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# Journal of Structural Engineering

## Modelling and parametric study of the re-anchorage of ruptured tendons in bonded post-tensioned concrete --Manuscript Draft--

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<b>Abstract:</b>	<p>The contribution of ruptured tendons to the residual strength of bonded post-tensioned concrete structures is currently assessed based on pre-tensioned concrete bond models. However, this approach is inaccurate due to the inherent differences between pre-tensioned and post-tensioned concrete. In this paper, a non-linear 3D finite element model is developed for the re-anchoring of a ruptured tendon in post-tensioned concrete. The model is validated using full-field displacement measurement from 33 post-tensioned concrete prisms and previous experimental data on beams from the literature. The influence of different parameters was investigated, including tendon properties (i.e. diameter, roughness), duct properties (i.e. diameter, thickness, material), initial prestress, concrete strength, grout strength, grout voids, stirrups, and strands, on the tendon re-anchorage. The most influential parameters are found to be tendon and duct properties.</p>
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<b>Suggested Reviewers:</b>	<p>Dario Coronelli , PhD Associate professor, Politecnico di Milano dario.coronelli@polimi.it His work is reference in this paper. The work presented in this paper fall on his research interest.</p> <p>Ha Minh, PhD Assistant Professor, Saitama University minh@mtr.civil.saitama-u.ac.jp Also can be approached: haminh99@gmail.com ==== His related work is referenced in this paper. More over the damage due to corrosion on post-tensioned concrete is one of his research interest</p> <p>Antony Jeyasehar, PhD Professor , Annamalai University auhse@sify.com also at: chellam.ajs@gmail.com ==== His work is referenced in this paper</p>
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# 1 **Modelling and parametric study of the re-anchorage of ruptured tendons**

## 2 **in bonded post-tensioned concrete**

3 A. O. Abdelatif<sup>1</sup>, J. S. Owen<sup>2</sup> and M. F. M. Hussein<sup>3</sup>

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### 4 **Abstract**

5 The contribution of ruptured tendons to the residual strength of bonded post-tensioned  
6 concrete structures is currently assessed based on pre-tensioned concrete bond models.  
7 However, this approach is inaccurate due to the inherent differences between pre-tensioned  
8 and post-tensioned concrete. In this paper, a non-linear 3D finite element model is developed  
9 for the re-anchoring of a ruptured tendon in post-tensioned concrete. The model is validated  
10 using full-field displacement measurement from 33 post-tensioned concrete prisms and  
11 previous experimental data on beams from the literature. The influence of different  
12 parameters was investigated, including tendon properties (i.e. diameter, roughness), duct  
13 properties (i.e. diameter, thickness, material), initial prestress, concrete strength, grout  
14 strength, grout voids, stirrups, and strands, on the tendon re-anchorage. The most influential  
15 parameters are found to be tendon and duct properties.

### 16 **Keywords**

17 Post-tensioned concrete; Re-anchorage; Corrosion; Tendon; Bond, Modelling; Finite element;  
18 Rupture; ESPI

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## 19 **1. Introduction**

20 Bonded post-tensioned concrete had been considered as a durable form of construction  
21 because of the multi-layered protection for the prestressing steel. However, many post-  
22 tensioned concrete bridges have been reported to have suffered ruptured tendons due to  
23 corrosion, which led to total structural collapse in some extreme cases (Concrete Society,  
24 2002, Highways Agency et al., 1999, NCHRP, 1998). Previous investigations showed that a  
25 ruptured tendon is able to re-anchor into the surrounding grout, which is mainly designed as a  
26 corrosion protection, and, as a result, contributes to the residual structural capacity of the  
27 structure (Highways Agency, 1995, Buchner and Lindsell, 1987b). While much effort has  
28 been devoted to developing corrosion detection techniques, little attention has been given to  
29 assessing the structural capacity of bonded post-tensioned concrete structures with ruptured  
30 tendons.

31 Approaches to the structural assessment of damaged post-tensioned bridges often utilise pre-  
32 tensioned models or empirical bond slip relations to approximate the re-anchorage length  
33 (Highways Agency et al., 1999, Cavell and Waldron, 2001, Coronelli et al., 2009). In some  
34 cases, the re-anchorage of tendons is completely ignored (Jeyasehar and Sumangala, 2006,  
35 Zeng et al., 2010, Watanabe et al., 2011). However, this is not appropriate. Wrong estimation  
36 of the re-anchoring phenomenon for a ruptured tendon can result in inaccurate predictions of  
37 the residual structural capacity. Accurate prediction enhances the process of decision making  
38 and helps in decreasing the maintenance cost. Equally important, it minimises disruption and  
39 avoids unnecessary replacement or strengthening work. Therefore, this paper aims to develop  
40 a 3D non-linear finite element (FE) model to simulate the re-anchorage phenomenon of the  
41 ruptured tendon in bonded post-tensioned concrete. The model will then be used in a  
42 parametric study to investigate the influence of different parameters. This will help improve

43 the understanding of the behaviour of bonded post-tensioned concrete structures with  
44 ruptured tendons and facilitate the prediction of their residual structural capacity.

45 This paper presents the background of bond in post-tensioned concrete in Section 2. Section 3  
46 presents a 3D non-linear FE model for the re-anchorage of a ruptured tendon. Section 4  
47 shows the experimental procedure used in the validation of model, which is used to validate  
48 the numerical model in Section 5. Section 6 presents a parametric study, which was  
49 performed using the developed FE model. Conclusions are summarised in Section 7.

## 50 **2. Bond in grouted post-tensioned concrete**

51 Bond between steel and grout is attributed to adhesion between steel and grout, friction  
52 between steel and grout, and the mechanical resistance. The adhesion always has an  
53 insignificant influence on the load-deformation response of the structure, because the  
54 adhesion fails after a very small relative slip (Marti et al., 2008, Cairns et al., 2007). The  
55 mechanical resistance only contributes to bond when deformed steel bars are used. However,  
56 when smooth strands are used, a strand slips through the grout following the pre-shaped  
57 groves without shearing off the concrete (fib, 2000, Abdelatif et al., 2015). Therefore, the  
58 friction between steel and grout is largely responsible for the transfer of stress into the  
59 surrounding material. In the following paragraphs, the literature on bond in grouted post-  
60 tensioned concrete is chronologically presented.

61 In 1960s, experiments on 19 beams were conducted to investigate the effect of grout  
62 properties on the re-anchorage length, indicated as “transmission length”, and the structural  
63 behaviour of bonded post-tensioned concrete beams (Geddes and Soroka, 1963, Geddes and  
64 Soroka, 1964). The investigations showed that the “transmission length” is independent of  
65 time, but depends on the compressive strength of the grout.

66 In controlled demolition tests in the eighties, important results about structures suffering from  
67 rupture of tendons were revealed (Buchner and Lindsell, 1987b, Buchner and Lindsell, 1988).  
68 These results were: 1) the ruptured tendon is able to re-anchor into surrounding material over  
69 a certain length known as the *re-anchorage length*; 2) the re-anchorage depends on the grout  
70 condition, friction between individual wires or strand within a tendon, and the level of  
71 confinement provided by shear links.

72 The Model code 1990 (MC90) introduced a model for bond in post-tensioned concrete. It is  
73 based on bond between concrete and the outer surface of tendon sheathing (CEB-FIP MC90,  
74 1990). In reality, however, the bond actually develops between pre-stressing steel and grout  
75 rather than between pre-stressing steel and concrete. This model for bond in post-tensioned  
76 concrete was removed in the latest version of the model code MC2010, (fib, 2010).

77 The UK Highways Agency, in DMRB BA51/95, has proposed a conservative empirical  
78 relationship to estimate the re-anchorage length of a ruptured bonded post-tensioning tendon  
79 (Highways Agency, 1995). It modified the BS5400 transfer length model (BS 5400, 1990) for  
80 *pre-tensioned* concrete to account for multi-strand tendons. The model assumes linear  
81 distribution of tendon stresses over the re-anchorage length.

82 In 2001, FE and experimental investigations were conducted to study the dynamic bond  
83 characteristics of smooth pre-stressing bars that are embedded in grout (Belhadj and Bahai,  
84 2001). The study demonstrated the importance of friction in controlling the slip of pre-  
85 stressing steel in grout. In another study in 2008, the influence of emulsifiable oil, which is  
86 used as a temporary corrosion protection, in bond behaviour in bonded post-tensioned  
87 concrete was investigated. The results showed a reduction on bond shear stress for treated  
88 strands compared to untreated ones (Marti et al., 2008, Luthi et al., 2008).

89 An empirical relation was proposed in 2011 to calculate the re-anchorage length, which is  
 90 referred to as “the size of the stress-decreasing region”, based on experiments on nine beams  
 91 subjected to tendon cutting (Watanabe et al., 2011). The proposed relation assumed constant  
 92 bond stress over the re-anchorage length, which gives a linear stress distribution. This  
 93 assumption contradicts with the findings of other experimental observations (Geddes and  
 94 Soroka, 1964, Coronelli et al., 2009).

95 Most of the reviewed literature that addresses the bond of post-tensioned tendons aims to  
 96 study the impact of certain parameters on the bond mechanism rather than developing a  
 97 model for the re-anchorage of the tendon. Therefore, in 2012, the authors developed an  
 98 analytical model based on the linear thick-wall cylinder theory and the Coulomb friction law  
 99 to estimate the stress distribution in the tendon after the rupture and hence the re-anchorage  
 100 length (Abdelatif et al., 2012), Eq. (1).

$$x = \frac{r_s}{2\alpha\phi} \left[ \left( \frac{1}{B} + \frac{\mu_s}{E_s} \frac{1}{B^2} \right) \ln \left( 1 + \frac{B}{A} f_s \right) - \left( \frac{1-\mu_s}{E_s} + \frac{\mu_s}{BE_s} \right) f_s \right] \quad (1)$$

101 Here  $f_s$  is tendon stress at distance  $x$  from the rupture point,  $\alpha$  is a factor to account for voids in  
 102 the grout,  $\mu_s$  and  $E_s$  are the Poisson’s ratio and the Young’s modulus of steel.  $A$  and  $B$  are  
 103 coefficients depending on geometry and material properties of steel, concrete, grout and duct  
 104 that can be calculated as shown in (Abdelatif et al., 2012). Eq. (1) estimates the re-anchorage  
 105 length when the stress in the pre-stressing steel ( $f_s$ ) is substituted by the effective pre-stress ( $f_{se}$ ).

106 The model has been verified using an axisymmetric FE model and validated experimentally  
 107 (Abdelatif et al., 2013). The results of axisymmetric and analytical model show that the stress  
 108 on the grout might exceed the tensile strength. Therefore, non-linear material behaviour  
 109 should be considered.

### 110 **3. 3D non-linear FE modelling of the re-anchorage of ruptured tendons**

111 In this paper, an FE package ABAQUS (Dassault Systemes Simulia, 2010) is used to model  
112 post-tensioned concrete members with a single wire. The modelling of the post-tensioned  
113 concrete components (i.e. concrete, grout, steel and duct), simulation of post-tensioning,  
114 tendon rupture, and the solution algorithms are discussed in this section. All post-tensioned  
115 concrete components are modelled using 8-node isoparametric elements with reduced  
116 integration points to minimise the cost of computation. The reduced integration method  
117 improves the computational efficiency without losing the accuracy of the results (Koh and  
118 Kikuchi, 1987).

#### 119 **3.1 Modelling concrete, grout, tendon and duct elements**

##### 120 **3.1.1 Concrete**

121 The magnitude of the radial stresses (compression) in concrete is always less than the  
122 magnitude of the circumferential stresses (tension) as shown in Eq. (2), based on thick-wall  
123 cylinder theory (Timoshenko et al., 1974).

$$\sigma_r = \sigma_\theta - r \frac{\partial \sigma_r}{\partial r} \quad (2)$$

124 This suggests that the compressive radial stress ( $\sigma_r$ ) will be less than the magnitude of  
125 concrete tensile strength ( $\sigma_\theta$ ). Therefore, the behaviour of concrete in compression was  
126 modelled as linear-elastic.

127 In tension, the behaviour of concrete is modelled as linear-elastic up to its tensile strength ( $f_t$ )  
128 which is taken here as a tenth of the concrete compressive strength. The post-cracking was  
129 modelled using the Concrete damage plasticity (CDP) model in ABAQUS (Dassault  
130 Systemes Simulia, 2010) with Hillerborg's fracture energy cracking concept (Hillerborg et

131 al., 1976) and assuming linear tension softening. More details about the CDP parameters used  
132 are discussed elsewhere (Abdelatif et al., 2015).

### 133 **3.1.2 Grout**

134 The grout material was modelled in a similar way as the concrete elements. According to  
135 EN447, a water cement ratio  $w/c$  of 0.4 is recommended for grout in prestressing tendons.  
136 For this  $w/c$ , the values of fracture energy,  $G_f$ , were found to be in the range of 22-26 N/mm  
137 (Padevčt and Zobal, 2011). In this study the averaged value of 24 N/mm was used.

### 138 **3.1.3 Prestressing steel, duct, and anchor plates**

139 Post-tensioning tendons are usually stressed to a level below the yield stress. Therefore,  
140 tendon, steel duct, and anchor plates are modelled using linear elastic material model  
141 adopting the idealised stress-strain constitutive model in both tension and compression (CEB-  
142 FIP MC90, 1990). In this study, the Young's modulus for steel material was assumed to be  
143 200 GPa.

144 As noted in section 2, friction is the principal means of transferring stress from the tendon  
145 into the surrounding material for both smooth strands and wires. Therefore only the frictional  
146 component was considered in modelling bond in this work. The pressure in the frictional  
147 component is generated by the radial expansion of the tendon after rupture as a result of the  
148 Poisson effect, Abdelatif et al., 2015. In this work, only tendons made from a single wire are  
149 considered to avoid the meshing problems that would occur for a helical strand. For a given  
150 change in pre-stress the Poisson effect will give the same change in diameter for both strand  
151 and wire. However, for the strand there is an additional effect that resulting from the  
152 mechanical interlocking of the wires making up the strand. Therefore, modelling the tendon  
153 as a wire will provide a lower bound on the bond and hence a conservative estimate of the re-  
154 anchorage length.

### 155 **3.2 Simulation of post-tensioning process**

156 To simulate the interface between steel-grout, grout-duct, and duct-concrete surface-to-  
157 surface contact elements were used. The tangential behaviour between steel and grout was  
158 modelled using Coulomb friction law with zero cohesion and 0.4 coefficient of friction  
159 (Abdelatif et al., 2012, Abdelatif et al., 2015, fib, 2000). Note that the type of corrosion  
160 usually found in post tensioned structures is the pitting corrosion, which is localised and  
161 occurs in grout voids due to the presence of chlorides and moisture. Therefore, in this study,  
162 the coefficient of friction between steel and concrete close to the tendon fracture was  
163 assumed to be unchanged by corrosion. Other contact interfaces (i.e. grout-duct, duct-  
164 concrete and end anchors-concrete) were considered to be fully bonded.

165 The slip between two paired nodes at contacted interfaces is considered to take place when  
166 the tangential friction exceed the static friction and the relative tangential displacement  
167 exceeds the specified tolerance. In ABAQUS by default, the tolerance set to 0.5% of the  
168 average length of all contact elements in the model (Dassault Systemes Simulia, 2010).

169 The normal and tangential contact behaviours were solved using an augmented Lagrange  
170 multiplier algorithm and Penalty method, respectively.

171 The model consists of three main solution steps: prestressing, grouting, and rupture.

172 1) The prestressing was modelled by applying an initial stress equivalent to the  
173 magnitude of prestress on steel elements. The model was then solved in this first step  
174 to allow transfer of prestress from steel to concrete through the end anchorage. In this  
175 step, the grout elements, contact between post-tensioning steel and grout, and contact  
176 between grout and duct are deactivated (no stress on grout in this step).

177 2) The grouting process was then simulated in the second solution step by activating the  
178 grout elements and grout's contact elements with steel and the duct. Note that the

179 grout element remain un-stressed throughout this step. This is because the contact  
180 elements can be established between any two paired of nodes if they are within the  
181 predefined tolerance without displacing the nodes.

182 3) In the third step the tendon rupture was simulated. The rupture of post-tensioning steel  
183 was modelled by deactivation steel elements at the location of the rupture, and then  
184 the model is solved for equilibrium. This simplification is supported by the fact that  
185 the corrosion causing rupture is localised and occurs in the form of pitting. With more  
186 localisation and high rate of corrosion, the pitting mechanism may produce points of  
187 stress concentration. Eventually this may lead to a sudden brittle failure after a  
188 negligible loss of material.

189 The model was solved utilising a full Newton-Raphson solver under the static condition, with  
190 un-symmetric matrix storage to handle the contact solution. A small time step size, and  
191 therefore, a large number of increments were used to promote the convergence of the  
192 complex non-linear material behaviour and the solution of the contact problem.

### 193 **3.3 Mesh sensitivity**

194 The mesh sensitivity study was conducted for a bonded post-tensioned concrete prism (Fig.  
195 1) in order to find an optimum spatial discretization. The study shows that, 32 segments  
196 around the tendons and 10 mm element size in the longitudinal direction satisfied the mesh  
197 sensitivity investigations, Fig. 2. The influence on the model result for elements smaller than  
198 this was found to be insignificant (Fig. 3).

## 199 **4. Experimental work**

200 A number of laboratory investigations have previously been carried out to study the bond  
201 behaviour between grout and the post-tensioning tendons, as well as the quality performance  
202 of the grout (Marti et al., 2008, Minh et al., 2007, Minh et al., 2008). However, only limited



203 experiments were conducted to understand the re-anchoring phenomenon of ruptured  
204 tendons.

205 In this section, a brief review of previous tests about measuring techniques, rupture  
206 simulation, and the size of test specimen will be given.

207 In previous studies on monitoring strain changes after tendon rupture/release on post-  
208 tensioned concrete, two types of strain gauges were used: the demountable  
209 mechanical (DEMEC) and the electrical gauges. The DEMEC strain gauges were used to  
210 investigate the effect of grout properties on transmission length on nineteen bonded post-  
211 tensioned concrete beams (Geddes and Soroka, 1964). The electrical strain gauges were  
212 usually attached on the concrete surface to (Schupack and Johnston, 1974, Buchner and  
213 Lindsell, 1987a, Buchner and Lindsell, 1988) or attached to the pre-stressing steel (Coronelli  
214 et al., 2009, Watanabe et al., 2011). However, the tendon slippage after the rupture might  
215 break the attached electrical strain gauges (Coronelli et al., 2009).

216 Because the simulation of the corrosion process is time demanding (Jeyasehar and  
217 Sumangala, 2006), the corrosion rupture was simulated by releasing the prestress force at the  
218 location of rupture. This can be done either by using nuts to simulate the rupture at the end  
219 (Geddes and Soroka, 1964) or by cutting the tendon through a prefabricated hole using a  
220 flame torch (Schupack and Johnston, 1974) or saw (Coronelli et al., 2009, Watanabe et al.,  
221 2011).

