

Interstitial Oxide Ion Order and Conductivity in $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ Melilite

Man-Rong Li, Xiaojun Kuang, Samantha Y. Chong, Zhongling Xu, Christopher I. Thomas, Hongjun Niu, John B. Claridge* and Matthew J. Rosseinsky*

Solid oxide fuel cells (SOFCs) are a major candidate technology for clean energy conversion because of their high efficiency and fuel flexibility.^[1] The development of intermediate temperature (500–750 °C) SOFCs requires electrolytes with high oxide ion conductivity (exceeding $10^{-2} \text{ S}\cdot\text{cm}^{-1}$ assuming an electrolyte thickness of $15\mu\text{m}$ ^[1]). This in turn needs enhanced understanding of the mechanisms of oxide ion charge carrier creation and mobility at an atomic level. The charge carriers are most commonly oxygen vacancies in fluorites^[2,3] and perovskites^[3,4] – there are fewer examples of oxygen interstitial-based conductors such as the apatites^[5–6] and $\text{La}_2\text{Mo}_2\text{O}_9$ ^[7–9] based materials, so information on how these excess anion defects are accommodated and the factors controlling their mobility is important.

The $\text{A}_2\text{B}_3\text{O}_7$ melilite structure consists of anionic layers of five-membered rings of two totally condensed (four neighbouring tetrahedra linked by B–O–B bonds) and three partially condensed (three neighbouring tetrahedra) BO_4 tetrahedra, separated by sheets of A cations located above the five-ring centres (Figures 1a, S1.1). Previously,^[10] we demonstrated that A site substitution in melilite $\text{LaSrGa}_3\text{O}_7$ ($\text{A}_2 = \text{LaSr}$, $\text{B} = \text{Ga}$) affords $\text{La}_{1.54}\text{Sr}_{0.46}\text{Ga}_3\text{O}_{7.27}$, where oxygen interstitials (O_{int}) are located in the five-rings of the two-dimensional tetrahedral network, gives pure oxide ion conductivity of $0.02\text{--}0.1 \text{ S}\cdot\text{cm}^{-1}$ over the $600\text{--}900^\circ\text{C}$ temperature range.^[11] $\text{LaCaGa}_3\text{O}_7$ also adopts the tetragonal melilite structure (space group $P4_2/m$) found for the Sr-doped phases.^[12–13] When doped to introduce oxide charge carriers in the $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$ series, the tetragonal structure is retained to $x = 0.5$. This paper addresses the impact on the physical properties of a new lower symmetry phase formed to accommodate the higher interstitial doping levels $0.55 \leq x \leq 0.64$.

X-ray powder diffraction from $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ (Section 2, SI) indicates the lowering of symmetry at high doping levels occurs by formation of an orthorhombic cell with expansion of the ab plane containing the B_3O_7 network, consistent with the $C_{mm}2$ subgroup of $P4_2/m$ ($a \sim 11.416 \text{ \AA}$, $b \sim 11.226 \text{ \AA}$, $c \sim 5.248 \text{ \AA}$, where $a \approx b \sim \sqrt{2} a_{\text{tetra}}$, $c = c_{\text{tetra}}$). Selected area electron diffraction and HRTEM imaging requires further doubling of c to give a body-centered supercell with no other systematic absences (Figures S3.2–3), consistent with space groups $Imm2$, $Imm1$ and II .

Variable temperature neutron powder diffraction (NPD) (Figures 1b (top-right inset) and S4.1) shows a transition between the low-

temperature orthorhombic and the small cell tetragonal structure between $600\text{--}700^\circ\text{C}$, corresponding to a strong anomaly in the

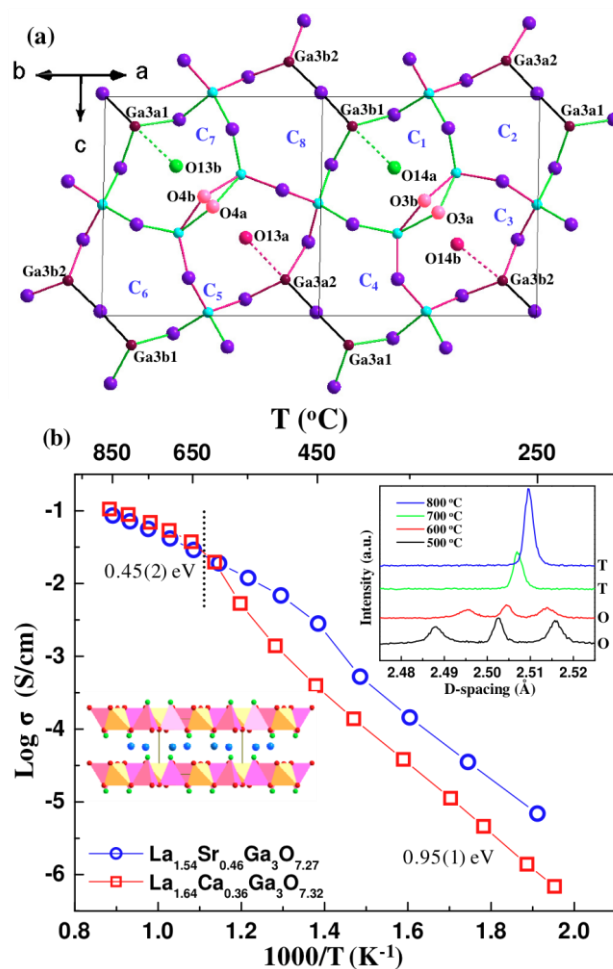


Figure 1 (a) View of the average structure of the $\text{Ga}_3\text{O}_{7+x/2}$ network along the [110] direction for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$. Four of the eight possible oxygen interstitial sites (C_n , $n = 1\text{--}8$) in the 5-rings are occupied ($\text{C}_1\text{--O}14\text{a}$, 58.1(1)%; $\text{C}_3\text{--O}14\text{b}$, 23.9(1)%; $\text{C}_5\text{--O}13\text{a}$, 28.0(1)%, $\text{C}_7\text{--O}13\text{b}$, 17.9(1)%). The local ordering involves coupled occupancy of the C_1/C_7 (green) and C_5/C_3 (red) sites, which differ in the polarity of the interstitial displacement along the [101] direction towards the single 3-connected GaO_4 within each ring indicated with broken lines of different colours. The two orientations of the three-connected Ga_2O_7 dimers within the five-rings are shown with black Ga–O–Ga bonds (unoccupied ring centroids) and by representing the bridging oxygens ($\text{O}3\text{a}/\text{O}3\text{b}$, $\text{O}4\text{a}/\text{O}4\text{b}$) of the centroid-occupied rings in pink. (b) Arrhenius plot of total conductivity for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ compared with that for $\text{La}_{1.54}\text{Sr}_{0.46}\text{Ga}_3\text{O}_{7.27}$. The dash line marks the phase transition shown by variable temperature NPD (top-right inset) from O (orthorhombic) to T (tetragonal), the bottom-left inset shows the stacking of $\text{La}_{1+x}\text{Ca}_{1-x}$ (blue) and Ga_3O_7 layers in melilite.

[*] Dr. M. R. Li, Dr. X. Kuang, Dr. S. Y. Chong, Dr. Z. Xu, Mr. C. I. Thomas, Dr. H. J. Niu, Dr. J. B. Claridge, Prof. Dr. M. J. Rosseinsky
Department of Chemistry, University of Liverpool
Liverpool, L69 7ZD (UK)
Fax: (+44) 151-794-3598
E-mail: claridge@liverpool.ac.uk; m.j.rosseinsky@liv.ac.uk

[**] Financial Support was provided by EPSRC (C511794)

Supporting information for this article is available on the WWW under <http://www.angewandte.org> or from the author.

temperature dependence of the conductivity around 650 °C (Figure 1b). Here the activation energy changes from 0.95(1) eV at low temperature to 0.45(2) eV at high temperature. The ionic conductivity of the distorted phase is lower than the less doped $\text{La}_{1.54}\text{Sr}_{0.46}\text{Ga}_3\text{O}_{7.27}$ which retains the small cell T structure at all temperatures, suggesting that the structural phase transition is produced by static ordering of the interstitial oxide charge carriers.

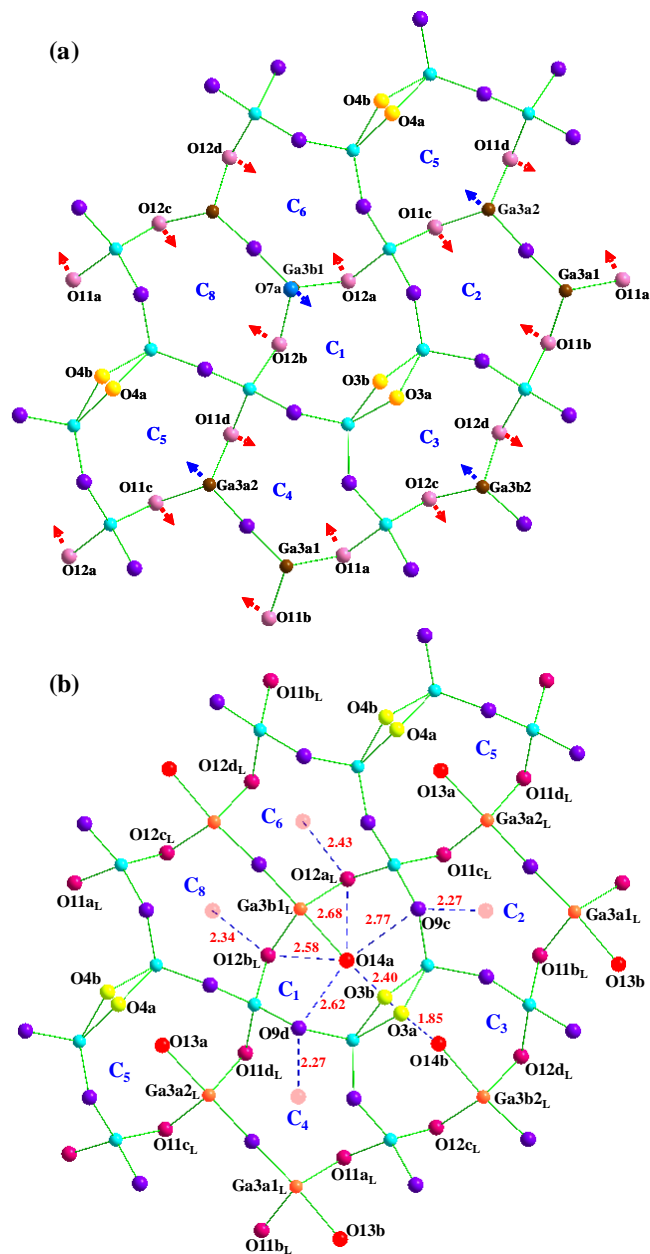


Figure 2 The projection along [110] of (a) bulk and (b) defect structure around the most highly occupied five-ring centroid C_1 . To accommodate the interstitial oxide $\text{O}14\text{a}$, $\text{O}12\text{a}$ and $\text{O}12\text{b}$ displace to $\text{O}12\text{a}_L$ and $\text{O}12\text{b}_L$ toward neighbouring C_6 and C_8 rings (marked with arrows in (a)). The occupancy of $\text{O}3\text{a}$ when $\text{O}14\text{a}$ is present locally makes C_3 the most distorted of all the five rings sharing edges with C_1 . Distances from the bridge oxides defining the five-ring around $C_1/\text{O}14\text{a}$ to the centroids of neighbouring channels are marked in (b).

Rietveld analysis of the NPD data showed the best fits were obtained in PI ($a = 9.5736(1) \text{ \AA}$, $b = 9.5748(1) \text{ \AA}$, $c = 9.5692(1) \text{ \AA}$, $\alpha = 106.78(1)^\circ$, $\beta = 108.17(1)^\circ$, $\gamma = 113.51(1)^\circ$, $V = 672.85(1) \text{ \AA}^3$ -

Figure S3.1 shows the relationship to the II cell). There are 8 inequivalent pentagonal channel candidate interstitial sites in the PI cell, rather than the single site in the disordered tetragonal structure. Conventional least-squares refinements and simulated annealing analysis reveal the ordering of the interstitial oxide charge carriers over these sites which produces the conductivity reduction. The interstitial content was constrained as $\text{O}_{7.32}$ per formula unit, with all eight sites equally occupied and random La/Ca site occupancy in the starting model. Refinement converged to $R_{wp}/R_p = 3.21/4.60\%$, $\chi^2 = 4.28$ (Figure S5.6; Table S5.4-5). The oxygen interstitials occupy four of the eight pentagonal channels (C_n , $n = 1-8$ in Figure 1a). Random occupancy of the interstitial sites gives a poorer fit ($\chi^2 = 5.27$). There is partial cation ordering on the A sites: half are fully occupied by La ($\text{La}1\text{a}$, $\text{La}2\text{a}$, $\text{La}2\text{b}$, and $\text{La}3\text{a}$), the others are La/Ca mixed sites ($\text{La}/\text{Ca}1\text{b}$, $\text{La}/\text{Ca}3\text{b}$, $\text{La}/\text{Ca}4\text{a}$, and $\text{La}/\text{Ca}4\text{b}$) of which only $\text{La}/\text{Ca}3\text{b}$ and $\text{La}/\text{Ca}4\text{a}$ have significantly more than statistical amounts of calcium (Figure S5.7, Table S5.4). The simulated annealing analysis, which is less susceptible to false minima,^[14] gives a qualitatively identical and quantitatively similar description of the A site and oxygen interstitial ordering (Section 6, SI). Although the refined average structure defines the O interstitial and La dopant occupancies relative to the symmetry-distinct centres of the five-rings of the Ga_3O_7 layer, a more chemically acceptable locally relaxed model is needed to give quantitatively reasonable bond valence sums (BVS) ^[15,16] at the under-bonded interstitial oxide sites and at the isolated three-connected GaO_4 tetrahedra which are closest to the interstitials (BVS ~ 3.30 , Table S5.5). A split model for relaxation around the defects was refined ($\chi^2 = 4.81$; Figures 2, S7.1, Table S7.1-3), with two sets of positions representing the resulting bulk (no interstitial present, tetrahedral Ga) and defect (five coordinate Ga) structural environment around the interstitial oxides. The gallium and oxygen displacements from the bulk to the defect structure are shown in Figures 2, 3, and Figure S7.2-4. We use the most highly occupied interstitial site $\text{O}14\text{a}$ (average structure BVS = 1.28) to show how synergic bonding geometry changes at the isolated three-connected $\text{Ga}3\text{b}1$ site and A counterion displacement towards $\text{O}14\text{a}$ accommodate the excess oxides.

The two A sites above and below the C_1 five-ring displace towards $\text{O}14\text{a}$, with the pure La site closer than the mixed site ($\text{La}3\text{a}_L\text{-O}14\text{a} = 2.51(1) \text{ \AA}$, $\text{La}3\text{a}_L\text{-O}14\text{a} = 2.46(1) \text{ \AA}$) to electrostatically stabilize the interstitial (Figure S7.2). The displacement of the defect model position $\text{Ga}3\text{b}1_L$ ($0.17(1) \text{ \AA}$) from the tetrahedron centre $\text{Ga}3\text{b}1$ in the bulk model towards $\text{O}14\text{a}$ into a triangular face of the original tetrahedron (Figure 3a) shortens this gallium-oxygen bond from $2.177(6) \text{ \AA}$ to $2.035(6) \text{ \AA}$. $\text{O}14\text{a}$ thus enters the coordination environment of $\text{Ga}3\text{b}1_L$ at one of the axial positions of the resulting trigonal bipyramidal $\text{Ga}3\text{b}1_L\text{O}_5$ unit (Figure 3b). It should be emphasized that when the other four Ga centres defining this five-ring are allowed to relax by a similar site-splitting, they move slightly away from $\text{O}14\text{a}$ rather than towards it, thus demonstrating that only the isolated three-connected Ga centre binds to the interstitial. The interstitial $\text{O}14\text{a}$ makes close contacts ($\sim 1.9\text{-}2.5 \text{ \AA}$) to three other oxygens ($\text{O}3\text{b}$, $\text{O}12\text{a}$, and $\text{O}12\text{b}$) in the five-membered ring compared to its distances to $\text{O}9\text{c}$ and $\text{O}9\text{d}$ ($2.70(1)$ and $2.77(1) \text{ \AA}$, Figure 2(b)). The resulting displacement of $0.56(1) \text{ \AA}$ to $\text{O}12\text{a}_L$ and of $0.49(1) \text{ \AA}$ to $\text{O}12\text{b}_L$ bound to $\text{Ga}3\text{b}1_L$ increases the mean $\text{O-Ga}3\text{b}1_L\text{-O}$ angles in the equatorial plane to $119.4(2)^\circ$ (from $105.2(2)^\circ$ in the average structure) and makes the mean $\text{O}_{\text{apical}}\text{-Ga}3\text{b}1_L\text{-O}_{\text{equatorial}}$ angle $89.7(2)^\circ$ (Table S7.2-3), while the mean $\text{O-Ga}3\text{b}1\text{-O}$ angle in the bulk GaO_4 tetrahedron is $108.9(1)^\circ$. These two bridging oxygens, and also $\text{O}3\text{a}$, which bridges the Ga_2O_7 dimer of

three-connected centres forming the pentagon edge opposite Ga3b1, are now 2.40(1)-2.70(1) Å from O14a and as a result are displaced towards neighbouring pentagonal channel centres (C_3 , C_6 , and C_8 in Figure 2a). This expansion of C_1 around O14a results in much shorter distances from its edge-bridging oxygens to the centroids of the five neighbouring edge-sharing channels than to O14a as shown in Figure 2b. This model decreases the BVS of Ga3b1 to 2.91 (Ga3b1O_4 tetrahedron) and 2.97 ($\text{Ga3b1}_L\text{O}_5$ trigonal bipyramid), and increases the O14a BVS to 1.91, providing a satisfactory description of the bonding around the defect.

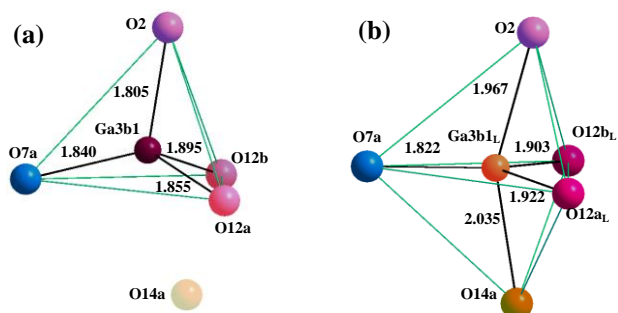


Figure 3 Structural relaxation around the most highly occupied interstitial oxide O14a. Ga3b1_L, O12a_L, O12b_L, O3a are involved in the local structural relaxation. (a) Tetrahedral GaO₄ in the absence of O14a. (b) GaO₅ trigonal bipyramid formed by O14a. O7a is the non-bridging terminal oxygen.

This relaxation around O14a prevents interstitial occupancy of any of the five nearest neighbor ring centres to C_1 (C_2 , C_3 , C_4 , C_6 , and C_8) (Figure 2a). The doping dependence of the structure can be rationalized by consideration of the longer-range interaction of these distortions. Each interstitial site is surrounded by seven nearest-neighbour interstitial sites (Figure 4), five sharing a common edge and the more distant two a fully condensed tetrahedral GaO₄ vertex. The closest of the five edge-sharing neighbours (C_3 in the case of the C_1 occupancy discussed above – this is the ring that is most distorted by the presence of the interstitial in the defect model) shares a Ga₂O₇ unit of two bridged three-connected GaO₄ tetrahedra, the four next nearest share edges linking three- and four-connected tetrahedra.

The observed supercell has eight crystallographically distinct centroids as candidate oxygen interstitial sites, and sole occupancy of one of these sets at 1/8 (12.5%) coverage ($x = 0.5$) would leave all seven of the rings neighbouring the occupied interstitial empty with none of the nearest neighbours of these rings occupied (Figure 4). This would allow the relaxations in the five nearest-neighbour edge-sharing rings around an interstitial (Figure 2) to take place without interference from similar distortions enforced by the nearest interstitials – only the more distant corner-sharing empty nearest-neighbours are shared by the occupied sites.

In fact, the situation is more complex as the interstitials remain disordered positionally in the tetragonal structure (where all five-ring centroid sites are equivalent) to beyond 12.5% coverage to 13.75% ($x = 0.55$). Sharing of the most distorted five edge-sharing neighbours can be avoided in disordered interstitial occupancies within the tetragonal structure up to $x > 0.5$ (Figure 5). The observation of long-range order of the displacements between $x = 0.5$ and 0.6 suggests that the sharing of the empty corner-shared neighbours by the occupied interstitials does have some energetic significance.

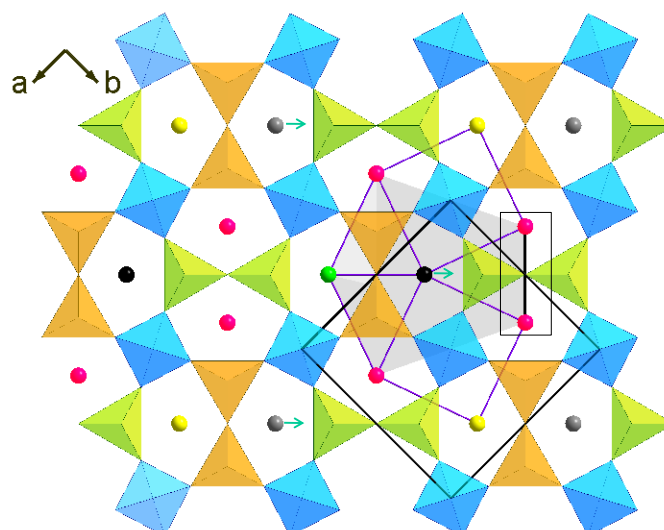


Figure 4 The seven five-ring centroids surrounding an occupied interstitial site (black sphere) - red spheres represent rings sharing an edge of 3- and 4-connected GaO₄ units; green spheres, a 3-connected Ga₂O₇ edge (this ring is the most heavily distorted by the presence of the interstitial); yellow spheres, rings linked by corner-sharing; 4-connected GaO₄ units are coloured cyan. The two orientations of the Ga₂O₇ dimers of 3-connected tetrahedra are shown in green (black bonds in Figure 1a) and orange (pink bridging oxygens in Figure 1a) and represent the two displacement directions of the interstitial oxide in the disordered tetragonal structure. The green arrow shows the single displacement direction in the ordered orthorhombic structure. The five nearest neighbour interstitial sites are represented as a grey pentagon centred on the occupied ring. The grey spheres represent a second set of sites whose occupancy does not share the most distorted near-neighbour ring (green spheres) of the first set. The highlighted black line connects two ring centroids (marked as black spheres in Figure 6) which can only have two of the three neighbour black and grey sites occupied at the observed composition..

At $x = 0.55$, interstitial ordering occurs to minimize the overlap of the strain fields produced by the displacements into neighbouring rings. This can be discussed in terms of the direction of the displacement of the interstitial oxide towards the isolated 3 connected GaO₄ unit within each ring, away from the edge defined by the Ga₂O₇ unit formed by the bridged 3-connecting GaO₄ units. In the disordered tetragonal structure, there are two equivalent orientations of this edge (Figure 4 and 5), so both displacement directions occur. In order to ensure that the most distorted neighbouring ring to an occupied interstitial (sharing the Ga₂O₇-bridged edge away from which O_{int} displaces to bond with the isolated 3 connected Ga) is not shared, it is necessary to order the occupancy of the interstitial sites at $x > 0.6$ by selecting one of these two displacement directions that are degenerate in the tetragonal structure. This requires four of the eight interstitial sites corresponding to the other displacement direction to be empty. It is then possible to select a second site from within the remaining four which has the same polarity of displacement along the unique direction as the first and will leave empty all seven nearest neighbours of both occupied sites (Figure 6). This leaves empty all four of the remaining edge-sharing rings around the most distorted ring produced by the both sets of interstitials (C_3 into which O3a

displaces in the case of the O14a interstitial – represented as white spheres in Figure 6). This avoids sharing the major distortions produced by the two occupied interstitial sites. The other four edge-sharing rings around the first interstitial share one of their four less distorted edges with the second occupied sublattice (Figure 6).

