

1 Anticipating species distributions: handling
2 sampling effort bias under a Bayesian
3 framework

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9 December 2, 2016

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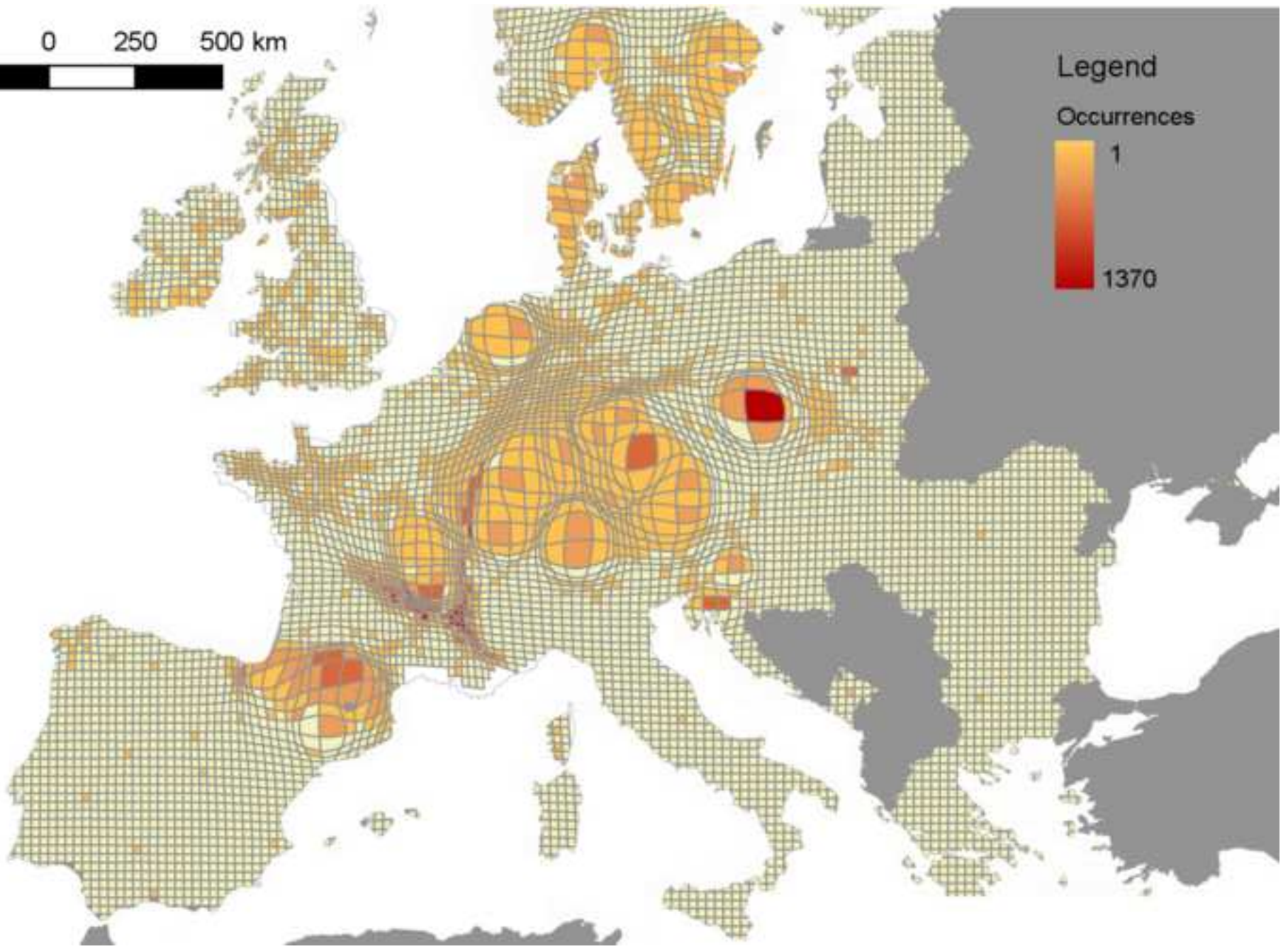
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37

Abstract

38 Anticipating species distributions in space and time is necessary for
39 effective biodiversity conservation and for prioritising management in-
40 terventions. This is especially true when considering invasive species.
41 In such a case, anticipating their spread is important to effectively plan
42 management actions. However, considering uncertainty in the output
43 of species distribution models is critical for correctly interpreting re-
44 sults and avoiding inappropriate decision-making. In particular, when
45 dealing with species inventories, the bias resulting from sampling effort
46 may lead to an over- or under-estimation of the local density of occur-
47 rences of a species. In this paper we propose an innovative method to
48 i) map sampling effort bias using cartogram models and ii) explicitly
49 consider such uncertainty in the modeling procedure under a Bayesian
50 framework, which allows the integration of multilevel input data with
51 prior information to improve the anticipation species distributions.

52

53 **Keywords:** anticipation, Bayesian theorem, sampling effort bias,
54 Species Distribution Modeling, uncertainty

55

56 **List of acronyms:** DIC: Deviance Information Criterion, MCMC:
57 Markov Chain Monte Carlo, PPD: posterior probability distribution,
58 SDM: Species Distribution Models

59 1 Introduction

60 Anticipation is an important topic in ecological fields such as food science
61 (Lobell et al., 2012), community ecology (Keddy, 1992), species distribution
62 modeling (Willis et al., 2009), landscape ecology (Tattoni et al., in press),
63 and biological invasion science (Rocchini et al., 2015). Anticipatory methods

64 are also crucial for developing effective management practices to deal with
65 invasive species (Rocchini et al., 2015).

66 Invasive species can modify the structure and functioning of ecosystems,
67 altering biotic interactions and homogenizing previously diverse plant and
68 animal communities over large spatial scales, ultimately resulting in a loss of
69 genetic, species and ecosystem diversity (Winter et al., 2009). The annual
70 economic impact of invasive species has been estimated at over 100 billion
71 dollars just within the USA (NRC, 2002), an order of magnitude higher than
72 those caused by all natural disasters put together (Ricciardi et al., 2011);
73 some authors go as far as to claim that the economic impact of invasive
74 species is incalculable (Mack et al., 2000).

75 Given the massive negative economic and ecological effects of invasive
76 species, a robust method for predicting species' distributions is crucial for an
77 early assessment of species invasions and effective application of appropriate
78 management actions (Malanson and Walsh, 2013).

79 Investigating how biodiversity is distributed spatially and temporally
80 across the globe has long been a central theme in ecology (Gaston, 2000)
81 and the methods developed to answer this question have become key tools for
82 biodiversity monitoring (Ferretti and Chiarucci, 2003). For example, species
83 distribution models (SDMs) have been used to map the current distribution
84 of a single species (Rocchini et al., 2011), model the potential distribution
85 of native and invasive species (Rocchini et al., 2015), investigate the sta-
86 tistical performance of different models to infer the distribution of species
87 under various ecological conditions (Guisan and Zimmermann, 2000; Elith
88 and Graham, 2009), test the transferability in space of modeled distribu-
89 tion patterns (Randin et al., 2006; Heikkinen et al., 2012), predict long term
90 changes to species distributions (Pearman et al., 2008) and make inferences
91 on future biodiversity scenarios (Pompe et al., 2008; Engler et al., 2009),
92 evaluate the potential of satellite imagery bands as predictors of biodiver-
93 sity patterns (Mathys et al., 2009), analyse spatial autocorrelation in species
94 distributions (Carl and Kühn, 2007; Dormann, 2007), and understand bio-
95 geographical patterns (Sax, 2001).

96 In combination with remote sensing products (e.g. Rocchini (2007); Feil-
97 hauer et al. (2013)) and current global data sets on in situ species observa-
98 tions, SDMs have become the method of choice for monitoring biodiversity at
99 multiple spatial and temporal scales. However, the strength of this combina-
100 tion depends on the careful selection and application of integrative modeling
101 approaches, in combination with a thorough assessment of uncertainty in
102 both data inputs and modeling methods.

103 Reliable anticipation of species invasions depends on the quality of input
104 data on one hand and robustness of the predictive SDM on the other. As

105 an example, Rocchini et al. (2011) demonstrated theoretically that input
106 data arising from biased species distribution maps could potentially lead to
107 unsuitable management strategies. In addition, Elith and Leathwick (2009)
108 demonstrated that, given the same input data set, different SDMs might
109 lead to dissimilar results (see also Bierman et al. (2010); Manceur and Kühn
110 (2014)).

111 The aim of this manuscript is to propose coherent and straightforward
112 methods to explicitly account for uncertainty when mapping species distribu-
113 tions in the light of anticipating the spread of invasive species. In particular
114 we will cover: i) explicitly mapping uncertainty in sampling bias, ii) mitigat-
115 ing uncertainty in data through prior beliefs and Bayesian inference and iii)
116 reporting uncertainty in species distribution maps through Markov Chain
117 Monte Carlo methods. The findings of this manuscript should be of partic-
118 ular interest to landscape managers and planners attempting to predict
119 the spread of species and deal with errors in species distribution maps in a
120 straightforward manner.

121 **2 Mapping input uncertainty related to sam-** 122 **pling effort bias**

123 In anticipating species distributions a first step is to ensure that the infor-
124 mation indicating where species are present is bias-free or, at least, that the
125 uncertainty of input data is explicitly taken into account in further modeling
126 steps.

127 One of the main problems with field data on species distributions is re-
128 lated to “sampling effort bias” (Rocchini et al., 2011), namely the bias inher-
129 ent in some areas being under-sampled with respect to others. Quantifying
130 and mapping the uncertainty derived from variation in the number of obser-
131 vations due to sampling effort can be achieved using cartograms (Gastner and
132 Newman, 2004), in which the shape of spatial objects (e.g. polygons, cells,
133 etc.) is directly related to a determined property, in our case to uncertainty.

