

# Structure and Properties of Some Layered $U_2O_5$ phases: a Density Functional Theory Study

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**ABSTRACT.**  $U_2O_5$  is the boundary composition between the fluorite and layered structures of the  $UO_{2-3}$  system and the least studied oxide in the group.  $\delta-U_2O_5$  is the only layered structure proposed so far experimentally, although evidence of fluorite-based phases has also been reported. Our DFT work explores possible structures of  $U_2O_5$  stoichiometry by starting from existing  $M_2O_5$  structures (where M is an actinide or transition metal) and replacing the M ions with uranium ions. For all structures, we have predicted structural and electronic properties including bulk moduli and band gaps. The majority of structures were found to be less stable than  $\delta-U_2O_5$ .  $U_2O_5$  in the R-Nb<sub>2</sub>O<sub>5</sub> structure was found to be a competitive structure in term of stability whereas  $U_2O_5$  in the Np<sub>2</sub>O<sub>5</sub> structure was found to be the most stable overall. Indeed, by including the vibrational contribution to the free-energy using the frequencies obtained from the optimized unit cells we predict that Np<sub>2</sub>O<sub>5</sub> structured  $U_2O_5$  is the most thermodynamically stable under ambient conditions.  $\delta-U_2O_5$  only becomes more stable at high temperatures and/or pressures. This suggests that a low temperature synthesis route should be tested and so potentially opens a new avenue of research for pentavalent uranium oxides.

**KEYWORDS.**  $U_2O_5$ , pentavalent uranium oxide, diuranium pentoxide, oxidised  $UO_2$ , layered uranium oxide, ab initio calculation, thermodynamic properties.

## Introduction

$\text{U}_2\text{O}_5$  marks an important, yet underexplored, area of the uranium-oxygen phase diagram. Although its practical applications have received little attention, owing to its instability relative to both higher and lower oxides<sup>1-8</sup>. One of its intriguing features is that it represents the composition of the transition point between the fluorite and layered uranium oxides, with reports of it forming in both types of structure<sup>1,9</sup>. As the existing data in the literature concerning any of the reported  $\text{U}_2\text{O}_5$  polymorphs is extremely limited, again most likely due to difficulties in synthesising it, computational investigations provide a convenient means of exploring the structural and electronic properties of this material and relating them to the coordination environments of uranium.

The only reported study of fluorite  $\text{U}_2\text{O}_5$  is from Hoekstra *et al.*, who give details on the synthesis and structures of  $\alpha$ -,  $\beta$ - and  $\gamma$ - $\text{U}_2\text{O}_5$  (although not enough information is available to produce a full atom description)<sup>1</sup>.  $\alpha$ - $\text{U}_2\text{O}_5$  was prepared by heating a mixture of  $\text{UO}_2$  and  $\text{U}_3\text{O}_8$  (673 K at 30 kbar) and found to have a density of  $10.5 \text{ gcm}^{-3}$ , approximately  $0.7 \text{ gcm}^{-3}$  less than other fluorite based phases, which suggests that the structure might be slightly closer to a layered type oxide<sup>10,11</sup>.  $\beta$ - $\text{U}_2\text{O}_5$  and  $\gamma$ - $\text{U}_2\text{O}_5$  were prepared by heating the same mixture in excess of 1073 K at 40-50 kbar and 60 kbar respectively.  $\beta$ - $\text{U}_2\text{O}_5$  has a hexagonal cell with  $a=b=3.813 \text{ \AA}$  and  $c=13.180 \text{ \AA}$  with a density of  $11.15 \text{ gcm}^{-3}$ , whereas  $\gamma$ - $\text{U}_2\text{O}_5$  has a monoclinic cell with  $a=5.410$ ,  $b=5.481$ ,  $c=5.410 \text{ \AA}$  and  $\beta=90.49^\circ$  with a density of  $11.36 \text{ gcm}^{-3}$ . These densities suggest that it is more likely to be a defective fluorite  $\text{UO}_2$ <sup>12</sup>.<sup>13</sup>. The lack of any atomic coordinates for fluorite based  $\text{U}_2\text{O}_5$  structures means that  $\text{UO}_2$  supercells with additional oxygen interstitials (Oi) are required to investigate these types of structure quantum mechanically<sup>12,13</sup>.

The only full crystallographic structure reported in the literature is the layered  $\delta$ - $\text{U}_2\text{O}_5$  polymorph. It has a density of  $8.22 \text{ gcm}^{-3}$  and crystallises in the orthorhombic  $Pnma$  space group with  $a=6.849$ ,  $b=8.274$  and  $c=31.706 \text{ \AA}$ <sup>9</sup>. It contains a mixture of six-fold (distorted octahedral) and seven-fold (distorted pentagonal bipyramidal) uranium environments and the structure is similar to  $\text{U}_3\text{O}_8$ ,

essentially an oxygen deficient version of this higher oxide. No thermodynamic information has been gathered experimentally for  $\text{U}_2\text{O}_5$ , nor has there been any further structural investigation since the original experiments of Hoekstra<sup>1,9</sup>. Early XPS studies have suggested a mixture of  $\text{U}^{4+}$  and  $\text{U}^{6+}$  ions<sup>14</sup>, but more recent experiments have proposed  $\text{U}_2\text{O}_5$  is composed entirely of  $\text{U}^{5+}$  ions<sup>15</sup>. Brincat *et al.* showed that the DFT + U methodology was able to reproduce the structure of  $\delta\text{-U}_2\text{O}_5$ <sup>3</sup> while Andersson *et al.* reported it to be thermodynamically unstable (with respect to  $\text{U}_3\text{O}_8$ ) with the highest formation energy of any uranium oxide<sup>4</sup>. Our aim is to develop reliable structural models to aid in the identification of possible phases and give a quantitative description of their relative stability.

