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Regional frequency analysis of short duration rainfall extremes using gridded daily rainfall data as co-variate

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1 **REGIONAL FREQUENCY ANALYSIS OF SHORT DURATION RAINFALL**
2 **EXTREMES USING GRIDDED DAILY RAINFALL DATA AS CO-VARIATE**

3
4
5 Short title: Regional frequency analysis of short duration rainfall extremes

6
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20 **ABSTRACT**

21 A regional partial duration series (PDS) model is applied for estimation of intensity duration
22 frequency relationships of extreme rainfalls in Denmark. The model uses generalised least
23 squares regression to relate the PDS parameters to gridded rainfall statistics from a dense
24 network of rain gauges with daily measurements. The Poisson rate is positively correlated to the
25 mean annual precipitation for all durations considered (1 min to 48 hours). The mean intensity
26 can be assumed constant over Denmark for durations up to 1 hour. For durations larger than 1
27 hour the mean intensity is significantly correlated to the mean extreme daily precipitation. A
28 Generalised Pareto distribution with a regional constant shape parameter is adopted. Compared
29 to previous regional studies in Denmark a general increase in extreme rainfall intensity for
30 durations up to 1 hour is found, whereas for larger durations both increases and decreases are
31 seen. A subsample analysis is conducted to evaluate the impacts of non-stationarities in the
32 rainfall data. The regional model includes the non-stationarities as an additional source of
33 uncertainty together with sampling uncertainty and uncertainty caused by spatial variability.

34

35 **KEYWORDS:** extreme rainfall, idf-curves, L-moments, partial duration series, regional analysis

36

37 **INTRODUCTION**

38

39 Design of water infrastructure is often based on intensity duration frequency (IDF) relationships
40 of extreme rainfall (e.g. Schilling, 1991; Arnbjerg-Nielsen *et al.*, 2013). They provide
41 information about the mean rainfall intensity of different durations for various frequencies or
42 return periods. IDF relationships are relevant for a wide range of temporal scales; from sub-
43 hourly duration for design of storm water pipes in the upstream parts of sewer networks to
44 several hours or days for design of retention basins that collect water from large catchments. IDF
45 relationships can be estimated by performing an extreme value analysis of rainfall data at the site
46 of interest. Such estimates, however, may be hampered by the lack of sufficiently long rainfall
47 records when extrapolating to large return periods. In regional frequency analysis data from
48 several sites within a region are pooled whereby the estimation uncertainty can be reduced
49 significantly (e.g. Madsen & Rosbjerg, 1997a; Kyselý *et al.*, 2011; Burn, 2014). In addition,
50 regional frequency analysis facilitates estimation of IDF relationships at ungauged sites by
51 combining regional extreme value statistics and site specific climatic and physiographic
52 characteristics.

53

54 A widely applied method in regional frequency analysis is the index-event approach (originally
55 named the index-flood approach in flood frequency analysis) using L-moments (Hosking &
56 Wallis, 1993; 1997). This approach has been used in several regional frequency analysis studies
57 of extreme rainfall, e.g. in Australia (Haddad *et al.*, 2011), Canada (Alila, 1999; Burn, 2014),
58 Czech Republic (Kyselý *et al.*, 2011), Italy (Di Baldassarre *et al.*, 2006), Slovakia (Gaál *et al.*,
59 2008), South Africa (Smithers & Schulze, 2001), and Washington State (Wallis *et al.*, 2007). All

60 these studies are based on the traditional index-event method using annual maximum series
61 (AMS). Madsen & Rosbjerg (1997a) developed a regional index-event approach based on Partial
62 Duration Series (PDS) that includes all events above a specified threshold level in the extreme
63 value analysis. Madsen *et al.* (1997) showed that the regional index-event PDS model with
64 generalized Pareto distributed exceedances, in general, is more efficient (in terms of quantile
65 estimation uncertainty) than the corresponding index-event AMS model based on the generalized
66 extreme value distribution. The regional PDS model has been further developed and applied for
67 estimation of IDF relationships in Denmark (Madsen *et al.*, 2002; 2009).

68

69 In the traditional index-event approach data are pooled within a fixed region that can be assumed
70 to be homogenous with respect to certain statistical characteristics, typically second and higher
71 order moments. Alternatively, a region of influence approach can be used to identify separate
72 homogeneous pooling groups for each site (Burn, 1990). The region of influence approach has
73 been applied to regional rainfall analysis by Kysely *et al.* (2011) and Burn (2014). Another
74 method that relaxes the use of fixed regions, or can be used in combination with a fixed region or
75 region of influence approach, is based on establishing regression relationships that describe the
76 spatial variation of extreme rainfall statistics using covariate information in terms of
77 physiographic and climatic characteristics. Such regional regression relationships also facilitate
78 estimation at ungauged sites. In a regional analysis in Washington State, Wallis *et al.* (2007)
79 found the L-Coefficient of variation (L-CV) and L-skewness to vary systematically with the
80 mean annual precipitation (MAP). Di Baldassarre *et al.* (2006) also related L-CV and L-
81 Skewness to MAP in their study of rainfall extremes in Northern Italy, and Madsen *et al.* (2002,
82 2009) found that the annual number of extreme events in a regional PDS model of Danish

83 rainfall extremes could be related to MAP. Haddad *et al.* (2011) related L-CV and L-skewness as
84 well as the index parameter to location and distance to the coast, whereas Beguería & Vicente-
85 Serrano (2006) applied a regional regression model relating the PDS parameters to location,
86 altitude and slope.

87

88 This study considers regional estimation of IDF relationships in Denmark. It builds on the
89 regional PDS model developed by Madsen *et al.* (2002) and later updated by Madsen *et al.*
90 (2009). The current study includes rainfall data up to 2012, corresponding to 50% more data in
91 terms of station-years compared to the previous study by Madsen *et al.* (2009). In addition, the
92 regional model is extended by using new covariate information in terms of gridded rainfall
93 statistics from a dense rain gauge network measuring daily rainfall. In the update of the regional
94 model by Madsen *et al.* (2009) a general increase in extreme rainfall was found, with most
95 pronounced increases for durations between 10 min and 3 hours. In a recent study by Gregersen
96 *et al.* (2013) a significant increase was found in the annual number of extreme events for all
97 durations analysed between 1 and 24 hours and in the mean extreme intensity for 1 and 3-hour
98 durations. In this study, the impacts of these non-stationarities on the regional model are
99 investigated using subsample analysis.

100

101

102 **DATA AND METHODS**

103

104 **Rainfall data**

105 Rainfall data from a network of high-resolution rain gauges in Denmark are used in the analysis.

106 The network is based on RIMCO tipping bucket gauges with 0.2 mm resolution and tips being

107 recorded every minute. The network was established in 1979 and is operated by the Water
108 Pollution Committee of the Society of Danish Engineers and the Danish Meteorological Institute
109 (Jørgensen *et al.*, 1998). The gauges have been maintained, but the principles of measuring and
110 calibrating the gauges have not been changed in the period investigated.

