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Application of Network-Constrained Transactive Control to Electric Vehicle Charging for Secure Grid Operation

Junjie Hu, *Member, IEEE*, Guangya Yang, *Senior Member, IEEE*, Henrik W. Bindner, *Member, IEEE*, and Yusheng Xue, *Member, IEEE*

Abstract—This paper develops a network-constrained transactive control method to integrate distributed energy resources (DERs) into a power distribution system with the purpose of optimizing the operational cost of DERs and power losses of the distribution network as well as preventing grid problems including power transformer congestion and voltage violations. In this method, a price coordinator is introduced to facilitate the interaction between the distribution system operator and aggregators in the smart grid. Electric vehicles are used to illustrate the proposed network-constrained transactive control method. Mathematical models are presented to describe the operation of the control method. Finally, simulations are presented to show the effectiveness of the proposed method. To guarantee its optimality, we also checked the numerical results obtained with the network-constrained transactive control method and compared them with the one solved by centralized control, and found a good performance of the proposed control method.

Index Terms—Distributed decision making, grid-interactive energy sources, network-constrained operation, transactive control.

I. INTRODUCTION

THE increasing penetration of distributed energy resources including renewable generations such as wind turbine and photovoltaic generation, electric vehicles etc flexible loads requires enhanced operation at distribution system level as well as closer interaction between distribution system level operation and transmission system level operation. For example, as suggested in [1], the functions at distribution system level should include grid operator function and market operator function. The grid operator secures the network operation while the market operator coordinates the electricity purchase and sale, and the interchange of power to other markets. In [2], a hierarchical electric market structure consisting of wholesale electricity market and distribution network electricity market is proposed to facilitate the coordination of energy markets in distribution and transmission networks. The proposed market structure

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enables the integration of microgrids, which provide energy and ancillary services in distribution networks.

The enhanced operation at distribution system level makes it possible to explore and engage DERs' flexibility potentials via different approaches, centralized mechanism have been proposed in studies [3], [4]. In [3], the proposed system integrates demand side management and active distributed generation in the wholesale market via a centrally optimized EMS (energy management system), which allows a better exploitation of renewable energy sources and a reduction of the customers energy consumption costs with both economic and environmental benefits. To distinguish the characteristics of inflexible load and flexible load, the authors in [4] presented optimal pricing tariff for flexible loads in distribution networks which ensures cost saving for them. The optimal pricing tariff is solved centrally by a load serving entity sitting at distribution system level. Although the centralized approach yields the optimal outcome from the global perspective, the method has drawbacks in term of its communication and computational scalability, privacy concerns issue. Alternatively, transactive control is proposed and promoted to manage the operation of DERs resources and flexibilities. Transactive control is defined as "a set of economic and control mechanisms that allows the dynamic balance of supply and demand across the entire electrical infrastructure using value as a key operational parameter" by the GridWise Architecture Council [5] and has been successfully applied in several demonstration projects in the US and Europe [6]. The intent of the control framework is to reach equilibriums by standardizing a scalable, distributed mechanism via exchanging information about generation, consumptions, constraints and responsive assets over dynamic, real-time forecasting periods using economic incentive signaling, and thus solving the increasingly complex power system problems.

In [7], a transactive control method named "PowerMatcher" was developed to balance supply and demand in electricity networks. In the PowerMatcher method each device is represented by a control agent, which tries to operate the process associated with the device in an economically optimal way. The design of the PowerMatcher is based on the theoretical finding that computational economies of local control agents using a dynamic pricing mechanism are able to handle scarce resources adaptively in ways that are optimal locally as well as globally. In [8], a hierarchical transactive control architecture is proposed to integrate renewables in smart grids considering the operation at primary, secondary and tertiary control levels. The transactive

control framework is applied at the tertiary control level with the purpose of using optimal allocation of resources in the presence of uncertainties in terms of renewables and loads. In [9], an integrated dynamic market mechanism is proposed that combines real-time market and frequency regulation allowing renewable generators and flexible consumers to iteratively negotiate electricity prices, with purpose of reducing the cost of regulation reserves. In [10], a transactive control framework is used to coordinate a population of thermostatically controlled loads with the purpose of allocating energy economically subject to a peak energy constraint. A mechanism is proposed in the paper to implement the desired social choice function in dominant strategy equilibrium.

As transactive control's application to electric vehicle (EV) integration studies, the authors in [11] propose a scalable three-step approach to manage the charging of electric vehicles on the demand side with the purpose of minimizing charging cost of EVs. The three steps consist of aggregation, optimization and control. Transactive control is applied in the third step, i.e., the real-time control step to divide the optimal power generated in step 2 among the individual EVs, which is determined by a priority-based scheme. The work is further developed in [12] where an event-driven dual coordination mechanism is presented at the real-time control level. The simulation result indicated that the number of messages exchanged with the EVs was significantly reduced, by at least 64%.

Although the transactive control framework has been widely used in the smart grid to reach an energy balance between supply and demand as well as for demand response management [7]–[12], such studies do not consider the network that is an indispensable factor in operational study. For example, as indicated in [13]–[15], a large penetration of EVs also means new loads on the electric utilities, and undesirable congestion and voltage violations may exist in the distribution network when the batteries are recharged because of uncoordinated or solely cost-minimization-based charging. The latter means the EVs react to the wholesale price/regulating power price in a correlated way, for example, all EVs are charged when electricity prices are low, it might create a new peak demand at that time. Typically, the challenges in the distribution grid caused by the increasing electricity consumption of EVs are resolved by expensive expansion of the grid to match the size and the pattern of demand. Alternatively, in a smart grid context, the problem of violation of grid constraints can also be solved smartly using advanced control strategies such as transactive control supported by an increased use of information and communication technology. To address the conflicting challenges, transactive control frameworks were used in [16] for the charging of electric vehicles that incorporated distribution transformer and voltage constraints. A hierarchical multi-agent structure was used in [16] that consists of auctioneer agent, substation agent, and EV device agent. The substation agent summed up the bid functions of all the underlying EV device agents in a low voltage network and in turn sent the bid function to the unique auctioneer agent who defined the equilibrium price. In addition, the substation agent also ensured that the grid constraints were not violated given the possible equilibrium price. But, the current application

of transactive control [7]–[12], [16] mainly focuses on real time operation that may limit its application in power systems where "scheduling and control" is a vital and useful operational principle.

This paper develops a multiple periods network-constrained transactive control method to integrate distributed energy resources (DERs) into the power distribution system, in particular using electric vehicles as an illustration. By the term network-constrained transactive control, we mean that network constraints including power transformer capacity and voltage limitations are considered in transactive control applications for integrating distributed energy resources like electric vehicles. With the extension to multiple periods, the energy inter-temporal characteristics of DERs, such as the dynamics of EV charging can be considered in the optimization. To implement the proposed network-constrained transactive control, a price coordinator is introduced in this study to coordinate the power flow between the distribution network operator and commercial actors, i.e., the aggregators, which fits the operations under the deregulated electricity market environment. As a result of including network constraints, the method will be able to provide granular information for locational marginal prices of each period at each bus. Besides, the method also includes power loss in the objective function that is one of the concerns of distribution operation. In addition, we compare the optimality of the numerical result obtained with the network-constrained transactive control method with one solved by centralized control; the results indicate good performance of the proposed transactive control method.

The remainder of the paper is organized as follows. In Section II, an energy management system using a transactive control framework is described to integrate distributed energy resources. A network-constrained transactive control method is presented in Section III. Section IV presents simulations to illustrate the performance of the proposed method. Finally, discussion and conclusions are made in Section V.

