PHYSICAL REVIEW C 72, 044902 (2005)

## Incident energy dependence of $\boldsymbol{p}_{\boldsymbol{t}}$ correlations at relativistic energies

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We present results for two-particle transverse momentum correlations, $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$, as a function of event centrality for $\mathrm{Au}+\mathrm{Au}$ collisions at $\sqrt{s_{N N}}=20,62,130$, and 200 GeV at the BNL Relativistic Heavy Ion Collider. We observe correlations decreasing with centrality that are similar at all four incident energies. The correlations multiplied by the multiplicity density increase with incident energy, and the centrality dependence may show evidence of processes such as thermalization, jet production, or the saturation of transverse flow. The square root of the correlations divided by the event-wise average transverse momentum per event shows little or no beam energy dependence and generally agrees with previous measurements made at the CERN Super Proton Synchrotron.

The study of event-by-event fluctuations in global quantities, which are intimately related to correlations in particle production, may provide evidence for the production of quarkgluon plasma (QGP) in relativistic heavy-ion collisions [1-15]. Various theoretical works predict that the production of a

QGP phase in relativistic heavy-ion collisions could produce significant dynamic event-by-event fluctuations in apparent temperature, mean transverse momentum, multiplicity, and conserved quantities such as net charge. Several recent experimental studies at the CERN Super Proton Synchrotron (SPS)
[16-18] and at the BNL Relativistic Heavy Ion Collider (RHIC) [19-24] have focused on the study of fluctuations and correlations in relativistic heavy-ion collisions. One possible signal of the QGP would be a nonmonotonic change in $p_{t}$ correlations as a function of centrality and/or as the incident energy is raised [8].

Here we report an experimental study of the incident energy dependence of $p_{t}$ correlations we obtained by using $\mathrm{Au}+\mathrm{Au}$ collisions ranging in center-of-mass energy from the highest SPS energy to the highest RHIC energy, which we measured by using the solenoidal tracker at RHIC (STAR) detector.

Fluctuations involve a purely statistical component arising from the stochastic nature of particle production and detection processes, as well as a dynamic component determined by correlations arising in various particle production processes. In this paper we first unambiguously demonstrate the existence of a finite dynamical component at all four incident energies by comparing the distribution of measured event-wise average transverse momentum per event, $\left\langle p_{t}\right\rangle$, with the same quantity from mixed events. We then analyze these dynamical fluctuations by using the two-particle transverse momentum correlations defined as covariance,

$$
\begin{equation*}
\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle=\frac{1}{N_{\text {event }}} \sum_{k=1}^{N_{\text {event }}} \frac{C_{k}}{N_{k}\left(N_{k}-1\right)} \tag{1}
\end{equation*}
$$

where

$$
\begin{equation*}
C_{k}=\sum_{i=1}^{N_{k}} \sum_{j=1, i \neq j}^{N_{k}}\left(p_{t, i}-\left\langle\left\langle p_{t}\right\rangle\right\rangle\right)\left(p_{t, j}-\left\langle\left\langle p_{t}\right\rangle\right\rangle\right), \tag{2}
\end{equation*}
$$

$N_{\text {event }}$ is the number of events, $p_{t, i}$ is the transverse momentum of the $i$ th track in each event, and $N_{k}$ is the number of tracks in the $k$ th event. The overall event average transverse momentum $\left\langle\left\langle p_{t}\right\rangle\right\rangle$ is given by

$$
\begin{equation*}
\left\langle\left\langle p_{t}\right\rangle\right\rangle=\left(\sum_{k=1}^{N_{\text {event }}}\left\langle p_{t}\right\rangle_{k}\right) / N_{\text {event }} \tag{3}
\end{equation*}
$$

where $\left\langle p_{t}\right\rangle_{k}$ is the average transverse momentum per event given by

$$
\begin{equation*}
\left\langle p_{t}\right\rangle_{k}=\left(\sum_{i=1}^{N_{k}} p_{t, i}\right) / N_{k} . \tag{4}
\end{equation*}
$$

$\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ is independent, to first order, of detection efficiencies because both the numerator $C_{k}$ and the denominator $N_{k}\left(N_{k}-1\right)$ are proportional to the square of the particle detection efficiency. Therefore the efficiency cancels. By construction, $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ is zero within statistics for properly mixed events because all correlations are removed. Note that we use mixed events only in Fig. 1.

