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1 **Megawatt-Scale Solar Variability Study: An Experience from a** 2 **1.2MWp Photovoltaic System in Australia over Three Years**

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27
28 **Abstract:** With more photovoltaic (PV) systems being integrated into distribution
29 networks, power utilities are facing many challenges in both planning and operation.
30 Network operators are concerned with PV variability and associated necessity of voltage
31 regulation, control coordination, reserve adequacy and dispatch constraints. While to

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32 address the obligatory connection agreement, it is vital for PV farm owners to accurately
33 estimate PV variability and then provide the most cost-effective compensation method. In
34 the literature, PV variability of different scales has been investigated over the last 20
35 years. However, little has focused on output fluctuations of PV systems with long-term
36 and high-resolution recorded data at a low-voltage distribution feeder level where voltage
37 regulation has become a serious issue. This is particularly true in Australia, where PV
38 penetration is growing in many states and is expected to grow further in the near future.
39 This paper utilizes the data of a distributed 1.2MWp PV system in the University of
40 Queensland recorded over the last 3 years with 1-min resolution to analyse the statistical
41 characteristics of PV power variability. The results from this study will provide very
42 useful information for both power utilities and solar farm owners regarding network
43 operation and future PV system development.

44

45 **Keywords:** PV output variability, PV integration, large-scale PV, PV data processing.

46

47 **1. Introduction**

48 Grid tied solar photovoltaic (PV) installation has substantially increased over the
49 last decade in Australia, from around 10MWp in 2006 to 4,177MWp by March 2015 [1].
50 In the sunshine state – Queensland, the installed PV capacity has risen from less than
51 500kWp in 2006 [2] to 1,325MWp by March 2015 [1]. This generally accounts for nearly
52 15% of the total demand in Queensland [1]. As PV becomes a significant generation
53 source, power system operators are considering its power output variability and
54 subsequent impacts on network management and security. At the same time, PV owners
55 (especially large-scale PV system owners) also express their concerns on PV power

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56 variation and its resultant compensation requirement for meeting their connection
57 agreement.

58 Firstly the owners of PV farms with more than 30kWp normally need to negotiate
59 with local utilities for terms and conditions of the connection agreement according to the
60 Australia Standard – AS 4777 [3]. Typically, distribution utilities require a PV farm to
61 comply with a certain voltage band, ramp rate limits, and reverse power flow constraints
62 regarding the time of a day; otherwise the PV farm can be disconnected and may be
63 penalized. Therefore, the owners need to know PV output variability in order to select the
64 correct type and sufficient size of reactive power compensation devices while considering
65 cost and benefit [4, 5]. For example, if a power variation of 90% PV system rating
66 statistically only occurs once every 3 years, the owner will first weigh the cost of
67 compensation devices and the penalty of voltage violation. Then a decision can be made
68 to fully compensate PV variability of 90% or a lower level with less cost for voltage
69 regulation.

70 Secondly, for distribution utilities, it is also crucial to understand PV power
71 variability of small PV systems collectively in a feeder or a large PV farm at a single
72 location in order to plan for the required additional compensation devices [4-6].
73 Moreover, necessary control coordination between network compensators, PV plants and
74 loads can be accordingly designed [5]. This will help to avoid negative interactions
75 between different controllers and undesirable impacts on network security.

76 Lastly, for independent system operators (ISOs), it is essential to comprehend PV
77 output variability of a single large PV farm and all PV plants in a region or in a state or in
78 the whole network. This will provide useful information for a better ancillary service plan

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79 and power dispatch, and it is also helpful for improving network operation stability and
80 reliability.

81 Therefore, PV power variability is of a particular interest of PV farm owners,
82 distribution utilities and ISOs. The related studies have been conducted over more than
83 two decades with some early attempts starting from late 1980s. The paper presented by
84 Jewell in 1987 [7] is one of the earliest studies on PV variability over the areas with
85 different sizes – from 10km² to 100,000km². This research concluded the tendency of
86 declination in the percentage of PV power fluctuations as a result of geographic diversity
87 – as known as the smoothing effect. Because of availability of data at that time, it could
88 only use simulated solar irradiance data instead of measured data. After Jewell, many
89 papers [8-19] had addressed the PV variability modelling and the smoothing effect for a
90 number of locations in different countries. Based on the suggestions from Suehrcke in
91 1989 [20] and Gansler in 1995 [21], researchers had a tendency of using instantaneously
92 measured high resolution data (normally from 10s to 5min) rather than the average hourly
93 data. Many of them had utilized both irradiance and PV power measurement. However,
94 due to the different data recording resolutions, area sizes and weather patterns, a variety
95 of PV variability had been reported ranging from a few percent to several tens of percent
96 per minute (or per hour).

97 Murata in 2009 [22] investigated the geographic correlation between PV output
98 fluctuations in different places in Japan and found PV variability depends on data
99 recording interval and physical distance between PV units. Larger space with higher data
100 resolution will result in lower variability correlation. Hoff [23] and Mills [24] in 2010
101 expanded the relationship developed by Murata [22] by including the number of PV

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102 systems and dispersion factor, and formulated them into equations for PV output
103 variability prediction.

104 At the same time, the purposes of the PV variability studies have never been left
105 behind – power engineers are concerned about the implications of PV generation
106 uncertainty on the related cost associated to additional regulation necessity, power
107 ramping requirement, and reserve adequacy [15, 25]. Many papers had explored these
108 issues since 1980s [12, 17, 24-32]. The main finding was that the rise of PV penetration
109 requires increase of extra compensation, ramp rate and capacity of dispatchable
110 generators while the subsequent cost and constraints may limit further PV development.

111 In the literature, there is a lack of studies focusing on a relatively small area which
112 is close to the size of a residential feeder with PV generation data recorded in high
113 resolution for multiple years. Especially in Australia, such research has not yet been
114 reported. In this paper, the University of Queensland (UQ) 1.2MWp PV system with 1-
115 min data resolution over the last three years is utilized for PV power variability analysis.
116 The output of different PV sites is recorded with synchronized instantaneous
117 measurement. The whole system is situated in an approximate 700m × 150m area which
118 is similar to a range of a typical residential feeder. With more PV being connected to
119 distribution networks, this study will certainly provide valuable statistical information to
120 both distribution utilities and PV owners for coordinating regulation and determining
121 compensation for either large-scale or distributed small-scale PV system development.

