

## Article

# Tensile and fatigue failure of 3D printed parts with continuous fibre reinforcement

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'This article is a revised and expanded version of a paper entitled [Dramatically Increasing the Mechanical Properties of 3D Printed Parts via Continuous Fibre Reinforcement and Coatings] presented at [14<sup>th</sup> Rapid Prototyping, Design and Manufacturing, Loughborough, 16<sup>th</sup> December 2015].'

## Tensile and Fatigue Failure of 3D Printed parts with Continuous Fibre Reinforcement

### ABSTRACT

This paper introduces a design methodology used to integrate continuous fibre reinforcement into AM polymer parts with the aim of improving their mechanical properties. Tensile and low cycle fatigue testing of reinforced parts is carried out for a range of load conditions and strain rates

Physical testing showed that it was possible to improve the strength of parts by 400% and cycles to failure by 42,800% with the addition of 4% carbon by weight. Logarithmic load/cycle relationships were found also samples showed significant variability in the number of cycles to failure. No correlation between the density of the polylactic acid (PLA) infill and the tensile strength or low cycle fatigue life.

Access holes used to thread the fibre into the reinforcement channels were identified as stress concentrators initiating cracks in the PLA and separation of the reinforcement from the PLA part.

**KEYWORDS:** Carbon fibre, Fatigue, Mechanical properties, Failure modes, Additive manufacturing.

### 1. INTRODUCTION

The term additive manufacturing (AM) encompasses a diverse set of technologies that share the principle of building parts in a layer based fashion (Gibson et al., 2010). This build strategy has the advantage of producing parts with complex geometries without the need for tooling. The AM sector continues to grow rapidly as new applications are found and knowledge of design for AM spreads. The desktop 3D printing market is one of the fastest growing segments in the AM sector with fused filament fabrication (FFF) printers found in schools, businesses and hospitals (Wohlers, 2016). Open source development of FFF printers has resulted in low cost machines and software with a wide range of capabilities. A study by Tymrak et al. (2014) shows parts made from well-tuned open-source desktop machines and generic materials have mechanical properties comparable to proprietary systems.

The inhomogeneous nature of FFF parts results in parts with approximately 80% the strength of injection moulded or machined parts of the same polymer (Montero et al., 2001, Ahn et al., 2002, Hambali et al., 2012, Ziemian et al., 2012). Despite this FFF parts exhibit excellent

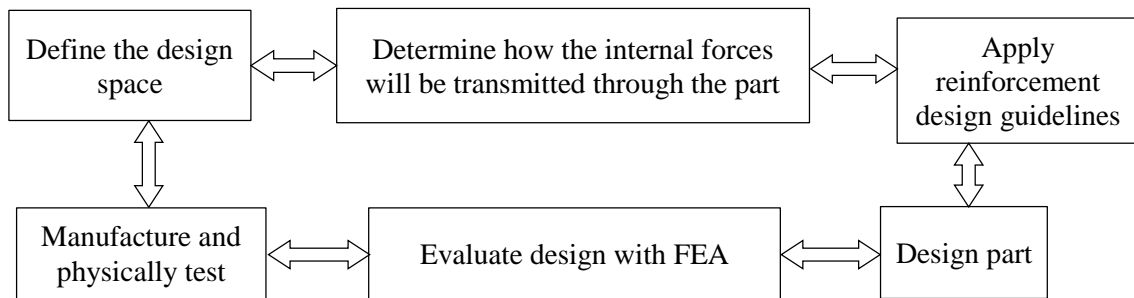
strength-to-weight ratios in many applications by incorporating light-weight cellular structures in areas of low stress and topologically optimised geometries (Lu et al., 2014, Villalpando et al., 2014, Rodríguez et al., 2003, Gardan and Schneider, Brackett et al., 2011).

For applications requiring higher strength or stiffness, conventional thermoplastics such as acrylonitrile butadiene styrene (ABS) or polylactic acid (PLA) are not adequate. Introducing reinforcement fibre into the part is an effective way to extend the capabilities of FFF machines for higher load applications. Short fibres can be mixed into the polymer feedstock and deposited in the usual way. The low volume fraction and pull out strength of the short fibres results in minor gains in strength and stiffness whilst toughness is often reduced (Ning et al., 2015, Mahajan and Cormier, 2015). FFF machines capable of depositing continuous fibre reinforcement are rare however studies suggest continuous fibre reinforced parts achieve significantly increased specific strength, stiffness and toughness (Namiki et al., 2014, Van Der Klift et al., 2015). One drawback of depositing continuous fibre reinforcement during the layered manufacturing process is that the fibres are confined to the build layers, preventing true three dimensional reinforcement.

Recent research has shown that designing reinforcement channels into AM parts, and adding continuous reinforcement in a post-build process, dramatic increases in mechanical properties are achievable regardless of the build orientation of the part (Brooks and Molony, 2016, Brooks and Molony, 2015). This method, briefly explained in the next section, also has the advantage of working with all AM technologies. Subsequently these types of parts will be referred to as reinforced FFF parts.

## 1.1 Reinforced FFF parts

The aim of this methodology is to design channels within the parts that may be filled with load bearing uniaxial continuous reinforcement. The design process can be summarised according to Figure 1.



**Figure 1:** Schematic of the design process.

In this process the load carrying material is assumed to be the reinforcement, whilst the printed part is considered a preform that holds the reinforcement in place. Assuming the reinforcement is much stiffer than the polymer part material ( $E_r \gg E_m$ ) it will take a proportionately higher percentage of the load, as demonstrated by applying the rule of mixtures to the Voigt model for axial loading [8].

$$E_c = \sigma_c / \varepsilon_c = \frac{(1-f)\sigma_m + f\sigma_r}{(\sigma_r/E_r)} = (1-f)E_m + fE_r \quad \text{Equation (1)}$$

The reinforcement design guidelines were developed in parallel with experimental testing and can be found in previous works (Brooks and Molony, 2016, Brooks and Molony, 2015). Figure 2 shows the outcome of applying the design methodology to a pulley housing.