Cartograms build on the standard treatment of diffusion theory by Gast-
ner and Newman (2004), in which the current spatial density of a population
is given by:

$$J = v(r, t)p(r, t) \quad (1)$$

134 where $v(r, t)$ and $p(r, t)$ are the velocity and density of the spread of the
135 population under study, respectively, at position r and time t .

136 Cartograms facilitate the visualization of spatial uncertainty in the data

137 by varying the size of each polygon according to the density of information
138 contained (e.g. number of observations, variation, etc.). As an example,
139 we show a cartogram of the distribution of *Abies alba* Miller overlapping a
140 grid to the set of records obtained from the Global Biodiversity Information
141 Facility (GBIF, <http://www.gbif.org>, Figure 1). GBIF offers free and open
142 access to hundreds of millions of records from over 30,000 species datasets
143 which are collated from around the world and stored with a common Darwin
144 Core data standard. The cartogram was developed using the free and open
145 source software ScapeToad (<http://scapetoad.choros.ch/>). Since cells with a
146 higher number species occurrences might be biased by the effort spent visit-
147 ing them, in Figure 1, the shape of each cell is determined by the the number
148 of times it was visited (i.e. number of different dates recorded in GBIF for
149 the species in that cell). From now on, we will refer to this as sampling effort.
150 The colour represents the spatial distribution (density of occurrences, sensu
151) of the species in each cell.
152 Therefore, cartograms allow uncertainty to be shown explicitly in a straight-
153 forward manner. Furthermore, sampling effort might be considered as a
154 variable in the SDM procedure, as described in the next section.

155 **3 Accounting for input uncertainty in the mod-** 156 **eling procedure: multi-level models, prior** 157 **beliefs and probability distribution surfaces**

158 Species observation records are often heterogeneous and incomplete because,
159 for example, they are unevenly distributed by year or area, or were collected
160 by different field operators. In addition, there is wide variation in recording
161 behaviours.

162 GBIF is a classic example of such heterogeneity: GBIF data is oppor-
163 tunistically gathered from a mixture of systematic surveys and volunteer
164 projects, and the intensity of publishing effort is strongly influenced by the
165 membership of the organisation. In terms of geographic coverage, GBIF con-
166 tains plentiful data from Northern Europe and America, parts of Latin and
167 Central America, South Africa, Australia and Oceania – but by contrast,
168 there are significant gaps in other regions, and there is a large variation
169 in sampling effort even between neighbouring European countries (see Ap-
170 pendix 1, Figure S1). This heterogeneity makes it difficult to estimate the
171 underlying variable (actual species presence and density of occurrences) and
172 potentially has an enormous impact on the information content of any one
173 species observation or set of observations (Isaac and Pocock, 2015). This

174 paper proposes methods by which ancillary knowledge about a species and
175 its environment might be exploited in a Bayesian framework to increase that
176 information content.

177 Multi-level models can be essential for detecting (spatially) clustered data
178 by considering the variation between groups (clusters). This approach is
179 more efficient and powerful than standard linear modeling techniques as it
180 provides a coherent and flexible method for modeling the effects of sampling
181 variation and allows uncertainty to be elegantly accounted for at all levels of
182 data structure (Gelman and Hill, 2006).

183 Furthermore, environmental variables with different spatial or temporal
184 resolution (i.e., country, regional or pixel level) are often used as predictors
185 in SDMs. Multi-levels models can simultaneously and coherently incorpo-
186 rate multi-level predictors allowing effects to be modelled at the appropriate
187 scale (Gelman and Hill, 2006). Hierarchical models are naturally handled
188 using Bayesian methods, which provide intuitive and direct estimates of un-
189 certainty around parameter estimates (Link et Sauer, 2002).

190 Despite tremendous effort by ecologists, collecting unbiased and reliable
191 data on the presence of species in a determined area/time to assess their
192 potential distribution through SDMs is sometimes not feasible since system-
193 atic field work is inherently expensive, time-consuming, and often involves
194 logistical hurdles, if the species under study is, for example, rare, elusive, in-
195 habits remote areas, or is in transitional equilibrium with its ecological niche
196 (as is the case with invasive species). Even for less problematic species, pres-
197 ence/absence data may also be distorted by several potential flaws, such as
198 sampling errors and subjectivity. As a result, SDM outputs may show high
199 uncertainty and be difficult to interpret, jeopardizing their utility in con-
200 servation applications. However, besides the availability of observation data
201 directly exploitable for modeling purposes, there is a wider set of ecological
202 data that can be used in SDMs, the so called “prior knowledge”. This data
203 is very often neglected and comprises information represented in different
204 formats; for example, previously conducted experiments, scientific literature
205 on the studied species or similar species, or even as “prior beliefs” (basic eco-
206 logical principles). Bayesian inference allows basic ecological principles and
207 prior data to be incorporated in a straightforward manner with potential
208 cost-effective consequences in increasing confidence of SDMs (McCarthy and
209 Masters, 2005; Bierman et al., 2010; Manceur and Kühn, 2014). The prior
210 information needs to be translated into a probability distribution, which is
211 then combined under Bayes’ rule with the likelihood information contained in
212 the original data to estimate a “posterior belief” or posterior probability dis-
213 tribution (PPD). The contribution of the prior and the data to the posterior
214 distribution depends on their relative precision, with the more precise of the

215 two having the greatest effect. A prior distribution can be non-informative
216 (flat prior), mildly informative (vague prior) or informative (strong prior).
217 In any case, the prior must be clearly described and justified according to
218 the context under investigation (Kruschke, 2015).

219 The result of the interaction between the likelihood of the data and the
220 prior distribution is itself a probability distribution (posterior probability
221 distribution or PPD). In an SDM, the advantage of having model parameter
222 estimations expressed as probability distributions, and not as point estima-
223 tion of the mean, is that the predicted suitability of the species in each
224 prediction unit (pixel) is itself a probability distribution. The suitability of
225 the PPD in each spatial unit represents the uncertainty of the prediction
226 in that unit. This uncertainty is stored in the Markov Chain Monte Carlo
227 (MCMC) model and can be re-used in future modeling exercises that, for
228 example, use a different set of data.

229 As an example, we applied a multi-level logistic regression with Bayesian
230 inference to model the distribution of *Abies alba* in Europe. We chose this
231 species due to its well known autoecology and actual distribution in Europe
232 (Farjon, 1998; Tinner et al., 2013; Gazol et al., 2015). We derived 44375
233 *Abies alba* presence records from the GBIF database, as points in vector
234 format (see Appendix 1, Figures S3 and S4). We generated an equal number
235 of pseudoabsences using the following strategy: we selected random points
236 a) within areas where conifers have been sampled (conifer occurrences in
237 the GBIF dataset) to pick the same areas that have been surveyed using the
238 sampling protocol used to record *Abies alba* presences, b) outside dry climatic
239 zones (e.g. Mediterranean climate) derived from the Köppen-Geiger climatic
240 zones map (Köppen and Geiger, 1930) where this species is not found and c)
241 outside a radius of 100 metres around the presence points to avoid overlap
242 with presence points.

243 We generated an equal number of absence locations at areas within which
244 conifers have been sampled (conifer occurrences in the GBIF dataset) and
245 outside a 100 meters radius from the presence points and the temperate and
246 dry climatic zones (e.g. mediterranean climate) derived from the Köppen-
247 Geiger climatic zones map .

248 To select the predictor variables, we performed a literature review on
249 the ecology of the species (Aussenac, 2002; Wolf, 2003; Rolland et al., 2009;
250 Tinner et al., 2013; Gazol et al., 2015). Hence, we relied on three different
251 datasets by selecting: i) the annual mean temperature (Bio1), and mean
252 diurnal temperature range (Bio2) obtained from the WorldClim dataset (Hi-
253 jmans et al., 2005), ii) radiation seasonality (Bio23) and the annual mean
254 moisture index (Bio28), obtained from the CliMond dataset (Kriticos et al.,
255 2012), and iii) the number of wet days during summer and frost days during

256 winter (and early spring) derived from the wet-days and ground-frost data
257 in the climate research unit dataset (Mitchell et al., 2004) (see Figure 2).

258
259 Considering sampling effort as a predictor, the sampling of the GBIF
260 dataset is clearly opportunistic. As a result, the unevenness of sampling
261 effort is particularly evident, with the Northern European region being more
262 sampled than other European regions (see Appendix 1, Figure S1). This bias
263 in GBIF data could generate unreliable predictions.

264 The clustering of GBIF data mainly derives from differences in surveys at
265 national and subnational level (Appendix 1, Figure S1). Thus, the sampling
266 effort was derived as the number (richness) of dates of survey recorded in the
267 GBIF dataset per polygon of the official administrative division of European
268 countries using the Nomenclature of Territorial Units for Statistics level 3
269 (NUTS 3).

270 We built a multi-level model to take into account the different resolution
271 of the predictor variables (Figure 2) and the differential sampling effort of
272 *Abies alba* occurrences in each NUTS3 polygon. The sampling effort was
273 used to re-scale the precision of the likelihood at pixel level, multiplying the
274 scaled sampling effort by the standard deviation of the Gaussian likelihood.
275 As a result, the likelihood estimate of pixels in regions with a higher number
276 of samples was expected to be more precise. The theoretical model (Figure
277 2) was coded in JAGS language and run in JAGS 4.2.0 through R (R Core
278 Team, 2016) using the R2jags (Su and Yajima, 2016) and CODA (Plummer
279 et al., 2002) packages. In order to allow reproducibility (Rocchini and Neteler
280 (2012)) of our approach we have included the complete R code in Appendix
281 2.

