Real-time Electrocardiogram (ECG) signal analysis and Heart Rate determination in FPGA platform

# Manas Rakshit (213EE1293)



Department of Electrical Engineering, National Institute of Technology, Rourkela, Rourkela-769 008, Orissa, India. May, 2015.

# Real-time Electrocardiogram (ECG) signal analysis and Heart Rate determination in FPGA platform

A dissertation submitted in partial fulfilment of the requirements for the degree of

# Master of Technology

in

# **Electronic Systems and Communication**

by Manas Rakshit (Roll No: 213EE1293)

Under the Guidance of Prof. Prasanna Kumar Sahu



Department of Electrical Engineering, National Institute of Technology, Rourkela, Rourkela-769 008, Orissa, India 2014-2015 Dedicated to The Dreams and Sacrifices of my Dear Ones who Love me a Lot.



# Certificate

This is to certify that the thesis entitled "Real-time Electrocardiogram (ECG) signal analysis and Heart Rate determination in FPGA platform " by Manas Rakshit, submitted to the National Institute of Technology, Rourkela for the award of Master of Technology in Electrical Engineering, is a record of bonafide research work carried out by him in the Department of Electrical Engineering, under my supervision. I believe that this thesis fulfills part of the requirements for the award of degree of Master of Technology. The results embodied in the thesis have not been submitted for the award of any other degree elsewhere.

Place: Rourkela Date: **Prof. Prasanna Kumar Sahu** Associate Professor Department of Electrical Engineering

National Institute of Technology, Rourkela Rourkela-769 008, Orissa, India.

### Acknowledgment

Most real spirit is to achieve a goal through a way of perfection. The achievement which I have gain cannot be possible without the cooperation of numerous personalities.

I am very much thankful to various personalities who helps me a lot for structuring my thesis. At the outset, I would like to express my thanks to Prof. P.K. Sahu for his guidance, supervision during this research work. As a guide his advice always encourage me and helps me a lot to find out suitable way for successful completion of this work. His idea, observations help me to enrich my knowledge.

I am grateful to all the professors of our department for their advice, support , encouragement and valuable comments.

I also like to thanks Damodar Sir, Astik Sir, K.P.sir and S.K.M Sir . Yours advice, idea, friendly behaviours make this research work so important, I am truly indebted.

I also want to thank academic resources that I have got from NIT Rourkela. My sincere thanks to all technical and non technical staff members for their help and support.

I am grateful to my friends, without whom, this journey would not be this much pleasant.

I am also grateful to my family for their blessing, advice and moral support. I want to dedicate this work to them which could not be fulfil without their love and blessing.

Manas Rakshit

#### Abstract

Heart disease is one of the leading cause for death of people globally. According to a recent study by the Indian Council of Medical Research (ICMR), about 25 percent of deaths in the age group of 25- 69 years occur because of heart diseases. Electrocardiogram (ECG) is one of the primary tool for the treatment of heart disease. ECG is an important biological signal that reflects the electrical activities of the heart. A typical ECG signal consists of mainly five components namely P, Q, R, S and T wave. Amplitude and morphology of each component contains numerous medical information. The automated detection and delineation of each component in ECG signal is a challenging task in Bio-medical signal processing community.

In this research work, a four stage method based on Shannon energy envelope has been proposed in order to detect QRS complex in ECG signal. Peak detection of the proposed algorithm is amplitude threshold free. To evaluate the performance efficiency of the proposed method standard MIT-BIH arrhythmia ECG database has been used and get an average accuracy of 99.84%, Sensitivity 99.95% and Positive Predictivity value 99.88%.

To detect and delineate P and T waves, an algorithm based on Extended Kalman Filter (EKF) with PSO has been proposed. For performance examination, standard QT ECG database has been used. The proposed algorithm yields an average Sensitivity of 99.61% and Positive Predictivity of 99.00% for the ECG signal of QT database.

A long term automatic heart rate monitoring system is very much essential for standard supervision of a critical stage patient. This work also includes a field programmable gate array (FPGA) implementation of a system that calculate the heart rate from Electrocardiogram (ECG) signal. FPGA provides easy testability that allows faster implementation and verification option for implementing a new design. FPGA-based design can act as a bridge for converting from a software algorithm to a dedicated hardware design based on Application-specific integrated circuits (ASICs). In this work a five stages methodology using basic VHDL blocks has been implemented that can detect the heart rate from a typical ECG signal.

**Keywords:** Electrocardiogram (ECG), Extende Kalman Filter (EKF), Field Programmable Gate Array (FPGA), Particle Swarm Optimization (PSO), Shannon Energy, VHSIC Hardware Description Language (VHDL)

Acronym	n Description					
ECG	Electrocardiogram					
Na	Sodium					
Κ	Potasium					
SA Nde	Sinoatrial Node					
AV Node	Atrioventricular Node					
FPGA	Field-programmable Gate Array					
DRWC	Dominant Resceled Wavelet Coefficient					
FND	False Noise Detection					
FRD	False R Detection					
PSO	Particle Swarm Optimization					
EKF	Extended Kalman Filter					
SNR	Signal to Noise Ratio					
ASICs	Application Specific Integrated Circuit					
BPF	Band-pass Filter					
FIR	Finite Impulse Response					
IIR	Infinite Impulse Response					
Se	Sensitivity					
Acc	Accuracy					
DER	Detection Error Rate					
PPV	Positive Productivity					
ТР	True Peak					
FN	False Negative					
FP	False Positive					
VHDL	VHSIC Hardware Description Language					

# List of Acronyms

# Contents

Ce	ertifi	cate	i
Ac	knov	wledgment	ii
A۱	ostra	ct	iii
Li	st of	Acronyms	$\mathbf{v}$
Li	st of	Figures	vii
Li	st of	Tables	ix
1	Intr 1.1 1.2 1.3 1.4 1.5 1.6	PoductionIntroductionHuman Cardiac System and ECG signal generationECG signal componentsMotivationObjective of the thesisObjective of the thesisThesis Organization1.6.1Chapter 2: Literature Survey1.6.2Chapter 3: Proposed Algorithms1.6.3Chapter 4: Results and Discussion1.6.4Chapter 5: Conclusion, Future Scope and Publications	$     \begin{array}{c}       1 \\       2 \\       4 \\       4 \\       5 \\       5 \\       6 \\       6 \\       6 \\       6     \end{array} $
2	<b>Lite</b> 2.1 2.2	Prature SurveyQRS Complex Detection	<b>7</b> 8 9
3	<b>Pro</b> 3.1 3.2 3.3	posed AlgorithmsProposed Algorithm for QRS complex detection in ECG signal3.1.1 Data pre-processing	<b>10</b> 11 12 13 14 15 16 17 18 19 21 21
	ე.ე	3.3.1 Data Conversion	$\frac{21}{22}$

		3.3.2	Filtering	22
		3.3.3	R Peak Detection	23
		3.3.4	Heart Rate Detection	23
		3.3.5	System Synthesize Information	24
4	Res	ults ar	nd Discussion	<b>25</b>
	4.1	Experi	imental ECG Database	26
		4.1.1	MIT-BIH Arrhythmia Database	26
		4.1.2	QT Database	26
	4.2	Simula	ation Software	26
	4.3	Result	and Discussion for QRS Detection Algorithm	26
		4.3.1	Result and Discussion for P and T wave Detection and De-	
			lineation Algorithm	29
		4.3.2	Result and Discussion for Heart Rate Determination in FPGA	
			Platform	31
<b>5</b>	Con	clusio	ns, Future Scope and Disseminations	<b>34</b>
	5.1	Conclu	usions	35
	5.2	Future	e Scope	36
	5.3	Dissen	ninations	36
Bi	bliog	graphy		37

# List of Figures

$\begin{array}{c} 1.1 \\ 1.2 \end{array}$	Human Cardiac System.	$\frac{2}{3}$
1.3	ECG Signal Components.	4
3.1	Block Diagram of Proposed Algorithm	11
3.2	Comparison of energy value for different envelope method using normalized amplitude	13
3.3	Different Signal processing steps of peak estimation logic stage.	14
3.4	Total signal processing steps of the described method: (a) ECG data(Record 205). (b) Filtered signal. (c) Output of normalize operation. (d)Smooth Shannon energy envelope. (e) Differentiation of Shannon Energy envelope. (f) Output of square operation. (g) Output of moving average filter (h) True detected B-peaks (Bed	
	colour impulses).	15
3.5	Block diagram of proposed methodology for P and T waves detec-	
0.0	tion and delineation in ECG	16
3.6	Comparison of mean SNR improvements achieved in different input SNRs for BW removal based on two-stage moving window median filter(MD2), single stage moving window median filter(MD1), two	
	stage moving average filter(MA2), low pass filter(LP), band pass filter using poise stress database( $PPE$ )	16
37	Baseline wander removed ECG signal	$10 \\ 17$
3.8	Baseline wander removed ECG signal.	17
3.9	Phase assignment of ECG of sel103 QT database.	18
3.10	Valley point detection logic.	21
3.11	Block diagram of FPGA implementation of the band-pass filter	23
3.12	Device Utilization Summary of the proposed FPGA System	24
3.13	RTL of the proposed FPGA System.	24
4.1	Performance of the proposed method for Record 103 (Low ampli-	
	tude QRS complexes and baseline drift.)	27
4.2	Performance of the proposed method for Record 232 (Long pauses.)	29
4.3	Performance of the proposed method for Record 106 (Continuously	20
1 1	varying QRS complex and tall 1 wave.)	3U 91
4.4	P wave and T wave extraction for ECG signal selection (QT database).	31 21
4.5 4.6	Detection of B neak location and calculation of heart rate using	υI
J.U	Xilinx from 101 of MIT-BIH arrhythmia database	32
4.7	Placement of extracted peaks of the ECG signal with id 101 of	
	MIT-BIH arrhythmia database.	32

