

IMF shape constraints from stellar populations and dynamics from CALIFA

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ABSTRACT

In this Paper, we describe how we use stellar dynamics information to constrain the shape of the stellar initial mass function (IMF) in a sample of 27 early-type galaxies from the CALIFA survey. We obtain dynamical and stellar mass-to-light ratios, Υ_{dyn} and Υ_* , over a homogenous aperture of $0.5 R_e$. We use the constraint $\Upsilon_{\text{dyn}} \geq \Upsilon_*$ to test two IMF shapes within the framework of the extended MILES stellar population models. We rule out a single power-law IMF shape for 75 per cent of the galaxies in our sample. Conversely, we find that a double power-law IMF shape with a varying high-mass end slope is compatible (within 1σ) with 95 per cent of the galaxies. We also show that dynamical and stellar IMF mismatch factors give consistent results for the systematic variation of the IMF in these galaxies.

Key words: galaxies: elliptical and lenticular, cD – galaxies: kinematics and dynamics – galaxies: stellar content.

1 INTRODUCTION

The stellar initial mass function (IMF) is a fundamental parameter in stellar population theory. Traditionally considered to be universal

(e.g. Bastian, Covey & Meyer 2010), over the last years, there is mounting evidence suggesting variations of the IMF, both between and within galaxies. These IMF variations are claimed based on a plethora of methods. The strength of gravity-sensitive stellar features in the spectra of galaxies implies a larger fraction of low-mass stars with increasing galaxy mass and decreasing radius (e.g. van Dokkum & Conroy 2010; Conroy & van Dokkum 2012; Ferreras

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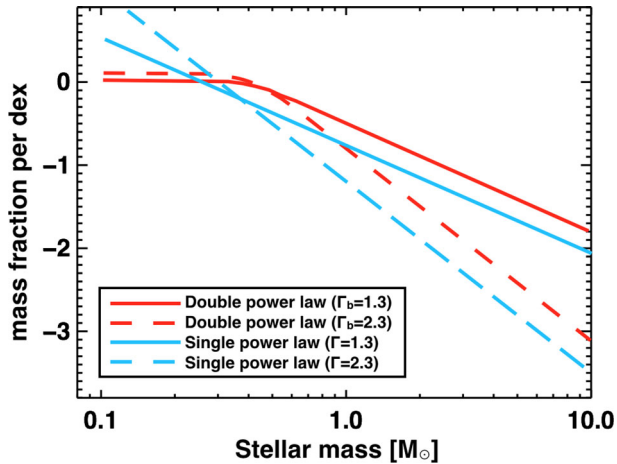


Figure 1. The two IMF shapes studied in this Paper.

et al. 2013; La Barbera, Ferreras & Vazdekis 2015; Martín-Navarro et al. 2015a). Further support for a varying IMF came by constraints from strong gravitational lensing (e.g. Treu et al. 2010; Spiniello et al. 2012; Dutton et al. 2013; Smith, Lucey & Conroy 2015) and/or stellar dynamics (e.g. Thomas et al. 2011; Cappellari et al. 2012; Tortora, Romanowsky & Napolitano 2013).

These studies, however, do not always agree on the kind of variation and which process is driving it (Smith 2014). There are several possible reasons ranging from random sample selections to differences between the adopted stellar population models and how they treat the variation of the IMF. The latter has been partially remedied by the comparison of Spiniello, Trager & Koopmans (2015). However, a systematic study to the same data employing a consistent set of assumptions between orthogonal IMF diagnostics is lacking. But before we are able to discuss any consistencies (or the lack thereof), it is worth exploring whether there are particular IMF shapes that are disfavoured by the constraints that the stellar kinematics of galaxies gives us, which are free from any assumptions of the stellar population modelling. This is the aim of the work presented here. We construct dynamical models of a sample of early-type galaxies from the CALIFA survey and use the stringent constraint that the dynamical mass-to-light ratio of a galaxy is an upper limit to the stellar populations mass-to-light ratio.

