

Test Set Diameter: Quantifying the Diversity of Sets of Test Cases

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Abstract—A common and natural intuition among software testers is that test cases need to differ if a software system is to be tested properly and its quality ensured. Consequently, much research has gone into formulating distance measures for how test cases, their inputs and/or their outputs differ. However, common to these proposals is that they are data type specific and/or calculate the diversity only between pairs of test inputs, traces or outputs.

We propose a new metric to measure the diversity of sets of tests: the test set diameter (TSDm). It extends our earlier, pairwise test diversity metrics based on recent advances in information theory regarding the calculation of the normalized compression distance (NCD) for multisets. A key advantage is that TSDm is a universal measure of diversity and so can be applied to any test set regardless of data type of the test inputs (and, moreover, to other test-related data such as execution traces). But this universality comes at the cost of greater computational effort compared to competing approaches.

Our experiments on four different systems show that the test set diameter can help select test sets with higher structural and fault coverage than random selection even when only applied to test inputs. This can enable early test design and selection, prior to even having a software system to test, and complement other types of test automation and analysis. We argue that this quantification of test set diversity creates a number of opportunities to better understand software quality and provides practical ways to increase it.

I. INTRODUCTION

Testing is a critical activity to ensure that software has sufficient quality and reliability. Since software projects often exceed the time and resources allocated to them, testing frequently has to make the most use of the least resources. This limits the number of test cases that can be selected even if automated techniques are used for test execution and/or when creating tests. Even if there is ample time to plan for testing and develop test cases, the tests will typically be re-executed frequently, within each iteration or prior to each release, which means that we need as small and as effective a set of tests as possible. Thus, a fundamental problem in software testing is *how to select a small set of test cases* that most efficiently tests a software system.

To achieve these goals a natural intuition among testers is to select a small set of diverse test cases. The idea is that test cases that differ are more likely to better cover the intended as well as the actual software behavior. This approach also

has support in the research literature. For example, adaptive random testing [1] only adds a new, randomly-generated test case if it has large distance to existing test cases. But Chen et al. [1] also note that a number of testing methods such as Restricted- [2], Anti- [3], and Quasi- [4] Random Testing are all based on the same idea: ‘evenly spreading’ test cases over the input domain. Critical to the success of these techniques is a generically applicable diversity measure and Chen et al. go as far as saying that ‘We have come to realise that “even spreading” can be better described as a form of diversity’ [1]. They describe a distance calculation scheme based on the category-partition (partition testing) method, but it requires that the tester manually identifies categories and levels which can be varied.

Most approaches to quantifying diversity among test cases are specific to a certain type of data. It is common to assume that the data is numeric since there are a multitude of existing distance functions that can then be applied. One example is the approach of Bueno et al. [5] which selects test sets that maximize the sum of the distances from each test input to its nearest neighbor. In their empirical work they use the Euclidean distance which requires the inputs to be numerical vectors. For data types for which it is not as simple to define distance functions, researchers typically revert back to basic forms of distance, such as binary distance, rather than quantifying it. For example, Alshawan et al. [6] proposed to select test cases for web application testing based on unique system outputs. Their empirical study [7] applied several uniqueness measures defined on the HTML output of five web applications. All of the uniqueness measures are binary in nature since they are based on comparing equality among parts of the HTML output.

Feldt et al. [8] proposed a test diversity metric with a stronger theoretical basis by using the concept of information distance from the field of Information Theory [9]. Although information distance is based on Kolmogorov complexity [10] which can only be approximated in practice, such approximations using modern compression algorithms have shown wide applicability [11]–[13]. One such distance metric calculated using compression algorithms is Cilibrasi and Vitanyi’s normalised compression distance (NCD) [14]. Apart from the theoretical motivation there are also practical benefits to their proposal: since information distance is universal and applies to any strings of data, it can be used regardless of data type investigated. The benefit to developers of testing

systems would be immediate. They need no longer develop specific metrics for each application domain or type of data. By basing diversity measurements on the normalized compression distance (NCD) automated testing systems can search for diverse tests in general [8].

A fundamental gap in the proposal of Feldt et al. is how the resulting diversity metric is to be used. Since NCD is a pairwise metric it can calculate a distance matrix between all pairs of (here) test cases, but it is not clear how to leverage that information for selecting test cases. In their study, Feldt et al. used a general approach (also employed in the original papers that proposed the NCD metric) to cluster the studied objects based on the distances. The result of such an analysis is a tree that defines an approximate order among the test cases. But Feldt et al. did not investigate concrete ways for selecting test cases to form a small, diverse test set.

This paper applies more recent results in Information Theory that extends NCD to multisets [15]. This gives a general approach to solve test selection problems that can work for any type of test input, output or other information collected about a test, such as its execution trace. Our conjecture is that such a theoretically motivated approach to test selection based on the diversity of a set can create more efficient test sets than heuristic methods such as the maximize-mean-diversity used by Bueno et al [5] and the maximize-min-diversity used in adaptive random testing [1]. The NCD for multisets can calculate the diversity in the whole set in a theoretically well-founded manner instead of approximating it based on pairwise comparisons. And since the underlying distance metric itself can be used for any data type, the approach can also be applied for as yet unknown data types or in new application domains.

Section II introduces NCD and its extension to multisets and Section III defines test set diameter and a test selection procedure based on it. The empirical study in Section IV presents the research questions, software under test, experimental procedures, and results. Finally, we discuss the implications of our results in Section IV and place them in the context of related work in Section VI, before we conclude the paper in Section VII.

II. NORMALIZED COMPRESSION DISTANCE FOR MULTISETS

In this section we describe the concepts from Information Theory that are used in this work: the information distance, its practical approximation as the normalized compression distance (NCD), and the recent extension of NCD to multisets.

A. Information Distance and its approximation

The Kolmogorov complexity of a string of symbols, x , is the length of the shortest program (typically measured in bits) that outputs x [10]. It is a measure of the information contained in x , which we denote here as $K(x)$. The conditional Kolmogorov complexity of x given y , $K(x|y)$, is the length of the shortest program that outputs x given the input y .

Bennett et al. proposed *information distance* as a similarity measure that is calculated using conditional Kolmogorov complexity [9] (for our purposes, we treat similarity as the inverse of diversity: a test set in which the inputs are very similar lacks

diversity). For two strings, x and y , the information distance is:

$$ID(x, y) = \max\{K(x|y), K(y|x)\} \quad (1)$$

In other words, the similarity between entities x and y is the length of the shortest program that converts x to y , or the shortest program that converts y to x , whichever is larger. Bennett et al. show that information distance is a *universal* measure of similarity in the sense that if any other admissible metric detects a similarity between x and y , then so will the information distance.