As previously stated, in heterogeneous datasets like the GBIF set, the sampling effort in a certain region may be correlated with the presence of the species under study. Therefore, a more highly sampled region should have also a higher probability of hosting the species. However, our data showed a weak sampling effort signal, with a high number of very low-sampled regions showing presence of *Abies alba*. This may result from errors, or low numbers of records not being representative of the distribution of the species under study. Therefore, we applied uninformative priors ($\mu = 0$, $SD = 1/10^{-2}$) for all the predictors but not for sampling effort, whose prior distribution $p(\theta)$ was given three different sets of parameters:

$$p(\theta) = \begin{cases} dnorm(0, 1/10^{-2}), & \text{uninformative prior.} \\ dnorm(1, 10), & \text{mild positive prior.} \\ dnorm(5, 5), & \text{strong positive prior.} \end{cases} \quad (2)$$

282

283 Such distributions were chosen as examples under the hypothesis that *i*)
284 data alone were enough to account for heterogeneity in sampling effort; *ii*)
285 a mildly informative (vague) prior knowledge about the positive correlation
286 of sampling effort was useful for improving the model; *iii*) imposing strong
287 prior knowledge on the positive influence of the prior would improve the
288 model output. These three hypotheses were translated in three models that
289 shared the same structure (Figure 2) except for the prior distribution imposed
290 on sampling effort. All the predictors were scaled and centered in order to
291 improve the efficiency of the MCMC process. PPDs for all parameters were
292 sampled from each of two chains with 10000 MCMC iterations using 1000
293 burn-in and 1000 adaptation iterations, with a thinning set of 20. Conver-
294 gence was assessed by the Gelman-Rubin statistic (Gelman and Rubin, 1992).
295 Each model was then used to estimate the suitability PPDs in each pixel of
296 the study area. The parameter estimates for the three models will show if
297 different prior belief on the role of sampling effort changed the model pa-
298 rameter estimates. Furthermore, the Deviance Information Criterion (DIC,
299 see Spiegelhalter et al. (2014)) was used to assess the model with the best
300 predictive power.

301 The Posterior Probability Distributions (PPDs) of model parameters for
302 the three models (with different priors on sampling effort, see Equation 2)
303 are reported in Figure 3. All the models agreed on the direction and effect
304 size of the predictors (Figure 3). Credible effects (no intersection with 0 in
305 Figure 3) were attained for those variables directly related to temperature. In
306 particular, annual mean temperature (Bio1 and Bio1²) and radiation season-
307 ality (Bio23) showed negative effects while mean diurnal temperature range
308 (Bio2) showed positive effects (Figures 3 and 4). The negative credible effect
309 of Bio1² implies that the relationship between the probability of presence
310 (suitability) of *Abies alba* and annual mean temperature has a “bell shape”,
311 by rising slowly to the left of the annual mean temperature average (7.8 °C)
312 and decreasing rapidly when on its right (Figure 4). On the contrary, the
313 distribution of wet days, annual mean moisture index (Bio28) and frost days
314 included 0, showing a non-credible effect on the presence of *Abies alba*.

315 The sampling effort coefficient changed heavily between models. In the
316 first model with an uninformative prior, the coefficient average was slightly
317 negative but with its high density interval comprising 0 (Figure 3). Therefore
318 we concluded that according to the data the sampling effort had a non-
319 credible effect. In the second model (Figure 3) a mildly informative positive
320 prior affected the estimate of the parameters, but yet was not enough to
321 derive a credible effect of the prior estimate. In the last model, the strong
322 informative prior pulled the estimation of sampling effort coefficient towards
323 positive values. This showed that, according to the data and to the “prior

324 knowledge”, the sampling effort was positively affecting the probability of
325 presence of *Abies alba*.

326 In summary, the model with the strong prior showed an improved preci-
327 sion of sampling effort, basically maintaining that of the others (Figure 3).
328 Based on this and since the DIC did not show differences for the strong prior-
329 model with respect to the uninformative prior-model (Table 1, $\delta DIC \leq 4$,
330 see Burnham and Anderson (2002)), we further focused on the model with
331 a strong prior to build the output distribution map. The resulting potential
332 niche distribution of *Abies alba* is thus shown in Figure 5.

333 4 Discussion

334 In this paper, we have demonstrated the importance of i) mapping uncer-
335 tainty derived from varying sampling effort and ii) considering it in an explicit
336 manner in order to anticipate species’ potential distributions. We have pro-
337 vided a case study with a plant species widespread throughout Europe (*Abies*
338 *alba*) where the observed data (Figure 1) and the modelled potential niche
339 (Figure 5) differed mainly because of tree plantations recorded in the GBIF
340 dataset. For example, Northern Europe was shown to be unsuitable for the
341 natural spread of the species in our Bayesian model (Figure 5), as well as in
342 previous studies on the distribution of the species (e.g. the European Forest
343 genetic Resources programme, <http://www.euforgen.org/>, see Appendix 1,
344 Figure S2), corroborating our results. However, it appeared to be present
345 in the GBIF field-based dataset (Figure 1, see also Appendix 1, Figure S3),
346 mainly because of human-related conifer plantations.

347 Notably, when we associated a stronger prior to sampling effort, model
348 coefficient estimates had lower uncertainty, and in addition, the model DIC
349 did not differ from the model with the uninformative prior. Therefore, a
350 strong prior allowed us to decrease uncertainty and maintain high model
351 quality ($\delta DIC \leq 4$, see Burnham and Anderson (2002)).

352 We have shown that multilevel models coupled with Bayesian inference
353 can be used to account for variability in sampling effort, integrating external
354 data on prior knowledge with species observations, to model species distribu-
355 tion more accurately and with higher certainty than previous methods. The
356 priors considered in the reported case study were only examples generated
357 here to illustrate how the precision of parameter estimates can potentially
358 be increased using prior knowledge about the system under study. However,
359 in order to have scientifically sound results, the priors considered should
360 obviously be fully justified and rooted in ecological theory.

361 Anticipating species potential distributions based on prior information

362 (Bayesian modeling) can help to predict the potential future spread of a
363 species in space (and time) in a robust manner (Bierman et al., 2010; Manceur
364 and Kühn, 2014). Using sampling effort bias among priors was important
365 in our case since it allowed such uncertainty to be considered explicitly in
366 the model. This can help to accommodate the error rate directly into the
367 modeling procedure.

368 Hence, calibrating models conditioned on previous knowledge and/or ob-
369 servations might be feasible when relying on a Bayesian framework in which:

$$P(Y|H) \tag{3}$$

370 where P = the probability of occurrence of patterns Y given a hypothesis
371 H is substituted by:

$$P(H|Y) \tag{4}$$

372 i.e. the probability P that a hypothesis H is true in light of the available
373 data.

374 Bayesian statistics have long been used in independent scientific disci-
375 plines and topics such as trait loci mapping (Ball, 2001), environmental sci-
376 ence (Clark, 2005), machine learning approaches in computer science (Di-
377 etterich, 2000), classification of remotely-sensed images (Goncalves et al.,
378 2009), conservation genetics (Bertorelle et al., 2004), statistical algorithm
379 development (Hoeting et al., 2009) and sampling strategies (Mara et al.,
380 2016).

381 In the framework of ecological patterns and processes, Ellison (2004)
382 makes an explicit quest for using known information to build a model, re-
383 lying on prior rather than posterior probabilities. This reinforces the view
384 of Ginzburg et al. (2007) that biology should constrain mathematical con-
385 structions. Quoting the authors, “While mathematics provides an incredibly
386 vast set of possible equations, logic dictates that only a small subset of these
387 equations can represent a given ecological phenomenon. A large number
388 of constructions, while mathematically sound, should be excluded based on
389 their inconsistency with biology.”

390 This is especially true when the results of model construction impact
391 decision-making, which could be more focused and effective if uncertainty
392 was explicitly taken into account based on previous literature regarding the
393 main drivers that shape the distribution of species (Ellison, 1996). Our
394 approach reduces the danger of relying on misleading predictions of alien
395 species invasions with high model errors, which are hidden or unrecognizable
396 using previous approaches (Rocchini et al., 2015).

397 In the framework of Species Distribution Modeling it has been demon-
398 strated that prior probabilities in the observation of a certain species might
399 improve model performance. This is true at various hierarchical levels, from
400 species to entire communities. Thus, applying Bayes' theorem to predict val-
401 ues at a certain site might thus allow known environmental properties to be
402 accounted for. If Bayesian models do not outperform other modeling tech-
403 niques, they at least better reflect the theory under the realized niche of a
404 certain species. A number of examples are provided in Guisan and Zimmer-
405 mann (2000), modeling different plant species in different habitat types.

406 5 Conclusion

407 In the light of the importance of anticipating species future distributions,
408 especially for economically important invasive species, it is crucial to detect
409 those areas into which such a species might be expected to disperse. Antici-
410 pating their spread based on the suitability of environmental conditions can
411 lead to more effective management strategies, allowing timely actions to be
412 initiated and preventing further spread (Rocchini et al., 2015).

This can be summarized by the following equation:

$$Decision = \begin{pmatrix} < E_m | > I & < E_m | < I \\ > E_m | > I & > E_m | < I \end{pmatrix} \quad (5)$$

413 In this case, a high (or low) invasion rate I might be related to high or
414 low error E_m in the output model being observed by decision makers. The
415 most dangerous situation is when a low predicted invasion rate is related to
416 a high error in the modeling procedure. In this case decision makers might
417 underestimate the effort against the likelihood of invasion, that, from the
418 species distribution map, is suspected to be low.

