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Transport properties of water molecules confined between hydroxyapaptite surfaces: A Molecular dynamics simulation approach

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Abstract

Water diffusion in the vicinity of hydroxyapatite (HAP) crystals is a key issue to describe biomineralization process. In this study, a configuration of parallel HAP platelets mimicking bone nanopores is proposed to characterize the nanoscopic transport properties of water molecules at HAP-water surface and interfaces using various potential models such as combination of the Core-Shell (CS) model, Lennard-Jones (LJ) potentials with SPC or SPC/E water models. When comparing all these potentials models, it appears that the core-shell potential for HAP together with the SPC/E water model more accurately predicts the diffusion properties of water near HAP surface. Moreover, we have been able to put into relief the possibility of observing hydroxyl (OH^-) ion dissociation that modifies the water structure near the HAP surface.

Keywords: Molecular Dynamics Simulation, HAP-Water Systems, Water Self Diffusion, H-bonding and Hydroxyl Dissociation

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1. Introduction

Investigation of bone-material is very important to understand the physical properties at bone-material interface [1-5]. Bone mineral phase is made of hydroxyapatite (HAP) [6] which is also present in the teeth enamel. It is often necessary to understand the phenomena occurring at the nanometric scale of the HAP minerals of bone (molecular unit formula $[Ca_{10}(PO_4)_6(OH)_2]$) to understand the macroscopic behaviour of this organ [7-9]. During biomineralization, bone-water interface plays an important role in the mechanism of bone reorganization [10]. Thus, the investigation of HAP-water interface materials received widespread attention to understand the chemical, physical and mechanical properties of these materials considering the confinement effect of water near the HAP surface [5,11-13].

Similarly, HAP scaffolds are often used in bone repair [14] and is thus the prototype model for the biomaterial adsorption studies [15,16]. The metabolism of bone tissue is characterized by the surface interactions between HAP crystals, cells, water molecules and bridging proteins [17]. Numerous studies have thus been devoted to understand the interaction between HAP surfaces with biomolecules, water, ions, and gases using experimental and theoretical methods [18-25].

In particular, it was shown that the interactions between a surface and water molecules may affect the local environment of the interface, modifying the diffusion properties of water molecules which tends to reduce when compared with the bulk phase properties. Several experimental and theoretical reports have been devoted to understand the unusual dynamics of water under confinement [26-32]. Orientation and diffusion mechanisms of water molecules in the vicinity of a surface is still unclear. These reports reveals that polarity, hydrogen bonding (H-bonding) and orientation play a vital role for diffusion of water molecules.

Using a molecular dynamics (MD) approach, we were recently able to tackle the question of the interstitial bone fluid flows at the nanoscale [5]. These preliminary results have suggested that mobile water can be observed within HAP pores of the same size as the nanopores measured in bone by Holmes et al. [33]. Based on a molecular dynamics approach involving inter-atomic potentials models for HAP and water systems

developed by Leeuw [34], this seminal study was well describing the HAP-water structure at the interface, but was badly adapted to properly describe the diffusive process of confined water [11]. That is why, in this paper, we intend to propose a comparison between different HAP-water models in the perspective of their ability to describe properly the confined diffusion of water in nanopores.

The structure of this paper is therefore rather classical since the different water-HAP models are presented in a first Materials and methods section. In particular, the simulation strategy is presented. Then, a section is devoted to present the results and discuss their implications. The peculiar phenomenon of hydroxyl dissociation is also stressed out. Finally, conclusions and prospects are presented.

2. Materials and methods

2.1. Simulation boxes

HAP [$Ca_{10}(PO_4)_6(OH)_2$] is seen as a hexagonal primitive cell with $P6_3/m$ space group, each sphere representing a tetrahedral (PO_4^{3-}) ionic complex. Its natural organization in bone matrix corresponds to a stack of thin micro-plates with dimensions (L × l × e), where L=250-500 Å, l=150-250 Å and e = 25 Å [35]. That is why, similarly to the configuration in our previous study [11], the dimensions of parallelepipedic shaped simulation boxes are adjusted to contain (3×3×4) such micro-plates.

Due to partial occupancy of OH sites, the orientation of OH groups always protruded away from the surface (i.e. c axis). Moreover, the simulation box contains a water layer whose height may be varied (in the *c*-axis direction) from 20 Å to 200 Å to mimic bone nanopores size. This variation of the water layer thickness is performed by adding or removing water molecules.