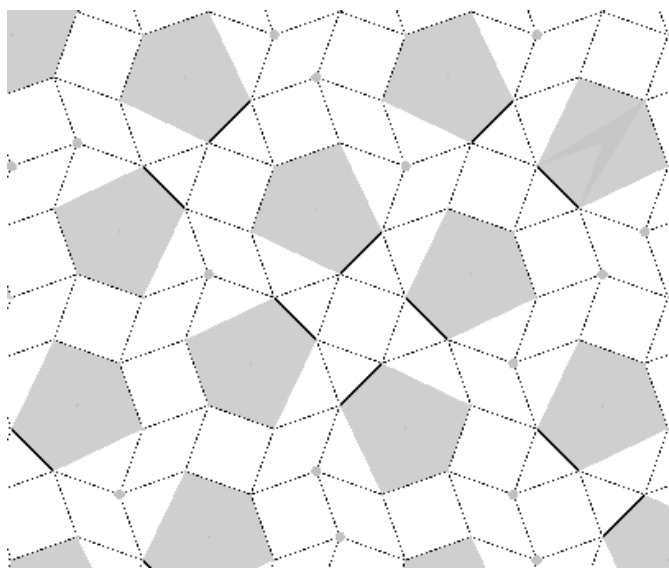


Figure 5 Disordered interstitial occupancy $> 1/8$ in the tetragonal structure, represented using the pentagon of five neighbours (Figure S8.1) to an occupied sphere from Figure 4. The pentagon edges highlighted in black connect the two five ring centroids neighbouring the occupied interstitial which share a common three-connected Ga_2O_7 dimer and indicate the two orientations of interstitial displacement possible in the T structure, in contrast to the distorted structure (Figure 1) where only one orientation/displacement direction is present.

Full occupancy of these two sites sharing the same direction and sense of displacement would give 25% coverage ($x = 1$). The real situation is more complex, as all four of the sites corresponding to one displacement direction (and thus to both senses of this displacement shown in Figure 1) are partly occupied. The observed composition can be rationalized in terms of minimizing the strain in two *next* most distorted rings neighbouring an interstitial (C_6 and C_8 in the case of C_1), which are bridged by a common Ga_2O_7 dimer (Figures 4, 6) either randomly or in an ordered manner. The C_1 (58%) and C_7 (18%) sites correspond to two arrays with the same direction and sense of displacement (green dotted lines in Fig 1), with the O14a C_1 occupancy locally allowing only $\approx 1/3$ of the C_7 sites to be occupied rather than all of them to minimize the strain associated with this empty near-neighbour ring sharing and give a total $2/3$ occupancy of the possible sites. This is an “ordered” model where one of the eight sites is fully occupied and the second site which shares the same sense and direction of the displacement is $1/3$ occupied. The occupancy of the C_3/C_5 pair at 24/28% corresponds to the remaining pair of the four centroids sharing the same displacement direction but with the sense of the displacement along that direction being opposed to the ordered pair (pink dotted lines in Figure 1) – as the occupancy of both sites is approximately equal this corresponds to disordered $2/3$ occupancy of both sites. As less than 40% of sites in total are occupied this can occur in regions not neighbouring the ordered regions referred to above. Simultaneous local occupancy of the C_1/C_7 and C_3/C_5 pairs would place

interstitials as nearest neighbours and would thus be disfavored as relaxation into the rings neighbouring an interstitial would be suppressed.

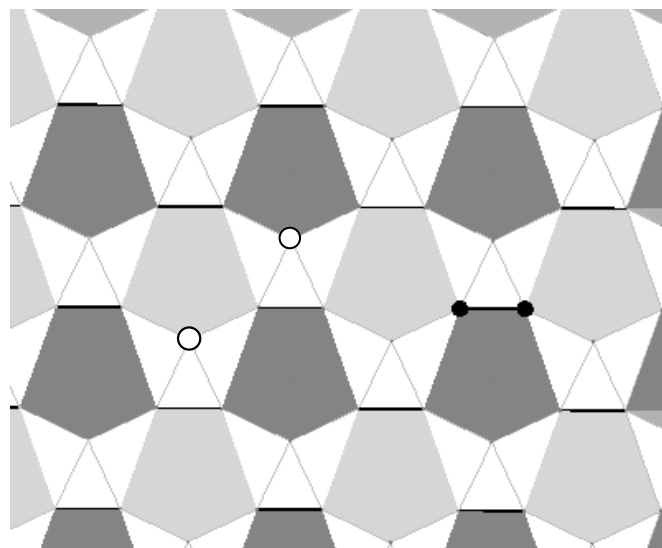


Figure 6 The maximally doped ordered interstitial structure (pentagon centroids represent occupied sites, vertices are empty ones) where the two of the eight sites which share a common interstitial displacement sense and direction are occupied. This avoids two interstitials sharing the most distorted unoccupied ring (white spheres) as a near neighbour. Dark spheres represent two ring centroids sharing a common three-connected Ga_2O_7 edge, equivalent to the highlighted spheres connected by a black line in Figure 4.

The refined structure of the interstitial-ordered orthorhombic phase reveals how the distortions required to stabilise the interstitials at both the tetrahedral and the larger A sites become coupled at high interstitial densities to prevent unfavorable local interactions between carriers. Although the refined cell would need to be doubled again to allow for total carrier order, explaining the rather high residual ionic conductivities, the effect on interstitial mobility through the need to rearrange the complex relaxation around a mobile carrier without adversely affecting potential neighbours in the surrounding five rings can be gauged by the extent of the displacements required between the interstitial-containing and interstitial-free parts of the superstructure, and the requirement to order the La dopants on the A site around the interstitials.

Experimental Section

See Supporting Information. Further details on the crystal structure investigation may be obtained from the Frachinformatiionszentrum Karlsruhe, 76344 Eggenstein-Leopoldsharen, Germany (fax: (+49)7427-806-666; e-mail: crysdta@fiz-karlsruhe.de), on quoting the depository numbers CSD-421081 and 421082.

Received: ((will be filled in by the editorial staff))
Published online on ((will be filled in by the editorial staff))

Keywords: defect structure modulation · interstitial oxide order · ionic conductivity · simulated annealing

[1] B. C. H. Steele, A. Heinzel, *Nature* **2001**, *414*, 345.

- [2] J. B. Goodenough, *Ann. Rev. Mater. Res.* **2003**, *33*, 91.
- [3] J. C. Boivin, G. Mairesse, *Chem. Mater.* **1998**, *10*, 2870.
- [4] T. Ishihara; H. Matsuda, Y. Takita, *J. Am. Chem. Soc.* **1994**, *116*, 3801.
- [5] S. Nakayama, T. Kageyama, H. Aono, Y. Sadaoka, *J. Mater. Chem.* **1995**, *5*, 1801.
- [6] E. Kendrick, M. S. Islam, P. R. Slater, *J. Mater. Chem.* **2007**, *17*, 3104.
- [7] F. Goutenoire, O. Isnard, R. Retoux, P. Lacorre, *Chem. Mater.* **2000**, *12*, 2575.
- [8] P. Lacorre, F. Goutenoire, O. Bohnke, R. Retoux, Y. Laligant, *Nature*, **2000**, *404*, 856.
- [9] I. R. Evans, J. A. K. Howard, J. S. O. Evans, *Chem. Mater.* **2005**, *17*, 4074.
- [10] X. Kuang, M. A. Green, H. Niu, P. Zajdel, C. Dickinson, J. B. Claridge, L. Jantsky, M. J. Rosseinsky, *Nature Mater.* **2008**, *7*, 498.
- [11] M. Rozumek, P. Majewski, H. Schluckwerder, F. Aldinger, *J. Am. Ceram. Soc.* **2004**, *87(9)*, 1795.
- [12] J. M. S. Skakle, R. Herd, *Powder Diffr.* **1999**, *14*, 195.
- [13] a) K. Hagiya, M. Ohmasa, K. Iishi, *Acta Cryst.* **1993**, *B49*, 172. b) K. Hagiya, K. Kusaka, M. Ohmasa, K. Iishi, *Acta Cryst.* **2001**, *B57*, 271. c) M. Ohmasa, K. Hagiya, K. Kusaka, *J. Mineral. Petrol. Sci.* **2002**, *97*, 199.
- [14] S. Kirkpatrick, C. D. Gelatt, M. P. Vecchi, *Science*, **1983**, *220*, 671.
- [15] I. D. Brown, D. Altermatt, *Acta Crystallogr.* **1985**, *B41*, 244
- [16] N. E. Brese, M. O'Keeffe, *Acta Crystallogr.* **1991**, *B47*, 192.
-

Entry for the Table of Contents (Please choose one layout)

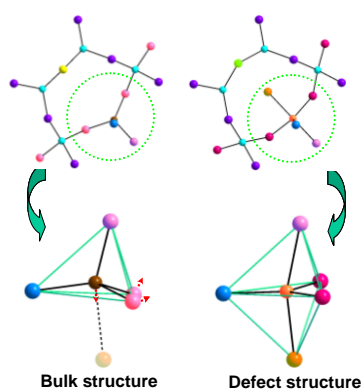
Layout 1:

Oxide Ion Conductors

M. R. Li, X. Kuang, S. Y. Chong, Z. Xu,
C. I. Thomas, H. J. Niu, J. B. Claridge*,
M. J. Rosseinsky*

_____ Page – Page

Interstitial Oxide Ion Order and
Conductivity in $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$
Melilite



The spatial ordering of the oxide interstitial charge carriers in $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ melilite reduces the ionic conductivity. The complex ordering pattern is produced by the cooperative accommodation of the local structural relaxation around the interstitials which extends well beyond the simple formation of GaO_5 trigonal bipyramids from GaO_4 tetrahedra apparent in disordered structures at lower interstitial concentrations.

Supporting Information

Interstitial Oxide Ion Order and Conductivity in $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ Melilite

Man-Rong Li, Xiaojun Kuang, Samantha Y. Chong, Zhongling Xu, Christopher I. Thomas, Hongjun

Niu, John B. Claridge and Matthew J. Rosseinsky**

Department of Chemistry, University of Liverpool, Liverpool, UK, L69 7ZD

The supporting information is organised as follows:

1. Experimental Section
2. XRD data for $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$
3. SAED and HRTEM analysis
4. Phase transition (VT NPD)
5. Structure refinement for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in average models
6. Simulated annealing approach
7. Structure refinement for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in split model
8. Interstitial oxide and A-site cation ordering--composition and crystal structure

1. Experimental Section

The $A_2B_3O_7$ melilite structure, where A is a large eight-coordinated cation ($A = \text{Ca, Sr, Na, Ba, La}$) and B is small cation ($B = \text{Mg, Zn, Al, Ga, Si, Ge, ...}$) in tetrahedral coordination, consists of anionic layers of five-membered rings of totally (four neighbouring tetrahedra) and partially condensed (three neighbouring tetrahedral with a terminal oxygen) BO_4 tetrahedra, separated by parallel sheets of A cations located over the five-ring centres along [001] (Figure S1.1).

$\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+\delta}$ ($0 \leq x \leq 0.7$) ($A = \text{La/Ca}$, $B = \text{Ga}$) were prepared by solid state reaction using La_2O_3 (99.999%, Alfa Aesar), CaCO_3 (99.997%, Alfa Aesar) and Ga_2O_3 (99.999%, Alfa Aesar) as starting materials, which were mixed in ethanol and calcined at 1200 °C for 12 h in alumina crucibles. After regrinding, the powders were uniaxially pressed into pellets and fired at 1400 °C for samples with $x < 0.5$ and 1350 °C for samples with $x > 0.5$ for 12 h at 5 °C/min heating and cooling rates. To compensate the Ga volatilization during the reaction which results in the form of the second phase Ca-doped LaGaO_3 , a slight excess of Ga_2O_3 (~0-1.7 mol% for $x \leq 0.6$; ~2-3.3mol% for $0.6 < x \leq 0.65$; ~5mol% for $x > 0.65$) was added into the initial starting mixture. Attempts to obtain single phase materials at $x = 0.65$ by adding excess Ga_2O_3 (e.g. ~ 2 mol% and ~ 3.3 mol%) failed to remove the second phase Ca-doped LaGaO_3 . Slightly reducing the La/Ca ratio to $x = 0.64$ with ~ 2.3 mol% extra Ga_2O_3 (i.e. initial composition $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_{3.07}$) produced a nearly single phase material $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ with a very small Ga_2O_3 impurity. To avoid reacting with the alumina, the pellets were put on platinum foil during the preparation. The phase purity was checked by powder X-ray diffraction data with a Panalytical X'pert Pro Multi-Purpose X-ray diffractometer (Co $K\alpha_1$ radiation $\lambda = 1.78901\text{\AA}$). Silicon was added as an internal standard during the laboratory XRD experiments in order to refine the variation of the cell parameter with composition. Time-of-flight (TOF) neutron powder diffraction (NPD) data of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ sample were collected from ambient temperature to 800 °C on the HRPD diffractometer at ISIS. After the variable temperature diffraction, the sample

was offline cooled to ambient temperature and another ambient temperature TOF data was collected from comparison with that for the as-made sample. Rietveld refinement was carried out using the GSAS package¹. Compositional analysis was carried out by using the EDAX analyzer on a JEOL 2000FX transmission electron microscope operated at 200 KV. Ac Impedance Spectroscopy (IS) measurements in air from 200 °C to 850 °C were performed with a Solartron 1255B Frequency

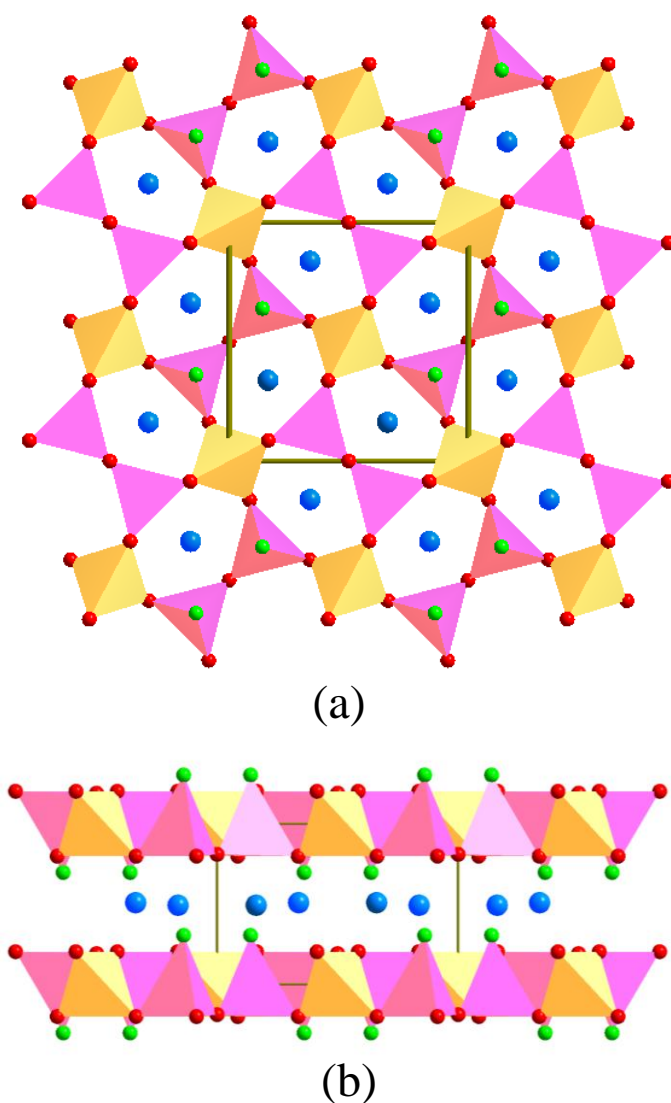


Figure S1.1. Slab view of $A_2B_3O_7$ melilite structure along (a) [001] and (b) [010] direction, showing the five membered BO_4 rings and location of A cations. Four connected BO_4 tetrahedron, yellow; three connected BO_4 , purple; A cation, blue; bridging oxygen, red; terminal oxygen, green.

Response Analyzer, a Solartron 1296 dielectric interface and a Solartron 1287 electrochemical interface over the 10^{-2} - 10^6 Hz frequency range. Prior to the measurement, platinum paste was painted on the opposite faces of the pellets and fired at 800 °C for 30 minutes in air.

2. XRD data for $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$

The parent material $\text{LaCaGa}_3\text{O}_7$ crystallizes in a tetragonal melilite structure in $P\bar{4}2_1m$ ($a = 7.9553(2)$ Å, $c = 5.2727(2)$ Å). With the substitution of Ca^{2+} by La^{3+} , the tetragonal phase extends to $\text{La}_{1.5}\text{Ca}_{0.5}\text{Ga}_3\text{O}_{7.25}$. The cell parameters of $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$ obey Vegard's law for $0 < x < 0.5$. The La^{3+} substitution expanded the a-axis and shortened the c-axis. The volume increased with increasing La^{3+} content. Each (hkl) (h and $k \neq 0$) reflection is broadened at $x = 0.525$ and splits into two distinct peaks at $x > 0.525$, which could be explained by a lower symmetry with inequivalent a-axis and b-axis, i.e. an orthorhombic cell (a and $b \sim \sqrt{2} a_{\text{tetra}}$, $c = c_{\text{tetra}}$) with a sub-group $Cmm2$ of $P\bar{4}2_1m$. The XRD patterns (Figure S2.1) suggested that the as-made samples $x > 0.5$ actually contained both tetragonal and orthorhombic phases and the orthorhombic phase dominates in the samples $x \geq 0.55$. The cell parameters for orthorhombic and tetragonal $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$, shown in Figure S2.2, become constant after $x = 0.65$ which suggests that the solid solution terminates at $x = 0.65$. The XRD pattern of the as-made $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ showed a pure orthorhombic phase with no apparent residual tetragonal phase in the sample. EDS (energy-dispersive spectroscopy) elemental analysis in the TEM investigation showed a homogenous cation ratio $\text{La}_{1.62}\text{Ca}_{0.36}\text{Ga}_3$ for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ against $\text{La}_{1.01}\text{Ca}_{0.93}\text{Ga}_3$ from the EDS analysis for the parent material $\text{LaCaGa}_3\text{O}_7$.

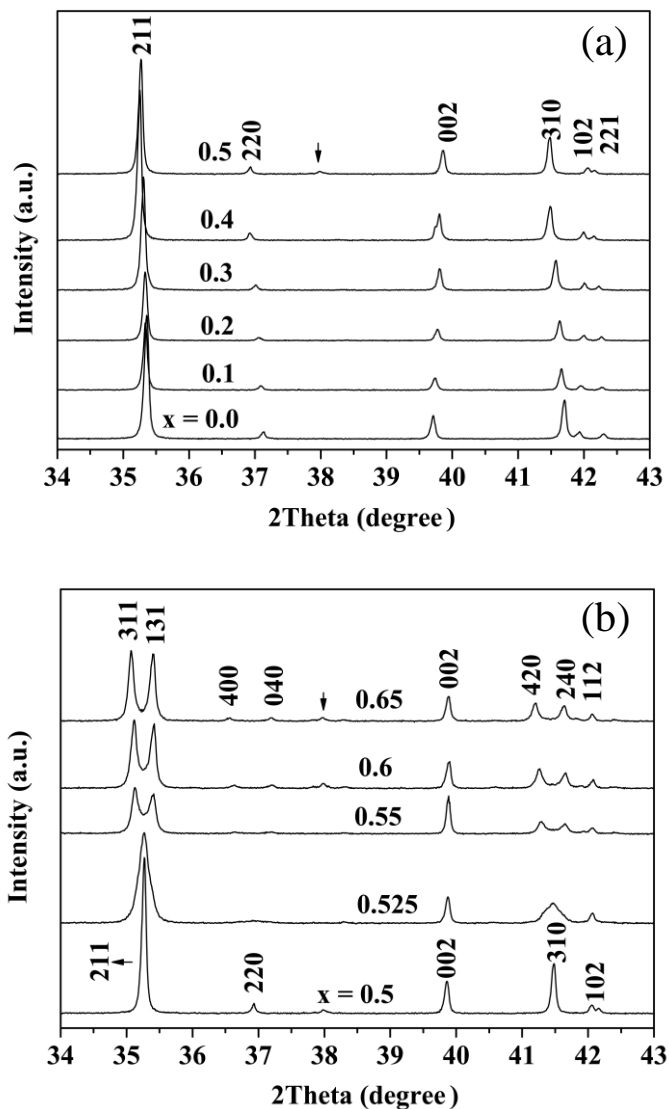


Figure S2.1. XRD patterns of as-made $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$. (a) $x \leq 0.5$ adopting the tetragonal cell and (b) $x \geq 0.55$ indexed with the orthorhombic cell. The arrows mark reflections from the second phase Ca-doped LaGaO_3 .

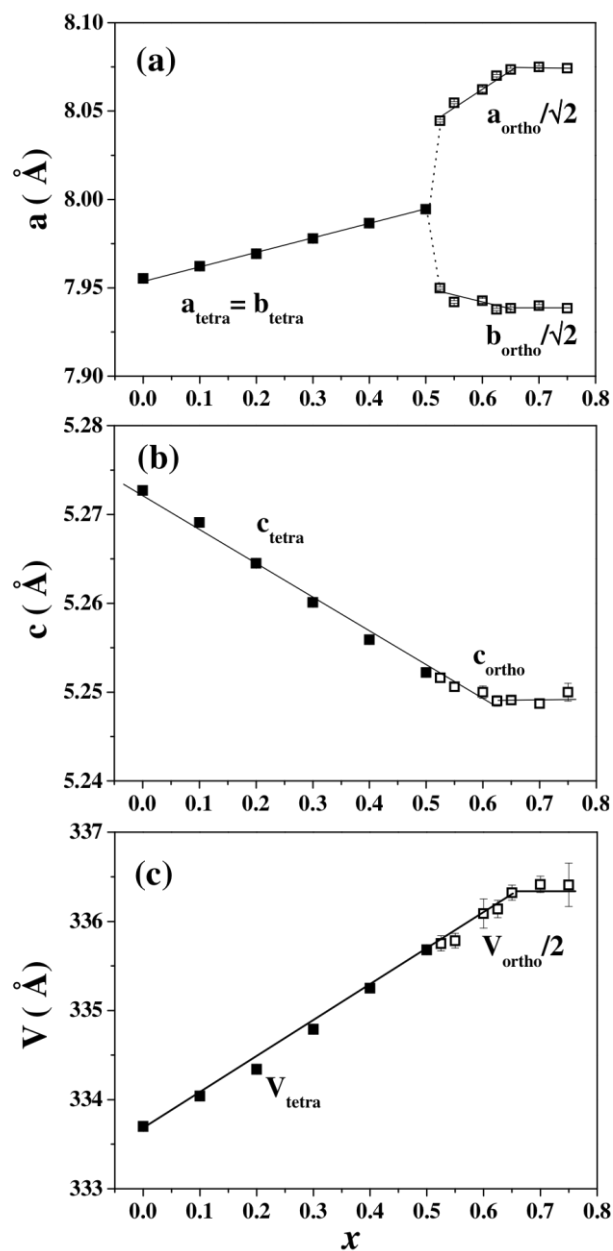


Figure S2.2. Cell parameters versus compositions for the $\text{La}_{1+x}\text{Ca}_{1-x}\text{Ga}_3\text{O}_{7+0.5x}$ solid solution. The orthorhombic cell parameters a_{ortho} and b_{ortho} were divided by $\sqrt{2}$ and volume by 2 for comparison with tetragonal cell. The tetragonal and orthorhombic cells are represented by using filled and open squares, respectively.

