

A Scalable Performance-Complexity Trade-off for Constellation-Randomization in Spatial Modulation

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Abstract—It is widely recognised that traditional single RF-chain aided spatial modulation (SM) does not offer any transmit diversity gain. As a remedy, constellation randomization (CR), relying on transmit pre-scaling (TPS), has been shown to provide transmit diversity for single RF-chain aided SM. In this paper we propose a low-complexity approach to SM with the aid of constellation randomization (SM-CR) that considerably improves the transmit diversity gain of SM at a reduced computational burden compared to conventional SM-CR. While conventional SM-CR performs a full search amongst a set of candidate TPS factors in order to achieve the maximum minimum Euclidean distance (MED) in the received SM constellation, here we propose a thresholding approach, where instead of the maximum MED the TPS aims to satisfy a specific MED threshold. This technique offers a significant complexity reduction with respect to the full maximization of SM-CR, since the search for TPS is terminated once a TPS set is found that satisfies the MED threshold. Our analysis and results demonstrate that a scalable trade-off can be achieved between transmit diversity and complexity by appropriately selecting the MED threshold, where a significant complexity reduction is attained, while achieving a beneficial transmit diversity gain for the single-RF SM.

Index Terms—Spatial modulation, constellation shaping, multiple-input-single-output, transmit pre-scaling

I. INTRODUCTION

Spatial Modulation (SM) has been shown to offer a low complexity design alternative to spatial multiplexing, where only a subset (down to one) of Radio Frequency (RF) chains are required for transmission [1], [2]. Early work has focused on the design of receiver algorithms for minimizing the bit error ratio of SM at a low complexity [1]-[5]. Matched filtering is shown to be a low-complexity technique for detecting the activated-antenna index [1]-[3]. A maximum likelihood (ML) detector is introduced in [4] for reducing the complexity of classic spatial multiplexing ML detectors, while the complexity imposed can be further reduced by compressive sensing detection approaches [5]. In addition to receive processing, several transmit pre-coding (TPC) approaches have been proposed for receive-antenna (RA) aided SM (RSM), where the spatial information is mapped onto the RA index [6]-[8].

Relevant work has also proposed constellation shaping for SM [9]-[14]. Specifically, in [9] the transmit diversity of coded SM is analyzed for different *spatial constellations*,

which represent the legitimate sets of activated transmit antennas (TAs). Furthermore, the authors of [10] conceived a symbol constellation optimization technique for minimizing the BER. Indeed, spatial- and symbol- constellation shaping are discussed separately in the above mentioned reference. By contrast, the design of the received SM constellation that combines the choice of the TA as well as the transmit symbol constellation, is the focus of this paper. A number of constellation shaping schemes [11]-[14] have also been proposed for the special case of SM, referred to as Space Shift Keying (SSK), where the information is purely carried in the spatial domain, by the activated antenna index (AI). However, the application of the above constellation shaping to the SM transmission, where the transmit waveform is modulated, is non-trivial.

Recent work has focused on shaping the receive SM constellation by means of symbol pre-scaling at the transmitter, aiming for maximizing the minimum Euclidean distance (MED) in the received SM constellation [15]-[17]. The constellation shaping approach of [15], [16] aims for fitting the receive SM constellation to one of the existing optimal classic constellation formats in terms of minimum distance, such as e.g. quadrature amplitude modulation (QAM). Due to the strict constellation fitting requirement imposed on both the amplitude and phase, this pre-scaling relies on the inversion of the channel coefficients. In the case of ill-conditioned channels, this substantially reduces the received signal to noise ratio (SNR). This problem has been alleviated in [17], where a constellation shaping scheme based on phase-only scaling is proposed. Still, the constellation shaping used in the above schemes is limited in the sense that it only applies to multiple input single output (MISO) systems, where a single symbol is received for each transmission and thus the characterization and shaping of the receive SM constellation is simple.

