



## A Model for Designing Adaptive Laboratory Evolution Experiments

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1 A Model for Designing Adaptive Laboratory Evolution Experiments

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9 Running Head: Designing Adaptive Laboratory Evolution Experiments

10

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12 **Abstract**

13 The occurrence of mutations is a cornerstone of the evolutionary theory of adaptation,  
14 capitalizing on the rare chance that a mutation confers a fitness benefit. Natural selection is  
15 increasingly being leveraged in laboratory settings for industrial and basic science applications.  
16 Despite an increasing deployment, there are no standardized procedures available for designing  
17 and performing adaptive laboratory evolution (ALE) experiments. Thus, there is a need to  
18 optimize the experimental design, specifically for determining when to consider an experiment  
19 complete and for balancing outcomes with available resources (i.e., lab supplies, personnel, and  
20 time). To design and better understand ALE experiments, a simulator, ALEsim, was developed,  
21 validated, and applied to optimize ALE experimentation. The effects of various passage sizes  
22 were experimentally determined and subsequently evaluated with ALEsim to explain differences  
23 in experimental outcomes. Further, a beneficial mutation rate of  $10^{-6.9}$ - $10^{-8.4}$  mutations per cell  
24 division was derived. A retrospective analysis of ALE experiments revealed that passage sizes  
25 typically employed in serial passage batch culture ALE experiments led to inefficient production  
26 and fixation of beneficial mutations. ALEsim and the results herein will aid in the design of ALE  
27 experiments to fit the exact needs of the project while taking into account the tradeoff in  
28 resources required, and lower the barrier of entry to this experimental technique.

29

30 Importance

31 Adaptive laboratory evolution (ALE) is a widely used scientific technique to increase scientific  
32 understanding, as well as create industrially relevant organisms. The manner in which ALE  
33 experiments are conducted is highly manual and uniform with little optimization for efficiency.  
34 Such inefficiencies result in suboptimal experiments that can take multiple months to complete.  
35 With the availability of automation and computer simulations, we can now perform these  
36 experiments in a more optimized fashion and design experiments to generate greater fitness in a  
37 more accelerated time frame, thereby pushing the limits of what adaptive laboratory evolution  
38 can achieve.

39

40 Highlights

- 41 - A tunable simulator, ALEsim, was constructed to simulate observed fitness increases in  
42 ALE experiments
- 43 - A control ALE experiment was performed to determine an observed beneficial mutation  
44 rate and quantify the effect of passage size in an ALE experiment – the beneficial  
45 mutation rate (BMR) is consistent with previous estimates
- 46 - A retrospective analysis of ALE experiments revealed limitations in experimental  
47 designs.
- 48 - ALEsim can be leveraged to optimize resources and time needed to conduct an ALE  
49 experiment by determining tradeoffs between a likely fitness increase and an increased  
50 run time

51

## 52 Introduction

53 Adaptive laboratory evolution (ALE) has been performed *in vitro* for decades and the field is  
54 expanding. ALE involves subjecting a population of organisms to a given environment, in the  
55 lab, and allowing natural selection to increase the overall fitness of the population. In laboratory  
56 settings, this is typically performed with organisms possessing short generation times. The basic  
57 principles governing ALE experiments are easily understood across a breadth of disciplines,  
58 which has led to its adoption in many laboratories (1, 2). The recent growth in the use of ALE  
59 can be attributed to the ease of access and decreasing costs of genome sequencing (3-5). Falling  
60 sequencing costs have led to the increased investigation of genomic, transcriptomic, and  
61 additional omics data types over the course of evolution (5). While the analysis of ALE  
62 experiments has grown, the manner in which the ALE experiments themselves are performed has  
63 remained relatively *ad hoc*. The most commonly employed techniques are chemostat adaptation  
64 and serially passaged batch culture adaptation, with batch culture adaptation being more popular  
65 as it is easily expanded and does not require setting up complex machinery (3, 6).

66 A primary attribute of any ALE experiment is the selection pressure imposed on the culture. The  
67 selection pressure (i.e., exponential growth, biomass yield, stationary phase, or lag phase) is  
68 responsible for the outcome of the evolution study (4, 7-10). For example, in a 24hr serially  
69 passaged batch culture ALE experiment with fast growing bacteria, the culture is subjected to  
70 alternating environments of feast and famine. At the beginning of each batch there are excess  
71 nutrients but inevitably, within 24hrs, the nutrients are consumed and stationary phase is reached.  
72 Because of this alternating environment, the selection pressure is complex and fitness is achieved  
73 through various methods (e.g., stationary phase fitness, lag phase duration, and growth rate all  
74 contribute) (9). This complexity often confounds the analysis depending on the application. To

75 alleviate complexity, the cells can be kept in one phase (e.g. exponential phase) to mitigate most  
76 of the alternating selection and focus selection specifically on fitness gains through growth rate.  
77 In such cases, fitness will be treated as interchangeable with growth rate. The desired outcome of  
78 the experiment would dictate the ideal selection pressure to be imposed and thereby the  
79 experimental design, but the difference between the two designs is non trivial.

80 There are several parameters that affect the outcome of a serially passaged batch culture ALE  
81 experiment. A primary parameter involved is the passage size (11-13). Specifically, passage size  
82 determines how much of the population is allowed to propagate to each subsequent batch culture.  
83 If a beneficial mutation occurs, but is lost when the bottleneck is imposed, the rate of evolution  
84 can be slowed or even halted. Since smaller passage sizes can hinder the rate of evolution, it is  
85 often easier to perform a serially passaged batch culture ALE under alternating environments of  
86 feast and famine where a change in passage size only effects the duration of growth and  
87 stationary phases. However, if the application requires exponential phase passaging, a change in  
88 passage size also changes the time when the culture must be passaged. Because of this, the  
89 passage size is often dictated by an individual's schedule. Typically, the time in between  
90 passaging can be no shorter than ~12hrs. Consequentially, as the culture adapts and begins to  
91 grow faster, the passage size must be decreased. As an example, a previous study adapting *E.*  
92 *coli* to glycerol in 250mL batches started with a passage size of approximately 100 $\mu$ L and by  
93 experiment's end was less than 0.1 $\mu$ L (14). A more in-depth retrospective analysis revealed  
94 similar trends where passage amounts were significantly decreased (14-18). In these studies, the  
95 reduction in population size, or bottleneck, (i.e., passage size) became so significant that the  
96 calculated number of cells being passed was on the order of 10 or even occasionally 1. The  
97 chance of capturing a beneficial mutation, when only passing tens of cells from a culture of

98 millions, is practically null over a reasonable timeframe. At this point, continuing the experiment  
99 is futile. The question then becomes at what point is the passage size too low?

100 Passage size can have a large impact on the trajectory of an ALE experiment. This can be seen in  
101 the comparison of two studies that evolved wild-type *E. coli* K-12 MG1655 on M9 glucose  
102 minimal media (7, 18). One study (7) used a consistent passage size of 800 $\mu$ L from 25mL  
103 batches on an automated platform. The second study (18) was done “by hand” and had widely  
104 varying passage sizes that were considerably smaller than the automated study. The outcomes of  
105 the ALE experiments were quite distinct. The final growth rates achieved were  $1.00\pm 0.24$  hr<sup>-1</sup>  
106 and  $0.79\pm 0.01$  hr<sup>-1</sup> in the consistent and variable passage size studies, respectively. The apparent  
107 lack of fitness achieved in variable passage study was not due to a lack of available beneficial  
108 mutations (as the same strains and culturing conditions were used), but rather insufficient  
109 experimental design to find and fix them in a reasonable amount of time. Understanding why  
110 these two outcomes differ is imperative to the efficient design of ALE experiments.