II. CONTROL SYSTEM DESCRIPTION

Fig. 1 presents the network-constrained transactive control system for distributed energy resources integration. In the system, several aggregators are specified to manage DERs and interact with a distribution system operator and a price coordinator to eliminate grid congestion and prevent voltage violations. The current system specifically introduces a price coordinator that facilitates the interactions between the DSO and aggregators. Note that the energy dispatch used is based on the spot market, since the aggregators procure the electricity when the price is low. The state of the distribution network is not considered which means a conflicting situation might happen, e.g., aggregators who aim to procure the energy from the spot market in a lower price period, while the power brings operational challenges to distribution networks.

In order to integrate DERs smoothly into the distribution network, novel control relationships are needed for the management system. In the proposed two-stage control system: 1) each aggregator centrally generates an individually optimal energy

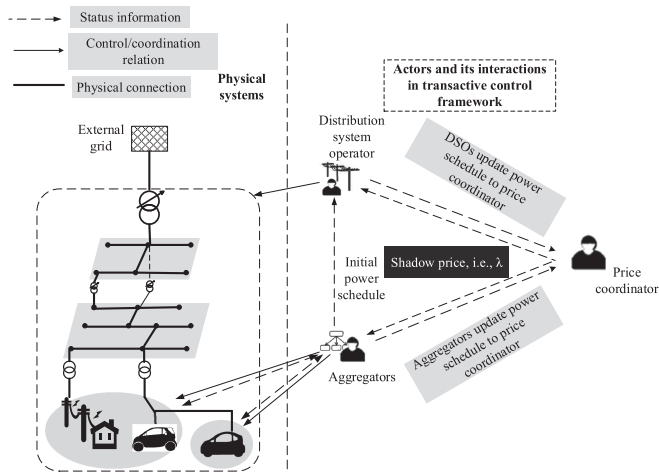


Fig. 1. A network-constrained transactive control system for distributed energy resources integration.

198 schedule for DERs as well as an aggregated power schedule
 199 over the whole scheduling period; 2) the aggregators and DSO
 200 interact with the price coordinator to reach a power consensus
 201 on each bus of the distribution network via iterative information
 202 exchange on price and power, if the aggregators' power schedule
 203 could potentially cause network problems to DSO. The information
 204 exchange on the power schedule and the shadow price
 205 i.e. $\lambda(i, l)$ used by the transactive control can be enabled and
 206 operated by the DSO, the aggregators and the price coordinator
 207 based on current infrastructure. Note regarding how to handle
 208 the shadow price in practice, suggestions have been made in
 209 the literature. In [16], the authors assumed that the customers
 210 are not charged the equilibrium price in the auction-based market/
 211 transactive control, instead, the equilibrium price is interpreted
 212 as a control signal that guarantees the necessary reserves are
 213 provided. Alternatively, it is argued in [5] that dynamic price
 214 at distribution system level should have real economical incentive.
 215 We recognise the value of $\lambda(i, l)$ represents a compromise
 216 between the utility of customer and the interests of grid, which
 217 shares similar features of the distribution locational marginal
 218 prices in [17]. Although straight-forward and easy to implement,
 219 the model [17] brings about the risk of causing new peaks
 220 in the grid due to unconfirmed power schedule of aggregators
 221 to the DSO. Instead, the method proposed in this study can guarantee
 222 explicit power limits issued to the aggregators for the DSO
 223 when solving grid congestion, because the price and the power
 224 schedules are fixed after a price-clearing mechanism. Furthermore,
 225 the implementation of the shadow price in the settlement
 226 phase is out of the scope of the paper but will be addressed in
 227 the future work from the authors.

228 Key operations of the three actors in the system are presented
 229 as follows:

230 1) *Aggregator's role and operational functions:* Aggregators
 231 provide energy services to DER users and coordinate
 232 with the DSO and price coordinator. Note the role of the
 233 aggregator here is similar to a retailer who on-behalf of
 234 customers to buy the electricity in the energy spot market.
 235 To support such a role, two stages are needed: DER

energy schedule generation and interaction with the DSO
 and price coordinator. In the first stage, aggregators collect
 information from the users to make an optimal energy schedule
 for DERs. Then, this initial energy schedule will be shared
 with the DSO to form the baseline. The baseline is normally
 defined as an estimate of the electricity that would have been
 consumed by a customer in the absence of a demand response
 event [18]. This implies that if there are no potential network
 problems, the aggregators' initial schedule will be accepted
 by the DSO; otherwise, this baseline will be used for later
 on cost function formulation.

- 2) *DSO's role and operational functions:* To ensure secure
 operation of the distribution network, the non-profit organization
 DSO needs to interact with the aggregators and price coordinator,
 exchanging buses' information on the network with the aggregators
 and the price coordinator and responding to the price set by price
 coordinator. Besides, DSO is informed about aggregators' initial
 power schedule since it will keep tracking the power schedule
 when responding to the price set by the price coordinator.
- 3) *Price coordinator's role and operational functions:* The
 price coordinator is an authorized entity to determine the shadow
 prices and facilitates the interactions between the DSO and the
 aggregators to reach a power consensus at each bus of the network.
 The price coordination center could be operated by a third party.
 The proposed third party is feasible¹ if more distributed energy
 resources are connected on the distribution network level. The
 independent third party could be used to provide such services to
 different distribution system operators and aggregators, for example,
 in Denmark, there are around 70 distribution companies which
 serves electricity to publics. In addition, the proposed third party
 could ensure fairness to aggregators and DSOs. If the price coordinator
 is operated by a DSO, it may discriminate some aggregators if
 their operational schedules have conflicts with DSO's own interests.
 From our view, the price coordinator should be a non-profit
 organization but will charge certain operational fee to its customers
 including DSOs and aggregators to maintain its operation and
 development.

III. MATHEMATICAL MODELING OF NETWORK-CONSTRAINED TRANSACTIVE CONTROL

In this section, mathematical models of the network-constrained
 transactive control method are introduced. An electric vehicle is
 used as an example to illustrate the developed transactive control
 method. Fig. 2 shows the functions and interactions of the entities
 in the proposed model. We start with the aggregator who uses
 linear programming to formulate an aggregated EV charging
 schedule in Stage I. The charging

¹<http://www.ipower-net.dk/news>. In the Danish iPower smart grid project, a flexibility clearing house software infrastructure is developed that enables Distribution System Operators and aggregators to interact, so the potential flexibility controlled by the aggregators can be provided to the DSOs in a market-based way.

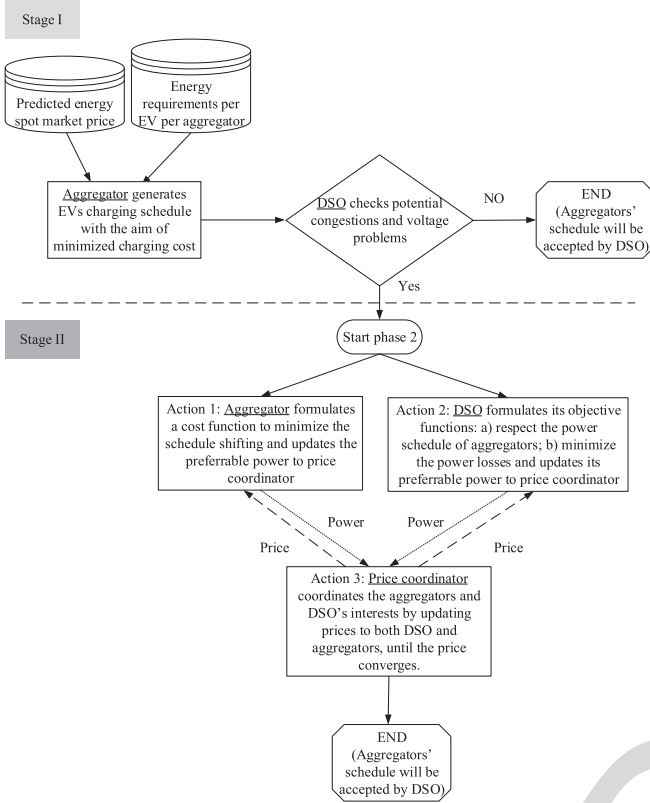


Fig. 2. Flowchart of the proposed method that describes the function and interactions of entities.

