

## **Title: Magnetic resonance characterisation of coupled gas and particle dynamics in a bubbling fluidized bed**

**September 14<sup>th</sup>, 2016**

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### **Abstract:**

Relative flow between granular material and gas can create phenomena in which particles behave like a liquid with bubbles rising through them. In this paper, magnetic resonance imaging (MRI) is used to measure the velocities of the gas and solid phases in a bubbling fluidized bed. Comparison with theory shows that the average velocity of gas through the interstices between particles is predicted correctly by classic analytical theory. Experiments were also used to validate predictions from computer simulations of gas and solid motion. The experiments show a wide distribution of gas velocities in both bubbling and emulsion regions, providing a new direction for computational and analytical theory.

## Introduction

Granular material displays solid-like, liquid-like and gas-like properties, creating complicated flow patterns, which present formidable challenges in characterisation [1–3] in part because conventional techniques cannot measure particle and gas dynamics quantitatively in opaque, 3D systems. Examples in which granular matter displays liquid-like properties include desert-dwelling animals “swimming” through sand [4], liquefaction during earthquakes [5], “bubbles” of gas rising through assemblies of solid particles [6], and an effective “surface tension” in granular streams falling through air [7]. Although conveying of granular materials is used widely in industry, understanding these flows presents challenges, giving uncertainty in plant design and potentially reduced output from industrial processes [8]. This difficulty in understanding systems employing granular flow stems from challenges in characterising them experimentally, especially two-phase systems employing gas and particles.

Fluidized beds are an important example of gas-particle flows, exhibiting fascinating phenomena such as bubbling; they are used in key processes in the chemicals, energy, food and pharmaceuticals industries. A fluidized bed can be formed in a vertical cylinder containing granular particles through which gas flows upwards. At a critical gas velocity, the minimum fluidization velocity ( $U_{mf}$ ), the drag force on the particles balances the gravitational force; the particles then exhibit liquid-like behaviour [6]. At velocities above  $U_{mf}$ , bubbles of gas may rise through the system, causing rapid mixing and efficient contact between the gas and particles. Such contact is needed in, *e.g.*, systems where the gas and solids have to react chemically whilst maintaining a nearly uniform temperature distribution. Analytical theory [6,9] and computer simulations [10] capture key elements of these macro-scale hydrodynamics and indicate that fluidized beds can be highly selective and minimize waste, making them ideal for the development of ‘green’ processes [11]. However, a lack of detailed, quantitative measurements of gas motion and meso-scale dynamics has limited the introduction of these processes at industrial scale [12]. In this paper, we report spatially-resolved magnetic resonance imaging (MRI) measurements of gas velocity distributions within a fluidized bed and use the results to interrogate analytical theory of two-phase fluidization and commonly used Euler-Lagrange simulations of fluid-particle flows.

Various techniques are available to measure granular dynamics [13–15] and liquid flow [16,17]. Measurements on gases are possible in dilute granular flow [18] and MRI has been used

to map flows of gas in fixed beds of solids [19]. However, the high diffusivity and low density of gases makes measurements challenging, especially when coupled with rapid motion of particles. Fluidized beds use particles with diameters  $d_p$  of  $\sim 1$  mm or less; previous MRI techniques have not been able to measure gas velocity accurately in beds of particles so small. Differences in the magnetic susceptibility between particles and fluid cause local variations in the strength of the magnetic field; these variations affect the measurement of motion. For low velocities of gas ( $< 0.05$  m/s), the field variations are overcome by using appropriate radiofrequency pulses to reverse the effect of the unwanted local variations in the magnetic field [20]. However, such an approach breaks down when studying faster flows of gas passing through beds of finer particles, *e.g.* in a fluidized bed, where local variations in the magnetic field are not constant for the required duration between radiofrequency pulses ( $\sim 1$  ms) and hence measurements are not quantitative [21,22].

The only previous characterisation of gas flow in fluidized beds using magnetic resonance used spatially-unresolved NMR to measure gas exchange coefficients between bubble, emulsion and absorbed states [23–26]. One of these studies [24] also conducted 1-D MRI measurements on particles to determine bubble rise velocities. Two of these studies [23,26] conducted preliminary, spatially-unresolved measurements of gas velocity distribution, showing wider distributions in gas velocities with increasing flow rate. In this study, we demonstrate the quantitative accuracy of our measurements and resolve gas velocity distributions spatially to view flow behaviour in bubbling and emulsion regions.

## **Materials and Methods**

### ***Fluidized bed arrangement***

Gas velocity measurements were conducted in a fluidized bed of particles contained in a PVC pipe. Details of the fluidized bed are summarised in Table 1. The bed had an internal diameter,  $D_{bed} = 52$  mm and was filled with poppy seeds of diameter  $d_p = 1.1$  mm, to a tapped bed height,  $H_0 = 100$  mm. The bed was fluidized using sulphur hexafluoride ( $\text{SF}_6$ ) gas at a pressure of 8.5 bar. The gas was kept at 8.5 bar in the bed in order to increase the NMR signal from it, as well as increase its relaxation times. Sulphur hexafluoride was chosen because each molecule contains six fluorine nuclei, and therefore the NMR signal is strong. In addition, the diffusivity of sulphur hexafluoride is low for a gas, which increases the resolution that can be achieved. Sulphur hexafluoride also has a relatively short  $T_1$  relaxation time (20 ms at 8.5 bar),

which permits a fast repetition rate for the experiments and hence reduces the total duration of the experiments. With the temperature of the SF<sub>6</sub> controlled at 25±3°C, its density was 56 kg/m<sup>3</sup> and its viscosity was approximately 1.6×10<sup>-5</sup> Pa·s. The particles were Group D according to Geldart's [27] classification. The minimum fluidization velocity,  $U_{mf}$ , which is the superficial, or open pipe, gas velocity at minimum fluidization, was measured to be 0.090±0.002 m/s based on the differential pressure across the bed. MRI was used to observe the onset of bubbling at  $U_{mb} = 0.090±0.002$  m/s. The values of  $U_{mf}$  and  $U_{mb}$  were thus found to be equal; this is to be expected for particles of Groups B or D. A porous plate distributor approximately 50 mm in diameter made of 250 µm sintered bronze was used. The plenum chamber beneath the distributor was filled with glass beads 2 mm in diameter. The pressure drop across the distributor was approximately 10 mbar at minimum fluidization, which is greater than the 6 mbar pressure drop across the bed thus ensuring even fluidization. MRI measurements of gas velocity near the distributor were indicative of even distribution of gas.

**Table 1.** Fluidized bed properties

Bed Property	Value
Inner diameter ( $D_{bed}$ )	52 mm
Tapped bed height ( $H_0$ )	100 mm
Particle type	Poppy seeds
Particle diameter ( $d_p$ )	1.1 mm
Geldart [27] Grouping	D
$U_{mf}$	0.090±0.002 m/s
$U_{mb}$	0.090±0.002 m/s
Gas molecule	SF <sub>6</sub>
Pressure	8.5 bar
Temperature	25±3°C
Gas density, $\rho$	56 kg/m <sup>3</sup>
Gas viscosity, $\mu$	1.6×10 <sup>-5</sup> Pa·s
Distributor type	Porous bronze plate

### ***MRI Arrangement***

MRI measurements were conducted using a Bruker DMX 200 spectrometer with a magnetic field strength of 4.7 T. The magnet was operated at a proton (<sup>1</sup>H) frequency of 199.7 MHz to measure signal from the oil in the poppy seeds and a <sup>19</sup>F frequency of 187.9 MHz to measure signal from the SF<sub>6</sub> gas. This separation of frequencies allowed signal from the particles and gas to be measured separately without interference. A birdcage radiofrequency (r.f) coil (capable of tuning to either the <sup>1</sup>H or the <sup>19</sup>F frequency) with an inner diameter of 64 mm was

situated around the fluidized bed to excite and detect signal from the seeds and gas. A shielded 3-axis gradient set capable of producing a maximum gradient of 0.139 T/m was used for imaging and velocimetry purposes.

The relaxation times ( $T_1$ ,  $T_2$ ,  $T_2^*$ ) for the poppy seeds and SF<sub>6</sub> gas were measured, to determine repetition times for successive MRI scans. These times are shown in Table 2. The repetition times were chosen as 3-5 times the spin-lattice relaxation time,  $T_1$ , so as to allow the net magnetisation to return almost completely to the vertical ( $z$ ) axis before the next excitation. The apparent transverse relaxation time,  $T_2^*$ , for both gas and particles was short, owing to background gradients arising from the difference in the magnetic susceptibility of the particles and the gas.