We measured the data used in this analysis by using the solenoidal tracker at RHIC (STAR) detector to study $\mathrm{Au}+\mathrm{Au}$ collisions at $\sqrt{s_{N N}}=20,62,130$, and 200 GeV [25]. The main detector was the time-projection chamber (TPC) located in a solenoidal magnetic field. The magnetic field was 0.25 T for the $20-$ and $130-\mathrm{GeV}$ data and 0.5 T for the $62-$ and $200-\mathrm{GeV}$ data. Tracks from the TPC with $0.15 \mathrm{GeV} / c \leqslant p_{t} \leqslant 2.0 \mathrm{GeV} / c$ with $|\eta|<1.0$ were used in the analysis. All tracks were required


FIG. 1. (Color online) Histograms of the average transverse momentum per event for $\mathrm{Au}+\mathrm{Au}$ at $\sqrt{s_{N N}}=20,62,130$, and 200 GeV for the $5 \%$ most central collisions at each energy. Both data and mixed events are shown for each incident energy. The lines represent gamma distributions.
to have originated within 1 cm of the measured event vertex. Events were selected according to their distance of the event vertex from the center of STAR. Events were accepted within 1 cm of the center of STAR in the plane perpendicular to the beam direction. For the $20-$ and $130-\mathrm{GeV}$ data sets, events were accepted with vertices within 75 cm of the center of STAR in the beam direction, whereas for the $62-$ and $200-\mathrm{GeV}$ data sets, events were accepted within 25 cm of the center.

Data shown for 62,130 and 200 GeV are from minimum bias triggers. Minimum bias triggers were defined by the coincidence of two zero-degree calorimeters (ZDCs) [26] located $\pm 18 \mathrm{~m}$ from the center of the interaction region. For 20 GeV , a combination of minimum bias and central triggers was used. Centrality bins were determined by use of the multiplicity of all charged particles measured in the TPC with $|\eta|<0.5$. The centrality bins were calculated as fractions of this multiplicity distribution starting with the
highest multiplicities. The ranges used were $0 \%-5 \%$ (most central), $5 \%-10 \%, 10 \%-20 \%, 20 \%-30 \%, 30 \%-40 \%, 40 \%-$ $50 \%, 50 \%-60 \%, 60 \%-70 \%$, and $70 \%-80 \%$ (most peripheral). Each centrality was associated with a number of participating nucleons, $N_{\text {part }}$, by use of a Glauber Monte Carlo calculation [27].

We treated the variation of $\left\langle\left\langle p_{t}\right\rangle\right\rangle$ within a given centrality bin by using the following procedure. We calculated $\left\langle\left\langle p_{t}\right\rangle\right\rangle$ as a function of $N_{\mathrm{ch}}$, the multiplicity used to define the centrality bin. We fitted this dependence and used the fit in Eqs. (1)-(4) on an event-by-event basis as a function of $N_{\mathrm{ch}}$. This method removes the dependence of the experimental results on the size of the centrality bin and slightly reduces $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ by removing correlations induced by the changing of $\left\langle\left\langle p_{t}\right\rangle\right\rangle$ within the experimental centrality bins. The results presented in this paper were obtained by use of this fitting procedure.