The Kolmogorov complexity of a long string will be, in general, larger than that of a short string. For this reason, the information distance between two long strings will be, in general, larger than that between two short strings. In order to be able to compare similarities between pairs of strings across a range of sizes, Li et al. proposed the *normalized information distance* (NID) that normalizes the information distance using the Kolmogorov complexity of the two strings [16]:

$$NID(x, y) = \frac{\max\{K(x|y), K(y|x)\}}{\max\{K(x), K(y)\}} \quad (2)$$

NID takes values in the interval $[0, 1]$, where values closer to 0 indicate greater similarity. This particular choice of normalization has the advantage that NID retains the characteristics of a metric, i.e. that (i) $NID(x, x) = 0$ (identity axiom); (ii) $NID(x, y) + NID(y, z) \geq NID(x, z)$ (triangle axiom); and, (iii) $NID(x, y) = NID(y, x)$ (symmetry axiom).

In practice, it is not generally feasible to determine the shortest program that outputs a given string, and thus the Kolmogorov complexities that are used to calculate NID. Cilibrasi and Vitányi describe a practical alternative: the normalized compression distance (NCD) [14].

NCD is based on the observation that size of the output when compressing a string with real-world compression programs, such as gzip and bzip2, is a good approximation of its Kolmogorov complexity. If $C(x)$ is the length of the string x after compression by a chosen compression program, then NCD is given by:

$$NCD(x, y) = \frac{C(xy) - \min\{C(x), C(y)\}}{\max\{C(x), C(y)\}} \quad (3)$$

where xy denotes the concatenation of x and y . NCD takes values in the range $[0, 1 + \epsilon]$ where ϵ is a small positive value that depends on the degree to which the compression program approximates the Kolmogorov complexity.

B. Extending NCD to Multisets

NCD is a pairwise metric: it measures the degree of similarity between two strings. Of more interest in some situations is a notion of similarity between a multiset of strings (we use the strict terminology of *multiset* rather than *set* since the collection may contain the same string more than once). This is the case in this paper where we are interested in the similarity (or conversely, diversity) of a set of test cases considered as a whole.

Recently Cohen and Vitányi have extended the notion of NCD to multisets for this purpose. For a multiset X , the NCD

is calculated via an intermediate measure, NCD_1 , as [15]:

$$NCD_1(X) = \frac{C(X) - \min_{x \in X} \{C(x)\}}{\max_{x \in X} \{C(X \setminus \{x\})\}} \quad (4)$$

$$NCD(X) = \max \left\{ NCD_1(X), \max_{Y \subset X} \{NCD(Y)\} \right\} \quad (5)$$

Here $C(X)$ denotes the length of compressing the strings in X after concatenating them in some specific order (Cohen and Vitányi proposes length-increasing, lexicographic order in [15]). By defining the NCD of a set of one string to be 0, the NCD of a multiset of two strings is identical to the pairwise NCD between the two strings.

Since the term $\max_{Y \subset X} \{NCD(Y)\}$ requires the recursive evaluation of NCD for each proper subset of X , the calculation of NCD for multisets has time complexity $\mathcal{O}(2^N)$ where N is the size of the multiset. This is likely to make the calculation of NCD impractical for anything but the smallest multisets.

Cohen and Vitányi suggest instead an algorithm that has time complexity $\mathcal{O}(N^2)$ to approximate NCD for multisets [15] using the intermediate measure NCD_1 defined in (4) above. The algorithm starts from the multiset $Y_0 = X = \{x_1, x_2, \dots, x_n\}$, and proceeds as:

- 1) Find index i that maximizes $C(Y_k \setminus \{x_i\})$.
- 2) Let $Y_{k+1} = Y_k \setminus x_i$.
- 3) Repeat from step 1 until the subset contains only two strings.
- 4) Calculate $NCD(X)$ as: $\max_{0 \leq k \leq n-2} \{NCD_1(Y_k)\}$.

III. TEST SET DIAMETER

Information distance, and its practical realization as the normalized compression distance (NCD), has an appealing characteristic when used to assess the similarity (or diversity) of software tests: it is universal in the sense that it “discovers all effective feature similarities or cognitive similarities between two objects” [9]. If information distance is used to measure diversity between inputs, it can therefore be applied to inputs of any data type and so may obviate the need for domain-specific distance metrics such as the Euclidean distance between numeric inputs used by Bueno et al. [5]. Once one has determined a consistent way to dump the input data types to strings NCD can be applied.

The generic applicability and universality of the metric also permits a much wider range of information to be considered when determining the diversity of test cases. This benefit was investigated in the earlier work of Feldt et al. on the application of NCD to software testing [8]. The authors proposed a variability model that identifies a wide number of aspects in which test cases may differ. These aspects include: the setup of the SUT prior to executing the test, the test inputs, the execution trace of the SUT, the SUT’s output, and non-functional aspects of the execution such as the performance. Feldt et al. proposed that any of these aspects, or combinations of them, carry information that may be used to assess the similarity of test cases, and an empirical investigation demonstrated the use of pairwise NCD for this purpose.

In this paper, we investigate how the extension of NCD for multisets described recently by Cohen and Vitányi [15] enables similarity to be measured by a universal metric at the

level of entire sets of test cases rather between pairs of test cases.

We introduce the term *Test Set Diameter (TSDm)* to be the diversity of a test set measured using the NCD for multisets metric defined in the previous section. Using the aspects identified in the variability model of Feldt et al. [8], we may define a family of such metrics: Input TSDm where NCD is calculated on the multiset of test inputs, Output TSDm calculated from the multiset of outputs, Trace TSDm calculated from the multiset of execution traces etc.

In this paper we investigate the use of TSDm for selecting a diverse test set of a specified size from a larger pool of potential test cases. For this purpose, we leverage the NCD_1 algorithm proposed by Cohen and Vitányi to approximate NCD for multisets that was described in section II-B above. Since this algorithm uses the NCD_1 metric to approximate NCD, we refer to this procedure for selecting diverse test cases as $TSDm_1$.

The $TSDm_1$ procedure is provided with a pool of potential test cases, the size of the pool being as least as great as the size of the desired test set. At each iteration of the algorithm a subset of the pool is created by removing a test case in order to maximise the NCD_1 metric as described in section II-B. Thus a sequence of test sets of decreasing size is created by the procedure, and the subset of the desired size in this sequence is then chosen as the diverse test set.