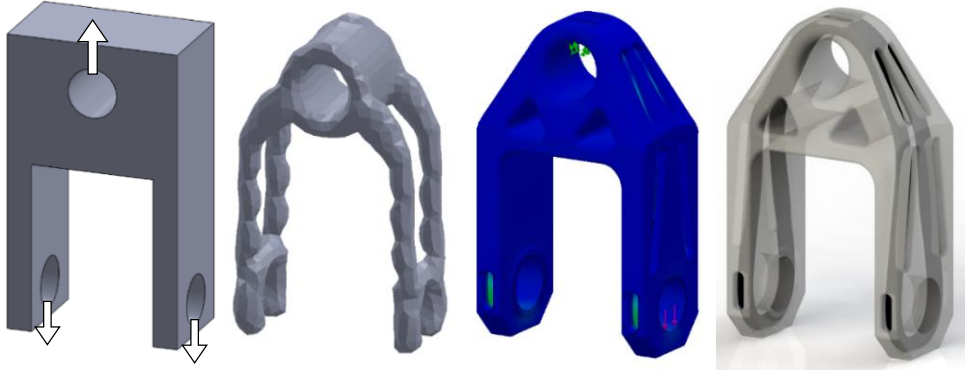


Figure 2: Evolution of the reinforced pulley from left to right: volumetric design space, topological optimisation, FEA of composite, final iteration after first physical tests.

Figure 3 shows the load-displacement curves for PLA pulley housings from a previous study (Brooks and Molony, 2016) with and without carbon fibre reinforcement with a strain rate of 2.5 mm/min. The reinforcement resulted in a 4,689% increase in tensile strength and a 2,212% increase in elongation to failure over the unreinforced part. The reinforced part exhibited steady deformation around the holes with minor cracks forming in the polymer/resin at around 2 mm of elongation (3.3% strain). Final failure of the reinforcement occurred near the holes.

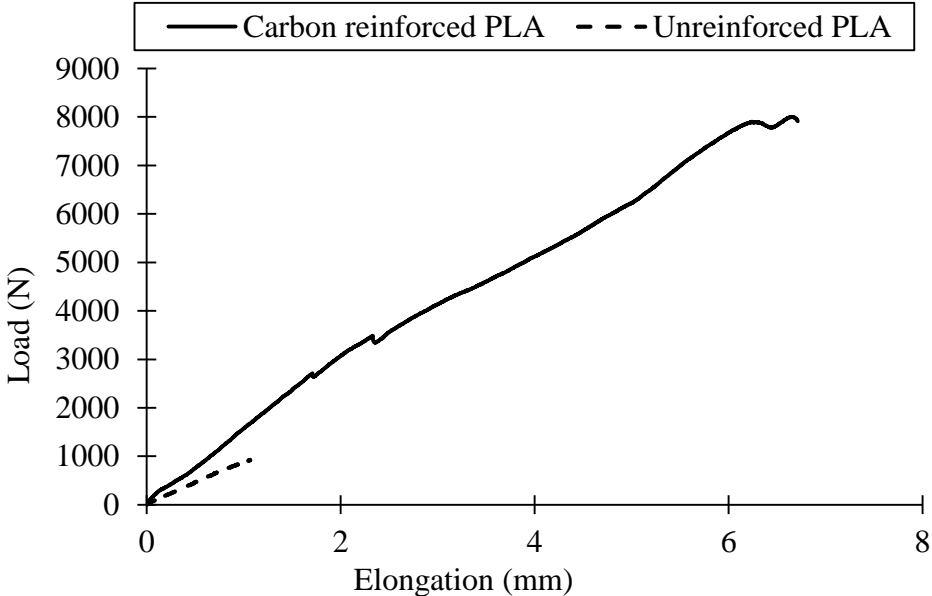


Figure 3: Load-elongation curves for PLA pulley housings with and without carbon reinforcement.

Many questions remain as to how the reinforced parts will perform in a variety of loading conditions and how repeatable the manufacturing process is. The aim of this study is to further investigate the tensile and low cycle fatigue failure of these parts for a variety of strain rates.

In order to provide a base for the interpretation of the results a short review of current literature into the failure of FFF parts and carbon fibre reinforced plastics (CFRP) is given below.

## **1.2 Failure of FFF parts**

There have been numerous studies into the tensile and compressive strength of FFF parts (Afrose et al., 2014, Ahn et al., 2002, Gardan and Schneider, Hambali et al., 2012, Montero et al., 2001, Rodriguez et al., 2000, Rodríguez et al., 2003, Sood et al., 2010, Tymrak et al., 2014, Villalpando et al., 2014, Ziemian et al., 2012, Bellehumeur et al., 2004, Sun et al., 2008). These studies found a wide range of factors impact on the strength of the parts including: material, extrusion temperature, layer heights, infill strategy, infill density, infill angle, number of shells, road width, air gap, strain rate, sample geometry and sample size. The variability in the way FFF parts are printed makes it difficult to directly compare results between the studies. However some commonly observed relationships are: higher infill densities lead to higher part strengths, longitudinal fill patterns are stronger than transverse fill patterns and parts built in the x-y plane (horizontally) are much stronger than parts built in the z or vertical plane. The most common tensile failure modes are layer delamination, fibre delamination or tensile fibre (also known as road, filament or bead) failure.