111 Theoretical studies have looked at the effect of passage size on serially passaged batch culture  
112 adaptation and resulted in varying predictions of an ideal passage size depending on the model  
113 used (19, 20). The ideal passage sizes calculated are ideal from a mathematical standpoint. This  
114 essentially gives the best chance for various mutations of different selective advantages to fix in  
115 a population. The ideal passage sizes calculated in these studies are relatively large (13.5% and  
116 20%)(19, 20). As mentioned previously, a larger passage necessitates an increase in resources.  
117 More specifically, the resources required increase exponentially with passage size, yet the gains  
118 slowly diminish. This work thus focuses on examining the diminishing returns in the context of  
119 the desired result and the resources available. We set out to examine the impact of the key ALE  
120 parameter: passage size. To address this, we created an *in silico* evolutionary model that

121 simulates the dynamics of capturing and fixing beneficial mutations in the context of an  
122 exponentially-passed batch culture ALE experiment. After building the model, we parameterize  
123 it using a combination of 30 independent ALE experiments of *E. coli* on glycerol minimal media  
124 across five different passage sizes (10%, 1%, 0.1%, 0.01%, and 0.001%). Using the  
125 parameterized model, we investigated the biological consequences of changing passage sizes and  
126 how close to optimal a given experiment is. With this knowledge, an experiment can be designed  
127 to fit the desired outcome, giving consideration to the resources required to achieve it, and the  
128 feasibility of performing such an experiment.

129



## 130 **Materials and Methods**

### 131 **Adaptive Laboratory Evolution**

132 Adaptive laboratory evolutions were started from wild-type *E. coli* strain MG1655  
133 (ATCC47076) glycerol frozen stock and grown up overnight in 15mL magnetically stirred 0.2%  
134 glycerol M9 minimal media supplemented with trace elements. The magnet was stirred at  
135 1150rpm, sufficient for completely aerobic growth. 30 experiments were started from 150 $\mu$ L  
136 aliquots from the overnight pre-culture. The experiments were subsequently grown in identical  
137 vessels and media as the pre-culture. Culture optical densities at 600nm (OD) were monitored  
138 over the course of each batch culture. When the culture reached an OD of 0.300 ( $\pm$ 10%) as  
139 measured by a plate-reader with 100 $\mu$ L sample volume in a 96 well flat bottom microplate, an  
140 aliquot was taken and passed to a new batch culture filled with sterile media. An OD of 0.300  
141 was chosen to preclude reaching stationary phase in any of the cultures and ensures OD  
142 measurements have not begun to saturate. Growth rates of each culture were determined using  
143 OD measurements taken over the lifetime of each batch culture.

### 144 **Media**

145 All cultures were grown in 0.2% glycerol M9 minimal media. The media consisted of 0.2%  
146 glycerol by volume, 0.1mM CaCl<sub>2</sub>, 2.0mM MgSO<sub>4</sub>, Trace element solution and M9 salts. 4000X  
147 Trace element solution consisted of 27g/L FeCl<sub>3</sub>\*6H<sub>2</sub>O, 2g/L ZnCl<sub>2</sub>\*4H<sub>2</sub>O, 2g/L CoCl<sub>2</sub>\*6H<sub>2</sub>O,  
148 2g/L NaMoO<sub>4</sub>\*2H<sub>2</sub>O, 1g/L CaCl<sub>2</sub>\*H<sub>2</sub>O, 1.3g/L CuCl<sub>2</sub>\*6H<sub>2</sub>O, 0.5g/L H<sub>3</sub>BO<sub>3</sub>, and Concentrated  
149 HCl dissolved in ddH<sub>2</sub>O and sterile filtered. 10x M9 Salts solution consisted of 68g/L Na<sub>2</sub>HPO<sub>4</sub>  
150 anhydrous, 30g/L KH<sub>2</sub>PO<sub>4</sub>, 5g/L NaCl, and 10g/L NH<sub>4</sub>Cl dissolved ddH<sub>2</sub>O and autoclaved. Final  
151 concentrations in the media were 1x.

152 **DNA Sequencing**

153 Genomic DNA was isolated using Macherey-Nagel NucleoSpin® Tissue kit. The quality of  
154 DNA was assessed with UV absorbance ratios using a Nano drop. DNA was quantified using  
155 Qubit dsDNA High Sensitivity assay. Paired-end resequencing libraries were generated using  
156 Illumina's Nextera XT kit with 700 pg of input DNA total. Sequences were obtained using an  
157 Illumina Miseq with a MiSeq 600 cycle reagent kit v3. The breseq pipeline version 0.23 with  
158 bowtie2 was used to map sequencing reads and identify mutations relative to the *E. Coli* K12  
159 MG1655 genome (NCBI accession NC\_000913.2) (21). All samples had an average mapped  
160 coverage of at least 25x.

161 **Computer Modeling**

162 Modeling of simulations was computed using MATLAB 2015b on a Windows 7 professional  
163 platform. Detailed descriptions are found as comments in the supplemental m-files. The  
164 beneficial mutation rate was computed by a maximum likelihood estimation. It was calculated  
165 for making a transition from State 1 to State 2 and State 2 to State 3 for passage sizes of 0.01%  
166 and 0.001%. These passage size were chosen as they were the only ones that showed a  
167 distribution of states achieved. The transition from State 1 to State 2 was capped at 20 days to  
168 give a maximally distributed data set. The transition from State 2 to State 3 was started by  
169 assuming that State 2 was already achieved. Thus, the length of time simulated was started based  
170 of when State 2 was achieved. This was variable for different experiments.

171 A value of  $1.55 \times 10^{12}$  cells·L<sup>-1</sup>· OD<sub>600nm</sub><sup>-1</sup> was used to estimate the number of cells in a culture  
172 for a given OD<sub>600nm</sub> with a 1 cm path length cuvette for the purposes of ALEsim. A standard  
173 curve relating the ODs measured in the plate reader with a 100µL sample volume in a 96 well

174 flat bottom microplate to the OD measured with a 1 cm cuvette to obtain a ratio of 3.15 for  
175 equivalent measurements between the two. The biomass (grams of dry weight) per OD<sub>600nm</sub> per  
176 volume was calculated by filtering known volumes of cultures at specific ODs through 0.22µm  
177 filters. The filters were weighed before and after filtering and drying to obtain the total dry  
178 weight of the culture. The differences in these values was used to calculate ratio of 0.45·gDW L<sup>-1</sup>  
179 ·OD<sub>600nm</sub><sup>-1</sup>. The dry mass per cell has previously been reported as 2.9×10<sup>-13</sup>gDW·cell (22). The  
180 quotient of these two values gives our final conversion factor of 1.55×10<sup>12</sup> cells·L<sup>-1</sup>·OD<sup>-1</sup> to  
181 estimate the cell counts of cultures at various ODs and volumes. . For *E. coli*, the dry mass per  
182 cell can vary over a range of growth rates (23). Using such a variable OD to cell count factor as a  
183 function of growth rate is possible with ALEsim, but incurs a marked increase in simulation  
184 time. Thus, identical simulations were performed using only the highest and lowest dry mass per  
185 cell values expected for the growth rates observed (i.e., the extremes). Only a 10% difference in  
186 the distribution of simulated endpoint growth rates were observed between the two extremes (see  
187 Supplementary Figure S1). Therefore, use of a constant average value for dry mass per cell over  
188 the range of growth rates expected was determined to be sufficient considering the benefit in  
189 computation time.