2 THE STELLAR POPULATIONS MODEL

For this study, we used the extended version of the MILES models (Vazdekis et al. 2010, 2012). These models allowed us not only to vary the slope of the IMF, but also its functional form, and thus they were optimally suited for the purpose of this study. We explored two different IMF shapes, namely, single and double power law (see Fig. 1). The single power-law IMF shape, also known as unimodal, is defined by a single power law, with a logarithmic slope Γ . Under this parametrization, a Salpeter IMF (Salpeter 1955) has $\Gamma = 1.35$. The double power-law IMF (or bimodal; Vazdekis et al. 1996) is described by two power laws joined by a spline. The only free parameter of that function is the slope of the high-mass end Γ_b (above $0.6 M_\odot$), and it is tapered for stars with masses below $0.5 M_\odot$. For $\Gamma_b = 1.3$, this double power-law IMF is almost indistinguishable from a Kroupa IMF (Kroupa 2001).

It is important to mention that for relatively old stellar populations (as expected in early-type galaxies), only stars with masses below $\sim 1 M_\odot$ are present. This limits our stellar populations-based IMF

analysis to its low-mass end. La Barbera et al. (2013) have shown that IMF measurements based on stellar population analysis to date are only sensitive to the ratio between stars above and below $\sim 0.5 M_\odot$ ($F_{0.5}$ hereafter). Although the two IMF parametrizations available in the MILES models formally vary the high-mass end of the IMF (through the Γ and Γ_b parameters), in practice, the $F_{0.5}$ is also varied since the models are normalized to a total mass of $1 M_\odot$.

3 THE GALAXIES AND THEIR MASS-TO-LIGHT RATIOS

We chose our sample of galaxies from the CALIFA survey (Sánchez et al. 2012). They all reside in the redshift range $0.018 < z < 0.030$ and have average stellar masses $\sim 10^{12} M_\odot$ (Salpeter IMF assumed; González Delgado et al. 2014). 20 of the galaxies were previously analysed by Martín-Navarro et al. (2015b). The remaining seven were observed as part of a dedicated proposal and are featured in the CALIFA Data Release 3 (Sánchez et al. 2016). The PMAS/PPAK IFU data have all been observed, reduced and analysed in the same way, both in terms of stellar populations and dynamics. All quoted mass-to-light ratios refer to Sloan Digital Sky Survey (SDSS) r band, i.e. $\Upsilon \equiv (M/L)_r$ in solar units.

We chose to explore only the inner $0.5 R_e$ of our sample of galaxies. In this way, we minimize the contribution of dark matter to the dynamical mass of the galaxies, which is expected to be increasing at larger radii (e.g. Treu & Koopmans 2004). We also ensured optimal signal-to-noise ratios to extract consistently dynamics and stellar population parameters.

3.1 Stellar mass-to-light ratios, Υ_*

To derive the stellar mass-to-light ratios Υ_* we followed the stellar population analysis described in Martín-Navarro et al. (2015b). In brief, we used the H_{β_0} , $[MgFe]'$, and $TiO_{2CALIFA}$ indices – an age, metallicity, and IMF slope indicator, respectively – as these have proved to be the most reliable index combination within the CALIFA wavelength range.¹ We measured their values in the spectra integrated over the $0.5 R_e$ elliptical aperture of each galaxy and compared them to the model predictions, convolved to the velocity dispersion of the galaxy. We thus obtained a best-fitting age, metallicity, and IMF slope, which were translated into SDSS r -band Υ_* predicted by the MILES models. All stellar population parameters are single stellar population (SSP)-equivalent parameters. We consider this choice to be safe following the work of La Barbera et al. (2013) and Martín-Navarro et al. (2015b) who showed that non-SSP star formation histories do not significantly alter the stellar population IMF determinations for early-type galaxies. The stellar $(M/L)_r$, in contrast, does depend on the star formation history, but the old luminosity-weighted ages in our sample (>8 Gyr) ensure a negligible contribution of young stars to the integrated light of our galaxies.

