

Plasma wakefield acceleration at CLARA facility in Daresbury Laboratory

G. Xia^{a,b}, Y. Nie^c, O. Mete^{a,b}, K. Hanahoe^{a,b}, M. Dover^a, M. Wigram^a, J. Wright^a, J. Zhang^a, J. Smith^d, T. Pacey^{a,b}, Y. Li^{a,b}, Y. Wei^{b,e}, C. Welsch^{b,e}

^a*School of Physics and Astronomy, University of Manchester, Manchester, United Kingdom*

^b*The Cockcroft Institute, Sci-Tech Daresbury, Daresbury, Warrington, United Kingdom*

^c*Deutsche Elektronen-Synchrotron DESY, Hamburg, Germany*

^d*Tech-X UK Corporation, Daresbury Innovation Centre, Warrington, United Kingdom*

^e*University of Liverpool, Liverpool, United Kingdom, United Kingdom*

Abstract

A plasma accelerator research station (PARS) has been proposed to study the key issues in electron driven plasma wakefield acceleration at CLARA facility in Daresbury Laboratory. In this paper, the quasi-nonlinear regime of beam driven plasma wakefield acceleration is analysed. The wakefield excited by various CLARA beam settings are simulated by using a 2D particle-in-cell (PIC) code. For a single drive beam, an accelerating gradient up to 3 GV/m can be achieved. For a two bunch acceleration scenario, simulation shows that a witness bunch can achieve a significant energy gain in a 10-50 cm long plasma cell.

Keywords: Plasma wakefield acceleration, Particle-in-cell, Quasi-nonlinear regime, Two-bunch acceleration

1. Introduction

Plasma wakefield acceleration is one of the most promising technologies to miniaturize the scale of next generation particle accelerators due to its capability to sustain very large electric field. From the initial idea proposed to nowadays, plasma based accelerators have achieved tremendous breakthroughs in the last three decades [1, 2]. Plasma accelerators driven by high power and short pulse lasers, so-called laser wakefield acceleration (LWFA) could achieve hundreds MeV to several GeV electron beam in a single stage acceleration. The resultant monoenergetic beams have the energy spread of only a few percent [3, 4, 5]. The recent highlight from LBNL has successfully demonstrated a 4.25 GeV electron beam acceleration from a 9 cm long capillary discharge plasma source [6]. This electron beam energy is already well comparable to most of today's third generation light sources and the resulting beam can be used to drive free electron laser as well [7]. On the other hand, the plasma accelerators driven by electron beam, so-called beam driven plasma wakefield acceleration (or PWFA) has doubled the energy of the electron beam from the Stanford Linear Collider (SLC) within an 85 cm plasma cell [8]. The FACET facility has recently also achieved the high efficient acceleration for a separate witness electron bunch [9]. The latest results showed that positron beam can also excite significant wakefield and accelerate the positrons at the rear part of the bunch in a self-loaded mode [10]. All these breakthroughs have shown great promise to build tabletop and efficient energy use of plasma accelerators as alternatives to conventional accelerators. This is mainly due to plasma based accelerators can provide an accelerating gradient of 1-100 GeV/m, which are usually over two to three orders of magnitude higher than the field in conventional RF-based accelerating structures (in general equal or less than

100 MeV/m) [11].

Compared to laser driven wakefield accelerators, the advantages of a relativistic beam driven plasma wakefield acceleration lie in that the beam can propagate in plasma for much longer distances than that of the laser beam in plasma, as the laser beam is subject to the 3D effect, i.e. diffraction, depletion and dephasing in the plasma. Therefore the energy gain for a one-stage acceleration is significant for PWFA. Secondly, the conventional RF-based accelerator can obtain the relativistic electron beam with relatively high efficiency (usually more than 10%). Using this relativistic beam as drive beam for plasma wakefield excitation is more efficient than using the laser beam for beam acceleration (if compared to low wall-plug efficiency for producing laser beam). Currently, there are a number of dedicated facilities to demonstrate the great potential of the beam driven plasma wakefield acceleration method, e.g. FACET and FACET II facility at SLAC[12], the FLASHForward at DESY[13], the SPARC LAB facility of INFN[14] and the AWAKE experiment driven by the 400 GeV proton beam from the SPS at CERN[15, 16, 17, 18], etc.

We have proposed a high gradient plasma wakefield acceleration experiment based at CLARA (Compact Linear Advanced Research Accelerator) facility in the Daresbury Laboratory[19, 20, 21]. The idea is to investigate the critical issues for the next generation plasma accelerators, e.g. test of the PWFA theory, high acceleration gradient (1-10 GeV/m), two-bunch acceleration, high transformer ratio, plasma focusing effect (plasma lens), and related advanced beam dynamics concepts etc. Since the CLARA beam is designed for Free Electron Laser (FEL) research, which makes the beam ideal for plasma wakefield acceleration experiments. Firstly, the beam is relativistic so it can propagate in plasma for a long distance, i.e. tens of centimetres. Therefore the energy gain from a one-stage acceleration will be