3. SAED and HRTEM analysis

SAED results showed that, although the main diffraction features were consistent with the crystal structure proposed by XRD (space group $Cmm2$, $a = 11.42 \text{ \AA}$, $b = 11.23 \text{ \AA}$ and $c = 5.25 \text{ \AA}$), extra weak reflections were observed in the diffraction patterns along certain crystal axes. These extra spots can be indexed simply by doubling the c axis of the proposed unit cell. The reciprocal lattice reconstruction indicates a c -axis doubled body-centered supercell based on the above $Cmm2$ cell with no other systematic absences observable, suggesting possible space groups $Imm2$, $Im11$, and even in triclinic cell $I1$. Figure S3.2 shows the simulated SAED patterns for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ according to the triclinic cell (Space group of $P1$, $a = 9.5735 \text{ \AA}$, $b = 9.5754 \text{ \AA}$, $c = 9.5691 \text{ \AA}$, $\alpha = 106.78^\circ$, $\beta = 108.17^\circ$, $\gamma = 113.51^\circ$, its relationship to the $I1$ cell is shown in Figure S3.1)

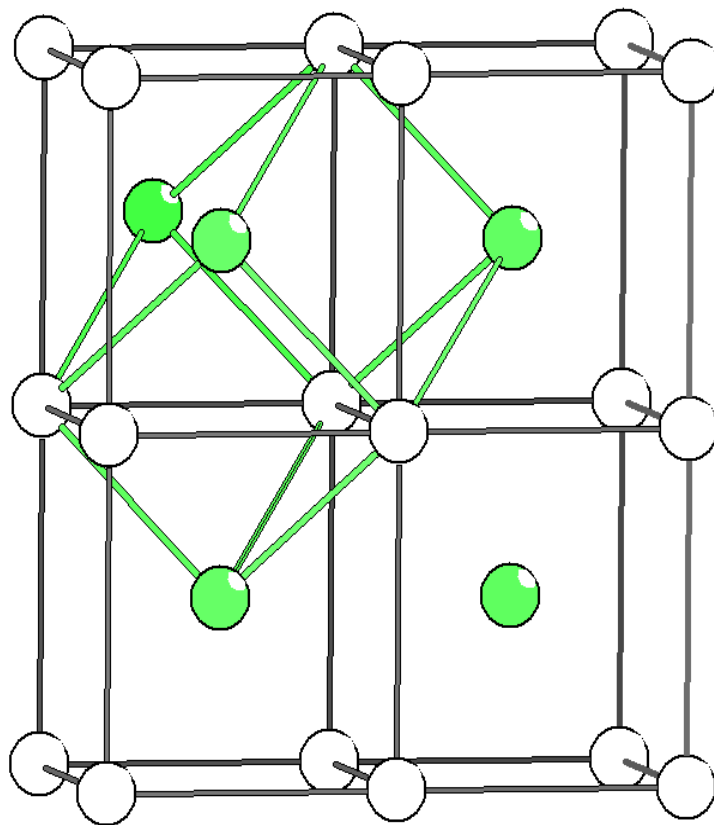


Figure S3.1 The relationship between body-centered (I) and primitive (P) unit cells, where the I -cell edges are black, P -cell edges green, and the green spheres are the centres of I -cell.

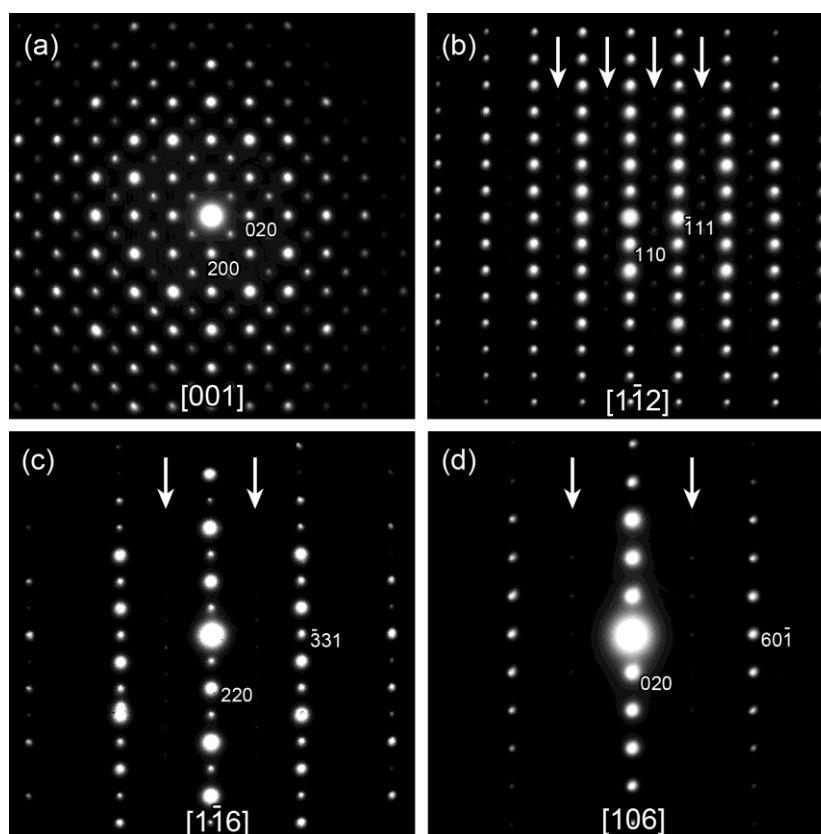


Figure S3.2 SAED patterns for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ along the (a) $[001]$ axis where no extra reflections are observed, and the (b) $[1\bar{1}\bar{2}]$ (c) $[1\bar{1}\bar{6}]$ and (d) $[106]$ axes where superlattice reflections (as marked by white arrows), which can be indexed as $(hk\frac{2n+1}{2})$, indicate the c -doubling. The axes and reflections are indexed according to the PI cell.

HRTEM was applied to check possible microstructural crystal defects, such as twinning, in order to investigate any relationship with the weak diffraction features. [Figure S3.3](#) is the HRTEM image along $[112]$ (left) and $[121]$ (right) simulated in the triclinic c -doubled supercell in PI with the final refined structural model. The images simulated from different directions are quite similar, and it is thus clear that the extra weak reflections in SAED are intrinsic features, instead of arising from microscopic defects, and responsible for the doubled c -axis.

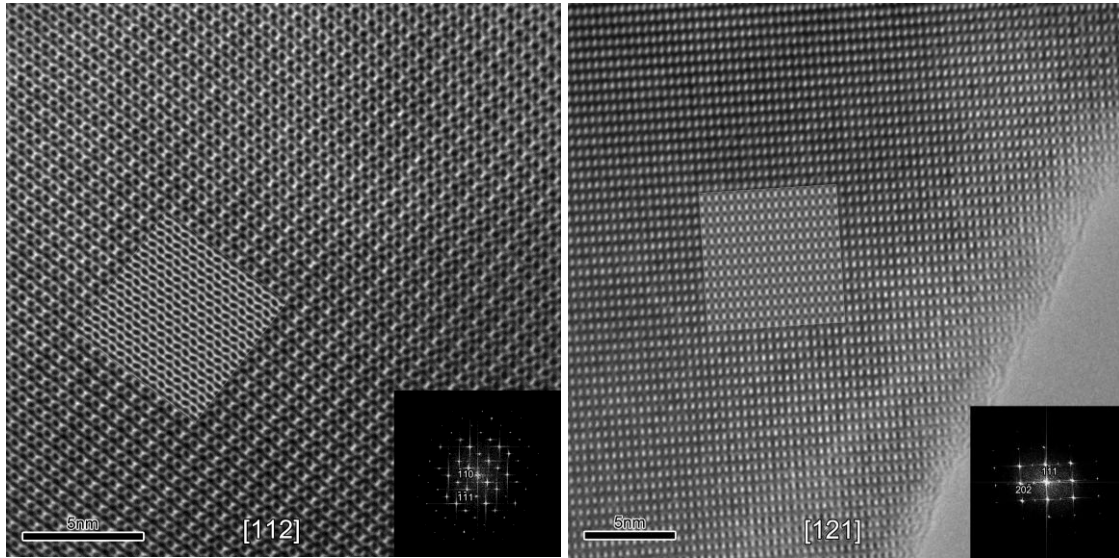


Figure S3.3 HRTEM of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ along [112](left) and [121](right) in *P1* cell. Inset is the simulated image from the final refined model along this direction.

4. Phase transition (Variable temperature NPD)

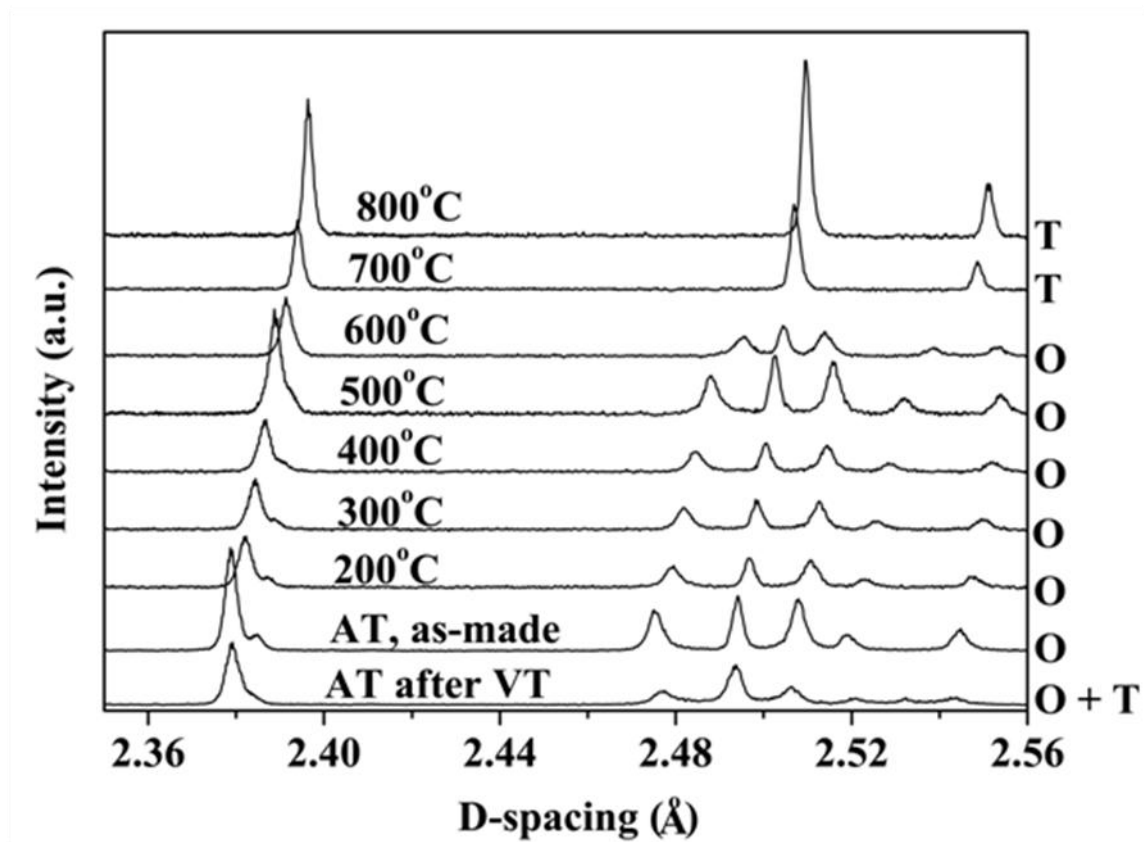


Figure S4.1 Variable temperature (VT) time-of-flight neutron diffraction (TOF ND) patterns for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ upon heating show a phase transition between 600 and 700 °C. The phases present at each temperature are marked as orthorhombic (O) and tetragonal (T) phases. The O and T phases coexist as shown in the ambient temperature (AT) data after VT experiment, compared with the AT data for as-made sample (O phase only).

5. Structure refinement for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in average models

High resolution neutron HRPD (TOF) data from both backscattering (NPD168) and 90 degree (NPD90) detectors were used for crystal structure refinement in GSAS. Refinements were carried out in the following sequence (Figure S5.1), in order to explore the possible space groups suggested by SAED.

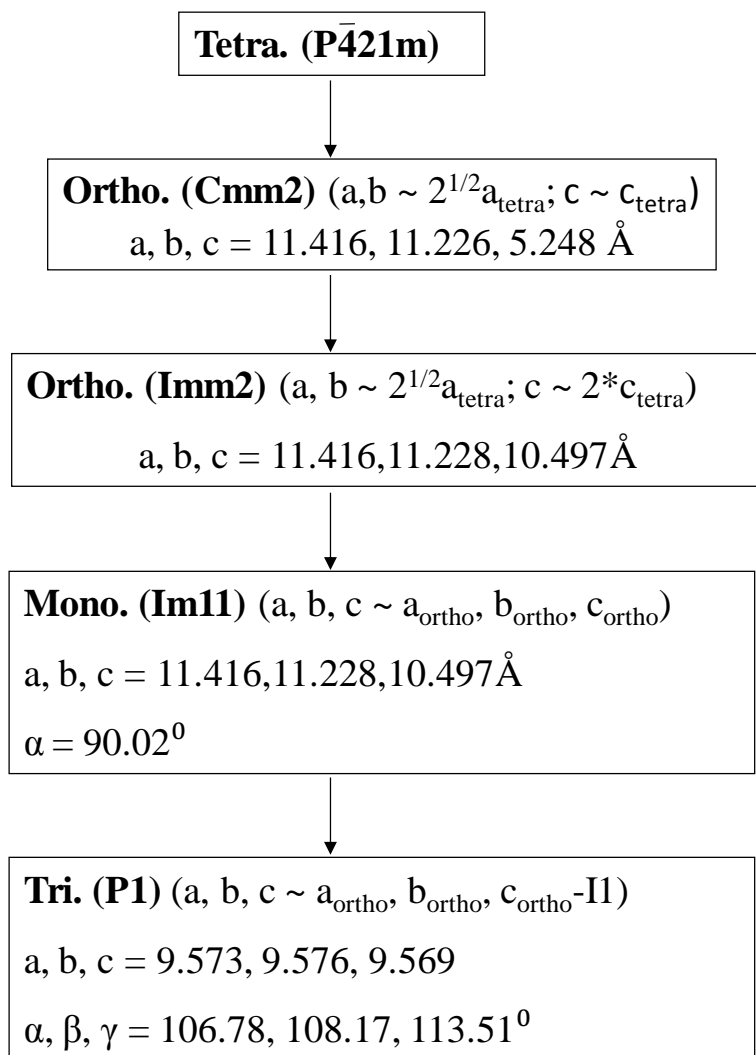


Figure S5.1 Schematic diagram for structure refinement

The general parameters, including histogram scale factors, background coefficients, unit cell parameters, zero error and peak shape coefficients, were varied for all refinements. Framework atoms of the starting model were derived from tetragonal melilite phase and the extra oxygen sites were

established using Fourier synthesis techniques and refined in accordance with nominal composition and charge balance. The atomic positional and displacement parameters of mixed site atoms were constrained to be the same. In the split-site model, the atomic displacement parameters (ADPs) for split sites were refined isotropically for convergence, and the related values for bulk and defect structure were simultaneously refined to be the same value. The final refined results were shown in [Table S5.1](#).

Table S5.1 The cell parameters, refined variables (RV), and fitted parameters from the final refinement in S.G. *Cmm2*, *Imm2*, *Im11*, *P1* (average model (*P1*-average) and split model (*P1*-split) for comparing.

S.G.	<i>Cmm2</i>	<i>Imm2</i>	<i>Im11</i>	<i>P1</i> -average	<i>P1</i> -split
a (Å)	11.41253(6)	11.41582(3)	11.41608(3)	9.57355(3)	9.57230(4)
b (Å)	11.22407(6)	11.22801(3)	11.22797(3)	9.57482(3)	9.57283(4)
c (Å)	5.24802(9)	10.49733(3)	10.49736(2)	9.56915(3)	9.56967(4)
α (°)	90	90	90.023(1)	106.781(1)	106.779(1)
β (°)	90	90	90	108.173(1)	108.176(1)
γ (°)	90	90	90	113.510(1)	113.501(1)
V (Å ³)	672.24(2)	1345.516(6)	1345.547(5)	672.846(4)	672.726(4)
RV	122	201	320	536	507
<i>R</i>_{wp}/<i>R</i>_p %	4.81/5.47	4.12/5.37	3.37/4.96	3.21/4.60	3.30/4.42
χ²	9.31	6.84	4.69	4.28	4.81

5.1 Orthorhombic cell, *Cmm2* space group

The Rietveld refinement plots of data in the *Cmm2* cell (see Section 3 and [Figure S5.1](#)) are shown in [Figure S5.2](#) ($R_{wp}/R_p = 4.81/5.47\%$, $\chi^2 = 9.31$). As can be seen in [Figure S5.2](#), the fit is poor, especially in the high d-spacing range (~ 2.4 Å). No significant improvement on the fitting was achieved by adding a tetragonal phase in the refinement, indicating that there is no minor quenched tetragonal phase. Excess weak reflections could be examined as shown in the inset of [Figure S5.2a](#), which requires a larger supercell. Thus, the following refinements were carried out considering the c-axis doubled supercell as discussed above (Section 3 and [Figure S5.1](#)).

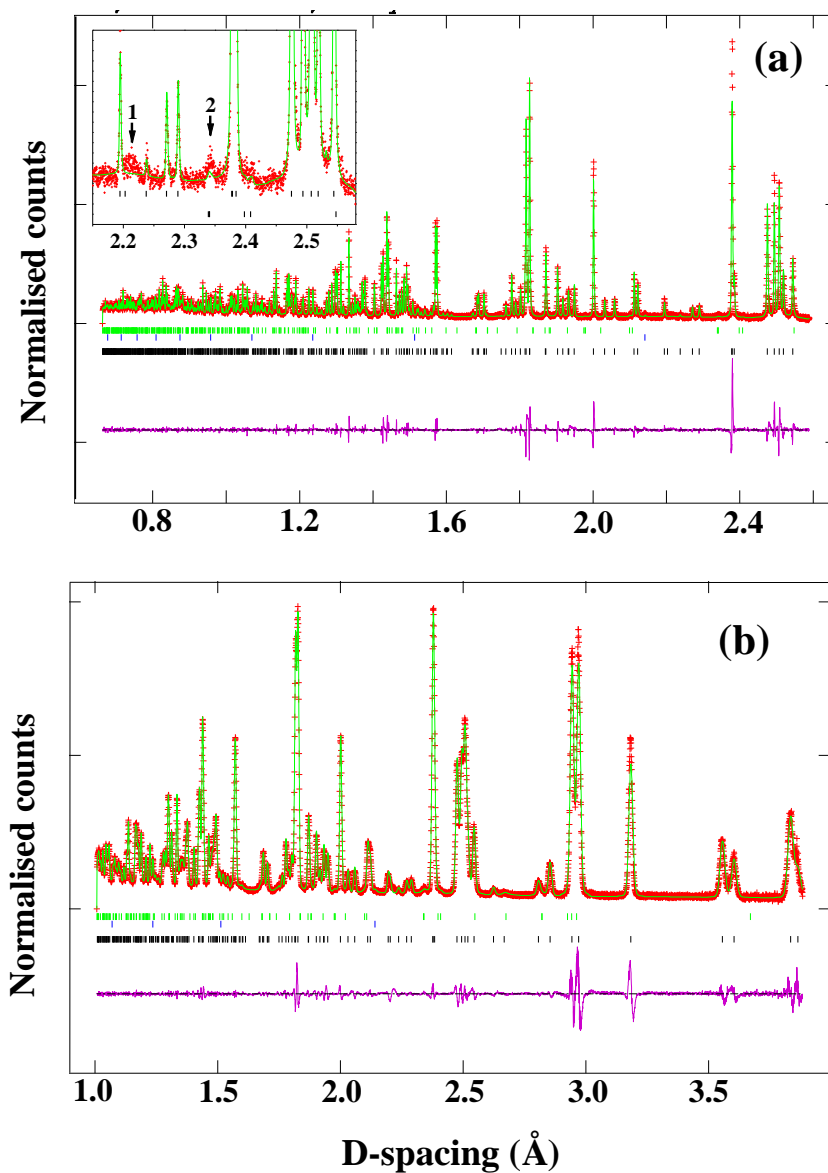


Figure S5.2 Rietveld refinement of RT HRPD ND data in S.G. *Cmm2* from (a) backscattering (b) 90 degree banks. Three rows of vertical tick mark the reflections from $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$, the vanadium container, and Ga_2O_3 from bottom to top, respectively. The enlarged inset of (a) between 2.15-2.56 Å of to show two set of weak reflections, which cannot be accounted for by the *Cmm2* cell, requiring a *Ic*-doubling cell. The impurity Ga_2O_3 has contribution to the weak reflections around 2.35 Å marked as 2.

5.2 Orthorhombic cell, *Imm2* space group

The followed Rietveld refinement in the c-doubled supercell in *Imm2* still gave poor fitting (Figure S5.3; $R_{wp}/R_p = 4.12/5.37\%$, $\chi^2 = 6.84$). The fit cannot be improved by switching to the Stephen's anisotropic broadening function² or by adding the tetragonal phase into the refinement, which suggested the investigation of lower symmetry for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$.

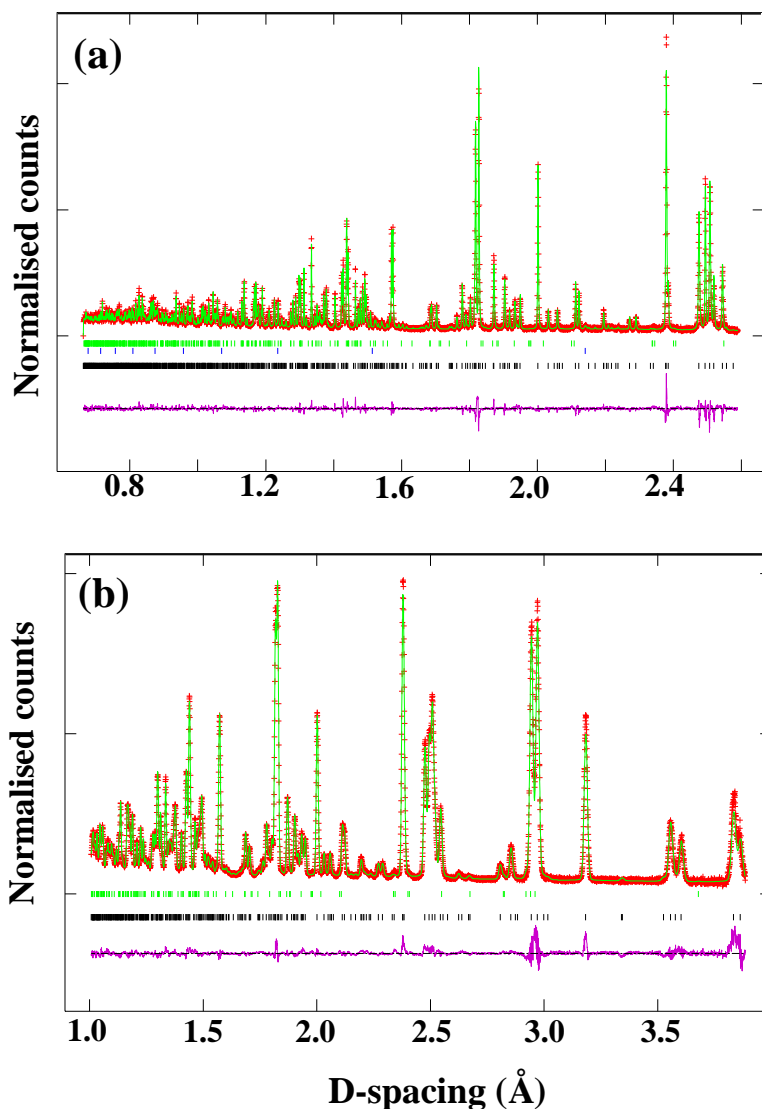


Figure S5.3 Rietveld refinement of RT HRPD ND data in S.G. *Imm2* from (a) backscattering (b) 90 degree banks. Three rows of vertical tick mark the reflections from $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$, the vanadium container, and Ga_2O_3 from bottom to top, respectively

5.3 Monoclinic cell, *Im11* space group

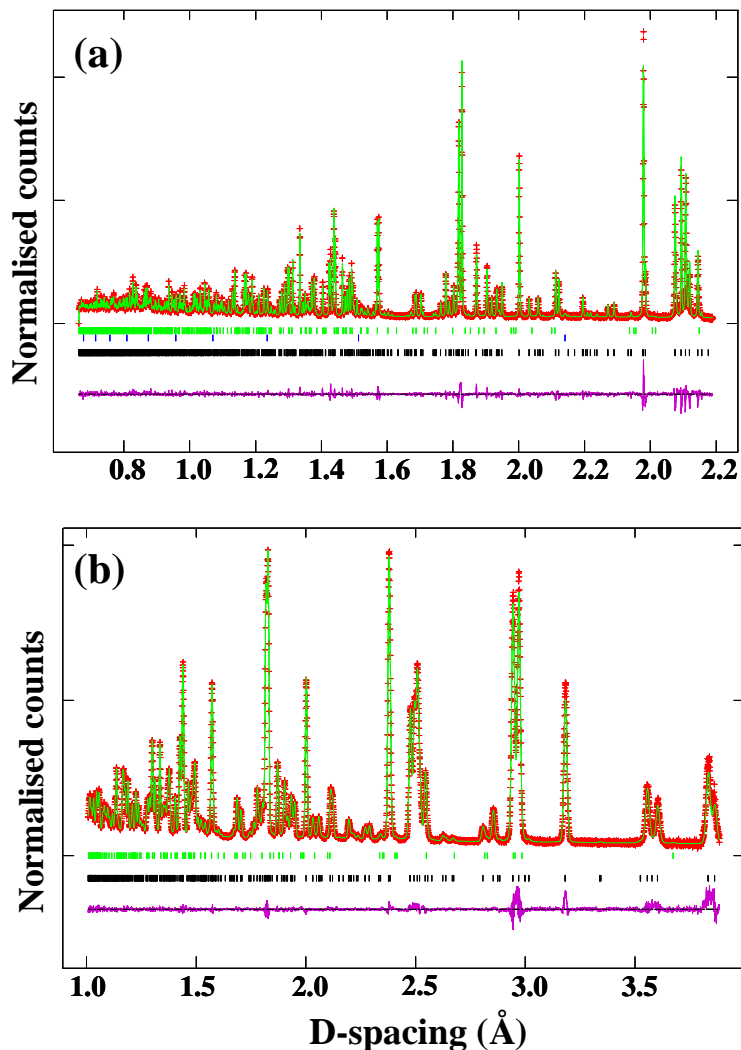


Figure S5.4 Rietveld refinement of RT HRPD ND data based on the average model in S.G. *Im11* from (a) backscattering (b) 90 degree banks. Three rows of vertical tick mark the reflections from La_{1.64}Ca_{0.36}Ga₃O_{7.32}, the vanadium container, and Ga₂O₃ from bottom to top, respectively.