Failure due to fatigue or impact loads have received less attention. Recent work into the fatigue of ABS and PLA FFF parts revealed logarithmic S-N curves where lower loads resulted in higher cycles to failure (Afrose et al., 2015, Lee and Huang, 2013, Ziemian et al., 2015). Infill angle and build orientation were found to have the similar effects on fatigue life as those found in tensile tests. Impact testing of FFF parts also confirms anisotropic material properties with longitudinal infill patterns and higher infill densities having superior strength and impact resistance over transverse infill patterns and lower infill densities (Es-Said et al., 2000, Sood et al., 2010).

## **1.3 Failure of CFRP parts**

Due to the importance of carbon fibre composites in safety-critical industries such as transportation, the tensile failure modes of fibre reinforced composites have been studied extensively (Bhat et al., 2008, Hashin and Rotem, 1973, Mallick, 2007). The dominant tensile failure modes of CFRPs are fibre pull out, fibre/matrix fracture and interlayer delamination (Mallick, 2007, Zweben, 1968, Batdorf, 1982).

Unidirectional CFRPs are known to have excellent high cycle fatigue (HCF) properties (Hashin and Rotem, 1973, Harris, 2003, Mallick, 2007, Harik et al., 2002). Damage accumulation is relatively slow with few fibres breaking in the early cycles. Over time small cracks and voids in the matrix grow and coalesce leading to matrix failure and subsequent fibre fracture. Carbon fibre composites with thermosets are often found to have superior fatigue life than thermoplastics due to higher fibre bond strength (Harris, 2003).

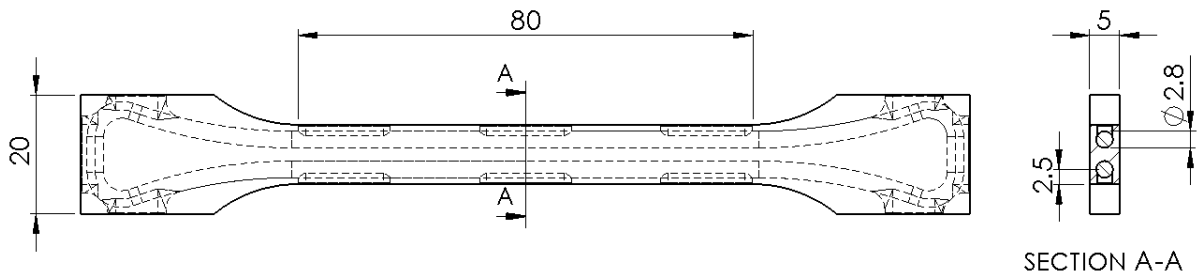
Deterioration of mechanical properties of CFRPs can be severe when subjected to large low cycle fatigue (LCF) loads. High levels of strain result in a high number of fibre breakages in the early cycles. While HCF of unidirectional composites are considered in many structural designs (e.g. shafts, flywheels beams etc.), the LCF limit is considered in the reliability estimates for safety, insurance risks and life cycle costs (Harik et al., 2002).

## 2. METHOD

This section outlines the method for the tensile and LCF testing of conventional and reinforced FFF parts. A dog bone sample shape was chosen to allow for better comparison with previous studies of unreinforced and reinforced AM parts.

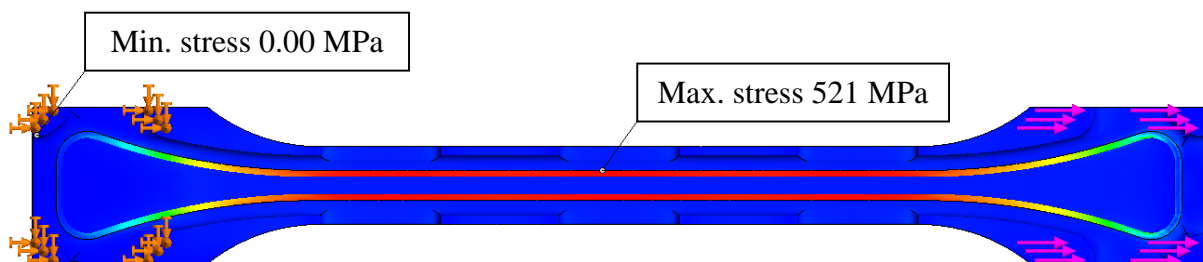
### 2.1 Specimen design

The dog bone (DB) specimens have been designed to comply with the BS 2782-3: 320C. This geometry was chosen to allow for the slight increase in thickness required for the reinforcement channel. The reinforcement channel is a continuous loop aligned with the direction of pull in the narrow section (Figure 4). Access holes are positioned around the sides of the specimens to allow the carbon fibre tows to be threaded. The unreinforced specimens share the same geometry but with the reinforcement channels and access ports removed.



**Figure 4:** Dog bone (DB) geometry showing reinforcement channels.

A static finite element analysis of the design was carried out as a preliminary check of the design. One tab of the sample was fixed while a 1000 N longitudinal load was applied to the opposite tab. The cross-section of the composite carbon fibre reinforcement was calculated to be 25% of the channel cross-section, based on two loops of 12K carbon fibre and a 60% volume fraction. The material properties for PLA and 0° carbon fibre composite were assumed to be isotropic with ideal bonding between the two. Figure 5 shows a cross-section of the FEA stress distribution. The higher stiffness of the reinforcement results in high levels of stress contained within the reinforcement while the PLA experiences negligible stress.



**Figure 5:** FEA stress distribution of the centre of a reinforced sample showing the highly loaded carbon fibre reinforcement.

The maximum stress of 521 MPa lies in the narrow part of the sample and is significantly lower than the ultimate tensile stress of 0° single tow carbon fibre composites which is approximately 2950 MPa.