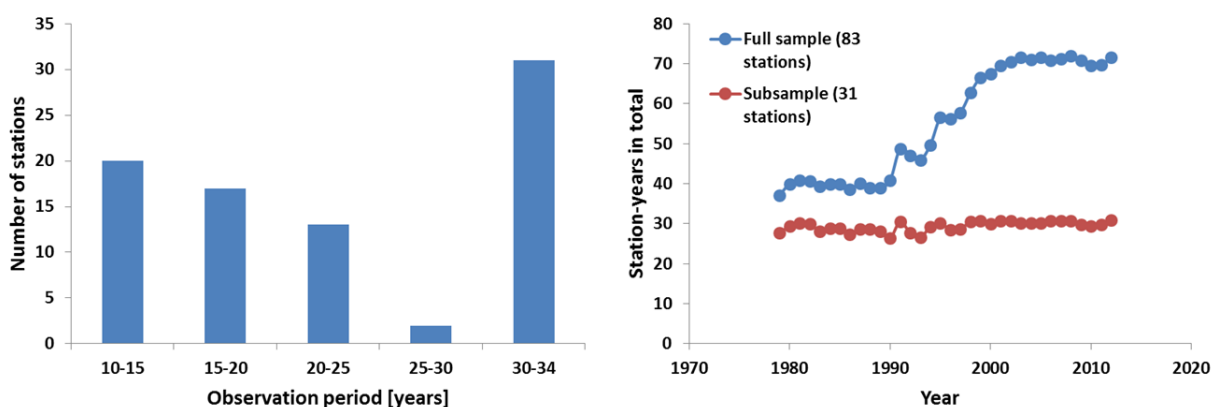
111
112 The data analysed consist of rainfall intensities with a temporal resolution of 1 minute for
113 individual rain events separated by dry periods of at least one hour. From the 1-minute intensity
114 data maximum rainfall intensities for durations ranging between 1 minute and 48 hours are
115 extracted using a moving window approach (Madsen *et al.*, 2002). For durations less than one
116 hour, independent events are separated by at least one hour dry periods. For durations larger than
117 one hour, independent events are separated by dry periods that are at least as large as the duration
118 considered. In this case the separate events defined for the 1-minute intensity data will be merged
119 into fewer and larger independent events. For the extreme value analysis Partial Duration Series
120 (PDS) are derived for each duration from the series of event-based maximum intensities by
121 including intensities above a pre-defined threshold level. The same threshold levels as applied in
122 the previous analyses (Madsen *et al.*, 2002; 2009) are used. Short-duration (less than 1-2 hours)
123 extremes are primarily caused by convective rainfall in summer months, whereas long-duration
124 (larger than 12-24 hours) extremes are caused by frontal rainfall and can occur all year round.

125
126 Rainfall data used in the analysis cover the period 1 January 1979 – 31 December 2012 and
127 include 83 stations with more than 10 years of observations. The location of the 83 stations is
128 shown in Supplementary Material Figure 1, and the distribution of observation periods is shown
129 in Figure 1. The dataset corresponds to a total of 1881 station-years. The earlier study by Madsen

130 *et al.* (2009) included 66 stations with a total of 1250 station-years, and hence the current study
131 comprises an increase in station-years of 50%.

132
133 The development of the annual number of station-years shows a relatively constant level of about
134 40 station-years per year up to 1990, followed by a steady increase up to a level of about 70
135 station-years per year during the last 10 years (see Figure 1). To evaluate the impact of the
136 development in data availability over time a subsample of 31 stations that have more than 30
137 years of observations is analysed. The subsample includes 999 station-years in total.

138



139
140 **Figure 1** Distribution of observation periods of the 83 stations included in the analysis (left),
141 and development of the annual number of station-years during the period 1979-2012
142 for, respectively, the full sample of 83 stations and the subsample consisting of the
143 31 stations with more than 30 years of data (right).

144
145 In the regional model covariate information from another precipitation dataset, the Climate Grid
146 Denmark (CGD), is used. CGD is a gridded dataset of daily precipitation prepared by the Danish
147 Meteorological Institute (Scharling, 2012). It has a spatial resolution of 10x10 km and covers the
148 period 1989-2010. The dataset is based on interpolation of rain gauge measurements from more
149 than 300 Hellman gauges using an inverse distance weighting approach (Scharling, 1999). From

150 the CGD dataset the mean annual precipitation and the mean extreme daily precipitation are
151 calculated. The mean annual precipitation (MAP) varies between 550 and 950 mm over
152 Denmark with the highest values in the Western part of the country (see Figure 3). The mean
153 extreme daily precipitation (μ_{CGD}) is estimated from the CGD data using a PDS model with a
154 regional constant threshold level corresponding to approximately three events per year. It varies
155 between 24.5 and 29.5 mm over Denmark with larger values in eastern Zealand, northern Jutland
156 and southern islands (see Figure 3).

157

158 In the previous studies by Madsen *et al.* (2002, 2009) different physiographic characteristics
159 (geographical location, altitude, shelter index) were included as covariates in the regression
160 analysis. However, none of these were found significant for describing the regional variability
161 and hence are not included in this study.

162

163 **Regional model**

164 The regional extreme value model developed by Madsen *et al.* (2002) is applied in this study.
165 The model is based on the PDS approach using a regional constant threshold level to define PDS
166 of extreme rainfall intensities at the different stations. In the regional PDS model the annual
167 number of extreme events is assumed to follow a Poisson distribution, and the magnitude of the
168 extreme events is assumed to follow a Generalised Pareto (GP) distribution. For determination of
169 a regional parent distribution the previous studies by Madsen *et al.* (2002, 2009) applied the L-
170 moment goodness-of-fit test proposed by Hosking & Wallis (1993) and extended by Madsen *et*
171 *al.* (2002) for application to two-parameter distributions used in PDS modelling. These studies

172 showed that the GP distribution was, in general, preferable for the range of rainfall durations
173 considered.

174

175 In the regional PDS model the Poisson rate (λ), and the mean (μ) and L-CV (τ_2) of the
176 exceedance magnitudes are modelled as regional variables. The regional model estimate of the
177 rainfall intensity for a given return period T is then given by (Madsen *et al.*, 2002)

178

$$\hat{z}_T = z_0 + \hat{\mu} \frac{1 + \hat{\kappa}}{\hat{\kappa}} \left[1 - \left(\frac{1}{\hat{\lambda}T} \right)^{\hat{\kappa}} \right], \hat{\kappa} = \frac{1}{\hat{\tau}_2} - 2 \quad (1)$$

179

180 where z_0 is the regional threshold level, $\hat{\lambda}$, $\hat{\mu}$, and $\hat{\tau}_2$ are regional model estimates of the Poisson
181 rate, mean, and L-CV, respectively, and $\hat{\kappa}$ is the corresponding estimate of the GP shape
182 parameter.

183

184 The regional variability of the PDS parameters are analysed using generalised least squares
185 (GLS) regression (Stedinger & Tasker, 1985; Madsen & Rosbjerg, 1997b). The GLS regression
186 model accounts for sampling uncertainties of the PDS parameter estimates as well as correlations
187 between the parameter estimates due to concurrent extreme events observed at different stations
188 in the region. The following regression model is considered

189

$$\hat{\theta}_i = \beta_0 + \sum_{k=1}^p \beta_k x_{ki} + \omega_i, i = 1, 2, \dots, M \quad (2)$$

190

191 where $\hat{\theta}_i$ denotes an estimate of one of the PDS parameters at station i , M is the number of
 192 stations, β_k are the regression parameters, x_{ki} are the covariates, and ω_i are the model residuals
 193 with covariance matrix

194

$$\Sigma = \begin{pmatrix} \sigma_{\varepsilon 1}^2 + \sigma_{\delta}^2 & \sigma_{\varepsilon 1} \sigma_{\varepsilon 2} \rho_{12} & \dots & \sigma_{\varepsilon 1} \sigma_{\varepsilon M} \rho_{1M} \\ \sigma_{\varepsilon 2} \sigma_{\varepsilon 1} \rho_{12} & \sigma_{\varepsilon 2}^2 + \sigma_{\delta}^2 & \dots & \sigma_{\varepsilon 2} \sigma_{\varepsilon M} \rho_{2M} \\ \vdots & \vdots & \ddots & \vdots \\ \sigma_{\varepsilon M} \sigma_{\varepsilon 1} \rho_{1M} & \sigma_{\varepsilon M} \sigma_{\varepsilon 2} \rho_{2M} & \dots & \sigma_{\varepsilon M}^2 + \sigma_{\delta}^2 \end{pmatrix} \quad (3)$$

195

196 In Eq. (3), $\sigma_{\varepsilon i}^2$ is the sampling error variance, σ_{δ}^2 is the residual model error variance, and ρ_{ij} is
 197 the sampling error correlation coefficient. Estimation of sampling variances and correlations to
 198 be used in the GLS regression model are described in Madsen *et al.* (2002). σ_{δ}^2 is estimated
 199 along with the regression parameters using an iterative scheme, see Madsen & Rosbjerg (1997b)
 200 for details.