The Rietveld refinement in the lower symmetry monoclinic space group *Im11* is significantly improved as shown in Figure S5.4 compared with Figure S5.3 and converged to $R_{wp}/R_p = 3.37/4.96\%$, and $\chi^2 = 4.69$. Three distinct interstitial sites were revealed and the total population was constrained to be 2.56 for charge balance as listed in Table S5.2 and Figure S5.5. However, a slight misfit in the high d-spacing range (~ 2.0 Å) could be observed (Figure S5.4), implying lower symmetry and/or more

ordered extra oxide distribution. Therefore, further refinement was performed in a triclinic cell (*PI*) by removing the mirror symmetry element in [Figure S5.5](#).

Table S5.2 Refined structural parameters for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ at room temperature for the average structure in monoclinic *Im11*

Atom	Site	x	y	z	Occupancy
La/Ca1	4b	0.3367(1)	0.4926(2)	0.7498(1)	0.780(1)/0.220(1) ^a
La/Ca2	4b	0.3371(1)	0.4904 (3)	0.2496(1)	0.984(1)/0.016(1) ^a
La/Ca3a	2a	0.5	0.8309(2)	0.7538(3)	0.915(1)/0.085(1) ^a
La/Ca3b	2a	0.5	0.1529(2)	0.7589(2)	0.620(1)/0.380(1) ^a
La/Ca4a	2a	0.5	0.8250(2)	0.2621(2)	0.651(1)/0.349(1) ^a
La/Ca4b	2a	0.5	0.1534(2)	0.2464(2)	0.846(1)/0.154(1) ^a
Ga1a	4b	0.2520(3)	0.7432(3)	0.4961(2)	1
Ga1b	4b	0.7491(3)	0.2423(3)	0.4969(2)	1
Ga2a	4b	0.1351(1)	0.4858(3)	0.5165(1)	1
Ga2b	4b	0.1371(1)	0.4851(2)	0.0170(1)	1
Ga3a1	2a	0.5	0.6368(2)	0.9818(2)	1
Ga3a2	2a	0.5	0.3360(2)	0.9805(2)	1
Ga3b1	2a	0.5	0.6378(2)	0.4867(2)	1
Ga3b2	2a	0.5	0.3438(2)	0.4823(2)	1
O1	2a	0.5	0.4871(4)	0.9088(2)	1
O2	2a	0.5	0.4926(4)	0.4044(2)	1
O3a	2a	0.5	0.0236(2)	0.5978(3)	0.704(8) ^b
O3b	2a	0.5	0.9884(11)	0.6074(6)	0.296(8) ^b
O4a	2a	0.5	-0.0047(11)	0.0952(5)	0.444(6) ^c
O4b	2a	0.5	0.9377(4)	0.0815(6)	0.556(6) ^c
O5	4b	0.1376(1)	0.4923(4)	0.8454(1)	1
O6	4b	0.1376(1)	0.4931(3)	0.3441(1)	1
O7a	2a	0.5	0.6286(2)	0.6580(3)	1
O7b	2a	0.5	0.3502(2)	0.6548(2)	1
O8a	2a	0.5	0.6238(3)	0.1540 (3)	1
O8b	2a	0.5	0.3538(2)	0.1501(2)	1
O9a	4b	0.2384(2)	0.5998(2)	0.0802(2)	1
O9b	4b	0.7897(2)	0.36108(2)	0.1053(2)	1
O10a	4b	0.2151(2)	0.6140(2)	0.6006(2)	1
O10b	4b	0.7895(2)	0.3630(2)	0.6020(2)	1
O11a	4b	0.8739(2)	0.2075(2)	0.3936(2)	1
O11b	4b	0.1383(2)	0.8017(2)	0.3938(2)	1
O12a	4b	0.8722(2)	0.1959(2)	0.8932(2)	1
O12b	4b	0.1235(1)	0.7790(1)	0.8923(2)	1
O13	4b	0.490(2)	0.1459(4)	0.0152(7)	0.155(2) ^d
O14a	2a	0.5	0.8271(3)	0.4961(4)	0.673(1) ^d
O14b	2a	0.5	0.1550(6)	0.484(3)	0.294(2) ^d

Space group: *Im11*; $Z = 8$; $a = 11.4161(1) \text{ \AA}$, $b = 11.2280(1) \text{ \AA}$, $c = 10.4974(1)$, $\alpha = 90.02(1)^\circ$, $V = 1345.55(1) \text{ \AA}^3$; $R_{wp}/R_p(\text{NPD168}) = 6.41/6.30\%$; $R_{wp}/R_p(\text{NPD90}) = 2.90/3.60\%$; $R_{wp}/R_p(\text{Total}) = 3.37/4.97\%$; and $\chi^2 = 4.72$.

^a Occupancies of mixed La/Ca site were constrained to be unity and the total La/Ca = 6.56/1.44

^{b,c} Occupancy (Occ.) sum of O3a and O3b was constrained to be unity (Occ.O3a + Occ. O3b = 1), as for O4a and O4b (Occ.O4a + Occ. O4b = 1).

^d The interstitial oxide content was constrained according to the charge-balanced nominal composition at 2.56 in the unit cell.

Atom	$U_{11}(\text{\AA}^2)$	$U_{22}(\text{\AA}^2)$	$U_{33}(\text{\AA}^2)$	$U_{12}(\text{\AA}^2)$	$U_{13}(\text{\AA}^2)$	$U_{23}(\text{\AA}^2)$
La/Ca1 ^a	0.0055(5)	0.0058(4)	0.0060(4)	0.001(2)	0.0001(6)	0.0015(13)
La/Ca2 ^a	0.0207(5)	0.0295(5)	0.0369(6)	-0.008(2)	-0.0039(7)	0.001(2)
La/Ca3a ^a	0.053(2)	0.053(1)	0.056(1)	0	0	-0.002(2)
La/Ca3b ^a	0.0065(10)	0.0060(9)	0.0066(10)	0	0	0.001(1)
La/Ca4a ^a	0.0134(11)	0.0132(10)	0.0205(11)	0	0	-0.004(1)
La/Ca4b ^a	0.0256(11)	0.0122(10)	0.0348(10)	0	0	0.005(1)
Ga1a	0.0092(5)	0.0093(5)	0.0103(4)	-0.0004(5)	0.003(2)	0.004(2)
Ga1b	0.0099(5)	0.0090(5)	0.0175(5)	0.0034(5)	0.007(2)	-0.005(2)
Ga2a	0.0237(6)	0.0361(7)	0.0260(7)	0.001(2)	-0.002(1)	-0.014(2)
Ga2b	0.0056(5)	0.0136(5)	0.0079(3)	0.001(1)	-0.0020(5)	-0.007(1)
Ga3a1	0.0069(9)	0.0114(10)	0.0118(10)	0	0	0.0072(11)
Ga3a2	0.0084(10)	0.0027(9)	0.0059(9)	0	0	-0.0039(9)
Ga3b1	0.087(11)	0.0228(1)	0.0225(12)	0	0	-0.003 (1)
Ga3b2	0.0149(10)	0.0206(11)	0.0141(11)	0	0	-0.004(1)
O1	0.034(1)	0.034(1)	0.024(1)	0	0	-0.016(4)
O2	0.0113(10)	0.0146(10)	0.001(1)	0	0	0.001(3)
O3a/O3b ^a	0.0021(11)	0.026(2)	0.009(1)	0	0	0.009(2)
O4a/O4b ^a	0.048(2)	0.071(4)	0.037(2)	0	0	-0.010(3)
O5	0.0243(9)	0.0290(9)	0.0255(8)	-0.006(3)	-0.0030(9)	0.001(2)
O6	0.0052(7)	0.0055(6)	0.0052(6)	0.001(1)	0.0003(7)	0.002(2)
O7a	0.019(1)	0.013(11)	0.0016(11)	0	0	0.001(1)
O7b	0.0018(11)	0.0019(1)	0.0018(1)	0	0	0.0002(5)
O8a	0.052(2)	0.034(2)	0.036(2)	0	0	-0.015(2)
O8b	0.0016(11)	0.0018(11)	0.0021(11)	0	0	0.0002(1)
O9a	0.0222(11)	0.050(1)	0.043(1)	0.0012(11)	-0.011(1)	0.002(1)
O9b	0.0245(9)	0.0103(8)	0.0124(9)	-0.0029(8)	0.0049(10)	-0.002(1)
O10a	0.0280(11)	0.0279(11)	0.0201(11)	-0.0066(9)	-0.009(1)	0.0154(10)
O10b	0.0364(11)	0.0214(10)	0.0203(11)	-0.009(1)	0.006(1)	0.001(1)
O11a	0.045(1)	0.057(1)	0.027(1)	0.014(1)	-0.004(1)	0.006(1)
O11b	0.0171(10)	0.0354(11)	0.0114(9)	0.0014(9)	-0.004(1)	-0.003(1)
O12a	0.0290(11)	0.047(1)	0.0249(11)	0.0114(10)	-0.004(1)	0.007(1)
O12b	0.0037(8)	0.0056(8)	0.0045(7)	0.0015(7)	-0.003(1)	-0.001(1)
O13	0.006(5)	0.008(4)	0.008(4)	0.004(11)	-0.005(1)	-0.005(4)

O14a	0.018(2)	0.038(2)	0.018(2)	0	0	-0.003(3)
O14b	0.024(9)	0.47(4)	0.55(5)	0	0	-0.22(4)

^a ADPs of mixed La/Ca and disordered O3a/O3b, O4a/O4b pairs were constrained to be the same value.

Table S5.3 Selected inter-atomic distances and BVS calculations for La_{1.64}Ca_{0.36}Ga₃O_{7.32} at room temperature from the average model in monoclinic cell (S.G. *Im11*)

Bond		Length(Å)		Bond		Length(Å)	
La/Ca1	O5	2.485(2)	(x1)	Ga1a	O11b	1.807(4)	(x1)
	O10a	2.498(3)	(x1)		O9b	1.803(3)	(x1)
	O1	2.507(2)	(x1)		O12a	1.825(4)	(x1)
	O10b	2.569(3)	(x1)		O10a	1.867(3)	(x1)
	O7a	2.595(3)	(x1)	BVS for Ga1a		3.10	
	O11b	2.639(3)	(x1)	Ga1b	O10b	1.808(4)	(x1)
	O7b	2.650(2)	(x1)		O9a	1.827(4)	(x1)
	O11a	2.877(3)	(x1)		O11a	1.833(4)	(x1)
BVS for La/Ca1		2.62/1.50			O12b	1.853(4)	(x1)
				BVS for Ga1b			
La/Ca2	O9a	2.437(3)	(x1)			3.05	
	O2	2.470(2)	(x1)	Ga2a	O4a	1.753(3)	(x1)
	O6	2.484(2)	(x1)		O4b	1.771(3)	(x1)
	O9b	2.550(3)	(x1)		O6	1.813(2)	(x1)
	O8a	2.590(3)	(x1)		O10b	1.857(3)	(x1)
	O8b	2.627(3)	(x1)	O10a	1.919(3)	(x1)	
	O12a	2.785(4)	(x1)	BVS for Ga2a		3.02	
	O12b	2.842(3)	(x1)	Ga2b	O5	1.804(2)	(x1)
BVS for La/Ca2		2.70/1.55			O3a	1.832(2)	(x1)
La/Ca3a	O3b	2.343(11)	(x1)	O3b	1.831(3)	(x1)	
	O11a	2.479(3)	(x2)	O9b	1.870(3)	(x1)	
	O7a	2.483(4)	(x1)	O9a	1.854(3)	(x1)	
	O6	2.585(3)	(x2)	BVS for Ga2b		2.98	
	O14a	2.705(5)	(x1)	Ga3a1	O8a	1.814(4)	(x1)
	O3a	2.714(4)	(x1)		O1	1.845(5)	(x1)
	O9b	2.882(2)	(x2)		O11a	1.8874(3)	(x2)
	BVS for La/Ca3a		2.84/1.63		BVS for Ga3a1		2.84
La/Ca3b	O3a	2.228(4)	(x1)	Ga3a2	O8b	1.791(3)	(x1)
	O3b	2.437(10)	(x1)		O1	1.853(5)	(x1)
	O7b	2.471(3)	(x1)		O11b	1.863(2)	(x2)
	O6	2.547(3)	(x2)		O13	2.169(5)	(x2)
	O11b	2.701(3)	(x2)	BVS for Ga3a2		3.57	
	O13	2.694(8)	(x2)	Ga3b1	O7a	1.802(3)	(x1)
	O14b	2.89(3)	(x1)				

BVS for La/Ca3b	3.03/1.74		O2	1.845(5)	(x1)		
			O12a	1.875(3)	(x2)		
La/Ca4a	O4b	2.279(6)	(x1)	O14a	2.127(4)	(x1)	
	O14a	2.457(6)	(x1)	BVS for Ga3b1	3.25		
	O12a	2.475(3)	(x2)				
	O8a	2.528(4)	(x1)	Ga3b2	O7b	1.813(3)	(x1)
	O4a	2.594(10)	(x1)		O12b	1.846(2)	(x2)
	O5	2.600(4)	(x2)		O2	1.860(5)	(x1)
	O10b	2.963(2)	(x2)		O14b	2.120(7)	(x1)
BVS for La/Ca4a	3.15/1.81		BVS for Ga3b2	3.31			
La/Ca4b	O4a	2.381(10)	(x1)	O3a	O3b	0.408(12)	(x1)
	O13	2.431(8)	(x2)		O14b	1.90(2)	(x1)
	O14b	2.49(3)	(x1)		O14a	2.452(5)	(x1)
	O8b	2.468(3)	(x1)	O3b	O14a	2.155(12)	(x1)
	O12b	2.515(3)	(x2)		O14b	2.28(2)	(x1)
	O5	2.611(4)	(x2)	O4a	O4b	0.663(13)	(x1)
	O10a	2.927(2)	(x2)		O13	1.891(12)	(x2)
	O4b	2.976(6)	(x1)	O4b	O13	2.442(7)	(x2)
BVS for La/Ca4b	3.35/1.92						

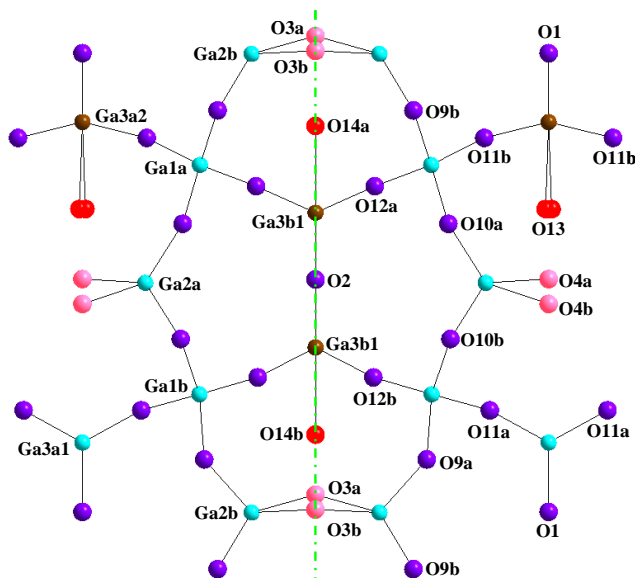


Figure S5.5 Projection view of the crystal structure along the *c*-axis in *Im11* symmetry. The dashed line shows the ‘mirror plane’. The A-site cations and oxygens overlapped with galliums were omitted for clarity.

Figure S5.5 shows a view of the crystal structure along the *c*-axis. In the crystal structure, Ga1aO₄ and Ga1bO₄ tetrahedra are 4-connected with no terminal oxygens, the other GaO₄ polyhedra are 3-

connected with one non-bridging oxygen. Two interstitial sites O14a and O14b are located on the “mirror” plane, O13 is disordered on either side of this plane. As in to $\text{La}_{1.54}\text{Sr}_{0.46}\text{Ga}_3\text{O}_{7.25}$, all the interstitial oxides are closest to tetrahedra with terminal oxygen, namely Ga3a2O_4 , Ga3b1O_4 , and Ga3b2O_4 . Ga2a and Ga2b are also 3-connected with disordered bridging oxygen pairs of O4a/O4b and O3a/O3b, respectively. There is no interstitial oxide connected to Ga2a and Ga2b, leaving the candidate interstitial sites empty inside the channels neighbouring the occupied interstitials.

5.4 Triclinic cell with space group of *PI*

The optimized refinement in triclinic *PI* ($R_{\text{wp}}/R_{\text{p}} = 3.21/4.60\%$, and $\chi^2 = 4.28$, [Figure S5.6](#)) exhibited four distinct interstitial sites with total population of 1.28 as listed in [Table S5.4](#). Compared with the crystal structure in monoclinic symmetry *Im11* ([Section 5.2](#)), all the interstitial oxides are incorporated into GaO_4 tetrahedra with terminal oxygens. Four of the A-sites show cation ordering and are occupied by La only - the occupancy of La was set to be one if it refined to be greater than 0.98. The other four A-sites are disordered and the occupancies were refined to yield a total La/Ca ratio of 6.54/1.44 ([Table S5.4](#)). Refinement of a random A-site distribution (La/Ca = 0.82/0.18 for each site) led to a poorer fit ($R_{\text{wp}}/R_{\text{p}} = 3.49/4.84\%$, $\chi^2 = 4.96$), which recovered to the previous A-site cation order after the occupancies were refined.

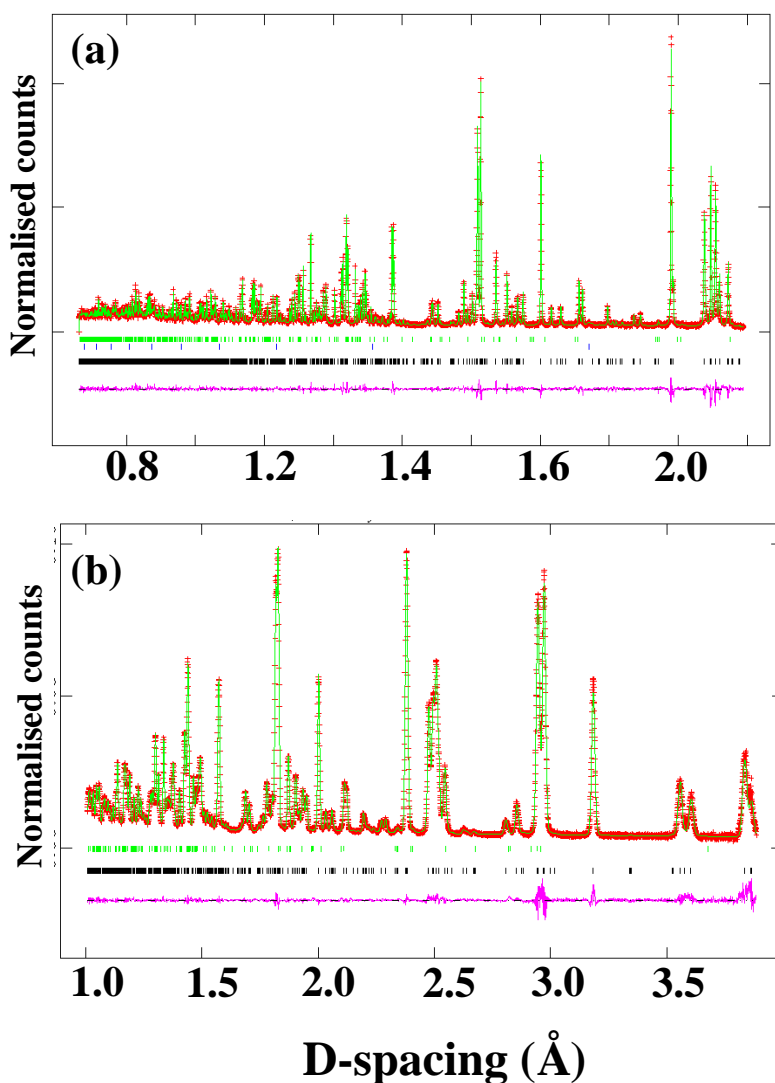


Figure S5.6 Rietveld refinement of RT HRPD ND data for the average model in *PI* from (a) backscattering (b) 90 degree bank. Three rows of vertical ticks mark the reflections from $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$, the vanadium container, and Ga_2O_3 from bottom to top, respectively

Table S5.4 Refined structural parameters for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ at room temperature for the average structure model in *PI*.

