

Technical University of Denmark



## Power Curves in a Wind Turbine Array: A Numerical Study

Meyer Forsting, Alexander Raul

*Publication date:*  
2016

*Document Version*  
Publisher's PDF, also known as Version of record

[Link back to DTU Orbit](#)

*Citation (APA):*  
Meyer Forsting, A. R. (2016). Power Curves in a Wind Turbine Array: A Numerical Study. Poster session presented at Wind Europe Summit 2016, Hamburg, Germany.

### DTU Library

Technical Information Center of Denmark

---

#### General rights

Copyright and moral rights for the publications made accessible in the public portal are retained by the authors and/or other copyright owners and it is a condition of accessing publications that users recognise and abide by the legal requirements associated with these rights.

- Users may download and print one copy of any publication from the public portal for the purpose of private study or research.
- You may not further distribute the material or use it for any profit-making activity or commercial gain
- You may freely distribute the URL identifying the publication in the public portal

If you believe that this document breaches copyright please contact us providing details, and we will remove access to the work immediately and investigate your claim.



# Power Curves in a Wind Turbine Array: A Numerical Study

Alexander R Meyer Forsting (alrf@dtu.dk),  
Niels Troldborg



DTU Wind Energy  
Department of Wind Energy

PO.276

## Abstract

The impact of **measuring a power curve inside a wind turbine array** is investigated using **computational fluid dynamics**. The array consists of five aligned rotors that yaw with the free-stream wind direction. The flow-field in front of a wind turbine array changes with wind direction and hence the individual power output of each turbine. By incorporating the current IEC standards on power performance measurements, the bias in the power performance of turbines in an array over an isolated rotor is determined. The **power change depends on the position of the turbine** in the array and reaches **maximally 9.03%** and **minimally -0.84%**.

## Introduction

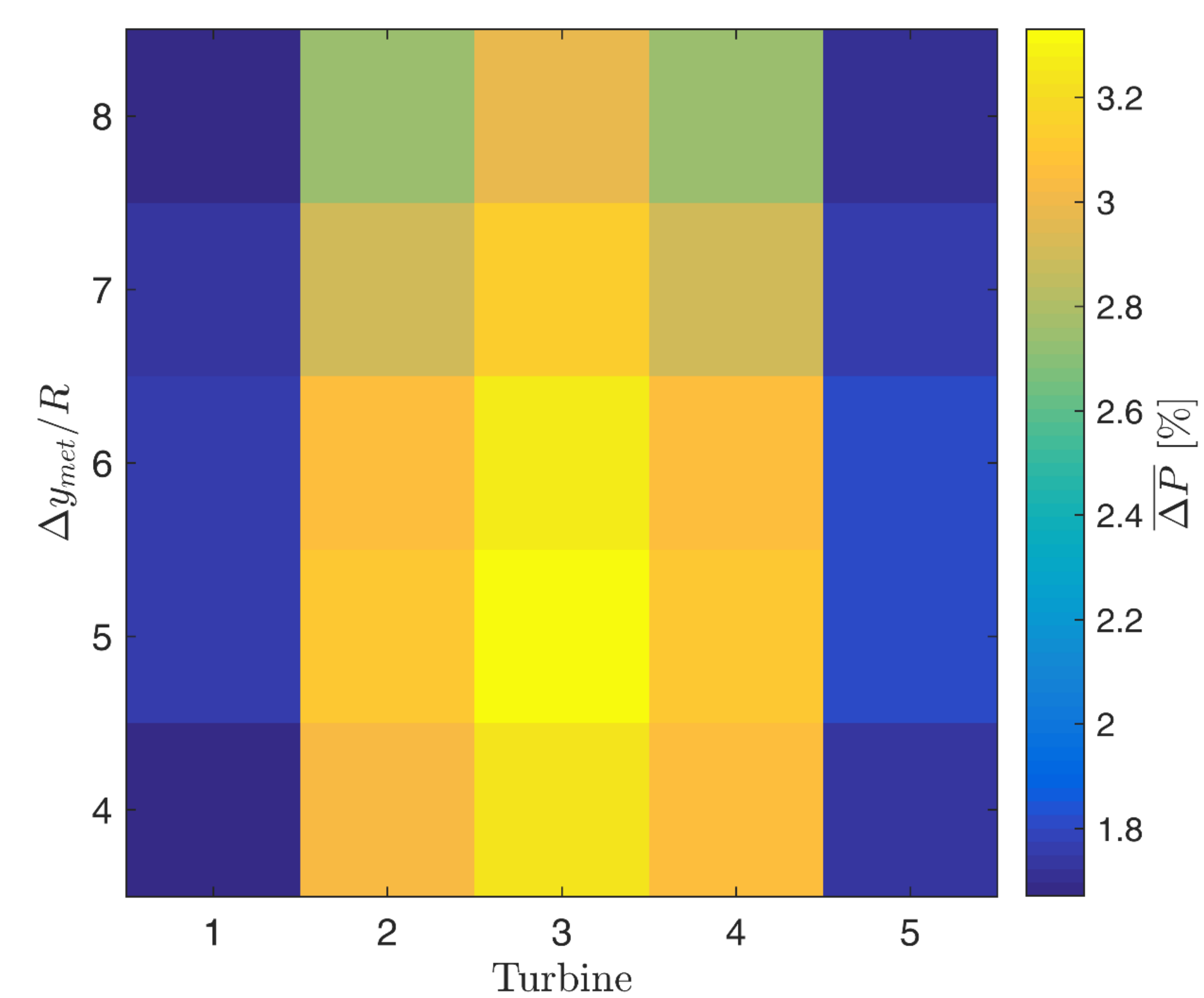
- Rotor thrust decelerates flow upstream continuously
- A **free-stream velocity reference** is needed for measuring the **power curve**
- **IEC standards** [1] expect the velocity reference to lie between **4 to 8 rotor radii (R) upstream** at hub height
- **Turbine arrays decelerate flow differently**, than a single turbine [2]
- **Changes in the flow are directly linked to power curves**

