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Stratified Spectral Mixture Analysis of Medium Resolution Imagery for Impervious Surface Mapping

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8 Abstract

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9 Linear spectral mixture analysis (LSMA) is widely employed in impervious surface estimation, especially for estimating impervious surface abundance in medium 10 spatial resolution images. However, it suffers from a difficulty in endmember 11 selection due to within-class spectral variability and the variation in the number and 12 the type of endmember classes contained from pixel to pixel, which may lead to over 13 or under estimation of impervious surface. Stratification is considered as a promising 14 process to address the problem. This paper presents a stratified spectral mixture 15 analysis in spectral domain (Sp SSMA) for impervious surface mapping. It 16 categorizes the entire data into three groups based on the Combinational Build-up 17 Index (CBI), the intensity component in the color space and the Normalized 18 Difference Vegetation Index (NDVI) values. A suitable endmember model is 19 developed for each group to accommodate the spectral variation from group to group. 20 The unmixing into the associated subset (or full set) of endmembers in each group can 21 make the unmixing adaptive to the types of endmember classes that each pixel 22 actually contains. Results indicate that the Sp SSMA method achieves a better 23 performance than full-set-endmember SMA and prior-knowledge-based spectral 24 mixture analysis (PKSMA) in terms of R, RMSE and SE. 25

26 Key words—Impervious surface, Stratification, Spectral mixture analysis, CBI

27 **1. Introduction**

Impervious surface is defined as any area consisting of constructed surface which 28 water cannot infiltrate to reach the soil (Yang et al, 2010; Weng, 2012), such as roads, 29 roofs, and parking lots. It not only serves as a key indicator of the degree of 30 urbanization, but also affects in the micro-ecosystem change (Wang et al, 2015). The 31 32 increasing replacement of nature landscape by impervious surface leads to the change of hydrological character (White & Greer, 2006; Xian et al, 2007; Du et al., 2015), the 33 generation of heat island effects (Kato & Yamaguchi, 2007; Yuan & Bauer, 2007; 34 Coseo & Larsen, 2014), deterioration in water quality (Conway, 2007) and other 35

detrimental effects. Therefore, it is essential to monitoring impervious surface
distribution timely and accurately to ensure urban development is sustainable (Wu &
Murray, 2005; Du & Du, 2014).

Remote sensing technology has become an important method, and may be the 39 only viable way, to effectively extract impervious surface due to its high efficiency 40 41 and low cost with large coverage (Yang et al, 2010; Lu & Weng, 2006). Various studies have been conducted for impervious surface mapping, with images from a 42 large range of satellite sensors and a variety of data sources, including MODIS images 43 with coarse spatial resolution (Yang & Lunetta, 2011; Deng & Wu, 2013), Landsat 44 TM/ETM+ and ASTER imagery (Hu & Weng, 2009; Sexton et al, 2013) with 45 moderate spatial resolution, and IKONOS and QuickBird data (Lu & Weng, 2009; 46 Zhou & Wang, 2008) with high spatial resolution. In addition to the optical remote 47 sensing data, some other types' data, such as nighttime photography (Kotarba & 48 Aleksandrowicz, 2016), Synthetic Aperture Radar (SAR) imagery (Zhang et al, 2016; 49 Zhang et al, 2014) and open social data (Hu et al, 2016), have also been studied on 50 their application to impervious surface estimation in recent years. Among them, 51 medium spatial resolution images might be a better choice for the urban impervious 52 surface mapping, because they provide a good trade-off among coverage, price, and 53 quality. 54

However, due to the heterogeneity of urban land covers and the limitation in 55 spatial resolution, the presence of mixed pixels has been recognized as a major 56 problem in the analysis of medium spatial resolution images (Weng, 2012). Several 57 unmixing methods have then been applied for impervious surface extraction, 58 including linear spectral mixture analysis (LSMA) (Weng et al, 2009; Hu & Weng, 59 2008; Yang & He, 2017), artificial neural network (ANN) (Mohapatra and Wu, 2008), 60 regression analysis (Yang et al, 2003; Yang & Liu, 2005; Kaspersen et al., 2015) and 61 regression trees (Huang & Townshend, 2003; Deng & Wu, 2013). Yet LSMA is still 62 the most popular approach due to its simplicity and physically-based description of 63 the fractions of different land covers (Small & Milesi, 2013; Burazerovic et al, 2013). 64

While LSMA and LSMA based methods are easy to use in estimating impervious 65 surface, several problems still exist. It has been found that impervious surface tends to 66 be overestimated in the areas with small amounts of impervious surface, but is 67 underestimated in the areas with large amounts of impervious surface (Weng, 2012; 68 Lu and Weng, 2006). The similarity in spectral properties between impervious and 69 pervious surface, especially impervious surface and soil, can be one of the main 70 reasons for underestimation in urban area and overestimation in pervious area. 71 Another problem is the difficulty in selecting endmembers due to within-class spectral 72 variability (Foody et al, 1997). It should be noted that the differences in type, 73 geometry and illumination etc. lead to the huge differences in term of spectral 74 characteristics of impervious surface. Therefore, using one endmember to represent 75 all types of impervious surfaces is often found problematic (Weng et al, 2008). The 76 performance of LSMA can also be reduced if every pixel in the image is unmixed into 77 a fix set of endmembers, where some pixels may only contain a subset of 78 endmembers. 79