222 Different sizes of specimens were used in previous experimental investigations. Experiments  
223 were conducted on real bridge girders (Buchner and Lindsell, 1987a, Buchner and Lindsell,  
224 1988), laboratory beams with large cross section (Schupack and Johnston, 1974) and long  
225 spans (~10 m) (Tanaka Y. et al., 2001), and on 3-5 metre beams (Coronelli et al., 2009,  
226 Geddes and Soroka, 1964, Watanabe et al., 2011).

227 The drawbacks of the previous experiments on the behaviour of the ruptured tendon can be  
228 summarized in three points:

- 229 • The use of electrical resistance strain gauges or DEMEC gauges restricts the number of  
230 the measuring points based on the specimen length. This will influence the prediction  
231 of strain profile along the tendon
- 232 • Simulating tendon rupture by saw cutting might disturb and damage the grout.
- 233 • Conducting experiments on large beams or in a real bridge beams restricts the number  
234 of parameters to be varied for practical and cost issues.

235 These drawbacks can be resolved by measuring the full-field displacement (instead of strain  
236 gauges) after the rupture on small prisms (instead of beams).

237 In this study, the 3D Electronic Speckle Pattern Interferometry (ESPI) system was utilised to  
238 measure the full field displacement on 500 mm long post-tensioned concrete prisms. ESPI  
239 has proven to be a valuable alternative to conventional displacement measuring techniques  
240 (Jones and Wykes, 1989). It provides considerably more information, such as full-field  
241 measurement, compared to the conventional method. The rupture of the tendon was simulated  
242 by undoing nuts of a special type of anchor (instead of using saw cutting or accelerated  
243 corrosion), which was designed for the purpose of the tests (Fig. 1). Undoing nuts also gives  
244 a sufficient number of steps/images to be capture by the ESPI system throughout the test.

#### 245 **4.1 Test setup**

246 33 Concrete prisms of 500x100x100 mm with an embedded duct along the centre were cast  
247 and then post-tensioned using a single pre-stressing wire (Fig. 1). The wire was tensioned  
248 using a manual hydraulic prestressing jack. The prestressing load was controlled by means of  
249 a load cell and adjusted with a bespoke extended anchor system before grouting. The prisms  
250 were grouted vertically from the anchor side using a manual pointing gun.

251 As illustrated in Fig. 4, the post-tensioned concrete prism was then bolted down to a vibration  
252 isolation table and two rounded bars were inserted below the prism to minimize expected  
253 downward movement during the test (because of the sensitivity of the ESPI system to rigid  
254 body motion). Two different support setups were used in this test to investigate the influence  
255 of the support position on the tendon re-anchorage. In the first one, the prism was bolted  
256 down from the releasing end (live end), and in the second, the prism was fixed at the other  
257 end (dead end). This support boundary condition (bolting-down) was represented in the FE  
258 model by fixing the nodes at the bottom of the end-plate.

259 The rupture of the tendon at the end of the prism (i.e. anchor) was simulated by gradually  
260 releasing the nuts between the extended anchorage plates (Fig. 1) in many steps. A load cell  
261 was used to monitor the level of prestress during releasing steps and to record the tendon  
262 force before and after the test to eliminate the prestress losses. The full-field displacement at  
263 the concrete surface after prestress release was measured using ESPI, Fig. 4.

264 One of the intrinsic limitations to be avoided in ESPI measurements is the rigid body motion  
265 (RBM). The presence of rigid body motion (i.e. movement of the sample) locates the speckle  
266 pattern fringes away from the surface of the tested object (Jones and Wykes, 1989).

267 Therefore, fringes can become unrelated to the surface displacement. This is a major  
268 disadvantage of the ESPI system, which limits its application. The correction of such errors  
269 might be difficult or impossible to account for and it is important to minimise this error by a  
270 suitable design of the testing setup. In this study, two LVDTs were used to monitor the  
271 prisms' rigid body motion. One third of the prisms used in this study were excluded because  
272 of the presence of the rigid body motion.

## 273 **5. Model validation**

274 The validation was conducted by comparing the results from the FE model with full field  
275 displacement at the concrete surface of post-tensioned concrete prisms. Many parameters  
276 were varied to examine the 3D FE model, these include: tendon diameter, duct material,  
277 prestressing force, concrete strength, grout strength, reinforcement and support setup (Table  
278 1). To increase the range of validation, previous experimental results on beams were also  
279 used to validate the FE model. The FE model stress profile was also compared to that from  
280 the analytical model proposed by the authors, Equation (1).

### 281 **5.1 Model validation against ESPI data**

282 The full-field displacement that was obtained from the ESPI test was compared with the 3D  
283 non-linear FE model displacement contour map in the longitudinal direction (Fig. 5 and Fig.  
284 6). The comparison shows a reliable simulation of 3D non-linear model for re-anchoring  
285 behaviour.

286 From the contour maps, the displacement profile at the level of the tendon can be extracted  
287 for each prism (Fig. 7 and Fig. 8). In order to accommodate the numerical model (Abdelatif  
288 et al., 2012) in the comparison, all results are normalised to the maximum displacement.  
289 Based on the impact of the rigid body motion on the test results, the results for negligible  
290 rigid body motion ( $c \leq 3\mu\text{m}$ ) are given in Fig. 7 while those with small rigid motion ( $3\mu\text{m}$   
291  $\leq \text{RBM} \leq 10\mu\text{m}$ ), are presented in Fig. 8. All the results for specimens with excessive rigid  
292 body motion group ( $\text{RBM} \geq 10\mu\text{m}$ ) were excluded for the reasons discussed in Section 4.1.  
293 From observations, it was found that the prisms which were fixed from the far end (i.e. dead  
294 end) exhibit less rigid body motion compared with those which were fixed from the releasing  
295 end (i.e. live end).

296 Both of the analytical and 3D non-linear FE re-anchorage models show satisfactory  
297 prediction of the real behaviour (Fig. 5 to Fig. 8). In a few cases, the agreement at the end the  
298 prism is poor; this can be due to the fact that the intensity of the laser at the end is quite low.  
299 This reason limits the use of ESPI system with large specimens (Jones and Wykes, 1989).

## 300 **5.2 Model validation using data from previous tests on beams**

301 In addition to the experimental work done as a part of this study, data from previous  
302 experiments on post-tensioned concrete beams were used to validate the proposed model  
303 (Geddes and Soroka, 1964). The beams had dimensions of 5 inch (127 mm) width by 6 inch  
304 (152.5 mm) height and were post-tensioned using a single 7/8 inch (22.225 mm) post-  
305 tensioning bar which was enclosed by 45mm/49mm steel duct filled with grout. The re-  
306 anchorage length was estimated at 95% of the average maximum strain (95% AMS) method  
307 (Russell and Burns, 1993, Abdelatif et al., 2012).

308 Fig. 9 shows normalised strain profile of the experimental data, 3D non-linear FE model, linear  
309 theoretical model, and Highways Agency model (Highways Agency, 1995). All strain data  
310 were normalised to average maximum strain. Good agreement between the proposed models  
311 (FE and analytical) with the experimental data are observed. The re-anchorage length is over  
312 predicted as 29% and 5% of the experimental value using the analytical and 3D FE model,  
313 respectively. The 29% is because of non-linear material behaviour is ignored while the 5% is  
314 regarded as acceptable. It is worth mentioning that the FE model runs in about three hours  
315 compared the milliseconds for the analytical model. In contrast, the Highways Agency model  
316 (DMRB BA51/95) overestimated the re-anchorage length by 125% from the experimental  
317 value assuming a linear stress profile which is clearly contradicted with the experimental results.  
318 The DMRB The DMRB BA51/95 overestimation of the re-anchorage length (and thereby  
319 underestimation of the residual capacity) could lead in practice to increased maintenance cost,  
320 traffic disruption and unnecessary replacement or strengthening work (Abdelatif et al., 2016).

### 321 **5.3 Stress distribution across the concrete section**

322 The von Mises contour plot on the cross section at the end of post-tensioned concrete beam  
323 after tendon rupture is shown in Fig. 10. It was found that, the stress contours in concrete tend  
324 to take a circular shape around the tendon. This finding supports the assumption of the thick-  
325 wall cylinder theory, which was used in development of the analytical model in Equation (1)  
326 (Abdelatif et al., 2012) and are in line with previous findings (Abdelatif et al., 2015).

## 327 **6. Parametric study on factors affecting the tendon re-anchorage**

328 Using the 3D non-linear FE model, the influence of different parameters on the re-anchorage  
329 of the ruptured tendon can be assessed. In this parametric study, the influence of the diameter  
330 and surface roughness of post-tensioning steel, diameter, thickness and material of sheathing  
331 (i.e. duct), initial prestress, concrete strength, grout strength, voids in the grout, and shear  
332 links, on the re-anchorage of a ruptured tendon are investigated. Unless stated otherwise, the  
333 beam that was used in this study has the properties shown in Table 2. The cross section of the  
334 beam was chosen from previous literature, (Coronelli et al., 2009), while the length was  
335 chosen to just occupy the re-anchorage length (to minimize the computational cost).

336 Re-anchorage length normalised to the diameter of the post-tensioning steel ( $l_r/d$ ) and the  
337 effective prestress is normalised to the initial prestress ( $f_{se}/f_{si}$ ) were considered as reference  
338 values in this study.

339 Studying the large number of parameters in this study was not possible without the aid of  
340 high performance computing cluster using eight CPUs with 16 GB RAM at the HPC unit in  
341 the University of Nottingham. This greatly reduced the computational cost.

### 342 **6.1 Diameter of post-tensioning steel**

343 Fig. 11 shows the influence of the tendon size on the re-anchoring behaviour in the case of a  
344 constant ratio of 2.3 for duct to diameter of post-tensioning steel. The length required for  
345 tendons to re-anchor is directly proportional to the diameter (Fig. 11b). It is found that the  
346 tendons with a smaller diameter tend to re-anchor in a short length and hold more force in  
347 comparison to those with a larger diameter (Fig. 11b and Fig. 11c). Fig. 11a shows that, the  
348 slope of the stress profile, which is related to the bond stress, is also affected by the size of  
349 the tendon. Small tendons tend to produce higher bond stress than large tendons, Fig. 11a.

### 350 **6.2 Surface roughness**

351 In this parametric study, the coefficient of friction was varied from 0.3 to 0.7 to investigate  
352 the influence of the surface roughness on the re-anchorage phenomenon. It was found that  
353 tendon re-anchorage depends significantly on the surface condition of the prestressing steel at  
354 the time of rupture (Fig. 12). Fig. 12 shows that rough tendons need a shorter length to re-  
355 anchor compare to the smooth tendons. A similar conclusion was drawn in pre-tensioned  
356 concrete elements (Abdelatif et al., 2015).

### 357 **6.3 Initial prestress**

358 The investigation is conducted on a 3000 mm beam using 7 mm wire and 20 mm steel  
359 ducting with 1.9 mm thickness. In general, no significant influence of initial prestress on the  
360 re-anchorage phenomenon was observed (Fig. 13). The influences on the stress profile (Fig.  
361 13a) and the effective prestress (Fig. 13c) are negligible. The difference of 1000 MPa in the  
362 initial prestress, results only in less than 5d difference in the re-anchorage length (Fig. 13b).  
363 As the higher initial prestress always generates higher hoop stresses in concrete and grout  
364 (due to the higher exerted radial pressure at the interface), this suggests that the non-linear  
365 behaviour of the concrete and grout has insignificant influence on the tendon re-anchorage.

#### 366 **6.4 Concrete strength**

367 In most design codes, the concrete compressive strength is recommended to be more than 35  
368 MPa for prestressed concrete structures. However, in this study, concrete with 20-50 MPa  
369 compressive strength is used to observe the overall influence of concrete strength on the re-  
370 anchoring. Generally, concrete with strength within the practical range does not show a  
371 significant influence on the tendon re-anchorage behaviour (Fig. 14). The difference of the  
372 re-anchorage length through the tested range of concrete strength is less than 2d while the  
373 difference in the effective prestress is about 2%. This finding supports the assumptions made  
374 in Section 6.3 that, the non-linear behaviour of concrete has an insignificant influence on the  
375 re-anchorage of the ruptured tendon.

#### 376 **6.5 Grout strength**

377 In this investigation, neither the stress distribution nor the effective prestress show significant  
378 changes due to the change of the grout compressive strength (Fig. 15). However, the re-  
379 anchorage length shows less than 10d difference through the tested range (10-40 MPa), Fig.  
380 15b. In other words, each 5 MPa increase in the grout strength results in only 1.5d decrease in  
381 the re-anchorage length in this simulation. This finding is in agreement with previous  
382 experimental results (Geddes and Soroka, 1964, Watanabe et al., 2011) and observations  
383 during demolition of bridge girders (Buchner and Lindsell, 1987b). This could be due to the  
384 confinement introduced by the duct to the grout.

#### 385 **6.6 Presence of the grout voids within the re-anchorage length**

386 Presence of voids on the grout is known to affect the re-anchorage behaviour of ruptured  
387 tendons in addition to creating a corrosive environment (Cavell and Waldron, 2001). In this  
388 investigation, three sizes of voids are considered: 25%, 50% and 100% void across the grout  
389 section (Fig. 16). Voids of 200 mm length (15.75d) were introduced in the grout to  
390 investigate the impact of grout voids on the re-anchorage mechanism. These voids were



391 located to start at 100 mm far from the end of the prism. The results show that, the presence  
392 of grout voids within the re-anchorage zone makes a significant change in the prestress  
393 profile and results in much longer re-anchorage length, Fig. 17a and Fig. 17b. If the beam is  
394 long enough for the tendon to re-anchor, no significant drop will occur in the effective  
395 prestress, Fig. 17c. The re-anchorage length of the voided tendons was approximated in a  
396 previous study by adding the void's length to the non-voided re-anchorage length (Cavell and  
397 Waldron, 2001). However this study shows, the re-anchorage length is increased by 67%,  
398 114%, and 142% of the void's length for 25%, 50%, and 100% of void in the grout cross  
399 section, respectively.

#### 400 **6.7 Duct diameter (Grout thickness)**

401 An increase in the diameter of the duct increases the grout thickness. Thicker grout allows the  
402 tendon to deform in the longitudinal direction more than the thinner grout. Therefore, tendons  
403 with a large duct diameter (thicker grout layer) were found to have a longer re-anchorage  
404 zone, a higher prestress and less bond stress in comparison with tendons with smaller duct  
405 diameter (thinner grout layer), Fig. 18.

#### 406 **6.8 Duct thickness**

407 The practical range of duct thickness is 0.25 mm for steel ducts, 2.5-3.0 mm for  
408 polypropylene (PP) ducts, and 4.0-6.0 mm for high density polyethylene (HDPE) ducts  
409 (Hewson, 2003). A steel duct with outer diameter of 30 mm was used to examine the impact  
410 of ducting thickness on the re-anchorage behaviour. It is found that, increasing the duct  
411 thickness increases the level of confinement around the post-tensioning steel which results in  
412 a shorter re-anchorage length (Fig. 19). No significant influence is observed on the effective  
413 prestress (Fig. 19c).

## 414 **6.9 Duct material**

415 The ducts used in post-tensioned concrete are usually manufactured from steel,  
416 polypropylene (PP), and high density polyethylene (HDPE). These materials, in addition to  
417 polyvinyl chloride (PVC), which is used in this study, were considered to investigate the  
418 influence of ducting material on the re-anchoring phenomenon. The investigation considered  
419 a 6000 mm beam that was post-tensioned to 750 MPa and injected with grout of 40 MPa  
420 compressive strength. The Young's moduli were taken as 200 GPa, 3.0 GPa, 1.75 GPa, and  
421 0.8 GPa for steel, PVC, PP, and HDPE respectively. The parametric study shows that, the  
422 tendons with a duct of low Young's modulus show poor re-anchorage (i.e. long re-anchorage  
423 length, small effective prestress and low bond stress) as shown in Fig. 20. The tendons with  
424 steel ducting show good re-anchorage behaviour compared to those with PP and HDPE ducts  
425 and less longitudinal deformation.

## 426 **6.10 Shear reinforcement**

427 Fig. 21 shows the influence of shear reinforcement (stirrup) on the re-anchorage of the  
428 ruptured tendon. In this simulation, no significant influence of stirrups spacing on the re-  
429 anchorage of the ruptured tendon was observed. This contradicts the observation during the  
430 controlled demolition of grouted post-tensioned concrete structures (Buchner and Lindsell,  
431 1987b). This contradiction can be attributed to:

- 432 i) Experimental point of view: The observation of Buchner and Lindsell (1987b) were based  
433 on comparisons between beams of two different bridges with different properties, different  
434 number of strands in tendon and different level of prestress.
- 435 ii) Modelling point of view: Modelling the behaviour of confined concrete correctly needs to  
436 consider the influence of confinement on the following factors in the CDP model: a) yield  
437 criterion; b) hardening and softening rule c) flow rule. None of the existing CDP type  
438 models includes all the three factors (Yu et al., 2010). However, the model shows good

439 agreement compared to experimental results in this study of post-tensioned concrete  
440 prisms with shear reinforcement as shown in Fig. 8e.