**Table 2** Relaxation times

<b>Molecule</b>	<b><math>T_1</math> (ms)</b>	<b><math>T_2</math> (ms)</b>	<b><math>T_2^*</math> (ms)</b>
<b>SF<sub>6</sub> in freeboard</b>	20	13	0.5
<b>SF<sub>6</sub> in bed of particles</b>	19	10	0.2
<b>Oil in poppy seeds</b>	373	75	0.3

### ***Horizontally-averaged measurements of time-averaged gas velocity***

Measurements of gas velocity averaged over the cross-section of the fluidized bed were conducted in the bed of particles under packed bed conditions in order to determine whether the gas velocity was measured accurately in a densely packed bed of small particles. The established 13-interval [20] pulse sequence was used as a control, representing the current state-of-the-art, and compared with the newly-developed 11-interval pulse sequence [28]. Fig. 1 shows a diagram of the radiofrequency (r.f.) pulses as well as the slice ( $G_{slice}$ ) and flow-encoding ( $g_{flow}$ ) gradients used for this pulse sequence. As detailed elsewhere [28], the pulse sequence was based on the 13-interval pulse sequence but designed to minimize the echo time ( $\tau$ ) and hence reduce the effect of the inhomogeneous magnetic field arising from the different magnetic susceptibility of the gas and particles. The inhomogeneous magnetic field was found to selectively attenuate signal from fast moving nuclei at high ( $> 0.03 \text{ m s}^{-1}$ ) gas velocities [28]. The attenuation occurs whilst the magnetisation is in the transverse plane (i.e. during the echo time). Thus the reduction in the echo time permitted by the 11-interval pulse sequence led to its increased accuracy in the measurement of the gas velocity. The parameters for the gas velocity measurements of the two pulse sequences are given in Table 3. For the 13- and 11- interval pulse sequences, the echo

times ( $\tau$ ) and flow encoding times ( $\delta$ ) were as short as possible given the slew rate limits for the gradient systems for the MRI system used. The observation times ( $\Delta$ ) were 6 ms, which is sufficiently long to encode for coherent motion, but short enough to avoid issues with fast moving signal leaving the r.f. coil undetected.

The range of velocities measured by MRI is determined by the field-of-flow, which is a function of the gradient strength, and timing parameters of the pulse sequence. For all experiments reported, the field-of-flow was kept constant at 2 m/s. The maximum gradient strength used for the experiments  $g_{flow}$  was 0.139 T/m.

To assess the accuracy of the measurements, the expected gas velocity ( $u_{z,expected}$ ) was evaluated according to

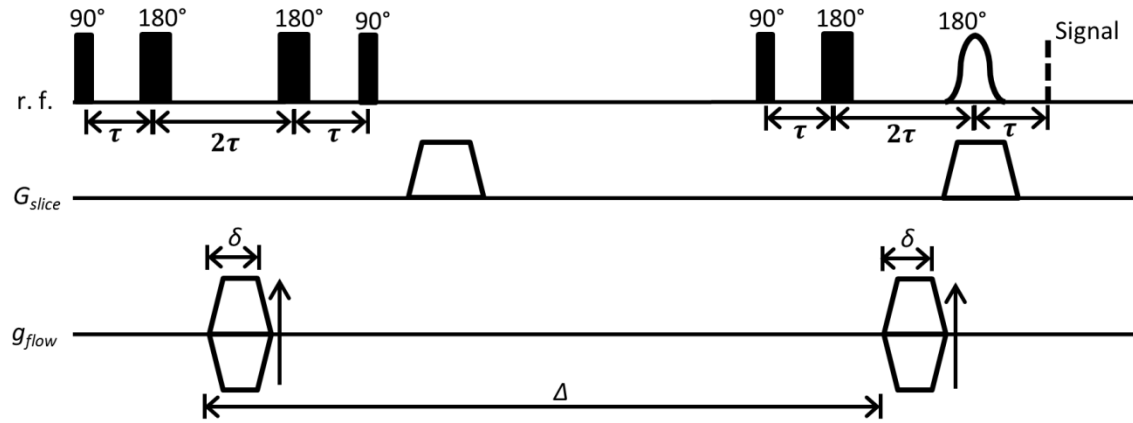
$$u_{z,expected}(U) = \frac{U}{1 - \phi(U)} \quad (1)$$

where  $\phi(U)$  is the solids volume fraction at a given superficial velocity and is defined by the void fraction  $\varepsilon$  according to  $\phi = 1 - \varepsilon$ , and  $U$  is defined as the volumetric flow rate divided by the cross-sectional area of the bed. The packing fraction was evaluated using magnetic resonance measurements of the poppy seeds, according to

$$\phi(U) = \phi_{packed} \cdot \frac{S(U)}{S_{packed}} \quad (2)$$

Where  $S(U)$  is the signal from a slice-selective spin echo pulse sequence on the poppy seeds at a given superficial velocity,  $U$ ,  $S_{packed}$  is the corresponding signal with the bed under packed conditions, for which the solids volume fraction was  $\phi_{packed} = 0.57$ . The low value of  $\phi_{packed}$  was due to the non-sphericity of the particles. This value of  $\phi_{packed}$  was measured by filling a graduated cylinder to a specified volume,  $V_{packed}$ , with poppy seeds. The packed volume,  $V_{packed}$ , consists of the volume of the seeds and the interstitial gas. The volume of the poppy seeds alone,  $V_{seeds}$ , was determined by submerging the seeds underwater in a graduated cylinder and measuring the increase volume after adding the seeds. Knowing the packed volume of the seeds,  $V_{packed}$ , and the actual volume of the seeds,  $V_{seeds}$ , the packing fraction was:

$$\phi_{packed} = \frac{V_{seeds}}{V_{packed}} \quad (3)$$



**Fig. 1.** Pulse sequence diagram for 11-interval MRI velocimetry.

**Table 3** Parameters for cross-section-averaged measurements of vertical gas velocity with different pulse sequences

Parameter	13-interval	11-interval
Field of flow (FoF)	2.00 m/s	2.00 m/s
Full-width-half-maximum slice thickness	4 mm (z)	4 mm (z)
Phase cycling	8-step cogwheel	12-step cogwheel
Observation time ( $\Delta$ )	6 ms	6 ms
Flow encoding gradient period ( $\delta$ )	100 $\mu$ s	100 $\mu$ s
Echo time ( $\tau$ )	780 $\mu$ s	360 $\mu$ s
Recycle time	75 ms	75 ms
Number of averages	3	2
Acquisition time	30 seconds	30 seconds

### ***Maps of time-averaged velocity and void fraction***

Maps of gas velocity were acquired in the bed of particles using the 11-interval pulse sequence shown in Fig. 1, but with additional phase encoding gradients used for imaging. The phase encoding gradients were applied at the same time as the second flow encoding gradient. Parameters for these measurements are summarised in Table 4. The experimental determinations of gas velocity were obtained using a circular sampling of 193 points on a 16 by 16 Cartesian grid in  $k$ -space. The circular sampling was used to decrease the acquisition times (256 points would need to be acquired for a full image in  $k$ -space) without losing significant signal intensity or sharpness of the circular image in real space. For images in the bed of particles, 8 averages were acquired requiring a total time of approximately 80 minutes. Images were zero-filled to 128 by 128 Cartesian grid points prior to Fourier transformation. The maximum spatial frequency

measured was  $\sim 150 \text{ m}^{-1}$ , corresponding to a resolution of 3.75 mm. Throughout this paper, the phrase pixel size is used to define the dimensions of pixels in the images after zero filling, which in all cases was 0.47 mm; the resolution is determined by the maximum spatial frequency measured. A 12-step cogwheel phase cycle was used, determined with the CCCP++ software [29], to negate erroneous signal arising in individual, free-induction decay readings. MRI measurements were made under bubbling fluidization conditions with  $U = 0.104 \text{ m/s}$  and in a packed bed state ( $U < U_{mf}$ , i.e. the particles were stationary) with  $U = 0.080 \text{ m/s}$  and  $0.065 \text{ m/s}$ . These measurements were made at a variety heights in the bed. The expanded bed height for  $U = 0.104 \text{ m/s}$  was  $H = 120 \text{ mm}$ . Determinations of gas velocity were made only for its vertical ( $z$ ) component; images attempted for the horizontal components of the gas velocity showed interference with the imaging gradients, and hence quantitative maps of velocity in the  $x$ - and  $y$ -directions were unobtainable.

