

Tracy, Saoirse R. and Daly, Keith R. and Sturrock, Craig J. and Crout, Neil M.J. and Mooney, Sacha J. and Roose, Tiina (2015) Three-dimensional quantification of soil hydraulic properties using X-ray computed tomography and image-based modeling. Water Resources Research, 51 (2). pp. 1006-1022. ISSN 1944-7973

Access from the University of Nottingham repository: http://eprints.nottingham.ac.uk/41200/1/141211 WRR srtsjmkrd.pdf

Copyright and reuse:

The Nottingham ePrints service makes this work by researchers of the University of Nottingham available open access under the following conditions.

This article is made available under the University of Nottingham End User licence and may be reused according to the conditions of the licence. For more details see: http://eprints.nottingham.ac.uk/end_user_agreement.pdf

A note on versions:

The version presented here may differ from the published version or from the version of record. If you wish to cite this item you are advised to consult the publisher's version. Please see the repository url above for details on accessing the published version and note that access may require a subscription.

For more information, please contact eprints@nottingham.ac.uk

| 2 | Tomography and image based modelling | |
|----|--|--|
| 3 | | |
| 4 | Author list: Saoirse R. Tracy ^{1\$} , Keith R. Daly ^{2\$} , Craig J. Sturrock ¹ , Neil M. J. Crout ¹ , Sacha | |
| 5 | J. Mooney ¹ , Tiina Roose ^{2§} | |
| 6 | | |
| 7 | Author affiliations: | |
| 8 | ¹ School of Biosciences, University of Nottingham, Sutton Bonington Campus, Leicestershire, | |
| 9 | LE12 5RD. | |
| 10 | ² Bioengineering Sciences Research Group, Faculty of Engineering and Environment, | |
| 11 | University of Southampton, University Road, SO17 1BJ. | |
| 12 | ^{\$} These authors are joint lead authors | |
| 13 | [§] Corresponding author: Bioengineering Sciences Research Group, Faculty of Engineering and | |
| 14 | Environment, University of Southampton, University Road, SO17 1BJ Southampton, United | |
| 15 | Kingdom, email: <u>t.roose@soton.ac.uk</u> | |
| 16 | | |
| 17 | Key Points: | |
| 18 | • X-ray Computed Tomography is used to image water distribution in soil. | |
| 19 | • 3D Computed Tomography images are combined with image based modelling. | |
| 20 | • Unsaturated hydraulic conductivity and the water release characteristic are obtained. | |

Three dimensional quantification of soil hydraulic properties using X-ray Computed

22 1. Abstract

23 We demonstrate the application of a high-resolution X-ray Computed Tomography (CT) 24 method to quantify water distribution in soil pores under successive reductive drying. We focus 25 on the wet end of the water release characteristic (WRC) (0 to -75 kPa) to investigate changes 26 in soil water distribution in contrasting soil textures (sand and clay) and structures (sieved and 27 field structured), to determine the impact of soil structure on hydraulic behaviour. The 3D 28 structure of each soil was obtained from the CT images (at a 10 μ m resolution). Stokes 29 equations for flow were solved computationally for each measured structure to estimate 30 hydraulic conductivity. The simulated values obtained compared extremely well with the 31 measured saturated hydraulic conductivity values. By considering different sample sizes we 32 were able to identify that the smallest possible representative sample size which is required to 33 determine a globally valid hydraulic conductivity.

34

35

36

Keywords: Matric potential; soil pores; water release characteristic; X-ray Computed
Tomography; image based homogenisation.

- 40 Abbreviations:
- 41 (3D) 3-dimensional
- 42 (CT) Computed Tomography
- 43 (ROI) Region of interest
- 44 (WRC) Water release characteristic

45 (WFP) – Water filled pores

46 (AFP) – Air filled pores

- 47 (REV) -Representative elementary volume
- 48

49 Short title for page headings: Three_dimensional quantification of soil hydraulic properties
 50

51 2. Introduction

52 Understanding the dynamic nature of water movement through, and storage within, soil is of 53 fundamental importance for most of its functions. A more detailed knowledge of how soil 54 structure influences soil water distribution and subsequently availability to plants is needed to 55 inform soil management practices and thus contribute to efforts in increasing crop yields for an expanding global population. However, to truly understand how water moves through soil 56 57 and is retained in soil pores whilst undergoing drying, non-destructive measurements of the 58 soil aggregate geometries and pore structure are needed. The use of X-ray Computed 59 Tomography (CT) to examine the 3D soil pore structure is rapidly gaining pace [Helliwell et al., 2014; Mooney et al., 2012]. The ability to segment water from a greyscale CT image 60 61 remains challenging due to limitations in the phase separation achievable with regular detectors 62 in benchtop CT scanners. Segmentation of fluids in alternative porous media such as glass 63 beads has been previously described in the literature [Haugen et al., 2014; Iassonov et al., 64 2009]. However, due to the more complex, heterogeneous structure of soil and the associated 65 challenges faced during image acquisition this brings, these segmentation techniques cannot 66 always be readily applied to the segmentation of soil phases in X-ray CT images [Houston et 67 al., 2013]. Yet, Crestana et al. [1985] highlighted the potential of CT for investigating water 68 movement through soil by quantifying the vertical and lateral water flows in 3D. By using dual

Deleted: well documented

| Deleted: be easily | |
|--------------------|--|
| Deleted: using | |

73 energy tomography Rogasik et al. [1999] showed it is possible to quantify soil water, pore 74 space and bulk density. Mooney [2002], compared dry and moist samples and developed an 75 imaging method to separate water from the bulk soil in undisturbed soil cores albeit at a coarse 76 resolution (0.5 mm) using a medical CT scanner. Water flow characteristics were well matched 77 to macropore structure, with *circa* 90% of macropore space active in water transport in a sandy 78 clay texture, compared to circa 50% in the sandy loam soil. Wildenschild et al. [2005] 79 investigated multiphase flow processes and quantified drainage paths, showing that water is 80 preferentially lost from larger pores and the drainage of the remaining disconnected pores is 81 prevented. Since then Tippkotter et al. [2009] detected soil water in macropores and measured 82 water film thickness at a 20 μ m resolution. They quantified the water without the use of contrast 83 enhancing agents or comparison of wet and dry scans. Partial volume effects make separating boundaries between phases of interest a challenging task, due to the material of concern often 84 85 failing to fully fill a voxel [Ketcham and Carlson, 2001]. This can lead to individual voxels 86 being misclassified. However, as a microfocus system with a fine resolution was used in the 87 study, the impact of voxel misclassification is minimised [Clausnitzer and Hopmans, 2000]. 88 The most recent advances in CT imaging technology now allow 3D non-destructive imaging 89 of soils at even higher resolutions, e.g. <3 µm spot size [Zappala et al., 2013], allowing water 90 to be observed in smaller pores than previously considered.

91

The macroscopic scale flow in saturated and unsaturated porous media are often described using a Darcy's law and Richards' equation [*Hornung*, 1997]. These equations are parameterised by the unsaturated hydraulic conductivity and WRC. From a mathematical perspective Darcy's law can be derived from the underlying Stokes equations using the method of homogenization [*Keller*, 1980]. This approach has been applied to single porosity materials [*Hornung*, 1997; *Keller*, 1980], double porosity materials [*Arbogast and Lehr*, 2006; *Panfilov*,

| -{ | Deleted: c.circa 0.5 mm |
|----|-----------------------------|
| -{ | Formatted: Font: Not Italic |
| -{ | Deleted: similar to |
| | |
| -{ | Deleted: c. |
| | |
| -{ | Deleted: c. |
| | |
| -{ | Deleted: , they |
| - | Deleted: ed |

Deleted:

105 2000], and porous media containing voids or vugs [Arbogast and Lehr, 2006; Daly and Roose, 106 2014]. This method is based on the idea that the underlying porous structure is periodic, *i.e.*, it 107 is composed of a set of regular repeating units. By calculating the average fluid velocity for a 108 single representative unit volume due to a unit pressure drop, Darcy's law and the 109 representative hydraulic conductivity can be derived [Pavliotis and Stuart, 2008; Taylor et al., 110 1970]. The mathematics underlying the WRC is less well established and homogenization 111 studies to date have assumed that the air water interface is known in advance [Taylor et al., 112 1970].

113

114 Image based modelling can be loosely divided into two categories: pore network modelling 115 and direct simulation [Blunt, 2001; Blunt et al., 2013]. The first of these, pore network modelling, refers to the extraction of a representative network from the pore scale geometry 116 117 [Fatt, 1956] and has been widely used to predict averaged properties of packed spheres [Bryant 118 and Blunt, 1992; Bryant et al., 1993b] and imaged porous media [Blunt, 2001; Blunt et al., 119 2013; Bryant et al., 1993a]. This technique is able to reproduce relative permeability curves and water release characteristics. However, the pore network extraction results in a simplified 120 geometry which may neglect important pore scale phenomena. The alternative technique of 121 122 direct modelling involves solving equations directly on the imaged geometries. This technique 123 captures the detail of the pore scale geometry down to the resolution limit. The key 124 disadvantage is that modelling multiphase flow is demanding from a computational point of 125 view. Typically models of this type are based on Lattice Boltzman simulations of two fluids as 126 these are highly parallel and relatively easy to implement [Gao et al., 2012; Ramstad et al., 127 2010]. Other image based modelling studies in porous media include 3D image based 128 simulations of nutrient transport [Keyes et al., 2013] and saturation based flow modelling of 129 water movement in 2-D image slices [Aravena et al., 2014; Aravena et al., 2011].

131 In this paper we demonstrate the application of a high resolution CT method to quantify water distribution in soil pores under successive reductive drying. Using the structural geometries 132 133 from the CT images we apply the method of homogenization combined with direct image based 134 modelling to calculate the hydraulic conductivity across a range of matric potentials. This can 135 be seen as analogous to the measurement of a wetting phase relative permeability curve. 136 Specifically the question we aimed to answer is: what is the smallest possible Representative Elementary Volume (REV) required to determine a hydraulic conductivity approximation 137 138 which is globally valid? In addition the soil moisture content is calculated directly from the CT 139 images at a range of different matric potentials and, hence, the WRC is derived. This approach 140 is chosen, rather than Lattice Boltzmann simulation, as it allows the WRC and hydraulic 141 conductivity to be calculated quickly without the need for time consuming two fluid 142 simulations. From the images we are able to obtain information on soil drainage in both 143 undisturbed field cores and sieved soils. This was used to accurately determine the impact of 144 soil structure on hydraulic behaviour.