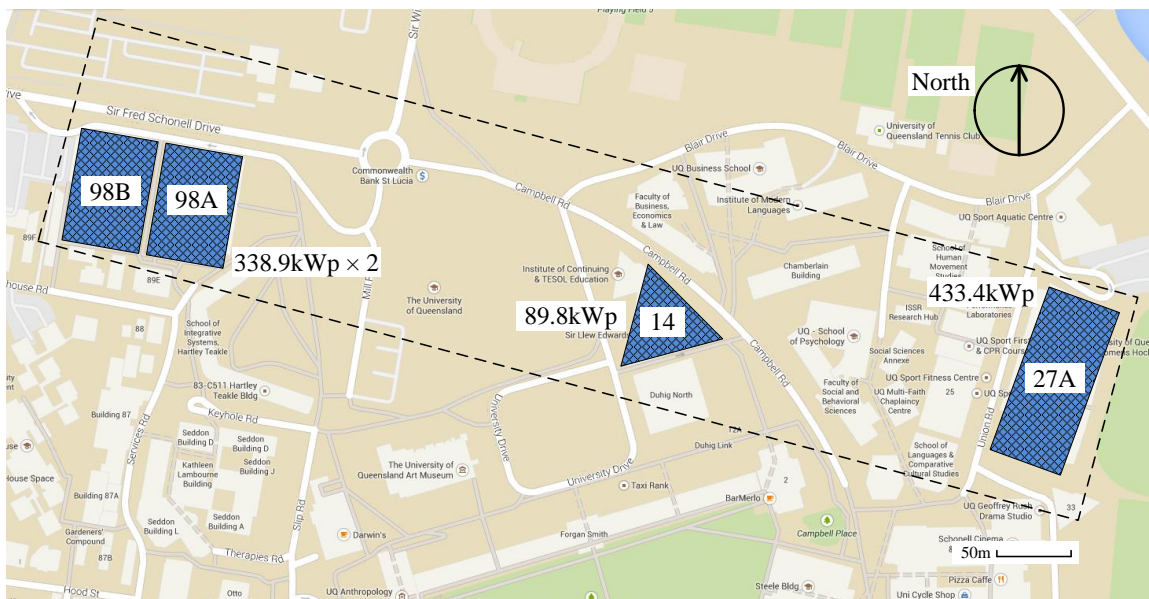
122 **2. UQ 1.2MWp PV System**

123 The UQ 1.2MWp PV system is installed on the rooftop of 4 buildings across the
124 UQ St. Lucia Campus (Brisbane, Australia) – Multilevel Car Parks (98A and 98B), Sir
125 Llew Edward (14) and UQ Center (27A) [33]. It consists of 5,004 polycrystalline PV

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126 panels (TSM-PC05, 240Wp [34]). The PV systems of two Car Parks (98A and 98B) are
127 identical – 338.9kWp (1412 panels) each. Building 14 has a much smaller PV capacity of
128 89.9kWp (374 panels), and the largest system is on Building 27A with 433.4kWp (1806
129 panels).

130 The four PV sites are distributed over an area around 700m x 150m as shown in
131 Figure 1. This dimension is comparable to a long low-voltage residential feeder with high
132 PV penetration or a several MW level solar facility situated at one location (such as the
133 UQ Gatton campus 3.4MWp PV system to be presented in Section 5); therefore, the
134 percentage variability of this PV system should reasonably represent power fluctuation of
135 distributed PV at a residential feeder level as well as output variability of a multi-MW
136 solar farm. This is the main reason why the UQ PV system can provide meaningful
137 statistical information to both solar farm owners and distribution utilities for tackling PV
138 induced voltage regulation issues.



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Figure 1 Dimension and capacity of UQ 1.2MWp PV system [35]

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141 All PV sites were brought to normal operation by the end of July 2011, and this
142 study covers a 3-year period from August 2011 to July 2014. The data logging system
143 synchronizes the clock of all sites and instantaneously collects measured data with 1-min
144 resolution (PV power).

145 **3. Overview of PV Generation and Analysis**

146 **3.1 Overall PV Power Generation**

147 The overall PV power output over the 3-year period is illustrated in Figure 2(a).
148 The seasonal effect can be clearly observed. The whole system generated more power
149 which was close to the 1.2MW rating during the summer (December to February in
150 Australia), and produced much less during the winter (June to August). Therefore, it is
151 evident that the majority of the most severe cloud induced PV power fluctuations should
152 occur between late spring to early autumn. However, it is hard to visualize PV output
153 variability from Figure 2(a). To give a clear picture of PV power variation, a sample
154 week in January 2013 is demonstrated in Figure 2(b). It can be seen that the PV system in
155 six out of seven days was heavily affected by cloud movement.

156 The monthly energy yield over three years is depicted in Figure 2(c), which
157 provides useful information to solar PV plant owners. The PV energy generation in
158 winter months can be as low as a half of energy production in summer months. It can be
159 seen that the tendency of the overall energy profile coincides with that of the power
160 profile in Figure 2(a).

161 **3.2 Definitions and Approaches for PV Power Variability**

162 Eq. (1) calculates variations in PV power over 'x' minute (x-min) intervals, where
163 x-min may be 1-min, 2-min or 5-min in this study. $P_{pv}(t)$ is the instantaneous power
164 generation from the UQ PV system at time t, measured at a resolution of once per minute.

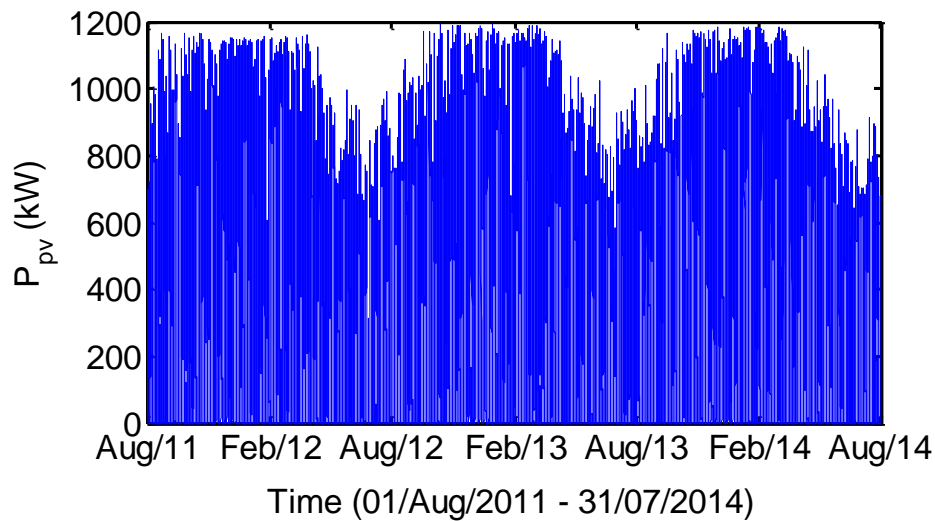
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165 For each time interval (1-min, 2-min or 5-min), Eq. (1) is evaluated at every reading.
166 Application of this method has the advantages of providing all possible PV variations
167 [$\Delta P_{pv\ x-min}(t)$] within each interval, better representing extreme changes in PV power,
168 and providing a uniform base for each of the time resolutions studied in this research.

