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DISSERTAÇÃO<br>Mestrado em Engenharia Eletrotécnica - Telecomunicações

# Disparity Compensation using Geometric Transforms 

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# $O_{\text {IPL }}$ <br> escala superiar de recnalagia e gestãa instriruto palitécnico de leiria 

## MASTER DISSERTATION

## Electrical Engineering - Telecommunications

# Disparity Compensation using Geometric Transforms 

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You have to learn the rules of the game. And then you have to play better than anyone else.
(Albert Einstein)

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#### Abstract

This dissertation describes the research and development of some techniques to enhance the disparity compensation in 3D video compression algorithms. Disparity compensation is usually performed using a block matching technique between views, disregarding the various levels of disparity present for objects at different depths in the scene. An alternative coding scheme is proposed, taking advantage of the cameras setup information and the object's depth in the scene, to compensate more complex spatial distortions, being able to improve disparity compensation even with convergent cameras.

In order to perform a more accurate disparity compensation, the reference picture list is enriched with additional geometrically transformed images, for the most relevant object's levels of depth in the scene, resulting from projections of one view to another. This scheme can be implemented in any state-of-the-art video codec, as H.264/AVC or HEVC, in order to improve the disparity matching accuracy between views.

Experimental results, using MV-HEVC extension, show the efficiency of the proposed method for coding stereo video, presenting bitrate savings up to $2.87 \%$, for convergent camera sequences, and $1.52 \%$ for parallel camera sequences. Also a method to choose the geometrically transformed inter view reference pictures was developed, in order to reduce unnecessary overhead for unused reference pictures. By selecting and adding to the reference picture list, only the most useful pictures, all results improved, presenting bitrate savings up to $3.06 \%$ for convergent camera sequences, and $2 \%$ for parallel camera sequences.


Keywords: Disparity compensation, 3D video coding, Geometric transforms

## Resumo

Esta dissertação descreve o estudo e desenvolvimento de um conjunto de técnicas para melhorar a compensação de disparidade em algoritmos para compressão de video 3D. A compensação de disparidade é normalmente aplicada utilizando técnicas baseadas em block matching, sem ter em conta a distorção geométrica que afeta cada objeto na cena, a várias profundidades e disparidades. Desta forma, é proposto um esquema de codificação alternativo, que tem em conta a orientação e posição das câmaras, bem como a profundidade dos objetos na cena relativamente às câmaras. Desta forma mesmo em agregados de câmaras convergentes é possível melhorar a qualidade da compensação de disparidade.

Com o objetivo de melhorar a compensação de disparidade, são criadas novas imagens de referência geometricamente transformadas, que compensam a distorção geométrica dos objetos que se encontram nos níveis de profundidade mais relevantes da cena. Este método pode ser aplicado em qualquer codec do estado da arte como o H.264/AVC ou o HEVC com o objetivo de melhorar a precisão da compensação de disparidade entre vistas.

Os resultados experimentais, obtidos com extensão MV-HEVC, comprovam a eficiência do método proposto em vídeo stereo, apresentando poupanças de débito binário que vão até $2.87 \%$ para sequências com conjuntos de câmaras convergentes e $1.52 \%$ para sequências com conjuntos de câmaras paralelas. Foi também desenvolvido um método para escolher as imagens compensadas geometricamente para predição inter vista, de forma a reduzir o custo em débito binário acrescido por cada imagem de referência, mesmo que as imagens não sejam utilizadas. Selecionando apenas as imagens mais úteis para o processo de codificação, e colocado-as na lista de imagens de referência, todos os resultados anteriores melhoraram, apresentando poupanças de débito binário que vão até $3.06 \%$ para sequências com conjuntos de câmaras convergentes e $2 \%$ para sequências com conjuntos de câmaras paralelas.

Palavras-chave: Compensação de disparidade, Codificação de vídeo 3D, Transformações geométricas

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## List of Abbreviations

| 2D | Two Dimensions |
| ---: | :--- |
| 3D | Three Dimensions |
| AMP | Aymmetric Motion Prediction |
| ARP | Advanced Residual Prediction |
| AVC | Advanced Video Coding |
| BMA | Block Matching Algorithm |
| BMGT | Block Matching with Geometric Transforms |
| CABAC | Context Adaptive Binary Arithmetic Coding |
| CB | Coding Block |
| CTB | Coding Tree Block |
| CTU | Coding Tree Unit |
| CU | Coding Unit |
| DBF | Deblocking Filter |
| DCT | Discrete Cosine Transform |
| DLT | Depth Look-up Table |
| DMM | Depth Modelling Modes |
| DST | Discrete Sine Transform |
| DoF | Degrees of Freedom |
| FS | Full Search |
| GT | Geometric Transform |


| HD | High Definition |
| :---: | :---: |
| HEVC | High Efficiency Video Coding |
| HEXBS | Hexagonal-Based Search algorithm |
| HTE | Helmholtz Tradeoff Estimator |
| IEC | International Electrotechnical Commission |
| ISO | International Standards Organization |
| ITU-T | International Telecommunications Union - Telecommunications Standardization Sector |
| JCT-3V | Joint Collaborative Team on 3D video |
| JCT-VC | Joint Collaborative Team on Video Coding |
| KLT | Kanade-Lucas-Tomasi |
| MPEG | Moving Picture Experts Group |
| MSE | Mean Squared Error |
| NBDV | Neighbouring Block-Based Disparity Vector Derivation |
| OSA | Orthogonal Search Algorithm |
| PB | Prediction Block |
| POC | Picture Order Count |
| PSKIP | Parameter Skip |
| PSNR | Peak Signal-to-Noise Ratio |
| PU | Prediction Unit |
| QP | Quantization Parameter |
| RANSAC | Random Sample Consensus |
| RBC | Region Boundary Chain |
| RDO | Rate-Distortion Optimization |
| RD | Rate-Distortion |


| RMGT | Region Matching using Geometric Transforms |
| ---: | :--- |
| SAD | Sum of Absolute Differences |
| SAO | Sample Adaptive Offset |
| SDC | Simplified Depth Coding |
| SIFT | Scale-Invariant Feature Transform |
| SSD | Sum of Square Differences |
| SURF | Speeded-Up Robust Features |
| TB | Transform Block |
| TSS | Three-Step Search |
| TUC | Temporal Updated Centroids |
| TU | Transform Unit |
| VCEG | Video Coding Experts Group |
| VSO | View Synthesis Optimization |
| VSRS | View Synthesis Reference Software |
| WPP | Wavefront parallel processing |

## Chapter 1

## Introduction

### 1.1 Context and motivations

In recent years there has been a growing interest of the consumer market in 3D video services and applications, spanning from broadcasting to internet and gaming, enhancing the user experience towards immersive and more natural viewing environments. This interest was followed by a standardization effort, allowing the development of several techniques, to further improve the compression performance of the existing encoders. State-of-the-art video coding standards, like H.264/AVC [1] and the most recent H.265/HEVC [2], are being extended to support multiview and video-plus-depth formats.

Among the various techniques developed to exploit the redundancy between adjacent pictures, motion estimation plays an essential role, by eliminating the temporal redundancy. In multiview video formats there is an additional source of redundancy between views of a sequence. In order to eliminate this redundant information among views, captured by different cameras, disparity compensation can be performed.

Current video standards use an algorithm similar to motion estimation Block Matching Algorithm (BMA) to perform block matching between a pair of images, and use a vector to represent either motion or disparity. However, this algorithm assumes that all pixels pixels in a block have the same motion/disparity, and are accurately described by a translation.

In most disparity compensation scenarios these restrictions do not apply, particularly for convergent camera arrangements. In such cases, the use of more flexible disparity compensation schemes, using a higher degree of freedom (DoF) operation, may result in performance gains. This can be obtained through the use of geometric transformations (GT) where, depending on the available DoF, it is possible to describe not only translations, but also rotations, scaling and shear. In order to achieve a higher motion/disparity compensation accuracy, the compression scheme using block matching requires more in-
formation to describe the transformation associated with each block. When the block size is reduced, the amount of data, per pixel, required to represent the block transformations increases significantly. However, the newest video coding standard HEVC supports larger block sizes, up to $64 \times 64$ pixels. Therefore, compensating the disparity of larger blocks with a more accurate block matching algorithm may overcome the necessary extra amount of bits, in terms of RDO (Rate-Distortion Optimization) .

The proposed method divides each scene into regions, corresponding to objects with different disparities. This segmentation is applied on the base view depth map and considers the amount of pixels present at each depth level. Based on the 3D scene information and the distortion achieved by a matching technique, new reference pictures are generated using geometric transforms (GT). These GT reference pictures, represented by its own coefficients, are used in MV-HEVC encoding scheme to compress a pair of video sequences.

### 1.2 Objectives

This work initially presents a study on the state-of-the-art proposals on this topic, as well as, the HEVC standard and multiview extensions, namely MV-HEVC and 3D-HEVC. Afterwards the following topics were developed:

- Implementation of various types of geometric transforms;
- Study and development of segmentation methods;
- Development of various disparity compensation techniques, through the use of geometric transforms;
- Integration of the proposed techniques in a state-of-the-art video codec;
- Objective performance evaluation using the state-of-the-art video codec as a benchmark.

The proposed techniques integrated in the state-of-the-art video codec are expected to improve RD performance.

### 1.3 Dissertation structure

This dissertation is organized in six chapters. This first chapter addresses a overall description of this work and objectives. The second chapter describes an overview of the most relevant coding tools in 3D video coding, based on HEVC standard and 3D-HEVC
extensions. The third chapter includes the related state-of-the-art, with a detailed study on geometric transforms, and their application to compensate motion. The fourth chapter shows an evaluation of two types of approaches developed to compensate disparity. The fifth chapter presents the result of the integration of the proposed methods on MV-HEVC extension and experimental results. Finally, in chapter six some conclusions are drawn and some possible future work.

In Appendix A, contributions associated with this dissertation are presented.

## Chapter 2

## 3D Video Coding

State-of-the-art video coding standards, like H.264/AVC [1] and the most recent H.265/HEVC [2], are being extended to support multiview and video-plus-depth formats [3]. HEVC is the most recent joint video project of the ITU-T Video Coding Experts Group (VCEG) and the ISO/IEC Moving Picture Experts Group (MPEG) standardization organizations. This partnership is known by Joint Collaborative Team on Video Coding (JCT-VC) .

HEVC has been developed to address the increasing diversity of services that use HD (High Definition) video e.g. $1920 \times 1080$ pixels, and ultra HD video e.g. $3840 \times 2160$ pixels. Not only it is necessary to have a codec that is more efficient for storage, but also for streaming through the network. The amount of necessary bandwidth increases even more when dealing with stereo or multiview video. HEVC development is also focused on parallel processing architectures due to the increasing availability of multi-core solutions for processing.

The main concept of the codec architecture is the same as H.264/AVC. Each picture is split into blocks. In order to exploit spatial and temporal redundancy, prediction algorithms are applied. Depending on the prediction scheme, the picture to be encoded can be either I, P or B. If the picture is I, intra prediction is applied, where only spatial redundancy is exploited. If the picture is either P or B , temporal prediction can be performed, which is usually the most common. The residue, i.e. the difference between the predicted block and the original block, is transformed using a spatial transform. The resulting coefficients are scaled and quantized. This information is entropy coded and transmitted with the prediction information, like the selected mode, or the motion vectors.

The encoder also includes an decoder such that the decoding process is replicated in the encoder side. This allows the decoded pictures to be used as reference pictures for the future frames. The decoding loop includes the reconstruction of the approximated residue
using the inverse quantization and transform. The residue is added to the prediction generating the decoded block. In order to reduce artifacts, the decoded picture may be filtered in the decoding loop process.

What differentiates HEVC from other extensions is the type and number of input signals. HEVC standard only accepts one input video sequence. MV-HEVC[4], the multiview extension, is used to encode several videos exploiting inter-view redundancy, while still maintaining backwards compatibility with monoscopic video coded by HEVC. This is done by adding pictures from one view to the reference picture list of another view. Since the various cameras capture the same scene a high percentage of the picture can be predicted using another camera perspective. The Joint Collaborative Team on 3D video (JCT-3V), which is the team that is working on the 3D extensions for HEVC, is also developing 3D-HEVC[5]. This 3D video group has been created to study advanced tools for coding multiple views. Just like MV-HEVC, inter-view prediction is performed, but also using depth maps, that are coded and transmitted. This video-plus-depth format uses coding tools specific to depth maps where sharp edges and large homogeneous areas are predominant. The main advantage of the this format, is the high number of views that can be artificially created on the receiver, due to the availability of the depth maps.

MV-HEVC does not have any exclusive coding tools, since inter-view prediction is also used by 3D-HEVC. Therefore the two following sections will address the common tools that are used in all extensions and the most relevant 3D-HEVC tools.

### 2.1 Common codec tools

Regardless of the extension, both MV-HEVC and 3D-HEVC are based on HEVC, in order to maintain compatibility [3]. At least the first video sequence encoded by one of these extensions uses HEVC. Either way the common tools are the tools used by HEVC. Therefore, the common codec tools are further explained in this section. Figure 2.1 shows the block diagram of the HEVC encoder.

The input video signal is split into CTUs (Coding Tree Unit) which are $N \times N$ quadtree elements. CTUs are composed by CTBs (Coding Tree Block), one for the luminance and two for the chroma components. The possible luminance CTB sizes are $64 \times 64,32 \times 32$ and $16 \times 16$. The CTUs are divided into CUs (Coding Unit), which contain luminance CB (Coding Block) and two chroma CBs. CUs can have PUs (Prediction Unit) and TUs (Transform Unit). A PU is a unit that can have a size between $4 \times 4$ and $64 \times 64$, where either intra or inter prediction is performed at a CU level. TU size depends on the PU size and can be between $32 \times 32$ and $4 \times 4$. Each CU can have more than one PU and it is always square shaped of size between $8 \times 8$ and the size of the CTU. A CB with


Figure 2.1: HEVC video encoder and decoder on the gray blocks [2].
$M \times M$ pixels can have partitioned PBs (Prediction Block), which are the luminance and chroma components of PU, as $2 N \times 2 N, N \times N, N \times 2 N$ and $2 N \times N$, where $M=2 N$. A PB can also be partitioned asymmetrically using AMP (Asymmetric Motion Prediction) using sizes: $2 N \times n U, 2 N \times n D, n L \times 2 N$ and $n R \times 2 N . U, D, L$ and $R$ correspond to Up, Down, Left and Right. For example, if $M=16$, the $2 N \times n U$ the resulting partition will be one $16 \times 4$ block on top and a $16 \times 12$ on the bottom, because the division is on horizontal and on the upper part of the block.

Table 2.1 shows all possible sizes for luma CTB, CB, PB and TB. Also the table is hierarchy organized. For example, for $16 \times 16 \mathrm{CTB}$ size, the only possible sizes for $\mathrm{CB}, \mathrm{PB}$ and TB are the ones on the same line or below in the table. Therefore the only possible CB sizes are $16 \times 16$ and $8 \times 8$ and TB sizes are between $16 \times 16$ and $4 \times 4$.