## Method

### Computational Fluid Dynamics Simulations

- Reynolds-averaged Navier-Stokes (**RANS**) simulations with in-house solver **EllipSys3D** [3]
- Modified  $k - \epsilon$  turbulence model
- Actuator disc model for **NREL 5MW** [4] without tower nor nacelle;  $R = 63$  m, hub at 90m
- **Sheared inflow** following log-law with roughness length  $z_0 = 0.05$
- Simulations covered entire velocity range below rated: **3 m/s to 11.4 m/s** at hub height
- The **wind directions  $\theta$**  were set to **0° and 45°**

## Results

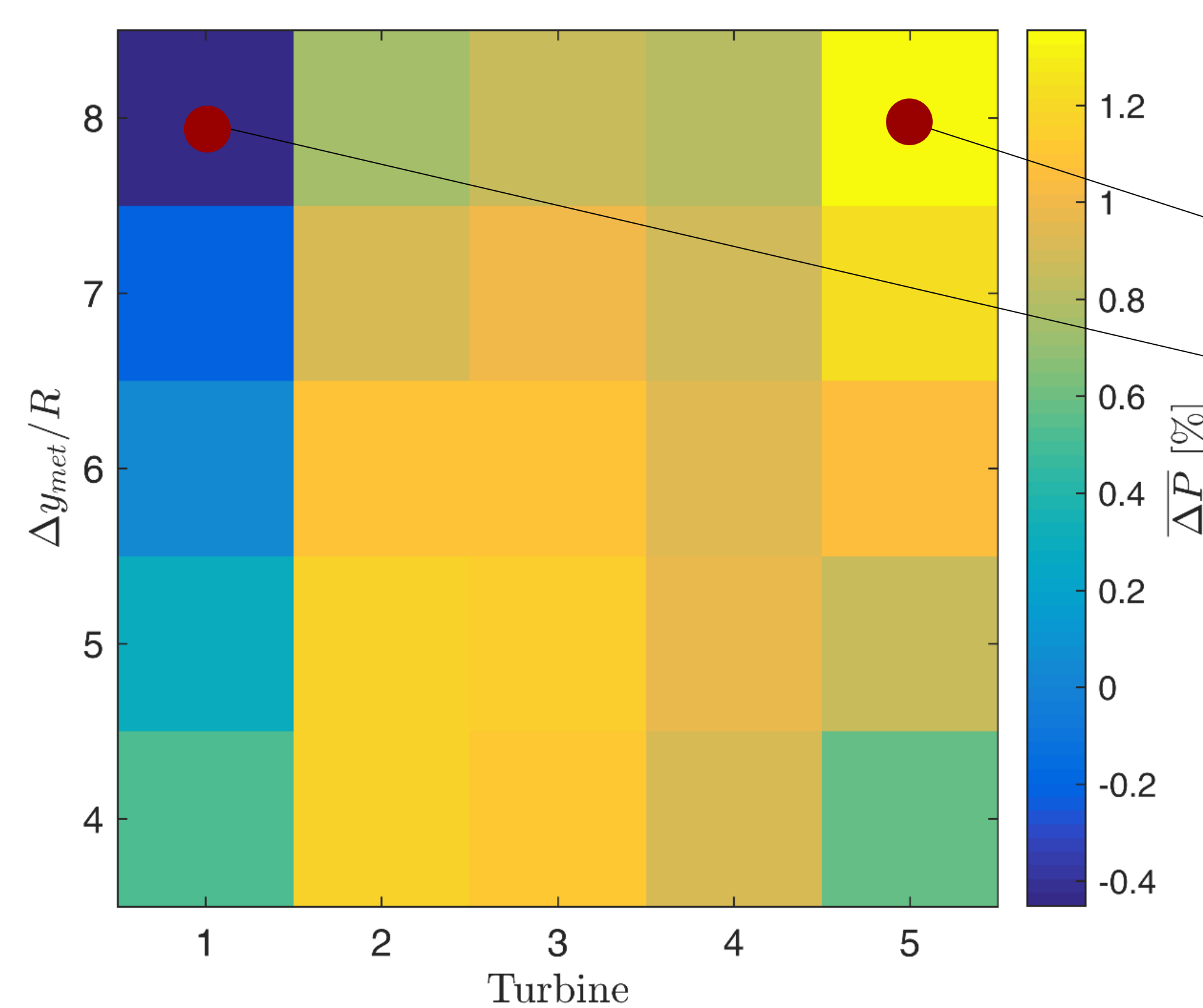


**Figure 3:** Average change in the power curve for an inflow angle  $\theta$  of 0° as a function of the turbine and the probe location upstream.