**Table 4** Parameters for measurements of maps of gas velocity

Parameter	Value
Field of view (FoV)	60 mm ( $x$ ) by 60 mm ( $y$ )
FWHM slice thickness	4 mm ( $z$ )
Resolution	3.75 mm ( $x$ ) by 3.75 mm ( $y$ )
Pixel Size	0.47 mm ( $x$ ) by 0.47 mm ( $y$ )
Pulse sequence	11-interval
Phase cycling	12-step cogwheel
Observation time ( $\Delta$ )	6 ms
Flow encoding gradient period ( $\delta$ )	100 $\mu\text{s}$
Echo time ( $\tau$ )	360 $\mu\text{s}$
Field of flow (FoF)	3 m/s
Recycle time ( $T_R$ )	75 ms
Number of flow encoding gradients	3
Number of averages ( $N_{avg}$ )	8
Acquisition time	80 min

Maps of particle velocities were also determined, at various heights above the distributor, using a spin echo pulse sequence [30] with the parameters in Table 5. The parameters in Table 5 were such that the pixel size was the same as for the maps of gas velocity; thus, particle and gas velocities could be compared directly. For the particles, circular sampling was used with 4 averages in  $k$ -space and a 4-step phase cycle. The recycle time for the particle measurements was 1.12 s thus exceeding the  $T_1$  of the oil in the particles, 373 ms; hence, the total acquisition time was approximately 180 minutes. The images were reconstructed by zero-filling to 128 by



128 grid points, prior to Fourier transformation. Intensity maps were approximately piece-wise constant and therefore these were reconstructed to 128 by 128 pixels using a compressed sensing algorithm to minimise Gibbs ringing artefacts [31]. From the  $k$ -space maps in which no flow gradient was turned on, maps of signal intensities arising from the particles were acquired and converted into maps of void fraction. For this conversion, an intensity map was first acquired of a packed bed with a solids volume fraction of  $\phi = 0.57$ . The signal for each pixel is dependent on the sensitivity of the radiofrequency coil. These variations also occur in images under flow conditions; hence, for images in the fluidized bed, the solids volume fraction for each pixel was assessed using the ratio of the signal intensity to the signal intensity from the corresponding packed bed image:

$$\phi_{fluidized}(x, y) = \phi_{packed} \cdot \frac{S_{fluidized}(x, y)}{S_{packed}(x, y)} \quad (4)$$

Here,  $\phi_{fluidized}(x, y)$  is the solids volume fraction of the pixel at coordinates  $x$  and  $y$  in a map under fluidized conditions,  $\phi_{packed}$  is the solids volume fraction for a packed bed (volumetrically measured to be 0.57),  $S_{packed}(x, y)$  is the signal intensity from a pixel in the packed bed map and  $S_{fluidized}(x, y)$  is the signal intensity from the corresponding pixel in the fluidized map. The maps of packing fraction for the fluidized images were then converted into void fraction maps using:

$$\varepsilon_{fluidized}(x, y) = 1 - \phi_{fluidized}(x, y) \quad (5)$$

where  $\varepsilon_{fluidized}(x, y)$  is the void fraction at a pixel of a fluidized map. Fig. 2 shows the map of signal intensity of a packed bed used in Equation 4. Fig. 2 shows variations in intensity due to sensitivity of the radiofrequency coil; additional variations in intensity owing to partial volume effects and Gibbs ringing are seen around the perimeter of the image. These effects are largely negated in the voidage maps under flow conditions by using the calculation shown in Equation 4.

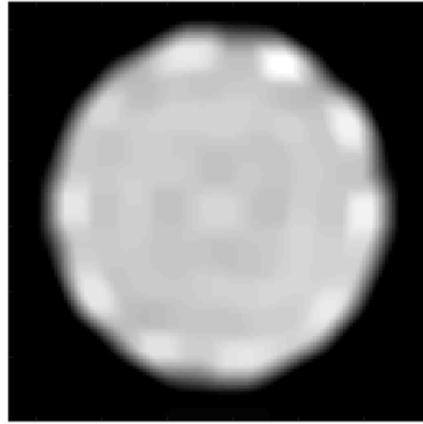
For comparison of flow patterns between simulation predictions and experimental results and assessment of the accuracy of measurements, it was useful to quantify average gas velocities in maps or regions of maps. The average velocity,  $u_{z,avg}$ , was calculated by weighting the gas velocity by the void fraction on a pixel-by-pixel basis:

$$u_{z,avg,map} = \frac{\sum_{N_{pixels}} u_z(x, y) \varepsilon(x, y)}{\sum_{N_{pixels}} \varepsilon(x, y)} \quad (6)$$

where  $N_{pixels}$  is the number of pixels in the averaging region and  $u_z(x, y)$  and  $\varepsilon(x, y)$  are the measured time-averaged vertical gas velocity and void fraction in a pixel of the averaging region, respectively.

**Table 5** Parameters for the acquisition of maps of particle velocity and void fraction

Parameter	Value
Field of view (FoV)	60 mm (x) by 60 mm (y)
FWHM slice thickness	4 mm (z)
Resolution	3.75 mm (x) by 3.75 mm (y)
Pixel size	0.47 mm (x) by 0.47 mm (y)
Pulse sequence	Spin echo SPI
Phase cycling	4-step
Observation time ( $\Delta$ )	2.33 ms
Flow encoding gradient period ( $\delta$ )	100 $\mu$ s
Echo time ( $\tau$ )	2 ms
Field of flow (FoF)	3 m/s
Recycle time ( $T_R$ )	1.12 s
Number of flow encoding gradients	3
Number of averages ( $N_{avg}$ )	4
Acquisition time	180 min



**Fig. 2** Map of signal intensity arising from oil in poppy seeds in packed bed used to calibrate void fraction in fluidized bed measurements with white regions indicating high signal intensity and black regions indicating zero signal. Field of view 60 mm (x) by 60 mm (y); slice thickness: 4 mm,  $z = 50$  mm above distributor; pixel size: 0.47 mm (x) by 0.47 mm (y).

### ***Measurements of gas velocity distribution***

Measurements of velocity distributions of  $\text{SF}_6$  gas averaged across the horizontal cross-section of the bed were acquired at different superficial velocities using propagator measurements. Propagator measurements are an MR technique similar to velocity measurements, but they use a number of small increments in the magnitude of the flow encoding gradient to

determine a distribution of velocities rather than an average velocity. The parameters for these propagator measurements in the bed of particles and the freeboard are summarised in Table 6. For all propagator measurements, the 11-interval pulse sequence [28] was used. The observation time,  $\Delta$ , was increased to 15 ms to enable 16 gradient steps to be acquired with a field of flow of 2 m/s. Longer observation times were not used as the signal to noise ratio became too low beyond this value and signal from fast moving gas could have been missed due to the limited size of the r.f. coil. The measurements were conducted to determine the distribution of the vertical component of gas velocity at a position  $z = 50$  mm above the distributor.

Average velocities from the velocity distributions were calculated using:

$$u_{z,avg,distribution} = \frac{\sum_{i=1}^{N_{vel}} u_{z,i} S_i}{\sum_{i=1}^{N_{vel}} S_i} \quad (7)$$

Here  $u_{z,i}$  is the value of velocity for bin  $i$ ,  $N_{vel}$  is the number of velocity bins in the distribution and  $S_i$  is the signal from bin  $i$ .

**Table 6** Parameters for measurements of gas velocity distributions averaged over the cross-section of the bed

Parameter	Value
Field of flow ( $FoF$ )	2.00 m/s
FWHM slice thickness	4 mm ( $z$ )
Velocity Resolution	0.0625 m/s
Pulse sequence	11-interval
Phase cycling	12-step cogwheel
Observation time ( $\Delta$ )	15 ms
Flow encoding gradient period ( $\delta$ )	100 $\mu$ s
Echo time ( $\tau$ )	360 $\mu$ s
Recycle time ( $T_R$ )	75 ms
Number of flow encoding gradients	16
Number of averages ( $N_{avg}$ )	128
Acquisition time	65 min

### ***Map of the distribution of the gas velocity at each cross-sectional position***

A cross-sectional map of the distribution of vertical gas velocities was acquired for the bubbling fluidization case,  $U = 0.104$  m/s, at a position  $z = 50$  mm above the distributor. This map was acquired in order to understand gas flow patterns in the bubbling and emulsion regions of a bubbling fluidized bed. The imaging parameters used for the measurement were the same as in the maps of gas velocity, shown in Table 5. The velocity distribution parameters were the

same as in the unresolved propagator measurements in the  $z$ -direction, shown in Table 6. The number of averages was reduced to 4, so as to avoid a prohibitively long acquisition time. The acquisition time was still long, 6.5 hours, and thus measurements were not conducted at other superficial velocities or positions in the bed.

### ***CFD-DEM simulations***

CFD-DEM simulations were run using open-source CFDEM [32] software which couples the DEM capabilities of LIGGGHTS [33] with the CFD capabilities of OpenFOAM [34]. Simulation parameters were set to match the system exactly, except that, for DEM purposes, spherical particles were simulated, even though the actual particles had a kidney shape.

**Table 7.** Discrete element model (DEM) parameters used in CFD-DEM simulations

Parameter	Value
Tapped bed height, $H_0$	100 mm
Bed diameter, $D_{bed}$	52 mm
Particle shape	Spherical
Particle diameter, $d_p$	1.07 mm
Particle density	1040 kg/m <sup>3</sup>
Coefficient of restitution	0.93
Coefficient of friction (particle-particle)	0.4
Coefficient of friction (particle-wall)	0.8
Young's modulus	1.2 MPa
Spring model	Hertzian

The discrete element method (DEM) was used to model the motion of each individual particle using contact mechanics and Newtonian physics. The DEM parameters are summarized in Table 7. A Hertzian spring model was used for normal and tangential contacts with a coefficient of restitution set to 0.93. This value of coefficient of restitution was chosen to match that used in previous CFD-DEM studies using poppy seeds [35–38]; a CFD-DEM study which varied coefficient of restitution from 0.47 to 0.97 and compared predictions with measurements of poppy seed velocity found the effect of coefficient of restitution to be minimal [39]. Coulomb's law was used to account for sliding, with a coefficient of friction for particle-particle interactions of 0.4 used based on the experimental value [40]. The coefficient of friction for particle-wall interactions was unknown, but was varied and found to have a negligible impact on simulation predictions.