Stratification is considered as a promising process to solve these problems. In 80 (Lu & Weng, 2004), stratification of a whole scene into subareas with similar 81 landscape structures is suggested to improve impervious surface mapping. Several 82 studies (Wu & Murray, 2003; Zhang et al, 2014; Small, 2001; Somers et al, 2009) have 83 attempted to employ different endmember class sets for urban and rural areas. 84 85 However, the endmembers sets applied to each subarea are extracted from the entire image scene. The weakness of this treatment is the spectral variability in different 86 subsets is not considered. The endmembers, which are selected at the extreme of an 87 n-dimensional scatter plot of the entire image may be less representative as the pure 88 pixels in each subset (Deng & Wu, 2013). The current methods stratify a remote 89 sensed image into urban and rural areas through spatial information, such as texture 90 and road density information (Zhang et al, 2014; Liu & Yang, 2013). The overlooked 91 the spectral information would result in mis-estimation of land cover abundances. 92

In this study, we address the above mentioned problems and propose a stratified 93 spectral mixture analysis in spectral domain (Sp SSMA) for impervious surface 94 mapping. We clipped an image data set into three groups to reduce the within class 95 variability in each subgroup based on three spectral character components, namely 96 Combinational Build-up Index (CBI)(Sun et al, 2015), Normalized Difference 97 Vegetation Index (NDVI) (Rouse et al, 1974) and color intensity. Then, endmembers 98 99 are selected from each group independently rather than from the entire image to cope with the within class variability. An endmember set with different types and numbers 100 is applied in each group to make it more adaptive. Impervious surface fractions are 101 estimated by LSMA and the results of the three subgroups are combined to produce a 102 103 complete map.

The remainder of this article is structured as follows. The second section presents the methodology of Sp_SSMA, including the stratification, the selection of endmembers and the procedures for deriving impervious surface abundance. The third section introduces the study areas and remotely sensed data, including data preprocessing. The comparative results and discussions are reported in Section 4. Finally, conclusions are provided in Section 5.

110 **2. Methodology**

Based on the definition, impervious surface is a unifying theme. However it 111 consists of a number of artificial features which have different spectral profiles in 112 general. Figure 1(a) illustrates the mean spectral values of different impervious 113 surface and other major land cover classes based on the pure pixels selected from a 114 Landsat TM image. It indicates that not only impervious surfaces consist of different 115 structures, colors, and materials, vegetation and soil also show great spectral 116 differences within each of them. Figure 1(b) is the corresponding grouped scatter 117 points of the sampled pixels in the feature space composed by the first two 118 components of minimum noise fraction (MNF1 and MNF2). We can see that the pure 119 pixels are not always located at the extremes of the scatter plot as it supposed to be 120 121 theoretically, due to the within-class variation of a land cover type. It also indicates

the spectral variability within several classes as well as the spectral confusion amongseveral land covers, especially between urban impervious surfaces and bare soil.

Therefore, simply extracting a single set of endmembers from the vertices in an n-dimensional scatter plot of an entire scene, like the treatment in (Powell, et al, 2007), is potentially less reliable because they cannot account for the considerable within-class variability (Rashed et al, 2003; Roessner et al, 2001). The similarity of spectral characteristics between impervious and pervious surface, especially bare soil, also prevent the SMA-based methods from achieving a promising result.

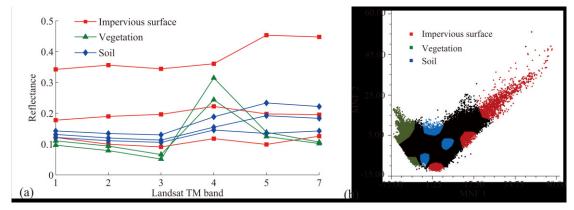
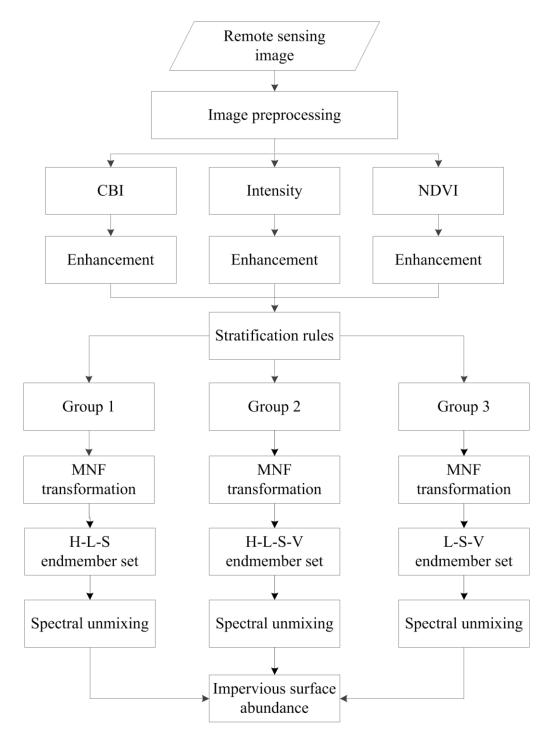


Figure 1 Reflectance of land feature endmembers (a) and the corresponding feature space representation of the firsttwo MNF components for Landsat TM reflectance image (b).

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To tackle this problem, we develop a stratified spectral unmixing method in 134 spectral domain (Sp SSMA). Three spectral feature components, CBI, intensity 135 component of intensity-hue-saturation (IHS) and NDVI, are utilized to partition the 136 entire data into three groups, named Group 1, Group 2 and Group 3. Each group is 137 processed independently, including endmember extraction and spectral unmixing, to 138 minimize the within class spectral variability and the confusion between some urban 139 features and non-impervious land covers. The major steps in Sp SSMA are described 140 141 in Figure 2.



- 142
- 143 Figure 2 Flowchart of the Sp_SSMA method.

