

## Spectroscopy and dynamics of unoccupied electronic states of the topological insulators $\text{Sb}_2\text{Te}_3$ and $\text{Sb}_2\text{Te}_2\text{S}$

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Time- and angle-resolved two-photon photoemission (2PPE) was used to study the electronic structure and ultrafast electron dynamics of the *p*-doped topological insulator  $\text{Sb}_2\text{Te}_3$  and its derivative  $\text{Sb}_2\text{Te}_2\text{S}$ . Our 2PPE experiments directly reveal that the massless Dirac-cone like energy dispersion of topological surface states is realized above the Fermi energy in both materials. The observed bulk conduction bands of  $\text{Sb}_2\text{Te}_2\text{S}$  are found to be shifted to higher energies as compared to  $\text{Sb}_2\text{Te}_3$ . This shift has, however, surprisingly almost no influence on the electron dynamics in the topological surface state, which proceed on a picosecond time scale.

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Three-dimensional topological insulators have attracted a lot of attention due to the unique transport properties of electrons in the topological surface state (TSS), which are directly related to its spin texture and Dirac-cone-like energy dispersion [1]. Particularly promising materials of this class are  $\text{Sb}_2\text{Te}_3$  and derivatives. The study of magnetic coupling, e.g., is most progressed in magnetic doped  $\text{Sb}_2\text{Te}_3$  compounds, which finally resulted in the observation of the anomalous quantum Hall effect [2]. Moreover, it has been suggested that the substitution of the central Te layer in the quintuple layers of  $\text{Sb}_2\text{Te}_3$  by S considerably increases the band gap and shifts the Dirac point above the valence-band maximum into the bulk band gap [3,4]. In this way,  $\text{Sb}_2\text{Te}_2\text{S}$  is expected to attain a number of specific advantages in terms of transport properties. Despite the importance of these compounds, experimental investigations of their electronic structure are scarce. So far, the presence of a massless energy dispersion of the TSS could be only concluded from Landau-level spectroscopy of  $\text{Sb}_2\text{Te}_3$  thin films [5]. The reason for this lack of spectroscopic data is substitutional Sb defects at Te sites [6], which result in *p* doping of  $\text{Sb}_2\text{Te}_3$ . This makes it difficult to perform direct band mapping of the TSS by angle-resolved photoelectron spectroscopy (ARPES) [7,8], unlike for the widely studied  $\text{Bi}_2\text{Se}_3$ , which has the same tetradymitelike crystal structure as  $\text{Sb}_2\text{Te}_3$  but is found to be *n* doped.

In this Rapid Communication, we present a study of the electronic structure and ultrafast electron dynamics of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  by two-photon photoemission (2PPE), a combination of ARPES with laser pump-probe techniques [9]. Because this technique uses short pump pulses to populate initially unoccupied states before the excited electrons are photoemitted by time-delayed probe pulses, it is particularly well suited for the investigation of *p*-doped topological insulators. It can not only explore the electronic structure above the Fermi energy, but makes it also possible to study the dynamics of excited electrons in the TSS directly in the time domain [9–15]. Our 2PPE experiments unambiguously

show that  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  both possess a TSS with a Dirac-cone-like energy dispersion above the Fermi energy. In agreement with theoretical predictions, we find that the unoccupied bulk bands of  $\text{Sb}_2\text{Te}_2\text{S}$  are shifted to higher energies as compared to  $\text{Sb}_2\text{Te}_3$ . This shift has, however, surprisingly almost no influence on the coupling between the TSS and the bulk bands.