201

202 The GLS regression model provides estimates of the PDS parameters and their associated
 203 variances at any location in the region. The T -year estimate at a given location is then obtained
 204 from Eq. (1). The variance of the T -year estimate is calculated based on the variances of the PDS
 205 parameter estimates from the GLS regression models using a Taylor series approximation of Eq.
 206 (1)

207

$$Var\{\hat{z}_T\} = \left(\frac{\partial z_T}{\partial \lambda}\right)^2 Var\{\hat{\lambda}\} + \left(\frac{\partial z_T}{\partial \mu}\right)^2 Var\{\hat{\mu}\} + \left(\frac{\partial z_T}{\partial \kappa}\right)^2 Var\{\hat{\kappa}\} \quad (4)$$

208

209 where the partial derivatives are evaluated around the GLS parameter estimates.

210

211 The variances of the estimated PDS parameters include both residual model error variance and
212 sampling variance corrected for intersite correlations. When only the intercept β_0 is included in
213 the regression model, the model provides an estimate of the regional mean PDS parameter, and
214 the estimate of the residual model error variance $\hat{\sigma}_\delta^2$ is then a measure of regional heterogeneity.
215 The regional mean is, in general, different from the arithmetic mean since the GLS model weighs
216 the estimated PDS parameters according to the error covariance matrix, hence giving less weight
217 to more uncertain estimates and groups of sites that have higher inter-site correlations (Madsen
218 and Rosbjerg, 1997b). If $\hat{\sigma}_\delta^2 = 0$, the region can be considered homogeneous and the observed
219 variability of the PDS parameter estimates at the different sites in the region can be explained by
220 sampling uncertainty. A residual model error variance larger than zero indicates a heterogeneous
221 region, and one can then apply the GLS regression model with available covariate information to
222 evaluate the potential of describing the regional variability.

223

224 Different diagnostics are applied to evaluate the GLS regression models. Madsen & Rosbjerg
225 (1997b) used the average prediction variance of the regression model estimates $\hat{\sigma}_{\theta_i}^2$ for all
226 stations $i = 1, 2, \dots, M$ in the region

227

$$\hat{\sigma}_{\theta_i}^2 = y_i^T \Sigma(\hat{\beta}) y_i + \hat{\sigma}_\delta^2 \quad , y_i = (1 \ x_{1i} \ \dots \ x_{pi}) \quad (5)$$

228

229 where $\Sigma(\hat{\beta})$ is the covariance matrix of the estimated regression parameters. The prediction
230 variance includes both the sampling uncertainty of the estimated regression model parameters
231 and the residual model error variance. When comparing different regression models, the model

232 with the smallest average prediction variance is preferred. The reduction in prediction variance
 233 (*RPV*) between a regression model with k explanatory variables, $\hat{\sigma}_{\theta_i}^2(k)$, and the regional mean
 234 model, $\hat{\sigma}_{\theta_i}^2(0)$, can be used as a measure of the value of covariate information

235

$$RPV = \frac{\sum_{i=1}^M \hat{\sigma}_{\theta_i}^2(0) - \sum_{i=1}^M \hat{\sigma}_{\theta_i}^2(k)}{\sum_{i=1}^M \hat{\sigma}_{\theta_i}^2(0)} = 1 - \frac{\sum_{i=1}^M \hat{\sigma}_{\theta_i}^2(k)}{\sum_{i=1}^M \hat{\sigma}_{\theta_i}^2(0)} \quad (6)$$

236

237 Note that *RPV* can become negative in the case where the inclusion of explanatory variables only
 238 provides a minor reduction in residual model error variance, which is smaller than the
 239 corresponding increase in the sampling uncertainty of the estimated regression model
 240 parameters.

241

242 Reis *et al.* (2004) proposed a pseudo coefficient of determination

243

$$R^2 = 1 - \frac{\hat{\sigma}_{\delta}^2(k)}{\hat{\sigma}_{\delta}^2(0)} \quad (7)$$

244 where $\hat{\sigma}_{\delta}^2(k)$ and $\hat{\sigma}_{\delta}^2(0)$ are the residual model error variances for, respectively, a regression
 245 model with k explanatory variables and the regional mean model. Note that if $\hat{\sigma}_{\delta}^2(k) = 0$ then R^2
 246 $= 1$ although the model is not perfect. In this case sampling errors account for the differences
 247 between the site specific PDS parameter estimates and the GLS regression model estimates.
 248 Compared to *RPV*, R^2 only considers the reduction in residual model error variance by using
 249 covariate information.

250

251 Finally, the significance of the estimated regression parameters is evaluated using a standard t-
252 test.

253

254

255 **RESULTS**

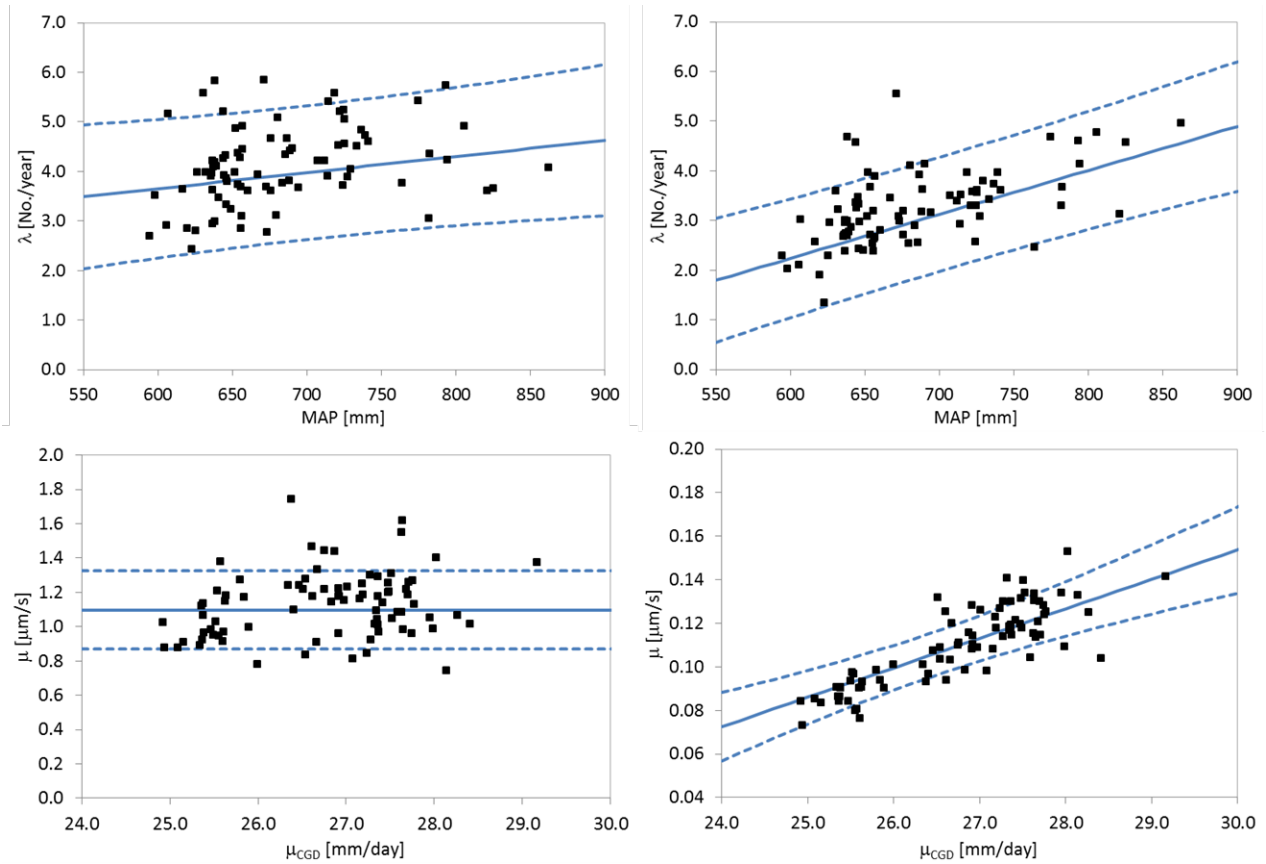
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257 **Regional model**

258 For the Poisson rate parameter λ the GLS results show regional variability ($\hat{\sigma}_\delta^2(0) > 0$) for all
259 durations, and a part of this variability can be explained by MAP. The GLS regression models
260 with MAP have smaller average prediction variances than the regional mean models. *RPV* ranges
261 between 0.01 and 0.54 and R^2 between 0.04 and 0.59 with the smallest values for the
262 intermediate durations 30-360 minutes, and the largest values for the 24 and 48-hour durations.