The position of each atom in the box is given using its Cartesian coordinates (x,y,z) in the orthogonal frame (e_1,e_2,e_3), see Fig. 1. The HAP platelets and water layers constitute the elementary cell which is repeated periodically along the $\mathbf{e_3}$ axis. The initial coordinates and crystal cell parameters were taken from [36].

2.2. Choice of different intermolecular interactions models

Four types of interatomic potential models were used to describe the interactions in the HAP nanopore-water systems. In the first model hereafter named ***CS-water***, the interactions between particles were represented by the core shell interatomic potential developed by de Leeuw and Parker for HAP and water systems [18,37], which includes electronic polarizability via the shell model of Dick and Overhauser. This model was used in our previous studies [11,12]. In this CS-water model the phosphate, hydroxyl group, and oxygen–hydrogen (H_w) bonds are described as the sum of a Morse and a Coulombic potential, the phosphate and water bond angles by a harmonic potential, and non-bonded interactions by Buckingham potentials. This force field makes use of a shell model to represent the oxygen's electronic polarizability in the phosphate and hydroxyl groups, and in the water molecules, in which each oxygen atom consists of both a core and a massless shell connected by a spring.

In the second model, hereafter named ***LJ-SPC***, the HAP interactions were described through Lennard-Jones potentials as proposed in [38] while water molecules were described by the SPC model.

The third model (noted ***LJ-SPC/E***) is the same as the LJ-SPC except that the SPC/E water model was used instead. This is motivated by the good ability of the simple point charge (SPC/E) model to represent density, radial distribution functions, self-diffusion coefficient for water; and hydrogen-bond dynamics in good agreement with experiment [39-41]. The parameters set for the SPC and SPC/E models can be found in [39,40].

In the fourth model (noted ***CS-SPC/E***) the core-shell representation of the HAP mineral of de Leeuw and Parker [37] was combined with the SPC/E water model. This combination of potentials models was validated by activation energy (Ea) calculations [42].

The parameters of these models are listed in Tab. 1 and Supplementary Material (Tables S1 and S2).

2.3. Simulation process

Simulations were performed using the DL POLY molecular dynamics package (version 4.05.1) [43]. Each system was equilibrated in the microcanonical (NVE) ensemble for 50 ps, followed by 100 ps simulations in the isothermal–isobaric (NPT) ensemble, during which the volume was monitored in order to confirm the system reached equilibrium. The Melchionna modification of the Nosé-Hoover algorithm [44] was used with 0.5 ps for the thermostat and barostat relaxation times to maintain an average pressure of 1 atm and an average temperature of 310 K. This choice was made for comparison purpose with our previous work [11], which dealt with human bone environment under in vivo conditions. Thus, pores sizes typically range to classical bone nanopore sizes measured by [33] (between 50 Å and 125 Å).

Production runs in the NPT ensemble were then conducted for at least 2000 ps (i.e. 2 ns). The leap-frog algorithm with a time step of 0.1 fs was used to integrate the equations of motion. Periodic boundary conditions were applied in all directions of the box. The long range electrostatic interactions between the charges of all species were computed using the Smoothed Particle Mesh Ewald (SPME) method with the acceptable relative error of 10^{-6} [45]. The cut-off for calculation of the non-bonding interactions was set to 9 Å.

3. Results and discussion

3.1. Self-Diffusion Coefficient of Water

Our analysis is here focused on describing water diffusion process by depicting the self-diffusion coefficients of water for the different water models for various degrees of confinement, that is to say for various pore sizes.

The self-diffusion coefficients of water molecules D were calculated from the mean-square displacement (MSD) using Einstein's expression:

$$D = \frac{1}{2}\frac{d\left\langle\left\langle\left|\left[r(t)-r(0)\right]^2\right|\right\rangle\right\rangle}{dt} \quad (1)$$

Here, *r(t)* corresponds to the position of a particle (water molecule) at time *t*. The chevrons notation stands for the averaging procedure.

Figure 2 displays the dependence of the self-diffusion coefficient *D* in terms of pore size *H* at 310K for the four HAP-water interaction potentials models. Note that the experimental bulk water self-diffusivity is also presented by the green bullet.