4.8	Detection of R peak location and calculation of heart rate using	
	Xilinx from 106 of MIT-BIH arrhythmia database	32
4.9	Placement of extracted peaks of the ECG signal with id 106 of	
	MIT-BIH arrhythmia database.	32
4.10	Detection of R peak location and calculation of heart rate using	
	Xilinx from 116 of MIT-BIH arrhythmia database	33
4.11	Placement of extracted peaks of the ECG signal with id 116 of	
	MIT-BIH arrhythmia database	33
4.12	Detection of R peak location and calculation of heart rate using	
	Xilinx from 203 of MIT-BIH arrhythmia database	33
4.13	Placement of extracted peaks of the ECG signal with id 203 of	
	MIT-BIH arrhythmia database	33

# List of Tables

1.1	Description of Components of ECG signal	4
4.1	Performance evaluation of R peak extraction algorithm on MIT-	
	BIH arrhythmia database ECG signal with the duration of 30 minutes.	28
4.2	Comparison of performance of our proposed method with other	
	methods for detecting R peaks using MIT BIH database	29
4.3	Comparison of the average Se and average PPV for all record of	
	QT ECG database with signal length 1 minute	30

Chapter 1 Introduction

# 1.1 Introduction

Electrocardiogram (ECG) is an important biological signal that reflects the electrical activities of heart system. A lot of cardiac decisions can be taken from the amplitude and morphology of a typical ECG signal [1]. ECG signal is produced by the movement of Na+ and K+ ions, which causes depolarization and repolarization into heart cell [2]. An ECG signal has a typical amplitude of 0.2 mv and to monitor ECG signal there is requirement of frequency range 0.1 to 120 Hz [3]. ECG signal can be collected by placing suitable electrodes at standard locations on the human skin. A particular ECG signal has mainly five components namely P, QRS complex and T wave. Every wave in ECG has a normal value of amplitude and duration [4]. Whenever there is any defect in heart system the normal morphology of these waves are changed and by detecting the change in ECG wave cardiac diseases are identified.

In order to monitor an ECG signal, two type methods are available. In manual detection method, ECG signal, taken from a patient body printed on a standard graph paper and checking visually clinician takes the decisions. This manual detection method is not suitable for a long-term monitoring system, and whenever we get an ECG from a patient body, a lot of noises accumulate with it, so proper detection is not an easy task. On the hand in automatic ECG monitoring system ECG signal is processed through a computer system that is suitable for long-term monitoring.

#### 1.2 Human Cardiac System and ECG signal generation

Human Cardiac system consists of several parts and heart is the central organ of the human cardiac system. Through cardiac system, total blood circulation process has been throughout the whole body. A pictorial diagram of human cardiac system has been described in Figure 1.1



Figure 1.1: Human Cardiac System.

A human heart is separated into two sections left and right, which are subdivided divided into two chambers, the upper chamber is known as atrium where the lower one is ventricle. The atriums are blood receiving chamber where ventricles are blood transmitting chambers. The atria, attached to ventricles by fibrous, non-conducting tissues that keep them electrically isolated [5]. The tricuspid valve isolates right atrium and right atrium, where mitral valve separates left atrium and left ventricle[6].

De-oxygen blood from the whole body is received to the right part by superior and inferior vena cava. Then the blood is passed into the right ventricle through the tricuspid valve and from that it is passed to lungs through pulmonary atria. Oxygen filled blood is collected from lungs through the pulmonary vein to the left atrium that transferred to the left ventricle through mitral value. Then this purified blood is spreaded throughout the whole body through the aorta. Now during this cardiac process positive ions Na+ in blood flowing through the cell membrane of the heart cell, so a voltage potential has been created between heart inside cells and the outside cells [7]. This processÂăisÂăknown as depolarization. Again similar to depolarization, in repolarization positive ions K+ flowing out from the cell membrane and creates a potential difference. When the potential difference is larger than the a threshold value the primary pacemaker of heart that is SA node produces an electrical pulse. This electric impulse travels to the right and left atrium causing them to contract and generates the first component of ECG that is the P-wave. After contraction of the atrium, the electrical pulse arrives at AV node that is responsible for contraction of the ventricle. This contraction of ventricles causes QRS complex. Then the signal is passed through His bundle and left and right Bundle Branches and spreaded through Purkinje fibre. This effect causes the depolarization of ventricle and generation of the T wave. The typical flow of this electrical signal has been described in Figure 1.2. By place in suitable electrodes in the standard locations of the human body, this ECG signal is collected and processed.



Figure 1.2: ECG Signal Flow.

# 1.3 ECG signal components

A typical ECG signal consists of mainly five components namely P wave, QRS complex and T wave. Figure 1.3 shows the components of ECG signal. Table1.1 presents a description of the components of a typical real ECG signal.



Figure 1.3: ECG Signal Components.

Table 1.1: De	escription	of Components	of ECG signal.
---------------	------------	---------------	----------------

Components Name	Description	Amplitude (mv)	Duration (Sec.)
P wave	Atrial delorization	0.10-0.20	0.12
PR Interval	Starting of P wave to end of QRS complex	-	0.20
QRS complex	Ventricle delorization	1.00-1.20	0.08
T wave	Ventricle repolarization	0.12-0.30	0.16
QT Interval	Starting of QRS complex to the end of T wave	-	0.40
R-R interval	One cardiac cycle	-	0.80

# 1.4 Motivation

ECG wave reflects the electrical activities of the heart. Every component of ECG signal has a particular morphology, whenever any problem causes into the heart the typical morphology of the ECG wave has been changed. In medical treatment, these changes are detected by cardiation and decisions have been taken [8]. Now as ECG is a non-stationary wave so to monitor visually is not an easy task for a clinician and also it is a time-consuming process. When a patient is in severe condition and requires long time monitoring, so it is not possible for a doctor for long time supervision. So an automated ECG monitoring system is required. Again, when an ECG wave is collected from a patient body a lot of noise such as electromagnetic noise, baseline wander noise, patient breathing and moving noise have been accumulated with it so it become a tedious work for a clinician to take important decision by only monitoring it visually. So a computer based

automated ECG monitoring system is required. Not only for an adult patient, ECG wave has a great importance to know the condition of fetal in the maternal abdomen. By processing the fetal ECG, the actual condition of fetal can be known [9],[10]. The above information clears that ECG signal has a great importance in medical science, and ECG signal processing is one the essential part of Biomedical signal processing. This information motivates me to work my research in this field.

# 1.5 Objective of the thesis

According to the motivational information, we get that design of an automatic ECG monitoring system is popular research work in the field of Biomedical Signal Processing. In this research work my primary focus is

- To design QRS detection algorithm without any amplitude threshold. The developed algorithm should require a low memory buffer and low processing time which are the basic characteristic of a real-time monitoring system. If we can detect R-peaks of an ECG signal then corresponding heart rate can easily calculated (HeartRate =  $\frac{60}{R-Rinterval}$  bpm). So we have to prepare our algorithm such that it can faithfully determine the heart rate from the ECG signal.
- Apart from QRS complex other waves (P and T waves) also contain cardiac information. My thesis work also includes designing an algorithm that can detect P and T waves and also delineate by finding ON and OFF of the P and T waves from a real ECG signal.
- In the present FGPA based system is a popular one. FPGA system creates the hardware environment. My work includes designing FGPA based heart rate detection from a real ECG signal.
- To determine the efficiency of my proposed algorithms I have validated my proposed algorithm with standard ECG signal. In my work, I have used standard MIT-BIH and QT database to validate my proposed algorithms.

# 1.6 Thesis Organization

Including this chapter this thesis consists of five chapters. The remaining thesis orientation is as follows:

#### 1.6.1 Chapter 2: Literature Survey

In this chapter the total literature survey of this work has been described. In order to get enough information about ECG wave signal processing, many literature review are undertaken. As my research are divided into twoÂăbasic parts, so literature review is also divided into twoÂăsection where first part consists information for detecting QRS complex, second one consists of information for detection of P and T-waves.

### 1.6.2 Chapter 3: Proposed Algorithms

In chapter 3 the implemented algorithms proposed in my thesis work have been described. This is also subdivided into three different parts to describe three proposed algorithms.

#### 1.6.3 Chapter 4: Results and Discussion

Here total experimental results have been described. In chapter also divided into three parts to show the performance of each algorithm separately. In result and discussion stage, the performance of proposed work has been compared with previously established works.

#### 1.6.4 Chapter 5: Conclusion, Future Scope and Publications

This is the last one. Here conclusive remarks and limitations of this work have been described. This part also contains the information about publications those have been made throughout this research. At last a brief future scope of this work has been described. Chapter 2 Literature Survey Since the last few year, ECG signal processing becomes a popular research topic in the field of biomedical signal processing. A number of research were taken by the different researcher in ECG signal processing. Few of these research idea enrich my knowledge to implement modified algorithms for processing of ECG. Here is the brief description of literature survey undertaken in this research work. As this research work has mainly three-part such as detection of QRS complex, P and T wave detection and delineation and last one FPGA implementation of the heart rate detection system, literature survey is divided as follows:

## 2.1 QRS Complex Detection

Pan and Tompkins (1985) [11] have proposed an algorithm for detection of QRS complex. This method is based on squaring and filtering process. According to this proposed algorithm raw ECG signal, has been passed through a low pass filter for noise extraction then differentiation and squaring operation have been performed. At last by typical peak detection operation R peaks are detected. This is one of the established QRS detection algorithms. Though it is a simple algorithm but accuracy is quite poor. Again as the peak detection is based on amplitude threshold do a suitable threshold value is required otherwise accuracy can be degraded.