## 2.2 Manufacture

All samples were printed with eSUN natural PLA filament on a MakerGear M2 with 0.15 mm layer heights, 3 solid shell layers and  $\pm 45^\circ$  rectilinear infill. The reinforced samples have a higher surface area and because the parts are printed with solid shells they weigh significantly more than the unreinforced samples, if equal infill densities are used. For this reason the unreinforced samples were printed with higher infill densities in order to mitigate the variation in sample weights.

High density reinforced DB samples were also printed to allow a comparison between reinforced parts with high and low infill densities. In addition, pulley housings as shown in section 1.1 were printed to see if the results from the dog bones are transferrable to parts with significantly different geometries. Table 1 summarises the build variations between the sample groups. Note that the reinforced DB with 25% infill contained more PLA than the unreinforced DB with 50% infill.

Table 1. Tensile and fatigue sample properties.

Sample group	Infill density (%)	Weight (g)				FFF build orientation
		PLA	Carbon fibre	Epoxy	Total	
Unreinforced DB	50	7.20	-	-	7.20	Horizontal
Reinforced low density DB	25	8.41	0.50	1.69	10.6	Horizontal
Reinforced high density DB	90	9.91	0.50	1.69	12.1	Horizontal
Reinforced pulley	25	13.70	0.43	0.86	15.0	Vertical

Tansome 12k H2550 fibre tow was threaded through the reinforcement channels twice resulting in approximately 500 mg of carbon fibre for each DB sample and 431mg for the pulley samples. Low viscosity epoxy laminating resin (EL2 from Easy Composites™) was used to bond the reinforcement within the channels. Excess resin was then allowed to drain from the part before being cured in an oven at approximately 50°C.

## 2.3 Testing

All samples were tested on a Testometric FS100SCCT universal testing machine. At least three samples were used for each combination of load and strain rate. The test schedule is shown in table 2.

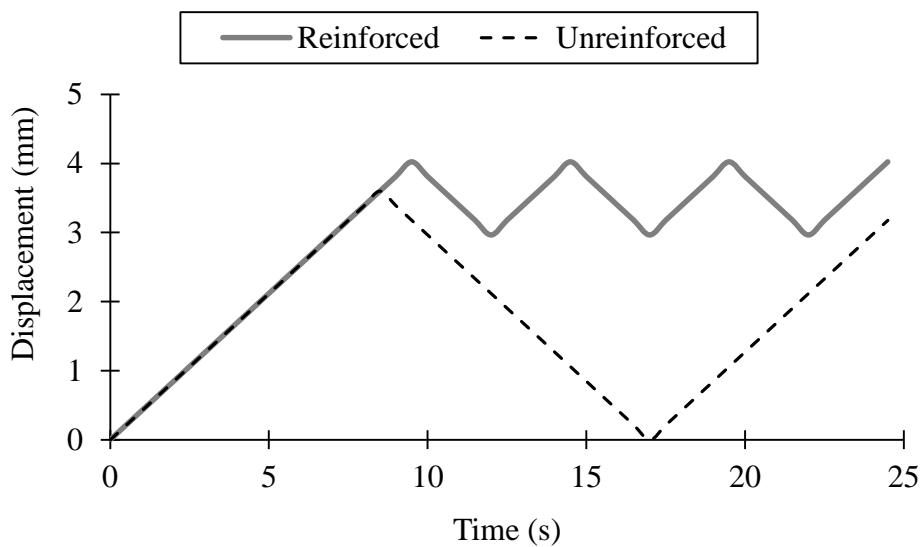
Table 2. Test schedule with strain rates and percentage of ultimate tensile load (UTL) combinations for each sample group.

Sample group	Strain rate		
	25.4 mm/min	127 mm/min	254 mm/min
	% of Ultimate tensile load		
Unreinforced DB	100, 80	-	100, 80
Reinforced low density DB	100, 90	100, 85	100, 90, 85, 80
Reinforced high density DB	90	-	-

Reinforced pulley	-	-	100, 90, 80
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The tensile tests were carried out first to determine an average ultimate tensile load (UTL) for each strain rate.

The maximum load for the unreinforced LCF tests was 0.8UTL with a minimum load of zero. The maximum load for the reinforced LCF tests varied between 0.8 and 0.9UTL with an alternating load of 0.2UTL. The lower alternating load for the reinforced samples was required to reduce the cycle time of the relatively long-lived composite samples. Figure 6 shows a typical displacement time curve for a reinforced and unreinforced LCF sample including the initial ramp up phase. The actual time taken for each cycle varied with the maximum force being tested in each sample group. For each test, data was recorded for force (N), displacement (mm), and time (s).



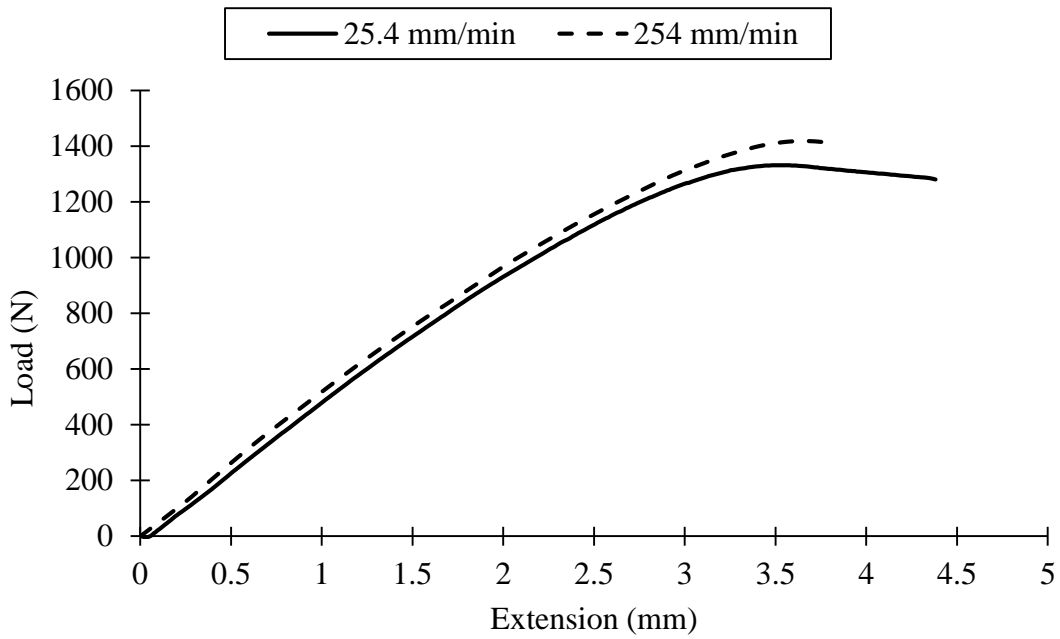
**Figure 6:** Displacement profile for samples with a 25.4 mm/min strain rate. Total cycle time varies for each cycle.