The spatial redundancy of the picture is exploited by using decoded boundary samples of adjacent blocks as reference data for intra prediction. The intra predictions modes include: DC mode, planar mode and 33 angular modes. The DC mode creates a flat surface that is the mean of the boundary samples. The planar mode is used to predict gradient surfaces of the picture. The 33 angular modes are only available for PB sizes of $32 \times 32,16 \times 16$ and $8 \times 8$. When the PB is $64 \times 64$ only 4 angular modes are available and if the PB is $4 \times 4$ only 16 are available. Figure 2.2 shows the intra prediction angular modes.

The inter prediction techniques are used to exploit temporal redundancy. Using de-

| CTB | CB | PB | TB |
| :---: | :---: | :---: | :---: |
| $64 \times 64$ | $64 \times 64$ | $64 \times 64$ $64 \times 32$ $32 \times 64$ $64 \times 16$ and $64 \times 48$ $16 \times 64$ and $48 \times 64$ |  |
| $32 \times 32$ | $32 \times 32$ | $32 \times 32$ $32 \times 16$ $16 \times 32$ $32 \times 8$ and $32 \times 24$ $8 \times 32$ and $24 \times 32$ | $32 \times 32$ |
| $16 \times 16$ | $16 \times 16$ | $16 \times 16$ $16 \times 8$ $8 \times 16$ $16 \times 4$ and $16 \times 12$ $4 \times 16$ and $12 \times 16$ | $16 \times 16$ |
|  | $8 \times 8$ | $\begin{aligned} & 8 \times 8 \\ & 8 \times 4 \\ & 4 \times 8 \end{aligned}$ | $8 \times 8$ |
|  |  | $4 \times 4$ | $4 \times 4$ |

Table 2.1: Possible CTB, CB, PB and TB luminance sizes.


Figure 2.2: Intra prediction angular modes [6].
coded pictures as references that where encoded previously, the encoder tests three different inter prediction modes: Skip, Merge and Motion Estimation. The Skip mode is used when the PB of one of the decoded pictures is equal to the PB in the same position of the current picture. The Motion Estimation mode uses a matching algorithm to identify similar PBs on previously encoded pictures for the PB of the current picture. The motion is therefore identified explicitly by a motion vector that has one quarter pixel precision. HEVC uses an eight-tap filter to interpolate the half-sample positions and then a seven-tap filter for the quarter-sample positions.

The motion vector can be generated relatively to one reference picture or two using bi-prediction. In bi-prediction two vectors are generated relative to two different reference pictures where the prediction block generated by both is combined as a simple average or an explicit weighted average. The Merge mode includes candidate vectors that were used on previously encoded PBs. Five spatial candidates are used, located on the upper, left, upper left, upper right and bottom left positions relative to the PB that is being encoded. Also one temporal candidate is used on the bottom right position relative to the PB. The merge candidate index is transmitted as well as the reference picture used.

After applying the prediction modes to the PB , the residue block is generated. This residue is spatially transformed using the DCT (Discrete Cosine Transform). The DCT block sizes vary from $32 \times 32$ to $4 \times 4$. Moreover, an alternative transform is used for $4 \times 4$ TB, the DST (Discrete Sine Transform). The DST tends to provide better results than the DCT when the residue amplitude is higher on the pixels that are furthest way from the boundary samples used for prediction. The transform coefficients are quantized using a quantization parameter (QP), as in H.264/AVC.

Entropy coding is used to encode all the quantized transform coefficients, intra prediction data, motion data and filter control data. The CABAC (Context Adaptive Binary Arithmetic Coding) core algorithm remains unchanged from H.264/AVC however improvements have been made in terms of computational complexity and memory requirements. The output is the HEVC bitstream.

The HEVC standard only specifies the bitstream structure and syntax, as has been the case for all past ITU-T and ISO/IEC video coding standards. This way the standard provides maximum flexibility to optimize implementations on the encoder side while still being standard compatible.

Two filters are applied by the decoder to the reconstructed samples before generating the reference picture list. The Deblocking Filter (DBF) is applied to all samples of adjacent PU or TU boundary using three variable strengths that are chosen by HEVC depending on the content. The only areas of the image where DBF is not applied are the boundaries of the picture or the slice or tile. The second filter is the Sample Adaptive

Offset (SAO), that is used after DBF in order to further improve the signal representation in smooth areas and around edges. The application of SAO consists in adding an offset value to the decoded samples that is based on a look-up table transmitted by HEVC encoder.

As stated before one of the key implementation features of HEVC is the possibility to use parallel processing. For this purpose two features have been added where the picture being encoded is divided into either tiles or rows of CTUs. Each region is encoded or decoded using a different CPU thread. The Tiles are similar to Slices although it is not intended to increase the error resilience and therefore some header information for each tile is shared. The advantage of this method is the fact that each tile is independent from each other, so it is not necessary to synchronize threads that are encoding or decoding each tile. The alternative to tiles is to use WPP (Wavefront parallel processing) where each thread is assigned to process each row of CTUs. Each row has to be processed with 2 CTUs distance from each other, so that when a second row of CTUs is being processed the upper CTUs can be available for prediction. The advantage of WPP is the fact that the performance is not affected as for the Tiles feature and also avoids visual artefacts on the boundaries of the tile. However it is necessary to maintain synchronization among all the threads in order to maintain the 2 CTU distance.

### 2.2 3D-HEVC tools

3D-HEVC is the extension created to use advanced coding tools specifically designed for the video-plus-depth formats. The higher efficiency compared with HEVC and MVHEVC comes from two types of tools: improved inter-view prediction and specific depth map coding tools [3]. As mentioned before, in order to maintain backwards compatibility with the single view video encoded by HEVC, the first view, or the base view is encoded using standard HEVC. Only the additional views or depth maps will use the 3D-HEVC exclusive tools.

3D-HEVC performs inter-view motion prediction by adding additional candidates to the list of merge mode. Merge mode includes six candidates as HEVC, and two that are generated using Neighbouring Block-Based Disparity Vector Derivation(NBDV) [7].

NBDV has its own various spatial and temporal candidates near the current PU. These candidates are checked in order to find a disparity vector. If a disparity vector is found the process stops saving the vector, the chosen candidate, and the reference picture index. If no disparity vector is found NBDV returns a null disparity vector.

As shown in Figure 2.3, the motion vector associated with the block found by NBDV is the first candidate. Moreover, this first candidate is called the inter-view candidate.


Figure 2.3: Inferred motion vector by NBDV [3].

The disparity vector derived by NBDV is used as the second candidate. This way, as in merge mode, if any candidate is chosen only one index is transmitted. Also if motion or disparity estimation is performed the vector is predicted using one of the candidates. The motion that occured in the base-view is correlated with the motion occuring in the non-base view. Also the disparity vector used in the previous PU or on a neighbouring PU is also probably very similar to the current PU.

NBDV is also used to perform inter-view residual prediction. As shown in Figure 2.4, NBDV identifies the $B c$ block as the reference block. This block was predicted using a motion vector $V_{D}$. By calculating the difference between the reconstructed Bc and Br of the base view, a residue block is generated. This residue block is used for prediction when the same $V_{D}$ vector is applied for motion compensation in the non-base view. Moreover, when this Advanced Residual Prediction (ARP) [8] technique is applied the prediction of the residue can be weighted by 0.5 or 1 .

When performing disparity compensation using an inter-view reference picture, there may be the need to adjust the illumination conditions [9] of one view relative to another, in order to improve the prediction efficiency. After the prediction is applied using a disparity vector for the current PU, the neighbouring samples, namely the upper row and left column of pixels relative to the reference block are used to calculate a linear model. This linear model is characterized by a scaling factor $a$, that has to be close to 1 , and an offset $b$, where both values are calculated using least-squares. The linear model is applied to each value improving the prediction.

In terms of specific depth coding tools, first it is necessary to point the differences between a depth map and texture. Depth maps are characterized by large homogeneous areas and sharp edges. The preservation of edges is very important because it directly affects the quality of synthesized views using reconstructed depth maps. Therefore some


Figure 2.4: Advanced residual prediction example [3].
tools used for texture are not used for depth map coding like DBF and SAO. Also motion compensation uses integer precision in order to disable interpolation filters.

A set of tools was created to divide the depth blocks into non-rectangular partitions. Depth Modelling Modes (DMM) [10] and Region Boundary Chain (RBC) [11] are used to divide the current PU into two zone with a DC value each. This DC value is predicted using neighbouring pixels. DMM has two modes, where the partition occur in a wedgeshaped pattern or contour pattern. The wedge-shaped pattern consists in dividing the PU into two parts using a straight line. The contour pattern uses the co-located texture PU contour to divide the current depth PU. The RBC uses series of connected chains within eight possible angles starting at $0,45,-45,90,-90$, and so on.

Simplified depth coding (SDC) [12] is used if DMM and RBC modes are used. SDC adds one partition per PU to model smooth regions. Transform and quantization is skipped when these modes are used, i.e. the samples of residual block are encoded. When encoding residual blocks directly, in order to reduce the dynamic range of values a Depth Look-up Table (DLT) is used, where all only used depth values appear. DLT is useful because in some cases not all the dynamic range is used, some depth maps have an accuracy lower than 8 bits.

Considering the correlation between texture and depth motion information, the motion vectors can be inherited from the texture to the depth map. Since texture is encoded first, the decoded motion vector used by a co-located PU is added as an extra merge candidate for the current depth PU. When this vector is chosen to be reused by the current depth PU the precision is adjusted from quarter pixel precision to integer precision, since depth motion compensation does not use interpolation filter.

3D-HEVC includes View Synthesis Optimization (VSO)[10], which is tool that is able to control and optimize the depth map encoding process. The encoding process of depth maps is very relevant for the final quality of synthesised views. Therefore a new distortion metric is used to encode the depth maps, where instead of controlling the distortion of the depth map, the distortion of the synthesised view is controlled. This control can be performed by rendering the actual synthesized view in the encoding process and calculating the distortion, or by estimating the result distortion of the synthesized view.

## Chapter 3

## Related State-of-the-art

The main objective of this chapter is to present a review of the state-of-the-art. This chapter is divided into two sections: the first section reviews the most relevant geometric transforms in the context of disparity compensation; in the second section, the most relevant applications of geometric transforms on motion compensation are addressed.

### 3.1 Geometric transforms

The main concept of geometric transforms is the mapping of one coordinate system into another. This process uses a function that contains the spatial correspondence between both coordinate systems. This function can be manipulated in order to adjust the shape of a quadrilateral in relation to another quadrilateral. An example of a forward and inverse mapping can be seen in Figure 3.1.

In Figure 3.1 two coordinate systems are presented, $[x, y]$ and $[u, v]$, showing the common Cartesian coordinates used in Euclidean geometry. The forward mapping function,


Figure 3.1: Example of forward and inverse mapping between two distinct coordinate system
that spatially relates both coordinate systems, can be described as:

$$
\begin{equation*}
[x, y]=[X(u, v), Y(u, v)] \tag{3.1}
\end{equation*}
$$

The inverse operation is:

$$
\begin{equation*}
[u, v]=[U(x, y), V(x, y)] \tag{3.2}
\end{equation*}
$$

In the forward mapping each point in the quadrilateral is mapped onto a different position given by $X$ and $Y$ mapping functions [13]. In the inverse mapping the $U$ and $V$ functions can be used, so that all points in the quadrilateral are mapped onto the original shape.

Geometric transforms can be characterized by a set of coefficients that are used by the mapping function. The number of coefficients influences the number of points that can be independently matched between two different coordinate systems, i.e the number of non-collinear points. In the case of 2D planes, each non-collinear point of correspondence needs 2 DoF (Degrees of Freedom). This means that in order to freely create a triangle one needs 6 DoF and 8 DoF for a quadrilateral. The number of DoF is directly related to the number of different shapes that is possible to create. However, the higher the number of DoF the higher the number of coefficients, resulting in a more complex transform. In the context of this dissertation, only simple geometric transforms will be considered i.e. geometric transforms with a small number of coefficients. The geometric transforms that will be considered are:

- Projective;
- Bilinear

These geometric transforms are the most commonly used for the purpose of this dissertation, that is disparity compensation $[14,15,16,17]$.

Although both geometric transforms have 8 DoF , the main difference lays on the distance between points along certain lines. If these points are equispaced, that property will be preserved only in the case of the bilinear transform [16].

### 3.1.1 Projective transform

In order to define these geometric transforms an homogeneous coordinate system is used. This coordinate system is used in projective geometry[18]. An Euclidean coordinate, like $[x, y]$, is represented by an homogeneous vector $[u, v, h]$. The correspondence between the two coordinate systems is given by:

$$
\begin{equation*}
[u, v, h]=[x h, y h, h] \tag{3.3}
\end{equation*}
$$

Although the third coordinate $h$ can be any value except zero, in this context it's simplified to $h=1$. Because an image can be defined with two dimensions only. The plane $h=1$ is going to be intersected by the homogeneous vector. The intersection of the various homogeneous vectors will result on the projection of the image on that plane.

The conversion between coordinate systems is made through a 3 x 3 transform matrix:

$$
\begin{equation*}
[x, y, 1]=[u, v, 1] H \tag{3.4}
\end{equation*}
$$

where:

$$
H=\left[\begin{array}{lll}
h_{11} & h_{12} & h_{13}  \tag{3.5}\\
h_{21} & h_{22} & h_{23} \\
h_{31} & h_{32} & h_{33}
\end{array}\right]
$$

This matrix defines how the conversion between two coordinate systems is made. When transforming a quadrilateral into another quadrilateral, the various coefficients in this matrix will have a certain role on that transformation. Taking this into, account the $H$ matrix can been divided into four parts:

$$
H=\left[\begin{array}{ll}
H_{11} & H_{12}  \tag{3.6}\\
H_{21} & h_{33}
\end{array}\right]
$$

where:

$$
H_{11}=\left[\begin{array}{ll}
h_{11} & h_{12}  \tag{3.7}\\
h_{21} & h_{22}
\end{array}\right], H_{12}=\left[\begin{array}{l}
h_{13} \\
h_{23}
\end{array}\right], H_{21}=\left[\begin{array}{ll}
h_{31} & h_{32}
\end{array}\right]
$$

The sub-matrix $H_{11}$ is responsible for a linear transform capable of rotations, scaling and shear. Moreover, the vector $H_{12}$ is used to generate perspective changes, while the vector $H_{21}$ specifies a translation of the x and y coordinates, respectively. Finally, the $h_{33}$ coefficient is a scaling factor of the plane $h$. Since the coefficients in the sub-matrix $H_{12}$ can be used for scaling purposes, the $h_{33}$ coefficient becomes redundant. Therefore, it is normally simplified to $h_{33}=1$.

Projective transforms include some simpler transformations, which rely only on a subset of the described coefficients. Those particular cases are Euclidean, Similarity and Affine transform.