Benitez et al. (2001) [12] have developed an algorithm for detection QRS complex using Hilbert Transform. This algorithm based on the zero crossing features of Hilbert transform. Primary steps of this method are filtering of raw ECG in order to remove noise, and then to get slope information first order differentiation has been performed. Hilbert Transform is used in order to detect peak locations. By applying this algorithm extraction of R peaks from large T, peaks is possible but this algorithm is quite complex. As Hilbert Transform is used here, so we have to go frequency domain and sampling of the signal are required, so a large amount of memory buffer is required.

Ghafffarl *et al.* (2008) [13] have proposed QRS detection algorithm in 2008. This algorithm is derived from the concept of the continuous wavelet transform. In order to emphasise QRS complex from other, he used dominant rescaled wavelet coefficient (DRWC). This method successfully detects QRS complex from long P and T peak signal, but accuracy degrades in few number of signals. The selected wavelet function for that data only suitable for that type of data morphology. If ECG morphology is changed, then the selected wavelet cannot give a better performance response. For random varying of the duration of QRS complex, the algorithm fails to detect QRS complex successfully.

Manikandan *et al.* (2012) [14] has proposed a new algorithm based on Shannon energy with Hilbert Transform. The primary stages of this algorithm as follows: first raw signal has been passed through a low pass filter for noise reduction then first ordered differentiation of the filtered signal has been performed to get slope information and remove low drift noise. After that Shannon energy envelope of the signal has been extracted. Here Shannon energy envelope is used in the place of squaring operation as it has benefits to amplify medium value components. If the square operation has been performed for low-value signal, then it is attenuated. After Shannon energy envelope extraction step, Hilbert Transform of the signal has been performed. Hilbert Transform has a particular characteristic to produce zero crossing at the position of peak values. Now according to zero crossing point cross ponding R peaks locations have been detected. Though this method has a better accuracy than the previous methods but for the long pauses signal it detects a large number of false peaks as true R-peaks. Again as there is Hilbert Transform, so we have to go for frequency domain where a large number of the memory buffer is required in order to sample the input signal, which not suitable in a real-time environment.

Zhu *et al.* (2013) [15] have proposed a QRS complex detection algorithm based on Shannon energy envelope. This amplitude based on amplitude and time decision criterion based. The primary steps of this algorithm, at the initial stage for noise filtering band pass filter is used. Then in order to get the slope information first order differentiation is performed. After that Shannon, energy envelope has been extracted from the differentiated signal. At peak, detection stage to detect False Noise Detection (FND) and False R Detection (FRD) in uses amplitude and time duration criteria. This algorithm shows better accuracy than the previously established methods and Hilbert Transform problem in the previous algorithm has been solved by this algorithm. The major drawback of this method is that it uses amplitude threshold that degrades accuracy for low amplitude ECG signal.

Apart from these Different methods for detecting R peaks in ECG are artificial neural network (ANN) [16], heuristic methods [17], wavelet transform (WT) [18], [19], [13], [20], [21], empirical mode of decomposition [22]. Shannon energy [23].

#### 2.2 P and T wave Detection

Thakor *et al.* (1991) [24] have proposed a method for noise cancellation and arrhythmia detection. This method is based on Adaptive Filter where a noise ECG has been choose as an input, and an impulse train of QRS wave has been chosen as reference. The basic strategy of the adaptive filter is to minimize the mean square error between the input signals to the reference signal. This method is applied in different arrhythmia detection problem and p wave detection method. The method successfully removed various artifacts but only P wave detection is possible, and accuracy is quite poor.

[25] proposed an algorithm for extraction of P and T wave based on Extended Kalman Filter. This method is based on Bayesian framework for estimation of denoised ECG from a raw ECG. For detection of peaks location, it used Bayesian estimation theory and to find the fiducial point it uses the width of corresponding wave component. This method has successfully detected wave components in ECG signal but for initialization of filter in this method requires operator interaction. For baseline fluctuation ECG signals the accuracy of this method is quite poor.

[26] proposed a Bayesian signal model for detection and delineation of P and T wave which is threshold free. To estimate the unknown parameters of Bayesian model Gibbs sampler is used. It creates complexity in the resulting posterior distribution. Apart from these Various techniques, based on nested median filter [27], adaptive filtering [24], low pass differentiation (LPD) [28], discrete cosine transform [29], hidden Markov model [30] and wavelet transform (WT) [31] have been proposed for automated extraction of P and T waves.

# Chapter 3 Proposed Algorithms

In this research work, total task is divided into three parts. In the first part, the main focus will be the extraction of QRS wave in ECG signal. In the second part implementation of P and T wave, extraction algorithm is described and finally an FPGA-based heart rate detection system using ECG signal has been implemented.

#### 3.1 Proposed Algorithm for QRS complex detection in ECG signal

The block representation of R peak detection algorithm is shown in Figure 3.1. This is divided into four stages namely pre-processing, extraction of Shannon energy envelope and peak finding logic followed by actual R peaks detection. In the pre-processing stage, noise is suppressed, and QRS complex is enhanced by using band pass filter, first order differentiation, and amplitude normalization respectively. In the Shannon energy envelope extraction stage, smooth Shannon energy envelope is produced by using Shannon energy calculation and moving average filter. In peak estimation logic stage, the pre-process for R peak detection is performed by using first order differentiation, amplitude normalization, and squaring, moving average filter. In actual(true) R peak detection stage, exact locations of R peaks are detected. The detailed discussion of each stage of Figure 3.1 is presented in the next subsections.



Figure 3.1: Block Diagram of Proposed Algorithm.

#### 3.1.1 Data pre-processing

In reality a typical pathological obtained ECG is corrupted by numerous noises such that power line interface (50 Hz), motion artifact due to electrode, skin interface, patient breathing etc. Moreover ECG signal contains P wave, T wave other than QRS complex which are not interested in our work. So we need a filtering system to extract QRS complex. From the power spectral analysis of various signal components in ECG signal, we observe that the maximum power density of QRS complex lies between 5-20 Hz. In our proposed method, the ECG is passed through a Chebyshev type I filter with bandwidth of [6-18] Hz.

After getting the filtered signal, we perform the first order differentiation of the signal to get the slope information. The first order differentiation is a high pass filter which attenuate lower frequency components (P and T wave) and passes higher frequency components (QRS wave). The mathematical implementation of the first order differentiation is shown below:

$$d[n] = f[n+1] - f[n]$$
(3.1)

After filtering and differentiating the signal is normalized in order to scale its value up to 1. This is done for preparing the signal for Shannon energy envelope computation.

$$\widehat{\mathbf{d}[\mathbf{n}]} = \frac{\mathbf{d}[\mathbf{n}]}{\max(|\mathbf{d}[\mathbf{n}]|)} \tag{3.2}$$

#### 3.1.2 Extraction of Shannon energy envelope

After differentiating the ECG signal it becomes a bipolar signal. As our method is based on peak detection, so we have to transform the differentiated signal into a unipolar signal. Now for this transform there are some transform methods those can be applied. They are absolute value method, squared value method, Shannon entropy method, Shannon energy envelope method. The mathematical formulation of these methods is described below.

Absolute value:y[n] = |a[n]|Squared value: $y[n] = a[n] \times a[n]$ Shannon entropy value: $y[n] = -|a[n]| \times ln(|a[n]|)$ Shannon energy value:  $y[n] = -(a[n])^2 ln((a[n])^2)$ 

where a[n], y[n] are input and output for the above equations respectively.

In our proposed method we have used Shannon energy envelope method as it has some advantages over the others. Figure 3.2 shows that absolute value method produces same weight value irrespective of the input amplitude. Shannon entropy method attenuates high-intensity components and gives high preference to low intensity components. The squared value method gives an exponential weightage response to the high-intensity components which will make difficulties in order to detect low-intensity components. For Shannon energy method, middle-intensity components are more emphasised and other intensity values are attenuated which gives a better detection of R-peaks.

After achieving Shannon energy envelope by using Shannon energy calculation the signal is passed through a zero shift moving the average filter to get a smooth Shannon energy envelope. A moving average filter is nothing but a moving window integrator. The mathematical expression of a moving average filter is expressed below.

$$y(nT) = \frac{1}{N} \left[ a(nT - (N - 1)T) + a(nT - (N - 2)T) + \dots + a(NT) \right]$$
(3.3)

The length of the moving average filter is an important parameter for this detection method. Generally the length of the moving average filter is taken approximately to the width of the QRS complex. If the length of moving average filter is too broad then for integration it takes the T wave also, again if the length of moving average filter is very narrower compared to the QRS complex, then for a single QRS complex it produces more spike which leads to an erroneous detection. In our proposed method we have taken a length of 65 samples moving average filter.



Figure 3.2: Comparison of energy value for different envelope method using normalized amplitude.

#### 3.1.3 Peak Estimation Logic

In this stage we introduce some different approaches from the other R-peak detection technique based on Shannon energy. In [14] for detection of R peaks use Hilbert Transform but for Hilbert transform it requires more memory buffer again in [15] have used some amplitude threshold in the decision stage for extraction for true R peaks. To overcome these problems our R peak detection logic should be free from amplitude threshold. After Shannon energy envelope extraction stage we get smooth peak signal but it contains both true R-peaks and false R-peaks. In this stage we actually attenuate the false R-peaks and emphasise the true R-peaks. This is done by following steps.

It is natural that the amplitude value for true R-peaks will be quite high than the false peaks. So if we take the first order differentiation of the signal, then it stores the slope information of the true peaks but it reduces the slope information of the false peaks.

Now in order to scale the signal to 1 the amplitude normalization of the signal has been performed.

Now the signal is a bipolar signal and for peak detection we have to make it a unipolar signal. So we performed square operation. The amplitude of false peaks are very low so when we apply square operation of these peaks they will be completely attenuated. As a result true R-peaks are amplified and false R peaks are diminished. Then the signal has been passed through a smoothing filter(moving average filter) in order to get a polished peak signal. In our proposed technique we use a moving average filter of length 85 samples.