145

146 **3. Materials and Methods**

147

148 *3.1. Sample preparation*

Soil was obtained from The University of Nottingham farm at Bunny, Nottinghamshire, UK
(52.52° N, 1.07° W). The soils used in this study were a Eutric Cambisol (Newport series,
loamy sand/sandy loam) and an Argillic Pelosol (Worcester series, clay loam). Particle size
analysis for the two soils was: 83% sand, 13% clay, 4% silt for the Newport series and 36%
sand, 33% clay, 31% silt for the Worcester series. Typical organic matter contents were 2.3%

Deleted: ¶

155 for the Newport series and 5.5% for the Worcester series [Mooney and Morris, 2008]. From 156 herein the two soil types are referred to as sand and clay soil. Loose soil was collected from 157 each site in sample bags and field cores (10 mm height, 10 mm diameter) were collected from 158 the immediate soil surfaces after any residues had been cleared. Four replicates were collected 159 for each soil type. Saturated hydraulic conductivity measurements of the field cores were 160 obtained via the standard laboratory method using a constant head device [Rowell, 1994]. 161 Experimentally obtained hydraulic conductivity measurements were made for comparison with 162 the calculated values.

163

164 *3.2. Measurement of the soil water release characteristic*

165 In order to investigate the effect of drying on soil water distribution and soil structural changes in 3D, a custom-built tension table was designed to hold the soil sample at a given matric 166 167 potential, whilst undergoing CT scanning. A small vacuum chamber was constructed 168 (Supplementary Figure 1), that contained a porous ceramic plate (Soil Moisture Corp, Santa 169 Barbara, CA, U.S.A) on top of which a field soil core was placed, with kaolin clay at the base 170 to ensure a good contact. The sample size was kept small to ensure high resolution scanning 171 based on the sample size: resolution trade off that limits CT studies [Wildenschild et al., 2002]. 172 The porous ceramic was first submerged in de-aired deionized water and a vacuum applied to 173 ensure no air bubbles remain trapped within the ceramic. The plastic chamber had an O-ring 174 seal at the base and a flange, which was screwed together to ensure an air-tight fit. All 175 components of the chamber were made from plastic to avoid possible image artefacts, which 176 could result from using high X-ray attenuating construction materials such as metal. A 0387 177 Millipore vacuum pump (Merck Millipore, MA, USA) was attached to the chamber and the 178 soil columns were initially saturated from below with deionized water before being placed

Deleted: Deleted: put

| 181 | under a vacuum of -5 kPa (50.8 mmHg), -10 kPa (76.2 mmHg), -20 kPa (152.4 mmHg), -40 |
|-----|---|
| 182 | kPa (304.8 mmHg), -60 kPa (457.2 mmHg) and -75 kPa (533.4 mmHg). <u>It was not possible to</u> |
| 183 | achieve, pressures in excess of -75 kPa in the system described. The vacuum pump was enabled |
| 184 | for 120 min then the valve sealed to retain the vacuum inside the chamber. At each matric |
| 185 | potential the soil core inside the chamber was scanned (further details in next section). After |
| 186 | each scan the soil core was removed from the chamber and weighed to calculate gravimetric |
| 187 | water content. |

Deleted: Despite testing
Deleted: , further
Deleted: were not possible
Deleted: turned on

188

189 Using a combination of sand tables, pressure plates and pressure membrane apparatus, the 190 WRC were obtained for both soil types. Using conventional methods the van Genuchten model 191 [van Genuchten, 1980] was fitted to the data. The sand table was prepared by filling the water 192 reservoir and raising it above the base height of the table to ensure full saturation of the sand 193 table with no air bubbles. Both undisturbed field cores and sieved samples (packed to a bulk density of 1.2 g cm⁻³) were placed flat on the sand table. To obtain the mid-range points on the 194 195 WRC, a pressure plate Model 1600 Pressure Plate Extractor (Soil Moisture Corp, Santa 196 Barbara, CA, U.S.A) was used. Samples were placed on the plate and the samples were 197 weighed frequently until equilibrating at a series of matric potentials. To obtain measurements 198 at lower matric potentials, a pressure membrane apparatus was used. For the sieved samples 199 the required mass of soil was carefully placed into the metal vessels of the pressure membrane 200 apparatus and saturated with air-free water. The field core samples were directly collected in 201 the metal cores and placed onto the apparatus. The collection tubes were weighed frequently 202 and once equilibrated the system was adjusted to higher pressures. After the final measurement, 203 soil samples were oven dried at 105 °C for 24 hr then weighed.

The measured volumetric water content of the field structured soil cores (θ), accounted for the likely presence of stones and their overall influence on the WRC [*Gardner*, 1965; *Reinhart*, 1961]. The volumetric water content of the soil is written as θ which is measured in $\frac{\text{cm}^3(\text{H}_2\text{O})}{\text{cm}^3(\text{Soil})}$. To calculate this a correction was applied to the measured volumetric water content of the sample, θ_m , which is measured as $\frac{\text{cm}^3(\text{H}_2\text{O})}{\text{cm}^3(\text{Total})}$. This stone correction was calculated using

$$\theta = \theta_m \left(1 + \frac{v_s}{v_f} \right), \tag{1}$$

where V_f is the fine soil volume measured in cm³(soil) and V_s is the volume of stones which is measured in cm³(stones) and calculated by subtracting the soil volume from the total sample volume.

217

218 3.3. X-ray Computed Tomography and analysis

219 Four replicates from each soil type of the field cores were scanned at the seven matric potentials 220 giving a total of 56 scans for the field structured cores. As they would not be used for individual 221 pore characterisation analysis only three replicates were scanned for the sieved soils leading to 222 42 additional scans and a total overall number of 98 scans. The field of view for each scan 223 included the entire sample and each scanned sample created a dataset approximately 25 224 gigabytes in size, which includes all the associated image stacks for analysis, therefore 2.4 225 terabytes of data was collected. X-ray CT scanning was performed using a Phoenix Nanotom 226 180NF (GE Sensing & Inspection Technologies GmbH, Wunstorf, Germany). The scanner 227 consisted of a 180 kV nanofocus X-ray tube fitted with a diamond transmission target and a 5-228 megapixel (2316 x 2316 pixels, 50 x 50 μ m pixel size) flat panel detector (Hamamatsu 229 Photonics KK, Shizuoka, Japan). A maximum X-ray energy of 100 kV and 140 µA was used

Deleted: giving a total of

Deleted: so overall

232 to scan each soil core. A total of 1440 projection images were acquired over a 360° rotation. 233 Each projection was the average of 3 images acquired with a detector exposure time of 1 s. 234 The resulting isotropic voxel edge length was 10.17 μ m and total scan time was 105 minutes 235 per core. Although much faster scan times are possible it was necessary in this instance to use 236 a longer scan time to acquire the highest quality images to aid with the phase separation. Two 237 small aluminium and copper reference objects (< 1 mm²) were attached to the side of the soil 238 core to assist with image calibration and alignment during image analysis. Reconstruction of 239 the projection images to produce 3D volumetric data sets was performed using the software 240 datos/rec (GE Sensing & Inspection Technologies GmbH, Wunstorf, Germany).

241

242 The reconstructed CT volumes were visualised and quantified using VG StudioMAX® 2.2 243 (Volume Graphics GmbH, Heidelberg, Germany). Air, soil and water phases of the scanned 244volume were segmented separately using a threshold technique based on the greyscale value of each voxel using a calibration tool within VG StudioMax v2.2. This works by selecting 245 246 specific areas of the scanned volume based on greyscale values, which are a result of (X-ray 247 attenuation) density differences within the sample. Image segmentation is the classification of 248 voxels within a CT volume that share common grayscale values and thus X-ray attenuation. 249 The calibration tool allows the user to sample the greyscale value of a selection of voxels that 250 correspond to the background (e.g. the phase/s not considered, this is usually the background 251 air) and then the process is repeated for voxels that correspond to the material of interest (e.g. 252 water, air or soil). Based on the greyscale range we segmented all voxels above a 50% mean 253 value between the background and material of interest and define them as a particular phase 254 (i.e. a region of interest). In a two phase sample air is usually used as the background greyscale 255 value to calibrate against. However, as we required the segmentation of three phases, two

Deleted: inside each chamber for each scan

257 vessels, one containing soil pore water and the other finely sieved soil (< 100 μ m) for either 258 the sand or clay soil were securely fitted to the inside of the chamber for each scan. The soil 259 pore water and finely sieved soil remained separate from the soil core, but within the imaging 260 field of view, which was important as the soil core sample can change in overall greyscale 261 range over the course of the experiment due to localised drying and X-ray filament aging. Using 262 this approach these separate vessels were used as reference objects during image analysis. It 263 was important that reference vessels were included in every scan as CT scanning is subject to minor variations in greyscales between scans as the system filament ages. A schematic 264 265 representation of the water segmentation method is presented in Supplementary Figure 2. The 266 first stage was to create a region of interest (ROI) that included <u>all phases except</u> the air filled 267 pore space. This was done by selecting the air space around the sample as the background, 268 ensuring <u>all voxels</u> except those of air would be included as the material of interest and a 3D 269 ROI was then created and labelled 'Water and soil ROI' e.g. air not included. The process was 270 then repeated, but <u>utilising</u> the soil inside the reference vessel as a reference value for the solid 271 material. It was used as a reference as it contained limited water and air, hence this 3D ROI 272 was labelled 'Soil'. Subtraction of the 'Soil ROI' from the 'Water and soil ROI' resulted in a 273 ROI with voxels of grey scale values attributed to 'soil water only', e.g. the range of voxels 274 remaining after the soil and air ROIs have been subtracted. The volume of the resulting 'Soil 275 Water' ROI was validated against the water reference object and traditional methods of 276 determining volumetric water content (weighing). Using this approach we assume all organic 277 matter is classified as 'soil'. To create an ROI that included solely the air filled pore space, the 278 ROI that included all material except the air was inverted using the 'Invert ROI' function in 279 VG_StudioMax software. The volume analyser tool in VG StudioMax was subsequently used 280 to quantify the total volume of the air and water filled pores. Reconstructed volumes for each 281 matric potential were aligned in VG StudioMax using the metal reference objects on the outside

| Deleted: throughout | | |
|--------------------------|------|--|
| | | |
| | | |
| Deleted: i | | |
| | | |
| Deleted: a | | |
| | | |
| | | |
| | | |
| | | |
| Deleted: everything, but | | |
| | | |
| | | |
| | | |
| | | |
| Deleted: everything else | | |
| | | |
| Deleted: was | | |
| Perecedi was | | |
| | | |
| Deleted: used | | |

| Deleted: just | | | |
|------------------|----------|--|--|
| | | | |
| Deleted: everyth | hing but | | |
| | - | | |
| Deleted: | | | |

| \square | Deleted: | manually |
|-----------|----------|----------|
| | Deleted: | |