## Euclidean transform

An Euclidean transform is a composition of a translation $(T)$ and a rotation $(R)$. This transform is represented as:

$$
[x, y, 1]=[u, v, 1]\left[\begin{array}{ll}
R & 0  \tag{3.8}\\
T & 1
\end{array}\right]=[u, v, 1]\left[\begin{array}{ccc}
\cos (\alpha) & \sin (\alpha) & 0 \\
-\sin (\alpha) & \cos (\alpha) & 0 \\
t_{x} & t_{y} & 1
\end{array}\right] .
$$

This operation is isometric because it preserves length between two points, angle between two lines and area. Figure 3.2 shows an example of an Euclidean transform applied to a square. The transform $E$ allows 3 DoF that are directly related to $t_{x}, t_{y}$, and $\alpha$.


Figure 3.2: Example of an Euclidean transform

The mapping functions for this transform are:

$$
\begin{align*}
& x=u \cos (\alpha)-v \sin (\alpha)+t_{x},  \tag{3.9}\\
& y=u \sin (\alpha)+v \cos (\alpha)+t_{y} . \tag{3.10}
\end{align*}
$$

## Similarity transform

A Similarity transform is a composition of a translation $(T)$, a rotation $(R)$ and scale $(s)$. The scale is isotropic because it's equal in both axis, and therefore preserves the shape. This transform can be represented as:

$$
[x, y, 1]=[u, v, 1]\left[\begin{array}{cc}
s R & 0  \tag{3.11}\\
T & 1
\end{array}\right]=[u, v, 1]\left[\begin{array}{ccc}
s \cos (\alpha) & s \sin (\alpha) & 0 \\
-s \sin (\alpha) & s \cos (\alpha) & 0 \\
t_{x} & t_{y} & 1
\end{array}\right] .
$$

This transform allows 4 DoF since it has the same properties of the Euclidean transform and additionally performs scale. Figure 3.3 shows an example of a Similarity transform applied to a square. Transform $S$ allows 4 DoF and is directly related to $t_{x}, t_{y}, \alpha$ and $s$.

Note that $s$ is a scaling ratio between the square before the transformation and after.


Figure 3.3: Example of a Similarity transform

The mapping functions for this transform can be described as:

$$
\begin{align*}
& x=s[u \cos (\alpha)-v \sin (\alpha)]+t_{x},  \tag{3.12}\\
& y=s[u \sin (\alpha)+v \cos (\alpha)]+t_{y} . \tag{3.13}
\end{align*}
$$

## Affine transform

The affine transform is characterized by a linear transformation $(A)$ followed by a translation $(T)$ and it's represented in the following form:

$$
[x, y, 1]=[u, v, 1]\left[\begin{array}{cc}
A & 0  \tag{3.14}\\
T & 1
\end{array}\right]=[u, v, 1]\left[\begin{array}{ccc}
a_{11} & a_{12} & 0 \\
a_{21} & a_{22} & 0 \\
t_{x} & t_{y} & 1
\end{array}\right]
$$

The main difference to the previous transforms is that the $A$ sub-matrix is not restricted by only one angle or scale factor. $A$ is a composition of rotations and non-isotropic scalings (the scale factors are not equal in both axis). The $A$ sub-matrix can be decomposed as:

$$
\begin{equation*}
A=R(\alpha) R(-\phi) D R(\phi) \tag{3.15}
\end{equation*}
$$

where,

$$
D=\left[\begin{array}{cc}
\lambda_{1} & 0  \tag{3.16}\\
0 & \lambda_{2}
\end{array}\right]
$$

The angle $\alpha$ is responsible for the same rotation as before, however the angle $\phi$ specifies the scale direction and $\lambda_{1}$ and $\lambda 2$ values are the scaling values for both axis. Notice that if $\phi=0$ and $\lambda_{1}=\lambda 2=s$, then $A=R(\alpha) s$, which represents the similarity transform without the translation coefficients.

By separating $x$ and $y$, the mapping functions became:

$$
\begin{align*}
& x=a_{11} u+a_{21} v+t_{x},  \tag{3.17}\\
& y=a_{12} u+a_{22} v+t_{y} . \tag{3.18}
\end{align*}
$$

The Affine transform achieves 6 DoF, allowing the transformation of a triangle into another triangle, because 6 DoF allow the correspondence of 3 non-collinear points in two different coordinate systems. Considering that those points are represented by $\left[x_{k}, y_{k}\right]$, where $k=0,1$ and 2, Equation 3.19 is used to determine the 6 coefficients that describe the mapping between the 3 corresponding points:

$$
\left[\begin{array}{lll}
x_{0} & y_{0} & 1  \tag{3.19}\\
x_{1} & y_{1} & 1 \\
x_{2} & y_{2} & 1
\end{array}\right]=\left[\begin{array}{lll}
u_{0} & v_{0} & 1 \\
u_{1} & v_{1} & 1 \\
u_{2} & v_{2} & 1
\end{array}\right]\left[\begin{array}{lll}
a_{11} & a_{21} & 0 \\
a_{21} & a_{22} & 0 \\
t_{x} & t_{y} & 1
\end{array}\right] .
$$

Nevertheless, 6 DoF are not enough to transform parallel lines into non-parallel. This transformation only allows to transform a square onto a parallelogram, not being able to perform more complex transformations on quadrilaterals. Figure 3.4 shows an example of the described transformation.


Figure 3.4: Example of an Affine transform

## Projective transform

The projective transform adds the missing parameters from the original $H$ matrix $\left(H_{12}\right)$ to the Affine transform:

$$
[x, y, 1]=[u, v, 1]\left[\begin{array}{lll}
h_{11} & h_{12} & h_{13}  \tag{3.20}\\
h_{21} & h_{22} & h_{23} \\
h_{31} & h_{32} & h_{33}
\end{array}\right]
$$

changing the mapping functions to (note that $h_{33}=1$ ):

$$
\begin{equation*}
x=u h_{11}+v h_{21}+h_{31}-x u h_{13}-x v h_{23} \tag{3.21}
\end{equation*}
$$

$$
\begin{equation*}
y=u h_{12}+v h_{22}+h_{32}-x u h_{13}-x v h_{23} \tag{3.22}
\end{equation*}
$$

By using 8 DoF, the projective transform is able to transform one quadrilateral into another quadrilateral. The quadrilateral transform is defined by 4 correspondent points $\left[x_{k}, y_{k}\right]$ where $k=0,1,2$ and 3 (one for each corner). In order to find the coefficients for that correspondence the system described in 3.23 must be solved:

$$
\left[\begin{array}{l}
x_{0}  \tag{3.23}\\
x_{1} \\
x_{2} \\
x_{3} \\
y_{0} \\
y_{1} \\
y_{2} \\
y_{3}
\end{array}\right]=\left[\begin{array}{cccccccc}
u_{0} & v_{0} & 1 & 0 & 0 & 0 & -u_{0} x_{0} & -v_{0} x_{0} \\
u_{1} & v_{1} & 1 & 0 & 0 & 0 & -u_{1} x_{1} & -v_{1} x_{1} \\
u_{2} & v_{2} & 1 & 0 & 0 & 0 & -u_{2} x_{2} & -v_{2} x_{2} \\
u_{3} & v_{3} & 1 & 0 & 0 & 0 & -u_{3} x_{3} & -v_{3} x_{3} \\
0 & 0 & 0 & u_{0} & v_{0} & 1 & -u_{0} y_{0} & -v_{0} y_{0} \\
0 & 0 & 0 & u_{1} & v_{1} & 1 & -u_{1} y_{1} & -v_{1} y_{1} \\
0 & 0 & 0 & u_{2} & v_{2} & 1 & -u_{2} y_{2} & -v_{2} y_{2} \\
0 & 0 & 0 & u_{3} & v_{3} & 1 & -u_{3} y_{3} & -v_{3} y_{3}
\end{array}\right]\left[\begin{array}{l}
h_{11} \\
h_{21} \\
h_{31} \\
h_{12} \\
h_{22} \\
h_{32} \\
h_{13} \\
h_{23}
\end{array}\right] .
$$

The equation system 3.23 can be rearranged as:

$$
\begin{align*}
& h_{11}=\frac{x_{1}-h_{31}}{u_{1}}+x_{1} h_{13}-\frac{v_{1}\left(h_{21}-x_{1} h_{23}\right)}{u_{1}} \\
& h_{12}=\frac{y_{1}-h_{23}}{u_{1}}+y_{1} h_{13}-\frac{v_{1}\left(h_{22}-x_{1} h_{23}\right)}{u_{1}} \\
& h_{13}=\frac{v_{2} h_{21}+u_{2} h_{11}+x_{0}-x_{2}-v_{2} h_{23} x_{2}}{u_{2} x_{2}} \\
& h_{21}=\frac{x_{3}-h_{31}}{v_{3}}+x_{3} h_{23}-\frac{u_{3}\left(h_{11}-x_{3} h_{13}\right)}{v_{3}}  \tag{3.24}\\
& h_{22}=\frac{y_{3}-h_{32}}{v_{3}}+y_{3} h_{23}-\frac{u_{3}\left(h_{12}-y_{3} h_{13}\right)}{v_{3}} \\
& h_{23}=\frac{v_{2} h_{22}+v_{2} h_{12}+y_{0}-y_{2}-u_{2} h_{13} y_{2}}{v_{2} y_{2}} \\
& h_{31}=-u_{0} h_{11}-v_{0} h_{21}+x_{0}+u_{0} x_{0} h_{13}+v_{0} x_{0} h_{23} \\
& h_{32}=-u_{0} h_{12}-v_{0} h_{22}+y_{0}+u_{0} y_{0} h_{13}+v_{0} y_{0} h_{23}
\end{align*}
$$

Equations 3.24 allow the calculations of the transform coefficients given the $\left[u_{k}, v_{k}\right]$ for the initial coordinates and $\left[x_{k}, y_{k}\right]$ for the intended coordinates after the transformation, the $H$ matrix is known.

If we consider the common case where a $m \times n$ rectangle is transformed into a quadrilateral, represented in Figure 3.5.


Figure 3.5: Example of a Projective transform on a $m \times n$ image

The system of equations results in:

$$
\begin{align*}
& h_{11}=\frac{x_{1}-x_{0}}{m-1}+x_{1} h_{13} \\
& h_{12}=\frac{y_{1}-y_{0}}{m-1}+y_{1} h_{13} \\
& h_{13}=\frac{(n-1) h_{21}+(m-1) h_{11}+x_{0}-x_{2}-(n-1) h_{23} x_{2}}{(m-1) x_{2}} \\
& h_{21}=\frac{x_{3}-x_{0}}{n-1}+x_{3} h_{23}  \tag{3.25}\\
& h_{22}=\frac{y_{3}-y_{0}}{n-1}+y_{3} h_{23} \\
& h_{23}=\frac{(n-1) h_{22}+(n-1) h_{12}+y_{0}-y_{2}-(m-1) h_{13} y_{2}}{(n-1) y_{2}} \\
& h_{31}=x_{0} \\
& h_{32}=y_{0}
\end{align*}
$$

At this point only $h_{13}$ and $h_{23}$ need to be determine in order to find all the remaining coefficients. In order to determine these two coefficients first the following terms have been defined:

$$
\begin{align*}
\Delta x_{1} & =x_{1}-x_{2} \\
\Delta x_{2} & =x_{3}-x_{2} \\
\Delta x_{3} & =x_{2}-x_{3}+x_{0}-x_{1}  \tag{3.26}\\
\Delta y_{1} & =y_{1}-y_{2} \\
\Delta y_{2} & =y_{3}-y_{2} \\
\Delta y_{3} & =y_{2}-y_{3}+y_{0}-y_{1}
\end{align*}
$$

The coefficients $h_{13}$ and $h_{23}$ can be determined by solving Equations 3.27 and 3.28:

$$
\begin{align*}
& h_{13}=\frac{1}{m-1}\left|\begin{array}{ll}
\Delta x_{3} & \Delta x_{2} \\
\Delta y_{3} & \Delta y_{2}
\end{array}\right|  \tag{3.27}\\
& \left|\begin{array}{ll}
\Delta x_{1} & \Delta x_{2} \\
\Delta y_{1} & \Delta y_{2}
\end{array}\right|  \tag{3.28}\\
& h_{23}=\frac{1}{n-1}\left|\begin{array}{ll}
\Delta y_{3} & \Delta y_{1} \\
\Delta x_{3} & \Delta x_{1}
\end{array}\right| \\
& \left|\begin{array}{ll}
\Delta y_{2} & \Delta y_{1} \\
\Delta x_{2} & \Delta x_{1}
\end{array}\right|
\end{align*}
$$

After determining the coefficients in 3.27 and 3.28 those values can be substituted in the other equations, finding the complete projective matrix. Notice that, this example is valid for both images and blocks, because in the case of square blocks $m=n$. Also, if $\Delta x_{3}=0$ and $\Delta y_{3}=0$, then $H_{12}=0$ and the resulting transform is Affine.

The case of square/rectangle-to-quadrilateral transform is important since it corresponds to the problem that is going to be exploited in the context of this dissertation due to the fact that both block and images are squares or rectangles.

### 3.1.2 Bilinear transform

The bilinear transform allows quadrilateral to non-planar quadrilateral transforms. Horizontal, vertical lines and points along these directions are preserved. The bilinear mapping functions are described as follows:

$$
[x, y]=[u v, u, v, 1]\left[\begin{array}{ll}
a_{0} & b_{0}  \tag{3.29}\\
a_{1} & b_{1} \\
a_{2} & b_{2} \\
a_{3} & b_{3}
\end{array}\right] .
$$

Performing the matrix multiplication:

$$
\begin{align*}
& x=a_{0}+a_{1} u+a_{2} v+a_{3} u v,  \tag{3.30}\\
& y=b_{0}+b_{1} u+b_{2} v+b_{3} u v . \tag{3.31}
\end{align*}
$$

In order to find the coefficients of two correspondent quadrilaterals from different coordinate systems 4 points are needed. These 4 points are related by using Equation 3.32:

$$
\left[\begin{array}{ll}
x_{0} & y_{0}  \tag{3.32}\\
x_{1} & y_{1} \\
x_{2} & y_{2} \\
x_{3} & y_{3}
\end{array}\right]=\left[\begin{array}{llll}
1 & u_{0} & v_{0} & u_{0} v_{0} \\
1 & u_{1} & v_{1} & u_{1} v_{1} \\
1 & u_{2} & v_{2} & u_{2} v_{2} \\
1 & u_{3} & v_{3} & u_{3} v_{3}
\end{array}\right]\left[\begin{array}{ll}
a_{3} & b_{3} \\
a_{2} & b_{2} \\
a_{1} & b_{1} \\
a_{0} & b_{0}
\end{array}\right] .
$$

Although the bilinear transform has the same number of DoF, the number of calculations needed to find the coefficients is smaller, compared to the Projective transform. As for the Projective transform, for an $m \times n$ (Figure 3.5) rectangle the coordinates of the corners may be substituted:

$$
\begin{align*}
& x_{0}=a_{0} \\
& x_{1}=x_{0}+(m-1) a_{1} \\
& x_{2}=x_{0}+(m-1) a_{1}+(n-1) a_{2}+(m-1)(n-1) a_{3} \\
& x_{3}=x_{0}+(n-1) a_{2}  \tag{3.33}\\
& y_{0}=b_{0} \\
& y_{1}=y_{0}+(m-1) b_{1} \\
& y_{2}=y_{0}+(m-1) b_{1}+(n-1) b_{2}+(m-1)(n-1) b_{3} \\
& y_{3}=y_{0}+(n-1) b_{2}
\end{align*}
$$

Rearranging the system of equations the transform coefficients may be obtained:

$$
\begin{align*}
a_{0} & =x_{0} \\
a_{1} & =\frac{x_{1}-x_{0}}{m-1} \\
a_{2} & =\frac{x_{3}-x_{0}}{n-1} \\
a_{3} & =\frac{x_{2}-x_{3}-x_{1}+x_{0}}{(m-1)(n-1)}  \tag{3.34}\\
b_{0} & =y_{0} \\
b_{1} & =\frac{y_{1}-y_{0}}{m-1} \\
b_{2} & =\frac{y_{3}-y_{0}}{n-1} \\
b_{3} & =\frac{y_{2}-y_{3}-y_{1}+y_{0}}{(m-1)(n-1)}
\end{align*}
$$

In the case of bilinear transform if $a_{3}=0$ and $b_{3}=0$, the resulting quadrilateral will be a parallelogram.