Now signal is ready for peak detection. This peak estimation logic stage is demonstrated in Figure 3.3



Figure 3.3: Different Signal processing steps of peak estimation logic stage.

#### 3.1.4 True R peak detection

In this stage by applying peak finding algorithm R-peaks are detected. But experimentally shows that detected peak locations are slightly different from the actual positions of peaks in the experimental signal. So in order to find the real positions of R-peaks, an operation is incorporated which finds the actual time instant of peaks in the ECG signal by determining the maximum signal value within  $\pm 25$  locations of the identified locations in previous step.

In Figure 3.4 the total signal processing of the entire algorithm is shown, wherein Figure 3.4(h) red impulses indicate the extracted R peaks by proposed algorithm.



Figure 3.4: Total signal processing steps of the described method: (a) ECG data(Record 205). (b) Filtered signal. (c) Output of normalize operation. (d)Smooth Shannon energy envelope. (e) Differentiation of Shannon Energy envelope. (f) Output of square operation. (g) Output of moving average filter. (h) True detected R-peaks (Red colour impulses).

### 3.2 Proposed Algorithm for Detection and Delineation of P and T wave in ECG signal

The schematic block representation of the P and T wave extraction algorithm is shown in Figure 3.5. It consists of five stages namely pre-processing, phase assignment, optimization parameter estimation using PSO, denoised ECG signal estimation logic, P and T wave detection and delineation logic. In the pre-processing stage, we have removed baseline wander and power line interference from the ECG signal. In the phase assignment stage at first R peak is detected by using a Shannon energy envelope method, described in the previous section and then phase is assigned to the ECG according to the detected R peaks. We have used PSO framework for calculation of optimized parameters of the ECG component in the ECG and set the parameters of EKF. In the fourth stage, EKF framework is used to estimate the denoised ECG. Finally in the P and T wave detection and delineation logic, square operation is used with the denoised ECG signal and optimized phase parameters calculated by PSO for detection and delineation of P and T waves.



Figure 3.5: Block diagram of proposed methodology for P and T waves detection and delineation in ECG.

#### 3.2.1 Pre-processing

The main aim of the pre-processing stage is to remove the baseline wander and power line interference from the ECG signal. Baseline wander noise is one of the common noise present in a typical ECG signal. It fluctuates the baseline from the reference axis of ECG signal. Various filters can be used to remove baseline wander noise such as two-stage moving window median filter (MD2), single stage moving window median filter(MD1), two stage moving average filter(MA2), low pass filter(LP), band pass filter using noise stress database(BPF) [32]. In my experiment, I have used two-stage median filter for removing the baseline wander noise. Figure 3.6 show that for different input SNR in case of two-stage median filter the output SNR improvement is highest. So I have used two-stage median filter for this particular problem. At first, the ECG signal is passed through a median filter with a window size of 200 ms which removes the P waves and QRS complexes. Then a median filter with window size of 600 ms removes the T waves and power line interference. The filtered signal represents the baseline wander which is then subtracted from the ECG recording to get the baseline wander removed ECG signal. Figure 3.7 shows the complete signal processing steps of two-stage median filter.



Figure 3.6: Comparison of mean SNR improvements achieved in different input SNRs for BW removal based on two-stage moving window median filter(MD2), single stage moving window median filter(MD1), two stage moving average filter(MA2), low pass filter(LP), band pass filter using noise stress database(BPF).



Figure 3.7: Baseline wander removed ECG signal.

In a typical ECG electromagnetic noise is present in the frequency range of 50 Hz. A notch filter centered at 50 Hz is implemented through a 50 tap finite impulse response filter to remove the power line interference. The complete steps for removing of electromagnetic noise has been described in Figure 3.8



Figure 3.8: Baseline wander removed ECG signal.

#### 3.2.2 Phase Assignment

The main aim of the phase assignment stage is to detect R peak in the ECG signal and then to assign the phase to each sample of the signal according to the detected R peak. In this stage, a Shannon energy envelope method is applied to detect R peak the ECG. We have used the concept of R peak detection of the ECG as explained in our proposed method above. The phase to each sample of ECG was assigned by using R-peaks of ECG.

Here  $\varphi_k =$  phase of ECG which varies between  $-\pi$  to  $\pi$ . Assign phase  $\varphi_k = 0$  when k=sample number where R peak is detected. The phase difference between two consecutive R peaks is  $2\pi$ . Let nlen = number of samples between the two nearest R peaks. Each sample is assigned a phase  $\frac{2\pi}{nlen}$  more than the phase of previous sample. Then  $2\pi$  is subtracted from the phase of the sample where the phase of the sample is more than  $\pi$  and less than  $2\pi$  because the phase of the sample is between  $-\pi$  to  $\pi$ . The phase assignment of ECG signal of sel103 QT database has been described in Figure 3.9



Figure 3.9: Phase assignment of ECG of sel103 QT database.

#### 3.2.3 Optimized Parameters Estimation Using PSO

The main aim of the optimization parameters estimation stage is to calculate optimized parameters of single cycle of the ECG envelope by using PSO. For modeling of a single cycle of ECG envelope, a set of optimized parameters (amplitude, width, phase) related to components of the ECG (P, Q, R, S and T wave) is required. In our proposed method for finding these optimum parameters we have applied PSO method.

Templates of ECG like mean of ECG, standard deviation of ECG and mean of phase are required for estimation of optimized parameters by using PSO. We have calculated the templates of ECG (mean of ECG, standard deviation of ECG, mean of phase) as explained in [33].

PSO is a stochastic random optimization process which is inspired by the behaviors of social animal like swarm of fish, flock of birds [34]. It is one of the powerful evolutionary technique that is capable to optimize a nonlinear equation with the least number of solution parameters. The basic concept of PSO lies in the fact of social sharing information [35]. For each solution variable a swarm of particles are taken. Movement of each particle is controlled by its current position and velocity. At each step, each particle remembers its local best position and global best position. For each variable, the optimum position of particle denoted as global best where local best denoted the last updated optimum position of the corresponding particle. Optimality of a particle is checked according to the problem statement [36].

For a given particle  $P_{ij}$  at k<sup>th</sup> iteration position and velocity updating formulae are given below.

$$v_{ij}^{k+1} = w \cdot v_{ij}^k + C_1 R_1 (p_{lij}^k - p_{ij}^k) + C_2 R_2 (p_{gi}^k - p_{ij}^k)$$
(3.4)

$$p_{ij}^{k+1} = p_{ij}^k + v_{ij}^{k+1} \tag{3.5}$$

Here i and j varies from 1 to NP and 1 to NG respectively. Where NP is number of particles in the swarm and NG is the number of variables in the problem.

Here  $v_{ij}^{k+1}$  = velocity of the ith particle of jth variable at iteration k+1,  $p_{ij}^{k+1}$  = position of the ith particle of jth variable at iteration k+1, w=inertia weight factor,  $C_1$  and  $C_2$  are acceleration constant,  $R_1$  and  $R_2$  are random values.

We have intelligently applied PSO for calculation of optimum parameters of the ECG. The suitable step for finding optimum parameters of the ECG for one cycle by using PSO as follows:

Step 1: Initialize the swarm by assigning random position value of the particles for the phase value of P, Q, S, T wave within the range of waves as given in paper[37]. The random phase value for P,Q, S, T are in ranges  $\frac{-\pi}{3} \pm 0.2$ ,  $\frac{-\pi}{12} \pm 0.2$ ,  $\frac{\pi}{12} \pm 0.2$ ,  $\frac{\pi}{3} \pm 0.2$  respectively. We have set R wave has phase zero.

Step 2: Fitness value (mean square error) of each particle is calculated. This is done by finding the amplitude value of mean of ECG correspond to each swarm (phase value) and calculated the error by subtracting the modeled ECG getting from each set of parameters using synthetic dynamic ECG model [37] from ECG mean value. Finally, mean square error is calculated from the error.

Step 3: Our main aim in PSO is to minimize mean square error. For each individual particle update local best position  $(P_{lij}^k)$  according to current fitness value.

Step 4: For each variable find the global best position  $(P_{gi}^k)$  by comparing the fitness value of the corresponding particles.

Step 5: Update the position and velocity of each particle according to equation (3.4) and (3.5).

Step 6: Go to step-2 until maximum iteration is reached or convergence condition(mean square error  $\leq 0.001$ ) is achieved.

We have got optimized parameters to model maternal ECG for one cycle at maximum iteration is 100,  $C_1 = C_2 = 2$ ,  $w_{\min} = 0.4$ ,  $w_{\max} = 0.9$ .

#### 3.2.4 Denoised ECG signal Estimation logic

In denoised ECG signal estimation logic stage, we have used EKF for estimate the denoised ECG signal.

The goal of the extended Kalman filter is to estimate the state of a discrete time controlled process [38]. Consider a state vector  $X_{k+1}$  governed by a nonlinear stochastic difference equation with measurement vector  $Y_{k+1}$  at instant k+1 [39]

$$X_{k+1} = f(X_k) + W_k$$
(3.6)

$$Y_{k+1} = h(X_{k+1}) + V_{k+1}$$
(3.7)

Where  $W_k$  and  $V_k$  represent process noise and measurement noise, f(.) defines system dynamic function and h(.) defines measurement function. Here  $E[W_k W_k^T] = Qn$  and  $E[V_k V_k^T] = Rn$ . Qn and Rn are the covariance of process noise and measurement noise respectively which are calculated from the mean and standard deviation of the ECG [33]. In this study, a synthetic dynamic ECG model[37] is used to estimate denoised ECG from the raw ECG. One ECG signal can be expressed as the sum of five Gaussian functions defined by their peak amplitude, width and center, denoted as  $\alpha_i$ ,  $b_i$ , and  $\phi_i$  respectively.

$$Z(\theta) = -\sum_{i \in W} \alpha_i \exp(\frac{-(\theta - \phi_i)^2}{2b_i^2})$$
(3.8)

Each Gaussian function models one of the five waves  $W = \{P, Q, R, S, T\}$  of heart beat. The state vector  $X_k$  in equation (3) is defined as  $X_k = \begin{bmatrix} \theta_k & Z_k \end{bmatrix}^T$ , where the  $\theta_k$  is phase and  $Z_k$  is amplitude of the ECG. The state process f(.) is:

$$\theta_{k+1} = (\theta_k + w\delta) \mod (2\pi) \tag{3.9}$$

$$Z_{k+1} = -\sum_{i \in W} \frac{\alpha_i w_f \delta \,\Delta \theta_{i,k}}{b_i^2} \exp(\frac{-\Delta \theta_{i,k}}{b_i^2}) + Z_k \tag{3.10}$$

Where  $w_f$  is the phase increment.