144

145 2.1 Stratification

146 2.1.1 CBI calculation

147 CBI is a feature-extraction based spectral impervious surface index. It reduces

the original multi-/hyper-bands into three thematic-oriented features. They are the first
component of a principal component analysis (PC1), Normalized Difference Water
Index (NDWI) (Gao, 1996) and Soil Adjusted Vegetation Index (SAVI) (Huete, 1988),
to represent high albedo, low albedo and vegetation respectively. The features are
calculated using the following equations (Sun et al, 2015):

153
$$CBI = \frac{(PCI_{nor} + NDWI_{nor})/2 - SAVI_{nor}}{(PCI_{nor} + NDWI_{nor})/2 + SAVI_{nor}}$$
(1)

154 with

155
$$SAVI = \frac{(\rho_{NIR} - \rho_{RED})(l+L)}{\rho_{NIR} - \rho_{RED} + L}$$
(2)

$$NDWI = \frac{\rho_{GREEN} - \rho_{NIR}}{\rho_{GREEN} + \rho_{NIR}}$$
(3)

157 where ρ_{GREEN} , ρ_{RED} , ρ_{NIR} represent the reflectance value of GREEN, NIR and

SWIR bands, respectively. *L* is a correction factor ranging from 0 to 1. In this study, 0.5 is taken to form a vegetation image. PCI_{nor} , $SAVI_{nor}$ and $NDWI_{nor}$ are the normalized PC1, SAVI and NDWI respectively.

In CBI, impervious surfaces are highlighted with positive values, vegetation is represented with negative values while bare soil and mixed land cover types are associated with numerical values about zero. Qualitative and quantitative assessments of accuracy analysis, separability between impervious surface and soil at different spatial and spectral resolutions as well as comparison with other indices indicate that CBI is a promising and reliable urban landscape index for mapping impervious surface areas (Sun et al, 2015).

168 2.1.2 I calculation

The IHS color space can be regarded as a two-dimensional color vector and one intensity vector (Córdoba-Matson et al, 2010). That is to say, the spectral magnitude of a land feature mainly lies in the intensity component, which is expressed as

$$I=\sum_{i=1}^{n}\rho_{VIR-i}/n \qquad (4)$$

where ρ_{VIR-i} is the *i*th VIR band of a pixel, n is the total number of VIR bands. The

intensity value of the bright impervious surface tends to show the largest distinctionwith the background land features.

176 2.1.3 NDVI calculation

NDVI (Rouse et al, 1974) is an effective index to measure vegetation content
which employs the peak and valley reflectances at NIR and RED bands to form the
vegetation index (Huete, 1988). In this study, NDVI is utilized to make the distinction
of vegetation due to their high NDVI values. The NDVI is calculated using Eq. (5)

181 (Rouse et al, 1974).

 $NDVI = \frac{\rho_{NIR} - \rho_{RED}}{\rho_{NIR} + \rho_{RED}}$ (5)

183 where ρ_{RED} and ρ_{NIR} represent the reflectance values of GREEN, NIR and SWIR 184 bands, respectively.

185 2.1.4 Threshold selection

The threshold selection for stratification is crucial to delineate the biophysical distribution of the impervious surface from other land covers. In this study, a transformation (Liu et al, 2011) was utilized to improve the separability between different land cover types. The gray-scaled index images, namely CBI, I and NDVI, were enhanced by adopting Eq. (6) (Liu et al, 2011).

191
$$i_{enh} = \left(\frac{1}{\pi} \arctan[\lambda \pi (i_{nor} - \theta)] + 0.5\right) \sqrt{i_{nor}} \qquad (6)$$

192 Where i_{enh} is the enhanced index map, i_{nor} is the normalized index map, λ is a 193 sensitivity factor and θ is the coarse estimation of mean value of the target land 194 cover type, or more precisely impervious surface in CBI and I while vegetation in 195 NDVI.

The enhanced intensity maps are used to stratify the whole image. Otsu (Otsu, 197 1979) proposed a histogram-based threshold selection method that is suitable for separating an object from its background. We use this method to automatically select the threshold T for stratification. In Otsu's method (Otsu, 1979), a threshold T is selected to maximize

201
$$\tilde{o}^2(T) = \frac{(\mu\omega_1(T) - \omega_2(T))^2}{\omega_1(T)\omega_2(T)}$$
(7)

where $\omega_I(T) = \sum_{i=0}^{T} p_i$, $\omega_2(T) = \sum_{i=T+i}^{255} p_i$, $\mu = \sum_{i=0}^{255} ip_i$, and p_i is the probability of the gray level i. T_{CBI} , T_I and T_{NDVI} , the threshold of the enhanced CBI, I and NDVI

respectively, are obtained using Eq. (7) and used to stratify the image. Three groupsare defined as follows.

Group 1:
$$CBI_{enh} > T_{CBI}$$
, $I_{enh} > T_I$ and $NDVI_{enh} < T_{NDVI}$

207 Group 3:
$$CBI_{enh} < T_{CBI}$$
 and $NDVI_{enh} > T_{NDVI}$

208 Group 2:
$$((CBI_{enh} < T_{CBI}) \cap (NDVI_{enh} < T_{NDVI})) \cup ((CBI_{enh} > T_{CBI}) \cap$$

209
$$(I_{enh} < T_I) \cup ((CBI_{enh} > T_{CBI}) \cap (I_{enh} > T_I) \cap (NDVI_{enh} > T_{NDVI})),$$
 (i.e. is the

210 remaining region.)