263 A t-test of the slope of the regression equation ($\hat{\beta}_1$) shows that the relationship with MAP can be
264 considered significant for all durations at a significance level of 5%, except for 60-minute
265 duration where the significance level is 7%. Estimated GLS regression models for 1-hour and
266 24-hour durations are shown in Figure 2. GLS regression results for all durations are summarised
267 in Supplementary Material Table 1.

268



269

270 **Figure 2** Regression model results. GLS regression model for the Poisson rate parameter λ
 271 with MAP as explanatory variable (top) and mean μ with μ_{CGD} as explanatory
 272 variable (bottom) for, respectively, 1-hour (left) and 24-hour (right) durations. Dotted
 273 lines represent the 95% confidence interval of the linear regression.

274

275 For the mean value of threshold exceedances μ the GLS regression results show regional
 276 variability for all durations. For durations 3-48 hours a significant part of this variability can be
 277 explained by μ_{CGD} . For these durations RPV ranges between 0.05 and 0.44 and R^2 between 0.17
 278 and 0.75, and the t-test shows that the relationship with μ_{CGD} is significant at a 5% level. The
 279 largest RPV , R^2 and most significant slopes of the regression line are obtained for 12- and 24-
 280 hour durations. For durations smaller than 3 hours there is no clear pattern in the relationship
 281 with μ_{CGD} . For some durations significant correlations are found, whereas for other durations the
 282 correlations are not significant and even result in poorer prediction variance compared to the

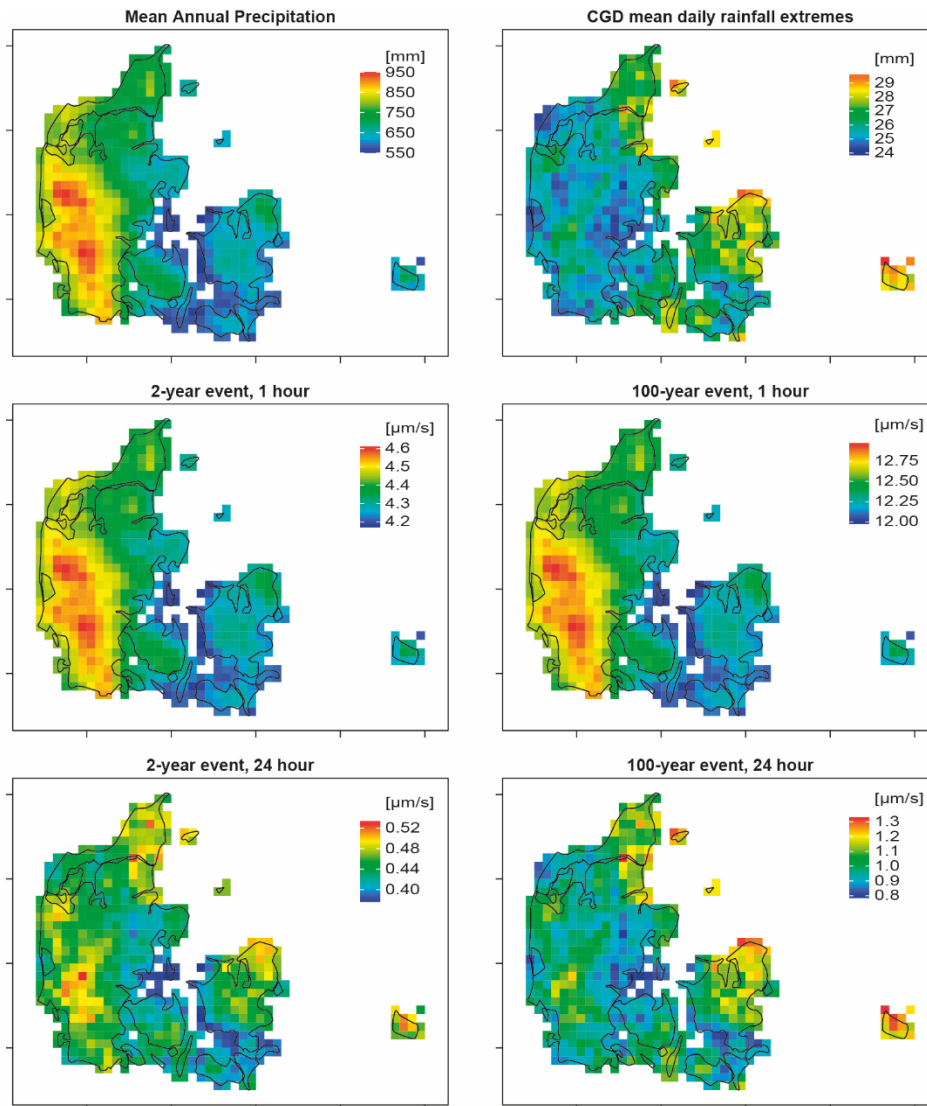
283 regional mean model (negative *RPV* for the 60-minute duration). For consistency, a regional
284 mean model is applied for all durations smaller than 3 hours. Estimated GLS regression models
285 for 1-hour and 24-hour durations are shown in Figure 2. GLS regression results for all durations
286 are summarised in Supplementary Material Table 2.

287

288 For the L-CV of threshold exceedances the GLS regression results indicate regional variability
289 for all durations except for 6 hours. No covariate information has been found to explain this
290 variability, and a regional mean model is applied for all durations. Results are summarised in
291 Supplementary Material Table 3.

292

293 Results of the regional model are shown in Figure 3. The figure shows estimated extreme
294 intensities for 1 and 24-hour durations mapped on the CGD grid. It should be noted that the
295 extreme intensities estimated from the regional model are point estimates and the maps in Figure
296 3 show the estimates at the grid centre points as gridded values. The explanatory variables used
297 in the regional model are mapped on the CGD grid in Figure 3 (top row). The spatial patterns of
298 the estimated PDS parameters λ and μ correspond to the spatial patterns of, respectively, MAP
299 and μ_{CGD} . For durations smaller than 3 hours the regional variability is only due to the variability
300 in λ as explained by MAP (Figure 3, middle row), whereas for durations of 3-48 hours the
301 regional variability in μ as described by μ_{CGD} also contributes to the regional differences in the
302 extreme intensities (Figure 3, bottom row). For smaller return periods the regional variability in
303 λ has a relatively larger contribution to the regional variability of extreme intensities, whereas
304 for larger return periods the regional variability in μ dominates.



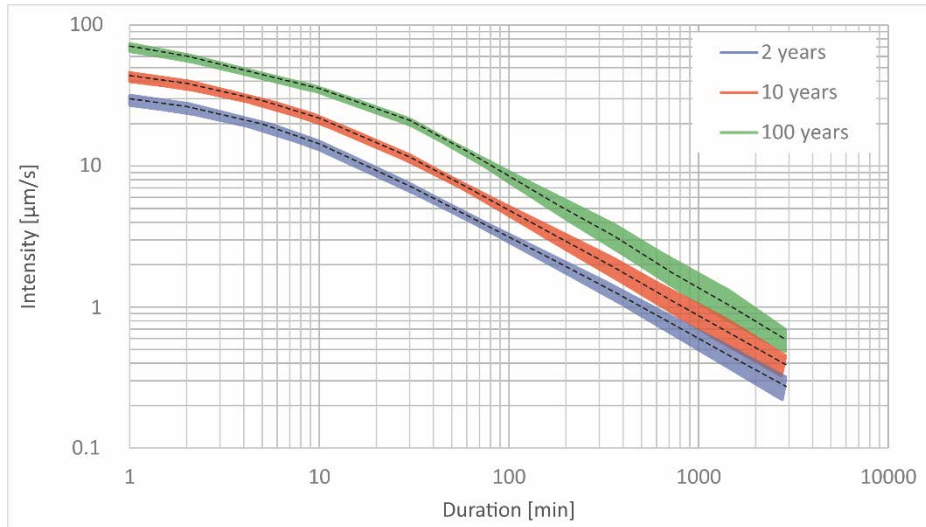
305

306 **Figure 3** Regional model results. Explanatory variables of the regional model (top row): MAP
 307 (left) and μ_{GCD} (right), and estimated 2-year and 100-year intensity for 1-hour
 308 duration (middle row) and 24-hour duration (bottom row).

