J. Fluid Mech. (2008), vol. 601, pp. 229–252. © 2008 Cambridge University Press doi:10.1017/S0022112008000530 Printed in the United Kingdom

Flow across microvessel walls through the endothelial surface glycocalyx and the interendothelial cleft

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(Received 8 March 2007 and in revised form 9 January 2008)

A mathematical model is presented for steady fluid flow across microvessel walls through a serial pathway consisting of the endothelial surface glycocalyx and the intercellular cleft between adjacent endothelial cells, with junction strands and their discontinuous gaps. The three-dimensional flow through the pathway from the vessel lumen to the tissue space has been computed numerically based on a Brinkman equation with appropriate values of the Darcy permeability. The predicted values of the hydraulic conductivity L_p , defined as the ratio of the flow rate per unit surface area of the vessel wall to the pressure drop across it, are close to experimental measurements for rat mesentery microvessels. If the values of the Darcy permeability for the surface glycocalyx are determined based on the regular arrangements of fibres with 6 nm radius and 8 nm spacing proposed recently from the detailed structural measurements, then the present study suggests that the surface glycocalyx could be much less resistant to flow compared to previous estimates by the one-dimensional flow analyses, and the intercellular cleft could be a major determinant of the hydraulic conductivity of the microvessel wall.

1. Introduction

The luminal surface of vascular endothelial cells is covered by a layer of macromolecules referred to as the glycocalyx. Its role as a molecular filter and diffusive barrier has been pointed out to be crucial for microvessel walls to maintain low permeability to macromolecules. In our previous paper (Sugihara-Seki 2006), we developed a theoretical model for transport of solutes and fluid across the endothelial surface glycocalyx, and successfully described the size selective properties of the glycocalyx for solute transport, such as diffusive permeability and reflection coefficient. For the fluid transport, on the other hand, it was indicated that the hydraulic conductivity L_p , which is defined as the ratio of the flow rate per unit surface area of the vessel wall relative to the pressure drop across it, cannot be accounted for by the glycocalyx property alone. In this paper, we develop a three-dimensional model to describe the hydraulic conductivity L_p across the entire endothelial barrier including the endothelial surface glycocalyx and the interendothelial cleft with its tight junction strand. This model is based on the latest detailed ultrastructural studies of venular microvessels in rat mesentery (see figure 1) (Adamson *et al.* 2004).

In electron micrographs of microvessels in transverse section, the clefts are seen as narrow spaces, typically 14–21 nm wide, between the outer leaflets of adjoining endothelial cells. The route from the luminal entrance to the abluminal exit along the cleft is interrupted by one or more tight junctions. The tight junctions form lines

229



FIGURE 1. Sketch of an interendothelial cleft and surface glycocalyx of a microvessel wall.

of contact between the adjacent cells which can be traced in serial sections to run approximately parallel to the luminal and abluminal surfaces of the endothelium. They appear to act as barriers for water and solute to flow within the cleft. Where the tight junction continuity ends, the distance between cells is observed to open to equal the width of the wide part of the cleft. Water and solutes are expected to bypass the tight junction through these discontinuities or gaps. The spacing between membranes of facing cells is of remarkable uniformity except for tight junctions. Although there is some experimental evidence of the presence of regularly spaced cleft-spanning structures in rat myocardial capillaries (Schulze & Firth 1992), little information is currently available as to whether such structures fill the entire cleft.

Existing models of the filtration flow in the cleft and through the breaks in the tight junction strand have all been based on the two-dimensional Hele-Shaw flow theory first proposed in Tsay, Weinbaum & Pfeffer (1989). This approach was suggested by the nearly uniform gap height of the cleft. At the time, there was conflicting evidence as to the nature of the pores in the tight junction strand, whether they were long discontinuities or small slit-like breaks. The latter was suggested by the ultra thin sections of rat heart capillaries (Bundgaard 1984). The paper by Adamson & Michel (1993) in which the tight junctions of frog mesentery microvessels were serially reconstructed provided convincing evidence that the dominant pathway for water through the cleft was large infrequent, widely spaced breaks (see figure 13a of Tsay et al. 1989). Since Hele-Shaw flow satisfies a potential flow equation, this observation allowed Parker et al. in the Appendix to Adamson & Michel (1993) to apply conformal mapping techniques to develop an analytical solution for a tight junction strand of zero thickness that was arbitrarily positioned in the depth direction of the cleft. The convergence and divergence of the flow on each side of the tight junction strand could be treated by introducing a correction factor C that described the reduction in flow resistance relative to a one-dimensional flow through the orifice-like break owing to the spreading of streamlines.