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$$\Delta P_{pv\ x-min}(t) = P_{pv}(t) - P_{pv}(t - x) \quad (1)$$

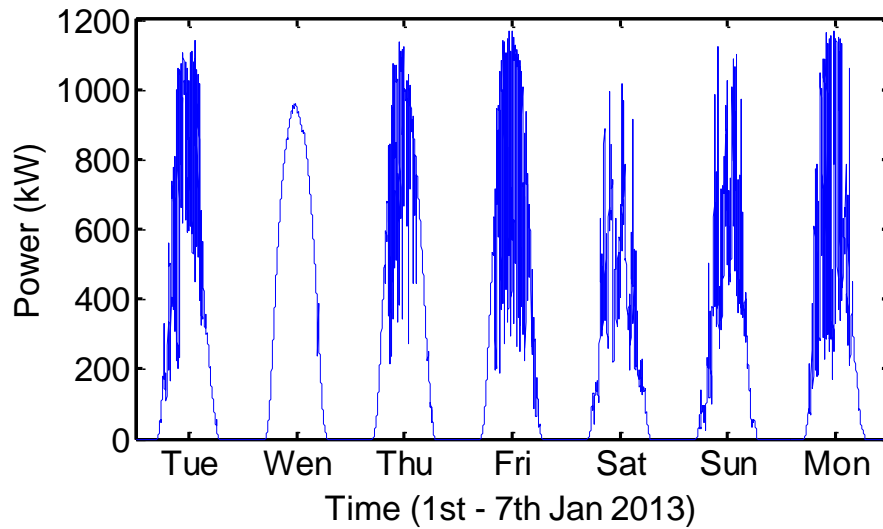
170 Based on the definition by Eq. (1), $\Delta P_{pv} > 0$ means power rise, while $\Delta P_{pv} < 0$
171 means power drop. To better present the scale of changes, per unit system (equivalent to
172 percentage) is utilized. For PV power, the UQ PV system ratings of overall and
173 individual sites are chosen as bases for per unit (pu) calculation.

174 (a) UQ PV power recorded over three years with 1-min resolution



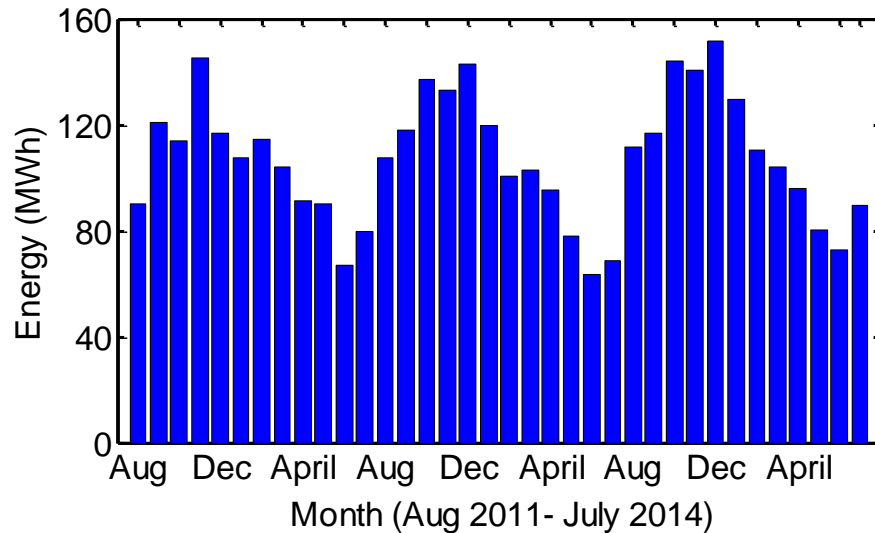
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(b) UQ PV power – a sample week in summer (1st – 7th Jan, 2013)



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(c) UQ PV monthly energy generation recorded over three years



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Figure 2 PV Power output and Energy generation

In order to study PV power variability in a statistical sense, a number of methods are applied for examining the tendency of PV output fluctuations, including distribution of the number of events, Quantile-Quantile Plot, Cumulative Distribution and variation correlation. These techniques and their analyses are presented in the next section.

4. PV Power Output Variability

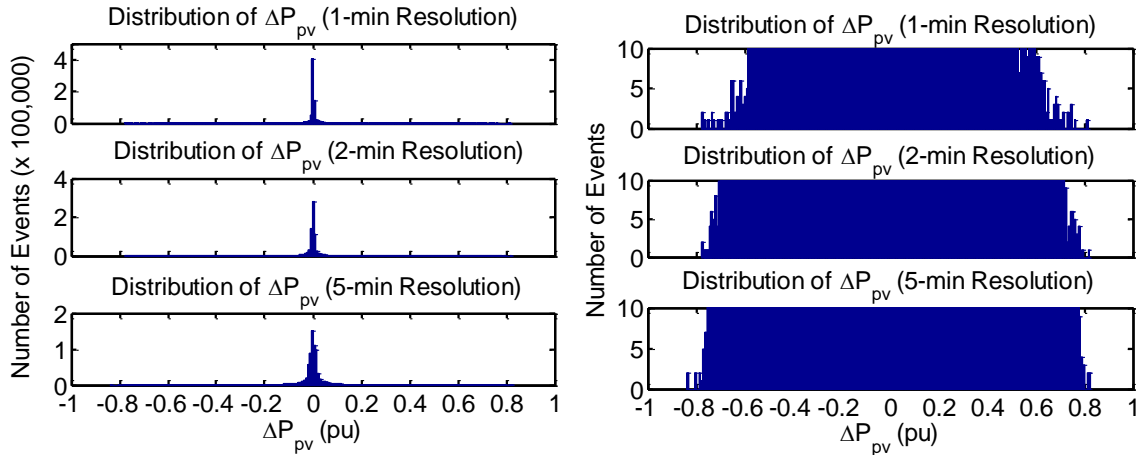
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189 **4.1 Distribution of the Number of Events**

190 **4.1.1 Overall System**

191 Distribution of the number of events (all ΔP_{pv} calculation) for the overall PV
192 system is shown in Figure 3(a). It can be noted that the majority of variations are centred
193 on 0 with a very small standard deviation, and the deviations get a little bit larger (a wider
194 base) for longer observation intervals. This means PV power variations are mainly slow
195 and smooth in nature. However, occasionally they can become very significant,
196 sometimes more than 80% of the rated power, due to movement of fast and thick clouds
197 over the area [Figure 3(b)].

198 Table 1 has listed all events in which PV output has changed more than 80% of its
199 rating. For both 1-min and 2-min intervals, $\Delta P_{pv} \geq 80\%$ has only happened once each in
200 the same day (2012-10-23 late spring), however, there were more chances for such event
201 in a 5-min scale (8 incidents). This is mainly due to the smoothing effect of the
202 geographically distributed PV systems. It really requires rare and special (thick and fast)
203 clouds to cover the area within 1-min or 2-min, however, in the 5-min scale a total
204 coverage by thick clouds becomes more probable. It can be noted that most of these
205 events happened during later spring, summer and early autumn (except two incidents in
206 one particular day in winter – 2011-08-23), and all of them occurred during the peak solar
207 radiation window from 10:30am to 14:30pm. It can also be seen that the power
208 fluctuation for the overall PV system over the 3-year period has never been greater than
209 85%.