Computational Fluid Dynamics (CFD) was used to model the gas phase as a continuum, with a discretized form of the volume-averaged fluid equations [41] used to solve for gas velocity and pressure on a co-located fluid grid. The CFD parameters used are summarized in Table 8. A code for incompressible flow was used with an implicit solver to allow for longer time steps. An unstructured grid was used to fit the cylindrical shape of the bed with mostly rectangular cells used in the centre of the system and wedge-shaped cells used near the walls. The grid spacing in the vertical direction was  $dz = 4$  mm, between 3 and 4 particle diameters, in order to achieve grid independent results while satisfying the conditions for the volume averaged fluid equations [35,42]. Similar grid spacing was used in the horizontal direction.

**Table 8.** CFD parameters used in CFD-DEM simulations

Parameter	Value
Overall height of simulation	400 mm
Bed diameter, $D_{bed}$	52 mm
Fluid grid spacing	~4 mm
Number of fluid grids	145,000
Superficial velocity, $U$	0.104 m/s
Inlet gas diameter	40 mm
Wall boundary condition	No slip
Outlet boundary condition	Constant pressure
Gas density	52 kg/m <sup>3</sup>

At the inlet, the gas velocity was set to match the superficial velocity used in experiments, with even distribution of gas to match the expected distribution obtained from the porous plate used experimentally. The diameter of the inlet area was set to 40 mm, to match the diameter of the plenum chamber. At the outlet, a constant pressure boundary condition was used. The no-slip boundary condition was used along the walls. Gas and particle motion were linked using the drag law of Beetstra *et al.* [43].

The particles in the experiments were non-spherical. In an effort to model the non-sphericity of the experimental particles, “effective particle diameters” were used in the model. In this approach, the particles were modelled as spherical in all aspects of the simulations, but different particle diameters were used for different calculations in the simulations. The particle diameter used for calculations related to contact mechanics and weight of the particles was  $d_{p,c} =$

1.07 mm, to match the experimental particles. Since spherical particles pack more densely than the experimental particles, the particle diameter used for calculating void fraction in all aspects of the simulations was reduced to  $d_{p,v} = 1.00$  mm, so that the void fraction at minimum fluidization from the simulations matched that measured experimentally. The particle diameter used for calculating drag force was increased to  $d_{p,d} = 1.55$  mm, so the minimum fluidization velocity given by simulations equalled that measured experimentally. This increase in particle diameter for calculating drag is consistent with non-spherical particles having a larger surface area per unit volume than their spherical counterparts.

CFD-DEM simulations were run for 5 s of simulation time and predictions from times  $t = 2$  s to  $t = 5$  s were used to generate the maps and probability distribution functions in the Results section. The simulations were run on 16 separate 2.3 GHz Intel Xeon E5-2470 processors, and each simulation took approximately 30 hours to run.

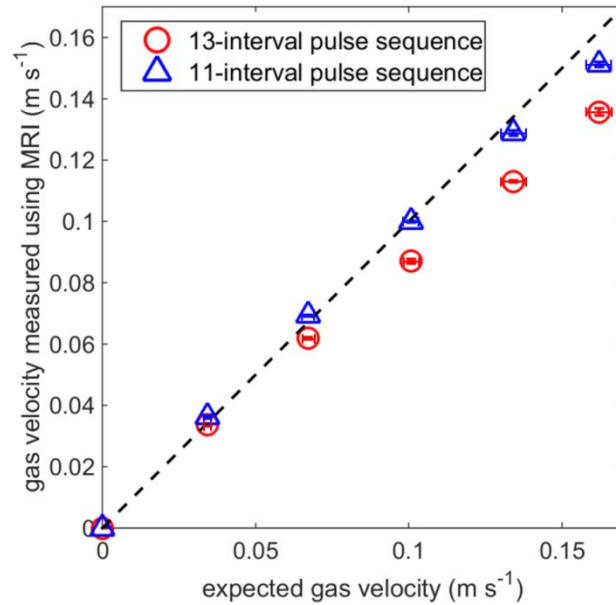
## Results and Discussion

### *Accuracy of measurements*

Fig. 3 shows measurements of time-averaged and cross-sectionally-averaged velocities of gas through the bed under packed conditions. The newly-developed 11-interval sequence is shown to enable quantitative measurements of the gas velocity at up to 0.15 m/s, which corresponds to the gas velocity during fluidization in this setup. The 11-interval sequence was able to measure gas velocity quantitatively at significantly higher velocities than the 13-interval sequence of Cotts *et al.* [20], the previous state-of-the-art for measuring fluid velocities in heterogeneous systems.

In order to understand gas dynamics in further depth, spatially-resolved measurements and measurements of gas velocity distribution must be conducted. With these added complexities, the accuracy of the measurements could be questioned further. The averaged velocities deduced from time-averaged velocity maps and velocity probability distribution functions for the bed under packed bed conditions, all from MRI measurements, are compared with expected values, given by  $U/\varepsilon$ , in Table 9. The measurements are all within 0.01 m/s of the expected value from the flow meter with the greatest differences coming from measurements at the highest superficial velocity. It is difficult to quantify the accuracy of the MRI measurements in the bubbling fluidized bed, since void fraction oscillated in time and only time-averaged measurements were obtained. However, the measurements in the bubbling fluidized bed are

expected to be as accurate as those in packed cases, since background gradients arise from tight packing of particles and there are almost no particles in bubbles. Thus, although the gas moves quickly through bubbles, the measurements of gas velocity in bubbles should be more accurate due to the lack of background gradients. As shown in Fig. 9 (A), the gas velocity distribution through the emulsion phase during bubbling is nearly identical to that at minimum fluidization, making the accuracy of measurements in the emulsion phase approximately the same as that in the  $U = 0.080$  m/s case.



**Fig 3.** Measurements of the vertical component of SF<sub>6</sub> gas velocity through a packed bed (i.e. no fluidization) of poppy seeds ( $d_p = 1.1$  mm). The measurements give the average gas velocity over the cross-section of the bed at a height 50 mm above the distributor. Measurements were made using (◐) the Cotts 13-interval pulse sequence [20], which is widely regarded as the best existing MRI technique for measuring flow in heterogeneous systems, and (◔) the newly-developed 11-interval pulse sequence [28]. All measurements were repeated 3 times and showed a standard deviation of less than 0.002 m/s. Measurements were compared with the expected velocity, given by the dotted black line and calculated as  $U/\varepsilon$ , where  $\varepsilon$  is the void fraction. The superficial velocity  $U$  was calculated from gas flow meter measurements. Uncertainty for the expected gas velocity, as given by the horizontal error bars, arises from the uncertainty in the void fraction measurement. Parameters for the measurements are shown in Table 3.

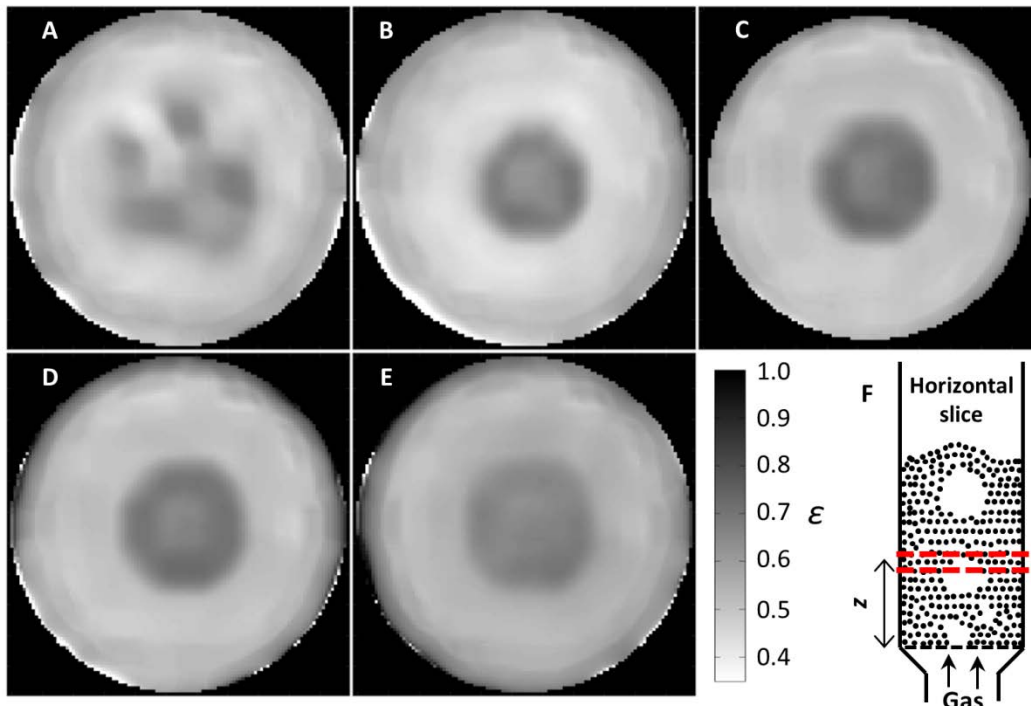
### ***Hydrodynamics at different vertical positions***

In order to understand hydrodynamics in the bubbling bed, time-averaged maps of void fraction, particle velocity and gas velocity were measured using MRI. Fig. 4 shows time-averaged void fraction maps at different vertical positions in the bed. The images start at a position (A) 10 mm above the bed and increase in vertical position to (E), 100 mm above the distributor. Figs. 5 (A)-(E) all show a time-averaged void fraction larger in the centre of the bed than near the walls, indicative of bubbles rising along the axis of the bed. At 10 mm above the

distributor (A), several regions are seen in the centre of the bed where the void fraction is slightly higher than at the extremities of the bed; the regions of higher void fraction are in a central circular region with a diameter approximately half that of the bed. At a position 25 mm above the distributor (B), the void fraction is much higher in the centre of the bed over a circular area with a diameter approximately one-third that of the bed. At positions 50 to 100 mm above the distributor (C-E), the contrast between the void fraction in the central region and the region near the walls diminishes, with the region of higher void fraction confined within a diameter slightly larger than in the  $z = 25$  mm position (B).