IV. EMPIRICAL STUDY

We focus on evaluating the use of the test set diameter in selecting test cases based on input diversity, i.e. Input TSDm (I-TSDm). Our motivation is that this is a more ambitious and novel use case for automation in software testing. If possible it could allow the selection and thus design of test suites prior to even having started the implementation of the software system. As long as at least a partial specification and description of the interface of the software is present we could generate test inputs based on them and, via I-TSDm, select a small, diverse test set from them. Future work will investigate applications of TSDm to test execution traces (as in [8]), outputs from the software under test (SUT), as well as to different combinations of test inputs, trace information, and outputs.

Below we describe the design of our experiments by detailing the five research questions, the four experimental subjects and the methods and measures common to all of the investigations. For each research question, in turn, we subsequently describe the specific methods used to answer it as well as the results.

A. Research questions

Since the test set diameter is a new test metric there are a number of both fundamental as well as practical experiments that are needed. The basic assumption implicit in the test heuristic ‘select diverse test cases’ is that such test cases are more likely to cover diverse parts of the specification and thus of the software (since it implements the specification). At the most fundamental level we thus would expect that test sets with higher test set diameter have higher code coverage. If this is not the case it would seem very unlikely that we can

exploit any TSDm metric to improve testing. The first research question we investigate is thus:

RQ1 – Correlation to code coverage: Are higher levels of I-TSDm associated with higher levels of code coverage?

We do not expect any such correlation to be perfect, but there must exist at least some correlation that any automated method can then exploit. To investigate RQ1 we consider large numbers of sets of test inputs randomly sampled from an initial pool of randomly generated test inputs. We additionally vary the size of the subsets to better understand the sensitivity to the test set size of any observed correlation. Since we have no reason to expect that either the TSDm values or the code coverage values are normally distributed, we use the Spearman rank correlation coefficient to study the association between TSDm and code coverage. This is a nonparametric dependence measure which is not sensitive to the underlying distributions of values [17].

If we can find any correlation in RQ1, it is then natural to study if the TSDm₁ selection procedure described in section III can be used in practice to select better test sets.

RQ2 – Structural coverage ability: Do test sets selected based on I-TSDm lead to higher code coverage than randomly selected test sets?

We compare to random selection of test sets since this is the baseline technique available at a very early stage of software development. More sophisticated testing techniques would require an executable version of the software under test and are thus not comparable. To provide an upper limit for the level of coverage that could reasonably be expected, we compare the results to a post-hoc greedy algorithm (described in section IV-C below) and normalize the attained coverage level in relation to its results. This way we can compare results between different softwares under test. For all three methods we study how quickly the coverage grows as the test set size increases.

During preliminary experimentation it was evident that the size of each test input is a key feature in determining diversity and thus of exploiting I-TSDm: the TSDm₁-based selection would include any long test inputs first in the test sets and then gradually include shorter test inputs. In retrospect this makes sense since, on average, the longer a test input is, the more room there is for it to be different from others. However, this means there is a risk that any effect seen when investigating RQ2 is due simply to the input size rather than to diversity *between inputs of a given size*.

RQ3 – Structural coverage ability w. size constraints: Do test sets selected based on I-TSDm lead to higher code coverage than randomly selected test sets when we control for the size of test inputs?

Even though the test data generation technique we use [18] can be used to generate data with a specific size, we use here a simpler approach in order to avoid introducing unnecessary biases into the generated inputs: a large number of inputs are generated and only those close to a target size are selected. We vary the target size and include generated inputs that are within 10% of the target in the initial pool of test cases to select from.

It is not enough to cover larger parts of a program; what we ultimately want is to find faults so that we can eliminate them. By studying a SUT for which there are seeded faults we can investigate any benefits in fault finding ability.

RQ4 – Fault finding ability: Do test sets selected based on I-TSDm lead to higher fault coverage than test sets based on random selection?

The I-TSDMm metric, being based on the Cohen and Vitnyis algorithm described in section II-B, will theoretically scale as $O(N^2)$ (see section II-B) where N is the size of the initial pool of tests selected from. We investigate the scalability, in practice, of an implementation of the selection procedure, and give an indication of the actual times that may be expected for realistically sized test sets.

RQ5: Selection time: How does the time to execute the selection method scale as the size of the initial pool increase?

B. Software Subjects

JEuclid 3.1.9 is a Java library that renders images from MathML, an XML format for describing the presentation of mathematical equations [19]. The library is exercised by an application that takes MathML as input and renders the equation it describes in SVG format as output. The inputs for this subject are generated based on the XML Schema specification of MathML 2.0; the reader is referred to [20] for details. Since rendering to SVG is only one of a number of capabilities JEuclid, we restrict our measurement of coverage to the JEuclid core rendering and document handling module rather than the entire library. The core module has 11,556 non-comment, non-blank lines of code (SLOC).

ROME 1.0 is a Java library for parsing and converting RSS and Atom XML formats for syndication feeds [21]. The library is exercised by an application that takes an Atom feed as input, parses the feed, and outputs the contents and structure as text. The inputs are generated based on the XML Schema specification of Atom 1.0. We measure coverage of the entire ROME library, which has 11,704 SLOC.

NanoXML is a small Java library for parsing XML. We use the version of NanoXML from the Software-artifact Infrastructure Repository (SIR) maintained by the University of Nebraska-Lincoln [22]. The library is exercised by an application that is a variant of software provided by SIR for this purpose. The application takes XML as input, parses it, and outputs the contents and structure as text. These inputs are generated using the MathML generator that is also used for JEuclid. We measure coverage of the entire NanoXML library, which has 1,630 SLOC.

Replace is a C application from the Software-artifact Infrastructure Repository that performs pattern matching and substitution. It takes three inputs: a string to be modified, a regular expression that defines matching text, and a string that replaces the matched text. The regular expression is generated using a custom generator based on the specification of Replace; the string to be modified and replacement string are generated as random sequences of characters of size between 0 and 32 characters. The application has 538 SLOC.

C. Measures

All experiments were run on a MacBook Pro (Retina, Mid 2012) with a 2.7Ghz Intel Core i7 CPU and 16GB of DDR3 memory. The experimental framework as well as the TSDm and NCD related code were implemented in the Julia programming language [23]. For all experiments we used Julia version 0.3.8 (2015-04-30). All experiments used 10 independent repetitions unless otherwise stated.

1) *Coverage*: JaCoCo 0.7.4 [24] was used to measure the structural coverage of the Java subjects: JEuclid, ROME, and NanoXML. JaCoCo collects coverage information at the bytecode level while the Java Virtual Machine is running and thus does not require the code to be instrumented. JaCoCo evaluates a number of structural coverage metrics: for this work the metric used was instruction coverage.