### 3.2 Applications of geometric transforms on motion and disparity compensation

Geometric transforms have been applied for both disparity and motion compensation. Although disparity and motion are two distinct types of information in multiview video coding, similar methods can be used to compensate both disparity and motion. The only difference is on the reference images used by the encoder. In the case of motion compensation reference images belong to the past or future of the video sequence in relation to the current frame. For disparity compensation, reference images belong to another view, either on the right or left, of the current frame. Hereupon the discussed proposals that are more relevant to this dissertation can be either about motion or disparity compensation.

When dealing with geometric transforms, the approaches may vary in terms of:

- Type of transform;
- Coefficient estimation;
- The area where the transformation is applied;
- Coefficients transmission.

Regardless of these properties the application of these techniques on video coding standards has been done at two levels: block-level and picture-level. At the block-level, the geometric transform is applied on each encoded block, using RDO (Rate-Distortion Optimization) criteria, and the coefficients need to be transmitted for each block. At a picture-level, prior encoded frames are analysed and compared with pictures that are being encoded. Geometrically transformed pictures are generated based on its similarity to the picture, or to some regions of the picture that is being encoded.

### 3.2.1 Block-level approaches

## Extending HEVC by an affine motion model

In previous research, Narroschke et al. [19] demonstrated that when using a motion compensated prediction based on an Affine model (6 DoF) the coding efficiency is improved. The affine model was integrated in HEVC as another motion compensated prediction technique. For each block, either the standard translation model is used or the affine model. The model is selected through a minimization of the Lagrangian cost, based on the required data the rate and sum of absolute values of the prediction error. The selected model is transmitted as additional information. The algorithm is more thoroughly explained through the following steps:

1. The translational model is applied by HEVC;
2. The affine parameters are estimated by a minimization of the squared prediction error $\left|E^{2}\right|$ :

$$
\begin{equation*}
e\left(x_{i}, y_{j}\right) \approx \phi\left(x_{i}, y_{j}\right)-h\left(x_{i}, y_{j}\right) A \tag{3.35}
\end{equation*}
$$

where $\phi$ represents the difference between the pixel value of the current image ( $s$ ) and the reference frame $\left(s^{\prime}\right)$ :

$$
\begin{equation*}
\phi\left(x_{i}, y_{j}\right)=s\left(x_{i}, y_{j}\right)-s^{\prime}\left(x_{i}, y_{j}\right) \tag{3.36}
\end{equation*}
$$

$h\left(x_{i}, y_{j}\right)$ is calculated using spatial gradients ( $G_{x_{i}}$ and $G_{y_{j}}$ ) on both axis (using Sobel operator):

$$
h\left(x_{i}, y_{j}\right)=\left(\begin{array}{llllll}
G_{x_{i}} & G_{y_{j}} & x_{i} G_{x_{i}} & x_{i} G_{y_{j}} & y_{j} G_{x_{i}} & y_{j} G_{y_{j}} \tag{3.37}
\end{array}\right)
$$

and A represents the affine parameters:

$$
A=\left(\begin{array}{llllll}
a_{1} & a_{2} & a_{3} & a_{4} & a_{5} & a_{6} \tag{3.38}
\end{array}\right)^{T}
$$

resulting in:

$$
\begin{equation*}
A=\left(H^{T} H\right)^{-1} H^{T} \phi \tag{3.39}
\end{equation*}
$$

3. The parameters that minimize the Lagrangian cost of data rate and summed absolute values of prediction error are selected;

In order to reduce the amount of additional information, the affine parameters are quantized with a step size of $1 / 16$ for $a_{1}$ and $a_{2}$ and $1 / 512$ for the remaining values. The lower precision for the first two coefficients is due to the fact that those values are responsible for $x$ and $y$ translations.

The authors tested this method limiting HEVC to a maximum block size of $16 \times 16$, $64 \times 64$ and $128 \times 128$. The average data rate reduction for a set of 10 sequences with non-transnational motion is $0.1 \%, 6.3 \%$ and $7.6 \%$ respectively. This shows that for these experimental tests, the increasing maximum block size benefits the application of an affine motion model.

## Motion compensation for very low bit-rate video

On this proposal, by Faria et al.[20], bilinear transforms are used to compensate motion. Each corner of a block is associated with a vector that must be transmitted in order to correctly decode the image. In order to find these vectors the BMA (Block Matching Algorithm) is applied between the current frame and the reference frame. After determining
the motion vector the algorithm BMGT (Block Matching with Geometric Transforms) is used as a enhancement step. The estimation of the transform coefficients is done by moving the four corners of each block of the frame independently. In order to compare the warped block with a square block, inverse mapping is applied to the warped block.

In order to reduce the complexity of this method, a fast search method, based on OSA (Orthogonal Search Algorithm), was implemented for each one of the corners of the blocks.

The experimental results demonstrate considerable improvements, compared to H.261, in terms of objective and subjective quality of the reconstructed frames using geometric transforms. Figure 3.6 shows the subjective quality achieved using only BMA (left image) and BMGT (right side).


Figure 3.6: Prediction image using BMA (left) and BMGT (right) on frame 20 of Sergio sequence [20]

### 3.2.2 Picture-level approaches

## A block-adaptive skip mode for inter prediction based on parametric motion models

The proposal of Glantz et al.[21] aims to improve the performance of a reference codec by adding a new prediction mode called PSKIP (Parameter SKIP). This new prediction mode is associated with a reference image generated using geometric transforms.

A group of parameters is generated for each image to be encoded. These parameters are used to describe the background movement i.e global motion. The algorithm used in this technique is divided into four steps:

1. Find correspondent features between the current frame and the reference frame
using KLT (Kanade-Lucas-Tomasi) algorithm;
2. Estimate the parametric model of movement through a method based on the Helmholtz principle [22] using the correspondent points;
3. After generating several groups of parameters, the HTE (Helmholtz Tradeoff Estimator) algorithm is used to remove the outliers in order to select the best group. This algorithm has the ability to detect $80 \%$ of the outliers in a given dataset[21];
4. After the best set of parameters has been found, blocks with this model are coded with the PSKIP mode.

The main advantage of the PSKIP mode, as for the traditional SKIP mode, is the fact that a block can be coded without transmitting any residue, which reduces the necessary bit-rate to code the block. However when using this mode, 8 uncompressed floats are transmitted, in order to describe the perspective transform. These 8 floats imply an increase of 256 bits per image. Even if the PSKIP mode is not used, these parameters are transmitted.

The integration of this mode on the encoder is done side by side with other prediction modes. The encoder tests all the available modes and the RDO (Rate Distortion Optimizer) selects the mode that is more appropriated to the block to be coded. The more appropriated mode is chosen taking into account both objective quality and the necessary bit-rate.

The PSKIP mode has been incorporated into the test module HM 1.0 of HEVC. The results show a bit-rate decrease, relative to the HM 1.0 without PSKIP mode, that reaches $29,1 \%$ (Low Delay condition). The worst case is an increase of $1,8 \%$ of the bit-rate (Random Access condition). However the author states that, by compressing the 8 float parameters, or by transmitting one vector for each corner of the image these results may improve.

This method has some drawbacks, like the fact that the transform coefficients are uncompressed and transmitted as floats. Instead of the eight float coefficients, four vectors could be transmitted (one for each corner of the image) in order to further decrease the bit-rate.

## Picture-level parametric motion representation for efficient motion compensation

This proposal, presented by Sung et al.[23], describes the introduction of geometric transforms on an hybrid codec like MPEG-4 or H.264/AVC, in order to improve the motion
compensation performance. Through the use of geometric transform new reference images are generated. Only the most similar images are selected to be reference images. This method provides an improved motion resulting in a reduction of the bit-rate, in comparison with reference codecs.

The proposed algorithm is divided into five steps:

1. Detection of common features points between the current frame and a reference frame that is available on the decoders buffer, using the KLT algorithm;
2. The corresponding points between the two frames are organized in clusters depending on the movement of each region of the image, using an algorithm based on region growing;
3. The perspective transformation coefficients are extracted for each set of points;
4. The new possible reference frames are generated using the Perspective transformation coefficients;
5. The generated frame that is more likely to be chosen by the encoder RDO is selected to be the new reference frame.

In order to decrease the computational complexity, two rules have been added to the algorithm:

- The new frame its added to the reference frame list only if at least $15 \%$ of the frame blocks have a SAD two times lower than the SAD of the same block of the original reference frame (without geometric transformation)
- If no image is inserted on the reference frame list it is assumed that the extracted coefficients are not correct. If this happens the algorithm is disabled for all the frames between the current frame and the reference frame without geometric transformations.

In order to be fully described the perspective transform needs eight coefficients to be transmitted. In this case, four vectors are transmitted that correspond to each one of the corners of the warped frame. This alternative uses a smaller amount of bits, by transmitting four vectors with quarter pixel precision in comparison with the eight float coefficients.

This proposal has been implemented on the test module TMuC 0.7.3 of HEVC. For low delay and random acess conditions the results show a decrease on the bit-rate by $3,1 \%$ and $3,5 \%$, respectively (in average). As expected the best results occur on the test
sequences that are characterized by complex motion, for example, the Station2 reaches $41,1 \%$ (Low Delay) and $28,9 \%$ (Random Access) of bit-rate reduction when comparing with TMuC 0.7.3 (HEVC).

This method has proven to be more efficient in terms of rate-distortion performance, comparing with TMuC 0.7.3 (HEVC).

## Improving H.264/AVC video coding with geometric transforms

Souza et al.[24] introduces the use of geometric transforms in the reference codec H.264/AVC to improve its performance. The proposal is entitled H.264/AVC-GT-N and includes $N$ reference frames generated by geometric transforms (GT).

This algorithm is organized as follows:

1. Partitioning of the macroblocks and motion estimation by H.264/AVC;
2. Estimate the best geometric transform for each block of the current frame;
3. A technique, based on region growing, is used to create $N$ sets of geometric transform, that better represent $N$ regions of the current frame;
4. $N$ new reference frames are generated with the geometric coefficients determined in the previous step;
5. The geometric transform is described by four vectors (one for each corner of the frame). These vectors are encoded using CABAC in order to be inserted on the bitstream.

The estimation of the best geometric transform is made through a search method for each corner of the frame. Each corner of the frame uses a $64 \times 64$ pixel search window. A search method, similar to FS (Full Search), is applied for each corner. The FS method applied in this context would imply testing more than $10^{19}$ possibilities for each block, because all the combinations of the four corners inside the 64 x 64 search window would be tested. This method would clearly be impracticable. By limiting the number of combinations between the four corners of the block the computational complexity is highly reduced.

This proposal was tested using $N=4$ and $N=8$ new reference frames generated through geometric transforms, achieving a mean bitrate saving of $-6,11 \%$ and $-5,18 \%$ respectively. These results indicate that having a higher number of reference frames is not always the most advantageous approach.

This proposal has shown to improve the reference codec H.264/AVC in terms of ratedistortion performance. The block-based search for the best $N$ sets of coefficients provide
a more localized motion compensation. The transform parameters are transmitted as four vectors for each of the $N$ reference frames, and these vectors are encoded using CABAC. The major drawbacks of this proposal are the necessary overhead to describe the geometric transforms and the computational complexity necessary by the search method.

## Motion vector analysis based homography estimation for efficient HEVC compression of 2D and 3D navigation video sequences

In the work by Springer et al.[25] the application of geometric transformed pictures is used to efficiently compress navigation video sequences. This type of sequences is mainly characterized by rotational motion, besides translational motion. Also these sequences have semi-transparent static areas that normally display information about the trip. Figure 3.7 shows an example of this type of sequences, highlighting both described areas.


Figure 3.7: Navigation sequences examples: Basel12D (left) and Insbruck3D (right) with two distinct areas: map and semi-transparent static areas [25]

HEVC was modified to accept these navigation sequences, using the following algorithm:

1. During the motion estimation process, all vector are collected in a list of floating point coordinates;
2. RANSAC [26] is used to filter all outliers (vectors that correspond to the static areas);
3. The selected inlier vectors are used to generate a Projective transformation $H$ matrix using least squares;
4. If the transform is a rotation the first reference frame is geometrically compensated using the $H$ matrix becoming a substitute for the second reference frame;
5. The motion estimation process step is reinitialized using the new reference image.

The $H$ parameters are transmitted as 18 bytes of additional information per frame, representing 9 numbers with a precision of 2 bytes each.

When comparing the application with the original encoder, on a low delay scenario, using four sequences, a mean BD-rate saving of $8,78 \%$ is achieved.

The authors claim that using the motion vectors and RANSAC instead of using a feature based approach (like their previous work [27]) combined with SIFT [28] or SURF [29] provides a similar performance with about $21 \%$ less computational complexity.

### 3.2.3 Applications summary

Table 3.1 shows a summary of the previously described applications. It is possible to identify a tendency towards transforms with 8 DoF where a quadrilateral to quadrilateral transform is available. Also none of the studied references uses an implicit algorithm, every transform that is chosen, either on a block or picture level, needs to be explicitly transmitted. In terms of computational complexity, methods based on Least Squares or Feature-based are normally faster than Brute force or Region growing.

Table 3.1: Summary of the previously described applications

| Approach | Ref. | Transform | Coefficient estimation | Coefficient transmission |
| :---: | :---: | :---: | :---: | :---: |
| Block-level | $[19]$ | Affine | Least squares <br> + Lagrangian cost | 6 quantized <br> coefficients |
| Block-level | $[20]$ | Bilinear | Brute force | 4 vectors <br> compressed with VLC |
| Picture-level | $[21]$ | Projective | KLT + Helmholtz <br> principle + HTE | 8 floats <br> $(256$ bit $)$ |
| Picture-level | $[23]$ | Projective | KLT + region <br> growing | 4 vectors with <br> $1 / 4$ pixel precision |
| Picture-level | $[24]$ | Projective | Brute force + <br> region growing | 4 vectors compressed <br> with CABAC |
| Picture-level | $[25]$ | Projective | Motion estimation + <br> RANSAC + Least squares | 9 values with <br> 2 bytes of precision |

## Chapter 4

## Disparity compensation using geometric transforms

The creation of 3D content is usually done through the recording of a scene using two or more cameras. Regardless of the displaying method, in the simplest form, i.e. stereo, one video sequence corresponds to the left eye and another video corresponds to the right eye.