211 2.2 Endmember selection

Endmember extraction is critical. In this study, endmembers were selected in

each group independently, rather than from the entire image, to achieve more adaptive 213 spectral characters. The endmember selection in each subset follows the usual 214 minimum noise fraction (MNF)-based procedure. Spectral feature spaces were 215 generated using the first three MNF components, and the typical pure pixels are those 216 located at the extreme vertices of the data cloud in the scatter plots. Endmembers of 217 218 the three sub-regions were indentified from the vertices of the scatterplots in each sub-scene independently. The extreme or less extreme pure pixels in the original 219 image located at the extreme points in different groups so as to balance the within 220 class variation and easy implement of extreme pixels selection. The number and type 221 of endmember sets in each sub-region is determined based on the corresponding 222 respective biophysical characteristics. 223

The combined criteria of Group 1 can make it reasonable to treat Group 1 data as 224 225 containing no vegetation component. That is to say, Group 1 is composed of impervious surface and soil with vegetation pixels masked out by intensity component 226 and NDVI. In contrast, the area of Group 3, which contains a low CBI value and high 227 NDVI value, is mainly composed of vegetation and soil, with small amount of low 228 albedo impervious surface. As for Group 2, impervious surface (high albedo and low 229 230 albedo), soil and vegetation form the land cover features. Therefore, different endmembers are defined for each Group as follows. 231

- Group 1: high-albedo, low albedo and soil (H-L-S).
- Group 2: high albedo, low albedo, soil and vegetation (H-L-S-V).
- Group 3: low-albedo, soil and vegetation (L-S-V).

235 2.3 Impervious surface estimation

236 The LSMA approach is physically based on the assumption that the spectrum for each pixel is a linear combination of all endmembers in the pixel (Wu, 2004) with the 237 proportions of the endmembers representing the percentage of the land feature. The 238 fraction image of each endmember is estimated through inversion of the linear 239 combination with the spectral proportions of the endmembers representing the 240 percentage of the land feature. LSMA was also under the assumption that no 241 interaction between the photons reflected by each component. With these assumptions, 242 a LSMA with full abundance constraints can be expressed as (Lu & Weng, 2006): 243

244
$$R_b = \sum_{i=1}^{N} f_i R_{i,b} + e_b$$
(8)

245 where

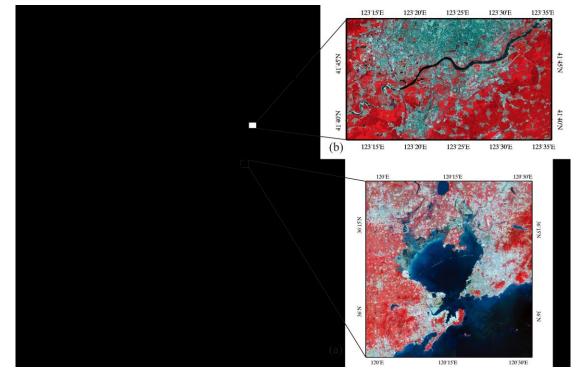
246
$$\sum_{i=1}^{N} f_i = 1 \land f_i \ge 0$$
 (9)

where R_b is a mixed pixel's reflectance at band b, N is the number of endmembers, $R_{i,b}$ is the reflectance of endmember i at band b, f_i is the fraction of endmember i, 249 and e_b is the residual error.

As high and low albedo endmembers both are associated to impervious surface, the final impervious surface fraction is calculated by summing the abundance of high and low albedo endmembers for each mixed pixel. Then, the impervious surface abundance in the three urban subsets was mosaicked to build the final regional impervious surface abundance map.

255 **3 Study area and data**

Multi-sensor data, namely Landsat TM and ASTER, with two study sites were investigated to test he proposed Sp_SSMA algorithm (Figure 3).



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Figure 3 The location of study area: (a)The false color image covering the Qingdao city, China, illustrated with
Landsat TM image (R: band 4, G: band 3, B: band 2), (b)The false color image covering the Shenyang city, China,
illustrated with ASTER image (R: band 3, G: band 2, B: band 1).

262 *3.1 Landsat TM imagery*

The first study area is an urban transect in the region of Qingdao, China. As shown in Figure 3(a), a scene of Landsat TM image acquired on July 15, 2009 was employed for this study, suggesting that a large diversity of land cover properties present within the study area. Different impervious surfaces, such as residential areas, mixed-use areas, commercial and industrial districts, are shown in the image. Non-urban land cover types include water bodies, green vegetation and bare soils.

The city of Qingdao is situated in the south of the Shandong Province, adjacent 270 to the Huanghai Sea (Figure 3(a)). As an important region in Eastern China, Qingdao 271 has seen rapid development. The annual GDP reached 869.2 billion Yuan in 2014, 272 with an increase of 8.0%, ranking first in Shandong Province and fourteenth out of 273 China's top 20 cities. The fast economic growth is accompanied by rapid urbanization, 274 275 causing transformation from nature environment to man-made surface. As for urban area, the historic town is located in the eastern part of the study area while the new 276 district mainly lies in the western part. The suburban area is dominated by forest land 277 while agriculture land located mainly in the northern part of the study area. 278

279 *3.2 ASTER imagery*

The second study area (Figure 3(b)), located in Shenyang, China, is a typical 280 281 heavy industrial area since early 1900s. Aster imagery was collected over the area on August 17, 2004. Shenyang is the provincial capital and largest city of Liaoning 282 Province, as well as an important heavy industrial base and a transportation hub in 283 Northeast China. Under the reform and open policies, Shenvang has experienced 284 sustained and high speed growth and urbanization since the late 1970s. After the 285 "revitalizing the old industrial bases in Northeastern China" strategy in 2003, 286 Shenyang was identified as the core of the new-industrialization zone for national 287 demonstration (Zhang et al, 2007). It is expected to offer a demonstration for China's 288 change in industrial and economic development mode. Under such circumstances, 289 Shenyang's urbanization will definitely continue to increase rapidly, and a more 290 complex landscape resulting from industrial transformation will be observed. 291