Deleted: that

| 295 | of the sample container. After segmentation of the soil core volumes, a cylindrical ROI shape |
|-----|---|
| 296 | template was used to subtract the surrounding column and air space from the volume to remove |
| 297 | the cylinder of soil. This template was used to ensure the same volume was <u>used for each</u> |
| 298 | sample before analysis. No significant evidence of shrinkage was observed across the range of |
| 299 | low matric potentials considered here. We note that when three phases (air water and soil) are |
| 300 | present in an image erroneous films of the intermediate phase can often be segmented out |
| 301 | between the high and low density phases. In this case erroneous films of water could be |
| 302 | introduced through segmentation. However, as thin water films only contribute a total flow |
| 303 | proportional to the third power of the film thickness these are not a concern in this study. |

305 Image stacks of the extracted volumes were exported and subsequently analysed for individual 306 water filled and air filled pore characteristics for the field structured soil only using ImageJ 307 v1.42 (http://rsbweb.nih.gov/ij/) [Ferreira and Rasband, 2011]. For 2D analysis objects less 308 than two pixels (twice the resolution) in diameter (0.02 mm) and for 3D analysis objects less 309 than two voxels in each direction (8 x 10⁻⁶ mm³) were regarded as potential noise as a 310 precaution [Wildenschild et al., 2005] and subsequently excluded from the analysis. The BoneJ 311 plugin algorithm [Doube et al., 2010] (http://bonej.org/) in ImageJ software was used to 312 measure discrete individual 3D water filled and air filled pore characteristics namely volume, 313 surface area and thickness (diameter). A voxel is classed as connected to another voxel if it at 314 least touches corner to corner. ImageJ was used to measure the 2D pore shape characteristic 315 'circularity', which is a measure of an object's similarity to a circle. A value of 1 describes a 316 perfect circle and as the value decreases, the object becomes increasingly elongated. The 317 circularity was determined using

| Deleted: | 20 μm |
|----------|---|
| | |
| Deleted: | 80 μm ³ |
| | |
| Deleted: | and subsequently excluded from the analysis |
| Deleted: | 1. |
| | |
| | |
| | |
| | |
| | |
| | |
| Deleted: | |
| Deleted: | - |

Deleted: cropped



$$\mathcal{C} = \frac{4\pi (A_p)}{(P_p)^2},$$

12

(2)

Deleted: perfect
Deleted: would be

where A_p is the pore area and P_p is the pore perimeter. The water-filled pore image stack was skeletonised and from this the 3D connectivity (the sum of all the thin (1 voxel) pathways that still preserve the connected topology and original shape of the object) of the water-filled pore volume was also calculated.

331

Jn order for the geometries of the water-filled pores to be modelled, surface mesh files (.stl)
were required which were generated in VG StudioMax v2.2. After segmentation of the soil
water phase, a cube shaped ROI template was imported to create identical cubes for the surface
mesh generation. Each sample was subsampled, from random initial coordinates, with 6 cubes
comprising side lengths of 3.8 mm. The same coordinates were used for different matric
potentials of the same sample. Each individual surface mesh file took between 0.5 – 2 hours to
generate depending on the complexity of the surface.

Moved (insertion) [1]

Deleted: ; these

339

340 3.4. Modelling

341 The hydraulic conductivity of the soil was calculated using the method of homogenization 342 [Pavliotis and Stuart, 2008]. This method allows an average Darcy's law to be defined which 343 is applicable to the soil column and is parameterised by the pore scale geometry of the soil. 344 The key assumption used was that the hydraulic properties of the soil can be accurately 345 captured by studying a small subsample of the soil [Fowler, 1997], this is often referred to as 346 the Representative Elementary Volume (REV). In this paper we were particularly interested in 347 determining the minimum size REV for which the calculated hydraulic conductivity converges 348 to the macroscopic hydraulic conductivity for soil samples of the order of a few millimetres.

Moved up [1]: In order for the geometries of the water-filled pores to be modelled, surface mesh files (.stl) were required; these were generated in VG StudioMax v2.2. After segmentation of the soil water phase, a cube shaped ROI template was imported to create identical cubes for the surface mesh generation. Each sample was subsampled, from random initial coordinates, with 6 cubes comprising side lengths of 3.8 mm. The same coordinates were used for different matric potentials of the same sample. Each individual surface mesh file took between 0.5 - 2 hours to generate depending on the complexity of the surface.

Deleted: ¶

| 501 | This method anowed us to theoretically determine the required sample size for CT analysis of | | |
|-----|--|---|---|
| 362 | water flow in soil <u>at this scale</u> | _ | Deleted: on |
| | | | Deleted: ¶ |
| 363 | | | |
| 364 | We note that the averaged hydraulic conductivity and WRC calculated at this scale are not | | Deleted: on |
| 365 | globally applicable. Rather they describe the average flow rate in soil of this type assuming no | | Deleted: that |
| 505 | | | |
| 366 | large scale features such as cracks or larger voids are encountered. In theory these features | < | Deleted: , |
| 367 | could be included by deriving an averaged Darcy's law for each soil type, Stokes' equations | | Deleted: or regions of different porosity |
| 368 | for large void spaces and approximate Darcy's laws for fractures equation [Hornung, 1997]. | | |
| 369 | These systems could, in principle, be upscaled to derive averaged Darcy's laws on a much | | |
| 370 | larger scale. However, in this paper our focus is in obtaining an estimate of the hydraulic | | Deleted: we are interested |
| 371 | properties of soils based on their pore structure. Hence, we neglect these larger scale features | | |
| 372 | but emphasise that they could be included through an additional level of upscaling. | | |
| | | | |
| 373 | | | |
| 374 | As we are able to segment the air and water separately from the CT images, the fluid dynamics | | |
| 375 | can be greatly simplified. Rather than focusing on the moving interface between each phase, | | Deleted: consider |
| 376 | we consider the relatively slow, flow of water about a fixed interface. The resulting equations | | |
| 377 | are introduced in the appendix. We further simplify the equations by assuming that the non- | | |
| | | | |
| 378 | wetting phase, in this case air, is stationary. This assumption is valid assuming that the air | | |
| 379 | phase is disconnected. If this is not the case then the movement of the air effectively lubricates | | |
| 380 | the movement of water resulting in an increase in the hydraulic conductivity. This approach is | | |
| 381 | valid assuming that the pressure gradients are sufficiently low, such that the interface remains | | |
| 382 | fixed, and that the non-wetting phase is not connected, hence, the trapped non-wetting phase | | |
| 383 | has zero average velocity. | | |

393 Strictly speaking the theory of homogenization requires the soil structure to be periodic. Clearly 394 for real soil samples this is not the case. This is overcome by enforcing an apparent image based periodicity either by translation or reflection of the CT image (Figure 1). In this paper 395 396 reflection was chosen as it simplifies the resulting calculations and does not introduce 397 discontinuities in the soil structure. The error induced by enforcing periodicity is that the 398 geometry considered numerically is now fully periodic rather than quazi-periodic and does not 399 truly represent the imaged soil structure. To overcome this, different size REVs were taken 400 from the segmented .stl files, see Figure 1. Specifically, the 6 cubes which were segmented 401 from each scan were of the same volume $V_m = 54.9 \text{ mm}^3$, and were assumed to be sufficiently 402 large that the soil properties would have converged. The REVs sampled from the six cubes 403 were of volume $V = V_m/(2^j)$, where j is a positive integer in the range 0 to <u>10</u> such that the 404 smallest volume we consider is 0.053, mm³ and the largest is V_m . As j is decreased and, hence, 405 the size of the REV is increased, the relative size of the errors induced by the reflection 406 decreases. Similarly as the REV size increases, the hydraulic properties of the subsample will, 407 in principle, converge to the hydraulic properties of the soil.

| Deleted: n |
|------------|
| Deleted: n |
| Deleted: 8 |
| Deleted: 2 |
| Deleted: n |
| |

408

409 A rigorous analysis of equations governing fluid flow through soil is given in [*Daly and Roose*, 410 2014]. Here we provide a brief description of the theory in the applied context with further 411 details given in the appendix. We consider a sample of soil which is large with respect to the 412 REV size. Specifically if the REV is a small cube with side length L_y and the large sample we 413 are interested in has characteristic length L_x then we require that the ratio of these two lengths 414 is small, *i.e.*, $\epsilon = L_y/L_x \ll 1$. For typical pore sizes observed in soil, the viscous forces 415 dominate [*Fowler*, 1997]. Hence, we may consider the Stokes limit of the Navier-Stokes

421 equations where all inertial terms are neglected. Mathematically the macroscopic hydraulic 422 conductivity, which is valid for the whole soil column, is obtained in two steps. First, it is 423 shown, see appendix for details, that <u>pressure</u> variations across the <u>REV</u> of size ϵ will induce 424 <u>a water</u> velocity <u>also</u> of size ϵ . Secondly, a set of equations are derived which allow the 425 pressure driven fluid velocity to be determined based on the soil (Figure 1). Finally, the average 426 velocity over the REV is used to determine a Darcy's law which is independent of ϵ . This value 427 is valid for the bulk soil and describes fluid driven by an external pressure gradient, see [Daly 428 and Roose, 2014]

$$\boldsymbol{u} = -\mathcal{K}(\boldsymbol{\nabla} p_0 - \rho g \hat{\boldsymbol{e}}_z), \tag{3}$$

429 where ρ is the fluid density ($\rho = 10^3$ kg m⁻³ in the case of water), g = 9.8 m s⁻² is the 430 acceleration due to gravity, p_0 is the applied pressure, **u** is the volume averaged water velocity 431 and \mathcal{K} is the relative permeability (in the general case a tensor) which has components defined 432 as

$$\mathcal{K}_{jk} = \frac{L_y^2}{\mu} \int_{\Omega_w} \hat{\boldsymbol{e}}_j \cdot \boldsymbol{\nu}_k^w \, dy. \tag{4}$$

433 Here $\hat{\boldsymbol{e}}_j$, for j = x, y, z is a unit vector in the *j*-th direction and $\boldsymbol{\nu}_k^w$ is the local velocity. 434 Assuming that the air velocity is slower than the water velocity then $\boldsymbol{\nu}_k^w$ satisfies the cell 435 problem

 $\boldsymbol{\nabla} \cdot \boldsymbol{\sigma}_{k}^{w} - \boldsymbol{\nabla} \boldsymbol{\pi}_{k}^{w} = \hat{\boldsymbol{e}}_{k}, \qquad \qquad \boldsymbol{x} \in \Omega_{w}, \quad (5a)$

$$\boldsymbol{\nabla} \cdot \boldsymbol{\nu}_k^w = 0, \qquad \qquad \boldsymbol{x} \in \Omega_w, \quad (5b)$$

$$\boldsymbol{\nu}_k^w = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_s, \qquad (5c)$$

$$\boldsymbol{v}_k^w = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_{aw}, \quad (5d)$$

| -1 | Deleted: ' |
|----|--|
| | |
| -1 | Deleted: unit cell |
| - | Deleted: only affect the average water |
| -1 | Deleted: by a quantity |

440 where $\sigma_k^w = (\nabla v_k^w) + (\nabla v_k^w)^T$, π_k^w is the local pressure correction due to the microscale 441 geometry, the superscript *w* denotes the water phase, Ω_w , Γ_s and Γ_{aw} denote the water domain, 442 the soil boundary and the air-water interface respectively. Physically this can be thought of as 443 calculating the fluid velocity subject to a unit pressure gradient. As the equations are linear 444 Darcy's law follows by multiplying the result by the desired pressure gradient.