286 schedule forms a baseline of the flexibility cost function used in
 287 section III-B where the modeling development of the network-
 288 constrained transactive control is presented in Stage II. Finally,
 289 a distributed computational algorithm is presented in Stage II
 290 that facilitates implementation of the transactive control.

291 A. Stage I: Aggregator's Electric Vehicles Charging 292 Schedule Generation

293 A linear programming-based electric vehicle charging opti-
 294 mization is formulated and used by the aggregators to gener-
 295 ate the optimal charging schedule, assuming knowledge of EV
 296 users' driving pattern and forecast electricity spot price. Note
 297 that the linear programming model and the assumptions adopted
 298 here may not accurately characterize the charging process of the
 299 electric vehicles in terms of the uncertainty of EV users' driving
 300 pattern, battery charging behavior, EV charging efficiency etc.,
 301 however, as discussed in [19], it is a sufficient method for gener-
 302 ating the optimal charging schedule to minimize the charging
 303 cost.

304 The charging objective is to minimize the charging cost as
 305 well as to fulfill the individual EV's energy requirements for the
 306 next twenty-four hours, and the discharging ability and battery
 307 degradation cost are not considered in the study. The solution is
 308 introduced similarly for each aggregator:

$$\min \sum_{j=1}^{N_k^E} \sum_{i=1}^{N_T} \Phi_{j,i} P_{j,i} t,$$

subject to

$$\begin{cases} SOC_{0,j} \cdot E_{cap,j} + \sum_{i=1}^{N_T} P_{j,i} t_{j,i} = SOC_{Max,j} \cdot E_{cap,j} \\ 0 \leq P_{j,i} \leq P_{max,j}, i = 1, \dots, N_T \end{cases} \quad (1)$$

where

$P_{j,i}$	Optimization variable, the j^{th} EV charging power at time interval i .	310 311 312
N_k^E	Number of EVs under aggregator k .	313
N_T	Number of time slots in the scheduling period.	314
j	Index for the number of EVs under each aggregator, $j = 1, 2, \dots, N_k^E$.	315 316
i	Index of time slot in the scheduling period, $i = 1, 2, \dots, N_T$.	317 318
$\Phi_{j,i}$	Predicted day-ahead electricity market price vector.	319 320
t	Length of each time slot.	321
$SOC_{0,j}$	Initial SOC of individual EV.	322
$SOC_{Max,j}$	Requested/targeted maximum SOC of individual EV at the end of the charging period.	323 324
$P_{max,j}$	Maximum charging rate of individual EV.	325
$E_{cap,j}$	Capacity of the battery of the EV.	326

In (1), the first constraint means that the energy to be charged should be equal to the requested energy at the end of the charging period for each electric vehicle. The second constraint represents that the charging rate is less than or equal to its maximum power rate of a charger. The physical meaning of the optimization variable vector $P_{j,i}$ is to make a decision on the charging power in the planned time slots, where the charging cost can be minimized.

With the above optimization problem, the aggregator can generate a unique energy schedule for individual EV as well as an aggregated power schedule in each time slot. Note that, when interacting with the DSO, the aggregator needs to provide charging locations of the aggregated charging schedules, which is assumed to be known by the aggregators. The previously obtained $P_{j,i}$ will be denoted as $P_{j,i,l}$. l is the bus index of the distribution network, $l = 1, \dots, N_B$. Thus, we calculate the sum of the individual EV energy schedule inside one aggregator k at bus l in time slot i and the total power is denoted as $P_{k,i,l}^E$, and

$$P_{k,i,l}^E = \sum_{j \mapsto l} P_{j,i,l}, k = 1, \dots, N_F, i = 1, \dots, N_T, l = 1, \dots, N_B \quad (2)$$

where

$j \mapsto l$	The electric vehicles of each aggregator connected at bus l .	345 346 347
N_F	Number of aggregators.	348
N_B	Number of buses.	349
k	Index for the number of aggregators, $k = 1, \dots, N_F$.	350
$P_{k,i,l}^E$	Power requirements of EVs of aggregator k in time slot i at bus l .	351 352

Note that the EV model used here does not consider the uncertainty of the EV travel pattern, thus the aggregated power consumption of the aggregator might deviate from the planned schedule which will certain influence the accuracy of this model.

357 This problem can be mitigated by: 1) when the size of the ag-
 358 gregator is bigger such as many flexible resources are controlled
 359 by the aggregator, since the uncertainty of individual EV can
 360 be evened, and 2) an agreement could be made between the
 361 aggregator and the customers that communicate timely on the
 362 customers' next day traveling plan.

363 B. Stage II: Network-Constrained Transactive Control 364 Modeling

365 In this study, the principle for applying the network-
 366 constrained transactive control application is that the DSO needs
 367 to check whether the charging schedule of aggregators will
 368 result in network operation violations. If there is a violation,
 369 a congestion price will be generated by the price coordina-
 370 tor to reflect the violations. Otherwise, the power schedule of
 371 aggregators will be accepted by the DSO.

372 To start the modeling of the control method, we propose a
 373 flexibility cost function that represents the cost of the power
 374 preference difference of aggregators in each time slot i per
 375 bus l ,

$$\mu_k = \zeta_k(\tilde{P}_{k,i,l}).$$

376 To facilitate the understanding, we assume

$$\mu_k = C_{k,i,l}(\tilde{P}_{k,i,l} - P_{k,i,l}^E)^2,$$

377 subject to

$$\sum_{i=1}^{N_T} \tilde{P}_{k,i,l} \cdot t_i = \sum_{j \rightarrow l} (SOC_{\text{Max},j} - SOC_{0,j}) \cdot E_{\text{cap},j} \quad (3)$$

378 where k, i, l remain the same with the above notation, $\tilde{P}_{k,i,l}$
 379 denotes the optimization variable, $P_{k,i,l}^E$ is the optimized power
 380 schedule shown in (2), $C_{k,i,l}$ means the weighting factor which
 381 are associated with the power difference, the larger $C_{k,i,l}$ means
 382 smaller difference preferred since the objective is to reduce the
 383 power shifting. The constraint in (3) means the individual EV
 384 energy requirements should always be fulfilled. The flexibil-
 385 ity cost function μ_k intends to penalize the deviation from its
 386 originally optimized schedule $P_{k,i,l}^E$.

387 For the DSO, the objective is to track and regulate the power
 388 schedule from aggregators with respect to the operational con-
 389 straints such as the transformer thermal capacity and the voltage
 390 limitations and to minimize the network losses:

$$\min a \cdot \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \left(P_{\text{trans}}(i, l) - \sum_{k=1}^{n_F} P_{k,i,l}^E \right)^2 + b \cdot P_{\text{loss}}$$

391 subject to

$$\begin{aligned} \sum_{l=1}^{N_B} P_{\text{trans}}(i, l) &\leq P_{\text{trans}}^{\text{Max}}(i), \\ U_0(i, l) + \Delta U(i, l) &\geq U_{\text{Min}}(i, l) \end{aligned} \quad (4)$$

392 where

393 a, b Weighting factors.
 394 P_0 Conventional load profiles.