66 significant. Secondly, the bunch length can be tuned from a
 67 few pico-second down to tens of femtosecond, which enables
 68 us to study the scaling laws for PWFA and reach high acceler-
 69 ating gradient in an ultrashort bunch operation case. Thirdly,
 70 the well-developed beam diagnostics at CLARA can be eas-118
 71 ily employed to characterise beam precisely, and knowing the-119
 72 beam parameters are crucial for PWFA experiments. 120

73 In this paper, the theory of quasi-nonlinear PWFA regime121
 74 (QNL) is introduced and analysed in section 2. The particle-in-
 75 cell (PIC) code VSIM [22] is employed to model the electron-
 76 plasma interactions for a single drive beam and two bunch ac-
 77 celeration case respectively based on the CLARA beam param-122
 78 eters. The detailed simulation results are presented in section123
 79 3. 124

80 2. PWFA in quasi-nonlinear regime 125

81 In the blowout regime of PWFA, the driving bunch has much126
 82 higher electron density n_b than the background plasma den-127
 83 sity n_p , i.e. $n_b \gg n_p$, and thus excites an ion filled bubble128
 84 behind it. The radial focusing field is linear along the bub-129
 85 ble radius and the longitudinal accelerating field is constant130
 86 in radius. However, the nonlinear plasma oscillation occurs131
 87 simultaneously, which limits the beam quality of the witness132
 88 bunches. Therefore, a new regime called weak blowout has133
 89 been proposed and investigated recently [23, 24, 25]. It op-134
 90 erates in the quasi-nonlinear regime (QNL), where the total135
 91 charge of the driving bunch is relatively low to maintain the136
 92 resonant plasma response, especially a constant wakefield fre-
 93 quency, while the density of the driving bunch is still larger than
 94 that of the plasma to form the bubble. Such a driving bunch can
 95 be achieved by using a cigar shape, where the transverse size
 96 of the bunch σ_r is much smaller than the bunch length σ_z , i.e.137
 97 $\sigma_r \ll \sigma_z$. The QNL-PWFA is very promising to provide high-138
 98 quality and high-energy bunches under ultra-high accelerating139
 99 gradient. Meanwhile, the transformer ratio is also an important140
 100 figure of merit, which is defined as the ratio of the maximum141
 101 accelerating wakefield behind the driving bunch and the max-142
 102 imum decelerating wakefield within it, i.e. $R = W_{acc}/W_{dec}$. R 143
 103 is usually less than two for a single symmetric driving bunch144
 104 in the linear regime. Fortunately, there are a few ways to145
 105 overcome this limit, for instance, using an asymmetric driving
 106 bunch [26, 27], a ramped bunch train [28, 29] and the nonlinear
 107 plasma dynamics [27, 30] as in the case of single bunch driven
 108 QNL-PWFA. 146

109 In the QNL-PWFA regime, several case studies have been147
 110 performed by using 2D particle-in-cell simulations. The idea is148
 111 to find out the optimal plasma density for certain driving beam149
 112 parameters. In order to enhance the transformer ratio, one can150
 113 manipulate the driving bunch shape, namely the ratio of σ_r to151
 114 σ_z . The test bunches to be used are typically achievable at a few152
 115 existing and oncoming facilities at the energy level of hundreds153
 116 of MeV, e.g. at CLARA facility. The driving bunches have the154
 117 azimuthally symmetric bi-Gaussian shape as follows: 155

$$156 \quad n_b(r, z) = n_b e^{-r^2/2\sigma_r^2} e^{-z^2/2\sigma_z^2}, \quad (1)157$$

here n_b is the driving beam density which is given by

$$n_b = N_b / ((2\pi)^{3/2} \sigma_r^2 \sigma_z), \quad (2)$$

The normalized charge that is used to evaluate the nonlin-
 earity in the PWFA is defined as the total electron numbers in
 the driving bunch N_b normalized to the numbers of the plasma
 electrons inside a cubic plasma skin depth k_p^{-3} as follows [23]

$$\tilde{Q}_n = N_b k_p^3 / n_p = n_b / n_p (2\pi)^{3/2} k_p \sigma_r \sigma_z (k_p \sigma_r)^2, \quad (3)$$

where $k_p = 2\pi/\lambda_p = \sqrt{e^2 n_p / m_e \epsilon_0} / c$ is the plasma wave num-
 ber with λ_p the plasma wavelength. In linear theory, the number
 of the plasma electrons that response to the driving beam is ap-
 proximately limited to $n_p k_p^{-3}$. It can be seen that \tilde{Q}_n should be
 smaller than 1 to have linear plasma response. On the other
 hand, n_b should be higher than (or comparable to) n_p to excite
 bubbles in plasma. $\tilde{Q}_n < 1$ and $n_b > n_p$ are the two condi-
 tions to achieve the QNL-PWFA. It has been demonstrated that
 the prediction from the linear theory that the maximum accel-
 erating gradient appears at $k_p \sigma_z = \sqrt{2}$ still holds even though
 the nonlinear blowout regime is reached, i.e. when $n_b \gg n_p$,
 as long as the normalised charge per unit length of the driving
 beam $\Lambda = (n_b/n_p)(k_p^2 \sigma_r^2) \ll 1$ [31]. Therefore, the bunch with
 a cigar shape ($\sigma_r \ll \sigma_z$) is the best candidate to drive a PWFA
 in the QNL regime.