We used the 1σ uncertainties of the line-strength measurements, propagated through our analysis, to estimate the errors on the resulting stellar mass-to-light ratios. As our analysis is based on the same set of population models, systematic errors will be common

¹ Note that the TiO_2 index increases with $[\alpha/Fe]$ but decreases with $[C/Fe]$. Since both α -elements and carbon are enhanced in early-type galaxies, the net sensitivity of the TiO_2 line to the abundance pattern remains marginal. A more detailed justification of our index selection is given in Martín-Navarro et al. (2015b).

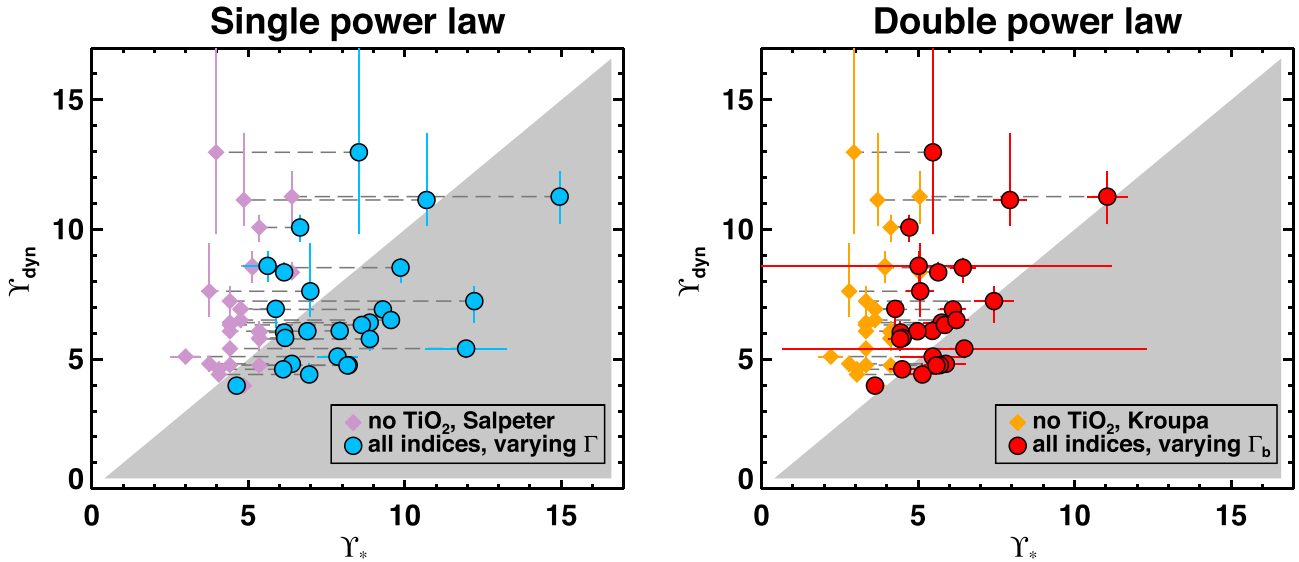


Figure 2. Dynamical versus stellar mass-to-light ratios of our sample of galaxies with the two chosen IMF shapes with varying slopes: single power law (left-hand panel) and double power law (right-hand panel). The shaded area represents the ‘forbidden’ region where the requirement of $\Upsilon_{\text{dyn}} \geq \Upsilon_*$ is violated. The lilac (Salpeter IMF assumed) and yellow (Kroupa IMF assumed) diamonds represent the Υ_* when the stellar population parameters are derived using the classical diagnostic diagram $H_{\beta_0} - [\text{MgFe}]'$. The blue and red circles denote the galaxies when Υ_* was determined including the stellar gravity-sensitive feature $\text{TiO}_{2\text{CALIFA}}$ and varying slopes of the IMFs. The grey horizontal dashed lines connect the various stellar mass-to-light ratios for the same objects for clarity.

to all models, and so we neglect any additional systematic error component.