## Methodology

Calculations were performed using the Vienna *Ab Initio* Simulation Package (VASP)<sup>16,17</sup>, with the PBE<sup>18</sup> exchange-correlation functional within the generalised gradient approximation (GGA). The Dudarev approach<sup>19</sup> to the GGA + U methodology<sup>20</sup> was employed to enforce localisation of U *5f* electrons. We have used an effective  $U_{\text{eff}}$  ( $U$ - $J$ ) parameter of 3.96 eV. The values of the  $U$  and  $J$  parameters were 4.5 eV and 0.54 eV respectively, which were taken from the XPS experiments of Yamazaki and Kotani on  $\text{UO}_2$ <sup>21</sup>. No such parameters have been derived for  $\text{U}_2\text{O}_5$  (or any other uranium oxides) and so in the interest of transferability of results we have used these values, as in our previous works<sup>3,10</sup>. Work in the literature has demonstrated that changing the effective  $U$  parameter mainly affects the predicted band gap, and has considerably less impact on the other calculated properties<sup>22</sup>.

Spin-orbit coupling has not been included in any of the calculations described here as it has been previously demonstrated on actinide dioxides<sup>23,24</sup> and  $\text{U}_3\text{O}_8$ <sup>25</sup> that the effects on structural and electronic properties and relative stabilities are inconsequential. The structural optimisations presented here were all allowed to proceed with unconstrained symmetries so that all volume and internal structure parameters were relaxed. The total energy was converged to at least  $1 \times 10^{-6}$

eV/atom for the electronic relaxation and the ionic relaxation was performed until the Hellmann-Feynman forces on each atom were less than  $0.01 \text{ eV}\text{\AA}^{-1}$ .

Convergence of the energy was reached with a cutoff energy of 500 eV to remove errors due to Pulay stress <sup>26</sup> during cell relaxation and automatically generated  $\Gamma$ -centred Monkhorst-Pack  $k$ -meshes of  $\delta$ -U<sub>2</sub>O<sub>5</sub> 3 x 2 x 1, Np<sub>2</sub>O<sub>5</sub> 4 x 6 x 4, *R*-Nb<sub>2</sub>O<sub>5</sub> 6 x 6 x 4, *Z*-Nb<sub>2</sub>O<sub>5</sub> 6 x 6 x 6, *N*-Nb<sub>2</sub>O<sub>5</sub> 1 x 4 x 2, B-Ta<sub>2</sub>O<sub>5</sub> 4 x 6 x 6,  $\alpha$ -V<sub>2</sub>O<sub>5</sub> 2 x 6 x 2 and  $\beta$ -V<sub>2</sub>O<sub>5</sub> 3 x 6 x 4. Although this results in a range of  $k$ -mesh densities convergence was reached in each case. All structures are free of imaginary modes. Vibrational frequencies are presented in Figure S1-S8. Elastic constants and bulk moduli were calculated for all polymorphs as detailed in our previous work on UO<sub>3</sub> <sup>10</sup>.

Ferromagnetic ordering was used for all of the M<sub>2</sub>O<sub>5</sub> structures, as the difference in energy between ferromagnetic and antiferromagnetic orderings was found to be negligible for  $\delta$ -U<sub>2</sub>O<sub>5</sub> <sup>3</sup>.

## Results and Discussion

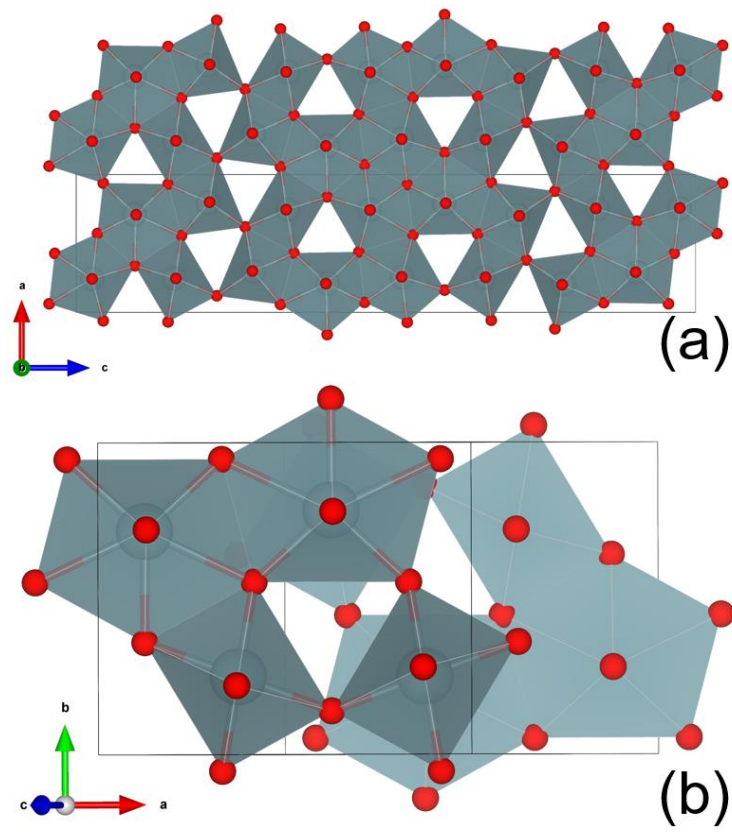
We have simulated different structures with U<sub>2</sub>O<sub>5</sub> composition; before assessing their order of stability, here we describe their structures.

