

3D IMAGE RECONSTRUCTION USING MULTIPLE IMAGES

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of the Requirements for the Award of the Degree of*

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In
Electronics and Communication Engineering**

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CERTIFICATE

This is to certify that the thesis entitled, “**3D image reconstruction from multiple images**” submitted by **Mr. Abhignana Mihir** and **Mr. Vinay kumar** is a record of an original research work carried out by them under my supervision and guidance in partial fulfilment of the requirements for the award of the degree of **Bachelor of Technology in Electronics and Communication Engineering** at the **National Institute of Technology, Rourkela**.

To the best of my knowledge, the matter embodied in the thesis has not been submitted to any other University/ Institute for the award of any degree or diploma.

DATE:

Dr. Ajit Kumar Sahoo

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ABSTRACT

The point in this thesis is to use a robot using which we can get photographs of a given thing from known edges. We mean to repeat and model these 2D photos to get the 3D sort of the article, which will be created and demonstrated in MATLAB. Demonstrating of 3D items from different pictures is one of the testing undertakings. Therefore our endeavor does not keep itself to giving the customer the adaptability of survey the article at any edge and in any presentation however outfits him with the complete model in space. This is an approach which retrieves the calibration from the image sequence only.

A 3D image reconstruction strategy from stereo pictures is displayed next that needs insignificant mediation from the client .The upside of this framework is that the stereo pictures don't have to be calibrated to acquire a remaking. Results for both the cam alignment and reproduction are displayed to confirm that it is conceivable to acquire a 3D model specifically from features of pictures 3D reproduction and demonstrating is utilized as a part of numerous fields like Virtual Reality, perceiving and controlling items and so on.

CHAPTER1: INTRODUCTION

1 INTRODUCTION:

The target of this thesis is to present a programmed 3D remaking strategy that employs stereo pictures and multiple images of a scene. The theme of acquiring 3D models from pictures is a genuinely new research field in PC vision. In photogrammetry, then again, this field is settled and has been round since almost the same time as the revelation of taking pictures itself. Though photogrammetrists are typically intrigued by construction itemized and precise 3D models from pictures, in the field of PC vision work is being done on computerizing the recreation issue and actualizing a keen human like framework that is fit for removing important data from picture information. This thesis will also present the 3D reconstruction using stereo images. The pair of images can be acquired from a single camera or from multiple cameras in stereo image reconstruction.

1.1 THE 3D RECONSTRUCTION PROBLEM:

Structure from uncalibrated pictures just prompts a projective reconstruction. Faugeras characterizes a matrix called the fundamental matrix, which portrays the projective structure of stereo images. Numerous calculations for deciding the fundamental matrix have subsequent to been added to. Strong routine for deciding the fundamental are particularly essential when managing genuine picture information. This picture information is as a rule as corners (high curve focuses), as they can be effectively spoke to and controlled in projective geometry. There are different corner identification calculations. The ones utilized in this proposition are by Kitchen and Rosenfeld and Harris and Stephens . On the other hand, Taylor and Kriegman develop a recreation calculation utilizing line fragments rather than corners. Image matching forms a fundamental part of epipolar analysis. Corners are accessed in both images independently, and the matching algorithm needs to pair up the corner points correctly. Initial matches are obtained by correlation and relaxation techniques. To update the projective reconstruction to a metric or Euclidean one, 3D vision is partitioned or stratified into four geometry gatherings, of which projective geometry shapes the premise. The four geometry strata are projective, relative, metric and Euclidean geometry. Stratification of 3D vision makes it simpler to perform a reconstruction.

1.2 3D RECONSTRUCTION

In a considerable lot of the previously stated claims, one of the important PC vision errands is the reconstruction of three-dimensional structure from two-dimensional advanced pictures. Amid the picture development procedure of the camera, express 3D data about the scene or protests in the scene is lost. In this manner, 3D structure or profundity data must be gathered certainly from the 2D power pictures. This issue is usually alluded to as 3D reconstruction.

The built systems for reconstructing 3D structure vary regarding the signals that they misuse, the quantity of pictures needed, and whether the routines are active or passive . Active routines are those in which the bounds of the vision framework are changed purposively for 3D image reconstruction.

1.2.1 Structure from Stereo

Structure from stereo uses cam pictures that are taken from diverse perspectives. For excellent binocular stereo, a solitary pair of pictures of the same item or scene is taken all the while by two cams situated at two distinctive spatial areas and here and there with diverse introduction. 3D structure is recouped in a manner undifferentiated from human stereopsis. Computational strategies utilize the area counterbalance of the substance between the two pictures to see profundity. On the other hand, the question for the comparing components in the two pictures stays to be a testing and unsolved issue.

1.2.2 Structure From Motion

Structure-from-motion utilizes a monocular succession of pictures that are examined in time. Over the course of the succession, either the cam, the scene, or both the cam and the scene experience some manifestation of movement. Natural seen frameworks use visual movement to derive properties of the three-dimensional world . In a comparable way, the examination of the evident movement of items in advanced pictures gives a solid visual signal to improving structure. Albeit theoretically, 3D image reconstruction from movement is like that from stereo, the computational methods are exceptionally distinctive as a result of the diverse properties controlled by the accessible pictures in every strategy. One downside utilizing movement is that the evaluated structure is just correct to a scale variable and any commotion

included in the process has a critical effect on the exactness of the image reconstruction.

1.2.3 Combination of Stereo and Motion

Numerous stereo sets of pictures that are nearly examined in time are caught, which give both stereo and visual movement signals for comprehension structure. Moreover, stereo and movement supplement one another in a specific manner when they are coordinated into a solitary reproduction framework. The outcomes from past work demonstrate that the utilization of stereo picture successions is a promising heading to seek after, however existing systems approach the issue from every distinctive course, every tending to a specific part of the reproduction issue without much thought of alternate viewpoints.

1.3 Thesis Overview

This proposal is fundamentally inspired by the issue of recuperating 3D data about an unbending item in a scene from advanced cam pictures; it expands on the work of numerous past endeavors to settle the issue of 3D reconstruction utilizing multiple images and stereo images. In Chapter 2 we are going to cover about 3D image reconstruction using multiple images and in chapter 3 we are going to cover about 3D image reconstruction using stereo images. Chapter 2 describes briefly about stratification of 3D vision, camera model and epipolar geometry, fundamental matrix estimation, camera calibration and stratified 3D reconstruction,

CHAPTER2: 3D IMAGE RECONSTRUCTION USING MULTIPLE IMAGES

2.1 INTRODUCTION:

Euclidean geometry portrays a 3D world exceptionally well. As a sample, the sides of items have known or measurable lengths, crossing lines focus points in the middle of them, and lines that are parallel on a plane will never meet. At the same time, regarding the matter of depicting the imaging methodology of a cam, the Euclidean geometry is not adequate, as it is impractical to focus lengths what's more, points any longer, and parallel lines may converge.