For comparison, we also estimated the galaxies’ mass-to-light ratios based on their H_{β_0} and $[\text{MgFe}]'$ line strengths only, i.e. without any constraint on the IMF slope, and assuming the two standard IMF shapes, Kroupa and Salpeter.

3.2 Dynamical mass-to-light ratios, Υ_{dyn}

We derived Υ_{dyn} values of the galaxies by fitting axisymmetric dynamical models to their stellar kinematic maps. In brief, we parametrized the galaxies’ stellar surface brightness by applying the multiGaussian expansion method (Emsellem, Monnet & Bacon 1994; Cappellari 2002) to their r -band images from the 7th data release of the SDSS (Abazajian et al. 2009). Then, we fitted the CALIFA stellar mean velocity and velocity dispersion fields (Falcón-Barroso et al. 2016) with axisymmetric dynamical models, based on a solution of the Jeans equations as implemented by Cappellari (2008). To be consistent with the aperture where the stellar mass-to-light ratio was derived, as explained above, we fitted the stellar kinematics maps only inside the elliptical aperture of $0.5 R_e$. We estimated the inclinations of the galaxies based on their global ellipticity (van de Ven et al., in preparation). We allowed the velocity anisotropy in the meridional plane β_z to vary in the range $(-0.5, 1)$. The best fit based on χ^2 statistics then yielded our Υ_{dyn} and the corresponding statistical error (typically ~ 5 per cent). In order to be consistent in our presentation, we did not take into account any systematic errors here, as in the case with Υ_* discussed above. We discuss the effects of these systematic errors on our analysis in Section 4.

While, in principle, both the velocity anisotropy and the mass-to-light ratio may vary with radius, we found that this did not significantly improve the fit within $0.5 R_e$. The strongest gradients in the stellar Υ are expected in low-mass early-type galaxies (Spolaor et al. 2009; Kuntschner et al. 2010), where the departure from

a standard IMF slope is minimal. Therefore, we do not expect a systematic bias in our measurements due to gradients in the stellar population properties. Whereas we choose to avoid fitting for a particular dark matter distribution, our dynamical mass-to-light ratio allows for a contribution from dark matter within the explored radius. When we compare with the best-fitting stellar mass-to-light ratio, we find small dark matter fractions in agreement with the ~ 13 per cent found previously in such massive early-type galaxies (Cappellari et al. 2013). The details of our dynamical models and resulting dark matter fractions are described in a forthcoming paper (Lyubenova et al., in preparation).

4 CONSTRAINING THE SHAPE OF THE IMF

We used the stringent requirement that the dynamical mass-to-light ratio (Υ_{dyn}) should be always greater than or equal to the stellar mass-to-light ratio (Υ_*) to exclude certain types of IMF shapes.

In Fig. 2, we compared the Υ_* and Υ_{dyn} of our sample of galaxies for a selection of IMF shapes. The diamond symbols denote Υ_* when we derived the stellar population parameters using only the H_{β_0} and $[\text{MgFe}]'$ line strengths under the assumption of a Salpeter IMF (lilac diamonds in the left-hand panel; Salpeter 1955) or a Milky Way-like IMF (yellow symbols in the right-hand panel; Kroupa 2001). We refer to these mass-to-light ratios as ‘classical’. The blue circles on the left-hand panel denote our Υ_* with stellar population parameters derived from the complete set of indices (H_{β_0} , $[\text{MgFe}]'$, and $\text{TiO}_{2\text{CALIFA}}$) and a single power-law IMF with a varying slope Γ . Under this parametrization, we find that $0.4 \lesssim \Gamma \lesssim 2.2$ in our sample of galaxies. On the right-hand panel, the red symbols denote Υ_* derived in the same way, but with a double power-law IMF, whose high-mass end slope Γ_b varies in the range $0.5 \lesssim \Gamma_b \lesssim 3.1$. The measured ranges of Γ and Γ_b values are in agreement with those found by La Barbera et al. (2016)