Atom	Site	x	y	z	Occupancy
La1a	1a	0.2395(2)	0.0877(2)	0.8281(2)	1
La/Ca1b	1a	0.2390(2)	0.4077(3)	0.1503(2)	0.814(1)/0.186(1) ^a
La2a	1a	0.7411(3)	0.5894(3)	0.8235(3)	1
La2b	1a	0.7325(2)	0.9107(3)	0.1506(2)	1

La3a	1a	0.5777(3)	0.2456(4)	0.3282(3)	1
La/Ca3b	1a	0.9118(3)	0.2640(3)	0.6550(3)	0.312(1)/0.688(1) ^a
La/Ca4a	1a	0.0860(2)	0.7608(3)	0.3237(3)	0.623(1)/0.377(1) ^a
La/Ca4b	1a	0.4022(3)	0.7509(2)	0.6536(2)	0.811(1)/0.189(1) ^a
Ga1a	1a	0.2323(4)	0.7434(4)	0.9860(4)	1
Ga1b	1a	0.2346(4)	0.2472(5)	0.4888(5)	1
Ga1c	1a	0.7319(5)	0.2385(4)	0.9810(4)	1
Ga1d	1a	0.7409(4)	0.7462(4)	0.4935(4)	1
Ga2a	1a	0.0023(2)	0.6555(3)	0.6233(2)	1
Ga2b	1a	0.0086(3)	0.3778(3)	0.3556(3)	1
Ga2c	1a	0.5084(2)	0.1534(2)	0.6255(2)	1
Ga2d	1a	0.5042(2)	0.8835(3)	0.3487(2)	1
Ga3a1	1a	0.6189(2)	0.4804(2)	0.1354(2)	1
Ga3a2	1a	0.3202(2)	0.4781(3)	0.8359(3)	1
Ga3b1	1a	0.1240(3)	0.9855(3)	0.1354(3)	1
Ga3b2	1a	0.8247(2)	0.9825(3)	0.8407(3)	1
O1	1a	0.3942(4)	0.4074(4)	0.9853(4)	1
O2	1a	0.8924(3)	0.9002(3)	0.9812(3)	1
O3a	1a	0.6267(4)	0.0856(4)	0.5294(4)	0.618(5) ^b
O3b	1a	0.5758(6)	0.0985(6)	0.4753(6)	0.382(5) ^b
O4a	1a	0.0958(9)	0.5927(8)	0.5029(8)	0.272(12) ^c
O4b	1a	0.0530(4)	0.5911(5)	0.4562(4)	0.728(12) ^c
O5a	1a	0.3367(3)	0.9809(3)	0.6249(3)	1
O5b	1a	0.3393(3)	0.7092(3)	0.3542(3)	1
O6a	1a	0.8382(3)	0.48417(29)	0.6314(3)	1
O6b	1a	0.8303(3)	0.2048(4)	0.3478(3)	1
O7a	1a	0.2877(3)	0.1566(3)	0.1268(3)	1
O7b	1a	0.0056(3)	0.1541(3)	0.8493(3)	1
O8a	1a	0.7779(3)	0.6501(3)	0.1216(3)	1
O8b	1a	0.5053(3)	0.6530(3)	0.8541(3)	1
O9a	1a	0.6767(4)	0.3178(5)	0.8344(5)	1
O9b	1a	0.6998(4)	0.8656(4)	0.3870(5)	1
O9c	1a	0.4697(4)	0.8887(4)	0.1435(4)	1
O9d	1a	0.4675(3)	0.3194(3)	0.5831(3)	1
O10a	1a	0.2110(4)	0.8137(4)	0.8281(4)	1
O10b	1a	0.2304(4)	0.4080(4)	0.4271(4)	1
O10c	1a	0.9664(4)	0.3801(4)	0.1482(4)	1
O10d	1a	0.9690(3)	0.8159(3)	0.5840(3)	1
O11a	1a	0.6277(5)	0.2858(5)	0.1047(5)	1
O11b	1a	0.5937(4)	0.5188(4)	0.3266(4)	1
O11c	1a	0.1844(3)	0.5249(3)	0.9256(3)	1
O11d	1a	0.1962(4)	0.2512(4)	0.6644(4)	1
O12a	1a	0.1043(4)	0.7740(4)	0.0825(4)	1

O12b	1a	0.0763(4)	0.0306(5)	0.3111(4)	1
O12c	1a	0.6720(3)	0.0155(31)	0.9100(3)	1
O12d	1a	0.6736(3)	0.7642(4)	0.6532(3)	1
O13a	1a	0.1577(9)	0.5008(8)	0.6453(8)	0.280(1) ^d
O13b	1a	0.8211(6)	0.4903(10)	0.3172(10)	0.179(1) ^d
O14a	1a	0.3346(6)	0.9991(5)	0.3248(5)	0.582(1) ^d
O14b	1a	0.6181(15)	0.9872(12)	0.6746(11)	0.239(1) ^d

Space group: *PI*; $Z = 4$; $a = 9.5735(1) \text{ \AA}$, $b = 9.5748(1) \text{ \AA}$, $c = 9.5691(1) \text{ \AA}$, $\alpha = 106.78(1)^\circ$, $\beta = 108.17(1)^\circ$, $\gamma = 113.51(1)^\circ$, $V = 672.85(1) \text{ \AA}^3$. $R_{wp}/R_p\%(ND168) = 6.08/5.84$, $R_{wp}/R_p\%(ND90) = 2.77/3.33$, $R_{wp}/R_p\%(Total) = 3.21/4.60$, $\chi^2 = 4.28$.

^a Occupancies of the mixed La/Ca site were constrained to be unity and the total La/Ca ratio 6.56/1.44

^{b,c} Occupancy sum of O3a and O3b was constrained to be unity (Occ.O3a + Occ. O3b = 1); the same to O4a and O4b (Occ.O4a + Occ. O4b = 1).

^d The interstitial oxide content was fixed according to the charge-balanced nominal composition of 1.28 in the unit cell.

Atom	$U_{11} (\text{\AA}^2)$	$U_{22} (\text{\AA}^2)$	$U_{33} (\text{\AA}^2)$	$U_{12} (\text{\AA}^2)$	$U_{13} (\text{\AA}^2)$	$U_{23} (\text{\AA}^2)$
La1a	0.0037(5)	0.0036(5)	0.0041(5)	0.0033(4)	0.0010(4)	0.0013(5)
La/Ca1b ^a	0.0087(6)	0.0098(6)	0.0054(7)	0.0081(5)	0.0019(5)	0.0037(6)
La2a	0.0399(8)	0.0441(11)	0.0471(11)	0.0291(7)	0.0209(7)	0.0078(9)
La2b	0.0263(7)	0.0344(9)	0.0289(9)	0.0188(6)	0.0172(6)	0.0112(7)
La3a	0.0441(9)	0.0463(11)	0.0474(12)	0.0279(7)	0.0207(9)	0.0172(8)
La/Ca3b ^a	0.0169(9)	0.0168(9)	0.0141(10)	0.0142(7)	0.0118(8)	0.0124(7)
La/Ca4a ^a	0.0104(7)	0.0144(9)	0.0136(9)	0.0101(6)	0.0034(7)	0.0040(7)
La/Ca4b ^a	0.0164(7)	0.0137(7)	0.0133(8)	0.0112(5)	0.0028(6)	0.0091(5)
Ga1a	0.0134(7)	0.0111(7)	0.0124(8)	0.0071(5)	0.0044(7)	0.0071(7)
Ga1b	0.0127(7)	0.0139(7)	0.0111(7)	0.0071(5)	0.0075(6)	0.0057(7)
Ga1c	0.0109(7)	0.0142(8)	0.0132(8)	0.0054(5)	0.0037(7)	0.0063(7)
Ga1d	0.0103(7)	0.0093(7)	0.0082(7)	0.0053(5)	0.0031(6)	0.0046(7)
Ga2a	0.0173(8)	0.0202(9)	0.0197(8)	0.0061(7)	0.0135(6)	0.0072(8)
Ga2b	0.0339(9)	0.0435(12)	0.040(1)	0.0119(9)	0.0267(7)	0.0117(11)
Ga2c	0.0018(6)	0.0016(6)	0.0017(6)	0.0009(5)	0.0007(5)	0.0015(6)
Ga2d	0.0146(7)	0.0212(9)	0.0163(8)	0.0051(7)	0.0142(5)	0.0070(8)
Ga3a1	0.0057(6)	0.0024(6)	0.0035(7)	0.0022(5)	0.0028(6)	0.0005(5)
Ga3a2	0.0099(7)	0.0190(9)	0.0216(9)	0.0091(6)	0.0052(7)	0.0030(7)
Ga3b1	0.0182(7)	0.0227(9)	0.0194(9)	0.0116(7)	0.0117(7)	0.0080(7)
Ga3b2	0.0145(8)	0.0206(9)	0.0231(9)	0.0090(7)	0.0105(7)	0.0057(7)
O1	0.0267(10)	0.0352(11)	0.0265(11)	0.0129(8)	0.0140(9)	0.0162(9)
O2	0.0114(8)	0.0171(9)	0.0121(9)	0.0051(7)	0.0083(7)	0.0103(7)

O3a/3b ^a	0.0031(11)	0.0032(13)	0.0030(11)	0.0001(11)	0.0025(7)	0.0001(10)
O4a/4b ^a	0.0493(15)	0.0486(18)	0.0525(17)	0.0093(14)	0.0316(11)	0.0203(14)
O5a	0.0107(10)	0.0107(11)	0.0092(10)	0.0011(9)	0.0071(8)	0.0053(9)
O5b	0.0262(12)	0.0304(13)	0.0338(14)	0.0192(10)	0.0183(9)	0.0164(11)
O6a	0.0040(9)	0.0071(10)	0.0068(10)	0.0023(8)	0.0047(7)	0.0019(8)
O6b	0.0245(12)	0.0283(14)	0.0211(12)	0.0084(11)	0.0111(9)	0.0164(11)
O7a	0.0043(8)	0.0037(9)	0.0035(9)	0.0022(7)	0.0022(8)	0.0028(7)
O7b	0.0203(12)	0.0195(11)	0.0222(11)	0.0065(10)	0.0071(10)	0.0145(8)
O8a	0.0089(9)	0.0156(11)	0.0147(11)	0.0055(9)	0.0082(9)	0.0058(8)
O8b	0.0209(11)	0.0210(12)	0.0331(14)	0.0136(9)	0.0097(11)	0.0101(10)
O9a	0.0547(16)	0.0484(19)	0.0508(20)	0.0319(12)	0.0310(14)	-0.006(2)
O9b	0.0489(17)	0.059(2)	0.078(2)	0.0346(13)	0.0332(17)	0.016(2)
O9c	0.0127(12)	0.0332(16)	0.0207(13)	0.0015(12)	0.0117(10)	0.0141(12)
O9d	0.006(1)	0.0077(10)	0.0182(12)	0.0042(8)	-0.0003(10)	0.0076(11)
O10a	0.0533(17)	0.0207(13)	0.0267(14)	0.0184(12)	0.0116(14)	0.0213(10)
O10b	0.0265(14)	0.0222(12)	0.0240(13)	0.0102(11)	0.0066(12)	0.0193(10)
O10c	0.0156(11)	0.0398(17)	0.0193(12)	0.0071(12)	0.0148(10)	0.0140(13)
O10d	0.0062(9)	0.0069(10)	0.0108(11)	0.0056(8)	0.0019(9)	0.0043(11)
O11a	0.0456(16)	0.0501(18)	0.0596(19)	0.0254(13)	0.0262(15)	0.0391(15)
O11b	0.0312(15)	0.0311(17)	0.0238(15)	0.0068(14)	0.0095(13)	0.0154(14)
O11c	0.0057(9)	0.0053(10)	0.006(1)	0.0016(8)	0.0052(9)	0.0030(9)
O11d	0.0164(12)	0.0159(14)	0.0270(13)	0.0009(11)	0.013(1)	0.0089(11)
O12a	0.0252(11)	0.0200(12)	0.0321(13)	0.0167(9)	0.0222(11)	0.0209(12)
O12b	0.0475(16)	0.0389(19)	0.0393(17)	0.0090(16)	0.0296(14)	0.0134(16)
O12c	0.0046(9)	0.0032(10)	0.0063(10)	0.0016(8)	0.0046(9)	0.0025(9)
O12d	0.0140(11)	0.0210(14)	0.0169(12)	0.0052(10)	0.0128(10)	0.0024(13)
O13a/13b ^a	0.025(3)	0.025(3)	0.026(3)	0.013(2)	0.020(2)	0.008(2)
O14a	0.035(2)	0.0115(18)	0.0145(19)	0.0155(14)	0.0122(17)	0.0114(12)
O14b	0.37(2)	0.53(5)	0.35(3)	0.16(2)	0.257(15)	-0.15(2)

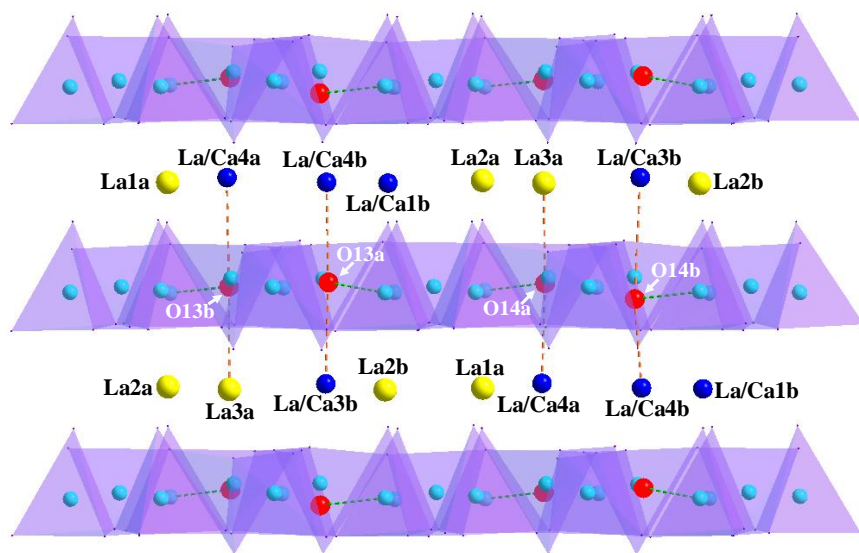
^a ADPs for La/Ca on all sites and for O3a/O3b, O4a/O4b, O13a and O13b were constrained to be the same value.

Table S5.5 Selected inter-atomic distances and BVS calculations for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ at room temperature from the average model in *PI*.

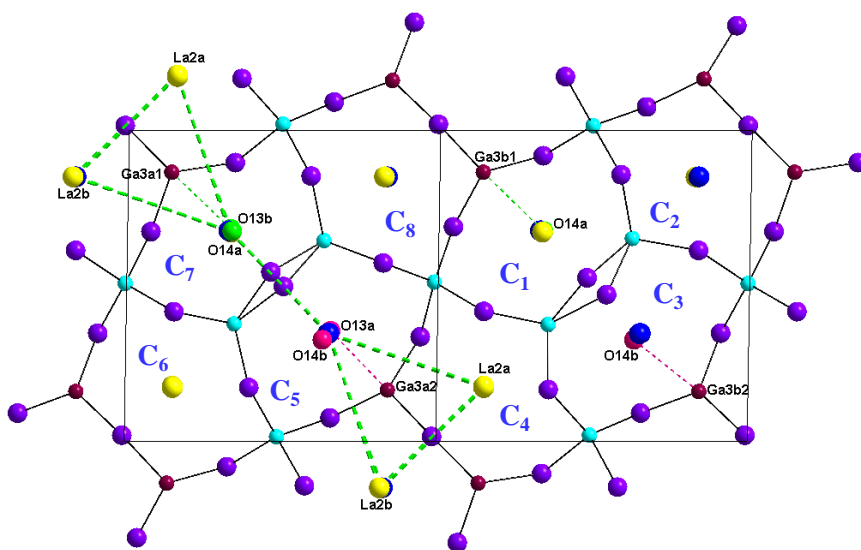
Bond			Length (Å)	Bond			Length (Å)
La1a	-O1	(x1)	2.482(4)	Ga1a	-O12a	(x1)	1.810(6)
	-O10d	(x1)	2.505(2)		-O10a	(x1)	1.812(6)
	-O10a	(x1)	2.527(5)		-O11c	(x1)	1.815(5)
	-O5a	(x1)	2.536(4)		-O9c	(x1)	1.871(4)
	-O11d	(x1)	2.570(5)	BVS for Ga1a			3.08

	-O7a	(x1)	2.581(3)				
	-O7b	(x1)	2.608(4)	Ga1b	-O10b	(x1)	1.811(7)
BVS for La1a			2.58		-O11d	(x1)	1.822(7)
					-O12b	(x1)	1.827(4)
La/Ca1b	-O1	(x1)	2.483(5)		-O9d	(x1)	1.849(5)
	-O10c	(x1)	2.509(5)	BVS for Ga1b			3.08
	-O5b	(x1)	2.536(4)				
	-O7a	(x1)	2.587(4)	Ga1c	-O12c	(x1)	1.814(5)
	-O7b	(x1)	2.608(3)		-O9a	(x1)	1.816(7)
	-O10b	(x1)	2.675(5)		-O11a	(x1)	1.841(7)
	-O11c	(x1)	2.704(4)		-O10c	(x1)	1.875(4)
	-O11b	(x1)	2.832(4)	BVS for Ga1c			3.01
BVS for La/Ca1b			2.50/1.44				
				Ga1d	-O9b	(x1)	1.812(7)
					-O10d	(x1)	1.814(5)
La2a	-O2	(x1)	2.415(4)		-O12d	(x1)	1.826(6)
	-O6a	(x1)	2.450(5)		-O11b	(x1)	1.849(4)
	-O9a	(x1)	2.464(6)	BVS for Ga1d			3.09
	-O9d	(x1)	2.498(3)				
	-O8a	(x1)	2.618(4)	Ga2a	-O4a	(x1)	1.778(10)
	-O8b	(x1)	2.638(5)		-O10d	(x1)	1.803(5)
	-O12d	(x1)	2.766(5)		-O6a	(x1)	1.805(4)
	-O12a	(x1)	2.924(4)		-O4b	(x1)	1.824(5)
BVS for La2a			2.77		-O10a	(x1)	1.886(3)
				BVS for Ga2a			3.10
La2b	-O9c	(x1)	2.417(5)				
	-O6b	(x1)	2.468(4)	Ga2b	-O4a	(x1)	1.772(7)
	-O9b	(x1)	2.510(6)		-O4b	(x1)	1.788(5)
	-O2	(x1)	2.561(4)		-O6b	(x1)	1.805(4)
	-O8b	(x1)	2.588(3)		-O10b	(x1)	1.884(5)
	-O8a	(x1)	2.652(5)		-O10c	(x1)	1.907(5)
	-O12b	(x1)	2.706(4)	BVS for Ga2b			2.96
	-O12c	(x1)	2.758(4)				
BVS for La2b			2.76	Ga2c	-O3b	(x1)	1.781(7)
					-O9a	(x1)	1.794(3)
La/Ca3a	-O3b	(x1)	2.260(8)		-O5a	(x1)	1.803(3)
	-O11a	(x1)	2.433(6)		-O3a	(x1)	1.855(5)
	-O7a	(x1)	2.444(4)		-O9d	(x1)	1.902(5)
	-O14a	(x1)	2.552(6)	BVS for Ga2c			3.06
	-O6b	(x1)	2.559(5)				
	-O11b	(x1)	2.563(6)	Ga2d	-O3b	(x1)	1.758(6)
	-O13b	(x1)	2.621(9)		-O3a	(x1)	1.761(3)
	-O6a	(x1)	2.640(3)		-O5b	(x1)	1.811(4)

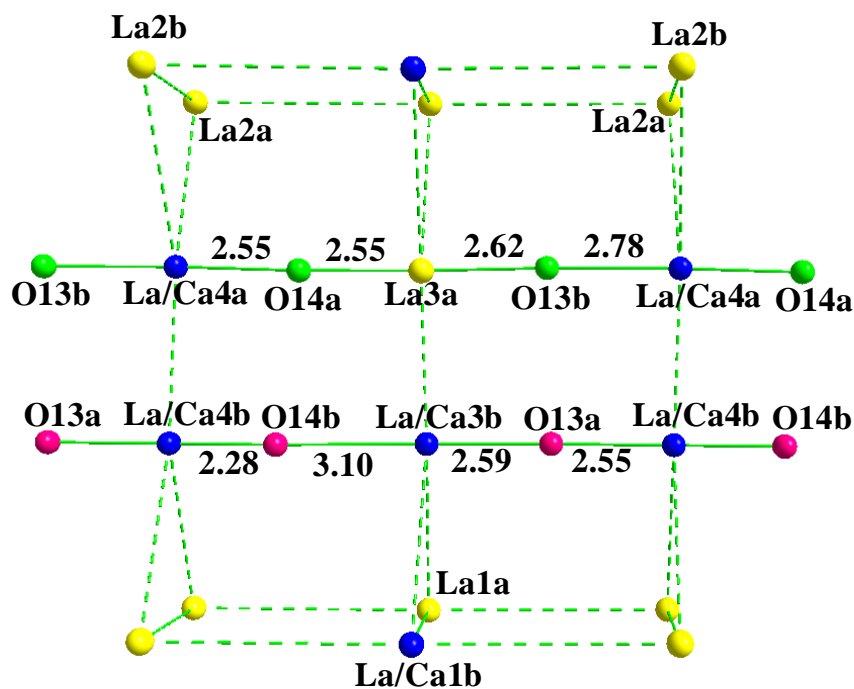
	-O3a	(x1)	2.826(6)		-O9b	(x1)	1.880(5)
	-O9c	(x1)	2.903(5)		-O9c	(x1)	1.906(5)
	-O9d	(x1)	2.960(5)	BVS for Ga2d			3.01
BVS for La/Ca3a			2.88/1.66				
				Ga3a1	-O8a	(x1)	1.803(4)
La/Ca3b	-O3a	(x1)	2.205(4)		-O11a	(x1)	1.841(6)
	-O7b	(x1)	2.492(5)		-O1	(x1)	1.864(4)
	-O6a	(x1)	2.521(5)		-O11b	(x1)	1.870(5)
	-O11c	(x1)	2.570(3)		-O13b	(x1)	2.107(9)
	-O13a	(x1)	2.587(8)	BVS for Ga3a1			3.30
	-O3b	(x1)	2.593(5)				
	-O6b	(x1)	2.613(4)	Ga3a2	-O8b	(x1)	1.802(4)
	-O11d	(x1)	2.748(5)		-O1	(x1)	1.820(5)
BVS for La/Ca3b			2.44/1.40		-O11d	(x1)	1.868(3)
					-O11c	(x1)	1.888(4)
La/Ca4a	-O4b	(x1)	2.319(6)		-O13a	(x1)	2.127(9)
	-O12a	(x1)	2.403(5)	BVS for Ga3a2			3.29
	-O8a	(x1)	2.516(3)				
	-O14a	(x1)	2.551(5)	Ga3b1	-O7a	(x1)	1.805(4)
	-O5a	(x1)	2.579(3)		-O12a	(x1)	1.853(5)
	-O5b	(x1)	2.609(4)		-O12b	(x1)	1.855(5)
	-O12b	(x1)	2.657(6)		-O2	(x1)	1.862(3)
	-O4a	(x1)	2.675(9)		-O14a	(x1)	2.177(6)
	-O13b	(x1)	2.777(8)	BVS for Ga3b1			3.28
	-O10d	(x1)	3.032(4)				
	-O10c	(x1)	3.059(4)	Ga3b2	-O7b	(x1)	1.809(4)
BVS for La/Ca4a			2.85/1.64		-O2	(x1)	1.823(4)
					-O12d	(x1)	1.866(3)
La/Ca4b	-O14b	(x1)	2.276(11)		-O12c	(x1)	1.878(5)
	-O4a	(x1)	2.352(7)		-O14b	(x1)	2.143(13)
	-O8b	(x1)	2.476(4)	BVS for Ga3b2			3.28
	-O12c	(x1)	2.519(2)				
	-O12d	(x1)	2.551(5)	O3a	-O3b	(x1)	0.670(7)
	-O13a	(x1)	2.554(8)	O4a	-O4b	(x1)	0.495(9)
	-O5a	(x1)	2.581(4)				
	-O5b	(x1)	2.608(4)	O13a	-O4a	(x1)	1.894(12)
	-O4b	(x1)	2.720(4)	O13b	-O4b	(x1)	1.827(6)
	-O10b	(x1)	2.746(4)	O14a	-O3b	(x1)	1.922(7)
	-O10a	(x1)	2.951(5)	O14b	-O3a	(x1)	1.895(13)
BVS for La/Ca4b			2.78/1.60				



(a)

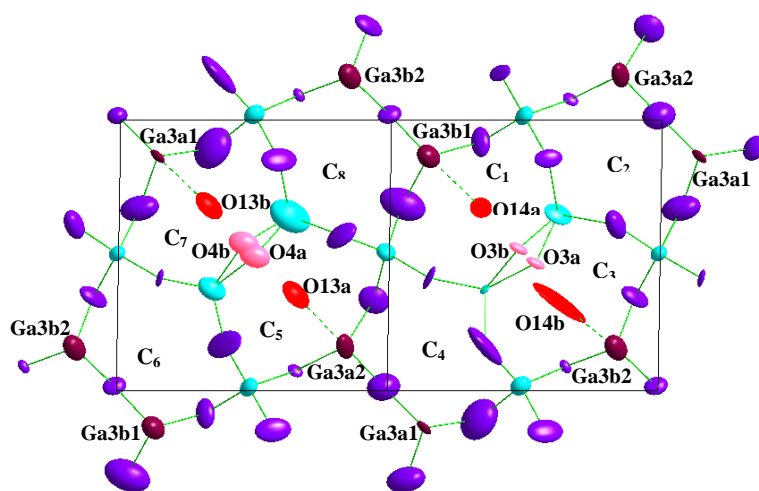


(b)

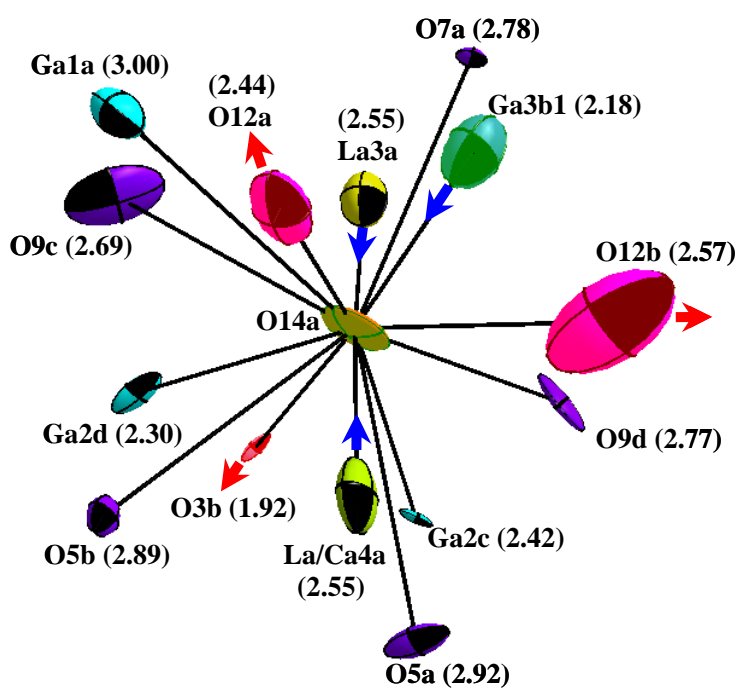


(c)

Figure S5.7 (a) Parallel polyhedral view and (b) projection view along the [110] direction of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ (*PI*, average model) to show the A site cation location and ordering. The A site cations fill the Ga_3O_7 interlayer space and sandwich the interstitial sites in the 5-rings. (c) Parallel view of the highlighted part in (b) to show ordered cations and their distances to interstitial oxide, where the Ga and framework oxygens were omitted for clarity. Paired interstitials O13a/O14b and O13b/O14a are shown as red and green spheres in (b) and (c), respectively. La-sites, yellow; La/Ca-sites, blue; $\text{La/Ca1b} = 0.814(1)/0.186(1)$, $\text{La/Ca3b} = 0.312(1)/0.688(1)$, $\text{La/Ca4a} = 0.623(1)/0.377(1)$, $\text{La/Ca4b} = 0.811(1)/0.189(1)$.