### 3. RESULTS

#### 3.1 Unreinforced FFF samples

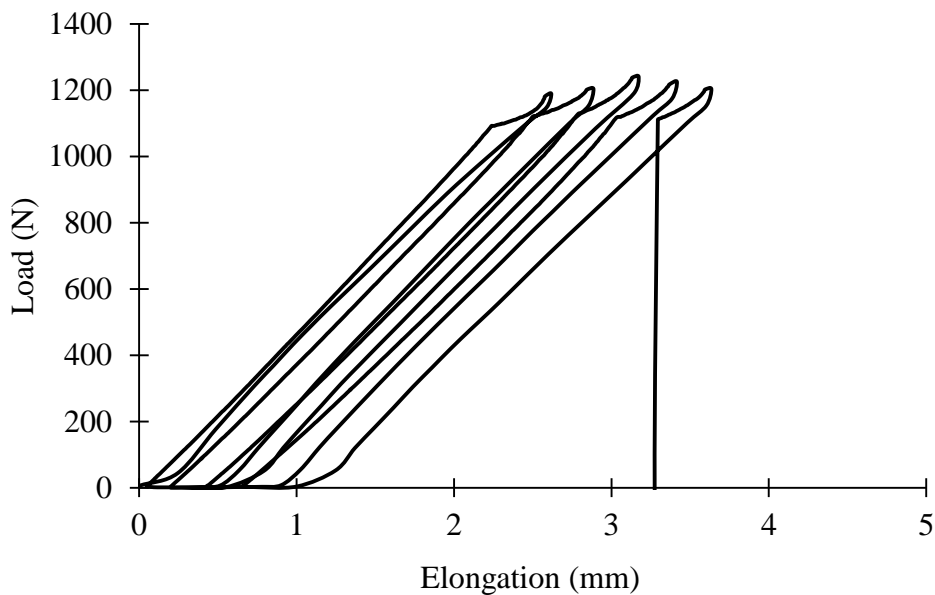
The unreinforced PLA tensile samples produced deformation curves with little plastic deformation which is typical for hard brittle polymers. Figure 7 shows force/elongation curves for strain rates of 25.4 and 254 mm/min. The faster strain rate was found to result in slightly higher UTLs but lower elongation to failure.





**Figure 7:** Typical load/elongation curves for unreinforced samples pulled at 25.4 and 254 mm/min.

The average UTL, elongation to failure and nominal strain energy for samples at both strain rates are shown in Table 3, along with their respective standard deviations. The nominal strain energy was calculated by summing the trapezoidal areas under adjacent data points and dividing by the nominal volume of the samples narrow section. The samples pulled at the lower strain rate had higher nominal strain energies and much higher cycles to failure. Figure 8 shows a typical load/elongation curve for a LCF sample with a maximum load 0.8UTL and a strain rate of 254 mm/min. All LCF samples showed characteristic hysteresis loops shifting along the elongation axis until final failure.



**Figure 8:** Typical load/elongation curve for a sample with 254 mm/min strain rates.

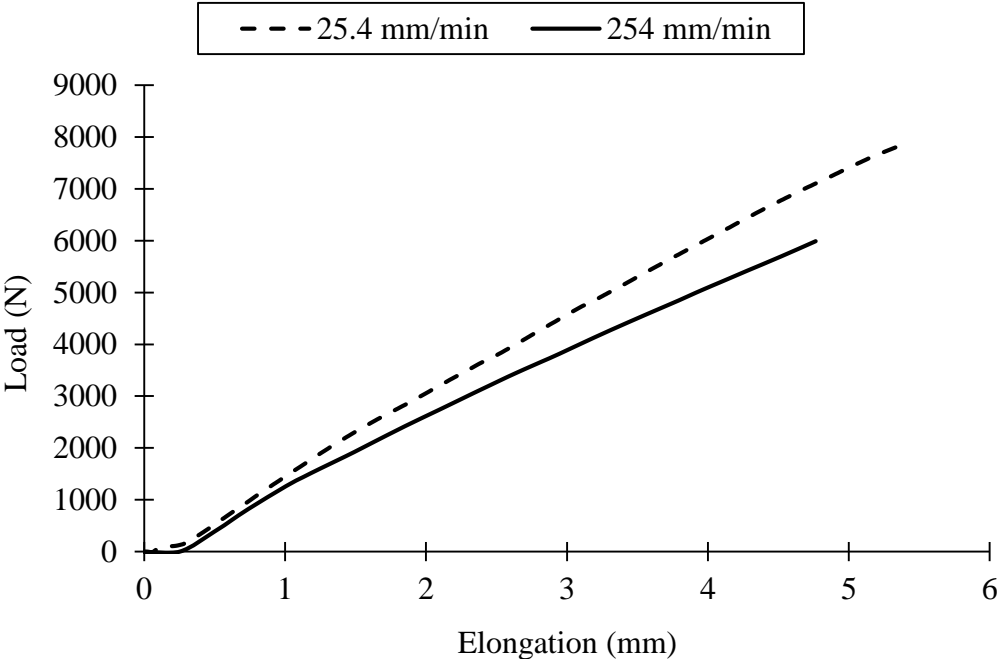
The UTL, elongation to failure and nominal strain energy data varied with standard deviations from 1.4 to 10%. The number of cycles to failure varied considerably with standard deviations over 30%.