**Structural properties.** A number of alternative M<sub>2</sub>O<sub>5</sub> (where M is an actinide or transition metal) structures have been investigated, replacing the metal ion with uranium, including Np<sub>2</sub>O<sub>5</sub> <sup>27</sup>, Nb<sub>2</sub>O<sub>5</sub> <sup>28-30</sup>, Ta<sub>2</sub>O<sub>5</sub> <sup>31</sup>, and V<sub>2</sub>O<sub>5</sub> <sup>32,33</sup> polymorphs. All relaxed structures retain the coordination environments of the original M<sub>2</sub>O<sub>5</sub> systems, although the symmetry is often lowered. This may be a direct consequence of the strain imposed by the large uranium cation (0.84 Å) substituting the transition metal ions (V, Nb, Ta) which are significantly smaller (0.54, 0.69 and 0.69 Å respectively) <sup>34</sup>. As the lattice parameter of the original structures cannot be directly compared to our simulation results, we do not report their details. We only report the experimental structure of Np<sub>2</sub>O<sub>5</sub> as a comparison to our calculated structure of U<sub>2</sub>O<sub>5</sub> in the Np<sub>2</sub>O<sub>5</sub> structure. From the comparison between the experimental and the calculated lattice parameters (Table 1) the agreement is excellent, most likely due to the

similarity between uranium and neptunium atomic radii (0.84 and 0.75 Å respectively<sup>34</sup>). If the change in volume is ascribed to the extra space filling of spherical uranium ions, the increase in volume would be predicted to be 5.7 Å<sup>3</sup>, which is close to the increase of 5 Å<sup>3</sup> actually calculated. To note, as customary with the PBE + U, the cell volume is overestimated for both U<sub>2</sub>O<sub>5</sub> and Np<sub>2</sub>O<sub>5</sub>, compared to the experimental data. Structural properties of the various systems are collated in Table 1 and Table 2 whilst their relaxed structures are shown in Figure 1 to Figure 4. All structures are presented in SI.

**δ-U<sub>2</sub>O<sub>5</sub>.** The simulated unit cell contains only U<sup>5+</sup>, half in pentagonal bipyramidal and half in octahedral coordination (Fig. 1a) environments. This coordination is equivalent to the one in the experimental unit cell. The layers stack in an eclipsed fashion such that the coordination of a given uranium ion is identical to the one directly above or below. The structure<sup>9</sup> resembles oxygen deficient α-U<sub>3</sub>O<sub>8</sub>. The U-O<sub>ax</sub> bonds (O<sub>ax</sub> are oxygen atoms lying above and below the equatorial plane of the coordination environment) between the layers range between 2.105 and 2.107 Å (longer than a typical uranyl bond<sup>10 35</sup>) and equatorial bonds similar to those in U<sub>3</sub>O<sub>8</sub><sup>3</sup>.

**U<sub>2</sub>O<sub>5</sub> in Np<sub>2</sub>O<sub>5</sub> structure.** The simulated structure consists of 8 uranium environments<sup>27</sup>, 4 with pentagonal bipyramidal coordination (although 2 U-O<sub>eq</sub> bonds are longer than 2.6 Å, O<sub>eq</sub> are oxygen atoms lying in the equatorial plane of the coordination environment) and 4 with octahedral coordination (Fig. 1b). Each pentagonal bipyramidal U site contains one U-O<sub>ax</sub> bond ~1.97 Å, slightly longer than a uranyl ion bond (1.7 – 1.9 Å). All uranium ions are predicted to be U<sup>5+</sup>. The stacking of layers gives alternating octahedral and pentagonal bipyramidal coordination, which is similar to β-U<sub>3</sub>O<sub>8</sub><sup>3</sup>.



**Figure 1.** Simulated structure of the (a) top view of  $\delta\text{-U}_2\text{O}_5$  and (b) top view of  $\text{U}_2\text{O}_5$  in the  $\text{Np}_2\text{O}_5$  structure.