Closely related to this work, a transmit pre-scaling (TPS) scheme was proposed in for SM [19], where the received SM constellation is randomized by TPS for maximizing the MED between its points for a given channel. A number of randomly generated candidate sets of TPS factors are formed off-line, known to both the transmitter and receiver, and the transmitter then selects that particular set of TPS factors which yields the SM constellation having the maximum MED. Against this background, in this paper we propose a low-complexity relaxation of the above optimization instead of an exhaustive search, where the first TPS factor set that is found to satisfy a predetermined threshold is selected, thus reducing the computational burden of the TPS operation. The proposed scheme is shown to provide a scalable trade-off

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between the performance attained and the complexity imposed, by accordingly selecting the MED threshold.

This paper is organised as follows: In Section II the basic system model is first introduced, and the proposed scheme then discussed. The computational complexity of the proposed technique is analysed in Section III, and its performance against the state-of-the-art is evaluated in Section IV. Finally, in Section V we draw the key conclusions of our study.

II. SPATIAL MODULATION WITH THRESHOLD CONSTELLATION RANDOMIZATION (SM-TCR)

Consider a MIMO system, where the transmitter and receiver are equipped with N_t and N_r antennas, respectively. For simplicity, unless stated otherwise, in this paper we assume that the transmit power budget is limited to unity, i.e. $P = 1$. We focus on the single-RF chain SM approach, where the transmit vector is in the all-but-one zero form $\mathbf{s}_m^k = [0, \dots, s_m, \dots, 0]^T$, with $[\cdot]^T$ denoting the transpose operator. Here, $s_m, m \in \{1, \dots, M\}$ is a symbol taken from an M -order modulation alphabet that represents the transmitted waveform in the baseband domain conveying $\log_2(M)$ bits, while k represents the index of the activated TA (the index of the non-zero element in \mathbf{s}_m^k) conveying $\log_2(N_t)$ bits in the spatial domain. Clearly, since \mathbf{s} is an all-zero vector apart from s_m^k , there is no inter-antenna interference.

For the per-antenna TPS approach, which is the focus of this paper, the signal fed to each TA is scaled by a complex-valued coefficient $\alpha_k, k \in \{1, \dots, N_t\}$ for which we have $E\{|\alpha_k|\} = 1$, where $|x|$ denotes the amplitude of a complex number x and $E\{\cdot\}$ denotes the expectation operator. Defining the MIMO channel vector as \mathbf{H} with elements $h_{m,n}$ representing the complex-valued channel coefficient between the n -th TA and the m -th receive antenna (RA), the received symbol vector can be written as

$$\mathbf{y} = \mathbf{H}\mathbf{A}\mathbf{s}_m^k + \mathbf{w}, \quad (1)$$

where $\mathbf{w} \sim \mathcal{CN}(0, \sigma^2 \mathbf{I})$ is the additive white Gaussian noise (AWGN) component at the receiver, with $\mathcal{CN}(\mu, \sigma^2)$ denoting the circularly symmetric complex Gaussian distribution with a mean of μ and variance of σ^2 . Furthermore, $\mathbf{A} = \text{diag}(\mathbf{a})$ is the TPS matrix with $\mathbf{a} = [\alpha_1, \alpha_2, \dots, \alpha_{N_t}]$ and $\text{diag}(\mathbf{g})$ represents the diagonal matrix with its diagonal elements taken from vector \mathbf{g} . Note that the diagonal structure of \mathbf{A} guarantees having a transmit vector $\mathbf{x} = \mathbf{A}\mathbf{s}$ with a single non-zero element, so that the single-RF-chain aspect of SM is preserved.