445

Equations (5) were solved numerically on each subsample obtained from the CT images using 446 447 OpenFOAM, an open source Computational Fluid Dynamics toolbox running on IRIDIS, the 448 High Performance Computing Facility at the University of Southampton. The hydraulic 449 conductivity is then calculated as the average water velocity due to gravity. Results were 450 obtained for each soil sample using the method illustrated in Figure 1. The 6 cube surface 451 meshes, generated from each soil core, were repeatedly sampled to obtain 3D REVs of 452 increasing size. The result is a set of hydraulic conductivity calculations which we expect to converge to the true hydraulic conductivity of the soil, at each point along the WRC, as the 453 454 sub-volume size is increased.

455

456 *3.5. Statistical analysis*

The results obtained directly from the CT images were analysed by general analysis of
variance (ANOVA) containing soil type and matric potential and all possible interactions
as explanatory variables using Genstat 15.1 (VSN International, UK).

460

461 4. Results & Discussion

463 4.1 Hydraulic properties

464

The clay soil contained an average stone volume of 0.2 cm³ whereas the average stone volume for the sand soil was 5.5 cm³ (total soil volume was 55 cm³). Therefore although field structured soil was able to retain water for longer, as shown by the curves from the conventional method (Figure 2), the influence of stones was not a consideration and the greater water holding capacity is attributed to the more complex pore network in the field structured soil.

470

471 There are clear differences between sieved soil and field structured soil (Figures 2 and 3). For 472 the field structured soil the imaging technique shows a good agreement with the conventional 473 methods with an average error of \leq 5% across the range of matric potentials considered. The 474 sieved soil responded more strongly to pressure change in comparison to the field structured 475 soil. However, the imaged sieved soil data did not show this trend, hence, there was quite a 476 large error of 9% at 0 kPa and as high as 65% at -75 kPa. This suggests that, for the field 477 structured samples, the segmentation procedure was successful at identifying the majority of 478 the water filled pores (WFPs).

479

It is somewhat surprising that the more homogeneous sieved soil is less well represented through the imaging technique than the field structured soil. However, we attribute this to the pore size distribution in the two soils. The field structured soil has a wider range of pore sizes than the sieved soil which contains macropores defined by the largest grain size. As the matric potential becomes increasingly negative, the water drains from smaller and smaller pores. In

| Deleted: samples | | |
|------------------|------|--|
| | | |
| Deleted: samples | | |
| | | |
| | | |
| | | |
| Deleted: is | | |
| | | |
| | | |

Deleted: less than

495 the case of the field structured soil this results in a gradual decrease in volumetric water content 496 with matric potential which the imaging technique can follow assuming the pore size is larger 497 than the image resolution. In the case of the sieved soil there is a reduced range of pore sizes 498 and the water quickly drains from the larger pores and remains trapped in a large number of 499 smaller pores. The result is that the volumetric water content drops quickly as the matric 500 potential is reduced and the imaging technique, which cannot resolve the smallest pores, fails 501 to capture this. We also note that the differences observed in the WRC between the two soil 502 types is smaller when measured using the imaging technique than using conventional methods. 503 This is again attributed to the finite resolution of the measurements and is analogous to the 504 increasing error observed as the saturation is decreased.

- 505
- 506

507 The hydraulic conductivity, which corresponds to the water release curves shown in Figure 2, 508 has been calculated by solving equations (5) for increasing subsample size. As the subsample 509 size was increased, the hydraulic conductivity converged to a fixed value which we interpret 510 as the macroscopic hydraulic conductivity (Figure 4). The sample size at which this occurred 511 was smaller for lower matric potentials. This is attributed to the increased air-filled porosity 512 which decreases the contact area between the water and the soil. Hence, the effect of the 513 heterogeneous soil boundary is decreased and the overall homogeneity of the sample is 514 increased. We note that, as convergence is seen to occur at smaller sample sizes for lower 515 saturation, fewer simulations were run at these saturation values. This occurs at approximately 516 ¹/₄ of the sample volume for all matric potentials for both soils. We note that although the REV 517 volume is approximately the same for all soil types considered, the properties obtained from 518 this analysis are different for different soil types. This method therefore enabled the required

Deleted: the macroscopic

Deleted: values

| 521 | sample size for CT analysis of water flow in <u>these samples</u> to be determined, which was a cube | | Deleted: soil |
|-----|---|---|----------------------------|
| 522 | volume of 11 mm ³ . This sample was large enough for convergence of the calculated hydraulic | | |
| 523 | conductivity, meaning that the sample size contained an adequate volume of soil to capture the | | |
| 524 | averaged hydraulic properties on this scale. Therefore considering the averaging method used | < | Deleted: We note that, due |
| 525 | in this paper, the hydraulic conductivity is globally valid. This means that the representative | | Deleted: to |
| 526 | volume of 11 mm ³ is an appropriate representative volume element for the global hydraulic | | |
| 527 | conductivity of the soil samples used in this study. However, there may be significant features, | < | Deleted: se |
| 528 | such as cracks or heterogeneities in the soil, which are not captured in the 11 mm ³ volume. | | Deleted: s |
| 529 | Hence, care must be taken in applying these results on the field scale and an additional level of | | Deleted: some |
| 530 | upscaling may be required to capture the properties of these features, | | Deleted: . |

532 The method described in Section 3.4 and the appendix allowed us to also obtain the hydraulic 533 conductivity in unsaturated soils as well as in x, y and z directions. It was expected the flow 534 would be dominant in the z direction due to gravity, however (possibly due to the size of the 535 samples) we did not observe this. The calculated hydraulic conductivities are shown as a 536 function of matric potential in Figure 5. The calculated hydraulic conductivities and the 537 corresponding WRC have been fitted to the van Genuchten model for the WRC and the 538 unsaturated hydraulic conductivity [van Genuchten, 1980] using a non-linear least squares 539 method. We note that we have only done this fitting for the imaged data as we do not have 540 hydraulic conductivity measurements for the full range of matrix potentials using conventional 541 <u>measurements.</u> The volumetric water content θ is given by

$$\theta = (\theta_s - \theta_r) \left(\frac{1}{1 + (\alpha h)^n}\right)^m + \theta_r, \tag{6}$$

Deleted: that

where θ_s and θ_r are the saturated and residual volumetric water content respectively, *h* is the is the <u>matric_head</u>, m = 1 - 1/n and *n* and α are the van Genuchten parameters. The corresponding hydraulic conductivity is given by $K = K_{sat}k_r^{vg}$. Here K_{sat} is the saturated hydraulic conductivity and the relative hydraulic conductivity is given by

$$k_r^{\nu g} = \frac{\{1 - (\alpha h)^{n-1} [1 + (\alpha h)^n]^{-m}\}^2}{[1 + (\alpha h)^n]^{m/2}}.$$
(7)

We take θ_r to be negligible and fit the remaining parameters to the imaged data. The average saturated hydraulic conductivity and the fitted parameters: K_{sat} , θ_s , α and n are shown in Table 1. The fitted hydraulic conductivity and WRC, obtained using these parameters, are shown in Figure 5.

558 **Table 1. Fitted van Genuchten parameters**

| Soil | | Calculated $K_{sat} [cm \ s^{-1}]$ | Saturated volumetric content θ_s | water | α [<i>cm</i> ⁻¹] | n |
|------|--------|------------------------------------|---|-------|-------------------------------|------|
| Sand | 0.0013 | 0.0014 | 0.418 | | 0.153 | 1.71 |
| Clay | 0.0004 | 0.0010 | 0.423 | | 0.148 | 1.66 |

559

The hydraulic conductivity decreases as the matric potential decreases from 0 kPa to -75kPa (P<0.001) and is slightly larger in the sand soil compared to the clay soil. The van Genuchten model fits the imaged data well with a slight discrepancy in the WRC at 0 kPa (RMSE=0.016 for the clay soil and RMSE=0.022 for the clay soil). The experimentally measured hydraulic conductivity agreed well with the calculated value for the sand soil. However, the data compares less favourably in the case of the clay soil where the experimentally measured hydraulic conductivity is less than half that of the calculated value.

567

Deleted: hydraulic

Deleted: t

570 The differences observed for the clay soil between the experimentally measured hydraulic 571 conductivity and the calculated values are attributed to a combination of image resolution and 572 segmentation limitations. Typically clay soils have much smaller pores than sand soils, due to 573 the differences in particle size and as such will have a large number of pores which are 574 comparable with or below the imaging resolution used in this study. Further complications 575 include partial volume effects, which can cause errors in voxel classification, if the boundary 576 is between two phases with wide ranging attenuation values, such as air and rock [Ketcham 577 and Carlson, 2001]. This therefore could lead to an incorrect classification of voxels resulting 578 in either an overestimate or an underestimate of the pore space and pore size distribution due 579 to the effect it has on objects of differing sizes, which may explain why we have an 580 overestimation at the wet end, and underestimation at the dry end. As the calculated hydraulic 581 conductivity is large with respect to the measured value we expect that the pore space is being 582 over estimated in this case.

