

ROAD TO THE MULTIVERSE PAVED BY QUANTUM INTERACTIONS

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INTRODUCTION

➤ Why multiverse?

- Emerges naturally in some physical theories
- It could solve some open cosmological questions (i. e. cosmological constant problem)
- Depends on the definition of a universe

➤ Physical multiverse

- Appropriate multiverse scenario to make observational predictions
- It need some kind of non standard interaction between universes (classical or quantum)
- It is not related with a particular multiverse theory

➤ Quantum correlations between universes

- Classically disconnected universes
- Quantum entanglement → effects of other universes on our own
- Consideration of the multiverse as a whole

➤ We need to make a simple model for the multiverse: the universes and the interactions between them

- Third quantization scheme
- Different models

1) Decoherence due to the environment made of other universes →
Master equation

2) Curvature Principle → Curvature invariant for each universe

3) Multiverse of interacting harmonic oscillators → Wigner quantization

THIRD QUANTIZATION FORMALISM

- Analogy with quantum field theory
 - WDW as K-G in superspace → Wavefunction as the field to quantize
 - Creation and annihilation of universes → baby universes
- Minisuperspace: Homogeneous and isotropic models → FLRW metric
 - Scale factor as a time variable

$$\left(\partial_{aa} + \frac{\Omega_0^2}{\hbar^2} a^{2(q+1)} \right) \phi(a) = 0$$

where $\Omega_0^2 = 4\pi G\rho_0$ & $q = \frac{3}{2}(1 - \omega)$

harmonic oscillator
(time dependent
frequency)

➤ Wavefunction of the multiverse $H|\Psi\rangle = i\hbar\partial_a|\Psi\rangle$

where $H = \frac{1}{2}\hat{P}_\phi^2 + \frac{\Omega^2(a)}{2}\hat{\phi}^2$

➤ Creation and annihilation operators
$$\begin{cases} b = \sqrt{\frac{\Omega(a)}{2\hbar}} \left(\hat{\phi} + \frac{i}{\Omega(a)} \hat{P}_\phi \right) \\ b^+ = \sqrt{\frac{\Omega(a)}{2\hbar}} \left(\hat{\phi} - \frac{i}{\Omega(a)} \hat{P}_\phi \right) \end{cases}$$

So, the Hamiltonian $H = \beta_- b^2 + \beta_+ b^{\dagger 2} + \beta_0 \left(b^\dagger b + \frac{1}{2} \right)$

DECOHERENCE IN THE MULTIVERSE

- The interaction can be represented by a total Hamiltonian

$$H = H_P + H_\varepsilon + H_{int}$$

where

- $H_P = \frac{1}{2}P_\Phi^2 + \frac{\Omega^2(a)}{2}\Phi^2$
- $H_\varepsilon = \sum_{i=1}^N \frac{1}{2}p_{\phi_i}^2 + \frac{\omega_i^2}{2}\phi_i^2$
- $H_{int} = \sum_i \lambda_i \Phi_P \otimes f(\phi_i) \rightarrow \begin{cases} f(\phi_i) \equiv \phi_i & \text{Linear interaction} \\ f(\phi_i) \equiv \phi_i^2 & \text{Quadratic interaction} \end{cases}$

➤ Master equation

$$\partial_a \rho_P = -i[\tilde{H}_P, \rho_P] - i\gamma[\Phi, \{P_\Phi, \rho_P\}] - \underbrace{D[\Phi, [\Phi, \rho_P]]}_{\text{noise kernel}} - \underbrace{f[\Phi, [P_\Phi, \rho_P]]}_{\text{dissipation kernel}}$$

with $\tilde{H}_P \equiv H_P + \frac{\tilde{\Omega}^2}{2}\Phi^2$

noise kernel

dissipation kernel

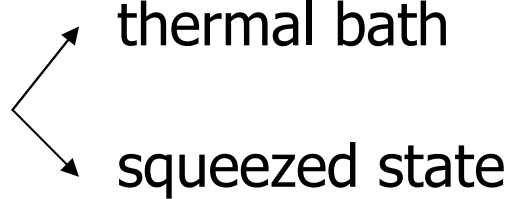
▪ Correlation function $\langle \phi^k(a) \phi^k(a') \rangle_b = \underbrace{\nu(a, a')}_{\text{noise kernel}} - \underbrace{i\eta(a, a')}_{\text{dissipation kernel}}$

• Solution to WDW + dissipation kernel ➡ Lamb shift

• Solution to WDW + dissipation kernel ➡ Normal-diffusion coefficient

➤ Calculating... $\begin{cases} \Omega^2(a) = c_1 f(a, q) \\ D(a) = c_2 g(a, q) \end{cases}$