At the receiver, a joint maximum likelihood (ML) detection of both the TA index and the transmit symbol is obtained by the minimization

$$\begin{aligned} [\hat{s}_m, \hat{k}] &= \arg \min_i \|\mathbf{y} - \hat{\mathbf{y}}_i\| \\ &= \arg \min_{m,k} \|\mathbf{y} - \mathbf{H}\mathbf{A}\mathbf{s}_m^k\|, \end{aligned} \quad (2)$$

where $\|\mathbf{x}\|$ denotes the norm of vector \mathbf{x} and $\hat{\mathbf{y}}_i$ is the i -th constellation point in the received SM constellation. By exploiting the specific structure of the transmit vector this can be further simplified to

$$[\hat{s}_m, \hat{k}] = \arg \min_{m,k} \|\mathbf{y} - \mathbf{h}_k \alpha_m^k s_m\|, \quad (3)$$

where \mathbf{h}_k denotes the k -th column of matrix \mathbf{H} . It is widely recognized that the performance of the detection as formulated above is dominated by the MED between the adjacent constellation points $\hat{\mathbf{y}}_i$ and $\hat{\mathbf{y}}_j$ in the receive SM constellation

$$d_{min} = \min_{i,j} \|\hat{\mathbf{y}}_i - \hat{\mathbf{y}}_j\|^2, \quad i \neq j. \quad (4)$$

Accordingly, to improve the likelihood of correct detection, constellation shaping TPS schemes conceived for SM aim for maximizing this MED. The optimum TPS matrix \mathbf{A}^* can be found by solving the optimization problem of [20]

$$\begin{aligned} \mathbf{A}^* &= \arg \max_{\mathbf{A}} \min_{i,j} \|\hat{\mathbf{y}}_i - \hat{\mathbf{y}}_j\|^2, \quad i \neq j \\ \text{s.t.c.} \quad &\text{trace}(\mathbf{A}^{*H} \mathbf{A}^*) \leq P, \end{aligned} \quad (5)$$

and, additionally for single RF-chain SM, subject to \mathbf{A}^* having a diagonal structure. In the above \mathbf{A}^H and $\text{trace}(\mathbf{A})$ represent the Hermitian transpose and trace of matrix \mathbf{A} respectively. The above optimization however, is an NP hard problem, which makes finding the TPS factors prohibitively complex, and motivates the conception of lower-complexity, suboptimal techniques. Indeed, it has been shown that the TPS approach in [19], by selecting among a set of pre-determined, randomly generated TPS vectors instead of fully optimising the TPS, offers a near optimal performance with the lowest complexity amongst the TPS optimization approaches [20], [21].

TPS Vector Generation: Accordingly, with SM-TCR first, a number of D random candidate TPS vectors are generated, in the form \mathbf{a}_d , where $d \in [1, D]$ denotes the index of the candidate set and \mathbf{a}_d is formed by the elements $\alpha_m^{k(d)} \sim \mathcal{CN}(0, 1)$. To ensure that the average transmit power remains unchanged, the scaling factors are normalized to unit power. These are made available to both the transmitter and receiver before transmission. These assist in randomizing the received constellation, which is most useful in the critical scenarios where two points in the constellation of $\mathbf{H}\mathbf{s}_m^k, m \in [1, M], k \in [1, N_t]$ happen to be very close.

A. Thresholded Selection of TPS

For a given channel, based on the knowledge of vectors \mathbf{a}_d , both the transmitter and receiver can determine the received SM constellation for the d -th TPS set by calculating the legitimate set of $[m, k]$ combinations in

$$\hat{\mathbf{y}} = \mathbf{H}\mathbf{A}_d \mathbf{s}_m^k, \quad (6)$$

where $\mathbf{A}_d = \text{diag}(\mathbf{a}_d)$ is the diagonal matrix that corresponds to the candidate set \mathbf{a}_d . Then, for the given channel coefficients, the transmitter and receiver can choose independently the scaling vector \mathbf{a}_o . Alternatively, if no channel state information is available at the transmitter (receiver), the receiver (transmitter) can inform the transmitter (receiver) concerning the optimum \mathbf{a}_o by transmitting a number of $\lceil \log_2(D) \rceil$ bits. Contrary to the SM-CR of [19], where the maximum MED amongst all D possibilities is chosen, here a threshold based approach is introduced, where the search for TPS is terminated when a candidate TPS is found that satisfies a MED threshold. This optimization problem can be expressed as