190 Although possible with ALEsim, deleterious and neutral mutations were not considered during  
191 this study. A deleterious mutation rate of 1 in 5,000 was previously computed (24). In the  
192 application demonstrated here, the population sizes were sufficiently large (10<sup>5</sup> – 10<sup>9</sup> cells) such  
193 that the effects of deleterious and neutral mutations would be negligible. With smaller population  
194 sizes (e.g., several orders of magnitude smaller than the population sizes modeled here), the  
195 effects of these mutations become more pronounced and should not be ignored.

196

197 **Results**

198 **Modeling the ALE process**

199 ALEsim is a model built on the basic principles of exponential growth in order to understand the  
200 dynamics of ALE. The scope of ALEsim is to predict the observed growth rate in each batch  
201 culture of an ALE experiment while allowing individual cells to change their growth rate when  
202 dividing (i.e., a proxy for receiving a beneficial mutation). This preferentially finds only those  
203 beneficial mutations that fix. There is a likely chance that other beneficially mutations are  
204 unobserved due to clonal interference. The observed population growth rate is different from a  
205 clonal growth rate in that each batch culture of an ALE experiment is a population of multiple  
206 clones with varying growth rates. Figure 1 provides a workflow of the modeling process and the  
207 full details are in Supplementary File ALEsim.txt. Each *in silico* experiment begins with a clonal  
208 inoculation of a strain with a given growth rate. A population of mixed phenotypes can be used  
209 in this framework, but here the starting population will be assumed to be isogenic with the same  
210 phenotypic behavior. This organism is allowed to replicate according to an exponential growth  
211 function. During each cell division event, there is a probability that it will mutate and start a new  
212 lineage with a mutated growth rate. This new lineage is allowed to grow alongside the parent  
213 strain according to exponential growth, but with its mutated growth rate. The new lineage is  
214 itself allowed to continue mutating in the simulation.

215 Mutated growth rates in ALEsim must be constrained to remain biologically meaningful, i.e.,  
216 growth rates that are of magnitudes that remain plausible. These rates are determined empirically  
217 by the user, as done here from the parameterization experiment (see section below). The growth  
218 rates can be constrained to allow various types of epistasis. For example, if two distinct growth  
219 rates are allowed, there is a possibility that a single cell line could mutate twice and receive both

220 of these mutations. ALEsim employs the flexibility to define the type of epistasis between these  
221 two mutations, if any epistasis at all is to occur. Similarly, an order to the mutations accumulated  
222 can be set, as certain mutations can be beneficial only in the presence of a pre-existing mutation  
223 (i.e., epistasis can be modeled). As the population of cells continues to replicate and mutate, their  
224 total cell count naturally increases. When the cell count reaches a given threshold, a simple  
225 random sample of cells is used to inoculate the next batch culture. The threshold corresponds to a  
226 target cell count at which to passage the cells to the next batch culture. The number of cells taken  
227 is determined by the passage size, which is a percentage of the total culture volume. After this  
228 sample is computed, a new batch culture is started with the chosen cells and corresponding  
229 growth rates. Figure 2 provides the key parameters of the model.

230 In using the basic principles of microbial growth and a brute force computational approach,  
231 many of the fundamental attributes of natural selection are intrinsically contained in the  
232 simulation. This includes clonal interference which is pervasive to asexual evolution. ALEsim  
233 can be used to model a system where two local maxima are possible but the greater maximum  
234 can only be found by first acquiring a mutation that is initially suboptimal compared to other  
235 possible single beneficial mutations (25). How to achieve this is shown in the model  
236 documentation (ALEsim.txt). The experimental parameters can be modulated to potentially find  
237 an experiment design that would find the desired optimum or both.

238 Given the stochastic nature of many steps in the model, the results are non-deterministic.  
239 Stochasticity is incorporated into the model in three ways: i) when a cell mutates its growth rate,  
240 ii) what growth rate a cell mutates to, and iii) what sample of cells are propagated to a  
241 subsequent batch culture. The simulation is then run multiple times to capture the dynamics of  
242 the stochasticity (26).

243 For a simulation to be biologically meaningful using the developed model, there are three types  
244 of parameter sets that must be determined. The first set of parameters is experimental: batch  
245 culture size, passage size, passage optical density (or cell count), and length of experiment.  
246 These can be set based on the desired experimental setup.(23) The second set is the statistical  
247 parameters: random number seed and the number of identical experiments to run. The random  
248 number seed is set by the native random number generator. The number of parallel simulations to  
249 run is determined by the statistical power needed. Depending on the magnitudes and  
250 complexities of the parameters set, the number of simulations can vary drastically. For the results  
251 shown here, 500 simulations were computed unless otherwise stated. It was found that after 500  
252 simulations there was no appreciable difference in the means or spread of the distribution of  
253 results calculated when combined with another set of 500. The third set of parameters is  
254 biological: beneficial mutation rate (BMR) and allowed increases in growth rate. These  
255 parameters are defined in the models and can be constrained by any method that can be  
256 expressed programmatically, whether this it is randomly decided within a meaningful range or  
257 set to distinct values. This set of parameters must be derived experimentally. Intuitively, these  
258 parameters can be different for different strains, conditions, and can even change along the  
259 course of a single experiment (27, 28). As long as the values determined are biologically  
260 meaningful, generalizations about the ALE process can be concluded.

261 Alternative models of evolution and adaption have been developed to understand the dynamics  
262 of evolution. These types of mathematical models capture various aspects of adaptation  
263 including selection, drift, and clonal interference (29-31). Classically, this has been a target of  
264 the field of population genetics (32-34). An expansion of the Fisher model was developed by  
265 Wahl et. al. which conceptually relates to ALEsim in that it targets the question of passage sizes

266 (35). However, ALEsim deviates from the classical mathematical approach and employs the use  
267 of an *in silico* organism that can then replicate, mutate, and evolve. Simulations here are carried  
268 out in brute force where they are allowed to grow under the conditions laid out by the user. The  
269 advantage of such a method is that the experimental and biological parameters can be strictly  
270 controlled over the course of an experiment. The resulting simulation is able to more closely  
271 mimic the conditions of an actual laboratory evolution experiment in its entirety where  
272 parameters are not always constant throughout. This approach differs from the use of a digital  
273 organism in that it is an attempt to model specific biology instead of general evolutionary  
274 dynamics which allows for direct modeling of the ALE experiment as would be performed in a  
275 laboratory (36).

#### 276 **Parameterization of ALEsim by evolving *E. coli* on Glycerol Minimal Media**

277 The two biological parameters, the beneficial mutation rate and allowed increase in growth rate,  
278 were determined using 30 independent cultures of *Escherichia coli* K-12 MG1655 evolved in  
279 15mL of 0.2% glycerol M9 minimal media until a stable growth rate was observed in most  
280 experiments (38 days). One experiment only lasted 23 days after it was restarted due to  
281 contamination. The 30 experiments were separated into five groups of six passage sizes and each  
282 group was evolved under identical conditions except for the passage size. The passage sizes used  
283 were 10%, 1%, 0.1%, 0.01%, and 0.001% of the culture size (15mL). The growth rate of each  
284 experiment was monitored over the course of the experiment using optical density measurements  
285 as a proxy for cell count (Figure 3). Fitness related details can be found in the supplement  
286 (Supplementary Table 1 and Supplementary File fitness\_data.xlsx).

