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Experimental and theoretical study of heterogeneous iron precipitation in silicon

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Experimental and theoretical study of heterogeneous iron precipitation in silicon

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Heterogeneous iron precipitation in silicon was studied experimentally by measuring the gettering efficiency of oxide precipitate density of $1 \times 10^{10} \text{ cm}^{-3}$. The wafers were contaminated with varying iron concentrations, and the gettering efficiency was studied using isothermal annealing in the temperature range from 300 to 780 °C. It was found that iron precipitation obeys the so-called s-curve behavior: if iron precipitation occurs, nearly all iron is gettered. For example, after 30 min annealing at 700 °C, the highest initial iron concentration of $8 \times 10^{13} \text{ cm}^{-3}$ drops to $3 \times 10^{12} \text{ cm}^{-3}$, where as two lower initial iron concentrations of 5×10^{12} and $2 \times 10^{13} \text{ cm}^{-3}$ remain nearly constant. This means that the level of supersaturation plays a significant role in the final gettering efficiency, and a rather high level of supersaturation is required before iron precipitation occurs at all. In addition, a model is presented for the growth and dissolution of iron precipitates at oxygen-related defects in silicon during thermal processing. The heterogeneous nucleation of iron is taken into account by special growth and dissolution rates, which are inserted into the Fokker-Planck equation. Comparison of simulated results to experimental ones proves that this model can be used to estimate internal gettering efficiency of iron under a variety of processing conditions. © 2007 American Institute of Physics. [DOI: [10.1063/1.2472271](https://doi.org/10.1063/1.2472271)]

I. INTRODUCTION

Purity requirements of starting materials and cleanliness of the processes are ever increasing in the modern semiconductor technology. Internal gettering (IG), i.e., the capability of oxide precipitate related defects to capture impurities, is widely utilized in the integrated circuit industry to remove harmful metal contaminants from the device areas. However, a full understanding of the gettering mechanism has not been achieved so far. Better knowledge about behavior of transition metals and defect dynamics in silicon is essential in controlling the impurities by gettering. Only with increased understanding it is possible to create fully predictive models for transition metal behavior under different processing conditions, and eventually, to optimize the device yield.

One of the most troubling and common contaminant in silicon is iron. It diffuses relatively rapidly and it has deleterious effects on the device performance even when present in small concentrations. As experimental process optimization for impurity gettering is expensive and time consuming, several papers¹⁻⁷ discuss modeling of iron gettering. In these papers, iron precipitation to oxide precipitates is usually modeled using Ham's law,⁸ and it is further assumed that all oxide precipitates are effective (active) gettering sites, i.e., each oxide precipitate contains iron precipitate(s). Indeed, it is experimentally confirmed that at very high supersaturation the iron precipitation can be described through Ham's law.^{1,9}

However, these simulations greatly overestimate the gettering efficiency in slowly cooled samples.¹⁰ A better agreement between simulations and experiments was achieved by using a significantly lower effective gettering site density compared with the oxide precipitate density.¹⁰ This means that the dynamics of nucleation of iron precipitates must be taken into account, and the number of effective gettering sites may be only a small portion^{1,11,12} of the total oxide precipitate density.

In Refs. 6 and 7 the nucleation is taken into consideration using a steady-state nucleation rate, and it is shown that iron precipitation can then be simulated at low supersaturation level. However, it is difficult to handle the size distribution in the steady-state approach. The proper treatment of the size distribution is especially important as more complex processes than cooling or isothermal annealing are simulated. We have recently suggested a model for heterogeneous precipitation of iron in silicon,¹³ in which we use chemical rate equations (CREs) to calculate the size distribution of the iron precipitates and the residual dissolved iron concentration.

In this paper we demonstrate experimentally that iron precipitation produces similar s-curve behavior to what is typical, e.g., for oxygen precipitation.^{14,15} We propose a model for heterogeneous iron precipitation, in which we use growth and dissolution rates¹³ and the Fokker-Planck equation (FPE) to simulate the cluster evolution. We show that the proposed model can capture the effect of supersaturation to iron precipitation and explain the s-curve behavior. We

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also show that the proposed model can be used to simulate IG in various processing conditions reported in the literature.