3D vision can be partitioned into four geometry gatherings or strata, of which Euclidean geometry is one. The least difficult gathering is projective geometry, which shapes the premise of every single other gathering. The different gatherings incorporate relative geometry, metric geometry and after that Euclidean geometry. These geometries are subgroups of one another, metric being a subgroup of relative geometry, and both these being subgroups of projective geometry.

Projective geometry considers viewpoint projections, and all things considered models the imaging methodology exceptionally well. Having a model of this viewpoint projection, it is conceivable to update the projective geometry later to Euclidean, by means of the relative and metric geometries.

Algebraic and projective geometry frames the premise of most PC vision assignments, particularly in the fields of 3D reconstruction from pictures and cam self-calibration.

2.2 PROJECTIVE GEOMETRY:

2.2.1 Homogeneous Coordinates and other Definitions

A point in projective space (n -measurements), P^n , is spoken to by a $(n + 1)$ -vector of directions $x = [x_1, \dots, x_{n+1}]^T$. No less than one of the x_i coordinates must be nonzero. Two focuses spoken to by $(n + 1)$ -vectors x and y are viewed as equivalent if a nonzero scalar λ exists such that $x = \lambda y$. Balance between focuses is shown by $x \sim y$. Since scaling is not essential in projective geometry, the vectors portrayed above are called homogeneous directions of a point.

A collineation or straight change of P^n is characterized as a mapping between projective spaces which safeguards collinearity of any arrangement of focuses. This mapping is spoken to by a

$(m + 1) \times (n + 1)$ grid H , for a mapping from $P^n \rightarrow P^m$. Again for a nonzero scalar λ , λH also, λH speak to the same collineation. In the event that H is a $(n + 1) \times (n + 1)$ lattice, then H characterizes a collineation from P^n into itself.

A projective premise for P^n is characterized as any situated of $(n+2)$ focuses of P^n , such that no $(n+1)$ of them are straightly subordinate. The set $e_i = [0 \dots 1 \dots 0]^T$, for $i = 1, \dots, n+1$, where 1 is in the i^{th} position, and $e_{n+2} = [1 \ 1 \ \dots \ 1]^T$ structure the standard projective premise. A projective point of P^n spoke to by any of its arrange vectors x can be depicted as a straight mix of any $n+1$ points.

$$x = \sum_{i=1}^{n+1} x_i \cdot e_i \dots \dots \dots (2.1)$$

Any projective premise can be changed by a collineation into a standard projective premise: "let x_1, \dots, x_{n+2} be $n + 2$ direction vectors of focuses in P^n , no $n + 1$ of which are directly subordinate, i.e., a projective premise. On the off chance that $e_1, \dots, e_{n+1}, e_{n+2}$ is the standard projective premise, then there exists a nonsingular lattice A such that $Ae_i = \lambda_i x_i$, $i = 1, \dots, n+2$, where the λ_i are nonzero scalars; any two lattices with this property vary at most by a scalar element".

2.2.2 PROJECTIVE PLANE:

The projective space P^2 is known as the projective plane. A point in P^2 is characterized as a 3-vector $x = [x_1 \ x_2 \ x_3]^T$, with $(u, v) = (\frac{x_1}{x_3}, \frac{x_2}{x_3})$ the Euclidean position on the plane. A line is likewise characterized as a 3-vector $l = [l_1 \ l_2 \ l_3]^T$ and having the mathematical statement of

$$\sum_{i=1}^3 l_i \cdot x_i = 0 \dots\dots\dots (2.2)$$

Point x is located on a line of

$$l^T \cdot x = 0 \dots\dots\dots (2.3)$$

This mathematical statement can be known as the line comparison, which implies that x is spoken to by a set of lines through it, or this mathematical statement is known as the point comparison, which implies that a line l is spoken to by an arrangement of focuses. These two announcements demonstrate that there is no distinction between focuses and lines in P^2 . This is known as the rule of duality. Any hypothesis or articulation that is valid for the projective plane can be revamped by substituting focuses for lines and lines for focuses, and the subsequent explanation will likewise be valid.

2.3 AFFINE GEOMETRY:

This stratum lies between the projective and metric geometries and contains more structure than the projective stratum, however not exactly the metric and Euclidean ones.

2.3.1 AFFINE PLANE:

The line in the projective plane with $x_3 = 0$ is known as the line at unendingness or l_1 . It is spoken to by the vector $l_1 = [0 \ 0 \ 1]^T$. The relative plane can be thought to be inserted in the projective plane under a correspondence of $A_2 \rightarrow P_2$: $X = [X_1 \ X_2]^T \rightarrow [X_1 \ X_2 \ 1]^T$. There "is a coordinated correspondence between the relative plane and the projective plane less the line at vastness with mathematical statement $x_3 = 0$ ". For a projective point $x = [x_1 \ x_2 \ x_3]^T$ that is not at stake at vastness, the relative parameters can be ascertained as $X_1 = \frac{x_1}{x_3}$ furthermore,

$$X_2 = \frac{x_2}{x_3}.$$

To ascertain any line's point at endlessness, this line needs to be just met with l_∞ . In the event that such a line is characterized as in mathematical statement, this convergence point is at $[-l_2 \ l_1 \ 0]^T$ or $l \times l_\infty$. Utilizing mathematical statement, the vector $[-l_2 \ l_1]^T$ gives the heading

of the relative line $l_1x_1 + l_2x_2 + l_3 = 0$. The relationship of the line at endlessness and the relative plane is then as takes after: any point $x = [x_1, x_2, 0]^T$ on l_∞ gives the course in the hidden relative plane, with the bearing being equivalent to the vector $[x_1, x_2]^T$.

Considering two parallel (not identical) lines in affine space, they must have the same path parallel to the vector $[-l_2 \ l_1]^T$. Then considering them as projective lines of the projective plane, they must intersect at the point $[-l_2 \ l_1 \ 0]^T$ of l_∞ . That shows that two different parallel lines intersect at a point of l_∞ .

2.4 METRIC GEOMETRY:

This stratum compares to the gathering of likenesses. The changes in this gathering are Euclidean changes, for example, pivot and interpretation. The metric stratum takes into account a complete remaking up to an obscure scale.

2.4.1 METRIC PLANE:

Relative changes can be adjusted to save the line at unendingness, as well as save two focuses on that line called unquestionably the outright focuses or circular points. The round focuses are two unpredictable reciprocal focuses lying at stake at endlessness. They are represented by $I = [1, i, 0]^T$ and $J = [1, -i, 0]^T$ with $i = \sqrt{-1}$.

Circular points are used to determine the angle between two lines .It is calculated by Laguerre Formula.

$$\alpha = \frac{1}{2i} \log(\{l_1 \ l_2; i_m \ j_m\}) \dots \dots \dots (2.4)$$

Expressed in words: "the point between two lines l_1 and l_2 can be characterized by considering their purpose of convergence m and the two lines i_m and j_m joining m to indisputably the focuses I and J ".The Laguerre equation can likewise be expressed in an unexpected way: it is equivalent to the cross-proportion of the four focuses I, J, m_1 and m_2 of convergence of the four lines with the line at limitlessness.