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(a) All events

(b) Focusing on the large variation events

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Figure 3 Distribution of the number of events for the overall system over three years

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Table 1 Significant PV Power Variation Events for Overall System – $|\Delta P_{pv}| \geq 80\%$

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Time Interval	Date (yyyy-mm-dd)	Time (hh:mm)	ΔP_{pv} (%)
1-min	2012-10-23	10:44	81.5
2-min	2012-10-23	10:50	82.2
5-min	2011-08-23	11:41	-80.6
	2011-08-23	11:42	-84.0
	2012-10-23	10:45	-83.5
	2012-10-23	10:50	81.4
	2013-01-30	10:54	82.5
	2013-11-24	14:13	81.4
	2013-11-24	14:14	82.7
	2014-03-13	12:22	-80.3

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4.1.2 Summary of the Number of Significant Events for All Sites

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Very detailed information can be presented using the approaches such as Figure 3

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and Table 1 in the last sub-section; however, this will become very complicated when

223

comparing between different locations. Since the significant events (large PV

224 fluctuations) should be the focus, a summary of the number of such events over a 3-year
 225 period is listed in Table 2. The following are the observations made from this table.

- 226 (1) The event of $75\% < \Delta P_{pv} < 80\%$ happened far more frequently than that of
 227 $\Delta P_{pv} \geq 80\%$ at all time-resolution levels
- 228 (2) Due to the smoothing effect, there were more incidents for significant power
 229 variations in a longer time-resolution scale than a shorter one.
- 230 (3) For the individual sites (27A, 98A, 98B and 14), although the PV area coverage
 231 of building 14 is the smallest (Figure 1), it does not mean more severe incidents
 232 could be observed than others. On the contrary, the statistics show that most of
 233 them are more or less at the same level. This is potentially due to the relatively
 234 small-scale of each site, and 1-min resolution may be too long for such a scale,
 235 which makes little difference in terms of full cloud coverage.

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Table 2 Summary of the Number of Significant Events Over Three Years

PV Site	ΔP_{pv}	Time Interval	Power Drop $\Delta P_{pv} < 0$	Power Rise $\Delta P_{pv} > 0$
27A	$\geq 80\%$	1-min	1	7
		2-min	4	15
		5-min	19	43
	75%-80%	1-min	32	59
		2-min	74	144
		5-min	159	257
98A	$\geq 80\%$	1-min	2	8
		2-min	3	18
		5-min	28	37
	75%-80%	1-min	29	89
		2-min	73	169
		5-min	187	334
98B	$\geq 80\%$	1-min	2	9
		2-min	2	18
		5-min	25	23
	75%-80%	1-min	27	69
		2-min	55	137

		5-min	167	298
14	$\geq 80\%$	1-min	4	6
		2-min	7	11
		5-min	23	32
	75%-80%	1-min	41	64
		2-min	79	139
		5-min	159	244
Overall	$\geq 80\%$	1-min	0	1
		2-min	0	1
		5-min	4	4
	75%-80%	1-min	4	2
		2-min	4	19
		5-min	24	77

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(4) The overall system had considerably fewer events at all time-resolution levels than the individual sites. This has further supported the spatial smoothing effect and the appropriateness of applying 1-min resolution to such an area for investigating the smoothing effect.

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(5) More significant power rise ($\Delta P_{pv} > 0$) events have been observed than the power drop ($\Delta P_{pv} < 0$) ones for almost all sites and the overall system at any time-resolution levels. This may be due to the characteristics of PV panels.

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- PV temperature effect: When clouds cover a PV system, the PV power will decrease. During this period, with less sunlight radiation and power generation, the PV array temperature will decline, which makes the PV panels more efficient. Therefore, after the clouds move away, for the same solar irradiance the PV system will be able to produce more power than that of before the cloud coverage.

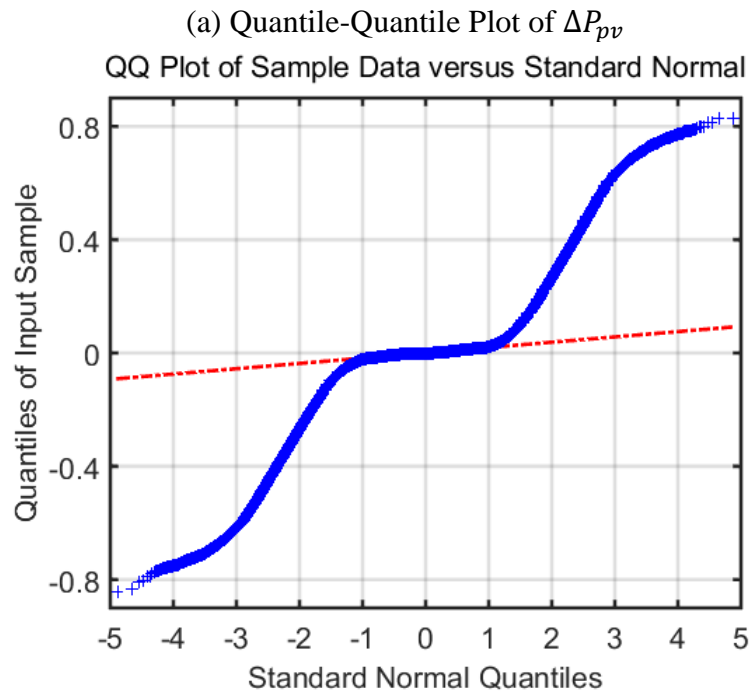
256 4.2 Probability Density Distribution

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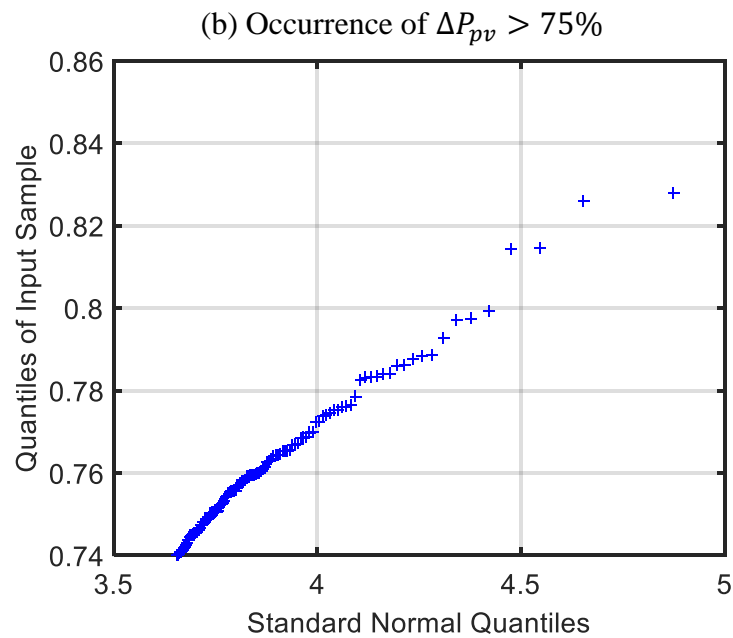
The distribution of PV power variations visually looks like a normal distribution by observing Figure 3(a). However, it is actually very different from the normal

259 distribution. This can be best analyzed by Quantile-Quantile Plot (Q-Q Plot) of PV output
260 variations over 3 years with 5-min resolution as shown in Figure 4(a).