287 Allowed increases in growth rate were determined by identifying jumps in growth rates from the  
288 fitness trajectories. A spline was fit to the growth rate of each experiment and significant

289 increases in growth rate were identified as discussed previously (7). The resulting jumps in  
290 growth rates showed that the plateaus in growth occurred at specific values (Figure 3, 4). These  
291 plateaus are identified as State 1, 2, 3A, and 3B. State 3 was split into two sub-states since there  
292 is a significant difference between those in state 3A and 3B (Wilcoxon rank sum  $p < 0.01$ ),  
293 however there exists no identifiable increase in growth rate or gap between states that would  
294 characterize this transition. This gap is most likely obscured since the difference between the  
295 growth rates is fairly small and noise in the measurements can bleed into any gap that might  
296 exist. Figure 4 groups the jumps in fitness observed by their transition between states. Contrary  
297 to the conclusion of other ALE experiments, the largest jump in fitness was not observed first but  
298 actually followed a smaller jump. This yields an allowed increase in growth rate that can be used  
299 to constrain ALEsim. In simulations run here, the growth rates allowed were set to the mean of  
300 the range of each state.

301 The beneficial mutation rate (BMR) can be calculated by fitting ALEsim to the distribution of  
302 the end states. Passage sizes of 10% - 0.1% did not show any appreciable variation between  
303 states, thus only the experiments with passage sizes of 0.01% and 0.001% were used for fitting.  
304 ALEsim was fit by performing simulations that only allowed for a single jump from one state to  
305 another. Multi-state jumps and two sequential jumps were not allowed. This simplification skews  
306 the BMR calculation to only include beneficial mutations that were fixed in the population.  
307 There is a potential that other beneficial mutations are possible, but were not observed due to  
308 either clonal interference or genetic drift (37). As observed in the fitness trajectories for passage  
309 sizes of 0.01% and 0.001%, not all experiments were able to make jumps to occupy all the states.  
310 For instance, with a passage size of 0.01%, only 4 of 6 experiments were able to make the  
311 transition from State 2 to State 3 by experiment's end. In simulation, the same distribution



312 among the various end states is observed. The distribution observed in simulation is highly  
313 dependent on the supply of beneficial mutations captured by the BMR parameter. Thus, the  
314 BMR can be fit to yield the same distribution across states as observed experimentally. The  
315 BMR was computed using transitions from both State 2 to State 3 and from State 1 to State 2.  
316 Since all experiments made the transition from State 1 to State 2, the distribution was used at the  
317 day 20 mark where a distribution existed. The 95% confidence interval for the BMR was  
318 calculated by fitting the BMR to the 95% confidence interval of the experimental distribution of  
319 states. The results yielded a BMR of  $10^{-6.9}$ - $10^{-8.4}$  mutations per cell division. The confidence  
320 interval was determined by a maximum likelihood estimate as implemented in the binofit  
321 function in MATLAB.

### 322 **Retrospective Validation of ALEsim**

323 ALEsim and the derived parameters (beneficial mutation rate and allowed increases in growth  
324 rate) were analyzed using two previously performed ALE experiments on glucose (7, 18) and a  
325 legacy experiment on glycerol (14). The outcomes of the two glucose experiments yielded  
326 disparate final growth rates despite identical strains and media (*E. coli* K-12 MG1655 in M9  
327 glucose minimal media),  $1.00 \pm 0.02$  with 6 replicates and  $0.79 \pm 0.01$  with 3 replicates,  
328 respectively. The only differences between the experiments were three experimental parameters:  
329 batch culture volumes (250 mL vs. 25 mL), optical densities when passed (variable vs.  $OD_{600nm}$   
330 1.2), and passage sizes (variable vs. 800 $\mu$ L) in the Charusanti et al. (18) and the LaCroix et al.  
331 (7) studies, respectively. ALEsim was constrained to allow only the jumps in growth rates  
332 observed in these studies and then simulated the expected fitness trajectories for the two different  
333 experimental parameters. The only differences explicitly defined in ALEsim were the different  
334 batch culture volumes, passage optical densities, and passage volumes. The results showed that

335 the difference in the final growth rates achieved can be sufficiently explained by the differences  
336 in these parameters only (Figure 5). Furthermore, when simulating a legacy dataset for evolving  
337 *E. coli* on glycerol minimal media, ALEsim was able to successfully predict that all experiments  
338 (n=4) should reach fitness state 3 for the given experimental parameters, as reported in the study  
339 (14). The largely different outcome in fitness (i.e., no fitness jumps vs. a significant increase) on  
340 glucose, as well as a consistent prediction of fitness on a legacy glycerol dataset, further  
341 highlights the importance of properly designing an experiment and validates ALEsim and its  
342 parameterization.

### 343 **ALEsim Applications**

344 Simulations of ALE experiments with the derived beneficial mutation rate and fitness states can  
345 enable statements to be made about optimality. The time required to see a given increase in  
346 fitness was simulated for a range of increases in growth rate over a range of passage sizes  
347 (Figure 6). The results show the average length of time needed to see a measurable change in  
348 growth rate due to a beneficial mutation for a range of passage sizes. Figure 6 was derived for  
349 growth rate increases that occur from a single mutational event. Based on the passage size and  
350 length of time with no increase in growth rate, a conclusion about how close a population is to  
351 reaching another state of increased fitness. For example, if a given evolution experiment has  
352 achieved a certain growth rate,  $\mu$ , and has not shown an increase in growth rate with a passage  
353 size of 0.1% for 13 days, then there is no likely increase in growth rate available which is greater  
354 than  $0.10 \text{ hr}^{-1}$  from a single mutational event.

355 Increasing the passage size raises the probability of capturing a beneficial mutation however this  
356 also leads to an inflation in the resources needed to sustain the experiment (Figure 6). For  
357 example, if an ALE experiment with a passage size of 0.1% were being passed twice a day

358 (every 12 hours), the same experiment with a passage size of 10% would need to be passed 6  
359 times per day (every 4 hours). The magnitude of resources needed to maintain an experiment  
360 tend to scale with each batch. Thus, the more batches needing to be processed, the more media,  
361 pipette tips, culture vessels, and labor costs are required. A single person can feasibly do an  
362 experiment passed every 12 hours whereas passing every 4 hours would require coordinated  
363 effort by multiple persons or an automated platform. Therefore, understanding what is gained  
364 with the larger passage size is important before committing to such a large expenditure of  
365 resources. ALEsim can quantify the gains or losses achievable with different passage sizes to  
366 help identify the ideal experimental setup (Figure 6).

367

#### 368 **Mutation Frequency Analysis by Passage Size**

369 Clones from the endpoint populations of each independent experiment were isolated and  
370 resequenced. Two clones showed hypermutating tendencies. This was identified by the number  
371 of mutations ( $p < 0.01$ ) and the presence of a mutation in *mutY* or *mutL*. Experiments with larger  
372 passage size led to an increase in the number of mutations found. Mutated alleles were therefore  
373 grouped by passage size. Clones isolated from larger passage size experiments, on average, had  
374 more alleles being selected (Figure 7). Of all mutations identified, those in *glpK* were  
375 specifically tracked. Mutations in *glpK* have previously been shown to be causal (with a  
376 significant impact on fitness) as well as ubiquitous, mutating more than any other alleles under  
377 glycerol growth conditions (14). Thus *glpK* is a good indicator of the how effective the various  
378 passage sizes are at fixing beneficial mutations. Consequently, there is a positive relationship  
379 between the fixing of *glpK* mutations and the passage size until saturation is reached. With the

380 passage size dropped to the lowest value (0.001%), the observed fraction that fixed was only  
381 0.33 (2/6).