While the classical Υ_* (yellow and lilac diamonds) stay within a narrow range, consistent with the narrow range of stellar

population properties of our sample of galaxies, Υ_{dyn} shows a much larger spread. If indeed we keep the assumption of a universal IMF, this would be indicative of extremely high dark matter fractions inside the central $0.5 R_e$ for many of the galaxies. The dark matter fractions are less high when using a classical Salpeter IMF instead of a classical Kroupa IMF (lilac versus orange points), but still in disagreement with previous dark matter-fraction derivations (e.g. Cappellari et al. 2013). Moreover, a Salpeter IMF does not match the observed $\text{TiO}_{2\text{CALIFA}}$ index values. The single power-law IMF with varying slope Γ (blue symbols on the left-hand panel) would bring the galaxies with the highest Υ_{dyn} closer to the one-to-one relation with Υ_* . However, if such an IMF variation is applied to our complete sample, ~ 75 per cent of our galaxies move to the ‘forbidden’ region. Thus, we disfavour this single power-law IMF shape.

We consider our result to be robust even when including systematic errors. A conservative estimate for these systematics is roughly 20 per cent on both Υ_* and Υ_{dyn} . The largest uncertainty in our method to estimate Υ_* is driven by the assumptions on the SFH (Gallazzi & Bell 2009). The largest uncertainty on Υ_{dyn} comes from the redshift-based distances to the galaxies (Falc3n-Barroso et al. 2011). However, even when taking into account these conservative error estimates, our result will not be affected.

As evident from the right-hand panel of Fig. 2, when we used a double power-law IMF with a varying high-mass end slope Γ_b (red symbols), 95 per cent of the galaxies in our sample are either above the forbidden area or within 1σ of the demarcation line. Our result is consistent with the finding of La Barbera et al. (2016) who constrain both the shape and the normalization of the IMF based only on their stellar populations analysis and favour the same double power-law IMF.

In the past, galaxies with Υ_{dyn} much higher than SSP-equivalent Υ_* have been explained with having composite star formation histories that would increase the Υ_* compared to the SSP-equivalent ones (e.g. Cappellari et al. 2006; Trager, Faber & Dressler 2008). However, this explanation was feasible only for the light-weighted properties of low-mass galaxies. We consider our result to be robust against composite SFH, as the choice of non-SSP SFH has little effect on the IMF determination in early-type galaxies (see Section 3.1).

5 STELLAR POPULATIONS AND DYNAMICS GIVE CONSISTENT RESULTS FOR THE IMF VARIATION

As outlined in Section 1, there are several approaches to test the (non)-universality of the IMF. The existence of non-universal IMFs requires, at the very least, a consistency between stellar population and dynamical estimates of mass-to-light ratios (Smith 2014). But a simple correlation between Υ_* and Υ_{dyn} , or the lack thereof, cannot be uniquely used to search for variations in the IMF as it can be largely driven by underlying stellar population properties, like age and chemical composition. Indeed, Smith (2014) has compared literature studies of 34 early-type galaxies and showed that their Υ_* correlate with Υ_{dyn} . However, when he considered the underlying stellar population properties, he found no further correlation on a galaxy-by-galaxy basis.

We used our sample to test whether stellar populations and dynamics give consistent results about a systematically varying IMF. We first removed the effect on Υ of the underlying stellar population properties, other than the IMF, by normalizing the mass-to-light ratios to a reference Υ_{ref} . This reference is the Υ of a stellar