Figure 1 shows histograms of $\left\langle p_{t}\right\rangle$ for the $5 \%$ most central $\mathrm{Au}+\mathrm{Au}$ collisions at $20,62,130$, and 200 GeV . Histograms for $\left\langle p_{t}\right\rangle$ are also shown for mixed events. The histograms for the data are wider than the histograms for mixed events, indicating that we observe nonstatistical fluctuations at all four incident energies. Similar results are obtained for all centralities. The overall normalization reflects the number events taken at each energy. The values of $p_{t}$ included in these histograms are not corrected for experimental momentum resolution, acceptance, or efficiency.

We created the mixed events at each energy by randomly selecting one track from an event chosen from measured events in the same centrality and event vertex bin. Ten centrality bins and either 5 or 10 bins (depending on the available number of events at each energy) in the event vertex position in the beam direction were used to create mixed events with the same multiplicity distribution as that of the real events. Note that we do not use mixed events for the quantitative analysis based on $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$.

The lines in Fig. 1 represent gamma distributions for both the data and mixed events. The parameters for the gamma distributions are shown in Table I. According to Ref. [28], without $p_{t}$ cuts, the parameter $\alpha$ divided by the average multiplicity in the centrality bin, $\langle N\rangle$, should be approximately two and the parameter $\beta$ multiplied by $\langle N\rangle$ should reflect the temperature parameter of the $p_{t}$ distributions. We find that


FIG. 2. (Color online) $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ as a function of centrality and incident energy for $\mathrm{Au}+\mathrm{Au}$ collisions compared with HIJING results.
$\alpha /\langle N\rangle$ varies from 2.27 to 1.93 and $\beta\langle N\rangle$ varies from 0.230 to $0.299 \mathrm{GeV} / c$ as the energy goes from 20 to 200 GeV .

To characterize the transverse momentum correlations, we use the quantity $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$, defined in Eq. (1). Figure 2 shows $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ for $\mathrm{Au}+\mathrm{Au}$ collisions at $\sqrt{s_{N N}}=20,62$, 130 , and 200 GeV as functions of centrality. One observes that $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ decreases with centrality at all four energies as expected because of a progressive dilution of the correlations resulting from the increased number of participants if the correlations are dominated by pairs of particles that originate from the same nucleon-nucleon collision. The correlations measured at 62,130 , and 200 GeV are similar, whereas the correlations for 20 GeV are smaller than those observed at the higher energies.

To explore the issue of the relative importance of shortrange correlations such as Coulomb interactions and Hanbury Brown-Twiss (HBT) effects, we extracted the correlations, excluding pairs with invariant relative momentum $q_{\text {inv }}$, less than $0.1 \mathrm{GeV} / c$, assuming that all particles were pions. We observed that $10 \%$ of the measured correlations at 62,130 , and

TABLE I. Parameters for the gamma distributions shown in Fig. 1. The gamma distribution is given by the form $f(x)=\left\{x^{\alpha-1} e^{-x / \beta} / \Gamma(\alpha) \beta^{\alpha}\right\}$ where $\alpha=\left(\mu^{2} / \sigma^{2}\right)$ and $\beta=\left(\sigma^{2} / \mu\right)$ in GeV/c; $\mu$ is the mean in $\mathrm{GeV} / c$; and $\sigma$ is the standard deviation in $\mathrm{GeV} / c$.

| Case | $\alpha$ | $\beta$ | $\mu$ | $\sigma$ |
| :--- | :---: | :---: | :---: | :---: |
| 20 GeV, real | 1096 | $4.772 \times 10^{-4}$ | 0.5228 | 0.01579 |
| 20 GeV, mixed | 1199 | $4.360 \times 10^{-4}$ | 0.5227 | 0.01510 |
| 62 GeV, real | 1445 | $3.786 \times 10^{-4}$ | 0.5471 | 0.01439 |
| 62 GeV, mixed | 1743 | $3.139 \times 10^{-4}$ | 0.5470 | 0.01310 |
| 130 GeV, real | 1556 | $3.608 \times 10^{-4}$ | 0.5614 | 0.01423 |
| 130 GeV, mixed | 1917 | $2.927 \times 10^{-4}$ | 0.5612 | 0.01282 |
| 200 GeV, real | 1853 | $3.129 \times 10^{-4}$ | 0.5799 | 0.01347 |
| 200 GeV, mixed | 2373 | $2.443 \times 10^{-4}$ | 0.5799 | 0.01190 |

