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# Data Dependent Energy Modeling for Worst Case Energy Consumption Analysis

James Pallister, Steve Kerrison, Jeremy Morse, Kerstin Eder Department of Computer Science, University of Bristol, BS8 1UB, UK firstname.lastname@bristol.ac.uk

# ABSTRACT

Safely meeting Worst Case Energy Consumption (WCEC) criteria requires accurate energy modeling of software. We investigate the impact of instruction operand values upon energy consumption in cacheless embedded processors. Existing instruction-level energy models typically use measurements from random input data, providing estimates unsuitable for safe WCEC analysis.

We examine probabilistic energy distributions of instructions and propose a model for composing instruction sequences using distributions, enabling WCEC analysis on program basic blocks. The worst case is predicted with statistical analysis. Further, we verify that the energy of embedded benchmarks can be characterised as a distribution, and compare our proposed technique with other methods of estimating energy consumption.

# **1** INTRODUCTION

In real-time embedded systems, execution time of a program must be bounded. This can provide guarantees that tasks will meet hard deadlines and the system will function without failure. Recently, efforts have been made to give upper bounds on program energy consumption to determine if a task will complete within an available energy budget [7, 8, 12, 17, 29]. Motivating this research is the developing Internet of Things (IoT) market, where pervasive deeply embedded devices require battery- or harvester-based energy sources. Inaccurate energy consumption estimates can lead to expensive maintenance, or task failure if power thresholds are exceeded.

However, existing WCEC analyses often use energy models that do not explicitly consider the dynamic power drawn by switching of data in instruction operands, instead producing an upper bound using averaged random or scaled instruction models [7, 8, 12, 17, 29]. A safe and tightly bound model for WCEC analysis must be close to the hardware's actual behaviour, but also give guarantees that it never under-estimates. Current models have not been analysed in this context to provide sufficient confidence, and power figures from manufacturer datasheets are not sufficiently detailed to provide tight bounds.

Energy modeling allows the energy consumption of software to be estimated without taking physical measurements. Models may assign an energy value to each instruction [13, 27], to a predefined set of processor modes [20], or use a detailed approach that considers wider processor state, such as the data for each instruction [26]. Although measurements are typically more accurate, models require no hardware instrumentation, are more versatile and can



Figure 1: Power map of mul instruction for the AVR processor; total range is 15 % of SoC power.

be used in many situations, such as statically predicting energy consumption [7, 8, 12, 16, 17, 29], which significantly reduces the costs and barriers to entry of energy estimation.

Changes in energy consumption caused by different data can have a significant impact on the overall energy consumption of a program. Previous work on a 32-bit processor [13] used in this paper has reported up to 20 % difference in energy consumption due to data values, while other processors may have up to 50 % of energy caused by data switching [1]. In our own experiments we find 15 % difference in a simple 8-bit AVR processor. This device has no caches, no OS and no high power peripherals. This difference can be seen in Figure 1, which shows the power for a single cycle, 8-bit multiply instruction in this processor.<sup>1</sup> The diagram was constructed by taking hardware measurements for every possible combination of eight bit inputs. In this paper we choose to focus on the contribution of operand data to WCEC as it has not been studied in detail, whereas program length and execution path analysis is the subject of much prior work. We wish to create energy models that can account for all sources of energy, including data dependent sources.

Accounting for data dependent effects in an energy model is a challenging task, which we split into two parts. Firstly, the energy effect of an instruction's manipulation of processor state needs to be modeled. This is an infeasible amount of data to exhaustively

<sup>&</sup>lt;sup>1</sup>All measurements in this paper are taken on physical hardware.

collect. A 32-bit three-operand instruction has  $2^{96}$  possible data value combinations.

