | 0.0665 ± 0.0537 |
| pNA | 2.0206 ± 0.0956 | 3.3550 ± 0.1590 × 10 ⁻²¹ | - | 0.2735 ± 0.0149 |

3.4.2 Orientation-Averaged $\chi^{(2)}$ Coefficients

The $\chi^{(2)}$ at 532 nm (i.e., 2ω of 1064 nm) for MoS₂ and WS₂ was calculated to be 660 ± 130 pm V⁻¹ and 280 ± 18 pm V⁻¹, respectively.²⁰⁷ Although β expresses second-order nonlinear efficiency on a per-nanoparticle basis, $\chi^{(2)}$ is an intrinsic property of said material and allows direct correspondence with CVD crystals. In the absence of SH surface contributions to I_{HRS} , β is readily converted to $\chi^{(2)}$ by

$$\langle \chi^{(2)} \rangle = \frac{2\langle \beta \rangle}{V} \quad (\text{Equation 3.6})$$

where V is the nanoparticle volume with non-centrosymmetric crystal structure (extracted herein from Figure 3.6 and Equations 3.1 and 3.2).²¹⁰ Second-order nonlinear processes rely on crystalline non-centrosymmetry of odd-layered TMD; even-layered stacking suppresses second-order response by inversion symmetry restoration.^{50,169} Monolayer TMD exhibit D_{3h} point-group symmetry giving a single non-zero $\chi^{(2)}$ tensor element $\chi_{xxx}^{(2)} = -\chi_{xyy}^{(2)} = -\chi_{yyx}^{(2)} = -\chi_{yxy}^{(2)}$, where x and y are crystal axes. Thus, brackets indicating orientational averaging were neglected for the special case of monolayer TMD since finite $\chi^{(2)}$ originated from the same tensor element.

Measured $\chi^{(2)}$ by HRS agreed well with other reported experimental and theoretical estimates. Table 3.3 summarizes measured and calculated $\chi^{(2)}$ using a variety of methods for both MoS₂ (row 1) and WS₂ (row 2) monolayers. By comparison to the measured 660 pm V⁻¹ $\chi^{(2)}$ for MoS₂, experimental estimates spanning 20-400 pm V⁻¹ have been calculated by scaling MoS₂ SH generation (SHG) intensity to an α -quartz reference;^{49,50} theoretical estimates by DFT, DMT, and BSE indicate 400-900 pm V⁻¹.^{49,53,54,206} By comparison to the measured 280 pm V⁻¹ $\chi^{(2)}$ for WS₂, the one reported work to date estimated 170 pm V⁻¹ via DFT and measured 9000 pm V⁻¹ at 416 nm via a sophisticated Green's function calculation.⁵² No measurements of SHG from WS₂ by

1064 nm irradiation have been reported for a direct comparison. Other studies measuring SHG from TMD monolayers were limited to 810 nm irradiation,^{48,51} and thus their $\chi^{(2)}$ estimations could not be directly compared herein.

Table 3.3: Literature comparison of measured and calculated $\chi^{(2)}$ values at 532 nm (2ω of 1064 nm excitation) for monolayer MoS₂ and WS₂.

| | HRS [pm V ⁻¹] | Measured [pm V ⁻¹] | | Simulated [pm V ⁻¹] | | |
|---|---------------------------|--------------------------------|---------------------------|---------------------------------|-------------|-------------|
| | | α -quartz ext. ref. | Green's function | DFT | DMT | BSE |
| MoS ₂ | 660±130 | 20-400 [49,50] | - | 400 [†] [49,205] | 400 [54] | 900 [53] |
| WS ₂ | 280±17 | - | 9000 [‡] [52] | 170 [52] | - | - |
| [†] with and without scissors correction [‡] taken at 416 nm; no measured 532 nm values reported to date | | | | | | |

Measured $\chi^{(2)}$ for MoS₂ and WS₂ herein may have been lower-end estimates due to the wide size/thickness heterogeneity of TMD crystals inherent to exfoliated dispersions, despite significant distribution reduction from the cascade centrifugations. Recent reports indicate SHG intensity exponentially decays with N_{TMD} in odd-layer TMD crystals, e.g., a 50% reduction for trilayer (from 1/3 $\chi^{(2)}$ reduction²⁰⁶) and an 80% reduction for pentalayer versus the monolayer signal.¹⁶⁹ Crystalline inversion symmetry in even-layered TMD suppresses SHG, in the absence of an electrical bias.²¹⁵ Therefore, it was inevitable some TMD crystals comprising the liquid exfoliated dispersion contributed little or no SH signal to the penultimate I_{HRS} from which β and $\chi^{(2)}$ were obtained. Importance of sample preparation for HRS experiments has been detailed.²¹⁰

3.4.3 Discrete Dipole Computation of $\chi^{(2)}$ via Miller's Rule

A nonlinear extension of approximate discrete dipole Maxwell's equations (i.e., DDA) via Miller's rule estimated $\chi^{(2)}$ at 532 nm for MoS₂ to be 460 pm V⁻¹, which was within a factor of 2

of HRS measurements.²⁰⁷ Miller's rule states that the ratio between nonlinear $\chi^{(2)}$ and the product of linear susceptibilities, χ , at the input and output frequencies is nearly constant for all non-centrosymmetric condensed matter.^{33,216} In other words, the nonlinear response is directly related to the linear response scaled by a proportionality factor. The DDA readily calculates linear polarizability, α ,⁹² and extensively χ , by the Lattice Dispersion Relation.¹⁰¹ Thereby DDA offered an accessible, *a priori* method to evaluate second-order nonlinear optical behavior at significantly less computational cost than DFT, DMT, or BSE provided (i) availability of a dielectric function and (ii) lack of crystalline inversion symmetry.

Linear polarizability of a 2D rectangular sheet of MoS₂ was calculated by DDSCAT v7.3.^{90,100} Its translation to $\chi^{(2)}$ assumed $\Im(\alpha)$ due to its relation to photon scattering.⁷⁴ Dielectric data for monolayer MoS₂ was taken from Mukherjee *et al.*²¹⁷ Absence of a rigorous dielectric function for monolayer WS₂ precluded its corresponding evaluation. The Miller proportionality factor is a function of material constants: free space permittivity ϵ_0 , electron mass m , carrier density $N \sim 10^{22} \text{ cm}^{-3}$, electron charge e , and some nonlinear strength coefficient a . Equation 3.7 expresses Miller's rule in the context of SHG.³³

$$\chi_{2\omega}^{(2)} = \frac{\epsilon_0^2 m a}{N^2 e^3} \chi_{2\omega}(\chi_\omega)^2 \quad (\text{Equation 3.7})$$

Charge displacement from equilibrium in a nonlinear Lorentz oscillator can be estimated to be on the order of inter-atomic separation, d , such that $a \sim \omega_o^2/d$, where ω_o is some resonant oscillation frequency.³³ The C exciton transition for MoS₂ was assumed for ω_o (because of its proximity within the 2ω spectrum) and 2.7 Å for d (corresponding to {100} planes).²¹⁸

Frequency dependence of $\chi^{(2)}$ for monolayer MoS₂ arising from its expanded density of states around the C transition due to its van Hove singularity is shown in Figure 3.11. At 532 nm, $\chi^{(2)}$ was calculated to be 460 pm V⁻¹, within a factor of 2 of the HRS measurement (blue square).

A 1642 pm V^{-1} maxima occurred at 444 nm , coinciding with the C transition. Theoretical estimates by DFT with and without scissors correction (Δ_{SCI}), DMT, and BSE also found close relation between $\chi^{(2)}$ and the C exciton in this spectral region,^{49,53,54,206} consistent with these data and those measured by Malard *et al.*⁵⁰ Lack of interband transitions above 700 nm ($\leq 1.77 \text{ eV}$) minimized impact of χ_{ω} on $\chi_{2\omega}^{(2)}$ despite quadratic dependence in Equation 3.7. Direct absorption at the 660 nm A transition resulted in an intense $\chi^{(2)}$ resonance at higher energy wavelengths, but this regime was not accessible by conventional laser/detection metrology.

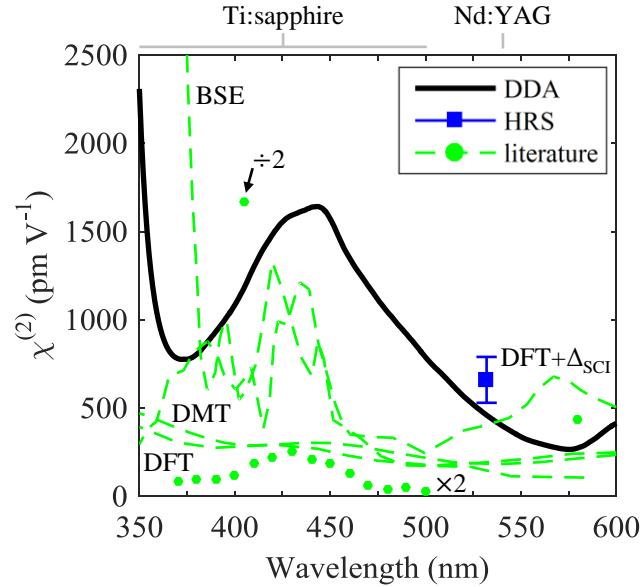


Figure 3.11: Frequency dependent $\chi^{(2)}$ spectra for MoS_2 calculated by DDA via Miller's rule. Measured value at 532 nm by HRS is superposed. Literature measurements (circles) and theoretical calculations (dashed lines) from DFT, $\text{DFT}+\Delta_{\text{sci}}$, DMT, and BSE are also superposed for comparison. Frequencies accessible by Ti:sapphire and Nd:YAG lasers are marked.

3.5 Summary

The linear and extraordinary nonlinear optical properties of 2D MoS_2 and WS_2 , the sulfide class of group-IV TMD, were examined using transmission UV-vis, PL, and Raman spectroscopies and HRS. Fabrication of monolayer TMD crystals by natural exfoliation (specifically, by liquid

means) and synthetic CVD was described. Transmission UV-vis and PL spectroscopies revealed three direct optical transitions in the electronic band structure of MoS₂ and WS₂. Raman spectroscopy confirmed monolayer TMD thicknesses by in-plane and out-of-plane phonon interactions unique to monolayers. HRS experiments of nonlinear SHG from liquid exfoliated MoS₂ and WS₂ permitted their first direct $\chi^{(2)}$ measurement of 660 ± 130 pm V⁻¹ and 280 ± 18 pm V⁻¹ at 532 nm, respectively, and was corroborated by an elegant Miller's rule adaptation to the linear DDA. Overall, the linear and nonlinear optoelectronic properties of 2D TMD monolayers were surveyed and measured for their use in optoelectronics.

CHAPTER 4

INTERFACING MONOLAYER TRANSITION METAL DICHALCOGENIDES WITH NANOANTENNAS

Decorating transition metal dichalcogenide (TMD) field-effect photodetectors,^{57,219–221} photocatalysts,^{30,58,222,223} and solar photovoltaic cells²²⁴ with metal nanoantennas has demonstrably improved their performance, ostensibly through augmented charge separation and photodoping. Nanoantennas can enhance emission from TMD up to 10x by optimizing plasmon-exciton coupling.^{219,221,225,226} However, phonon scattering,²⁰ photo-induced doping from plasmonic hot electrons,¹⁶ and inherent quenching²²⁷ limit TMD emission enhancements by surface plasmons. Advancement beyond initially promising prototypes has been constrained by inability to interpret experimental results with compact, experimentally validated models. The discrete dipole approximation (DDA) was introduced herein to characterize predominant optoelectronic modes observed in transmission UV-vis extinction spectra of TMD-nanoantenna heterostructures.

4.1 Fabrication Techniques

Plasmonic nanoantennas were interfaced with liquid exfoliated TMD by (i) top-down drop-casting²²⁸ and (ii) bottom-up *in situ* chemical methods.²²⁹ Use of liquid suspensions of TMD (i.e., liquid exfoliated) and nanoantennas (i.e., colloidal dispersions from wet-chemical synthesis) allowed facile, economical heterostructure formation onto a variety of substrates. Heterostructure samples were deposited onto silica (SiO_x) for spectroscopic characterization by a bright-field optical microscope (Eclipse LV100; Nikon Instruments, Melville, NY USA) coupled to a spectrometer (Shamrock 303; Andor Technology, Belfast, UK) and/or transmission electron microscopy (TEM) analysis (Titan³ 80-300; FEI, Hillsboro, OR USA).

4.1.1 Drop Cast

Gold (Au) nanospheres and silver (Ag) nanoprisms were drop-cast onto monolayer molybdenum disulfide (MoS_2) covered SiO_x glass.²³⁰ Au nanospheres 76 ± 13 nm in diameter with poly(vinylpyrrolidone) (PVP) ligand (GEPE75; nanoComposix, San Diego, CA USA) were dispersed in isopropanol to a concentration of 2.3×10^9 mL^{-1} . Ag nanoprisms 53 ± 19 nm in edge length and 10 nm thickness with PVP ligand (SPPN550; nanoComposix, San Diego, CA USA) were dispersed in 5 mM aqueous sodium borate to a concentration of 1.6×10^{11} mL^{-1} . Substrates were cleaned in 25% nitric acid for 30 minutes to improve their hydrophilicity, rinsed in distilled-deionized water, and dried under nitrogen gas. MoS_2 was deposited onto preheated SiO_x by a 1.5 μL drop. Successively, MoS_2 -covered SiO_x substrates were heated to 90°C (105°C) for additional drop-cast of 5 μL (10 μL) volumes of Au-isopropanol (Ag-water). The pre-heat rapidly evaporated solvent to minimize aggregation from contact-line pinning. See Ref. 230 for details.

Visual and spectroscopic examples of singularly drop-cast (a) MoS_2 , (b) Au nanospheres, and (c) Ag nanoprisms are shown in Figure 4.1, exhibiting no apparent signs of aggregation. Optical images were taken in bright-field reflection mode with a 100x objective. Insets in (a) shows Raman and (b)-(c) transmission UV-vis extinction spectra of the imaged areas. The in-plane E_{2g}^1 and out-of-plane A_{1g} Raman modes for deposited MoS_2 were measured to be 384 cm^{-1} and 408 cm^{-1} ,²⁰³ respectively, confirming no aggregation.²⁰⁴ Localized surface plasmon resonances (LSPR) of Au nanospheres and Ag nanoprisms were measured at 561 nm and 687 nm, respectively, in agreement with cuvette measurements; aggregation causes LSPR red-shifts. Although deposited MoS_2 altered the SiO_x surface hydrophilicity prior to forming heterostructures with nanoantennas, no spectral signatures appeared from accrued aggregation beyond the pristine SiO_x surface (to be detailed in forthcoming sections).

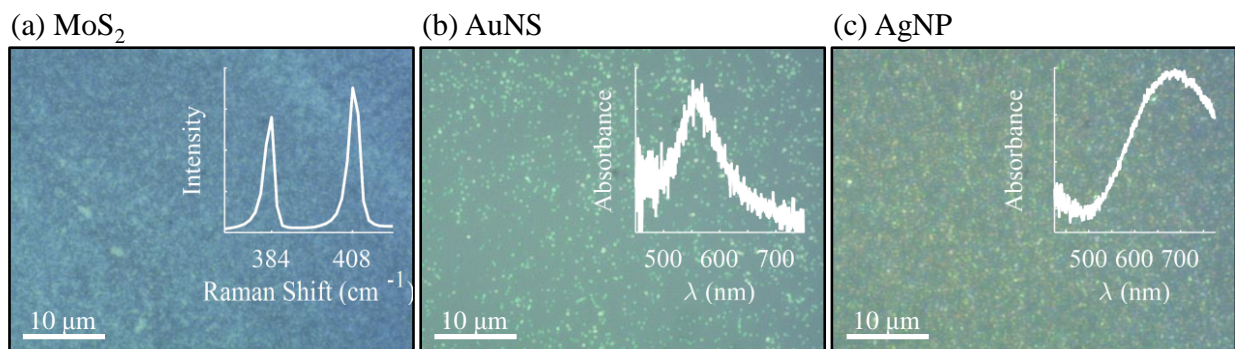


Figure 4.1: Optical bright-field images taken at 100x objective magnification of (a) mono- to few-layer MoS₂, (b) Au nanospheres (AuNS) with 76 ± 13 nm diameter, and (c) Ag nanoprisms (AgNP) with 53 ± 19 nm edge length drop-cast deposited onto SiO_x. Upper insets show (a) Raman and (b)-(c) transmission UV-vis extinction spectra.

4.1.2 *in situ* Chemical Reduction

Stochastic distributions of quasistatic gold nanoantennas were grown *in situ* onto liquid exfoliated tungsten disulfide (WS₂) by a batch chemical reduction process,²²⁹ shown in Figure 4.2. Gold chloride (AuCl₃; 334049; Sigma Aldrich, St. Louis, MO USA) was added in bulk to aqueously stabilized WS₂ (see § 3.2.1), whereby Au was reduced to form nanoantennas preferentially at the edges of the WS₂ crystals. Figure 4.3(a)-(c) show aberration-corrected TEM images of three representative Au-decorated WS₂ crystals used in this work. The 2.3 Å (111) Au constant and 1.6/2.7 Å {110}/{111} WS₂ constants were measured by fast-Fourier transform (FFT) in Figure 4.3(d).

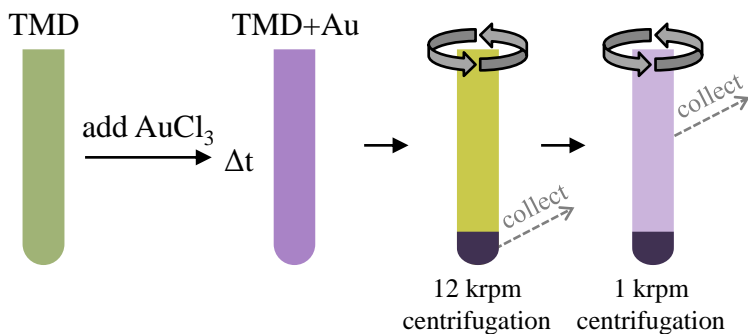


Figure 4.2: Process schematic for *in situ* decoration of liquid exfoliated TMD crystals with AuNA. Gold salt was added to aqueously suspended WS₂ to nucleate/grow AuNA at the edges of the WS₂ crystals. Subsequent centrifugation steps removed residual Au salt and bulk Au.

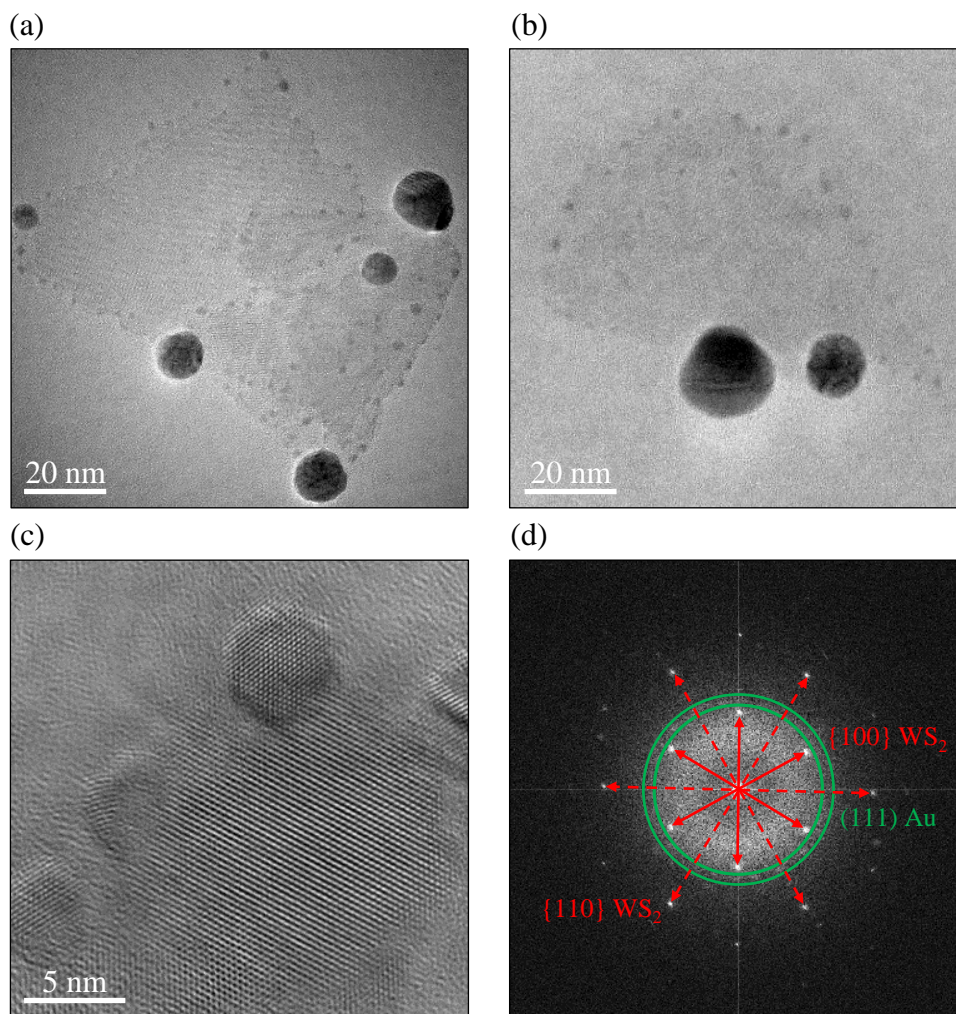


Figure 4.3: (a)-(c) Aberration-corrected TEM images of increasing magnification and (d) FFT of liquid exfoliated WS₂ crystals decorated *in situ* with AuNA.