As expected, it is found from our calculation that the self-diffusivity of water gradually increases with the pore sizes, whatever be the type of interaction potential model.

Indeed, at 298 K for instance, the bulk water diffusion coefficients for SPC or SPC/E models are 3.85 and 2.3×10^{-9} $m^2.s^{-1}$, respectively [46]. Here, due to the confinement effect, the calculated values are always lower even if the higher temperature should induce an increase in the water molecules mobility. This is due to the strong electrostatic interactions between the HAP surface and water which tend to limit the diffusion process. This will also affect the orientation of water and cooperative effect between surrounding water molecules. A similar trend has also been observed for the other nanoporous materials such as SiO_2, Fe_3O_4, CNT, and proteins [46].

When focusing on the differences between the different potentials models, it is first to notice that the LJ-SPC model always provides a much higher value of the water diffusivity than the other potentials models (LJ-SPC/E, CS-SPC/E, CS-water) which give more similar values. This may be explained by the charges of the SPC water model that are lower than the ones of the SPC/E model for instance, causing a faster diffusive transport.

Furthermore, for the small pores (H < 80 Å), it appears that the CS-water model of our previous study [11] and the CS-SPC/E present diffusion values that are slightly lower than the LJ-SPC/E predictions. For larger pores, this trend becomes the opposite.

It is interesting to note that for small pore sizes (between 20 and 50 Å), the confinement effect on the diffusivity coefficient is linear, whereas for larger pores, this is no more the case. This clearly states that two different kind of diffusion mechanism are possible in structures presenting a HAP-water interface. This may be an evolution from a quasi 1D diffusion process in the narrow pores to anisotropic diffusion of water molecules for lower confinement.

Moreover, for the largest simulated pore size value H = 200 Å, that is to say for the weakest degree of confinement, it appears that the value obtained from the CS-SPC/E combination potentials model is in very close agreement with the experimental bulk water property. Indeed, a comparison of CS-SPC/E and LJ-SPC/E potentials models gives meaningful insights on the selection of suitable force field for the study of water in contact with HAP surface. For a 200 Å pore size, the CS-SPC/E calculated value of the water self-diffusion, respectively its experimental bulk value, is 2.62×10^{-9} $m^2.s^{-1}$, respectively 3.02×10^{-9} $m^2.s^{-1}$. This confirms earlier reports that concluded that CS potentials are more suited for describing the HAP-water interface phenomena [2].

The role of interstitial fluid flow in bone activity is central through its contribution to the transmission of remodeling signals [47,48]. In particular, nanoscopic flows occurring inside the collagen-apatite matrix of bone may modify the vicinity of the osteocytes [5] which are key actors of bone adaptation. As a result, water diffusion occurring in the vicinity of the HAP crystals is an avenue of research of great interest in bone physiology.

3.2. Observation of Hydroxyl ions dissolution

Due to the strong inductive effect from Ca ion and Ca-O_w bond, water molecules can adsorb/desorb at this interface. This phenomenon plays a role in the OH^- ion reorganization on HAP surface, and may locally affect the ionic concentration since we observed hydroxyl dissociation through our simulation with the CS-SPC/E model (see Figures 3 and 4). This anionic specie tends to form multiple H-bonds (acting as a donor as well as

acceptor) with the surrounding water molecules. Due to this effect, the translational and rotational mobility of water molecules at this interface become unusual. To describe this phenomenon, atomistic modeling approach can give valuable information to understand the adsorption/desorption and reorganization mechanism in HAP interface. This point is crucial during the biomineralization for instance.

It is interesting to note that from our calculations, the hydroxyl dissociation always depends on the pore size. In most of the cases, OH- ions are dissociated and localized only near the surface (see Figure 3) whereas in the case of medium pore sizes (i.e. H=50-70 Å, see Figure 4) we also observed OH^- ion slightly moving away from the HAP surface and becoming fully surrounded by water molecules via H-bonding interactions. Notice that H-bonding interactions between OH^- ion and water molecules are stronger and shorter compared to the normal water-water H-bonding interactions (see Figure 4).

4. Conclusions and perspectives

We have conducted extensive molecular dynamics simulations of nanopores of HAP containing liquid water in order to determine the effect of confinement on the diffusion properties of water by comparing various combination potentials models. When comparing all these potentials models, it appears that the core-shell potential for HAP together with the SPC/E water model more accurately predicts the diffusion properties of water, the obtained values of the average diffusion coefficients being in good agreement with the experimental data from both bulk and bone-water interfaces [49-51].