For the Replace subject, coverage was assessed in terms of the detection of seeded faults in the application. This assessment used 32 variants of application provided by the Software-artifact Infrastructure Repository: each variant contained one fault that had been manually seeded (for reasons related to the framework used to perform the experiments, 1 of the 32 variants was excluded and so considered undetected by any test case). A fault was considered to be detected by a test case if the output and/or return status from the variant differed from that of the unmodified application.

2) *Greedy Coverage Algorithm*: The greedy algorithm starts with an empty test set. At each iteration, it considers all the test cases remaining in the pool and selects from these the test case that, if added to set, would improve the coverage the set achieves the most. This test case is then removed from the pool and added to the test set. This form of greedy algorithm is termed the ‘additional’ approach in the context of regression testing [25]. While I-TSDm uses only the test inputs themselves to select test cases, the greedy algorithm uses information obtained by dynamically executing the software under test using the test inputs. For this reason we consider the coverage achieved by the greedy algorithm as the best that could reasonably be achieved using the given pool of test cases.

D. Experiment 1: Correlation to code coverage

In order to investigate the relationship between I-TSDm and code coverage we would like a large number of test sets with as wide a range as possible of test set diameters. We could then measure their code coverage and study if there is any correlation. If we were to randomly sample subsets, it is likely we get mostly test sets with an average diameter and thus would be unable to assess the correlation over its full range of values. Simply increasing the sample size is not feasible since it would take a very long time evaluate code coverage for all of them.

We thus opted for a stratified sampling of test subsets based on an initial application of I-TSDm to 1000 randomly generated test inputs. These test inputs are considered in the order in which they are removed during the I-TSDm selection procedure and are divided into 10 consecutive strata: strata 1 includes test inputs numbered 1 to 100, strata 2 include numbers 101 to 200, and so on. To select test sets for experiment 1 we randomly select a strata and then randomly

TABLE I. SPEARMAN RANK CORRELATION VALUES BETWEEN I-TSDM AND INSTRUCTION COVERAGE FOR THREE DIFFERENT SUTS AND THREE DIFFERENT TEST SET SIZES.

SUT	Test Set Size		
	10	25	50
JEuclid	0.59	0.67	0.52
NanoXML	0.50	0.40	0.26
ROME	0.60	0.57	0.82

sample inputs within the strata. We repeat this procedure 100 times for each of the subset sizes 10, 25, and 50. This stratified sampling ensures a better spread of TSDm values and allows us to study any correlation to code coverage.

In Table I we can show the Spearman rank correlation values for each of the three investigated SUTs and for each investigated subset size. In all cases we are able to reject the null hypothesis that there is no correlation between I-TSDm and instruction coverage at p-values less than 10^{-4} , with the alternative hypothesis that the correlation is higher than 0.

The correlation values are in the range 0.40 to 0.82 with one outlier (NanoXML at subset size 50) with a lower correlation value (0.26). Overall the correlation between I-TSDm and instruction coverage can be considered a moderate positive correlation. In Figure 1 the three sets for each subject are plotted next to each other using the same scales for the instruction coverage (y axis) and I-TSDm (x axis). The pattern can be seen most clearly that as I-TSDm values increase on average as the test set size increase, and the same trend can be seen for the coverage values. For example, for ROME the average coverage is 0.254, 0.277, and 0.285 for test set sizes 10, 20, and 50 respectively. Note also that the spread of TSDm values shrinks as the subset size increases and that there is in general more variation for the smaller subset sizes.

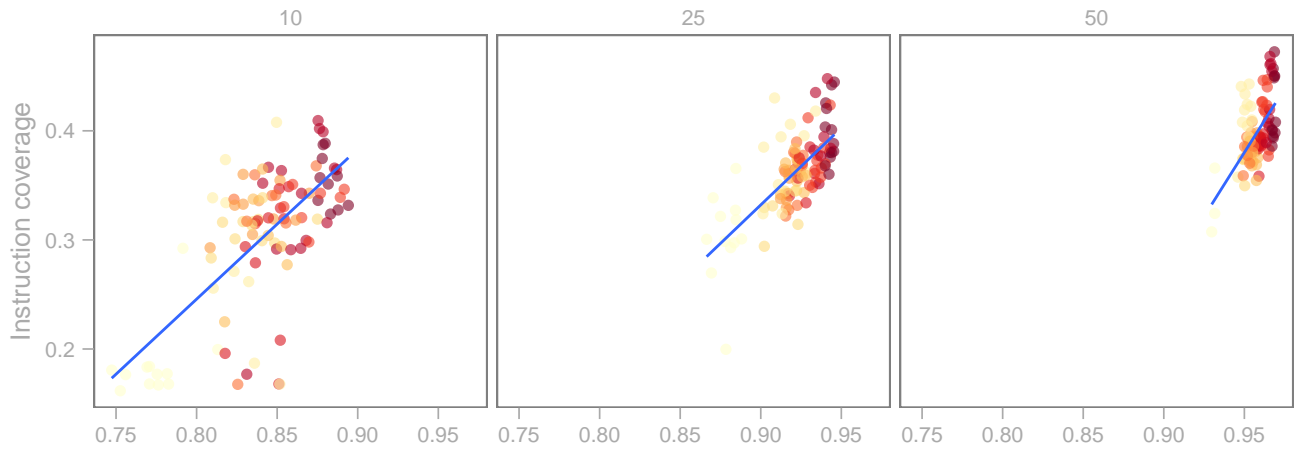
Test sets with higher input diameter (I-TSDm) on average have higher code coverage.