INTERACTION OF A UNIVERSE WITH ITS QUANTUM FLUCTUATIONS

- Creation and annihilation operators 
 - thermal bath
 - squeezed state
- The expressions for the noise and dissipation kernel involves the spectral density → encapsulates the physical properties of baby universes

$$J(\omega) = J_0^2 \omega^3 e^{-\omega/\Lambda}$$

➤ Results

- Linear interaction $\begin{cases} c_1 \sim \text{cte} \\ c_2 \sim N \end{cases}$
- Quadratic interaction $\begin{cases} c_1 \sim N \\ c_2 \sim N^2 \end{cases}$

- Scale for the decoherence $a_D = \frac{1}{\sqrt{c_2}}$

➔ Decoherence scale: very small, more in quadratic interaction

➔ Lamb shift: constant or dependent on the strenght of fluctuations

INTERACTION OF A UNIVERSE WITH OTHER UNIVERSES

- The squeezing effect asymptotically disappears
- We choose the spectral density as $J(\Omega) \sim \delta(\Omega' - \Omega_0)$
- So, we obtain
$$\begin{cases} c_1^p \approx \Omega_0 \\ c_2^p \approx 2N \end{cases}$$
- ➔ Decoherence is very effective for a large number of universes
- ➔ Lamb shift: same order energy density of the Universe (without interactions)



effective energy of the Universe turns out to be approximately zero

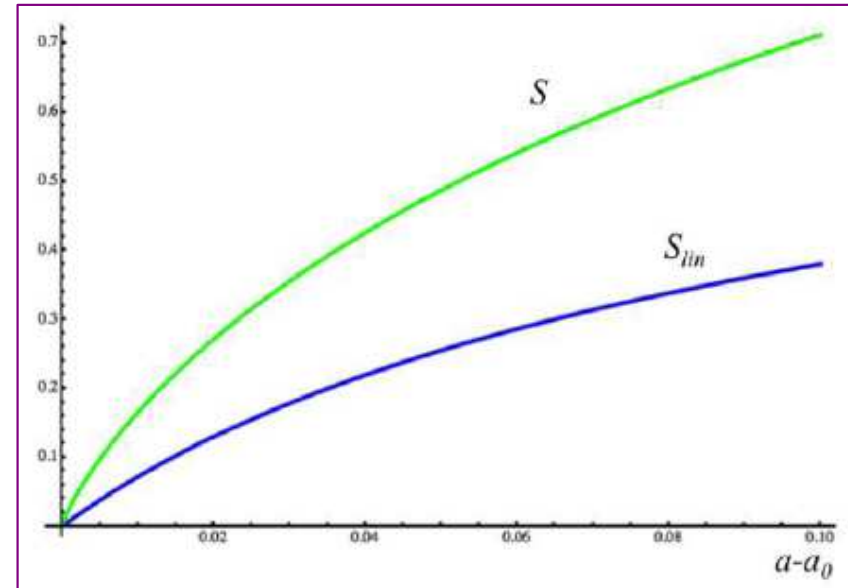
THERMODYNAMICAL QUANTITIES

- Interaction with environment → effectively non unitary evolution
- The previous master equation can be solved with the Gaussian ansatz → the solution depends on coefficient c_2
- Considering an initial pure state
- This coefficient allows us to obtain thermodynamical properties of the parent universe

➤ Entropy of a parent universe interacting with the environment

$$S_{lin} = 1 - \zeta$$

$$S = -\frac{1}{p_0}(p_0 \ln p_0 + q_0 \ln q_0)$$



➔ Interaction with the environment → evolution to a mixed state → loss of information



Decoherence process → Universe described in terms of the semiclassical branch which we live in

➔ Total system retains all information

CURVATURE PRINCIPLE

- Each universe described in terms of a curvature invariant → sensitive to the vacuum energy
- Hamiltonian evolution that reflects the interaction between universes
- We consider the third quantization formalism for homogeneous and isotropic universes → WDW as a harmonic oscillator

$$\ddot{\phi} + \frac{\dot{M}}{M}\dot{\phi} + \omega\phi = 0 \quad \text{with } M(a) = a \quad \text{and} \quad \omega(a) = \frac{a}{\hbar}\sqrt{a^2\Lambda - 1}$$

- The total Hamiltonian is given by

$$H_T = H_1 + H_2 + H_I \quad \text{where} \quad \begin{cases} H = \frac{1}{2M}p_\phi^2 + \frac{M\omega^2}{2}\phi^2 \\ H_I = \frac{Ma^4k}{2}(\phi_2 - \phi_1)^2 \end{cases}$$

➤ A non-trivial choice of canonical transformation to $(\Phi_1, \Phi_2, P_1, P_2)$

$$H_N = \frac{1}{2M}P_1^2 + \frac{M\Omega_1^2}{2}\Phi_1^2 + \frac{1}{2M}P_2^2 + \frac{M\Omega_2^2}{2}\Phi_2^2$$

where $\left\{ \begin{array}{l} \Omega_1^2 = a^4 f(\Lambda_1, \Lambda_2, k) \\ \Omega_2^2 = a^4 g(\Lambda_1, \Lambda_2, k) \end{array} \right.$