II. EXPERIMENT

The silicon wafers used in the experiments were boron doped and their resistivities were about 30 Ω cm. The oxygen content¹⁶ was 15 ppma. First, a 15 min dry oxidation (homogenization) at 1050 °C was performed, which was followed by low-high annealings (6 h 650 °C + slow ramp + 6 h 1100 °C) to form oxide precipitates. The slow ramp was 0.5 °C/min from 650 to 800 °C, was 1 °C/min from 800 to 900 °C, and 2 °C/min from 900 to 1100 °C. The oxide layer was then removed and the wafers were contaminated in a SC1 solution with 30 ppb iron added impurities. The wafers were divided into three separate groups. Each group was submitted to a different temperature, 760, 850, or 940 °C, at which iron was driven in the wafers. The goal was to get three groups of wafers with different iron concentrations. After the indiffusion, the residual surface contamination was removed by etching the wafers in a H₂O:HF:H₂O₂ (24:1:1) solution and by cleaning in a sequence of SC1, SC2, and HF dips. The wafers were then dry oxidized at 900 °C for 20 min to form an oxide layer of about 10 nm. The initial iron concentrations were measured to be 5×10^{12} , 2×10^{13} , and 8×10^{13} cm⁻³, respectively. The initial iron concentrations were measured using deep level transient spectroscopy (DLTS) after a quench from indiffusion temperature.

The oxide precipitate density after low-high annealing was about 1×10^{10} cm⁻³, as measured using optical microscopy after a selective Wright etch step. The homogeneity of oxygen precipitation was also checked with microwave detected photoconductive decay (μ -PCD). The size of oxide precipitates measured by transmission electron microscopy (TEM) was about 80 nm.

Before each gettering annealing, the wafers were annealed for 30 min at the indiffusion temperature to dissolve the possible iron nuclei that may have been formed during the temperature ramps¹⁷ after the oxidation annealing. The wafers were then cooled at a rate of 50 °C/min to the gettering temperature, and the actual gettering annealing took 30 min at different temperatures (300–800 °C). After the gettering annealing, the wafers were cooled to room temperature at a rate of 100 °C/min. In other words, the outline of the gettering annealing is as follows: 30 min dissolution annealing \rightarrow cooling 50 °C/min \rightarrow 30 min@200–800 °C \rightarrow cooling 100 °C/min to RT. It should be noted here that the cooling rates mentioned here are programmed rates of furnace and actual cooling rates were not measured and they might deviate from programmed rates. However, in these experiments we tried to maximize the cooling rates so that the gettering annealings, as much as possible, determine the iron precipitation behavior. The remaining interstitial iron concentration after gettering was measured using μ -PCD.^{18,19} μ -PCD measurement has been calibrated against DLTS, and the iron concentrations of individual sample were also checked by DLTS if the iron concentration was close to the detection limit of μ -PCD.¹⁹

III. MODEL FOR HETEROGENEOUS PRECIPITATION OF IRON

The CRE can be solved using the selected grid point method²⁰ as we have done earlier in Ref. 13. This solution is rather time consuming. That is why we use here the FPE to simulate the evolution of the size distribution of iron precipitates

$$\frac{\partial f(n,t)}{\partial t} = \frac{\partial}{\partial n} \left[-A(n,t)f(n,t) + B(n,t) \frac{\partial f(n,t)}{\partial n} \right], \quad (1)$$

where $f(n,t)$ is the density of heterogeneous precipitation sites containing n atoms of precipitated iron and

$$\begin{aligned} A(n,t) &= g(n,t) - d(n,t), \\ B(n,t) &= \frac{g(n,t) + d(n,t)}{2}. \end{aligned} \quad (2)$$

The growth and dissolution rates are¹³

$$g(n,t) = 4\pi r_{\text{ox}} D C_{\text{Fe}} \quad \text{and} \quad d(n,t) = 4\pi r_{\text{ox}} D C_{\text{eq}}, \quad (3)$$

where r_{ox} is the average radius of the oxide precipitates (considered as an effective value if morphology is not spherical), D is the diffusion constant of iron, C_{Fe} is the interstitial iron concentration, and C_{eq} is the equilibrium iron concentration at the interface of gettering site. We presume that the equilibrium iron concentration at the interface depends on the number of iron atoms precipitated to the gettering site and has the form¹³

$$C_{\text{eq}} = C_{\text{Sol}} \exp\left(\frac{E_a}{kTn^{1/2}}\right), \quad (4)$$

where $E_a/n^{1/2}$ describes the fact that iron has a higher chemical potential in a small cluster than in a large cluster and C_{Sol} is the equilibrium concentration at the interface of a very large iron precipitate. E_a is a fitting parameter which is related to surface energy and it also includes possible effects of strain^{21–23} and the morphology¹ of oxide precipitates as well as the charge state²⁴ of iron.