The experiments were carried out in a  $\mu$ -metal shielded UHV chamber at a base pressure of  $3 \times 10^{-11}$  mbar. The optical setup is described in detail in Ref. [16]. It is based on a 250-kHz laser system that provides tunable laser pulses in the visible range with a typical photon energy of 2.58 eV and a pulse length of 50 fs. One part of these pulses was used as visible pump pulses (50 nJ/pulse) with variable time delay, while the other part was frequency doubled to provide ultraviolet probe pulses (80 fs, 0.5 nJ/pulse). The *p*-polarized light was focused onto the sample at an angle of incidence of  $78^\circ$  into a spot with a diameter of 100  $\mu\text{m}$ . Photoelectrons were detected by a hemispherical analyzer (Specs Phoibos 150) with a display-type detector. The angular dispersion was measured within the plane of light incidence. The photon energy of the pump pulses (5.15 eV) was matched to the work function of the samples in order to reduce the background due to one-photon photoemission. Single-crystal  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  samples were cleaved *in situ* by the Scotch tape method at a pressure of  $3 \times 10^{-10}$  mbar followed by a rapid recovery back to the base pressure within a minute. On the one hand, this procedure ensures minimal surface contaminations, on the other hand, we find that both,  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ , are astonishingly insensitive to the exposure of residual gases [17]. Most data shown here were acquired at room temperature.

Figures 1(d) and 1(e) give an overview of the 2PPE spectra of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ . These data have been acquired for temporal overlapping pump and probe pulses where all bands can be observed simultaneously. Both materials show similar spectral structures which will be discussed in the following from low to high energies.

The high intensity close above the Fermi energy  $E_F$  is assigned to the transiently populated valence band (VB), which overlaps with the lower branch of the topological

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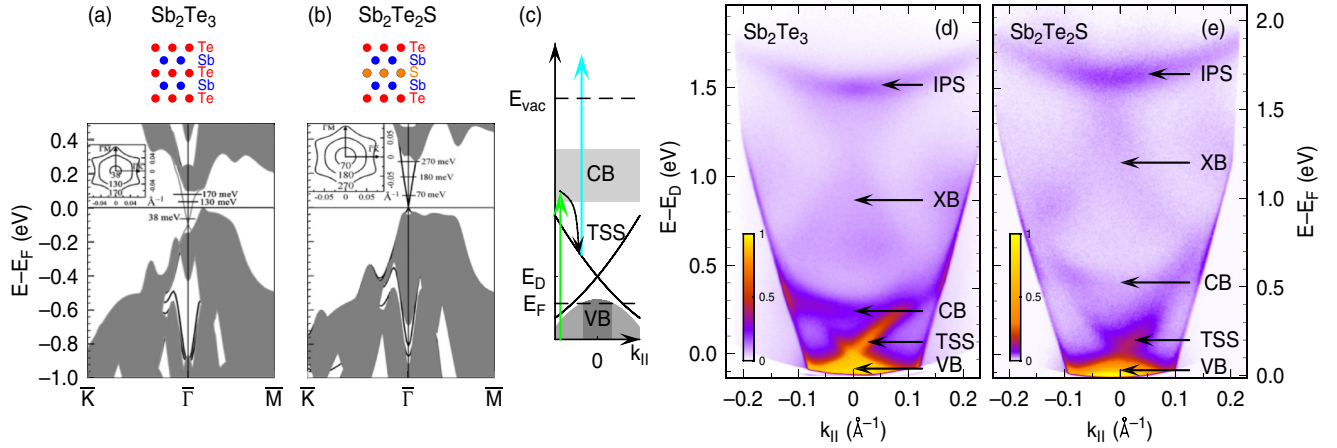


FIG. 1. (Color online) (a) and (b) Calculated band structure together with the stacking order of Te, Sb, and S atoms in the quintuple layers of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ , respectively (taken with permission from Ref. [3]). Shaded areas show the surface-projected bulk bands, lines indicate the topological surface state. (c) Excitation scheme for the population of the TSS with visible pump pulses via transfer from the bulk conduction band and subsequent photoemission with ultraviolet probe pulses. (d) and (e) Angle-resolved 2PPE spectra for temporal overlapping pump and probe pulses of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ , respectively. The arrows indicate the top of the valence band (VB), the topological surface state (TSS), the bulk conduction band (CB), higher bulk and surface bands (XB), and the first image potential state (IPS).