**Table 9** Comparison of average velocity measurements from velocity maps and velocity distributions with expected velocities for packed bed conditions ( $U < U_{mf}$ )

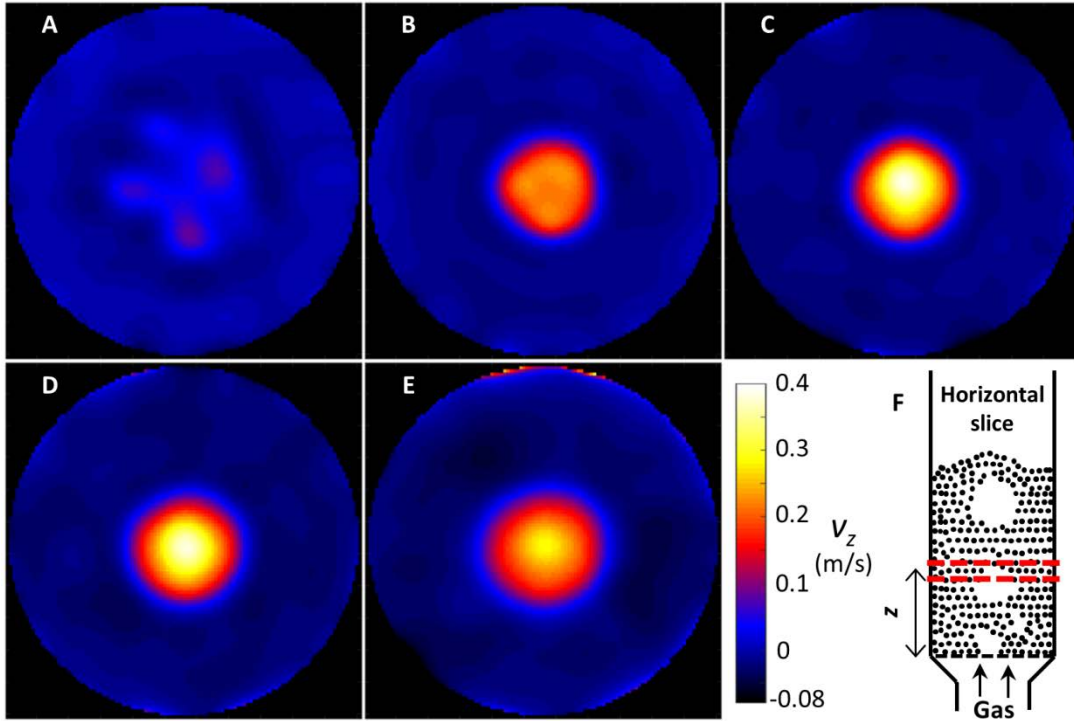
Measurement	Superficial velocity, $U$ (m/s)	Average velocity from MRI (m/s)	Expected velocity from flow meter, $U/\epsilon$ (m/s)
Gas velocity map	$0.065 \pm 0.001$	$0.125 \pm 0.004$	$0.127 \pm 0.004$
Gas velocity map	$0.080 \pm 0.001$	$0.147 \pm 0.004$	$0.151 \pm 0.004$
Gas velocity distribution	$0.065 \pm 0.001$	$0.122 \pm 0.004$	$0.127 \pm 0.004$
Gas velocity distribution	$0.080 \pm 0.001$	$0.146 \pm 0.004$	$0.151 \pm 0.004$



**Fig. 4** Time-averaged void fraction maps obtained from intensity maps of poppy seeds at different vertical positions in the fluidized bed. Fluidization regime: bubbling;  $U = 0.104$  m/s; field-of-view: 53 mm ( $x$ ) by 53 mm ( $y$ ); FWHM slice thickness: 4 mm ( $z$ ); pixel size: 0.47 mm ( $x$ ) by 0.47 mm ( $y$ ); vertical positions above distributor: (A)  $z = 10$  mm, (B)  $z = 25$  mm, (C)  $z = 50$  mm, (D)  $z = 75$  mm, (E)  $z = 100$  mm; expanded bed height: 120 mm.



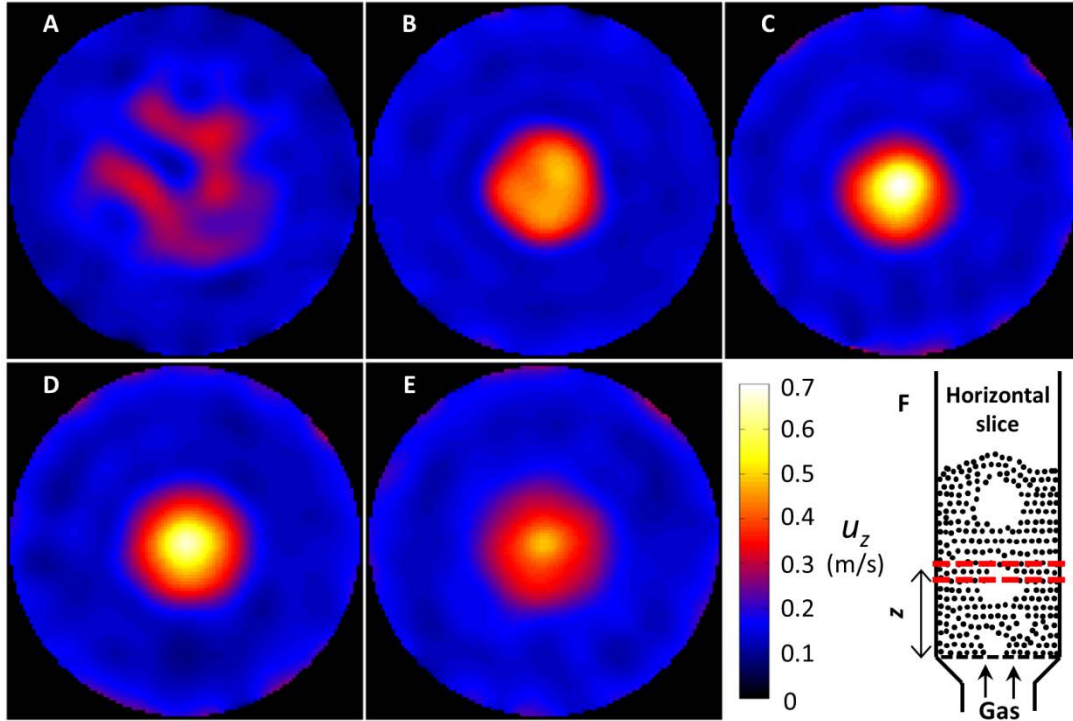
Fig. 5 shows maps of the time-averaged vertical particle velocity ( $v_z$ ) at different vertical positions in the bed of particles. These maps show an upward moving profile in the centre of the bed with time-averaged velocities of up to 0.4 m/s. The diameter of this upward velocity region is similar to the diameter of the high void fraction region for the corresponding void fraction images in Fig. 4. In Figs. 5 (B)-(E) the region of upward velocity is surrounded by a much larger region of downward velocity with an almost uniform time-averaged velocity just below 0 m/s. For the  $z = 10$  mm case in Fig. 5 (A), the profile is similar to those in Figs. 5 (B)-(E), except that the upward moving profile is slightly wider and the maximum time-averaged velocity is only about 0.1 m/s.



**Fig. 5** Time-averaged particle velocity maps of poppy seeds at different vertical positions in the fluidized bed. Fluidization regime: bubbling;  $U = 0.104$  m/s; field-of-view: 53 mm ( $x$ ) by 53 mm ( $y$ ); FWHM slice thickness: 4 mm ( $z$ ); pixel size: 0.47 mm ( $x$ ) by 0.47 mm ( $y$ ); vertical positions above distributor: (A)  $z = 10$  mm, (B)  $z = 25$  mm, (C)  $z = 50$  mm, (D)  $z = 75$  mm, (E)  $z = 100$  mm; expanded bed height: 120 mm.