For the QNL-PWFA, the maximum accelerating wakefield
 may be estimated by the following equation of the linear theory:

$$E_{z,max} \approx 236 MV/m \left(\frac{N_b}{4 \times 10^{10}} \right) \left(\frac{600}{\sigma_z (\mu m)} \right)^2 \ln \left(\sqrt{\frac{10^{16}}{n_p (cm^{-3})}} \frac{50}{\sigma_r (\mu m)} \right), \quad (4)$$

which shows that $E_{z,max}$ depends not only on the driving bunch
 charge and length, but also on the optimum plasma density and
 the bunch spot size σ_r . According to the linear theory, the op-
 timal plasma density occurs at $k_p \sigma_z = \sqrt{2}$. However, beyond
 this limit $\sigma_r \ll \sigma_z$ when σ_r approaching σ_z , the optimal plasma
 density n_p will be lower and $k_p \sigma_z < \sqrt{2}$ [32], since in this case
 the driving bunch density n_b will be likely decreases along with
 the increasing of the spot size. In addition, $E_{z,max}$ can also be
 predicted by the following expression if $n_b/n_p \leq 10$ [32]:

$$E_{z,max}/E_{0,max} \approx 1.3 (n_b/n_p) (k_p \sigma_r)^2 \ln(1/k_p \sigma_r), \quad (5)$$

for the narrow driving bunch, i.e. $k_p \sigma_r < 0.3$ and in the weakly
 nonlinear limit $\Lambda < 1$, where the wave breaking wakefield
 $E_{0,max} = m c \omega_p / e \sim 100 \sqrt{n_p (cm^{-3})} V/m$.

The maximum energy that can be given to the witness bunch
 is limited by the transformer ratio R . For the single symmetric
 driving bunch, the limit of $R < 2$ can be overcome by oper-
 ating the PWFA in the QNL regime, where nonlinear blowout
 occurs. It is meaningful to study the dependence of R on the
 plasma density for given driving bunch parameters. Due to the
 incomplete nonlinear theories, numerical simulations must be
 employed to study the detailed wakefield structures in the QNL
 regime.

3. Simulation study of beam-plasma interactions

3.1. Electron beam from CLARA facility

CLARA is a normal conducting linear electron accelerator. It can generate ultrashort and bright electron bunches and use these bunches in the experimental production of stable, synchronised, ultrashort photon pulses of coherent light from a single pass free electron laser (FEL) with techniques directly applicable to the future generation of light source facilities [19]. The CLARA facility comprises of a photo-injector electron gun, S-band normal conducting accelerating cavities, magnetic bunch compressor, fourth harmonic lineariser, dedicated beam diagnostic sections at low and high energies and FEL beam line, as illustrated in Fig. 1. CLARA facility can provide 250 MeV electron bunch with bunch charge of 250 pC. The detailed electron beam parameters are listed in Table 1.

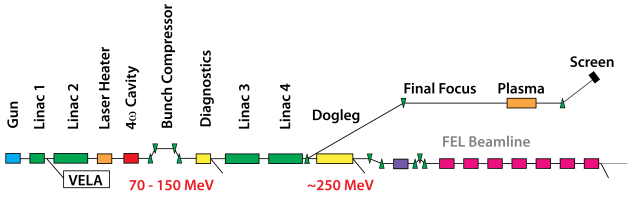


Figure 1: Conceptual layout of the CLARA facility and the PARS beam line.

For the electron beam driven plasma wakefield experiment at PARS (Plasma Accelerator Research Station), a dogleg will be built to guide the CLARA beam to a parallel beam line, off-set by $\sim 1.5m$ from the CLARA beam axis, but still contained within the CLARA shielding area. The conceptual layout of the PARS beam line is also shown in Fig. 1. It consists of the dogleg beam line, final focus, plasma cell, energy spectrometer and a final beam dump (not shown). The dogleg beam line consists of arrays of dipoles and quadrupoles to guide and focus the beam from the CLARA beam line to the PARS. The final focus, which is prior to the plasma cell, is designed to focus the electron beam transversely and to match the electron beam parameters with the plasma parameters. A variable length capillary discharge plasma source (10-50 cm) is currently being built at Daresbury Laboratory. The key issues for the PWFA at various beam and plasma parameter ranges will be studied extensively, including the PWFA in QNL regime. An energy spectrometer will be employed to characterise the energy of electrons exiting the plasma cell. The final beam dump will absorb the energy of electrons after exiting the plasma cell. Prior to the final focus and plasma cell, a magnetic chicane may be needed to compress the bunch further to an extremely short length.

3.2. Wakefield optimisation for one drive bunch in QNL regime

2D particle-in-cell simulations have been performed using the software VSim from the Tech-X Corporation [22]. The first relativistic driving bunch has the following parameters: $N_b = 1.56 \times 10^9$ (bunch charge of 250 pC), $\sigma_z = 75\mu m$, $\sigma_r = 20\mu m$ and $n_b = 3.31 \times 10^{15} cm^{-3}$. For the above parameters, $\Lambda = 0.048$ and the optimum plasma density for the maximum accelerating gradient is $9.8 \times 10^{15} cm^{-3}$ according to the linear theory. The plasma density scanned is thus from

$3.3 \times 10^{14} cm^{-3}$ to $3.3 \times 10^{16} cm^{-3}$ so as to cover all interested ranges.