292 *3.3 Data preprocessing*

The Landsat TM image has six spectral bands (except the thermal band) with a spatial resolution of 30m. The ASTER image has 9 bands with different spatial resolutions (except the thermal bands), two visible bands, and one near infrared (NIR) band with the spatial resolution of 15 m, six short wavelength IR (SWIR) bands with 30m resolution. The 15m ASTER bands were resampled to 30m with the application of nearest-neighbor resampling algorithm.

Atmospheric correction was applied to neither of the images due to generally good weather condition. Radiation calibration was conducted prior to data processing. With the Landsat TM and ASTER reflectance images, water pixels were identified and removed with the help of unsupervised classification. Additionally, the Google Earth images acquired on July 22, 2009 and Oct 19, 2004 were used as ground reference data for accuracy assessment respectively.

306 4 Experimental Results and Discussions

307 *4.1 Experimental design*

To evaluate the performance of the proposed method for mapping impervious surface abundance and distribution, the corresponding Google Earth images, which were generated near the acquisition date of Landsat TM and ASTER images respectively, were used as the ground reference. The spatial resolution of Google Earth images in both study areas is 0.5 m and each pixel is then treated as pure pixel.

After obtaining the estimation for the actual imperviousness and estimated 313 imperviousness, three quantitative estimators were adopted to assess the accuracy of 314 impervious surface abundance modeled by Sp SSMA. They are correlation 315 coefficient (R), root mean square error (RMSE) and systematic error (SE). 316 Specifically, R means the statistical relationships between the estimated and actual 317 imperviousness, RMSE reflects the relative estimated errors of impervious surface 318 abundances, and SE measures the bias, an overall tendency of over- or 319 under-estimation. These three accuracy metrics can be calculated using Eqs. (11) to 320 (13) respectively as follows. 321

322
$$R = \frac{\sum_{i=1}^{N} (f_i - \overline{f})(\hat{f}_i - \overline{\hat{f}})}{\sqrt{\sum_{i=1}^{N} (f_i - \overline{f})^2 \cdot \sum_{i=1}^{N} (\hat{f}_i - \overline{\hat{f}})^2}}$$
(1)

$$RMSE = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (\hat{f}_i - f_i)^2}$$
(1)

324
$$SE = \frac{1}{N} \sum_{i=1}^{N} (\hat{f}_i - f_i)$$

325 where \hat{f}_i is the estimated impervious surface fraction of sample *i* using Sp_SSMA,

1)

2)

(13)

326 $\overline{\hat{f}}$ is the mean value of the samples; f_i is the true impervious surface proportion 327 derived from Google Earth of pixel *i*; and N is the number of samples.

In order to compare the performance of impervious surface estimation of Sp_SSMA, comparative analysis is performed with a simple fixed four-endmembers SMA (fixed SMA) and the state-of-the-art hierarchical SMA, Prior-knowledge-based spectral mixture analysis (PKSMA) (Zhang et al, 2014). As for fixed SMA and PKSMA, high albedo, low albedo, soil and vegetation are chosen as a fixed set of endmembers. The extreme pixel clusters at MNF-based feature space are utilized to identify the spectral of each endmember.

335

336 *4.2 Stratification result*

As presented in Section 3, the enhanced CBI, I component and NDVI values 337 were taken to construct the subgroups for spectral unmixing. In this study, 338 λ_{CBL} , λ_L , λ_{NDVI} are 20 and θ_{CBL} , θ_L , θ_{NDVI} are 0.5 for the normalized indices in both the 339 images. Figures 4 and 5 show the original indices images and their histograms, 340 together with the corresponding transformed result the two study areas respectively. It 341 is clear that the separation between impervious surface and background information in 342 CBI, I and vegetation and background fraction in NDVI is improved effectively. The 343 histograms clearly show the apparent separations between the lower and higher values. 344 345 It is suggested that the transformation plays an active role in urban image description, which may have a positive impact on stratification. 346

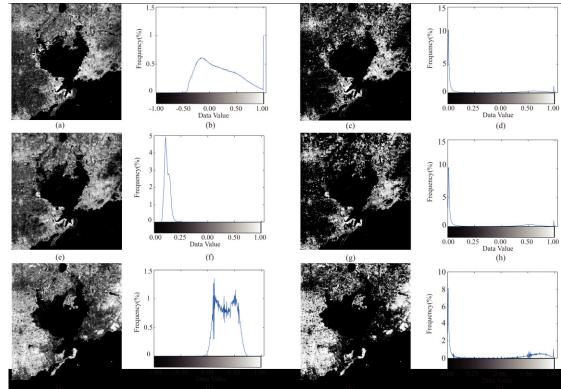
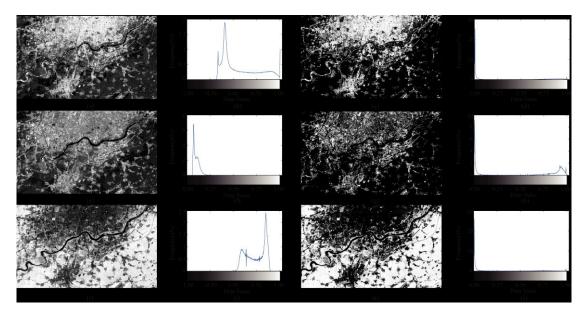


Figure 4 The transformation for feature indices enhancement in Landsat TM: (a), (e), (i) are the original CBI, I and
NDVI images, (b), (f), (j) are their corresponding histogram images; (c), (g), (k) are the enhanced CBI, I and NDVI
images, (d), (h), (l) are their corresponding histogram images.