E. Experiment 2: Structural coverage

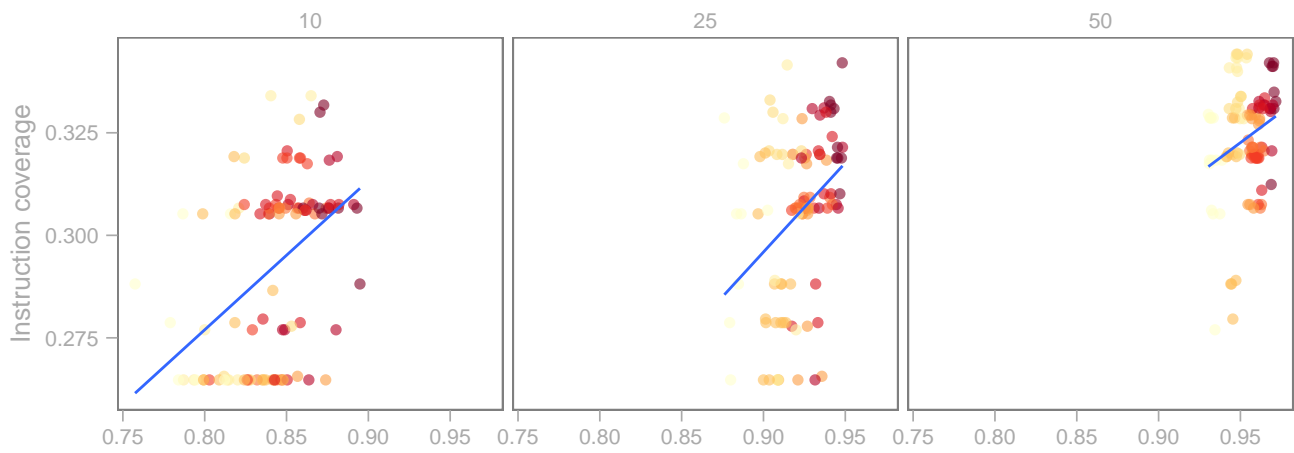
Since Experiment 1 demonstrated a correlation between I-TSDm and code coverage, we may reasonably expect that the TSDm selection procedure can be used to select high-coverage test sets. The results of Experiment 2 confirm that this is the case.

Figure 2 is a typical example of the coverage achieved by test sets selected using I-TSDm. The graph plots the instruction coverage of the ROME library against size for test sets selected using the greedy algorithm (red), I-TSDm₁ procedure (green), and random algorithm (blue) from an initial pool of 250 randomly-generated MathML inputs. The results are averaged over 10 runs and normalized to the maximum coverage attained by the test sets derived using the greedy algorithm.

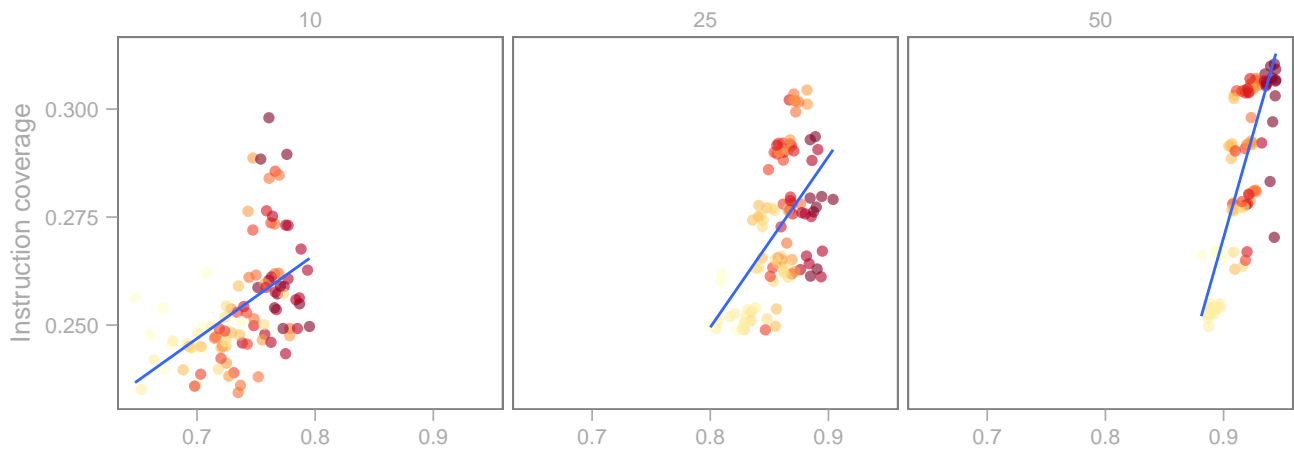
Interpreting the same results in a different way, Table II shows the average size of the test sets that are needed to reach 90%, 95%, and 99% of the maximum coverage using I-TSDm or random selection. On average, the random selection procedure require test sets that are 2 to 6 times larger than sets selected using I-TSDm. For example, test sets that achieve 95% normalised coverage are 77% (ROME), 80% (NanoXML), and 83% (JEuclid) smaller when selected using the I-TSDm₁ procedure than when selected randomly.



(a) JEuclid



(b) NanoXML



(c) ROME

Fig. 1. Scatterplots showing the correlation between Input-TSDm (x axes) with instruction coverage (y axes) for test sets of three different sizes (10, 25, and 50 test inputs respectively) randomly sampled from 10 different strata. Test sets with darker colors are sampled from strata with test inputs that are selected by the I-TSDm selection procedure when the subset is the smallest.

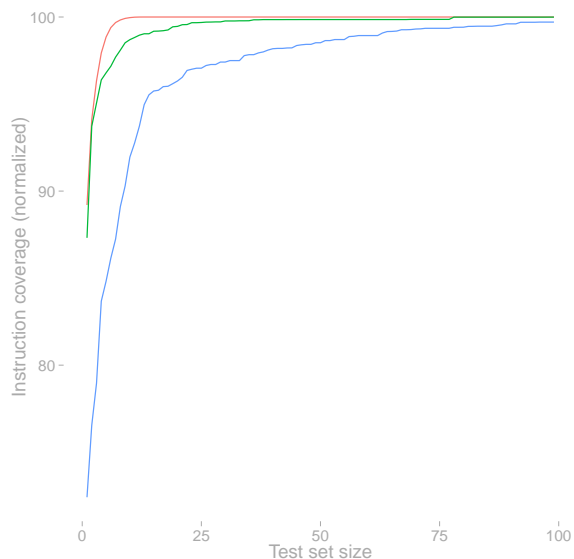


Fig. 2. Instruction coverage (normalized) of the ROME library against size for test sets selected using the greedy algorithm (red), I-TSDm₁ procedure (green), and random algorithm (blue) from an initial pool of 250 randomly-generated MathML inputs. The plots show the average values over 10 runs.

TABLE II. AVERAGE TEST SET SIZE NEEDED TO REACH 90%, 95%, AND 99% OF THE MAXIMUM INSTRUCTION COVERAGE REACHED BY THE GREEDY ALGORITHM WHEN SELECTING TEST INPUTS USING THE I-TSDm₁ PROCEDURE AND THE RANDOM ALGORITHM FROM AN INITIAL POOL OF 250 INPUTS.