 $\Delta \theta_{i,k} = (\theta_k - \phi_i) mod(2\pi)$  and w = the angular velocity of the trajectory as it moves around the limit cycle.

The equation (3.6) represents the state equation and a description of the state equation is given above. The next step of the extended kalman filter is an observation equation as represented in equation (3.7).

Observation data  $Y_{k+1} = \begin{bmatrix} \varphi_{k+1} & S_{k+1} \end{bmatrix}^T$  where  $\varphi_{k+1} =$  the phase of ECG which is between  $-\pi$  to  $\pi$  and is explained in phase assignment subsection.  $S_{k+1}$  is the amplitude of the ECG at an instant k + 1.

The measurement function  $h(X_{k+1}) = X_{k+1}$ .

In this stage we have initialized the parameters of the extended Kalman filter such as initial state  $\widehat{X}_0$  and initial covariance  $P_0$ .

$$\widehat{X}_0 = \begin{bmatrix} -\pi & 0 \end{bmatrix}^T$$
$$P_0 = \begin{bmatrix} (2\pi)^2 & 0 \\ 0 & 10 \max(|S|)^2 \end{bmatrix}$$

#### **Computation of Extended Kalman Filter**

For [k = 0, 1, 2....N]State prediction  $:[\overline{X_{k+1}} = f(\overset{\wedge}{X_k})]$ 

State prediction covariance :  $\overline{P_{k+1}} = \nabla f_x P_k \nabla f_x^T + Qn$ 

$$\nabla f_x = \begin{bmatrix} 1 & 0\\ -\sum_{i \in w} \frac{\alpha_i w_f \delta}{b_i^2} (1 - \frac{\Delta \theta_i^2}{b_i^2}) exp(\frac{-\Delta \theta_i^2}{2b_i^2}) & 1 \end{bmatrix}$$

$$Sg = \nabla h \ \overline{P_{k+1}} \ \nabla h^T + Rn$$
  
As  $h \left( \overline{X_{K+1}} \right) = \overline{X_{K+1}}$   
So  $\nabla h = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$ 

Kalman Gain:  $Kg = \overline{P_{k+1}} \nabla h^T Sg^{-1}$ 

$$P_{K+1} = \overline{P_{K+1}} - ((Kg)Sg(Kg^T))$$

$$\widehat{X_{k+1}} = \overline{X_{k+1}} + Kg\left(Y_{k+1} - h\left(\overline{X_{k+1}}\right)\right)$$

#### 3.2.5 P and T wave Detection and Delineation Logic

The main aim of this stage is to detect and delineate P and T wave (detect P ON position, P OFF position, P Peak, T ON position, T OFF position, T Peak). The optimized phase of P and T wave, calculated by PSO has been compared with the phase value correspond to each estimated ECG sample using EKF. The exact location of P and T peak can be found by searching the maximum signal value within  $\pm 30$  of the identified location in the previous step. In order to find on and off position of P and T wave we first squared the estimated denoised ECG. Then we have detected the valley point of both sides of detected peak locations (P and T peak) which gives location of on and off position of P and T wave (delineation). Figure 3.10 demonstrates the delineation logic of P and T waves(T-On, T-Off, P-On, P-Off).



Figure 3.10: Valley point detection logic.

#### 3.3 Heart Rate determination from an ECG signal in FPGA platform

Heart Rate detection is one of the basic clinical jobs to determine the condition of a patient. Heart rate can easily be calculated from ECG signal. In an ECG signal if the locations of R-peaks are known then heart rate can easily determine by the following formula: HeartRate  $=\frac{60}{R-Rinterval}$  bpm. A real-time QRS detection algorithm has been proposed in this research work, this algorithm can extended for heart rate detection also. In this section, we implemented the design in field programmable gate array (FPGA). FPGA is a very popular field to design a hardware environment [40]. FPGA provides easy testability allow faster implementation and verification option for implementing a new design [41]. Field Programmable Gate Array (FPGA) allow rapid prototyping and quick programming [42]. FPGA based design can act as a bridge in converting from a software algorithm to dedicated hardware design based on Application-specific integrated circuits (ASICs). In this section, a brief description of the primary jobs those are undertaken to design the heart rate detection algorithm in FPGA.

#### 3.3.1 Data Conversion

The amplitude value of a typical ECG signal is in real numbers format. But real number format is not compatible for FPGA. For the implementation of ECG signal in FPGA, two formats are present (i) fixed point format, (ii)Floating point format.Here fixed point format has been used because it is easier to understand and implement, require less memory and less processor time. We have converted the real number to 16 bits fixed-point format. The amplitude of the ECG signal ranges between -15 to 15. So we have multiplied the number with  $2^{11}$ . Then we convert to the nearest integer and if the number is positive we represent the binary form of the number. If negative, at first convert the number into the binary then represent the number as 1's complement of the binary number.

#### 3.3.2 Filtering

In our proposed method, the ECG is passed through a finite impulse response (FIR) band-pass filter with Kaiser window with a bandwidth of [6-18] Hz. We have used FIR band-pass filter with Kaiser Window for easier implementation and avoid complexity compare to the infinite impulse response (IIR) filter [43]. [44]. We have used direct form-I for implementation of FIR band-pass filter. The mathematical representation of direct form-I:

$$Y = \sum_{n=0}^{N-1} a(n).b(n)$$
 (3.11)

Here Y=output of the band-pass filter, a is shifted matrix, b is the coefficient matrix shown in Figure 3.11 and N is the length of the coefficient matrix. The block diagram for FPGA implementation of the band-pass filter (equation-1) shown in Figure 3.11. We have calculated coefficients of FIR band-pass filter (coefficient matrix) with Kaiser Window with a bandwidth of [6-18] Hz. We have used Filter Design Toolbox (FDT) in MATLAB for calculation of coefficient matrix [45]. We have converted the each coefficient from the real number to the 16 bits fixed-point format by using the algorithm 1 and store in the coefficient matrix. We have used shifted form to store the input values. The length of the shifted matrix is 31 because the length of the coefficient matrix is 31. In shifted matrix, all the values in shifted matrix shift one unit right and store input at zeroth location (shifted

matrix (1 to 30) =shifted matrix (0 to 29) and shifted matrix (0) = X (n). Where input is X (n) (real ECG converted to fixed point format) at instant n.



Figure 3.11: Block diagram of FPGA implementation of the band-pass filter.

#### 3.3.3 R Peak Detection

For peak detection, we have used two previous samples with current samples of moving average filter output. Let three samples are a, b, c then b to be peak b should be more than a and c, for that we have used subtraction operation. We find d=a-b and e=c-b by using 2 subtraction block, then we have checked whether d and e are negative or not (d (31) = '1' and e (31) = '1'). When these are negative, we assign that as the peak and that location we put as '1' otherwise '0'.

But experimentally shows that detected peak locations are slightly different from the actual positions of the peaks in the experimental signal. So to find the real positions of actual R-peaks, we have searched the maximum amplitude within 50 previous samples of the identified location.

We have used 50 previous samples of actual ECG signals from the identified location. Then we find the maximum amplitude of that 50 samples by using subtraction operation and distance between the highest amplitude in 50 samples and identified the location calculated.

The current location automatically incremented by one when we give sequential inputs.

Finally subtracting the distance from the current location we got the R peak.

#### **3.3.4** Heart Rate Detection

After ECG extraction, heart rate can be calculated using the interval between two consecutive detected R-peaks of the ECG signal. Heart rate between two consecutive R-peaks= $\frac{1}{T}$  bits/min =  $\frac{60 f_s}{n}$  bits/min. Where T = R-R interval of the two consecutive R-peaks in minute, =sampling

Where T = R-R interval of the two consecutive R-peaks in minute, =sampling frequency, n=number of samples between the two successive R peaks.

Here fs=360

We first convert 60<sup>\*</sup>fs to binary value consist of 32 bits. Then we calculate n by using subtraction algorithm, where inputs are two consecutive R-peak locations.

Then by using division operation calculate heart rate where inputs are binary values of  $60^*$ fs and n.

#### 3.3.5 System Synthesize Information

After implementation of this proposed FPGA system, it is synthesized to check whether it is possible to implement it in the available hardware system. In this work, the proposed system has been synthesized in Vertex 5. The synthesized report as follows. Figure 3.12 shows the device utilization summary of the proposed system, where Figure 3.13 displays the RTL model of the system.

Device Utilization Summary (estimated values)								
Logic Utilization	Used	Available	Utilization					
Number of Slice Registers	5728	607200		0%				
Number of Slice LUTs	88456	303600		29%				
Number of fully used LUT-FF pairs	188	93996		0%				
Number of bonded IOBs	114	700		16%				
Number of BUFG/BUFGCTRLs	1	32		3%				

Figure 3.12: Device Utilization Summary of the proposed FPGA System.



Figure 3.13: RTL of the proposed FPGA System.

# Chapter 4 Results and Discussion

In order to evaluate the efficiency of proposed methods, the performance of these methods has been evaluated on real ECG signals.