surface state (TSS). Both samples are found to be  $p$ -doped with  $E_F$  being close below the top of the VB at  $\bar{\Gamma}$ . In the 2PPE spectra shown in Figs. 1(d) and 1(e), the energy of the Dirac point  $E_D$  is located at  $E_D - E_F = 135(20)$  meV and  $120(20)$  meV, respectively. These values vary within  $\pm 50$  meV for different preparations, which we attribute to a varying density of surface defects. For this reason, we give in the following all energies with respect to  $E_D$  rather than to  $E_F$ . A considerable population of the TSS can be observed for energies above  $E_D$  of  $\sim 350$  meV for  $\text{Sb}_2\text{Te}_3$ . For  $\text{Sb}_2\text{Te}_2\text{S}$ , it extends up to 500 meV. It is evident that the 2PPE data for both materials show a pronounced asymmetry in the emission from the TSS with the intensity for negative values of  $k_{\parallel}$  being strongly suppressed. Such asymmetric intensity distribution has been also observed in ARPES spectra of  $\text{Bi}_2\text{Se}_3$  and has been explained by an interference effect in the photoemission process [18].

The main difference between the spectra of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  is related to the energy position of the TSS with respect to the higher-lying bands. In agreement with the theoretical calculations [Figs. 1(a) and 1(b)], we observe an upshift of these bands for  $\text{Sb}_2\text{Te}_2\text{S}$  as compared to  $\text{Sb}_2\text{Te}_3$ . This can be already concluded from the position of the conduction band (CB), which we identify as the parabolic band close above the TSS. It is more pronounced for  $\text{Sb}_2\text{Te}_3$  where its minimum is  $\sim 250$  meV above  $E_D$ . For  $\text{Sb}_2\text{Te}_2\text{S}$ , the position of the minimum is shifted towards a higher energy by at least 100 meV. The determination of the actual position of the conduction-band minimum (CBM) with a single probe photon energy is, however, not unambiguous due to the  $k_z$  dependence of the photoemission intensity [19], but the upshift of the bands can be also clearly seen by comparing the faint X-shaped structures (XB), which we assign to higher-lying bulk and surface bands. The parabolic band above  $E - E_F = 1.5$  eV stems from the first ( $n = 1$ ) image-potential state (IPS), which is only apparently located at this low energy because the roles of pump and probe pulses are interchanged [20].

Figure 2 presents the high-resolution 2PPE data of the TSS of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  for a comparison with the calculated surface band structure of Ref. [3]. The data of  $\text{Sb}_2\text{Te}_3$  show an excellent agreement with the theory for the dispersion along the  $\bar{\Gamma} - \bar{K}$  direction (solid lines) [Fig. 2(a)]. For other sample orientations we find some indications of the predicted dispersion asymmetry between  $\bar{\Gamma} - \bar{M}$  and  $\bar{\Gamma} - \bar{K}$  directions, the so-called warping [1]. For  $\text{Sb}_2\text{Te}_2\text{S}$ , theory predicts a much less pronounced warping as compared to  $\text{Sb}_2\text{Te}_3$  [Fig. 2(b)]. Our data for the TSS of  $\text{Sb}_2\text{Te}_2\text{S}$  agree very well with the calculations including details such as a stronger flattening of the lower branch of the surface state below  $E_D$  as compared to  $\text{Sb}_2\text{Te}_3$ .