$P_{\text{trans}}(i, l)$ Optimization variable and its physical meaning is
 the desirable power of DSO for EVs charging, ex-
 clude the base load profile.
 n_F Number of aggregators which has EVs attached in
 bus l .
 A Full bus incidence matrix, $N_B \times N_{\text{Line}}$, associated
 to the reference direction of branches. If bus m is
 the initial node of branch $[m, n]$, $A(m, n) = 1$, else
 $A(m, n) = -1$. Note the matrix is not necessary a
 square matrix.
 N_{Line} Number of branches.
 $P_{\text{trans}}^{\text{Max}}$ Power transformer capacity for all the aggregators,
 for example, it can be estimated by the DSO after
 deducting the conventional loads.
 $U_0(i, l)$ The initial voltage of the buses of the network.
 $U_{\text{Min}}(i, l)$ The minimum allowable voltage of the buses of
 the network.

Note that normally in practice, the non-profit organization
 DSO aims to ensure the safe and efficient operation of the net-
 work, provide non-discriminate electricity distribution services
 to customers, and minimize energy losses of the system. In this
 study, we proposed that the DSO also aims to supply the desired
 power schedule of aggregators as much as possible, in addition
 to the loss minimization objective. It is envisioned in the near
 future smart grid, the DSO can adapt the objective functions like
 the one presented in (4) with the real needs.

In (4),

$$P_{\text{loss}} = \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \left(\frac{P_{\text{line}}^2(i, l) + Q_{\text{line}}^2(i, l)}{V^2} \right) R_l$$

$$P_{\text{line}}(i, l) = (A \cdot A^T)^{-1} \cdot A \cdot (P_0(i, l) + P_{\text{trans}}(i, l))$$

where $P_{\text{loss}} = \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \left(\frac{P_{\text{line},l}^2(i) + Q_{\text{line},l}^2(i)}{V^2} \right) R_l$ can be ap-
 proximated as $P_{\text{loss}} = \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} P_{\text{line}}^2(i, l) R_l$, since Q is usu-
 ally small in low voltage network, and as long as the voltage
 is close to nominal. $\Delta U(i, l)$ is calculated from the following
 simplified equation [20], [21]

$$\begin{bmatrix} \Delta P \\ \Delta Q \end{bmatrix} = \begin{bmatrix} \frac{\partial P}{\partial \Theta} & \frac{\partial P}{\partial U} \\ \frac{\partial Q}{\partial \Theta} & \frac{\partial Q}{\partial U} \end{bmatrix} \begin{bmatrix} \Delta \Theta \\ \Delta U \end{bmatrix}$$

Denote J the load flow Jacobian from the last iteration,

$$J = \begin{bmatrix} \frac{\partial P}{\partial \Theta} & \frac{\partial P}{\partial U} \\ \frac{\partial Q}{\partial \Theta} & \frac{\partial Q}{\partial U} \end{bmatrix}$$

then the voltage increment can be calculated by the injection
 increment times the reverse of the Jacobian, as shown below,

$$\begin{bmatrix} \Delta \Theta(i, l) \\ \Delta U(i, l) \end{bmatrix} = J^{-1} \begin{bmatrix} \Delta P(i, l) \\ \Delta Q(i, l) \end{bmatrix} = J^{-1} \begin{bmatrix} P_{\text{trans}}(i, l) \\ 0 \end{bmatrix} \quad (5)$$

Here, we assume the reactive power injection increment is zero.
 Θ means voltage angle and it is not considered in the study.

432 Thus we have

$$\Delta U(i, l) = J_{21}^{-1} \cdot P_{\text{trans}}(i, l). \quad (6)$$

433 where J_{21}^{-1} means only a submatrix of J^{-1} is used.

434 From a social fairness point of view, it is desirable to minimize
435 the cost to the aggregator as well as minimizing the power losses
436 and mitigating the impact on the distribution system operator.
437 The social welfare maximization is mathematically formulated
438 as follows:

$$\begin{aligned} \min \quad & \sum_{k=1}^{N_F} \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} C_{k,i,l} (\tilde{P}_{k,i,l} - P_{k,i,l}^E)^2 \\ & + a \cdot \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} (P_{\text{trans}}(i, l) - \sum_{k=1}^{n_F} P_{k,i,l}^E)^2 + b \cdot P_{\text{loss}} \end{aligned}$$

439 subject to

$$\begin{aligned} \sum_{k=1}^{n_F} \tilde{P}_{k,i,l} &= P_{\text{trans}}(i, l), i = 1, \dots, N_T, \\ \sum_{i=1}^{N_T} \tilde{P}_{k,i,l} \cdot t_i &= \sum_{j=1}^{N_k^E} (SOC_{\text{cap},j} - SOC_{0,j}) \cdot E_{\text{cap},j}, \\ \sum_{l=1}^{N_B} P_{\text{trans}}(i, l) &\leq P_{\text{trans}}^{\text{Max}}(i), \\ U_0 + \Delta U &\geq U_{\text{Min}}, \end{aligned} \quad (7)$$

440 where the optimization variables of this optimization problem
441 are $\tilde{P}_{k,i,l}$ and $P_{\text{trans}}(i, l)$. The first constraint of (7) implies that
442 sum of the new optimal power of aggregators should be equal
443 to the new optimal power of the DSO. Let $\lambda(i, l)$ denote the
444 Lagrange multiplier corresponding to the first constraint of (7),
445 and keep the rest of the constraints implicit, so the Lagrangian
446 function for (7) is

$$\begin{aligned} L(\lambda(i, l), \tilde{P}_{k,i,l}, P_{\text{trans}}(i, l)) &= \\ & \sum_{k=1}^{N_F} \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} C_{k,i,l} (\tilde{P}_{k,i,l} - P_{k,i,l}^E)^2 \\ & + a \cdot \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \left(P_{\text{trans}}(i, l) - \sum_{k=1}^{n_F} P_{k,i,l}^E \right)^2 + b \cdot P_{\text{loss}} \\ & + \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \lambda(i, l) \cdot \left(\sum_{k=1}^{n_F} \tilde{P}_{k,i,l} - P_{\text{trans}}(i, l) \right) \end{aligned} \quad (8)$$

447 where the optimization variables of optimization problem (8)
448 are $\lambda(i, l)$, $\tilde{P}_{k,i,l}$ and $P_{\text{trans}}(i, l)$.

449 C. Stage II: Network-Constrained Transactive Control 450 Implementation

451 In order to solve the optimization problem (8), this section
452 applies a distributed computing algorithm which has been ap-
453 plied in several studies [22], [23]. The Lagrangian minimiza-
454 tion can be solved by subgradient methods [24] which usually

require multiple iterations or information exchange. In the iter- 455
456 ation, the minimization problems are seen to be decomposable
457 to the DSO and to the aggregators. Specifically, the subgradient
458 method consists of the following iterations, indexed by ω and
459 initialized with arbitrary $\lambda_1^*(i, l) \geq 0$:

1) aggregator minimization at step ω 460

$$\begin{aligned} \min \quad & \left(\sum_{k=1}^{N_F} \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} C_{k,i,l} (\tilde{P}_{k,i,l} - P_{k,i,l}^E)^2 + \right. \\ & \left. \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \lambda_{\omega}^*(i, l) \sum_{k=1}^{n_F} \tilde{P}_{k,i,l} \right) \\ \text{s.t.} \quad & \sum_{i=1}^{N_T} \tilde{P}_{k,i,l} \cdot t_i = \sum_{j \in l} (SOC_{\text{cap},j} - SOC_{0,j}) \cdot E_{\text{cap},j} \end{aligned} \quad (9)$$

To solve problem (9) and obtain the value of optimization vari- 461
462 able $\tilde{P}_{k,i,l}$ we use CVX, a package for specifying and solving
463 convex programs [25], [26].