The practical numerical solution of the FPE, which is unconditionally stable and relatively larger time steps are allowed, is given in Ref. 25. The solution of the FPE requires boundary condition at size of 1,

$$f(1,t) = P_1 f(0,t) \exp\left[\frac{kT \ln(C_{\text{Fe}}/C_{\text{Sol}}) - 2E_a}{kT}\right], \quad (5)$$

which is actually the size distribution function for a quasi-equilibrium state in an ideal heterogeneous nucleation process adjusted with a fitting parameter P_1 .¹⁵ In the IG simulation,

$$f(0,t) = N_{\text{ox}} - \int_1^{n_{\text{max}}} f(n,t) dn \quad (6)$$

is the density of such gettering sites that do not contain iron and N_{ox} is the density of oxide precipitates.

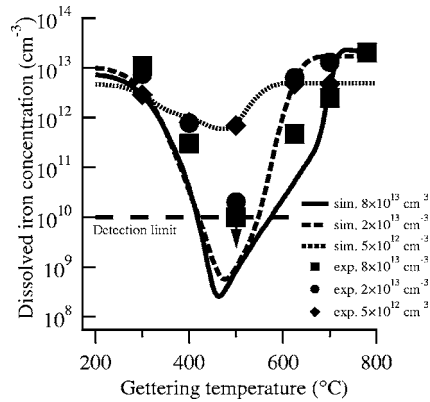


FIG. 1. Comparison of simulated (lines) and experimental results (symbols) of remaining dissolved iron concentration measured after 30 min of isothermal annealing. Initial iron concentrations were $8 \times 10^{13} \text{ cm}^{-3}$ (square, solid line), $2 \times 10^{13} \text{ cm}^{-3}$ (circle, dashed line), and $5 \times 10^{12} \text{ cm}^{-3}$ (diamond, dotted line). The simulations include programmed temperature ramps of the furnace.

IV. RESULTS AND DISCUSSION

A. Experimental and simulation

The symbols in Fig. 1 show the experimental results. At 300 °C, gettering is limited by diffusion, and almost no gettering takes place in any wafer. More interesting observations can be made at higher temperatures. The remaining dissolved iron concentration depends strongly on the initial iron concentration: the higher the initial iron concentration the less iron is measured after gettering. Note that at 500 °C the highest initial contamination level is gettered below our detection limit of $1 \times 10^{10} \text{ cm}^{-3}$. Therefore, the level of supersaturation, $kT \ln(C_{\text{Fe}}/C_{\text{Sol}})$, plays evidently a very significant role in the final gettering efficiency. The effect of supersaturation level is further supported by the observation that a rather high supersaturation is required before precipitation occurs at all. The supersaturation increases with lower temperature in all wafers, thus reducing the measured iron concentration as a function of temperature for temperatures above 450 °C. In other words, iron must be highly supersaturated and mobile at the same time, and this will result in a certain optimum “processing window,” where gettering is efficient. The optimum temperature depends on the initial iron concentration and the gettering time. The smaller the initial concentration, the lower the optimum temperature is. Notice that the wafer with the lowest initial iron concentration does not experience almost any gettering at any temperature. This is because the combination of high enough supersaturation together with high diffusivity is not reached at all.

The corresponding simulation results are shown by lines also in Fig. 1. In our simulations we use $C_{\text{Sol}} = 4.3 \times 10^{22} \exp(-2.10 \text{ eV}/kT) \text{ cm}^{-3}$ (Ref. 26), $D = 1 \times 10^{-3} \exp(-0.67 \text{ eV}/kT) \text{ cm}^2/\text{s}$ (Ref. 27), and gettering site parameters $N_{\text{ox}} = 1 \times 10^{10} \text{ cm}^{-3}$ and $r_{\text{ox}} = 40 \text{ nm}$. The fitting parameters of the model were obtained using least square method and experimental results of 30 min isothermal annealing. Fitted parameters are $P_1 = 1 \times 10^4$, $E_a = (1.015 \times 10^{-4}T + 0.8033) \text{ eV}$,