309

310 Figure 4 shows the range of the estimated IDF curves over Denmark for 2, 10 and 100-year
 311 return periods. The range is calculated as the minimum and maximum extreme intensity for the
 312 different durations from the CGD gridded estimates as shown in Figure 3. The relative range
 313 (range divided by the average) is smallest for durations up to 1 hour, reflecting the regional
 314 constant μ for these durations. For durations larger than 1 hour the relative range increases for

315 increasing duration caused by an increasing regional variability of μ and λ . For 24 and 48-hour
316 durations the upper limit of the 2 and 10-year events are similar to the lower limit of,
317 respectively, the 10 and 100-year events.



318

319 **Figure 4** IDF curves for 2-year (blue), 10-year (red) and 100-year (green) events based on the
320 regional model. The coloured areas represent the variability over Denmark, and the
321 black dotted lines the corresponding regional averages.

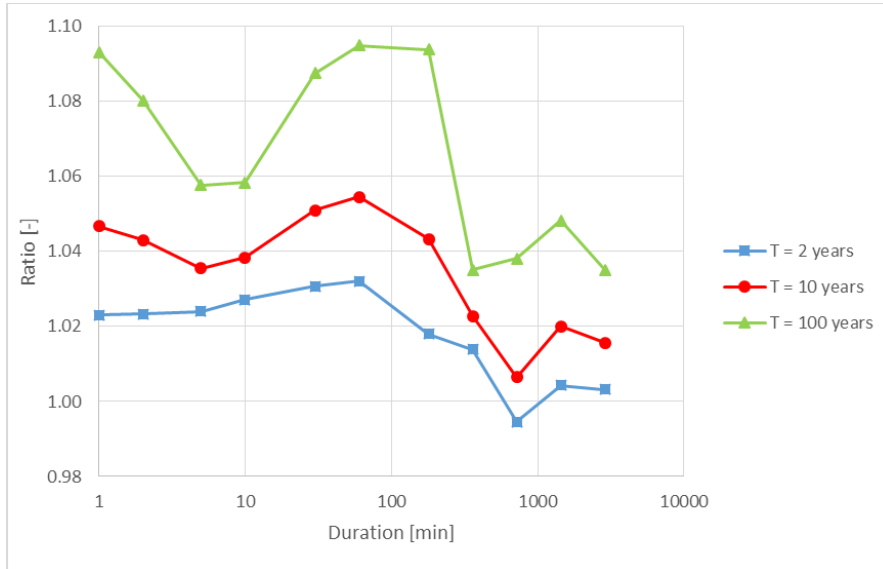
322

323 **Subsample analysis**

324 To evaluate the impact of the development in data availability over time as shown in Figure 1 the
325 subsample of 31 stations that covers almost the entire observation period has been analysed
326 separately using the same regional modelling approach. The regional model estimated from the
327 subsample gives, in general, smaller estimates of extreme intensities. The difference between the
328 two models is largest for durations up to 3 hours, and larger differences are seen for larger return
329 periods (see Figure 5). The prediction variances of the extreme intensity estimates from the
330 regional model are smaller for the model based on the subsample. This is illustrated in Figure 6
331 for one location. The differences in prediction variances are largest for smaller durations and
332 larger return periods. For 1-hour duration the uncertainty of the 2-year event estimate of the

333 regional model based on the full sample (relative standard deviation of 8.7%) is about twofold
 334 compared to the estimate based on the subsample (4.6%), and larger differences are seen for the
 335 100-year event estimate (23.6% and 9.2%, respectively). For the 24-hour duration the differences
 336 between the two models are smaller.

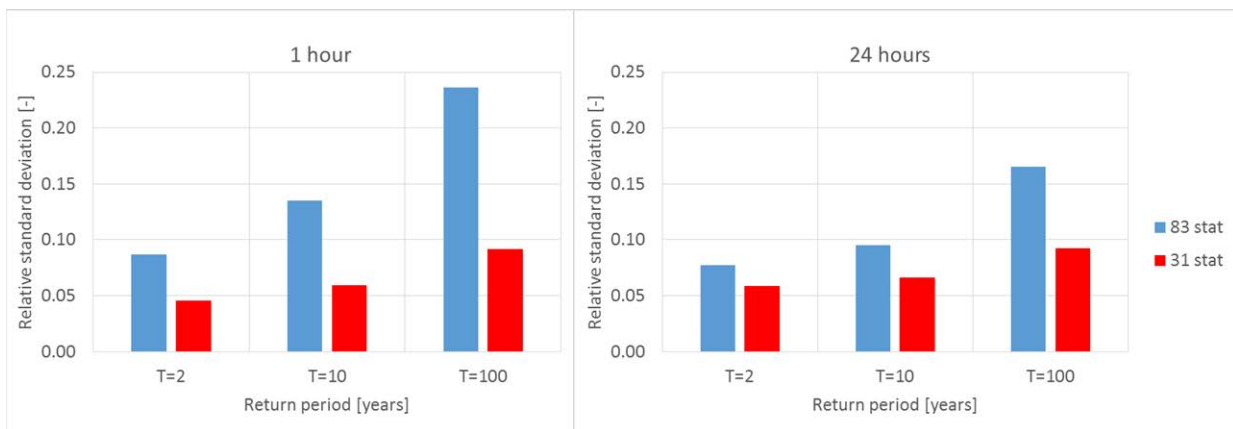
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338

339 **Figure 5** Ratio of regional average intensity estimates based on data from the full sample (83
 340 stations) and the subsample (31 stations) for different durations and return periods T .

341



342

343 **Figure 6** Relative standard deviation (standard deviation divided by intensity estimate) at a
 344 location with $MAP = 632$ mm and $\mu_{CGD} = 28.3$ mm for different return periods T
 345 using the regional model based on data from the full sample (83 stations) and the
 346 subsample (31 stations) for 1-hour (left) and 24-hour (right) durations.

347 For the Poisson parameter λ GLS regression results show, in general, larger R^2 values for the
348 subsample compared to the full sample, except for the intermediate durations 30-180 minutes.
349 However, due to the smaller sample, the subsample has larger sampling uncertainties resulting in
350 smaller RPV values for most durations. The estimated slope of the regression models are smaller
351 for the subsample for all durations and is not significant (at a 5% level) for the durations 30-360
352 minutes. In general, the subsample has a smaller range of λ -estimates over Denmark and smaller
353 prediction uncertainties. The results are summarised in Supplementary Material Table 1 and
354 Table 4.

355
356 For the mean value of threshold exceedances μ results from the subsample analysis show that the
357 relationship with μ_{CGD} is not significant for durations up to 3 hours where negative RPV values
358 and non-significant slope estimates (at a 5% level) are obtained. For larger durations, slope
359 estimates are significant for the subsample regressions but with smaller slope estimates (except
360 for 12-hour duration where similar slope estimates are found). In general, the subsample results
361 show smaller μ -estimates over Denmark. The subsample provides both smaller and larger
362 prediction uncertainties, depending on duration, than those obtained from the full sample. The
363 results are summarised in Supplementary Material Table 2 and Table 5.

364
365 For the shape parameter in the regional GP distribution κ larger (less negative) shape parameters
366 are obtained for the subsample, revealing lighter-tailed GP distributions. The subsample provides
367 smaller prediction uncertainties for durations larger than 10 minutes, except for 6-hour duration.
368 Results are summarised in Supplementary Material Table 3.

369

370 The analysis shows larger estimates of λ and μ in the full sample, which in combination with the
371 increase in station-years included in the regional model indicate an increasing trend in λ and μ .
372 These results correspond well with the findings of Gregersen *et al.* (2013) who analysed a subset
373 of the rainfall data used in this study, including 70 stations with 10–31 years of observations in
374 the period 1979–2009. They found a significant increasing trend of λ for all durations analysed
375 (1, 3, 6, 12 and 24 hours). Increasing trends were also found for μ for all durations, but they were
376 statistically significant only for 1 and 3-hour durations.