One remarkable difference between the spectra of  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  is related to the form of the dispersion of the TSS. In all of our data,  $\text{Sb}_2\text{Te}_3$  shows a straight linear dispersion with a Fermi velocity of  $v_F = 2.5(0.2) \times 10^5$  m/s [21]. The

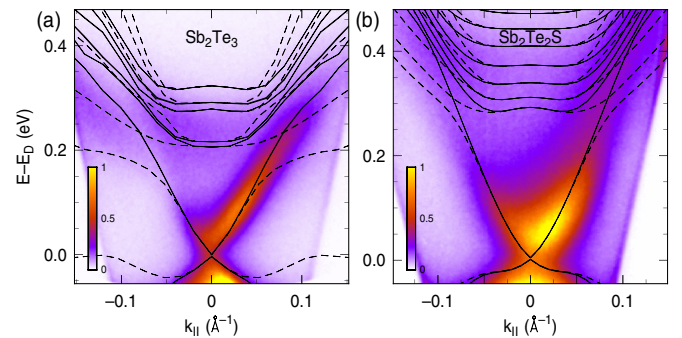


FIG. 2. (Color online) Angle-resolved 2PPE spectra of  $\text{Sb}_2\text{Te}_3$  along  $\bar{\Gamma} - \bar{K}$  (a) and of  $\text{Sb}_2\text{Te}_2\text{S}$  along a direction in between  $\bar{\Gamma} - \bar{K}$  and  $\bar{\Gamma} - \bar{M}$  (b) for the energy region of the TSS at a pump-probe delay of 670 and 870 fs for  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ , respectively. The lines show the calculated surface band structure of Ref. [3] along  $\bar{\Gamma} - \bar{K}$  (solid lines) and  $\bar{\Gamma} - \bar{M}$  (dashed lines).