2.5 EUCLIDEAN GEOMETRY:

Euclidean geometry is the same as metric geometry, the main contrast being that the virtual lengths are moved up to total lengths. This implies that the Euclidean change framework is the same as in comparison (2.33), however without the scaling component

$$T_E \sim \begin{bmatrix} C & b \\ 0_3^T & 1 \end{bmatrix} \dots\dots\dots (2.5)$$

All through the proposition, strong images speak to vectors and grids. In the accompanying sections, the accompanying documentation is utilized to speak to the homogeneous directions of a vector: $m = [x, y]^T \rightarrow m \sim = [m, 1]^T$

2.6 CAMERA MODEL AND EPIPOLAR GEOMETRY:

2.6.1 CAMERA MODEL:

A camera is normally depicted utilizing the pinhole model. As specified, there exists a collineation which plots the projective space to the cam's retinal plane: $P^3 \rightarrow P^2$. At that point the directions of a 3D point $M = [X \ Y \ Z]^T$ in an Euclidean world direction framework what's more, the retinal picture coordinates $m = [u \ v]^T$ are connected by the accompanying mathematical statement:

$$sm \sim = PM \sim \dots\dots\dots (2.6)$$

where s is a scale component, $m \sim = [u \ v \ 1]^T$ and $M \sim = [X \ Y \ Z \ 1]^T$ are the homogeneous directions of vector m and M, and P is a 3×4 framework speaking to the collineation:

$P^3 \rightarrow P^2$. P is known as the viewpoint projection matrix.

Figure represents this methodology. The figure demonstrates the situation where the projection focus is set at the root of the world direction outline and the retinal plane is at

$Z = f = 1$. At that point $u = \frac{f \cdot x}{z}$, $v = \frac{f \cdot y}{z}$ and

$$P = [I_{3 \times 3} \quad O_{3 \times 3}] \dots\dots\dots (2.7)$$

The optical hub goes through the focal point of projection (cam) C and is perpendicular to the retinal plane. The point c is known as the main point, which is the convergence of the optical hub with the retinal plane. The central length f of the cam is additionally indicated, which is the separation of the focal point of two planes.

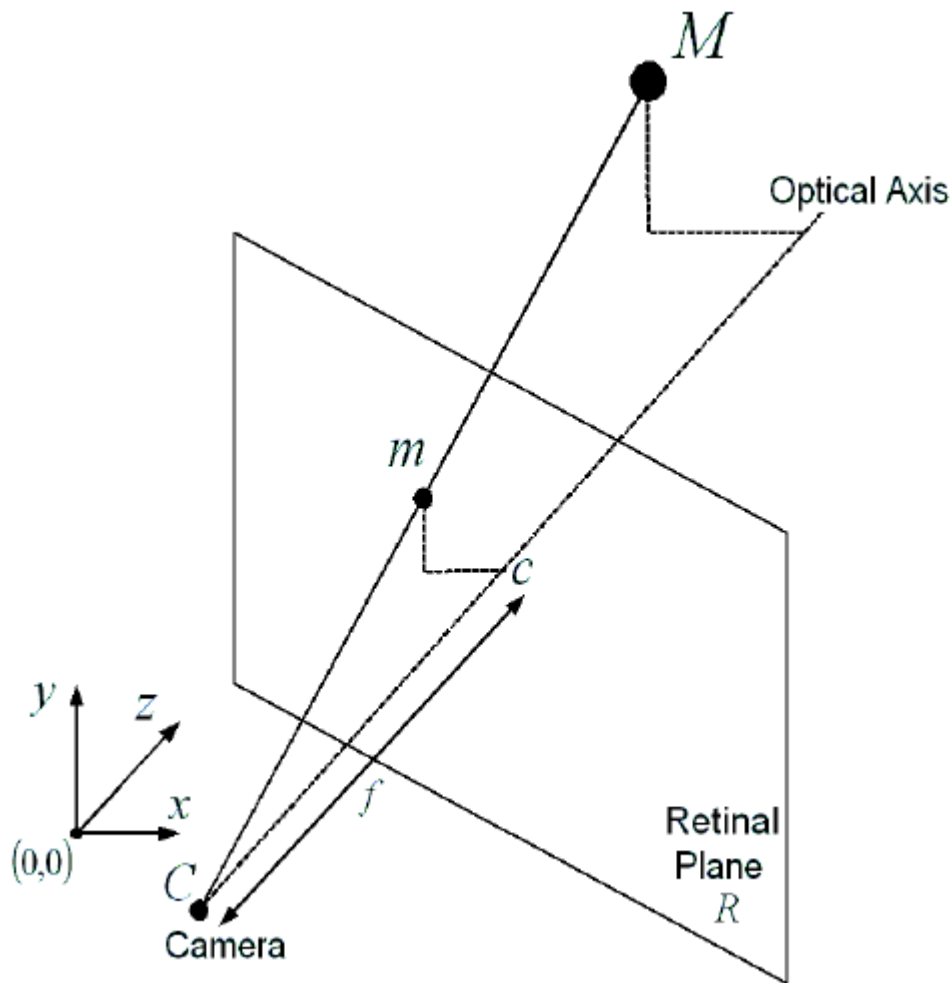


FIGURE2. 1 PERSPECTIVE PROJECTION

If the point of view projection grid P is accessible, it is conceivable to recoup the directions of the optical focus or cam. The world direction framework is typically characterized as takes after: the positive Y -heading is indicating upwards, the positive X-course is indicating the privilege and the positive Z-heading is indicating into the page.

2.6.2 CALIBRATION MATRIX:

The stereo camera adjustment grid, indicated by K, contains the inborn constraints of the camera utilized as a part of the imaging methodology. This grid is utilized to change over between the retinal plane and the real picture plane:

$$k = \begin{bmatrix} \frac{f}{p_u} & \tan \alpha \cdot \frac{f}{p_v} & u_0 \\ 0 & \frac{f}{p_v} & v_0 \\ 0 & 0 & 1 \end{bmatrix} \dots \dots \dots (2.8)$$