$$\mathbf{A}_o = \begin{cases} \mathbf{A}_t, \text{ if } \exists \mathbf{A}_t : \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{H}\mathbf{A}_t \mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{A}_t \mathbf{s}_{m_2}^{k_2}\|^2 \geq \theta \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{H}\mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{s}_{m_2}^{k_2}\|^2 \\ \arg \max_d \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{H}\mathbf{A}_d \mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{A}_d \mathbf{s}_{m_2}^{k_2}\|^2, \text{ otherwise} \end{cases} \quad (7)$$

where θ represents the MED threshold with respect to the MED without TPS. Equivalently, for the case of single RF-chain based SM this can be simplified to

$$\mathbf{A}_o = \begin{cases} \mathbf{A}_t, \text{ if } \exists \mathbf{A}_t : \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{h}_{k_1} a_{m_1}^{k_1} s_{m_1} - \mathbf{h}_{k_2} a_{m_2}^{k_2} s_{m_2}\|^2 \geq \theta \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{h}_{k_1} s_{m_1} - \mathbf{h}_{k_2} s_{m_2}\|^2 \\ \arg \max_d \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \|\mathbf{h}_{k_1} a_{m_1}^{k_1} s_{m_1} - \mathbf{h}_{k_2} a_{m_2}^{k_2} s_{m_2}\|^2, \text{ otherwise} \end{cases} \quad (8)$$

In other words, the search stops if a TPS set is found that satisfies the threshold, otherwise the TPS that offers the maximum MED is returned, following a full search as in SM-CR. For completeness, we present the associated algorithm in Table I. It will be shown that this process offers significant computational benefits with respect to full SM-CR.

Based on (8), the transmitter sends $\mathbf{x} = \mathbf{A}_o \mathbf{s}_m^k$ and the receiver applies the ML detector according to

$$[\hat{s}_m, \hat{k}] = \arg \min_{m,k} \|\mathbf{y} - \mathbf{H}\mathbf{A}_o \mathbf{s}_m^k\|. \quad (9)$$

It should be noted that, to dispense with the need for channel state information at the transmitter (CSIT), the receiver can select the best scaling factors using (8) and then feed the index of the scaling matrix \mathbf{A}_o selected from the set of D candidates back to the transmitter, using $\lceil \log_2(D) \rceil$ bits. This constitutes a major overhead saving for the proposed scheme with respect to existing TPS schemes for SM that require full CSIT, while obtaining similar performance.

Input : $\mathbf{H}, M, \quad \mathbf{Output} : \mathbf{A}_o$

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e = []
for t = 1 to D do
    e[t] := min_{\{m_i, k_j\} \neq \{m_l, k_p\}} \|\mathbf{H}\mathbf{A}_t \mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{A}_t \mathbf{s}_{m_2}^{k_2}\|^2
    % calculate the MED for the t-th TSP vector
    if e[t] \ge \theta \min_{\{m_i, k_j\} \neq \{m_l, k_p\}} \|\mathbf{H}\mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{s}_{m_2}^{k_2}\|^2
    % check if the MED satisfies the MED threshold \theta
        \mathbf{A}_o := \mathbf{A}_t
        % if so, select \mathbf{A}_t and terminate the algorithm
        break
    end
end
t_o = \arg \max_t e
% if not, select the TPS vector with the max MED
\mathbf{A}_o := \mathbf{A}_{t_o}