419 In this paper we have demonstrated the power of incorporating sampling
420 bias into the model being used by relying on prior probabilities of distribu-
421 tion of a plant species widely spread in Europe. We believe this is a good
422 example to further encourage species distribution modellers and environmen-
423 tal planners and conservationists to account for uncertainty and bias in the
424 sampling effort in anticipating the spatial spread of species, instead of relying
425 on distribution maps with potentially hidden uncertainty.

426 6 Acknowledgments

427 We are particularly grateful to the handling Editor Rocco Scolozzi and to
428 two anonymous Reviewers who provided useful insights which improved a

429 first draft of this manuscript. We thank Ingolf Kühn for precious sugges-
430 tions.

431 DR was partially supported by the EU BON (Building the European Biodi-
432 versity Observation Network) project, funded by the European Union under
433 the 7th Framework programme (Contract No. 308454), by the ERANET
434 BioDiversa FP7 project DIARS, funded by the European Union and by the
435 Life project Future For CoppiceS.

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Tables

Model	DIC	Gelman diagnostic	Burn In	Iterations	Chains
Uninformative prior	1938	1.13	2000	10000	2
Mild prior	2133	1.15	2000	10000	2
Strong prior	1940	1.22	2000	10000	2

Table 1: Deviance Information Criterion (DIC) used to assess the prior with the best predictive power. Notice that $\delta DIC \leq 4$ using an uninformative prior and a strong prior on sampling effort. Therefore, a strong prior allowed us to decrease uncertainty and maintain high model quality. Refer to the main text for additional information.

639 **Figures**

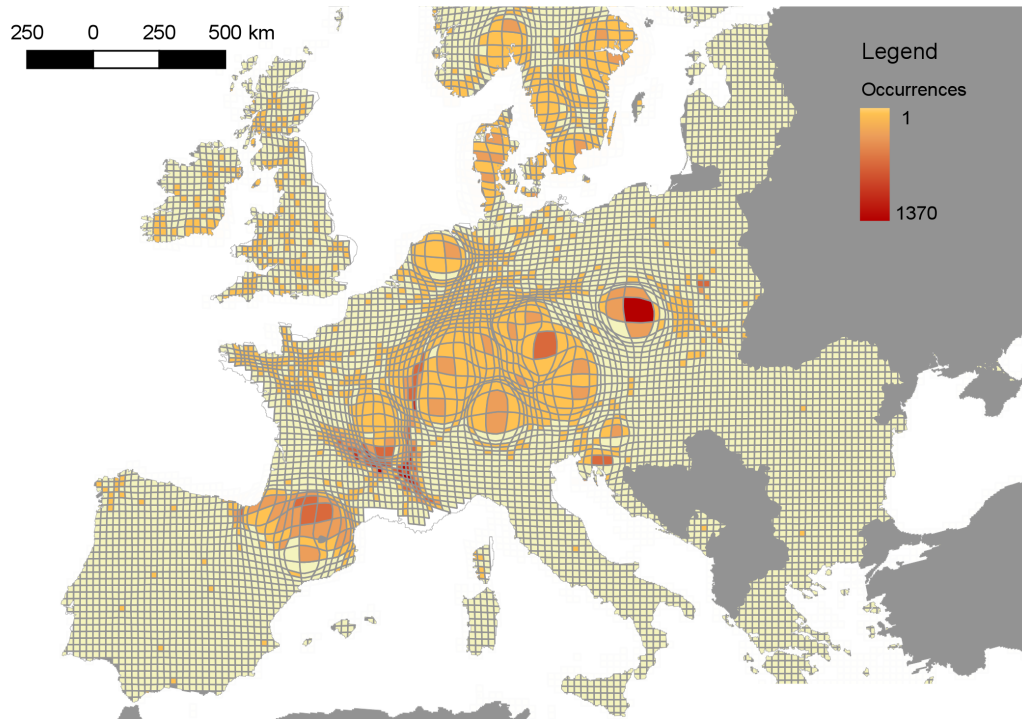


Figure 1: Cartogram representing the sampling effort bias (cell distortion) of the GBIF dataset related to *Abies alba*. This species is not native in Northern Europe, although it is widely cultivated as a timber tree, as thus present in the GBIF dataset.

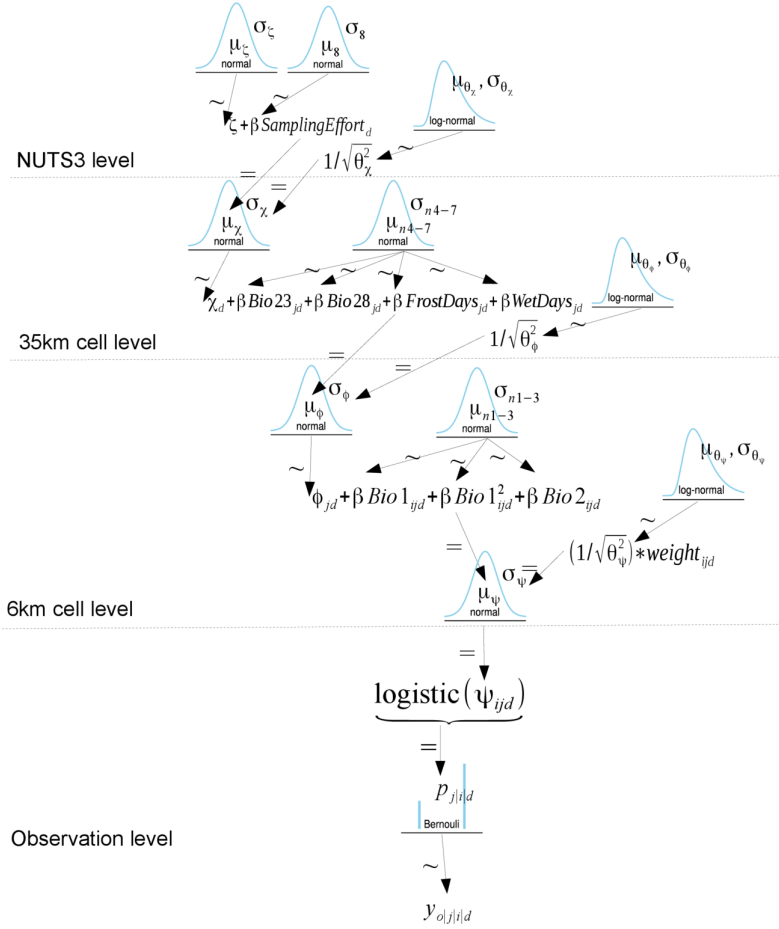


Figure 2: The multi-level model represented through a pictogram. To select the predictor variables, we performed a literature review on the ecology of the species, finally selecting: radiation seasonality (Bio23), the annual mean moisture index (Bio28), the number of wet days during summer and the frost days during winter and early spring, the annual mean temperature (Bio1), the mean diurnal temperature range (Bio2). Sampling effort was calculated as the richness of dates of survey recorded in the GBIF dataset for each NUTS3 country. Refer to the main text for additional information on the source of each dataset. Symbols used in this figure: μ, σ = mean and standard deviation of prior and hyperprior distributions; ζ, χ, ϕ = intercepts for NUTS3, 35km, 6km level of the model; subscript d, j, i, o = index for NUTS3, 35km, 6km and observation level; $weight_{ijd}$ = scaled weights for sampling effort; $\text{logistic}(\psi)$ = logistic transformation of the model output (link function); $p_{i|j|d}$ = probability of occurrence; $y_{o|i|j|d}$ = presence or absence. Refer to Kruschke (2015) for a complete dissertation about the terms and the graphical representation of the proposed model. Notice that variables at 6km resolution were resampled from an original resolution of 1km to allow the Bayesian model to be run in R. The R code of the model is available in Appendix 2.

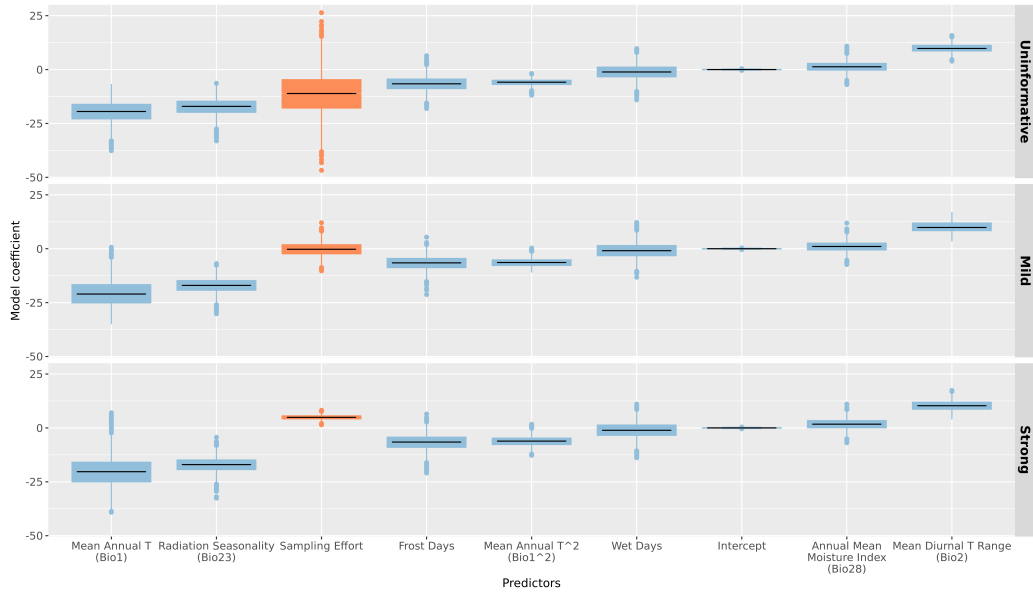


Figure 3: Boxplots of the β coefficient PPDs for the three models (in the three figure facets). Each box represents the 1st and 3rd quartiles of a coefficient distribution, the black horizontal line the distribution median, the whiskers the limits of the 1.5*interquartile range, while the filled circles represent the outlying points. If whiskers did not overlap 0 we inferred as “credible effect”. We showed in red the boxplots reporting the distribution of the β coefficient of the sampling effort. It is clear that the major difference among models was related to the precision of sampling effort, which increased passing from the model with an uninformative prior on sampling effort, through that with a mild prior, reaching its highest value in the model with a strong prior.