(a)



(b)

Figure S5.8 Projection view of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in PI along $[110]$ direction to show (a) the location of interstitial oxides and atomic displacement parameters (ADPs, 80% probability shown) within the rings and (b) the environment of O14a within 3\AA in the average structure. The numbers denote the distances from each atom to O14a. Local atomic displacements of La3a, La/Ca4a, O3b, O12a, and O12b towards La3a_L, La/Ca4a_L, O3a, O12a_L, and O12b_L due to the O14a incorporation are marked by arrows.

6. Simulated annealing (SA) approach

To validate the structure model (*PI*) from the least-squares Rietveld refinement, simulated annealing (SA) analysis was performed. Peak shape and background parameters were obtained by Le Bail refinement of the NPD data from the 90° and backscattering banks of detectors of the HRPD instrument using TOPAS³, with a single main melilite phase. The standard simulated annealing macro implemented within TOPAS was run using a fixed framework model from the GSAS Rietveld refinement, with eight possible interstitial oxygen sites specified. The occupancies of these sites were allowed to vary during the minimization, along with the La and Ca occupancies of the split A sites. Penalty functions were specified to bias the total interstitial oxygen and La/Ca occupancies towards previously obtained values constrained by the chemical composition. The SA result ($R_{wp} = 6.78\%$, $R_p = 7.72\%$, $\chi^2 = 4.32$, Figure S5.2) is in good agreement with refined structure (Figure S5.1 and Table S5.2) and confirmed the reliability of the proposed structural model regarding the interstitial occupancies and A site cation ordering.

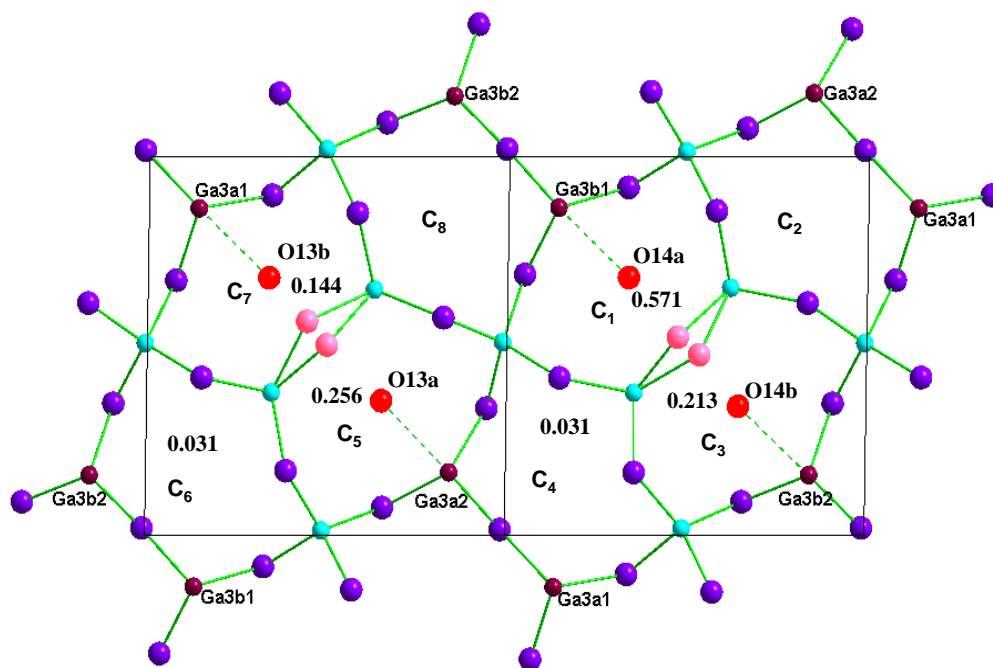


Figure S6.1 Interstitial oxide location and population from the simulated annealing analysis with TOPAS

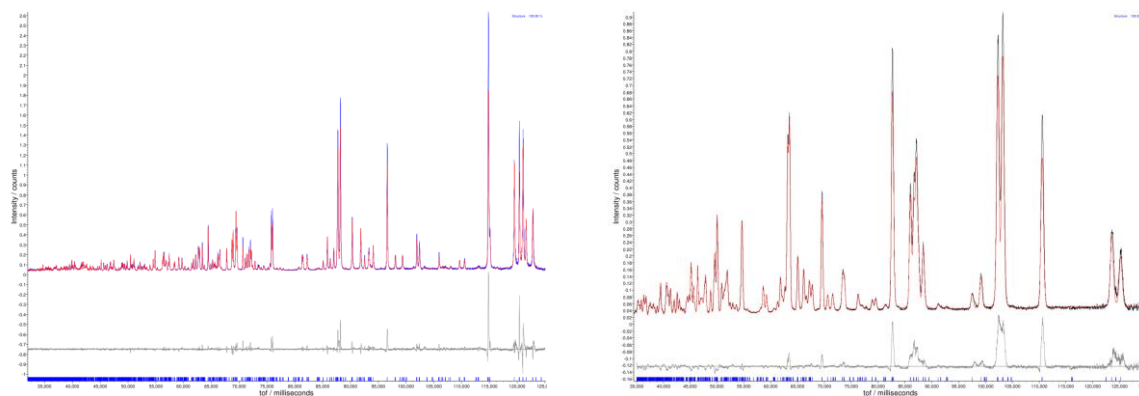


Figure S6.2 SA plots for neutron data from backscattering (left) and 90° bank (right), respectively.

Table S6.1 A-site La/Ca cation ordering extracted from the crystal structure from different approaches (1% error of occupancy), a) GSAS Rietveld refinement (La/Ca = 6.56/1.44); b) TOPAS simulated annealing (La/Ca = 6.61/1.39).

	La/Ca1a	La/Ca1b	La/Ca2a	La/Ca2b	La/Ca3a	La/Ca3b	La/Ca4a	La/Ca4b
a	1.00/000	0.81/0.19	1.00/0.00	1.00/0.00	1.00/0.00	0.31/0.69	0.62/0.38	0.81/0.19
b	0.99/0.01	0.91/0.09	1.00/0.00	0.94/0.06	1.00/0.00	0.35/0.65	0.60/0.40	0.82/0.18

7. Structure refinement for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in split model (triclinic $P1$)

In this split-site model, the relaxations around interstitials were modelled by introducing atomic displacements as shown in Table S7.1-3. Ga3a1, O11a, O11b, and La3a were displaced to Ga3a1_L, O11a_L, O11b_L, and La3a_S around O13b, including O4a in the local defect structure. Similarly, Ga3a2_L, O11c_L, O11d_L, La/Ca3b_L, La/Ca4b_L, and O4b are involved in the local defect structure around O13a, Ga3b1_L, O12a_L, O12b_L, La/Ca3a_L, La/Ca4a_L, and O3a around O14a, Ga3b2_L, O12c_L, O12d_L, La/Ca4b_S, and O3b around O14b, respectively. This models the cases where an interstitial defect is present and where it is absent.

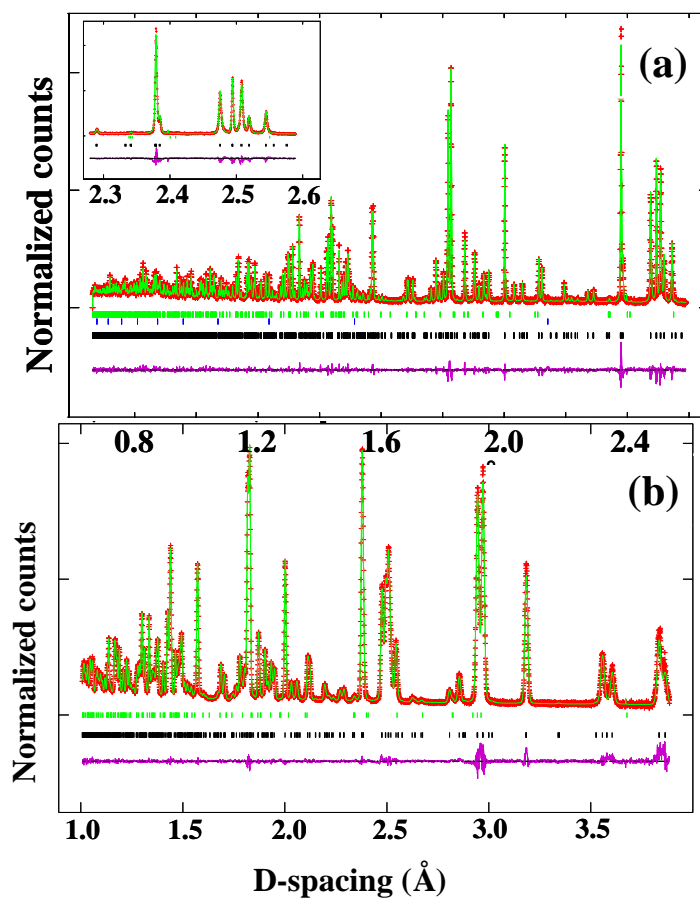


Figure S7.1 Rietveld refinement of RT HRPD ND data for the split-site model for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ in PI from (a) backscattering bank and (b) 90 degree bank. Three rows of vertical tick mark the reflections from $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$, the vanadium container, and Ga_2O_3 from bottom to top, respectively.

Table S7.1 Refined structural parameters for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ at room temperature for the split-site model in the triclinic cell (PI)

Atom	x	y	z	$U_{\text{iso}} (\text{\AA}^2)$	Occupancy
La1a	0.2389(3)	0.0887(2)	0.8285(3)	-	1
La/Ca1b	0.2381(2)	0.4102(3)	0.1501(2)	-	0.825(1)/0.175(1) ^a
La2a	0.7381(4)	0.5852(3)	0.8259(4)	-	1
La2b	0.7343(2)	0.9124(3)	0.1514(2)	-	1
La3a	0.5747(11)	0.2569(8)	0.3257(10)	0.0411(6)	0.241(1) ^b
La3a _L	0.5747(5)	0.2394(5)	0.3306(5)	0.0411(6)	0.582(1) ^{b,3}
La3a _S	0.5896(13)	0.2644(14)	0.3227(14)	0.0411(6)	0.177(1) ^{b,2}
La/Ca3b	0.9059(4)	0.2661(4)	0.6588(4)	0.0027(5)	0.227(1)/0.501(1) ^b
La3/Ca _{bL}	0.9158(10)	0.2669(10)	0.6426(10)	0.0027(5)	0.085(1)/0.187(1) ^{b,1}

La/Ca4a	0.0758(7)	0.7556(7)	0.3202(7)	0.0118(5)	0.260(1)/0.157(1) ^b
La/Ca4a _L	0.0886(4)	0.7659(5)	0.3173(5)	0.0118(5)	0.363(1)/0.220(1) ^{b,3}
La/Ca4b	0.4020(1)	0.7539(1)	0.6549(1)	0.0127(5)	0.375(1)/0.100(1) ^b
La/Ca4b _L	0.3808(9)	0.7289(10)	0.649(1)	0.0127(5)	0.220(1)/0.051(1) ^{b,1}
La/Ca4b _S	0.4121(1)	0.7643(1)	0.6548(1)	0.0127(5)	0.199(1)/0.046(1) ^{b,4}
Ga1a	0.2302(4)	0.7429(3)	0.9842(3)	-	1
Ga1b	0.2353(4)	0.2495(5)	0.4926(4)	-	1
Ga1c	0.7337(4)	0.2434(3)	0.9842(4)	-	1
Ga1d	0.7373(4)	0.7481(4)	0.4931(4)	-	1
Ga2a	0.0023(3)	0.6538(3)	0.6262(3)	-	1
Ga2b	0.0053(3)	0.3810(3)	0.3494(3)	-	1
Ga2c	0.5013(2)	0.1549(2)	0.6210(2)	-	1
Ga2d	0.5006(2)	0.8853(3)	0.3501(3)	-	1
Ga3a1	0.6144(2)	0.4834(3)	0.1359(3)	0.0028(4)	0.823(1) ^b
Ga3a1 _L	0.6366(4)	0.4876(3)	0.1548(3)	0.0028(4)	0.177(1) ^{b,2}
Ga3a2	0.3251(3)	0.4794(3)	0.8403(3)	0.0135(5)	0.729(1) ^b
Ga3a2 _L	0.3073(4)	0.4826(4)	0.8215(5)	0.0135(5)	0.271(1) ^{b,1}
Ga3b1	0.1140(4)	0.9782(3)	0.1257(4)	0.0105(4)	0.418(1) ^b
Ga3b1 _L	0.1314(3)	0.9838(3)	0.1438(2)	0.0105(4)	0.582(1) ^{b,3}
Ga3b2	0.8262(3)	0.9852(3)	0.8482(3)	0.0238(5)	0.755(1) ^b
Ga3b2 _L	0.8116(4)	0.9844(4)	0.8281(4)	0.0238(5)	0.245(1) ^{b,4}
O1	0.3945(3)	0.4098(4)	0.9902(3)	-	1
O2	0.8923(3)	0.8988(3)	0.9824(3)	-	1
O3a	0.6158(4)	0.0934(4)	0.5246(4)	-	0.645(6) ^c
O3b	0.5634(6)	0.1024(6)	0.4654(6)	-	0.355(6) ^c
O4a	0.0860(12)	0.5971(12)	0.4910(12)	-	0.157(7) ^c
O4b	0.0396(4)	0.5909(4)	0.4463(4)	-	0.843(7) ^c
O5a	0.3384(3)	0.9802(3)	0.6286(3)	-	1
O5b	0.3343(3)	0.7086(3)	0.3516(3)	-	1
O6a	0.8374(3)	0.4824(3)	0.6339(3)	-	1
O6b	0.8429(3)	0.2076(3)	0.3571(3)	-	1
O7a	0.2889(3)	0.1587(2)	0.1307(2)	-	1
O7b	0.0052(3)	0.1542(3)	0.8507(3)	-	1
O8a	0.7797(3)	0.6522(3)	0.1232(3)	-	1
O8b	0.5078(3)	0.6625(3)	0.8650(3)	-	1
O9a	0.6688(4)	0.3144(5)	0.8340(4)	-	1
O9b	0.7051(5)	0.8742(5)	0.3911(5)	-	1
O9c	0.4649(4)	0.8869(4)	0.1437(4)	-	1
O9d	0.4659(3)	0.3170(4)	0.5778(4)	-	1
O10a	0.2092(4)	0.8201(3)	0.8299(3)	-	1
O10b	0.2237(4)	0.4015(4)	0.4210(4)	-	1
O10c	0.9655(4)	0.3805(5)	0.1486(4)	-	1
O10d	0.9667(3)	0.8159(3)	0.5881(4)	-	1

O11a	0.6190(4)	0.2813(3)	0.0961(5)	0.0453(13)	0.823(1) ^b
O11a _L	0.5777(6)	0.2560(5)	0.0496(9)	0.0453(13)	0.177(1) ^{b,2}
O11b	0.5872(3)	0.5166(5)	0.3255(3)	0.0155(9)	0.823(1) ^b
O11b _L	0.5580(5)	0.5326(13)	0.3135(4)	0.0155(9)	0.177(1) ^{b,2}
O11c	0.1701(4)	0.5185(4)	0.9060(4)	0.0087(7)	0.729(1) ^b
O11c _L	0.2004(5)	0.5327(6)	0.9464(6)	0.0087(7)	0.271(1) ^{b,1}
O11d	0.1791(5)	0.2578(4)	0.6579(4)	0.0136(8)	0.729(1) ^b
O11d _L	0.1995(12)	0.2440(8)	0.6682(8)	0.0136(8)	0.271(1) ^b
O12a	0.1210(6)	0.7819(4)	0.1003(7)	0.0243(12)	0.418(1) ^{b,1}
O12a _L	0.0653(4)	0.7473(4)	0.0355(5)	0.0243(12)	0.582(1) ^{b,3}
O12b	0.1112(6)	0.0199(8)	0.3305(4)	0.0148(10)	0.418(1) ^b
O12b _L	0.0678(4)	0.0352(5)	0.3128(4)	0.0148(10)	0.582(1) ^{b,3}
O12c	0.6620(3)	0.0147(3)	0.8920(4)	0.0037(7)	0.755(1) ^b
O12c _L	0.6854(5)	0.0286(6)	0.9398(5)	0.0037(7)	0.245(1) ^{b,4}
O12d	0.6683(4)	0.7692(4)	0.6517(4)	0.0095(9)	0.755(1) ^b
O12d _L	0.7090(7)	0.7465(4)	0.6809(5)	0.0095(9)	0.245(1) ^{b,4}
O13a	0.1511(7)	0.4990(7)	0.6405(7)	-	0.271(1) ^{d,1}
O13b	0.8136(4)	0.5007(6)	0.3454(6)	-	0.177(1) ^{d,2}
O14a	0.3330(4)	1.0134(4)	0.3316(4)	-	0.582(1) ^{d,3}
O14b	0.6262(6)	0.9658(5)	0.6346(4)	-	0.245(1) ^{d,4}

$R_{wp}/R_p\%$ (ND168) = 6.32/5.99, $R_{wp}/R_p\%$ (ND90) = 2.83/3.41, $R_{wp}/R_p\%$ (Total) = 3.30/4.72, $\chi^2 = 4.81$.

^a Occupancies of mixed La/Ca sited were constrained to be unity, the ADPs were refined to have the same values.

^b ADPs for related bulk- and defect- structure atoms were constrained to be the same, and the total occupancy was constrained to be unity, e.g. $\text{Occ.}(\text{La}3a) + \text{Occ.}(\text{La}3a_L) + \text{Occ.}(\text{La}3a_S) = 1$.

^c Occupancies of O3a/O3b, and O4a/O4b pairs were constrained to be unity, and the ADPs were refined to have the same values, respectively.

^d The interstitial oxide content was fixed according to the charge-balanced nominal composition of 1.28 in the unit cell.

^{1,2,3,4} Occupancies were constrained to have the same values as the defect interstitials with which they are associated.

Atom	$U_{11} (\text{\AA}^2)$	$U_{22} (\text{\AA}^2)$	$U_{33} (\text{\AA}^2)$	$U_{12} (\text{\AA}^2)$	$U_{13} (\text{\AA}^2)$	$U_{23} (\text{\AA}^2)$
La1a	0.0094(6)	0.0083(6)	0.0101(7)	0.0085(5)	0.0033(5)	0.0025(6)
La/Ca1b ^a	0.0067(7)	0.0073(7)	0.0058(7)	0.0047(6)	0.0018(6)	0.0042(6)
La2a	0.0406(9)	0.0485(12)	0.0465(12)	0.0287(8)	0.0213(7)	0.0109(10)
La2b	0.0160(7)	0.0254(8)	0.0195(9)	0.0126(6)	0.0110(6)	0.0089(7)

Ga1a	0.0119(8)	0.0112(8)	0.0153(8)	0.0039(6)	0.0056(7)	0.0083(7)
Ga1b	0.0163(7)	0.0139(8)	0.0127(8)	0.0068(5)	0.0108(6)	0.0050(8)
Ga1c	0.0116(7)	0.0141(8)	0.0189(9)	0.0102(5)	0.0042(7)	0.0094(8)
Ga1d	0.0069(7)	0.0044(7)	0.0060(5)	0.0042(5)	0.0011(6)	0.0033(7)
Ga2a	0.0156(8)	0.0256(10)	0.0256(10)	0.0112(7)	0.0128(6)	0.0052(10)
Ga2b	0.0298(10)	0.0392(12)	0.0350(11)	0.0193(9)	0.0201(7)	0.0099(11)
Ga2c	0.0013(6)	0.0015(6)	0.0021(7)	0.0010(5)	0.0005(5)	0.0009(7)
Ga2d	0.0116(8)	0.0232(10)	0.0174(9)	0.0071(8)	0.0129(6)	0.0064(9)
O1	0.0289(11)	0.0313(12)	0.0290(12)	0.0146(8)	0.0161(9)	0.0121(10)
O2	0.0096(9)	0.0134(9)	0.0095(9)	0.0030(7)	0.0079(7)	0.0069(8)
O3a/3b ^a	0.0061(11)	0.0037(13)	0.0031(12)	-0.001(1)	0.0031(8)	-0.001(1)
O4a/4b ^a	0.0423(16)	0.0468(19)	0.0397(18)	0.0109(16)	0.0217(12)	0.0163(13)
O5a	0.0132(12)	0.0144(13)	0.0150(13)	0.0038(10)	0.0051(9)	-0.001(1)
O5b	0.0224(13)	0.0228(14)	0.0263(14)	0.0102(11)	0.0135(9)	0.0135(12)
O6a	0.0042(10)	0.0062(11)	0.0078(11)	0.0021(8)	0.0034(8)	-0.001(1)
O6b	0.0161(12)	0.0169(12)	0.0196(12)	0.0065(10)	0.0078(9)	0.0179(10)
O7a	0.0022(9)	0.0018(9)	0.0021(10)	0.0015(7)	0.0009(8)	0.0016(8)
O7b	0.0239(13)	0.0170(11)	0.0243(12)	0.009(1)	0.0096(11)	0.0195(8)
O8a	0.0151(12)	0.0168(14)	0.0243(14)	0.0041(10)	0.0091(11)	0.0065(10)
O8b	0.0186(11)	0.0212(11)	0.0338(14)	0.0175(9)	0.0108(11)	0.0185(10)
O9a	0.0463(15)	0.0380(17)	0.0393(19)	0.0303(11)	0.0209(14)	-0.007(2)
O9b	0.0693(18)	0.071(2)	0.089(3)	0.0565(13)	0.0456(19)	0.016(2)
O9c	0.0079(11)	0.0316(16)	0.0228(15)	0.0096(11)	0.0085(11)	0.0081(14)
O9d	0.0031(11)	0.0130(12)	0.0152(12)	-0.001(1)	-0.001(1)	0.0123(11)
O10a	0.0306(15)	0.0181(13)	0.0222(15)	0.0135(11)	0.0009(14)	0.0161(11)
O10b	0.0154(13)	0.0138(12)	0.0113(12)	0.0053(10)	0.0013(11)	0.0113(10)
O10c	0.0215(13)	0.051(2)	0.0231(16)	0.0127(14)	0.0161(11)	0.0046(17)
O10d	0.0115(11)	0.0142(12)	0.0246(16)	0.0121(8)	0.0014(12)	0.0071(13)
O13a/13b ^a	0.009(3)	0.006(4)	0.023(4)	-0.002(2)	0.008(3)	-0.009(3)
O14a	0.0088(18)	0.0042(18)	0.0030(18)	0.0011(14)	0.0030(15)	0.0027(12)
O14b	0.34(4)	0.21(3)	0.37(4)	0.04(2)	0.11(2)	-0.21(2)

^a ADPs for La/Ca on all sites and for O3a/O3b, O4a/O4b, O13a and O13b were constrained to be the same value.