377

378 Larger estimates of λ and μ , and smaller (more negative) regional GP shape parameters in the
379 full sample all point towards larger intensity estimates as shown in Figure 5. The larger
380 prediction uncertainties generally found for λ , μ and κ using the full sample indicate that the
381 impact of non-stationarities is more important than the expected reduction in sampling
382 uncertainty for increasing sample size. However, it could also reflect an increase in the spatial
383 variability caused by adding additional stations in the analysis. It is very difficult to verify which
384 causes are predominant due to the spatial and temporal heterogeneity of the data.

385

386 **Comparison with previous studies**

387 In the previous regional studies of Danish rainfall extremes (Madsen *et al.*, 2002; 2009) it was
388 also found that the Poisson rate is significantly correlated with MAP. In Supplementary Material
389 Table 4 the range of λ -estimates over Denmark from the previous studies are compared to those
390 obtained in the current study. A general increase in λ is seen, with more pronounced increases
391 for smaller durations. It should be noted that in the studies by Madsen *et al.* (2002, 2009) a

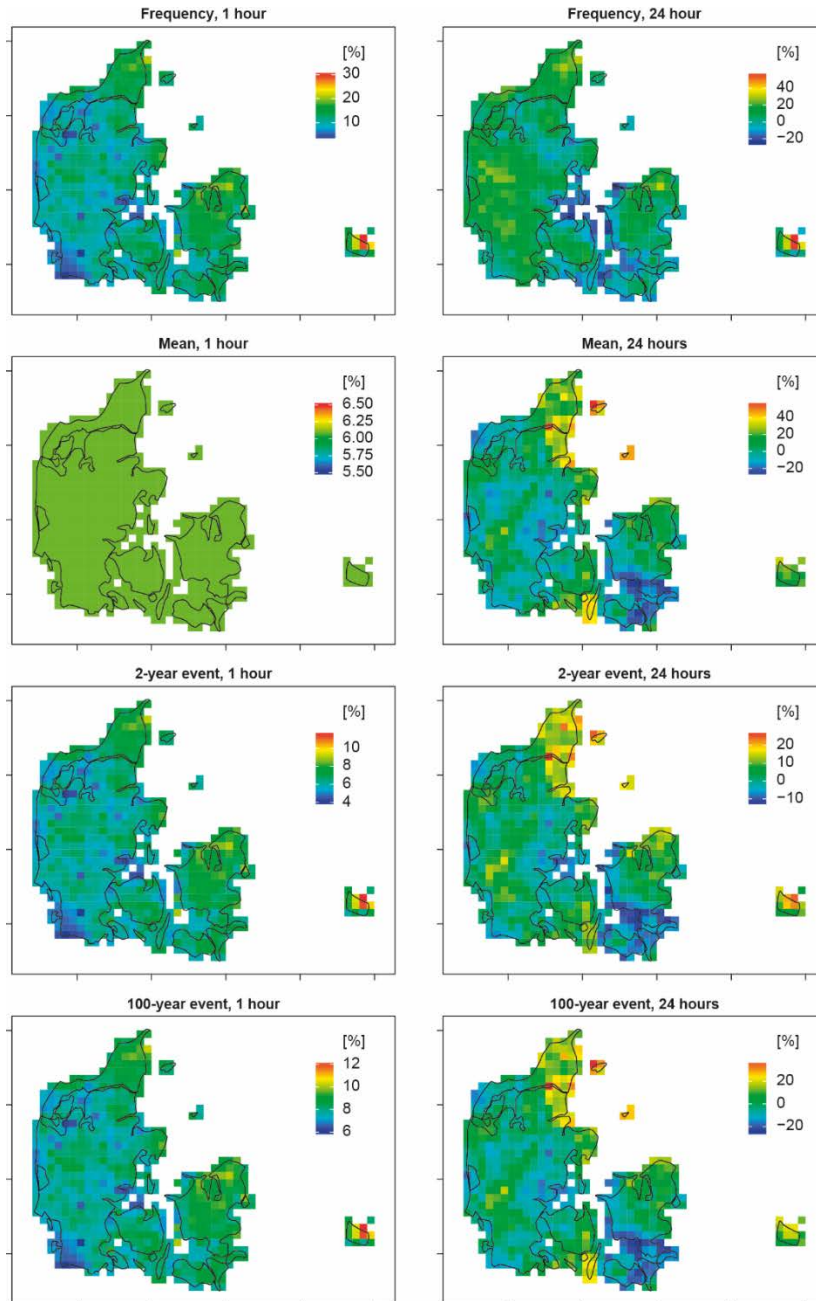
392 different MAP was used based on data from the standard normal period 1961-1990 (Frich *et al.*,
393 1997).

394
395 The regional variability of the mean value of threshold exceedances was in the previous studies
396 described by defining sub-regions with a constant mean. In the first study by Madsen *et al.*
397 (2002) a larger mean intensity was seen in the Copenhagen area for durations larger than 1 hour,
398 with differences between the western and eastern Copenhagen area for some durations. A
399 regional model was defined with three sub-regions, respectively, (i) Copenhagen East, (ii)
400 Copenhagen West, and (iii) the rest of the country. In the subsequent study by Madsen *et al.*
401 (2009) the regional model was revised. For durations up to 3 hours a regional mean model was
402 applied for the whole country, whereas for larger durations significant differences between west
403 and east Denmark were found and two sub-regions were defined, respectively, west and east of
404 the Great Belt. In this study new covariate information in terms of the extreme value statistic
405 μ_{CGD} is applied. For durations 3-48 hours a significant part of the regional variability can be
406 described by μ_{CGD} , hence allowing a more elaborate assessment of the regional variability as
407 compared to the previous studies. For durations smaller than 3 hours, the results of the current
408 study confirm the use of a regional mean model as in the previous studies. Regional model
409 estimates of μ from the different studies are compared in Supplementary Material Table 5. For
410 durations up to 1 hour a general increase in the regional mean of μ is seen. For larger durations,
411 the range of μ over Denmark shows an increasing trend.

412
413 With respect to the L-CV the current study provides similar results as the previous study,
414 supporting the use of a regional constant L-CV (GP shape parameter). Results from the different

415 studies are compared in Supplementary Material Table 3. For durations up to 6 hours there is, in
416 general, a decreasing trend towards more negative shape parameters (heavier-tailed
417 distributions), whereas for the largest durations 24-48 hours an increasing trend (lighter-tailed
418 distributions) is seen.

419



420

421 **Figure 7** Differences in [%] between estimates based on the regional model in Madsen *et al.*
422 (2009) and the new regional model for 1-hour intensity (left) and 24-hour intensity
423 (right). The figure shows from top to bottom changes in Poisson rate (frequency),
424 mean intensity, and 2- and 100-year intensities.

425

426 The regional model estimates of the current study and the study by Madsen *et al.* (2009) are
427 compared in Figure 7. For the 1-hour intensity there is an increase in the Poisson rate, with a
428 general increase from west (from about 2%) to east (up to about 30%). For the 24-hour intensity,
429 a larger variation in the Poisson rate is seen, ranging from -25% to 58%. For the 1-hour intensity
430 there is an increase in the mean intensity of about 6%, which is constant over Denmark since the
431 models have a regional constant mean intensity. For the 24-hour intensity the change in mean
432 intensity varies from -30% to 60%, with a regional pattern similar to μ_{CGD} (Figure 3, top right).
433 For the 1-hour intensity, the changes in the extreme intensities follow the west-east pattern of the
434 changes in the Poisson rate with an increase between 4% and 12% for the 2 and 100-year return
435 periods. For the 24-hour intensity, the changes in the 2 and 100-year intensities follow the
436 pattern of the changes in the mean intensity. There are both decreases and increases; from -13%
437 to 27% for the 2-year event, and from -26% to 40% for the 100-year event. Main increases are
438 seen in the northern part of Jutland, north-east Zealand, southern islands and Bornholm.