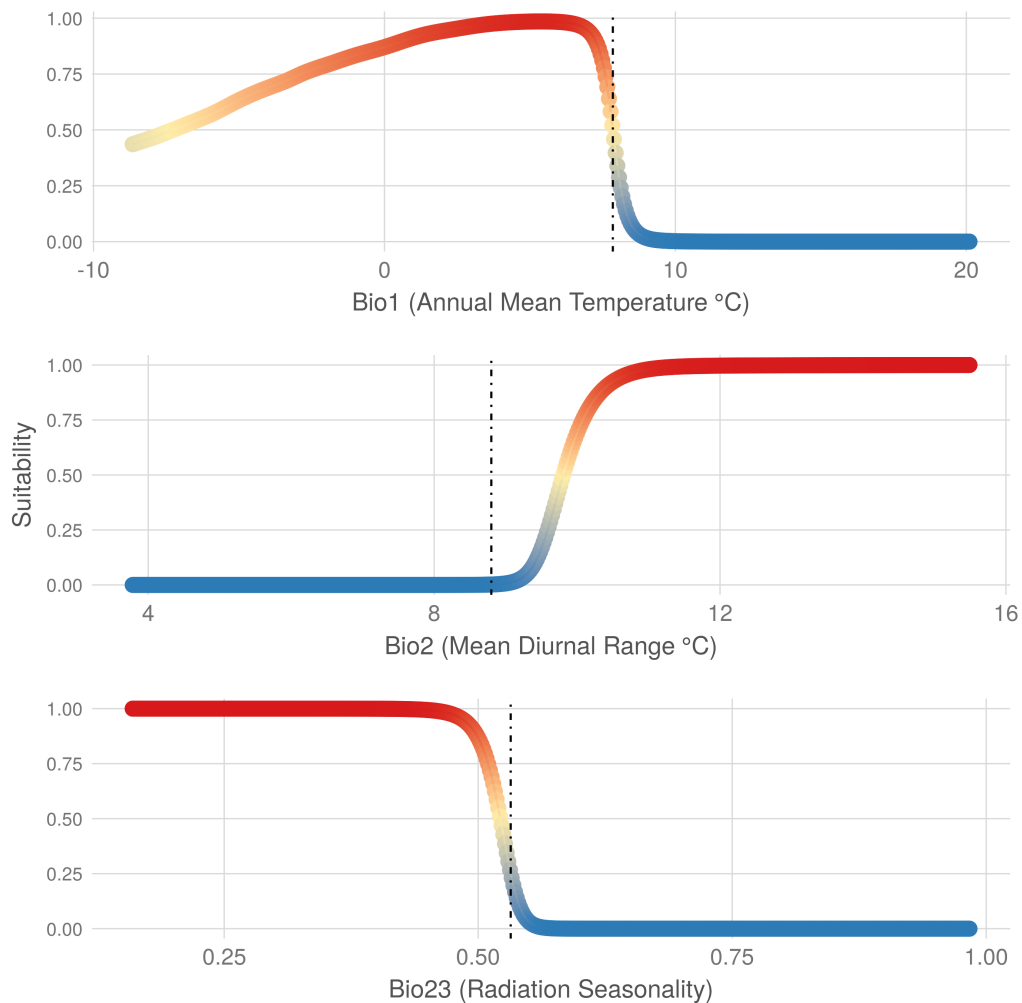


Figure 4: In this figure the average probability of presence (suitability) of *Abies alba* is plotted against the three variables with the highest average coefficient effect size in the model (top: range of annual mean temperature Bio1, middle: mean diurnal range Bio2, bottom: Radiation Seasonality or Bio23). The relationship between the probability of presence (suitability) of *Abies alba* and annual mean temperature has a “bell shape”, rising slowly moving from the left of the study area average (7.8 °C), peaking just before the average and decreasing rapidly when on its right. The shape of the relationship between the probability of presence and the mean diurnal temperature range is inverted. A low diurnal temperature range is associated with a low suitability while a wide temperature variability is associated with high suitability. The highest suitability is reported for Bio2 values higher than 11 °C. The Radiation Seasonality (the standard deviation of the weekly solar radiation estimates expressed as a percentage of the mean of those estimates) shows a negative pattern with respect to suitability. Areas with a very high average difference in solar radiation during the year (i.e. Northern Europe) are reported as weakly suitable for *Abies alba*. All the curves were obtained varying the value and the model coefficient of Bio1, Bio2 and Bio23 while keeping the values of the other predictors at their average. As reported in the main text, this results as well as that in Figure 5 is derived from the model with a strong prior on sampling effort.

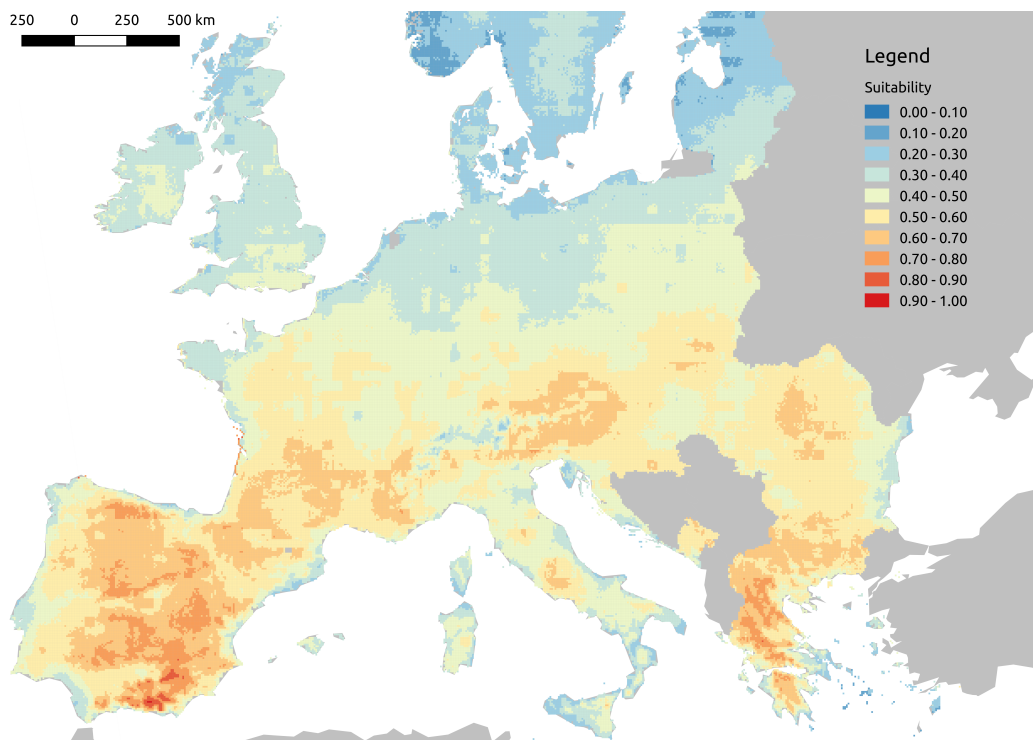


Figure 5: *Abies alba* suitability distribution as derived from the multi-level model with strong prior on sampling effort. The pixel value is the average of the PPDs for that pixel.