SUT	Avg. Test Set Size					
	I-TSDm			Random		
	90%	95%	99%	90%	95%	99%
JEuclid	3.6	6.8	49.3	20.2	39.2	100.8
NanoXML	3.5	8.7	75.3	13.9	43.1	183.8
ROME	1.4	3.0	12.5	8.8	13.1	58.5

Test sets selected for highest test input diameter lead to higher code coverage than randomly selected test sets.

However, if we look at the length of test inputs as selected by the I-TSDm₁ procedure we can see an almost perfect correlation between test case length and the size of the test set in which they are first included. Figure 3 plots the length of the test inputs for one such sequence of test sets (for JEuclid). The Spearman rank correlation was 0.96 in this case, 0.93 for ROME and 0.96 for NanoXML.

In hindsight this effect is rather obvious: the longer the input the more opportunity there will be for the input to exercise different parts of the software under test. This suggests that rather than using elaborate test design strategies such as TSDm, simply selecting a few, large test inputs might be enough to cover a diverse set of aspects of the input space. In the next experiment we investigate whether I-TSDm is beneficial when the effect of input length is controlled for.

F. Experiment 3: Structural coverage under a length constraint

In this experiment, the benefit of I-TSDm is explored when the length of the test inputs is restricted to a small range. This corresponds to a requirement in practice to limit the

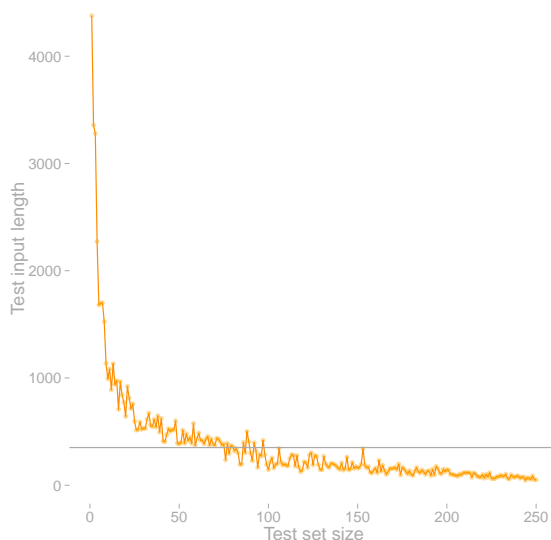


Fig. 3. Length of test inputs (for JEuclid) selected by the I-TSDm₁ procedure from an initial pool size of 250 plotted against the size of the test set in which they are first included, for one sequence of test sets. The mean value of 351.4 is indicated with the grey horizontal line.

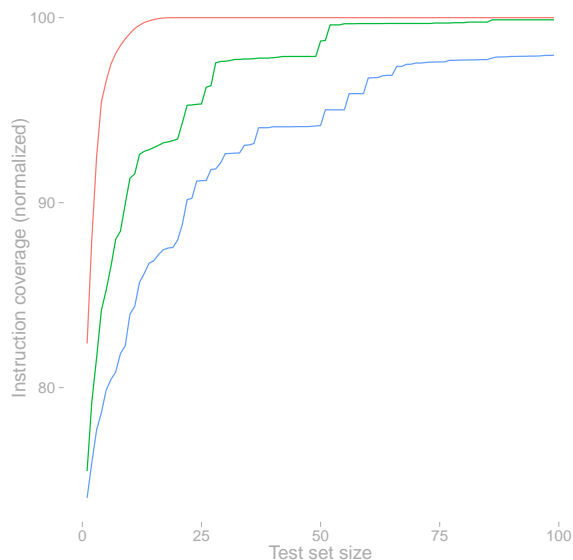


Fig. 4. Instruction coverage (normalized) of the ROME library against size for test sets selected using the greedy algorithm (red), I-TSDm₁ procedure (green), and random algorithm (blue) from an initial pool of 250 randomly-generated MathML inputs with lengths between 90 and 110 bytes. The plots show the average values over 10 runs.

length of test inputs: even when the test generation process is automated, the oracle is likely to be manual and thus the longer the test inputs the more difficult, and more costly, it will be to apply the oracle [26]. To evaluate if TSDm can help in this situation we re-ran Experiment 2 but limited the length of inputs in the initial pool to within 10% of a target length using a generate-and-filter approach, i.e. random inputs were generated and inputs outside the allowed length interval were discarded.

TABLE III. AVERAGE TEST SET SIZE NEEDED TO REACH 90%, 95%, AND 99% OF THE MAXIMUM INSTRUCTION COVERAGE REACHED BY THE GREEDY ALGORITHM WHEN SELECTING TEST INPUTS USING THE I-TSDM₁ PROCEDURE AND THE RANDOM ALGORITHM FROM AN INITIAL POOL OF 250 INPUTS WITH LENGTHS BETWEEN 90 AND 110 BYTES.

SUT	Avg. Test Set Size					
	I-TSDm			Random		
	90%	95%	99%	90%	95%	99%
JEuclid	29.9	40.9	90.3	82.2	135.3	217.3
NanoXML	1.9	19.4	75.1	18.7	38.2	207.2
ROME	9.1	21.7	51.3	21.9	51.0	129.0

Figure 4 shows the graphs for how instruction coverage (normalized) grows as the size of the test set increases. This corresponds to Figure 2 above but here the length of the inputs in the initial pool has been limited to range of 90-110 bytes. We can see that the coverage of the test sets selected using I-TSDm is now less competitive compared to the greedy algorithm than when the input length was unconstrained. However, it still maintains a considerable advantage compared to randomly-selected test sets. We tested with several target lengths, all with an arbitrary length range of +/- 10% for the generate-and-filter approach to be practical, and the patterns persist until the target length is large and the advantage to select based on diversity diminishes. It seems that when each input is long enough to exercise a large part of the intended behavior we can pick any, i.e. random selection ‘catches up’. Selection based on diversity thus seems to have a use for applications of automated test generation where humans will look at the generated tests, since humans will generally prefer shorter over longer test inputs and test cases.

Table III shows the average test set size to reach different levels of the maximum instruction coverage reached by any of these test sets. We note that for a given coverage level, a test set selected using the I-TSDm₁ procedure is 2 to 9 times smaller than a randomly selected set. For example, test sets that achieve 95% normalised coverage are 49% (NanoXML), 57% (ROME), and 70% (JEuclid) smaller when selected using the I-TSDm₁ procedure than when selected randomly.