2) DSO minimization at step ω 464

$$\begin{aligned} \min \quad & a \cdot \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \left(P_{\text{trans}}(i, l) - \sum_{k=1}^{n_F} P_{k,i,l}^E \right)^2 + \\ & b \cdot P_{\text{loss}} - \sum_{i=1}^{N_T} \sum_{l=1}^{N_B} \lambda_{\omega}^*(i, l) P_{\text{trans}}(i, l) \\ \text{s.t.} \quad & \sum_{l=1}^{N_B} P_{\text{trans}}(i, l) \leq P_{\text{trans}}^{\text{Max}}(i), \\ & U_0(i, l) + \Delta U(i, l) \geq U_{\text{Min}}(i, l) \end{aligned} \quad (10)$$

To solve problem (10) and get the value of optimization vari- 465
466 able $P_{\text{trans}}(i, l)$, we use CVX and MATPOWER, a MATLAB
467 power system simulation package.

3) Price coordinator: lagrangian multiplier updating for step 468
469 $\omega + 1$

$$\lambda_{\omega+1}(i, l) = \lambda_{\omega}^*(i, l) + \alpha_{\omega} \cdot \left(\sum_{k \in l} \tilde{P}_{k,i,l}^* - P_{\text{trans}}(i, l)^* \right) \quad (11)$$

where ω is the index for the iterations, $\tilde{P}_{k,i,l}^*$ is the solution of 470
471 problem (9), $P_{\text{trans}}(i, l)^*$ is the solution of (10), $\alpha_{\omega} \in R$ denotes
472 the step size and can be chosen as $\alpha_{\omega} = \alpha$ which is a positive
473 constant and with the choice, the convergence is guaranteed
474 [24]. Note that λ is converged at each bus in each time slot. A
475 simple step size is chosen here to update the λ , but as discussed
476 in [24], some heuristic approaches can be performed to improve
477 the convergence speed.

478 IV. CASE STUDY

479 A. Case Specification

1) *EV charging parameters*: Two EV penetration levels are 480
481 studied, i.e., the 50% EV level and the 100% EV level. All the
482 EVs are affiliated to either *aggregator 1 (Agg.1)* or *aggregator*
483 *2 (Agg.2)*. The number of the EVs operated by *Agg.1* and *Agg.2*

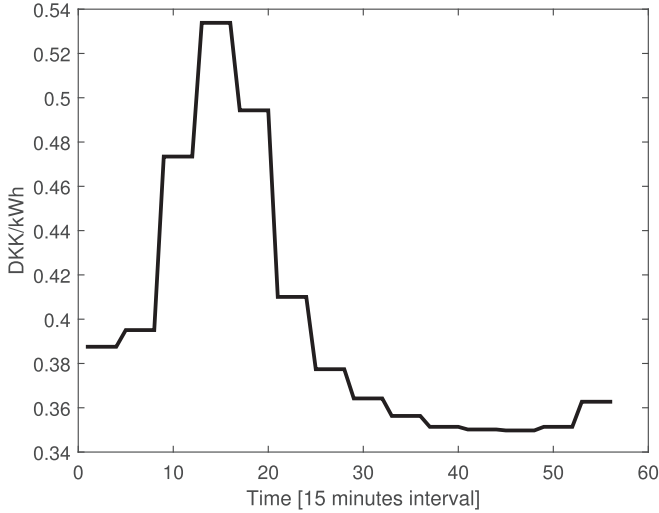


Fig. 3. Electricity energy price, an example from NordPool.

is 18 and 36 in each level, respectively. The scheduling period considered in this case is from 16.00 to 06.00 and a 15-min interval is used. The hourly predicted day-ahead market price from 16.00 to 06.00 is assumed to be known to the aggregator and the price² is shown in Fig. 3, the price will be used in stage I for generating EV charging schedule.

For other parameters in EV charging:

- 1) Battery capacity E_{cap} is set to 24 kWh
- 2) SOC_o is set to 0.2 of the battery capacity
- 3) SOC_{max} is set to 100% of the battery capacity
- 4) Maximum charging power is limited to 3.7 kW which fits with the Danish case (16 A, 230 V connection).

2) *Distribution network and control parameters:* A representative Danish distribution grid is illustrated in Fig. 4 where 72 households are connected to the feeders: 51 households are attached to the left branch and 21 households are located on the right side of the network. For the parameters used in the network-constrained transactive control, a time series base load is assumed to be known by the distribution system operators. With the base load, the DSO can calculate the base voltage, i.e., the U_0 in (4) per bus. In all time slots, the power transformer capacity allocated to two EV aggregators is 120 kW in both EV penetration cases, the minimum voltage U_{Min} per bus is assumed to be 0.905 p.u. for the 50% EV penetration case and 0.88 p.u. for the 100% EV penetration case. Note the 0.905 p.u. and 0.88 p.u. are given empirically, for the 100% EV penetration case, the EV charging power is very high for the distribution network, but the method still converges for the relaxed voltage constraint. In reality, the minimal voltage 0.88 p.u. is not recommended, here it is mainly used for presenting the effectiveness of the proposed control method, even under the 100% EV penetration case. The initial Lagrangian multipliers are assumed to be zero per bus in all the time slots and are updated per iteration to the aggregators and the DSO. The weighting factor rate $C_{1,i,l}$ and $C_{2,i,l}$ is set to 0.5 and 0.1, respectively. A constant stepsize ($\alpha_\omega = 0.1$) is

²The electricity price assumed here is drawn from the real electricity price from NordPool spot market (<http://www.nordpoolspot.com/>)

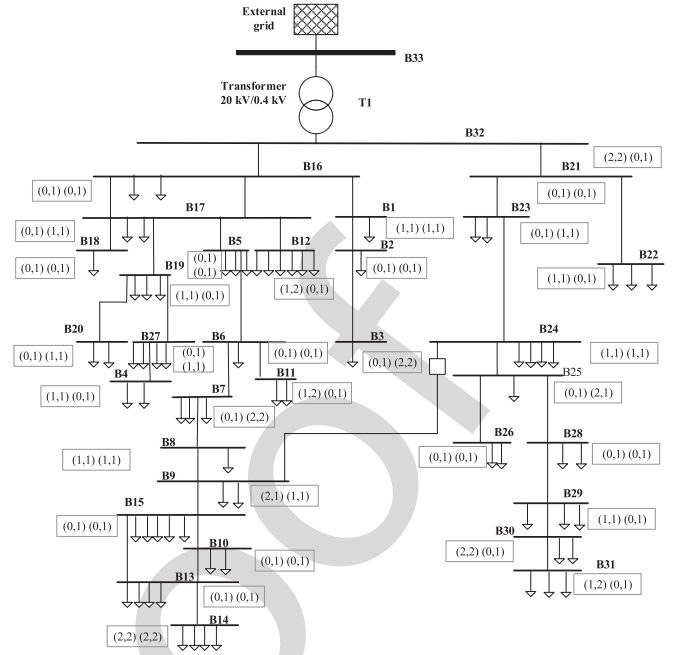


Fig. 4. A representative Danish distribution network with EV connected. We use two sets of parentheses inside the block under each bus index to show the EVs that are connected to the bus. The left set of parentheses represents Agg.1's EV information and the right one shows Agg.2's EV information. In each set of parentheses, the number of the EVs assigned to the two EV penetration levels is indicated (left for 50% EV penetration case, right for 100% EV penetration case).

chosen for the Lagrangian multiplier update. The value of a and b is 0.1 and 300, respectively.

Note the values of a and b can influence the performance of both DSO and aggregators. Therefore, the values must be tuned properly when use in real. Technically, the value of a and b is chosen based on empirical study in this work and the principle is to make the optimum of different actors (DSO and aggregators) have the same order of magnitude. Economically, the values should be agreed based on negotiation between the DSO and the aggregators, since it will influence the cost of aggregators and DSO. It is noted there is work remaining on this matter, and how exactly the process should be will be investigated in further research effort.