- H_N represents dynamical evolution of non-interacting universes
- Normal modes of oscillation
- Vacuum energy associated with new frequencies

➤ Considering two “nearby” universes

$$\Lambda_1 = \Lambda + \varepsilon$$

$$\Lambda_2 = \Lambda - \varepsilon$$

So

$$\left\{ \begin{array}{l} \Omega_1^2 \approx a^4 \Lambda_1^{\text{ef}} \\ \Omega_2^2 \approx a^4 \Lambda_2^{\text{ef}} \end{array} \right. \xrightarrow[k = -\frac{\Lambda}{2}]{} \left\{ \begin{array}{l} \Lambda_1^{\text{ef}} \approx \frac{2\varepsilon^2}{\Lambda} \approx 0 \\ \Lambda_2^{\text{ef}} \approx \Lambda - \frac{2\varepsilon^2}{\Lambda} \approx \Lambda \end{array} \right.$$

- Point of view of an internal observer that perceives its universe as isolated → value of the cosmological constant as proper of the universe
 - Observer in universe 1: see a nearly zero value of the cosmological constant → cannot identify to any effect of its universe
 - Mechanism for reducing the cosmological constant of a universe by means of the interaction of different universes
- We also extend this study to a general quadratic potential

MULTIVERSE OF INTERACTING HARMONIC OSCILLATORS

- Multiverse can exhibit collective phenomena → new perspective
- Considering N de Sitter universes interacting → represented in third quantization as harmonic oscillators
- Assuming “nearest interaction” and the interaction governed by Hooke’s law

$$\hat{H} = \sum_{r=1}^N \left(\frac{\hat{p}_r^2}{2M} + \frac{M\omega^2}{2} \hat{\phi}_r^2 + \frac{Mc}{2} (\hat{\phi}_r - \hat{\phi}_{r+1})^2 \right)$$



$$\hat{H} = \sum_{r=1}^N \left(\frac{1}{2M} \hat{P}_r \hat{P}_r^\dagger + \frac{M\omega_r^2}{2} \hat{\Phi}_r \hat{\Phi}_r^\dagger \right) \quad \text{with} \quad \omega_r^2 = \omega^2 + 4c \sin^2 \left(\frac{\pi r}{N} \right)$$

➔ We can follow a more general quantization procedure

➤ Canonical commutation relations replaced by compatibility conditions

➤ In addition to the standard solution, it allow us to obtained more solutions → be described by means of representations of Lie superalgebras

➤ Defining the operators
$$\begin{cases} a_r^- \equiv \sqrt{\frac{M\omega_r}{2}} \hat{\Phi}_r + \frac{i}{\sqrt{2M\omega_r}} \hat{P}_r^\dagger \\ a_r^+ \equiv \sqrt{\frac{M\omega_r}{2}} \hat{\Phi}_r^\dagger - \frac{i}{\sqrt{2M\omega_r}} \hat{P}_r \end{cases}$$

the Hamiltonian takes the form
$$\hat{H} = \sum_{r=1}^N \frac{\omega_r}{2} \{a_r^-, a_r^+\}$$

➤ Compatibility condition $[\hat{H}, a_r^\pm] = \pm \omega_r a_r^\pm$

➤ These relations have solutions in a particular Lie superalgebra → We can diagonalize the Hamiltonian and obtain the energy spectrum

- We consider a multiverse with explicit interaction or without it
- For the given representation the spectrum of the Hamiltonian splits into a large number of different levels for both cases (different each other)



Even in the case without explicit interaction → there are quantum interactions with no classical analogue

- The energy levels depends strongly on the interaction between universes
- Given some conditions, the ground state of the new spectrum approaches to zero
- The collective phenomena of the multiverse provide a mechanism to fix the cosmological constant to a value arbitrarily close to zero

CONCLUSIONS

- The interaction of a parent universe with a multiverse environment
→ parallel development to quantum optics
 - Decoherence effect permit the emergence of a classical Universe
 - An analogue effect to Lamb shift, provide a mechanism that allows to reduce the value of the cosmological constant, due to the interaction of the Universe with a multiverse environment
 - We also show the entropy increase of the state of the Universe → loss of information that is maintained in the whole multiverse
- By means of the Curvature Principle we obtain a reduction of the value of the cosmological constant in the Universe, due to the interaction with other universe

➤ We can consider collective phenomena in the multiverse → give us new tools to understand cosmological issues

- Take N universes in the multiverse as harmonic oscillators, and use the Wigner Quantum System → quantum interaction in the multiverse without classical analogue
- The interactions between universes produce new energy levels for the Hamiltonian → In any case we can fix the vacuum energy to a value arbitrary close to zero
- So, the vacuum energy of a universe depends not only on the interaction between universes but also on the structure of the multiverse as a whole

➤ These simple models show that an interacting multiverse could solve some cosmological problems and open the door to a new range of effects that could give physical predictions of the multiverse

Thank you for your attention!