Dangling sulfur atoms predominantly at the WS₂ crystal edges and basal plane lattice defects served as reduction sites for Au nucleation.²³¹ Growth of nucleated Au into nanoantennas was controlled by the stoichiometric ratio between AuCl₃ and WS₂. A relatively low 1 stoichiometric ratio was chosen herein to promote growth of few Au nanoantennas (AuNA) to 15-30 nm diameter and numerous sub-5 nm nanoantennas. A wide-range exploration of process parameters on the outcome of Au-decorated WS₂ is detailed in Ref. 229. This protocol served as an alternative to drop-cast methods, but ongoing refinement of the chemistry prevented its use

throughout this work. Protocols for *in situ* decoration of MoS₂ with Au, Ag, palladium, and platinum sans covalent bonding have also been described.^{58,222,232}

4.2 Discrete Dipole Model

Far-field optical extinction spectra showing LSPR and bandgap excitation modes of nanoantenna-MoS₂ heterostructures were modeled using the DDA solutions to Maxwell's equations.²³⁰ A single (i) AuNS of 76 nm diameter and (ii) triangular AgNP of 53 nm (assumed equilateral) edge length with 10 nm height were each discretized into a cubic lattice of point dipoles according to their Cartesian description and placed onto a two-dimensional (2D), dipole-discretized circular plane of MoS₂ atop a SiO_x cylinder. Each dipole was susceptible to electromagnetic polarization by a polarized plane wave according to its specified dielectric function (Au/Ag¹¹³ or MoS₂²¹⁷). Maxwell's equations were solved by DDSCAT v7.3.¹⁰⁰⁻¹⁰² The SiO_x cylinder was given a radius and height equal to twice the nanoantenna radius based on the plasmonic decay length;^{97,233} surface plasmons only “see” media within approximately one nanoantenna radius beyond its surface.¹⁰⁶ Figure 4.4 shows the corresponding target heterostructures, discretized for the DDA.

Little precedent existed for use of DDA to accurately simulate optics of 2D materials at the time of this work. Metal-graphene heterostructures were modeled with the DDA beginning in 2014,^{234,235} but were not corroborated with experimental results. Boundary element method (BEM) and finite difference time domain (FDTD) algorithms appeared concomitantly with this work to study Au-TMD heterostructures, but were limited to estimating strength of local plasmonic electric fields.^{221,236} Open-source DDA (i) significantly reduced computational requirements (e.g., time and memory) over BEM and FDTD and (ii) was not limited to geometries whose volumes

may be approximated as one-dimensional surface contour, as in BEM. Neither DDA, BEM, or FDTD can represent TMD edge states²³⁷ because of their classical dielectric function treatment, as opposed to spatial electron density utilized in density functional theory (DFT) models.

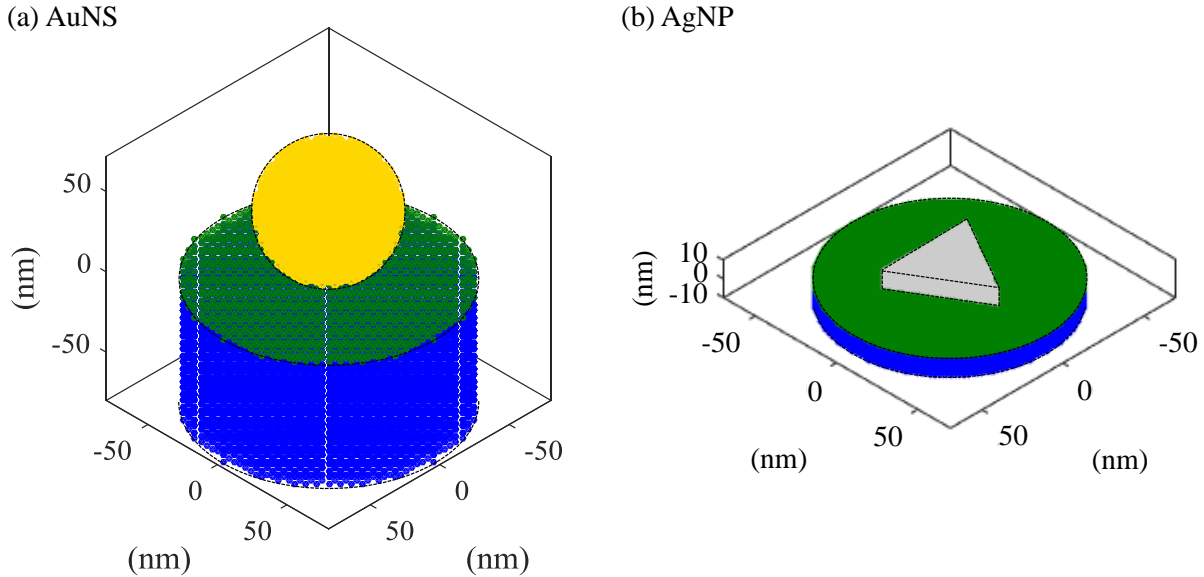


Figure 4.4: DDA targets of (a) 76 nm Au nanosphere and (b) 53 nm Ag nanoprism on a monolayer of MoS₂ atop a SiO_x substrate. Inter-dipole spacings were 4 nm and 1 nm, respectively. Point dipoles comprising the target are illustrated as spheres: yellow represents Au, gray represents Ag, green represents MoS₂, and blue represents SiO_x.

4.3 Interfacing with Gold Nanospheres

Interfacing monolayer MoS₂ with 76±13 nm Au nanospheres resulted in a hybridized optical extinction spectra with a 4 nm red-shifted LSPR from MoS₂ screening whose bandwidth was expanded 19%, indicative of augmented damping from the MoS₂.²³⁰ Figure 4.5(a) shows measured (solid, LHS axis) and calculated (dashed, RHS axis) optical extinction spectra for a 76 nm diameter Au nanosphere on monolayer MoS₂ atop a SiO_x substrate (black data). Maximas corresponding to nanosphere LSPR and the A exciton of MoS₂ were observed at 566 nm and 670 nm (1.85 eV), respectively. The B exciton was not observable because of the higher intensity

LSPR. For comparison, optical extinction spectra are also shown for independently deposited Au nanospheres (red) and MoS₂ (green). All spectral features were observed in triplicate or greater in multiple areas of each sample to verify reproducibility.

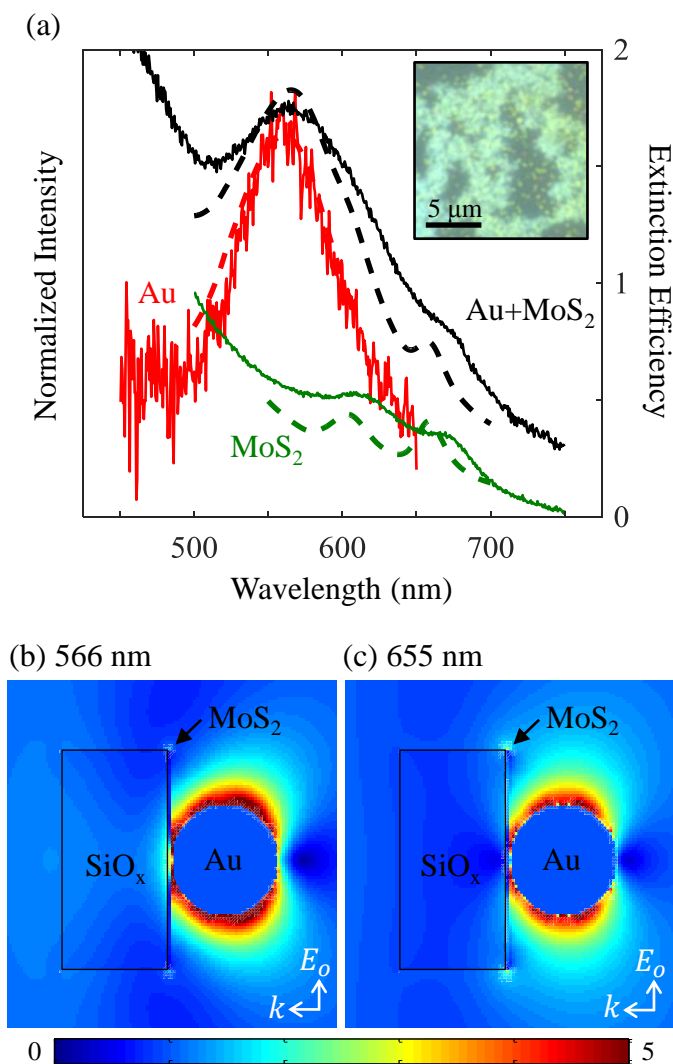


Figure 4.5: Optical response of Au nanosphere-decorated monolayer MoS₂. (a) Optical extinction spectra measured by transmission UV-vis spectroscopy (solid) and calculated by the DDA (dashed) for a 76 nm diameter Au nanosphere (red), monolayer MoS₂ (green), and 76 nm Au nanosphere-decorated MoS₂ (black). Inset shows representative optical bright-field image taken at 100x objective magnification. Enhanced electric near-field plots at (b) 566 nm and (c) 655 nm represent nanoantenna LSPR and monolayer MoS₂ A exciton, respectively. Field within the Au nanosphere was set equal to 1.

Optical extinction spectra for the Au nanosphere-MoS₂ heterostructure calculated by the DDA were consistent with the measured spectra.²³⁰ Predicted LSPR and A exciton resonances of the heterostructure at 566 nm and 657 nm (1.89 eV) were within 1% and 2%, respectively, of their measured wavelengths. A 556 nm LSPR was reported previously for a 60 nm Au nanosphere on monolayer MoS₂ under electron excitation.⁵⁸ The A exciton transition blue-shifted by 4 nm (0.01 eV) to 655 nm (1.89 eV) relative to the MoS₂ monolayer control, consistent with reported PL spectra of MoS₂ after addition of Au nanoshells.²¹⁹ Absorption enhancements of the A and/or B exciton transitions were not evident, e.g., the LSPR overlaid the B exciton and prevented further analysis. FDTD simulations of 150 nm AuNS on MoS₂ suggest little far-field absorption enhancement of exciton features by surface plasmons.²³⁶ The A and B bandgaps were simulated to occur ca. 30 meV higher than measurements, attributable to differences between the liquid-exfoliated MoS₂ used herein versus CVD-grown MoS₂ employed as the basis for dielectric data incorporated into the DDA.²¹⁷ Previous reports for A exciton energy for CVD-grown monolayer MoS₂ span a 60 meV range from 1.82-1.88 eV,^{187,202,217,238} likely due to contaminants accrued from preparation/handling protocols.²³⁹

Excitation of different resonant modes of the Au nanosphere-MoS₂ heterostructure, specifically the LSPR and A exciton, and their unique energy localization characteristics were captured in electric near-field enhancement maps of Figure 4.5(b) and 4.5(c).²³⁰ Excitation of the 566 nm LSPR exhibited electric field enhancement within the MoS₂ monolayer from the plasmonically-excited Au nanosphere. Enhancement magnitude decreased laterally away from their contact point. Concomitantly, the LSPR bandwidth in Figure 4.5(a) expanded ca. 15%. This suggested accrued plasmon damping from the MoS₂ was represented in the near-field map, possibly through radiative scattering and/or nonradiative transport of plasmonic hot

electrons.^{16,22,240} Electron injection from metal nanocubes into semiconductors was recently inferred from electron-excitation DDA.²⁴¹ Imaginary component of dielectric functions empirically represent total Drude damping comprising electron-electron scattering, electron-phonon scattering, and scattering by crystalline defects.¹¹⁰ However, whether the classical DDA could represent quantum-mechanical changes in electron mass between two distinct materials over time remained uncertain. An experimental estimate of possible plasmonic hot electron transport was not made because of the intrinsic LSPR bandwidth expansion arising from variation in Au nanosphere diameters.²⁴²

Direct bandgap excitation across the A transition was represented as a ca. 1.5 electric field enhancement factor within the MoS₂ monolayer, shown in Figure 4.5(c). Little to no energy transfer was apparent from the semiconducting MoS₂ to the insulative SiO_x or conductive Au. A dipole was formed across the nanosphere, but was not a LSPR. Electrostatic charge polarization in response to the incident plane wave formed the dipole to satisfy Coulomb's law.³¹

Agreement between the DDA and experimental data was verified independently against measured photocurrent by Lin *et al.* for a four-layer MoS₂ field-effect transistor decorated with 15 nm Au nanospheres,⁵⁷ shown in Figure 4.6. A DDA target consisting of a single 16 nm Au nanosphere supported by four stacked layers of monolayer MoS₂ on top of a SiO₂ substrate in an effective refractive index of 1.35 (to account for citrate coating) was constructed based on the description of Lin *et al.* in Ref. 57. Although the given dielectric function for MoS₂ was based on a monolayer, the difference between the A and B exciton energies of a single- versus four-layer differ by less than 10 meV.⁴² Reported spectral photocurrent maxima at 540, 600, and 660 nm were attributable to LSPR, B exciton, and A exciton resonances using DDA. The 540 nm

photocurrent maxima had been inferred by Lin *et al.* to result from plasmonic activity based on a 517 nm LSPR measured from a liquid suspension of the Au nanospheres in a cuvette.

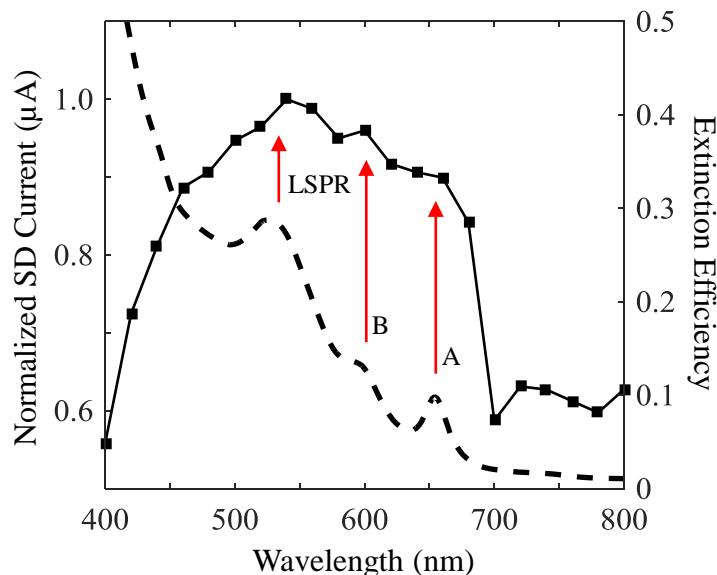


Figure 4.6: Measured source-drain (SD) photocurrent (squares) from 400 nm – 800 nm irradiation of a four-layer MoS₂ field-effect transistor decorated with 15 nm diameter Au nanospheres from Lin *et al.* in Ref. 57. Optical extinction efficiency spectra generated from the DDA is superposed (dashed). LSPR and A/B exciton features are labeled.

4.4 Interfacing with Silver Nanoprisms

Interfacing MoS₂ with 53±19 nm Ag nanoprisms resulted in an 87 nm LSPR red-shift, due to MoS₂ screening, to an energy beneath the A and B exciton transitions whose absorptions appeared enhanced.²³⁰ In contrast to the Au nanospheres, the Ag nanoprisms featured (i) more surface area contact with MoS₂, (ii) lower energy LSPR, and (iii) multiple bright surface plasmon modes. Figure 4.7(a) shows measured (solid, LHS axis) and calculated (dashed, RHS axis) optical extinction spectra for a 53 nm edge length Ag nanoprism on monolayer MoS₂ atop a SiO_x substrate (black data). Maxima corresponding to orientation-averaged nanoprism LSPR was observed at 774 nm. The A and B excitons were not apparent because of the higher intensity LSPR. For

comparison, optical extinction spectra are also shown for independently deposited Ag nanoprisms (red) and MoS₂ (green). All spectral features were observed in triplicate or greater in multiple areas of each sample to verify reproducibility.

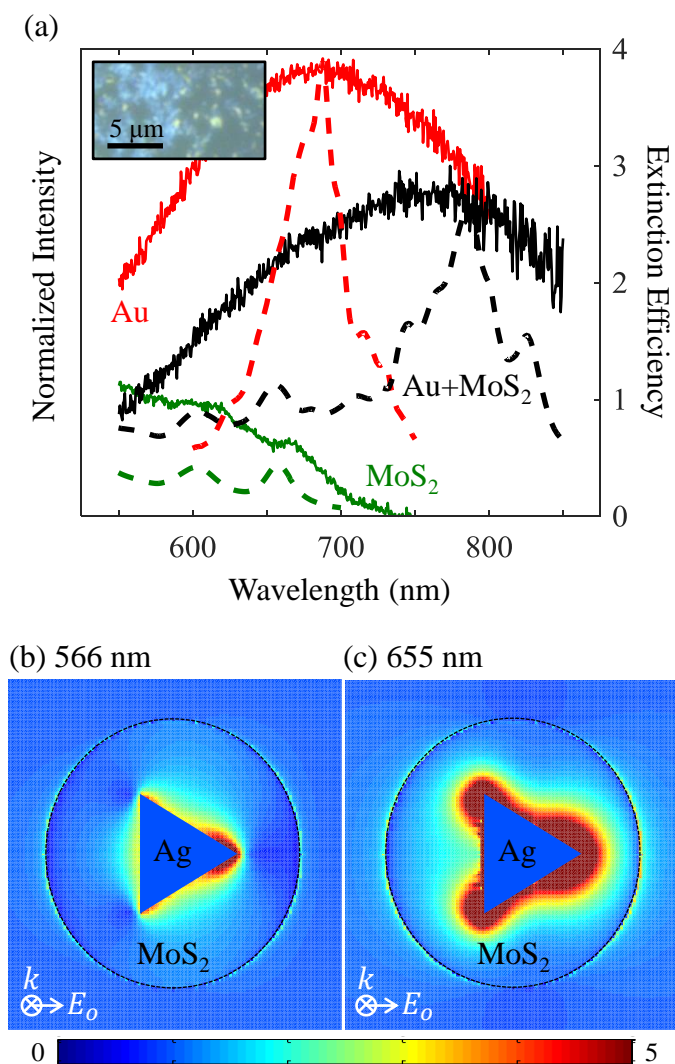


Figure 4.7: Optical response of Ag nanoprism-decorated monolayer MoS₂. (a) Optical extinction spectra measured by transmission UV-vis spectroscopy (solid) and calculated by the DDA (dashed) for a 53 nm edge length Ag nanoprism (red), monolayer MoS₂ (green), and 53 nm Ag nanoprism-decorated MoS₂ (black). Inset shows representative optical bright-field image taken at 100x objective magnification with 5 μm scale. Enhanced electric near-field plots at (b) 655 nm and (c) 788 nm represent monolayer MoS₂ A exciton and nanoantenna LSPR, respectively. Field within the Ag nanoprism was set equal to 1.

Optical extinction spectra for the Ag nanoprism-MoS₂ heterostructure calculated by the DDA were consistent with the measured spectra, albeit with evident exciton transitions and narrower LSPR bandwidth.²³⁰ Calculated spectra were averaged over 0° and 90° polarizations to reflect their random orientation following deposition.⁹⁷ Predicted LSPR, A exciton, and B exciton features of the heterostructure at 788 nm, 655 nm (1.89 eV), and 603 nm (2.06 eV) were within 2% of their measured wavelengths. Extinction intensity of the A exciton was enhanced by 20% after introduction of the Ag nanoprism. As described in § 4.3, the A and B bandgaps were simulated ca. 30 meV higher than measurements, attributable to differences between the liquid-exfoliated MoS₂ used herein versus CVD-grown MoS₂ used to obtain the dielectric function.²¹⁷

Measured LSPR bandwidth was much wider than the simulated bandwidth because of large variation in Ag nanoprism sizes versus the single size considered in the DDA. Optical averaging of LSPR unique to each Ag nanoprism size/geometry comprising the ±35% size distribution (i.e., edge lengths, equilaterally, vertex truncations) contributed to the bandwidth difference. Impacts of triangle edge length and vertex truncation on LSPR of nanoprisms has been detailed elsewhere.^{97,233,243} For example, it has been shown that a 10 nm vertex truncation can blue-shift the LSPR of a nanoprism by almost 200 nm.⁹⁷ Notwithstanding this anticipated variance, the DDA accurately calculated the central resonant wavelength using mean edge length.

Excitation of the dominant LSPR and A exciton modes of the Ag nanoprism-MoS₂ heterostructure and their unique energy localization characteristics were captured in electric near-field enhancement maps of Figure 4.7(b) and 4.7(c) taken at the Ag-MoS₂ interface.²³⁰ Direct bandgap excitation across the 655 nm (1.89 eV) A transition was represented as a ca. 1.5 electric field enhancement factor throughout the MoS₂ monolayer, shown in Figure 4.7(b). A dipole was formed across the nanoprism, but was not a LSPR. Again, electrostatic charge polarization in

response to the incident plane wave formed the dipole to satisfy Coulomb's law.³¹ The B exciton was not examined despite its prevalence in the spectra.