When $n_p \leq 8 \times 10^{15} cm^{-3}$ we have $\tilde{Q}_n < 1$ and $n_b > n_p$ (or $n_b \approx n_p$), so the PWFA will work in the QNL regime. For the cases of $n_p > 8 \times 10^{15} cm^{-3}$, $\tilde{Q}_n > 1$ and $n_b \ll n_p$, thus the linear response occurs. Over the studied plasma range, the parameters $k_p \sigma_r$ and $k_p \sigma_z$ vary from 0.07 to 0.69 and 0.26 to 2.59, respectively. The dependences of the decelerating wakefield W_{dec} , the accelerating wakefield W_{acc} and the transformer ratio R on the plasma density n_p are shown in Fig.2. At the lower plasma densities, $k_p \sigma_z \ll 1$, i.e. the driving bunch is much shorter than a plasma skin depth. As a result, the blowout will occur and the wakefield will depend on the total charge of the bunch other than the peak current. From Eq. (3) we can see that the normalized total charge $\tilde{Q}_n \propto \sqrt{n_p}$. This is why both of W_{dec} and W_{acc} increase as n_p increases at the beginning in Fig.2. In the intermediate plasma density range, as $k_p \sigma_z$ increases, there is an optimum value of $n_p = 6.5 \times 10^{15} cm^{-3}$ that gives the maximum W_{acc} about 2.25 GV/m. Here we have $\tilde{Q}_n = 0.87$, $n_b/n_p = 0.51$ and $k_p \sigma_r = 0.31$. The optimal parameter $k_p \sigma_z = 1.15$ is 0.81 times the prediction from the linear theory ($k_p \sigma_z = \sqrt{2}$ from the linear theory), since the bunch is not ideally narrow with the ratio of $\sigma_r/\sigma_z = 0.27$. Notice that the calculated accelerating wakefields using Eq. (4) and Eq. (5) are 668 MV/m and 594 MV/m, 3.4 and 3.8 times lower than the simulation results, respectively. As n_p increases further, the wakefield becomes weaker and weaker, since the ambient electrons are only perturbed and the driving bunch length becomes longer than the plasma wavelength so the wakefield can only be driven by a part of the bunch unless the self-modulation instability is resonantly excited. As for the transformer ratio R , it increases quickly at the beginning and becomes saturated around 2.36 when n_p is about $1.5 \times 10^{16} cm^{-3}$. It is important to figure out that when the accelerating gradient reaches the maximum value of 2.25 GV/m, $R \approx 2.1$ is still much lower than the saturated value. Figures 3 and 4 plot the longitudinal wakefield distribution and the longitudinal accelerating field after the bunch propagates through 29.7 mm in plasma with an optimum plasma density $n_p = 6.5 \times 10^{15} cm^{-3}$ for the first driving bunch, respectively. It can be seen that the PWFA works in the weakly blowout regime, and the bubble radius can be roughly estimated as twice the equilibrium channel radius $R_b \approx 2\sigma_r \sqrt{n_b/n_p} = 2\sqrt{\Lambda}/k_p$ [33], which is $29\mu m$. The value of $k_p R_b \approx 0.44 < 1$, so the wakefield structure is dominated by the linear plasma response, as shown in Fig. 4.

In order to improve the wakefield gradient as well as the transformer ratio, we decrease the ratio of σ_r/σ_z while keeping the total electron charge unchanged. The second driving bunch parameters are as follows: $N_b = 1.56 \times 10^9$, $\sigma_z = 100\mu m$, $\sigma_r = 10\mu m$ and $n_b = 9.92 \times 10^{15} cm^{-3}$ that has been enhanced. The smaller transverse size of the bunch may be obtained by using a triplet of permanent magnet quadrupoles as used in the Accelerator Test Facility (ATF) at BNL. For the above parameters, $\Lambda = 0.036$ and the optimum n_p to have the maximum accelerating gradient is $5.5 \times 10^{15} cm^{-3}$ according to the linear theory. We used the same n_p range as in the first case. The ma-

Table 1: Three operation regimes for the PWFA experiment at the CLARA/PARS facility.

Operating modes	Long Pulse	Short Pulse	Ultra-Short Pulse
Beam energy (GeV)	250	250	250
Charge/Bunch Q (pC)	250	250	20-100
Electron/Bunch N_b ($\times 10^9$)	1.56	1.56	0.125-0.625
Bunch length rms (fs)	250-800	100-250	≤ 30
Bunch length (μm)	75-240	30-75	9
Bunch radius (μm)	10-100	10-100	10-100
Normalised emittance (mm mrad)	≤ 1	≤ 1	≤ 1
Energy spread (%)	1	1	1