The human visual system is able to have a 3D perception of the world using two images projected into our retina [30]. Since such images represent two different points of view depth can be perceived. Depth perception is the result of binocular disparity, corresponding to the difference in position of an object between the two projected images. Figure 4.1 shows an example of binocular disparity.

The example in Figure 4.1 shows that when the circle is being focused the square appears in different positions of the retina for both eyes. From the left eye perspective the square appears to be close to the circle, however from the right eye point of view the objects are further away. This difference between the position of the square in the left eye and the right eye (disparity) is dependent on the depth of the square relative to the eyes plane.

When using two cameras to replicate the two different points of view, the same disparity can be observed. Figure 4.2 shows a pair of images captured with a pair of cameras where the left picture corresponds to the left camera point of view and the right picture corresponds to the right camera point of view.

Three green blocks are marked in the same position in both images, where a small horizontal displacement of the scenes objects can be noticed. If the correspondent objects are marked on the right picture with blue squares, the displacement can be measured in pixels.

In 3D video coding the inter-view redundancy between adjacent views can be exploited


Figure 4.1: Example of binocular disparity [31]


Figure 4.2: Example of disparity in a pair of images acquired with parallel camera arrangement
using the disparity information, in order to encode the various videos more efficiently. Since images captured from several cameras are very similar, one view can be predicted using previously encoded views. The most recent standards use vectors to describe the disparity between adjacent views, using similar techniques to those used for motion estimation, like BMA (Block Matching Algorithm). Disparity is highly dependent on the position and orientation of the camera array. If the camera array is parallel, like the example in Figure 4.2, the disparity is mainly horizontal. However, in a convergent camera array (Figure 4.3)the existing disparity is much more complex, and may not be accurately describe by only one translational vector i.e. 2 DoF.


Figure 4.3: An example of a pair of images acquired with a stereo pair of convergent camera arrangement

The following sections present other techniques based on geometric transforms that can be used to estimate disparity in block and region based approaches in a more accurate way. These techniques were implemented outside of a coding environment in order to be compared and individually tested. The technique that achieves the best tradeoff between distortion and extra bits generated is integrated in a coding environment described in the next chapter.

### 4.1 Block based approach

Disparity compensation is preformed by the multiview extensions of the most recent coding standards, in order to exploit the redundancy between different views of the same scene. BMA (Block Matching Algorithm) is used to compensate disparity at the block level. BMA divides the image into blocks and searches for the best match of each block on another image. The disparity is described by a vector that represents the difference in position between corresponding areas in both images. The matching is performed by measuring the distortion between a block in a reference picture and a block in the other
picture, for several locations. The block location that represents the lowest distortion is used to determine the disparity of that area. Figure 4.4 shows an example of block matching using $m \times n$ blocks. The left image represents a block from the reference picture and the right image represents a block on the picture that is being compared. The difference in position is given by the vector $v$.

The metric used to calculate the distortion is normally the SAD (Sum of Absolute Differences) or the SSD (Sum of Square Difference), as represented by equations 4.1 and 4.2. Equations 4.3 and 4.4 define the $x$ and $y$ components of vector $v$, respectively.

$$
\begin{gather*}
S A D=\sum_{j=j_{0}}^{n} \sum_{i=i_{0}}^{m}\left|p_{0}(j, i)-p_{1}\left(j+v_{y}, i+v_{x}\right)\right| ;  \tag{4.1}\\
S S D=\sum_{j=j_{0}}^{n} \sum_{i=i_{0}}^{m}\left[p_{0}(j, i)-p_{1}\left(j+v_{y}, i+v_{x}\right)\right]^{2}  \tag{4.2}\\
v_{x}=i_{1}-i_{0}  \tag{4.3}\\
v_{y}=j_{1}-j_{0} . \tag{4.4}
\end{gather*}
$$

On the example shown in Figure 4.4 the SAD and SSD are calculated for vector $v$, where $p_{0}$ and $p_{1}$ represent the pixel value in both blocks, respectively.

SSD normally achieves better results because the most commonly used metric to evaluate objective quality, PSNR (Peak Signal-to-Noise Ratio), is calculated using MSE (Mean Squared Error), which is the SSD divided by the number of pixels. However, SSD has a higher computational complexity due to the multiplication of each pixel difference.

BMA may not be the most appropriated matching algorithm for all cases. The following subsections represent a study showing how geometric transforms can be added to BMA to improve the algorithm performance.

### 4.1.1 Block matching using geometric transforms

When performing BMGT (Block Matching with Geometric Transforms), instead of describing the matching between blocks by a translation, using one vector, four vectors are used, one for each corner. This results in a block matching that can move any corner of the block independently from each other, allowing to match more complex geometric distortions.

Although this method strongly increases the matching efficiency, the computational complexity is much higher than BMA. Even if the search area for each corner of the block is limited by a search window, it's impracticable to use a FS (Full Search) method to test all the possible combination of corner positions. In order to reduce the number of


Figure 4.4: An example of one of the matching cases when applying BMA.
matching positions, the block matching is divided into two steps:

- The BMA is applied using FS method;
- The BMGT is applied as a refinement step using a fast search method (applied to the vector associated with each corner of the block).

The first step is used to center the block on the best matching position of the picture, within a search window. The second step, shown on Figure 4.5, is used to improve the BMA result, if possible. Each one of the four corners has its own search window, where the fast search method is applied. All combinations within the fast search methods of the four corners are tested. In this algorithm instead of one vector, like BMA, four vectors are necessary, one for each corner of the block. The gray squares on each one of the corners represent the search window for the fast search method.

By dividing the algorithm into two steps one can ensure that the final result has, at least, the same distortion as applying the BMA alone, while reducing substantially the computational complexity, making this method more practicable.

Several algorithms have been developed to reduce the number of matching possibilities. The matching solution obtained by these methods is sub-optimal However the computational complexity is largely reduced when compared with the FS method. In this context, three fast search methods were tested:

- OSA (Orthogonal Search Algorithm) [32];
- TSS (Three-Step Search algorithm) [33];
- HEXBS (Hexagonal-Based Search algorithm) [34].


Figure 4.5: Example of block matching with BMGT.

The OSA starts by applying a step that is half the size of the search window. For each iteration the step size is halved until it becomes unitary. The search direction is alternated between the horizontal and vertical axis after each iteration. Figure 4.6 shows an example of OSA. Each color represents two iterations. For each pair of iterations, the first search is in the horizontal direction and the second is vertical, centred on the horizontal point with lowest distortion.

The TSS has a nine point square format. All nine points are tested and the one with the lowest distortion value will be the origin to the next iteration. At each iteration the step size is halved until it becomes unitary, ending the search afterwards. Figure 4.7 shows an example of TSS. Each color represents one iteration that is directly related with the step size, 4, 2 and 1 for this example. Each square shape of one iteration is centred on the previous best point.

The HEXBS is divided into two steps. The first step is a seven point hexagonal format with a fixed size step (does not varies with the window size). All the seven points are tested and if the point with the lowest distortion is not at the center of the hexagon then a new hexagon format is centred on the point with the lowest distortion. This happens on every iteration until the point with the lowest distortion is the center of the hexagon. When it occurs, a five point cross format is tested on the center of the hexagon. Selecting the best match by the lowest distortion. Figure 4.8 shows an example of HEXSB. Each iteration is a different hexagon. When the point with the lowest distortion is in the center of the hexagon, a cross search is preformed around that point.

In order to test the BMGT algorithm two images from different views of the same


Figure 4.6: An example of one of the matching cases when applying OSA.


Figure 4.7: An example of one of the matching cases when applying TSS.


Figure 4.8: An example of one of the matching cases when applying HEXBS.

| Block size | BMGT Window | BMA only | BMGT |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | OSA | TSS | HEXBS |
| Vassar |  |  |  |  |  |
| 8 x 8 | $3 \times 3$ | 31.757 | 33.121 | 33,397 | 33,121 |
|  | $7 \times 7$ |  | 33,822 | 34,181 | 33,995 |
| 16x16 | 7 x 7 | 29.167 | 30,591 | 30,832 | 30,719 |
|  | $15 \times 15$ |  | 31,070 | 31,358 | 30,867 |
| Ballet |  |  |  |  |  |
| 8 x 8 | 3 x 3 | 32.101 | 32.841 | 32.992 | 32.841 |
|  | 7 x 7 |  | 33.493 | 33.775 | 33.634 |
| 16x16 | 7 x 7 | 29,501 | 30.363 | 30.542 | 30.456 |
|  | $15 \times 15$ |  | 30.922 | 31.206 | 30.613 |
| Book Arrival |  |  |  |  |  |
| 8x8 | 3 x 3 | 32.539 | 33.249 | 33,317 | 33,249 |
|  | 7x7 |  | 33,763 | 33,900 | 33,768 |
| 16x16 | 7 x 7 | 31.536 | 32.557 | 32.629 | 32.594 |
|  | $15 \times 15$ |  | 32.941 | 33.052 | 32.674 |

Table 4.1: Experimental results comparing the BMA and the BMA+BMGT and the different fast search methods.
scene were processed with this method. The result is the best match between the two images using a vector for each corner of every block in the image. Using this information and the right view, the left image is reconstructed. The result is compared with the original image using the PSNR. The preformed tests are shown on Table 4.1. The BMA window is $65 \times 65$ for Vassar sequence and $193 \times 193$ for the Ballet and Book Arrival.

The chosen values for the BMGT window take into account the block size. For each block size the BMGT search window has either, half the size of the block (on each direction) or the same size. This way, the tested deformations will always remain a convex quadrilateral.

As expected, all the tests using the refinement step with BMGT resulted in a reconstructed image with higher PSNR. Even when using a small search window, like $3 \times 3$ the PSNR increases almost 1dB in many cases. In the best cases the PSNR is increased by more than 2 dB .

The fast search algorithm that achieved the best results on the preformed tests is the TSS. This is an expected result because it tests a higher number of matches than its counterparts. However the TSS is the most complex algorithm amongst the three.

### 4.1.2 BMA+BMGT using a grid

One of the methods that achieved a high improvement in standard codecs performance was the use of non-integer precision like half or quarter pixel when applying the interframe prediction. That improvement results from the fact that motion can not always be correctly described by a vector with integer coordinates, in terms of pixel distance. When applying a higher precision the final result is able to describe more precisely the motion or the disparity between two images.

To test this technique with geometric transform a new parameter was added, the grid size. As is shown on Figure 4.9 instead of deforming the block, the grid that surrounds the block is deformed. Comparatively, in the previous tests the grid was the same size as the block, resulting in integer precision.

In the following tests the grid is twice, four times and eight times the size of the block. Because the block is centred on the grid, a change of one pixel on the corner of the grid results in a change of only a fraction of a pixel in the correspondent corner of the block. A change to the corner of the block is proportional in the relation between a block and the grid size. The search window for each corner was the same size as the grid. The preformed test results are shown in Table 4.2. The BMA window is $65 \times 65$ for Vassar sequence and $193 \times 193$ for the Ballet and Book Arrival.

As in the previous tests, the TSS algorithm achieves the highest PSNR. All fast search

| Block size | BMGT Window | Grid Size | BMA only | BMGT |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | OSA | TSS | HEXBS |
| Vassar |  |  |  |  |  |  |
| 8x8 | 7x7 | 8x8 | 31.757 | 33,822 | 34,181 | 33,995 |
|  | 15x15 | 16x16 |  | 33.950 | 34.308 | 33.702 |
|  | $31 \times 31$ | $32 \times 32$ |  | 33.923 | 34.299 | 33.230 |
|  | $63 \times 63$ | $64 \times 64$ |  | 33.968 | 34.417 | 32.924 |
| 16x16 | 15x15 | 16x16 | 29.167 | 31,070 | 31,358 | 30,867 |
|  | $31 \times 31$ | $32 \times 32$ |  | 31.142 | 31.516 | 30.569 |
|  | $63 \times 63$ | 64x64 |  | 31.238 | 31.548 | 30.335 |
|  | $127 \times 127$ | 128x128 |  | 31.247 | 31.627 | 30.171 |
| Ballet |  |  |  |  |  |  |
| 8x8 | 7 x 7 | 8x8 | 32.101 | 33,493 | 33.775 | 33,634 |
|  | $15 \times 15$ | 16x16 |  | 33,678 | 33,994 | 33,303 |
|  | $31 \times 31$ | $32 \times 32$ |  | 33,761 | 34,173 | 32,958 |
|  | $63 \times 63$ | 64 x 64 |  | 33,983 | 34,495 | 32,783 |
| 16x16 | $15 \times 15$ | 16x16 | 29.501 | 30.922 | 31.206 | 30.613 |
|  | $31 \times 31$ | 32x32 |  | 31,125 | 31,463 | 30,327 |
|  | $63 \times 63$ | $64 \times 64$ |  | 31,314 | 31,735 | 30,192 |
|  | $127 \times 127$ | 128x128 |  | 31,622 | 32,168 | 30,140 |
| Book Arrival |  |  |  |  |  |  |
| 8 x 8 | 7 x 7 | 8x8 | 32.539 | 33.763 | 33.900 | 33.768 |
|  | 15x15 | 16x16 |  | 34.090 | 34.376 | 33.649 |
|  | $31 \times 31$ | $32 \times 32$ |  | 33.094 | 34.259 | 33.437 |
|  | $63 \times 63$ | $64 \times 64$ |  | 33.984 | 34.137 | 32.287 |
| 16x16 | $15 \times 15$ | 16x16 | 31.536 | 32.941 | 33.052 | 32.674 |
|  | $31 \times 31$ | 32x32 |  | 33.125 | 33.318 | 32.521 |
|  | 63x63 | $64 \times 64$ |  | 32.955 | 33.135 | 32.440 |
|  | $127 \times 127$ | 128x128 |  | 33.410 | 33.650 | 32.368 |

Table 4.2: Experimental results comparing BMA and BMA+BMGT for different grid sizes.


Figure 4.9: An example of one of the matching cases when applying BMGT to the grid of the red block.
algorithms achieved improvements in PSNR when increasing the grid size, with the exception of HEXBS. HEXBS is the only one of the tested algorithms that does not increases the size of its format with the search window. This is why the PSNR tendentiously decreases when the grid size is increased.

In most cases for OSA and TSS algorithms the increase of the grid size improves the PSNR of the reconstructed view. In particular, the results for the sequence Ballet show the highest PSNR increase grid size increases. This is because the camera setup of this scene is convergent instead of parallel, like the Vassar or Book Arrival sequences. This kind of sequences take most advantage of geometric transformation in terms of subjective results.

For some cases the PSNR decreases with the increase of the grid size. By increasing the grid size, the precision of the geometric transformation is improved, but it is a different quadrilateral that is deformed. The matches are not the same, so the final result is different and the reconstructed image can have a lower PSNR.