Deleted: , this Deleted: and

583

584 4.2 Pore characteristics

585 In order to obtain a better understanding of the pore scale processes which contribute to the 586 macroscopic hydraulic properties we consider the distribution of air and water within the soil 587 matrix on the pore scale. In order to quantify the air and water content we define Air Filled 588 Pores (AFPs) and Water Filled Pores (WFPs) as single connected regions of air or water 589 respectively. We also define the pore space as the union of all the AFPs and WFPs. Throughout 590 this paper when discussing connected regions of water and air we exclusively use this 591 terminology in keeping with the soil science literature. In addition we refer to individual pores 592 within the soil to define simply connected pathways between two distinct points within the 593 pore space. Typically, the pore space contains a single large WFP which contains over 50% of

| 596 | the water within the pore space and a large number of much smaller AFPs and WFPs. The |
|-----|--|
| 597 | connected WFPs are the main contributor to both the WRC and the hydraulic conductivity |
| 598 | calculations. However, insight may be gained into the wetting and drying behaviour of the |
| 599 | soils by considering the properties of the AFPs. <u>It is possible to determine the interfacial area</u> |
| 600 | between water and air phases [Costanza-Robinson et al., 2008]. However, as previous studies |
| 601 | have made the calculations based on porous media other than soil, this is not comparable to the |
| 602 | work undertaken in this study. In addition the majority of the previous work in soil [Falconer |
| 603 | et al., 2012; García-Marco et al., 2014; Tucker, 2014], refer directly to WFPs and AFPs as |
| 604 | such it is more meaningful in the context of the literature to consider the WFP and AFP surface |
| 605 | area. |

Formatted: Font color: Text 1

Formatted: Font color: Text 1
Deleted: researchers working in soil science

Formatted: Font color: Text 1

606

607 At 0 kPa we have a residual AFP volume of approximately 6% of the total pore space, see 608 supplementary Figure 3. This volume corresponds to trapped air pockets which, due to the high 609 tortuosity of the soil structure, remain in the pore space at saturation. As the matric potential is made more negative, the total WFP volume decreases and the corresponding AFP volume 610 611 increases (Figure 6; P<0.001). In addition to the change in WFP and AFP volume, the total soil 612 volume is seen to increase by up to 10%. Whilst this may, in part, be attributed to segmentation 613 issues and partial volume effects, it is also likely that changes in soil structure are responsible 614 for this apparent increase. The total AFP volume and the corresponding AFP surface area did 615 not vary significantly across the different soil types (sand and clay). However, the average 616 volume and the corresponding surface area of an individual AFP averaged across all matric potentials shows significant variation across soil types (P<0.001) with average AFP volume of 617 0.00115 mm³ in the clay soil compared with 0.00163 mm³ in the sand soil and with average 618 AFP surface area of 0.0109 mm² in the clay soil and 0.0182 mm² in the sand soil. This greater 619 surface area corresponds to a much greater number of AFPs at -75 kPa in the clay soil (104 620 23 pores/mm³) than the sand soil (55 pores/_mm³), (P<0.05). The average pore thickness decreased significantly with decreasing matric potential (Figure 7; P<0.001), from an average of 0.030 mm at 0 kPa to 0.026 mm at -75 kPa. There was no significant difference between soil types. At 0 kPa the average pore thickness for the clay soil was 0.027 mm compared to 0.033 mm for sand. At -75 kPa the average pore thickness for the clay and the sand soils was just 0.026 mm.

628

629 To highlight the differences in the soil types we classify the AFPs as air filled macro (> 100 630 μ m), air filled meso (30 - 100 μ m) and air filled micropores (21 - 30 μ m), see supplementary 631 Figure 4. This classification is based on the pore diameter, *i.e.* the maximum sphere diameter 632 which can fit inside the pore. The air filled micropore range is <u>limited</u> by the achievable 633 resolution based on our estimation of image noise (> 2 voxels). As the matric potential is 634 decreased, the total number of AFPs classified into each category changes with an overall 635 increase in the number of air filled macropores seen in the case of the sand soil. In the sand soil there is a linear increase in the percentage of air filled macropores with soil drainage, this 636 637 was expected due to the high number of macropores throughout the sand structure, which is 638 typically more homogenous compared to the clay. The clay soil had a less regular drainage 639 pattern than the sand soil. There is a linear increase in the air filled micropore percentage as 640 the clay dried. However, the percentage of air filled macropores is quite irregular and can be 641 attributed to the occurrence of crack formation which is more likely in clay soil. The average 642 pore circularity of the AFPs, equation (2), also increased as matric potential decreased. At -75 643 kPa the AFP space was comprised of pores with an average circularity of 0.78 compared to a 644 circularity value of 0.72 at 0 kPa (P<0.001). Our results also show that at drier matric potentials 645 the shape of the air and water filled pores become increasingly rounded possibly linked to air bubble-style pore formation. This measurement enables us to quantify the influence of pore 646

Deleted: per
Deleted: per

Deleted: It is possible to determine the interfacial area between water and air phases [*Costanza-Robinson et al.*, 2008], however as previous studies have made the calculations based on glass beads and pure sand mixtures, this is not comparable to the work undertaken in this study. However, further investigation into this measurement for porous media with two fluid flows would be of interest. Our work agrees with Kibbey [2013], in that microscopic surface roughness is likely to have a relatively small effect on the accuracy of the fluid flow at the air and water boundaries providing that the surface scale of the surface roughness is sufficiently small [*Daly and Roose*, 2014]. This means our imaging resolution should not be a limiting consideration on the surfaces obtained [*Brusseau et al.*, 2010]. ¶

Deleted: determined

| Deleted: , | |
|----------------------|--|
| Deleted: t | |
| Deleted: gives | |
| Deleted: a | |
| Deleted: ication | |
| Deleted: of | |
| Deleted: drainage on | |

| 669 | shape on soil drainage, However we note this is only a single measure and further descriptors |
|-----|--|
| 670 | that account for the shape of the soil porous architecture in 3D are required to advance |
| 671 | understanding in this area., The 3D connectivity of the WFPs decreased with decreasing matric |
| 672 | potential (P<0.05), pore connectivity was significantly greater in the clay soil at all matric |
| 673 | potentials (P<0.01). The differences in the AFP structure in the two soil types are indicative |
| 674 | of the soil structure. The clay soil contains a large number of micro-pores which corresponds |
| 675 | to the large number of air filled micropores trapped within the soil structure. In contrast the |
| 676 | sand soil contains a larger number of meso- and macro-pores causing the air to be contained in |
| 677 | relatively few, larger volumes. It is highly likely that the clay soil contained many pores that |
| 678 | were too small to be imaged at the achievable resolution <u>in this study</u> . |

| 1 | Deleted: , |
|------------------|--|
| 1 | Deleted: h |
| $\left(\right)$ | Deleted: are urgently required for this type of work |
| | |
| ſ | Deleted: |

| 679 |
|-----|
|-----|

680 5. Conclusions

681

| 682 | In this paper we have used a combination of CT imaging and mathematical modelling to derive |
|-----|--|
| 683 | the WRC and unsaturated hydraulic conductivity in contrasting soil textures (<i>i.e.</i> clay and sand) |
| 684 | and structures (i.e. sieved and field structured soil). The ability to non-destructively scan the |
| 685 | soil cores and segment the water and air filled pores from the soil matrix combined with the |
| 686 | mathematical modelling have provided a unique insight into the WRC and hydraulic properties |
| 687 | of contrasting soils. A comprehensive study of the hydraulic properties of different soil types |
| 688 | based on a <u>quantitative</u> visual assessment of the soil structure has been carried out across a |
| 689 | range of different saturation values. The results predict the increase in hydraulic conductivity |
| 690 | with saturation and highlight the structural basis for the differences between sand and clay |
| 691 | soils. |

692

Deleted: the

Deleted: more

699 The data obtained via CT imaging allows us to visualise the soil structure in 3D and, hence, to 700 measure the effects of pore geometry on the WRC. Using the scanned geometry combined with 701 detailed mathematical modelling, the unsaturated hydraulic conductivity and, hence, hydraulic 702 conductivities were obtained at the precise measured matric potentials. These values are not 703 easily measured in the laboratory through experimentation alone. Using the measured saturated 704 hydraulic conductivity and typical soil parameters we have compared the computed values 705 against the van Genuchten model. The simulated values compared well with the measured 706 saturated hydraulic conductivity values. The calculated hydraulic properties of the clay soil 707 against the van Genuchten model compare well. However, in the case of the sand soil, the 708 calculated values are lower than those obtained using the van Genuchten model. This 709 highlights the potential structural differences between two soils of a particular <u>textural</u> class 710 and the potential role played by the micro-porous structure of the aggregates which are 711 currently below the imaging resolution of CT for this sample size.

712

722

713 The combination of CT imaging and modelling provides a new level of understanding of the 714 role that structure plays in the averaged properties of soil. The WRC has been obtained via CT 715 imaging and provides a detailed geometric representation of how the water is retained in pores 716 of, different sizes. A downside to the imaging approach is the time investment required to 717 collect the data. However, this is comparable to the conventional laboratory method as the 718 majority of time is spent allowing the sample to equilibrate. However, this detailed information 719 on the pore-scale architecture represents a significant development in our ability to study soil 720 systems which will continue to advance pore scale modelling by providing three dimensional 721 geometries against which the numerical models can be tested [19].

Deleted: structural

Deleted: used in this paper

| -{ | Deleted: the |
|----|-----------------|
| -{ | Deleted: d pore |
| Y | Deleted: The |

728 6. Acknowledgements

| 730 | The authors acknowledge the use of the IRIDIS High Performance Computing Facility, and |
|-----|--|
| 731 | associated support services at the University of Southampton, in the completion of this work. |
| 732 | This project was funded by BBSRC BB/J000868/1, a collaborative project between |
| 733 | Southampton and Nottingham, PI and overall lead Roose. All reconstructed scan data will be |
| 734 | available on request by emailing <u>microct@nottingham.ac.uk</u> . The authors extend their thanks |
| 735 | to the anonymous reviewers for constructive feedback on their manuscript. |

| 737 | Table A1. Values of parameters used in numerical calculations |
|-----|---|
| | |

| Constant | Value | Units | Description |
|----------------------|-----------------------|------------------------------------|--|
| ρ^w | 10 ³ | kg m ⁻³ | Density of water |
| ρ^a | 1.2 | kg m ^{−3} | Density of air |
| μ^w | 10 ⁻³ | | Viscosity of water |
| μ^a | 20×10^{-6} | kg m ⁻¹ s ⁻¹ | Viscosity of air |
| \widetilde{g} | 9.8 | m s ⁻² | Acceleration due to gravity |
| r_y | 100×10^{-6} | m | Typical pore radius |
| L_y | 10 ⁻³ | m | Typical size of microscale geometry |
| L_x | 10 ⁻¹ | m | Typical size of macroscale geometry |
| $\widetilde{\gamma}$ | 7.28×10^{-2} | kg s ⁻² | Surface tension |
| Ñ | 10 ⁴ | m ⁻¹ | Curvature |
| ϵ | 10 ⁻² | | Ratio of geometry sizes |
| κ | 2.97×10^{2} | | Scaled surface tension-curvature product |
| g | 1 | | Scaled gravitational force |
| δ_u | 0.16 | | Typical velocity ratio |
| δ_p | 8.33 | | Typical pressure ratio |

739 Appendix

- 740 The starting point is the non-dimensional Stokes equations using the scaling given in [Daly and
- 741 Roose, 2014]. The dimensional variables, denoted with a ~, are scaled using

$$\begin{split} \boldsymbol{v}^{w} &= \frac{4\mu^{w}}{\rho^{w}\tilde{g}r_{y}^{2}} \, \tilde{\boldsymbol{v}}^{w}, \qquad \qquad p^{w} = \left(\frac{L_{x}}{L_{y}}\right) \frac{4L_{y}}{\rho^{w}\tilde{g}r_{y}^{2}} \, \tilde{\boldsymbol{p}}^{w}, \\ \boldsymbol{v}^{a} &= \left(\frac{L_{x}}{L_{y}}\right) \frac{4\mu^{a}}{\rho^{a}\tilde{g}r_{y}^{2}} \, \tilde{\boldsymbol{v}}^{a}, \qquad \qquad p^{a} = \left(\frac{L_{x}}{L_{y}}\right)^{2} \frac{4L_{y}}{\rho^{a}\tilde{g}r_{y}^{2}} \, \tilde{\boldsymbol{p}}^{a}, \\ t &= \left(\frac{L_{x}}{L_{y}}\right) \frac{\rho^{w}r_{y}^{2} \, \tilde{g}}{4\mu^{w}L_{y}} \, \tilde{t}, \end{split}$$