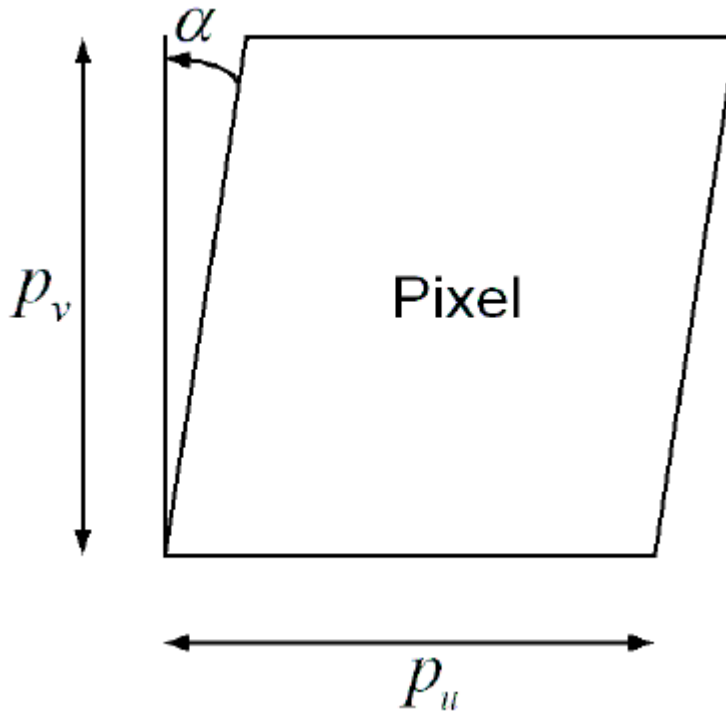


FIGURE 2. ILLUSTRATION OF PIXEL SHOW

Here, the central length f goes about as a scale component. In an ordinary cam, the central length specified above does not for the most part relate to 1. It is likewise conceivable that the central length changes amid a whole imaging methodology, so that for every picture the cam alignment lattice needs to be restored. The qualities p_u and p_v speak to the width and stature of the pixels in the picture, $c = [u_0, v_0]^T$ is the vital point and is the skew edge.

$$k = \begin{bmatrix} f_u & s & u_0 \\ 0 & f_v & v_0 \\ 0 & 0 & 1 \end{bmatrix} \dots\dots\dots (2.9)$$

Here f_u, f_v are the focal lengths which are measured in width and height of the pixels.

2.7 EPIPOLAR GEOMETRY:

The epipolar geometry occurs between a two camera system. With reference to figure 3.3, the two cameras are spoken to by C_1 and C_2 . Focuses m_1 in the picture 1 and m_2 in the picture 2 are the mapped purposes of the 3D points M . Focuses e_1 and e_2 are the supposed epipoles, and they are the convergences of the line joining the two cams C_1 and C_2 with both picture planes or the projection of the cams in the inverse picture. The plane framed with the three focuses $\langle C_1 M C_2 \rangle$ is known as the epipolar plane. The lines l_{m1} and l_{m2} are known as the epipolar lines and are framed when the epipoles and picture focuses are merged.

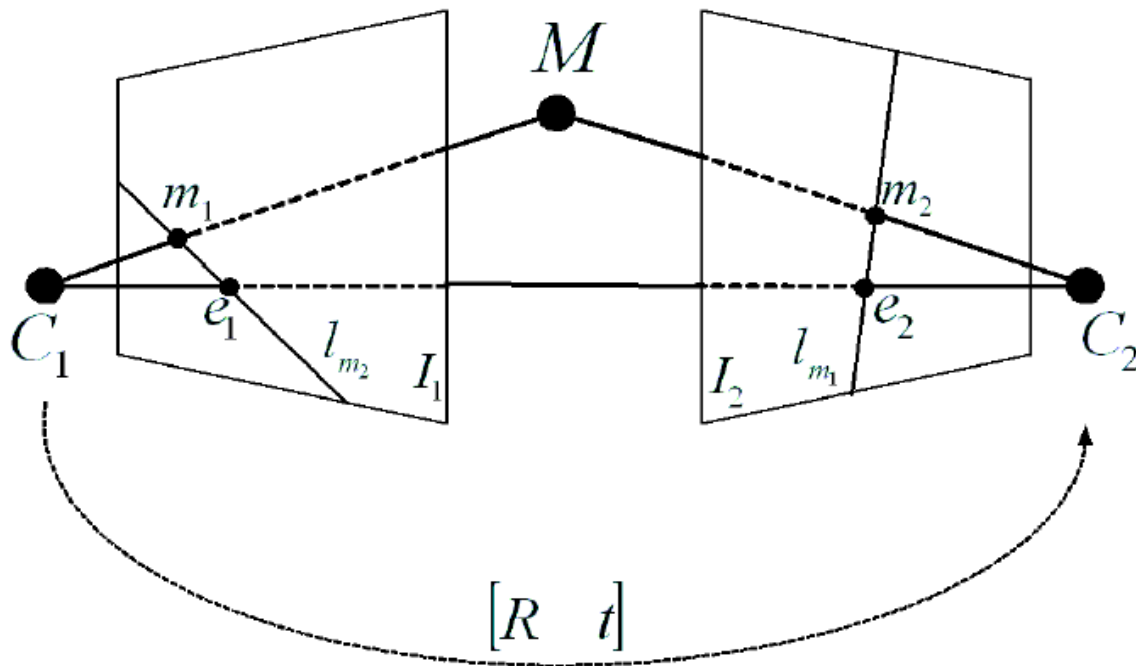


FIGURE 2.3 EPIPOLAR GEOMETRY

m_2 is obliged to lie on the epipolar line l_{m_1} of point m_1 . It is known as the epipolar imperative. To picture it in a different way: the epipolar line l_{m_1} is the connection of the epipolar plane said above with the second picture plane I_2 . This implies that picture point m_1 can compare to any 3D point on the line $\langle C_1M \rangle$ and that the estimate of $\langle C_1M \rangle$ in the second picture I_2 is the line l_{m_1} . All epipolar lines of the focuses in the first picture go through the epipole e_2 and shape therefore a pencil of planes containing the baseline $\langle C_1C_2 \rangle$. Expressing the epipolar imperative mathematically, the accompanying comparison needs to be fulfilled in request for m_1 and m_2 to be matched.

$$m_2^{\sim T} \cdot F \cdot m_1^{\sim} = 0 \dots\dots\dots (2.10)$$

Here F is called the *fundamental matrix*.

The following equation also holds:

$$l_{m_1} = F \cdot m_1^{\sim} \dots\dots\dots (2.11)$$

Here the point m_2 corresponding to point m_1 belongs to the line l_{m_1} .

$$F = K_2^{-T} [t]_x \cdot R \cdot K_1^{-1} \dots\dots\dots (2.12)$$

where $[t]_x$ is the antisymmetric matrix as described in the above equation. K_1 and K_2 are the camera calibration matrices for each camera, and R and t describe a change (turn and interpretation) which gets focuses communicated the first arrange framework to the second one.

The other property of fundamental matrix is

$$F \cdot e_1 \sim = F^T \cdot e_2 \sim = 0 \dots\dots\dots (2.13)$$

It shows that the epipolar line of epipole e_1 is $F \cdot e_1 \sim$.

2.8 FUNDAMENTAL MATRIX:

As the fundamental matrix has just seven degrees of flexibility, it is conceivable to estimate F specifically utilizing just 7 point matches. As a rule more than 7 point matches are available and a strategy for tackling the fundamental matrix utilizing 8 point matches is given.