However, in general the highest PSNRs were achieved for larger grid sizes. In order to establish the increase in precision and the increase in PSNR, more tests are necessary, using larger grid sizes. Tests in Table 4.3 use a grid that in the first test starts of as block size and the last test is 128 times the size of the block. Note that, since the TSS algorithm
is the search method presenting highest PSNR for all tests, from now on it will be used with BMGT. Moreover, a block size of $8 \times 8$ is used for all experimental tests. The BMA window is $65 \times 65$ for Vassar sequence and $193 \times 193$ for the Ballet and Book Arrival.

The experimental results confirm that the increase in grid precision will result in an increase in PSNR. This occurs for both sequence types, either using a parallel or convergent camera setup.

Nevertheless it's important to understand why the increase on objective quality occurs. Figure 4.10 compares reconstructed images of Ballet sequence using a grid size of $64 \times 64$ and $1024 \times 1024$. The image on the left use a $64 \times 64$ grid and the image on the right were reconstructed using a $1024 \times 1024$ grid

The improvement in PSNR when increasing the grid size resulted for the better reconstructed occlusion areas. The reconstructed images from Book Arrival only differ on the left side of the picture where there is an occlusion. The same occurs on Ballet, although in this case the occlusion areas are much larger because of the convergent camera setup. In the occlusion areas the right camera has no information about some areas of the scene, so the BMA tries to fit the best matching block within its search range. When the BMGT is applied the deformation allows an improvement on the matching capabilities. When increasing the precision of the deformation more matching possibilities are tested so its more likely to find a match with lower distortion.

One should notice that despite the increase in PSNR when using higher grid sizes, each time the grid size is doubled the search window is also doubled. Consequently, the amount of bits necessary to represent the deformation vector increases by 1 bit each time the vector's dynamic range is doubled. It's necessary to have this into account if using this kind of methods within a codec.

The TSS search algorithm preforms one more step each time the search window is doubled. This means that when using a grid size of $8 \times 8$ the TSS preforms two steps, using step sizes of: 2 and 1 . When using the $1024 \times 1024$ grid the number of steps is nine, with step size of: $256,128,64,32,16,8,4,2,1$. However, for the $1024 \times 1024$ grid not all the steps introduce the same gain in the final PSNR. Table 4.4 shows the PSNR of the reconstructed view of Ballet and Book Arrival using the $1024 \times 1024$ grid. The TSS was limited to a certain number of iterations in order to understand what is the gain of each step, when doubling the vector dynamic range

As expected, the progressive increase in the number of steps results in a progressive increase of the PSNR, for both reconstructed images. The first iteration reconstructs the Book Arrival image with a PSNR of 37.329 dB and the disparity vectors can be represented with only 4 bits per vector, because there are only 3 possible values: $-256,0$ and 256 . The same number of bits necessary to represent the first test on Table 4.3 where the grid size

| BMGT Window | Grid Size | BMA only | BMGT |
| :---: | :---: | :---: | :---: |
| Ballet |  |  |  |
| $7 \times 7$ | $8 \times 8$ |  | 33.775 |
| $15 \times 15$ | $16 \times 16$ |  | 33.994 |
| $31 \times 31$ | $32 \times 32$ |  | 34.173 |
| $63 \times 63$ | $64 \times 64$ | 32.101 | 34.495 |
| $127 \times 127$ | $128 \times 128$ | 35.140 |  |
| $255 \times 255$ | $256 \times 256$ |  | 36.249 |
| $511 \times 511$ | $512 \times 512$ |  | 37.700 |
| $1023 \times 1023$ | $1024 \times 1024$ | 39.789 |  |
| Book Arrival |  |  |  |
| $7 \times 7$ | $8 \times 8$ |  | 33.900 |
| $15 \times 15$ | $16 \times 16$ |  | 34.376 |
| $31 \times 31$ | $32 \times 32$ |  | 34.259 |
| $63 \times 63$ | $64 \times 64$ | 32.539 | 34.137 |
| $127 \times 127$ | $128 \times 128$ | 36.592 |  |
| $255 \times 255$ | $256 \times 256$ |  | 38.476 |
| $511 \times 511$ | $512 \times 512$ |  | 39.545 |
| $1023 \times 1023$ | $1024 \times 1024$ |  | 39.988 |

Table 4.3: Experimental results comparing the BMA and the BMA+BMGT and different grid sizes.


Figure 4.10: Part of the reconstructed images of Ballet.

| Last step | Iterations | Book Arrival | Ballet |
| :---: | :---: | :---: | :---: |
| 256 | 1 | 37.329 | 35.315 |
| 128 | 2 | 38.200 | 36.556 |
| 64 | 3 | 38.535 | 37.551 |
| 32 | 4 | 38.813 | 38.324 |
| 16 | 5 | 38.993 | 38.929 |
| 8 | 6 | 39.152 | 39.342 |
| 1 | 9 | 39.988 | 39.789 |

Table 4.4: Experimental results using the TSS method.
is 8 x 8 resulting in a PSNR of 33.9 dB . This means that using the same amount of bits the difference in distortion is about 3.5 dB . Also in Table 4.4 one can see that the increase on PSNR tends to be smaller each time a new step is added. This means that not all step are worth the extra complexity and bitrate.

Not all step introduce the same gain, in terms of PSNR, and each step greatly increases the complexity, and the computation time. Table 4.5 shows the amount of time needed to process the first frame of the Ballet sequence with different grid sizes and the number of steps for each test. Also the complexity is compared with the search method used by Souza et al. [24] when applied to the same test sequence under the same test conditions. These conditions include the grid size represented on Table 4.5 using a search window with the same size for each corner of the grid.

Souza et al. [24] search method matches each corner individually. The upper left corner is matched first and all the possible positions within that corner are tested. Then the upper right corner is matched using all possible corner positions. This method continuous using a clockwise order through all four corners. Testing the four corner is considered an iteration. After five iterations the method stops and the resulting value is the one with the lowest distortion. Moreover, if after one iteration no change occurs that combination of vectors is chosen.

| Grid Size | Souza et al.[24] |  | TSS |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | PSNR | Time | PSNR | Time | Steps |
| $8 \times 8$ | 32,741 | 0 m 17.709 s | 33,775 | 33 m 12.793 s | 2 |
| 16 x 16 | 32,738 | 0 m 29.150 s | 33,994 | 155 m 6.510 s | 3 |
| 32 x 32 | 32,816 | 1 m 7.524 s | 34,173 | 427 m 21.334 s | 4 |
| 64 x 64 | 33,095 | 3 m 16.288 s | 34,495 | 878 m 58.156 s | 5 |
| 128 x 128 | 33,826 | 10 m 42.180 s | 35,140 | 1519 m 3.192 s | 6 |
| 256 x 256 | 35,178 | 36 m 17.132 s | 36,249 | 2374 m 15.523 s | 7 |
| 512 x 512 | 36,959 | 131 m 7.200 s | 37,700 | 3525 m 14.651 s | 8 |
| 1024 x 1024 | 37,351 | 452 m 35.057 s | 39,789 | 5037 m 41.010 s | 9 |

Table 4.5: Experimental results comparing the Souza's search method and the TSS.

All the processing time tests, on Table 4.5, were achieved using the following specifications: Intel® Xeon(R) CPU E5504 @ 2.00GHz, 12Gb Ram, Ubuntu 12.04 LTS (64 bits).

As can be seen the complexity of the developed method is much higher then the proposed by Souza et al. This results in a higher PSNR for the proposed method. In order to decrease the computational complexity of the proposed method using the TSS the resulting PSNR of all the steps must be analysed. For example the last steps of the higher grids may not represent a significant increase in the final PSNR. In order to test this, Figures $4.11,4.12$ and 4.13 compare the PSNR using various grid sizes with the same limited number of steps. The BMA search window is $193 \times 193$ for Ballet and Book Arrival and $65 \times 65$ for Vassar.

As can be seen in both Figures 4.12 and 4.13 using the same number of steps but a larger grid, widely increases the PSNR. This occurs due to the fact that when the grid size is increased the BMGT window is also increased, allowing the block to reach larger areas. Note that when both grid and window sizes are increased but the number of steps is maintained, the resulting vectors can be described using the same amount of bits and no processing time is added. This happens because the total number of tested cases is the same.

In the case of Figure 4.13 the PSNR variation is relatively small compared to the previous figures. Comparing the $64 \times 64$ grid with the highest grid $1024 \times 1024$ for 1,3 and 5 steps the maximum PSNR variation is about 0.4 dB . In terms of different number of steps, generally the PSNR increase is very high when using 3 steps instead of just 1. However when comparing 3 and 5 steps the same does not occur with the same magnitude and the complexity increases about six times higher.

These experimental results show that in terms of complexity, final PSNR and necessary bits to represent the transformation vectors, using a $1024 \times 1024$ grid with only 3 steps is the most favourable scenario. Table 4.6 shows the experimental results using the TSS search algorithm using the previously described set of parameters and the equivalent application of Souza et al. search algorithm (i.e. the same grid and window size).

| Sequence | Souza et al. [24] |  | TSS |  |
| :---: | :---: | :---: | :---: | :---: |
|  | PSNR | Time | PSNR | Time |
| Ballet | 37.351 | 452 m 35.057 s | 37.551 | 65 m 39.626 s |
| Book Arrival | 38.995 | 380 m 43.508 s | 38.535 | 64 m 10.949 s |
| Vassar | 34.041 | 172 m 33.603 s | 33.677 | 27 m 43.076 s |

Table 4.6: Experimental results comparing the search method used by Souza et al. and the TSS.

Ballet (0 and 4), Block size $8 \times 8$


Figure 4.11: PSNR variation for the same number of steps/iterations with different grid sizes.


Figure 4.12: PSNR variation for the same number of steps/iterations with different grid sizes.


Figure 4.13: PSNR variation for the same number of steps/iterations with different grid sizes.

As shown in Table 4.6, the PSNR is similar for both methods, the highest difference is about 0.4 dB for the Vassar sequence. However the TSS achieves a similar objective quality in about one sixth of the time. This shows that the TSS search algorithm is more efficient compared with Souza et al. search method.

The lack of efficiency in the compared algorithm lies on the fact that each iteration of the search algorithm fixates each corner while matching the remaining ones. When matching one corner the other remain fixated on their last position. This fact drastically reduces the probability of finding good matches on the next corner. By the time all 4 corners were tested a new adjustment to any corner rarely decreases the resulting distortion.

### 4.2 Region based approach

In the region based approaches, instead of a high number of blocks, each one associated with a geometric transform, a smaller number of regions is used. On this type of approaches, the first step is to segment the picture that is going to be compensated and then compensate the disparity of each region individually. The segmentation step can be applied to various types of information depending on the intended desired regions. These types of information can be, texture, motion, disparity or depth. In this case, since it is intended to compensate disparity, the disparity map can be used. However the depth map can be captured using depth cameras or generated using the disparity map and the camera parameters that are normally known in multiview arrays of cameras. Also the
depth map gives more information about the actual 3D scene than the disparity map.

### 4.2.1 Segmentation step

Several types of image segmentation methods can be used, like: threshold, clustering, histogram, edge detection and region growing methods. In this dissertation two methods were tested to segment the depth map, a clustering method (K-Means [35]) and an edge detection method (Watershed [36]).

The K-Means based method is a clustering method that divides the depth map into $K$ clusters. The algorithm for this method is described as follows:

1. $K$ seeds are randomly placed in the depth map that represent the initial centroids;
2. The distance between the centroids and all the remaining pixels is calculated. The distance can be calculated using several metrics, in this case, the Squared Euclidean distance was used;
3. Each cluster is created by grouping the pixels that have the lowest distance to each centroid;
4. $K$ new centroids are calculated by averaging all the pixels on each cluster. The new centroid on each cluster substitutes the last centroid;
5. Steps 2, 3 and 4 are repeated until no changes occur on each cluster, which means that the method has converged, or, in this case, until the steps are repeated ten times.

Moreover, for this application, if any of the final clusters are empty, the whole algorithm is repeated.

The used Watershed based method, has some initial steps that are used to improve the application of the Watershed transform. In this case, the background and foreground are marked to reduce over-segmentation result that is common on the Watershed approach. The algorithm is explained as follows:

1. A segmentation function is used to detect the objects to be segmented. In this case a gradient function was used with the Sobel edge masks. The resulting image has typically high values on edges and low values on the inside the objects;
2. The foreground is marked using a method that can create plane surfaces inside each object. This is normally done using morphological operators such as an erosion followed by a dilation;
3. The background is marked using a thresholding operation applied to the resulting picture of Step 2 and then applying the watershed transform. The result is a picture with rigid lines marking the background;
4. The Watershed transform is applied to a picture that combines the foreground and background markers. The output picture contains the segmented regions.

The results of applying both K-Means and Watershed methods on segmenting depth maps is shown on Figure 4.14. The first pair of images is the original depth map, the second is the result of a segmentation using K-Means and the last one is using Watershed. The segmentation of Breakdancers resulted into five regions and the Ballet sequence resulted in six regions.

Observing the results on Figure 4.14 it is clear that the K-Means algorithm adapts better to the segmentation of both depth maps. In the K-Means case each zone represents an area where the depth is fairly constant relative to the camera. The Watershed results, even when marking the background and foreground using the described algorithm, groups background and foreground areas. This effect is more notorious on the Ballet depth map, where the background is on the same region as the man's legs, which is clearly the closest object to the camera. For these reasons, the segmentation method which was used in this work is the K-Means.

### 4.2.2 Region Matching using Geometric Transforms

Region Matching using Geometric Transforms (RMGT) uses the same algorithm as BMGT, although instead of matching blocks, regions are matched. These regions are determined using the segmentation step previously discussed. A geometric transform is applied to each region by associating four vectors to the corners of the picture. The search method is applied the same way as for the BMGT method where the first step is to match the whole region using only one vector per region (similar to BMA). The second step is to combine four TSS methods, one for each corner of the picture (for each region). The resulting vectors represent the geometric transform achieving 8 DoF. Figure 4.15 represents an example a of one region being geometrically compensated. In the example the first region to be matched is the black region, and then, the white region, resulting in two groups of vectors.

After determining the $N$ geometric transforms for each of the $N$ regions, the vectors are used to create $N$ geometrically compensated images. These pictures become useful in the next chapter to be used as additional reference frames for MV-HEVC. An example of these pictures can be seen in Figure 4.16, for 3 regions. The first two images are the left and right cameras of the Ballet sequence. The picture on the second row on the left side


Figure 4.14: Segmentation of the first frame of the depth map sequences Breakdancers (left) and Ballet (right) using K-Means and Watershed methods.


Figure 4.15: An example of RMGT method application.
has the segmentation result for three regions using K-Means method on the left depth map. The following three pictures, on the second row on the right and the third row, represent the reconstruction of each region of the segmentation map.

Figure 4.17 show the objective results when performing RMGT using 2 DoF (similar to BMA) and 8 DoF using both Projective and Bilinear transform. The PSNR results for each picture are calculated using only the pixels that where within the segmentation masks of the respective region. The experimental results are shown using K-Means method with 2, 4 and 8 regions for two sequences. Balloons and Ballet, with a parallel and convergent camera array, respectively. Each bar represents the PSNR of a region of the picture. The results for the Balloons sequence are in the left side and Ballet on the right side. The tests where performed using 2 Dof, 8 DoF using Projective transform and 8 DoF using the Bilinear transform.