Comparing these results to Table II, it is clear that larger test sets are required than when the input length is unconstrained, and this occurs for *both* I-TSDm and the random algorithm. For ROME a test set of approximately 22 inputs is required to reach the 95% coverage using I-TSDm, while only 3 inputs are needed when the length is constrained. However, we exercise caution in comparing these tables since the unnormalized coverage values reached differ for some of the SUTs. For NanoXML and ROME a similar coverage level is obtained with and without a length constraint—36.1% and 32.8% respectively; but for JEuclid a coverage of 46.8% is reached when input length is constrained, and 59.8% when it is unconstrained.

Test set diameter can lead to higher code coverage even if we control for the size of test inputs; test diversity is more than simply the input length.

We note that in future work one should investigate if the coverage ability per bit (or byte) of a test set is a useful metric when comparing and searching for test sets. Our results on the importance of test case length implies that considering the total length of a test set is very important.

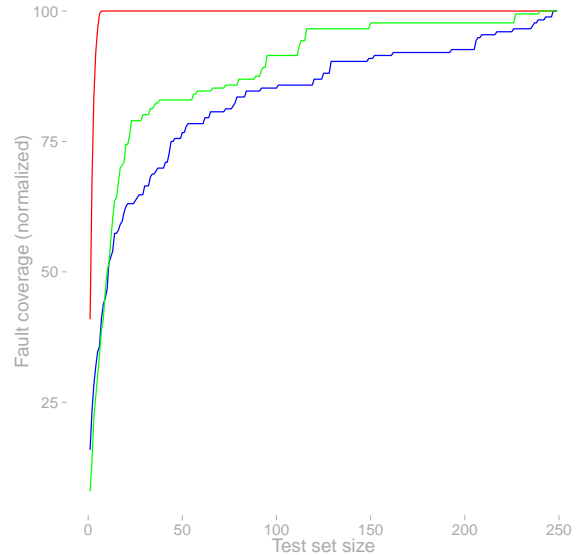


Fig. 5. Fault coverage (normalized) of the Replace SUT against size for test sets selected using the greedy algorithm (red), I-TSDm₁ procedure (green), and random algorithm (blue) from an initial pool of 250 randomly-generated inputs with the length of the regular expression between 9 and 11 bytes. The graphs are the average values over 10 repeated runs.

G. Experiment 4: Fault-finding ability

For effective testing, structural coverage is not enough; ultimately the objective is to find faults. In this experiment we used the variants of Replace SUT with seeded faults to compare the fault-finding ability of the different procedures for selecting test inputs. As discussed in section IV-B, this SUT takes three inputs, but the regular expression input is by far the most important in determining the execution path. We therefore consider, and control for, only the length of this input.

Figure 5 shows that I-TSDm selects test sets with higher fault coverage than randomly selected ones, on average, and the greedy algorithm has a fault-finding ability that is substantially better than both. Test sets that achieve 95% normalised fault coverage are 45% smaller when selected using the I-TSDm₁ procedure than when selected randomly.

Test sets with larger test set diameter (I-TSDm) may have better fault-finding ability.

Of course, additional experiments that apply I-TSDm to the selection of test sets for a wider range of SUTs is necessary to be confident of the generality of this result.

H. Experiment 5: Test set selection time

By collecting the run times of the I-TSDm test selection procedure during the experiments above, we are able to model its performance. Since we expected a $\mathcal{O}(N^2)$ overall scaling (see section II), we investigated a few different models that included this term. We found that a model of the form $S_{avg} \times N^2$ where S_{avg} is the average length of the strings being selected and N is the number of elements in the initial pool explains the observed times very well. This is natural; we expect a linear scaling in the average length of the elements

being compressed, as well as the $\mathcal{O}(N^2)$ scaling from the NCD_1 reduction procedure. The R^2 goodness-of-fit had a value of over 0.99 when we fit this model with ordinary least squares regression.

The TSDm test selection procedure scales quadratically in the size of the initial pool of tests to select from, and linearly with the average length of the tests.

In practice this means that 40-60 minutes of compute time were required on the machine we experimented on for an initial pool of 1000 test inputs with an average size of a couple of hundred bytes. Future work should investigate ways to speed up the process; possibly one can parallelize the calculations and/or exploit approximations based on initial filtering using pairwise NCD calculations.

V. DISCUSSION

We have proposed the test set diameter (TSDm) as a family of diversity metrics with general applicability for software test generation and analysis. Our empirical study applied TSDm to the selection of test sets from a pool of randomly-generated test inputs and confirmed that it has a moderate to high correlation with structural code coverage. This is important since it can then be used early in a development process and uses a metric which is neither data type nor domain specific and thus can be applied in general, without further specialisation. An important result from the study is the superiority of TSDm selection procedure compared to selecting test sets at random. For three Java software systems that take XML-based inputs, TSDm selects test sets that are 2 to 9 times smaller than randomly-selected sets that reach the same, high level of coverage. And on a software function implemented in C using a pool of inputs generated by a naively-implemented generator, TSDm demonstrated improved fault coverage compared to random selection. However, calculating TSDm is not cheap; even its approximation scales quadratically with the size of the pool from which test cases are selected.

Our results have implications for both theory and practice. There is a general lack of theories in Software Engineering [27], but as already noted by Chen et al [27] when discussing the merits of adaptive random testing, diversity is a common thread to a large number of results in software testing. By taking a theoretically well-founded perspective of diversity based on Information Theory [9], [10], we can formalize what diversity means in software testing and explore if there are limiting laws. As we have argued elsewhere [28] there are a number of connections from Information Theory to software testing but diversity quantification is an important one and should be explored further. Our results on the importance of considering the length of test inputs generated should also be a word of caution to other researchers in automated software testing; are their results valid for different sizes of generated test cases?

For practice, there are numerous implications of our results. It is clear that TSDm can be used to select test sets that are more effective than randomly selected ones. Even if this will not always hold true there seems to be little risk in applying I-TSDm since there are so few alternative techniques that apply at early software development phases. Even if testers

will continue to manually select test cases they can then use TSDm to search for additional test cases that most increase the overall test set diameter [18], [29]. This process could even be interactive: the tester is iteratively presented with a selection of highly diverse test cases to choose from [30], [31].

An intriguing practical implication of our results is that we can use TSDm to analyse existing test suites. For example, ordering manually created test cases in a test set by TSDm, visualizing the results and discussing them with the testers might lead to insights into the relative importance of test cases in a similar way to what have been achieved for historical test outcomes [32]. This can also help guide reductions of the test set as well as evaluation of newly proposed test cases that would most increase test set diversity.