- 742 where v^w and v^a are the water and air velocities, p^w and p^a are the water and air pressures, t
- rise the dimensionless time and the remaining parameters are listed in table A1 and the nondimensional constants are

| $\kappa = \left(\frac{L_y}{L_x}\right) \frac{4L_y \tilde{\gamma}}{\rho^w r_y^2 \tilde{g}} \tilde{\kappa},$ | $\boldsymbol{g} = \frac{\boldsymbol{\hat{e}}_{x} L_{y}^{3}}{r_{y}^{2} L_{x}},$ | $\delta_u = \left(\frac{L_y}{L_x}\right) \frac{\rho^w \mu^a}{\rho^a \mu^w},$ | $\delta_p = \left(\frac{L_y}{L_x}\right) \frac{\rho^w}{\rho^a},$ |
|--|--|--|--|
|--|--|--|--|

Typical values for the non-dimensional numbers are given in table A1. The resulting non-dimensional Stokes equations are:

$$\begin{split} \epsilon \nabla \cdot \sigma^{w} - \nabla p^{w} &= \epsilon g & \qquad \qquad x \in \Omega_{w}, \quad \text{(A1a)} \\ \epsilon \nabla \cdot \sigma^{a} - \nabla p^{a} &= \epsilon^{2} g & \qquad \qquad x \in \Omega_{a}, \quad \text{(A1b)} \end{split}$$

$$\epsilon \phi \,\frac{\partial S^w}{\partial t} + \boldsymbol{\nabla} \cdot \boldsymbol{\nu}^w = 0, \qquad \qquad \boldsymbol{x} \in \Omega_w, \quad (A1c)$$

$$\epsilon \phi \frac{\partial S^a}{\partial t} + \delta_u \nabla \cdot \boldsymbol{v}^a = 0, \qquad \qquad \boldsymbol{x} \in \Omega_a, \quad (A1d)$$

$$\boldsymbol{v}^{w} = 0, \qquad \boldsymbol{v}^{a} = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_{s}, \qquad (A1e)$$

$$\widehat{\boldsymbol{n}} \cdot \boldsymbol{v}^{w} = 0, \qquad \widehat{\boldsymbol{n}} \cdot \boldsymbol{v}^{a} = 0,$$
 $\mathbf{r} \in \Gamma$
(A1g)
 $\mathbf{r} \in \Gamma$

$$\hat{\boldsymbol{\tau}} \cdot [\boldsymbol{v}^{w} - \delta_{u} \boldsymbol{v}^{a}] = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_{aw}, \quad (\Pi_{g})$$

$$\widehat{\boldsymbol{n}} \cdot \left[(\epsilon \sigma^w - lp^w) - \delta_p (\epsilon \sigma^a - lp^a) \right] = \widehat{\boldsymbol{n}} \kappa, \qquad \qquad \boldsymbol{x} \in \Gamma_{aw}, \quad (A1h)$$

747 combined with periodic boundary conditions in the x y and z directions. To simplify the 748 problem we notice that $\delta_u^{-1} < 1$ and $\delta_p < 1$ and, therefore, they can be neglected to first 749 approximation. The result is that the air and water velocities decouple we need only consider 750 the flow of water through the soil. The air velocity could in principle be calculated as a 751 perturbation of order δ_u which in turn would create a water velocity perturbation of order 752 δ_u/δ_p . However, we expect that this perturbation will be small with respect to the uncertainty 753 in the segmentation and the temperature dependent variations of the water viscosity. The 754 simplified equations are:

$$\begin{split} \epsilon \nabla^2 \boldsymbol{v}^w - \boldsymbol{\nabla} p^w &= \epsilon \boldsymbol{g} & x \in \Omega_w, \quad (A2a) \\ \boldsymbol{\nabla} \cdot \boldsymbol{v}^w &= 0, & x \in \Omega_w, \quad (A2e) \\ \boldsymbol{v}^w &= 0, & x \in \Gamma_s, \quad (A2f) \\ \boldsymbol{v}^w &= 0, & x \in \Gamma_{aw}, \quad (A2g) \end{split}$$

We expand the gradient operator $\nabla = \epsilon \nabla_x + \nabla_y$ and look for a power series solution to equations (A4) of the form

$$\boldsymbol{v}^{w} = \boldsymbol{v}_{0}^{w} + \boldsymbol{\epsilon} \boldsymbol{v}_{1}^{w} + \boldsymbol{0}(\boldsymbol{\epsilon}^{2})$$
(A3a)
$$\boldsymbol{p}^{w} = \boldsymbol{p}_{0}^{w} + \boldsymbol{\epsilon} \boldsymbol{p}_{1}^{w} + \boldsymbol{0}(\boldsymbol{\epsilon}^{2})$$
(A3b)

Substituting equations (A3) into equations (A2) and retaining terms $O(\epsilon^0)$ we obtain $\nabla_y p_0^w = 0$, *i.e.*, the largest component of the pressure is constant over the microscale. Expanding to

 $0(\epsilon^1)$ we effectively convert the leading order pressure drop into a body force and obtain

760
$$\boldsymbol{\nu}_0^w = \sum_{k=1}^3 \boldsymbol{\nu}_k \partial_{x_k} p_0^w$$

761 Where $\boldsymbol{\nu}_k$ satisfy the cell problem

$$\nabla_y^2 \boldsymbol{\nu}_k - \nabla_y \pi_k^w = \hat{\boldsymbol{e}}_k, \qquad \qquad \boldsymbol{x} \in \Omega_w, \quad (A4a)$$

$$\boldsymbol{\nabla}_{\boldsymbol{y}} \cdot \boldsymbol{\nu}_{k} = 0, \qquad \qquad \boldsymbol{x} \in \Omega_{w}, \quad (A4b)$$

$$\boldsymbol{\nu}_k = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_s, \qquad (A4c)$$

 $(\Delta 1f)$

Г

$$\boldsymbol{\nu}_k = \boldsymbol{0}, \qquad \qquad \boldsymbol{x} \in \boldsymbol{\Gamma}_{aw}, \quad (A4d)$$

$$\boldsymbol{\nu}_k, \pi^w_k$$
 periodic with period 1 (A4e)

Averaging the velocity over the unit cell we obtain the non-dimensional form of Darcy's lawfor the average velocity

764
$$\boldsymbol{u}_0^w = \int_{\Omega} \boldsymbol{\nu}_k \otimes \hat{\boldsymbol{e}}_k \, dy \, (\boldsymbol{\nabla}_{\!\! \mathbf{x}} \boldsymbol{p}_0^w + \boldsymbol{g})$$

which in dimensional form is equation (3) and (4) in the main paper.

As discussed in the main text we impose periodicity via reflection of the geometry about the x, y and z axis. The result is that the velocity is, for the *k*-th cell problem, the pressure correction π_k^w is even odd in the direction x_k and even in the direction x_j for $j \neq k$. Similarly we find that the *k*-th component of the velocity, $\hat{\boldsymbol{e}}_k \cdot \boldsymbol{v}_k$ is even in all directions. The remaining velocity components, $\hat{\boldsymbol{e}}_j \cdot \boldsymbol{v}_k$ for $j \neq k$, are odd in the directions x_k and x_j , however, they are even in the direction x_p for $p \neq k$ and $p \neq j$. Specifically the resulting boundary equations and boundary conditions are:

$$\nabla_y^2 \boldsymbol{\nu}_k - \nabla_y \pi_k^W = \hat{\boldsymbol{e}}_k, \qquad \qquad \boldsymbol{x} \in \Omega_w, \quad (A5a)$$

$$\boldsymbol{\nabla}_{\boldsymbol{y}} \cdot \boldsymbol{\nu}_{k} = 0, \qquad \qquad \boldsymbol{x} \in \Omega_{\boldsymbol{w}}, \quad (A5b)$$

$$\boldsymbol{\nu}_k = 0, \qquad \qquad \boldsymbol{x} \in \boldsymbol{\Gamma}_s, \qquad (A5c)$$

$$\boldsymbol{\nu}_k = 0, \qquad \qquad \boldsymbol{x} \in \Gamma_{aw}, \quad (A5d)$$

$$\pi_{k}^{w} = 0, \ \frac{\partial}{\partial x_{k}} (\hat{\boldsymbol{e}}_{k} \cdot \boldsymbol{v}_{k}) = 0, \ \hat{\boldsymbol{e}}_{j} \cdot \boldsymbol{v}_{k} = 0, \ j \neq k \qquad \qquad \boldsymbol{x} \in \partial x_{k} \qquad (A5e)$$
$$\boldsymbol{x} \in \partial x_{k} \qquad (A5f)$$

$$\frac{\partial}{\partial x_j} \pi_k^w = 0, \ \frac{\partial}{\partial x_p} (\hat{\boldsymbol{e}}_p \cdot \boldsymbol{v}_k) = 0, \ \hat{\boldsymbol{e}}_j \cdot \boldsymbol{v}_k = 0, p \neq k, \ p \neq j$$

where ∂x_k is the boundary located at $x_k = 0$ and $x_k = 1/2$, ∂x_j is the union of the boundaries located at $x_j = 0$ and $x_j = 1/2$ for $j \neq k$.