In both sequences when increasing the number of regions, each region normally achieves a higher PSNR, since a smaller region is being matched, improving the efficiency. Both 8 DoF transforms achieve higher PSNR, on the corresponding regions, than in the 2 DoF transforms. Moreover, this improvement occurs in both type of sequences, although not with the same magnitude. As expected, convergent camera array sequences tend to take more advantage of the more complex geometric transform matching approach. The Bilinear transform is less complex and since it achieved similar results compared with the Projective transform, it's going to be used as transform for the proposed method

In terms of comparing this type of approach with the block-based one, it depends


Figure 4.16: An example of the output images of RMGT.


Figure 4.17: Objective quality reconstruction at each region.
on application. Since when using a block-based approach the objective quality is largely improved so is the necessary overhead, when on a region-based approach the improvement is not so high however the overhead is lower. The trade-off between distortion and the necessary bits to transmit the extra information can be optimized using an encoder RDO cost function.

## Chapter 5

## Integration of proposed methods on MV-HEVC

In the previous chapter, the performance of two types of approaches have been tested, block based and region based approaches. The block based approach has the advantage of achieving low distortions when reconstructing the geometrical compensated pictures. However, a high amount of extra information is necessary for each picture, which makes this approach less viable. Since the region based approach generates less extra information, it's more suitable to incorporate in a codec environment.

The MV-HEVC codec was chosen as the basis for the methods proposed in this dissertation, because it is a state-of-the-art multiview video codec. The integration of the proposed methods was done on MV-HEVC using a combination of techniques to generate new reference pictures to improve the inter view prediction for the non-base views. All the proposed methods have been implemented in a stereo video codec only, but they can be used in a multiview environment, with more than two views.

### 5.1 Proposed methods

The proposed methods are based on a four step algorithm:

1. Segment the depth map into $N$ regions;
2. Estimate geometric transform coefficients for each one of the $N$ regions;
3. Compensate disparity using the $N$ set of estimated parameters generating $N$ pictures;
4. Insert the $N$ pictures into the MV-HEVC reference picture list.

The segmentation step is used to identify which are the most relevant regions in the 3D scene. Because we intended to identify regions which can be represented with the same geometric transform, it is very useful to use a depth map. With this information it is possible to obtain a projection from one view to another. Additionally, the depth map presents less information than a texture view, allowing for a simple segmentation approach. A depth map may be regarded as parallel to the camera with similar disparity. Taking this into account, one geometric transform could be associated with each depth plane, being used to compensate the disparity for each plane individually. However, the depth map normally has a precision of 8 bits, which corresponds to 256 possible depth values. Since not all planes may include useful information, it is necessary to select the key depth planes that are used the most on the 3D scene.

The estimation of the geometric transform coefficients that provide the best possible match for each region is done using either a brute force method like RMGT or by exploring the 3D scene geometry. This process is followed by a disparity compensation step, where the left view is compensated using the geometric transform coefficients.

Finally the generated pictures are added to the reference picture list for iter-view prediction i.e. only being used when encoding the right view. Since every time a picture is added to reference picture buffer more bits are needed to signal the usage of the selected reference pictures, the number of added pictures is limited to 4 .

The inter-view prediction structure of MV-HEVC will work as in the example of Figure 5.1, where $N$ geometrically transformed frames are added as reference pictures.

Note that, since these methods are implemented in MV-HEVC, the picture, from the left camera, that is being compensated, is a reconstructed picture previously encoded.


Figure 5.1: Modified inter-view prediction structure, where View 0 corresponds to the left view and View 1 is the right view.

### 5.1.1 K-Means+RMGT

In the first proposed method, K-Means algorithm is used to generate a segmentation map of the depth map into $N$ regions, as explained in chapter 4. Using the segmentation map, the reconstructed left picture and the right picture the RMGT algorithm generates the geometric transform coefficients, using any number of DoF between 2 and 8. After estimating the geometric transform coefficients the disparity is compensated on the left camera aiming to achieve a point of view similar to the right camera, for each region. This approach is shown in Figure 5.2.

Some side information has to be transmitted, in order to correctly reconstruct the new reference pictures. When using RMGT, it is necessary to transmit the GT coefficients, the amount of data depends on which number of DoF used to perform the matching.

### 5.1.2 K-Means+VSRS

The second approach consists on using the 3D scene information to generate the reference pictures that compensate the disparity of each region. The 3D scene information includes both camera parameters, and the centroids selected by the K-Means method.

The camera parameters are used to map world coordinates (3D) onto pixel coordinates (2D grid). There are two types of camera parameters: extrinsic and intrinsic. Extrinsic camera parameters describe the position and orientation of the camera, relative to the world. Thus, the world coordinates $\left[x_{w}, y_{w}, z_{w}\right]$ can be mapped onto camera coordinates [ $x_{c}, y_{c}, z_{c}$ ], using the same principle as in homogeneous coordinates, by a $4 \times 4$ matrix:

$$
\left[x_{c}, y_{c}, z_{c}, 1\right]=\left[x_{w}, y_{w}, z_{w}, 1\right]\left[\begin{array}{cccc}
r_{11} & r_{12} & r_{13} & t_{1}  \tag{5.1}\\
r_{21} & r_{22} & r_{23} & t_{2} \\
r_{31} & r_{32} & r_{33} & t_{3} \\
0 & 0 & 0 & 1
\end{array}\right]
$$

The orientation and position of the camera relative to the world is described in (5.1) by $R$ ( $3 \times 3$ matrix) and $T$ ( $3 \times 1$ matrix), respectively. Parallel camera setups usually present the same orientation as world coordinates in order to simplify the calculations, in this case $R=I_{3}$.

In order to convert 3D camera coordinates to a 2D grid of pixels, another transformation is performed using the intrinsic camera parameters:

$$
\left[x_{\text {pixel }}, y_{\text {pixel }}, 1\right]=\left[x_{c}, y_{c}, z_{c}\right]\left[\begin{array}{ccc}
\alpha_{x} & s & p_{x}  \tag{5.2}\\
0 & \alpha_{y} & p_{y} \\
0 & 0 & 1
\end{array}\right] .
$$



Figure 5.2: Example of the method where K-Means clustering and RMGT are combined to generate new reference pictures for MV-HEVC.

The matrix on (5.2) is also known as calibration matrix. The values of $\alpha_{x}$ and $\alpha_{y}$ represent the focal length in terms of pixels. As pixels are not always perfectly square, the $s$ factor is used to shear the pixels to a square format. The principal point of the camera, ideally in the middle of the plane, is given by $p_{x}$ and $p_{y}$. At this point, the relation between world coordinates $\left[x_{w}, y_{w}, z_{w}\right]$ and the pixels of a picture $\left[x_{p i x e l}, y_{p i x e l}\right]$ can be found. By considering this relation in a two camera setup, it is possible to create a projection of the left view onto the right camera perspective. This process is referred to as synthesis.

In this approach the complete depth map is not available at the decoder. Depth is only being used as additional information about the 3D scene at the encoders side, it is not encoded and transmitted. Also a depth sensor is not imperative because the depth map can be generated using a disparity map and the camera parameters. The depth map was used for sake of simplicity.

Alternatively to transmit the depth map, only the centroids generated by K-Means are transmitted, representing the key depth planes of the 3D scene. The centroids, camera parameters and the left view are used to generate a projection onto the right view. The VSRS [37] (View Synthesis Reference Software) was used to perform the projection, due to the fact that is capable of performing synthesis on both parallel and convergent camera arrays. This software is used to map the left camera 2D grid onto the 3D world, where the coordinates are common to any point of view, and then project those points to a 2 D grid that is in a different point of view (right camera position). The centroids are used as
depth maps for the VSRS, where each one represents a plane parallel to the camera as it is shown in Figure 5.3.

The depth values represented on Figure 5.3 are 82, 111 and 143. The first value represents a region that is further away from the camera, and the last value represents a value that is closer to the camera. Notice that, the region on the left side of the second and third picture, are the occlusions, unknown pixels. Also the size of that region is related with the amount of disparity that was compensated. The third picture represents the disparity compensation of the region including the man, the disparity is higher than in the first picture where the key region is the background. This approach that combines K-Means clustering and VSRS is shown in Figure 5.4.

In the case of the VSRS method, it is only necessary to send the centroid values. However, the VSRS method can also be implicit, if instead of estimating the centroids with K-Means clustering, the centroids are assumed to be uniformly distributed e.g. 32, 96, 160 and 224 (for 4 regions).

### 5.1.3 Experimental results

The proposed methods have been tested using version 10.0 of the reference software HTM, with a random access prediction structure. Four pairs of test sequences where used, Ballet (cameras 2 and 0 ), Breakdancers (cameras 2 and 0), Balloons (cameras 1 and 3) and Kendo (cameras 1 and 3). The first two use a convergent camera array and the remaining use parallel camera arrangement. Encoding 24 frames of each sequence, using four QPs, 23, 28, 33 and 38, the quality of the results is measured using the Bjoontegard delta metrics [38]. The PSNR and bitrate achieved when compressing the non-base view, corresponds to the right view, using the original HTM reference software, and HTM using the extra GT reference frames.

Both proposed methods were tested using 1 or 3 regions, resulting in 1 or 3 extra reference pictures for inter-view prediction. The K-Means+RMGT method was tested using either 2 Dof or 8 Dof using the bilinear transform. The VSRS method was tested using K-Means to generate the centroids and using uniformly spaced centroids. Some additional data may be transmitted to the decoder to generate the extra reference frames. The amount of necessary data is shown on Table 5.1. The $n r$ value corresponds to the number of regions, the 16 bit value corresponds to the size of a vector with a precision of 8 bits for each dimension. In the case of K-Means+VSRS 8 bits is the precision of the centroids.

The experimental results for the chosen methods is shown in Table 5.2. The results marked with bold are the positive results, where there exits PSNR gains and Bitrate savings.


Figure 5.3: Example of VSRS output for the same picture using different depth planes.

| Method | Bits | Region update |
| :---: | :---: | :---: |
| K-Means + RMGT 2 DoF | $16 \times n r$ | every second |
| K-Means + RMGT 8 DoF | $16 \times 4 \times n r$ | every second |
| K-Means + VSRS | $8 \times n r$ | every frame |
| Uniform + VSRS | 0 | no update |

Table 5.1: Number of transmitted extra bits, necessary to reconstruct the GT reference frames at the decoder.


Figure 5.4: Example of the method where K-Means clustering and VSRS are combined to generate new reference pictures for MV-HEVC.

|  | Sequences |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ballet |  | Breakdancers |  | Balloons |  | Kendo |  |  |
| regions <br> Methods | 1 | 3 | 1 | 3 | 1 | 3 | 1 | 3 |  |
| K-Means+VSRS | $\begin{gathered} \hline 0.05 \\ -1.48 \end{gathered}$ | $\begin{gathered} \hline 0.06 \\ -1.96 \end{gathered}$ | $\begin{gathered} 0.01 \\ -0.30 \end{gathered}$ | $\begin{gathered} -0.01 \\ 0.37 \end{gathered}$ | $\begin{gathered} \hline-0.02 \\ 0.62 \end{gathered}$ | $\begin{gathered} -0.05 \\ 1.38 \end{gathered}$ | $\begin{gathered} \hline 0.01 \\ -0.35 \end{gathered}$ | $\begin{aligned} & \hline 0.00 \\ & 0.04 \end{aligned}$ | $\begin{gathered} \hline \text { PSNR } \\ \text { BD (\%) } \end{gathered}$ |
| Uniform+VSRS | $\begin{gathered} 0.09 \\ -2.87 \end{gathered}$ | $\begin{gathered} 0.08 \\ -2.60 \end{gathered}$ | $\begin{gathered} 0.01 \\ -0.31 \end{gathered}$ | $\begin{gathered} -0.01 \\ 0.16 \end{gathered}$ | $\begin{gathered} -0.01 \\ 0.09 \end{gathered}$ | $\begin{gathered} -0.06 \\ 1.60 \end{gathered}$ | $\begin{gathered} 0.05 \\ -1.52 \end{gathered}$ | $\begin{gathered} 0.02 \\ -0.61 \end{gathered}$ | $\begin{gathered} \text { PSNR } \\ \text { BD (\%) } \end{gathered}$ |
| RMGT 2 DoF | $\begin{gathered} -0.01 \\ 0.58 \end{gathered}$ | $\begin{gathered} -0.05 \\ 1.02 \end{gathered}$ | $\begin{aligned} & 0.00 \\ & 0.66 \end{aligned}$ | $\begin{gathered} -0.03 \\ 1.33 \end{gathered}$ | $\begin{gathered} 0.00 \\ -0.01 \end{gathered}$ | $\begin{gathered} -0.04 \\ 1.02 \end{gathered}$ | $\begin{gathered} 0.04 \\ -1.02 \end{gathered}$ | $\begin{gathered} 0.01 \\ -0.36 \end{gathered}$ | $\begin{gathered} \text { PSNR } \\ \text { BD (\%) } \\ \hline \end{gathered}$ |
| RMGT 8 DoF | $\begin{gathered} -0.02 \\ 0.84 \end{gathered}$ | $\begin{aligned} & \hline 0.00 \\ & 0.29 \end{aligned}$ | $\begin{gathered} -0.02 \\ 0.82 \end{gathered}$ | $\begin{gathered} -0.02 \\ 0.95 \end{gathered}$ | $\begin{gathered} \hline-0.01 \\ 0.04 \end{gathered}$ | $\begin{gathered} \hline-0.07 \\ 1.79 \end{gathered}$ | $\begin{gathered} 0.04 \\ -0.98 \end{gathered}$ | $\begin{gathered} \hline 0.01 \\ -0.22 \end{gathered}$ | $\begin{gathered} \hline \text { PSNR } \\ \text { BD }(\%) \end{gathered}$ |

Table 5.2: Experimental results using both RMGT and VSRS proposed methods for 1 and 3 regions.

The experimental results show that, in general using the 3D scene information to generate disparity compensated pictures is better than using a distortion based method such as RMGT 8 DoF. This fact is most noticeable when using convergent camera array sequences such as Ballet or Breakdancers. In this cases the VSRS results show bitrate savings, but RMGT always needs more bits to achieve a similar result. This happens regardless of the fact that RMGT produces reference pictures that are more similar to the picture that is being encoded.

RMGT 2 DoF remains competitive against VSRS methods, for parallel camera setups, because it performs a simple transformation (translation) that works like a global disparity value and also the amount of extra bits is relatively low e.g. 32 and 96 bits per second for 1 and 3 regions, respectively. Also RMGT 2 DoF achieves the best results for Balloons sequence among the remaining techniques. As expected, for convergent camera arrays, the 2 DoF are not enough to generate useful reference pictures.