Secondly, a technique is required to derive the energy consumption for a sequence of instructions from such a model. The composition of data dependent instruction energy models is a particularly difficult task. The data causing maximum energy consumption for one instruction may minimise the cost in a subsequent, dependent instruction. Finding the greatest cost for such sequences requires searching for inputs that maximise a property after an arbitrary computation, which is again an infeasibly large task [18]. Overapproximating by summing the worst possible data dependent energy consumption of each instruction in a sequence, regardless of whether such a computation can occur, would lead to a significant overestimation of the upper bound.

We analyse individual instructions and explore probabilistic modeling approaches to determine the maximum energy consumption of instruction sequences. This provides a means to analyse complex programs at the block level. The analysis exposes how data correlations reduce maximum energy. A degenerate case is discovered, where the sequence of instructions results in a bimodal energy distribution.

We then explore the effect of data on the maximal energy consumption of programs, performing probabilistic analysis on the distributions of energy consumption obtained. Data's effect on entire programs is explored through several methods, finding that random data forms distributions from which a maximum energy can be estimated. To the best of our knowledge we believe that this is the first work to statically estimate energy variability due to operand data in programs, or to use probabilistic techniques to model data-dependent energy consumption.

This paper is organised as follows. The next section discusses related work. Section 3 models individual and sequences of instructions in the AVR, and Section 4 describes a sequence that causes a bimodal energy distribution. In Section 5 the effect of data on two full programs is explored for two processors. Section 6 discusses the implications of our work, while Section 7 concludes and gives an outlook on future work.

#### 2 RELATED WORK

Worst Case Execution Time (WCET) analysis attempts to find an upper bound on the time taken for an arbitrary program to execute [9, 30]. A key approach is a method called Implicit Path Enumeration Technique (IPET) [15], which estimates an upper bound given information about a program's control flow graph. Of recent interest has been work on Worst Case Energy Consumption (WCEC), utilising methods from WCET, combining them with energy modeling to bound program energy consumption [7, 12, 29]. In many of these studies, energy models are not tailored to the worst case, nor is the impact of data on energy consumption adequately reflected. This can lead to unsafe results if the analysis is to be relied on for guarantees of system behaviour within a given energy budget, as discussed extensively in [7], or bounds will be overly pessimistic if conservative over-approximations are used to ensure safety, as identified in [29].

A common form of model for embedded systems is an instruction level model. For example, Tiwari et al. [28] use an energy cost for each instruction and an energy cost for the circuit switching effect between each instruction, as well as an extra term to cover other external system effects.

Steinke et al. [26] construct a more detailed energy model that does consider the effects of data as well as the instructions. The Hamming distance between consecutive data values and their Hamming weights are considered with respect to both register and memory access. The technique achieves a 1.7 % average error, however every input must be known and every internal state calculated under the technique, an infeasibly large problem for reasoning about programs as a whole. Park et al. [22] consider how different operand values affect the energy consumption, using a range of values between 0x0000 and 0xFFFF to ensure that there is a large number of different Hamming distances between operands. Further studies have extensively used the Hamming weight to account for data energy [25]. The study notes that the Hamming distance and weight are particularly useful for subsequent values on busses in the processor, and less useful for combinatorial instructions, such as arithmetic.

Ascia et al. [1] build upon the approach, exploring how the data transitions from 0 to 1 and 1 to 0 can be given different energy costs. In a study of the Leon3 processor [23], taking data into account was found to reduce the model error when a 'typical' number of switching bits was factored in.

Kojima et al. [14] measure the data's effect on power of hardware units such as adder, multiplier and registers in a DSP. Register file power was found to show linear dependence on the Hamming weight of operands, while the adder shows moderate correlation with the Hamming distance between successive operands. However, the multiplier shows very little correlation with Hamming distance, except when one of the inputs is held constant. This supports the suggestion that combinatorial blocks require parameters other than the Hamming distance and weight [25]. Similar conclusions have been reached in studies which attempt to find the maximum power a circuit may trigger [19]. Many studies attempt to maximise the power consumption of a circuit, using a weighted maximum satisfiability approach [4] and genetic algorithms [10].