382 **Discussion**

383 The conceptual purpose of an ALE experiment is to move an organism towards a more optimal  
384 (fit) state in the presence of a selection pressure. Absolute optimality is difficult, if even possible,  
385 to define. It has been shown that even for a laboratory evolution, there is still room for evolution  
386 after 50,000 generations (38). The continual ability of organisms to evolve and innovate makes it  
387 difficult to analyze the results of an ALE experiment in the context of optimality. What is  
388 immediately apparent is that there are diminishing returns. As an ALE experiment progresses,  
389 the increase in growth rate or fitness tends to decrease in magnitude (1, 39-43). The smaller  
390 increases take longer lengths of time to occur and become fixed in the population  
391 (Supplementary Text). Given this property and the desire to understand and leverage the ALE  
392 process, ALEsim was built and validated through performing a control experiment. ALEsim was  
393 first parameterized with a set of control experiments using different passage sizes.  
394 Parameterization revealed a beneficial mutation rate of  $10^{-6.9}$ - $10^{-8.4}$  mutations per cell division,  
395 consistent with previously reported values and distinct fitness states (27, 28). Validation was  
396 then carried out using additional legacy experiments and ALEsim proved sufficient for  
397 explaining the differences in observed experimental outcomes (i.e., growth rates) based on the  
398 parameters employed in each study (i.e., passage size, passage OD, and culture volume) (Figure  
399 5). Lastly, ALEsim was applied to quantify tradeoffs in experimental design considerations for  
400 desired outcomes and was used to demonstrate how it can be leveraged for determining the key  
401 aspect of experiment termination.

402 The ability to optimize and design ALE experiments is possible with the ALEsim computational  
403 framework. Given a certain amount of resources, ALEsim can calculate how best to deploy them  
404 at different stages of an experiment to shorten project timelines and achieve desired outputs. For

405 example, near the beginning of the ALE experiments, the increases in growth rates found are  
406 typically quite large. Because of this, a large passage size does not have an additional benefit.  
407 This is evident in the experiment performed here in that passage sizes of 0.1%, 1%, and 10%  
408 mostly reached states 1, 2, and 3A at about the same time (Figure 3). In planning future ALE  
409 experiments, the added resource usage needed to maintain an experiment at a 10% passage size  
410 does not appear to be justified. However, the added benefits become apparent when looking at  
411 the transition from state 3A to 3B. It could then be suggested that if the goal is to get as close to  
412 the absolute optimal state as reasonably possible, the added resources of maintaining a 10%  
413 passage size experiment only need to be maintained after initial large increases in growth rate or  
414 fitness are found. This would not eliminate the difficulty in maintaining such an experiment, but  
415 would at least reduce the length of time the experiment would need to be run at such a high  
416 resource ‘burn’ rate. With ALEsim, these types of resource/fitness tradeoff analyses can now be  
417 calculated and should be leveraged in experimental design. The approach of dynamic resource  
418 allocation opens the door for project optimization typical of engineering process design.

419 Knowing the distance to optimality can aid in determining when to terminate an ALE  
420 experiment. The typical method of determining when to stop an ALE experiment is to  
421 subjectively determine that no more increases in fitness are being observed. However, this  
422 approach of waiting to observe a plateau in fitness can be artificial given a small passage size.  
423 An example of how this approach can be misleading is the observation that passage sizes of  
424 0.1% and 1% showed no increase in growth rate after reaching state 3A for at least 15 days  
425 (Figure 3). However, given that slight increases in growth rates beyond state 3A to state 3B with  
426 a passage size of 10% were observed, it can be concluded that state 3A is not the optimal state.  
427 Thus, if only a 1% passage size was used, the experiment could be terminated before finding

428 state 3B. Further, it would be incorrect to compare experiments with a 10% passage size to a 1%  
429 passage size without understanding the context of the effects of the different passage sizes.  
430 Perhaps the best example of this is provided through the analysis of legacy ALE experiments  
431 (Figure 5). Two experiments with the same strain and media conditions yielded vastly different  
432 fitness outcomes. This difference is subsequently explainable within the scope of ALEsim.  
433 Therefore, having access to a computational framework such as ALEsim can enable the  
434 researcher to make an informed decision about when to terminate an experiment given the  
435 capacity and resources of the experimental setup and the desired/acceptable outcome. This type  
436 of termination analysis is laid out in Figure 6 and can be calculated *de novo* for any experiment  
437 given the current growth rate and passage size. It also should be noted that this type of analysis  
438 could result in a standard for the ALE community as one could state the ALEsim generated  $\Delta\mu$  at  
439 the time of termination.

440 The ability to design and carry out complicated and high resource burn ALE experiments is  
441 likely only feasible though automation of the ALE process. Automation was utilized here and in  
442 previous studies (4, 7, 44). Manual processes are often hindered by researcher availability  
443 whereas machines can measure and pass around the clock (e.g., approximately 5-7 passages per  
444 day were performed in automated studies (4, 7, 44), compared to 1-2 per day manually (14, 15,  
445 18). Thus, the ability to automate and optimize ALE is likely to accelerate adoption of the ALE  
446 experimental technique and broaden the application areas. Furthermore, the ALEsim framework  
447 and output can also be used as a basis for modeling much of the legacy data currently available  
448 for ALE experiments which include lag, exponential, stationary, and/or stressed phases. As the  
449 selection pressure in such experiments is more complex and growth is defined by more than the  
450 growth rate parameter (e.g. lag phase duration, stationary phase mutation rate, growth phase

451 transistions, etc...), ALEsim in its current format would have to be expanded. Nonetheless,  
452 ALEsim and its parameterization here demonstrates the utility of using simulated design in the  
453 ALE process and establishes a portable code base.

454 The field of adaptive laboratory evolution is expanding, largely due to lower costs of next  
455 generation sequencing. Innovative applications are appearing and are being applied to a range of  
456 organisms (1, 3). This growth in ALE use has occurred without a standard operating procedure  
457 for performing and quantifying these experiments. Consequently, this leads to ill-defined  
458 endpoints of experiments and the inefficient use of resources. The ALEsim computational  
459 platform developed here would provide a basis with which to quantify experiments and aid in  
460 their design; matching the desired outcome with resources available.

461



462 **List of Supplementary Files**

463 - Supplemental text (calculations)

464     o Supplemental Table – ALE Fitness Stats

465     o Supplemental Figure 1 – Sensitivity analysis of dry weight per cell values

466 - Supplementary File 1 – MATLAB m files: ALE Model m-files

467

468

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473

474 **Tables**

475 None

476

477 **Figure Legends**478 **Figure 1 - ALEsim Flow Chart**

479 A workflow outlining the logical steps the simulator takes when performing a single simulated  
480 ALE experiment. Due to the stochastic nature of ALE experiments, *in vivo* and *in silico*, multiple  
481 experiments are averaged together to identify general trends.

482 **Figure 2 - Governing Equations, Assumptions, and Parameters for ALEsim**

483 a) Microbe growth occurs according to an exponential growth curve where  $\mu$  is the growth rate,  $t$   
484 is the time elapsed,  $N_0$  is the initial cell count at  $t=0$ , and  $N(t)$  is the cell count at a given time,  $t$ .  
485 No lag phase or stationary phase is modeled. The total cell count ( $N(t)$ ) is determined by the  
486 summation of exponential growth curves for all individual cells lines. b) Favorable mutations  
487 occur during cell growth according to a binomial distribution where each cell division represents  
488 one Bernoulli trial with a probability of success equal to the beneficial mutation rate (BMR). c)  
489 Each flask is modeled as a completely homogenous culture. d) The number of cells represented  
490 for each cell line in each inoculum is randomly chosen according to a normal distribution with a  
491 mean and variance equal to the number of cells represented in the flask,  $N_{Green}^{Flask}$  times the ratio of  
492 the flask volume,  $V_{Flask}$ , to inoculum volume,  $V_{Inoculum}$ . e-g) The volume of media per flask,  
493 inoculum volume, and passage optical density can be altered. h) The simulated ALE experiment  
494 can be stopped after a specified amount of time or maximum number of flasks. i) Based on the

495 relative growth rate increases seen in ALE experiments, a range of allowable growth rate  
496 increases is determined. j) Based on matching the evolution trajectory (plot of growth rate vs.  
497 flask #) with varying the beneficial mutation rate (BMR), the probability of a favorable mutation  
498 is obtained. k) Since each ALE is based on randomly generated mutations, multiple ALE  
499 simulations are averaged together to get repeatable results from the same parameters. The  
500 number of simulations is user controlled.