**Table 1.** Predicted properties of  $U_2O_5$ . Space groups are calculated to a tolerance of 0.01 Å.  $\Delta\%$  is the percentage difference between a calculated structure and experiment and is not presented for any of the  $M_2O_5$  structures (where M is a metal ion other than uranium). The enthalpy of formation ( $E_{form}=E(U_2O_5) - 2E(U) - 5E(O)$ ) is calculated with respect to the energy of  $\alpha$ -U metal (8.43 eV/U) and the  $O_2$  molecule (-4.93 eV/O ca. expt. -5.10 eV/O<sup>36</sup>). The energy of an O atom was predicted to be -4.93 eV, calculated from an  $O_2$  molecule in a 20 Å box using the  $\Gamma$ -point. \* The experimental structure is for  $Np_2O_5$ .

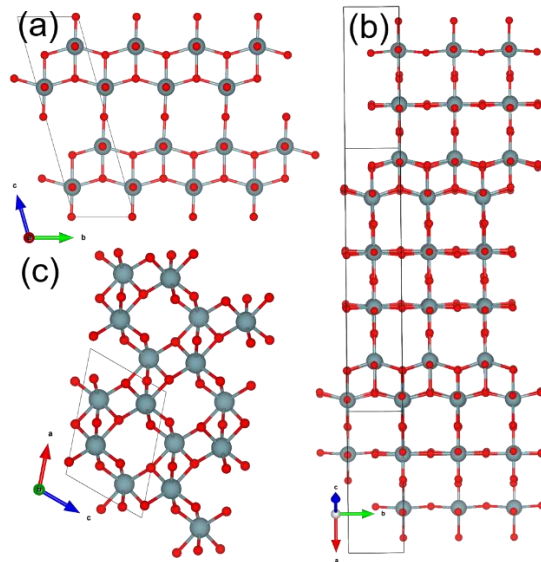
Phase	Method	Lattice Parameters (Å)			Lattice Parameters (°)			Vol (Å <sup>3</sup> /U <sub>2</sub> O <sub>5</sub> )	Space Group	E <sub>gap</sub> (eV)	B (GPa)	E <sub>form</sub> (eV/U <sub>2</sub> O <sub>5</sub> )
		a (Δ%)	b (Δ%)	c (Δ%)	α (Δ%)	β (Δ%)	γ (Δ%)					
$\delta$ - $U_2O_5$ <sup>9</sup>	Expt.	6.85	8.27	31.71	90.0	90.0	90.0	112.27	<i>Pnma</i> (62)	-	-	-
	PBE + U	7.0225 (2.52)	8.4219 (1.84)	31.4605 (-0.79)	90.0	90.0	90.0	116.29 (3.58)	<i>Pcma</i> (55)	1.69	160	-23.01
$Np_2O_5$ <sup>27</sup>	Expt.*	8.17	6.58	9.31	90.0	116.1	90.0	112.46	<i>P2/c</i> (13)	-	-	-
	PBE + U	8.1358 (-0.42)	6.8289 (3.78)	9.3972 (0.94)	90.00	115.91 (-0.16)	90.00	117.41 (4.40)	<i>I2/a</i> (15)	2.45	133	-23.24
<b>R-Nb<sub>2</sub>O<sub>5</sub></b> <sup>28</sup>	PBE + U	4.2126	4.3586	14.9779	106.82	90.00	89.99	131.63	<i>Pm</i> (6)	2.07	149	-22.98
<b>Z-Nb<sub>2</sub>O<sub>5</sub></b> <sup>29</sup>	PBE + U	7.0092	5.2237	5.8121	89.97	104.67	90.04	108.40	<i>P1</i> (1)	2.20	88	-22.45
<b>N-Nb<sub>2</sub>O<sub>5</sub></b> <sup>30</sup>	PBE + U	31.4749	4.2998	19.1689	90.05	124.94	89.90	132.91	<i>P1</i> (1)	1.30	108	-22.48
<b>B-Ta<sub>2</sub>O<sub>5</sub></b> <sup>31</sup>	PBE + U +	14.2946	5.2982	6.1399	90.00	104.40	90.01	112.60	<i>P-1</i> (2)	2.25	57	-22.72
$\alpha$ - $V_2O_5$ <sup>32</sup>	PBE + U	11.5425	4.3638	10.5977	90.02	90.00	89.98	133.45	<i>P2<sub>1</sub></i> (4)	1.99	82	-22.35
$\beta$ - $V_2O_5$ <sup>33</sup>	PBE + U	6.6125	4.0259	7.3203	90.00	79.71	90.00	95.87	<i>Pm</i> (6)	1.35	176	-21.94