Table S7.2 Selected inter-atomic distances and BVS calculations for $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$ at room temperature from the split-site model in *PI*.

Bulk Structure				Defect Structure			
Bond		Length (Å)		Bond		Length (Å)	
La1a	-O10a	(x1) 2.476(4)		La1a	-O11d _L	(x1) 2.471(9)	
	-O1	(x1) 2.495(4)			-O11a _L	(x1) 2.679(5)	

	-O10d	(x1)	2.503(3)				
	-O5a	(x1)	2.534(4)				
	-O7b	(x1)	2.605(4)				
	-O7a	(x1)	2.608(3)				
	-O11d	(x1)	2.701(5)				
	-O11a	(x1)	3.051(4)				
	BVS for La1a		2.59				
La1b	-O1	(x1)	2.452(5)	La1b	-O11b _L	(x1)	2.507(5)
	-O10c	(x1)	2.505(5)		-O11c _L	(x1)	2.554(7)
	-O5b	(x1)	2.518(4)				
	-O7b	(x1)	2.605(3)				
	-O7a	(x1)	2.607(4)				
	-O10b	(x1)	2.662(5)				
	-O11b	(x1)	2.797(4)				
	-O11c	(x1)	2.818(5)				
	BVS for La1b		2.51				
La2a	-O2	(x1)	2.434(4)	La2a	-O12d _L	(x1)	2.393(6)
	-O9a	(x1)	2.438(6)		-O12a _L	(x1)	2.579(4)
	-O6a	(x1)	2.459(5)				
	-O9d	(x1)	2.511(3)				
	-O8a	(x1)	2.589(5)				
	-O8b	(x1)	2.684(5)				
	-O12d	(x1)	2.875(6)				
	-O12a	(x1)	3.084(5)				
	BVS for La2a		2.65				
La2b	-O9c	(x1)	2.467(5)	La2b	-O12c _L	(x1)	2.585(7)
	-O6b	(x1)	2.472(4)		-O12b _L	(x1)	2.615(4)
	-O9b	(x1)	2.505(6)				
	-O8b	(x1)	2.511(3)				
	-O2	(x1)	2.546(4)				
	-O8a	(x1)	2.649(5)				
	-O12c	(x1)	2.911(5)				
	-O12b	(x1)	3.029(6)				
	BVS for La2b		2.58				
La3a	-O3b	(x1)	2.256(12)	La3a	-O13b	(x1)	2.436(10)
	-O7a	(x1)	2.367(9)		-O14a	(x1)	2.578(10)
	-O11a	(x1)	2.421(12)		-O11a _L	(x1)	2.649(14)
	-O11b	(x1)	2.441(10)		-O11b _L	(x1)	2.740(16)
	-O6a	(x1)	2.655(7)				

	-O6b	(x1)	2.733(12)	La3a _L	-O7a	(x1)	2.437(5)
	-O3a	(x1)	2.823(11)		-O14a	(x1)	2.463(6)
	-O9d	(x1)	2.912(12)		-O6b	(x1)	2.647(6)
	-O9c	(x1)	3.002(8)		-O3a	(x1)	2.653(7)
BVS for La3a			2.71		-O6a	(x1)	2.654(4)
					-O11a _L	(x1)	2.747(10)
					-O9c	(x1)	2.864(6)
					-O9d	(x1)	2.893(7)
					-O11b _L	(x1)	2.922(14)
				BVS for La3a _L			2.31/1.33
				La3a _S	-O13b	(x1)	2.306(13)
					-O3b	(x1)	2.336(16)
					-O7a	(x1)	2.447(11)
					-O11a _L	(x1)	2.556(17)
					-O6a	(x1)	2.628(9)
					-O6b	(x1)	2.634(15)
					-O14a	(x1)	2.712(13)
					-O11b _L	(x1)	2.725(20)
					-O3a	(x1)	2.886(16)
					-O9c	(x1)	3.021(13)
					-O9d	(x1)	3.030(15)
				BVS for La3a _S			2.85/1.64
La/Ca3b	-O3a	(x1)	2.232(4)	La/Ca3b	-O13a	(x1)	2.611(8)
	-O11c	(x1)	2.434(3)		-O11c _L	(x1)	2.721(4)
	-O6a	(x1)	2.458(5)		-O11d _L	(x1)	2.877(13)
	-O7b	(x1)	2.507(5)		-O14b	(x1)	2.929(6)
	-O6b	(x1)	2.593(5)				
	-O11d	(x1)	2.650(7)				
	-O3b	(x1)	2.659(6)	La/Ca3b _L	-O3a	(x1)	2.317(8)
BVS for La/Ca3b			2.60/1.50		-O6b	(x1)	2.423(10)
					-O13a	(x1)	2.464(11)
					-O6a	(x1)	2.473(12)
					-O7b	(x1)	2.603(11)
					-O3b	(x1)	2.718(9)
					-O11d _L	(x1)	2.752(16)
					-O11c _L	(x1)	2.758(7)
				BVS for La/Ca3b _L			2.65/1.52
La/Ca4a	-O4b	(x1)	2.233(9)	La/Ca4a	-O14a	(x1)	2.645(7)
	-O12a	(x1)	2.338(10)		-O12a _L	(x1)	2.672(9)
	-O12b	(x1)	2.383(11)		-O12b _L	(x1)	2.728(9)

	-O8a	(x1)	2.432(6)		-O13b	(x1)	2.854(8)
	-O4a	(x1)	2.536(15)				
	-O5b	(x1)	2.630(8)	La/Ca4a _L	-O4b	(x1)	2.341(7)
	-O5a	(x1)	2.655(5)		-O8a	(x1)	2.493(4)
	-O10c	(x1)	3.032(8)		-O14a	(x1)	2.510(5)
	-O10d	(x1)	3.049(9)		-O5b	(x1)	2.567(6)
BVS for La/Ca4a			3.23/1.82		-O12a _L	(x1)	2.583(7)
					-O5a	(x1)	2.630(4)
					-O4a	(x1)	2.630(14)
					-O12b _L	(x1)	2.675(7)
					-O10c	(x1)	3.084(6)
				BVS for La/Ca4a _L			2.71/1.55
La/Ca4b	-O12c	(x1)	2.414(2)	La/Ca4b	-O14b	(x1)	2.403(5)
	-O4a	(x1)	2.433(9)		-O13a	(x1)	2.582(6)
	-O12d	(x1)	2.505(4)		-O12c _L	(x1)	2.695(3)
	-O8b	(x1)	2.507(4)		-O12d _L	(x1)	2.903(7)
	-O5a	(x1)	2.530(4)				
	-O5b	(x1)	2.629(3)				
	-O10b	(x1)	2.823(3)	La/Ca4b _L	-O13a	(x1)	2.369(11)
	-O4b	(x1)	2.831(3)		-O8b	(x1)	2.441(11)
	-O10a	(x1)	2.976(4)		-O5a	(x1)	2.644(11)
BVS for La/Ca4b			2.51/1.44		-O10b	(x1)	2.663(8)
					-O5b	(x1)	2.675(11)
					-O4b	(x1)	2.702(8)
					-O12c _L	(x1)	2.852(6)
					-O10a	(x1)	2.916(11)
					-O12d _L	(x1)	2.990(12)
				BVS for La/Ca4b _L			2.48/1.42
				La/Ca4b _S	-O14b	(x1)	2.295(5)
					-O5a	(x1)	2.487(4)
					-O4a	(x1)	2.505(9)
					-O8b	(x1)	2.555(4)
					-O5b	(x1)	2.589(3)
					-O12c _L	(x1)	2.640(3)
					-O12d _L	(x1)	2.853(7)
					-O10b	(x1)	2.885(3)
					-O4b	(x1)	2.895(3)
					-O10a	(x1)	3.034(4)
				BVS for La/Ca4b _S			2.69/1.55
Ga1a	-O12a	(x1)	1.806(8)	Ga1a	-O12a _L	(x1)	1.805(6)

	-O11c	(x1)	1.823(5)		-O11c _L	(x1)	1.822(7)
	-O10a	(x1)	1.824(5)		-O10a	(x1)	1.824(5)
	-O9c	(x1)	1.858(4)		-O9c	(x1)	1.858(4)
BVS for Ga1a			3.08	BVS for Ga1a			3.08
Ga1b	-O10b	(x1)	1.804(7)	Ga1b	-O10b	(x1)	1.804(7)
	-O11d	(x1)	1.814(6)		-O11d _L	(x1)	1.828(10)
	-O9d	(x1)	1.841(5)		-O12b _L	(x1)	1.832(4)
	-O12b	(x1)	1.857(6)		-O9d	(x1)	1.841(5)
BVS for Ga1b			3.07	BVS for Ga1b			3.09
Ga1c	-O9a	(x1)	1.805(6)	Ga1c	-O12c _L	(x1)	1.799(7)
	-O11a	(x1)	1.819(7)		-O9a	(x1)	1.805(6)
	-O12c	(x1)	1.831(4)		-O11a _L	(x1)	1.822(9)
	-O10c	(x1)	1.852(4)		-O10c	(x1)	1.852(4)
BVS for Ga1c			3.08	BVS for Ga1c			3.14
Ga1d	-O9b	(x1)	1.815(7)	Ga1d	-O9b	(x1)	1.815(7)
	-O12d	(x1)	1.826(6)		-O10d	(x1)	1.829(5)
	-O10d	(x1)	1.829(5)		-O11b _L	(x1)	1.856(7)
	-O11b	(x1)	1.876(4)		-O12d _L	(x1)	1.903(7)
BVS for Ga1d			3.01	BVS for Ga1d			2.90
Ga2a	-O4a	(x1)	1.788(13)				
	-O6a	(x1)	1.807(4)				
	-O10d	(x1)	1.824(5)				
	-O4b	(x1)	1.846(5)				
	-O10a	(x1)	1.882(3)				
	-O13b	(x1)	2.284(5)				
BVS for Ga2a			3.00				
Ga2b	-O4a	(x1)	1.779(10)				
	-O4b	(x1)	1.792(5)				
	-O6b	(x1)	1.806(4)				
	-O10c	(x1)	1.836(5)				
	-O10b	(x1)	1.892(5)				
BVS for Ga2b			3.06				
Ga2c	-O3b	(x1)	1.784(7)				
	-O3a	(x1)	1.798(5)				
	-O9a	(x1)	1.808(3)				
	-O5a	(x1)	1.815(4)				
	-O9d	(x1)	1.843(5)				

BVS for Ga2c			3.13				
Ga2d	-O3a	(x1)	1.775(3)				
	-O3b	(x1)	1.779(6)				
	-O5b	(x1)	1.810(4)				
	-O9c	(x1)	1.902(5)				
	-O9b	(x1)	1.926(6)				
BVS for Ga2d			2.90				
Ga3a1	-O1	(x1)	1.814(3)	Ga3a1	-O1	(x1)	1.814(3)
	-O8a	(x1)	1.823(4)		-O8a	(x1)	1.823(4)
	-O11b	(x1)	1.868(4)		-O11a _L	(x1)	1.927(6)
	-O11a	(x1)	1.882(5)		-O11b _L	(x1)	1.927(6)
BVS for Ga3a1			2.93		-O13b	(x1)	2.203(6)
				BVS for Ga3a1			3.03
				Ga3a1 _L	-O8a	(x1)	1.806(4)
					-O11a _L	(x1)	1.899(6)
					-O11b _L	(x1)	1.911(6)
					-O13b	(x1)	1.996(6)
					-O1	(x1)	2.019(4)
				BVS for Ga3a1 _L			3.01
Ga3a2	-O8b	(x1)	1.802(4)	Ga3a2	-O8b	(x1)	1.802(4)
	-O1	(x1)	1.804(5)		-O1	(x1)	1.804(5)
	-O11d	(x1)	1.864(3)		-O11c _L	(x1)	1.913(7)
	-O11c	(x1)	1.904(6)		-O11d _L	(x1)	1.923(6)
BVS for Ga3a2			2.96		-O13a	(x1)	2.221(8)
				BVS for Ga3a2			3.11
				Ga3a2 _L	-O8b	(x1)	1.810(4)
					-O11c _L	(x1)	1.879(8)
					-O11d _L	(x1)	1.917(7)
					-O13a	(x1)	1.997(8)
					-O1	(x1)	2.015(6)
				BVS for Ga3a2 _L			3.03
Ga3b1	-O2	(x1)	1.805(4)	Ga3b1	-O2	(x1)	1.805(4)
	-O7a	(x1)	1.840(4)		-O7a	(x1)	1.840(4)
	-O12a	(x1)	1.855(6)		-O12a _L	(x1)	1.916(5)
	-O12b	(x1)	1.895(6)		-O12b _L	(x1)	1.955(6)
BVS for Ga3b1			2.91		-O14a	(x1)	2.206(5)
				BVS for Ga3b1			2.98

				Ga3b1 _L	-O7a	(x1)	1.822(3)				
					-O12b _L	(x1)	1.903(5)				
					-O12a _L	(x1)	1.922(4)				
					-O2	(x1)	1.967(3)				
					-O14a	(x1)	2.035(4)				
				BVS for Ga3b1 _L			2.97				
Ga3b2	-O2	(x1)	1.805(4)	Ga3b2	-O2	(x1)	1.805(4)				
	-O7b	(x1)	1.815(4)		-O7b	(x1)	1.815(4)				
	-O12c	(x1)	1.849(5)		-O12c _L	(x1)	1.931(7)				
	-O12d	(x1)	1.894(3)		-O12d _L	(x1)	1.941(4)				
BVS for Ga3b2			2.98		-O14b	(x1)	2.221(5)				
				BVS for Ga3b2			3.02				
				Ga3b2 _L	-O7b	(x1)	1.807(4)				
					-O12d _L	(x1)	1.907(5)				
					-O12c _L	(x1)	1.932(7)				
					-O2	(x1)	1.985(5)				
					-O14b	(x1)	2.029(6)				
				BVS for Ga3b2 _L			2.96				
O13a	-O4b	(x1)	2.413(9)	O13b	-O4a	(x1)	2.160(11)				
O14a	-O3a	(x1)	2.395(5)	O14b	-O3b	(x1)	2.436(8)				

Table S7.3 Bond angles in the GaO_n polyhedra of La_{1.64}Ca_{0.36}Ga₃O_{7.32} from the split-model in *PI*.

Bulk structure				Defect structure			
Bond		Angle (°)		Bond		Angle (°)	
G1aO ₄ tetrahedron				G1aO ₄ tetrahedron			
O12a	-Ga1a-	O11c	109.8(3)	O12a _L	-Ga1a-	O11c _L	106.2(3)
O12a	-Ga1a-	O10a	113.4(2)	O12a _L	-Ga1a-	O10a	102.1(2)
O12a	-Ga1a-	O9c	103.5(3)	O12a _L	-Ga1a-	O9c	120.8(3)
O11c	-Ga1a-	O10a	115.6(2)	O11c _L	-Ga1a-	O10a	125.0(3)
O11c	-Ga1a-	O9c	109.2(2)	O11c _L	-Ga1a-	O9c	100.0(2)
O10a	-Ga1a-	O9c	104.4(2)	O10a	-Ga1a-	O9c	104.4(2)
Average			109.3	Average			109.8
Ga1bO ₄ tetrahedron				Ga1bO ₄ tetrahedron			
O10b	-Ga1b-	O11d	113.4(3)	O10b	-Ga1b-	O11d _L	121.5(3)

O10b	-Ga1b-	O9d	104.5(3)	O10b	-Ga1b-	O12b _L	105.3(3)
O10b	-Ga1b-	O12b	116.6(4)	O10b	-Ga1b-	O9d	104.5(3)
O11d	-Ga1b-	O9d	108.2(3)	O11d _L	-Ga1b-	O12b _L	109.0(3)
O11d	-Ga1b-	O12b	108.3(2)	O11d _L	-Ga1b-	O9d	101.3(4)
O9d	-Ga1b-	O12b	105.1(3)	O12b _L	-Ga1b-	O9d	119.3(3)
Average			109.4	Average			109.6

Ga1cO ₄ tetrahedron				Ga1cO ₄ tetrahedron			
O9a	-Ga1c-	O11a	100.0(2)	O12c _L	-Ga1c-	O9a	126.8(3)
O9a	-Ga1c-	O12c	114.4(3)	O12c _L	-Ga1c-	O11a _L	103.2(3)
O9a	-Ga1c-	O10c	116.4(2)	O12c _L	-Ga1c-	O10c	102.4(3)
O11a	-Ga1c-	O12c	110.2(2)	O9a	-Ga1c-	O11a _L	91.3(3)
O11a	-Ga1c-	O10c	103.6(3)	O9a	-Ga1c-	O10c	116.4(2)
O12c	-Ga1c-	O10c	110.9(2)	O11a _L	-Ga1c-	O10c	116.2(3)
Average			109.3	Average			109.4

Ga1dO ₄ tetrahedron				Ga1dO ₄ tetrahedron			
O9b	-Ga1d-	O12d	111.6(3)	O9b	-Ga1d-	O10d	110.0(3)
O9b	-Ga1d-	O10d	110.0(3)	O9b	-Ga1d-	O11b _L	96.5(3)
O9b	-Ga1d-	O11b	105.4(3)	O9b	-Ga1d-	O12d _L	127.5(3)
O12d	-Ga1d-	O10d	109.9(3)	O10d	-Ga1d-	O11b _L	123.9(3)
O12d	-Ga1d-	O11b	106.7(2)	O10d	-Ga1d-	O12d _L	96.2(3)
O10d	-Ga1d-	O11b	113.2(2)	O11b _L	-Ga1d-	O12d _L	105.5(2)
Average			109.5	Average			109.9

Ga2aO ₄ tetrahedron			
O4a	-Ga2a-	O6a	118.5(4)
O4a	-Ga2a-	O10d	103.1(4)
O4a	-Ga2a-	O10a	101.4(3)
O6a	-Ga2a-	O10d	120.2(2)
O6a	-Ga2a-	O4b	116.8(2)
O6a	-Ga2a-	O10a	116.0(2)
O10d	-Ga2a-	O4b	92.8(2)
O10d	-Ga2a-	O10a	93.3(2)
O4b	-Ga2a-	O10a	113.4(2)
Average			108.4

Ga2bO ₄ tetrahedron			
O4a	-Ga2b-	O6b	117.8(4)
O4a	-Ga2b-	O10c	104.5(4)
O4a	-Ga2b-	O10b	96.3(4)
O4b	-Ga2b-	O6b	117.0(2)
O4b	-Ga2b-	O10c	93.3(2)

O4b	-Ga2b-	O10b	109.1(2)
O6b	-Ga2b-	O10c	119.6(2)
O6b	-Ga2b-	O10b	114.4(2)
O10c	-Ga2b-	O10b	100.5(2)
Average			108.1

Ga₂cO₄ tetrahedron

O3b	-Ga2c-	O9a	119.1(2)
O3b	-Ga2c-	O5a	118.7(2)
O3b	-Ga2c-	O9d	94.8(2)
O3a	-Ga2c-	O9a	104.2(2)
O3a	-Ga2c-	O5a	114.1(2)
O3a	-Ga2c-	O9d	112.6(2)
O9a	-Ga2c-	O5a	107.4(2)
O9a	-Ga2c-	O9d	91.9(2)
O5a	-Ga2c-	O9d	122.2(2)
Average			109.5

Ga₂dO₄ tetrahedron

O3a	-Ga2d-	O5b	117.1(2)
O3a	-Ga2d-	O9c	114.4(2)
O3a	-Ga2d-	O9b	94.0(2)
O3b	-Ga2d-	O5b	121.0(3)
O3b	-Ga2d-	O9c	96.9(2)
O3b	-Ga2d-	O9b	109.7(3)
O5b	-Ga2d-	O9c	119.1(2)
O5b	-Ga2d-	O9b	111.9(2)
O9c	-Ga2d-	O9b	94.5(2)
Average			108.7

Ga₃a₁O₄ tetrahedron

O1	-Ga3a1-	O8a	112.5(2)
O1	-Ga3a1-	O11b	97.4(2)
O1	-Ga3a1-	O11a	105.2(2)
O8a	-Ga3a1-	O11b	123.7(2)
O8a	-Ga3a1-	O11a	116.2(2)
O11b	-Ga3a1-	O11a	98.7(2)
Average			109.0

Ga₃a₁O₄ tetrahedron

O1	-Ga3a1-	O8a	112.5(2)
O1	-Ga3a1-	O11a _L	94.0(3)
O1	-Ga3a1-	O11b _L	88.5(2)
O8a	-Ga3a1-	O11a _L	118.4(2)
O8a	-Ga3a1-	O11b _L	122.4(2)
O11a _L	-Ga3a1-	O11b _L	112.4(3)
Average			108.0

Ga₃a₁_LO₄ trigonal bipyramid

Equatorial planar

O8a	-Ga3a1 _L -	O11a _L	120.8(2)
O8a	-Ga3a1 _L -	O11b _L	124.3(3)

O11a _L	-Ga3a1 _L -	O11b _L	114.4(3)
Average			119.8
Apex			
O13b	-Ga3a1 _L -	O1	155.8(2)
Others			
O8a	-Ga3a1 _L -	O13b	99.6(2)
O8a	-Ga3a1 _L -	O1	104.3(2)
O11a _L	-Ga3a1 _L -	O1	88.5(3)
O11b _L	-Ga3a1 _L -	O13b	80.4(2)
O11b _L	-Ga3a1 _L -	O1	83.2(2)
Average			89.7

Ga3a2O ₄ tetrahedron			
O8b	-Ga3a2-	O1	111.3(2)
O8b	-Ga3a2-	O11d	127.3(2)
O8b	-Ga3a2-	O11c	117.6(2)
O1	-Ga3a2-	O11d	95.1(2)
O1	-Ga3a2-	O11c	95.5(2)
O11d	-Ga3a2-	O11c	103.4(2)
Average			108.4

Ga3a2O ₄ tetrahedron			
O8b	-Ga3a2-	O1	111.3(2)
O8b	-Ga3a2-	O11c _L	115.6(2)
O8b	-Ga3a2-	O11d _L	126.4(3)
O1	-Ga3a2-	O11c _L	87.0(2)
O1	-Ga3a2-	O11d _L	88.1(3)
O11c _L	-Ga3a2-	O11d _L	114.8(3)
Average			107.2

Ga3a2_LO₄ trigonal bipyramid

Equatorial planar			
O8b	-Ga3a2 _L -	O11c _L	116.9(3)
O8b	-Ga3a2 _L -	O11d _L	126.3(3)
O11c _L	-Ga3a2 _L -	O11d _L	116.7(4)
Average			120.0
Apex			
O13a	-Ga3a2 _L -	O1	162.5(3)
Others			
O8b	-Ga3a2 _L -	O13a	95.4(3)
O8b	-Ga3a2 _L -	O1	102.0(2)
O11c _L	-Ga3a2 _L -	O13a	88.8(3)
O11c _L	-Ga3a2 _L -	O1	82.1(2)
O11d _L	-Ga3a2 _L -	O13a	88.3(3)
O11d _L	-Ga3a2 _L -	O1	82.5(3)
Average			89.9