## 441 **7. Conclusions**

442 The paper has presented 3D non-linear finite element model for re-anchorage of a ruptured  
443 tendon in bonded post-tensioned concrete structures. The model was compared to previous  
444 analytical models and validated using experimental data on prisms, utilising the 3D  
445 Electronic Speckle Pattern Interferometry system (ESPI). The proposed model was also  
446 validated against previous experiments on beams and compared with the Highways Agency  
447 DMRB BA51/95 re-anchorage model. The developed model was found to be able to predict  
448 the re-anchorage length compared to the Highways Agency model DMRB BA51/95 which  
449 greatly overestimates the re-anchorage length. The findings related to the tendon re-  
450 anchorage (modelling and experiments) are:

- 451 • The experiments confirmed the re-anchorage of the ruptured tendon
- 452 • The 3D finite element is able to capture the re-anchorage phenomenon
- 453 • The developed models and experiments support the hypothesis that the re-anchorage  
454 phenomenon is influenced by the confining materials

455 The 3D FE non-linear re-anchorage model was then used in a parametric study to investigate  
456 the influence of prestressing steel diameter and surface roughness, duct diameter and  
457 thickness, duct material, initial stress, concrete strength, grout strength, presence of voids in  
458 the grout, longitudinal reinforcement, shear links, and number of strands in the tendon on the  
459 re-anchoring behaviour of the ruptured tendon. The results of this parametric study is  
460 summarised as follows:

461 • The parameters that have a significant influence on the re-anchorage are tendon  
462 properties (i.e. diameter, roughness) and duct properties (i.e. diameter, thickness, and  
463 material)

464 • Tendons with larger diameter have a long re-anchorage length whereas those with  
465 thicker duct and those with smaller diameter have a shorter re-anchorage length

466 • Tendons with rough surfaces re-anchor better than those with smooth surfaces

467 • Tendons with steel ducts re-anchor much better compared to those with polypropylene  
468 (PP), and high density polyethylene (HDPE) ducts

469 The presence of voids in the grout around the ruptured tendons results in longer re-  
470 anchorage length depending on the size of the voids

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579 **Table 1: Test matrix showing variation of model parameters**

Test No.	Prism ID	Stress (MPa)	Bar Dia.	Duct Material	Duct OD/T (mm)*	Concrete			Grout			Steel		End Cond.	Remarks						
						E	$f_t$	$f_c$	E	$f_t$	$f_c$	E	$f_t$			$f_c$					
1	P1	1020	7	PVC	20/1.9	31.0	3.6	57.1	26.8	2.1	68.9	207	1562	Setup-1	Plain concrete						
	P2	1030																			
	P3	1021																			
2	P4	607.5	7	PVC	20/1.9	37.9	3.9	56.9	24.9	11.1	60.8	207	1562			Setup-1	Plain concrete				
	P5	755.7																			
	P6	815.7																			
3	C1	783	7	PVC	20/1.9	43.2	3.8	50.6	23.7	7.5	47	207	1562					Setup-1	Plain concrete		
	C2	880																			
	C3	807.3																			
4	G1	917.3	7	PVC	20/1.9	43.2	3.9	50.6	18.7	2.5	39	207	1562							Setup-1	Plain concrete
	G2	1032																			
	G3	-																			
5	CG1	866.5	7	PVC	20/1.9	43.4	3.6	46.1	19.2	9.5	31.7	207	1562	Setup-1	Plain concrete						
	CG2	980.7																			
	CG3	922.3																			
6	CC1	872	7	PVC	20/1.9	43.9	3.6	46.6	-	-	51.7	207	1562			Setup-1	Plain concrete				
	CC2	1090																			
	CC3	832.4																			
7	Dm1	900.4	7	Steel	19.05/1.59	44.0	4.0	49.0	8.53	12.7	53.7	207	1562					Setup-2	Reinforced concrete**		
	Dm2	837.3																			
	Dm3	800.6																			
8	C10	922	7	PVC	20/1.9	42.3	4.1	51.2	21	14.8	58.1	207	1562							Setup-2	Reinforced concrete**
	C20	1098																			
	C30	953																			
9	ST1	861.5	7	PVC	20/1.9	44.0	4.5	52.5	25.1	12.4	71.6	207	1562	Setup-2	Reinforced concrete**						
	ST2	970.7																			
	ST3	953.4																			
10	V1	1113	5	PVC	20/1.9	44.3	3.6	53.7	24.5	3.2	53.7	207	1562			Setup-2	Reinforced concrete**				
	V2	1062																			
	V3	1096																			
11	Gr1	801	7	PVC	20/1.9	44.6	2.7	46.8	13.2	3.8	15.2	207	1562					Setup-2	Reinforced concrete**		
	Gr2	983																			
	Gr3	866																			

\*OD/T: Outer diameter/wall thickness

\*\* Four 6 mm steel bars were used as main reinforcement with 6 mm stirrups every 50 mm

\*\*\*  $f_c, f_t, f_y$ : compression, tensile, yield strength in MPa. E: Young's modulus in GPa

580 **Table 2: Properties of the beam used in the parametric study**

Beam			Prestressing steel			Grout	Concrete	Steel Duct	
width (mm)	height (mm)	Length (mm)	Initial prestress (MPa)	Diameter (mm)	$E_s$ (GPa)	$f_{cg}$ (MPa)	$f_c$ (MPa)	Outer dia. (mm)	Thickness (mm)
150	200	1500	1250	12.7	2.07	20	50	25	2.5

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## Figures captions

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583 **Fig. 1: Geometry of the test specimens (dimensions are in mm)**

584 **Fig. 2: Typical mesh arrangement for the prism models**

585 **Fig. 3: results of mesh sensitivity study**

586 **Fig. 4 Test setup: post-tensioned concrete prism with the anchorage system and ESPI camera on**  
587 **vibration isolated table**

588 **Fig. 5: Prism G2 full field displacement: a) ESPI data; b) FE results ( $\mu m$ )**

589 **Fig. 6: Prism C10 full field displacement: a) ESPI data; b) FE results ( $\mu m$ )**

590 **Fig. 7: Deformation at concrete surface after release: a) Prism DM2; b) Prisms C10, C20 and C30; c)**  
591 **Prism V3**

592 **Fig. 8: Deformation at concrete surface after release: a) Prism P5; b) Prisms C2 and C2; c) Prism G2; d)**  
593 **Prism CG1 and CG2; e) Prism ST1; f) Prism V2**

594 **Fig. 9: Strain changes at concrete surface after the rupture at the level of the tendon**

595 **Fig. 10: von Mises contours on a concrete cross section within the re-anchorage zone (MPa)**

596 **Fig. 11: Influence of tendon's diameter on: (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
597 **prestress**

598 **Fig. 12: Influence of the tendon's surface roughness on: (a) Stress distribution; (b) Re-anchorage length;**  
599 **(c) Effective prestress**

600 **Fig. 13: Influence of the initial stress on: (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
601 **prestress**

602 **Fig. 14: Influence of the concrete compression strength on: (a) Stress distribution; (b) Re-anchorage**  
603 **length; (c) Effective prestress**

604 **Fig. 15: Influence of the grout compression strength on: (a) Stress distribution; (b) Re-anchorage length;**  
605 **(c) Effective prestress**

606 **Fig. 16: Size of the voids introduced in the grout**

607 **Fig. 17: Influence of grout voids on: (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
608 **prestress**

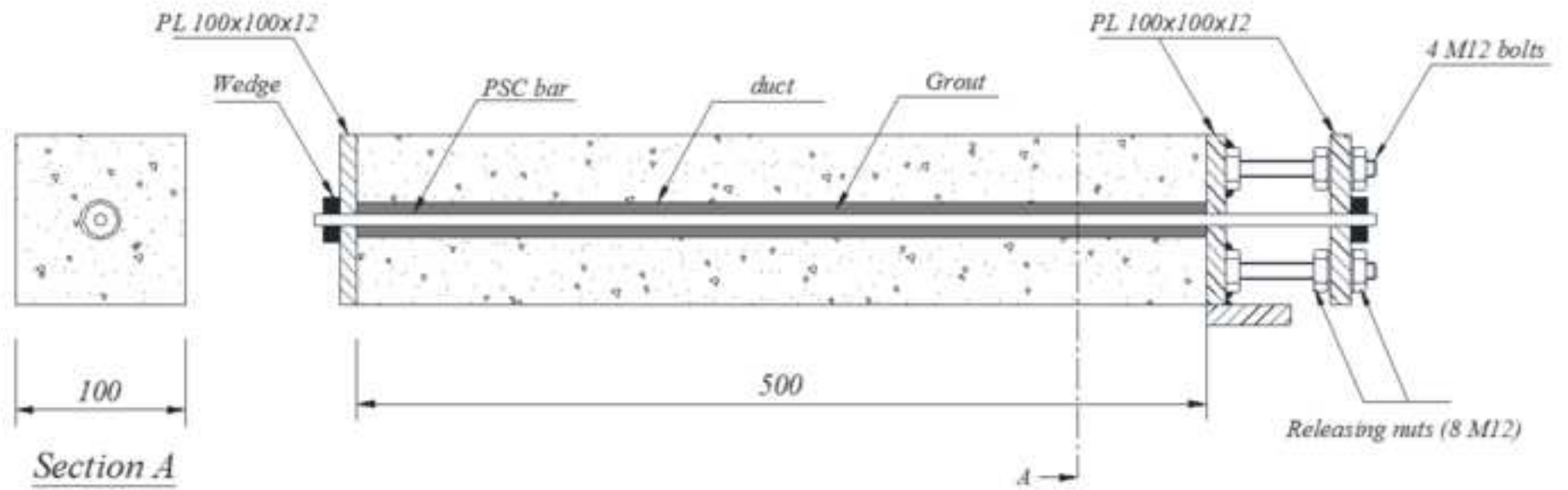
609 **Fig. 18: Influence of the duct diameter and grout thickness on: (a) Stress distribution; (b) Re-anchorage**  
610 **length; (c) Effective prestress**

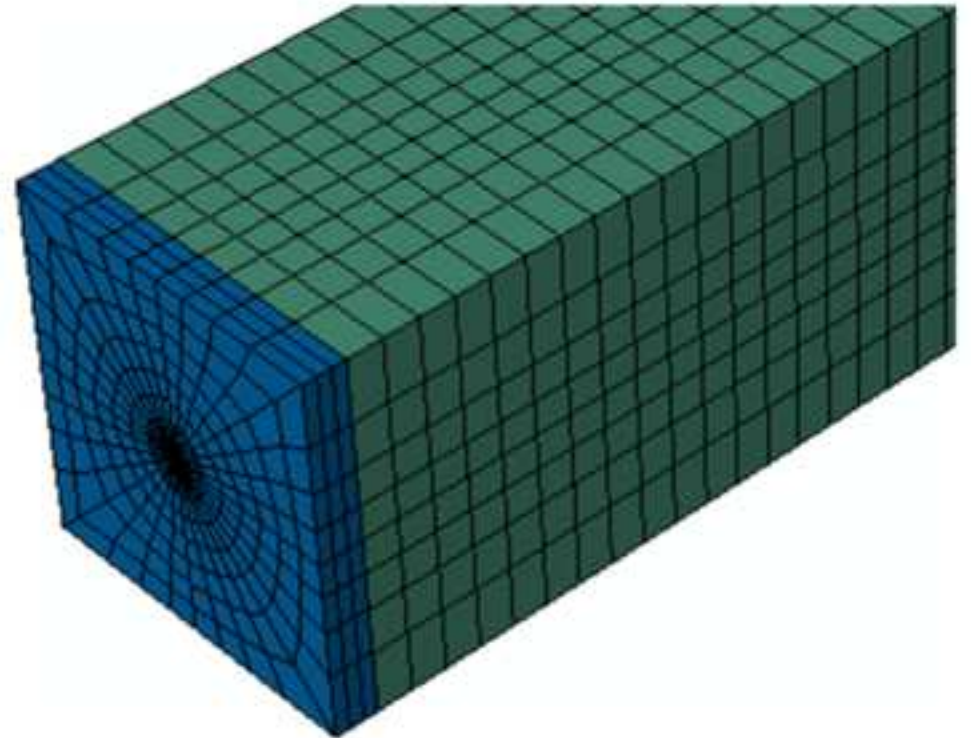
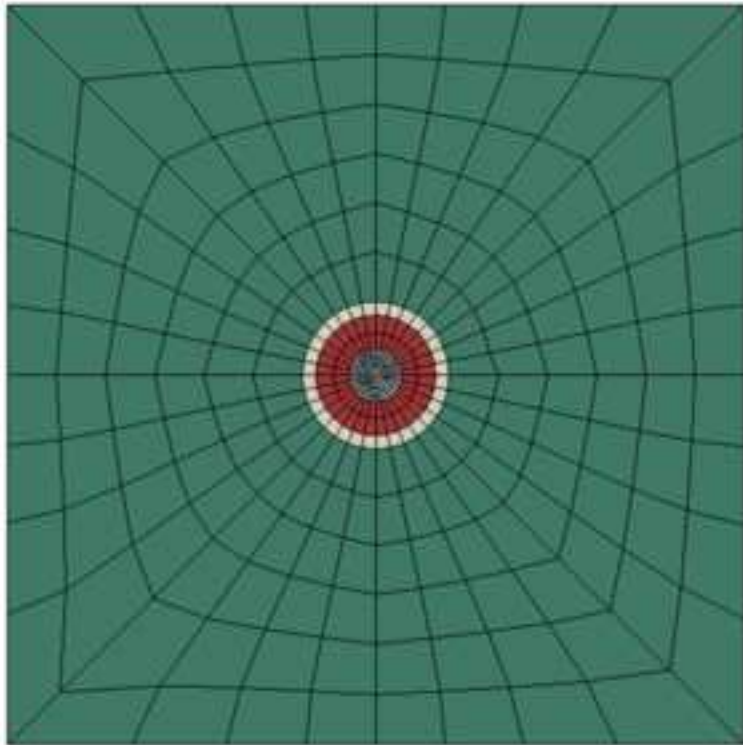
611 **Fig. 19: Influence of the duct thickness on: (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
612 **prestress**

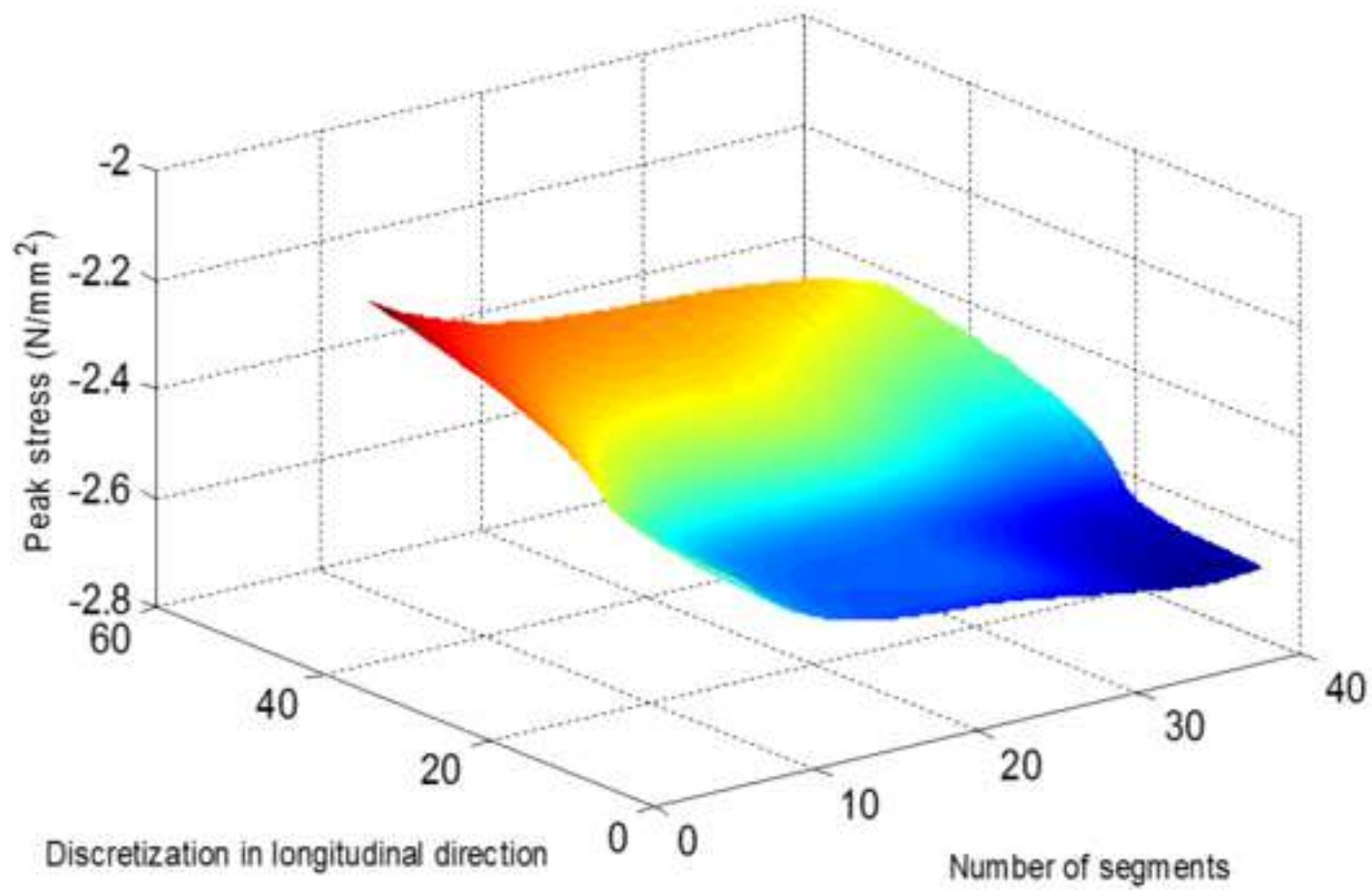
613 **Fig. 20: Influence of the duct material (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
614 **prestress**

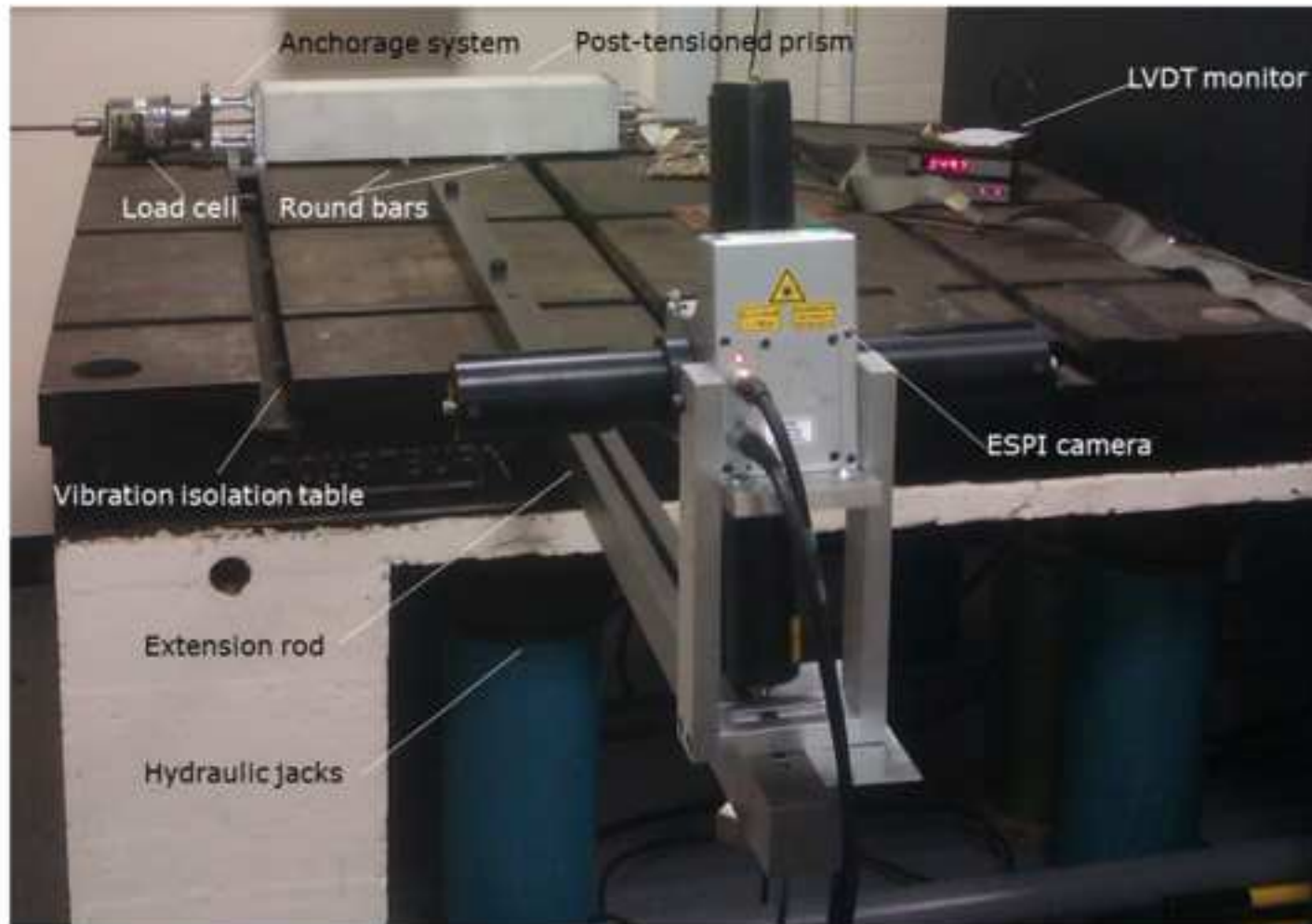
615 **Fig. 21: Influence of shear links on: (a) Stress distribution; (b) Re-anchorage length; (c) Effective**  
616 **prestress**