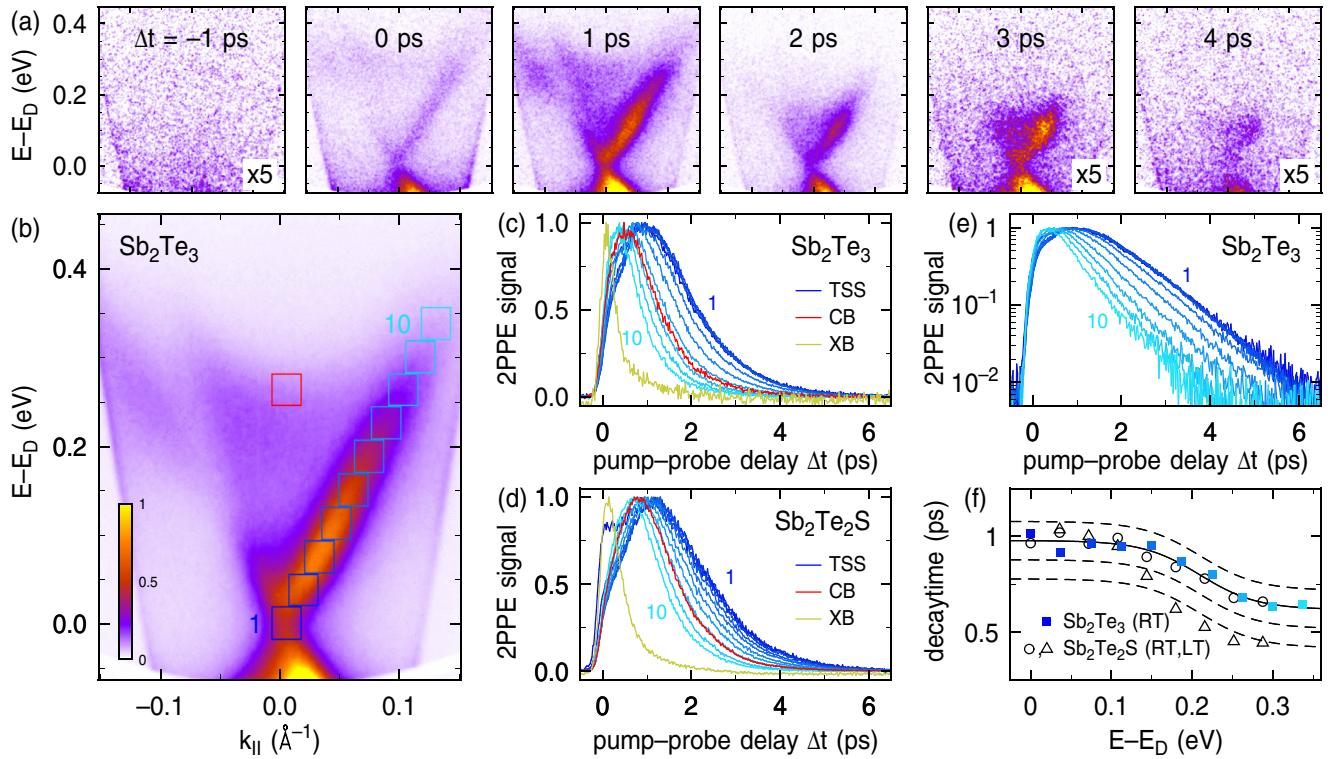


FIG. 3. (Color online) (a) Snapshots of the 2PPE spectra of  $\text{Sb}_2\text{Te}_3$  for selected pump-probe delays  $\Delta t$ . The intensity for  $\Delta t = -1, 3,$  and  $4$  ps is enhanced by a factor of 5. (b) 2PPE data of  $\text{Sb}_2\text{Te}_3$  (compare Fig. 2(a)) with rectangles that indicate the integration windows for the transient 2PPE intensities. (c) Transient 2PPE intensities for  $\text{Sb}_2\text{Te}_3$  within the integration windows shown in (b). The curve for XB corresponds to a window at  $E - E_D = 650$  meV. All data are normalized to their respective maximum. (d) Transients for  $\text{Sb}_2\text{Te}_2\text{S}$  within corresponding windows at the same energies above  $E_D$ . (e) Logarithmic plot of the data in (c) for the TSS. (f) Decay times of the 2PPE intensity along the TSS for  $\text{Sb}_2\text{Te}_3$  at room temperature (RT; filled blue squares) and for  $\text{Sb}_2\text{Te}_2\text{S}$  at room temperature (RT; open dots) and at 40 K (LT; open triangles). The solid line is a guide to the eye. The dashed lines indicate the variation of the decay times for different preparations at room temperature.

data for  $\text{Sb}_2\text{Te}_2\text{S}$ , on the other hand, clearly show a finite curvature close to  $E_D$ . Such deviation from a strict linear dispersion is also visible in ARPES data of other multinary compounds [22,23]. Its origin is, however, still unclear.

Data on the electron dynamics in the TSS are summarized in Fig. 3, where (a) shows snapshots of the 2PPE spectra at selected pump-probe delays  $\Delta t$ . Almost no intensity can be observed for negative delays ( $\Delta t = -1$  ps), because we exclusively probe the initially unoccupied states with the chosen probe photon energy. A considerable population of the TSS can be already observed for  $\Delta t = 0$  even if the maximum population is reached at  $\Delta t \approx 1$  ps. The decay of the populations proceeds on a picosecond time scale. Already from these snapshots it becomes apparent that two energy ranges with different decay dynamics can be distinguished. While the distribution of the population below  $E - E_D \approx 150$  meV remains almost unchanged as a function of delay for  $\Delta t > 1$  ps and therefore decays with a common decay time, the population at higher energies decays on a faster time scale.

This can be seen in more detail in Fig. 3(c) where the 2PPE intensity within different integration windows as depicted in Fig. 3(b) is plotted as a function of pump-probe delay. The curves for the five lowest energy windows along the TSS are almost identical, whereas the decay becomes faster for higher energy. The red curve shows the intensity within an integration window that is located in the conduction band (CB) at  $\bar{\Gamma}$ .

Obviously, the dynamics is very similar to that of the TSS at the respective energy. This applies for all energies along the TSS and we do not find the sudden increase of the decay rate in the CB just at the CBM as has been reported for  $\text{SnSb}_2\text{Te}_4$  [15]. For increasing energies above  $E_D$ , the decay time in the bulk bands (XB) further decreases as indicated by the yellow curve which shows the dynamics at  $E - E_D = 650$  meV. Corresponding data for  $\text{Sb}_2\text{Te}_2\text{S}$  are presented in Fig. 3(d). They exhibit a very similar behavior.