Figure 1
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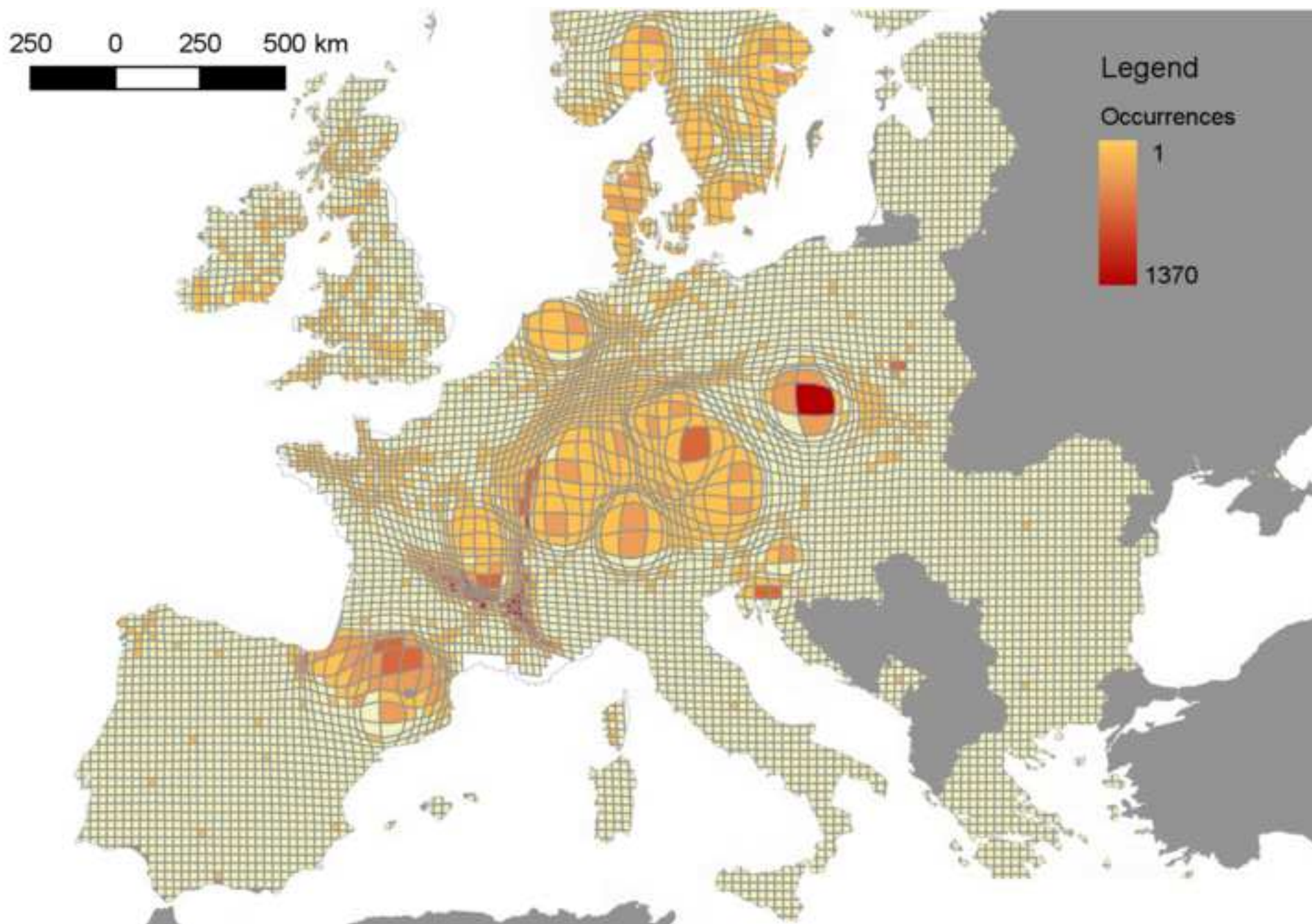


Figure 2

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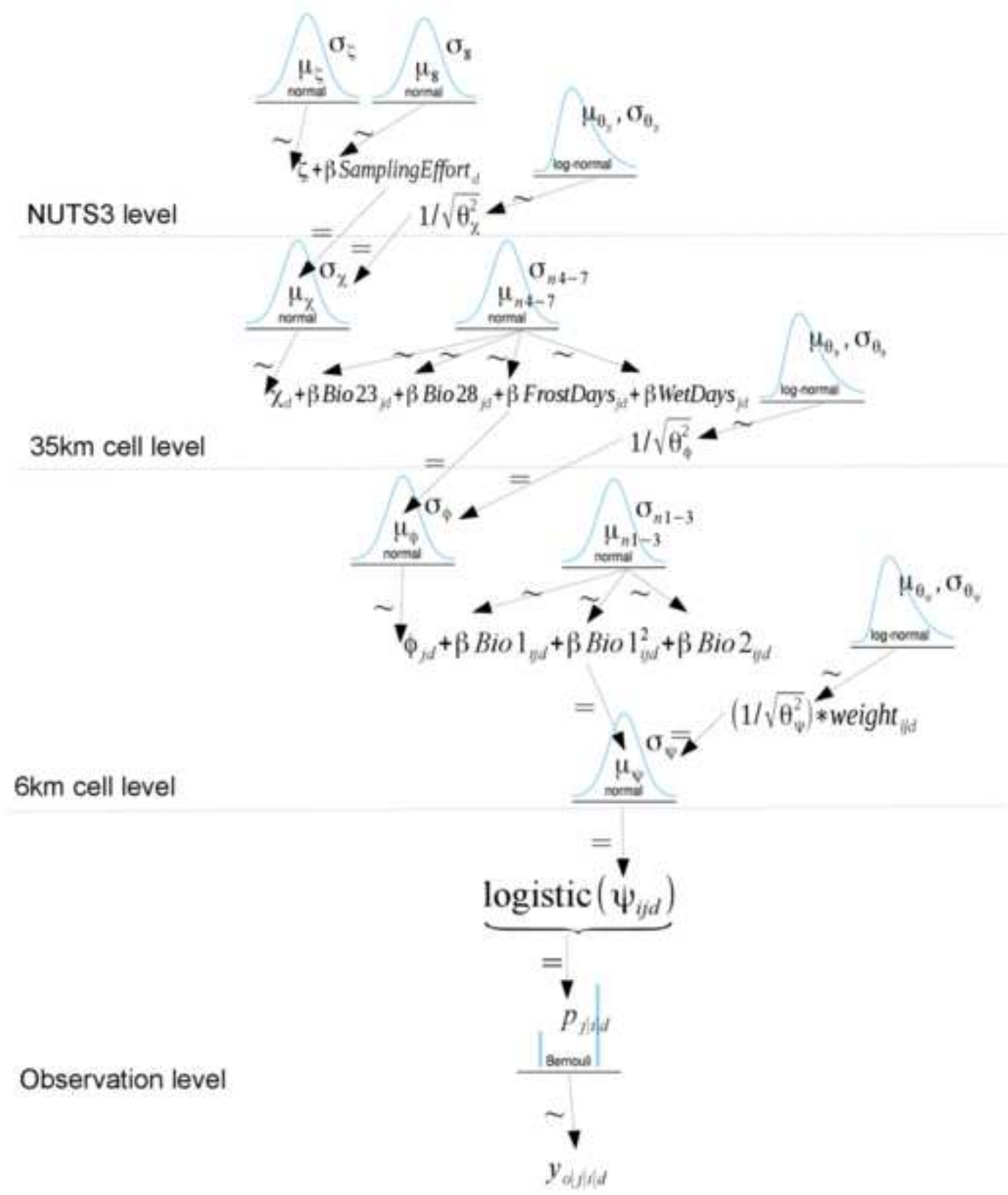


Figure 3
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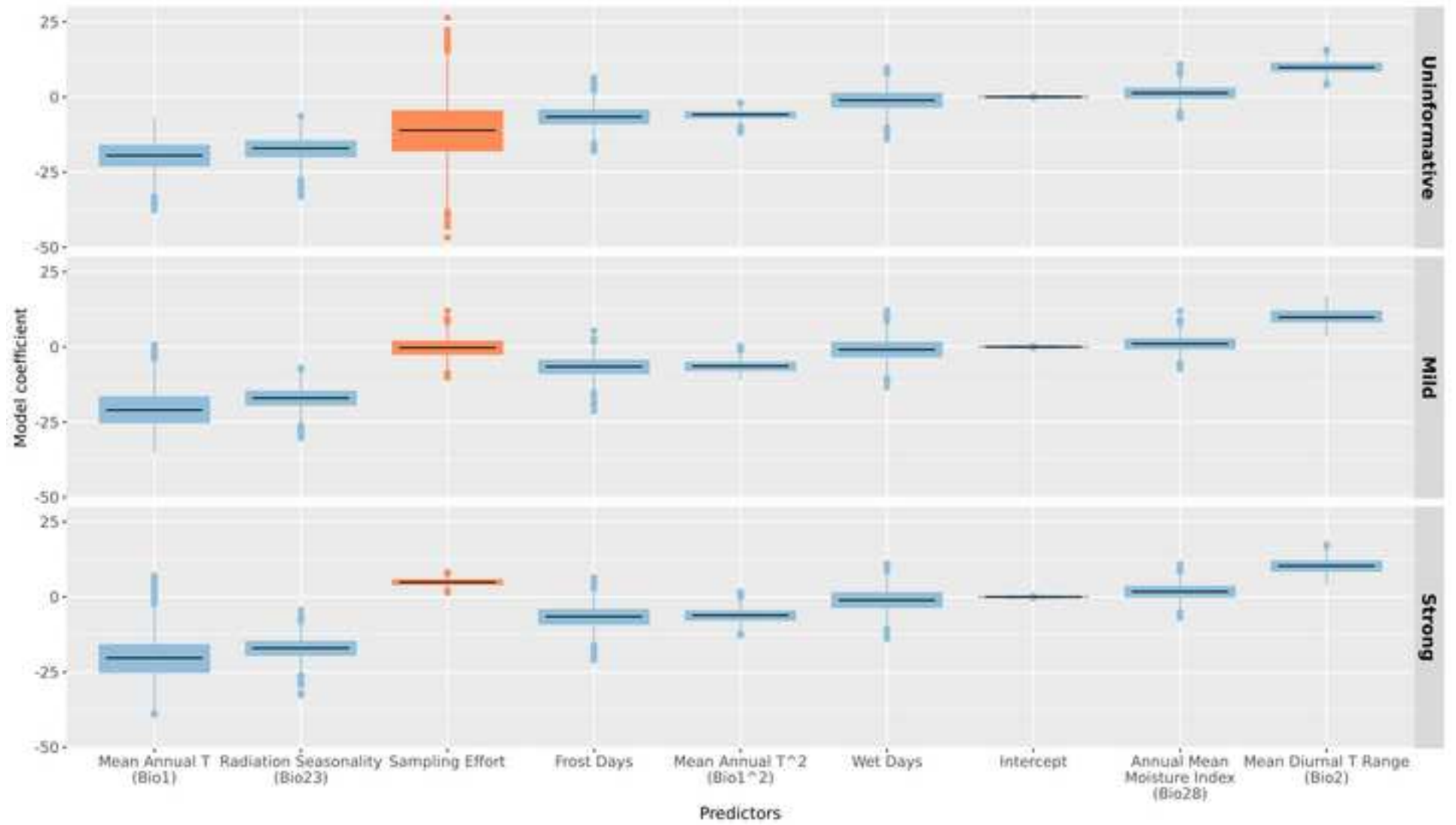