Due to the strong interactions between water molecules and the functional groups of HAP which are dominant in such confined environment, the diffusion in the nanopore direction is significantly faster than in the direction perpendicular to the HAP surface. As a result the diffusion process depends on H-bonding and orientation of water molecules on the surface. We showed that water molecules mainly interact with calcium ions, reducing its adsorption in the vicinity of the phosphate sites. Thus both Ca ion and OH groups protect the interaction between water and phosphate groups (Fig. S1).

Therefore we propose that strong inductive effect from Ca^{2+} and electrostatic interactions between water and

surface tend to limit the diffusion process along the z-direction and at the same time induce the water molecules to move along x-direction via H-Bonded interactions. Our study can thus provide the valuable information to understand the mechanism of water movement during the biomineralization process.

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TABLES AND FIGURES

Tables

Table 1. Potential parameters used in this work for the Lennard-Jones and water models.

Atomic Partial Charges: (for LJ)	
Atom Types	**Charges (e)**
Ca	+1.5
P	+1.0
Phosphate Oxygen (O2)	-0.8
Hydroxy Oxygen (O1)	-1.1
Hydroxy Hydrogen (H1)	+0.2
Water Oxygen (Ow)	SPC= -0.82; SPC/E= -0.8476
Water Hydrogen (Hw)	SPC= +0.41; SPC/E=+0.4238

Lennard-Jones (LJ) Potential: $U(r) = 4\varepsilon\left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^{6}\right]$		
Ion Pair	ε (in kcal/mol)	σ (in Å)
Ca-O1	0.10198	3.5
Ca-O2	0.09539	3.35
O1-O1	0.08	3.7
O1-O2	0.07483	3.55
O2-O2	0.07	3.4
O_w-O1	0.1115	3.433
O_w-O2	0.104298	3.283
O_w-Ca	0.142434	3.233
O_w-O_w	0.1554	3.166

Harmonic Potential: $U(r) = \frac{1}{2}k(r - r_0)^2$		
Ion Pair	k(kcal/(mol.Å^2))	r_0(Å)

P-O2	430	1.57
H1-O1	500	0.94
O_w-H_w	1108.2698	1.00
Three-body Potential: $U(\theta) = \frac{1}{2}k(\theta - \theta_0)^2$		
Ion Group	k(kcal/(mol.rad^2))	θ_0(°)
O2-P-O2	125	109.47
H_w-O_w-H_w	91.5392	109.47