775

776

777

778 **7. References**

- Aravena, J., M. Berli, S. Ruiz, F. Suarez, T. Ghezzehei, and S. Tyler (2014), Quantifying coupled deformation and water flow in the rhizosphere using X-ray microtomography and
- numerical simulations, *Plant and Soil*, 376(1-2), 95-110.
- Aravena, J. E., M. Berli, T. A. Ghezzehei, and S. W. Tyler (2011), Effects of Root-Induced
 Compaction on Rhizosphere Hydraulic Properties X-ray Microtomography Imaging and
- 785 Numerical Simulations, Environmental Science & Technology, 45(2), 425-431.
- Arbogast, T., and H. L. Lehr (2006), Homogenization of a Darcy–Stokes system modeling
 vuggy porous media, *Computational Geosciences*, 10(3), 291-302.
- Blunt, M. J. (2001), Flow in porous media—pore-network models and multiphase flow,
 Current opinion in colloid & interface science, 6(3), 197-207.
- 790 Blunt, M. J., B. Bijeljic, H. Dong, O. Gharbi, S. Iglauer, P. Mostaghimi, A. Paluszny, and C.
- Pentland (2013), Pore-scale imaging and modelling, *Advances in Water Resources*, 51, 197-216.
- Bryant, S., and M. Blunt (1992), Prediction of relative permeability in simple porous media,
 Physical Review A, 46(4), 2004.
- Bryant, S., D. Mellor, and C. Cade (1993a), Physically representative network models of
 transport in porous media, *AIChE Journal*, *39*(3), 387-396.
- 797 Bryant, S., P. King, and D. Mellor (1993b), Network model evaluation of permeability and
- ransport in Porous Media, 11(1), 53-70.
- 799 Clausnitzer, V., and J. W. Hopmans (2000), Pore-scale measurements of solute breakthrough
- using microfocus X-ray computed tomography, *Water Resources Research*, 36(8), 2067-2079.
 Costanza-Robinson, M. S., K. H. Harrold, and R. M. Lieb-Lappen (2008), X-ray
- microtomography determination of air- water interfacial area- water saturation relationships
 in sandy porous media, *Environmental science & technology*, 42(8), 2949-2956.
- Crestana, S., S. Mascarenhas, and R. S. Pozzi-Mucelli (1985), Static and dynamic 3
 dimensional studies of water in soil using computed tomographic scanning, *Soil Science*, *140*,
 326-332.
- Boly, K. R., and T. Roose (2014), Multiscale modelling of hydraulic conductivity in vuggy
 porous media, *Proceedings of the Royal Society A: Mathematical, Physical and Engineering Science*, 470(2162).
- 810 Doube, M., M. M. Kłosowski, I. Arganda-Carreras, F. P. Cordelières, R. P. Dougherty, J. S.
- Jackson, B. Schmid, J. R. Hutchinson, and S. J. Shefelbine (2010), BoneJ: Free and extensible
 bone image analysis in ImageJ, *Bone*, 47(6), 1076-1079.
- 813 Falconer, R. E., A. N. Houston, W. Otten, and P. C. Baveye (2012), Emergent Behavior of Soil
- Fungal Dynamics: Influence of Soil Architecture and Water Distribution, *Soil Science*, *177*(2),
 111-119 110.1097/SS.1090b1013e318241133a.
- 816 Fatt, I. (1956), The network model of porous media.
- 817 Ferreira, T. A. W. R., and W. Rasband (2011), The ImageJ User Guide, Version 1.45., 818 (http://rsbweb.nih.gov/ij/docs/user-guide.pdf).
- Fowler, A. C. (1997), *Mathematical models in the applied sciences*, Cambridge University
 Press, U.K.
- Bao, W., T. Ren, A. G. Bengough, L. Auneau, C. W. Watts, and W. R. Whalley (2012),
 Predicting Penetrometer Resistance from the Compression Characteristic of Soil, *Soil Science Society of America Journal*, *76*(2), 361-369.
- 64 García-Marco, S., S. R. Ravella, D. Chadwick, A. Vallejo, A. S. Gregory, and L. M. Cárdenas 65 (2014), Ranking factors affecting emissions of GHG from incubated agricultural soils, 66 (2014), Ranking factors affecting emissions of GHG from incubated agricultural soils, 67 (2014), Ranking factors affecting emissions of GHG from incubated agricultural soils,
- European Journal of Soil Science, 65(4), 573-583.
- 827 Gardner, W. H. (1965), Water Content, in Methods of Soil Analysis. Part 1. Physical and
- 828 *Mineralogical Properties, Including Statistics of Measurement and Sampling*, edited by C. A.
- 829 Black, pp. 82-127, American Society of Agronomy, Soil Science Society of America.

- Haugen, Å., N. Mani, S. Svenningsen, B. Brattekås, A. Graue, G. Ersland, and M. Fernø
 (2014), Miscible and Immiscible Foam Injection for Mobility Control and EOR in Fractured
- 832 Oil-Wet Carbonate Rocks, *Transport in Porous Media*, 104(1), 109-131.
- 833 Helliwell, J. R., A. J. Miller, W. R. Whalley, S. J. Mooney, and C. J. Sturrock (2014),
- Quantifying the impact of microbes on soil structural development and behaviour in wet soils,
 Soil Biology and Biochemistry, 74(0), 138-147.
- 836 Hornung, U. (1997), Homogenization and porous media, Springer, Berlin, Germany.
- Houston, A. N., W. Otten, P. C. Baveye, and S. Hapca (2013), Adaptive-window indicator
 kriging: A thresholding method for computed tomography images of porous media, *Computers & Geosciences*, 54(0), 239-248.
- Iassonov, P., T. Gebrenegus, and M. Tuller (2009), Segmentation of X-ray computed
 tomography images of porous materials: A crucial step for characterization and quantitative
- analysis of pore structures, *Water Resources Research*, *45*(9), W09415.
- Keller, J. B. (1980), Darcy's law for flow in porous media and the two-space method, paper
 presented at Nonlinear partial differential equations in engineering and applied science (Proc.
 Conf., Univ. Rhode Island, Kingston, RI, 1979), Dekker New York.
- Ketcham, R. A., and W. D. Carlson (2001), Acquisition, optimization and interpretation of X-ray computed tomographic imagery: applications to the geosciences, *Computers & Geosciences*, 27(4), 381-400.
- 849 Keyes, S. D., K. R. Daly, N. J. Gostling, D. L. Jones, P. Talboys, B. R. Pinzer, R. Boardman,
- I. Sinclair, A. Marchant, and T. Roose (2013), High resolution synchrotron imaging of wheat
 root hairs growing in soil and image based modelling of phosphate uptake, *New Phytologist*,
 198(4), 1023-1029.
- Mooney, S. J. (2002), Three-dimensional visualization and quantification of soil macroporosity and water flow patterns using computed tomography, *Soil Use and Management*, *18*(2), 142-
- and water now patterns using compated tomography, *son ose and management*, 16(2), 142855 151.
- Mooney, S. J., and C. Morris (2008), A morphological approach to understanding preferential
 flow using image analysis with dye tracers and X-ray Computed Tomography, *CATENA*, 73(2),
 204-211.
- Mooney, S. J., T. P. Pridmore, J. Helliwell, and M. J. Bennett (2012), Developing X-ray
 Computed Tomography to non-invasively image 3-D root systems architecture in soil, *Plant and Soil*, 352(1-2), 1-22.
- Panfilov, M. (2000), Macroscale models of flow through highly heterogeneous porous media,
 Springer.
- Pavliotis, G., and A. Stuart (2008), *Multiscale Methods: Averaging and Homogenization*,
 Springer.
- Ramstad, T., P. E. Oren, and S. Bakke (2010), Simulation of Two-Phase Flow in Reservoir
 Rocks Using a Lattice Boltzmann Method, *Spe Journal*, *15*(4), 923-933.
- Reinhart, K. G. (1961), The Problem of Stones in Soil-Moisture Measurement1, *Soil Sci. Soc. Am. J.*, 25(4), 268-270.
- Rogasik, H., J. W. Crawford, O. Wendroth, I. M. Young, M. Joschko, and K. Ritz (1999),
 Discrimination of soil phases by dual energy x-ray tomography, *Soil Science Society of*
- 872 America Journal, 63(4), 741-751.
- Rowell, D. L. (1994), *Soil science : methods and applications* Longman Scientific & Technical
 Prentice Hall.
- Taylor, H. M., M. G. Huck, B. Klepper, and Z. F. Lund (1970), Measurement of Soil-grown Roots in a Rhizotron, *Agron. J.*, 62(6), 807-809.
- Tippkötter, R., T. Eickhorst, H. Taubner, B. Gredner, and G. Rademaker (2009), Detection of
- soil water in macropores of undisturbed soil using microfocus X-ray tube computerized
 tomography (μCT), *Soil and Tillage Research*, *105*(1), 12-20.

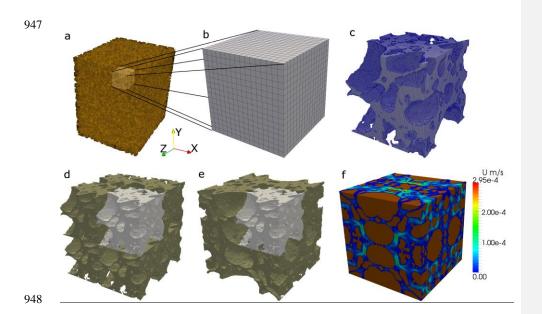
- Tucker, C. (2014), Reduction of air- and liquid water-filled soil pore space with freezing
 explains high temperature sensitivity of soil respiration below 0 °C, *Soil Biology and Biochemistry*, 78(0), 90-96.
- van Genuchten, M. T. (1980), A Closed-form Equation for Predicting the Hydraulic
 Conductivity of Unsaturated Soils1, *Soil Sci. Soc. Am. J.*, 44(5), 892-898.
- Wildenschild, D., J. W. Hopmans, M. L. Rivers, and A. J. R. Kent (2005), Quantitative
- Analysis of Flow Processes in a Sand Using Synchrotron-Based X-ray Microtomography,
 Vadose Zone J., 4(1), 112-126.
- 888 Wildenschild, D., C. M. P. Vaz, M. L. Rivers, D. Rikard, and B. S. B. Christensen (2002),
- Using X-ray computed tomography in hydrology: systems, resolutions, and limitations, *Journal of Hydrology*, 267(3–4), 285-297.
- 891 Zappala, S., J. R. Helliwell, S. R. Tracy, S. Mairhofer, C. J. Sturrock, T. Pridmore, M. Bennett,
- and S. J. Mooney (2013), Effects of X-Ray Dose On Rhizosphere Studies Using X-Ray
- 893 Computed Tomography, *PLoS ONE*, 8(6), e67250.