Excitation of the 788 nm LSPR indicated a dipolar profile, matching other reports, with apparent electric field enhancement within the MoS₂ monolayer. Concomitantly, the LSPR bandwidth in Figure 4.7(a) expanded ca. 19%. This suggested accrued plasmon damping from the MoS₂ was represented in the near-field map, possibly by radiative scattering and/or nonradiative transport of plasmonic hot electrons.^{16,22,240} Larger bandwidth expansion for the Ag nanoprisms versus the Au nanospheres was consistent with the increased surface area contact (i.e., more interaction with the MoS₂). Similar results were found using solely 0° or 90° polarization, showing Γ expansion was consistent independent of plasmon mode type. Related FDTD simulations report the LSPR electric field enhancement factor of Ag nanodisc-MoS₂ heterostructure corresponded directly with its measured PL enhancement factor.²⁴⁴ Again, experimental estimate of plasmonic hot electron transport quantum efficiency was not made because of intrinsic LSPR bandwidth expansion from wide variation in nanoprism sizes/geometries.²⁴²

4.5 Summary

Transmission UV-vis spectroscopy and DDA were used in parallel to characterize the origin of and interactions between resonances in heterostructures of monolayer MoS₂ and Au/Ag nanoantennas. Top-down drop-casting and bottom-up *in situ* synthesis of metal-TMD heterostructures was described. The DDA was introduced as a compact electrodynamic model to describe the linear optoelectronic interactions in metal-TMD heterostructures. Agreement was benchmarked within 2% against experimental transmission UV-vis extinction spectra. Calculated optical extinction spectra revealed (i) LSPR of nanospheres and nanoprisms modulated by MoS₂

screening and (ii) MoS₂ exciton transitions whose absorption were enhanced, depending on proximity to the nanoantenna LSPR. Energy localization and transport between the nanoantennas and MoS₂ was represented in electric near-field plots. Overall, the DDA was introduced as a guiding model to optimize fabrication and electrodynamic description of nanoantenna-decorated TMD monolayers for optoelectronic implementations.

CHAPTER 5

ENERGY CONVERSION BY PLASMONIC HOT ELECTRON TRANSPORT

Interfacing two-dimensional (2D) transition metal dichalcogenides (TMD) with plasmonic nanoantennas was hypothesized to introduce an intrinsic energy conversion mechanism: plasmonic hot electron transport.²⁴⁵ Energy of localized surface plasmons are transduced through radiative photon scattering into the environment or nonradiative Landau damping into hot electron-hole pairs in the nanoantenna. Following Landau damping, plasmonic hot electrons traditionally decay via (i) phonon scattering into the crystal lattice or (ii) interfacial losses.¹⁷⁻²¹ Contact between nanoantennas and a semiconductive TMD potentiate an additional damping pathway for plasmonic hot electrons via transport into the TMD, provided their energy exceeds the metal-TMD Schottky barrier.^{16,22,23} Plasmonic hot electron transport into 2D materials has been inferred in catalysis^{30,58,223} and photodetection schemes.^{29,57,219,220,246} This chapter examined augmented plasmonic damping in metal nanoantenna-TMD heterostructures attributable to transport of plasmonic hot electrons into the TMD.

5.1 Electron Energy Loss Spectroscopy

Electron energy loss spectroscopy (EELS) identifies where and how energy is transduced to a plasmonic nanoantenna through excitation of resonant eigenstates.²⁴⁷ Swift electrons in the nanometer probe of a scanning transmission electron microscope (STEM) lose energy according to resonant eigenstates of a nanoantenna, e.g., surface plasmon resonance. Inelastically transmitted electrons are dispersed by a magnetic prism according to their kinetic energy and loss intensity is quantified by a CCD detector.²⁴⁸ This metrology, which analyzes the energy distribution of

transmitted electrons, is referred to as the “GIF” and is shown in Figure 5.1. Reviews by Egerton, Garcia de Abajo, and Kociak provide comprehensive discussions of EELS.^{91,145,248}

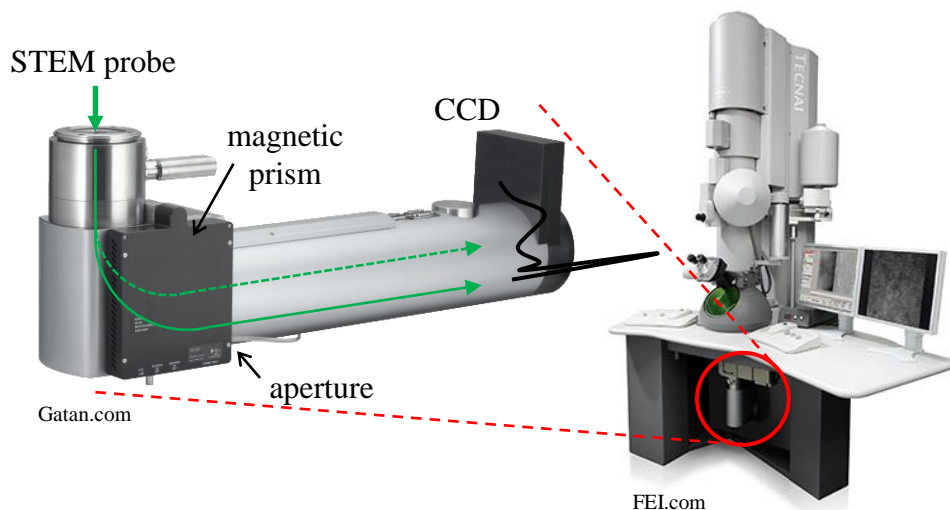


Figure 5.1: Schematic of EELS metrology in a GIF-outfitted STEM. A magnetic prism disperses the electron beam (green) according to energy losses were quantified by the CCD to give an EELS spectrum (black).

EELS spectra is comprised of three distinct regions: (i) the zero-loss peak (ZLP), (ii) the low-loss region, and (iii) the high-loss region.²⁴⁸ The ZLP feature represents the natural energy spread of the STEM probe and defined the energy resolution of an EELS spectra according to its full width at half maximum (FWHM). The low-loss region quantifies energy loss to valence band interactions, e.g., localized surface plasmon resonance (LSPR) or bandgap excitation. The high-loss region quantifies inner-shell interactions, e.g., ionization edges, to fingerprint different elemental compounds. Low-loss eigenstates less than ca. 3 eV are obfuscated by breadth of the ZLP and require empirical background subtraction algorithms to deconvolute the eigenstate. Typical ZLP background models for subtraction include power-law, log-law, reflected-tail, polynomial, and Lorentzian ZLP fits^{150,248} or Richardson-Lucy deconvolution.²⁴⁹

EELS allows qualitative insights into the electromagnetic local density of states (ELDOS).¹⁴⁴ Quantitative correlation between EELS and the ELDOS is precluded by differences

in the electric-field distributions of a photon versus a swift electron.^{135,145} Electric resonance mode types may be spatially distinguished in EELS maps, which correlate loss to particular locales on a nanoantenna. EELS maps are generated by rastering the STEM probe across a nanoantenna whilst recording EELS spectra at discrete intervals.^{137–139,141,151,250} Resonances in EELS may be correlated to “bright” optical resonances using modal decomposition.¹⁴³ However, EELS was unique in that it may also excite “dark” plasmon resonances which cannot be directly accessed by optical methods. Dark resonances exhibit net a zero dipole moment (i.e., $\sum \vec{p} = 0$) whereas bright modes, such as the LSPR, exhibit a finite dipole moment ($\sum \vec{p} \neq 0$).⁹⁴

EELS was performed herein on a FEI Tecnai G² F-20 (FEI, Hillsboro, OR USA) outfitted with a GATAN post-column imaging filter (GIF Quantum 963; GATAN, Pleasanton, CA USA). Energy resolution, as defined by the ZLP FWHM, was approximately 0.55 eV. Energy binning of the GIF was 50 meV. Spatial resolution, as defined by the electron beam diameter, was measured to be 2-3 nm. EELS acquisition conditions were optimized for each experiment according to its unique circumstances, e.g., relative strength of LSPR activity or electron-optic alignment of the STEM column. Generally, EELS spectra were taken at 120-200 kV accelerating voltage and summed from 50-100 distinct 10-200 ms acquisitions, followed by subtraction of the CCD dark current²⁵¹ and ZLP removal using power- or log-law fit.

5.2 Plasmon Bandwidth Analysis of Damping Mechanisms

Total bandwidth of a surface plasmon resonance contains signatures regarding the rate and quantum efficiency of its damping mechanisms. Total bandwidth, Γ , was comprised of summative contributions of each i^{th} damping mechanism, Γ_i , viz.^{240,242}

$$\Gamma = \sum_i \Gamma_i = \Gamma_r + \Gamma_{nr} + \Gamma_c . \quad (\text{Equation 5.1})$$

Subscript r denotes a radiative contribution, nr denotes nonradiative contributions, and c identifies a putative carrier injection contribution arising from nanoantenna contact with TMD. There is correlation between Γ and the Drude damping rate (denoted γ in Equation 2.8). In the absence of elastic dephasing,^{18,242} quantum efficiency, η_i , of the i^{th} damping pathway may be calculated according to Γ_i by Equation 5.2.²⁴⁰

$$\eta_i = \frac{\Gamma_i}{\Gamma} \quad (\text{Equation 5.2})$$

Bandwidth analysis was performed on surface plasmon resonances induced in EELS to quantify η_c and timescale of possible plasmonic transduction into injected hot electrons from nanoantennas into TMD. The nanometer STEM probe in EELS avoided (i) direct excitation of carriers in the TMD and (ii) diffraction-limited excitation of many nanoantenna, which convoluted similar studies using exciton binding energy shifts,²⁵² transient absorption spectroscopy,^{223,253} and photoluminescence (PL).²⁴² Previously, LSPR Γ measured in EELS and PL spectroscopy were decomposed using Equation 5.1 to estimate 10% and 20% η_c in gold (Au) nanoantenna-graphene heterostructures.^{242,240} Herein, a putative Γ_c contribution to plasmon damping was elucidated by measuring mean Γ for multiple nanoantennas with the appropriate negative control, i.e., $\Gamma_r + \Gamma_{nr}$ versus $\Gamma_r + \Gamma_{nr} + \Gamma_c$. This analysis assumed transport of Landau-damped hot electrons away from the nanoantenna did not redistribute prevalence of other nonradiative mechanisms.

Wien-type monochromation of the STEM probe's Gaussian energy distribution by the GIF convolutes the underlying Lorentzian Γ of the surface plasmon resonance to a measured Voigt profile. In other words, measured Voigt Γ in EELS is a convolution of the Lorentzian plasmon resonance with the Gaussian ZLP profile. The Lorentzian FWHM may be *a priori* converted to

its observable Voigt FWHM in EELS, and vice versa, using an empirical relation developed by Olivero and Longbothum with an accuracy of $\pm 0.02\%$,²⁵⁴ viz.

$$\Gamma_V = 0.5346\Gamma_L + \sqrt{0.2166\Gamma_L^2 + \Gamma_G^2} \quad (\text{Equation 5.3})$$

where Γ_V , Γ_L , Γ_G are the Voigt, Lorentzian, and Gaussian bandwidths, respectively. In this work, Γ_V was the measured FWHM of a plasmon resonance in EELS and Γ_G was the 0.55 eV ZLP FWHM. Ascertaining changes to plasmonic Γ less than 0.55 eV by emergence of additional damping mechanisms remained possible through this relation, despite definition of the ZLP as the ultimate energy resolution of the system.

Plasmon dephasing times bound by Heisenberg's uncertainty principle may be calculated for damping mechanism i according to its Γ_i , viz.^{18,240}

$$T_{2,i} = \frac{2\hbar}{\Gamma_i}. \quad (\text{Equation 5.4})$$

Static and dynamic charge transport processes with plasmon hot electrons, as defined by interfacial damping contributions in nonradiative dephasing,²¹ differ from hot electron injection. Static charge transfer represents entrapment of hot carriers into trap states near the Fermi level. Dynamic charge transfer involves carriers returning to the nanoantenna and depolarizing coherence of the dipole oscillation, thereby shortening overall surface plasmon lifetime.

To distinguish contributions from Γ_r and Γ_{nr} to the measured Voigt Γ , theoretical Lorentzian FWHM were estimated *a priori* using two numerical approaches based on the discrete dipole approximation (DDA) and convoluted with a 0.55-0.60 eV FWHM Gaussian.^{247,254} Electron-excitation DDA package eDDA v1.2¹⁰⁴ and light-excitation DDA package DDSCAT v7.3^{100,102,103} were used. Complex TMD and SiO₂ dielectric functions were used.^{214,217,255} For DDSCAT, scattering (absorption) cross section was normalized against extinction cross section at

resonance to calculate Γ_r (Γ_{nr}) after multiplying by the extinction FWHM. Results for DDSCAT were taken at a refractive index for which LSPR matched transmission UV-vis extinction measurements, due to its light excitation treatment. Corresponding estimates based on analytical Mie theory,⁶⁴ semi-analytical quasistatic and modified long wavelength approximate dipole polarizability,⁹⁷ and an empirical relation based on geometry¹⁸ were also considered.

5.3 Gold Nanospheres on Molybdenum Disulfide

Heterostructures of Au nanospheres and molybdenum disulfide (MoS_2) were interrogated using EELS to quantify the probable extent of energy conversion into plasmonic hot electrons. Heterostructures were fabricated by sequential drop-casting of liquid-exfoliated MoS_2 (60-370 nm length; 1-2 layers; ethanol solvent) and Au nanospheres (76 ± 13 nm; isopropanol solvent) onto a 20 nm silicon dioxide (SiO_2) membrane,²¹⁸ as described in § 4.1.1. Use of liquid-exfoliated MoS_2 avoided (i) atomic-scale defects (e.g., ripples²⁵⁶ or lattice strains⁵⁴) accrued from transferring synthetic TMD to the delicate membrane and (ii) thickness polydispersity of mechanically exfoliated TMD. Monolayer MoS_2 crystals were distinguished according to plasmon signatures at ca. 18-20 eV (bulk plasmon)²⁵⁷ and 6 eV (π^* plasmon) that were red-shifted and less intense versus their few-layer MoS_2 counterparts.^{176,218} A 200 kV STEM probe was placed at the edge (center) of the Au nanospheres to induce a bright (dark) surface plasmons, akin to the nanodisc simulations of Figure 2.6. FWHM of the bright and dark plasmon excitations in the presence and absence of MoS_2 were analyzed by Equation 5.1 to deduce a possible Γ_c contribution to damping.

5.3.1 Plasmonic Mode Structure

EELS analysis of five Au nanospheres in the absence of MoS_2 revealed two resonant plasmon modes: the bright LSPR at ca. 2.11 eV and a dark mode at ca. 2.03 eV.^{150,218} Figure 5.2(a)

shows representative EELS spectra obtained from edge (red) and center (blue) excitation of ca. 80 nm diameter Au nanospheres in the absence (hollow data points) and presence (filled data points) of underlying MoS₂. Bright and dark modes are labeled “B” and “D,” respectively. Figure 5.2(b) and 5.2(c) show the corresponding high-angle annular dark-field (HAADF) STEM images with labeled impact points. Monolayer MoS₂ appeared dark-gray in STEM mode relative to Au because of its low electron-scattering cross section, inherent to an atomically-thin crystal. Screening by ca. 10 nm poly(vinylpyrrolidone) (PVP) ligands encapsulating the Au nanosphere may have red-shifted the dark mode from the 2.45 eV bulk plasma energy anticipated for nanoantennas of this size.⁹⁴ A 2.4 eV eigenstate was simulated by eDDA for edge excitation, both in the presence and absence of MoS₂; however, the PVP was not included.

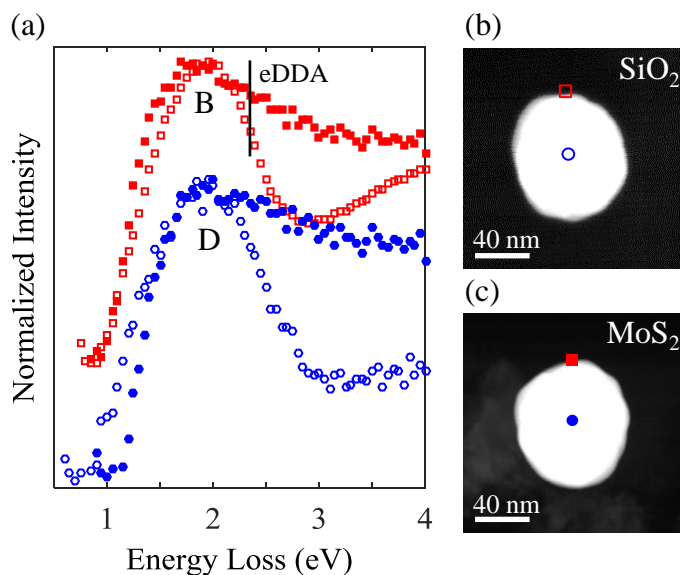


Figure 5.2: (a) EELS spectra from edge (red) and center (blue) impact of a ca. 80 nm Au nanosphere with (filled) and without (hollow) an underlying MoS₂ monolayer. Corresponding HAADF-STEM images are shown in (b) and (c). Spectra were normalized and vertically offset for clarity. Accelerating voltage was 200 kV. Black solid line shows surface plasmon energy simulated using eDDA for edge excitation both with and without MoS₂ (same energy resulted).

Presence of a MoS₂ monolayer beneath the Au nanosphere expanded FWHM of the bright LSPR by ca. 0.08 eV averaged across five measurements, ostensibly due to emergence of

additional plasmon damping pathway(s).^{22,240,242} Energies of the bright and dark both modes (ca. 2.15 eV and 2.09 eV, respectively) remained essentially unchanged. Graphene also did not significantly change resonant plasmon energies of a Au nanoellipse in a previous report.²⁴⁰ In another report, MoS₂ red-shifted the bright plasmon resonance of 60 nm silver nanodiscs by 36 meV,²⁵⁸ which was less than the binning resolution of the GIF. The dark mode FWHM remained unchanged. Reported 10 meV red-shift in A exciton energy for MoS₂ from n-type doping was also beneath resolution of the GIF.²⁵² eDDA computed a 0.03 eV bandwidth expansion for the bright mode by comparison (data not shown). EELS spectral profiles for Au nanospheres with MoS₂, such as those shown in Figure 2(a), were similar to those without MoS₂, but with more intense 2-4 eV energy loss. This appeared due to absorption in MoS₂ above its 1.85 eV direct bandgap.⁴²

Table 5.1 summarizes mean energy occurrence and FWHM for bright and dark plasmonic resonances measured in EELS on ten ca. 80 nm Au nanospheres; five without and five with underlying MoS₂. Presence of the MoS₂ altered resonant energy of the bright (dark) mode from 2.11 eV (2.03 eV) to 2.15 eV (2.09 eV), albeit shifts were statistically insignificant. Welch's t-test confirmed statistical significance of the ca. 0.08 eV FWHM expansion for the bright LSPR with 95% confidence. FWHM change for the dark plasmon mode was insignificant. Thus, putative hot electron transport from the Au nanosphere to the MoS₂ appeared unique to bright plasmonic excitation, consistent with graphene-based heterostructures.²⁴⁰ Carrier injection into the electrically insulative SiO₂ membrane was neglected as in previous studies.^{242,259}

Table 5.1: Mean EELS-measured energy and FWHM for bright and dark plasmonic resonances for ca. 80 nm Au nanospheres (AuNS) with and without an underlying MoS₂ monolayer.

| | Diameter [nm] | Energy [eV] | | FWHM, Γ [eV] | |
|-----------------------|---------------|-------------|-----------|---------------------|-----------|
| | | Bright | Dark | Bright | Dark |
| AuNS | 79±2 | 2.11±0.01 | 2.03±0.02 | 1.28±0.01 | 1.32±0.02 |
| AuNS-MoS ₂ | 78±2 | 2.15±0.01 | 2.09±0.02 | 1.36±0.02 | 1.30±0.02 |

5.3.2 Bandwidth Analysis

Bright surface plasmon resonance energy of ca. 2.1 eV exceeded the 0.9 eV Schottky barrier of Au-MoS₂ interfaces,¹⁹⁴ thus potentiating a finite Γ_c contribution to overall plasmon damping. A corresponding energy band diagram is shown in Figure 5.3.²¹⁸ Landau damping of the plasmon resonance created hot electrons²² one plasmon quanta of ca. 2.1 eV (measured in EELS) above the Fermi level, E_F , and potentiated transfer into the MoS₂ conduction band, E_c . Transfer of these plasmonic hot electrons across the Au-MoS₂ Schottky barrier was measured herein according to a concomitant increase in overall Γ , attributable to emergence of Γ_c . Table 5.2 summarizes measured and simulated bright LSPR Voigt Γ , along with its known Γ_r and Γ_{nr} contributions in the absence of MoS₂, to distinguish a possible Γ_c contribution for the Au nanosphere-MoS₂ heterostructure.