The reachability of a particular state has large implications for maximum energy consumption. Hsiao et al. [11] use a genetic algorithm (GA) to determine the maximum power per cycle in VLSI circuits. They show that the peak power for a single cycle is higher than the peak power over a series of cycles, as sequences of operations constrain the state transitions, making repeated worst cases unreachable. Therefore, for instructions, the data triggering highest energy consumption in one may preclude subsequent instructions from consuming their maximal energy.

GA techniques have also been used to estimate the WCEC of certain software components: Wägemann et al. [29] use GAs to search for the maximum amount of energy a single instruction can consume. Liqat et al. [16] apply GAs to program basic blocks, to search for the worst-case input of a sequence of instructions. Both require on-line testing of the hardware, and yield an energy value that is likely to be close to the WCEC for the instruction or block, however this cannot be guaranteed.

Probability theory has also been used to characterise how circuits dissipate power. Burch et al. [2] take a Monte Carlo approach,



Figure 2: Distribution of energy (mJ) for 1s1.

simulating the power of different input patterns to a circuit. The paper hypothesises that the distribution of powers can frequently be approximated by a normal distribution, as a consequence of the central limit theorem [6]. While the central portions of the probability distribution fit well to a normal distribution, the tails diverge, implying that a different distribution would be a better fit when maximum power is of interest. Studies have used extreme value theory to rectify this issue. The extreme value distribution is of importance when the maximum of a series of random variables is needed. It has been used in maximum power estimation of VLSI circuits [5], giving a probabilistic estimate of maximum power with a small number of simulations. Further, the WCET community have used extreme value techniques to probabilistically bound program execution times [3].

In summary, energy consumption and data dependency have been considered at the VLSI level using a variety of techniques. However, there has been little exploration of data dependency at the instruction or application level for worst case energy consumption analysis. The study of data dependency is fundamental in establishing both tighter WCEC upper bounds as well as providing greater confidence in the safety of those bounds. To support program level analysis, our challenge is to associate energy consumption costs with software constructs, rather than hardware blocks.

#### **3 INSTRUCTION MODELING**

#### 3.1 Individual instructions

While characterising energy consumption of the entire state space of an instruction is infeasible, requiring all combinations of all inputs to be tested, we can statistically characterise an instruction's energy consumption for a representative input sample. We use the AVR platform for our initial experiments due to its simplicity, repeatedly running code sequences that load random values (uniformly distributed) into registers and then executing an instruction using those registers. An example of the resulting distribution of energy values can be seen in Figure 2.

We fit the Weibull distribution to the random data energy distribution, under the hypothesis that the switching and hence power dissipation caused by random data will be close to the maximum. The distribution can then be examined to estimate an upper bound. The Weibull cumulative distribution function is a stretched exponential, allowing it to characterise many distributions with a high density followed by a long tail. This matches our hypothesis of most random-data power dissipation being close to the maximum, followed by a tail of less-than-maximum samples. Figure 2 shows



Figure 3: Comparison of predicted energy for the combination of a com and a lsl instruction with a simplistic model.

the regular Weibull distribution and an extreme value fit, the reversed Weibull distribution. The latter fits best, however it operates on the premise that there is a finite cut-off point (furthest right) beyond which there are no samples, which we cannot guarantee. This could lead to underestimation of an upper bound, compromising safety, and so we proceed with the regular Weibull distribution. The Weibull cumulative probability distribution (CDF) is given by:

$$F(x;k,\mu,\sigma) = 1 - e^{-\left(\frac{x-\mu}{\sigma}\right)^k}.$$
(1)

where

- *x* is the random variable,
- *k* is the shape parameter, defining the extent to which the distribution is stretched,
- μ is the location parameter, defining the shift of the distribution,
- $\sigma$  is the scale parameter, defining the size of the distribution.