# 4.1 Experimental ECG Database

In my research work, two real ECG databases have been used namely MIT-BIH Arrhythmia Database and QT Database.

#### 4.1.1 MIT-BIH Arrhythmia Database

MIT-BIH Arrhythmia Database is one of the major contributions of cooperative work of Boston's Israel Hospital Laboratory and MIT laboratory. This database was introduced in 1980 and the main contents of this database are standard material for evaluation of arrhythmia detection [46]. This database consists 48 half hours two-channel ECG recording obtained from 47 subjects studied by the BIH Arrhythmia Laboratory [47].

The sampling frequency of the digitized ECG signal is 360 samples per second per second with 11-bit resolution over a 10 mV range.

#### 4.1.2 QT Database

QT database is one of the popular real databases that is used in different research work [28]. It is used as a reference for finding the validity of an automated ECG components delineation algorithm. It consists of two channel real ECG signal collected from various subjects. It is an annotated by the cardiologist for a minimum of 30 beats per channel [31]. The cardiologist annotation of QT database is being done by two leads where in this work annotation is one using single lead. To find the performance of the proposed technique the annotation result of this technique have been compared with manual annotation of QT database [48].

# 4.2 Simulation Software

A couple of software have been used in this work. For software simulation, MAT-LAB 2012B has been used. For FPGA system design, Xilinx ISE 14.2 has been used. Like the arrangement of Proposed Algorithms, result and discussion section also divided into three part as follows.

## 4.3 Result and Discussion for QRS Detection Algorithm

To evaluate the performance of our proposed R peak detection method, we require three parameters namely true positive (TP), false negative (FN) and false positive (FP) from detected R peak. Here TP is the number of correctly detected R peaks, FN is the number of missed R peaks, FP is the number of noise spikes detected as R peaks. Sensitivity (Se) and positive predictive value (+P) and detection error rate (DER) and accuracy (Acc) are calculated using TP, FN and FP by the following equations respectively.

$$Se = \frac{TP}{TP + FN} \times 100\%$$
(4.1)

$$+P = \frac{TP}{TP + FP} \times 100\%$$
(4.2)

$$DER = \frac{FP + FN}{TP} \times 100\%$$
(4.3)

$$Acc = \frac{TP}{TP + FP + FN} \times 100\%$$
(4.4)

The performance of the proposed R-peak detection method for 48 ECG recording of the MIT-BIH arrhythmia database is summarized in Table 4.1. The proposed method detects a total number of 109474 true peaks. It also produces 58 false negatives (FN) and 116 false positive (FP). The average accuracy of the proposed method is 99.841% but for individual detection accuracies vary from 99.26% to 100%. In Table 4.2. The performance of the proposed method on MIT-BIH arrhythmia database is compared with other existing methods. It shows that our proposed method has a better accuracy than the other methods like wavelet transform techniques, differential operation method, Pan-Tompkins algorithm, Shannon energy with Hilbert transform technique, Shannon energy technique

In MIT-BIH arrhythmia database, records 104,108,203,228 contains high-grade of noise that's why the accuracy of the method for these records are comparatively weaker than other records. Record 103 contains low amplitude QRS complexes and baseline drift, the performance of the proposed method for this record is shown in Figure 4.1



Figure 4.1: Performance of the proposed method for Record 103 (Low amplitude QRS complexes and baseline drift.)

DATA NO	TP	FN	FP	Se (%)	+P(%)	DER (%)	Acc (%)
100	2272	1	0	99.96	100.00	0.04	99.96
101	1866	0	2	100.00	99.89	0.11	99.89
102	2187	0	0	100.00	100.00	0.00	100.00
103	2084	0	0	100.00	100.00	0.00	100.00
104	2255	0	4	100.00	99.82	0.18	99.82
105	2581	5	5	99.81	99.81	0.39	99.61
106	2000	3	5	99.85	99.75	0.40	99.60
107	2136	1	0	99.95	100.00	0.05	99.95
108	1762	5	8	99.72	99.55	0.74	99.27
109	2532	0	3	100.00	99.88	0.12	99.88
111	2124	0	4	100.00	99.81	0.19	99.81
112	2539	0	1	100.00	99.96	0.04	99.96
113	1795	0	0	100.00	100.00	0.00	100.00
114	1879	0	4	100.00	99.79	0.21	99.79
115	1954	0	6	100.00	99.69	0.31	99.69
116	2405	5	1	99.79	99.96	0.25	99.75
117	1535	0	1	100.00	99.93	0.07	99.93
118	2276	2	5	99.91	99.78	0.31	99.69
119	1985	2	4	99.90	99.80	0.30	99.70
121	1866	0	4	100.00	99.79	0.21	99.79
122	2476	0	0	100.00	100.00	0.00	100.00
123	1520	0	5	100.00	99.67	0.33	99.67
124	1628	0	8	100.00	99.51	0.49	99.51
200	2610	0	4	100.00	99.85	0.15	99.85
201	1962	1	2	99.95	99.90	0.15	99.85
202	2136	0	2	100.00	99.91	0.09	99.91
203	2981	9	8	99.70	99.73	0.57	99.43
205	2655	1	0	99.96	100.00	0.04	99.96
207	1857	3	5	99.84	99.73	0.43	99.57
208	2948	7	3	99.76	99.90	0.34	99.66
209	3003	2	0	99.93	100.00	0.07	99.93
210	2633	1	2	99.96	99.92	0.11	99.89
212	2748	0	0	100.00	100.00	0.00	100.00
213	3250	1	2	99.97	99.94	0.09	99.91
214	2264	0	2	100.00	99.91	0.09	99.91
215	3362	1	0	99.97	100.00	0.03	99.97
217	2208	0	1	100.00	99.95	0.05	99.95
219	2154	0	0	100.00	100.00	0.00	100.00
220	2048	0	0	100.00	100.00	0.00	100.00
221	2427	0	1	100.00	99.96	0.04	99.96
222	2482	0	1	100.00	99.96	0.04	99.96
223	2606	0	0	100.00	100.00	0.00	100.00
228	2053	0	5	100.00	99.76	0.24	99.76
230	2256	0	2	100.00	99.91	0.09	99.91
231	1571	0	0	100.00	100.00	0.00	100.00
232	1780	0	4	100.00	99.78	0.22	99.78
233	3070	8	2	99.74	99.93	0.33	99.68
234	2753	0	0	100.00	100.00	0.00	100.00
Total	109474	58	116	99.95	99.88	0.16	99.84

Table 4.1: Performance evaluation of R peak extraction algorithm on MIT-BIH arrhythmia database ECG signal with the duration of 30 minutes.

Record 232 contains a number long pauses in the ECG signal. Our proposed method has a better response to this signal shown in Figure 4.2. Record 106 has tall T waves, and it contains continuously varying QRS complex. Detection performance of the expressed method for this signal is shown in Figure 4.3.

$\mathbf{Method}$	Total beats	$\mathbf{FN}$	$\mathbf{FP}$	Se (%)	+P (%)	DER (%)	Acc (%)		
Proposed method 109,532		58	116	99.95155	99.88416	0.164668	99.84131		
PSEE [15]	109,494	93	91	99.92	99.92	0.168	99.832		
WT [18]	104,184	65	112	99.94	99.89	0.17	99.83		
SEHT [14]	109,496	79	140	99.93	99.87	0.2	99.8		
DOM [49]	109,809	58	166	99.95	99.85	0.204	99.796		
WT [31]	109,428	220	153	99.8	99.86	0.34	99.66		
WT [13]	110,159	322	120	99.89	99.7	0.402	99.599		
PT [11]	109,809	507	277	99.54	99.75	0.712	99.288		
$ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( ) \\ ( )$									
Samule Instant									

Table 4.2: Comparison of performance of our proposed method with other methods for detecting R peaks using MIT BIH database

Figure 4.2: Performance of the proposed method for Record 232 (Long pauses.)

#### 4.3.1 Result and Discussion for P and T wave Detection and Delineation Algorithm

In order to evaluate that how much efficiently our proposed method is working on ECG signals of QT database we have need three parameters True Positive (TP), False Positive (FP), False Negative (FN) respectively. Where TP is the number of correctly detected the delineation points (P 'On', P 'Off', P-Peak, T 'On', T 'Off', T-Peak), FN is the number of missed delineation points ((P 'On', P 'Off', P-Peak, T 'On', T 'Off', T-Peak). FP is the number of noise detected as delineation points ((P 'On', P 'Off', P-Peak, T 'On', T 'Off', T-Peak). In our evaluation process, we have separately calculated these three parameters corresponds to every peak (P and T) and "ON" and "OFF" position of P and T waves. With the help of these parameters Sensitivity(Se), Positive Predictivity (PPV) have been calculated for 1 minute ECG signals of QT database. In Table4.3 the performance of our proposed method has been compared with formally established methods. In Figure 4.4 and Figure 4.5. a pictorial description of detected and delineated P and T waves of ECG signals namely sele0133, sel230 (QT database) have been described respectively.

Formulae for calculating Sensitivity (Se) and Positive Predictivity (PPV) have



Figure 4.3: Performance of the proposed method for Record 106 (Continuously varying QRS complex and tall T wave.)

been expressed below.

$$Se = \frac{TP}{TP + FN} \times 100\%$$
(4.5)

$$PPV = \frac{TP}{TP + FP} \times 100\%$$
(4.6)

Table 4.3: Comparison of the average Se and average PPV for all record of QT ECG database with signal length 1 minute

Algorithm	Parameter	P 'On'	Р	P 'Off'	T 'On'	Т	T 'Off'
Proposed Work	${ m Se}(\%)$	97.80	99.61	98.33	99.04	99.61	96.12
T Toposed Work	PPV(%)	98.40	100	99.70	99.42	100	96.50
WT[31]	${ m Se}(\%)$	98.87	98.87	98.75	98.87	99.17	99.17
VV 1 [31]	PPV(%)	91.03	91.03	91.03	98.03	97.79	97.79
FKF[95]	${ m Se}(\%)$	97.7	99.7	97.7	98.70	99.00	98.70
	PPV(%)	98.17	98.17	97.17	99.17	98.74	97.74



Figure 4.4: P wave and T wave extraction for ECG signal sele0133 (QT database).