### 501 **Figure 3 – Fitness Trajectory of *E. coli* evolved on Glycerol**

502 The absolute growth rates of independently evolved cultures of *E. coli* as fitted by a cubic spline  
503 for all ALE experiments separated by the different passage sizes. Dashed lines represent regions  
504 where the spline fit is based on sparse data, and therefore not considered accurate. The small  
505 upturn in growth rates at the endpoint is an artifact of the spline interpolation and is ignored  
506 when determining endpoint growth rates. All except five ALE experiments reached fitness State  
507 3. The rate at which the final growth rate was achieved varied. The hypermutating strain with a  
508 passage size of 10% reached State 3 significantly faster than all others (it possessed a mutation in  
509 *mutY*). The purple hypermutating strain was identified as a potential hypermutating strain based  
510 on the number of mutations fixed ( $p=0.003$ ,  $FDR=0.087$ ) and the presence of a frame shift  
511 insertion in *mutL*.

### 512 **Figure 4 – Distribution of Fitness Increases in Glycerol ALE**

513 A histogram of the normalized increases in growth rate ( $\mu_{\max} = 0.64 \text{ hr}^{-1}$ ) attributed to each jump  
514 for the different experiments. The fitness increases were categorized by which state transition  
515 was made. The different passage sizes (indicated by different colors) did not show any  
516 significant variance in the ability to fix distinct increases in growth rate. A few small jumps not

517 shown are small observed increases in fitness that did not jump between any of the states  
518 identified.

519 **Figure 5 – Simulated vs Experimental Results with Large and Small Passage Sizes**

520 Two ALE experiments of *E.coli* MG1655 in glucose M9 minimal media were simulated using  
521 ALEsim. The strain and media conditions were identical in the two experiments. The only  
522 differences were in the culture volume (25ml vs. 250mL), optical density when passed (variable  
523 vs. 1.2 OD<sub>600nm</sub>), and passage volume (variable vs 800μL). The variable nature of the optical  
524 density when passed and the passage size in the latter experiment was a consequence of  
525 manually passing the culture each day. The former experiment employed an automated system of  
526 monitoring and passing the culture to maintain consistency. Despite being the same strain and  
527 conditions, the final fitness achieved in the two experiments were quite different. ALEsim was  
528 used to simulate these same experiments with the only differences being the three  
529 aforementioned parameters. Consequently, the ALEsim results showed that the differences in  
530 these parameters were sufficient to explain why the final growth rates achieved were different,  
531 further highlighting the importance of choosing these parameters properly. The simulated  
532 results are represented by a 95% confidence interval. The confidence interval for Experiment  
533 #2 is too small to be visible.

534 **Figure 6 – Upper Bound on possible jumps in growth rates**

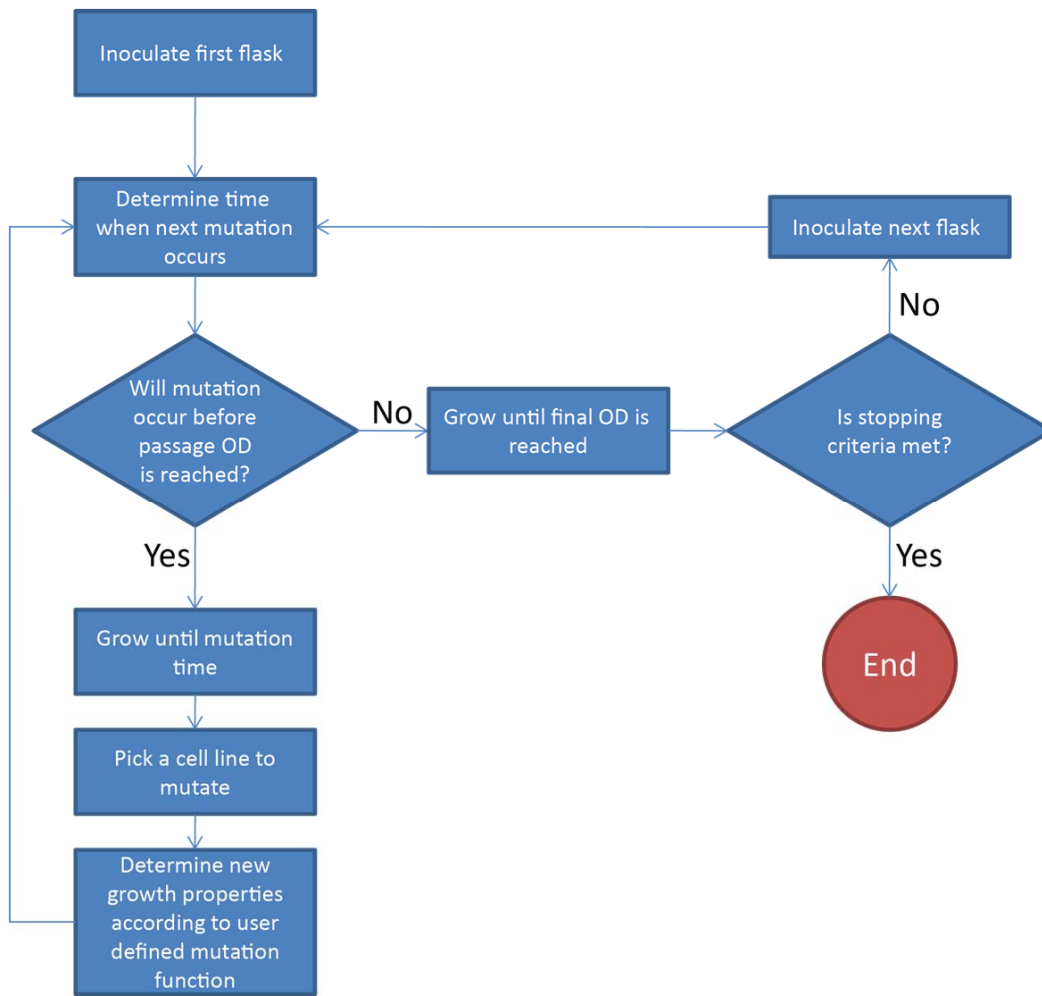
535 A. Upper bounds on possible jumps in growth rates are shown. At a given point in time, a jump  
536 that reaches above the upper bound is statistically infeasible (95% confidence) from a single  
537 mutation, whereas jumps that stay below the line are possible. B. The upper bound on jumps is  
538 shown for varying passage sizes. These experiments were simulated with parameters that

539 matched the experimental parameter used. Increasing the passage size can have a significant  
540 impact on the upper bound. Consequently, the time required to eliminate jumps of certain  
541 magnitudes can take much longer to achieve. However, as the passage size increases there comes  
542 a point when the returns begin to diminish such that passage sizes between 0.1% and 10% did  
543 not show a large difference in the time required to find a given jump. C. Relative amount of  
544 resources needed to perform an ALE experiment normalized to the lowest passage size. As the  
545 passage size is increased the resource usage begins to increase greatly.