B. Simulation Scenarios

With the provided parameters of the EVs, Agg.1 and Agg.2 calculate their optimal schedules according to (1). The power schedule of the EVs is firstly allocated in the time period 45 to 48 because of the lower electricity price, i.e., 02:00 to 03:00 AM, thus this hour is used for illustrating the control performance. The sum of the power in these time periods is higher than the allocated power transformer's capacity. To illustrate the effectiveness of the network-constrained transactive control and to examine the effect of adding power loss objective function as well as voltage constraints in (4), three scenarios are considered here:

- 1) Scenario 1: Basic network-constrained transactive control. In this scenario, only congestion is considered, the

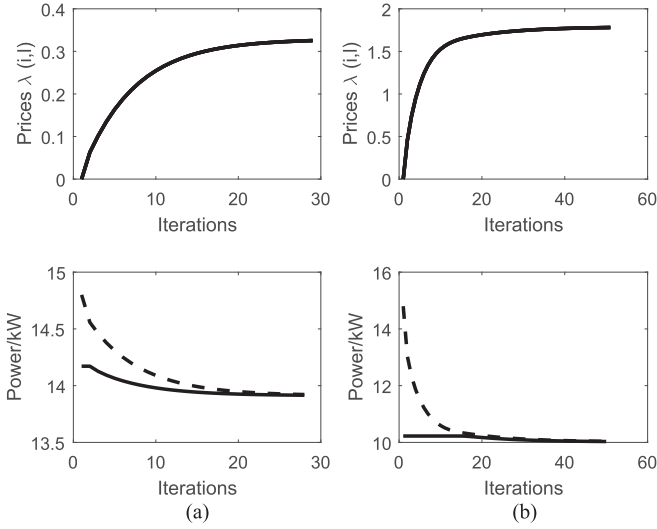


Fig. 5. Convergence of $\lambda(i, l)$ and power of DSO and aggregators at bus 14, $i = 45, \dots, 48$, in scenario 1. Dotted power profile: The sum of Agg.1 and Agg.2; solid power profile: DSO.

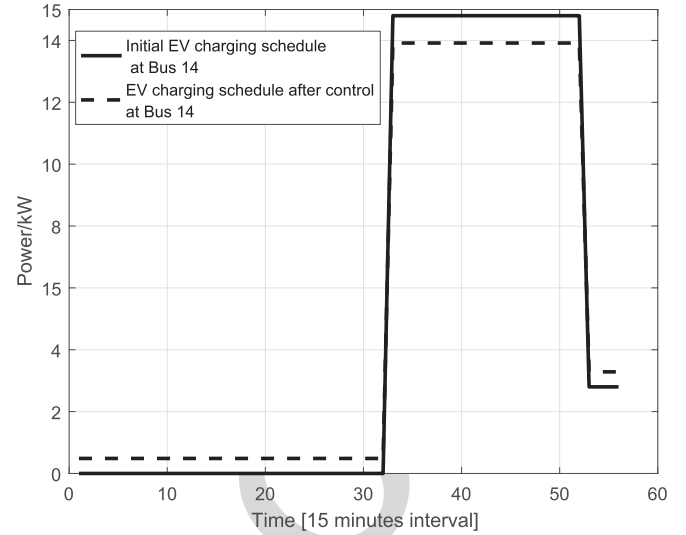


Fig. 6. Comparison of the charging schedule of EVs connected at bus 14 in presence of control in scenario 1.

546 power loss and the voltage constraints are not included in
547 the optimization problems.

548 2) Scenario 2: Network-constrained transactive control with
549 voltage constraints. In this scenario, the voltage con-
550 straints are included on top of scenario 1.

551 3) Scenario 3: Network-constrained transactive control with
552 voltage constraints and power loss. In this scenario, the
553 power loss objective is included on top of scenario 2.

554 Note the method does not require a fixed bus location of
555 individual EV; however, in order to compare the differences
556 between these scenarios, we use the same setting for electric
557 vehicles' locations in the network that is shown in Fig. 4.

558 C. Simulation Results

559 1) Scenario 1: Fig. 5(a) shows the simulation result of the
560 50% EV penetration case where the problem is solved after 29
561 iterations. It means the DSO and the aggregators reach consen-
562 sus in terms of power at each bus for all the time slots. The
563 power of the DSO and aggregators is regulated by the shadow
564 prices presented in the upper level of the figure. In the simula-
565 tion, bus 14 has the lowest voltage and thus the power profile of
566 DSO and aggregators at bus 14 is presented. The figure shows
567 that four electric vehicles are initially scheduled to charge from
568 02:00 to 03:00 AM. However, to respect the power transformer
569 constraint, the charging power is reduced in this hour and the
570 required additional energy is compensated in other time slots
571 that is not shown here. To demonstrate the changes before and
572 after the control, the charging profile of EVs on bus 14 (includ-
573 ing two EVs of Agg.1 and two EVs of Agg.2) is shown in Fig. 6
574 during the entire scheduling period. In addition, Fig. 5(b) shows
575 the results of the 100% EV penetration case. The congestion
576 price increases in this case because of the higher EV charging
577 power, correspondingly, the converged power of the DSO and
578 the aggregators is less than the one in 50% EV penetration case.

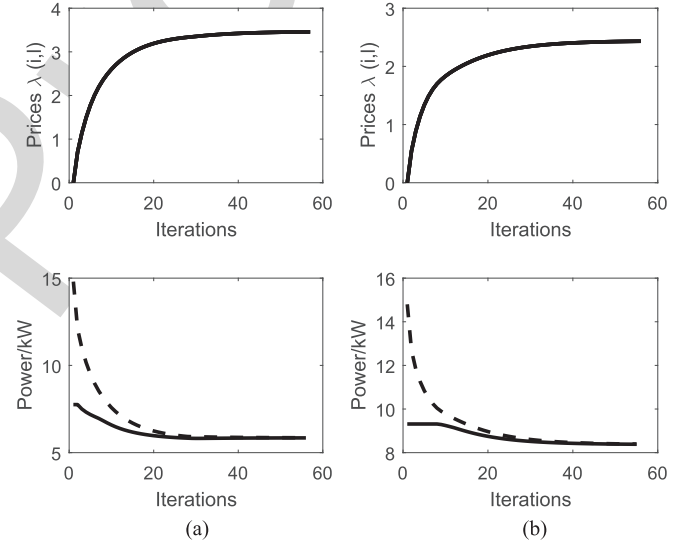


Fig. 7. Convergence of $\lambda(i, l)$ and power of DSO and aggregators at bus 14, $i = 45, \dots, 48$, in scenario 2. Dotted power profile: the sum of Agg.1 and Agg.2; solid power profile: DSO.