Using the distribution calculated, and the total size of the input data space,<sup>2</sup> an estimate of the maximum possible average power can be calculated,

$$(1 - \mathrm{CDF}(x)) \cdot S = 1, \tag{2}$$

where CDF(x) is the cumulative density function of the probability distribution, and *S* is the total size of the data space. Intuitively, this is equivalent to finding the value of the percentile representing the highest power dataset in the entire data space.

#### 3.2 Composing instructions

To statistically characterise programs, our model must support modeling sequences of instructions. The natural unit of such sequences is a *basic block*, a sequence with a unique entry point and ending with a branch instruction. A simplistic method to generate basic block energy distribution would be to measure each block in isolation with random input data. However, even for small programs this is significant work that increases prohibitively with program size.

A more tractable approach is to take the energy model for each instruction in a basic block and compose these models. This only requires each individual instruction to be characterised, after which any size basic block can have its model deduced.

<sup>&</sup>lt;sup>2</sup> i.e., the finite set of all inputs an instruction may operate upon

By convolving the individual distributions of instructions together, a prediction of multiple instructions can be constructed. Figure 3 shows the distributions for the instructions com (bitwise complement) and lsl (logical shift left). The dashed curve shows the expected distribution. The two curves marked in green and orange show the actual distributions of the energy for each instruction — one for com, then lsl, and the second for lsl, then com. These distributions are not similar, and more importantly are higher than the prediction, resulting in an underestimate of the worst case energy consumption.

The difference in distributions stems from the surrounding instructions — to evaluate the instructions, the sequence is prefixed with a mov instruction to set up the values going into com and lsl. This suggests that the actual switching of data between the instructions can have a significant impact on not only the average energy, but the shape of the distribution too.

#### 3.3 Instruction transitions

In light of the inaccuracy of single instruction models, we use a model based on Tiwari et al. [27], using transition distributions to represent the data dependent transition between instructions. We assume that the energy consumption can be characterised using only transitions and no instruction base costs. To calculate the program energy  $E_p$ , formally,

$$E_{p} = \sum_{(i,j)\in TRACE_{p}} E_{i,j}, \text{ where } E_{i,j} \sim \text{Weibull distribution.}$$
(3)

With  $TRACE_p$  the sequence of instruction pairs  $ISA \times ISA$  that make up the execution of the program p, ISA the set of all instructions, and  $E_{i,j}$  being the energy distribution of switching from instruction i to j.  $E_p$  can be calculated by convolving the individual probability distributions,

$$f_p(x) = \bigotimes_{(i,j)\in TRACE_p} f(x; k_{i,j}, \mu_{i,j}, \sigma_{i,j}).$$
(4)

where  $\mu$ ,  $\sigma$  and k are the parameters for the Weibull probability density function of each transition, f. The symbol  $\bigotimes$  is the convolution operator, and  $f_p$  is the probability density function of the instruction sequence. The convolution of two Weibull probability density functions is not known to have an analytical solution, so it is solved numerically for the purposes of this study: we project the distributions onto histograms and then directly convolve the distributions, at the expense of some sampling error.

#### 3.4 Data collection

The collection of transition distributions for each pair of instructions is particularly challenging. The most simplistic approach is to repeat a pair of instructions with specified data and measure the energy, e.g.

However, after the first repetition r0 and r3 will not exhibit the same switching as they did in the first iteration — the value in the register will not change. Therefore, register values should be randomised before and after the execution of the instructions,

1	mov	r0,	х		- r
2	mov	r3,	Y		
3	add	r0,	r1,	r2	$= \frac{E}{E}mov, add$
4	sub	r3,	r4,	r5	$\Box E_{add,sub}$
5					_ <i>∟ <sup>L</sup>sub</i> ,

where *X* and *Y* are unique registers containing independent, uniform random variables. In addition to *X* and *Y*, registers r1, r2, r4 and r5 are initialised to random variables. This ensures all variables that could affect the transition distribution between two instructions are random and should lead to each transition distribution conforming to the Weibull distribution. The above test forms the  $E_{x,y}$  distributions seen to the right of the instructions. This approach introduces additional mov instructions to the test. These are convolved with the distribution that is of interest, so they must first be found in order to then be eliminated.