Apart from the quadratic scaling of the test selection procedure time, there are a number of other limitations to our approach. One disadvantage to using NCD is that it is unclear what is the basis for a difference between two test cases. Test sets are not solely used for finding faults or ensuring coverage, but are also important elements in arguments for the quality, reliability and safety of a software system. For this use case there would be a benefit in a method that could not only select test cases but could explain why it has made a certain selection. Creating such a system based on NCD seems harder than creating one based on data type specific metrics.

Another limitation is that we do not yet understand the effect that the choice of compression algorithm has on NCD metrics. In informal investigations we have found TSDm results to be robust to variations in the compression algorithm used. However, many compression algorithms have some idiosyncratic design or implementation choices that might make them more or less suitable for the NCD calculation. For example, we tried to switch the default Zlib compressor for some of the faster ones in the Blosc library [33]. However, they do not compress at all if the input string is less than 128 bytes. Such discontinuities might negatively impact the value from applying NCD based metrics. Preliminary investigations indicate that this is less of a problem for NCD for multisets that for pairwise NCD calculations since the former concatenates several strings and thus, in general, leads to longer strings.

The generality of NCD for multisets might make it attractive also to analyze and exploit non test-related software information in testing. For example, the text that can be found in software artefacts such as requirements, specifications, design documents, and source code might be used to find both test cases that are close to or different from such information. However, we note that the base NCD measure might not be applicable for things that are named rather than self-describing. Cilibrasi and Vitányi have proposed to instead use the Normalized Web Distance for such information [34]. Exploring this metric for software testing purposes remains an important area of future work.

An alternative method against which to compare I-TSDm test set selection would be manual selection, i.e. test sets created by humans. For two of the SUTs we have studied the Software-artifact Infrastructure Repository (SIR) provides test sets, but the test strategy used to create the test cases is not always clear, and we could not reliably use them for this purpose. For this study we thus consider maximum coverage

level attained by the greedy selection algorithm as a good approximation of what a human tester could achieve. Future research should nevertheless investigate the comparison to manual selection in more detail.

VI. RELATED WORK

The notion that more diverse test sets are beneficial for software testing has been around for some time; what has varied in the literature is the definition of the distance on which the diversity is defined. In a very limited sense, diversity can be interpreted as trying not to use the same subset of test cases repeatedly. Kim and Porter implemented this idea as the history-based test prioritization, in which the chance of selecting a test case is proportional to the elapsed time since its last execution [35]. Yoo et al. argued that repeated use of the same subset can ‘wear out’ the selected test cases, and recommended using different subsets at each test iteration [36]. While these works can be considered to concern test diversity, they are limited to making the best use of a given set of tests and cannot help test engineer to compare two sets of tests.

Test execution traces have been used as the basis of a richer diversity measure. Leon and Podgurski [37] used the proportional binary distance (a variation of Euclidean distance for binary strings) to cluster test coverage vectors, and concluded that the more diverse the chosen subset of tests is, the higher the fault detection capability is. Nikolik has incorporated both control and data flow information to the definition of test diversity [38]. Ciupa et al. introduced the *object distance* for object oriented programming languages by defining the distance between two object instances as the weighted sum of the distances between primitive members [39]. Bueno et al [5] introduced a pairwise test set diversity measure based on Euclidean distance, and applied a metaheuristic search in the context of adaptive random testing. In a later study the authors mention that other distance measures could be used but the empirical work investigates numerical vectors only [40]. The common thread in the existing work is the underlying use of Euclidean, Hamming, or Levenshtein distance, which either limits the applicability of the technique to numerical data, or loses high-level semantics. In contrast, we use a universal distance measure, NCD, which is free from the dependence on numerical vectors and has been proven to handle high-level semantics in the data. Feldt et al. [8] applied NCD to test execution traces but in a pairwise manner and thus could not help test engineers to compare *sets* of test cases, as we do here. Related is the work by Hemmati et al [41] that study a large number of different similarity functions applied pairwise to abstract test cases in model-based testing. Their paper can serve as an extensive overview of many of the pair-wise distance functions that exist.

Obtaining test execution traces requires instrumentation of the SUT. Alshawan and Harman focused instead solely on the output of the SUT [6], [7] and showed that the test set with more diverse output can produce correspondingly higher fault detection capability and structural coverage. While Alshawan and Harman’s work focused on the diversity in the observed output, the current paper focuses on the diversity in the test *input*, thereby allowing the analysis to take place even before test execution or system implementation. Since multiset NCD can be applied also to outputs a more fundamental difference

is that Alshawan and Harman’s output uniqueness measures are essentially binary since they only judge if two output are different or not. In contrast, the NCD metric used here can also quantify *how* different, for example, outputs are. This should be important for software systems with large output spaces where most inputs are likely to return unique outputs or, in general, since it gives a more graded response than binary. Alshawan and Harman’s measures instead filter the outputs before judging uniqueness and can thus consider uniqueness for different aspects. However, filters can also be used prior to applying NCD as noted by [8]. Future work should investigate the relative benefits of filters and/or binary uniqueness versus continuous measures such as NCD, for both inputs and outputs.

VII. CONCLUSIONS

Even though it has been long-argued that test sets with more diverse test cases are better, this notion has remained fuzzy and has been hard to apply in practice. Previous research has either focused on measuring distance only between pairs of test cases, or has been limited to specific data types. In this paper, we propose a metric called the test set diameter (TSDm) that measures the diversity of the test set as a whole. It has a formal basis in Kolmogorov complexity and applies to any data type and source of test related information. By approximating its calculation using modern compression algorithms it can be put to practical use for test selection and analysis.

Our empirical work evaluated the TSDm applied to test inputs. This is one of the more ambitious and difficult tasks in automated testing; one in which we need not even have started to implement the software we are going to test. Our results show that the input TSDm measure shows moderate to high positive correlation to instruction coverage for three open-source Java systems. A test selection procedure based on TSDm can approach a post-hoc greedy test selection procedure that needs actual coverage information from all test inputs in an initial pool. However, TSDm’s success appeared to be in part achieved by selecting large test inputs early. By controlling for input size we show that TSDm still gives a considerable advantage compared to random selection. Finally, we applied the input TSDm selection procedure to a software implemented in C which has seeded faults. There is a positive effect on fault coverage: test sets that reach the same fault coverage level are 27 to 45% smaller than those selected at random.

We argue that being able to rank test sets based on their diversity is important for software quality in general. However, diversity quantification is not enough; based on our empirical study we conjecture that many factors together determine the effectiveness of a test set including the diversity of the test data generator and the size and diversity of the initial pool selected from. Future work should evaluate them in detail and quantify their effect. We propose that this can lead both to a more fundamental understanding of test quality as well as practical techniques that improve it.

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