579 2) Scenario 2: In this scenario, bus voltage constraints are
580 included in the optimization problem. Fig. 7(a) presents the con-
581 vergence of the power and the congestion price. Compared with
582 Fig. 5(a), the results indicate longer iterations are needed to
583 reach the convergence. Besides, the congestion prices increase
584 a lot to further reduce the power at bus 14 during these four
585 time periods (i.e., 45 to 48) and the purpose is to ensure that the
586 voltage is not violated. Table I presents the voltage comparison
587 calculated from scenario 1 and scenario 2. In each scenario, we
588 calculate the voltage using the loading profiles (base load plus
589 the EVs charging load) before and after the transactive control. It
590 can be seen that the minimum voltage of the distribution network
591 in scenario 2 increases a lot compared with the one in scenario 1,
592 which show the effectiveness of the voltage approximation
593 method in (5) and (6). The minimum voltage is recalculated

TABLE I
 POWER LOSSES AND VOLTAGE BEFORE AND AFTER TRANSACTIVE CONTROL

Electric Vehicle With 50% Penetration					
Scenarios	Control	Loss (MWh)	Energy (MWh)	Loss ratio	Voltage (p.u.)
Scenario 1	Before control	0.1348	2.0699	6.51%	0.8548
	After control	0.1270	2.0611	6.16%	0.8634
Scenario 2	Before control	0.1348	2.0699	6.51%	0.8548
	After control	0.1106	2.0454	5.41%	0.9035
Scenario 3	Before control	0.1348	2.0699	6.51%	0.8548
	After control	0.1096	2.0443	5.36%	0.9036
Electric Vehicle With 100% Penetration					
Scenarios	Control	Loss (MWh)	Energy (MWh)	Loss ratio	Voltage (p.u.)
Scenario 1	Before control	0.3086	2.9349	10.51%	0.7675
	After control	0.1904	2.8150	6.76%	0.8684
Scenario 2	Before control	0.3086	2.9349	10.51%	0.7675
	After control	0.1893	2.8148	6.72%	0.8753
Scenario 3	Before control	0.3086	2.9349	10.51%	0.7675
	After control	0.1890	2.8150	6.71%	0.8753

594 after the power reaches consensus and thus the voltage is not
 595 exactly the expected 0.905 p.u. in all scenarios. We note that,
 596 compared with scenario 1, the voltage profiles in scenario 2
 597 are kept above 0.9 p.u. that fulfills the European standard EN
 598 50160. The voltage results of the 100% EV penetration case are
 599 also presented, the voltage here illustrates the effectiveness of
 600 the method, since compared to scenario 1 of 100% EV penetra-
 601 tion case, the voltage increases. In addition, Fig. 7(b) shows the
 602 results of the 100% EV penetration case. The congestion price
 603 increases a bit in this case compared with the one in Fig. 5(b)
 604 because of the voltage constraints.

605 3) *Scenario 3*: Compared with scenario 2, the power loss
 606 objective is included in the optimization problem. Similarly, the
 607 power of the DSO and the aggregators as well as the regulating
 608 congestion prices during the transactive control are shown in
 609 Fig. 8(a). The results indicate that a longer iteration number is
 610 required before consensus is reached. Besides, the congestion
 611 price is higher and thus the converged power is smaller than
 612 the one shown in Fig. 7(a). Furthermore, we compare the power
 613 loss of scenario 3 with scenarios 1 and 2. The results are shown
 614 in Table I. Here, the power loss ratio is a relationship between
 615 the energy losses and the energy injected at bus 33. The results
 616 show that the loss in scenario 3 is optimal compared with the
 617 one in scenario 2. The minimum voltage of scenario 3 is also
 618 included in Table. I. In addition, Fig. 8(b) shows the results of
 619 the 100% EV penetration case. The congestion price increases
 620 further in this case compared with the one in Fig. 7(b) because
 621 of the inclusion of objective loss.

622 D. Optimality Verification

623 To investigate the optimality of the numerical result obtained
 624 with the network-constrained transactive control method, we
 625 compare the results with the one solved directly from the opti-
 626 mization problem (7) that is named centralized control. Table II
 627 presents the results obtained in each scenario for the two EV
 628 penetration levels. The value shown in the table is the power at
 629 bus 14 corresponding to time slot 45. It is seen that the value
 630 obtained by centralized control (Central) and transactive control

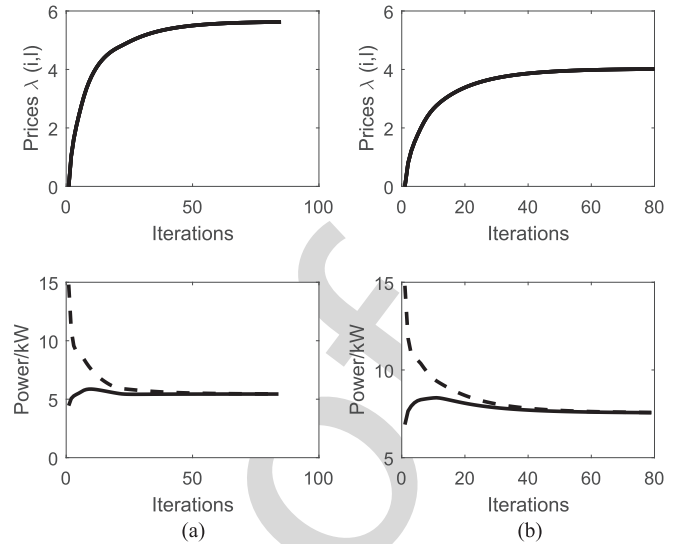


Fig. 8. Convergence of $\lambda(i, l)$ and power of DSO and aggregators at bus 14, $i = 45, \dots, 48$, in scenario 3. Dotted power profile: The sum of Agg.1 and Agg.2; solid power profile: DSO.

 TABLE II
 COMPARISON OF SCENARIOS SOLVED BY CENTRALIZED CONTROL AND TRANSACTIVE CONTROL

EV Penetrations		50% Penetration		100% Penetration	
		P_{DSO}	P_{Agg}	P_{DSO}	P_{Agg}
Scenario 1	Central	13.9118	13.9118	10.0159	10.0159
	Transactive	13.9156	13.9218	10.0312	10.0380
Scenario 2	Central	5.8490	5.8490	8.3725	8.3725
	Transactive	5.8457	5.8549	8.3854	8.3935
Scenario 3	Central	5.3661	5.3661	7.5809	7.5809
	Transactive	5.4410	5.4507	7.5662	7.5747

(Transactive) is comparable, which verifies the optimality of the
 proposed model. Note from algorithm perspective, the proposed
 method is solved by introducing a Lagrange multiplier λ and the
 dual problem gives the same solution as the one in centralized
 control due to the convexity of the optimization problem [24].
 Thus we concludes the optimality of the proposed method with
 the comparison, although the solution of the central and trans-
 active control in the table is not exactly the same because the
 problem is solved numerically here.

640 V. DISCUSSION AND CONCLUSIONS

641 In this study, the bid cost function that EV aggregators used
 642 to express their charging flexibility to the price coordinator is
 643 quadratic, as discussed in [16], popular utility/cost functions
 644 include a linear and quadratic utility function which means
 645 equilibrium prices can usually be found. However, in some situ-
 646 ations, the equilibrium may not be identified. In this case, re-
 647 laxation of the constraints or heuristic methods may be needed.
 648 Furthermore, note that the case study is towards EU system
 649 where the distribution network is normally planned as three
 650 phases, also the approximation of the load flow model though
 651 is not exact however the results show the effectiveness. As ap-
 652 plication of this method to unbalanced distribution system, it

is applicable and in that case the adaption requires introducing lamada, i.e., the shadow price on each phase.

In addition, it is one of the assumptions that there are flexibilities within an EV fleet who can shift the demand over a planning horizon to avoid high market price. For a few inflexible customers, their demands can be handled in the aggregators optimisation model by adding additional constraints for their specific energy charging requirements. If it causes violations of network constraints or higher charging cost, then there should be mechanisms between the aggregators and the customers to handle such issue.

Although the EV is used as an example to illustrate the effectiveness of the proposed method, it is note that the method can also be extended to capture other flexible loads such as heat pumps and storages. In addition, the model can be also demonstrated in a distribution system with high penetration of distributed generator such as wind/solar generators. Under this circumstance, the condition will become complex, such as the distributed generator might bring over-voltage problem, if it is the case, a similar penalized method could be used to manage the power flow of the distributed generators. Moreover, it is envisioned that, if distributed generations have contracts with the aggregator, the distributed generator and the flexible loads should be jointly optimally operated by the aggregator, then the DSO only interacts with the aggregators based on the net-power (generation minus consumption) of the aggregator.