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TABLE I: ALGORITHM SM-TCR

SM-TCR	Operations	
<i>Constellation Optimization</i>		
$\mathbf{H}\mathbf{A}_d \mathbf{s}_m^k, \forall m, k$	$\times t$	$(2N_r + 1)N_t M t$
$\mathbf{f}_{m_1, m_2}^{k_1, k_2(d)} = \ \mathbf{H}\mathbf{A}_d \mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{A}_d \mathbf{s}_{m_2}^{k_2}\ , \forall m_1, m_2, k_1, k_2, m_1 \neq m_2, k_1 \neq k_2$	$\times t$	$2N_r \binom{N_t M}{2} t$
check: $\min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \{\mathbf{f}_{m_1, m_2}^{k_1, k_2(d)}\} \geq \theta \min_{\substack{\{m_i, k_j\} \neq \\ \{m_l, k_p\}}} \ \mathbf{H}\mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{s}_{m_2}^{k_2}\ ^2$	$\times t$	$\binom{N_t M}{2} t$
<i>ML Detection</i>		
$g_m^k = \ \mathbf{y} - \mathbf{H}\mathbf{A}_o \mathbf{s}_m^k\ ^2, \forall m, k$	$\times B$	$2N_t M N_r B$
$\arg \min g_m^k$	$\times B$	$N_t M B$
Total: $(2N_r + 1) \left[\binom{N_t M}{2} + N_t M \right] t + (2N_r + 1) N_t M B$		

TABLE II: Complexity for the proposed SM-TCR scheme.

B. Transmit Diversity and Performance Trends

While the transmit diversity order of the single-RF SM is known to be one [9], the proposed TPS introduces an amplitude-phase diversity in the transmission, which is an explicit benefit of having D candidate sets of TPS factors to choose from. Accordingly, it was shown in [19] that the obtained transmit diversity order corresponds to the θ -dependent gain in the average MED associated with constellation randomization as

$$G(\theta) \triangleq \frac{E\{\min_{m,k} \|\mathbf{H}\mathbf{A}_o \mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{A}_o \mathbf{s}_{m_2}^{k_2}\|^2\}}{E\{\min_{m,k} \|\mathbf{H}\mathbf{s}_{m_1}^{k_1} - \mathbf{H}\mathbf{s}_{m_2}^{k_2}\|^2\}}. \quad (10)$$

In addition, SM systems with N_r uncorrelated RAs have been shown to experience a unity transmit diversity order and a receive diversity order of N_r . Accordingly, since the proposed scheme attains a θ -dependent transmit diversity order of $G(\theta)$, the total diversity order becomes $\delta = N_r G(\theta)$. The resulting probability of error P_e obeys the high-SNR trend of

$$P_e = \alpha \gamma^{-N_r G(\theta)}, \quad (11)$$

where γ is the transmit SNR, and α is an arbitrary non-negative coefficient. We verify the above theoretical performance trend against simulation in the following.

III. COMPUTATIONAL COMPLEXITY

It is clear from the above discussion that the proposed SM-TCR leads to a computational complexity reduction with respect to conventional SM-CR, due to the early termination of the TPS search, after a calculation of $t \leq D$ out of D TPS sets. In this section we analyze this computational complexity reduction at the receiver. This analysis is complemented by the following results on the distribution of t . For reference, we have assumed an LTE Type 2 TDD frame structure [18]. This has a 10ms duration which consists of 10 sub-frames out of which 5 sub-frames, containing 14 symbol time-slots each, are used for downlink transmission yielding a frame size of $F = 70$ for the downlink, while the rest are used for both uplink and control information transmission. A slow fading

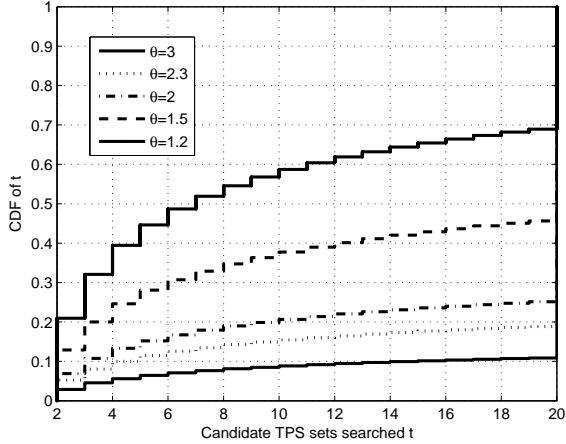


Fig. 1. CDF of the number of candidate TPS searched (t) for various values of θ , $D=20$, 4QAM.