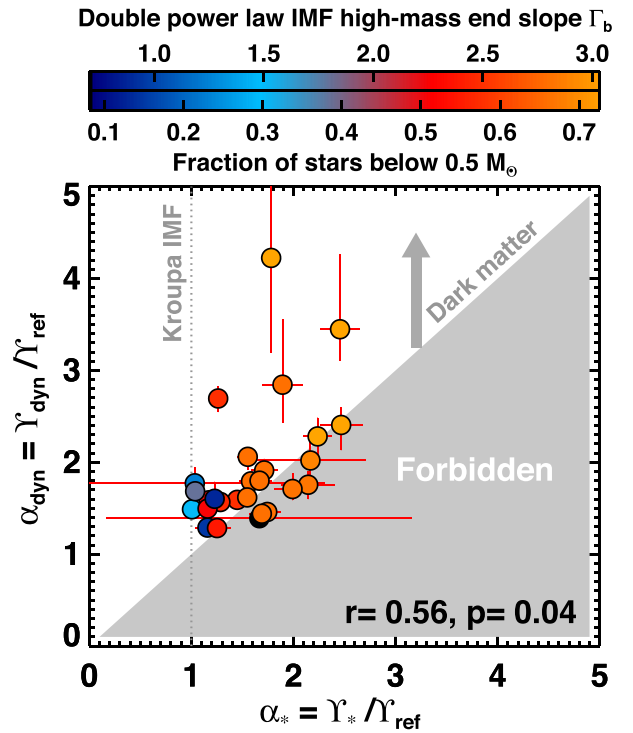


Figure 3. Stellar and dynamical IMF mismatch factors. Their Spearman rank correlation test coefficient r and probability of no correlation p are displayed in the lower-right corner. The galaxies are colour-coded by their fraction of stars below $0.5 M_{\odot}$ (i.e. $F_{0.5}$), as inferred from their stellar populations analysis. The corresponding slope Γ_b of the high-mass end of a double power-law IMF is also given for clarity.

population with the same age and metallicity as the one derived when we allowed the IMF slope to vary but with a fixed IMF shape and normalization. Our chosen Υ_{ref} is that based on a Kroupa IMF (i.e. double power law). This ratio then is often called ‘the IMF mismatch factor’, α_* . $\alpha_* = \Upsilon_* / \Upsilon_{\text{ref}} = 1$ implies that the galaxy has a mass-to-light ratio with the chosen reference IMF (e.g. Milky Way like in our case). $\alpha_* > 1$ indicates departures from this IMF normalization towards both lower or higher $F_{0.5}$ (i.e. top- or bottom-heavier IMF) due to the higher fraction of stellar remnants or low-mass stars, respectively. $\alpha_{\text{dyn}} = \Upsilon_{\text{dyn}} / \Upsilon_{\text{ref}} = 1$ indicates that the galaxy has the chosen reference IMF and no dark matter content. Thus, $\alpha_{\text{dyn}} > 1$ is indicative of either IMF variation or presence of dark matter inside the probed aperture, or both.

In Fig. 3, we plotted our derived dynamical and stellar IMF mismatch factors. For α_* , we used the mass-to-light ratios coming from the fits with a double power-law shape IMF with a varying high-mass end slope. We note that, on average, our sample has a mean $\alpha_* \sim \alpha_{\text{dyn}} \sim 1.6$. Therefore, we conclude, similarly to Smith (2014), that the spectroscopic and dynamic claims of a variable IMF agree on average. These average values are remarkably close to the mass scaling factor when one converts from Kroupa to a Salpeter IMF. However, in Section 4, we showed that our dynamical mass-to-light ratios allow us to exclude single power-law IMFs, such as the Salpeter one, for 75 per cent of our sample, as their stellar mass-to-light ratios become unphysical.

Further, we used the Spearman rank correlation test to probe the correlation between the stellar and the dynamical α , taking into account their uncertainties. The corresponding correlation coefficient is $r = 0.56$. This correlation is much stronger than the one found by