A large number of values can then be assigned to all variables in the sequence, s, and the energy,  $E_s$  measured for each. For example, this can form the following equation that must be solved to find  $E_{add,sub}$ ,

$$E_s = E_{mov,mov} \otimes E_{mov,add} \otimes E_{add,sub} \otimes E_{sub,mov}.$$
 (5)

To solve, we first find the distribution for  $E_{mov,mov}$ , then the distributions for  $E_{mov,i}$ , where *i* is another instruction. For simplicity it is assumed that  $E_{i,j} \equiv E_{j,i}$ . The  $E_{mov,mov}$  distribution can be found by finding the distribution for a repeating sequence of four movs, alternating between two destination registers and each using a unique source register containing an independent uniform random variable. The resulting distribution is  $E_{mov,mov}$  convolved with itself four times. This, along with similarly formed tests to find  $E_{mov,i}$  and  $E_{mov,j}$  yields the transition distribution for any  $E_{i,j}$ .

Currently, we have used this approach to obtain transition distributions for a subset of the AVR's instruction set. For each instruction pairing we used 256 random number assignments for single operand instructions and 1024 for two operand instructions. For each assignment of random numbers, we ran an unrolled loop of the code sequence 65536 times and took the average energy consumption across this period. Each such measurement takes on average one second, and each instruction pairing takes between five and twenty minutes to be characterised.

#### 3.5 Instruction sequence tests

Using the previously described method, Figure 4 shows the predicted distributions for three short instruction sequences as dashed lines. In all cases the prediction is conservative, with the mean of the distribution overestimated. This makes it useful in a worst case energy model, since the 99<sup>th</sup> percentile can be taken as a probabilistic estimation of maximum energy, for example. While we test only arithmetic instructions, we expect that loads, stores and branches can also be characterised in the same way.

The figure also demonstrates the case where values in the registers are not randomly distributed (dashed lines with points). Instead, they are dependent on the results of previous instructions. All of these distributions have a smaller mean, where the correlation between registers causes lower overall energy and so the upper bound holds, as one would expect.

The tests in this section only showed arithmetic instructions. However, the distributions for load and store instructions are similar



Figure 4: Energy distributions of three sequences.



Figure 5: Histogram showing energy distribution for a sequence of multiplies.

and can be composed similarly. It is expected that branch instructions will be simple to characterise — while there are often no direct inputs to a conditional branch, the state of the control flags influences the direction of the branch. Characterising the whole instruction set of a machine would mean testing each pairing of instructions. This would require a significant number of experiments for large machines, but is potentially feasible.

### 4 DATA DEPENDENCY

The previous section suggests that effects of computation may impact the location of the distribution. This section presents a case where this occurs in certain sequences of multiplication. Consider a sequence of mul and mov instructions calculating  $a^{13} \cdot b^8$ , where r20 = *a* and r21 = *b*:

1	mov r3,	r20;	mov r4,	r21;	
2	mul r3,	r4;	mov r2,	r0; 🗌	
3	mul r2,	r3;	mov r4,	r0;	Repeat 2 times
4	mul r4,	r2;	mov r3,	r0;	

Note that on AVR, mul implicitly writes to r0.

The sequence was measured for its energy under different inputs to produce the histogram in Figure 5. The distribution has two large peaks, labelled with two modes. In this particular example, the lower energy peak is caused by the computation collapsing to a zero value that persists throughout the sequence. The upper mode is caused by neither of the inputs to any of the multiplies being zero, which occurs for every multiply when both inputs are odd.