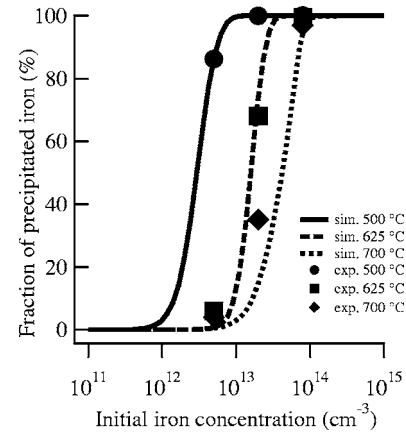


FIG. 2. Simulated and experimental s curve of iron precipitation at 700 °C (diamond, dotted line), 625 °C (square, dashed line), and 500 °C (circle, solid line). The simulations include programmed ramps of the furnace.

$T < 773 \text{ K}$, and $E_a = (6.038T \times 10^{-4}T + 0.4150) \text{ eV}$, $T \geq 773 \text{ K}$. With these parameters the experimental results can be fitted quite well, as shown in Fig. 1.

The results of Fig. 1 can be plotted as an s curve, which is typical, e.g., for oxygen precipitation.^{14,15} In Fig. 2 the results of gettering at temperatures 500, 625, and 700 °C are shown. Figure 2 clearly points out that as the initial supersaturation is above some threshold, nearly all iron will precipitate. This is well captured by the proposed model.

B. Dependency on size and density of gettering site

Takahashi *et al.*²¹ reported interesting results that, for a fixed amount of precipitated oxygen, the gettering efficiency of large oxide precipitates was higher than the gettering efficiency of small oxide precipitates, in case of fast cooling at a rate of 25 °C/s. In case of isothermal annealing at 190 °C the result was opposite: the gettering efficiency of small oxide precipitates was higher.²¹

We fitted the oxide precipitate densities and radii using the experimental results of isothermal annealing at 190 °C (Fig. 3) and using the sizes and areal densities reported by Takahashi *et al.*²¹ In the fitting we first fitted the density of the smallest (size of 10–15 nm) oxide precipitate, as their size distribution is narrow, using average radius of 6.3 nm. Then the other two oxide precipitate densities were calculated using the reported areal densities, and their average radii were obtained through a fit to the gettering results. The fitted average radii of 24 and 33 nm correspond to reported sizes of 25–35 and 40–80 nm, respectively. We set the initial iron concentration to $4.3 \times 10^{14} \text{ cm}^{-3}$, which corresponds to C_{Sol} value at the reported contamination temperature of 1050 °C. The exponential decay as seen in Fig. 3 is commonly observed at high supersaturation levels^{1,9} and can be well explained using Ham’s equation.⁸

The precipitation rate is always set by the $N_{\text{ox}}r_{\text{ox}}$ product in Ham’s equation and the experimental results at 190 °C support this (Fig. 3). However, Ham’s equation cannot describe properly the fast cooling experiments of Takashi *et al.*²¹ Figure 4 shows simulated iron concentrations as functions of temperature, with the measured final concentrations taken from Ref. 21. The simulation agree relatively well with

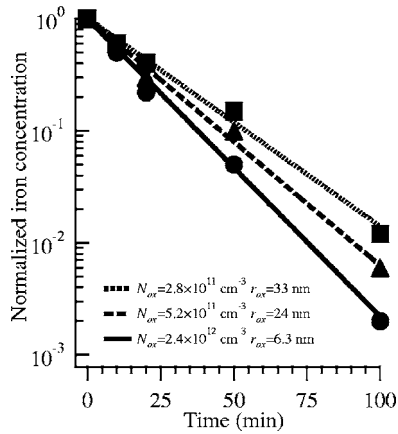


FIG. 3. Comparison of simulated (lines) and experimental results (symbols from Ref. 21) of remaining dissolved iron concentration measured during isothermal annealing at 190 °C. The concentrations are normalized to the initial iron concentration, which was set to $4.3 \times 10^{14} \text{ cm}^{-3}$ in the simulations. The fitted densities and average radii of oxide precipitates are shown in the legend.

experimental results, as the model suggests that larger oxide precipitates became effective gettering sites more easily than small ones simply due to the fact that growth and dissolution rates are proportional to the radii of precipitates. In reality, this may also be caused by strain field and extended defects that are often associated with large precipitates.^{21–23}