In the one-dimensional flow of the plane Poiseuille flow between two parallel plates with separation distance 2h, the flow rate per unit length in the span-wise direction is given by $2h^3\Delta p/3\mu l_c$, where l_c is the distance from the vessel lumen to the interstitium, Δp is a pressure drop across them and μ is the fluid viscosity. Thus, if we denote the length of intercellular cleft per unit area of vessel wall as A, and the length of the discontinuities expressed as a fraction of the total length of the cleft as f, then the hydraulic conductivity for the one-dimensional flow and that for the two-dimensional flow can be described as (Adamson & Michel 1993)

$$L_{p}^{(1)} = Af \frac{2h^{3}}{3\mu l_{C}}, \quad L_{p}^{(2)} = CL_{p}^{(1)}, \tag{1}$$

where superscripts (1) and (2) denote the one-dimensional flow and the twodimensional Hele-Shaw flow, respectively. In the Appendix to Adamson & Michel (1993), the correction factor C was plotted as a function of the junction position relative to the cleft depth for various lengths of the discontinuities (see figure 10).

This same approach could also be used if there was a fibre matrix in the cleft, provided the pressure at the entrance and exit was uniform, since Darcy flow also satisfies a potential flow equation. A more sophisticated analysis of the Stokes flow around possible cross-bridging fibres in the cleft was developed in Tsay & Weinbaum (1991) who also showed that the flow through the fibres could be accurately modelled by a Brinkman equation (see equation (2)). This model was extended to treat the diffusion of solutes through a cross-bridging fibre array in Weinbaum, Tsay & Curry (1992).

Although electron-microscopic studies as early as Luft (1966) had indicated that the surface of vascular endothelium was covered by a glycocalyx, it was not realized until Adamson & Clough (1992) that this coating was of nearly uniform thickness and completely covering the cleft entrance. To treat this complication, Fu *et al.* (1994) proposed a junction-orifice-fibre entrance layer model to describe both the hydraulic and diffusive permeabilities of the entire endothelial layer. They converted the thickness of the surface glycocalyx to an approximate equivalent thickness of matrix inside the cleft by comparing the Darcy permeability of the unbounded fibre matrix with the effective values of the bounded fibre array. It was predicted that the matrix layer of ordered periodic structure of about 100 nm thickness could provide the hydraulic conductivity L_p compatible with experimental observations, and a thicker layer would offer too much hydraulic resistance for frog mesentery capillaries.

Subsequent papers by Weinbaum and coworkers were motivated by the recognition that the classical Starling hypothesis (1896) required a major revision to account for the measured Starling force balance properly (Michel 1997; Weinbaum 1998). These investigators proposed that the Starling forces, which had been widely believed to act globally between plasma and tissue, actually acted just across the endothelial surface glycocalyx. This being the case, the model in Fu et al. (1994) was modified in Hu & Weinbaum (1999) to couple the filtration flow to the convective and diffusive transport of albumin through the glycocalyx layer and the underlying cleft with its tight junction. The major feature of this new model was the treatment of the back diffusion of solute from the tissue and the theoretical prediction of the oncotic forces that were measured in the experiments in frog mesentery (Hu et al. 2000) and rat mesentery (Adamson et al. 2004). To accommodate the nonlinear coupling of the water and solute fluxes, these more recent papers attempted to simplify the junction-orifice-fibre matrix model in Fu et al. (1994) by treating the flow through the glycocalyx as a slowly varying one-dimensional flow while retaining the Hele-Shaw description of the flow in the cleft. This model was then further simplified in Zhang et al. (2006) into an equivalent one-dimensional model for the entire layer including the back diffusion from the tissue.