- The difference to an isolated power curve is calculated

$$\Delta P = \frac{P - P_{iso}}{P_{iso}}$$

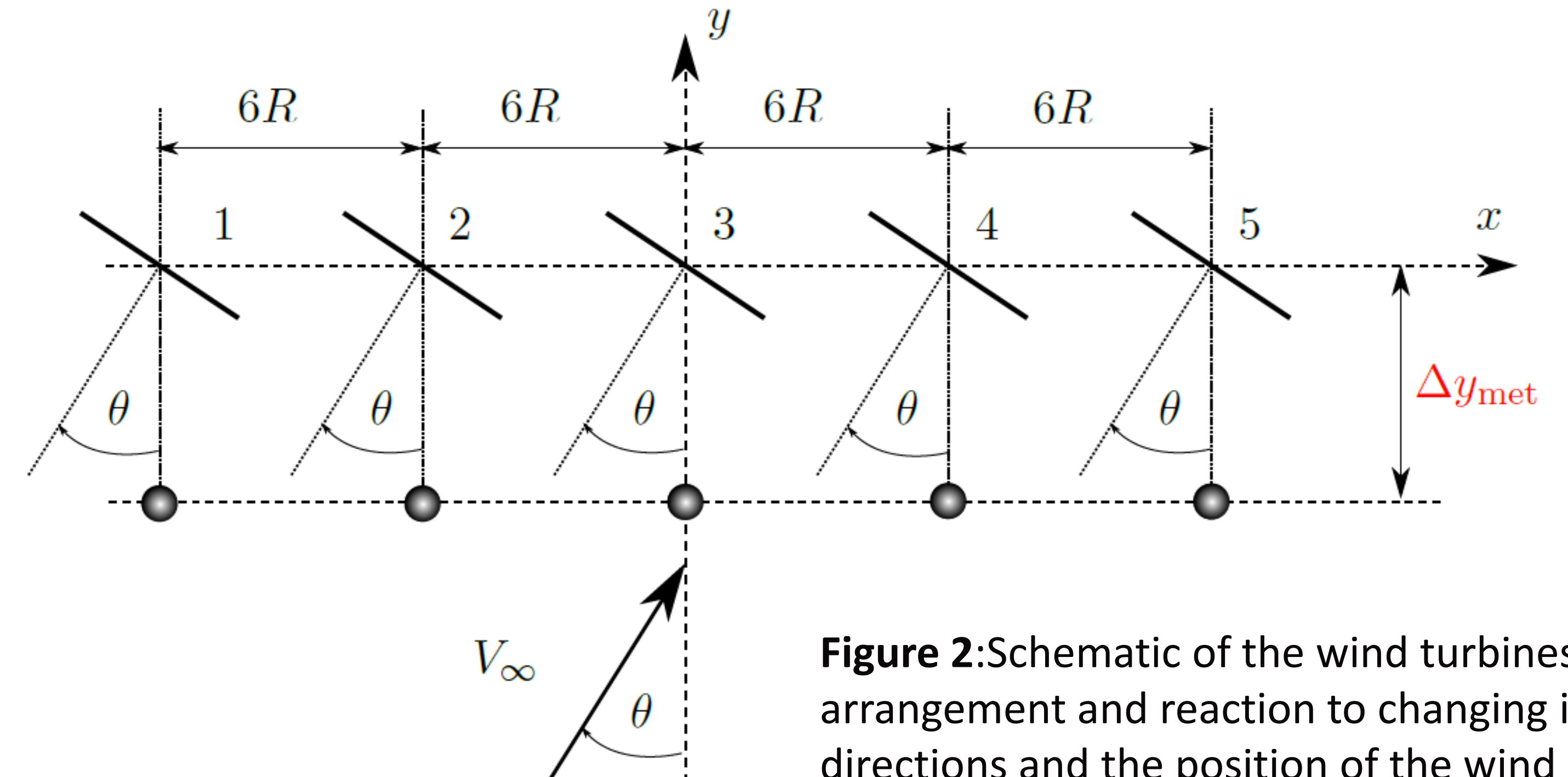
$\max(\Delta P), \theta = 0^\circ$     9.03% for T3 and  $\Delta y_{met}/R = 3.0$   
 $\min(\Delta P), \theta = 0^\circ$     0.84% for T1 and  $\Delta y_{met}/R = 2.0$   
 $\max(\Delta P), \theta = 45^\circ$     3.03% for T3 and  $\Delta y_{met}/R = 2.5$   
 $\min(\Delta P), \theta = 45^\circ$     -0.84% for T5 and  $\Delta y_{met}/R = 2.0$



**Figure 4:** Average change in the power curve for an inflow angle  $\theta$  of 45° as a function of the turbine and the probe location upstream.