260 jority points locate at $\tilde{Q}_n < 1$ and $n_b > n_p$, while $k_p\sigma_r$ and $k_p\sigma_z$
 261 varying from 0.035 to 0.35 and 0.35 to 3.5, respectively. Figure 5 shows that the optimum n_p is near $5 \times 10^{15} \text{cm}^{-3}$, where
 262 $\tilde{Q}_n = 0.76$, $n_b/n_p = 2.0$ and $k_p\sigma_r = 0.13$. The parameter
 263 $\tilde{Q}_n = 0.76$, $n_b/n_p = 2.0$ and $k_p\sigma_r = 0.13$. The parameter
 264 $k_p\sigma_z = 1.35$ becomes much closer to $k_p\sigma_z = \sqrt{2}$ compared
 265 to the previous case, since the ratio of σ_r/σ_z has been reduced
 266 to 0.1 and the bunch is narrower than before. Figure 6 plots
 267 the longitudinal wakefield distribution at the optimum plasma
 268 density of $5 \times 10^{15} \text{cm}^{-3}$ after the bunch traveling in a 31.5 mm
 269 plasma. It can be seen that the wakefield in first accelerating
 270 bubble is very strong. The details can also be found in Fig.7,
 271 the maximum accelerating gradient is $W_{acc} = 3.73 \text{GV/m}$, 5.7
 272 and 5.6 times larger than the results from Eq. (4) and Eq. (5),
 273 respectively, and $R = 2.3$ is very close to the peak value shown
 274 in Fig. 5. In principle, it is possible to merge the two peaks of
 275 the accelerating wakefield and the transformer ratio by manipu-
 276 lating the driving bunch shapes. In Fig. 6, it can be seen that
 277 the bubble structure is quite clean with a radius of $R_b \approx 40 \mu\text{m}$
 278 that is greater than the estimation of $28 \mu\text{m}$. Compared to the
 279 first case study, the optimal plasma wavelength increases from
 280 $409 \mu\text{m}$ to $467 \mu\text{m}$, and there is no sharp spike in the accel-
 281 erating wakefield structure, leading to high useful accelerating
 282 field [23]. Meanwhile, longer wavelength of the accelerating
 283 wakefield allows longer bunch length of the externally injected
 284 witness bunch concerning with the field curvature effect, and
 285 brings benefit to maintaining high beam quality during accel-
 286 eration in the plasma [34].

287 The normalized amplitudes of the accelerating wakefield for
 288 the above two cases are plotted in Fig.8. The peak values do not
 289 necessarily appear at the optimum plasma densities that give
 290 the maximum W_{acc} . The normalized wakefield amplitudes of
 291 the second driving bunch are much higher than those of the first
 292 one due to the improved bunch shape, but still less than unity.

293 3.3. Simulation of two-bunch acceleration

294 To get the benefit from the plasma wakefield, a two-bunch
 295 acceleration needs to be studied [12, 35]. In this scheme, the
 296 witness bunch will need to follow behind the drive bunch at a
 297 position of the maximum accelerating field. Meanwhile a much
 298 lower final energy spread is desired after the witness bunch ex-
 299 iting from the plasma. Theoretically the position of witness
 300 bunch should be about $\lambda_p/2$ behind the drive beam, i.e. in terms
 301 of the wakefield oscillations, a phase-lag of π behind the drive
 302 beam. However, due to finite size and the associated electro-

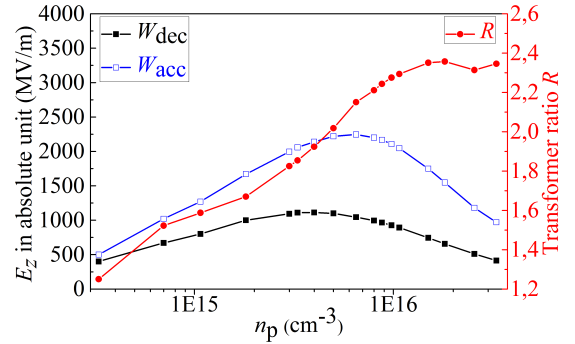


Figure 2: The accelerating/decelerating field and transformer ratio as a function of n_p for the first driving bunch.

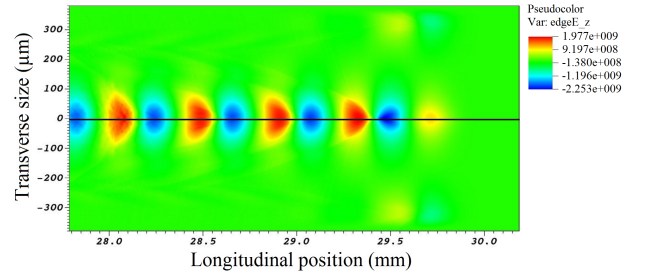


Figure 3: The longitudinal wakefield distribution at the ambient plasma density of $6.5 \times 10^{15} \text{cm}^{-3}$ for the first driving bunch.

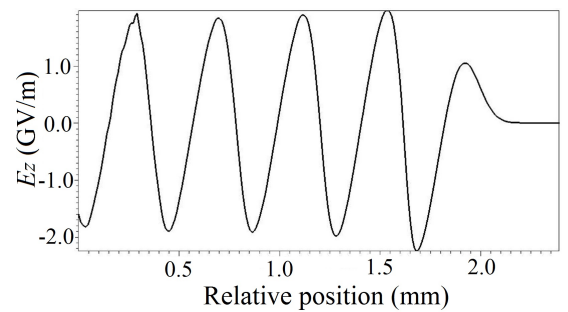


Figure 4: The accelerating wakefield after the bunch propagates through 29.7 mm in plasma for the first driving bunch.

magnetic fields of the electron bunch, the witness beam will dis-
 tort the shape of the excited wakefield, a phenomenon known as
 beam loading [36]. This can sometimes alter the wakefield sig-
 nificantly, in both peak position and field magnitude, depending
 on the strength of the beam loading effect.