Fig. 6 shows time-averaged maps of the vertical component of gas velocity ( $u_z$ ) at the same positions and the same fluidizing velocity as Figs. 4 and 5. Qualitatively, the maps look very similar to those for particle velocity at the corresponding vertical position in the bed of particles. For  $z = 25$ -100 mm above the distributor in Figs. 6 (B)-(E), there is a region of fast upward velocities (up to 0.7 m/s) in the centre of the bed, and a region of much lower, upward-

moving velocities (around 0.15 m/s) in the larger outer annulus of pixels. In Fig. 6 (A), a wider central profile shows gas velocities up to 0.25 m/s while the outer annulus has upward gas velocities around 0.1 m/s.

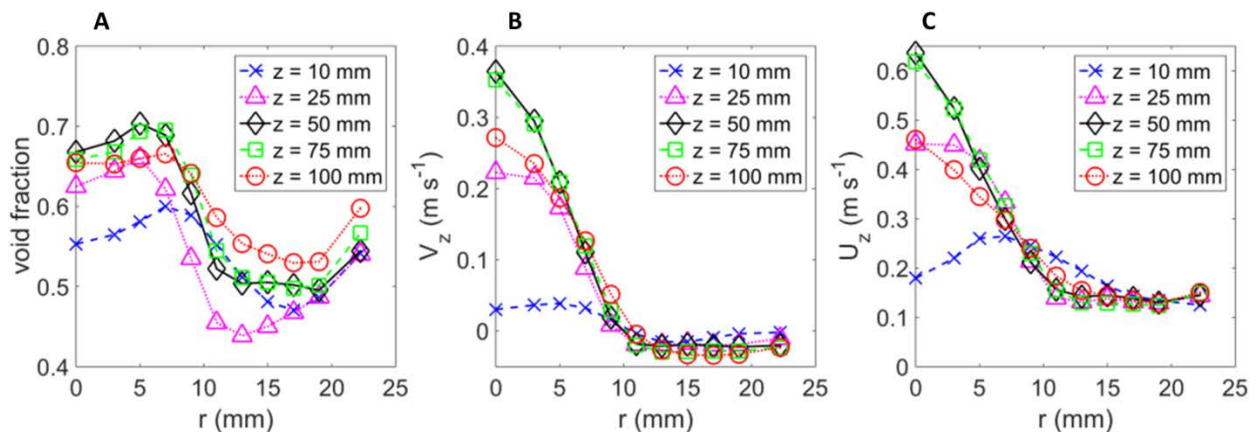


**Fig. 6** Maps of time-averaged gas velocity of  $\text{SF}_6$  at different vertical positions in the fluidized bed. Fluidization regime: bubbling;  $U = 0.104$  m/s; field-of-view: 53 mm ( $x$ ) by 53 mm ( $y$ ); FWHM slice thickness: 4 mm ( $z$ ); pixel size: 0.47 mm ( $x$ ) by 0.47 mm ( $y$ ); vertical positions above distributor: (A)  $z = 10$  mm, (B)  $z = 25$  mm, (C)  $z = 50$  mm, (D)  $z = 75$  mm, (E)  $z = 100$  mm; expanded bed height: 120 mm.

The results for particle and gas velocity, as well as void fraction, at  $U = 0.104$  m/s in Figs. 4-6 are consistent with a stream of bubbles rising through the centre of the bed. Because bubbles have a void fraction close to unity, having bubbles periodically pass through the centre of the bed would lead to a higher time-averaged void fraction in the centre of the bed than near the walls, as seen in Figs. 4 (B)-(E). Bubbles often form after very small void regions coalesce just above the distributor, explaining the wide region of higher time-averaged void fraction seen 10 mm above the distributor in Fig. 4 (A). In bubbling fluidized beds, it is common to see a “gulf-stream” pattern in which particles move quickly upwards in the wakes of bubbles and then slowly downwards near the walls. This pattern is consistent with the time-averaged particle velocities seen in Fig. 5. The gas flow in a fluidized bed is usually greatest through the bubbles as there is less resistance to flow due to the small numbers of particles in the bubbles. This flow pattern is consistent with the time averaged gas velocities seen in Fig. 6.

An alternative explanation for the gas and particle motion seen in Figs. 4-6 would be the formation of a jet or spout. This explanation seems, at first, plausible, since the sizes of the time-averaged void regions are fairly narrow and do not change much with distance above the distributor in the  $z = 25$ -100 mm range. However, it is unlikely that a spout would have formed because a porous distributor with a significant pressure drop was used; this would give an even distribution of gas, rather than a jet. Additionally, if a jet were formed, the maximum gas and particle velocities would be expected at the  $z = 10$  mm position. Experimentally the gas and particle velocities in the centre of the bed increased to a maximum between 50 mm and 75 mm above the distributor, consistent with the velocity arising from the motion of bubbles.

The results at  $z = 10$  mm are particularly interesting because they are most different from the results at other heights in the bed, and they demonstrate the least radial symmetry. As discussed earlier, we explain the behaviour seen at  $z = 10$  mm as a position at which smaller bubbles are forming before they quickly coalesce into a single central bubble before the  $z = 25$  mm height. From the void fraction map in Fig. 4 (A), there appear to be four or five small regions with higher void fraction near the centre of the bed, but not arranged in a radially symmetric manner. The velocity maps in Fig. 5 (A) and Fig. 6 (A) are indicative of particles and gas rising faster in these four or five regions. This pattern can be explained by defects in the distributor or instabilities in the flow causing persistent nucleation points for bubbles just below these four or five regions. Since the averaging time for these experiments was such that thousands of bubbles were able to form over the course of the averaging, it seems likely that these are indeed persistent flow features and unlikely that a different or more radially symmetric pattern would form at  $z = 10$  mm if a larger averaging time were used.



**Fig. 7.** MRI measurements of time-averaged (A) void fraction, (B) vertical particle velocity and (C) vertical gas velocity as a function of radial position at different heights ( $z$ ) above the distributor; expanded bed height: 120 mm.

To compare flow behaviour at different heights in the bed more quantitatively, Fig. 7 shows line plots for (A) void fraction, (B) particle velocity and (C) gas velocity as a function of radial position for different heights in the bed. Similar flow patterns are seen at  $z = 25$ - $100$  mm, with a higher void fraction and velocities in the centre of the bed due to bubbles rising through this central region. The similarity of these line plots is indicative that bubbles maintain a similar size without coalescing or splitting within this range of heights. Void fraction surprisingly increases close to the walls in this region: this is likely due to particles not being able to pack as closely near the walls as well as artefacts due to inhomogeneity in the magnetic field near the walls. The void fraction is slightly lower in the very centre of the bed than at radial positions  $r \sim 2$ - $8$  mm. As shown in Fig. 8 (H), the same trend is seen in CFD-DEM simulations. CFD-DEM simulations show that this void fraction pattern arises due to bubbles having a dimple at their bottom, thus creating slightly more void region at  $r \sim 5$  mm than  $r \sim 0$  mm. In the  $z = 25$ - $100$  mm range, nearly identical hydrodynamics are observed for the  $z = 50$  mm and  $z = 75$  mm heights, while profiles with slightly lower void fractions and velocities in the centre of the bed are observed for the  $z = 25$  mm and  $100$  mm heights. The lower velocities and void fractions at  $z = 25$  mm are likely indicative that the bubbles are still growing and developing into a stable state at this height. The lower values at  $z = 100$  mm are likely indicative of deformation of the bubbles as they approach the bed surface, given the fact that the bubbles are approximately 20 mm in diameter and the expanded bed height is approximately 120 mm. These same trends were seen in CFD-DEM simulations due to bubble growth low in the bed and bubble deformation high in the bed. The nearly identical profiles for  $z = 50$  mm and  $z = 75$  mm are likely indicative that the bubbles are fully-developed in this range of heights and are not influenced by entrance or exit effects. For  $z = 10$  mm, the same trends are seen as at the other heights, but the maximum void fraction and velocity reached are much lower than at higher points in the bed; this is likely due to small bubbles forming and coalescing at this height before fully-formed bubbles persist higher in the bed.

### ***Comparison with computational and analytical models***

In order to shed light on the accuracy of computational and analytical models, predictions from these models were compared with MRI measurements. Fig. 8 shows time-averaged maps of void fraction and vertical velocities of both particles and gas measured using MRI at a height  $z = 50$  mm above the gas distributor at the base of the bed. The superficial velocity of the gas was

0.104 m/s. In Fig. 8 (A), a central region, approximately 20 mm in diameter, can be seen with a void fraction significantly higher than that outside the dotted lines. The void fraction distribution seen in Fig 8 (A) is indicative of a stream of bubbles passing successively through the central region of the bed, as demonstrated in Figs. 4-6. Beyond a radius of 10 mm, the void fraction is  $\sim 0.51$ , equal to the void fraction at minimum fluidization. Thus, few bubbles, if any, pass through the outer region of the bed. For ease of reference, the regions inside and outside the dotted lines of Fig. 8 (A) are referred to here as the “bubbling region” and the “emulsion region”, respectively. Figures 8 (B) and (C) show that particle and gas velocities are significantly higher in the bubbling region than in the emulsion region, consistent with classical theory [6]. The reasoning for the cutoff line being at  $r = 10$  mm and the sensitivity of results to this selection are discussed in Appendix A.