2.8.1 LINEAR LEAST-SQUARES TECHNIQUE:

Having matched a corner point $m_{1i} = [u_{1i}, v_{1i}]^T$ in the first picture with a corner point $m_{2i} = [u_{2i}, v_{2i}]^T$ in the second picture, the epipolar mathematical statement can be composed as takes after:

$$m_{2i} \sim^T \cdot F \cdot m_{1i} \sim = 0 \dots\dots\dots (2.14)$$

The above formula can be also written as homogeneous formula in the 9 unknown coefficients of Fundamental matrix F

$$u_i^T \cdot f = 0 \dots\dots\dots (2.15)$$

where

$$u_i = [u_{1i} \cdot u_{2i} \quad v_{1i} \cdot u_{2i} \quad u_{2i} \quad u_{1i} \cdot v_{2i} \quad v_{2i} \quad u_{1i} \quad v_{1i} \quad 1]^T$$

$$f = [F_{11} \quad F_{12} \quad F_{13} \quad F_{21} \quad F_{22} \quad F_{23} \quad F_{31} \quad F_{32} \quad F_{33}]^T$$

and F_{ij} is the element of F at row i and column j .

The above equation in linear system can be presented as

$$U_n \cdot f = 0 \dots\dots\dots (2.16)$$

$$U_n = [u_1, \dots, u_n]^T$$

If that 8 or more corner point correspondences are available and disregarding the rank-2 constraint, a least-squares method can be used to solve.

$$\min_F \sum_i (m_{2i} \sim^T \cdot F \cdot m_{1i} \sim)^2$$

Which can be also written as

$$\min_f \|u_1 \cdot f\|^2 \dots\dots\dots (2.17)$$

Different strategies exist to solve for f . They are known as the 8-point algorithms, as 8 or more points are expected to solve for f . One of the techniques sets one of the coefficients of F to 1 and then solves equation using a LLS technique.

2.9 CAMERA CALIBRATION:

Calibration is a major property of 3D reproduction. Typically the interior parameters of every camera are precisely known previously and the entire environment is profoundly controlled, or an calibration object in the scene is utilized to calibrate the camera. Yet, in numerous circumstances the source of images is not known, which implies that the camera's inner parameters are additionally not known, or it is alluring to change a camera halfway through a image application. This implies that the interior parameters of the camera must be separated from the images themselves.

2.9.1 CAMERA CALIBRATION METHODS:

The classical calibration method makes utilization of an alignment example of known size inside the perspective of the camera. Infrequently this will be a level plate with a customary example marked on it. A disadvantage of these routines is that it is difficult to adjust a camera while it is included in some image tasking. In the event that any adjustment in the cam's settings happen, a rectification is unrealistic without interrupting the task. The change of the camera's settings may be an adjustment in the focal length, or little mechanical or warm changes influencing the camera as whole.

2.9.2 ESTIMATING THE PERSPECTIVE PROJECTIVE MATRIX:

By minimizing the image error, the pERspective projection grid is assessed for n 3D images M_i comparing to image points m_i . This image error is the distance between the real image point and the projection of the world point onto the image plane utilizing P . Using these comparisons $m^{\sim} = [u \ v \ 1]^T$ and $M^{\sim} = [X \ Y \ Z \ 1]^T$, three mathematical statements can

be acquired, but dividing by the third one gives two comparisons in the 12 obscure parameters of P:

$$u = \frac{P_{11} \cdot X + P_{12} \cdot Y + P_{13} \cdot Z + P_{14}}{P_{31} \cdot X + P_{32} \cdot Y + P_{33} \cdot Z + P_{34}}$$

$$v = \frac{P_{21} \cdot X + P_{22} \cdot Y + P_{23} \cdot Z + P_{24}}{P_{31} \cdot X + P_{32} \cdot Y + P_{33} \cdot Z + P_{34}}$$

The function which needs to be reduced is characterized as the squared geometric distance between the genuine image points and the projected image points:

$$E_g = \frac{1}{n} \cdot \sum_{i=1}^n [(u_i - u)^2 + (v_i - v)^2] \dots\dots\dots (2.18)$$

Above equation is non-linear and can be minimized utilizing the Levenberg-Marquardt Minimisation algorithm. Between iterations, the matrix P is more often than not scaled ($k_{pk} = 1$) or one parameter of P can be altered ($P_{34} = 1$). To find the initial estimate, as opposed to minimizing the geometric distance E_g , an arithmetical distance E_a is minimized.

$$E_a = \frac{1}{n} \cdot \sum_{i=1}^n [(u_i \cdot (P_{31} \cdot X + P_{32} \cdot Y + P_{33} \cdot Z + P_{34}) + P_{12} \cdot Y + P_{13} \cdot Z + P_{14})^2 + (v_i \cdot (P_{31} \cdot X + P_{32} \cdot Y + P_{33} \cdot Z + P_{34}) + P_{22} \cdot Y + P_{23} \cdot Z + P_{24})^2] \dots\dots\dots (2.19)$$

It is a linear equation and it can be written as

$$\min_p \|Z_p\|^2$$

The p vector is the elements of Prospective Matrix P , and the Matrix Z is

$$Z = \begin{bmatrix} M_1 \sim^T & \dots & -u_1 \cdot M_1 \sim^T \\ \vdots & \ddots & \vdots \\ O^T & \dots & -v_1 \cdot M_1 \sim^T \end{bmatrix} \dots\dots\dots (2.20)$$

2.9.3 ESTIMATING THE CAMERA CALIBRATION MATRIX:

After estimating the perspective projection matrix, 3* 3 submatrix of P can be written as

$$\begin{bmatrix} P_{11} & P_{12} & P_{13} \\ P_{21} & P_{22} & P_{23} \\ P_{31} & P_{32} & P_{33} \end{bmatrix} = K \cdot R \dots\dots\dots (2.21)$$

Here K is the camera calibration matrix and R is the orthogonal matrix

2.10 STRATIFIED 3D RECONSTRUCTION:

Here we are obtaining a 3D model of an object in a stereo image pair. 3D vision can be divided into geometry groups. Stratification is used for calculating the geometric relationship between structures in image pair.

To obtain full metric reconstruction, Projective reconstruction is needed.

2.10.1 PROJECTIVE RECONSTRUCTION:

First the Fundamental Matrix F needs to be assessed from corner point matches. The essential grid then gives the intends to register the two projective cam lattices for both the images.

Let the first camera coincide with the source of the world coordinate system. The projective camera matrix for the first camera is then characterized as follows:

$$P_1 = [I_{3 \times 3} \quad O_3] \dots\dots\dots (2.22)$$

The second projective camera matrix is picked such that the epipolar geometry relates to the recovered fundamental matrix. Generally it is characterized as follows:

$$P_2 = [M \quad \sigma e_2] \dots\dots\dots (2.23)$$

where e_2 is the epipole in the second picture and M is a component of the major network:

$F = [e_2]_x M$, where $[e_2]_x$ is the antisymmetric grid of epipole e_2 . This epipole can be extricated from the basic fundamental matrix. Variable σ represents the global scale of the reconstruction, and as that scale is not known, it is discretionarily picked and situated to 1.