Figures

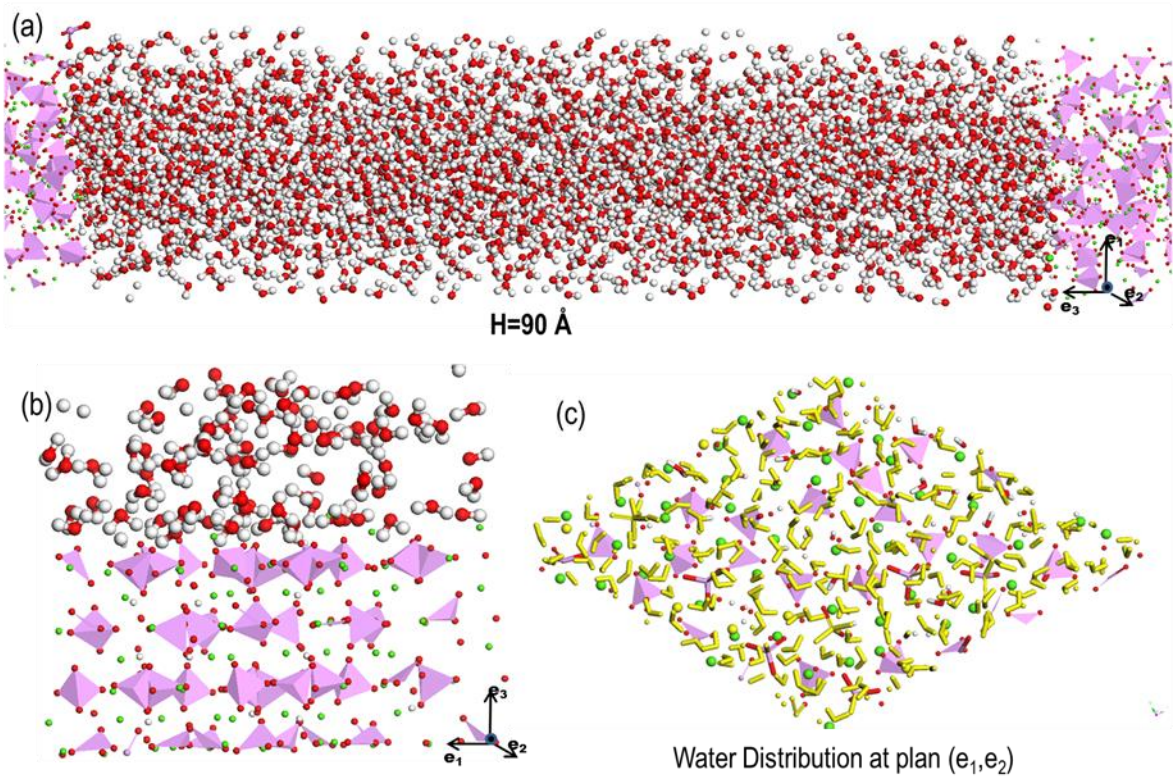

Fig. 1. Water-HAP system (Ca-green, PO_4^{3-}-pink, O-red, H-white): (a) Molecular arrangement of water molecules in a 90Å HAP pore; (b) Interaction of water layers with surfaces; (c) Water layer (yellow) adsorbed on the HAP surface.

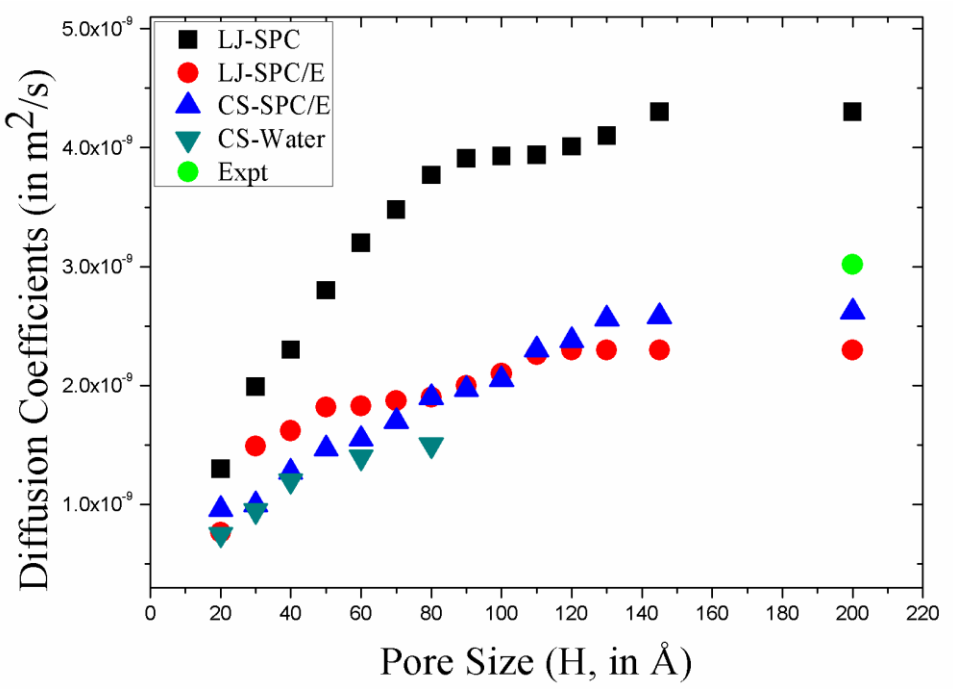

Fig. 2. Self-diffusion coefficients of water molecules calculated at 310 K for various pore sizes (H = 20 to 200 Å) with different potentials models: LJ-SPC, LJ-SPC/E, CS-SPC/E, CS-water. The experimental diffusion coefficient is also presented.