200 GeV and $20 \%$ of measured correlations at 20 GeV could be attributed to these short-range correlations. These estimates agree with those extracted for $17-\mathrm{GeV} \mathrm{Pb}+\mathrm{Pb}[16]$ by use of a somewhat different method. We also estimated the contribution of resonances and other charge-ordering effects by studying the reduction in the correlations for same charge (negative) particles compared with correlations for all charged particles. This study indicated that the reduction in $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ is $40 \%$ at $20 \mathrm{GeV}, 20 \%$ at 62 and 130 GeV , and $15 \%$ at 200 GeV . We do not correct $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ for short-range correlations or resonance contributions.

The errors shown in all figures are statistical unless otherwise noted. We estimate the systematic relative errors for $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ by using studies of the effects of $p_{t}$-dependent efficiencies (1.2\%) and sensitivity to track merging and splitting ( $1.4 \%$ ). These values give an overall systematic relative error of $2 \%$. The measured correlations were lowered approximately $3 \%$ when the fitting method rather than the binning method was used. The reported values are sensitive to the $p_{t}$ cuts for kinematic and physics reasons. Using HiJing [29], we observe a $6 \%$ increase in correlations when the lower $p_{t}$ cut is removed. Raising the upper $p_{t}$ cut increases the correlations. We used $0.15 \mathrm{GeV} / c \leqslant p_{t} \leqslant 2.0 \mathrm{GeV} / c$ for all the results reported in this paper. The upper $p_{t}$ cut was chosen to be consistent with previous work [19,24].

Also shown in Fig. 2 are HIJING calculations for $\mathrm{Au}+\mathrm{Au}$ collisions at $\sqrt{s_{N N}}=20,62,130$, and 200 GeV [29]. We used HIJING version 1.36 with the default options, which include jet quenching. The hiJing results were obtained by the selection of particles with $0.15 \mathrm{GeV} / c \leqslant p_{t} \leqslant 2.0 \mathrm{GeV} / c$ with $|\eta|<1.0$ without further efficiency corrections. HIJING reproduces correlations in $p+p$ and $\alpha+\alpha$ collisions at Intersecting Storage Rings (ISR) energies [30], $p+p$ collisions at RHIC energies, and $p+\bar{p}$ collisions at CERN $\mathrm{p}+\overline{\mathrm{p}}$ Collider $(\mathrm{SppS})$ energies [31]. We use HIJING to provide a reference that incorporates a superposition of nucleon-nucleon interactions. Any differences between HIJING and the experimental results might signal phenomena unique to nucleus-nucleus collisions. The HIJING calculations exhibit little incident energy dependence and decrease with increasing centrality. The values for $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ predicted by HIJING are always smaller than the data.

To address the observed dilution of the correlations with centrality and to check the hypothesis that the correlations scale as inverse multiplicity, we multiply $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ by the charged-particle pseudorapidity density at a given centrality, $d N / d \eta$. We use fully corrected values for $d N / d \eta$ from published work [32-34]. The quantity $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ then is insensitive to efficiency and is similar to the (efficiencycorrected) quantity $\Delta \sigma_{p t}$ [19] that STAR reported previously.

In Fig. 3 we show the quantity $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ for $\mathrm{Au}+\mathrm{Au}$ collisions at $20,62,130$, and 200 GeV as functions of centrality. In this figure the errors include the quoted errors in $d N / d \eta$. This quantity increases with incident energy at all centralities. At each energy this measure of the correlations increases quickly as the collisions become more central and then saturates in central collisions. The behavior of this quantity is similar to that of the quantity $\Delta \sigma_{p t}$ previously studied by STAR [19]. This saturation might indicate effects


FIG. 3. (Color online) $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ as a function of centrality and incident energy for $\mathrm{Au}+\mathrm{Au}$ collisions compared with HIJING results.
such as the onset of thermalization [15], the onset of jet quenching [14], the saturation of transverse flow [35] in central collisions, or other processes.