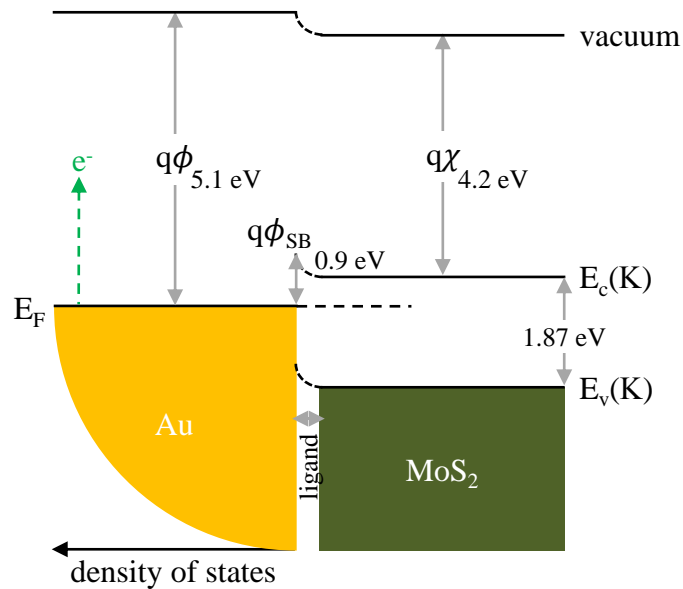


Figure 5.3: Energy band diagram of a Au-MoS₂ junction at thermal equilibrium. Resonant excitation at 2.1 eV of the Au nanosphere exceeded the 0.9 eV Schottky barrier ($q\phi_{SB}$), calculated from the Au work function ($q\phi$) of Au and MoS₂ electron affinity ($q\chi$), and potentiated transport of hot electrons into the MoS₂ conduction band (E_c). Possible quantum confinement effects and finite Au ligand thickness were neglected for simplicity.

Table 5.2: Plasmonic damping of the bright LSPR for ca. 80 nm Au nanospheres (AuNS) with and without an underlying MoS₂ monolayer. Resonant plasmon FWHM, Γ , were calculated using electron- and light-excitation DDA models, labeled eDDA and DDSCAT, respectively.

| | Method | Diameter [nm] | Radiative, Γ_r [eV] | Nonradiative, Γ_{nr} [eV] | Total, Γ [eV] |
|-----------------------|-----------------------|---------------|----------------------------|----------------------------------|----------------------|
| AuNS | eDDA [†] | 80 | - | - | 0.87 |
| | DDSCAT [†] | | 0.31 | 0.57 | 0.88 |
| | measured [‡] | 79±2 | - | - | 1.28±0.01 |
| AuNS-MoS ₂ | eDDA [†] | 78 | - | - | 0.90 |
| | DDSCAT [†] | | 0.35* | 0.57 | 0.92 |
| | measured [‡] | 78±2 | - | - | 1.36±0.02 |

[†] after convolution with 0.60 eV Gaussian ZLP
[‡] included PVP
* assumed contribution from MoS₂ to Γ (i.e., 0.88 eV - 0.83 eV) was attributable to Γ_r

In the absence of MoS₂ (i.e., $\Gamma_c = 0$), measured resonant bandwidth of the Au nanospheres on SiO₂ was $\Gamma = 1.28 \pm 0.01$ eV.²¹⁸ Estimates for $\Gamma_r + \Gamma_{nr}$ of 0.87 eV and 0.88 eV were obtained using eDDA and DDSCAT, respectively. Photon and phonon scattering contributed 36% and 64%, respectively, to total damping according to DDSCAT. Measured Γ was 0.41 ± 0.01 eV larger than eDDA simulated Γ , apparently due to concomitant influences of (i) drift in ZLP energy alignment on the GIF over 100 acquisitions, (ii) ZLP background subtraction bias, and/or (iii) interfacial damping by physisorbed PVP on the Au surface.^{19,21}

Measured plasmonic FWHM of the Au nanospheres expanded to $\Gamma = 1.36 \pm 0.02$ eV in the presence of underlying MoS₂.²¹⁸ This indicated $\Gamma_c = 0.05 \pm 0.03$ eV, after 0.87 eV for $\Gamma_r + \Gamma_{nr}$ for the Au nanosphere on SiO₂ (from eDDA), 0.03 eV in accrued Γ_r from MoS₂ (from eDDA), and 0.41 ± 0.01 eV (PVP interfacial effects and contributions intrinsic to EELS metrology and interpretation) from Γ using Equation 5.1. Bandwidth expansion in the DDA models was conservatively attributed to accrued Γ_r through TMD screening. Large Γ_{nr} can limit PL

enhancement in MoS₂ from plasmons due to plasmon-phonon scattering transduced by the nanoantenna into the TMD.²²⁵

A putative η_c of up to 4±2% for transport of plasmonic hot electrons from the Au nanospheres to MoS₂ was conservatively estimated by Equation 5.2 using inferred $\Gamma_c = 0.05\pm 0.03$ eV and measured $\Gamma = 1.36\pm 0.02$ eV.²¹⁸ Corresponding n-type doping densities may be calculated from plasmon-induced changes to exciton binding energy of MoS₂,²⁵² but were not considered in this work. Possible interfacial damping from the MoS₂ underlying the residual 0.05 eV Γ expansion was assumed negligible because of the PVP interlayer. Plasmon-excited hot electrons ostensibly dephased into the MoS₂ over a 26±16 fs period, via Equation 5.4. This value fell within the 1-100 fs timescale reported for Landau damping of metallic plasmons.¹⁶ A 200 fs timescale was recently measured by transient absorption spectroscopy for Au nanorods into MoS₂.²⁵³ Lifetime of injected carriers in MoS₂ has been estimated to be 800 ps prior to radiative recombination.²²³

Relatively low conversion efficiency was likely due to the high resistance ohmic junction between the Au nanospheres and MoS₂. High resistance arose from (i) lack of direct physical Au-MoS₂ contact because of the PVP coating around Au and (ii) strict linear momentum conservation constraints. Dielectric spacers between the metal and TMD can mitigate, and even abolish,²⁶⁰ quantum yield of injected carriers by increasing the resistance of the metal-TMD ohmic junction. Rough, polycrystalline metal interfaces ease electron momentum orientation requirements for transfer of plasmonic hot electrons into adjacent media.²³ Thus, direct physicochemical contact between a reduced nanoantenna and TMD crystal, i.e., an optimal ohmic contact with minimized resistance, was postulated to signify the ultimate extent to which energy could be converted towards plasmonic hot electron injection.

5.4 Effect of Ohmic Contact Quality on Plasmonic Hot Electron Transport

Plasmonic hot electron transport across an optimized Au-TMD ohmic contact, where ca. 20 nm Au nanoantennas (AuNA) were physicochemically bonded to the edges of mono- to few-layer liquid exfoliated tungsten disulfide (WS_2), was measured using EELS.²⁶¹ Formation of Au-sulfur bonds was confirmed by x-ray photoelectron spectroscopy (XPS), detailed in Refs. 229 and 261. Briefly, a secondary S2p doublet emerged upon WS_2 reaction with gold chloride (AuCl_3) of ca. 1 eV lower binding energy relative to the WS_2 S2p doublet, attributable to formation of Au-sulfur bonds.^{262,263} AuNA-decorated WS_2 crystals were fabricated as described in § 4.1.2 and drop-cast onto a 20 nm thick SiO_2 membrane. In previous studies of plasmonic hot electron transport into 2D materials, the ohmic junction was limited to physical contact with the basal plane of the 2D material.^{218,223,242,252} AuNA were physicochemically bonded onto the WS_2 edges in this work. Unique lattice terminations at 2D material edges provide extraordinary optical behavior from the basal plane,^{180,187,237,264,265} which could be more receptive to plasmonic hot electrons.

A bright ca. 2.1 eV LSPR was measured by EELS for three ca. 20 nm AuNA in the absence of WS_2 .²⁶¹ Attachment of three comparably sized AuNA to the edge of WS_2 expanded bright LSPR Γ by ca. 0.23 eV, ostensibly due to emergence of additional plasmon damping pathway(s) including hot electron transport.^{22,218,242} Figure 5.4(a) shows representative EELS spectra obtained from ca. 20 nm AuNA with (filled data points) and without (hollow data points) attachment to a WS_2 edge, each atop SiO_2 . Impact point of the 120 kV STEM probe was at the far edge of each AuNA opposite of the WS_2 . This minimized any WS_2 interaction and prevented its losses from obfuscating the LSPR.²¹⁸ Figure 5.4(b) and 5.4(c) show HAADF-STEM images with labeled impact points. The *in situ* chemical reduction protocol secondarily resulted in WS_2 -free AuNA,

thought to originate from reduction by the sodium cholate surfactant used for suspension stability. These AuNA were used as the negative control data.

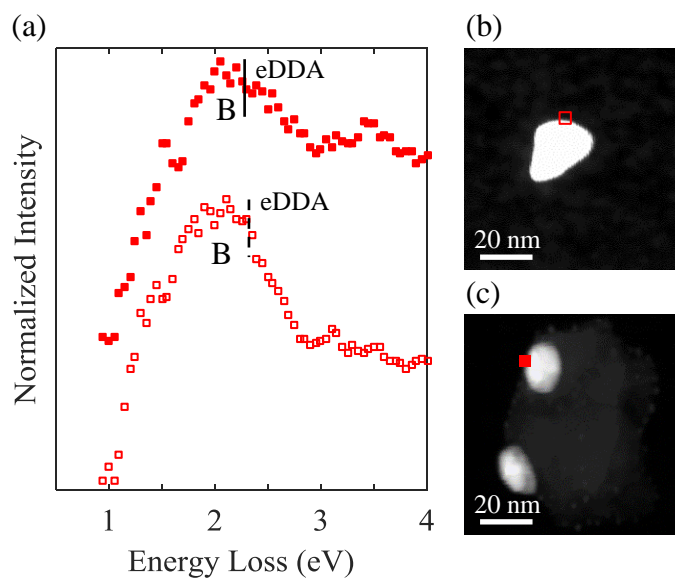


Figure 5.4: (a) EELS spectra from edge excitation of a ca. 20 nm AuNA isolated (hollow) or reduced (filled) onto the edge of a 2D WS₂ crystal. Corresponding HAADF-STEM images are shown in (b) and (c). Accelerating voltage was 120 kV. Spectra were normalized and vertically offset for clarity. Estimates for LSPR according to eDDA in the presence (solid vertical line) and absence (dashed vertical line) of WS₂ are superposed.

A 2.38 eV bright LSPR was anticipated by eDDA (vertical solid line) for a 20 nm Au sphere placed at the edge of a 90x45 nm WS₂ sheet, which signified a simplification of the measured heterostructures sans the SiO₂ membrane.²⁶¹ This was red-shifted 0.05 eV relative to the 2.43 eV LSPR in the absence of WS₂ (vertical dashed line). Experimental LSPR may have been red-shifted from the theory due to screening from the SiO₂ and/or quantum confinement.¹⁵⁰ Also, WS₂ edge states were could not be represented because of dielectric function treatment of the WS₂, as opposed to density functional theory models. Dark plasmon resonances inducible at the AuNA center⁹⁴ were not examined because damping by hot electron transfer was found to originate from the bright LSPR in § 5.3.1 and other reports.^{218,240}

Table 5.3 summarizes mean energy occurrence and FWHM for the LSPR measured in EELS across six ca. 20 nm AuNA; three without and three with attachment to WS₂.²⁶¹ LSPR blue-shift from 2.08 eV to 2.15 eV upon interaction with WS₂ was statistically insignificant. Welch's t-test confirmed statistical significance of the ca. 0.23 eV FWHM expansion for the LSPR with 95% confidence. Accrued bandwidth was ostensibly due to ca. 2.1 eV hot electrons transported across the 0.6 eV Au-WS₂ $q\phi_{SB}$; the corresponding energy band diagram is shown in Figure 5.5.²⁶¹ However, $q\chi$ value²⁶⁶ was taken from measurements of the WS₂ basal plane. Possible ELDOS alterations in its band structure associated with physicochemical Au reduction onto WS₂ edges with unique lattice terminations²³¹ were not considered due to absence of associated data. This $q\phi_{SB}$ was lower than the 0.9 eV Au-MoS₂ $q\phi_{SB}$ studied in § 5.3, and thus potentiated an intrinsically higher η_c .

Table 5.3: Mean EELS-measured energy and FWHM for bright LSPR for three ca. 20 nm AuNA with and without attachment to the edge of a WS₂ crystal.

| | Measured Diameter [nm] | LSPR [eV] | | FWHM, Γ [eV] | |
|----------------------|------------------------|-----------------------|------|-----------------------|-------------------|
| | | measured [†] | eDDA | measured [†] | eDDA [‡] |
| AuNA | 22±5 | 2.08±0.04 | 2.43 | 1.38±0.05 | 0.82 |
| AuNA-WS ₂ | 19±4 | 2.15±0.08 | 2.38 | 1.61±0.03 | 0.86 |

† included 20 nm SiO₂ substrate and/or nearby AuNP
‡ after convolution with 0.55 eV Gaussian ZLP

Reduction of AuNA onto the edge of WS₂ expanded the measured resonant bandwidth to $\Gamma = 1.61\pm 0.03$ eV from 1.38 ± 0.05 eV in the absence of WS₂. This conservatively indicated $\Gamma_c = 0.19\pm 0.08$ eV, after subtracting 0.82 eV for $\Gamma_r + \Gamma_{nr}$ for the AuNA [from eDDA and supported by DDSCAT (data not shown for brevity)], 0.04 eV in accrued Γ_r from WS₂ (from eDDA), 0.04 eV for SiO₂ interfacial losses,²¹⁸ and 0.52 ± 0.05 eV (contribution intrinsic to EELS metrology and interpretation). A portion of the residual 0.19 eV expansion in Γ could result from entrapment of

plasmonic hot electrons into WS₂ trap states and/or return of hot electrons back to the AuNA, thereby depolarizing its oscillation.²¹ Role of Au-sulfur bonds in plasmon damping remains unclear. Covalent Au-sulfur bonds on organic thiol-coated AuNP notably expands Γ ,²⁶⁷ but crystalline WS₂ is fundamentally distinct from organic substituents.

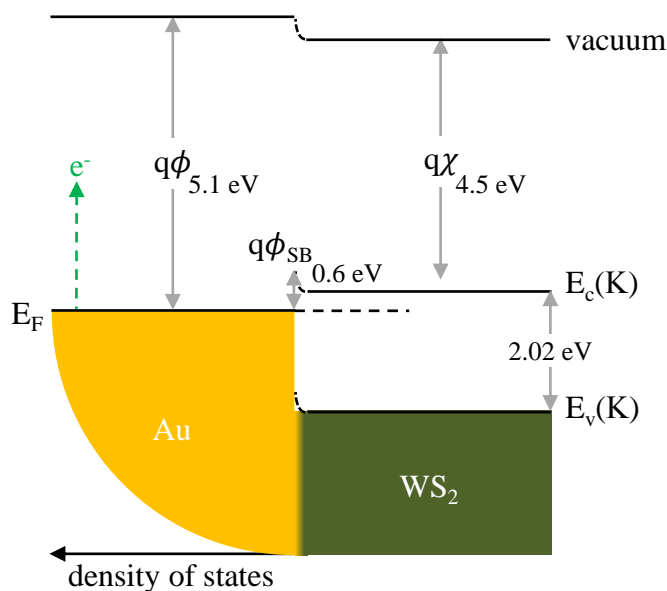


Figure 5.5: Energy band diagram of a Au-WS₂ junction at thermal equilibrium. Resonant excitation at 2.1 eV of the AuNA exceeded the 0.6 eV Schottky barrier ($q\phi_{SB}$), calculated from the Au work function ($q\phi$) of Au and WS₂ electron affinity ($q\chi$), and potentiated transport of hot electrons into the WS₂ conduction band (E_c). Possible quantum confinement effects were neglected for simplicity.

A putative η_c of up to 11±5% was conservatively estimated for putative transport of plasmonic hot electrons from AuNA to WS₂. Changing the relative proximities of STEM probe, AuNA, and WS₂ crystal edge could affect calculation or measurement of η_c due to increased optical activity at WS₂ edges.^{180,231,237} Based on measured damping, estimated dephasing time for each Landau-damped plasmonic hot electron to ostensibly transfer into the WS₂ was 7±3 fs. This value was lower than previous estimates ranging from 26 to 200 fs for plasmonic hot electrons to transfer from Au nanospheres and nanorods *across a dielectric spacer* into MoS₂.^{218,253} Improved contact quality (i.e., lower resistance) between the AuNA and WS₂ via covalent bonding, lower

Schottky barrier, and eased momentum conservation constraints²³ appeared to increase the transport damping rate.

5.5 Summary

Possible transport of plasmonic hot electrons from 80 nm Au nanospheres and ca. 20 nm AuNA to 2D TMD crystals was measured for the first time by comparing measured plasmonic bandwidth in EELS with those computed using DDA models. The nanometer STEM probe allowed single-particle resolution and avoided confounding effects associated with optical measurements, e.g., direct electron-hole pair generation in the TMD. A quantum yield of up to $4\pm 2\%$ for putative transport of plasmonic hot electrons was estimated for 80 nm Au nanospheres deposited onto MoS₂, albeit with a high resistance ohmic contact due to PVP ligands on the Au. Putative quantum yield of plasmonic hot electron transport increased to $11\pm 5\%$ for ca. 20 nm AuNA physicochemically bonded to WS₂, representing an optimized ohmic junction with minimized resistance and intrinsically lower $q\phi_{SB}$. Plasmonic damping through hot electron transport was found to originate solely from excitation of the bright LSPR. Dark plasmonic modes, whose measurement are unique to electron-excitation in EELS, were found not to contribute to transport of plasmonic hot electrons. Overall, the extent to which electromagnetic energy above the nanoantenna-TMD ϕ_{SB} could be passively converted into plasmonic hot electrons dissipated into TMD was conservatively measured to be 11%.

CHAPTER 6

SURFACE PLASMON-ENHANCED NONLINEAR ENERGY MIXING

Rejection and conversion of infrared energy through nonlinear frequency mixing phenomena^{32,33} was tested with two-dimensional (2D) molybdenum disulfide (MoS_2)⁴²⁻⁴⁴ interfaced with gold (Au) nanoshells. Monolayer MoS_2 was selected for its high susceptibility to second-order nonlinear interactions, $\chi^{(2)}$, measured at $660 \pm 130 \text{ pm V}^{-1}$ at 532 nm.²⁰⁷ Local electric field augmentation by the metal nanoshells was hypothesized to passively enhance nonlinear energy conversion from the MoS_2 .^{75,92,94} This chapter quantitatively examined second harmonic generation (SHG) from a MoS_2 monolayer within the electric field of localized surface plasmons using multi-photon confocal microscopy.

6.1 Multi-Photon Confocal Microscopy

Confocal microscopy is a laser-scanning, episcopic imaging technique which detects multi-photon emission (e.g., two-photon scattering for SHG) at improved x-y spatial resolution over conventional optical microscopes.^{268,269} It accomplishes this via a pinhole aperture placed in front of the detector at the objective lens focus point to eliminate out-of-focus z-axis contributions. Figure 6.1 schemes the working-principle for a basic multi-photon confocal microscope via optical ray diagram. Detection metrology is comprised of a photomultiplier tube (PMT) array, where each PMT is dedicated to some band of wavelengths tailored by a sequence of dichroic mirrors. Laser-scanning nature of the technique allows hyperspectral image reconstruction, such that a unique scattering spectra may be accessed for each pixel within the confocal image.

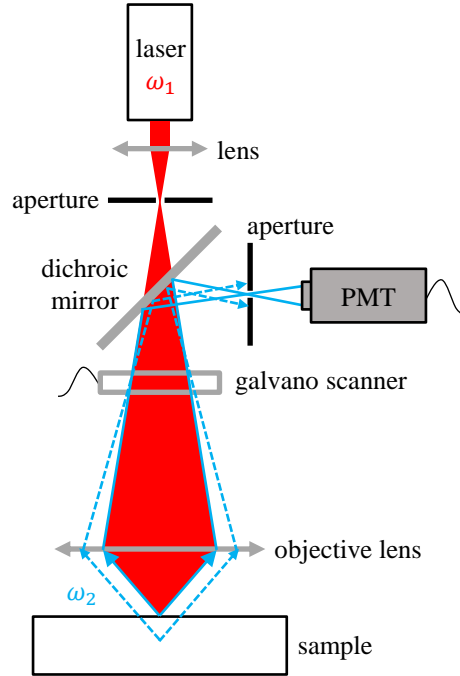


Figure 6.1: Schematic of a multi-photon confocal microscope. An excitation laser (ω_1 ; red) is focused onto a sample which emits higher frequency signals (ω_2 ; blue), where $\omega_1 < \omega_2$. In-focus scattered photons are detected by a PMT array. Out-of-focus contributions are blocked by a pinhole aperture.