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(c) Occurrence of $\Delta P_{pv} < -75\%$

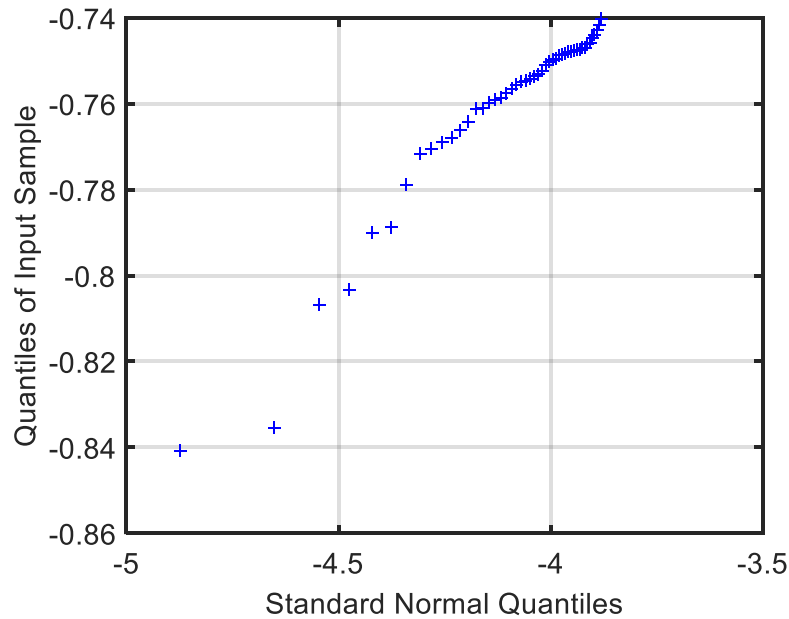


Figure 4 Quantile-Quantile Plot of PV output variations over 3 years (5-min resolution)

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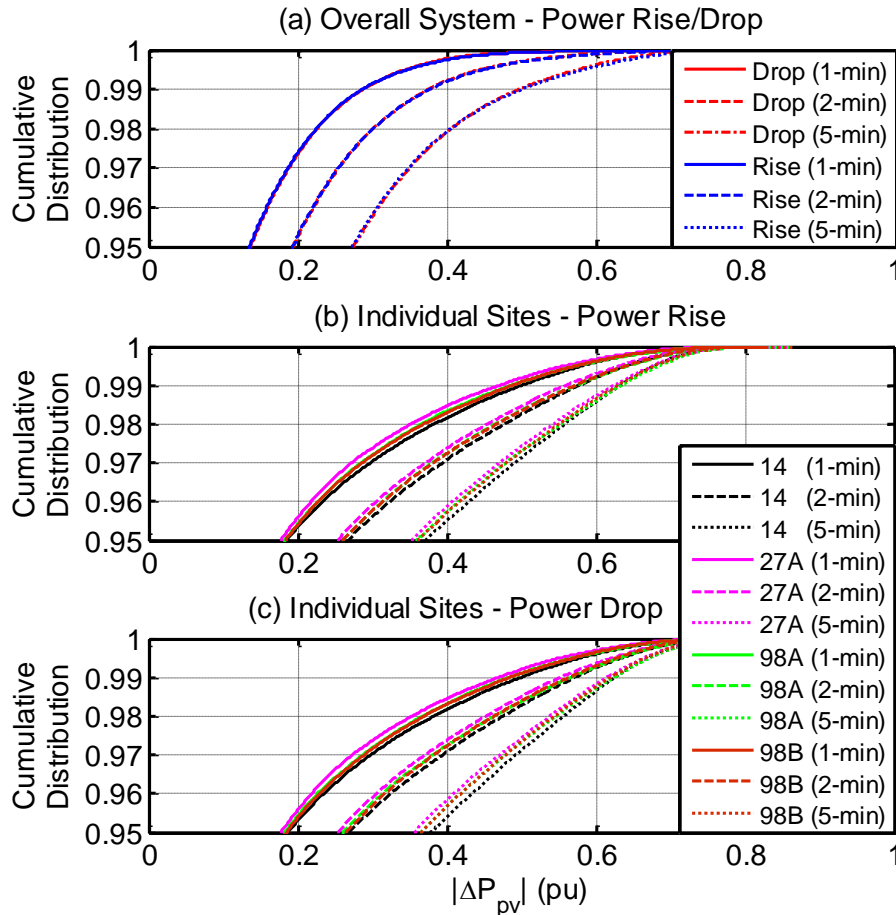
Firstly, the probability of occurrence of PV power drop ($\Delta P_{pv} < 0$) is almost 0.5, which clearly indicates the overall numbers of PV power drops and rises are approximately the same. Secondly, the region of low power variations does resemble the normal distribution as this part of the contour (blue “+”) closely coincides with the normal distribution curve (red dash-dot). Thirdly, the tendency of the medium to high PV power variations has significantly deviated from the normal distribution. This is illustrated as a heavy-tailed distribution suggesting that the probability for an incident occurring far away from the mean value is much more than that in a normal distribution. Such a distribution curve tends to have large value of standard deviation. Finally, a close observation around the tail part on each end also shows the number of significant power rises is far more than that of the PV power drops and clearly the most significant PV power fluctuation has never been greater than 85% [Figures 4 (b-c)].

283 4.3 Cumulative Distribution

284 4.3.1 Individual Sites and Overall System

285 Cumulative Distribution (CD) is another great tool that can be utilized for
286 analyzing the tendency of PV power variability with statistical confidence. The CDs of
287 the individual PV sites and the overall system are calculated and compared in Figures 5
288 and 6. If a cumulative distribution curve (say Curve CD-1) shifts toward the left-hand
289 side or lies on top of another cumulative distribution curve (say Curve CD-2), it means
290 the realizations of the PV power variations that are below a certain value (say $\Delta P_{pv} \leq$
291 $0.4pu$) from CD-1 are more likely than those from the Curve CD-2. In another word, the
292 realizations of the high PV power variations (e.g. $\Delta P_{pv} > 0.4pu$) from the Curve CD-2
293 are more probable than those from the Curve CD-1. From Figures 5 and 6, the
294 observations from Section 4.1.2 can be further evidenced, and the conclusions are made
295 as follows:

- 296 (1) All three graphs in Figure 5 show that a shorter time-resolution curve is located
297 on the left/top position of a longer time-resolution curve, which provides
298 evidence that PV power variations over a longer time intervals are more likely
299 to exceed those over a shorter time intervals – Observations (1) and (2) in
300 Section 4.1.2.
- 301 (2) Figures 5 (b) and (c) illustrate despite the size of the individual PV sites their
302 CD curves show very similar ΔP_{pv} distributions at each time-resolution level,
303 which is aligned with Observation (3) in Section 4.1.2.
- 304 (3) All CD curves of the overall system in Figure 5 (a) are on the left/top place of
305 those of the individual sites in Figures 5 (b) and (c), and this further supports
306 Observation (4) in Section 4.1.2 – the smoothing effect.