**Table 2.** Coordination and charges of Uranium in simulated U<sub>2</sub>O<sub>5</sub> phases.

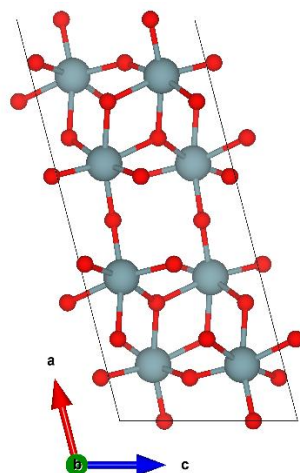
U environment	Number of U Environments per simulated unit cell							
	$\delta$ -U <sub>2</sub> O <sub>5</sub>	Np <sub>2</sub> O <sub>5</sub>	R-Nb <sub>2</sub> O <sub>5</sub>	Z-Nb <sub>2</sub> O <sub>5</sub>	N-Nb <sub>2</sub> O <sub>5</sub>	B-Ta <sub>2</sub> O <sub>5</sub>	$\alpha$ -V <sub>2</sub> O <sub>5</sub>	$\beta$ -V <sub>2</sub> O <sub>5</sub>
U <sup>5+</sup> trigonal bipyramid								
U <sup>5+</sup> distorted octahedron	8		4	4		8	8	
U <sup>5+</sup> octahedron	8	4			16			
U <sup>5+</sup> pentagonal bipyramid	16	4						
U <sup>5+</sup> 7-fold								2
U <sup>6+</sup> octahedron					8			
U <sup>6+</sup> 7-fold								1
U <sup>4+</sup> distorted octahedron					8			
U <sup>4+</sup> 7-fold								1
Uranyl Bond		U <sup>5+</sup> -O 1.98Å*			U <sup>6+</sup> -O 1.97Å			U <sup>6+</sup> -O 1.93Å

**U<sub>2</sub>O<sub>5</sub> in Nb<sub>2</sub>O<sub>5</sub> structure.** We have simulated R-<sup>28</sup> Z-<sup>29</sup> and N-<sup>30</sup> Nb<sub>2</sub>O<sub>5</sub> polymorphs. It is worth commenting that R- and N-Nb<sub>2</sub>O<sub>5</sub> phases are anatase-like structures, and as shown in Figure 2a and Figure 2b respectively, have layers of edge sharing MO<sub>6</sub> octahedra. In R-Nb<sub>2</sub>O<sub>5</sub> the layers are continuous in the c direction (Figure 2a), while in N-Nb<sub>2</sub>O<sub>5</sub> they are separated by 2 layers of a skutterudite-like structure resembling  $\delta$ -UO<sub>3</sub>. The structure can be considered as a Magneli-like structure<sup>37</sup>, which has alternating MO<sub>6</sub> rich layers perovskite (without the A cation, i.e. ReO<sub>3</sub> structured) layers. Z-Nb<sub>2</sub>O<sub>5</sub> does not resemble the anatase structure and is more comparable to a distorted brookite structure (Figure 2c). All systems have monoclinic symmetry. In the R- and Z-Nb<sub>2</sub>O<sub>5</sub> phases all uranium ions are U<sup>5+</sup> in octahedral coordination. In contrast, for the N-Nb<sub>2</sub>O<sub>5</sub> structure we found a mixture of U<sup>4+</sup> (25%), U<sup>6+</sup> (25%) and U<sup>5+</sup> (50%), again all uranium ions are in octahedral coordination. However, U<sup>4+</sup> sites have a highly distorted octahedral environment whereas U<sup>6+</sup> have the least distorted octahedral environment with a U-O<sub>ax</sub> bond of 1.97 Å.



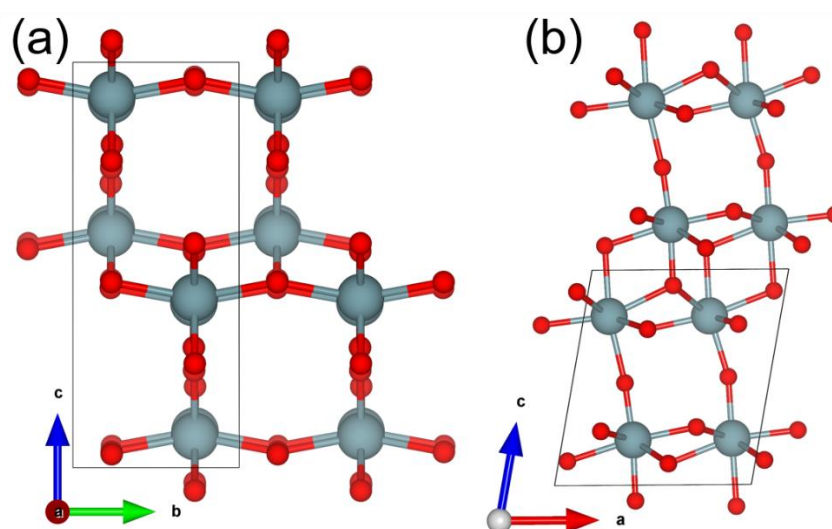
**Figure 2.**  $\text{U}_2\text{O}_5$  in (a) R- $\text{Nb}_2\text{O}_5$ , (b) N- $\text{Nb}_2\text{O}_5$ , and (c) Z- $\text{Nb}_2\text{O}_5$  structures.

**$\text{U}_2\text{O}_5$  in  $\text{Ta}_2\text{O}_5$  structure.** Although many polymorphs exist for this oxide, they are for the most part very similar to  $\text{Nb}_2\text{O}_5$ . Thus, only one polymorph was simulated (B- $\text{Ta}_2\text{O}_5$ )<sup>31</sup>. All uranium ions are in distorted octahedral coordination and predicted to be  $\text{U}^{5+}$ .