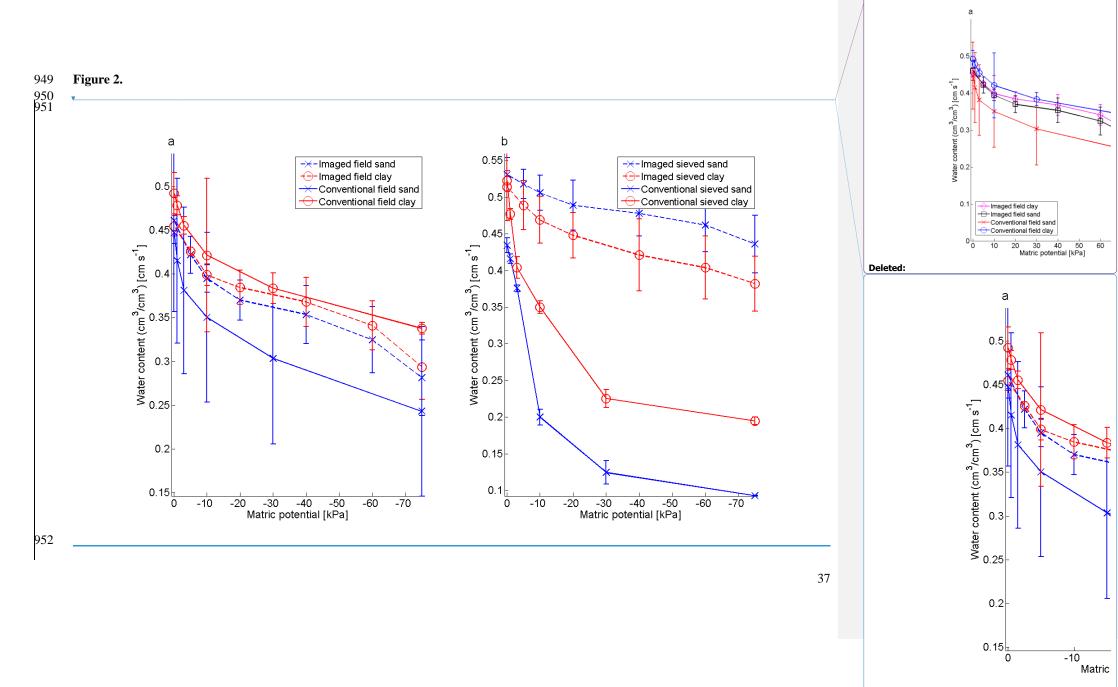
895

897 8. Figures

898 Figure 1. Outline of steps used in the subsampling, meshing and solution of cell 899 problem. Figures (a) and (b) show the subsampling of a 1.2 mm side length cube of the 900 segmented .stl file. Figure (c) shows the mesh generation. Figures (d) and (e) show the 901 generation of a truly periodic geometry through translation (d) and reflection (e), the original 902 volume mesh is shown in a lighter shade. Figure (f) shows the numerical solution for the local 903 velocity magnitude in the subsampled soil. 904 905 Figure 2. Water release characteristic of the sand and clay sieved (a) and field structured (b) 906 soils fitted to the van Genuchten (VG) curve. Error bars associated with histograms show one 907 standard deviation. Note the different scaling on the y axis for figures (a) and (b). 908 909 Figure 3. Greyscale images showing examples of field structured (a) & (b) and sieved (c) & 910 (d) clay (a) & (c) sand soil (b) & (d) at -75 kPa. Scale bar = 0.25 mm. 911 912 Figure 4. Hydraulic conductivity of field structured sand and clay soils averaged over all 913 directions for decreasing j corresponding to increasing volume. The dots show the result from 914 each of the cubic volumes, the lines show, the average. The corresponding saturated hydraulic Deleted: s conductivity measured for the sand and clay soils are 1.3×10^{-3} cm s⁻¹ and $0.4 \times$ 915 916 10^{-3} cm s⁻¹ respectively.

| 919 | Figure 5. Hydraulic conductivity of field structured sand and clay soils as a function of | | | |
|------------|---|------------|----------------------|--|
| 920 | matric potential. | | | |
| 921 | Figure 6. 3D core section of a sand (a) and clay (b) soil sample at the specific matric potentials | Deleted: ¶ | | |
| 922 | from saturation (left) to drier (right). Segmented phases are coloured brown (soil), blue (water | | | |
| 923 | filled pores) and black (air filled pores). Scale bar = 5 mm. | | | |
| 924 | | | | |
| 925 | Figure 7. 3D pore thickness heat maps for a representative sand (a-c) and clay (e-f) sample at | | | |
| 926 | 0 (a, d), -20 (b, e) and -75 (c, f) kPa. (g) total air filled pore volume (bars) and average individual | | | |
| 927 | pore volumes (lines) for sand and clay soil. Error bars associated with histograms show one | | | |
| 928 | standard deviation. | | | |
| 929 | | | | |
| 930 | | | | |
| 931 | | | | |
| 932 | | | | |
| 933 | | | | |
| 934 | | | | |
| 935 | | | | |
| 936 | | | | |
| 937 | | | | |
| 938 | | | | |
| 939 | | | | |
| 940 941 | | | | |
| 941 942 | Figure 1. | Deleted: ¶ | | |
| 742 | rigure 1. | ¶ | Page BreakPage Break | |

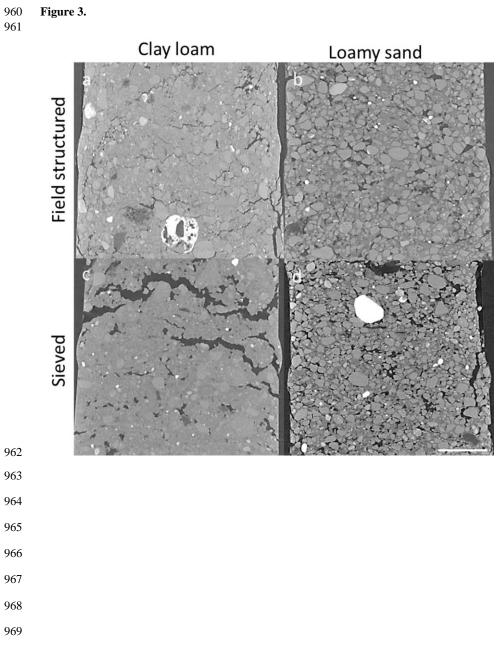


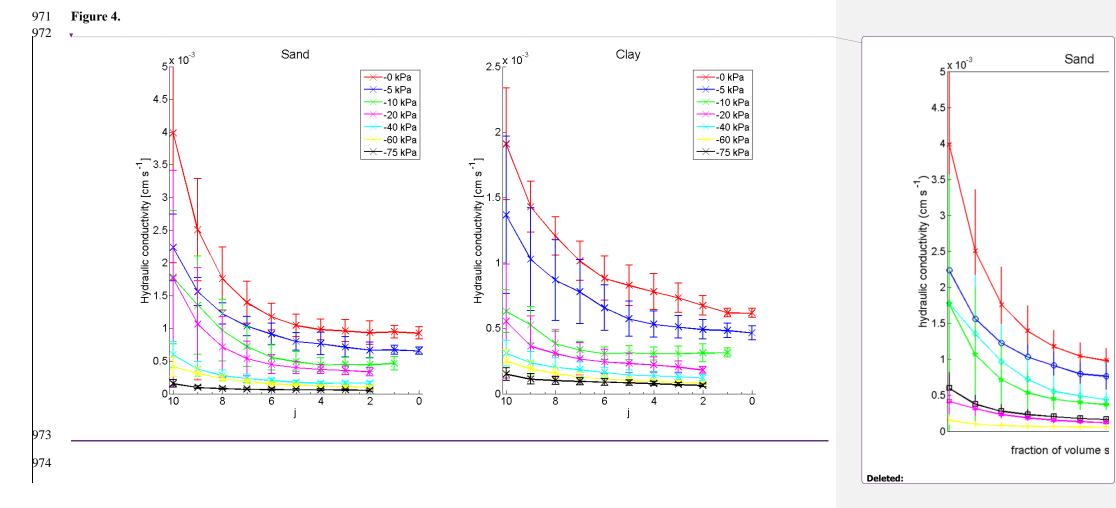


Deleted:

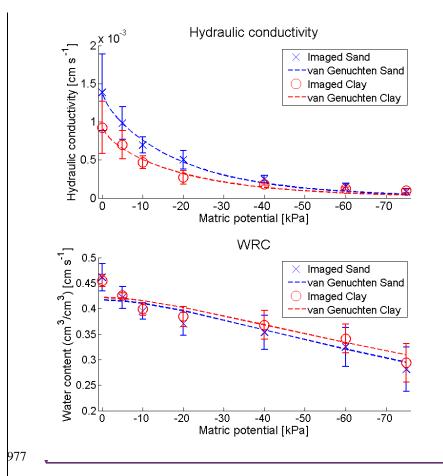
ted:

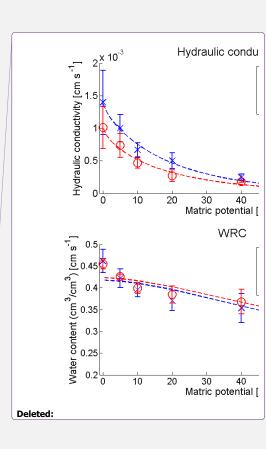
Deleted: ¶

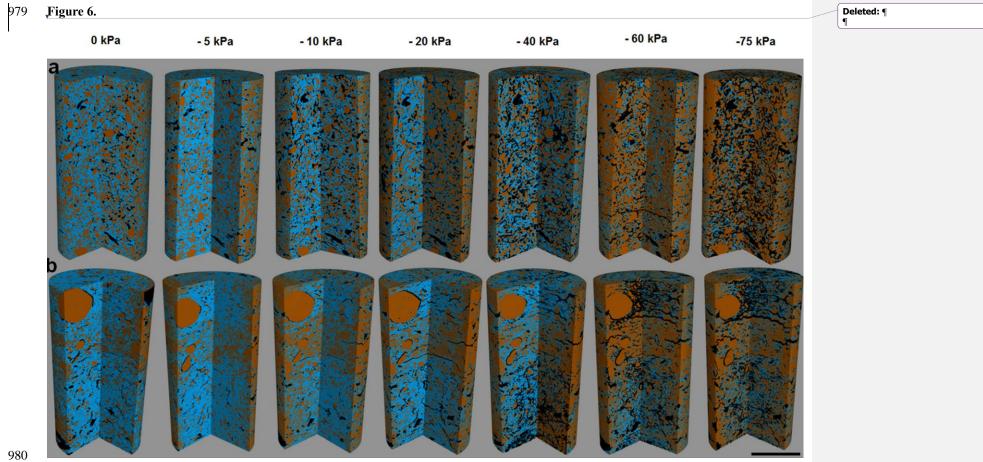




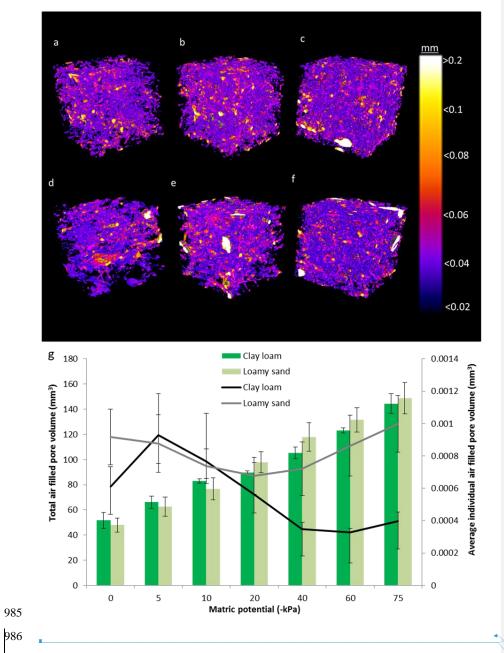












Deleted:

Formatted: Normal, No bullets or numbering
Formatted: Font: Bold