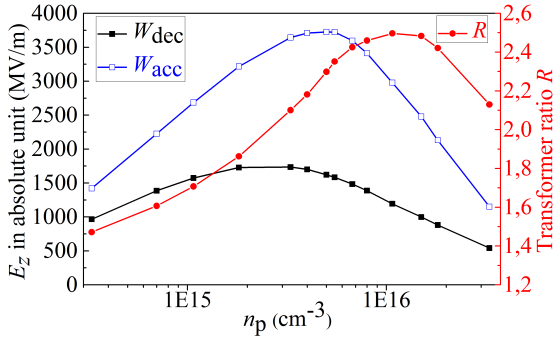


Figure 5: The accelerating/decelerating field and transformer ratio as a function of n_p for strongly focused beam, i.e., the second driving bunch.

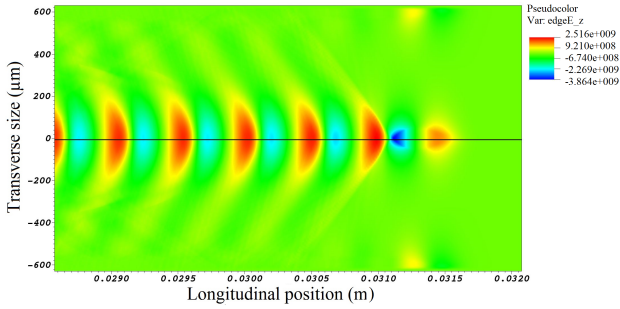


Figure 6: The longitudinal wakefield distribution at the ambient plasma density of $5 \times 10^{15} \text{ cm}^{-3}$ for the second driving bunch.

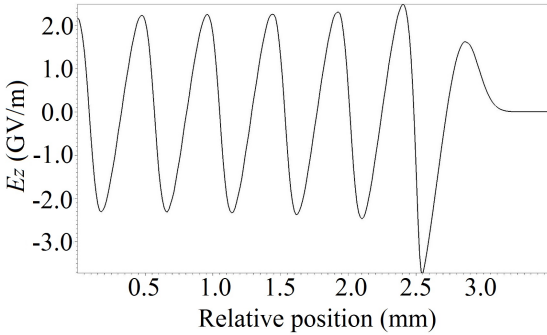


Figure 7: The accelerating wakefield after the bunch propagates through 31.5 mm in plasma, for the second driving bunch.

In order to find an optimum drive-witness phase lag, a two-beam case was implemented for the VSIM simulations. An additional Gaussian beam (witness beam) was introduced to the macro-particle weighting, as shown in Fig. 9, with a beam offset of $\lambda_p/2$ behind the drive beam, plus an additional offset specified by the user. The bunch densities for the drive bunch and witness bunch are shown in Fig. 10. We assume that the witness beam has the same specifications as the drive beam, i.e. its energy, transverse size and bunch length are the same, except an additional weighting factor of 0.2 is introduced so that the witness beam has a bunch charge of 50 pC. An initial energy spread of 1% is also introduced for both the witness and the drive beams, to better match the CLARA beam parameters.

Simulations were performed with the witness beam offset being increased from $0.5\lambda_p$ up to $0.75\lambda_p$ behind the drive

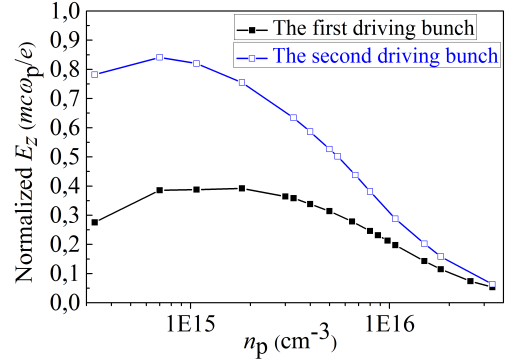


Figure 8: The normalized wakefield amplitudes for different plasma densities using normal and strong focused driving bunches.

beam for each plasma density of $0.5, 1.0, 3.0 \times 10^{15} \text{ cm}^{-3}$ and $5.0 \times 10^{15} \text{ cm}^{-3}$ for a maximum 50 cm long plasma, covering the full potential plasma cell length at PARS. The final average energy of the witness bunch was recorded, and used to calculate an average accelerating gradient experienced by the bunch over the length of the plasma, with the aim of finding the phase-lag that produced the highest average acceleration, and hence the highest final energy.