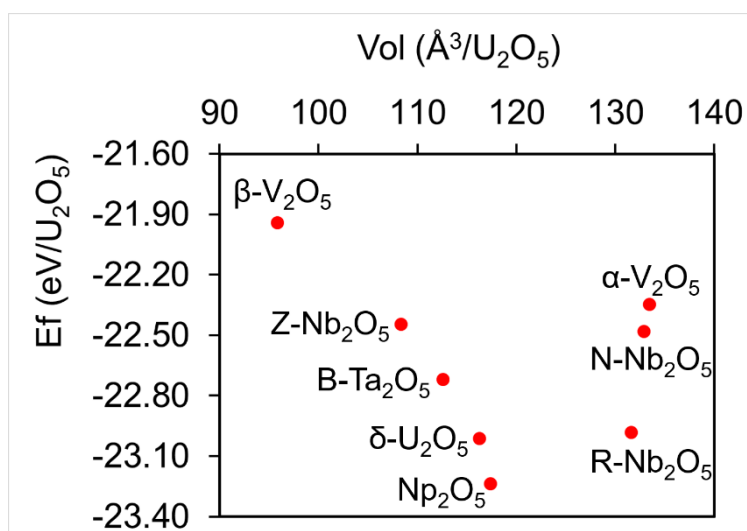
**Figure 3.**  $\text{U}_2\text{O}_5$  in the B- $\text{Ta}_2\text{O}_5$  structure.

**U<sub>2</sub>O<sub>5</sub> in V<sub>2</sub>O<sub>5</sub> structure.** Two polymorphs have been studied,  $\alpha$ - and  $\beta$ -V<sub>2</sub>O<sub>5</sub>. The  $\alpha$ - polymorph crystallises in an orthorhombic unit cell, with all uranium ions in distorted octahedral environments<sup>32</sup>.  $\beta$ -V<sub>2</sub>O<sub>5</sub> has U sites in 7-fold coordination<sup>33</sup>, with the equatorial bonds extended above and below the equatorial plane in a similar manner to  $\alpha$ -UO<sub>3</sub><sup>10</sup>. U sites are occupied entirely by U<sup>5+</sup> in  $\alpha$ -V<sub>2</sub>O<sub>5</sub> whereas the distribution is 25% U<sup>4+</sup>, 25% U<sup>6+</sup> and 50% U<sup>5+</sup> in  $\beta$ -V<sub>2</sub>O<sub>5</sub>. U<sup>6+</sup> sites have U-O axial bonds of 1.93 Å.



**Figure 4.** U<sub>2</sub>O<sub>5</sub> in the (a)  $\alpha$ - and (b)  $\beta$ -V<sub>2</sub>O<sub>5</sub> structures.

**Stability.** The formation energies of the simulated structures with U<sub>2</sub>O<sub>5</sub> composition are listed in Table 1. For clarity, we have plotted these energies against the volume per U<sub>2</sub>O<sub>5</sub> unit in Figure 5. There is a clear dependence of the formation energy on the volume, with a decrease in stability for volumes smaller or larger than the most stable phases (Np<sub>2</sub>O<sub>5</sub> and U<sub>2</sub>O<sub>5</sub>).



**Figure 5.** Stability plot of formation energy per  $\text{U}_2\text{O}_5$  in eV vs volume per  $\text{U}_2\text{O}_5$  unit. The phases are named with the original  $\text{M}_2\text{O}_5$  structures for clarity.

There are a number of factors, including the distribution of uranium charges and uranium coordination that influence the stability. The  $\text{Np}_2\text{O}_5$  structure is the most stable overall, 0.23 eV more stable than  $\delta\text{-U}_2\text{O}_5$  although both structures contain half U in pentagonal bipyramidal and half in octahedral coordination. As with  $\delta\text{-U}_2\text{O}_5$ , the  $\text{Np}_2\text{O}_5$  structure resembles oxygen deficient  $\text{U}_3\text{O}_8$ .  $\text{R-Nb}_2\text{O}_5$  is found to be just slightly less stable than  $\delta\text{-U}_2\text{O}_5$  (0.03 eV). In this structure U ions are all  $\text{U}^{5+}$  and all in distorted octahedral coordination. Phases with mixed U charges are amongst the most unstable although this effect is exacerbated by small volumes.

The other phases follow the order of stability of  $\text{Np} > \text{Nb/Ta} > \text{V}$ , with the  $\text{Np}_2\text{O}_5$  structure noticeably more stable than  $\delta\text{-U}_2\text{O}_5$ . As  $\text{U}^{5+}$  prefers higher coordination numbers compared to the 6-fold octahedral coordination, all the structures featuring uranium ions entirely in six-fold coordination are consequently less stable.  $\text{V}_2\text{O}_5$  structured oxides are the least stable with the  $\beta$ - polymorph less stable than the  $\alpha\text{-V}_2\text{O}_5$  structure, due to the presence of U in mixed oxidation states ( $\text{U}^{4+}$  and  $\text{U}^{6+}$ ) compared to  $\alpha\text{-V}_2\text{O}_5$  comprised of only  $\text{U}^{5+}$  ions.