Grid M is characterized as takes after:

$$M = -\frac{1}{\|e_2\|^2} \cdot [e_2]_x \cdot F \dots\dots\dots (2.24)$$

Matrix M is no single, because if M is a solution, then $M + e_2 \cdot v^T$ is also a result for a vector v .

CHAPTER 3: 3D IMAGE RECONSTRUCTION USING STEREO IMAGES

3.1 INTRODUCTION:

Stereo vision is the methodology of recovering depth from camera images by looking at two or more perspectives of the same scene. The yield of this calculation is a 3-D point cloud, where every 3-D point compares to a pixel in one of the images. Binocular stereo uses just two images, brought with cameras that were differentiated by a flat separation known as the "baseline". Aligning the stereo camera system permits us to process the 3-D world points in real units, for example, millimetres relative to the cameras.

3.1.2 OUR APPROCH:

Here we would like to use disparity map in scene reconstruction in pair of images because it has two advantages.

- Disproportion estimates are less delicate to illumination changes, as they are processed by amplifying a closeness amount on the squares in two pictures taken in the similar time. If the illumination change is not compelling, the surface similarity in the two pictures is saved.
- Background subtraction in light of profundity is much simpler than the one in light of picture intensities. To be completely frank, fundamental histogram techniques or morphological frameworks could be used to portion the closer view question despite when the foundation subtraction is not especially displayed. The slightest troublesome foundation subtraction in divergence pictures can be accomplished by straightforward thresholding which destroys the unmistakable item

Range estimation based on image disparity likewise has two disadvantages:

- Confident picture connection is conceivable just in textured regions; along these lines the inequality is not accessible at consistently coloured parts of the image. This reasons issues in assessing the profundity of the foundation dividers, for instance. Notwithstanding, people do seem sufficiently coarse in images, regardless of the fact that they are wearing uniformly coloured clothing. The wrinkles of the fabric make varying image intensity which is adequate for comparing the images. Indeed, the impact of cloth wrapping rules the surface in the lower tenacity images of people even at the point when the dress has strong patterns.

- Since separation is contrarily corresponding to uniqueness, and the pixel size is restricted, the profundity accuracy drops quickly as the partition to the cams increases. This controls the degree in which a solitary restricted pattern stereo pair is satisfactory for careful following to a couple of meters. Nevertheless, this is adequate for the framework that are away for perceiving human positions in working environments, and little meeting rooms also concerning most applications including dissimilarity control. Greater spaces can be secured by a couple of stereo framework.

Here we develop a graphical model for human appearance in disparity maps.

3.2 CALIBRATE THE STEREO CAMERA SYSTEM:

The initial step in the calibration procedure is to get a 3×3 matrix speaking to a tomography between the imaged focuses and the 3D points of the calibration design. To make this conceivable the world coordinate system is picked so that its both axes to the both axes of the pixel coordinate framework with the upper left corner point as the root . Thus a corner point which is third from the left, fourth from the top has 3D homogeneous directions $[2 \times 30, 3 \times 30, 0, 1]^T = [60, 90, 0, 1]^T$ on the planet direction outline where all units are in mm. It is demonstrated that the connection between the point on the plane and the imaged point is given by

$$x = HX^{\wedge} \dots\dots\dots (3.1)$$

Here

$$X^{\wedge} = [X \quad Y \quad 1]^T \dots\dots\dots (3.2)$$

3.2.2 INTERNAL CALIBRATION:

The ascertained homographies are utilized to place limitations on the internal parameters. To get these requirements consider the equation.

$$H = \lambda K[r_1 \quad r_2 \quad t] \dots\dots\dots (3.3)$$

where λ shows the obscure homogeneous scaling component of the assessed H. Utilizing ortho-normality of r_1 and r_2 the accompanying requirements are derived .

$$r_1^T \cdot r_2 = r_1 r_2^T \dots\dots\dots (3.4)$$

These limitations are then used to understand for the inside parameters of the camera .No less than three perspectives are obliged if no data is accessible also, two perspectives are adequate

if skew is thought to be zero. The arrangement got from this straight calculation is then used to figure the outer parameters for each view.

3.2.3 EXTERNAL CALIBRATION:

In the camera setup utilized the left cam coordinate framework is decided to be the world direction framework. The outside alignment of the stereo cam framework is at that point characterized to be the pivot and interpretation of the right cam regarding the left cam. The officially processed data can be utilized to compute these two parameters if the processings are in view of stereo pictures of the adjustment design. Accept that the turn and interpretation from the world directions to the left and right imaging planes are (R_0, t_0) and (R_1, t_1) . At that point the change from the left camera to the imaging plane is the opposite change. The change from the left cam to one side cam can then be registered as

$$\begin{bmatrix} r_1 & t_1 \\ o^T & 1 \end{bmatrix} \begin{bmatrix} R_0^T & -R_0^T \cdot t_0 \\ o^T & 1 \end{bmatrix} = \begin{bmatrix} R_1 R_0^T & -R_1 R_0^T t_0 + t_1 \\ o^T & 1 \end{bmatrix} \dots\dots\dots (3.5)$$

In prior dialogs the world directions framework is brought to correspond with the planar surface of the adjustment design. Henceforth the introduction of every cam with deference to this regular direction framework has as of now been registered. At that point for every pair of pictures we can figure the outer adjustment of the cam framework. However since Past steps utilized a solitary cam framework, the steadiness of the outer adjustment Of the stereo cam framework is not implemented amid the reckoning. This outcome in Different answers for the outer adjustment.

3.3 RECTIFICATION OF CAMERA MATRICES:

We accept that the stereo mechanical assembly is balanced, i.e., the PPMs $P_{o1} \sim$ and $P_{o2} \sim$ are known. The thought behind correction is to characterize two new PPMs $P_{n1} \sim$ and $P_{n2} \sim$ acquired by turning the old ones around their optical focuses until focal planes gets the opportunity to be coplanar, thus containing the pattern. This ensures that epipoles are at perpetuation; hence, epipolar lines are parallel. To have level epipolar lines, the example must be parallel to the new X hub of both cams. Besides, to have a real remedy, conjugate

centers must have the same vertical course. This is gotten by requiring that the new cams have the same trademark parameters. Note that, being the focal length the same, retinal planes are coplanar

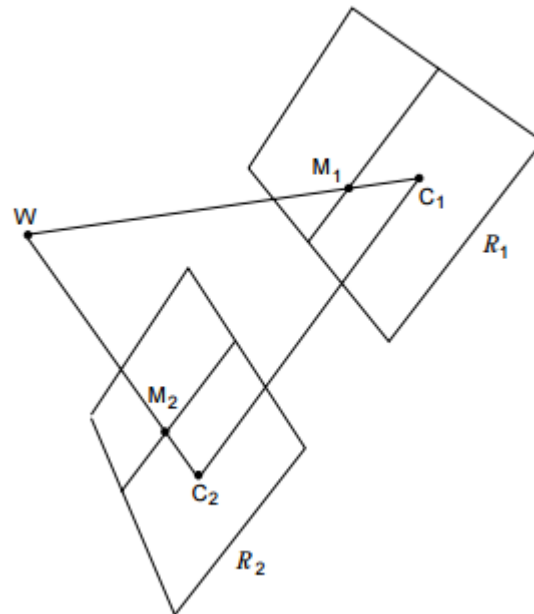


FIGURE3. 1 TRIANGULATION

In rundown: positions of the new PPMs are the same as the old cams, while the new introduction (the same for both cams) contrasts from the old ones by suitable turns; characteristic parameters are the same for both cams. Thusly, the two consequent PPMs will differentiate just in their optical focuses, and they can be thought as a solitary cam interpreted along the X pivot of its reference framework.