channel is assumed, where the channel remains constant for the duration of the frame. Following the complexity analysis of [19], we quantify the number of operations required in each step of the SM-TCR search in Table II. From the table, we have a total SM-TCR receiver complexity of

$$C(t) = (2Nr + 1) \left[\binom{N_t M}{2} + N_t M \right] t + (2Nr + 1) N_t M B. \quad (12)$$

To complete this complexity discussion, in Fig. 1 we show the distribution of t as a function of the increasing threshold values of θ . It can be seen that low numbers of candidate TPS searched t are obtained with high probability, especially in the cases of low MED thresholds θ . While large complexity savings can be observed in the figure, it is important to note that the complexity of SM-TCR is upper bounded by that of SM-CR, since $t \leq D$.

IV. SIMULATION RESULTS

To evaluate the benefits of the proposed technique, this section presents numerical results based on Monte Carlo simulations of conventional SM without scaling (termed as SM in the figures), SM-CR and the proposed SM-TCR. The channel's impulse response is assumed to be perfectly known at the transmitter. Without loss of generality we assume that the transmit power is restricted to $P = 1$. MIMO systems with 4 TAs employing 4QAM and 16QAM modulation are explored, albeit it is plausible that the benefits of the proposed technique extend to larger-scale systems and higher order modulation.

First, we characterise the attainable BER performance with increasing transmit SNR for a (4×2) -element MIMO employing 4QAM and 16QAM, for various values of the MED threshold θ in Fig. 2. The performance of the highly-complex TPS design in [21] based on convex optimization, and termed SM-OTPS in the figure, is also shown here for reference, where it can be seen that the proposed SM-TCR, with orders-of-magnitude less complexity than SM-OTPS still performs

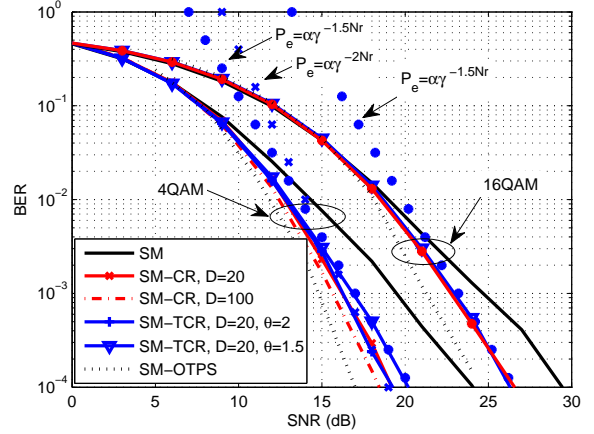


Fig. 2. BER vs. SNR for a (4×2) element MIMO with SM, SM-OTPS, SM-CR and SM-TCR, 4QAM and 16QAM.

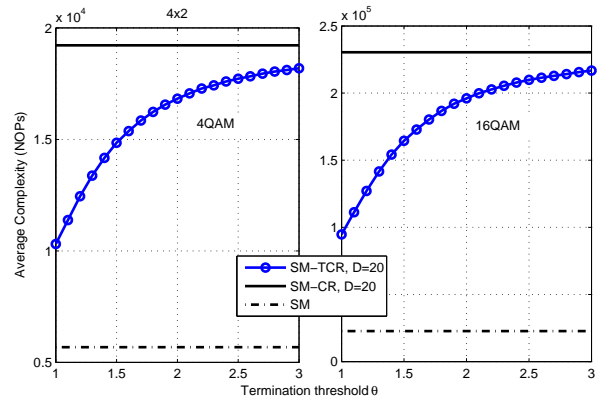


Fig. 3. Average complexity vs θ for a (4×2) element MIMO with SM-TCR, 4QAM and 16QAM.

within 1-2dB from the optimization-based SM-OTPS. The theoretical trends of (11) are also shown where it can be seen that they provide a close match for the high-SNR system behaviour. It can be seen that the slope of the BER curves increases with increasing θ which indicates an increase in transmit diversity order. Indeed, the BER of SM-TCR is identical to that of SM-CR for $\theta = 2$ in the case of 4QAM and $\theta = 1.5$ in the case of 16QAM. In both cases significant complexity savings are obtained, as shown in the results that follow.