These energetics show that  $\text{U}_2\text{O}_5$  could crystallise in the  $\text{Np}_2\text{O}_5$  structure, but due to the relative instability of the  $\text{U}_2\text{O}_5$  stoichiometry compared to the other uranium oxides, it has not been synthesised or reported experimentally. The difficulty in synthesising layered  $\text{U}_2\text{O}_5$  is likely to stem from the fact that the structure is essentially oxygen deficient  $\text{U}_3\text{O}_8$  and  $\text{U}^{5+}$  is more stable in pentagonal bipyramidal coordination<sup>3</sup>. This relative instability of  $\delta\text{-U}_2\text{O}_5$  (and (Np)  $\text{U}_2\text{O}_5$ ) likely arises from the presence of octahedrally coordinated uranium ions, it is highly favourable for this polymorph to gain more oxygen so that  $\text{U}^{6+}$  can occupy octahedral sites and  $\text{U}^{5+}$  may retain pentagonal bipyramidal coordination. This coordination behaviour is observed for both  $\alpha$ - and  $\beta$ - $\text{U}_3\text{O}_8$  phases<sup>3</sup>.

One can also consider the formation of the studied  $\text{U}_2\text{O}_5$  phases as a function of pressure representing a range of conditions; from negative pressure (high temperature) to positive (high) pressure. The formation enthalpies as a function of pressure are presented in Figure S9 and are normalised with respect to the most stable  $\text{U}_2\text{O}_5$  (i.e. the  $\text{Np}_2\text{O}_5$  structure) such that  $\delta H_f = \Delta H(x) - \Delta H(\text{Np}_2\text{O}_5)$ , where x is the phase in question and  $\Delta H(x)$  correspond to  $E_{\text{form}}$  in Table 1. Of interesting note is that we predicted that at high pressure (above 97 kbar)  $\text{U}_2\text{O}_5$  will be more thermodynamically stable in  $\beta\text{-V}_2\text{O}_5$  structure, although its dynamical stability will need to be checked via the calculation of the vibrational frequencies.

Using the predicted vibrational frequencies (Figure S1 to S8) calculated for each unit cell, we evaluated the vibrational contribution to a number of thermodynamic properties such as the Helmholtz free energy  $A_{\text{vib}}$  (Figure S10), vibrational entropy  $S_{\text{vib}}$  (Figure S11) and vibrational energy  $E_{\text{vib}}$  (Figure S12), Helmholtz free energy  $A_{\text{tot}} = E_{\text{form}} + A_{\text{vib}}$  (Figure S13) and the zero point energy (ZPE, Table 3). All these properties are expressed per  $\text{U}_2\text{O}_5$  unit and a sample of values at 300 K is presented in Table 3. A full calculation of the phase stability for  $\text{U}_2\text{O}_5$  phases is beyond the scope of this work, however, the calculations show that the energy minimised  $\delta\text{-U}_2\text{O}_5$  phase has a lower vibrational entropy and a smaller ZPE than the  $\text{Np}_2\text{O}_5$  phase. Hence, at high temperatures the  $\delta\text{-U}_2\text{O}_5$

phase will be thermodynamically favoured. Using our calculated values  $\delta$ -U<sub>2</sub>O<sub>5</sub> is predicted to be the preferred structure at around 800 C and 0 bar (Figure S13). Furthermore, the delta phase has a smaller molar volume, which means that it is further stabilised at high pressures, where the PV term in the Gibbs free energy will dominate. Thus it is not surprising that given the synthesis conditions reported for U<sub>2</sub>O<sub>5</sub>,<sup>1,9</sup> i.e. high temperatures and pressures that our predicted Np<sub>2</sub>O<sub>5</sub> phase has not been spotted.

**Table 3.** Predicted thermodynamic properties of U<sub>2</sub>O<sub>5</sub> phases at 300 K using the zone centre vibrational frequencies.

Phase	A <sub>vib</sub> (meV)	S <sub>vib</sub> (meV/K)	E <sub>vib</sub> (meV)	ZPE (meV)	A <sub>tot</sub> (eV)
Np <sub>2</sub> O <sub>5</sub>	156	1.61	638	380	-23.08
$\delta$ -U <sub>2</sub> O <sub>5</sub>	112	1.79	647	371	-22.90
B-Ta <sub>2</sub> O <sub>5</sub>	205	1.46	643	401	-22.52
$\beta$ -V <sub>2</sub> O <sub>5</sub>	231	1.33	630	407	-21.71
Z-Nb <sub>2</sub> O <sub>5</sub>	154	1.5	606	358	-22.29
R-Nb <sub>2</sub> O <sub>5</sub>	89	1.72	604	346	-22.89
$\alpha$ -V <sub>2</sub> O <sub>5</sub>	214	1.46	653	414	-22.14
N-Nb <sub>2</sub> O <sub>5</sub>	70	1.92	645	360	-22.41

**Elastic properties.** It is somewhat complicated to compare elastic constants, which are presented in Table S1. Thus we will focus on the bulk modulus for the different structures. There is no evident

correlation between the bulk moduli and the volume or formation energy of the  $U_2O_5$  phases. The only noticeable correlation is that those structures with mixed charges ( $U^{6+}$  and  $U^{4+}$ ) have higher bulk modulus ( $\beta$ - $V_2O_5$  and N- $Nb_2O_5$ ). However, as these structures are amongst the least stable, they are unlikely to be readily synthesised.