The resulting average accelerating gradients for the density of $1.0 \times 10^{15} \text{ cm}^{-3}$ are plotted in Fig.11. The data actually shows the average experienced gradients after 40 cm of propagation in the plasma. After this distance a numerical instability occurs, disrupting the fields and the witness beam energy sharply drops. An identical effect is also observed for the plasma density of $3.0 \times 10^{15} \text{ cm}^{-3}$, but not for the case when the plasma density is $0.5 \times 10^{15} \text{ cm}^{-3}$. This is mainly due to the dephasing length for different plasma densities. It is possible that this instability is caused by a breakdown in the physics of the simulation. All the particles in the simulation move at speed of light c , regardless of their energies, so no dephasing occurs and the simulation no longer represents the reality of the laws of the physics. The data after this is considered unreliable and only data acquired up to the instabilities is used.

The maximum average accelerating field experienced is found as 0.8 GV/m at an offset of $0.67\lambda_p$, as shown in Fig.11. The beam energy variation for drive bunch and witness bunch as function of propagating distance in plasma is plotted in Fig.12. It can be seen that after a 50 cm long plasma, the drive beam loses its energy and the witness can gain significant amount of energy from the plasma. Figure 13 shows the energy gain and energy loss for a 250 pC, 250 MeV drive bunch with $\sigma_r = 40 \mu\text{m}$, $\sigma_z = 75 \mu\text{m}$, and a 50 pC witness bunch with $\sigma_r = 25 \mu\text{m}$ and $\sigma_z = 10 \mu\text{m}$ after propagating in a 10 cm long plasma. The distance between the witness bunch to the drive bunch is $\lambda_p/2$, with the witness offset from this by $20 \mu\text{m}$ forwards. The plasma density is set as an optimum value of $5 \times 10^{15} \text{ m}^{-3}$ (or $5 \times 10^{15} \text{ cm}^{-3}$). The lines are linear fits with gradients corresponding to an average decelerating gradient of 289 MeV/m for the drive bunch and an accelerating gradient of 519 MeV/m for the witness. It can be seen that in this case, the energy gain is much more significant than that of the low plasma density case, as shown in Fig.12.

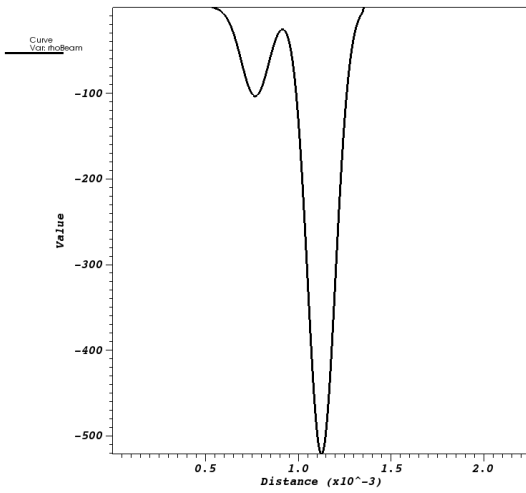


Figure 9: Bunch charge for the drive bunch and witness bunch.

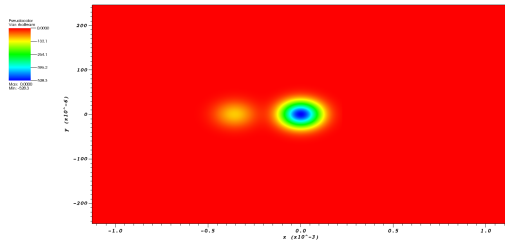


Figure 10: Bunch density for the drive bunch and witness bunch.

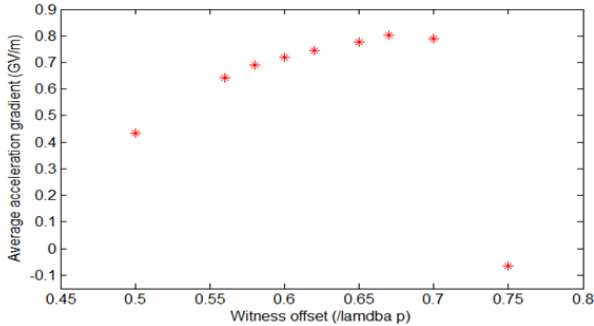


Figure 11: Average accelerating gradient experienced by the witness beam against witness beam offset behind the drive beam, given as a fraction of λ_p , for a plasma density of $1.0 \times 10^{21} m^{-3}$. The peak in acceleration gradient occurs at $0.67\lambda_p$, with an average gradient of 0.80 GV/m.

4. Conclusions

The PARS facility will be built to study the key issues in the next generation plasma wakefield acceleration based at the CLARA facility at the Daresbury Laboratory. Simulation has shown that the relativistic electron beam from CLARA can excite the plasma wakefield with amplitude up to 3 GV/m in the quasi-nonlinear regime. A witness bunch placed at the appropriate position can gain significant energy in a 10-50 cm long plasma cell with plasma density of $\sim 10^{15} cm^{-3}$.