Fig. 3 illustrates the average computational complexity expressed in terms of numbers of operations (NOPs) for SM-TCR with increasing MED threshold values θ . The complexity of SM and SM-CR is also depicted for reference. It can be seen that as the MED threshold increases, the optimization becomes tighter, leading to complexity close to that of the full SM-CR. For reduced values of θ however, significant complexity gains are obtained, where the NOPs for SM-TCR are down to less than 55% of those for SM-CR for 4QAM and 40% for 16QAM, respectively. A similar trend can be observed in Fig. 4 where the performance is shown for increasing θ , where

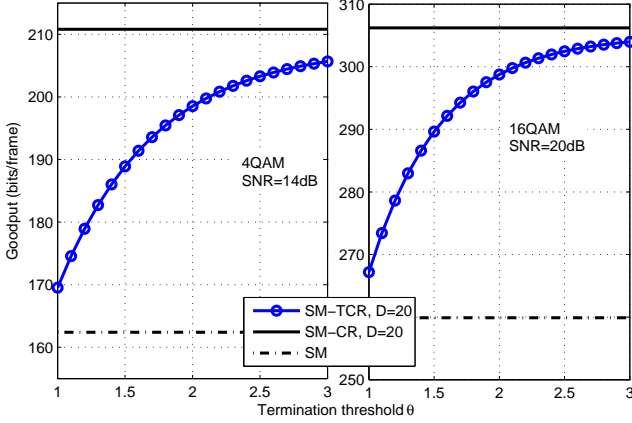


Fig. 4. Goodput vs θ for a (4×2) element MIMO with SM-TCR, 4QAM and 16QAM.

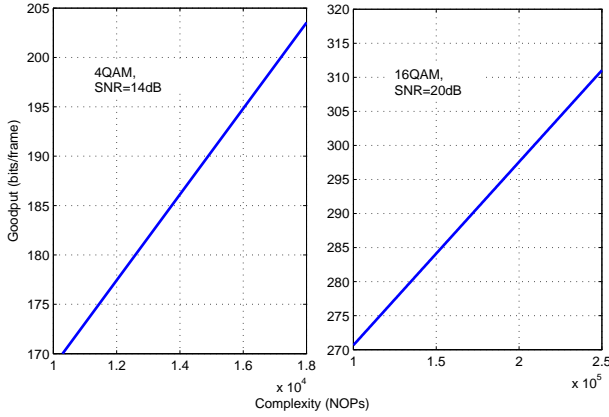


Fig. 5. Goodput vs average complexity for a (4×2) element MIMO with SM-TCR, 4QAM and 16QAM.

performance is quantified in terms of goodput in bits per frame

$$T = \log_2(N_t M) \cdot F(1 - P_F), \quad (13)$$

with P_F denoting the frame error probability and $F = 70$ being the frame length used in these results, following [19]. The specific selection of the MED threshold θ in practice can be based on the desired tradeoff between the complexity in Fig. 3 and (12), the transmit diversity obtained and the performance observed in Fig. 4 and (10) - (11). Finally, Fig. 5 shows the direct performance-vs-complexity trade-off. A linear relation between goodput and complexity can be observed. More importantly, where previously either a low-complexity unit-diversity SM or a high-complexity high-diversity SM-CR alternative could be chosen, here a scalable trade-off is offered between these two extremes with the aid of SM-TCR, by selecting the MED thresholds θ accordingly.

V. CONCLUSIONS

A new low-complexity constellation shaping approach has been introduced for spatial modulation. While conventional constellation randomization offers a considerable transmit diversity gain at the cost of an increased computational complexity compared to the conventional SM, the proposed scheme

delivers a scalable trade-off between the transmit diversity obtained and the complexity by appropriately selecting the MED threshold values. Complexity reduction of up to 60% over conventional constellation randomization was demonstrated, while still considerably improving the attainable performance of conventional SM.

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