351 352



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Figure 5 The transformation for feature indices enhancement in ASTER: (a), (e), (i) are the original CBI, I and
NDVI images, (b), (f), (j) are their corresponding histogram images; (c), (g), (k) are the enhanced CBI, I and NDVI
images, (d), (h), (l) are their corresponding histogram images.

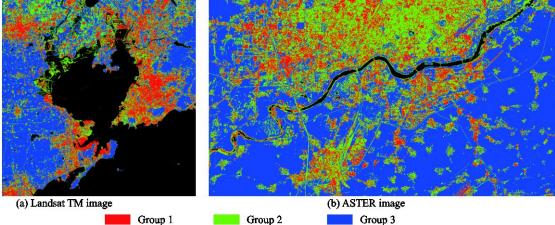
357

358 Table 1. The threshold values.

	Landsat TM	ASTER
CBI _{enh}	0.40	0.42
I _{enh}	0.38	0.38
NDVI _{enh}	0.42	0.45

359

The automatically selected thresholds and rules for stratification in this 360 experiment were shown in Table 1. The location of each sub-region obtained by the 361 stratification rules (Figure 6) illustrates that Group 1 mainly lies in the new distinct in 362 urban area, while Group 2 mainly lies in the urban fringe, industrial district and 363 historic town, and Group 3 in suburban area. Further analysis demonstrated that the 364 three main land cover types show significant differences among three groups. As for 365 impervious surface, in the area of Group 1, the high and low albedo both present a 366 relatively higher reflectance comparing with impervious surface fractions in other 367 subsets. As for Group 2, the impervious surfaces are mainly made up of tile-roofed 368 historic buildings, industrial area and mixed types of impervious material. The low 369 albedo impervious surface pixels belong to Group 3 are mainly composed of metal 370 sheet masonry. When considering the soil fraction, it tends to be composed of nature 371 impervious land covers, such as sand and stone in construction sites and bare rocks in 372 Group 1 and artificial land feature such as farmland and wasteland in Group 2. The 373 374 nature dark bare soil is predominant in soil fractions in Group 3. Vegetation only appears in Group 2 and 3. Crops in growing season, nature grasslands, shrub lands 375 and forest are the main composition in Group 3, whilst some artificial green land in 376 urban area and urban fringe are graded into Group 2. As results, the three unmixing 377 models are suitable to be applied to the three groups respectively. 378



381 Figure 6 The stratification result: (a)Landsat TM image, (b)ASTER image.

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383 In order to evaluate the accuracy of stratification, that is to say, there should be no vegetation fractions in Group 1 and no high albedo fractions in Group 3, 200 pixels 384 were randomly selected in Group 1 and 3 in both study sites respectively. The overall 385 accuracy of the stratification method were 92.75% in Group 1 and 95.50% in Group 3 386 with the help of Google Earth images as the reference data. The mis-stratifications 387 were part of the error sources. Therefore, the high accuracy obtained indicates that 388 389 this error can be neglected.

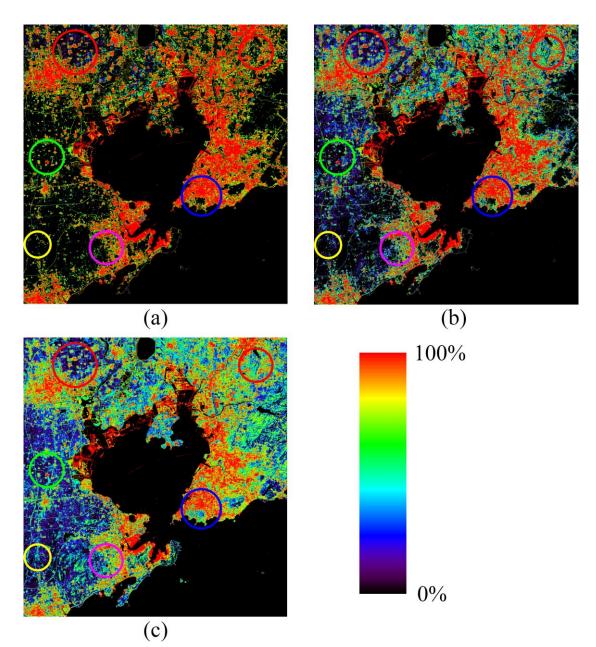
4.3 Impervious surface abundance 390

With the identified three urban area subgroups and different endmember sets 391 achieved independently in each subarea, spectral unmixing was performed. The 392 impervious surface abundance images are reported in Figures 7(a) and 8(a). Visual 393 inspection found that the spatial distribution of impervious surface fraction matches 394 395 well with known impervious surface distribution of Qingdao and Shenyang. A detailed insight into the general pattern of impervious surface fraction saw that the 396 abundance value was higher in the central business district (CBD) areas and along the 397 transportation lines, lower in suburban areas, and near zero in the rural and vegetated 398 areas as expected. However, in less developed areas, especially the areas of Group 3, 399 several paths of impervious surface areas failed to be recognized which could be a 400 primary error source. 401

402 Quantitative validations were also conducted. 400 sites were randomly selected on the Landsat and ASTER images, respectively, for validation. Each site is a window 403 of 3 pixels by 3 pixels, covering 90 m by 90 m, since their spatial resolution is 30 m. 404 180 pixels by 180 pixels on the Google Earth images are associated with each site, 405 since its spatial resolution is 0.5 m. The estimated total impervious surface abundance 406 for each site is compared with the ground reference provided by the Google Earth 407

images. The reason to utilize a window area to validate the performance is to reducethe problem caused by image registration error.