**Table 3.** Average ultimate tensile load, elongation to failure, strain energy, and cycles to failure for tensile and LCF unreinforced DB samples with corresponding standard deviations in %.

Strain rate mm/min	Tensile test			LCF 80% UTL	
	Average UTL (N)	Average Elongation (mm)	Nominal strain energy (kJ/m <sup>3</sup> )	Average cycles to failure	Average elongation at failure (mm)
25.4	1273 ± 3.0%	4.18 ± 4.0%	877 ± 7.3%	55.2 ± 30%	2.87 ± 5.5%
254	1423 ± 1.4%	3.73 ± 4.1%	778 ± 3.5%	8.00 ± 47%	3.67 ± 9.9%

### 3.2 Reinforced FFF samples

The reinforced tensile samples failed at significantly higher loads than the unreinforced samples with modest increases in elongation to failure (Figure 9). Higher strain rates were found to lead to lower UTLs, elongation to failure and nominal strain energies.



**Figure 9:** Load/elongation curves for reinforced samples pulled at 25.4 and 254 mm/min.

In most cases the only visible evidence of damage accumulation before sudden fracture was crazing of the PLA near the ends of the access holes. Figure 10 a) shows a fractured sample after a high strain rate tensile test whilst Figure 10 b) shows low strain rate fatigue failure. The high strain rate resulted in the PLA rupturing as the curved reinforcement located in the lower tab straightened. This failure mode was not predicted by the static FEA due to the assumption of ideal bonding. The failure shown in Figure 10 b) is characteristic of the majority of LCF failures seen in this study with cracks forming in the PLA near the access holes, gradual delamination of the reinforcement from the PLA and then simultaneous fracture of the PLA and carbon fibre/epoxy.

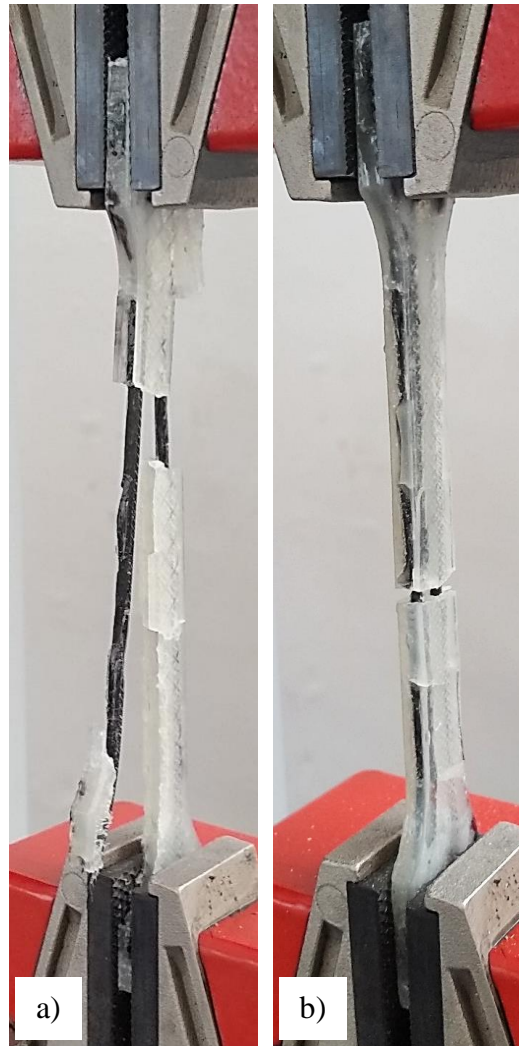


Figure 10: a) Sample after 254 mm/min tensile test. b) Sample after 25.4 mm/min LCF test.

Table 4 summarises the average UTL, elongation and nominal strain energies for the reinforced sample tensile tests.

Table 4. Average ultimate tensile load, elongation to failure, strain energy, and cycles to failure for tensile and LCF unreinforced DB samples with corresponding standard deviations in %.

Strain rate mm/min	Tensile test		
	Average UTL (N)	Average Elongation (mm)	Nominal strain energy (kJ/m <sup>3</sup> )
25.4	6593 ± 14%	5.27 ± 9.8%	4648 ± 21%
254	4496 ± 38%	4.61 ± 18%	3341 ± 17%

A direct comparison between the 0.8UTL reinforced and unreinforced LCF samples shows the reinforced samples life was 428 times greater (on average), whilst supporting an extra 3073 N tensile load.

Figure 11 shows the load/cycle graph for LCF samples with strain rates of 25.4 and 254 mm/min. Each point represents an average of at least 3 samples cycled to failure. A logarithmic relationship, with a relatively high R<sup>2</sup> value of 0.808, was found between load and cycles to failure for samples strained at 254 mm/min.

Samples strained at 25.4 mm/min with 0.9UTL had two orders of magnitude more cycles to failure than samples strained at 254 mm/min with 0.9UTL. This shows the LCF life of reinforced FFF parts are highly strain rate dependant.