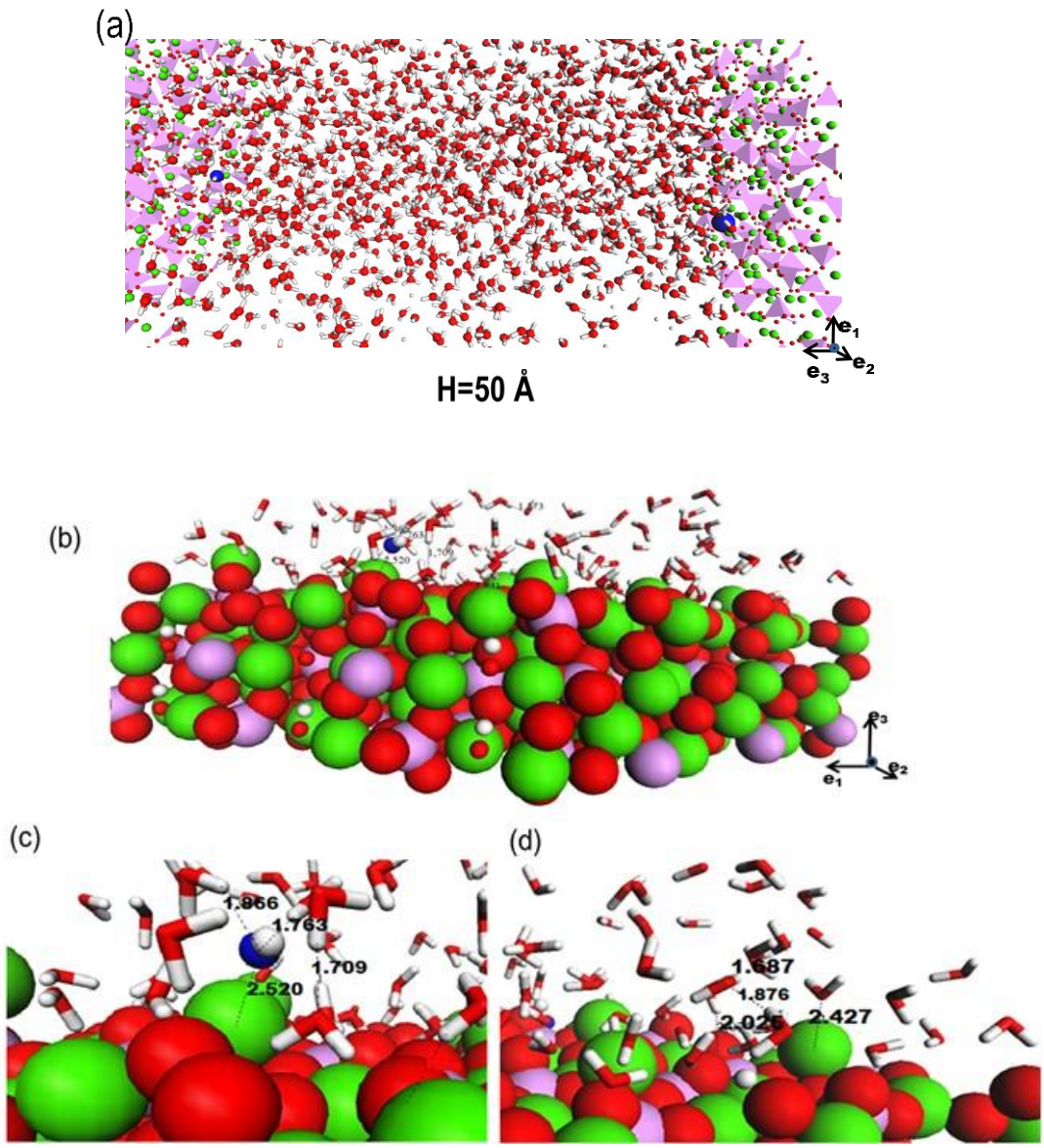

Fig. 3. Hydroxyl ions in HAP-Water system (Ca-green, PO_4^{3-}-pink, O-red, H-white and hydroxyl O-blue): (a) Molecular arrangement of water molecules and OH^- ions in a 50 Å HAP nanopore; (b) Interaction of OH^- ions with HAP-water layers; (c) and (d) shows the close views of H-bonds (distances are in Å) for OH^--water and water-water, respectively, at the vicinity of HAP interface.