The objectives of the present study are to examine critically some of the important simplifications in the hydrodynamic assumptions used in these previous models. In particular, (i) we examine the slowly varying one-dimensional approximation for the flow through the glycocalyx which neglects the convergence of streamlines at the cleft

entrance, (ii) we examine the use of a Hele-Shaw approximation for the flow in the cleft which does not satisfy the no-slip boundary conditions on the tight junction strand and the edges of the orifice breaks, and (iii) we also present the first results for a glycocalyx with an inner sieving layer and a more diffuse outer layer as proposed in Pries, Secomb & Gaehtgens (2000). In addition, we calculate the fluid shear stress acting on the membranes bounding the cleft and forces acting on the tight junction strands, and present detailed solutions for the velocity field at the entrance of the cleft and in the vicinity of the orifice breaks.

We shall present our formulation and methods of analyses in §2, and the numerical results will be provided in §3 for the flow structure, the hydraulic conductivity, the fluid shear stresses on the membrane and the forces exerted on the tight junction strand. By comparing the present results with previous model studies and experimental studies, we shall discuss the contribution of the glycocalyx to L_p and the corrections necessary for the previous estimates in §4.

2. Formulation and methods

We consider the flow of an incompressible Newtonian fluid across a microvessel wall from the vessel lumen to the tissue space. The pathway of the fluid consists of the endothelial surface glycocalyx and clefts between neighbouring endothelial cells. Figure 1 shows a schematic view of ultrastructures of the interendothelial cleft and the surface glycocalyx (Squire *et al.* 2001; Weinbaum *et al.* 2003; Adamson *et al.* 2004). Adamson *et al.* (2004) showed from their detailed structural morphology measurements for rat mesentery venules that the clefts between adjacent endothelial cells have uniform width of 2h = 18 nm on average and there are tight junction strands with discontinuous leakages, or gaps, of mean width 2d = 315 nm and mean spacing 2D = 3590 nm. It was reported that, on average, the total cleft depth is $l_c = 411$ nm, and the tight junction strand is located at 15% of the cleft depth or $l_J = 67$ nm from the luminal cleft opening (table 1). They made simultaneous measurements of the hydraulic conductivity for rat mesentery venules that are on average $L_p = 1.0 - 1.3 \times 10^{-7}$ cm (cmH₂O)⁻¹ s⁻¹. Note that 1 cm (cmH₂O)⁻¹ s⁻¹ $\approx 10^{-4}$ m Pa⁻¹ s⁻¹.

Based on figure 1, we have adopted an idealized geometry depicted in figure 2 as a model for the fluid flow pathway across microvessel walls. Endothelial cells are assumed to be rectangular hexahedrons, and the two sidewalls of neighbouring cells facing each other compose the cleft with uniform width 2h and depth l_C from the luminal cleft opening to the abluminal cleft exit. The tight junction strand is represented by an impermeable barrier to flow with thickness δ , that lies parallel to the luminal front with depth l_J from the luminal cleft entrance, and it has discontinuous gaps with length 2d, periodically placed at a spacing of 2D along the tight junction strand. The surface glycocalyx is assumed to cover the entire surface of the endothelial cells including the entrance region to the cleft, and have a constant thickness l_G . We assume that there is a uniform space of the vessel lumen upstream of the glycocalyx, with thickness l_L , and there is a uniform tissue space downstream from the cleft exit, with thickness l_T .

The Cartesian coordinate system (x, y, z) is introduced such that the (x, y)-plane is the mid-plane of the cleft, the (y, z)-plane corresponds to the luminal surface of the endothelial cells, and the x-axis is along the line from the vessel lumen to the tissue space, passing the centre of the gap of the junction strand. Figure 2 shows a periodic unit of the model geometry, which repeats in the y- and z-directions. The period 2D in the y-direction represents the separation distance between neighbouring gaps