Figures 3(c) and 3(d) also clearly show that the maximum of the population is not reached during the temporal overlap of pump and probe pulses, but at a much later time. Such delayed filling of the TSS has been also observed in previous 2PPE studies [11,14,15] and has been taken as an evidence for a strong coupling between the TSS and the CB. Our data clearly show that this coupling is also important for  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$ . In contrast to the previous 2PPE studies, which all have used pump photon energies around 1.5 eV, however, we observe that the rise of the population in the TSS proceeds on two different time scales. Figures 3(c) and 3(d) clearly show that the initial increase of the 2PPE intensity at  $\Delta t = 0$  is very rapid and is followed by a slower increase due to the delayed filling. We attribute the initial faster increase, which accounts for 30%–50% of the total population, to a direct optical excitation of the TSS in  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  with 2.58 eV pump photons.



The decay of the population in the TSS for large delays can be well described by a single-exponential decay [Fig. 3(e)]. Both materials exhibit similar decay times, which are almost constant for low energies and start to decrease at  $E - E_D \sim 150$  meV [Fig. 3(f)]. The differences between the two materials are smaller than the variations due to different preparations (dashed lines), which are related to slight variations of  $E_D - E_F$ . This indicates that the decay is dominated by the number of unoccupied states in the VB as has been concluded for other  $p$ -doped materials [14,15].

The onset of the decay time decrease is close to the lower edge of the 2PPE signal from the CB of  $\text{Sb}_2\text{Te}_3$  [see Fig. 1(d)]. For this material, an accelerated decay for higher energies is easy to understand, because one can expect a stronger coupling between TSS and CB if both become degenerated. For  $\text{Sb}_2\text{Te}_2\text{S}$ , it is surprising, because we concluded from the 2PPE spectra in agreement with the theory that the CB of  $\text{Sb}_2\text{Te}_2\text{S}$  is shifted by  $\sim 100$  meV towards higher energies as compared to  $\text{Sb}_2\text{Te}_3$ . Experiments at a lower temperature of 40 K at which the electron mobility in the bulk is enhanced show, however, that the decay times of  $\text{Sb}_2\text{Te}_2\text{S}$  become even faster, but only for energies above the onset [open triangles in Fig. 3(f)]. This is a clear indication that the decay of the 2PPE signal at these energies is affected by electron transport into the bulk as has been found for metal and semiconductor surfaces [24–26]. This contradiction might be only solved by

performing experiments with different probe photon energies in order to better discriminate between photoemission from bulk and surface states. From the absence of a considerable temperature dependence of the decay times for energies below 150 meV, we conclude that phonons play only a minor role for the decay.

In summary, we have directly accessed the unoccupied electronic structure of  $p$ -doped  $\text{Sb}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_2\text{S}$  with 2PPE, which has unambiguously showed that the massless Dirac-cone-like energy dispersion of the topological surface state is realized for both materials. In agreement with theoretical predictions, we find that the unoccupied bands of  $\text{Sb}_2\text{Te}_2\text{S}$  are shifted to higher energies as compared to  $\text{Sb}_2\text{Te}_3$ . The observed electron dynamics strongly indicates that transport perpendicular to the surface is important for the decay in the TSS. Surprisingly, this decay channel becomes operative at the same energy above  $E_D$  for both materials. Moreover, our data provide first evidence of a direct optical excitation of the TSS at 2.58-eV photon energy, which might open the possibility to drive a spin current via the circular photogalvanic effect [27]. 2PPE would allow to study its dynamics in unprecedented detail.

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- the experimental uncertainty we find the same work function of 5.0(0.1) eV for both materials from which we determine  $E - E_{\text{vac}} = 0.85(0.10)$  eV ( $\text{Sb}_2\text{Te}_3$ ) and  $E - E_{\text{vac}} = 0.80(0.10)$  eV ( $\text{Sb}_2\text{Te}_2\text{S}$ ), respectively.
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