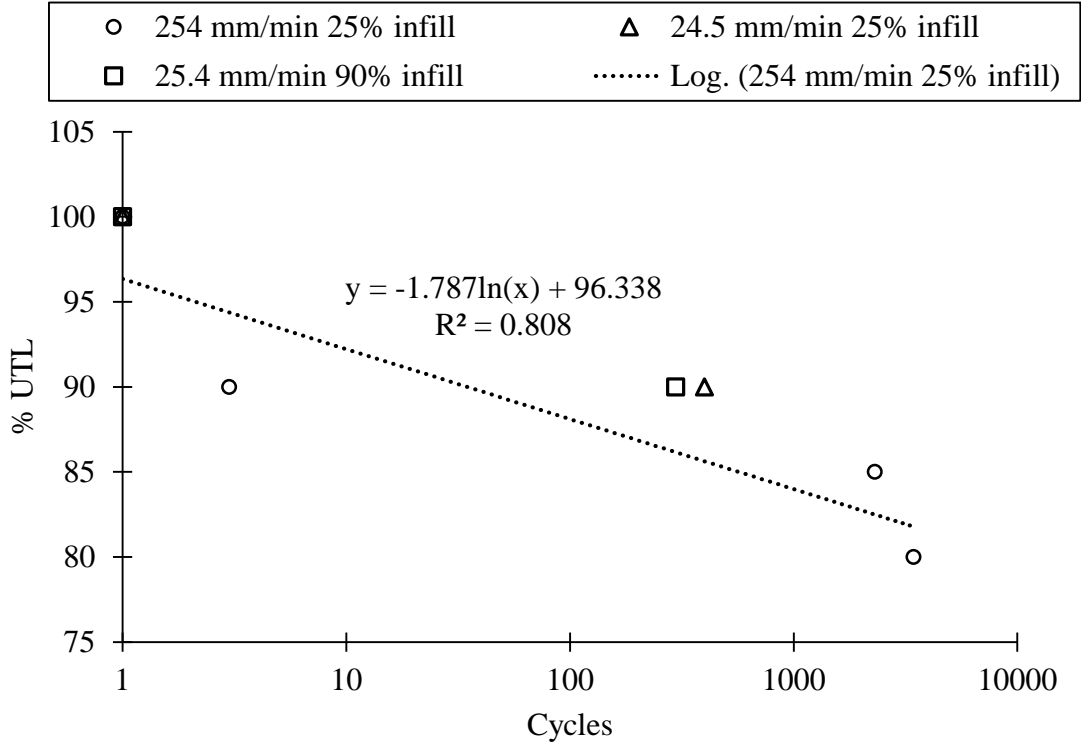


Figure 11: LCF life data for reinforced FFF parts with various normalised loads and strain rates. The stress ratio, R, is 0.2.

No significant correlation was found between the tensile strength, elongation to failure, strain energy and FFF infill density.

Table 5. Average cycles to failure and elongation to failure, for LCF unreinforced DB samples.

Strain rate (mm/min)	Average low cycle fatigue test data					
	80% UTL		85% UTL		90% UTL	
	Cycles to failure	Elongation at failure (mm)	Cycles to failure	Elongation at failure (mm)	Cycles to failure	Elongation at failure (mm)
25.4*	-	-	-	-	400	4.80
25.4**	-	-	-	-	297	4.74
254*	3435	4.41	2306	5.32	3	5.05

\* Infill density of 25%. \*\*Infill density of 90%

### 3.3 Reinforced Pulley Housing

Three pulley housings were printed and reinforced using the methodology outlined in section 2. Tensile tests were carried out on two of the pulleys to determine an average UTL. A third sample was then tested using a LCF load profile, but failed at the start of the first relaxation phase. It appears inertia of the cross-head resulted in a maximum load higher than the specified 0.85UTL. The load/elongation profiles for all three samples can be seen in figure 12.

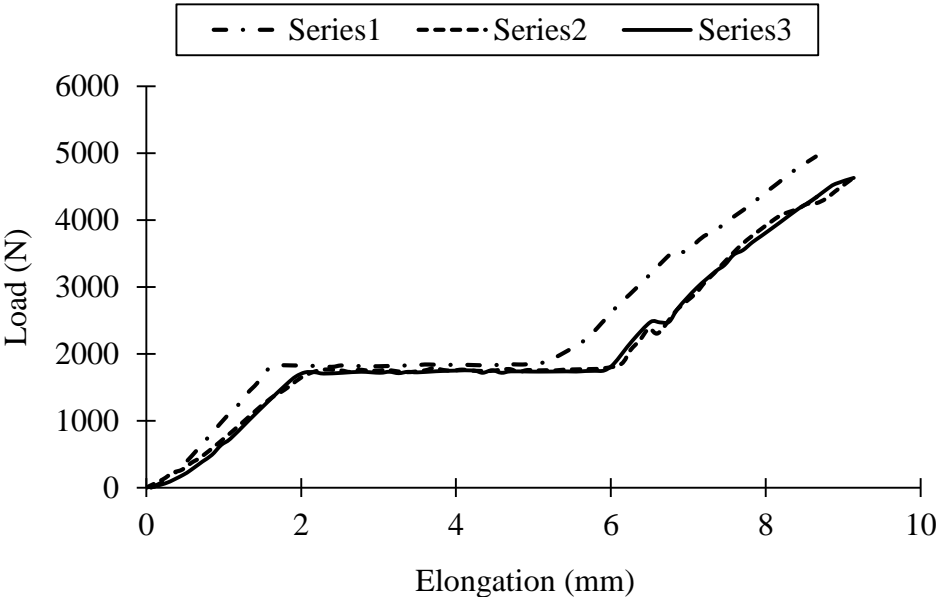


Figure 12: Load/elongation curves for reinforced pulley housings at 254 mm/min.