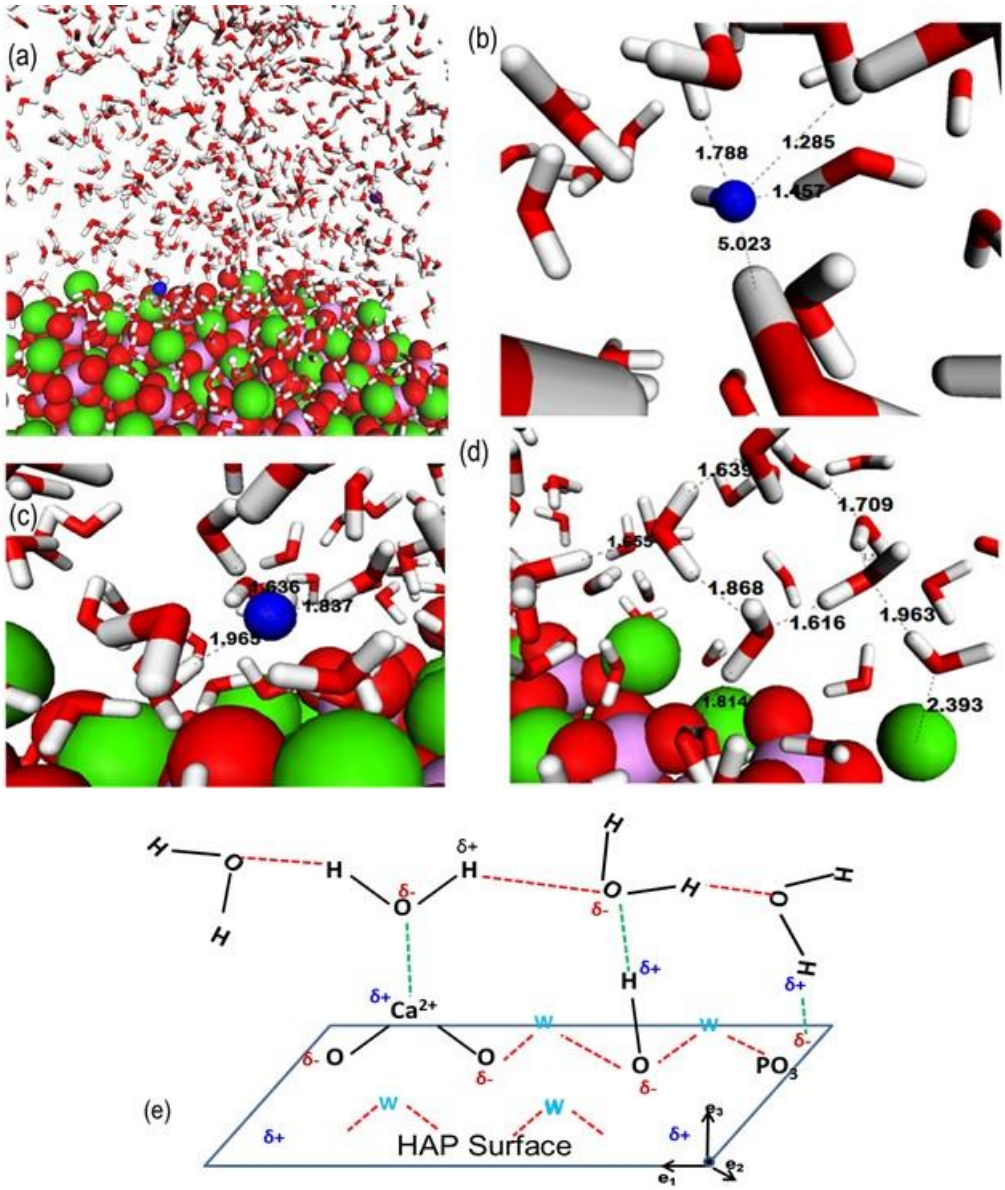

Fig. 4. Unusual hydroxyl ion diffusion in HAP-Water system (Ca-green, PO_4^{3-}-pink, O-red, H-white and hydroxyl O-blue): (a) Molecular arrangement of water molecules and OH^- ions in a 70 Å HAP pore; (b) and (c) Interactions of OH^- ion with water molecules near and far away from the HAP surface respectively; (d) H-bonded network between water molecules and Ca^{2+}-water interactions (Distances are in Å). (e) Schematic representation of HAP and water adsorption sites through H-bonding at interface.