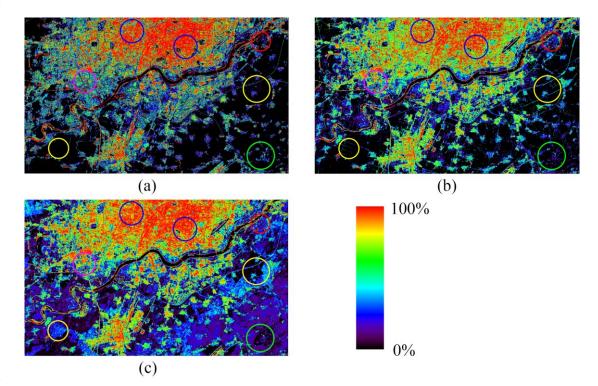
410 Quantitative analysis in Table 2 indicates that strong positive correlations with 411 reference impervious surface fraction with relatively small RMSE and SE values with 412 an R of 0.89 and 0.83, SE of 2.37% and 3.59%, whilst RMSE of 10.24% and 12.57% 413 respectively. With a detailed analysis, we see a better performance is achieved in 414 developed areas (e.g. an R of 0.86 and 0.81, an SE of 0.91% and 1.58%, a RMSE of 415 8.53% and 11.91%) when compared to less developed areas (e.g. an R of 0.84 and 416 0.79, an SE of 5.23% and 4.86%, RMSE of 12.89% and 15.32%).





 $\label{eq:419} Figure \ 7 \ The \ impervious \ surface \ abundance \ images \ of \ Landsat \ TM \ using \ Sp_SSMA \ (a), \ PKSMA \ (b) \ and$

- 420 fixed-SMA(c).
- 421



424 Figure 8 The impervious surface abundance images of ASTER using Sp_SSMA (a), PKSMA (b) and

425 fixed-SMA(c).

427 Table 2. Accuracy assessment of impervious surfaces with Sp_SSMA, PKSMA and fixed- SMA.

		Sp_SSMA		PKSMA		Fixed-SMA	
		Landsat	ASTER	Landsat	ASTER	Landsat	ASTER
Over all	R	0.89	0.83	0.84	0.76	0.79	0.75
	RMSE	10.24%	12.57%	11.24%	17.10%	15.13%	19.28%
	SE	2.37%	3.59%	3.47%	6.11%	5.09%	8.19%
Developed	R	0.86	0.81	0.89	0.63	0.73	0.63
	RMSE	8.53%	11.91%	9.72%	14.91%	15.52%	13.02%
	SE	0.91%	1.58%	1.43%	-3.91%	-8.18%	3.34%
Less-developed	R	0.84	0.79	0.76	0.64	0.81	0.51
	RMSE	12.89%	15.32%	14.76%	19.49%	14.13%	21.22%
	SE	5.23%	4.86%	8.05%	8.47%	7.84%	12.47%

430 *4.4 Comparative analysis*

To demonstrate the effectiveness of proposed Sp SSMA, PKSMA (Figures 7(b) 431 and 8(b)) and fixed-SMA (Figures 7(c) and 8(c)) were carried out for comparison. 432 Through a visual qualitative comparison, a similar impervious surface distribution 433 illustration is observed in most parts of the study sites. Impervious surface of high 434 abundance lies along the coastline and the northwest portion with low fraction in 435 suburban and rural areas in Qingdao. The ASTER image, which covers an urban 436 transect in the region of Shenyang, possesses a higher impervious surface fraction 437 values in the north part of the study area. 438

439 However, severe misestimation can be observed in both four-endmember SMA and PKSMA. Generally, an overestimation can be observed in suburban and rural 440 areas while the impervious surface abundance value of inner-city regions is more 441 likely to be under-estimated in fix-SMA and PKSMA. The area in magenta circle is 442 443 impervious surface mixed up with pervious materials. An obvious overestimation is 444 observed in PKSMA in Figures 7(b) and 8(b). The land surface in red circles on Figures 7 and 8, which are graded in Group 2 in Sp SSMA, are ought to be mainly 445 composed of farmland and other pervious surface which have extremely low 446 impervious surface fraction values. Severe over-estimation can be observed in both 447 PKSMA and four-endmember SMA. As for the area with high impervious surface 448 fraction values, PKSMA and four-endmember SMA tend to be underestimated. On 449 one hand, the small impervious surface patches in green circles in suburban and rural 450 areas which are supposed to have high impervious surface abundance, are 451 undervalued seriously in four-endmember SMA and PKSMA. On the other hand, 452 PKSMA and fixed-SMA tend to underestimate the impervious surface fraction values 453 in the highly urbanized old districts as marked by blue circles. This phenomenon is 454 much more obvious in Shenyang city as reported in Figure 8. The reason lies in the 455 inability of entire-image-achieved endmember spectrum in expressing the complex 456 impervious surface constitution, especially in the historic towns. Shenyang, in 457 particular, is composited of diverse industrial, commercial and residential landscape 458 that can be traced from decades ago to present day. The industrial and economic 459 development transformation also contributed to the complexity of impervious surface 460 types. The results indicate that it is important that the endmembers subsets are 461 extracted and applied in each group of data separately and highlight the advantage of 462 spectral domain stratification. However, Sp SSMA shows a relative poor performance 463 in mapping transportation lines when compared with four-endmember SMA and 464 PKSMA as shown by the region in yellow circle. The reason lies in that transportation 465 lines are likely to be mixed up with pervious surface in suburban or rural areas due to 466 the limited resolution. The absence of the representative endmembers leads to the 467 poor performance on transportation lines. 468