The “z-scan” technique pioneered by Van Stryland *et al.* was an alternative method to explore the nonlinear optical properties of a material,^{270,271} namely the nonlinear refractive index, n_2 , and absorption coefficient, α_2 . Briefly, the technique examines intensity-dependent transmission changes and phase distortions in a Gaussian laser beam as a nonlinear material is translated through its focus point; hence, its denotation as a z-scan. Changes in transmittance accrued from multi-photon absorption processes,³³ presumed to be dominated by two-photon absorption, enables quantitation of α_2 . Intrinsic Kerr self-focusing of the laser within the nonlinear material accrue from $n_2 > 0$,³³ causing minute phase shifts observable in the far-field as changes in transmittance when a small aperture is placed in front of the detector. However, both n_2 and α_2 are third-order nonlinear processes associated with $\chi^{(3)}$.^{32,33} This work focuses on $\chi^{(2)}$ frequency conversion. Despite its misleading nomenclature, two-photon absorption falls under

third-order classification because: (i) direct dependence on $\mathfrak{I}(\chi^{(3)})$ and (ii) it is a cascaded linear absorption process not limited to non-centrosymmetric crystallinity (as with $\chi^{(2)}$ processes).³³

SHG from monolayer MoS₂ in the presence and absence of nanoantennas was measured from an inverted, laser-scanning confocal microscope (A1R-MP; Nikon Instruments, Melville, NY USA) coupled to a unpolarized, wavelength tunable Ti:sapphire laser (MaiTai Deep See; Spectra-Physics, Santa Clara, CA USA). A 60x water-immersion objective (1.27 NA CFI Plan Apo IR; Nikon Instruments, Melville, NY USA) focused the rastering laser (100 fs pulse width; 80 MHz) onto the sample. Scattered photons were episcopically collected at 50 nm raster intervals (i.e., each pixel) and delivered to an array of 32 PMT at 2.5 nm wavelength binning. Excitation was limited to a 810-1000 nm spectrum herein because of detector incompatibility with sub-400 nm wavelengths. Data were captured at 1.1 μ s of irradiation per pixel, gained by the PMT at 160 V, and averaged over 16 acquisitions to increase signal-to-noise ratio. Power of the laser was 5 mW (\pm 0.35 mW) across all excitation wavelengths. Diameter of the focused laser beam was ca. 0.8-1.0 μ m, per the Abbe criterion.²⁷² Post-processing of hyperspectral images, including extraction of spectra from regions of interest (ROI), was performed in Nikon NIS-Elements Confocal (v4.3; Nikon Instruments, Melville, NY USA).

6.2 Heterostructure Prototype

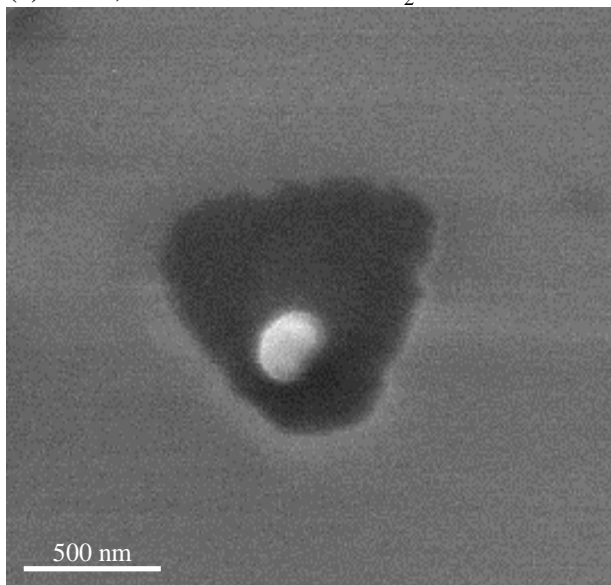
Synthetic monolayer MoS₂, grown via chemical vapor deposition (CVD), interfaced with 150 nm Au nanoshells was used as a prototype for enhanced nonlinear infrared frequency conversion. Plasmon enhancement of nonlinear activity, both third- and second-order, has been examined in other nanomaterial heterostructures: ionic polymer bilayer films doped with silver nanospheres,²⁷³ organic dyes with gold nanospheres,²⁷⁴ barium titanate nanoparticles encapsulated

in Au,²⁷⁵ zinc oxide nanowires on a Au pentamer,²⁷⁶ rubidium titanyl phosphate with silver nanoantennas,²⁷⁷ and various instantiations of indium tin oxide (ITO) placed within a Au dimer.^{278–280} Intensity of the SH was enhanced 60-1700x over the nonlinear source component, with one citing a 0.00003% conversion efficiency.^{273,275–277} The prototype Au-MoS₂ heterostructure herein improves over aforementioned systems by (i) higher $\chi^{(2)}$ of 660 pm V⁻¹ versus 6 pm V⁻¹ for zinc oxide, 14 pm V⁻¹ for the ionic polymer bilayers, 31 pm V⁻¹ for rubidium titanyl phosphate, and 34 pm V⁻¹ for barium titanate,^{281–284} (ii) a polarization independent LSPR; and (iii) nanoantenna morphology amenable to high-volume chemical synthesis.

6.2.1 Fabrication

Figure 6.2(a) shows a scanning electron microscopy (SEM) image of single representative Au nanoshell-MoS₂ heterostructure. Au nanoshells 148±8 nm in overall diameter, with 119±9 nm silica (SiO_x) inner core and poly(vinylpyrrolidone) (PVP) ligand (lot MGM1774; nanoComposix, San Diego, CA USA),²⁸⁵ were dispersed in water to a concentration of 3.6x10⁹ mL⁻¹. These nanoshells were three-dimensional analogs to the 2D nanorings studied in § 2.4 to circumvent need for top-down lithography. An energy-filtered transmission electron microscopy (EFTEM) image of the Au nanoshells is shown in Figure 6.2(b). The Au nanoshells were drop-cast²²⁸ (3 μL volume) onto MoS₂ grown via CVD on a silicon (Si) wafer with 300 nm of thermal oxide (CVD-MOS₂; 2Dsemiconductors, Scottsdale, AZ USA) preheated to 105 °C. The MoS₂-Si wafer was pre-cleaned to improve hydrophilicity by sequential 3 min immersions into acetone, methanol, and isopropanol followed by a water rinse and dried under nitrogen gas. MoS₂ is a noted catalyst for methanol dissociation,²⁸⁶ which caused apparent removal of some MoS₂ monolayers from the Si during the methanol immersion step. Nitric acid treatment, an alternative hydrophilic treatment used in § 4.1 for SiO_x, was observed to structurally degrade the MoS₂ (data not shown).

(a) SEM, Au nanoshell on MoS₂



(b) EFTEM, Au nanoshells

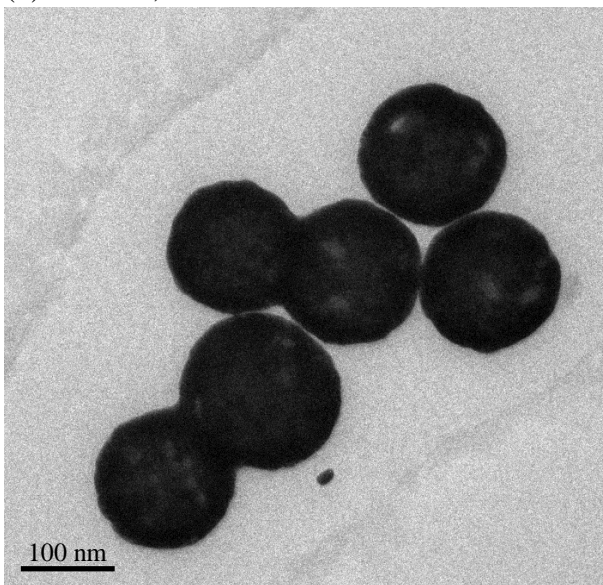


Figure 6.2: (a) SEM image of a representative heterostructure comprised of triangular monolayer of MoS₂ and a Au nanoshell. (b) EFTEM image of the Au nanoshells revealing SiO_x core. Accelerating voltages were 5 kV and 120 kV, respectively.

6.2.2 Nanoantenna Characterization

The Au nanoshells exhibited an *in vacuo* dark plasmon resonance at 1.60 eV and bonding-type bright LSPR at 1.89 eV, as measured in electron energy-loss spectroscopy (EELS) and shown in Figure 6.3(a).²⁸⁷ An EELS map taken at the 1.89 eV resonance mode revealed loss characteristics indicative of a bright mode (discussed in § 2.4). High-angle annular dark-field (HAADF) scanning transmission electron microscopy (STEM) images of measured nanoantennas corresponding to each spectra are shown in Figure 6.3(b). Despite energy difference of the bright and dark modes falling beneath the 0.55 eV EELS energy resolution, the two apparent modes were not artifacts from zero-loss peak (ZLP) subtraction or other numerical processing. A comparison between one representative EELS spectra before and after ZLP subtraction is shown in Figure 6.3(c). Both modes were evident across measures of six distinct nanoantennas and power-law, log-law, reflected tail, and direct reference subtractions of the ZLP.

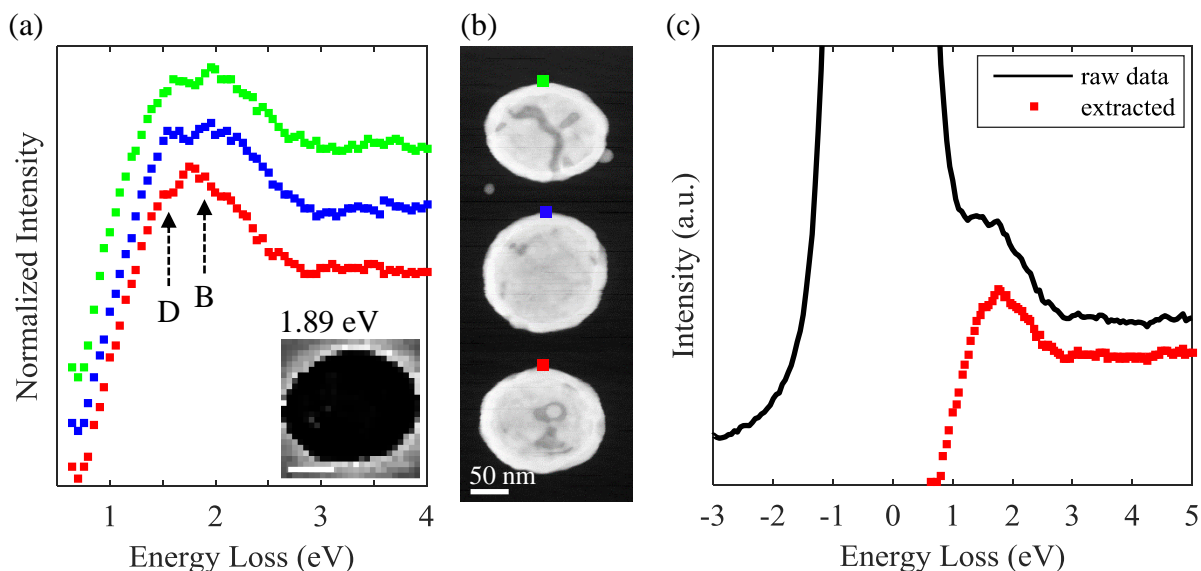


Figure 6.3: (a) EELS spectra from edge excitation of a three representative ca. 150 nm Au nanoshells (15 nm Au shell; 120 nm diameter SiO_x core) exhibiting 1.89 eV bright and 1.60 eV dark plasmonic resonances on average. Spectra were normalized and vertically offset for clarity. Inset to (a) is an EELS map taken at the 1.89 eV mode with 50 nm scale. (b) HAADF-STEM images with labeled impact points corresponding to each of the spectra. (c) Comparison between one EELS spectra with and without ZLP subtraction according to a $y = Ae^{-x} + B$ power-law fit. Accelerating voltage was 120 kV.

The *in vacuo* LSPR energy agreed well with 1.86-1.90 eV estimates from analytical Mie theory⁶⁴ and numerical discrete dipole approximation (DDA)^{90,100,104} for a 150 nm diameter Au- SiO_x nanoantenna (15 nm Au shell; 120 nm diameter SiO_x core) atop a 20 nm thick silicon dioxide (SiO_2) membrane (data not shown for brevity).²⁸⁷ Computationally placing a swift electron beam at the edge of the nanoshell (i.e., eDDA¹⁰⁴) revealed a low energy shoulder from a dark mode. This was consistent with the experimental EELS spectra. However to date, only Au nanoshells at much larger aspect ratios (0.4 versus 0.2 herein) have been characterized using EELS and dark resonances were not considered,¹⁵⁷ which precluded a rigorous comparison with published reports.

The LSPR red-shifted to 1.52 eV (817 nm) upon immersion of the nanoshells into water, which fell within the 700-1000 nm excitation spectrum of the Ti:sapphire excitation laser coupled into the multi-photon confocal microscope outfitted with water-immersion objectives. Figure 6.4

compares experimental transmission UV-vis extinction spectra (solid) with those calculated by DDA (dashed) and Mie theory (dotted). Maximas at 625 nm and 817 nm corresponded to the quadrupole and dipole LSPR, respectively [dipole is plotted in Figure 6.4(b)]. Experimental data were taken from the nanoantennas suspended in water within a cuvette.²⁸⁵ Experimental LSPR breadth reflects the size distribution. DDA and Mie data were taken at an effective refractive index of 1.40 to account for screening contributions from the PVP ligand (refractive index of 1.52).¹⁰⁶

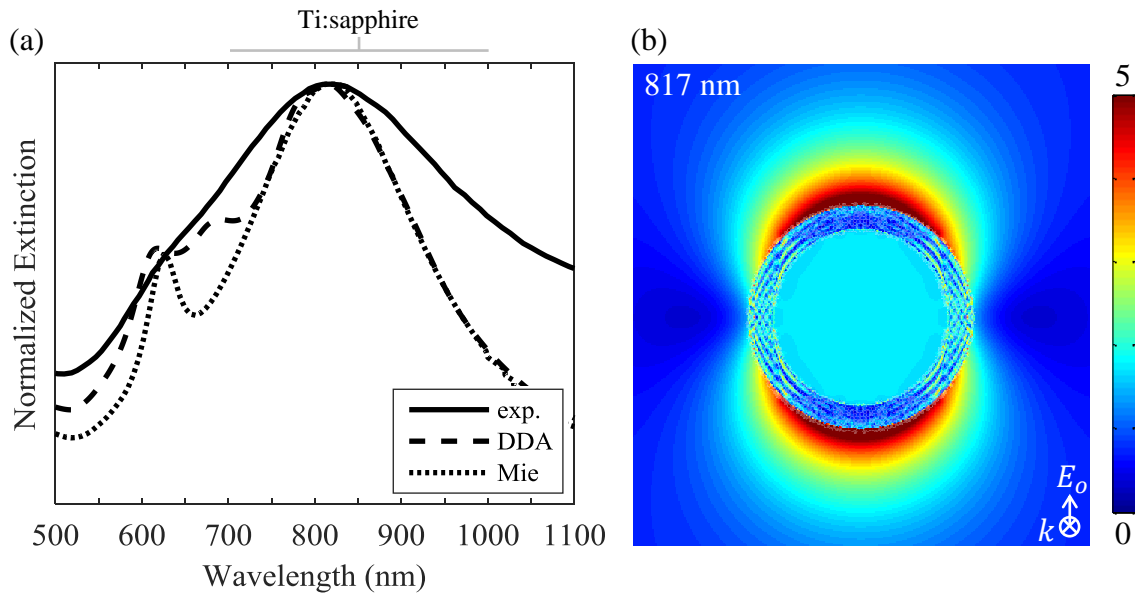


Figure 6.4: (a) Normalized extinction spectra for 150 nm Au nanoshells (15 nm Au shell; 120 nm diameter SiO_x core) in water according to transmission UV-vis measurements (solid), DDA (dashed), and Mie theory (dotted). Results from DDA and Mie theory were taken at an effective refractive index of 1.40 to account for PVP ligands on the Au. (b) Electric near-field enhancement (E/E_0) at the 817 nm dipole LSPR.

6.3 Second Harmonic Generation

Nonlinear SHG intensity from a ca. 1 μm length MoS_2 monolayer in the absence and presence of a plasmonic field from a 150 nm Au nanoshell (15 nm Au shell; 120 nm diameter SiO_x core) was measured using multi-photon confocal microscopy.²⁸⁸ Figure 6.5 shows calculated linear optical extinction efficiency spectra for the Au nanoshell- MoS_2 heterostructure atop SiO_x

(to account for thermal oxide on the Si wafer) sans any nonlinear optical effects. Electric near-field intensity maps taken at each optical resonance are also shown. Maximas corresponding to MoS₂ C exciton, MoS₂ B exciton coupled with the Au nanoshell quadrupole LSPR, MoS₂ A exciton, and Au nanoshell dipole LSPR were observed at 450 nm, 623 nm, 660 nm, and 820 nm, respectively. The dipole and quadrupole LSPR of the Au nanoshell both red-shifted 3 nm from screening by the MoS₂ monolayer, consistent with related measurements.²³⁰ Single photon (ω) and two-photon frequency (2ω) ranges accessible by the 810-1000 nm excitation spectrum used in the confocal microscope herein are labeled red and blue, respectively, for reference.

Equation 6.1 adapted Equation 1.5 to describe intensity of SHG as a function of competing mechanisms within the heterostructure across the 810-1000 nm excitation spectrum, assuming an undepleted pump and phase coherence.³³

$$I_{2\omega} = \frac{\epsilon_0 \omega^2}{8n_{2\omega} c} [\chi_{2\omega}^{(2)}]^2 L^2 |E_\omega|^4 \quad (\text{Equation 6.1})$$

As the material source for SHG, monolayer MoS₂ determined $\chi_{2\omega}^{(2)}$ (second-order susceptibility) over L (its thickness) and n (linear refractive index). The Au nanoshells only augmented the excitation electric field intensity, E_ω ; their centrosymmetric crystal structure precluded SHG by $\chi^{(2)} = 0$. Calculated linear optical extinction spectra in Figure 6.5 provided qualitative insights towards anticipated SHG trends based on competing influences of MoS₂ $\chi^{(2)}$ in the 2ω regime (blue) versus the Au nanoshell-enhanced E_ω in the ω regime (red). However based on Au nanoshell activity in the ω spectrum, the undepleted pump assumption underlying Equation 6.1 was not anticipated to hold constant across all excitation wavelengths. This constituted a third competing effect on SHG from the heterostructure.

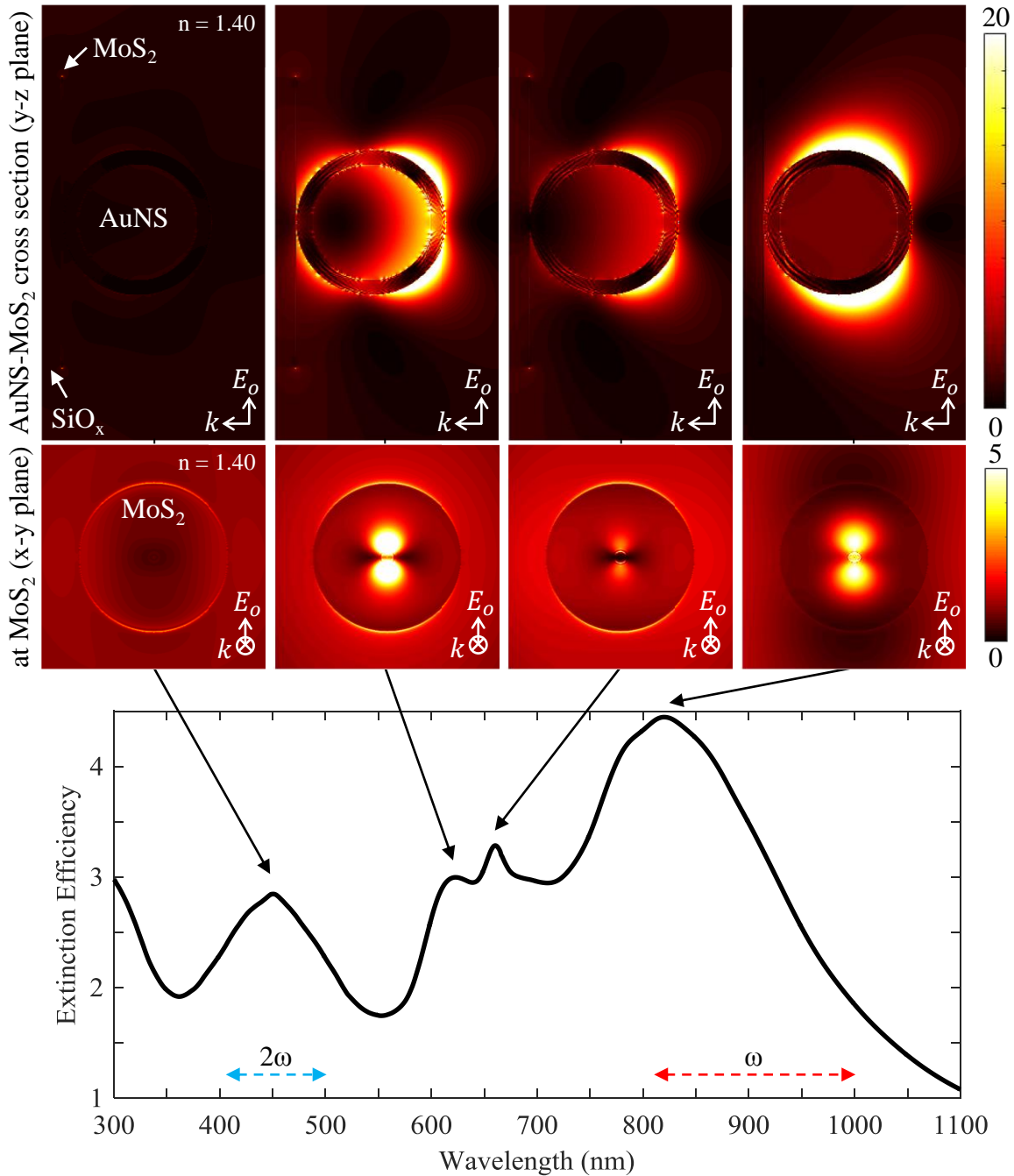


Figure 6.5: Calculated linear optical extinction efficiency of a 150 nm Au nanoshell (AuNS; 15 nm Au shell; 120 nm diameter SiO_x core) and monolayer MoS₂ heterostructure in water. The ω excitation and 2ω detection frequencies measured herein are labeled for reference. Enhanced electric near-field intensity $[(E/E_0)^2]$ plots at 450 nm, 623 nm, 660 nm, and 820 nm at two vantage points: (top) y-z plane cross-section of the AuNS and MoS₂ and (bottom) x-y plane of electric field incident upon the MoS₂ monolayer.