While this type of behaviour will affect the tightness of the energy's upper bound, it does not affect its safety, since it is the upper mode that is captured by the prediction. Additionally we believe this circumstance, where integer values overflow register sizes, is rare in real-world code as most programming languages (particularly C) treat integer overflow as undefined (i.e. erroneous) behaviour.

### 5 ANALYSING WHOLE PROGRAMS

We wish to validate that our modeling technique can be applied to whole programs and that it works on more platforms than just the Atmel AVR. However, the cost of modeling all the instructions that appear in a full program is large. Therefore, we measure the energy distribution of full embedded software programs on different processors to determine whether it can be characterised by the Weibull distribution. If so, and similar results are seen on different processors, then our composition technique should be capable of modeling the behaviour of a full program.

Additionally, we seek to verify that the probabilistic upper bound of a program distribution is sound, by using hand-crafted data to try and exercise a range of data switching behaviours in the processor, and existing GA techniques to search for inputs with high energy consumption (in the manner of Wägemann [29] and Liqat [16]).

To demonstrate that this technique (i.e. energy distribution) is not specific to the Atmel AVR, we test benchmarks on the XMOS XS1-L, a deeply embedded cacheless processor. Both the AVR and XS1-L are appropriate for IoT applications. The AVR has an 8-bit data-path, whereas XS1-L is 32 bits. The XS1-L is a single-core operating at 400 MHz with a four-stage hardware multi-threaded pipeline. Using single threaded benchmarks, the pipeline is only 25% utilised. However, the effects of data on these benchmarks is still measurable.



Figure 6: Power distributions (mW) for random datasets over full program benchmarks.



Figure 7: Distribution of benchmark average power (mW), when run with hand-crafted datasets.

#### 5.1 Benchmarks

For benchmarks, we select programs that have no data dependent branches, therefore changes in energy are purely due to different data progressing through the computational path in the processor. Programs that have data-dependent branches may execute different sequences of instructions, and may have different execution times, thus we exclude these to focus purely on changes in energy due to data values, not program flow. This matter is discussed further in Section 6.

The benchmarks used for this test are *fdct* and *matmult-int*, taken from BEEBS, an embedded benchmark suite [21]. These tests are purely integer, because the target processors in this work have no hardware floating-point support.

*fdct* has a state space of 1024 bits (one 8x8 block of 16 bit pixel data), while *matmult-int* performs a 20x20 matrix multiplication of 8 bit integers. Both cannot be explored exhaustively, and thus

would benefit from statistical characterisation. Neither of the chosen benchmarks have data dependent branches, thus their execution time is identical even with different input data.

#### 5.2 Random data

Figure 6 shows the average power when the *fdct* and *matmult-int* benchmarks use random data. The dashed line shows the Weibull distribution fitted to these data. Overall, the distributions are narrow, indicating a low variation caused by the data. The variations for both benchmarks on AVR are similar, however, each has a different mean, since different instructions are executed, each with a different average power.

Fitting these parameters to the Weibull distribution for each of the benchmarks results in an estimation of the maximum achievable average power for each benchmark, as in Section 3. For example the probabilistic maximums for AVR are 20.64 mW for *fdct* and 21.20 mW for *matmult*. These bounds are shown by the solid vertical lines in Figure 6.

#### 5.3 Genetic algorithm

Related work shows that genetic algorithms (GAs) are an effective technique to find the maximum power dissipation for circuits and software. Our paper instantiates a GA that attempts to find a dataset which increases the energy or power for the entire program.

The results are included in Figure 6 as dotted vertical lines. These data points are slightly higher and lower than the points found by the random data — the guidance provided by the GA allows both higher and lower solutions to be found quickly. Since the parameters to the Weibull distribution were found for each distribution, the probability of finding a more extreme solution can be calculated. For our test cases, the probabilities are less than  $10^{-9}$ , provided the assumption of the distribution being a good fit holds. However, the size of the data input space is so large that there are many possible states which may trigger a larger energy consumption.