The quantitative results of accuracy assessment via R, RMSE and SE are reported in Table 2. Note that these accuracy assessments were calculated for the entire image, and for developed areas (impervious surface abundance great than or equal to 30%) and less-developed areas (impervious surface abundance less than 30%)

as well. The quantitative accuracy assessment in Table 2 shows that the overall 473 performance of the Sp SSMA is better than the others, with R of 0.79 and 0.75, SE of 474 5.09 % and 8.19%, RMSE of 15.13% and 19.28% for simple four-endmember SMA, 475 while R of 0.84 and 0.76, SE of 3.47 % and 6.11%, RMSE of 11.24% and 17.10% for 476 PKSMA. As for the fixed-endmember SMA, a much higher error level was observed. 477 478 Further analyses reveal that a severe over-estimation is given by PKSMA and four-endmember SMA in less developed areas with significantly high values of SE, 479 and RMSE. That's because in PKSMA, some low-density areas were misclassified as 480 high-density areas, resulting some soil were regarded as impervious surface during 481 spectral unmixing processes on one hand. Moreover, in order to ensure the integrity of 482 impervious surface information, NDVI and RED band doesn't always perform well in 483 eliminate vegetation information. On the other hand, the endmember sets for all 484 subsets in PKSMA were chosen through the original image while different 485 combinations were applied for each subgroup. It ignored the variability within each 486 land feature class which would lead to confusion between land cover with similar 487 spectral characteristics. For developed areas, the performance of the PKSMA and the 488 proposed SMA method is satisfactory and comparable in new-districts-dominated 489 Qingdao, with old-districts-dominated Shenyang on the opposite site. When compared 490 to Sp SSMA, PKSMA undervalued some high abundance impervious surface in rural 491 492 area with low density due to the confusion with soil. As for regions with high impervious surface fraction in urban area, overestimation can be observed due to the 493 absence of soil endmember in high-density new district areas in PKSMA whilst old 494 districts are suffering from underestimation. Meanwhile, PKSMA achieved a slightly 495 496 better performance than that of Sp SSMA in transportation lines.

497

498 **5** Conclusions

In this paper, a stratified spectral mixture analysis in spectral domain (Sp SSMA) 499 method was presented for estimating the impervious surface fraction in urban areas 500 through stratification. The Sp SSMA takes advantage of the features of CBI, I 501 component and NDVI to stratify the entire image into three subareas, named Group 1, 502 Group 2 and Group 3. The performance of Sp SSMA is demonstrated through the 503 relationship with the impervious surfaces abundance derived from Sp SSMA and 504 manual digitizing which are regarded as ground reference. Moreover, visual 505 inspection and quantitative analysis show that Sp SSMA improved the accuracy of 506 507 impervious surface estimation when compared with the existing LSMA-based method (e.g. fixed-SMA, PKSMA). A further analysis suggests that Sp SSMA estimates 508 impervious surface abundances in both developed and less-developed areas with 509 satisfying results. The proposition of Sp SSMA improved the accuracy of mapping 510 impervious surface fraction with simple and convenient image stratification approach 511 which may offer a help to urban land use management. 512

513 It can be considered that implementing the stratification approach into

impervious surface abundance estimation may further reduce the spectral similarity 514 between impervious surface and bare soil and reduce the within class variability in 515 each subgroup. Though the three land cover types still suffer from intra-class 516 variability due to the complex light scattering mechanisms in surface objects, different 517 constituent materials, the differences between impervious surfaces are small enough 518 519 to be represented by 1 or 2 endmembers while vegetation and soil can be characterized by 1 endmember respectively. Thus, Sp SSMA can promise more 520 reliable impervious surface fraction estimation. However, there are still confusions 521 between impervious surface and soil in urban fringe, since the land use structures are 522 tend to be disordered and the spectral information of impervious surface and bare soil 523 is quite alike. 524

Another advantage of the proposed Sp SSMA is that it takes advantage of 525 stratification information to select endmembers in each sub-group independently. 526 While stratification has been studied extensively [32], [38]-[40], little research has 527 been conducted to consider the spectral variability in different subareas. Although the 528 existing researches applied different endmembers to different subset, the endmembers 529 530 were achieved from the entire image scene rather than each sub-area that have been classified. The Sp SSMA takes advantage of the reduction of spectral confusion 531 between similar objects and within class variability in each sub-group to obtain 532 endmembers in each sub-group independently. Therefore, by using Sp SSMA, inner 533 layer information is made the best use. 534

Even though Sp SSMA markedly improved the accuracy of impervious surface 535 estimation, confusion between impervious surface and soil in suburban areas is still a 536 major concern. This confusion results in the overestimation of impervious surface 537 abundance in suburban and rural areas. More effort is still needed to address this 538 dilemma. In addition, less estimation of the traffic roads in the rural areas is another 539 540 problem to overcome. Furthermore, the accuracy and efficiency of stratification affects the result of impervious surface abundance extraction largely. Specifically, the 541 non-existing of a specific land cover endmember, such as transformation lines in 542 543 Group 2, may lead to misestimation of impervious surface fraction. Future research is needed to enhance the stratification model with more divisibility between land cover 544 features with similar characteristics. 545

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