Second harmonic (SH) intensity per unit area was extracted from a ROI encompassing a Au nanoshell-MoS₂ heterostructure or one of its individual components. ROI for each MoS₂ site (with or without Au nanoshells) was selected based on its triangular boundaries. ROI for each isolated Au nanoshell was a circle with equivalent pixel area as the triangular ROI for MoS₂ sites. Total SH intensity per unit area at a given excitation wavelength was taken as raw intensity integrated across the finite SH bandwidth (dependent on temporal coherence of the Ti:sapphire laser). Inhomogeneity of drop-cast protocol secondarily resulted in isolated Au nanoshells and MoS₂ monolayers without Au nanoshells. These sites were analyzed independently as negative control data in § 6.3.1 and 6.3.2 to provide context for SHG from the heterostructure in § 6.3.3.

6.3.1 Molybdenum Disulfide

Nonlinear SHG from monolayer MoS₂ exhibited frequency-dependent intensity with maxima corresponding to expanded density of states from its van Hove singularity.^{158,288} Figure 6.6 shows 2ω emission spectra arising from 810-1000 nm ω excitation of a ca. 1 μm length triangular MoS₂ monolayer. A SEM image and SHG micrographs (colored according to wavelength) are shown above; arrows correspond each micrograph with its spectra. Scattered SH signals appeared Lorentzian with ca. 5 nm bandwidths. Inset graph confirms second-order nonlinear behavior with a 1.80 dependence, which was lower than 2.0 likely due to absorption of the SH above the 1.86 eV MoS₂ bandgap. The C transition acts as a loss (absorption of SH signal) and as a SHG gain ($\chi^{(2)}$ resonance) simultaneously. It was noteworthy that SHG from MoS₂ remained finite at excitation wavelengths less than 810 nm and greater than 1000 nm, but acquisition parameters were optimized to fully capture the resonance behavior accessible from Ti:sapphire excitation. Intensity of the SH did not vary with time (data not shown for brevity), indicating no induced photodamage.

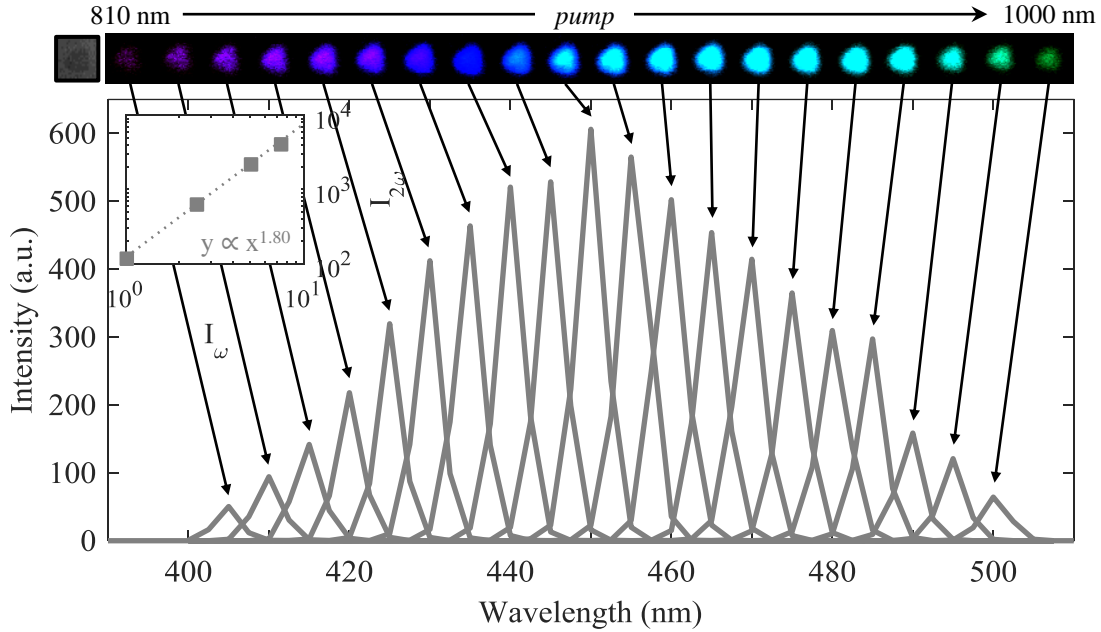


Figure 6.6: Representative SH scattering (per unit area) spectra from a ca. 1 μm MoS₂ monolayer at 810-1000 nm excitation (10 nm step). Inset shows 1.80-power dependence between SH and pump intensities taken at 880 nm excitation, confirming a second-order nonlinear process. SEM and SH micrographs of the MoS₂ crystal at each excitation wavelength are shown (top) with arrows indicating corresponding spectra.

Mean SHG intensity measured from ten distinct monolayer MoS₂ crystals exhibited a maxima at 450 nm associated with the C exciton, which was consistent with the DDA-calculated $\chi^{(2)}$ spectra in Figure 3.11 (see § 3.4.3).²⁸⁸ Malard *et al.* also measured an association of SHG in this spectrum to the direct C exciton transitions near the Γ point at ca. 2.8 eV (450 nm).⁵⁰ Figure 6.7 shows the (a) mean SHG intensity per unit area and (b) mean of sample-normalized SH intensity of ten MoS₂ monolayers, along with superposed DDA-calculated $\chi^{(2)}$ spectra (dashed) and measured linear optical extinction spectra revealing the C transition in (b). Wide error bars in Figure 6.7(a) reflect minute variations in MoS₂ crystal size; SHG signal scales with material volume.²¹⁰ Normalizing SHG from each MoS₂ sample and taking the mean at each excitation frequency removed size dependence and allowed insights into the frequency-dependence of SHG arising from its electronic band structure.

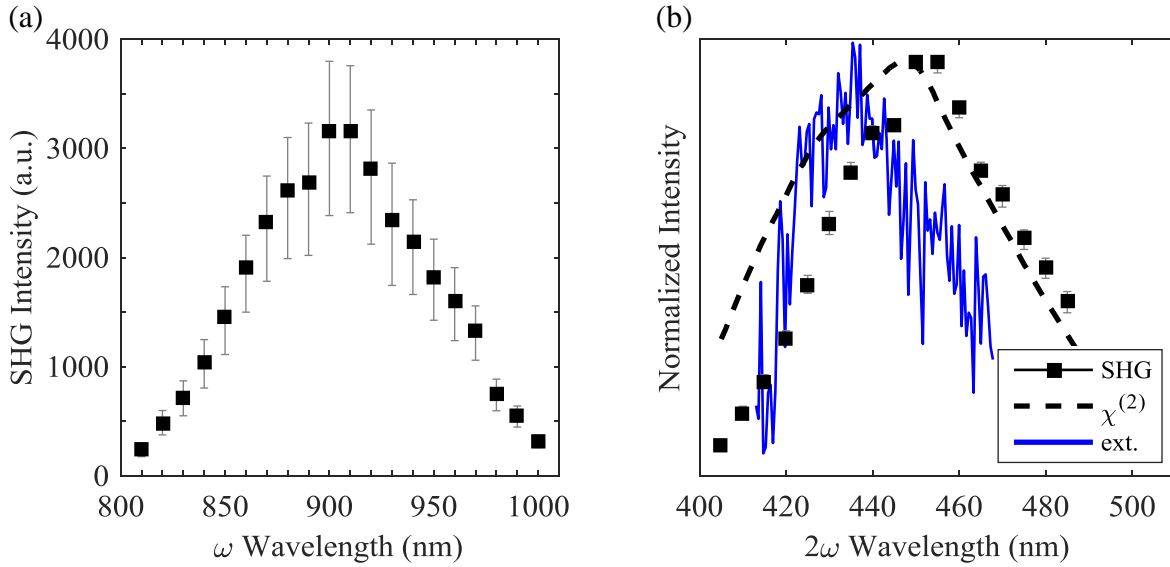


Figure 6.7: SHG behavior of averaged across ten distinct ca. 1 μm MoS₂ monolayers at 810-1000 nm ω excitation (10 nm step). (a) Mean integrated intensity per unit area of the SH versus excitation wavelength. (b) Mean of normalized intensity per unit area versus SH wavelengths (black squares; LHS) with superposed (i) DDA-calculated $\chi^{(2)}$ (dashed) and (ii) linear optical extinction spectra (blue). Error in each graph is the maximum and minimum from the mean; error in (a) accrued from minute variations in MoS₂ crystal size.

Measured SHG trend aligned closely with DDA-calculated $\chi^{(2)}$, which was based on a linear dielectric function and Miller's rule.^{33,207,216} Increased states around the C exciton transition, shown in the linear optical extinction spectra, occurred 15 nm offset from the 450 nm SHG maximum, consistent with measurements by Malard *et al.*⁵⁰ Computation by density functional theory (DFT), density matrix theory (DMT), and a Bethe-Salpeter exciton (BSE) model of $\chi^{(2)}$ for MoS₂ corroborated these measured SHG trends.^{49,53,54,206} A ca. 7 nm offset between maximal measured SHG and theoretical $\chi^{(2)}$ was ostensibly attributable to differences in experimental environment and handling protocols²³⁹ between the MoS₂ sample used herein versus that used to obtain linear dielectric data by Mukherjee *et al.*²¹⁷ A 7 nm offset in occurrence of the C exciton maxima was also observed. Polarization-resolved SHG from the MoS₂ crystals to elucidate depolarization or crystal axis orientation was not measured herein, but has been well-characterized elsewhere.⁴⁹⁻⁵¹

6.3.2 Gold Nanoshells

The Au nanoshells exhibited broadband luminescence rather than nonlinear SHG.²⁸⁸ Figure 6.8 shows the negligible mean detected intensity in the 2ω spectrum from 810-1000 nm ω excitation of five Au nanoshells. Centrosymmetric face-centered cubic crystal structure of Au and amorphous structure of SiO_x prohibited SHG beyond minute surface contributions, where crystal symmetry was inherently broken.²⁸⁹ Broadband luminescent emission independent of excitation frequency was observed, consistent with other reports of high-fluence laser excitation of metal nanoantennas.²⁹⁰⁻²⁹³ The broadband luminescent emission was attributed to interband relaxation of d-orbital electrons in the Au.²⁹³

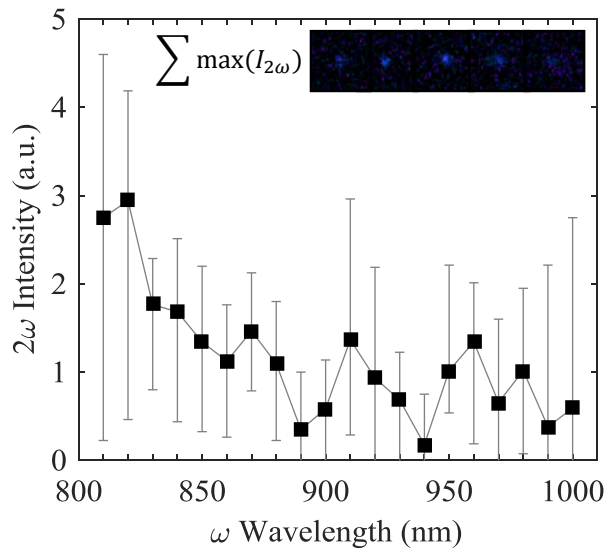


Figure 6.8: Mean 2ω emission intensity (per unit area) averaged across five distinct 150 nm Au nanoshells (15 nm Au shell; 120 nm diameter SiO_x core) from 810-1000 nm ω excitation (10 nm step). Error is the maximum and minimum from the mean. Inset are confocal images of the five individual Au nanoshells according to summed, maximum luminescence from 400 nm to 480 nm detected from a 5 μm z-scan using 820 nm excitation.

Spectral profile of 2ω luminescence was consistent with the LSPR profile in Figure 6.4, where intensity decreased as excitation was detuned from the dipole LSPR, similar to another report.²⁷⁶ Inset to Figure 6.8 shows confocal images of the five isolated Au nanoshells that were

acquired from 820 nm excitation by translating maximal detected 400-480 nm luminescence over a 5 μm z-scan into a 2D projection. This method of secondary image acquisition enabled visualization of singular, isolated Au nanoshells and was corroborated by SEM.

Nonlinear SHG from metal nanoantennas has been observed,²⁹⁴⁻²⁹⁹ but with the caveat that progressive deviation from morphological centrosymmetry returned SH signal that would have been otherwise suppressed.^{294,300,301} For example, Walsh *et al.* enhanced SHG 40x from Au nanocylinder arrays by plasmon-phonon transduction at various laser intensities to introduce morphological disorder into the otherwise centrosymmetric cylinders.²⁹⁵ Augmentation of solely surface SHG by plasmon-enhanced local electric fields is an alternative mechanism that has been studied.²⁹⁸ Spherical Au nanoshells with both centrosymmetric morphology and underlying crystallinity were studied herein, which resulted in negligible SHG.

6.3.3 Molybdenum Disulfide with a Gold Nanoshell

Nonlinear SHG from monolayer MoS₂ was enhanced, ostensibly by the surface plasmon-augmented local electric field from a single Au nanoshell.²⁸⁸ Figure 6.9 shows 2ω emission spectra arising from 810-1000 nm ω excitation of a ca. 1 μm MoS₂ monolayer in the absence (gray) and presence (red) of one 150 nm Au nanoshell at its center. Corresponding SEM images and SHG micrographs (colored according to wavelength) are shown above; arrows correspond each confocal micrograph with its associated spectra. Inset graph confirms second-order nonlinear behavior of the heterostructure with a 1.77 dependence, which was 0.03 lower than the coefficient for MoS₂ due ostensibly to increased absorption from the Au nanoshell. Again, SHG remains finite at excitation wavelengths less than 810 nm and greater than 1000 nm.

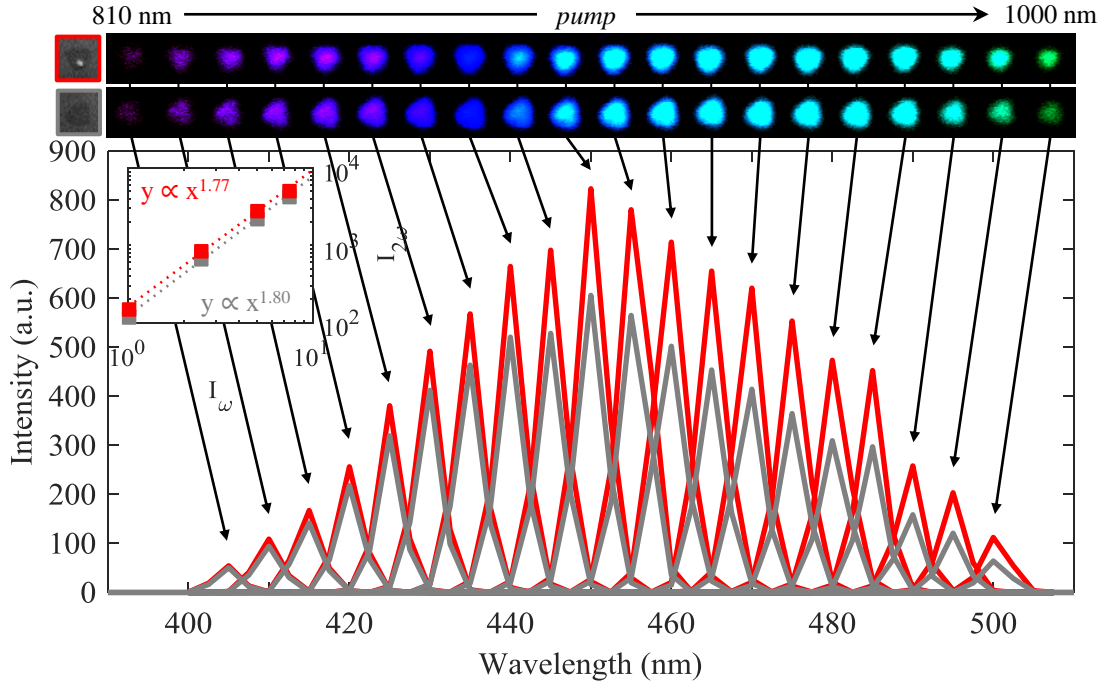


Figure 6.9: SH scattering (per unit area) spectra from a ca. 1 μm monolayer MoS_2 crystal at 810-1000 nm excitation (10 nm step) in the absence (gray) and presence (red) of a single 150 nm Au nanoshell (15 nm Au shell; 120 nm diameter SiO_x core). Inset shows 1.77- and 1.80-power dependence between SH and pump intensities taken at 880 nm excitation, confirming a second-order nonlinear process for the heterostructure and negative control, respectively. SEM and SH micrographs at each excitation wavelength are shown (top) with arrows to corresponding spectra.

Although enhanced 17-84%, frequency-dependence of enhanced SHG from the Au nanoshell- MoS_2 heterostructure shown in Figure 6.10 did not match the anticipated profile based on Equation 6.1 and the linear optical extinction spectrum in Figure 6.5.²⁸⁸ The LSPR at 820 nm was anticipated to predominate and given higher SHG enhancements. Competition between (i) the plasmon-enhanced local field and (ii) MoS_2 $\chi^{(2)}$ was expected to yield to the former, whereby power dependence in Equation 6.1 was 4 versus 2, respectively.³³ Reported error for MoS_2 was the maximum and minimum from the mean across four crystals adjacent to the heterostructure. Potential consequences from plasmonic hot electron injection remained unclear. Overall, spectrum profile of enhanced SHG from the heterostructure closely resembled $\chi^{(2)}$ of MoS_2 because of nanoantenna design limitations, to be discussed in the forthcoming section.

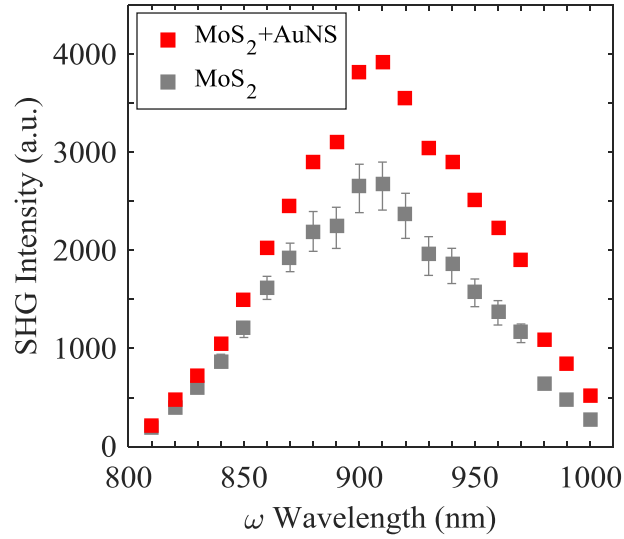


Figure 6.10: Integrated SHG intensity (per unit area) of a ca. 1 μm monolayer MoS_2 crystal at 810-1000 nm ω excitation (10 nm step) in the absence (gray; sample size of four) and presence (red; sample size of one) of a single 150 nm Au nanoshell (AuNS; 15 nm Au shell; 120 nm diameter SiO_x core). Error is the maximum and minimum from the mean.

6.4 Enhanced Nonlinear Frequency Conversion Efficiency

Surface plasmon-augmented local fields appeared to be primarily responsible for enhanced SHG conversion efficiency from the Au nanoshell- MoS_2 monolayer heterostructure.²⁸⁸ To date, plasmonic enhancement of SHG from an adjacent material has been quantified by (i) an intensity enhancement factor^{274–277} or (ii) enhancement to an effective $\chi^{(2)}$ of the composite media.²⁷³ Although magnitude and frequency dependence of intensity enhancement factors contain fingerprints of the underlying responsible mechanisms, its scope portrays a limited insight. Herein, performance of the heterostructure to convert incident irradiation to a SH was examined heuristically from the viewpoint of a conversion efficiency.