We were not able to fit N_{ox} and r_{ox} values (Figs. 3 and 4) to a fixed total amount of precipitated oxygen even though it, measured using Fourier transform infrared spectroscopy (FTIR), was kept constant in experiments.²¹ Furthermore, we found out that for constant initial iron concentration, the model predicts $N_{\text{ox}}r_{\text{ox}}^2$ dependency in gettering efficiency if nucleation limits the gettering efficiency. This result can be easily explained as nucleation produces a density of effective gettering sites $N_{\text{eff}} \sim N_{\text{ox}}r_{\text{ox}}$ [Eqs. (3) and (5)], and the final gettering efficiency (GE) after growth of iron precipitates depends on $N_{\text{eff}}r_{\text{ox}}$ product as

$$\text{GE} = 100[1 - \exp(-t_G 4\pi D N_{\text{eff}} r_{\text{ox}})], \quad (7)$$

where t_G is the length of the growth annealing.

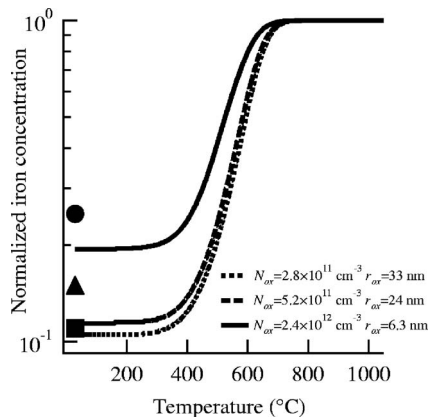


FIG. 4. Simulated interstitial iron concentrations during fast cooling (about 25 K/s). The initial iron concentration was $4.3 \times 10^{14} \text{ cm}^{-3}$. The densities and average radii of oxide precipitates used in the simulations are shown in the legend. The experimental results (marked with symbols) are from Ref. 21.

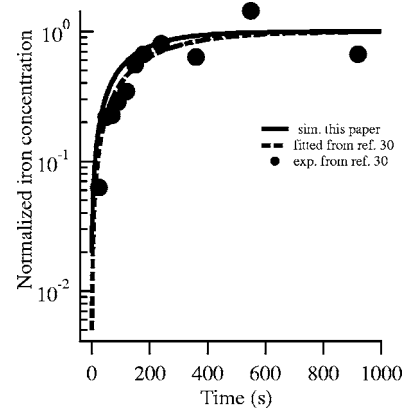


FIG. 5. Simulated (solid line) and experimental (circle) results show dissolved iron concentration vs time in dissolution annealing at 800 °C, after iron had been gettered to oxide precipitates. The experimental results are from Ref. 30.

Ogushi *et al.*²⁸ reported that gettering efficiency of iron correlates with total volume of oxide precipitates, which is clearly in disagreement with results of Takashi *et al.*²¹ however, the contamination level and gettering technique were different. Ogushi *et al.*²⁸ used initial contamination level of about $1 \times 10^{12} \text{ cm}^{-3}$, and the gettering was done in a long isothermal annealing after quenching to room temperature. This means that the final gettering efficiency was determined by iron nucleation during the ramp to room temperature and ramp up to gettering temperature.

C. Dissolution of iron precipitates

In addition to the gettering behavior, the thermal stability of iron precipitates is of interest for process simulations. The thermal stability of internally gettered iron has been studied by many authors,^{23,29,30} and it is known that after a sufficiently long high temperature annealing iron will be completely dissolved. Zhang *et al.*³⁰ studied the dissolution process in more detail using wafers with an oxide precipitate density of $5 \times 10^9 \text{ cm}^{-3}$, and the average radius was estimated to be 88 nm from decrease in the interstitial oxygen concentration. They contaminated samples to a level of about $1 \times 10^{14} \text{ cm}^{-3}$ at 950 °C. After that, the gettering was performed by cooling samples down to 700 °C at rate of 14 °C/min. The samples were kept at 700 °C for 30 min and then cooled to 450 °C at a rate of about 8 °C/min. The final ungettered iron concentration was $5 \times 10^{10} \text{ cm}^{-3}$. Iron dissolution was then studied at temperatures between 750 and 900 °C.

In the simulation, we used initial iron concentration of $9.6 \times 10^{13} \text{ cm}^{-3}$, which is the C_{Sol} value at the contamination temperature of 950 °C. The simulation gives the remaining dissolved iron concentration of $1.2 \times 10^{11} \text{ cm}^{-3}$, a value that is reasonably close to the measured value of $5 \times 10^{10} \text{ cm}^{-3}$.