Smith (2014). Moreover, the probability that a correlation between α_* and α_{dyn} does not exist is only 4 per cent. This is in stark contrast with the conclusion of Smith (2014) that there is no agreement on a case-by-case basis. There are several reasons which might lead to these differences. Smith (2014) compares α_* and α_{dyn} derived on the same objects but using two very different data sets that cover different extents of the galaxies. Υ_{dyn} is derived from integral field data covering up to $1 R_e$ from the Atlas3D survey (Cappellari et al. 2013). On the other hand, Υ_* is derived after fitting the galaxies' spectra integrated over $1/8 R_e$, covering a different and more extensive range of features (Conroy & van Dokkum 2012). However, these aperture differences are unlikely to be the dominant source of scatter. Actually, approximately half of the compared galaxies lie in the forbidden by dynamics area (see fig. 1 of Smith 2014). Therefore, the lack of correlation might, in part, be caused by unphysical stellar mass-to-light ratios as a result of the adopted IMF shape by Conroy & van Dokkum (2012). It is beyond the scope of this Paper to investigate the differences in the resulting mass-to-light ratios between the double power-law IMF shape that we used here and the three segmented IMF shape of Conroy & van Dokkum (2012), moreover, that the two stellar population analysis methodologies differ significantly. Alternatively, the lack of correlation between α_* and α_{dyn} could be due to the non-optimal correction of the dynamical mass-to-light ratios for dark matter by Cappellari et al. (2013). This, however, is less likely as these authors tested various dark matter profiles and found similar results. Moreover, we obtained consistent dark matter fractions (see the end of Section 3.2), despite the different approach in determining this contribution to the total mass budget of the galaxies.

Almost all of the galaxies in our sample have α_* and α_{dyn} values consistently above unity. These variations of the α values are larger than the measurement errors and imply inconsistency with a single universal IMF. For a better illustration of this, we colour-coded the galaxies in Fig. 3 according to their fraction of stars below $0.5 M_{\odot}$ ($F_{0.5}$) as derived from the stellar population analysis. For guidance, we also indicated with a colour bar the inferred high-mass end slope Γ_b of the double power-law IMF. The variation in α_* directly follows the change in $F_{0.5}$ as we use the $F_{0.5}$ to determine Υ_* from the stellar population analysis. However, α_{dyn} is independent of the $F_{0.5}$. Thus, the observed correlation between these two – in other words, galaxies with a higher dynamical IMF mismatch factor have also a higher content of low-mass stars (or bottom-heavier IMF) – is yet another consistency check for a systematically varying IMF between early-type galaxies.

6 CONCLUSIONS

The ongoing debate about the exact kind of variation of the stellar IMF in early-type galaxies poses several challenges in our understanding of galaxy evolution (e.g. Martín-Navarro 2016). Before accepting any of the proposed variations, it is of paramount importance to perform consistency checks by independent methods. In this Paper, we tested a few particular shapes of the IMF within the framework of the MILES stellar population models (Vazdekis et al. 2010, 2012). We used a sample of 27 CALIFA galaxies and performed a homogenous analysis of their stellar populations and kinematics. We obtained their stellar and dynamical mass-to-light ratios over the same aperture of $0.5 R_e$ for every galaxy. Our stellar mass-to-light ratios are determined by the combination of the $H_{\beta 0}$, $[\text{MgFe}]'$, and $\text{TiO}_{2\text{-CALIFA}}$ indices – an age, metallicity, and IMF slope indicator, respectively – in the integrated spectra of the galaxies. Our

dynamical mass-to-light ratios are the result of Jeans axisymmetric dynamical models of the two-dimensional stellar kinematics.

After comparing the so derived stellar and dynamical mass-to-light ratios, we find the following results.

(i) Single power-law (unimodal) IMF with a varying slope is excluded for 75 per cent of the galaxies in our sample.

(ii) Conversely, a double power-law (bimodal) IMF shape with a varying high-mass end slope is consistent (within 1σ) with the dynamical constraints for 95 per cent of our sample.

(iii) Stellar populations and dynamics IMF mismatch factors give consistent results for the IMF variation for our CALIFA sample.

In this Paper, we have illustrated how valuable the constraints from dynamics can be when determining the shape of the stellar IMF in early-type galaxies. In this study, we chose to limit our analysis to only one stellar population model that allowed us to vary the slope of the IMF and its functional form. We leave the investigation of other shapes of the IMF, as well as other stellar population models, to a forthcoming publication. Furthermore, this method is applicable not only to the integrated spectra of galaxies, but gives promising results when constraining the radial IMF variation and dark matter content of giant early-type galaxies, independent on any assumptions on the dark matter halo profile, as we will show in a forthcoming publication.

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