439

440

441 **DISCUSSION AND CONCLUSIONS**

442

443 A new regional model has been developed for estimation of IDF relationships of extreme rainfall
444 in Denmark. The model is based on 50% more data than used in the previous regional analysis
445 by Madsen *et al.* (2009) and uses new covariate information in terms of gridded rainfall statistics
446 from a dense network of gauges with daily measurements (CGD). The analysis confirms

447 previous results regarding the spatial variability of the Poisson rate; that is, the rate increases for
448 increasing MAP for all durations analysed between 1 minute and 48 hours. With respect to the
449 mean value of threshold exceedances μ , significant correlation with the mean extreme intensity
450 from CGD was found for durations between 3 and 48 hours. For durations below 3 hours μ is
451 assumed constant over Denmark in accordance with the previous studies. Finally, the analysis of
452 L-CV of the exceedance magnitudes confirms the previous studies, and a regional constant L-CV
453 (GP shape parameter) is applied in the model. The use of the mean extreme intensity from CGD
454 as covariate information in the regional model allows a more elaborate assessment of the
455 regional variability and a more consistent estimation of extreme rainfall intensities in Denmark.
456 Based on gridded maps of μ_{CGD} and MAP the IDF relationships can be estimated at an arbitrary
457 site in Denmark.

458

459 Compared to the previous study by Madsen *et al.* (2009) there is a general increase in extreme
460 rainfall intensity for durations up to 1 hour caused by a general increase in the Poisson rate and
461 the mean extreme intensity and a more negative GP shape parameter. For larger durations both
462 increases and decreases are seen due to the correlation with μ_{CGD} compared to the division into
463 two regions with constant mean extreme intensity in the previous study.

464

465 To analyse the impacts of using the temporal heterogeneous dataset a subsample analysis was
466 conducted including only stations that cover almost the entire observation period. The analysis
467 showed that the relatively larger contribution of station-years in recent years combined with
468 increases in λ and μ and decreasing (more negative) GP shape parameters give larger estimates
469 of extreme intensities compared to including only records that cover the full observation period

470 in the regional model. The regional model based on the full sample has larger prediction
471 uncertainty of intensity estimates than the model based on the subsample. This is due to the non-
472 stationarities in the data but may also reflect larger spatial variability in the full sample.

473

474 Gregersen *et al.* (2015) analysed long records of daily rainfall dating back to 1874 and found a
475 general increase in the Poisson rate but overlaid by a multi-decadal variability that indicated a
476 cyclic behaviour. The increase seen in recent years is much larger than the long-term trend but
477 may, at least to some extent, be attributed to the multi-decadal variability seen in the long
478 records. Since it is currently not possible to attribute the recent increases to anthropogenic
479 changes or natural variability, the regional model using the full sample provides the best estimate
480 according to current knowledge of extreme rainfall characteristics and associated uncertainties.
481 Rather than including the non-stationarities in the regional model implicitly as an additional
482 source of uncertainty, a model that explicitly describes non-stationarities in the PDS parameters
483 could be developed. This is currently being investigated.

484

485

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489 Research as part of the RiskChange project, contract no. 0603-00390
490 (<http://riskchange.dhigroup.com>).

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589

590 **SUPPLEMENTARY MATERIAL**

591

592 **Table 1** GLS regression results for the Poisson rate parameter λ using MAP as explanatory
 593 variable. Reduction in average prediction variance RPV , pseudo R^2 , estimated slope
 594 of regression equation $\hat{\beta}_1$ (10^{-3} years⁻¹/mm) with corresponding standard deviation
 595 (10^{-3} years⁻¹/mm) in parenthesis, and t-test significance level α .

Duration [min]	83 stations				31 stations			
	RPV	R^2	$\hat{\beta}_1$	α	RPV	R^2	$\hat{\beta}_1$	α
1	0.24	0.27	7.29 (1.64)	< 0.001	0.23	0.31	4.55 (1.57)	0.005
2	0.19	0.22	6.63 (1.68)	< 0.001	0.27	0.40	4.08 (1.37)	0.004
5	0.13	0.16	5.49 (1.69)	0.002	0.10	0.21	2.89 (1.38)	0.04
10	0.10	0.13	5.88 (1.91)	0.003	0.09	0.18	3.29 (1.55)	0.04
30	0.06	0.08	4.34 (1.77)	0.02	-0.04	0.04	1.99 (1.53)	0.20
60	0.01	0.04	3.26 (1.80)	0.07	-0.08	0	1.39 (1.59)	0.38
180	0.02	0.05	3.35 (1.66)	0.05	-0.07	0	1.48 (1.67)	0.38
360	0.06	0.09	4.36 (1.63)	0.009	0.02	0.09	2.91 (1.63)	0.08
720	0.11	0.15	5.52 (1.60)	0.001	0.15	0.23	4.25 (1.56)	0.008
1440	0.30	0.33	8.85 (1.58)	< 0.001	0.46	0.55	7.39 (1.50)	< 0.001
2880	0.54	0.59	12.4 (1.47)	< 0.001	0.66	0.73	11.0 (1.61)	< 0.001

596

597

598 **Table 2** GLS regression results for the mean μ using μ_{CGD} as explanatory variable. Reduction
 599 in average prediction variance RPV , pseudo R^2 , estimated slope of regression
 600 equation $\hat{\beta}_1$ ($\mu\text{m/s/mm}$) with corresponding standard deviation ($\mu\text{m/s/mm}$) in
 601 parenthesis, and t-test significance level α .

Duration [min]	83 stations				31 stations			
	RPV	R^2	$\hat{\beta}_1$	α	RPV	R^2	$\hat{\beta}_1$	α
1	0.01	0.08	2.09E-01 (1.20E-01)	0.09	-0.10	0	1.53E-01 (1.63E-01)	0.35
2	0.05	0.15	2.13E-01 (1.08E-01)	0.05	-0.11	0.01	1.54E-01 (1.47E-01)	0.30
5	0.16	0.28	2.17E-01 (8.72E-02)	0.01	-0.02	0.17	1.80E-01 (1.17E-01)	0.13
10	0.04	0.15	1.28E-01 (6.55E-02)	0.06	-0.43	0.01	8.18E-02 (8.12E-02)	0.32
30	0.05	0.12	9.12E-02 (4.14E-02)	0.03	-0.34	0	2.71E-02 (5.02E-02)	0.59
60	-0.03	0.04	4.26E-02 (2.81E-02)	0.13	-0.46	0	2.10E-03 (3.22E-02)	0.95
180	0.05	0.17	3.33E-02 (1.28E-02)	0.01	-0.09	0.25	2.89E-02 (1.60E-02)	0.07
360	0.13	0.25	2.77E-02 (8.10E-03)	0.001	0.01	0.39	2.29E-02 (9.90E-03)	0.02
720	0.31	0.60	1.94E-02 (4.41E-03)	< 0.001	0.40	1.00	1.95E-02 (5.80E-03)	0.001
1440	0.44	0.75	1.35E-02 (2.42E-03)	< 0.001	0.26	0.79	1.09E-02 (3.34E-03)	0.002
2880	0.13	0.27	5.26E-03 (1.45E-03)	< 0.001	-0.06	0.40	3.75E-03 (1.88E-03)	0.05

602

603

604

605 **Table 3** GLS regression results for the shape parameter κ . Regional estimate of GP shape
 606 parameter and corresponding standard deviation in parenthesis for current and
 607 previous studies.