Regarding the two methods that select the centroids for VSRS, Uniform and K-Means, one is implicit and the other is explicit. This means that when using the Uniform method no extra bits are needed because the centroids are determined implicitly and are dependent on the number of regions. The clear advantage in terms of data transmission is noticed on the results because in most cases the resulting centroids are similar in both methods. However in some cases even not considering the extra bits for the K-Means method, the Uniform is still superior. This particular case occurs more frequently on Ballet and Kendo with one region only. When using the K-Means method on one region the result is not very accurate because it represents a mean value of the depth map. The K-Means tends to be more accurate when using a higher number of regions.

The new reference pictures demonstrate to have potential to improve the MV-HEVC encoding performance. However, when introducing the pictures in the reference list, some overhead added for signalling these new reference pictures. Nevertheless not all reference pictures may be necessary every time in the encoding process.

### 5.2 Optimized Reference List

In order to improve previous results, the number and order of the pictures that are added to the reference list was optimized. Pictures that are added to the list are not always useful and therefore have different importance among in the prediction structure. When encoding the first pictures of the enhancement view not always near temporal references exist. Table 5.3 shows the reference pictures POC (Picture Order Count) used for each picture of the first nine frames of the enhancement view. Note that POC represents the visualization order of the pictures.

| POC | 0 | 8 | 4 | 2 | 1 | 3 | 6 | 5 | 7 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | MV | 0 | 0 | 0 | 0 | 0 | 2 | 0 | 4 |
|  | N GT | MV | 8 | 4 | 2 | 2 | 4 | 4 | 6 |
| References |  | N GT | MV | 8 | 4 | 4 | 8 | 6 | 8 |
|  |  |  |  | N GT | MV | MV | 8 | MV | 8 |
|  |  |  |  | N GT | N GT | MV | N GT | MV | N GT |
|  |  |  |  |  |  | N GT |  | N GT |  |

Table 5.3: Reference pictures, by POC (Picture Order Count), used to encode the enhancement view.

In order to maximize the efficiency the reference picture must be as close as possible to the current picture. Notice that, on Table 5.3 the first frame (POC 0 ) only has interview references, the MV (Main view) reference and $N$ GT pictures. The second frame already has temporal references. However such reference occurs 8 frames earlier in the video sequence. This distance between the current picture and the reference picture may compromise the efficiency of the encoding process, depending on the video content. This distance between the reference and the current picture is only 2 . The usefulness of the inter-view reference pictures may be therefore higher on the first frames of the GOP and lower for the last frames. Figure 5.5 shows the usage of GT reference pictures for the Ballet and Balloons sequences.

As shown in Figure 5.5, the highest usage for both sequences is on the first frames of the GOP. These examples where chosen because they achieved the highest and the lowest results on the previous experimental tests, respectively. Notice that in the case of Ballet sequence non of the GT references is used, however in the Balloons case this happens in several pictures for every GT reference. On convergent camera array sequences like Ballet, the inter-view prediction usage is normally very low when compared to parallel camera array sequences. This difference in inter-view prediction usage is due to the existing


Figure 5.5: Usage of the GT reference pictures on the Ballet and Balloons sequences.
disparity on both types of camera arrangements, where in the case of convergent cameras is much more complex. Since in some cases not all references are being used, unnecessary overhead is being added to the encoding process.

The encoding loop has two steps, the coding optimization and the encoding step. The coding optimization step is where all the possible decisions in terms of block structure, intra and inter prediction are tested and chosen using RDO, where a cost function (5.3) is minimized.

$$
\begin{equation*}
J=D+\lambda R \tag{5.3}
\end{equation*}
$$

Where $D$ is the distortion, $\lambda$ is the Lagrangian multiplier, related to the QP, $R$ is the rate and $J$ is the resultant cost. After this step, each CU has an associated cost that is the minimum possible value among all possible decisions.

The encoding step is where those decisions are gathered and used to encode the video sequence creating a stream.

The encoding loop has been modified, such that after the coding optimization step all the cost values for each CU are gathered in order to analyse the importance of each reference picture. The goal is to estimate the cost $J$ per pixel associated with each reference. Using this information and the usage of each reference picture, the reference pictures that are used less than a $1 \%$ threshold, are removed from the list. The remaining pictures are reordered in an ascendant order of cost, because the first pictures on the list are encoded using less bits than the last positions. This method is more thoroughly explained as follows:

Every CU has a cost value referent to $64 \times 64$ pixels $\left(J_{C U}\right)$. Each CU has 256 elements of $4 \times 4$ pixels, associated with a reference picture if inter prediction was used. For each CU the cost per reference frame is calculated according to Equation 5.4.

$$
\begin{equation*}
J_{C U r}=\frac{J_{C U} \times \text { elem }_{r}}{256} \tag{5.4}
\end{equation*}
$$

Considering the number of elements using each reference picture elem ${ }_{r}$, where $r$ represents the index of the GT reference picture. $J_{C U r}$ is an estimate cost for the reference picture $r$ for that CU.

By adding all the cost contributions, of every $N$ CUs, for a reference picture, and dividing it by the total number of pixels compensated using that reference picture, the cost per pixel is calculated for each reference picture (Equation 5.5).

$$
\begin{equation*}
J_{r}=\frac{\sum_{n=1}^{N} J_{C U r}}{\sum_{n=1}^{N} \text { elem }_{r} \times 4 \times 4} \tag{5.5}
\end{equation*}
$$

This $J_{r}$ represents both the necessary cost to use the reference picture and the amount of compensated pixels. Therefore the lowest the value the higher the quality of the reference picture is considered.

The inter-view reference pictures, including the inter-view reference that is not geometrically compensated, are classified using this process. After being classified the inter-view reference pictures are first reordered in a crescent order of $J_{r}$ and the ones with a pixel usage lower than $\% 1$ are discarded. The coding optimization step is repeated with the changes in the reference picture lists. The resultant global cost of the encoding process is compared with the one achieved in the first run of the coding optimization step. The inter-view reference picture selection that achieves the lowest global cost is chosen to be transmitted in the encoding step.

Moreover, the disparity estimation performed by MV-HEVC was disabled for the interview reference pictures for parallel camera array sequences. Since this case is simpler than the convergent camera arrays, the reference pictures are enough to provide global disparity compensation. This way the disparity vectors are always null when using these reference pictures. Moreover, experimental results confirm the improved efficiency.

### 5.2.1 Experimental results

The experimental results where obtained with the same experimental setup as before. However in these experiments every possible number of regions between 1 and 4 was tested. Also a new variation of K-Means+VSRS method is introduced, the K-MeansTUC+VSRS (Temporal Updated Centroids), where the centroids are updated only once a second, instead of once a frame. The RMGT 8 DoF was not tested because it has been proven to be inefficient, when compared with VSRS based methods.

The experimental results for convergent and parallel camera array sequences are shown in Table 5.4 and 5.5, respectively. The results marked with bold are the positive results where it is achieved PSNR gain and Bitrate saving.

Table 5.4 and 5.5 shows that, all the results have been improved with the introduction of the reference list optimization. Since the overhead is reduced the same methods are allowed to use more regions and still manage to achieve bitrate savings e.g. the bitrate saving increase of $1 \%$ in Kendo sequence for 3 regions. Also, almost all negative results have been mitigated, because the reference pictures are only used when necessary.

|  | Sequences |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Ballet |  |  |  | Breakdancers |  |  |  |  |
| regions | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 |  |
| K-Means+VSRS | 0.05 | 0.05 | 0.07 | 0.08 | 0.01 | 0.01 | -0.01 | -0.01 | PSNR |
|  | -1.76 | -1.58 | -2.09 | -2.46 | -0.40 | -0.24 | 0.23 | 0.46 | BD (\%) |
| Uniform+VSRS | 0.10 | 0.09 | 0.09 | 0.08 | 0.01 | 0.01 | 0.00 | 0.00 | PSNR |
|  | -3.06 | -2.95 | -2.92 | -2.81 | -0.43 | -0.33 | 0.01 | -0.10 | BD (\%) |
| K-Means-TUC+VSRS | 0.06 | 0.06 | 0.07 | 0.09 | 0.01 | 0.01 | 0.01 | 0.00 | PSNR |
|  | -2.20 | -2.20 | -2.34 | -3.05 | -0.39 | -0.43 | -0.39 | 0.34 | BD (\%) |

Table 5.4: Experimental results using both VSRS proposed methods for 1, 2, 3 and 4 regions on convergent camera array sequences.

|  | Sequences |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Balloons |  |  |  | Kendo |  |  |  |  |
| regions | 1 | 2 | 3 | 4 | 1 | 2 | 3 | 4 |  |
| K-Means+VSRS | 0.00 | -0.01 | -0.04 | -0.02 | 0.07 | 0.06 | 0.03 | 0.01 | PSNR |
|  | 0.02 | 0.23 | 0.97 | 0.64 | -1.84 | -1.65 | -0.91 | -0.43 | BD (\%) |
| Uniform+VSRS | 0.01 | 0.01 | -0.01 | -0.02 | 0.07 | 0.06 | 0.05 | 0.03 | PSNR |
|  | -0.21 | -0.22 | 0.28 | 0.56 | -2.00 | -1.65 | -1.41 | -0.74 | BD (\%) |
| K-Means-TUC+VSRS | 0.01 | 0.01 | 0.01 | 0.01 | 0.05 | 0.05 | 0.04 | 0.05 | PSNR |
|  | -0.28 | -0.32 | -0.20 | -0.06 | -1.40 | -1.43 | -1.31 | -1.32 | BD (\%) |
| RMGT 2 DoF | 0.01 | 0.00 | -0.01 | -0.03 | 0.05 | 0.05 | 0.06 | 0.05 | PSNR |
|  | -0.18 | -0.07 | 0.19 | 0.82 | -1.44 | -1.47 | -1.66 | -1.31 | BD (\%) |

Table 5.5: Experimental results using both RMGT 2 DoF and VSRS proposed methods for $1,2,3$ and 4 regions parallel camera array sequences.

The K-Means+VSRS method, was implemented to be more accurate in terms of describing the 3D scene than the uniform selection. Nevertheless, since it has to transmit extra bits for the centroids to be available on the decoder side, it becomes less efficient. By choosing only the most useful reference pictures the bitrate saving improved between $0.2 \%$ and $1.5 \%$. However, in most cases the centroid values did not change that much on every frame. This led to the development of TUC in which the centroids are updated only once a second. K-Means+VSRS achieves a high efficiency improvement when this change is applied. Almost all results improve the bitrate savings, up to $0.7 \%$.

The fact that the K-Means-TUC+VSRS and the Uniform+VSRS methods have the best overall results shows that the necessary accuracy for the centroid selection is not very high. The tradeoff between precision and extra bits is achieved by K-Means-TUC+VSRS which obtained almost no negative results for all test sequences and number of regions.

The only drawback of this method is the increase in computational complexity, because the coding optimization step contributes for most complexity of the encoding loop. Also each one of the included reference pictures adds computational complexity because the encoder has to test disparity compensation for all reference pictures. However in order to reduce the increasing computational complexity instead of running the full coding optimization step twice, partial coding optimization steps could be tested, only on $64 \times 64$ blocks for example.

## Chapter 6

## Conclusions

The most recent video coding standard, HEVC, has been developed to be more efficient than its predecessors, when encoding pictures HD and ultra HD resolutions. The increased efficiency has been achieved using mostly the same architecture as its predecessors.

HEVC extensions like MV-HEVC and 3D-HEVC provide coding tools that can improve the coding efficiency, however they depend on the application. MV-HEVC extension can be used for multiview inputs where inter view prediction is applied to non base views. 3DHEVC extension encodes a video-plus-depth format where more advanced coding tools are used. These tools include improved inter view prediction and tools specific to depth maps. Depending on the application it may be necessary to implement a simpler codec like MV-HEVC or a more efficient codec like 3D-HEVC.

Even in the most recent multiview extensions, motion and disparity are estimated using a technique like BMA. The resulting disparity is described by a disparity vector. However, this algorithm assumes that all pixels in a block have the same disparity, and are accurately described by a translation. Disparity estimation can benefit from the use of more complex transformations.

In order to improve the matching algorithm, various geometric transforms have been studied. Geometric transforms based on projective transform can have between 2 and 8 DoF. The higher the number of DoF the higher the number of coefficients that are necessary to represent the geometric transform. An alternative geometric transform, the bilinear transform, has been studied as well. This transform has the same 8 DoF as the projective transform, however the computational cost is lower. The bilinear transform was chosen to be used as one of the proposed methods geometric transform for this reason.

When combining geometric transforms with a matching algorithm, two types of approaches have been tested: block and region based approaches. On the block base approach instead of using one vector to represent disparity, four vectors are used, one for each corner of the block. In order to improve the matching precision, instead of trans-
forming the block, a grid surrounding the block is transformed. Since the grid has a larger size than the block and the vectors are on the corners of the grid a precision equivalent to fractions of pixels can be achieved on the block region. However even using fast search methods like TSS to find the best match coefficients, the BMGT has proven to be very computational expensive. For this reason the number of matching possibilities used by the fast search method was reduced. The results that achieve lower distortions for the computational cost where using a grid size 128 times the size of the block and limiting the TSS to only three step sizes.

Since BMGT generates a considerably high amount of coefficients that have to be transmitted as side information in order to correctly reconstruct the predicted blocks, RMGT was implemented. RMGT uses the same basis of BMGT although using a region based approach. By segmenting the picture into a limited number of regions and compensating disparity on each region using a vector on each corner much less side information is necessary. However, as expected the reconstructed images have higher distortion compared with BMGT results.

The integration of the proposed method was done on MV-HEVC using a combination of techniques to generate new reference pictures to improve the inter view prediction for the non-base views. The first combination of techniques was the K-Means+RMGT using 2 and 8 DoF, where K-Means was used to segment the picture and RMGT to generate the coefficient parameters. The second technique was K-Means+VSRS where the generated centroids by K-Means are used to identify the key depth planes. VSRS was used to project the base view into the non-base view perspective. A variation of this method, Uniform+VSRS, was also tested where the centroids are implicit. Experimental results show potential to improve MV-HEVC encoding performance achieving bitrate savings of $2.87 \%$ for a convergent camera sequence and $1.52 \%$ parallel camera sequence using Uniform+VSRS. However the overhead that was being added by each picture even when some pictures were not being used affected the results.

In order to prevent the unnecessary overhead produced by adding reference pictures that were not being used an optimization method was created to selected the most useful reference pictures. By analysing the achieved cost per pixel for each reference picture, the pictures are reorder within the list and the pictures that are not used are removed. The encoding optimization step is repeated with the optimized choices in terms of reference pictures. Experimental results show improvements in all previous tests achieving bitrate savings of $3.06 \%$ for a convergent camera sequence and $2 \%$ parallel for camera sequences using Uniform+VSRS. Moreover a variation of K-Means+VSRS method was also tested where the centroids are reset only once a second reducing the necessary side information. Experimental results has shown that K-Means-TUC+VSRS remains competitive against Uniform+VSRS and in some cases when the number of regions is higher achieves better
results.
Future work includes further study of the optimization process of the pictures added to the reference picture list. As well as reducing the extra amount of computational complexity added by this process.

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## Appendix A

## Contributions

## A. 1 Conferences

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