#### 5.4 Hand-crafted data

Due to the extremely large number of input states, certain configurations of input are never considered by random search or the GA. This includes data such as every bit set and every bit cleared, which could be important and trigger an unusually high or low energy consumption. We hand crafted certain inputs to exercise these edge cases, to evaluate whether the GA or probabilistic bounds could be exceeded. The types of hand-crafted data fed into each benchmark are:

**All bits zero.** All of the bits in the data values are set to zero. **All bits one.** All of the bits in the data values are set to one.

- **Strided ones.** The data element is set to one at various strides, such as every 2, 4, 8 or 16 bytes.
- Strided rand. As above, with stride contents randomised.
- **Patterns.** Patterns known to cause high energy consumption. E.g. 0xa..a and 0x5..5 in multiplication [13].

Sparse. Only one element set to one in various positions.

**Restricted bit-width.** Setting random *n*-bit values in a *m*-bit offset region, as shown below:



**All elements the same.** Every element in the data is set to the same value. A range of values are tested.

Figure 7 shows the average power when all of these hand-crafted sets of data are measured on each benchmark. There are many different components of these graphs — each caused by a different part of the hand-crafted data. They are discussed below, starting with *matmult*.

- **A** This mode is around the lowest average power achievable for the *matmult* benchmark, all zero data or sparse data.
- **B** The distribution consists of sparse elements with few bits set to one. This causes low average power since at most single bits set to one are multiplied, with repeated zeros in-between.

- **C** There are a spread of points at this location, formed from tests with more dense data.
- **D** The highest consumption observed in the non-sparse tests is 21.04 mW for AVR, and is caused by data which has the same value in all the elements. The values of the elements for the top results are 247, 253, 181, 221 and 245 close to having all bits set. These are the only tests which significantly exceed the distribution obtained from random data. For the XS1-L, a larger proportion of tests dissipate a higher power, visible in the form of a third peak.

There are three modes of interest for *fdct*:

- **E** Three data points which are far lower than any other. These are all zero data and two instances of strided data, when the first in every 32 elements is one and all elements are zero. This is sparse data, however any of the other sparse data still triggers much higher power. This characteristic is observed on both architectures.
- **F** The majority of tests occur in this bracket, below the expectation given by random data. The AVR is an 8-bit processor, so 16-bit arithmetic can require two instructions, for upper and lower bits. Many of the hand-crafted data sets use zero or close to zero value data, resulting in the upper operation having lower power. This is not the case with the 32-bit XS1-L, which produces a single peak.
- **G** These tend to be triggered by higher-order bits set. With high valued data, the second (upper) part of the arithmetic operation has non-zero value, corresponding to a higher average power on AVR.

# 5.5 Analysis

Overall, there is a trend towards higher average power as data becomes more random or dense. The distribution predicted by random data is a good estimation of the upper bound. Several tests exceed the limits found with GAs, but all are bounded by the probabilistic highest value.

Comparing the characteristics observed on both processors, the distributions take similar forms for both *matmult* and *fdct*. The XS1-L dissipates more power, but is a more complex device with a higher operating frequency. However, the separation between the distributions A and B in *matmult* are within the same order of magnitude for both devices. Similarly, the widths of the features denoted F in *fdct* differs by a comparable amount. Overall, for AVR and XS1-L respectively, *matmult* is shown to have a power variation of 6.5 % and 2.2 %, with *fdct* showing 9.1 % and 6.0 %. These are within the error margins of many energy models, and are in fact likely to be a contributing factor to these errors. These variations, along with environmental factors that may influence device energy consumption, must be considered in order to establish upper energy bounds with adequate safety.

In summary, it appears that for both platforms tested, the energy distribution of a program can be characterised as a statistical distribution, and further that the probabilistic upper bound exceeds all tests tried. With full instruction models, our technique should be able to statically determine this distribution.