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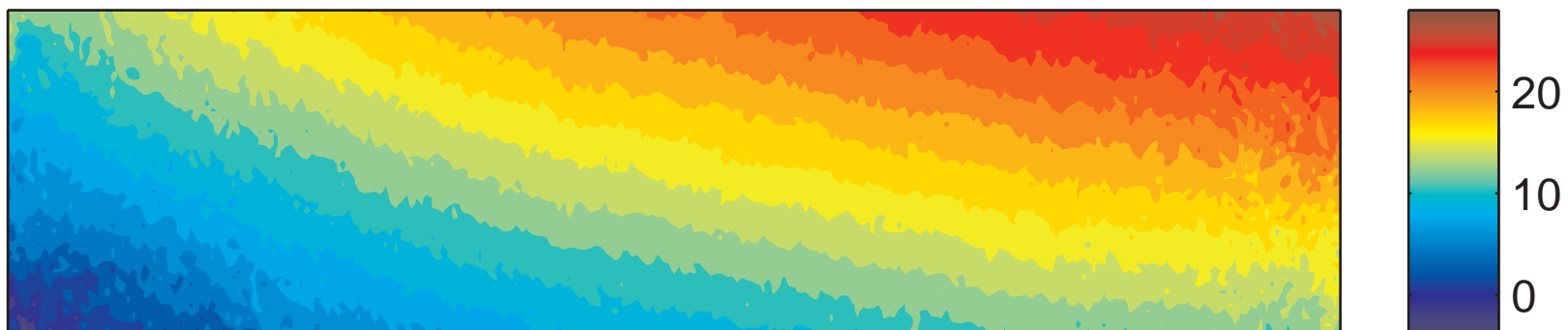








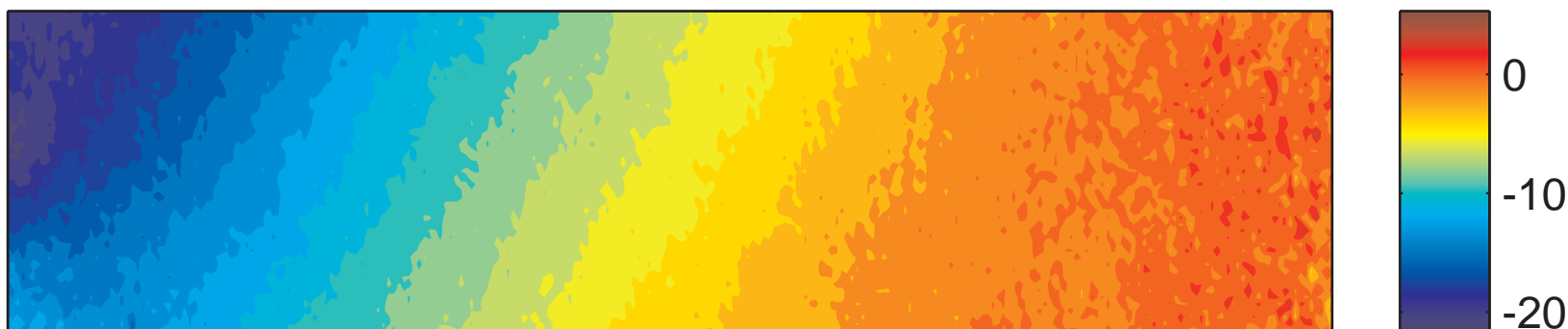
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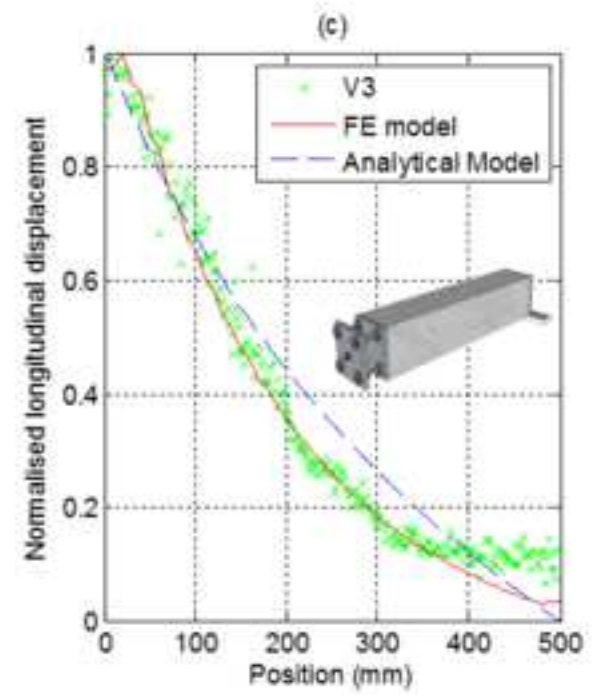
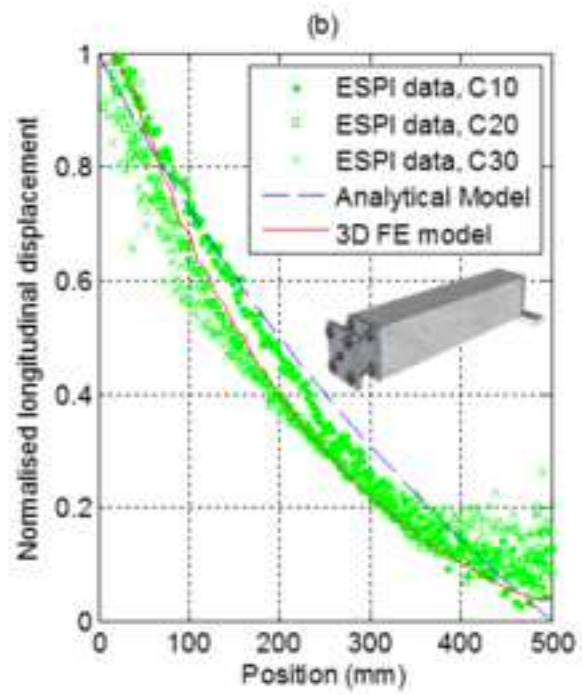
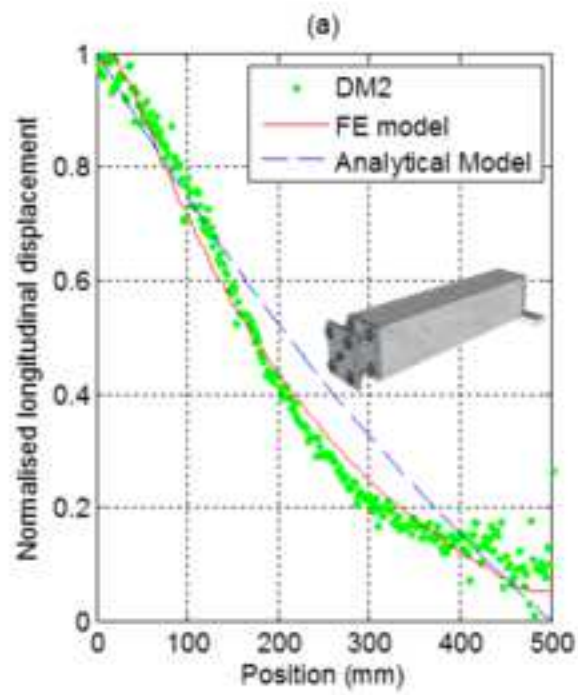


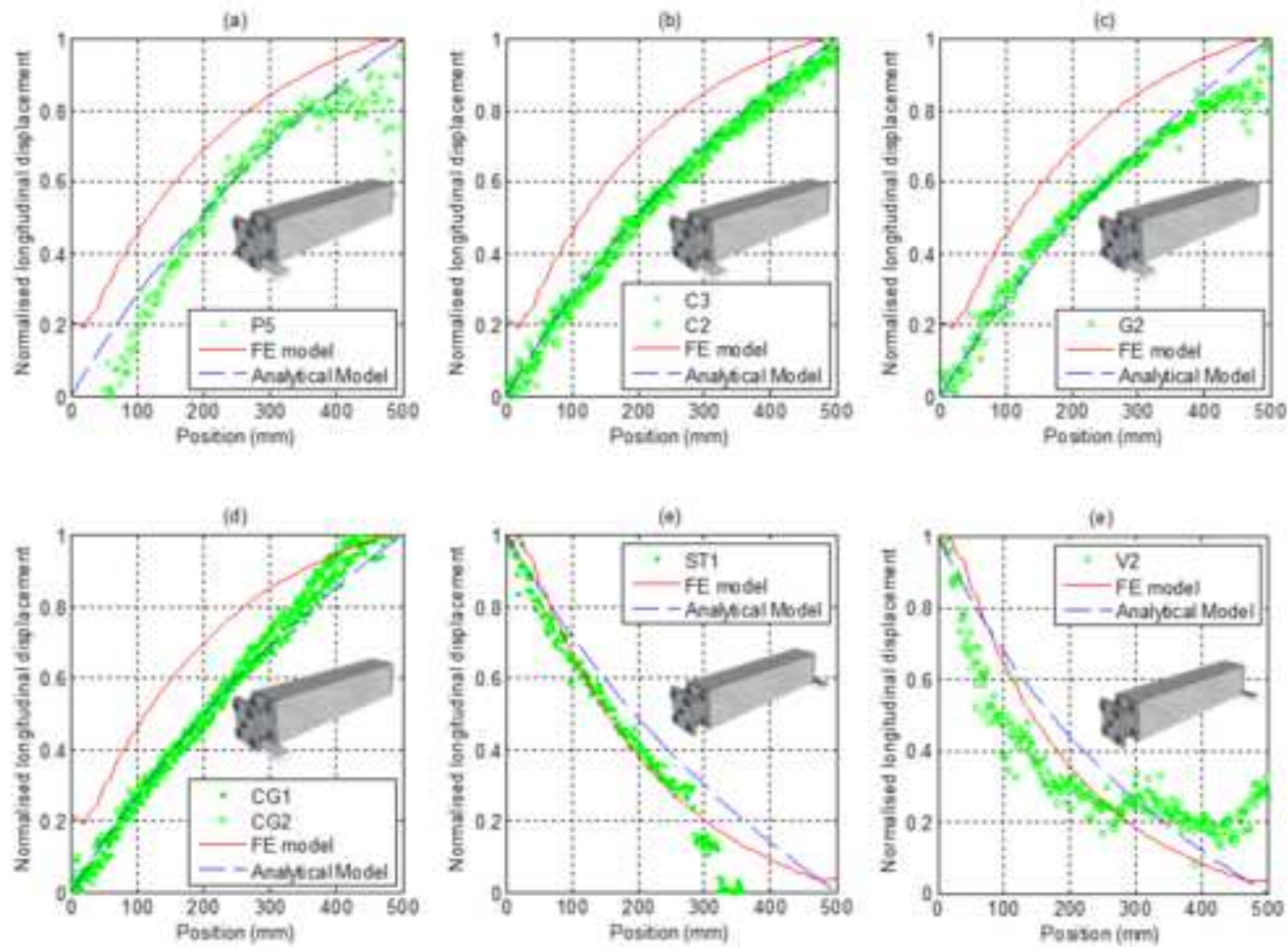
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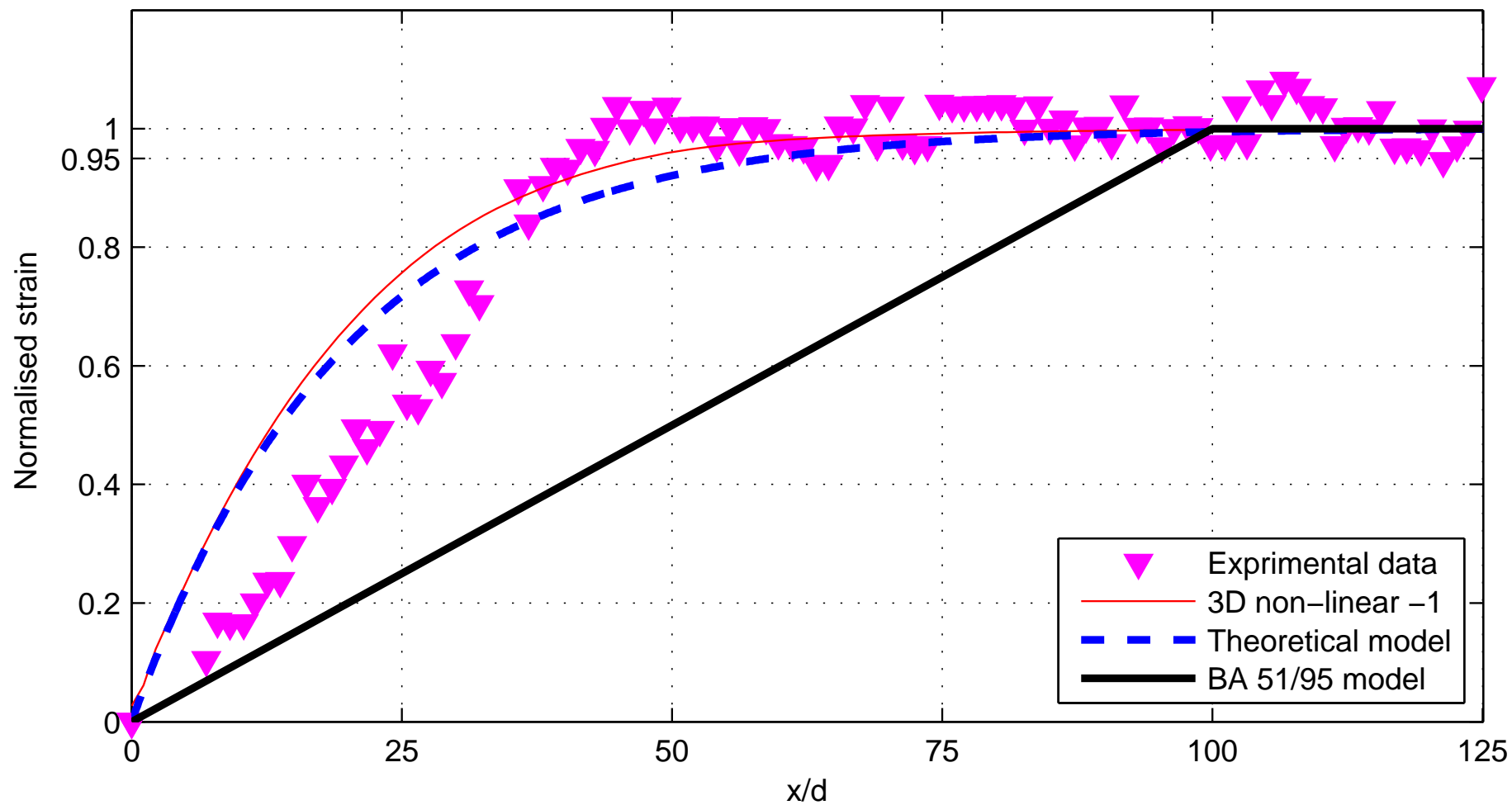


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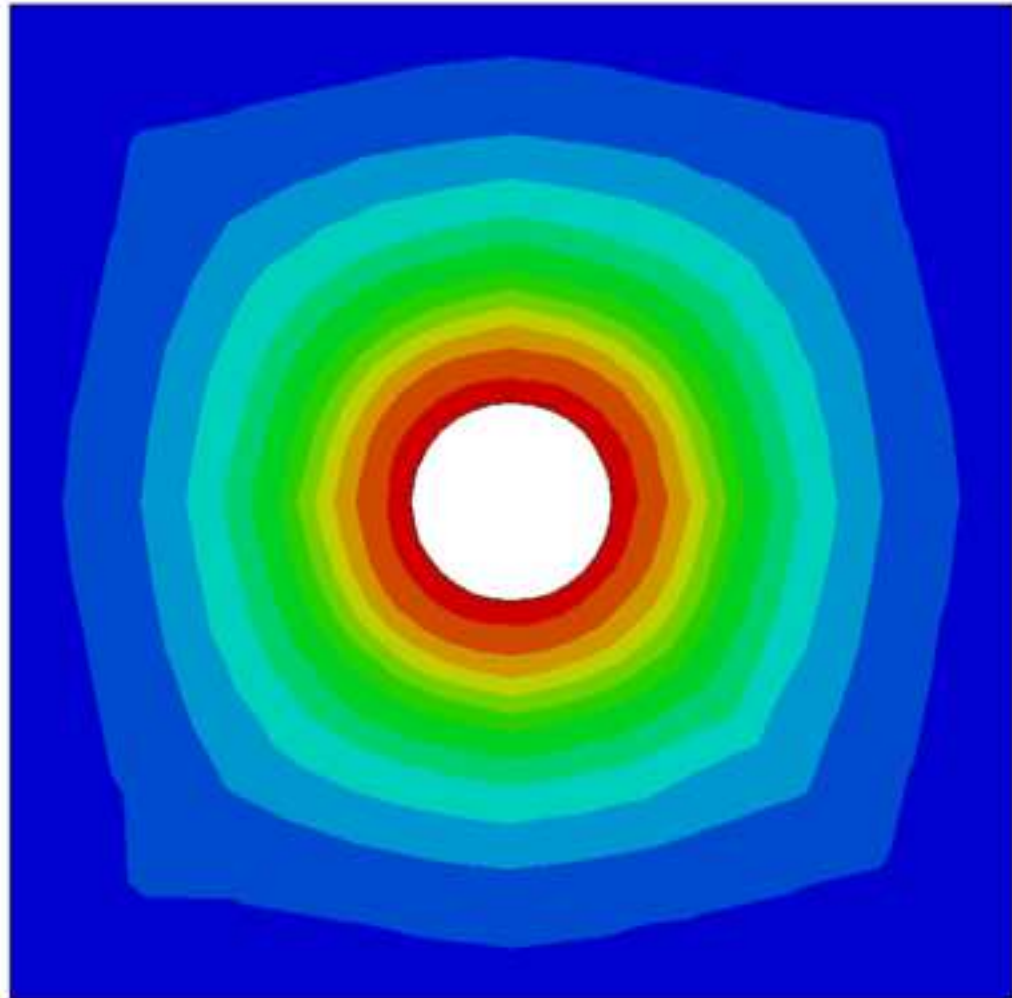
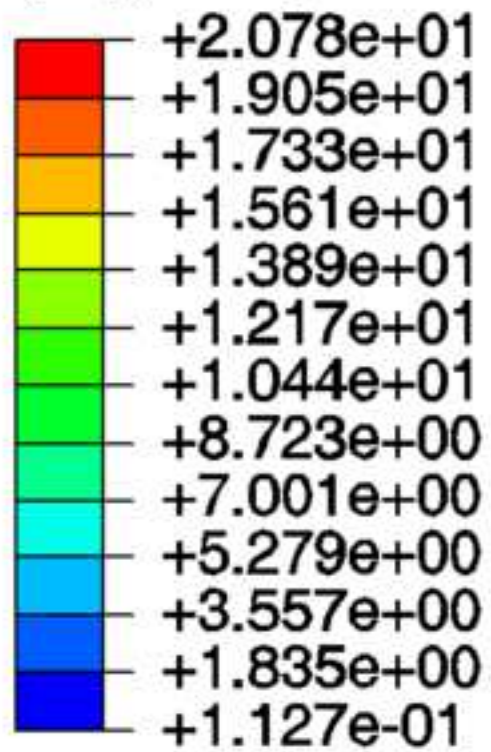