Gap length ¹	2d = 315 nm
Gap spacing ¹	2D = 3590 nm
Cleft spacing	2L = 10000 nm
Cleft width ¹	2h = 18 nm
Cleft length per area vessel wall ¹	$A = 0.10 \mathrm{\mu m^{-1}}$
Glycocalyx thickness ²	$l_G = 150 - 400 \text{ nm}$
Total cleft depth ¹	$l_{C} = 411 \text{ nm}$
Depth of strand ¹	$l_I = 67 \text{ nm}$
Strand thickness ³	$\delta = 15 \mathrm{nm}$
Vessel lumen thickness	$l_{\rm L} = 150-400 \rm nm$
Tissue space thickness	$l_{\rm T} = 1000 \rm nm$
Endothelial surface glycocalyx	
Fibre radius ⁴	6 nm
Fibre spacing ⁴	8 nm
Darcy permeability for the flow parallel to the core proteins	
$K_p^{G_{//}} = 6.10 \mathrm{nm}^2$	
Darcy permeability for the flow perpendicular to the core proteins	
$K_p^{G_\perp} = 3.16 \mathrm{nm}^2$	
Interendothelial cleft	
Fibre radius ⁵	1.25 nm
Fibre spacing ⁶	15 nm
Darcy permeability	$K_n^C = \infty$ or 32.84 nm ²
Tissue space	Υ .
Darcy permeability ^{7,8}	$K^{T} = 190 \text{ nm}^{2}$
Dury permeability	np 190 mm

¹Adamson *et al.* (2004), ²Weinbaum *et al.* (2003), ³Adamson & Michel (1993), ⁴Squire *et al.* (2001), ⁵Shapiro *et al.* (1995), ⁶Schulze & Firth (1992), ⁷Levick (1987), ⁸Intaglietta & de Plomb (1973).

TABLE 1. Parameter values.

of the tight junction strand, and 2L represents the distance between neighbouring clefts. Adamson *et al.* (2004) measured the perimeters and luminal surface areas of individual endothelial cells by using confocal microscopy techniques, and calculated the mean cleft length per unit surface area of the vessel wall A as $0.100 \,\mu\text{m}^{-1}$ for rat mesentery venules. Applying this value to the present model, we have $2L = 10 \,\mu\text{m}$ since $A = 2D/(2D \times 2L) = 0.100 \,\mu\text{m}^{-1}$. The parameter values are summarized in table 1.

We analyse the motion of water from the vessel lumen to the tissue space. Because of comparable sizes of mean distance between adjacent water molecules of about 0.3 nm and cleft width of 18 nm, the best analysis would be performed based on their molecular nature. One of the most important differences from a continuum approach would be the possible presence of liquid slippage along the interface of the liquid and solid phases (Priezjev & Troian 2006). Despite a long history of work on this topic as well as recent developments of molecular-dynamics simulations and experiments, there remains a significant debate concerning the validity of slip conditions as well as the degree of slip possible at liquid/solid interfaces. Little is known about the motion of water molecules near biological membranes. Thus, the current study is performed based on continuum mechanics under the conventional no-slip condition on the membrane surface. Future information about the molecular dynamics will help us to improve the present analysis.

We consider the flow of a Newtonian fluid with viscosity μ from the vessel lumen to the tissue space, when a certain pressure drop Δp is prescribed between them.



FIGURE 2. Model for a serial pathway of water flow from the vessel lumen to the tissue space through the endothelial surface glycocalyx and the interendothelial cleft. The geometry is repeated in the y- and z-directions.

The domain of the numerical computation contains four regions. The first region is the vessel lumen at $-(l_G + l_L) \leq x \leq -l_G$. The pressure at $x = -(l_G + l_L)$ is given as p = 0. The second region is the endothelial surface glycocalyx at $-l_G \leq x \leq 0$, the third region is the interendothelial cleft at $0 \leq x \leq l_C$, and the fourth region is the tissue space at $l_C \leq x \leq l_C + l_T$. The pressure at $x = l_C + l_T$ is prescribed as $p = -\Delta p$. From the flow rate J_v per unit cross-sectional area and the pressure drop Δp , we calculated the hydraulic conductivity $L_p = J_v /\Delta p$. Some typical *in vivo* permeability experiments are performed in the range of Δp from about $10 \text{ cmH}_2\text{O}$ to 50 or $60 \text{ cmH}_2\text{O}$ (Adamson *et al.* 2004; Truskey, Yuan & Katz 2004).