In Fig. 3 the results of HIJING calculations for $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ are also shown. In contrast to the experimental results, the HIJING results show little dependence on centrality.

To account for possible changes of $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ that are due to possible changes in $\left\langle\left\langle p_{t}\right\rangle\right\rangle$ with incident energy and/or centrality of the collision, we also study the square root of the measured correlations scaled by $\left\langle\left\langle p_{t}\right\rangle\right\rangle$. The resulting quantity $\sqrt{\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle} /\left\langle\left\langle p_{t}\right\rangle\right\rangle$ is shown in Fig. 4 for $\mathrm{Au}+\mathrm{Au}$ collisions


FIG. 4. (Color online) $\sqrt{\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle} /\left\langle\left\langle p_{t}\right\rangle\right\rangle$ as a function of centrality and incident energy for $\mathrm{Au}+\mathrm{Au}$ collisions compared with HIJING results for corresponding systems. The inset shows the excitation function for the most central bin.
at $20,62,130$, and 200 GeV . Similar results from $\mathrm{Pb}+\mathrm{Pb}$ collisions at 17 GeV [16] are also shown in Fig. 4. These values are consistent with our measured results for $\mathrm{Au}+\mathrm{Au}$ at 20 GeV . We observe little or no dependence on the incident energy for this quantity. The inset in Fig. 4 demonstrates the incident energy dependence of $\sqrt{\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle} /\left\langle\left\langle p_{t}\right\rangle\right\rangle$ for the $0 \%-5 \%$ most central bin, in which the $\mathrm{Pb}+\mathrm{Pb}$ results are from Ref. [16].

In contrast to the measured correlations, HIJING predictions for $\sqrt{\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle} /\left\langle\left\langle p_{t}\right\rangle\right\rangle$ vary with incident energy. HIJING predicts a different centrality dependence as well as a noticeable dependence on the incident energy.

In conclusion we observe clear nonzero $p_{t}$ correlations, $\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ in $\mathrm{Au}+\mathrm{Au}$ collisions from $\sqrt{s_{N N}}=20$ to 200 GeV . The quantity $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ increases with beam energy. The centrality dependence of $(d N / d \eta)\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle$ may show signs of effects such as thermalization [15], the onset of jet suppression [14,24], the saturation of transverse expansion in central collisions [35], or other processes. The quantity $\sqrt{\left\langle\Delta p_{t, i} \Delta p_{t, j}\right\rangle} /\left\langle\left\langle p_{t}\right\rangle\right\rangle$ shows little or no change with beam energy. HIJING model calculations
underpredict the measured correlations and do not predict the observed centrality dependence.

## ACKNOWLEDGMENTS

We thank the RHIC Operations Group and RCF at BNL and the NERSC Center at Lawrence Berkeley National Laboratory for their support. This work was supported in part by the HENP Divisions of the Office of Science of the U.S. Department of Energy; the U.S. National Science Foundation; the Bundesministerium für Bildung, Forschung und Technologie; of Germany; IN2P3, RA, RPL, and EMN of France; Engineering and Physical Sciences Research Council of the United Kingdom; Fundacão de Amparoà Pesguisa do Estado de São Paulo of Brazil; the Russian Ministry of Science and Technology; the Ministry of Education and the NNSFC of China; IRP and GA of the Czech Republic; FOM of the Netherlands; DAE, DST, and Council of Scientific and Industrial Research of India; the Swiss National Science Foundation; the Polish State Committee for Scientific Research; and the STAA of Slovakia.
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