307

308 Figure 5 Cumulative distributions (95th-100th percentiles) of PV power changes of

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individual sites and the overall system over three years

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(4) When CD curves of the power drop and power rise in all individual sites and the

311

overall system are compared in Figure 6 (a), it is found that the power drop CD

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curves are situated to the right/bottom position of the power rise CD curves for

313

the low to medium PV power variation range (approximately $|\Delta P_{pv}| < 40\%$).

314

However, the reverse is true for the medium to high variation range based on

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Figure 6 (b), which supports Observation (5) in Section 4.1.2. The reasons are

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explained in the last section as the PV temperature effect. Since the total power

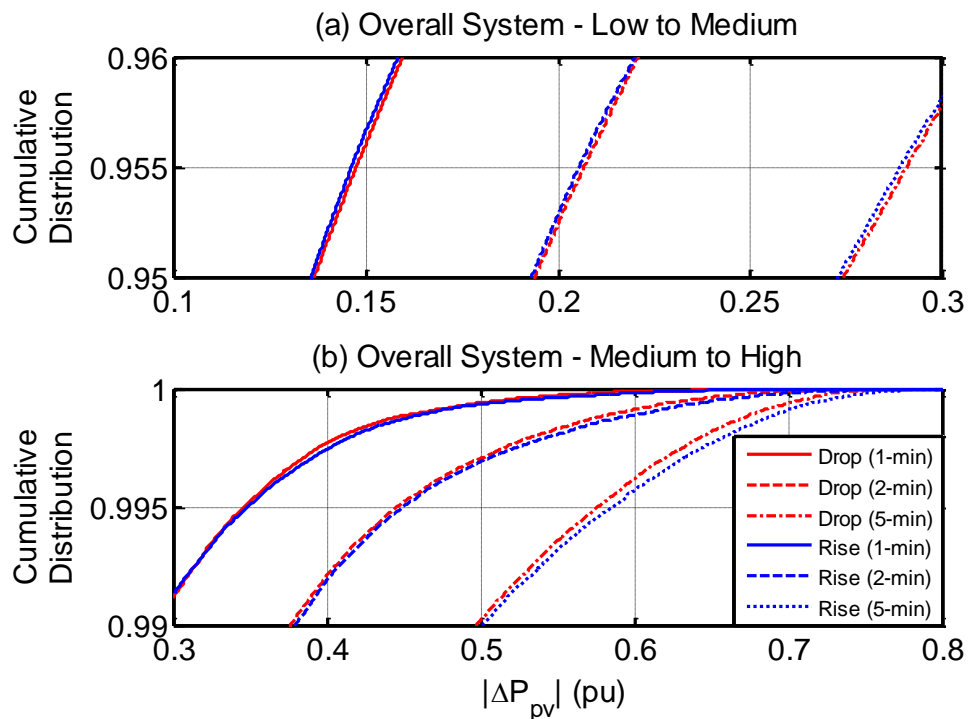
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drop and rise incidents were almost equal, a relatively larger number of power

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rising events in the medium to high variation range certainly lead to marginally

319 fewer power rising events in the low to medium variation range. However, it
 320 should be pointed out that the difference between power rise and power drop is
 321 very small. Whether it is statistically significant will be up to further
 322 observations and justification in the future.



323
 324 Figure 6 Cumulative distributions (99th-100th percentiles) of PV power changes of
 325 individual sites and the overall system over three years

326 4.3.2 Yearly Comparison

327 Annual cumulative distributions of PV power variations are shown in Figure 7(a).
 328 There is no substantial difference between the yearly tendencies of the CD curves for
 329 each time-resolution scale. It can also be noted that from 2011-2012 to 2013-2014, the
 330 CD curves were slightly moving toward the right/bottom position. This means there were
 331 more significant PV power variation incidents in 2013-2014 than those in 2011-2012.
 332 Moreover, Figure 7(a) also indicates the yearly statistical results are very close at all

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333 time-resolution levels, so annual statistics should be able to provide a fairly good
334 overview of the studied PV system.

335 The yearly PV power variability can also be evaluated based on the Smoothing
336 Factor – an index for measuring PV power fluctuations. The Smoothing Factor (S) can be
337 calculated by (2) [36].

$$338 \quad S = \frac{\sigma_{98A} + \sigma_{98B} + \sigma_{27A} + \sigma_{14}}{\sigma_{overall}} \quad (2)$$

339 where “ σ ” represents the standard deviation of the daily PV output changes for a
340 particular PV site or the overall site. For a perfectly sunny day or a totally overcast day
341 when PV power variations of all sites are slow and occur at the same time, there is nearly
342 no smoothing effect for the overall system. In this case, the common Smoothing Factor is
343 around 1.0~1.2. While for a partially cloudy day when the smoothing effect is observed,
344 the typical Smoothing Factor is generally above 1.2. Therefore, a higher value of the
345 Smoothing Factor means a greater smoothing effect.

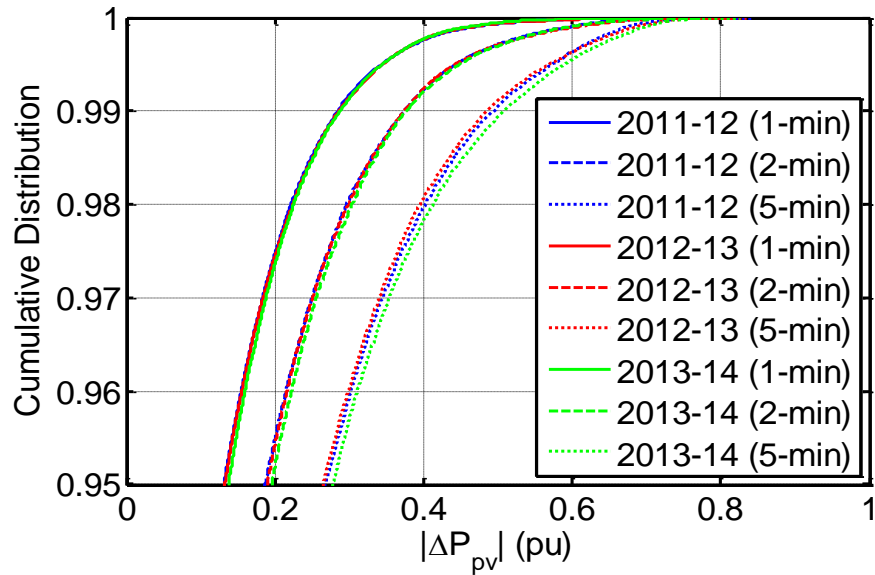
346 Figure 7(b) shows the frequency of occurrence of the Smoothing Factor during
347 the years 2011-12, 2012-13 and 2013-14. It can be observed that the frequency of
348 occurrence has a very similar profile for each year, which is in agreement with the results
349 of the cumulative distribution analysis as in Figure 7(a). Further, it can also be seen that a
350 noticeable dip of the Smoothing Factor occurred for the year 2013-14 in the range of
351 1.1~1.2, which implies relatively fewer incidents with low smoothing effect have
352 happened. While the Smoothing Factor of the year 2013-14 in higher ranges (1.3-1.7) is
353 marginally larger than that of the previous years. This potentially indicates there were
354 more significant PV power variations in this year, which also aligns with the observation
355 from Figure 7(a).