Since the Reynolds number is extremely small, the inertia of the fluid motion can be neglected. The effect of the presence of the fibre matrices in the endothelial surface glycocalyx, the interendothelial cleft and the tissue space was considered approximately by adding a Darcy force term proportional to the fluid velocity to the Stokes equation, called the Brinkman equation (Brinkman 1947):

$$-\nabla p + \mu \Delta \boldsymbol{u} - \frac{\mu}{K_p} \boldsymbol{u} = 0, \qquad (2)$$

where $\boldsymbol{u} = (u, v, w)$ is the fluid velocity, p is the pressure and K_p is the Darcy permeability. This equation has been widely used to represent the viscous flow through fibrous media, from the similarity to the flow through porous media (Damiano *et al.* 1996; Feng, Ganatos & Weinbaum 1998; Feng & Weinbaum 2000; Sugihara-Seki 2004, 2006; Han *et al.* 2006). We assume the viscosity of water $\mu = 0.69 \times 10^{-3}$ Pa s⁻¹ at 37 °C.

The value of K_p depends on the fibre geometry. For instance, if we assume the fibres to be circular cylinders with radius r_f , the Darcy permeability K_p for a flow

perpendicular to a two-dimensional hexagonal array of the circular cylinders can be expressed by using the solutions in Sangani & Acrivos (1982) as

$$\frac{K_p}{r_f^2} = \frac{\ln\left(c^{-1/2}\right) - 0.745 + c - c^2/4 + O(c^4)}{4c},\tag{3}$$

where c is the volume fraction of the cylinders. In terms of spacing Δ between neighbouring cylinder surfaces instead of c, Tsay & Weinbaum (1991) obtained a useful approximate expression for equation (3):

$$\frac{K_p}{r_f^2} = 0.0572 \left(\frac{\Delta}{r_f}\right)^{2.377}.$$
(4)

The glycocalyx has a very delicate fragile structure with high water content (Pries et al. 2000; van den Berg, Vink & Spaan 2003; van den Berg et al. 2006). It is so tenuous that knowledge of its ultrastructure and constitutive behaviour in vivo are very limited. As a result, its value of the Darcy permeability is currently unknown. In the present study, we have estimated the Darcy permeability for the surface glycocalyx K_n^{β} based on the detailed structural measurements of the glycocalyx (Squire *et al.* 2001). From the observation by the autocorrelation imaging techniques, they proposed a structural model where the surface glycocalyx is composed of bushlike clusters of core proteins projecting normally to the surface of the luminal wall (figure 1). Within each cluster, the scattering centres along the core proteins are 10– 12 nm in diameter and their interval is roughly 20 nm in the directions both parallel and perpendicular to the endothelial surface. If we simplify this model by assuming core proteins to be circular cylinders with radius $r_f = 6 \text{ nm}$ which align regularly perpendicular to the endothelial luminal surface in a hexagonal array with spacing $\Delta =$ 8 nm, then (3) gives $K_p^{G_\perp} = 3.16 \text{ nm}^2$ for the volume fraction $c = 2\pi r_f^2 / \sqrt{3}(2r_f + \Delta)^2 = 0.326$. Here the superscript \perp indicates the value for the flow perpendicular to the cylinder axis.

For the flow parallel to the cylinder axis, Sugihara-Seki (2006) solved the Stokes equation and estimated the Darcy permeability to be $K_p^{G_{1/2}} = 6.10 \text{ nm}^2$. Corresponding to (3), an approximate analytical representation of the Darcy permeability for parallel flow in the case of low volume fraction c can be deduced from equation (18) in Sparrow & Loeffler (1959) after some manipulation:

$$\frac{K_p}{r_f^2} = \frac{2c - \ln c - c^2/2 - 1.5}{4c}.$$
(5)

If we put c = 0.326, equation (5) gives $K_p^{G_{\parallel}} = 6.07 \text{ nm}^2$. This is close to the above estimate in spite of a fairly large value of c.