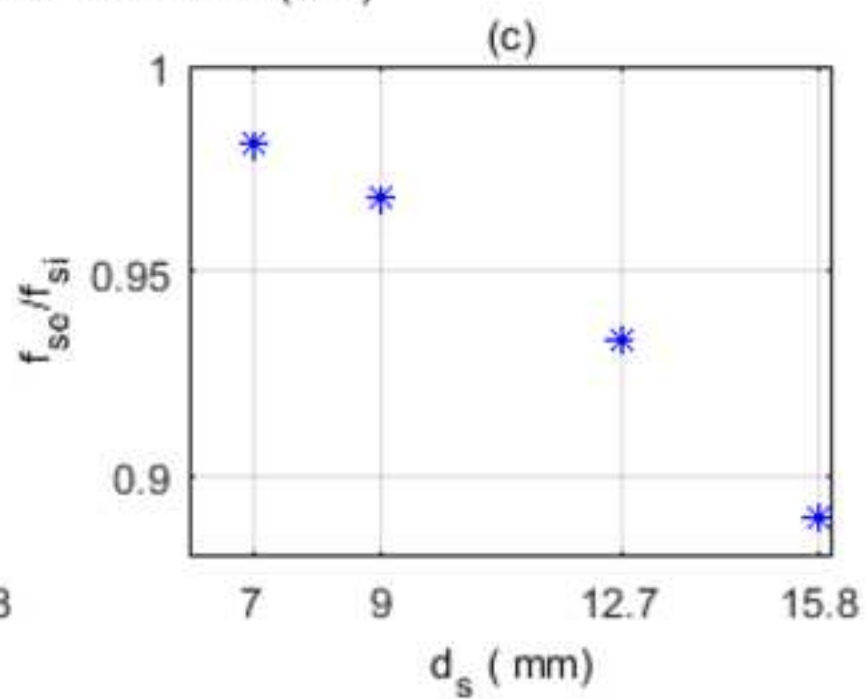
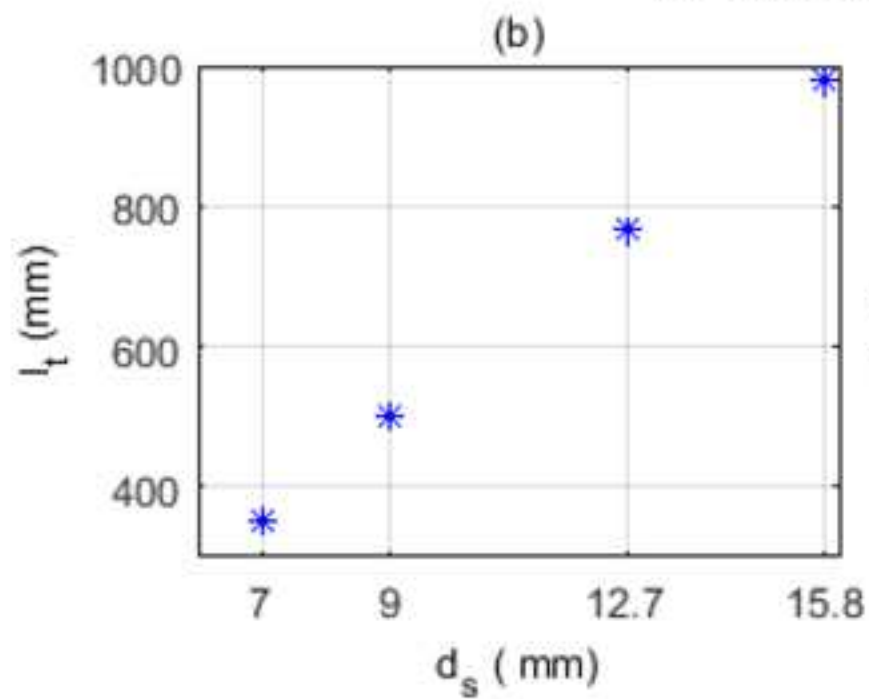
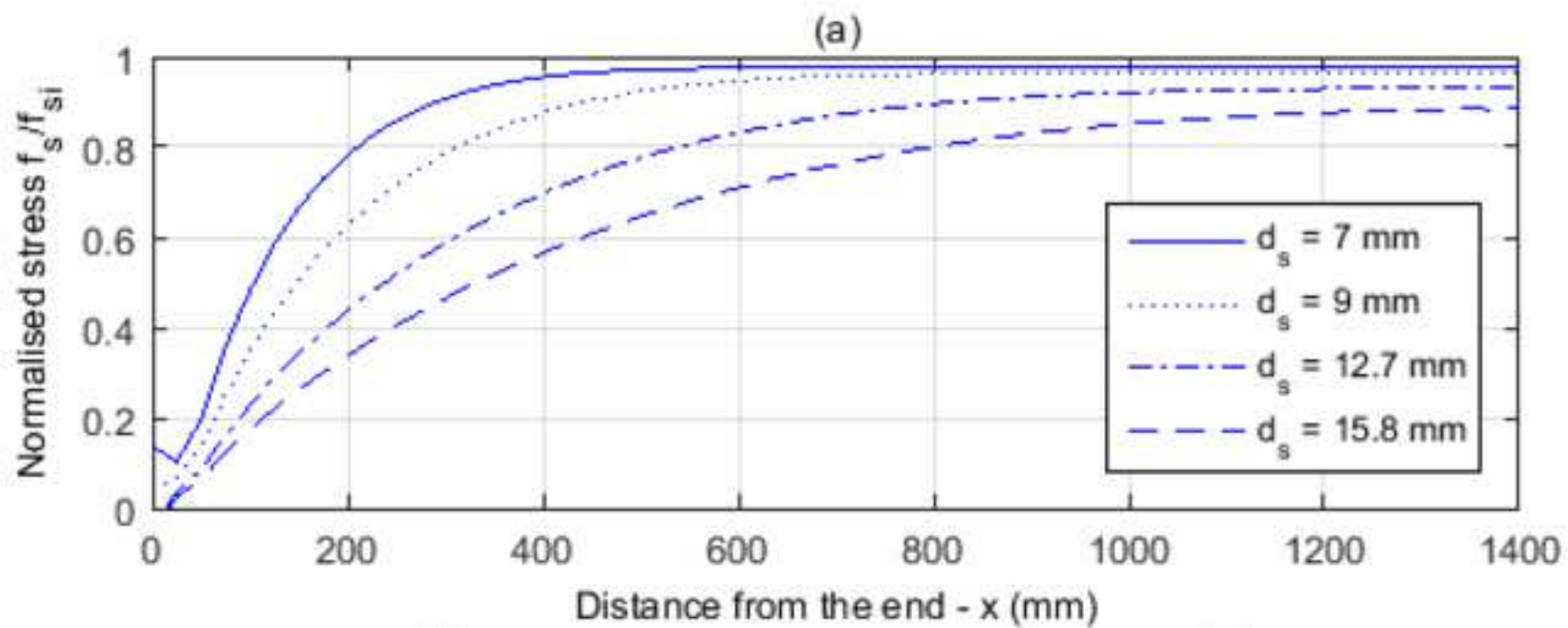




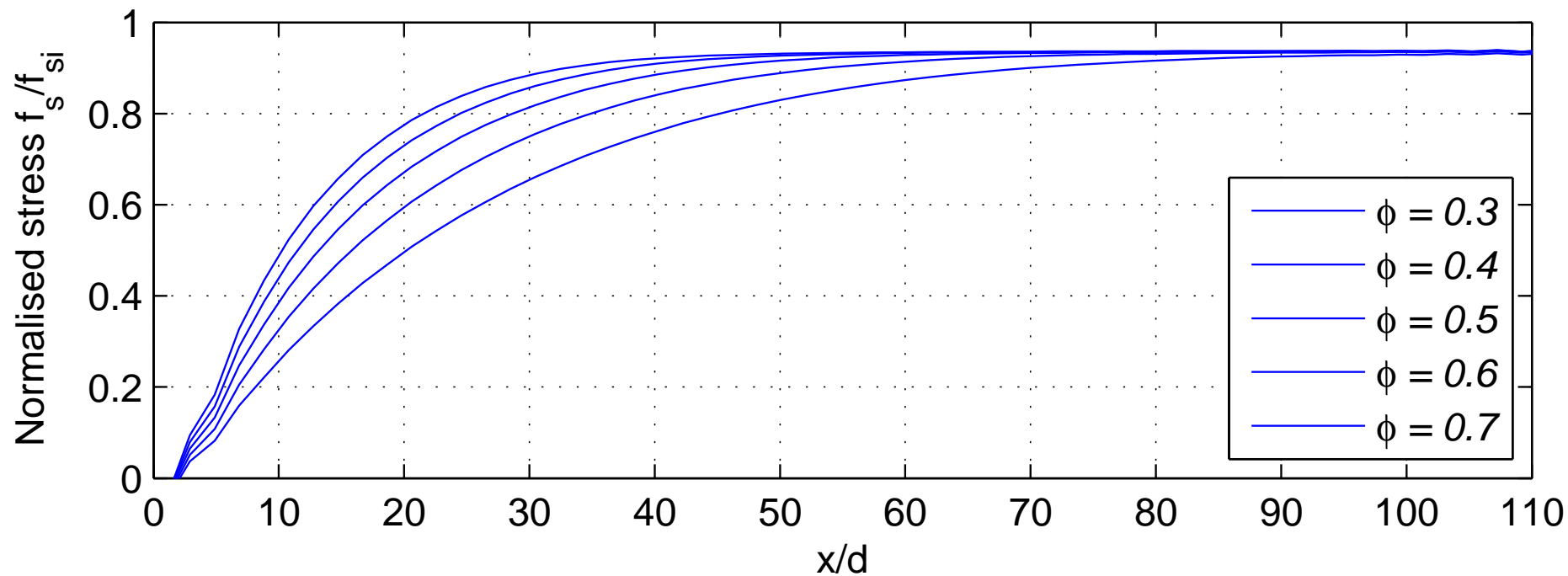


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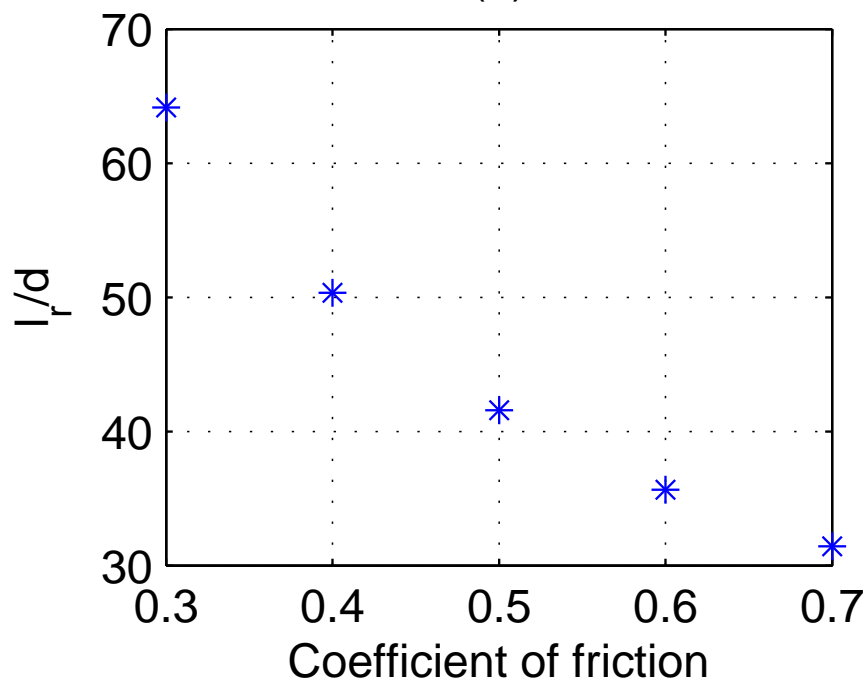