Figure 4.5: P wave and T wave extraction for ECG signal sel230 (QT database).

#### 4.3.2 Result and Discussion for Heart Rate Determination in FPGA Platform

Performance the proposed heart rate calculation system is evaluated by using real ECG database namely MIT-BIH arrhythmia database. The proposed method is implemented on Xilinx. From the Xilinx, we got the location of the actual R-peaks of the ECG.

Figure 4.6, Figure 4.8 and Figure 4.10 present the actual R peak location and heart rate using Xilinx from 101, 106 and 116 of MIT-BIH arrhythmia database respectively. Figure 4.7, Figure 4.9 and Figure 4.11 present the placement of detected actual R peak on the ECG signal from 101, 106 and 116 of MIT-BIH arrhythmia database.

Finally Figure 4.12 shows the result of R peak detection and heart rate calculation from 203 of MIT-BIH arrhythmia database. From the above analysis, it is found that actual R peak detection is encouraging even with ill-conditioned data, which has been shown in Figure 4.13.

Į														
	Name	Value	20 us	40 us	60 us	80 us	100	us IIIIIIII	120 us	140 us	60 us	190 us	200 u	5
ĺ	le sig1	-0.310000												
I	lig dk	1												
	lin pdetled	0												118
	lig acturdet	10101011001	1010011	1100011	01 (	1011001000	Þ	( 1000	0001001 )	1010101100	1	11010110001		11111.
	le riocreal	1369.000000	83.000000	397.000	00 )	712.000000	Þ	1033	000000 )	1369.00000	)	1713.000000	$\square$	2037
	10 heartout	1000001	1001000	)	1000101		Þ	( 10	0100 )	1000001		111111		1000011
I	le heartoutreal	65.000000	72.000000	(	69.000000			68.	000000 )	65.00000		63.000000		67.00

Figure 4.6: Detection of R peak location and calculation of heart rate using Xilinx from 101 of MIT-BIH arrhythmia database.



Figure 4.7: Placement of extracted peaks of the ECG signal with id 101 of MIT-BIH arrhythmia database.

Name	Value	milion	40 us	nton	60 us	80 us	duu	100 u	duu	120 us	140 us	l	160 us	180 us		200 us
le sig1	-0.275000															
dk dk	0															
pdetled	0						No.		19 H.	<u> </u>					-	1
🖟 acturdet	10000111111	101100000		101	1010110		1000011	1111		1011010100			11100100111	(	10	0010010111
🖟 riocreal	1087.000000	352.000000		726	000000		1087.00	0000		1449.0000	0		1831.000000	X	2	99.000000
le heartout	111100	1001000		1	11010				111100				111001			111011
le heartoutreal	60.000000	72.000000		58	00000				60.0000	0			57.000000	X		9.000000

Figure 4.8: Detection of R peak location and calculation of heart rate using Xilinx from 106 of MIT-BIH arrhythmia database.



Figure 4.9: Placement of extracted peaks of the ECG signal with id 106 of MIT-BIH arrhythmia database.

Name	Value	40 us	60 us	80 us   100 us	120 us	140 us   160	us	180 us 200 us	220 us
le sig1	1.170000								
1 dk	1								
le pdetled	0						1:10		11
le acturdet	10101011011	100011101 )	1000110011	1101000111	0001010010	1010101011	)( 1100	01001 ( 11101110111	) 1001.
e riocreal	1371.000000	285.00000	563.000000	X 839.00000	106.000000	1371.000000	1641	d00000 X 1911.000000	2182.0
le heartout	1010010	1001000 )	1001110	) 1001111	) 1010001	1010010	)	1010000	
le heartoutreal	82.000000	72,00000 )	78.000000	79.000000	81.00000	82.00000	)	80.000000	

Figure 4.10: Detection of R peak location and calculation of heart rate using Xilinx from 116 of MIT-BIH arrhythmia database.



Figure 4.11: Placement of extracted peaks of the ECG signal with id 116 of MIT-BIH arrhythmia database.

V		M.L.,	12	0 um	ຟີເຫ		ID us	160		170.00		191 uz		00.uz	100 uz	110 ur	120
Name		value	1 3		-1111	Luu		n,	ĥuluu	111	duu		ц.				
6	sig1	-0.190000															
16	dk	0								<b>İ</b>							
16	pdetled	0	}	1									3				1:
16	acturdet	110101110		1100001		(	1101011110				101001011	1)		1101100001 )		1111001010	)
16	riocreal	430.000000		97.000000			430.000000				663.00000			855.000000		1002.000000	X
16	heartout	1000001		1001000			1000001				1011101			1101011		10011110	X
1	heartoutreal	65.000000	-	72.000000			65.000000		(		93.00000			107.000000		158,00000	X

Figure 4.12: Detection of R peak location and calculation of heart rate using Xilinx from 203 of MIT-BIH arrhythmia database.



Figure 4.13: Placement of extracted peaks of the ECG signal with id 203 of MIT-BIH arrhythmia database.

Chapter 5

Conclusions, Future Scope and Disseminations

## 5.1 Conclusions

This research work mainly deals with signal processing of Electrocardiogram (ECG) signal. The primary focus of this work is to design real-time ECG analyzer that include real-time ECG components detection and real-time heart rate detection system. At the final it has been focused to implement an FPGA-based heart rate detection system. At the completion of this research work, a number of matters can be concluded.

- A real-time QRS detection method has been implemented. The proposed method detection logic is amplitude threshold free and the processing time of the proposed method is very less which is suitable for real-time application.
- The efficiency of the proposed method has been validated with real ECG database namely MIT-BIH arrhythmia database. The proposed method shows an average Accuracy of 99.84% and Sensitivity of 99.95% for MIT-BIH arrhythmia database.
- The performance of the proposed work has been compared with existing method namely Shannon energy with Hilbert Transform, Peak Shannon energy method, Wavelet Transform method etc.
- For detection and delineation of P and T waves, a method based on EKF with PSO has been proposed in this research work. In this proposed method for initialization of Kalman Filter, no operator interaction is required, and PSO is used here for finding the set of optimized parameters for modeling a complete ECG envelope.
- The validation of this proposed method has been evaluated using real ECG database namely QT database. This method shows an average Sensitivity of 99.61% and Positive Productivity of 100% for P wave and for T wave an average Sensitivity of 99.61% and Positive Productivity of 100%.
- The proposed method can successfully extract the baseline wander noise and Electromagnetic noise for ECG signal.
- The performance of the proposed work has been compared with existing method namely Low pass Detector (LPD) method and Wavelet Transform (WT) method.
- In this research work an FPGA-based heart rate detection system has been proposed. The heart rate detection system has been implemented using VHDL environment and it can detect heart rate from a typical ECG signal.
- The performance of this FPGA system has been evaluated in VHDL Test Bench environment and for input the ECG signals from MIT-BIH arrhythmia database have been used.

# 5.2 Future Scope

This work implements a couple of methods in order to detect and delineate all the components of a typical ECG signal. However for future scope aspect following works can be done in future.

- Better accuracy model can be developed with modification of the algorithm.
- Automatic Cardiac disease detection with the hardware interface.
- Fetal status determination using abdominal ECG.
- Biometric application.

# 5.3 Disseminations

- M. Rakshit, D. Panigrahy, P.K. Sahu, "EKF with PSO Technique for delineation of P and T Wave in electrocardiogram(ECG) Signal", 2nd IEEE conf. DOI: 10.1109/SPIN.2015.7095293, Page(s): 696 - 701.
- D. Panigrahy, **M. Rakshit**, P.K. Sahu, "An efficient method for fetal ECG extraction from single channel abdominal ECG", IEEE conf. College of Engg. Pune (paper presented).

# Bibliography

- D. B. Geselowitz, "On the theory of the electrocardiogram," Proceedings of the IEEE, vol. 77, pp. 857–876, 1989.
- [2] R. Tung and P. Zimetbaum, "Use of the Electrocardiogram in Acute Myocardial Infarction," in *Cardiac Intensive Care*, 2010, pp. 106–109.
- [3] U. Rajendra Acharya, J. S. Suri, J. A. E. Spaan, and S. M. Krishnan, Advances in cardiac signal processing, 2007.
- [4] I. R. Legarreta, P. Addison, N. Grubb, G. Clegg, C. Robertson, K. Fox, and J. Watson, "R-wave detection using continuous wavelet modulus maxima," *Computers in Cardiology*, 2003, 2003.
- [5] C. Bearzi, M. Rota, T. Hosoda, J. Tillmanns, A. Nascimbene, A. De Angelis, S. Yasuzawa-Amano, I. Trofimova, R. W. Siggins, N. Lecapitaine, S. Cascapera, A. P. Beltrami, D. A. D'Alessandro, E. Zias, F. Quaini, K. Urbanek, R. E. Michler, R. Bolli, J. Kajstura, A. Leri, and P. Anversa, "Human cardiac stem cells." *Proceedings of the National Academy of Sciences of the United States of America*, vol. 104, pp. 14068–14073, 2007.
- [6] D. S. Park and G. I. Fishman, "The cardiac conduction system," pp. 904–915, 2011.
- [7] A. A. Grace and D. M. Roden, "Systems biology and cardiac arrhythmias." *Lancet*, vol. 380, pp. 1498–508, 2012.
- [8] V. X. Afonso, W. J. Tompkins, T. Q. Nguyen, and S. Luo, "ECG beat detection using filter banks." *IEEE transactions on bio-medical engineering*, vol. 46, pp. 192– 202, 1999.
- [9] P. P. Kanjilal, S. Palit, and G. Saha, "Fetal ECG extraction from single-channel maternal ECG using singular value decomposition," *IEEE Transactions on Biomedical Engineering*, vol. 44, pp. 51–59, 1997.
- [10] S. Kharabian, M. B. Shamsollahi, and R. Sameni, "Fetal R-wave detection from multichannel abdominal ECG recordings in low SNR," in *Proceedings of the 31st* Annual International Conference of the IEEE Engineering in Medicine and Biology Society: Engineering the Future of Biomedicine, EMBC 2009, 2009, pp. 344–347.
- "A Real-Yime and W. J. Tompkins, QRS Detection Al-[11] J. Pan gorithm," IEEEtransactions on bio-medical engineeringBiomedical En-230-236, 1985.[Online]. vol. BME-32, gineering, pp. Available: http://ieeexplore.ieee.org/xpls/abs\_all.jsp?arnumber=4122029
- [12] D. Benitez, P. A. Gaydecki, A. Zaidi, and A. P. Fitzpatrick, "The use of the Hilbert transform in ECG signal analysis," *Computers in Biology and Medicine*, vol. 31, pp. 399–406, 2001.
- [13] A. Ghaffarl, H. Golbayani, and M. Ghasemi, "A new mathematical based QRS detector using continuous wavelet transform," *Computers & Electrical Engineering*, vol. 34, pp. 81–91, 2008.
- [14] M. Manikandan and K. Soman, "A novel method for detecting Rpeaks in electrocardiogram (ECG) signal," *Biomedical Signal Processing* and Control, vol. 7, no. 2, pp. 118–128, Mar. 2012. [Online]. Available: http://linkinghub.elsevier.com/retrieve/pii/S1746809411000292