An *ab initio* estimation of SH conversion efficiency, $\eta_{2\omega}$, for MoS_2 was calculated to be up to $7 \times 10^{-11}\%$ at 5 mW irradiation per Equation 6.2 under the following assumptions:^{302,303} (i) L

of MoS₂ (6.5 Å) was within the confocal focus depth,³² (ii) no pump depletion by the 2D MoS₂, (iii) phase coherence,^{32,33} and (iv) DDA-calculated $\chi^{(2)}$ via Miller's rule.²⁰⁷

$$\eta_{2\omega} = \eta_{norm} (I_{\omega} L^2) \quad (\text{Equation 6.2})$$

$$\eta_{norm} \equiv \frac{2\pi^2 [\chi_{2\omega}^{(2)}]^2}{n_{\omega}^2 n_{2\omega} c \epsilon_0 \lambda_{\omega}^2} \quad (\text{Equation 6.3})$$

To allow direct comparison of SHG performance with other nonlinear materials, Equation 6.3 defines the normalized SHG conversion efficiency, η_{norm} , of excitation wavelength λ_{ω} . Note η_{norm} was independent of L and I_{ω} . An absolute calculation of $\eta_{2\omega}$ according to the relative measured intensities of the SH and excitation beams was precluded absent rigorously characterized signal losses in the confocal microscope (e.g., reflection losses at each lens/mirror, quantum efficiencies of PMT, etc.).

The η_{norm} for monolayer MoS₂ on SiO_x across the 810-1000 nm excitation spectrum was calculated using (i) DDA-simulated $\chi^{(2)}$ (via Miller's rule and corroborated by Hyper Rayleigh Scattering measurements; see § 3.4)²⁰⁷ and (ii) n taken from Mukherjee *et al.*²¹⁷ In contrast to examining $\chi^{(2)}$ as the sole precursor for SHG spectrum profiles, Equation 6.3 also accounts for the wavelength and optical dispersion at the SH and excitation frequencies. Under the condition that local electric field augmentation by the Au nanoshell enhanced SHG, η_{norm} for MoS₂ was multiplied by DDA-calculated $(E/E_0)^2$ power enhancement factors at each excitation wavelength. This represented a theoretical η_{norm} for the heterostructure according to Equation 6.2. For a heuristic comparison, η_{norm} for MoS₂ was multiplied by the measured SHG enhancement factors at each excitation wavelength (i.e., ratio of curves in Figure 6.10). This comparison allowed attribution of measured SHG enhancement to enhanced local fields from the Au nanoshell in the absence of other gain mechanisms.

Enhanced optical power “delivered” to the MoS₂ monolayer from the Au nanoshell was first calculated by the DDA to account for frequency-dependent violation of the undepleted pump approximation underlying Equation 6.1.²⁸⁸ Maximum optical power enhancement factor at the MoS₂ by the Au nanoshell dipole LSPR was 1.25, shown in Figure 6.11. Despite detuning away from the dipole LSPR, the enhanced optical power was nearly constant (within $\pm 5\%$) across the 810-1000 nm excitation spectrum. This design deficiency was because of the spherical morphology of the Au nanoshell. Surface plasmon strength decays exponentially across space.^{60,73,304} Herein, 75 nm separated the MoS₂ monolayer from the dipole axis of the Au nanoshell. Presence of PVP ligands (ca. 10 nm in length) likely exacerbated this issue.

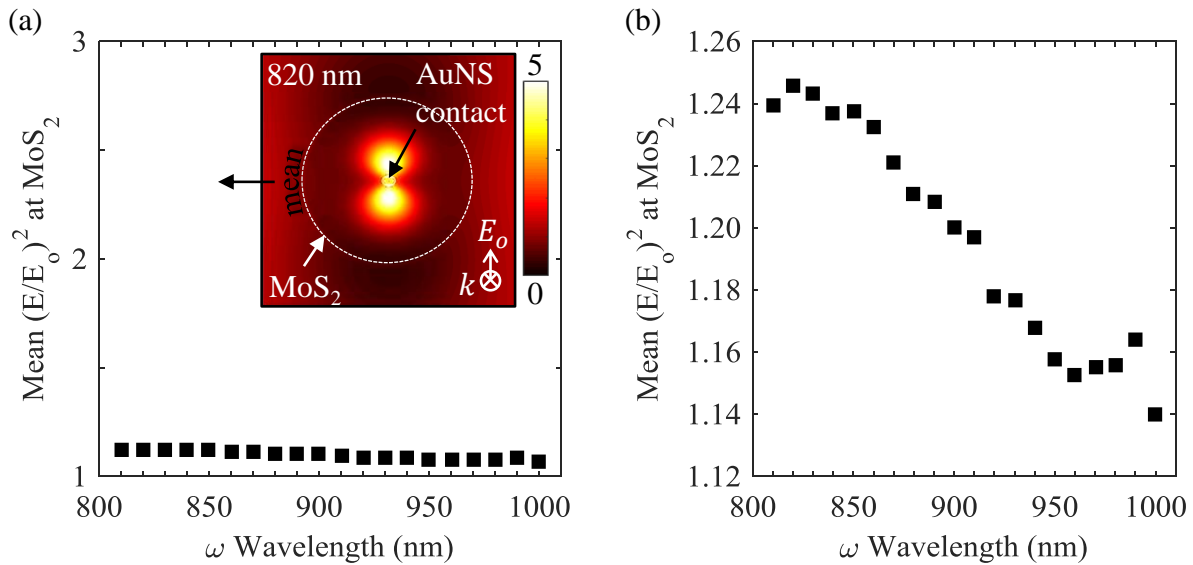


Figure 6.11: Mean enhanced optical power incident upon a 300 nm diameter MoS₂ monolayer by a 150 nm Au nanoshell (AuNS; 15 nm Au shell; 120 nm diameter SiO_x core) at 810-1000 nm ω excitation calculated by DDA plotted at (a) 0 to 5 scale and (b) 1.12 to 1.26 scale. The former was chosen according to scale of corresponding enhanced optical power plot at 820 nm, taken verbatim from Figure 6.5.

Conversely, excitation at the 623 nm quadrupole LSPR would have “delivered” more power to the MoS₂ because of closer physical proximity of its oscillating electrons to the MoS₂ monolayer, seen in its electric near-field plot of Figure 6.5. Replacement of the spherical Au

nanoshell with an alternative nanoantenna of flat morphology, e.g., a nanorod or nanoring,^{75,119,154} could have more effectively “delivered” optical power to the MoS₂.²³⁰ LSPR activity of nanorods, however, are dependent on incident polarization which would have introduced an additional degree of convolution in data interpretation. Spherical nanoshells did not exhibit polarization dependence.⁹⁴ Nanorings would have required complex top-down lithography schemes.^{120,125}

Figure 6.12(a) shows theoretical η_{norm} for monolayer MoS₂ in the absence (gray line) and presence (red line) of a single plasmonic Au nanoshell, under the conditions that the Au nanoshell (i) did not contribute SHG and (ii) enhanced η_{norm} according to its local electric field.²⁸⁸ The MoS₂ control exhibited peak η_{norm} of 0.016% W⁻¹, which increased to 0.019% W⁻¹ upon addition of a single nanoantenna. By comparison, ca. 10⁻⁴ % W⁻¹ has been reported for lithium niobate technology^{305–307} and ca. 1% W⁻¹ for a complex Au metasurface coupled to indium gallium arsenide multi-quantum wells.³⁰⁸

Superposed as red squares Figure 6.12(a) is MoS₂ η_{norm} multiplied by the measured SHG enhancement factors (X ; taken from Figure 6.10).²⁸⁸ These heuristic “experimental” η_{norm} values agreed well with theoretical estimations in magnitude and frequency dependence. Subtle variances could be interpreted, however, such as the shoulder at 870 nm prevalent in the experimental data. Such subtleties ostensibly arose from differences between MoS₂ samples measured herein and that used by Mukherjee *et al.*,²¹⁷ as discussed earlier in § 6.3.1. This analysis was repeated in Figure 6.12(b) with an adjusted MoS₂ $\chi^{(2)}$ profile to resemble the unique sample studied herein. Briefly, the initial DDA-calculated $\chi^{(2)}$ based upon Mukherjee *et al.*²⁰⁷ was red-shifted 7 nm according to equivalent mismatches in measured versus calculated (i) C exciton transition and (ii) SHG maxima [see Figure 6.7(b)]. Subsequently, the measured normalized SHG profile in Figure 6.7(b) was linearly scaled to their equivalent DDA-calculated $\chi^{(2)}$ magnitudes (see Figure 3.11).

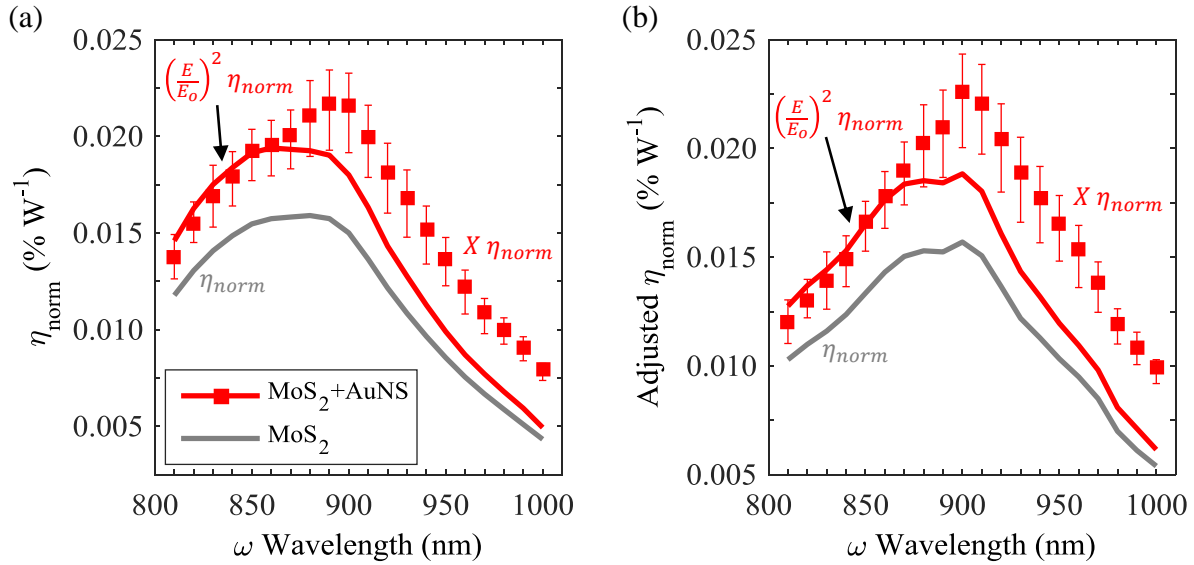


Figure 6.12: The η_{norm} for a MoS₂ monolayer in the absence (gray) and presence (red) a single 150 nm Au nanoshell (AuNS; 15 nm Au shell; 120 nm diameter SiO_x core) according to an enhancement in the local electric field. “ $(E/E_0)^2 \eta_{norm}$ ” represents theoretical η_{norm} for the heterostructure (red line). “ $X \eta_{norm}$ ” represents measured η_{norm} for the heterostructure (red squares), where X is the measured SHG enhancement factors (ratio of curves in Figure 6.10). Two approaches to the analysis are presented in (a) and (b), where the latter features an adjusted η_{norm} for each scenario after tuning the MoS₂ control η_{norm} to resemble the measured profile in Figure 6.7. Error is the maximum and minimum from the mean.

Agreement improved between the theoretical and heuristic experimental η_{norm} scenarios for the Au nanoshell-MoS₂ heterostructure after adjusting the profile of their underlying MoS₂ control η_{norm} to resemble measured SHG data in this work, shown in Figure 6.12(b). Taken together with underlying assumptions of the analysis, the overall agreement in magnitude and frequency dependence throughout Figure 6.12 implied that plasmonic electric-field augmentation was primarily responsible for measured SHG enhancement in the Au nanoshell-MoS₂ heterostructure. Ultimate $\eta_{2\omega}$ for the heterostructure improved to $9 \times 10^{-10} \%$ at 5 mW irradiation, per Equation 6.2. Other influences leading to measured SHG gain remain to be identified. Similar analyses were recently performed on SHG from tungsten diselenide (WSe₂) enhanced by a Si photonic crystal,³⁰⁹ but absence of a negative control and convolution of the SH with broad luminescence made a rigorous comparison difficult.

6.5 Second Harmonic Generation Enhanced by Gold Nanoshell Dimers

Nonlinear SHG intensity from ca. 1 μm length MoS_2 monolayers interfaced with dimers of 150 nm Au nanoshells (15 nm Au shell; 120 nm diameter SiO_x core) exhibited enhancements consistent with surface plasmon-augmentation of the local electric field. Figure 6.13 shows measured SHG intensity enhancement factors, X , by a Au nanoshell dimer with (blue) 320 nm and (black) 150 nm gap relative to their negative controls. Strength of the local electric field within nanoantenna dimers scales with decreasing gap size due to capacitive coupling.^{310–312} Corresponding SEM images are inset. Second-order dependence of SHG on excitation intensity was measured with 1.87 and 1.82 dependencies for 320 nm and 150 nm gap dimers, respectively (data not shown). Error bars represent the maximum and minimum from the mean arising from differences in MoS_2 control sample size, which was two in each case. Only one Au nanoshell dimer was measured at each gap size.

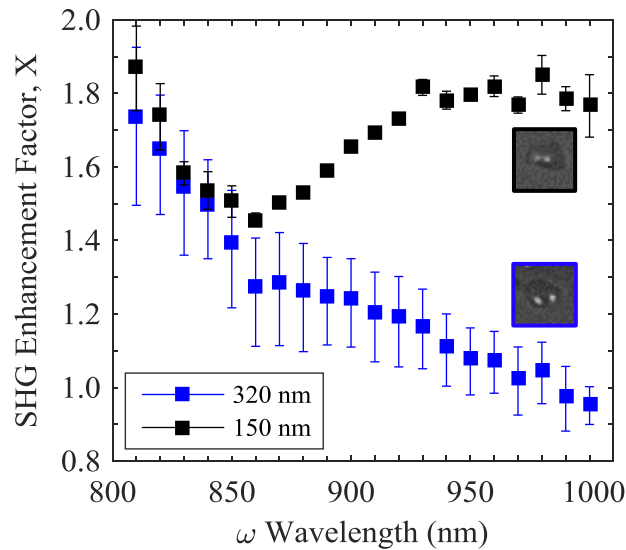


Figure 6.13: Measured SHG enhancement factor for ca. 1 μm monolayer MoS_2 crystals at 810–1000 nm ω excitation (10 nm step) by 150 nm Au nanoshell (AuNS; 15 nm Au shell; 120 nm diameter SiO_x core) dimers with (blue) 320 nm and (black) 150 nm gaps. Error is the maximum and minimum from the mean enhancement over two MoS_2 negative controls; one dimer was measured for each gap size.

Enhancement of SHG from MoS₂ at the nanoshell LSPR was highest for the 150 nm gap Au nanoshell dimer, reaching up to an 88% enhancement. Expanding the gap to 320 nm appeared to decrease the maximum enhancement to 74%, consistent with reduced inter-nanoshell coupling within the dimer. SHG enhancement decreased as the excitation wavelength was detuned from the LSPR, closely resembling profile of the DDA-calculated $(E/E_o)^2$ factors in Figure 6.11. Beyond 860 nm excitation, however, the measured SHG enhancement factor increased for the 150 nm gap dimer, ostensibly due to the emergence of a secondary plasmon resonance around 960 nm. Emergence of secondary plasmonic resonances at lower energies to the LSPR for nanosphere and nanorod dimers has been observed theoretically and experimentally,^{133,148,313} arising from the coupled interaction. Appearance of such a coupled resonance was confirmed by DDA simulation for longitudinal excitation of the Au nanoshells arranged in a chain with 320 nm constant. Detailed characterization of these Au nanoshell dimer-based heterostructures is ongoing.

6.6 Summary

Nonlinear SHG from a ca. 1 μm length MoS₂ monolayer was broadband enhanced 17-84% by the surface plasmon activity of a single 150 nm Au nanoshell. Intensity of SHG from ten MoS₂ monolayers, five Au nanoshells, and a Au nanoshell-MoS₂ heterostructure were measured using a tunable Ti:sapphire laser coupled to a multi-photon confocal microscope with hyperspectral imaging capability. Plasmonic mode structure of Au-SiO_x nanoshell was characterized for the first time using EELS, revealing a 1.60 eV dark mode and 1.89 eV bright LSPR which red-shifted to 1.52 eV upon immersion into water. The 1.52 eV LSPR was responsible for measured SHG enhancement of the heterostructure. The SHG behavior of monolayer MoS₂ was measured to follow its frequency-dependent $\chi^{(2)}$ profile calculated by the DDA and agreed with other reports.

The Au nanoshells did not exhibit SHG in favor of broadband luminescence. Performance of the heterostructure was examined heuristically using a first-principles SHG conversion efficiency metric and enhanced optical power calculations from the DDA. Enhanced SHG from MoS₂ consistent with local field augmentation was also observed for Au nanoshell dimers. Overall, nonlinear SHG from MoS₂ in the presence of plasmonic fields was measured and described using *ab initio* theory and numerical computation.

CHAPTER 7

CONCLUDING REMARKS

Resonant photon-electron interactions in heterostructures of plasmonic nanoantennas and two-dimensional (2D) transition metal dichalcogenides (TMD) were examined, with emphasis in their infrared energy conversion capabilities through plasmonic hot electron transport and nonlinear frequency mixing. Plasmonic activity of nanoantennas in the presence of 2D TMD exhibited augmented damping characteristics, ostensibly due to hot electron transport. Nonlinear second harmonic generation (SHG) from monolayer molybdenum disulfide (MoS_2) was enhanced by the nanoantennas through their ability to localize energy into intense electric fields. Both findings supported the hypothesis. This chapter summarizes broader importance of the research, findings to date, and ongoing efforts in pursuit of nanoantenna-decorated 2D TMD as an optoelectronic material platform with improved heat rejection beyond conventional thermodynamic paths.

7.1 Importance of Work

Passive recycling of waste infrared energy for optoelectronic signal functionality has short-term importance in enhanced heat rejection and long-term impacts in device power consumption towards energy sustainability. Modern electronic devices (e.g., communication devices and medical sensors) are powered from environmentally toxic batteries or fossil fuel energies, of which approximately 60% of generated energy is wasted to radiation.^{4,5} Concomitantly at the device level, efficient power consumption is limited by up to 80% losses across their electrical interconnects.^{12,13} Rapid heat rejection mechanisms via nonlinear frequency conversion and/or

hot electron transport could complement conventional thermodynamic mechanisms. Integration of such components could provide infrastructure to integrate all-optical, low loss interconnects at $10^3\times$ higher data densities.^{12,13} The U.S. Department of Energy has advocated that energy decarbonization and improving energy yield are keys to a sustainable future.¹

7.2 Summary of Findings

Conversion of infrared energy through (i) plasmonic hot electron transport and (ii) nonlinear frequency mixing was examined in heterostructures of plasmonic nanoantennas and 2D TMD. Nonlinear SHG from infrared irradiation of a MoS₂ monolayer was enhanced 17-84% in the presence of a localized surface plasmon resonance (LSPR) on a gold (Au) nanoshell with efficiency up to 0.023% W⁻¹.²⁸⁸ Capacitive coupling within nanoshell dimers further enhanced SHG from MoS₂. A 150 nm Au nanoshell was chosen for the heterostructure prototype, designed for an infrared LSPR according to discrete/coupled dipole models (i.e., DDA and CDA) for light extinction and electron energy loss spectroscopy (EELS).^{82,94,287} Monolayer MoS₂ was chosen as the nonlinear optical source in the heterostructure prototype because of its intrinsically high second-order nonlinear susceptibility, $\chi^{(2)}$, measured to be 660 ± 130 pm V⁻¹ by Hyper Rayleigh Scattering.²⁰⁷

Transport of plasmonic hot electrons into 2D TMD was measured using EELS in a scanning transmission electron microscope (STEM). Initial studies on 80 nm Au nanospheres physically deposited onto MoS₂ suggested up to $4\pm 2\%$ quantum efficient hot electron transport over a 26 fs timescale.²¹⁸ Optimization of the nanoantenna-TMD ohmic junction by physicochemically bonding 20 nm Au nanoantennas to the TMD improved quantum efficiency to $11\pm 5\%$ and accelerated transport time to 7 fs.²⁶¹ Measured LSPR bandwidth expansion in the

presence of TMD allowed quantitation of putative hot electron injection, after subtracting known damping contributions using DDA. Reliability of the DDA to describe resonant excitation and damping in metal-TMD heterostructures was explored using 80 nm Au nanospheres and 53 nm silver (Ag) nanoprisms interfaced with monolayer MoS₂.²³⁰ Transmission UV-vis extinction measurements corroborated DDA-simulated resonant energies within 2% across different metals, shapes, proximity of LSPR to the MoS₂ bandgap energy, and nanoantenna-MoS₂ contact area. These studies allowed interpretation of their demonstrably enhanced SHG performance and plasmonic damping, ostensibly via hot electron transport.

Material and morphological parameters for designing infrared active plasmonic nanoantennas were expounded by Drude-Lorentz theory and the DDA.^{75,82,94} Although aluminum-doped zinc oxide (Al:ZnO) and indium tin oxide (ITO) appeared well-suited for plasmon-functionalized infrared energy conversion because of their temperature stability above 1500 °C, immature characterization and synthesis protocols precluded their use in favor of Au. Mimicking EELS in the DDA comprehensively characterized the morphological influences of radial elongation and annulation on the appearance of plasmonic modes in Au nanoantennas.⁹⁴ Infrared plasmonic activity of spherical Au nanoshells at ca. 1.5 eV was characterized by EELS in a STEM.²⁸⁷ Overall, new insights into the resonant optoelectronics of coupled plasmonic and excitonic materials spanning the linear and nonlinear optical regimes were introduced in the contact of enhanced infrared energy conversion.