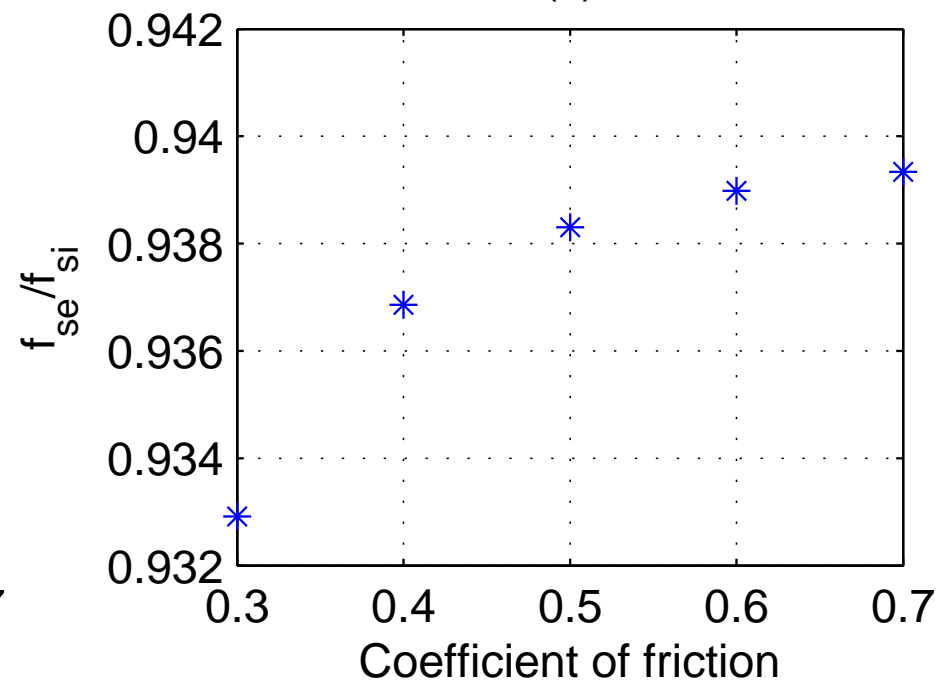
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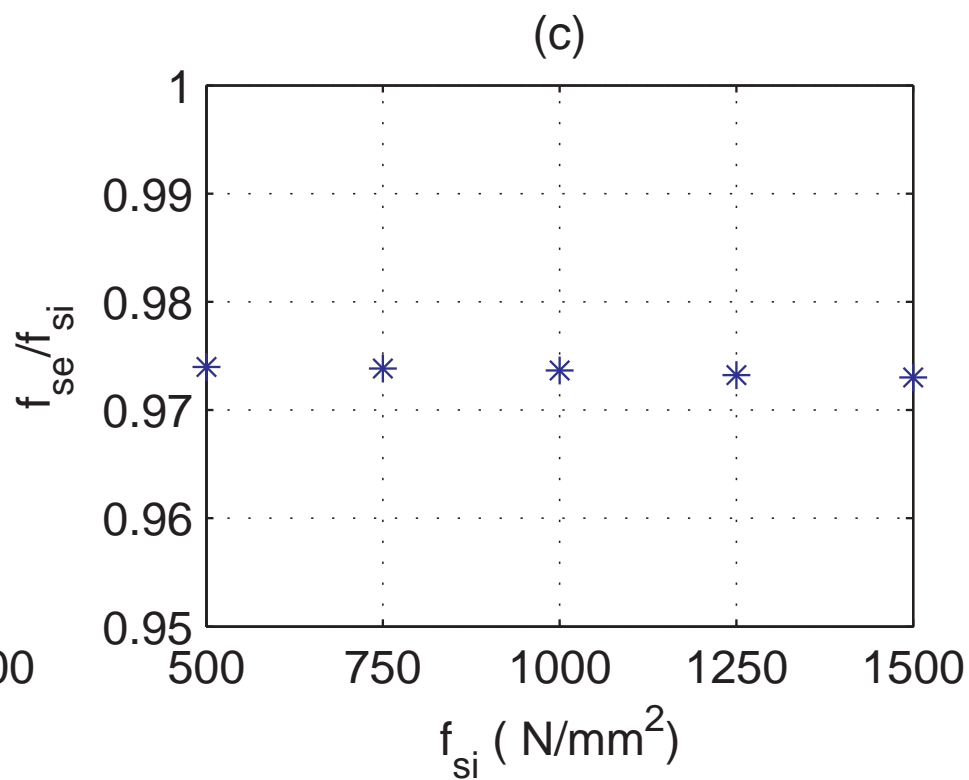
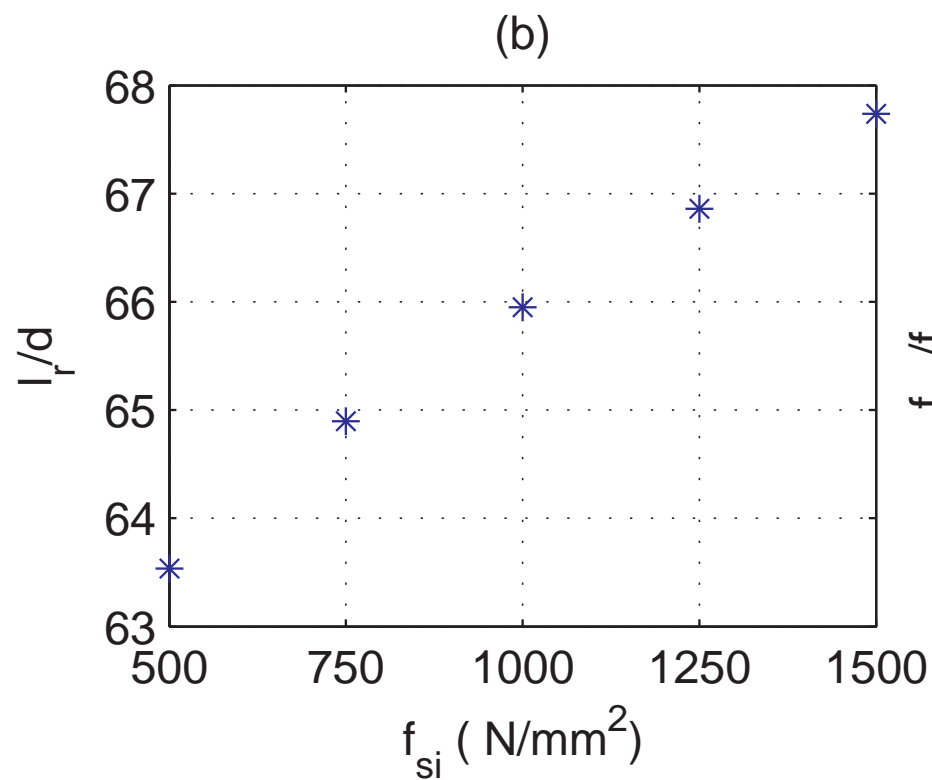
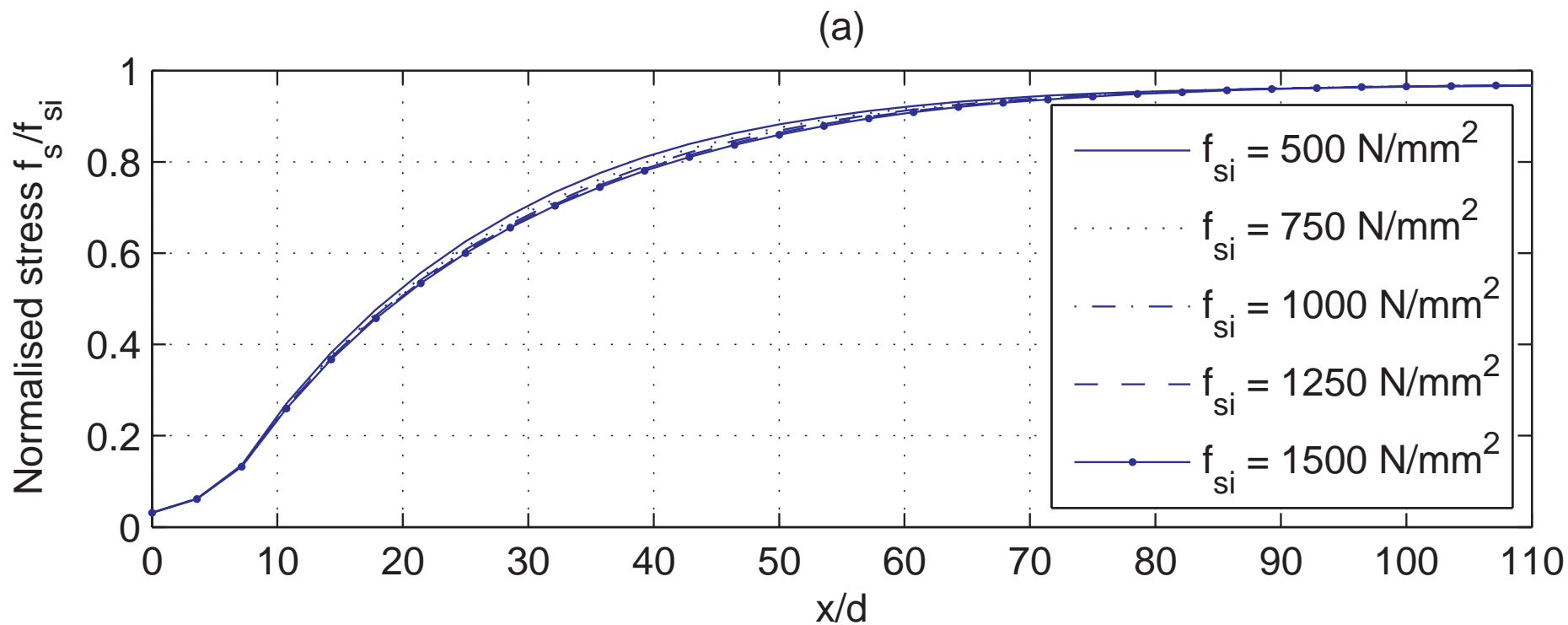
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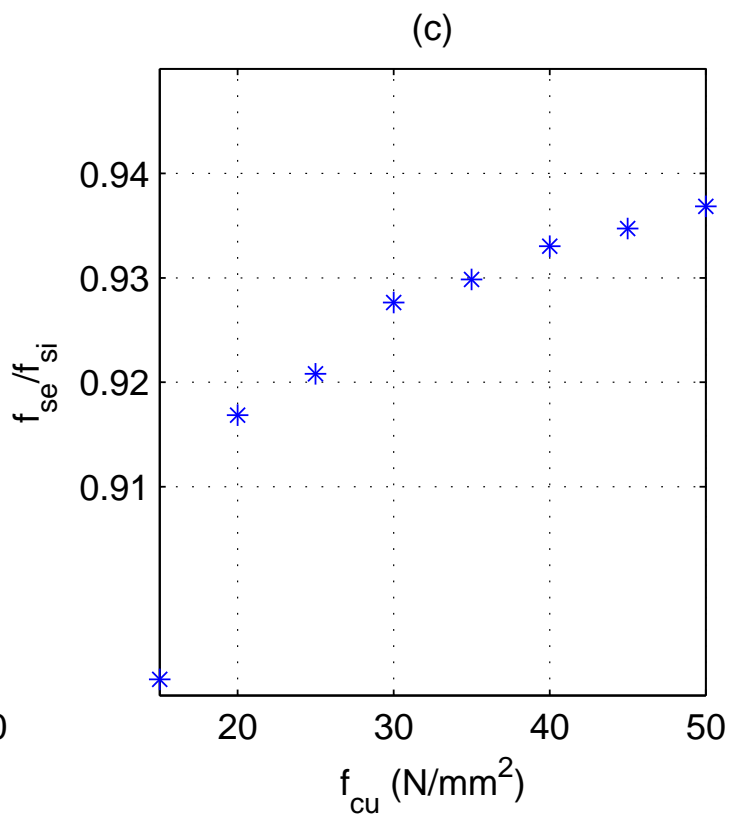
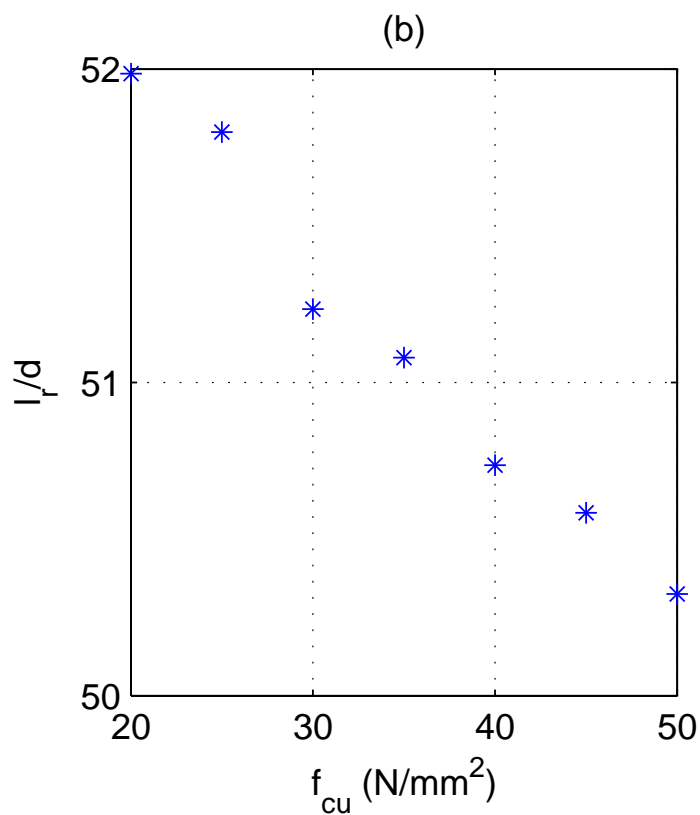
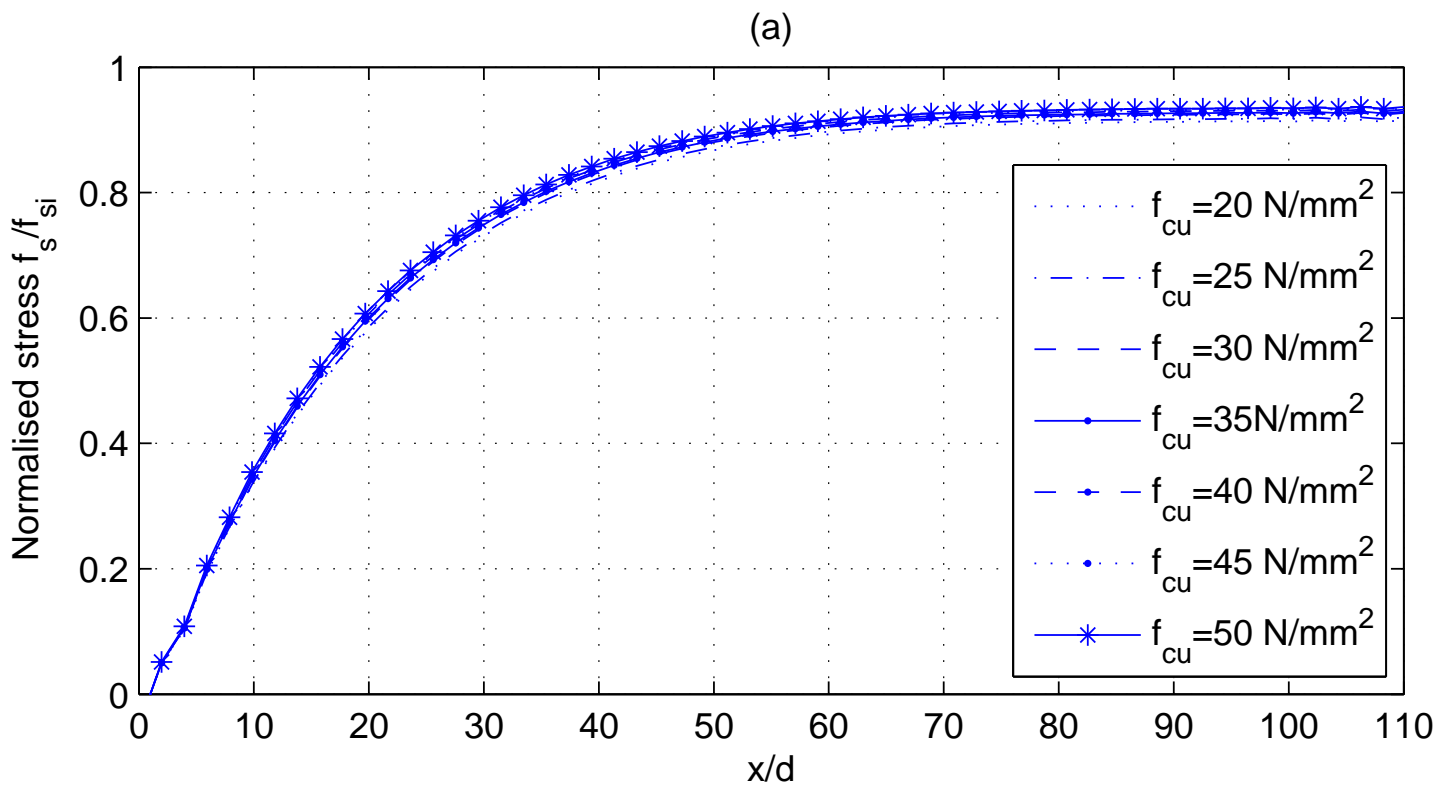


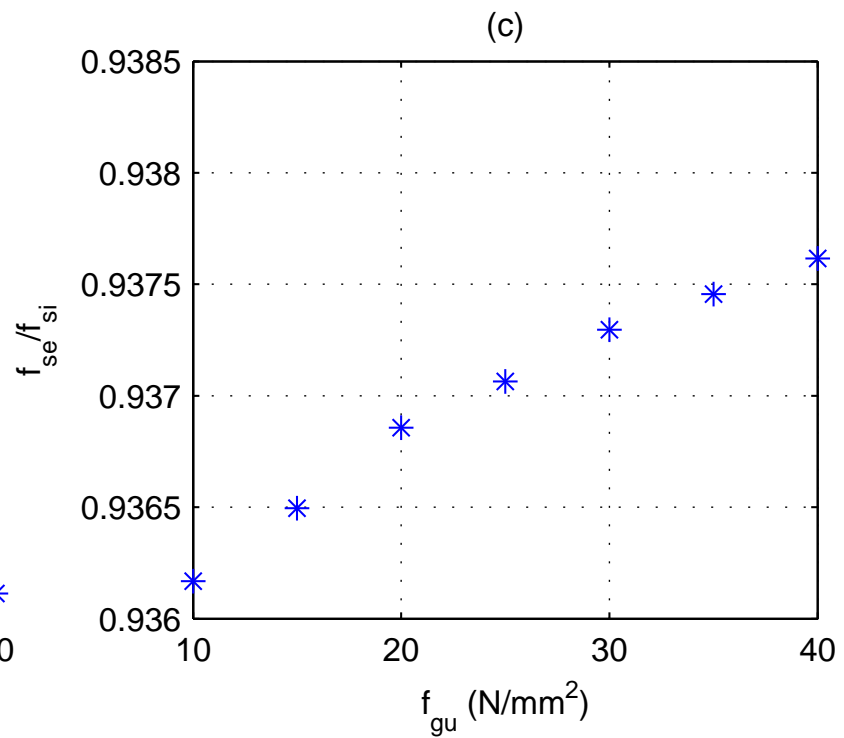
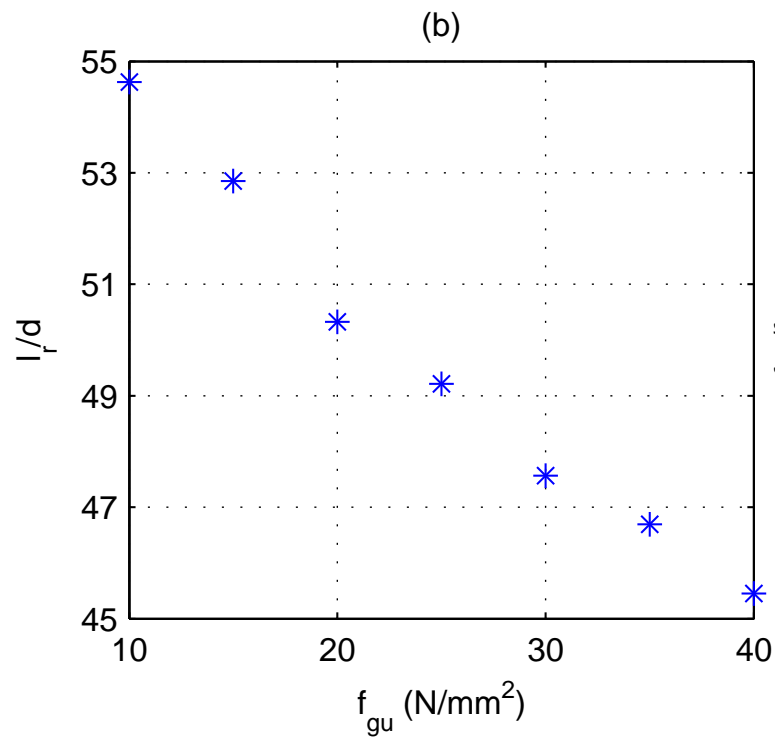
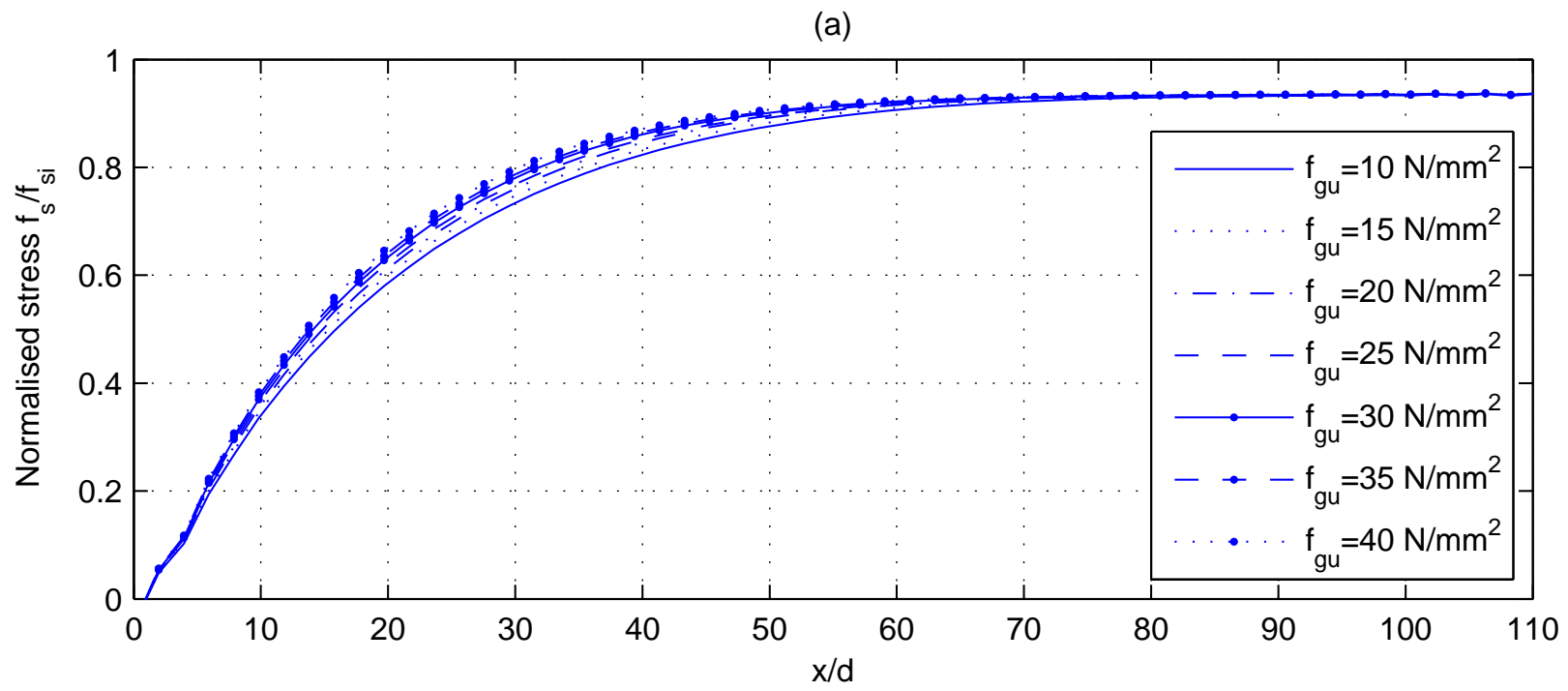
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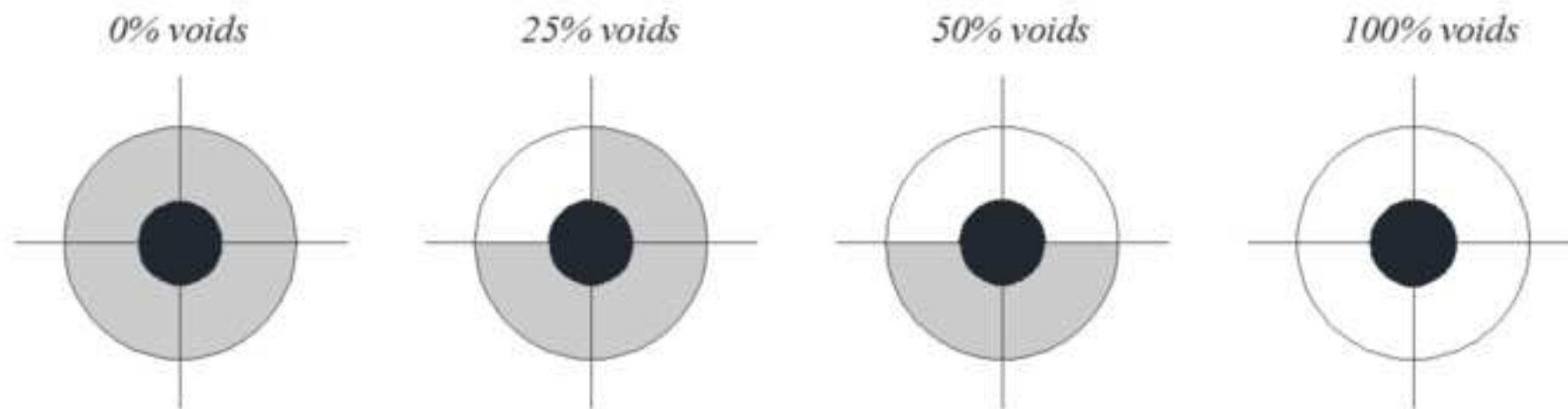