In a fluidized bed reactor, the gas velocities in the bubble and emulsion phases determine the contacting of gaseous reactants with reacting solids [6]. Classical theory postulates that for bubbling fluidization, the gas velocity relative to the particles [44] and void fraction in the emulsion phase are both equal to those at minimum fluidization,  $(U_{mf}/\varepsilon_{mf})$  and  $(\varepsilon_{mf})$ , respectively [9]. Thus, the gas velocity in the emulsion phase,  $(u_{z,e})$  is given by:

$$u_{z,e} = U_{mf}/\varepsilon_{mf} + v_{z,e} \quad (8)$$

where  $v_{z,e}$  is the vertical component of the average particle velocity in the emulsion phase. However, there has been significant debate over the correct division of gas flow between bubbles and interstitial flow [45–47]. Table 10 indicates that classical theory is in excellent agreement with MRI measurements of average void fraction and gas velocity in the emulsion phase for this particular system.

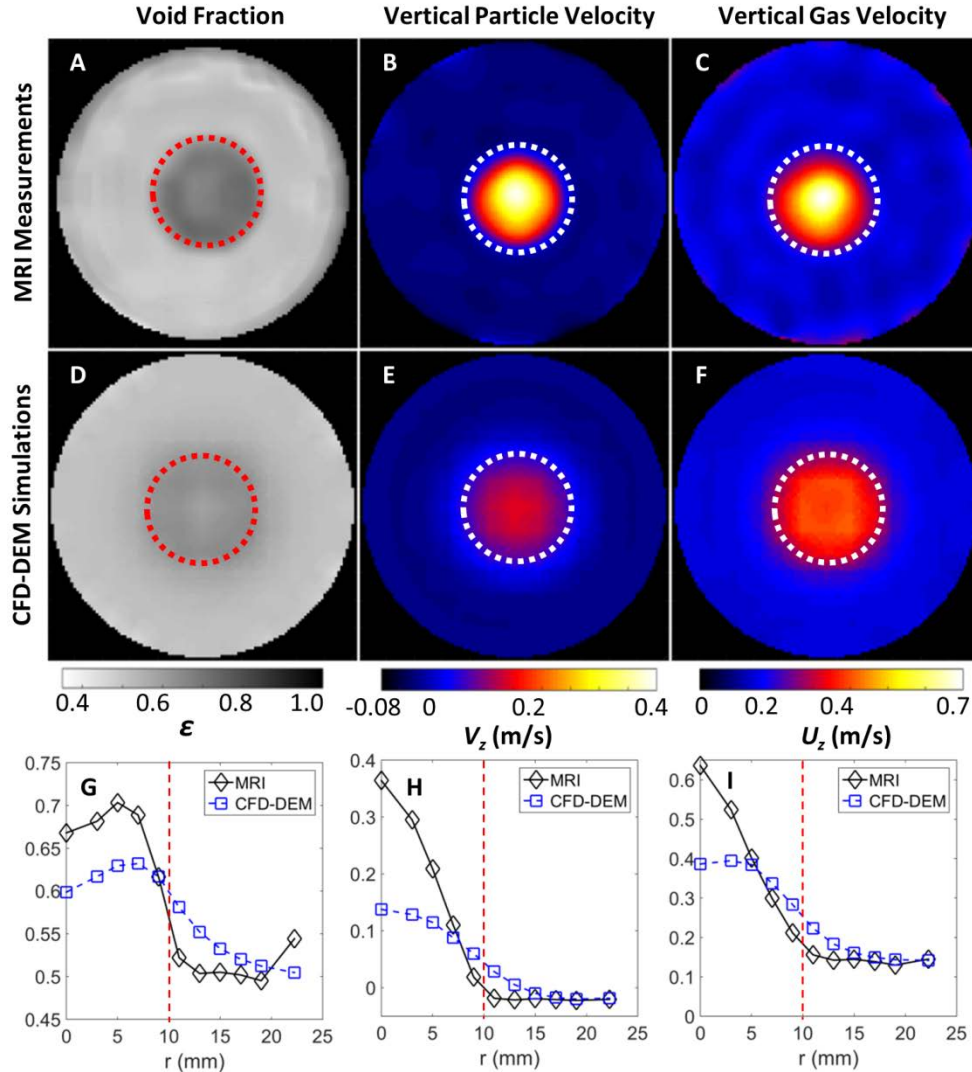
The design of fluidized beds for new applications is facilitated by the use of computational models, which require experimental validation [12]. To date such studies have been restricted to experimental measurements of particle motion and void fraction [48,49]; however, the greatest uncertainty in some of these models has been attributed to the interaction of the gas and solids [50]. Figs. 8 (D-F) show predictions from computational fluid dynamics – discrete element method (CFD-DEM) simulations [51] of time-averaged hydrodynamics in the bubbling bed for direct comparison with MRI measurements in Figs. 8 (A-C). CFD-DEM simulates the motion of each individual particle, according to Newtonian and contact mechanics,

while simulating gas motion on a CFD grid and coupling the phases using a drag law. These simulations are at too small a scale to be used in the design of industrial reactors directly; however, they form a key part of the multi-scale simulation methodology that is required to develop simulations of industrial scale processes [10,42]. Here, effective particle diameters were used in calculations of drag and void fraction in the simulations, in order to model the non-sphericity of the poppy seeds. The maps produced from CFD-DEM simulations in Figs. 8 (D-F) show patterns consistent with MRI results, shown in Figs. 8 (A-C). Fig. 8 (G-I) shows that the simulations capture the features of the experimental data, but produce lower values for gas void fraction and velocity in the centre of the bed. Table 10 shows that predictions from the simulation for the emulsion and bubbling regions match the experimental results very closely when averaging over the regions, with the largest difference being in the particle velocity in the bubbling region. The agreement between the MRI measurements and CFD-DEM predictions indicates that non-sphericity can be adequately modelled by incorporating effective particle diameters to match the values of  $U_{mf}$  and  $\varepsilon_{mf}$  seen experimentally for non-spherical particles.

Additional MRI measurements were conducted to obtain the full probability distribution function of vertical gas velocities, as shown in Fig. 9. Interstitial velocities ranging from approximately 0 m/s to 0.4 m/s are seen in the emulsion region, with a distribution close to Gaussian (Fig. 9 (A)). The particle Reynolds number ( $Re = \rho U d_p / \mu$ ) is  $\sim 400$  for this system, indicating flow in the transitional regime to turbulent flow. Higher gas velocities, ranging from approximately 0 to 1.0 m/s, were measured in the bubbling region with a distribution skewed slightly towards lower velocities (Fig. 9 (B)). Fig. 9 (A) shows that the measured distribution in the emulsion region (labelled Emulsion MRI) is nearly identical to that measured at minimum fluidization (labelled Minimum MRI), but is shifted to lower gas velocities by about 0.02 m/s to account for the average downward motion of the particulate phase as noted above. Two-phase theory postulates that the mean gas velocity through the emulsion phase is similar to that at minimum fluidization [9]; our measurements reveal a stronger result, namely, the full velocity distribution is very similar.

The distributions predicted by CFD-DEM simulations (Fig. 9) are similar in shape and modal velocity to the MRI results, but the standard deviation of the distribution measured experimentally in the emulsion region is 2.2 times greater than that given by the simulations. We attribute this difference in width to the fact that MRI measurements capture the full distribution

of velocities, accounting for each gas molecule, while CFD-DEM is inherently limited to predicting only the average gas velocity in fluid cells larger than the particle diameter. In practice, a no-slip boundary condition must exist between the gas and the surface of each particle, necessitating appreciable gas velocity variations in every void space between particles; neither this nor turbulence is accounted for in CFD-DEM simulations.