Give us a chance to create the new PPMs to the extent their factorization.

$$p_{n_1} \sim = A|R| - Rc_1]$$

$$p_{n_2} \sim = A|R| - Rc_2]$$

The intrinsic parameters lattice A is equal for both PPMs, what's more, can be picked randomly. The optical focuses c₁ and c₂ are given by the old optical focuses, processed with Equation. The matrix R, which gives the cam's posture, is equal for both PPMs. It will be determined by method for its row vectors.

$$R = \begin{bmatrix} r_1^T \\ r_2^T \\ r_3^T \end{bmatrix} \dots\dots\dots (3.6)$$

Those are the X, Y, and Z pivots, separately, of the camera reference axis, communicated in

world coordinates. As indicated by the past remarks, we take:

1. The new X-pivot parallel to the standard baseline: $r_1 = \frac{(c1 - c2)}{||c1 - c2||}$
2. The new Y-pivot orthogonal to X (required) and to k: $r_2 = k \wedge r_1$.
3. The new Z-pivot orthogonal to XY (required) : $r_3 = r_1 \wedge r_2$

In suspicion 2, k is a self-confident unit vector, which fixes the position of the new Y hub in the plane orthogonal to X. We take it proportionate to the Z unit vector of the old left grid, along these lines obliging the new Y pivot to be orthogonal to both the new X and the old left Z.

This estimation comes up short when the optical pivot is parallel to the pattern, i.e., when there is a flawless forward movement.

3.4 DENSE BASED CONVERSION:

Most semiautomatic routines for stereo transformation use depth maps and profundity image based rendering. The depth guide is a different grayscale image having the same measurements as the original 2D image, with different shades of dim to demonstrate the depth of all aspects of the casing.

3.5 BINOCULAR DISPARITY:

With two images of the same scene caught from somewhat distinctive perspective points, the binocular disparity can be used to recuperate the depth of an object. This is the primary system for depth perception. To begin with, set of corresponding points in the image pair are found. At that point, by method for the triangulation technique, the depth data can be recovered with a high level of exactness when all the parameters of the stereo system are known. At the point when just characteristic camera parameters are accessible, the depth can be recouped effectively up to a scale component. When no camera parameters are known, the

subsequent depth is right up to a projective transformation .

The uniqueness estimation of a point is regularly interested as the inversed separations to the watched objects. Consequently, discovering the disparity map is key for the development of the depth map. Epipolar geometry and camera adjustment are the two most every now and again utilized limitations. With these two limitations, image pairs can be corrected. Another broadly acknowledged presumption is the photometric constraint, which expresses that the intensities of the comparing pixels are like one another. The requesting requirement expresses that the order of points in the picture pair is normally the same.

3.5.2 DISPARITY ESTIMATION:

In our investigations, we utilized the financially accessible real-time stereo framework called Triclops which is manufactured by Point- Dark .As of now, this system runs at casing rate with image size of 160x120, and gives for every pixel the uniqueness between the pictures from a image pair. The system has three cameras so that the even and vertical disparity can both be utilized to reduce the correlation problems. The accompanying comparisons portray the relation between the 3-D coordinates $x=[x \ y \ z]'$ of a point imaged by the stereo framework, the directions of the point's viewpoint projection onto the picture plane $[X \ Y]'$ and the uniqueness $D(X, Y)$:

$$x = \frac{Xz}{f} \dots\dots\dots (3.7)$$

$$z = \frac{bf}{D(X,Y)} \dots\dots\dots (3.8)$$

$$y = \frac{Yz}{f} \dots\dots\dots (3.9)$$

Here b implies the standard baseline length, and f is the focal length of the cameras. A sample of a difference map $D(X,Y)$ is given. Pixels for which uniqueness couldn't be evaluated because of the absence of surface are dark.

CHAPTER4: RESULT AND DISCUSSION

4.1 SIMULATION RESULTS:

The results obtained after simulating the code has been shown below. For the reconstruction of 3D image from multiple images 5 images have been taken from multiple views.by using these 5 images the article has been reconstructed.

4.1.1 3D IMAGE RECONSTRUCTION FROM MULTIPLE IMAGES:

INPUT IMAGES:



OUTPUT IMAGE:

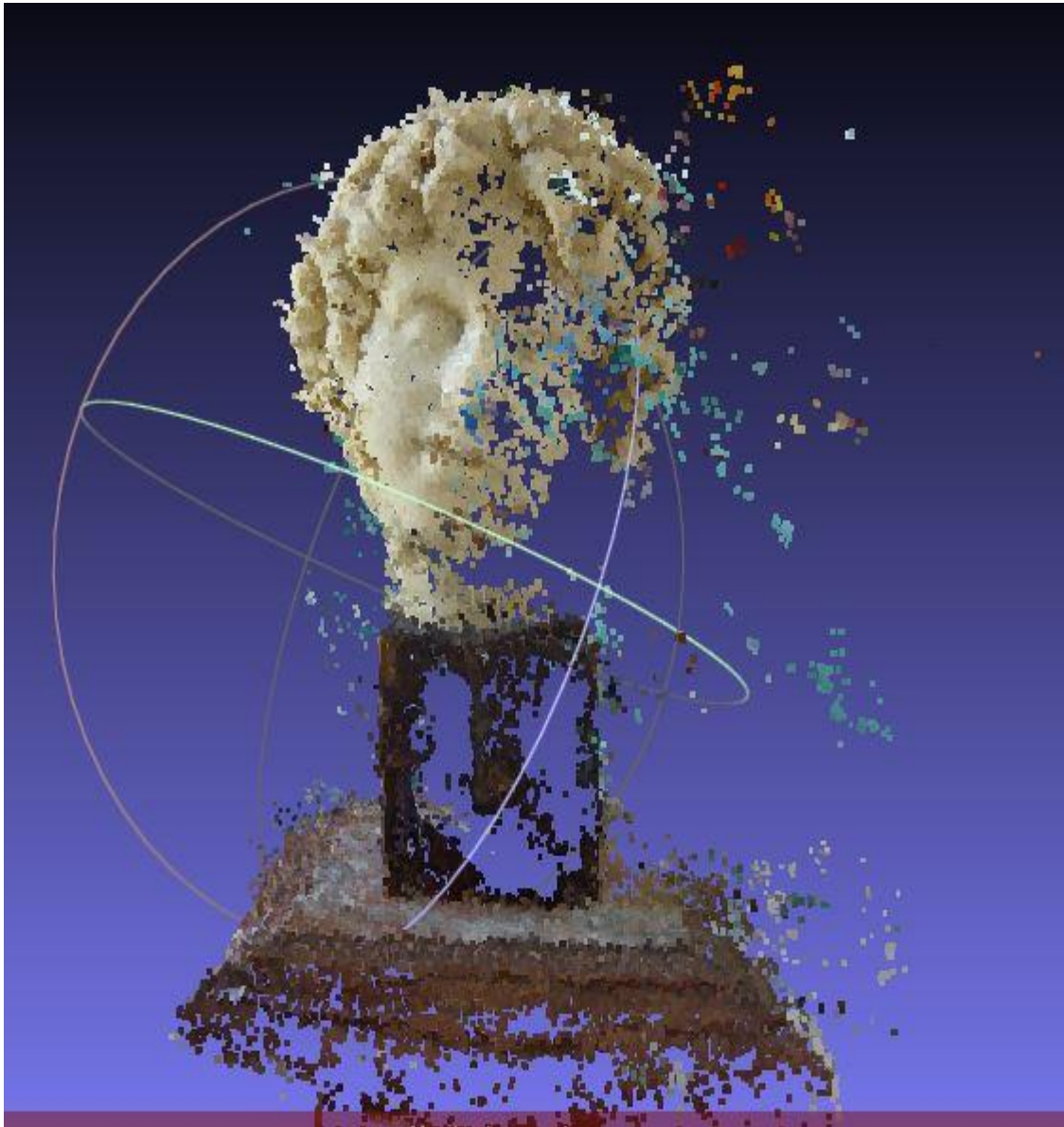
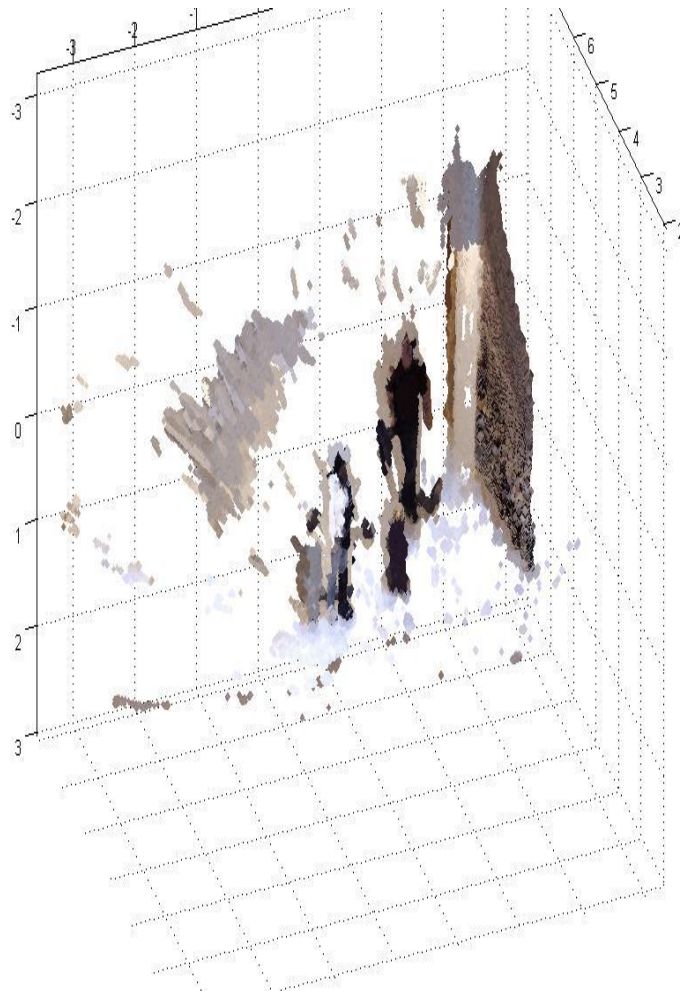


FIGURE4. 1 3D RECONSTRUCTED IMAGE

4.1.2 3D IMAGE RECONSTRUCTION FROM STEREO IMAGES:

INPUT IMAGES:



OUTPUT IMAGE:**FIGURE4. 2 3D POINT CLOUD****4.2 CONCLUSION:**

The trials talked about in Section 4.1 utilizing manufactured information consolidate a large portion of the critical components of the work in this theory. The outcomes are very persuading and propose that the ideas exhibited so far are doable and are advantageous for examination. Obviously, almost a perfect circumstance has been made utilizing the

engineered information on the grounds that the majority of the highlights are unmistakable by any means times and the movement of the item conforms to the movement model utilized for the calculation. At the point when connected to a real image arrangement, the outcomes are not as acceptable, which recommend that there is still a significant measure of chance to improve set up for the incremental reproduction calculation to be usable in a continuous application.

4.3 FUTURE WORK:

Not very shockingly, the work in this postulation has in no way, shape or form tended to all the issues nor does it give a perfect answer for the 3D reconstruction issue. Numerous subtle elements have been considered in any case, are purposefully overlooked in this postulation in light of the fact that they require more far reaching research that is not plausible since time is running short limitations on this postulation. The accompanying rundown of potential future exploration is not intended to be comprehensive; in any case, it addresses the more immense errands required before an era quality incremental 3D reproduction system can be fulfilled.

Local feature matching:

The approach that this proposal has taken for highlight coordinating is to simply use epipolar and movement requirements to survey potential arranging candidates. The qualities of this methodology are that it can for the most part be connected to any sorts of features, dodging the pitfalls when lighting conditions and geometric contorting cause the highlights to look through and through changed, and the computational cost is low.

Global constraints:

Presently, no worldwide imperatives, for example, uniqueness and contrast smoothness are constrained on the stereo arranging piece of the work.. One conceivable basic expansion is to implement the balanced relationship between highlights in the left and the right pictures. In the present set-up, every highlight on the left picture is guaranteed to have stand out coordinating highlight from the right. On the other hand, the converse is not forced. A portion of the highlight crisscrosses may have been evaded on the off chance that we additionally implement that every highlight point in the right picture has one and only match from the left picture.

As a consummation take note of, one lesson that has been adapted before the end of this proposition is that in any case of the measure of exploration that regardless of the measure of investigation that has starting now been done in the past two decades, the issue of 3D remaking from numerous photos still stays, to some degree, unsolved. There are numerous issues and potential outcomes yet to be considered and investigated. From scrutinizing existing written work and individual experience, it has been viewed that it is difficult to add to a PC vision framework that is totally independent with no human alignment of parameters or different sorts of intervention.

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