The load profiles for the pulley housings show a constant load phase which spans approximately 45% of the total elongation. This feature was not observed in any of the DB load curves or the previous pulley tensile tests carried out at 2.5 mm/min. The average UTL for the pulleys was found to be 4746 N which is similar to the UTL of the reinforced samples.

The PLA material was found to crack near access holes and preferentially fracture between build layers (Figure 13). The composite carbon fibre reinforcement failed with a ruptured appearance.

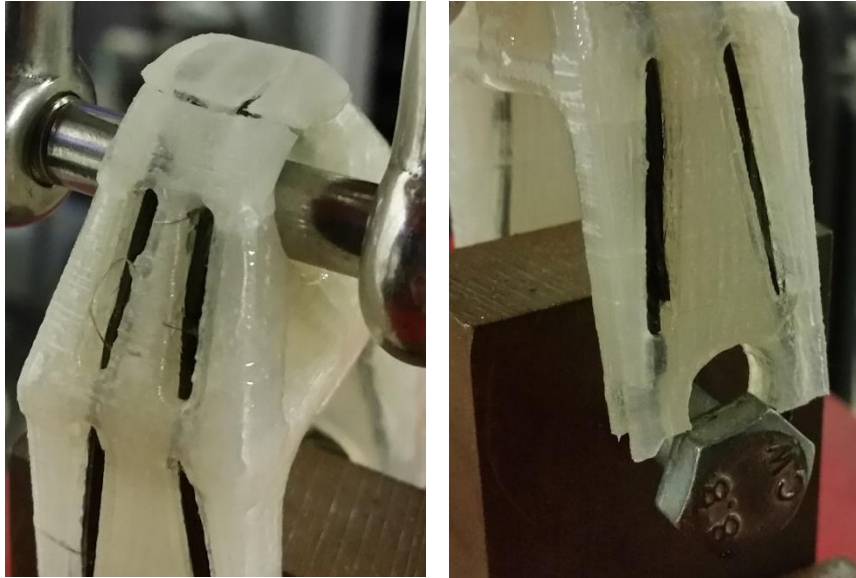


Figure 12: PLA and reinforcement fractures after high strain rate tensile loading.

## 5. DISCUSSION

PLA FFF parts were found to have short LCF lives with brittle fracture occurring on the order of 10 cycles at 0.8UTL. Reinforcing FFF parts with 4.7% carbon fibre by mass, increased the ultimate tensile strength by a factor of 4 (25.4 mm/min strain rate) and the LCF life by a factor of 428 (254 mm/min strain rate). In the majority of cases the reinforced LCF samples fractured in the narrow section of the sample near an access hole. Initial cracks near the access holes in the first few cycles led to progressive delamination of the reinforcement from the inner surface of the channels. Incremental separation of the reinforcement from the PLA was clearly visible in the longer LCF tests. This separation coupled with growing cracks in the PLA eventually lead to fast fracture. The access holes proved to be significant stress concentrators, suggesting new methods of introducing the fibres are needed.

Variation in the cycles to failure for all LCF samples was found to be far greater than the variation in elongation to failure. Strain based failure criteria could offer a more accurate failure criteria than cycle based approaches.

The pulley housing load/elongation curves at high strains had remarkably different geometries from the low strain rate curves in Figure 3. They also differed from the DB samples which had near linear stress/strain profiles with similar strain rates. This suggests that the load/elongation relationship for reinforced FFF parts depends on both part geometry and strain rate. It is likely that dynamic loading of the pulley caused previously unseen rapid plastic deformation of the PLA until the reinforcement tightened and continued to resist elongation. This is supported by the fact the pulley had a strain at failure of approximately 18% compared to 4.7% for the DB sample at the same strain rate. An extensive study is required to further understand the interrelationship between strain rate and geometry.

The average UTL for the pulley housings was found to be comparable to the DB samples with similar strain rates. This is an important result as it shows that if equivalent quantities of carbon

fibre are used and they are aligned with the 1<sup>st</sup> principle stresses then you can expect similar UTLs regardless of the overall part geometry.

## 6. CONCLUSIONS AND RECCOMENDATIONS

The geometric complexity offered by AM allows for the design of parts with complex internal channels which may be filled with continuous fibre reinforcement. By routing the channels through regions of high Von Mises stress and aligning them with the 1<sup>st</sup> and 2<sup>nd</sup> principal stresses it is possible to gain the maximum advantage from the mechanical properties of the fibres.

This study investigated the tensile and LCF failure characteristics of unreinforced and reinforced FFF PLA parts for a range of strain rates and loads. The main findings are summarised as follows:

- The small (4% by mass) addition of carbon fibre to FFF DB samples was found to increase tensile strength by 400% and LCF life by 42,800%.
- Reinforced FFF parts exhibit logarithmic load-cycle relationships.
- High strain rates result in reduced LCF life and unpredictable failure modes.
- In all cases elongation to failure was found to vary less than cycles to failure.
- Access ports used to thread the carbon fibre into the parts act as stress concentrators, initiating crack formation and separation of the reinforcement from the PLA.
- The near linear load/elongation relationship of the DB samples was not replicated by the pulley housing at high strain rates.
- The UTL values for the DB samples were comparable to the pulley values.

Further studies are required to test other load types such as bending, torsion, impact loads, HCF and the effects of scale. Continuous fibre reinforced AM parts would also benefit from:

- Automated design of the reinforcement channels from FEA data.
- Improved methods of introducing the reinforcement.
- Cost analysis and eco-audits to compare the economics and environmental benefits of AM polymer composite parts with other manufacturing methods.
- The application of engineering coatings and metallic inserts to improve thermal resistance, friction and wear.
- The integration of condition monitoring capabilities.

Research is ongoing to test whether coatings can be used to significantly improve surface properties. In addition novel internal structures and infills are being investigated for their ability to improve the parts thermal properties.

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