7.3 Future Directions

Understanding passive conversion of infrared energy via nonlinear frequency mixing or plasmonic hot electron injection could provide foundations to engineer heat rejection/harvesting

strategies using surface plasmon resonance. Alternative plasmonic materials, namely aluminum-doped zinc oxide (Al:ZnO) or indium tin oxide (ITO), would be prime candidates for practical implementation of such strategies. Future nanoantenna-TMD heterostructure prototypes should consider use of Al:ZnO or ITO as their synthesis and electrodynamic understanding matures. Low losses relative to noble metals and resistance to structural deformation from greater than 1000 °C thermal gradients support their use as nanoantennas for such systems.¹¹⁵

Nonlinear SHG from ITO across a 1150-1670 nm infrared range was recently examined, showing broadband SHG from a 37 nm ITO that was equivalent to a 0.5 mm quartz plate.³¹⁴ Hence, ITO could serve a secondary energy conversion source. Nanoantenna morphology could reflect a recently proposed trapezoidal log-periodic architecture that was engineered for broadband infrared resonances with greater than 100x local power augmentation.³¹⁵ In lieu of nonlinear frequency mixing processes, infrared photons could also be upconverted to higher energies at 25% quantum efficiency through radiative recombination of plasmonic hot electrons injected into a quantum well.²⁸

Efficiency of SHG conversion could be increased by engineering a secondary, higher-energy plasmon resonance with high scattering activity to emerge at the 2ω wavelength. Many nanoantenna designs have been proposed,³¹⁵⁻³¹⁹ taking advantage of multi-pole resonances or near-field Fano coupling. Irradiation at the characteristic Fano dip, a dark plasmon resonance, avoids associated intrinsic losses in favor of improved field augmentation metrics over isolated or randomly arranged nanoantennas.³¹⁸ However, little experimental work has been performed^{318,319} to date to corroborate frequency conversion performance of proposed designs. Such concepts could be extended to ITO or Al:ZnO nanoantennas to further improve SHG from TMD. Coupling the 2ω -active plasmon resonance with TMD excitonic transitions could further enhance SHG from

heterostructures.⁵³ Unfortunately prototyping on these premises is hampered by laser technology and detection deficiencies of modern spectroscopy instrumentation.

Far-field Fano resonant coupling between surface plasmons and lattice diffraction in periodic lattices, resulting in a coupled lattice resonance (CLR), offer order-of-magnitude enhancements to TMD SHG in next-generation prototypes. Irradiation at the CLR of a Au dimer lattice has been shown to enhance its intrinsic SHG response by 30x.³¹¹ Appearance of the CLR persists in the presence of TMD, whereby photoluminescence (PL) from monolayer molybdenum diselenide (MoSe_2) was recently enhanced 25x by the CLR of a Au nanorod lattice.³²⁰ It is proposed herein to engineer a nanoantenna lattice with localized and coupled resonances (i.e., a surface plasmon and CLR) occurring at the 2ω and ω frequencies, respectively, to leverage their favorable electrodynamic behavior towards facilitating energy conversion processes for optoelectronics.

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Appendix A: Description of Research for Popular Publication

The global progression towards “green energy” has reduced fossil fuel consumption by improving performance and consumer acceptance of alternative energy technologies, such as solar cells and hybrid cars. However almost 60% of energy generated by traditional and alternative methods is wasted away as heat, never to be used in our smart phones or car engines. Gregory Forcherio, a student at the University of Arkansas under the guidance of Dr. D. Keith Roper, is working to recapture that wasted heat energy and use it to power the next generation of technology.

Recycling heat energy is not a new idea. Products developed and tested to date, from body-heat powered watches to combustion engines without alternators, were unsuccessful because of efficiency limitations inherent to the materials that were used. Forcherio and Roper hypothesize entirely new ways to recover heat energy.

At the heart of this new technology are engineered nano-sized structures, called nanoparticles, which can guide light and heat in ways not typically seen in nature. Decorating specific materials with intrinsic frequency conversion properties, such as atomically-thick molybdenum disulfide, a common machining lubricant, with nanoparticles has the ability to transform heat into optical or electronic signals. “Nanoparticles have the ability to focus light for strengthening conversion of heat radiation frequencies to telecom frequencies,” says Forcherio.

Still in the prototyping stage, the combination of nanoparticles and atomically thick materials can potentially revolutionize the way our devices are powered and function. Personal power networks, battery-less medical monitors, and faster computers are a few examples of where Forcherio and Roper’s efforts could lead down the road.

Appendix B: Newly Created Intellectual Property

The following list indicates newly created intellectual items.

1. Method to simulate optical interactions between nanoantennas and arbitrary, multi-scale, complex dielectric materials by discrete dipole approximation
2. Method to simulate optical properties for two-dimensional regular lattices of arbitrarily-shaped nanoantennas embedded in inhomogeneous, complex dielectric environments
3. Method to measure orientation-averaged second nonlinear coefficients (β and $\chi^{(2)}$) for two-dimensional materials by Hyper Rayleigh Scattering
4. Mechanisms for heat recycling/rejection from temperature gradients by (i) plasmonic hot electron transport and/or (ii) multi-order nonlinear frequency conversion

Appendix C: Potential Patent & Commercialization Aspects

C.1 Patentability of Intellectual Property

Potential patentability of each item in Appendix B was considered. It was determined that one of the items could be patented. This is described in detail for each item below:

1. An open-source computational technique based on Maxwell's equations was used to simulate optical properties of nanocomposites featuring two-dimensional material components. The approach was published by John Wiley & Sons on June 8, 2016 [G. T. Forcherio *et al.*, *Adv. Opt. Mater.* (2016), 4, 1288]. The item is patentable for one month. It is of the opinion of the author pursuit of a patent is not warranted.
2. Use of an established modeling technique to synthesize the coupled and discrete dipole approximations was extended to account for inhomogeneous, complex dielectric environments. The approach was published by Elsevier on August 4, 2015 [G. T. Forcherio *et al.*, *J. Quant. Spectrosc. Radiat. Transfer* (2015), 166, 93]. The item is no longer patentable. It is of the opinion of the author pursuit of a patent was unwarranted.
3. An established technique in nonlinear optical characterization was used for the first time to examine nonlinear coefficients of a two-dimensional material. Intellectual property is shared in part with University of Geneva in Switzerland and University of Savoy in France. It is of the opinion of the author pursuit of a patent is not warranted.
4. Two mechanisms were proposed for passive heat management (e.g., rejection or recycling) applications utilizing quantum electrodynamic processes in a novel way. This item could be patentable. It is of the opinion of the author further studies are required to examine practicality and gauge economic feasibility prior to pursuit of a patent.

C.2 Commercialization Aspects of Intellectual Property

Commercialization opportunities for each item in Appendix B was considered. It was determined that one of the items exhibited commercial appeal. These opportunities are described in detail for each item below:

1. The underlying computational algorithm is open-source freeware and thus does not exhibit commercial appeal.
2. The individual, underlying computational algorithms are open-source freeware and thus do not exhibit commercial appeal. A streamlined software package could be of interest to a minute subset of the scientific community, but is too limited in its applicability to appeal to a broader scientific community.
3. The measurement technique is highly accessible in optics laboratories featuring pulsed lasers and does not require special optical components or apparatuses. This item, in of itself, does not exhibit commercial appeal.
4. Design and implementation of novel nanomaterials for thermal energy management exhibits commercial appeal as an alternative to thermoelectric materials. However, it is of the opinion of the author the path to market timeline, at this stage, exceed the 20 year patent term of protection.

C.3 Possible Prior Disclosure of Intellectual Property

Disclosure of each item in Appendix B which could impact patentability was considered. These disclosures described in detail for each item below:

1. The underlying software is open-source. The approach was published by John Wiley & Sons on June 8, 2016 [G. T. Forcherio *et al.*, *Adv. Opt. Mater.* (2016), 4, 1288] and SPIE

on September 16, 2016 [G. T. Forcherio *et al.*, Proceedings of SPIE 9919, Nanophotonic Materials XIII, 991911]. The approach was presented to an audience without non-disclosure agreements on August 31, 2016 at the SPIE Optics + Photonics conference. A computational tool enabling other researchers to re-create published results and generate new results was published open-source on nanoHUB [M. Seeram *et al.*, nanoHUB, DOI: 10.4231/D3J960B3D].

2. The underlying software used are open-source, although one was modified to obtain the intellectual property. The approach was published by Elsevier on August 4, 2015 [G. T. Forcherio *et al.*, *J. Quant. Spectrosc. Radiat. Transfer* (2015), 166, 93] and SPIE on March 14, 2016 [G. T. Forcherio *et al.*, Proceedings of SPIE 9756, Photonic and Phononic Properties of Engineered Nanostructures VI, 975615]. The approach was presented to an audience without non-disclosure agreements on February 17, 2016 at the SPIE Photonics West conference.
3. Experiments and data interpretation were conducted in collaboration with colleagues at University of Geneva in Switzerland and University of Savoy Mont Blanc in France.
4. This item has not been disclosed publically.

Appendix D: Broader Impact of Research

D.1 Applicability of Research Methods to Other Problems

Theoretical and experimental methods employed in this work are directly applicable to research problems throughout the nanoscience community. The open-source discrete dipole approximation (DDA) is readily available to describe electrodynamic behavior of non-metallic nanoantennas, two-dimensional materials beyond transition metal dichalcogenides (e.g., phosphorene), and bulk media. Electron energy loss spectroscopy (EELS) may be used for chemical mapping/identification of materials or studying time-resolved phase change mechanisms. Identification of plasmon decay pathways not yet known is possible. Multi-photon confocal microscopy can three-dimensionally reconstruct or track nanoparticle-labeled biomolecules.

D.2 Impact of Research Results on U.S. & Global Society

Recovering and utilization of waste heat, which comprises 60% of all generated energy, complements policies set by the International Energy Agency to save 160 gigatonnes of projected carbon emissions by 2033. Reducing power requirements of optoelectronic devices and developing emission-less energy sources is advocated by the U.S. Department of Energy. Convergence of thermal energy harvesting and electronics hybridized with optical data transmission could manifest as novel communication devices, wearable medical monitors, and personal power networks with performance unprecedented in the commercial market.

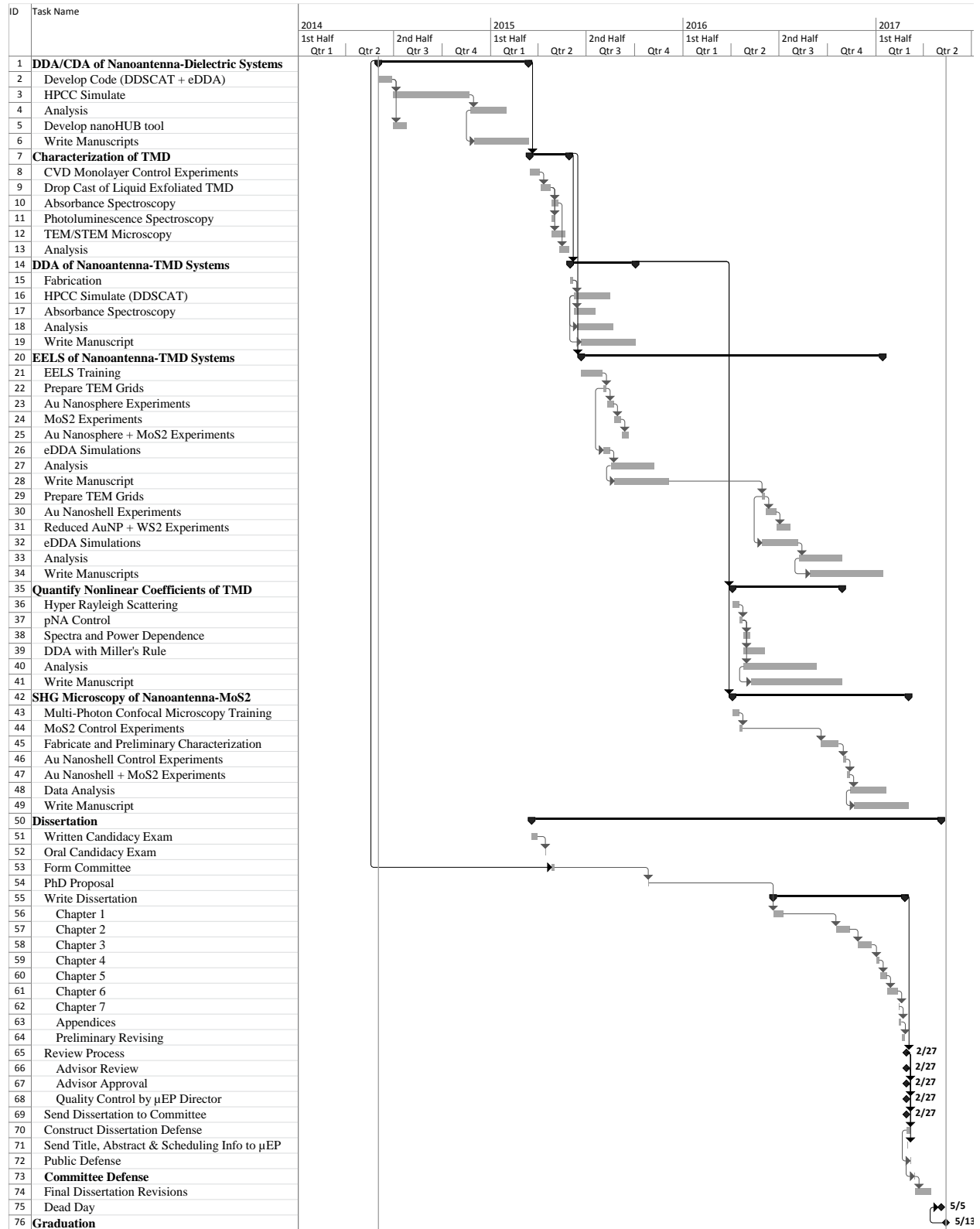
Improved fundamental understanding of plasmon excitation and decay in various environments (e.g., carrier channels in CMOS transistors or biological analyte) accelerates optimization of nanoantenna-based materials into practical devices. Mitigation of ohmic losses in noble metal plasmons to exploit radiative or hot electron damping could provide new avenues

towards improved solar photovoltaics, photodetectors, and biosensors with documented plasmon enhancement. Significant ohmic losses has, to date, prevented their advancement into commercial markets. An experimental and theoretical framework was described herein to assess plasmonic losses in functional devices.

D.3 Impact of Research Results on the Environment

The aim of energy recycling schemes is reduce fossil fuel dependence and shrink the global carbon footprint. Recycling thermal energy within optoelectronics by heat rejection and/or transduction into electric or optical signals could lower effective electric grid power consumption. In niche applications, it is also possible to disrupt reliance on batteries through advancing photocatalytic solar fuel generation. Batteries are known to leak heavy metals (e.g., lithium and lead) into the Earth's soil and water as a consequence of improper disposal. Research is ongoing to determine environmental toxicity of nanoparticles; no adverse effects are known to date. Recent work on bulk silver and copper suggests nanoparticle formation is a naturally occurring process in natural environments.

Appendix E: Microsoft Project for Ph.D. Degree Plan



Appendix F: Identification of Software Used for Dissertation Generation

Computer #1:

Model: Dell Precision T3500
Serial Number: DCRB3L1
Location: Institute for Nanoscience and Engineering, Room 301
Owner: NanoBio Photonics Group, University of Arkansas

Software #1:

Name: Microsoft Office, Professional Plus 2013
Purchased By: Department of Chemical Engineering, University of Arkansas
License: 00216-40000-00000-AA837

Software #2:

Name: Mendeley (v1.16)
Purchased By: Gregory T. Forcherio
License: Freeware

Software #3:

Name: Matlab R2015b (v8.6)
Purchased By: Department of Chemical Engineering, University of Arkansas
License: 601103

Computer #2:

Model: ASUS VivoBook X202E
Serial Number: D2N0BC006118059
Location: Home
Owner: Gregory T. Forcherio

Software #1:

Name: Microsoft Office 365, 2013
Purchased By: Gregory T. Forcherio
License: 00201-10029-87936-AA207

Software #2:

Name: Mendeley (v1.16)
Purchased By: Gregory T. Forcherio
License: Freeware

Software #3:

Name: Matlab R2015b (v8.6, student version)
Purchased By: Gregory T. Forcherio

Appendix G: Published Peer-Reviewed Articles & Conference Proceedings

Peer-Reviewed Articles

- **G. T. Forcherio**, M. Benamara, and D. K. Roper, “Electron energy loss spectroscopy of hot electron transport between gold nanoantennas and molybdenum disulfide by plasmon excitation,” *Advanced Optical Materials* (2017), 5, 1600572.
- J. R. Dunklin, C. Bodinger, **G. T. Forcherio**, and D. K. Roper, “Describing plasmonic extinction in optically dense, multi-scale gold nanoparticle-polymer films,” *Journal of Nanophotonics* (2017), 11, 016002.
- **G. T. Forcherio**, D. DeJarnette, M. Benamara, and D. K. Roper, “Electron energy loss spectroscopy of surface plasmon resonances on aberrant gold nanostructures,” *Journal of Physical Chemistry C* (2016), 120, 24950.
- **G. T. Forcherio**, and D. K. Roper, “Spectral characteristics of noble metal nanoparticle-molybdenum disulfide heterostructures,” *Advanced Optical Materials* (2016), 4, 1288.
- **G. T. Forcherio**, P. Blake, M. Seeram, D. DeJarnette, and D. K. Roper, “Coupled dipole plasmonics of nanoantennas in discontinuous, complex dielectric environments,” *Journal of Quantitative Spectroscopy and Radiative Transfer* (2015), 166, 93.
- J. R. Dunklin, **G. T. Forcherio**, and D. K. Roper, “Gold nanoparticle-polydimethylsiloxane films reflect light internally by optical diffraction and Mie scattering,” *Materials Research Express* (2015), 2, 085005.
- J. R. Dunklin, **G. T. Forcherio**, K. R. Berry, and D. K. Roper, “Plasmon optics and thermal dissipation in nanocomposite thin films,” *MRS Proceedings* (2015), 1788.
- **G. T. Forcherio**, P. Blake, D. DeJarnette, and D. K. Roper, “Nanoring structure, spacing, and local dielectric sensitivity for plasmonic resonances in Fano resonant square lattices,” *Optics Express* (2014), 22, 17791.
- P. Blake, S. Kühne, **G. T. Forcherio**, and D. K. Roper, “Diffraction in nanoparticle lattices increases sensitivity of localized surface plasmon resonance to refractive index changes,” *Journal of Nanophotonics* (2014), 8, 083084.
- M. Lisunova, X. Wei, D. DeJarnette, **G. T. Forcherio**, K. R. Berry, P. Blake, and D. K. Roper, “Photothermal response of plasmonic nanoconglomerates in films assembled by electroless plating,” *RSC Advances* (2014), 4, 20894.
- J. R. Dunklin, **G. T. Forcherio**, K. R. Berry, and D. K. Roper, “Gold nanoparticle-polydimethylsiloxane thin films enhance thermoplasmonic heating by internal reflection,” *Journal Physical Chemistry C* (2014), 118, 7523.
- J. R. Dunklin, **G. T. Forcherio**, and D. K. Roper, “Geometric optics of gold nanoparticle-polydimethylsiloxane thin film systems,” *Optical Materials Express* (2014), 4, 375.

- D. DeJarnette, P. Blake, **G. T. Forcherio**, and D. K. Roper, “Far-field Fano resonance in nanoring lattices modeled from extracted, point dipole polarizability,” *Journal of Applied Physics* (2014), 115, 024306.
- M. Lisunova, J. C. Norman, P. Blake, **G. T. Forcherio**, D. F. DeJarnette, and D. K. Roper, “Modulation of plasmonic Fano resonance by the shape of the nanoparticles in ordered arrays,” *Journal of Physics D: Applied Physics* (2013), 46, 485103.
- J. R. Dunklin, **G. T. Forcherio**, K. R. Berry, and D. K. Roper, “Asymmetric reduction of gold nanoparticles into thermoplasmonic polydimethylsiloxane thin films,” *ACS Applied Materials and Interfaces* (2013), 5, 8457.
- **G. T. Forcherio** and D. K. Roper, “Optical attenuation of plasmonic nanocomposites within photonic devices,” *Applied Optics* (2013), 52, 6417.

Conference Proceedings Published

- **G. T. Forcherio**, M. Benamara, and D.K. Roper, “Plasmon excitation and damping in noble metal nanoparticle-MoS₂ nanocomposites,” *Proceedings of SPIE 9919, Nanophotonic Materials XIII*, 991911.
- J. R. Dunklin, **G. T. Forcherio**, K. R. Berry, and D. K. Roper, “Interfacial reflection enhanced optical extinction and thermal dynamics in polymer nanocomposite films,” *Proceedings of SPIE 9919, Nanophotonic Materials XIII*, 99190X.
- D. K. Roper, **G. T. Forcherio**, and D. DeJarnette, “Compact simulation guides subnanometer, femtosecond measure of energy transfer between quasiparticles and hot carriers at interfaces between metals and two dimensional materials,” *Proceedings of SPIE 9923, Physical Chemistry of Interfaces and Nanomaterials XV*, 992312.
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