# 6 DISCUSSION

Our technique allows for characterising and bounding the amount of energy consumption caused by variations in data operands in a program. A complete analysis requires a model for each instruction pairing for each platform, which, while costly, is a worthwhile trade-off for accurate offline energy estimation. In comparison with the technique of Steinke et al. [26], rather than characterising each instruction by its input and the current processor state, we instead produce a single probability distribution representing the likely costs of transitioning from one instruction to another, enabling composition.

However, the technique does not fully account for all energy consumption in a processor. A large cost in many processors is static leakage, the energy lost for every moment that the processor is active. Existing WCEC techniques [7, 12, 29] combine both (an approximation of) circuit switching costs with standard techniques to estimate worst case code paths, such as IPET [15]. To fully account for processor costs, our probabilistic technique would need to be combined in a similar fashion to find the greatest probabilistic upper bound on energy on all paths through a program. We have not yet explored this as we focus only on data dependent costs here.

Our technique also benefits from the predictable nature of processors suited for the IoT domain, i.e. those without caches, branch prediction or speculative execution, all of which have energy costs that heavily depend on program state. Were the technique to be applied to processors with such features, then probabilistic models would need developing for those features too, such as the work of Puranik et al. [24], although they focus on the mean execution time rather than either energy or upper bounds. The tightness of bounds achievable for such features remains an open question.

Finally our technique does not address external factors in energy consumption, such as system-level energy or variability due to environmental conditions. These full-system factors fall well outside the bounds of embedded software analysis.

## 7 CONCLUSION AND FUTURE WORK

This paper has analysed how data values within processors affect energy consumption. Basic blocks can be modeled by composing instruction models, and programs with complex control flow can be modeled by composing basic blocks. To create a composable analysis, the transition between instruction pairs was modeled as a Weibull distribution. Distributions for instruction pairs can then be convolved to give a probability distribution of energy for an instruction sequence.

Several instruction sequences were tested, comparing the predictions to the actual measured distributions to validate our model. The prediction is tight, but overestimates the energy consumption in all cases, providing an estimate of the likely worst case energy consumption. The prediction assumes that all of the instructions are independent of each other, which is not generally true. Repeating the measurements with dependent variables in an instruction sequence shows that added correlation between the values decreases the total energy consumption. The prediction (ignoring dependencies) still provides an upper bound as expected in this case, but it is not as tight. The correlation between data values input and output from instructions can lead to unusual energy behaviour. An instruction sequence was shown to produce bimodal energy behaviour across a range of random data, caused by repeatedly biasing data values towards zero. In such a case of strong correlation between data values, our model will over-predict.

Initial analysis of full programs suggests that using random data to create a Weibull distribution allows a probabilistic worst case for that program to be estimated. This worst case was higher than could be found using a GA, random or hand-crafted data, giving us confidence that our estimates are safe.

More generally, this work has shown that worst case energy analysis requires more than simply a model generated from profiling with random input data. The distribution of profiling results must be analysed to determine a likely maximum. Physical system properties such as energy consumption are inherently noisy, and cannot be as tightly or reliably bound as execution time. However, we demonstrate empirically that taking a high-order percentile of a Weibull distribution, fit to random input data, provides a basis for pragmatic WCEC modeling. We also show that the distributions of energy for instruction transitions, rather than individual instructions, are necessary when creating a composable model.

A next step towards more accurate static techniques for WCEC estimation would be to model the entire instruction set using the energy modelling technique presented in this paper, and to combine such a cost model with a worst-case analysis technique such as IPET, creating a technique that considers both length and data effects on program energy probabilistically. Following existing WCEC techniques, this should yield a more accurate upper bound through consideration of additional energy contributors.

A further observation is that programs have differing degrees of data dependency — some instructions in the program are purely control, and do not operate on the data input to the program. Static analysis could find only the instructions that are in the data path of the program, and an estimate of the total variability due to data could be constructed from these instructions and their transition distributions.

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