- [15] H. Zhu and J. Dong, "An R-peak detection method based on peaks of Shannon energy envelope," 2013.
- [16] R. Silipo and C. Marches, "Artificial neural networks for automatic ECG analysis," *IEEE Transactions on Signal Processing*, vol. 46, pp. 1417–1425, 1998.
- [17] P. S. Hamilton and W. J. Tompkins, "Quantitative investigation of QRS detection rules using the MIT/BIH arrhythmia database." *IEEE transactions on bio-medical* engineering, vol. 33, no. 12, pp. 1157–65, Dec. 1986.
- [18] H. Zhang, "An Improved QRS Wave Group Detection Algorithm and Matlab Implementation," in *Physics Procedia*, vol. 25. Elsevier Srl, Jan. 2012, pp. 1010–1016.
- [19] I. R. Legarreta, P. Addison, N. Grubb, G. Clegg, C. Robertson, K. Fox, and J. Watson, "R-wave detection using continuous wavelet modulus maxima," *Computers in Cardiology*, 2003, 2003.
- [20] A. Daamouche, L. Hamami, N. Alajlan, and F. Melgani, "A wavelet optimization approach for ECG signal classification," *Biomedical Signal Processing and Control*, vol. 7, pp. 342–349, 2012.
- [21] C. Li, C. Zheng, and C. Tai, "Detection of ECG characteristic points using wavelet transforms," *IEEE Trans Biomed Eng*, vol. 42, pp. 21–28, 1995.
- [22] S. Pal and M. Mitra, "Empirical mode decomposition based ECG enhancement and QRS detection," *Computers in Biology and Medicine*, vol. 42, pp. 83–92, 2012.
- [23] Z. Zidelmal, A. Amirou, D. Ould-Abdeslam, A. Moukadem, and A. Dieterlen, "QRS detection using S-Transform and Shannon energy," *Computer Methods and Programs* in *Biomedicine*, vol. 116, pp. 1–9, 2014.
- [24] N. V. Thakor and Y. S. Zhu, "Applications of adaptive filtering to ECG analysis: Noise cancellation and arrhythmia detection," *IEEE Transactions on Biomedical Engineering*, vol. 38, pp. 785–794, 1991.
- [25] O. Sayadi and M. B. Shamsollahi, "A model-based Bayesian framework for ECG beat segmentation." *Physiological measurement*, vol. 30, pp. 335–352, 2009.
- [26] C. Lin, G. Kail, A. Giremus, C. Mailhes, J.-Y. Tourneret, and F. Hlawatsch, "Sequential beat-to-beat P and T wave delineation and waveform estimation in ECG signals: Block Gibbs sampler and marginalized particle filter," *Signal Processing*, vol. 104, pp. 174–187, Nov. 2014. [Online]. Available: http://www.sciencedirect.com/science/article/pii/S0165168414001066
- [27] P. Strumillo, "Nested median filtering for detecting T-wave offset in ECGs," p. 682, 2002.
- [28] P. Laguna, R. Jané, and P. Caminal, "Automatic detection of wave boundaries in multilead ECG signals: validation with the CSE database." Computers and biomedical research, an international journal, vol. 27, pp. 45–60, 1994.
- [29] R. J. Martis, U. R. Acharya, C. M. Lim, and J. S. Suri, "Characterization of ECG beats from cardiac arrhythmia using discrete cosine transform in PCA framework," *Knowledge-Based Systems*, vol. 45, pp. 76–82, 2013.
- [30] A. Doucet, N. J. Gordon, V. Krishnamurthy, and S. Member, "Particle Filters for State Estimation of Jump Markov Linear Systems," *IEEE TRANSACTIONS ON* SIGNAL PROCESSING, vol. 49, pp. 613–624, 2001.
- [31] J. P. Martínez, R. Almeida, S. Olmos, A. P. Rocha, and P. Laguna, "A Wavelet-Based ECG Delineator Evaluation on Standard Databases," *IEEE Transactions on Biomedical Engineering*, vol. 51, pp. 570–581, 2004.
- [32] P. K. Sinha and Q. H. Hong, "An improved median filter," *IEEE Transactions on Medical Imaging*, vol. 9, pp. 345–346, 1990.

- [33] R. Sameni, M. B. Shamsollahi, C. Jutten, and G. D. Clifford, "A nonlinear Bayesian filtering framework for ECG denoising," *IEEE Transactions on Biomedical Engineering*, vol. 54, pp. 2172–2185, 2007.
- [34] Y. Da and G. Xiurun, "An improved PSO-based ANN with simulated annealing technique," pp. 527–533, 2005.
- [35] Y. del Valle, G. K. Venayagamoorthy, S. Mohagheghi, J. C. Hernandez, and R. G. Harley, "Particle Swarm Optimization: Basic Concepts, Variants and Applications in Power Systems," *Evolutionary Computation, IEEE Transactions on*, vol. 12, pp. 171–195, 2008.
- [36] R. Poli, J. Kennedy, and T. Blackwell, "Particle swarm optimization," pp. 33–57, 2007.
- [37] P. E. McSharry, G. D. Clifford, L. Tarassenko, and L. A. Smith, "A dynamical model for generating synthetic electrocardiogram signals," *IEEE Transactions on Biomedical Engineering*, vol. 50, pp. 289–294, 2003.
- [38] Y. P. Meau, F. Ibrahim, S. A. L. Narainasamy, and R. Omar, "Intelligent classification of electrocardiogram (ECG) signal using extended Kalman Filter (EKF) based neuro fuzzy system," *Computer Methods and Programs in Biomedicine*, vol. 82, pp. 157–168, 2006.
- [39] G. Welch and G. Bishop, "An Introduction to the Kalman Filter," In Practice, vol. 7, no. 1, pp. 1–16, 2006.
- [40] J. Matai, A. Irturk, and R. Kastner, "Design and Implementation of an FPGA-Based Real-Time Face Recognition System," 2011 IEEE 19th Annual International Symposium on Field-Programmable Custom Computing Machines, pp. 97–100, 2011.
- [41] K. C. Chang and G. E. Sobelman, "FPGA-based design of a Pulsed-OFDM System," in *IEEE Asia-Pacific Conference on Circuits and Systems, Proceedings, APCCAS*, 2006, pp. 1128–1131.
- [42] N. Ravanshad, H. Rezaee-Dehsorkh, R. Lotfi, and Y. Lian, "A level-crossing based QRS-detection algorithm for wearable ECG sensors," *IEEE Journal of Biomedical* and Health Informatics, vol. 18, pp. 183–192, 2014.
- [43] Z. Shen, "Improving FIR filter coefficient precision," in IEEE Signal Processing Magazine, vol. 27, 2010, pp. 120–124.
- [44] R. Lehto, T. Taurén, and O. Vainio, "Recursive FIR filter structures on FPGA," *Microprocessors and Microsystems*, vol. 35, pp. 595–602, 2011.
- [45] R. A. Losada, "Practical FIR Filter Design in MATLAB," Technical Paper, pp. 1-31, 2003. [Online]. Available: papers2://publication/uuid/BA3E4D27-C4EF-4758-B1F7-0A79E742DB35
- [46] I. I. Christov, "Real time electrocardiogram QRS detection using combined adaptive threshold." *Biomedical engineering online*, vol. 3, p. 28, 2004.
- [47] A. L. Goldberger, L. A. Amaral, L. Glass, J. M. Hausdorff, P. C. Ivanov, R. G. Mark, J. E. Mietus, G. B. Moody, C. K. Peng, and H. E. Stanley, "PhysioBank, PhysioToolkit, and PhysioNet: components of a new research resource for complex physiologic signals." *Circulation*, vol. 101, pp. E215–E220, 2000.
- [48] P. C. Chen, S. Lee, and C. D. Kuo, "Delineation of T-wave in ECG by wavelet transform using multiscale differential operator," *IEEE Transactions on Biomedical Engineering*, vol. 53, pp. 1429–1433, 2006.
- [49] Y. C. Yeh and W. J. Wang, "QRS complexes detection for ECG signal: The Difference Operation Method," Computer Methods and Programs in Biomedicine, vol. 91, pp. 245-254, 2008.