356 **4.4 Correlation of PV Power Output Variation**

357 Correlation coefficient is a measure of strength and direction of the linear
358 relationship between two variables [37]. A superior positive coefficient of correlation
359 between two variables indicates that if the value of one of the variables is changed then
360 the probability of change in the same direction for the second variable is greater. In this
361 research, correlation coefficient has been utilized to investigate the relationship between
362 two different PV sites. A larger correlation between the output variations of the two PV
363 generators implies that if one of them is affected by the cloud movement, then the
364 probability of the other one which is also influenced by the same factor becomes higher.

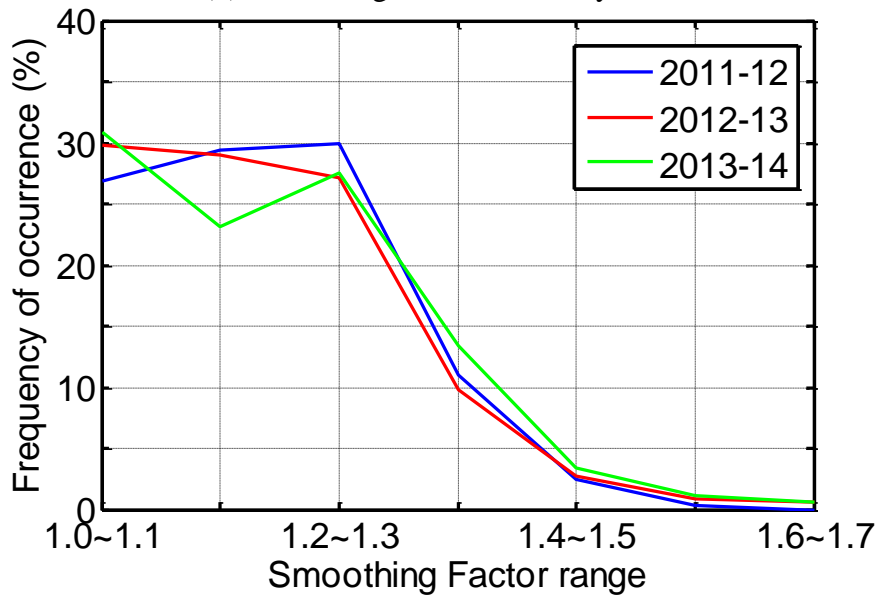
365 In this paper, the correlation coefficient between two PV sites (27A and 98A) on
366 power fluctuations is examined at three different time resolution levels, and the results
367 are listed in Table 3. It can be seen that the correlation coefficients increase with time
368 resolution intervals, and this means the two PV sites are more correlated with a longer
369 period of time. It is due to the fact that the clouds are more likely to shade or clear the
370 area coverage of these PV sites at the 5-min resolution level rather than at the 1-min level,
371 which again is an indication of the smoothing effect.

372 (a) Cumulative Distribution of PV power output change



373
374

(b) Smoothing Factor for all 3 years



375
376
377

Figure 7 Comparison of yearly variability

378 Table 3 Mean value of correlation coefficient for three different time resolutions
379

Time Resolution	Annual mean of correlation coefficient		
	2011-12	2012-13	2013-14
1-min	0.41	0.42	0.41
2-min	0.49	0.50	0.49
5-min	0.59	0.60	0.59

380

381 The correlation is also examined with respect to cloudiness, which is classified to
 382 four different levels – clear-sky, partly-cloudy (with infrequent transient clouds),
 383 extremely-cloudy (with frequent transient clouds) and overcast (totally cloudy or rainy
 384 without transient clouds). The mean values of correlation coefficients for different
 385 cloudiness are summarized in Table 4. Surely, the smoothing effect can again be
 386 observed from the tendency of the correlation values with different time intervals.
 387 However, more importantly the correlation in the horizontal direction shows an
 388 increasing trend with a sequence of extremely-cloudy, partly-cloudy, clear-sky and
 389 overcast. This indicates that when there are more frequent transient clouds, the
 390 correlation between two distanced PV sites becomes weaker, which is in turn also an
 391 evidence of the smoothing effect. It should be pointed out that the differences in
 392 correlation between clear-sky and overcast categories are probably due to small PV
 393 variability from low PV power generation in overcast days when comparing to that in
 394 clear-sky days. Therefore, the overcast set has the highest correlation coefficient.

395 Table 4 Mean value of correlation coefficient for different cloudiness
 396

Time Resolution	Mean of correlation coefficient for different cloudiness			
	Clear-sky	Partly-cloudy	Extremely-cloudy	Overcast
1-min	0.46	0.41	0.28	0.70
2-min	0.59	0.48	0.36	0.77
5-min	0.75	0.58	0.46	0.86

397

398 5. An Application Example

399 To further demonstrate the value of the statistical analysis provided in this paper,
 400 an example of its application is presented in this section. In late 2013, the University of
 401 Queensland was granted to complete a 3.4MWp PV plant in UQ Gatton campus, which
 402 has an approximate area of 700m × 300m (slightly bigger than that in Figure 1). The local

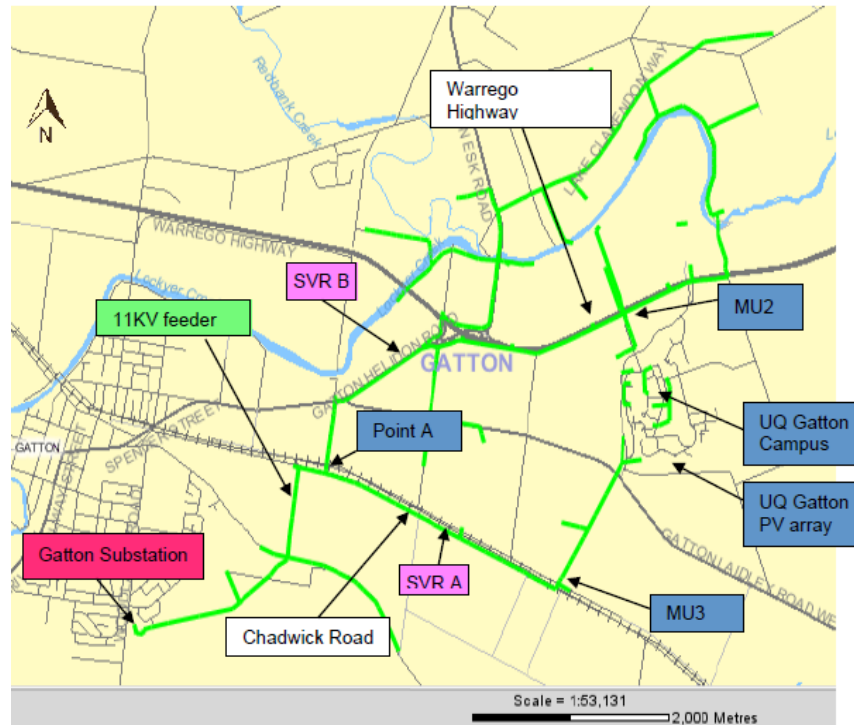
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403 power network structure is shown in Figure 8 [38]. The Gatton substation transforms grid
404 voltage from 33kV to 11kV, and then the 11kV network stretches around 7.5km to serve
405 UQ campus load, which normally ranges from 1MW to 3MW [39]. The line voltage is
406 traditionally supported by a step voltage regulator (SVR), which has an action time delay
407 of 2-min according to the regulation rules. The PV system, which is formed by 5 identical
408 684kWp array blocks in parallel, was planned to be connected to the 11kV level. Based
409 on the connection agreement [40], the voltage fluctuation limits are summarized in Table
410 5.