It may be interesting to compare these values of the Darcy permeability with the value obtained from the well-known Carman–Kozeny equation (Happel & Brenner 1973). In terms of the volume fraction of fibres c, the fibre radius r_f and the so-called Kozeny constant k, this may be written as (Curry & Michel 1980)

$$\frac{K_p}{r_f^2} = \frac{(1-c)^3}{4kc^2}.$$
(6)

Substituting c = 0.326, $r_f = 6$ nm and k = 5.6 for flow through random orientation of cylinders, equation (6) gives $K_p = 4.63$ nm², which lies between $K_p^{G_{\perp}} = 3.16$ nm² and $K_p^{G_{\parallel}} = 6.10$ nm².

Squire et al. (2001) pointed out that the thickness of the glycocalyx having the ultrastructure of core proteins is no more than 200 nm. On the other hand, the work of Duling and coworkers (Vink & Duling 1996; Henry & Duling 1999, 2000) and Damiano and coworkers (Smith et al. 2003; Damiano, Long & Smith 2004; Long et al. 2004) provide evidence for a 400–500 nm thick surface layer in capillaries and venules in vivo. Thus, it may be plausible to assume the possible presence of another layer extending further into the vessel lumen than the core proteins. Such a layer, hereinafter called the apical layer, may have constituents different from those of the core-protein layer, and may be composed of adsorbed plasma components and glycosaminoglycans (GAGs) (Pries et al. 2000). Since the permeability property of the apical layer is unknown, we assume, in the present study, constant values of the Darcy permeability for the whole endothelial surface layer including the coreprotein layer and the apical layer, for simplicity, and call the whole surface layer the endothelial surface glycocalyx. We examine the two cases of $l_G = 150$ nm and 400 nm as representative values of the glycocalyx thickness. The effect of different values of the Darcy permeability between the two layers on L_p will be discussed in §4.

If there are no cleft-spanning molecules in the intercellular cleft, the Darcy permeability for the cleft would be $K_p^C = \infty$. In this case, (2) reduces to the Stokes equation. If we assume that the cleft-spanning molecules are placed perpendicular to the cleft surface in a hexagonal array at 15 nm intervals and their diameter is taken as 2.5 nm (Schulze & Firth 1992; Shapiro *et al.* 1995; Boggon *et al.* 2002; Adamson *et al.* 2004), then we have $K_p^C = 32.84 \text{ nm}^2$ from (4). It is not certain whether the cleft-spanning molecules fill the entire cleft or not, but it is more likely that the link proteins, VE cadherins, may occur only in localized regions (Thi *et al.* 2004; Zhang *et al.* 2006). Thus, in the present study, the case of $K_p^C = \infty$ is mainly treated and the results of this case are reported in §3 unless otherwise noted. Some cases of $K_p^C = 32.84 \text{ nm}^2$ are also examined to compare with previous studies. For the Darcy permeability in the tissue space, we adopted $K_p^T = 190 \text{ nm}^2$ from measurements on mesentery (Intaglietta & de Plomb 1973; Levick 1987).

In a brief summary of the present analysis, we have solved the Brinkman equation (equation (2)) simultaneously in the whole domain, with the Darcy permeability appropriate to each region such as

$$K_{p} = \begin{cases} \infty & \text{for} - (l_{G} + l_{L}) < x < -l_{G} \text{ (vessel lumen)}, \\ K_{p}^{G_{/\!/}}, \ K_{p}^{G_{\perp}} & \text{for} - l_{G} < x < 0 \text{ (glycocalyx)}, \\ K_{p}^{C} & \text{for } 0 < x < l_{C} \text{ (cleft)}, \\ K_{p}^{T} & \text{for } l_{C} < x < l_{C} + l_{T} \text{ (tissue space)}, \end{cases}$$
(7)

where the values of $K_p^{G_{\parallel}}$, $K_p^{G_{\perp}}$, K_p^C and K_p^T are given in table 1. Boundary conditions are no-slip condition on the surfaces of endothelial cells and tight junction strands. Periodic boundary conditions are adopted in the *y*- and *z*-directions, and up- and down-stream boundary conditions are

$$\partial u/\partial x = 0, \quad v = w = 0 \quad \text{at} \quad x = -(l_G + l_L), \, l_C + l_T,$$
(8a)

$$p = 0$$
 at $x = -(l_G + l_L), p = -\Delta p$ at $x = l_C + l_T$. (8b)

Note that, since (2) is linear in u, the flow rate J_v is proportional to Δp and the hydraulic conductivity $L_p = J_v / \Delta p$ is independent of Δp in the present model. With regard to a choice of the vessel lumen length, l_L , we found negligible effects on L_p , which is due to negligible pressure drop across the vessel lumen (see figures 3 and 4).