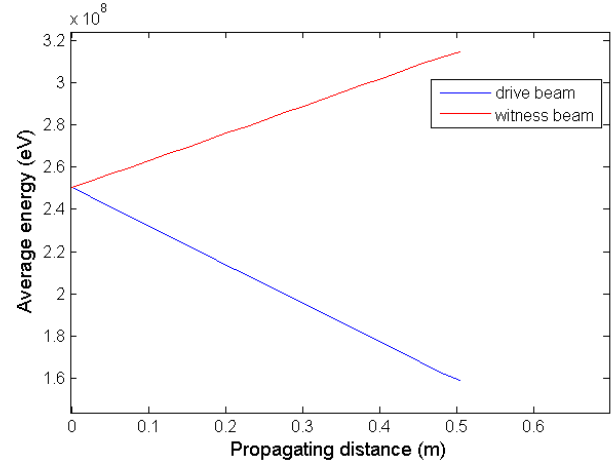


Figure 12: Energy variation for drive bunch and witness bunch as function of propagating distance in plasma with plasma density of $1.0 \times 10^{21} m^{-3}$.

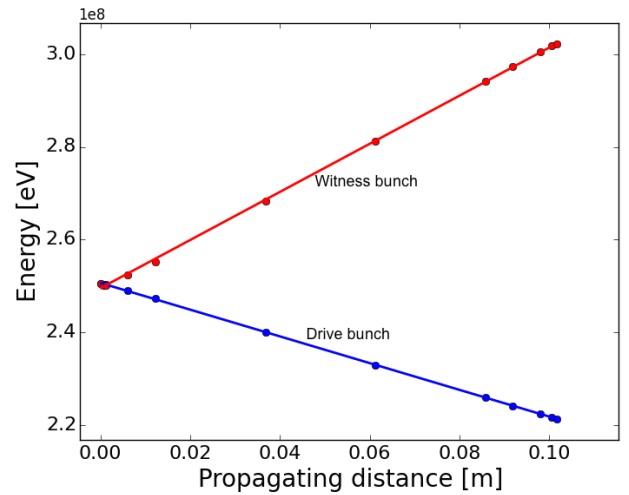


Figure 13: Energy variation for drive bunch and witness bunch as function of propagating distance in plasma with plasma density of $5.0 \times 10^{21} m^{-3}$.

Acknowledgements

This work is supported by the STFC and the Cockcroft Institute Core Grant.

- [1] E. Esarey et al., IEEE Transactions on Plasma Science, 24 (1996) 252.
- [2] C. Joshi et al., New J. Phys. 12 (2010) 045003.
- [3] W. Leemans et al., Nature Physics 2, (2006) 696.
- [4] W. Leemans et al., Phys. Today 62 (3) (2009) 44.
- [5] X. Wang et al., Nat. Commun. 4 (2013) 2988.
- [6] W. Leemans et al., Phys. Rev. Lett. 113, 245002 (2014).
- [7] S. Cipiccia et al., Nature Phys. 7 (2011) 867.
- [8] I. Blumenfeld et al. Nature 445 (2007) 741.
- [9] M. Litos et al. Nature 515 (2014) 92.
- [10] S. Corde et al., Nature 524 (2015) 442.
- [11] P. Muggli et al., C. R. Physique 10 (2009) 116.
- [12] M. J. Hogan et al., New Journal of Phys. 12 (2010) 055030.
- [13] J. Grebenyuk et al., Nucl. Instrum. Meth. A 740 (2014) 246.
- [14] Andrea R. Rossi et al., Nucl. Instrum. Meth. A 740 (2014) 60.
- [15] A. Caldwell et al., CERN-SPSC-2013-013 (2013).
- [16] G. Xia et al., AIP Conf. Proc. 1299 (2010) 510.
- [17] G. Xia et al., J. Plasma Physics 78 (2012) 347.
- [18] R. Assmann et al., Plasma Phys. Control. Fusion 56 (2014) 084013.
- [19] J.A. Clarke et al., Journal of Instrumentation 9 (05), (2014) T05001.

- 388 [20] G. Xia et al., Nucl. Instrum. Meth. A 740 (2014) 165.
389 [21] O. Mete et al., Phys. Plasmas 22 (2015) 103117.
390 [22] <http://www.txcorp.com/products/VORPAL/>.
391 [23] J. B. Rosenzweig et al., Phys. Rev. Spec. Topics Acc. Beams 7, (2004)
392 061302.
393 [24] J. B. Rosenzweig et al., AIP Conference Proceedings 1507 (2012) 612.
394 [25] P. Londrillo et al., Nucl. Instrum. Meth. A 740 (2014) 236.
395 [26] K.L.F. Bane et al., IEEE Trans. Nucl. Sci., NS-32 (1985) 3524.
396 [27] F. Massimo et al., Nucl. Instrum. Meth. A 740 (2014) 242.
397 [28] C. Jing et al., Phys. Rev. Lett. 98 (2007) 144801.
398 [29] B. Jiang et al., Phys. Rev. Spec. Topics Acc. Beams 15, (2012) 011301.
399 [30] J. B. Rosenzweig et al., Phys. Rev. A 39 (1989) 1586.
400 [31] W. Lu et al., New Journal of Phys. 12 (2010) 085002.
401 [32] W. Lu et al., Phys. Plasmas 12 (2005) 063101.
402 [33] S. Lee et al., Phys. Rev. E 61, (2000) 7014.
403 [34] J. Grebenyuk et al., Proceedings of IPAC2014 (2014) 1515.
404 [35] B. Hidding et al., Phys. Rev. Lett 104 (2010) 195002.
405 [36] N. Vafaei-Najafabadi et al., Phys. Rev. Lett 112 (2014) 025001.