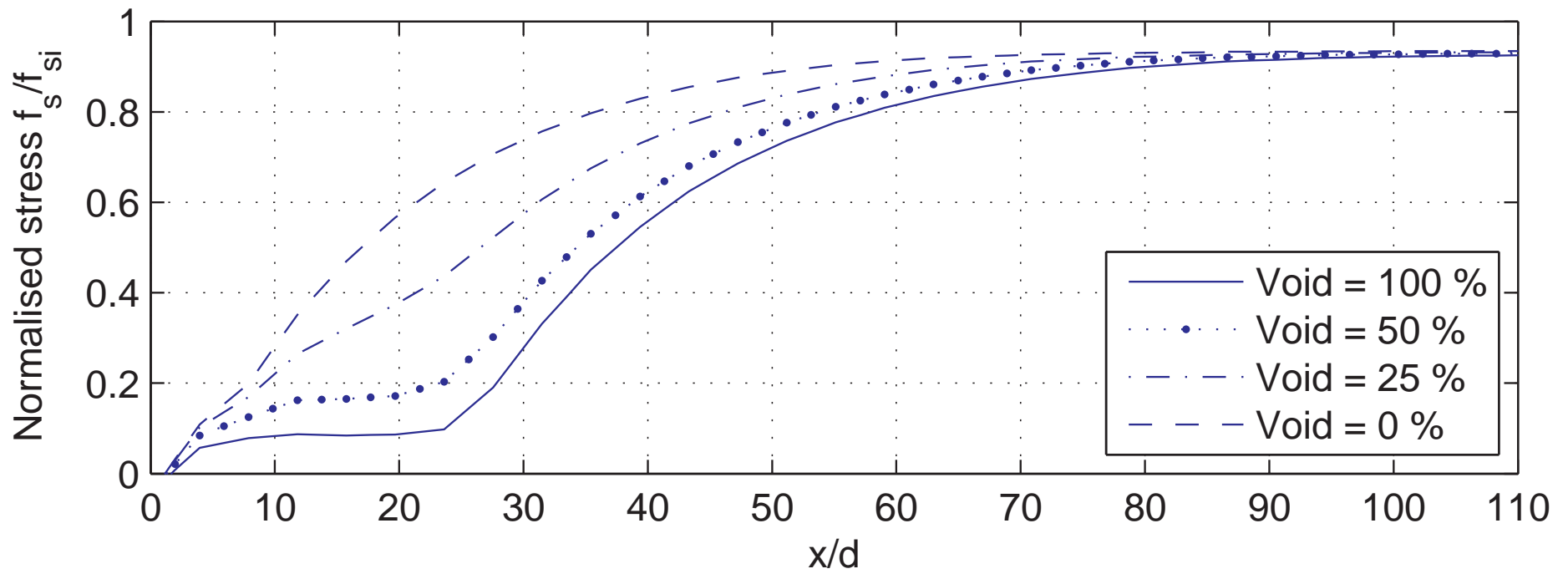




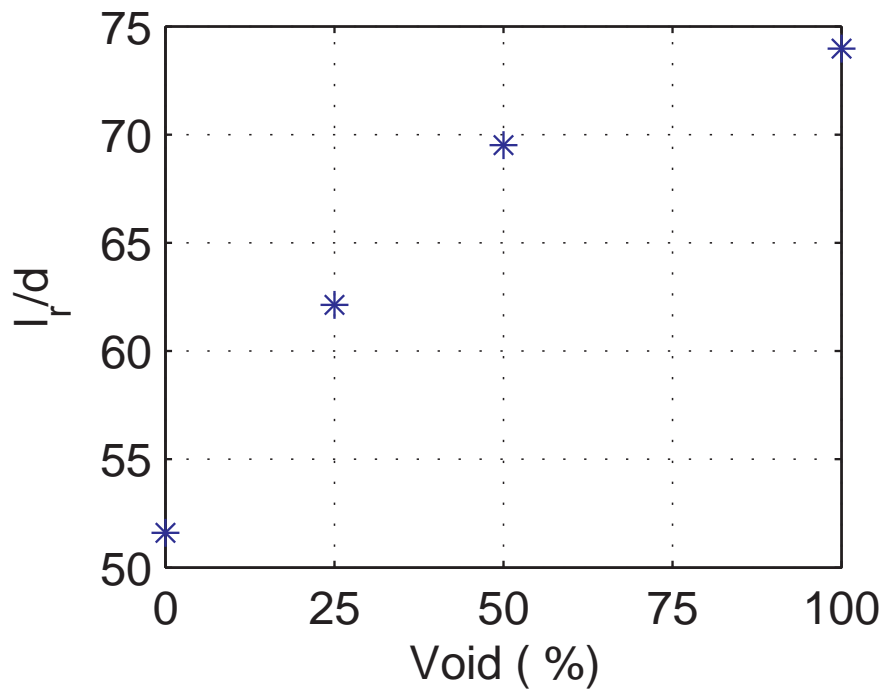




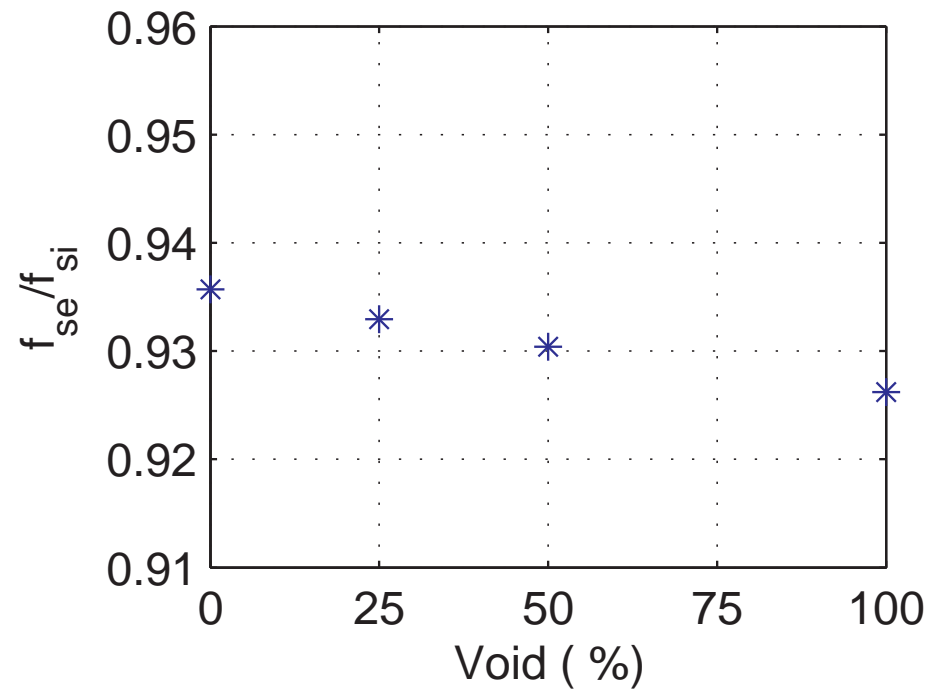
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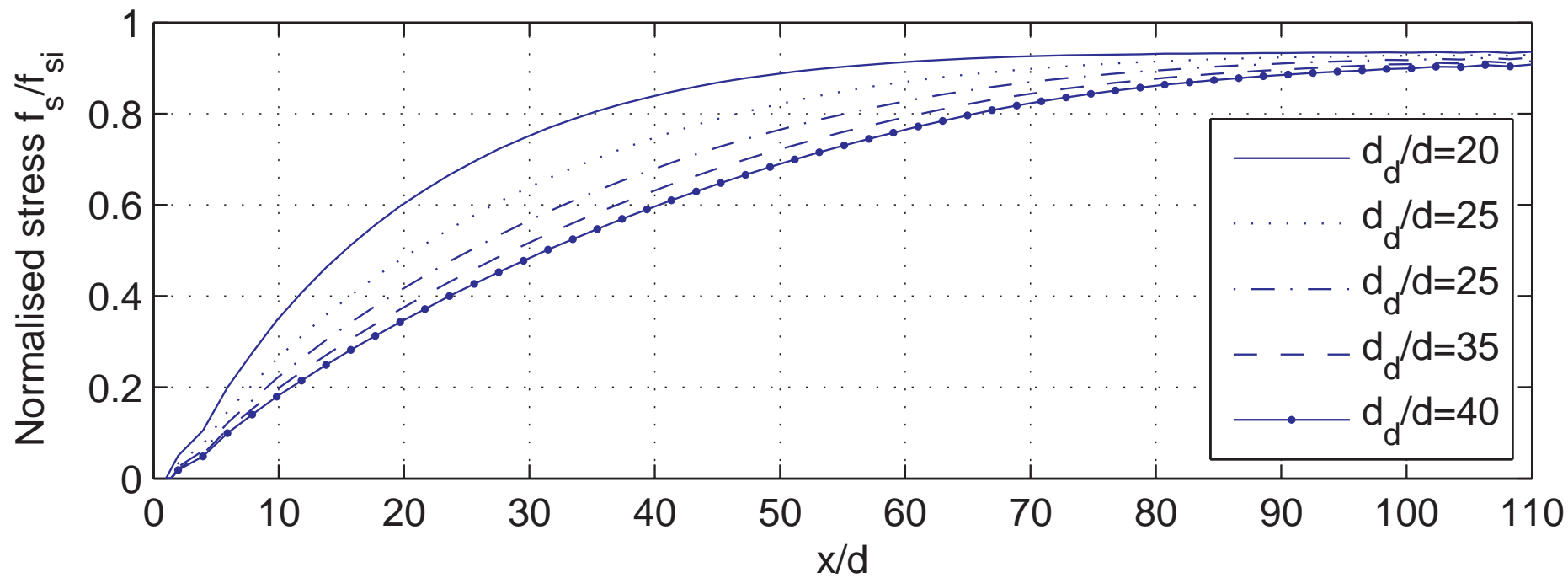
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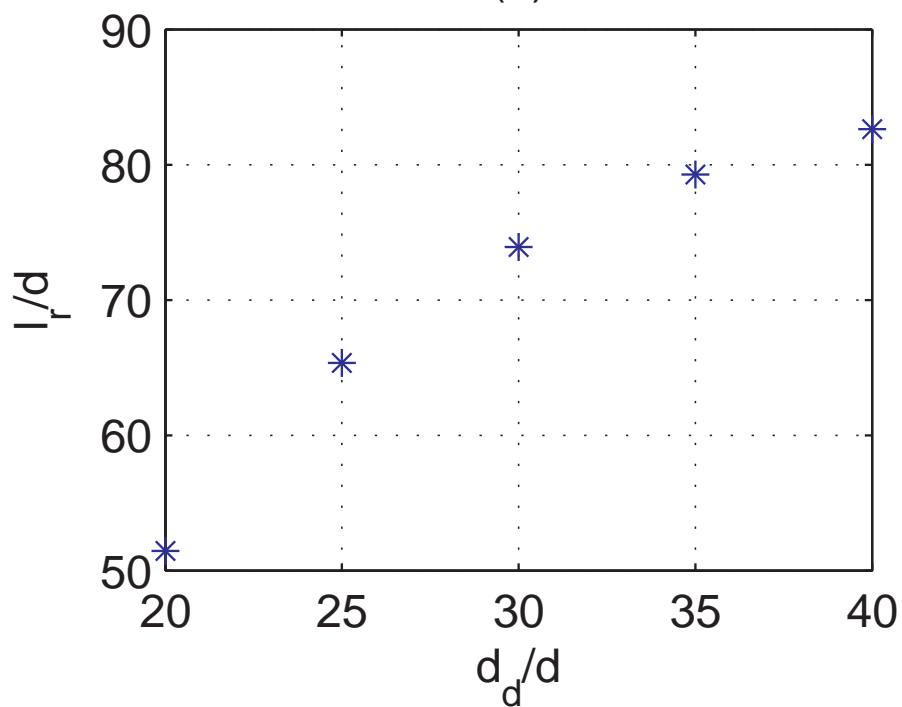
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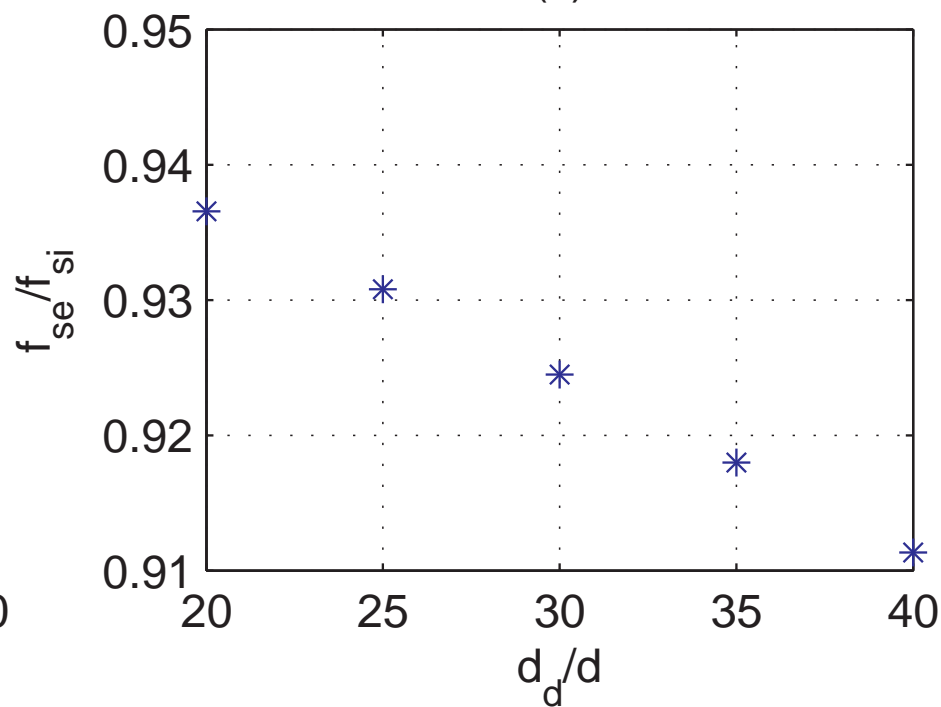
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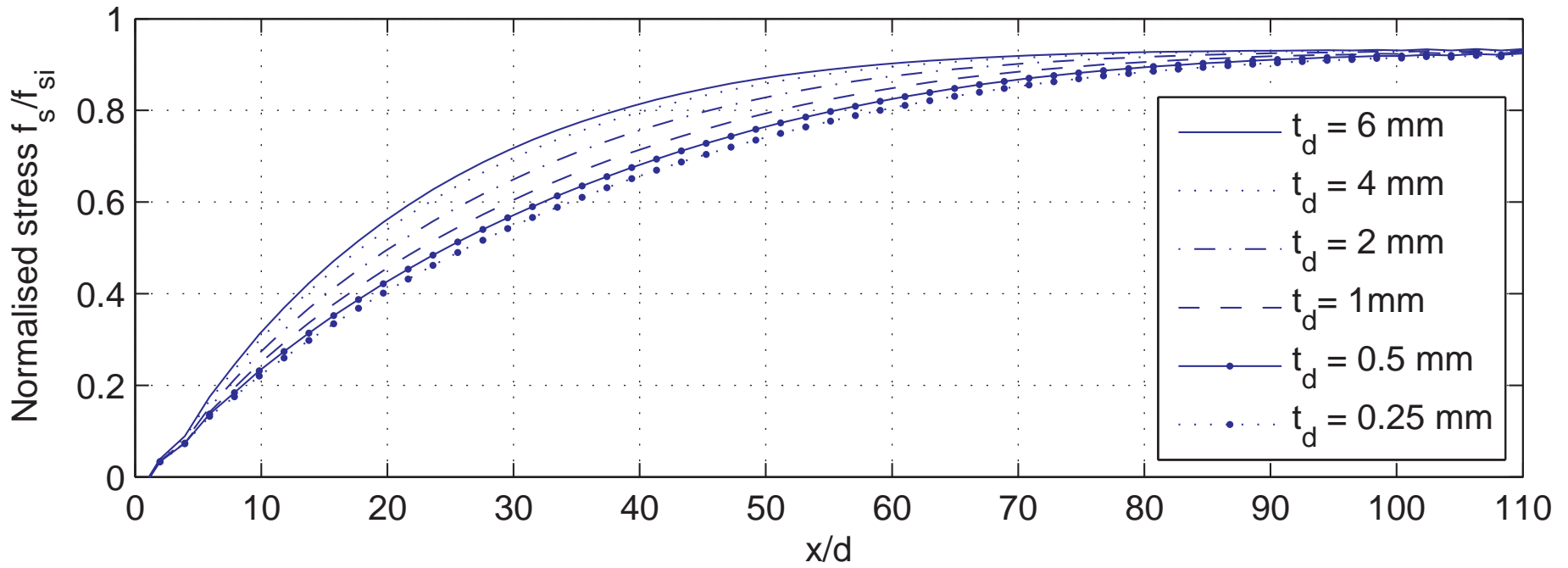
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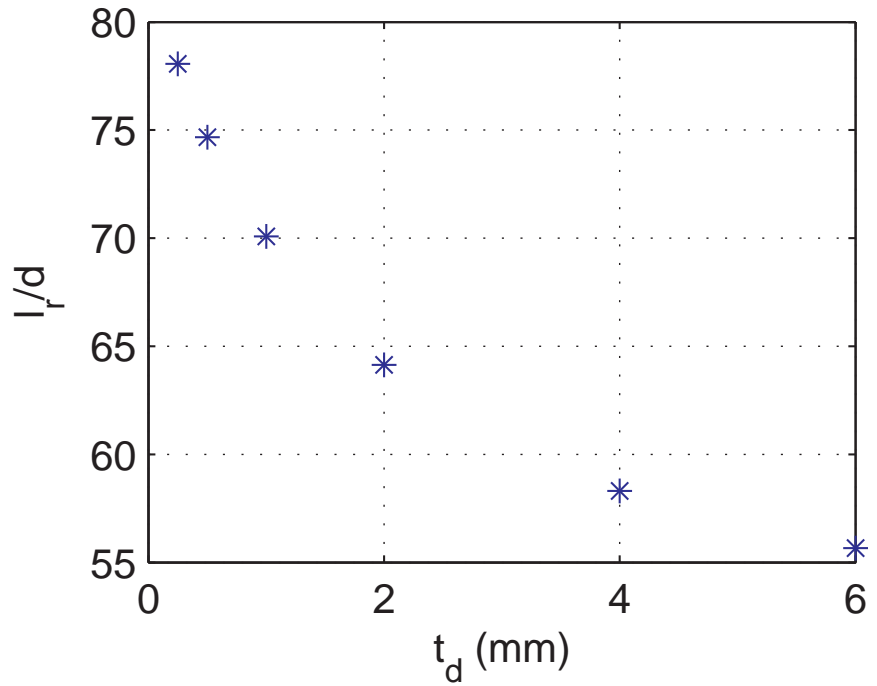
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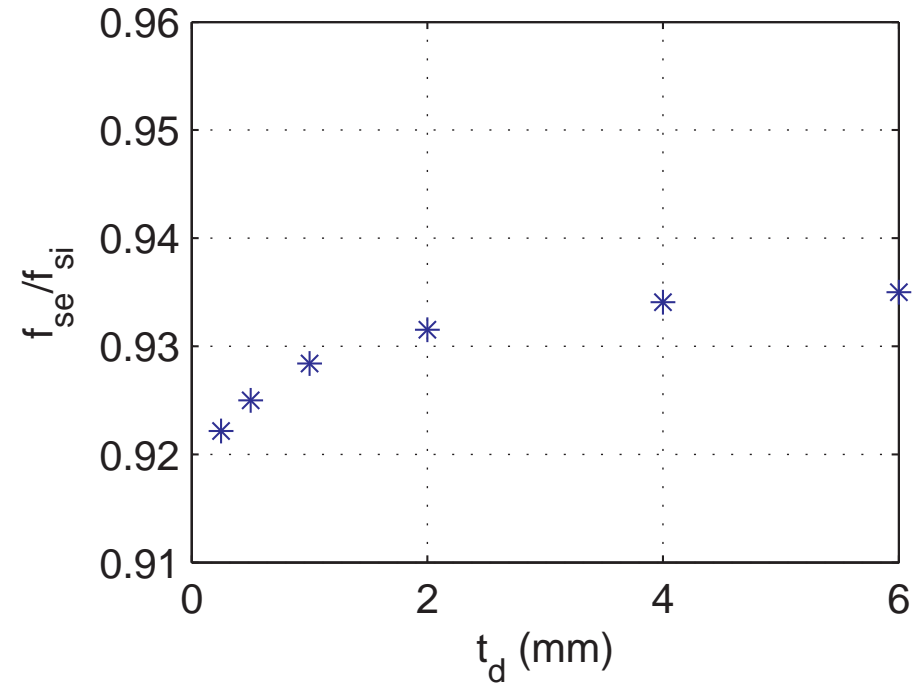
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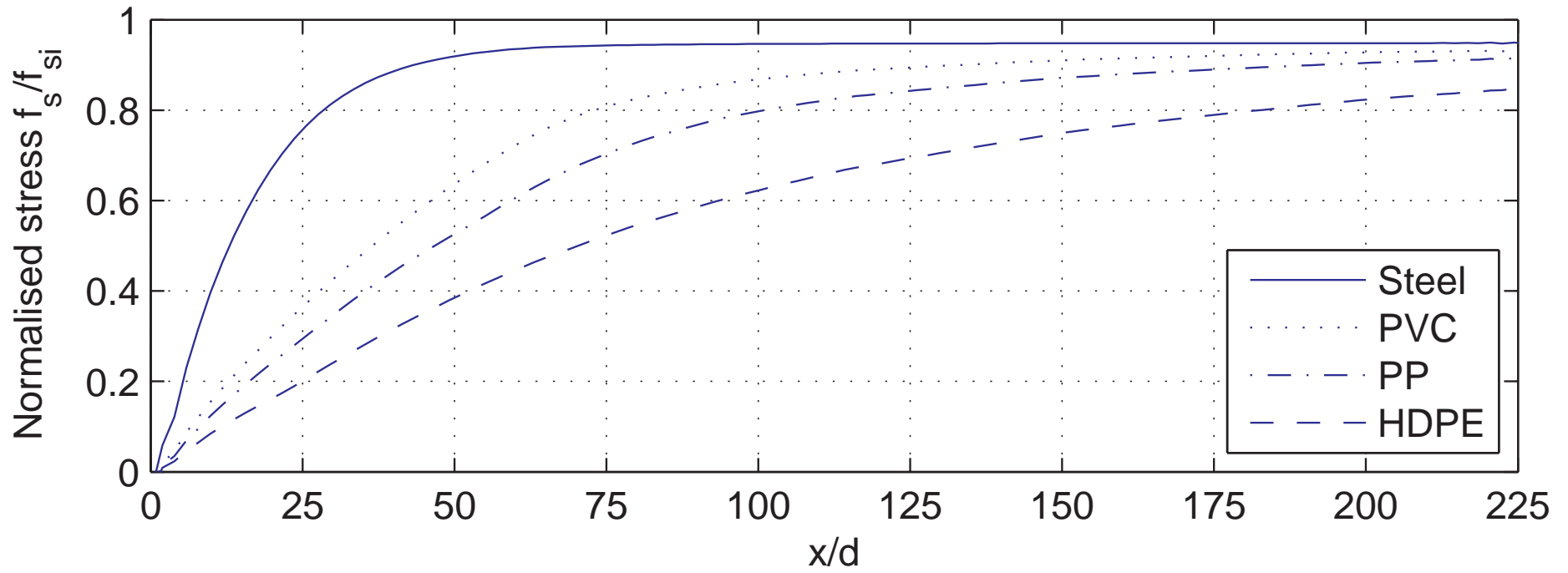
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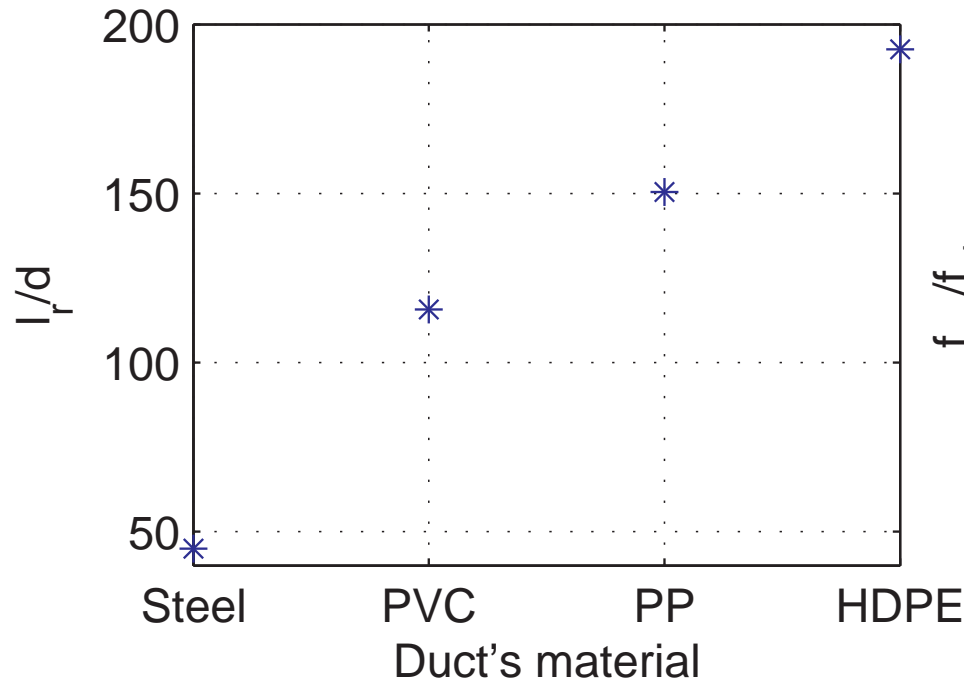
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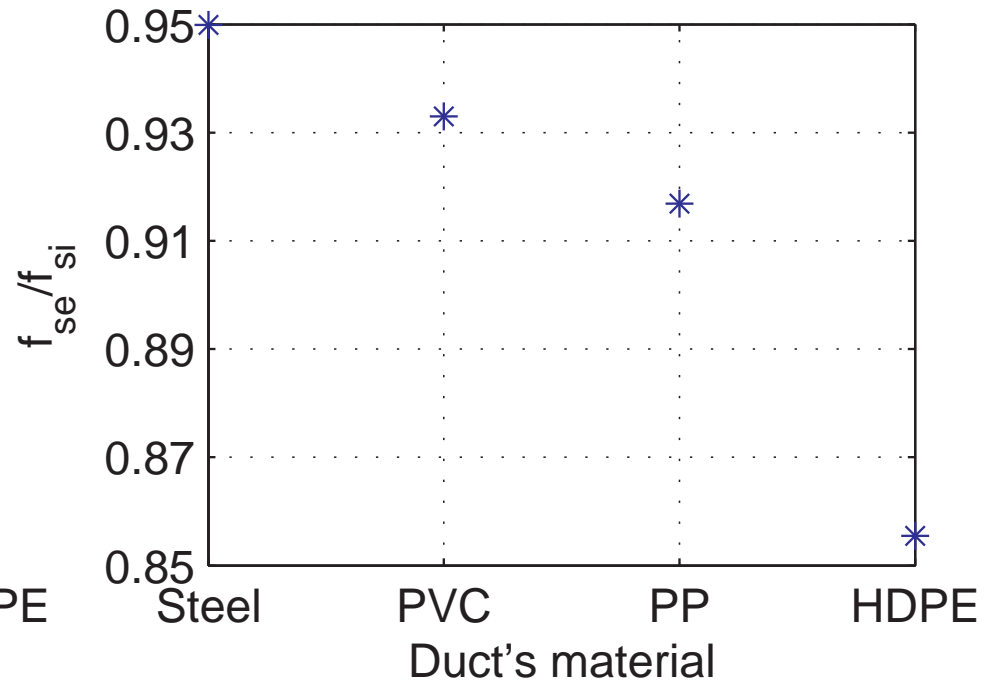
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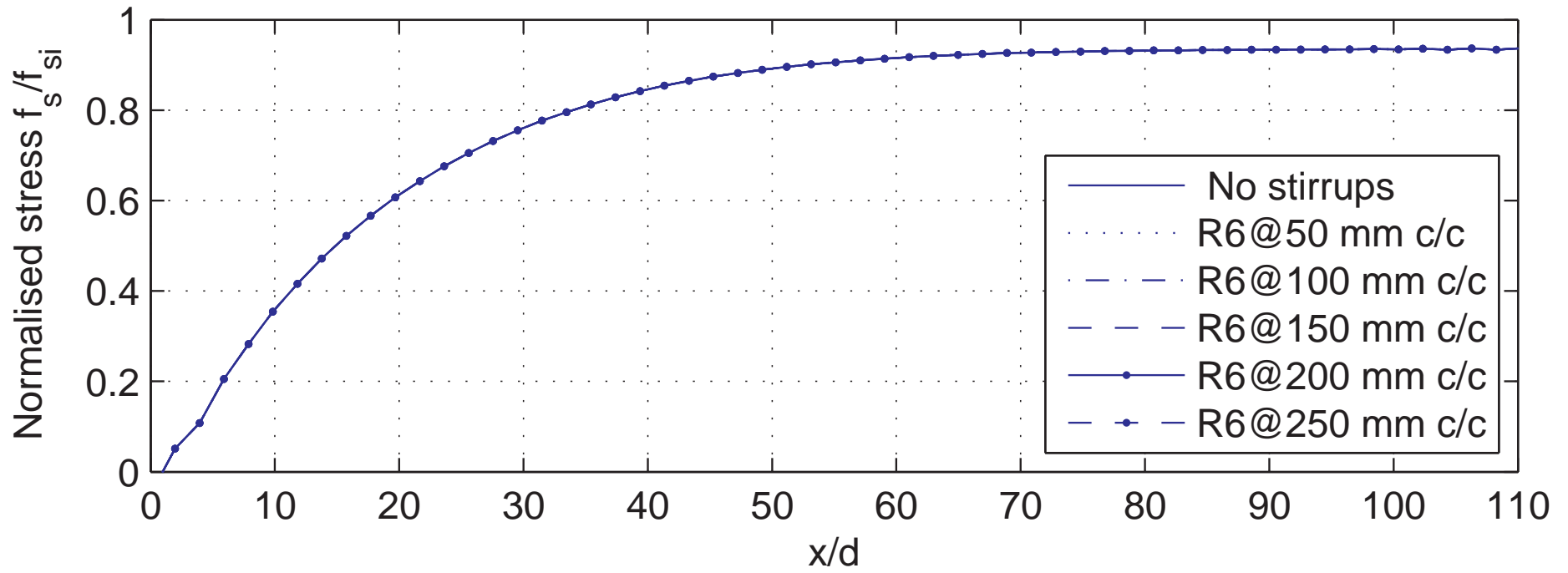


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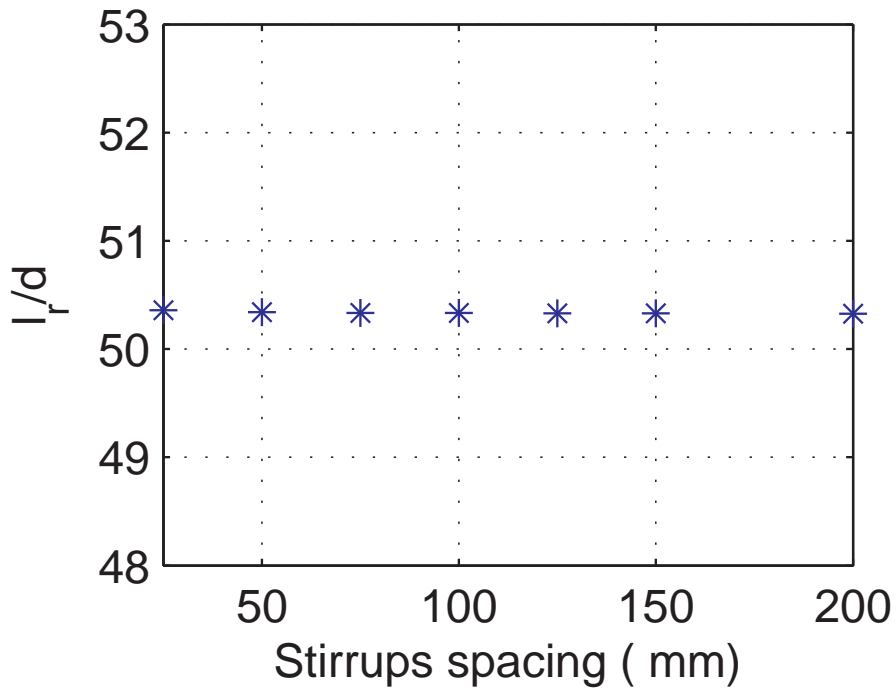




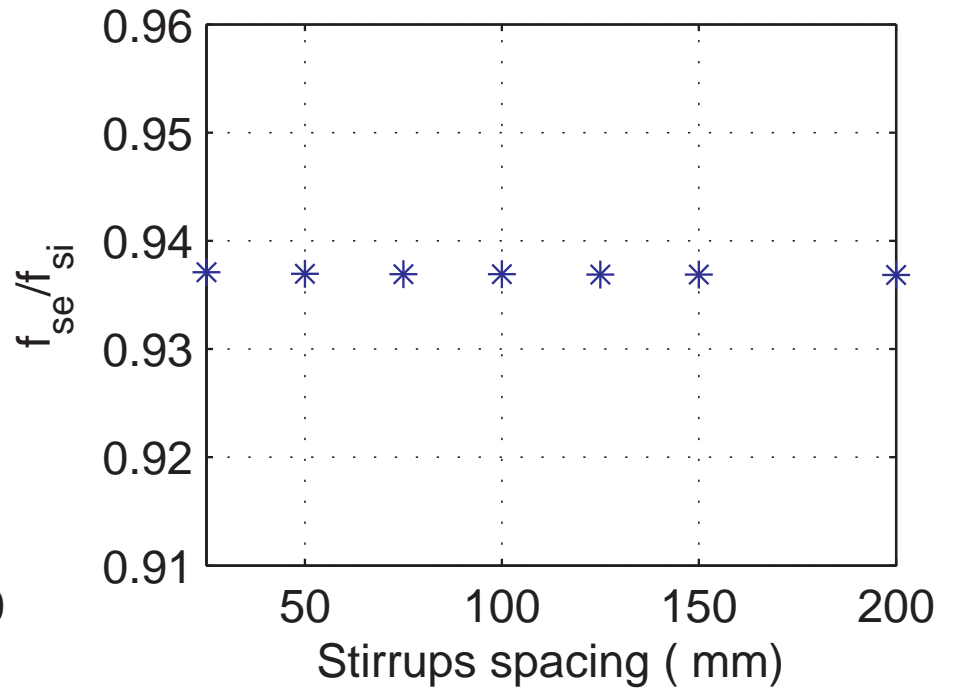
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## Modelling and parametric study of the re-anchorage of ruptured tendons in bonded post-tensioned concrete

A. O. Abdelatif<sup>1</sup>, J. S. Owen<sup>2</sup> and M. F. M. Hussein<sup>3</sup>

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Jennifer Chapman  
Editorial Coordinator  
ASCE's Journal of Structural Engineering  