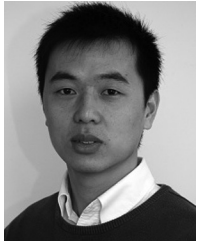
To sum up, this paper develops a network-constrained transactive control method and applies it specifically for integrating electric vehicles into power distribution systems. The proposed modeling method covers multiple time periods, which extends the application of transactive control that has been reported in previous studies. The extensions make the transactive control technique fit better with the normal operation of power system operators since ‘schedule and control’ is a typical approach used by the system operators. Furthermore, the proposed method considers the energy inter-temporal characteristics of electric vehicles, i.e., the dynamics of electric vehicle charging. By using the proposed transactive control method, the system operator can ensure a safe operation of the network and the aggregators can optimize the electric vehicles’ charging schedules.

The merit of the work is that it represents a decentralized operation instead of a centralized dispatch, as for centralized mechanism, there would be questions like computational requirements issue, privacy issue? Such questions are addressed and eliminated through transactive control, as each actors keep their operational cost functions and only communicate the solutions with the price coordinator through a negotiation mechanism.

REFERENCES

- [1] D. Apostolopoulou, S. Bahramirad, and A. Khodaei, “The interface of power: Moving toward distribution system operators,” *IEEE Power Energy Mag.*, vol. 14, no. 3, pp. 46–51, May/Jun. 2016.
- [2] S. D. Manshadi and M. E. Khodayar, “A hierarchical electricity market structure for the smart grid paradigm,” *IEEE Trans. Smart Grid*, vol. 7, no. 4, pp. 1866–1875, Jul. 2016.
- [3] C. Cecati, C. Citro, and P. Siano, “Combined operations of renewable energy systems and responsive demand in a smart grid,” *IEEE Trans. Sustain. Energy*, vol. 2, no. 4, pp. 468–476, Oct. 2011.
- [4] D. T. Nguyen, H. T. Nguyen, and L. B. Le, “Dynamic pricing design for demand response integration in power distribution networks,” *IEEE Trans. Power Syst.*, vol. 31, no. 5, pp. 3457–3472, Sep. 2016.
- [5] R. B. Melton, “Gridwise transactive energy framework version 1,” Grid-Wise Archit. Council, Richland, WA, USA, Tech. Rep. PNNL-22946, 2015.
- [6] A. Nilgun and Z. Marzia, “Transactive energy: A surreal vision or a necessary and feasible solution to grid problems?,” California Public Utilities Commission, Policy Planning Division, San Francisco, CA, USA, Tech. Rep., 2014.
- [7] K. Kok, C. Warmer, and I. Kamphuis, “Powermatcher: Multiagent control in the electricity infrastructure,” in *Proc. 4th ACM Int. Joint Conf. Auton. Agents Multiagent Syst.*, New York, NY, USA, 2005, pp. 75–82.
- [8] A. K. Bejestani, A. Annaswamy, and T. Samad, “A hierarchical transactive control architecture for renewables integration in smart grids: Analytical modeling and stability,” *IEEE Trans. Smart Grid*, vol. 5, no. 4, pp. 2054–2065, Jul. 2014.
- [9] D. J. Shiltz, M. Cvetkovi, and A. M. Annaswamy, “An integrated dynamic market mechanism for real-time markets and frequency regulation,” *IEEE Trans. Sustain. Energy*, vol. 7, no. 2, pp. 875–885, Apr. 2016.
- [10] S. Li, W. Zhang, J. Lian, and K. Kalsi, “Market-based coordination of thermostatically controlled loads-part I: A mechanism design formulation,” *IEEE Trans. Power Syst.*, vol. 31, no. 2, pp. 1170–1178, Mar. 2016.
- [11] S. Vandael, B. Claessens, M. Hommelberg, T. Holvoet, and G. Deconinck, “A scalable three-step approach for demand side management of plug-in hybrid vehicles,” *IEEE Trans. Smart Grid*, vol. 4, no. 2, pp. 720–728, Jun. 2013.
- [12] K. De Craemer, S. Vandael, B. Claessens, and G. Deconinck, “An event-driven dual coordination mechanism for demand side management of phevs,” *IEEE Trans. Smart Grid*, vol. 5, no. 2, pp. 751–760, Feb. 2014.
- [13] Z. Darabi and M. Ferdowsi, “Aggregated impact of plug-in hybrid electric vehicles on electricity demand profile,” *IEEE Trans. Sustain. Energy*, vol. 2, no. 4, pp. 501–508, Oct. 2011.
- [14] M. S. ElNozahy and M. M. A. Salama, “A comprehensive study of the impacts of PHEVs on residential distribution networks,” *IEEE Trans. Sustain. Energy*, vol. 5, no. 1, pp. 332–342, Jan. 2014.
- [15] Y. O. Assolami and W. G. Morsi, “Impact of second-generation plug-in battery electric vehicles on the aging of distribution transformers considering TOU prices,” *IEEE Trans. Sustain. Energy*, vol. 6, no. 4, pp. 1606–1614, Oct. 2015.
- [16] S. Weckx, R. D’hulst, B. Claessens, and J. Driesensam, “Multiagent charging of electric vehicles respecting distribution transformer loading and voltage limits,” *IEEE Trans. Smart Grid*, vol. 5, no. 6, pp. 2857–2867, Nov. 2014.
- [17] S. Huang, Q. Wu, S. S. Oren, R. Li, and Z. Liu, “Distribution locational marginal pricing through quadratic programming for congestion management in distribution networks,” *IEEE Trans. Power Syst.*, vol. 30, no. 4, pp. 2170–2178, Jul. 2015.
- [18] H. Chao, “Demand response in wholesale electricity markets: The choice of customer baseline,” *J. Regulatory Econ.*, vol. 39, no. 1, pp. 68–88, Nov. 2011.
- [19] O. Sundstrom and C. Binding, “Flexible charging optimization for electric vehicles considering distribution grid constraints,” *IEEE Trans. Smart Grid*, vol. 3, no. 1, pp. 26–37, Mar. 2012.
- [20] F. Marra, G. Yang, C. Træholt, J. Østergaard, and E. Larsen, “A decentralized storage strategy for residential feeders with photovoltaics,” *IEEE Trans. Smart Grid*, vol. 5, no. 2, pp. 974–81, Mar. 2014.
- [21] G. Yang *et al.*, “Voltage rise mitigation for solar PV integration at LV grids,” *J. Modern Power Syst. Clean Energy*, vol. 3, no. 3, pp. 411–21, Sep. 2015.
- [22] N. Gatsis and G. Giannakis, “Residential load control: Distributed scheduling and convergence with lost AMI messages,” *IEEE Trans. Smart Grid*, vol. 3, no. 2, pp. 770–786, Jun. 2012.
- [23] B. Moradzadeh and K. Tomovic, “Two-stage residential energy management considering network operational constraints,” *IEEE Trans. Smart Grid*, vol. 4, no. 2, pp. 2339–2346, Dec. 2013.
- [24] S. Boyd, L. Xiao, and A. Mutapic, “Subgradient methods,” *Stanford University, Stanford, CA, USA, Autumn Quarter*, 2003.
- [25] M. Grant and S. Boyd, CVX: Matlab software for disciplined convex programming, version 2.1, (Mar. 2014). [Online]. Available: <http://cvxr.com/cvx>
- [26] M. Grant and S. Boyd, “Graph implementations for nonsmooth convex programs,” in *Recent Advances in Learning and Control*. Berlin, Germany: Springer, 2008, pp. 95–110. Available: http://stanford.edu/boyd/graph_dcp.html

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