546 **Figure 7 – Genetic Analysis – By Passage Size**

547 A bar chart representing the observed fraction of mutations at a given passage volume. As a  
548 general trend, the larger the passage size, the greater the probability of a mutation in a given  
549 allele fixing in the population. A key mutation in the *glpK* gene is displayed as well as all  
550 mutations. The ordinal rank of passage size was compared to the observed fraction of mutations  
551 using a Wilcoxon rank test and resulted in p-values of 0.008 and 0.024 for all mutations and  
552 *glpK* mutations, respectively.

553

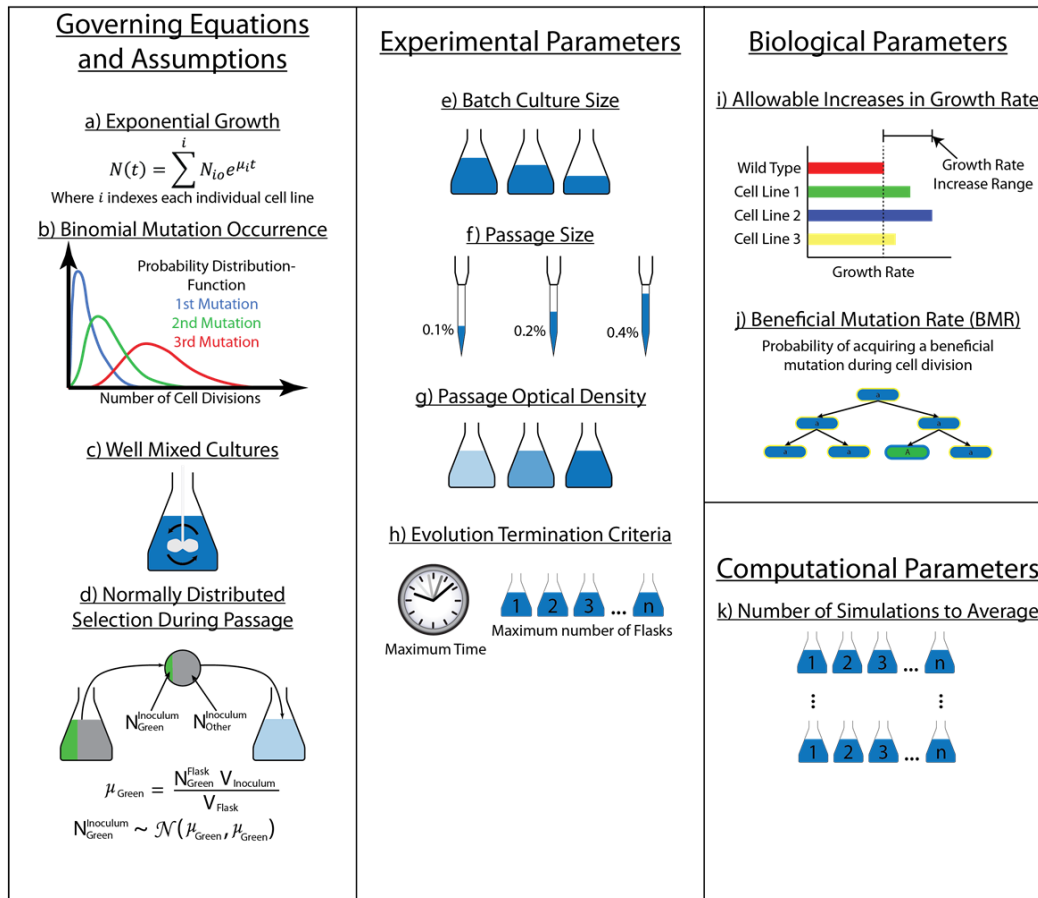


554

555 **Figure 1**

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557



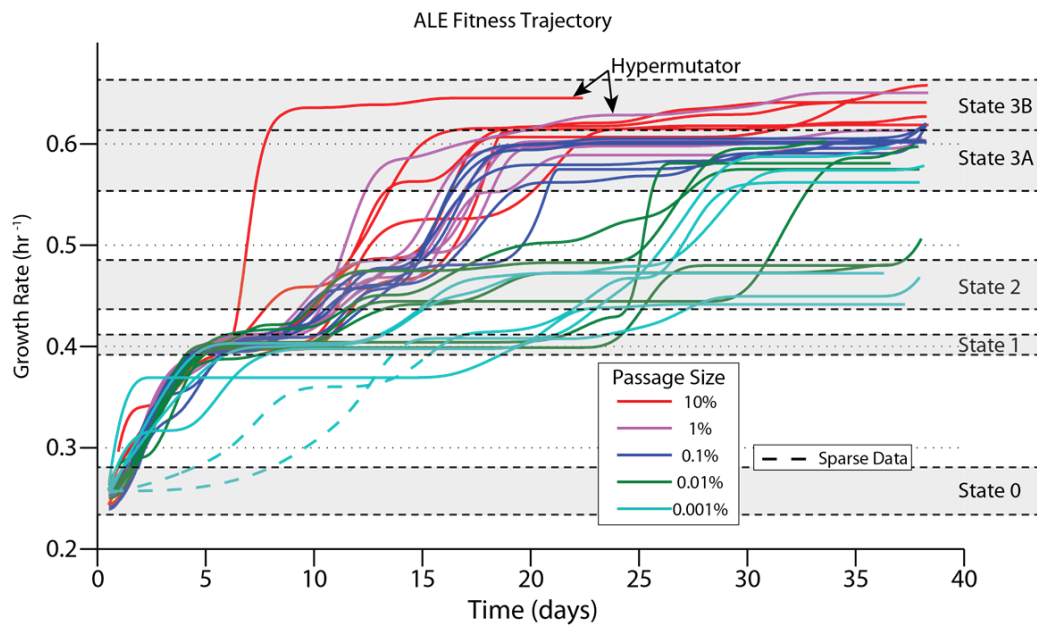
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559 **Figure 2**