26 May 2017

Dear MS Chapman,

Re: Decision on Manuscript MS STENG-5593R1 - [EMID:4b1d9ef1e0025fec]

The authors appreciate the final acceptance of the manuscript by reputable ASCE's Journal of Structural Engineering. The comments address by the reviewers have been responded as follows:

**Reviewer #1:** The authors addressed the reviewer's comments properly. I recommend its publication in this journal.

The authors thankfully appreciate the Reviewer #1 decision.

**Reviewer #3:** The authors have addressed the reviewers' comments and I recommend the paper be accepted. Some minor editorial changes are recommended.

The authors thankfully appreciate the Reviewer #3 decision. The minors comments response are given below:

- Same sentence is repeated on lines 159-160 and 164-165: The sentence in lines 159-160 is deleted.
- Provide citation and/or brief explanation of Highway Agency Model on line 310: Citation of the Highway Agency model is provided as recommended.
- Sentence that starts "These voids" on line 391-392 is unclear and should be rewritten: The sentence is re-written as follows: Voids of 200 mm length (15.75d) were introduced in the grout to investigate the impact of grout voids on the re-anchorage mechanism.

Moreover, as required, all text in the manuscript is turned in black font. Also, the space of the reference list is doubled.

Yours sincerely,  
Amged O. Abdelatif, Dr.  
Civil Engineering Department  
University of Khartoum  
Khartoum, Sudan  
On behalf of Dr. John Owen and Dr. Mohammed Hussein

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