411 The focus was once to determine the size of the inverter (e.g. SMA
412 630kVA/720kVA/760kVA/800kVA ... [41]) that can guarantee there is enough reactive
413 power capacity to quickly compensate PV real power variations, therefore, the
414 corresponding voltage fluctuations can be controlled well within the limits in Table 5.
415 According to the connection agreement with the local distributor, the number of 4%
416 (0.04pu) voltage fluctuations cannot be more than once per hour, and 3% (0.03pu)
417 voltage fluctuations cannot be more than 10 times per hour. Surely, such estimation was
418 conducted before the construction of the Gatton PV plant, and only the sunlight radiation
419 data from a single station was available over a limited period. As a result, it is assumed
420 that PV power generation proportionally varies with sunlight radiation, which also
421 implies a linear relationship between PV power variations and radiation changes Next,
422 the emission evaluation of voltage fluctuation is conducted. Without any knowledge of
423 PV variability of such a scale, 90%/min power variation of the rated PV capacity was
424 concluded based on the recorded radiation profile at a single spot. However, 80%/min is
425 found to be more realistic for the dimension of this PV system as evidenced in previous
426 sections, and a comparison study will be presented next to show the importance of the

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427 knowledge of PV variability. The quasi-static time-series method [39] was applied with
 428 reactive power control suppressing voltage fluctuations [42] during investigation as
 429 shown in Figure 9.



430

Figure 8 UQ Gatton power network and PV connection map [38]

431

Table 5 Emission limits of voltage fluctuations [40]

432

433

Repetition frequency r (hour ⁻¹)	$\Delta V/V_N$ (%)
	MV (11/33kV)
$r \leq 1$	4
$1 < r \leq 10$	3

434

435

436

437

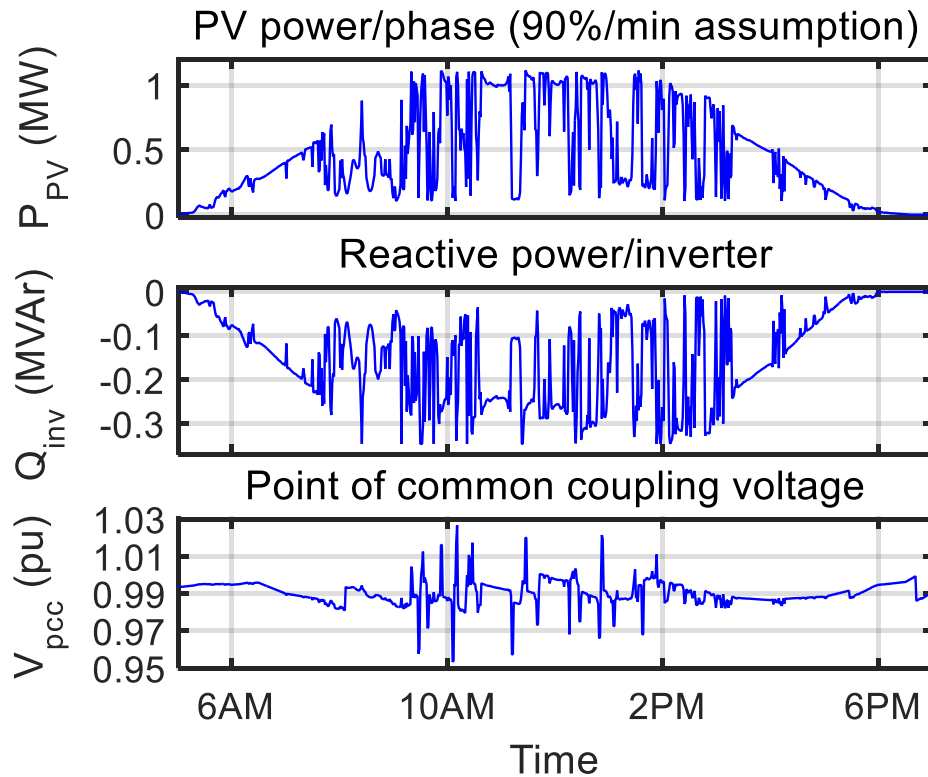
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440

The overall results are summarized in Table 6. Firstly, without any reactive power compensation (2nd and 3rd columns), the voltage fluctuations will become a serious concern for UQ to fulfill the connection agreement. Secondly, if such evaluation is conducted with an assumption of maximum 90%/min for ΔP_{pv} , the more expensive SMA 760kVA inverter would have been chosen rather than the SMA 720kVA inverter when considering to leave a certain safety margin. However, with certain knowledge of PV

441 variability of such a dimension (around 80%/min), the SMA 720kVA inverter was found
 442 to be sufficient for this application, which reduces the cost of the project.



443

444 Figure 9 Simulation results with Quasi-Static Time-Series method (720kVA inverter)

445

446

447

Table 6 Evaluation results

	Repetition frequency (maximum times per hour)				
	80%	90%	80%	90%	90%
ΔP_{pv_max}	No Q	No Q	720kVA	720kVA	760kVA
$\Delta V > 4\%$	1	4	0	1	0
$\Delta V = 3-4\%$	4	3	0	2	0
$\Delta V = 2-3\%$	6	6	1	3	0

448

449 6. Conclusions

450

451

452

This paper utilizes the recorded data over a 3-year period of a distributed PV system in the University of Queensland in Brisbane and performs statistical analyses for PV power variability. It has been observed that PV power variation in the studied time-

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453 resolution scale (1-min, 2-min and 5-min) has never exceeded 85% from August 2011 to
454 July 2014. The smoothing effect has a significant impact on the dispersed PV system of
455 the studied scale (a 700m × 150m area), and this effect has been evidenced via different
456 approaches, such as distribution of the number of events, cumulative distribution and
457 correlation coefficient. Moreover, the results suggest that PV power rise has happened
458 more frequently than power drop for significant power fluctuation events (approximately
459 $|\Delta P_{pv}| > 50\%$) due to potential PV temperature effect. This has been supported through a
460 few methods including distribution of the number of events, Quantile-Quantile Plot and
461 cumulative distribution. An application example has been presented to show the value of
462 statistical analysis. The information in this study will provide valuable statistics to current
463 and potential PV farm owners and power utilities for evaluating voltage regulation
464 requirement, determining compensation devices, and developing future network plans.

465

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472

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