Ga3b1O ₄ tetrahedron			
O2	-Ga3b1-	O7a	117.2(2)
O2	-Ga3b1-	O12a	105.2(3)
O2	-Ga3b1-	O12b	102.3(2)
O7a	-Ga3b1-	O12a	119.2(2)

Ga3b1O ₄ tetrahedron			
O2	-Ga3b1-	O7a	117.2(2)
O2	-Ga3b1-	O12a _L	89.9(2)
O2	-Ga3b1-	O12b _L	90.0(2)
O7a	-Ga3b1-	O12a _L	123.1(2)

O7a	-Ga3b1-	O12b	115.8(3)	O7a	-Ga3b1-	O12b _L	116.4(2)
O12a	-Ga3b1-	O12b	93.4(3)	O12a _L	-Ga3b1-	O12b _L	112.2(2)
Average			108.9	Average			108.1

Ga3b1_LO₄ trigonal bipyramid

Equatorial planar

O7a	-Ga3b1 _L -	O12b _L	120.0(2)
O7a	-Ga3b1 _L -	O12a _L	123.8(2)
O12b _L	-Ga3b1 _L -	O12a _L	114.3(2)
Average			119.4

Apex

O2	-Ga3b1 _L -	O14a	160.6(2)
----	-----------------------	------	----------

Others

O7a	-Ga3b1 _L -	O2	110.4(2)
O7a	-Ga3b1 _L -	O14a	88.9(2)
O12b _L	-Ga3b1 _L -	O2	86.8(2)
O12b _L	-Ga3b1 _L -	O14a	82.0(2)
O12a _L	-Ga3b1 _L -	O2	85.1(2)
O12a _L	-Ga3b1 _L -	O14a	85.2(2)
Average			89.7

Ga3b2O₄ tetrahedron

O2	-Ga3b2-	O7b	114.4(2)
O2	-Ga3b2-	O12c	102.8(2)
O2	-Ga3b2-	O12d	95.8(2)
O7b	-Ga3b2-	O12c	122.7(2)
O7b	-Ga3b2-	O12d	119.3(2)
O12c	-Ga3b2-	O12d	97.3(2)
Average			108.7

Ga3b2O₄ tetrahedron

O2	-Ga3b2-	O7b	114.4(2)
O2	-Ga3b2-	O12c _L	93.3(2)
O2	-Ga3b2-	O12d _L	80.8(2)
O7b	-Ga3b2-	O12c _L	122.8(2)
O7b	-Ga3b2-	O12d _L	119.7(2)
O12c _L	-Ga3b2-	O12d _L	113.2(2)
Average			107.4

Ga3b2_LO₄ trigonal bipyramid

Equatorial planar

O7b	-Ga3b2 _L -	O12d _L	121.9(3)
O7b	-Ga3b2 _L -	O12c _L	123.2(3)
O12d _L	-Ga3b2 _L -	O12c _L	114.8(3)
Average			120.0

Apex

O2	-Ga3b2 _L -	O14b	152.8(2)
----	-----------------------	------	----------

Others

O7b	-Ga3b2 _L -	O2	106.6(2)
O7b	-Ga3b2 _L -	O14b	99.8(2)
O12d _L	-Ga3b2 _L -	O2	77.2(2)
O12d _L	-Ga3b2 _L -	O14b	83.5(2)

O12 _{c_L}	-Ga3b2 _L -	O2	87.8(2)
O12 _{c_L}	-Ga3b2 _L -	O14b	83.0(2)
Average			89.7

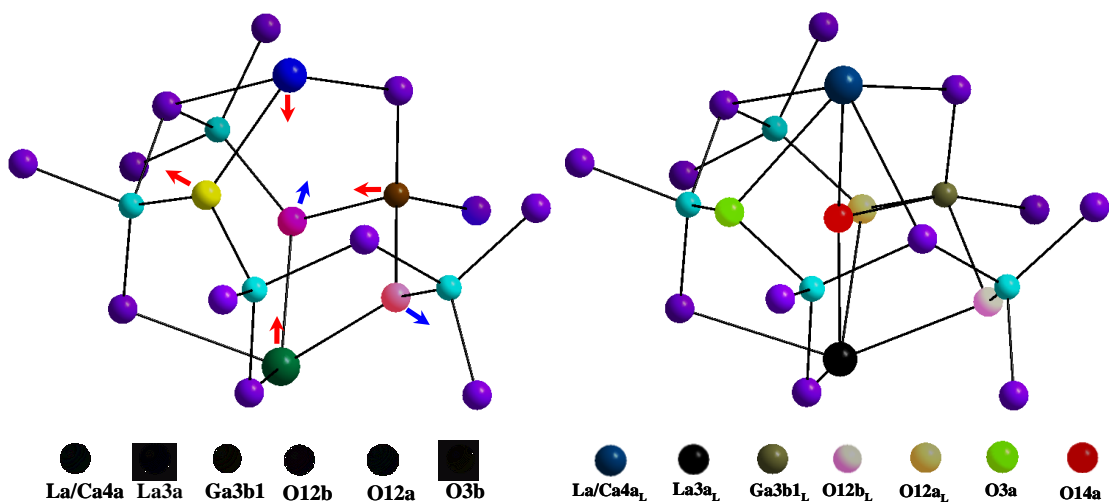


Figure S7.2 Environment of the C_1 ring centroid in (left) bulk and (right) defect structure in $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$. The local displacement of La3a, La/Ca4a, Ga3b1, O12a, and O12b to accommodate the O14a interstitials are marked with arrows in the bulk structure. The displacements (\AA) calculated using the split-model for La3a, La/Ca4a, Ga3b1, O12a, and O12b are 0.19(1) (La3a-La3a_L), 0.14(1) (La/Ca4a-La/Ca4a_L), 0.17(1) (Ga3b1-Ga3b1_L), 0.56(1) (O12a-O12a_L), and 0.49(1) (O12b-O12b_L), respectively.

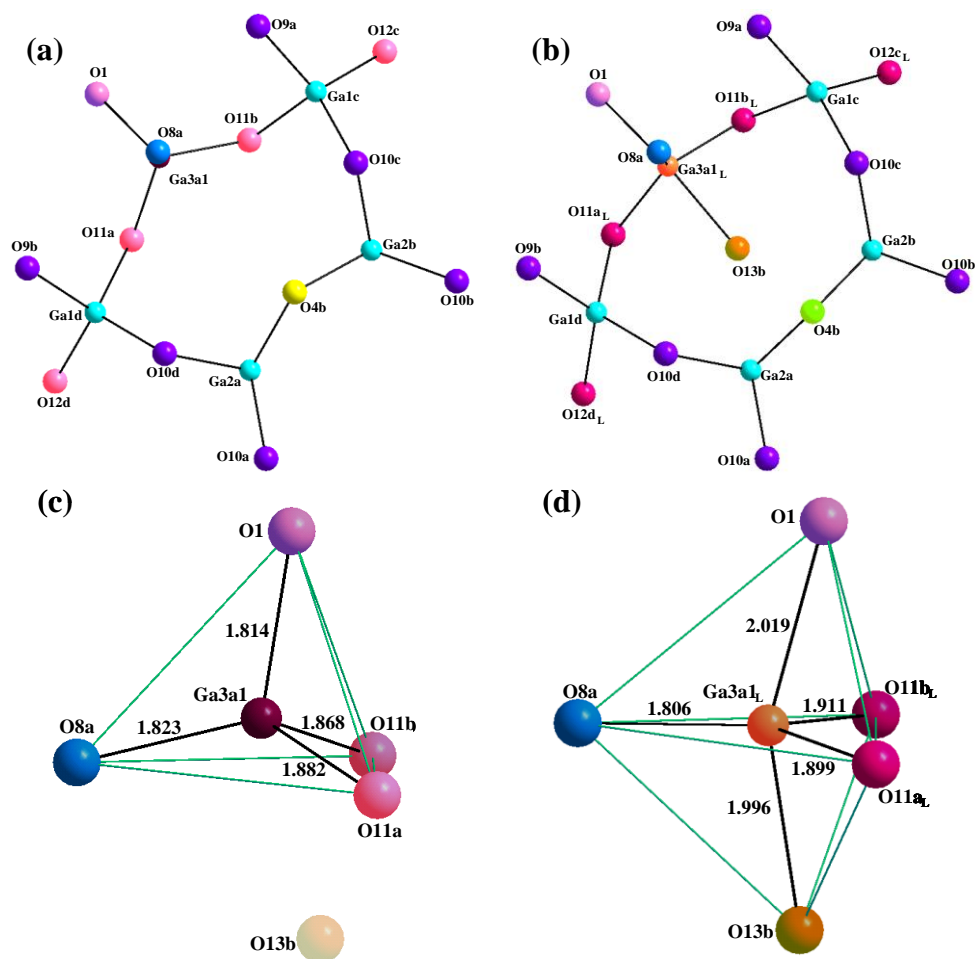


Figure S7.3 Structural relaxation around the interstitial oxide O13b in the split-model of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$. Ga3a1_L, O11a_L, O11b_L, O4b, and La3a_s are involved in the local structural relaxation. (a) and (c) represent the refined structure in the absence of the interstitial O occupancy of this site with (b) and (d) showing the ring geometry and Ga trigonal bipyramidal structure formed when the interstitials (occupancy of 17.9(1)%) are present. O8a is the terminal oxygen in the polyhedron.

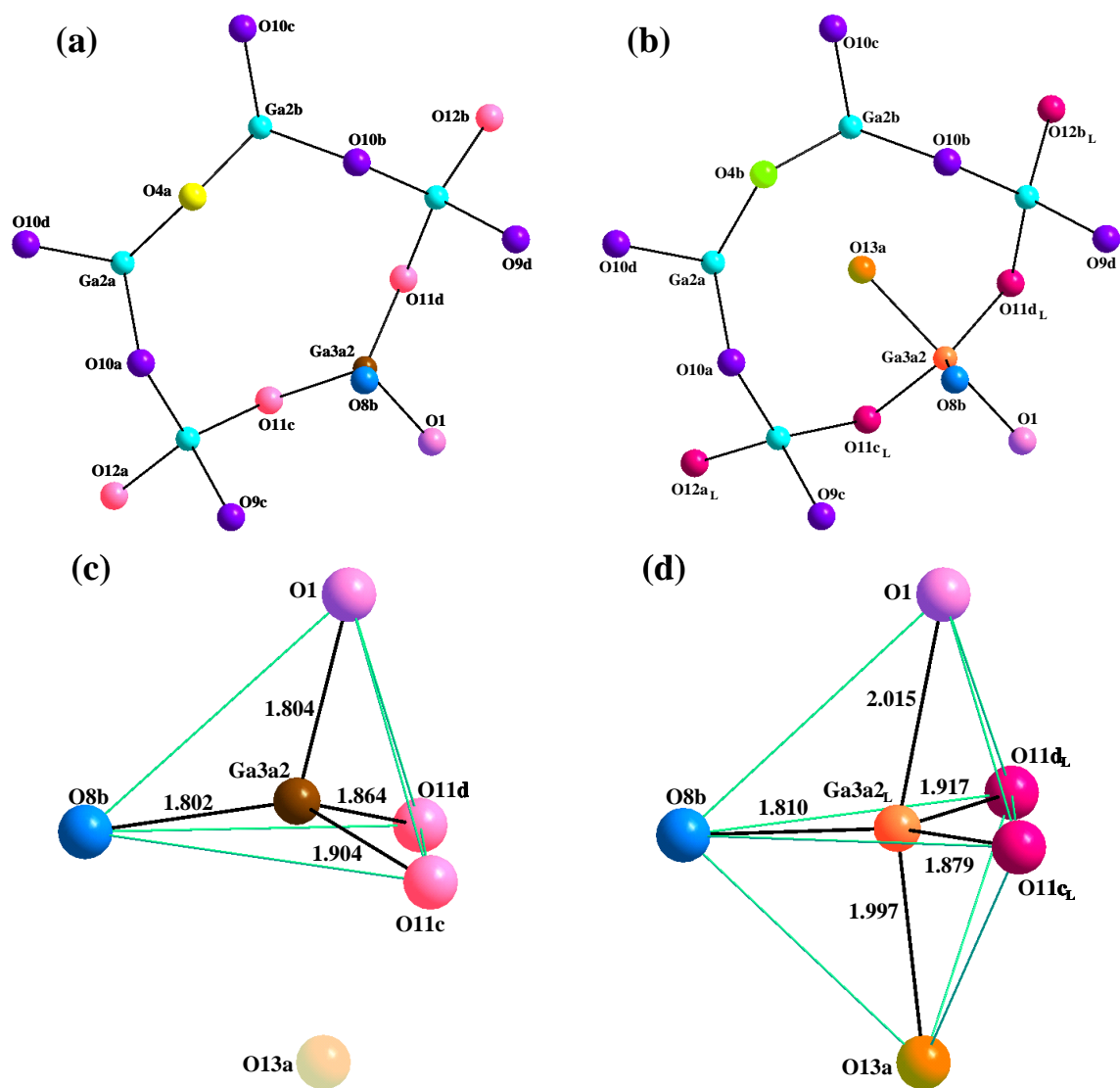


Figure S7.4 Structural relaxation around the interstitial oxide O13a in the split-model of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$. Ga3a2_L, O11c_L, O11d_L, O4b, La3b_L and La/Ca4b_L are involved in the local structural relaxation. (a) and (c) represent the refined structure in the absence of the interstitial O occupancy of this site with (b) and (d) showing the ring geometry and the Ga trigonal bipyramidal structure formed when the interstitials (occupancy of 28.0(1)%) are present. O8b is the terminal oxygen in the polyhedron.

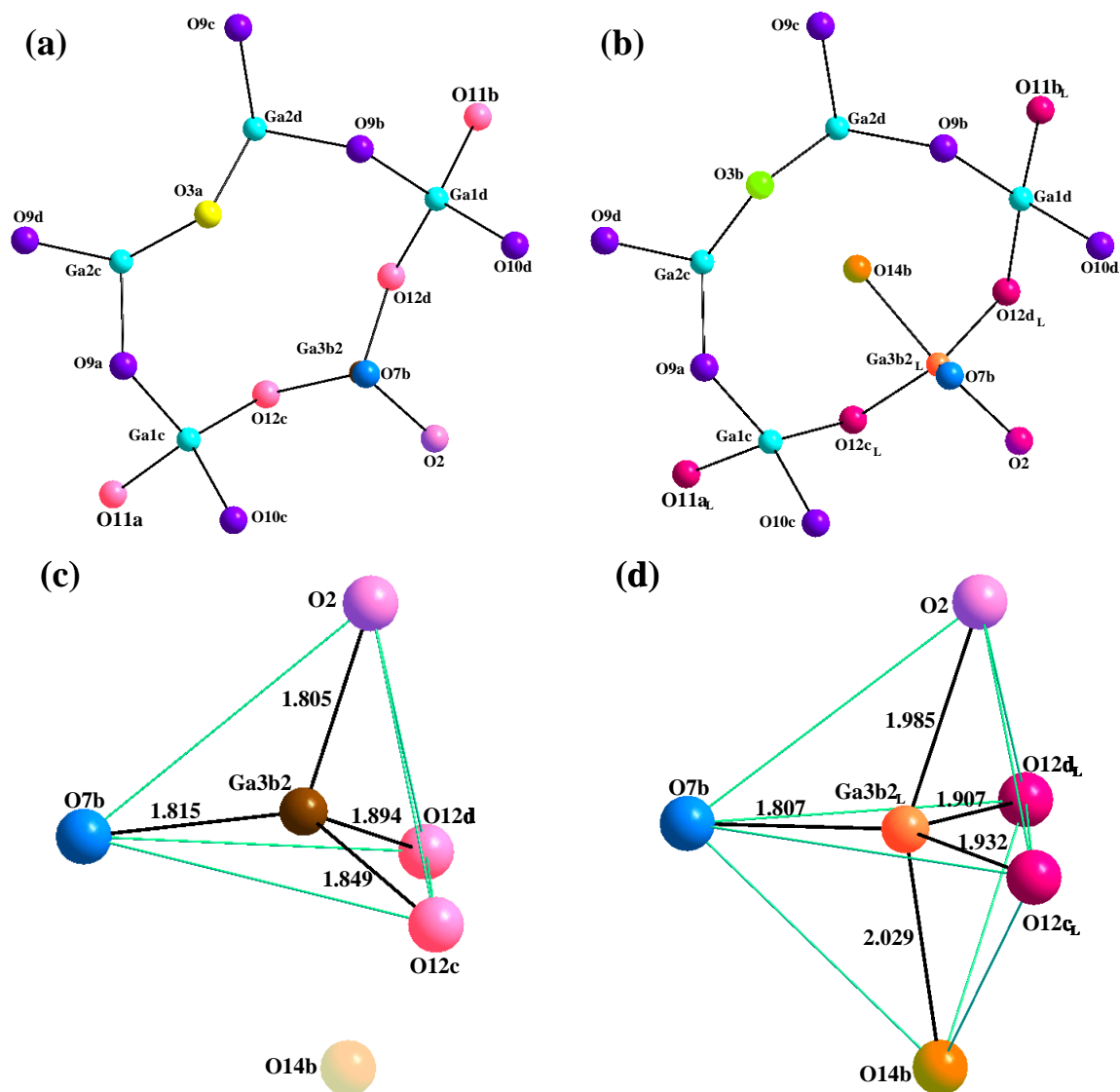


Figure S7.5 Structural relaxation around the interstitial oxide O14b in the split-model of $\text{La}_{1.64}\text{Ca}_{0.36}\text{Ga}_3\text{O}_{7.32}$. Ga3b2_L, O12c_L, O12d_L, O3b, and La/Ca4b_S are involved in the local structural relaxation. (a) and (c) represent the refined structure in the absence of the interstitial O occupancy of this site with (b) and (d) showing the ring geometry and Ga trigonal bipyramidal structure formed when the interstitials (occupancy of 23.9(1)%) are present. O7b is the terminal oxygen in the polyhedron.

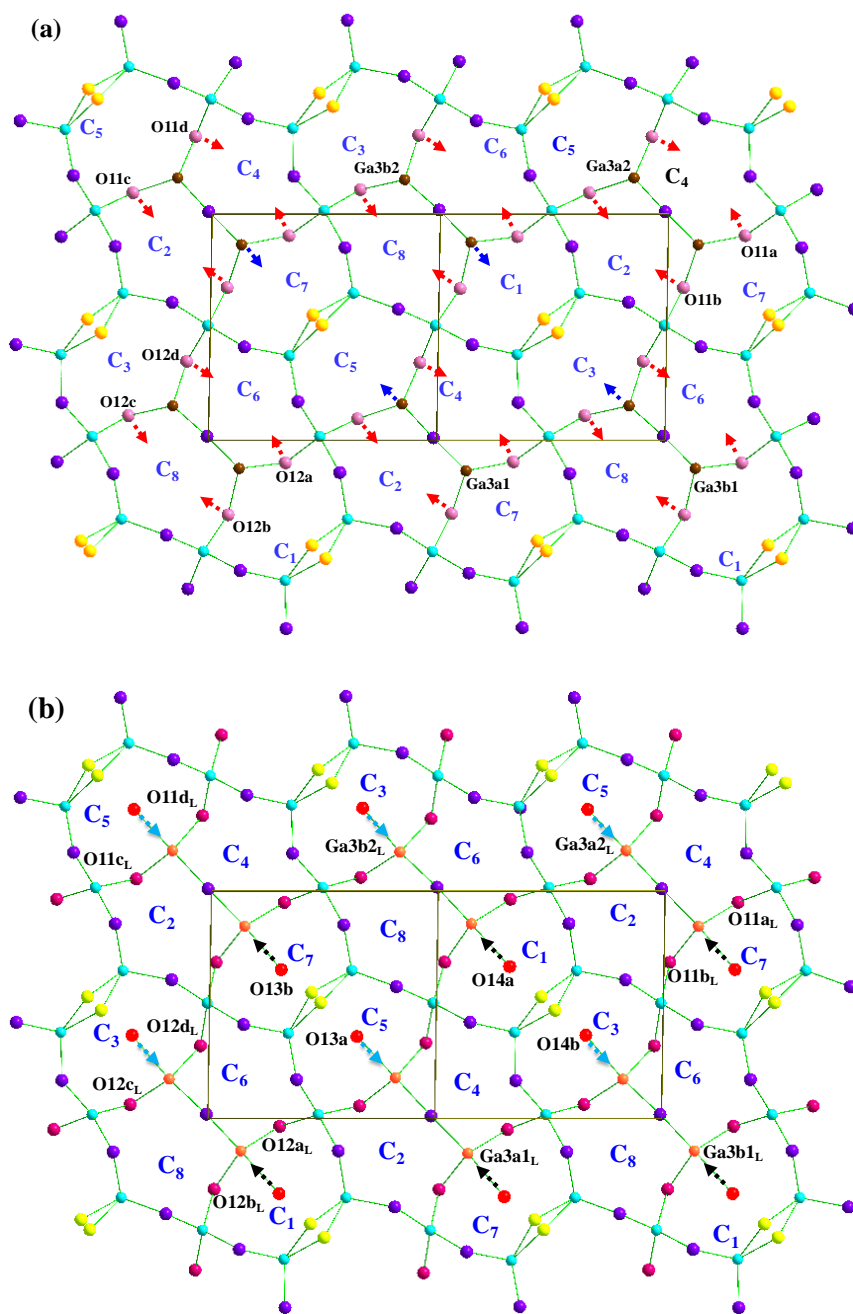


Figure S7.6 Enlarged projection along $[110]$ of (a) bulk and (b) defect structure to show the structural displacement to permit interstitial accommodation. The occupancy of two sets of centroids (C_1/C_7 and C_3/C_5) shares the same direction of displacement as marked by black and cyan arrows in (b), with the sense of the displacement being different in the two pairs.

8. Interstitial oxide and A-site cation ordering--composition and crystal structure

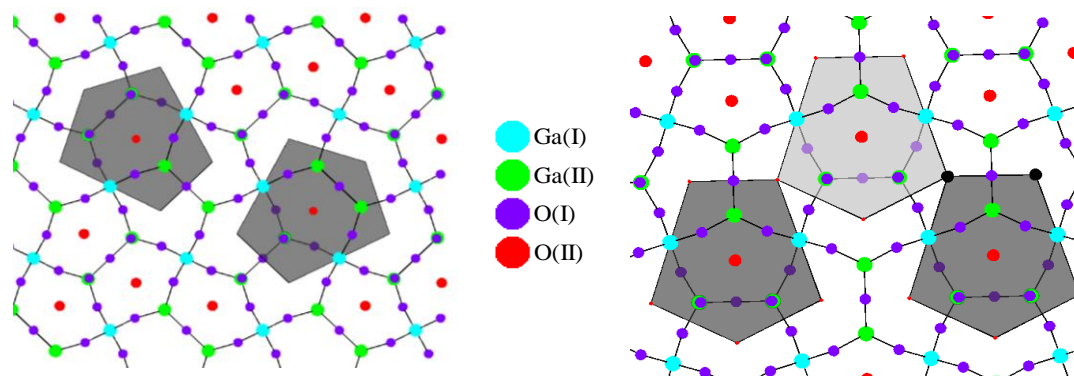


Figure S8.1 Pentagons represent the interstitial sites in the five nearest edge-shared rings with a random tiling, corresponding to disordered interstitial occupancy of the 5-rings which are the centroids of the pentagons, with interstitial occupancy $> 1/8$ (left), and maximally doped structure of either randomly $2/3$ occupied or partially ordered by dark grey, fully occupied and light grey $1/3$ occupied (right, dark spheres represent two ring centroids sharing a common three-connected Ga_2O_7 edge). Ga(I)O_4 , 4-connected; Ga(II)O_4 , 3-connected; O(I), framework oxygens; O(II), interstitial sites.

References

1. Larson, A. C., von Dreele, R. B., General Structure Analysis System (GSAS), Los Alamos National Laboratory Report LAUR 86-748. 2004.
2. P. W. Stephens, J. Appl. Crystallogr. 1999, 32, 281.
3. Coelho, A., *TOPAS-Academic, General Profile and Structure Analysis Software for Powder Diffraction Data*, version 4.1; <http://www.topas-academic.net/>, 2007.