Duration [min]	1979-2012 (83 stations)	1979-2012 (31 stations)	1979-2005 ¹ (66 stations)	1979-1997 ² (41 stations)
1	-0.158 (0.0767)	-0.125 (0.0591)	-0.152 (0.104)	-0.132 (0.103)
2	-0.110 (0.0681)	-0.0803 (0.0740)	-0.0971 (0.0621)	-0.101 (0.136)
5	-0.0743 (0.0399)	-0.0549 (0.0609)	-0.0769 (0.0209)	-0.0616 (0.0965)
10	-0.122 (0.0417)	-0.107 (0.0615)	-0.116 (0.0410)	-0.0620 (0.0286)
30	-0.207 (0.0500)	-0.185 (0.0193)	-0.200 (0.0350)	-0.165 (0.0274)
60	-0.207 (0.0733)	-0.182 (0.0267)	-0.205 (0.0615)	-0.134 (0.0309)
180	-0.175 (0.0768)	-0.140 (0.0248)	-0.170 (0.0333)	-0.0806 (0.0395)
360	-0.180 (0.0233)	-0.174 (0.0259)	-0.189 (0.0628)	-0.155 (0.0427)
720	-0.137 (0.0680)	-0.107 (0.0596)	-0.145 (0.0658)	-0.134 (0.0495)
1440	-0.124 (0.0644)	-0.103 (0.0299)	-0.149 (0.0945)	-0.169 (0.0479)
2880	-0.0894 (0.0681)	-0.0754 (0.0325)	-0.105 (0.0910)	-0.106 (0.109)

608 ¹Madsen *et al.* (2009), ²Madsen *et al.* (2002)

609

610

611 **Table 4** Range over Denmark of Poisson rate parameter λ (years⁻¹) and corresponding
612 standard deviation in parenthesis (years⁻¹) with MAP as explanatory variable for
613 current and previous studies.

Duration [min]	1979-2012 (83 station)	1979-2012 (31 stations)	1979-2005 ¹ (66 stations)	1979-1997 ² (41 stations)
1	3.13 – 6.10 (0.628 – 0.752)	3.43 – 5.29 (0.406 – 0.571)	2.74 – 5.35 (0.539 – 0.614)	2.63 – 4.36 (0.482 – 0.609)
2	3.23 – 5.93 (0.658 – 0.784)	3.50 – 5.16 (0.314 – 0.467)	2.82 – 5.02 (0.528 – 0.599)	2.60 – 4.21 (0.280 – 0.406)
5	3.27 – 5.50 (0.661 – 0.786)	3.51 – 4.69 (0.324 – 0.475)	2.73 – 4.77 (0.540 – 0.610)	2.36 – 4.00 (0.323 – 0.436)
10	3.62 – 6.01 (0.756 – 0.897)	3.86 – 5.20 (0.378 – 0.543)	3.09 – 5.12 (0.557 – 0.629)	2.63 – 4.30 (0.398 – 0.512)
30	3.43 – 5.19 (0.678 – 0.811)	3.68 – 4.49 (0.379 – 0.540)	2.88 – 4.57 (0.568 – 0.640)	2.43 – 4.30 (0.471 – 0.586)
60	3.47 – 4.79 (0.675 – 0.811)	3.64 – 4.21 (0.394 – 0.560)	2.88 – 4.42 (0.583 – 0.655)	2.50 – 4.16 (0.478 – 0.592)
180	3.02 – 4.39 (0.590 – 0.719)	3.26 – 3.86 (0.436 – 0.604)	2.77 – 4.15 (0.562 – 0.636)	2.56 – 3.82 (0.464 – 0.576)
360	2.56 – 4.33 (0.591 – 0.716)	2.77 – 3.96 (0.433 – 0.594)	2.32 – 4.07 (0.511 – 0.579)	2.16 – 4.00 (0.350 – 0.442)
720	2.08 – 4.33 (0.593 – 0.713)	2.26 – 3.99 (0.422 – 0.575)	1.82 – 3.85 (0.481 – 0.548)	1.66 – 4.11 (0.285 – 0.377)
1440	1.74 – 5.35 (0.574 – 0.695)	2.02 – 5.03 (0.395 – 0.543)	1.63 – 4.62 (0.513 – 0.573)	1.31 – 5.01 (0.318 – 0.408)
2880	1.57 – 6.61 (0.498 – 0.614)	1.87 – 6.34 (0.436 – 0.594)	1.67 – 5.94 (0.482 – 0.538)	1.40 – 5.88 (0.354 – 0.453)

614 ¹Madsen *et al.* (2009), ²Madsen *et al.* (2002)

615

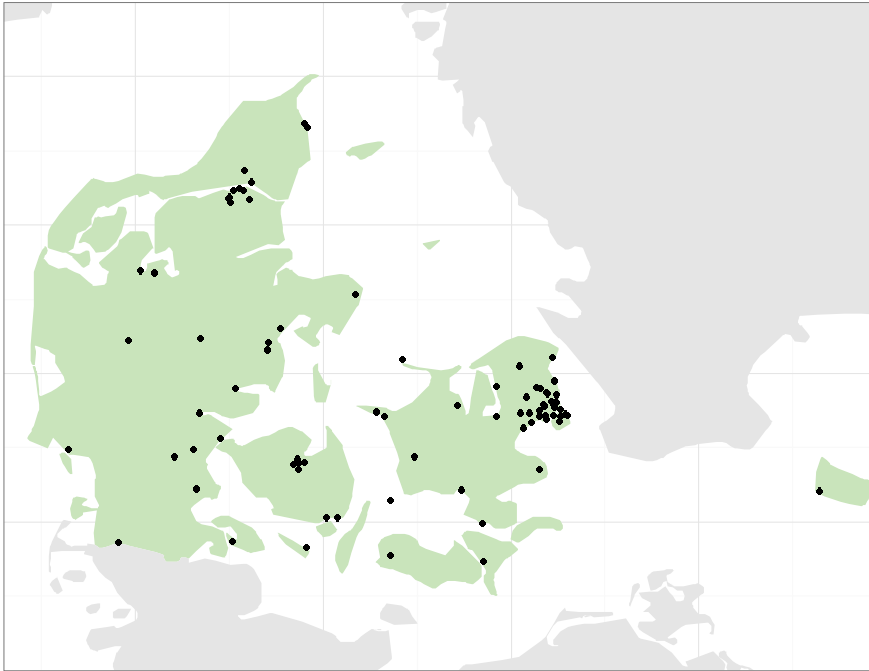
616 **Table 5** Range over Denmark of mean μ ($\mu\text{m/s}$) and corresponding standard deviation in
 617 parenthesis ($\mu\text{m/s}$) for current study using μ_{CGD} as explanatory variable and previous
 618 studies based on sub-regional divisions.

Duration [min]	1979-2012 (83 station)	1979-2012 (31 stations)	1979-2005 ¹ (66 stations)	1979-1997 ² (41 stations)
1	6.22 (0.491)	6.03 (0.520)	5.97 (0.368)	5.85 (0.766)
2	5.99 (0.380)	5.84 (0.418)	5.78 (0.345)	5.47 (0.689)
5	4.90 (0.295)	4.80 (0.286)	4.71 (0.191)	4.54 (0.541)
10	3.58 (0.225)	3.49 (0.124)	3.45 (0.129)	3.33 (0.110)
30	1.82 (0.165)	1.76 (0.102)	1.74 (0.0572)	1.61 (0.0551)
60	1.10 (0.114)	1.05 (0.0582)	1.03 (0.0464)	0.948 (0.0354)
180	0.410 – 0.608 (0.0386 – 0.0595)	0.405 – 0.577 (0.0286 – 0.0658)	0.466 (0.0188)	0.432 – 0.517 (0.0246 – 0.0757)
360	0.222 – 0.387 (0.0247 – 0.0377)	0.224 – 0.360 (0.0172 – 0.0405)	0.263 – 0.292 (0.0244 – 0.0279)	0.257 – 0.340 (0.0181 – 0.0479)
720	0.128 – 0.243 (0.00956 – 0.0180)	0.130 – 0.246 (0.00775 – 0.0230)	0.167 – 0.183 (0.0203 – 0.0277)	0.162 – 0.234 (0.0130 – 0.0284)
1440	0.0725 – 0.153 (0.00505 – 0.00980)	0.0757 – 0.140 (0.00526 – 0.0136)	0.0921 – 0.115 (0.00755 – 0.0151)	0.0940 – 0.131 (0.00872 – 0.0218)
2880	0.0489 – 0.0802 (0.00460 – 0.00690)	0.0507 – 0.0730 (0.00381 – 0.00810)	0.0551 – 0.0700 (0.00436 – 0.00834)	0.0581 – 0.0756 (0.00499 – 0.0127)

619 ¹Madsen *et al.* (2009), ²Madsen *et al.* (2002)

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623

624 **Figure 1** Location of the high-resolution rain gauges used in the study.