Figure 5 compares the simulated and experimental³⁰ results of dissolution of gettered iron at 800 °C. The simulated and experimental results agree quite well and the simulation gives an effective gettering site density of $9.5 \times 10^7 \text{ cm}^{-3}$. The dissolution time constant calculated using this effective gettering site density is 132 s, whereas fitted time constant is

198 ± 83 s.³⁰ Actually, calculated time constants deviated significantly only at 750 °C, compared with the experimental, fitted dissolution time constants.³⁰ This means that the simulation of iron precipitation and dissolution can be performed consistently using the same model, with no need to use a dissolution barrier proposed by Zhang *et al.*³⁰

D. Gettering sites

One of the questions about IG is the type of defect, induced by oxygen precipitation, which is mainly responsible for iron precipitation. In the present model one can easily use different parameters for different types of defects: dislocations, stacking faults, and oxide precipitates. However, these parameters are hard to determine experimentally and this obviously makes the model less robust. Graff *et al.*³¹ stated that the IG of iron is mainly due to the presence of bulk stacking faults, and it does not depend on the density of oxide precipitates. On the other hand, they also stated that in many cases the density and size of oxide precipitates correlate with the existence of the bulk stacking faults.

Shen *et al.*^{32,33} studied the precipitation of copper and iron to dislocations³² in floating-zone grown silicon and iron precipitation to bulk stacking faults,³³ using different cooling rates. They reported that, after slow cooling, only some of the gettering sites are decorated by metals, whereas after fast cooling all of the gettering sites are decorated. These results can be easily reproduced in our simulations. During slow cooling the excess contamination is consumed by growth of existing metal precipitates and further nucleation, i.e., generation of new effective precipitation sites, is suppressed due to low supersaturation. On the other hand, during fast cooling the supersaturation remains high and nearly all possible precipitation sites become effective. Interestingly, Shen *et al.*^{32,33} explained their results in a similar manner.

As discussed previously, it seems that reasonably accurate modeling can be performed using the total defect density and some effective radius. How then should the total density and the effective radius be determined for simulation of iron IG? In this paper we use defect etching for density measurements and TEM to estimate the size of precipitation site. The size could be also estimated from oxygen loss as shown by analyzing the results of Zhang *et al.*³⁰ If either density or radius is known, then the other can be determined from a low temperature of 200 °C gettering test at a contamination level higher than 1×10^{13} cm⁻³, just as we have done in simulation of the results of Takahashi *et al.*²¹ The model parameters can also be taken from any experimentally confirmed oxygen precipitation simulator.

E. Precipitation of nickel and copper

In the literature^{34–36} it is speculated that heterogeneous precipitations of iron, copper, and nickel in the presence of oxide precipitates and extended defects may be different from each other. This speculation is supported by the fact that the gettings of copper and nickel cannot be explained by Ham's equation^{35,36} which can be used for iron at sufficiently high supersaturation. We expect that the model presented here can easily be extended to copper and nickel pre-

cipitation, if the experimental results^{35,36} are explained taking nucleation into account too, rather than through reaction limited precipitation only. Then the density of effective precipitation sites will be significantly smaller than the density of oxide precipitates. Note that in our model the gettering efficiency has the experimentally observed^{35,36} $N_{\text{ox}} r_{\text{ox}}^2$ dependency. Isomae *et al.*³⁷ also reported that the gettering efficiency of copper depends on the initial copper contamination level, which is naturally included in our model.

V. CONCLUSIONS

The experimental results of iron gettering in silicon by oxide precipitates and related defects revealed that rather high supersaturation is needed before nucleation of iron precipitates can take place. After nucleation the iron precipitation is fast due to relatively fast diffusion of iron. We proposed a model for heterogeneous iron precipitation, in which we use the FPE to simulate the cluster time evolution. Experimental results were used to find values for fitting parameters for the model. It was shown, comparing experimental results of Takahashi *et al.*²¹ to our simulations, that the model captures the effect of oxide precipitate radius and density to iron gettering. We were also able to simulate the gettering-dissolution experiment, reported by Zhang *et al.*,³⁰ in a consistent manner using the same model. Furthermore, the model can easily be expanded for precipitation of copper and nickel.

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