Figure 4

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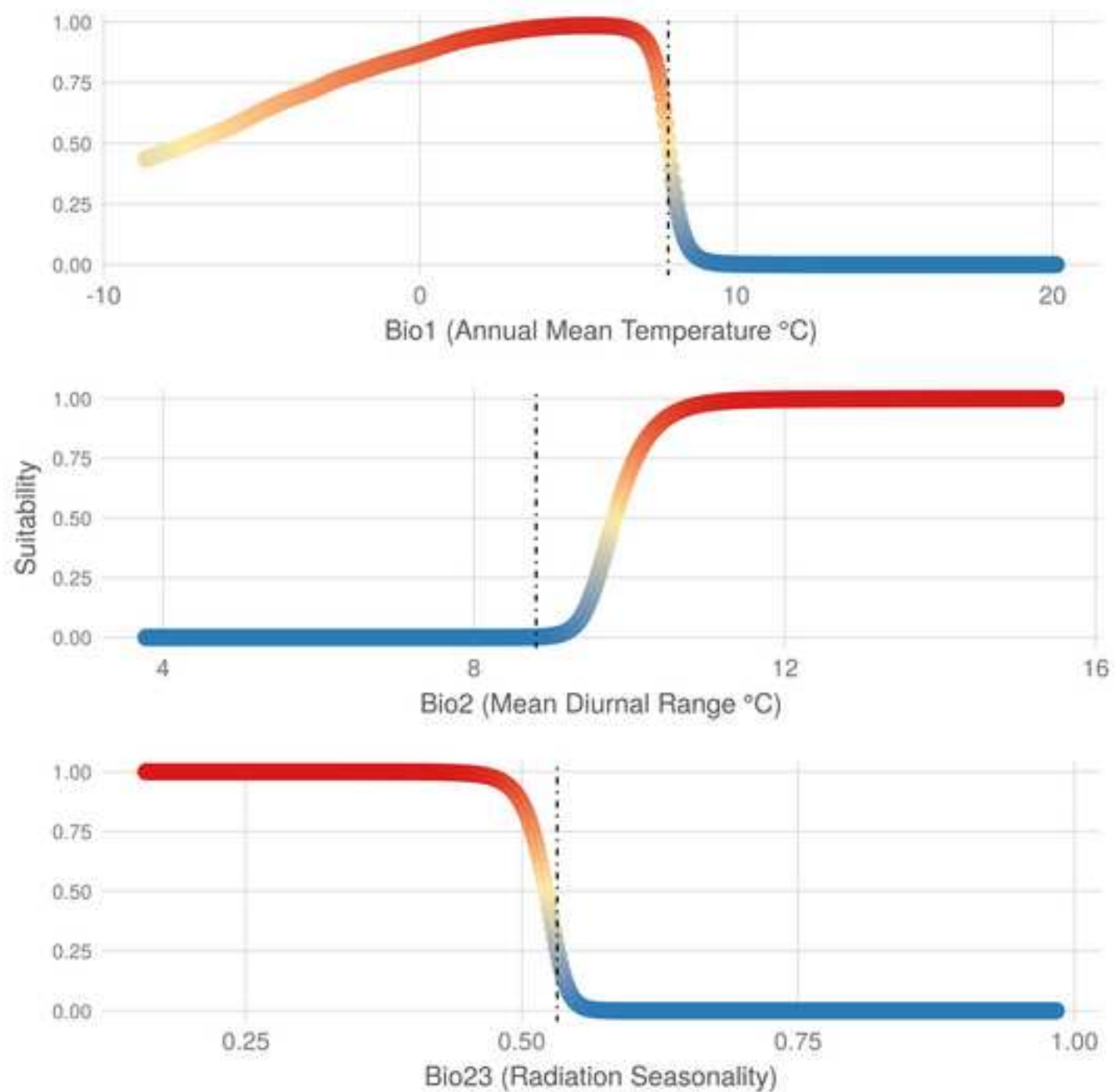


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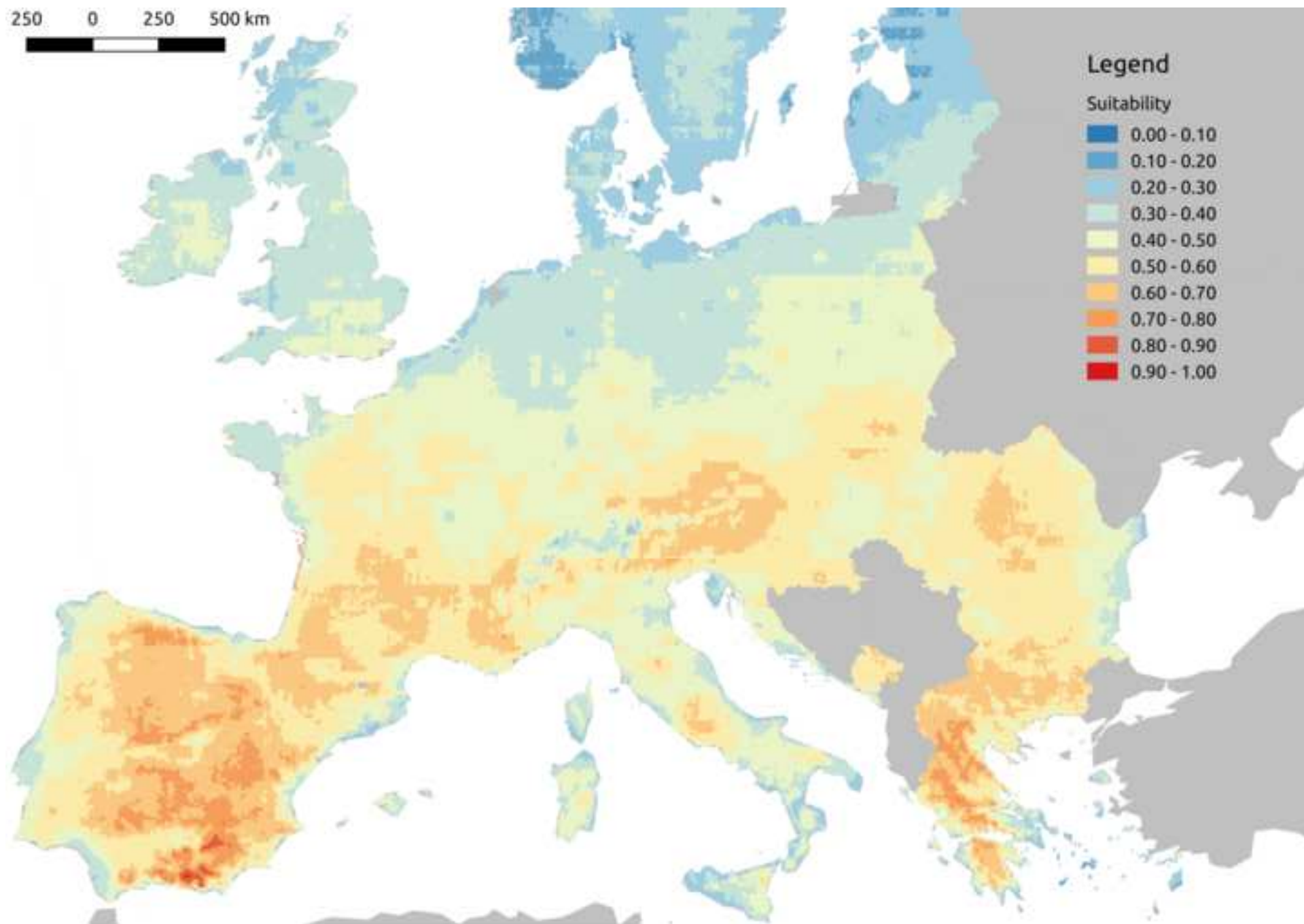