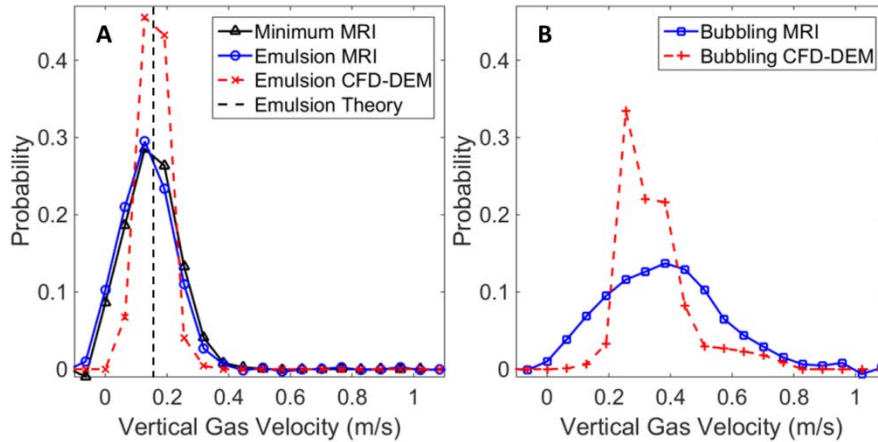
**Fig. 8** (A) Diagram of bubbling fluidization conditions and horizontal slice (between the green lines) taken through the bed for measurements in (A-F) at a height  $z = 50$  mm above the distributor. (A-F) Comparison of cross-sectional maps of time-averaged void fraction (first column), vertical particle velocity (second column) and vertical gas velocity (third column) for MRI measurements (A-C) and CFD-DEM simulations (D-F). Third row (G-I): line plots for void fraction, particle and gas velocities *versus* radial position. Bubbling region: inside dotted lines in (A-F), to the left of vertical dotted line (G-I); emulsion region: outside dotted lines (A-F), right of dotted lines (G-I). Field-of-view: 53 mm ( $x$ ) by 53 mm ( $y$ ); slice thickness: 4 mm ( $z$ ), pixel size: 0.47 mm ( $x$ ) by 0.47 mm ( $y$ ).

The velocity distribution affects inter-phase species and energy transfer, and thus capturing the distribution accurately is necessary for accurate modelling of many reactors.

Models are available to describe distributions of velocities arising from free fluid turbulence at a sub-grid scale [18], but these are unlikely to be applicable here as the variations in velocity are induced by flow around the particles and the particle concentration is very high. Analytical and computational models, similar to turbulence models but accounting for the influence of many particles on flow, need to be developed to account for the effects of these particle-scale distributions of velocities on transport and ultimately on chemical reactions.

**Table 10** Average values of void fraction and velocities from MRI maps in Fig. 2 (B-D), CFD-DEM maps in Fig. 2 (E-G) and as predicted by two-phase theory [9,44].

Region of bed	Avg. void fraction ( $\varepsilon_{avg}$ )	Avg. particle velocity (m/s)	Avg. gas velocity (m/s)
Emulsion region (MRI)	0.51±0.02	-0.021±0.004	0.147±0.004
Emulsion region (CFD-DEM)	0.52	-0.01	0.15
Emulsion Region (two-phase theory)	0.51±0.02	-	0.155±0.006
Bubbling region (MRI)	0.66±0.02	0.130±0.004	0.340±0.004
Bubbling region (CFD-DEM)	0.63	0.10	0.35



**Fig 9.** Probability distribution functions of vertical gas velocity in (A) the emulsion region and (B) the bubbling region (regions shown in Fig. 8). MRI measurements were compared with CFD-DEM predictions. In (A), comparison is also given with MRI measurement of velocity distribution across the entire cross-section at minimum fluidization, and the vertical dashed line gives the prediction of analytical theory (Eq. 8) [9,44] for gas velocity in the emulsion region.

## Conclusions

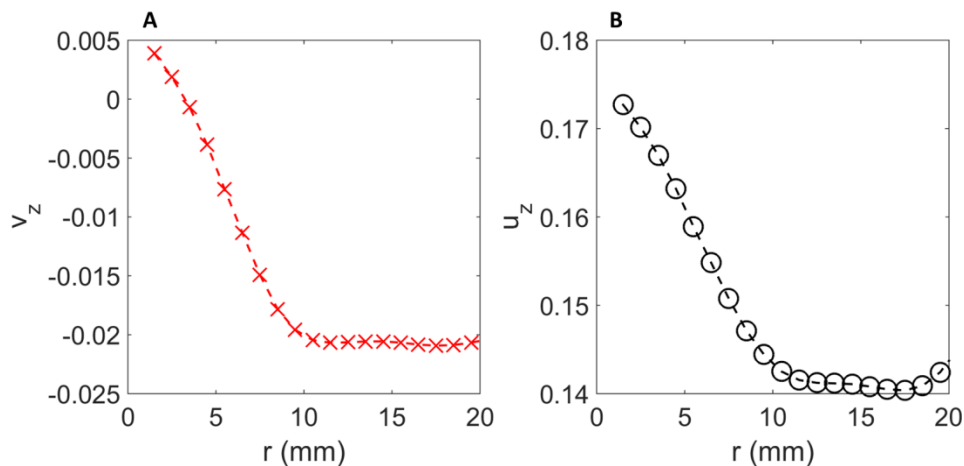
In this paper, MRI measurements are introduced to shed light on coupled gas-solid flow, using a bubbling fluidized bed as an example. Quantitative measurements of the gas and particle velocity are presented, as well as measurements of the local void fraction within the bed.



Measurements show that the mean velocity is consistent with classical analytical theory, but that a wide distribution of velocities exists. These techniques will be useful to probe flows in more complex and inadequately characterised systems, such as fluidized and moving beds involving a third liquid phase, interparticle forces, rapid phase changes or temperature gradients from exothermic reactions.

### Appendix A. Dividing point between emulsion and bubbling regions

As shown in Fig. 8, the lines dividing the bubbling and emulsion regions were drawn at a value  $r = 10$  mm. These lines were drawn based on a point of a large gradient in the void fraction, very close to where the void fraction becomes essentially constant with increasing radial position for the experimental data. This can be seen in Fig. 8 (H). Additionally, the particle and gas velocities also reached a near constant value with increasing radius at the dividing line between the bubbling and emulsion regions. The same dividing lines were used for the experimental and computational model data. For the experimental data, the results were more sensitive to the dividing line than for the computational data because there was a more sharp division between the bubbling and emulsion regions, based on gradient in void fraction, for the experimental data. Fig. A1 shows the sensitivity of particle velocity and gas velocity in the emulsion region as a function of the dividing line. If the radius of the bubbling region were significantly smaller than 10 mm, a different value would be recorded; however, if the value were increased a nearly identical value would be recorded, indicating that a radius of 10 mm is the point at which the emulsion region starts.



**Fig. A1.** Particle velocity (A) and gas velocity (B) in the emulsion region for the experimental data as a function of radius used for the cutoff between the bubbling and emulsion regions.

## **Acknowledgments**

CMB acknowledges financial support from the Gates Cambridge Trust and Syncrude Canada Ltd. CMB acknowledges Meenal Pore, Christine Schmaus, Nicholas Ramskill and Mick Mantle for help with experimental setup.

## Notation

### Latin Characters

<i>CFD-DEM</i>	Computational Fluid Dynamics – Discrete Element Method
$D_{bed}$	bed diameter
$d_p$	particle diameter
<i>FoF</i>	Field of flow
<i>FoV</i>	Field of view
<i>FWHM</i>	Full-width-half-maximum
$g_{flow}$	flow encoding gradient
$G_{slice}$	Slice gradient
$H_0$	Tapped bed height
<i>MR</i>	Magnetic Resonance
<i>MRI</i>	Magnetic Resonance Imaging
$N_{avg}$	Number of averages
$N_{pixels}$	Number of pixels
$N_{vel}$	Number of velocity bins in a distribution
<i>NMR</i>	Nuclear Magnetic Resonance
Re	Reynolds Number
r.f.	radiofrequency
<i>S</i>	Signal
$S_{fluidized}$	Signal under fluidized conditions
$S_i$	Signal in a bin from a velocity distribution
$S_{packed}$	Signal in a packed bed
<i>SPI</i>	Single point imaging
$T_1$	Spin-lattice relaxation time
$T_2$	Spin-spin relaxation time
$T_2^*$	Apparent transverse relaxation time
$T_R$	Recycle time
<i>U</i>	Superficial velocity
$U_{mb}$	Minimum bubbling velocity
$U_{mf}$	Minimum fluidization velocity
$u_z$	Local vertical component of gas velocity
$u_{z,avg,map}$	Average vertical component of gas velocity from velocity map
$u_{z,avg,distribution}$	Average vertical component of gas velocity from velocity distribution
$u_{z,i}$	Vertical component of gas velocity in a bin for a distribution
$u_{z,e}$	Average vertical component of gas velocity through the emulsion phase
$u_{z,expected}$	Expected average vertical component of gas velocity
$u_{z,mf}$	Average vertical component of gas velocity at minimum fluidization
$V_{packed}$	Volume of seeds and void regions in a packed bed of seeds
$V_{seeds}$	Volume of seeds
$v_z$	Vertical component of particle velocity
$v_{z,e}$	Average vertical component of particle velocity in the emulsion phase
<i>x</i>	horizontal component (1)
<i>y</i>	horizontal component (2)
<i>z</i>	vertical position above distributor

## Greek Characters

$\Delta$	observation time
$\delta$	flow encoding period
$\varepsilon$	void fraction
$\varepsilon_{fluidized}$	void fraction under fluidized conditions
$\varepsilon_{mf}$	void fraction at minimum fluidization
$\varepsilon_{mf}$	void fraction in a packed bed
$\mu$	gas viscosity
$\phi$	solids volume fraction
$\phi_{fluidized}$	solids volume fraction under fluidized conditions
$\phi_{packed}$	solids volume fraction in packed bed
$\rho$	gas density
$\tau$	echo time

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