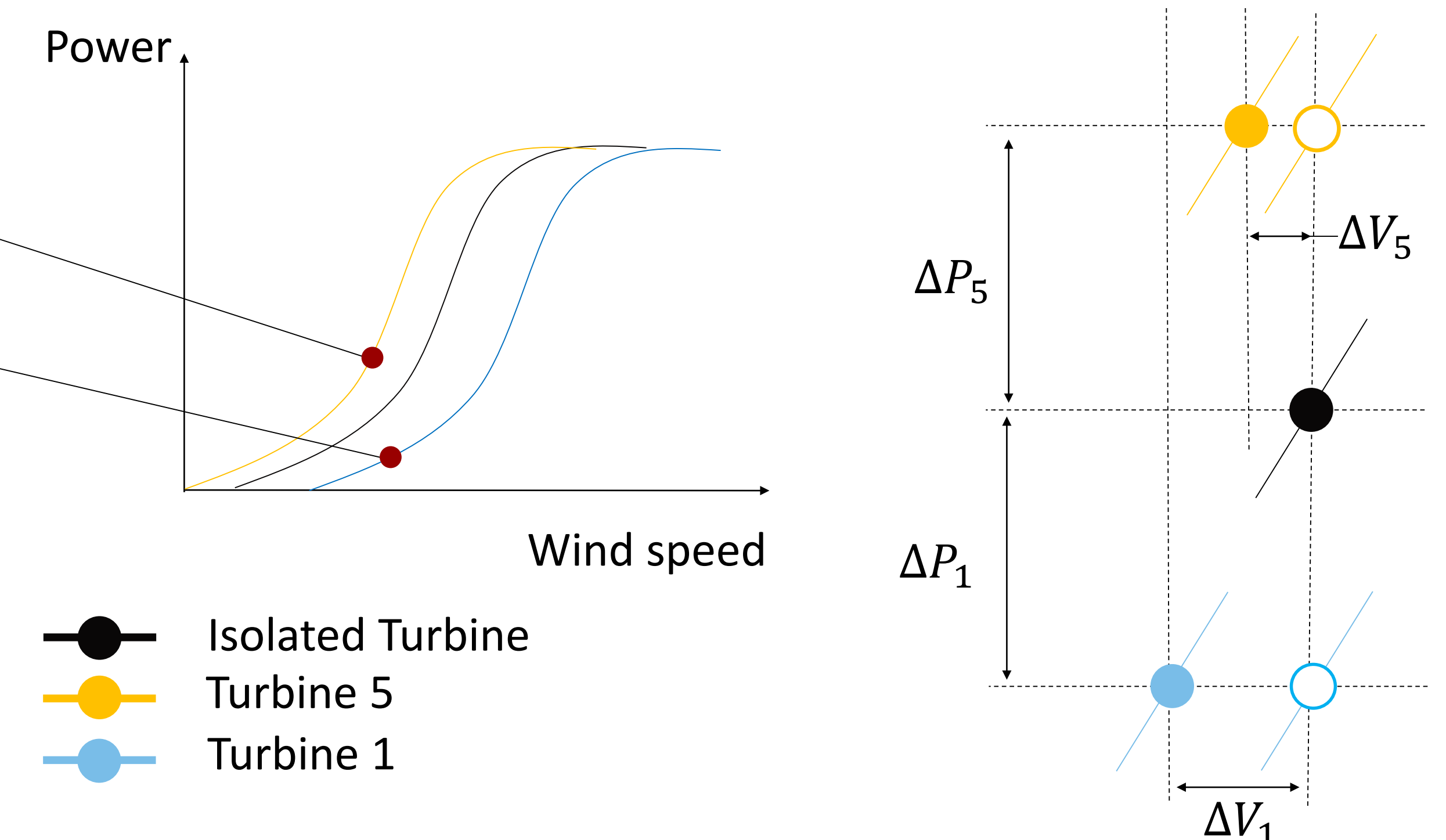
**Figure 1:** DTU test site Høvsøre



**Figure 2:** Schematic of the wind turbines' arrangement and reaction to changing inflow directions and the position of the wind speed measurements

### Numerical setup

- **Generic turbine arrangement** shown in Figure 2 with **resemblance** of a common turbine **testing facility** as DTU Høvsøre (Figure 1)
- Turbines followed the wind direction  $\theta$
- Velocity was probed at hub height,  $\Delta y_{met}$  upstream of each turbine
- $\Delta y_{met}/R = 4.0, 5.0, 6.0, 7.0, 8.0$



**Figure 5:** Demonstration of the underlying reasons for the changes in power. As outlined in detail in [2] the flow accelerates along the row of turbines, resulting in rotor 5 **producing more power** than rotor 1. In fact the **power drops for rotor 1**, as it is experiencing larger deceleration upstream than an isolated turbine. However, the **changing velocities also affect the reference velocities**, making the loss in power produced by rotor 1 appear smaller as function of wind speed. Turbine 5 seems to produce even more power as its power curve is shifted to the left.

## Acknowledgements

This work was performed inside the **UniTe project (unitte.dk)**, which is financed by The Innovation Fund Denmark, grant number 1305-00024B. Special thanks also to Antoine Borraccino

## References

1. IEC 61400-12-1:2005, Power performance measurements of electricity producing wind turbines.
2. Meyer Forsting AR, Troldborg N, Gaunaa M. The flow upstream of a row of aligned wind turbine rotors and its effect on power production. *Wind Energy*. 2016. Available from: 10.1002/we.1991

3. Sørensen N. General purpose flow solver applied to flow over hills. *PhD Thesis, Risø National Laboratory 1995*.
4. Jonkerman J, Butterfield S, Musial W, Scott G. Definition of a 5-mw reference wind turbine for offshore system development. *Technical Report, NREL 2009*.