Figure S1
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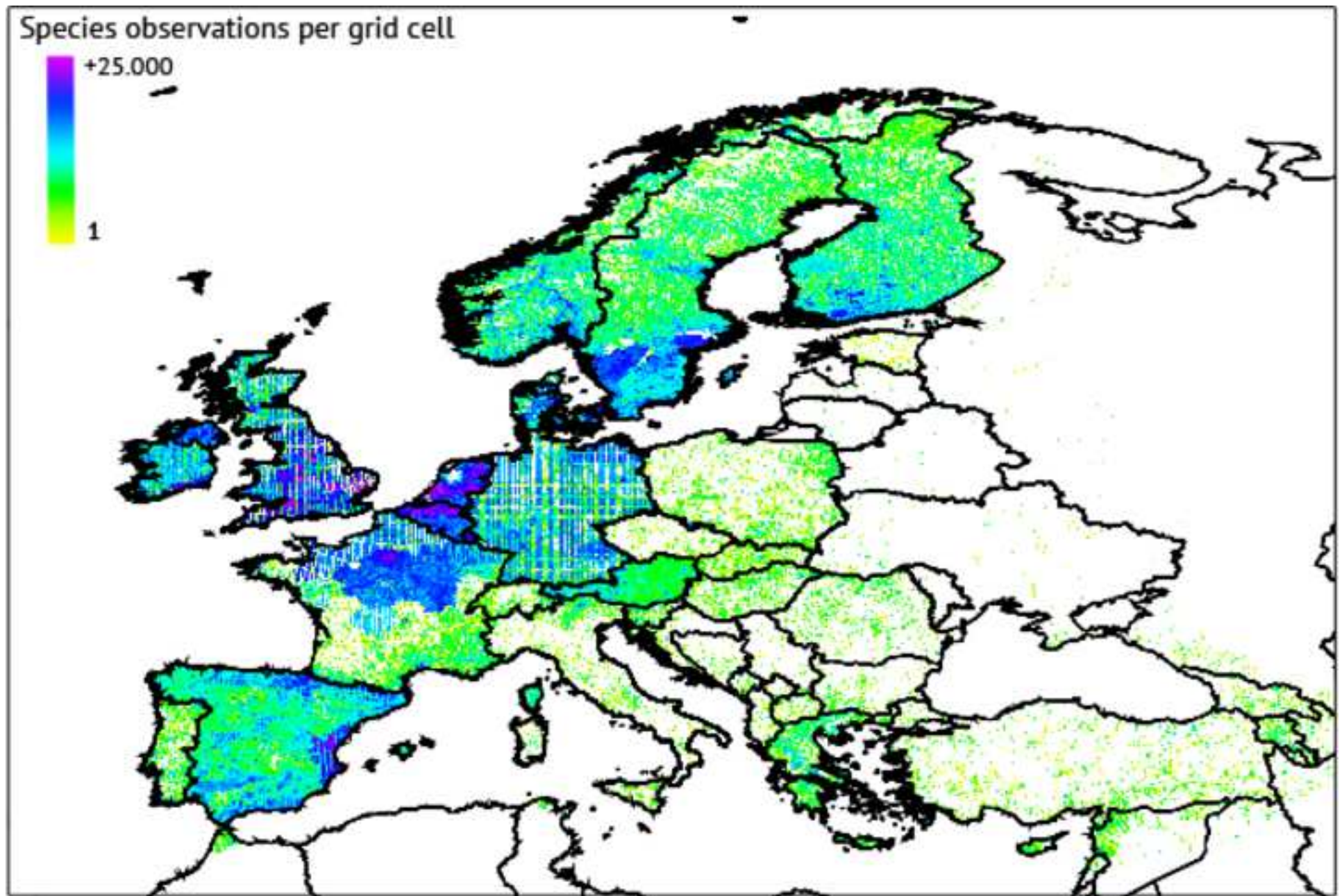


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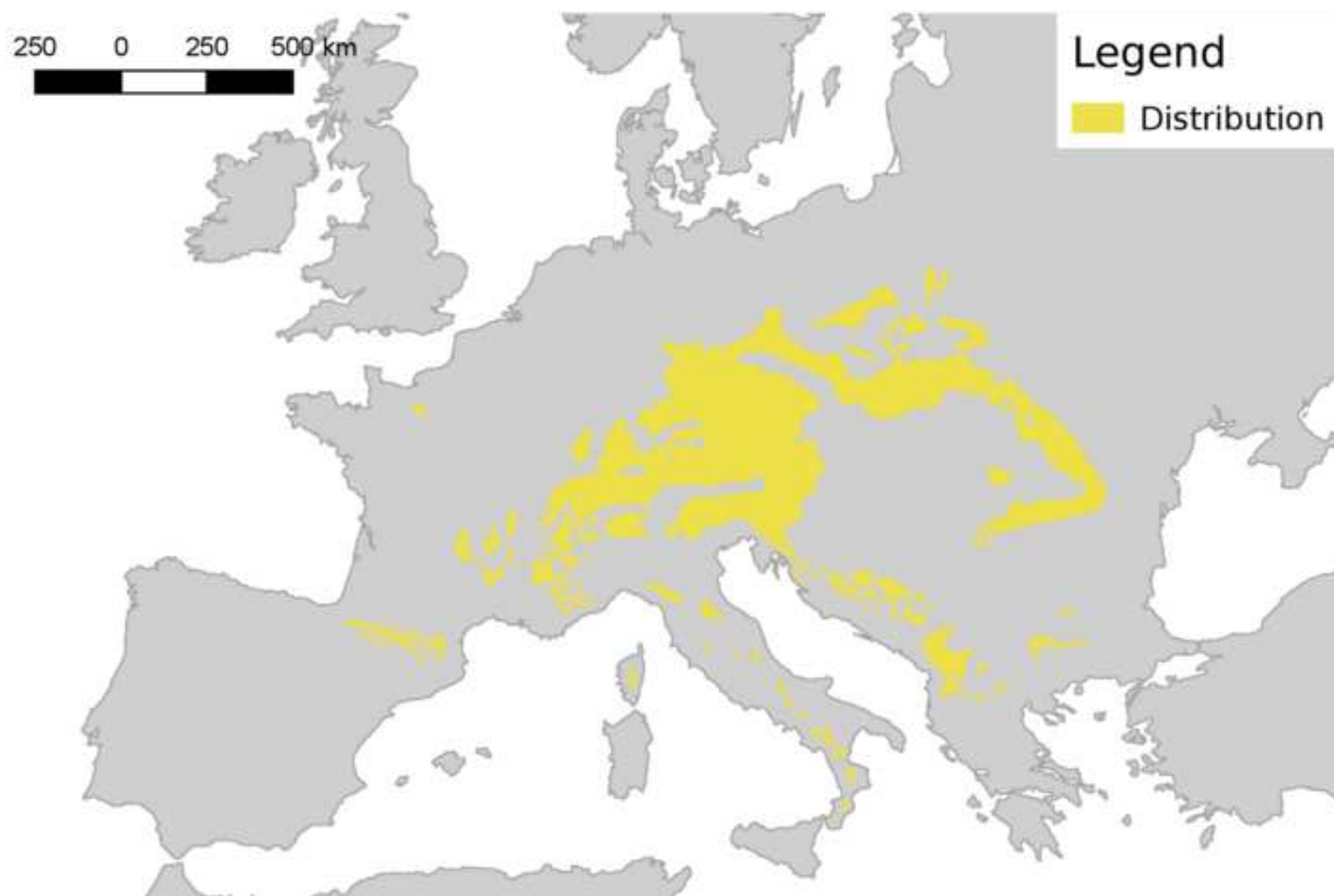


Figure S3
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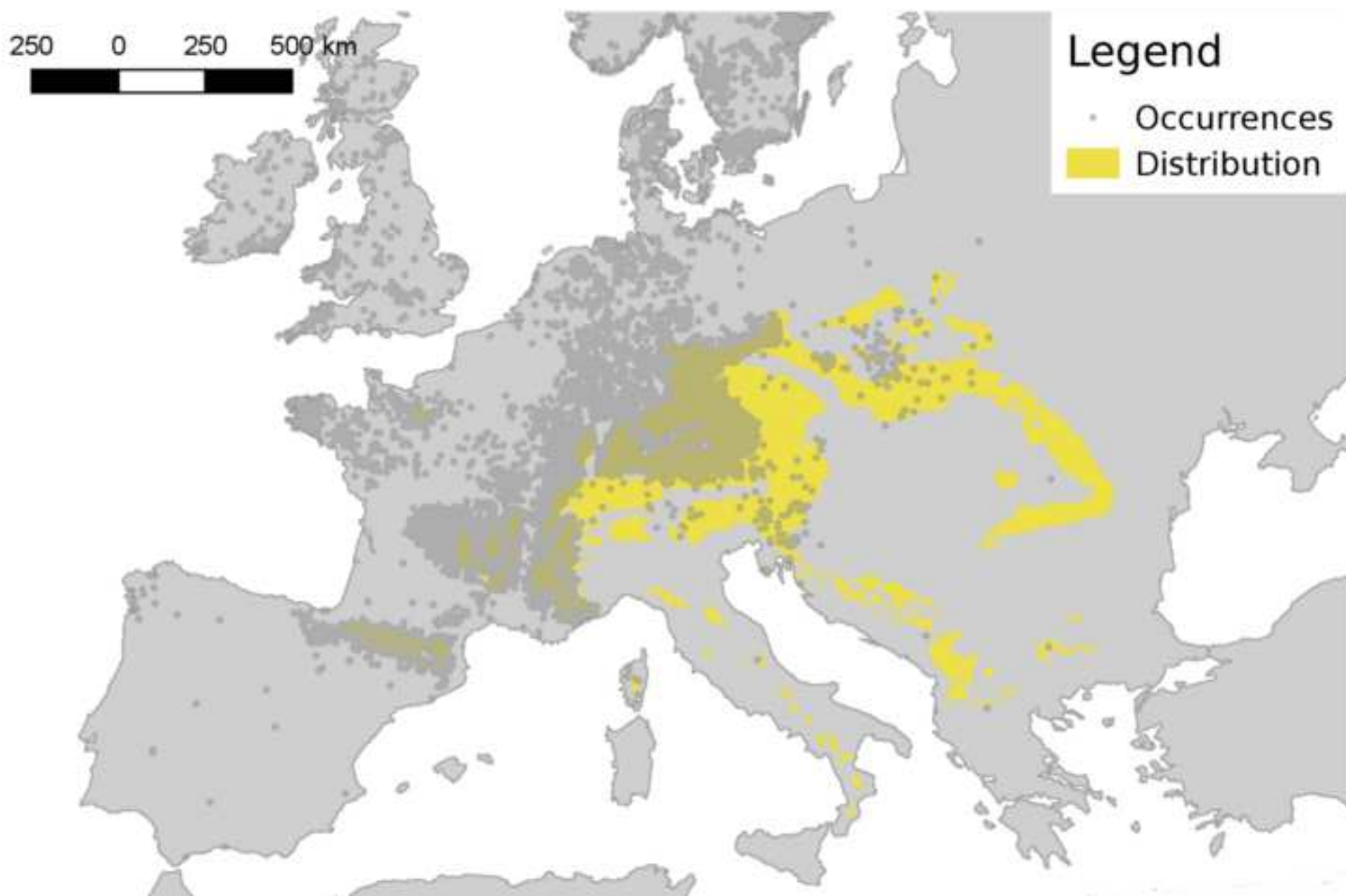


Figure S4
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