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31

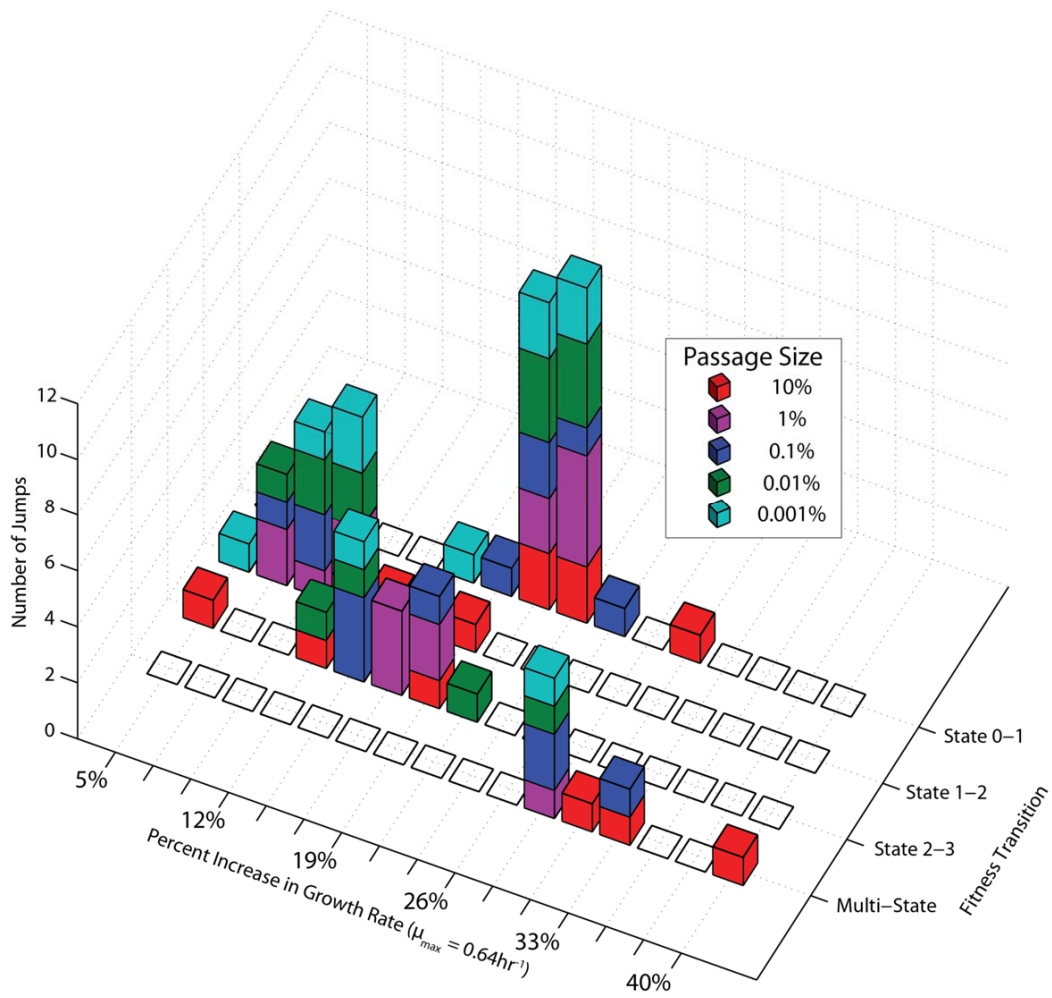




561

562 **Figure 3**

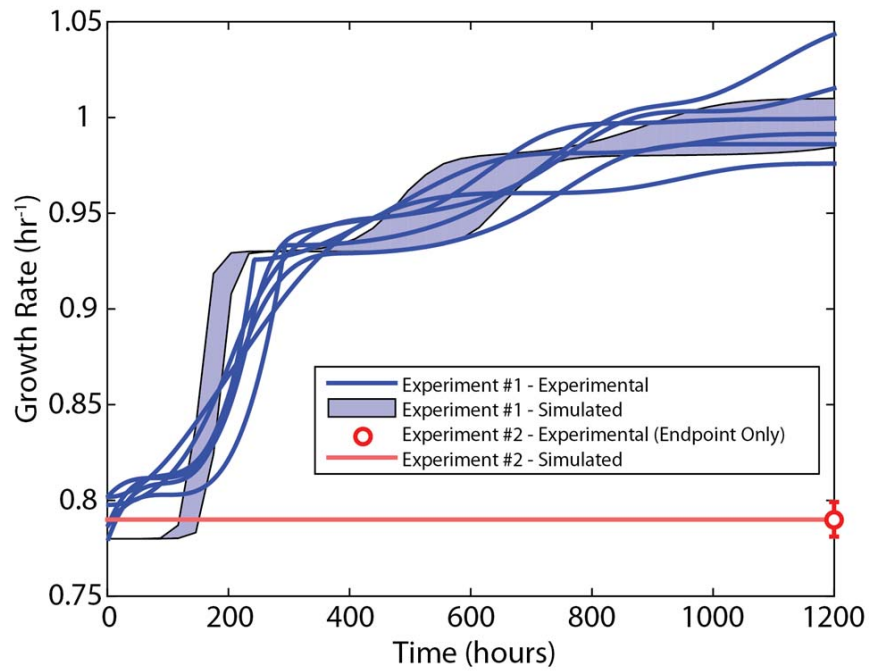
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565 **Figure 4**

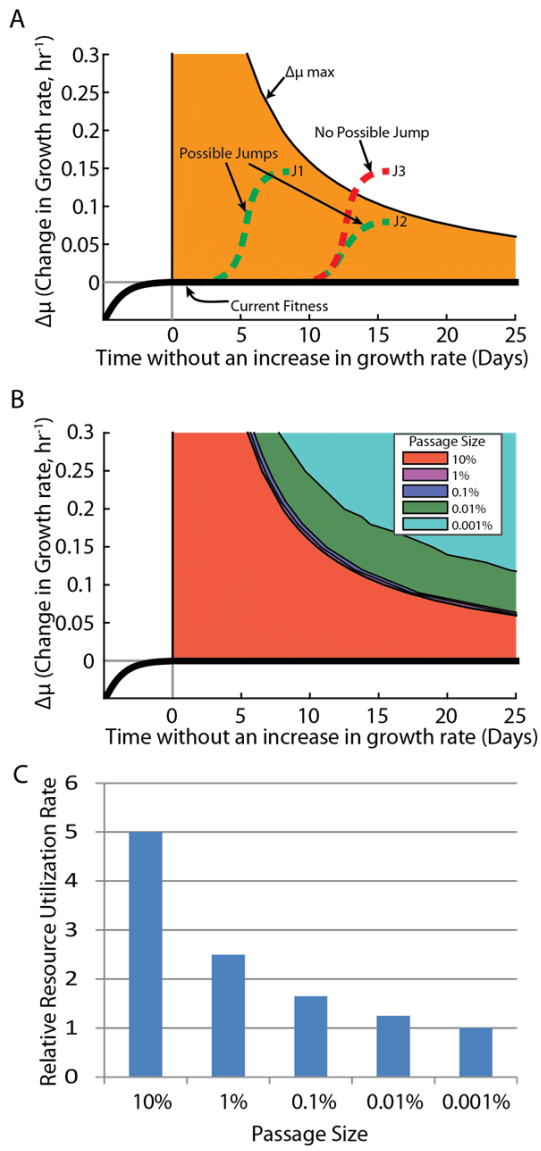
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567

568 **Figure 5**

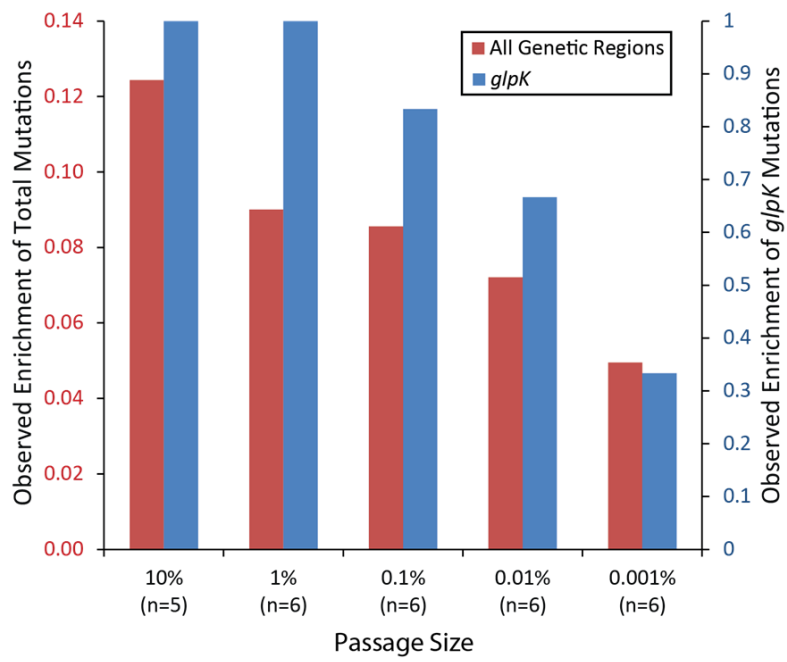
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570

571 **Figure 6**

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573

574 **Figure 7**

575 **References**

576

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