**Electronic properties.** The experimental electronic properties of  $U_2O_5$  are not currently available and the only simulated electronic properties of  $\delta$ - $U_2O_5$  are that of Brincat *et al.*<sup>3</sup>. In keeping with the higher layered oxides  $U_3O_8$ <sup>3</sup> and  $UO_3$ <sup>10</sup>, all structures are predicted to be charge transfer insulators, with a conductance band composed of U 5f states and valence band comprised of O 2p states, with higher energy U 5f states at the core. The presence of U 5f states in the valence band suggests a degree of covalent mixing with O 2p (fully ionic bonding would feature no overlapping states). There is very little overall contribution from U 6d states, with most of it confined to the lower valence band. There is a great variation in predicted band gaps, with  $\delta$ - $U_2O_5$  predicted to be 1.69 eV, which is relatively close to the experimentally determined  $\alpha$ - $U_3O_8$  band gap of 1.76 eV<sup>38</sup>. Those structures with mixed charges ( $U^{6+}$  and  $U^{4+}$ ) have lower band gaps ( $\beta$ - $V_2O_5$  and N- $Nb_2O_5$ ), whereas all other structures have band gaps in line with PBE + U  $U_3O_8$  (2.05 – 2.23 eV)<sup>3</sup>.

## Conclusions

Our results show clearly that  $U_2O_5$  structures prefer U ions in homogeneous  $U^{5+}$  oxidation states rather than a mixed charge state ( $U^{4+}$  and  $U^{6+}$ ) and that higher coordination numbers are favoured, such as pentagonal bipyramids compared to octahedra. The simulations predict that the  $Np_2O_5$ -structured  $U_2O_5$  is the most stable of those considered under ambient conditions. The observed  $\delta$ - $U_2O_5$  structure is found to be second most stable and, surprisingly, given that it contains only octahedrally coordinated U is closely followed by R- $Nb_2O_5$ . The bulk moduli of the most stable polymorphs are also very similar to  $U_3O_8$ , as would be expected given their close structural resemblance.

Hence, one could infer that the order of stability of  $U_2O_5$  increases with the concentration of  $U^{5+}$  and oxygen content before reaching the  $U_3O_8$  stoichiometry, which will stabilize  $U^{6+}$ , destabilizing the  $U_2O_5$  phases. To this end it would be expected that uranium can crystallise with the  $Np_2O_5$  structure, however it has not been observed experimentally. We suggest it is due to a combination of synthesis difficulties, as the composition is meta-stable with respect to  $U_3O_8$ , and the fact that the  $Np_2O_5$  structure is destabilised with respect to the observed  $\delta$ - $U_2O_5$  structure at the high temperatures and pressures more commonly used in many of the reported structural investigations of this composition from the 1960s. The stoichiometry is clearly worthy of synthetic investigation though as the  $Np_2O_5$  structure is found to be a stable phase. The experimental challenge will be to develop lower temperature synthesis routes while calibrating the oxygen content extremely carefully.

Future simulation work will focus on using a more pragmatic approach to model fluorite-based  $U_2O_5$  phases, potentially using the methodology set out in our previous studies of  $U_4O_9$ <sup>12</sup> and  $U_3O_7$ <sup>13</sup>, in order to better understand the fluorite to layered transformation.



## **ASSOCIATED CONTENT**

Supporting Information includes Density Functional Theory optimized uranium oxides at the U<sub>2</sub>O<sub>5</sub> stoichiometry in the fractional format. The zone centre vibrational frequencies, the independent elastic constants, and thermodynamic properties are also presented. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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### **Notes**

The authors declare no competing financial interest.

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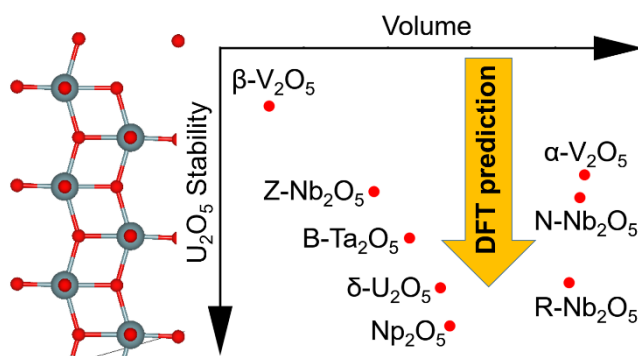
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## For Table of Contents Only



Density Functional Theory calculations were employed to predict layered structures of uranium oxide at U<sub>2</sub>O<sub>5</sub> stoichiometry using known structures with the same composition. The structures are characterized in terms of relative stability and structural, elastic and electronic properties. U<sub>2</sub>O<sub>5</sub> in the Np<sub>2</sub>O<sub>5</sub> structure is predicted to be the most stable uranium pentoxide.