FIGURE 3. Streamlines (solid curves) and pressure contours (dashed curves) in the (x, z)-plane (a) and in the (x, y)-plane (b), for $l_G = 150$ nm, $l_T = 150$ nm and $K_p^C = \infty$ with the other parameters in table 1. In (a), the streamlines are drawn in such a way that the flow rates on the (x, z)-plane across the mid-cross-section of the gap $(x = l_J + \delta/2)$ are the same between any two adjacent streamlines. In (b), the streamlines cross the line at $x = l_J + \delta/2$ with an equal interval along the gap of the junction strand.

In our numerical analysis, we have adopted a finite-element spectral method applied to the Brinkman equation and continuity equation. The fluid domain shown in figure 2 was divided into a number of finite elements with hexahedral shapes. Within each element, the velocity and pressure were interpolated by Chebyshev polynomials of Nth degree and (N - 1)th degree, respectively. Special attention was paid in making elements to the corner regions where singular behaviours are expected in the velocity and the pressure. To overcome this difficulty, we adopted the gradual *h*-refinement method, in which sizes of elements were progressively decreased toward the corners with size ratio = 0.15 (Babuska & Suri 1994; Karniadakis & Sherwin 2005). The finite-element scheme was formulated in terms of the primitive variables based on the variational principle $\delta J = 0$ (Sugihara-Seki 1996, 2004). Here, the variational functional was chosen as

$$J = \int_{\Omega} \left[\mu e^2 - p(\nabla \cdot u) + \frac{\mu}{K_p} \frac{u^2}{2} \right] dx \, dy \, dz - \int_{\partial \Omega} \tau_n \cdot u \, dS, \tag{9}$$

where $e = (\nabla u + (\nabla u)^t)/2$, Ω represents the fluid domain, and $\delta \Omega$ is the boundary where the fluid stress exerted on it is prescribed as τ_n . In the present computation, the x-components of τ_n were given on the up- and down-stream cross-sections at $x = -(l_G + l_L)$ and $l_C + l_T$, from (8).



FIGURE 4. Streamlines (solid curves) and pressure contours (dashed curves) in the (x, z)-plane (a) and in the (x, y)-plane (b), for $l_G = 0$, $l_T = 300$ nm and $K_p^C = \infty$ with the other parameters in table 1.

In order to ascertain the validity of the computation, we calculated the flow rate Q across several cross-sections along the pathway, and estimated its variation relative to the inlet value, $Q(x)/Q_0$, where $Q_0 = Q(-(l_G + l_L))$ represents the flow rate across the most upstream cross-section in the vessel lumen at $x = -(l_G + l_L)$. For various degrees N of Chebyshev polynomials, we calculated the relative flow rate $Q(x)/Q_0$, along the x-axis at $x = -l_G$ (glycocalyx surface), x = 0 (luminal cleft entrance), $x = l_J$ (entrance of the gap of the tight junction), $x = l_J + \delta$ (exit of the gap), $x = l_C$ (abluminal cleft exit) and $x = l_C + l_T$ (tissue space). For the cases of N = 2, deviations from unity are significant at the luminal cleft entrance and the abluminal exit, but they are progressively decreased as the polynomial degrees are increased. For the cases of N = 4 and 183 elements, the relative errors are within 0.5% for all cross-sections, and we have adopted N = 4 in the present study. In a representative computation, the CPU time for the computation of one configuration with double precision was approximately 6 hours on the FACOM HPC.

3. Results

A representative result of our numerical computations is shown in figure 3, where streamlines and pressure contours are plotted in the (x, z)-plane and (x, y)-plane, for $l_G = 150$ nm and $l_T = 150$ nm. In figure 3(b) the streamlines in the glycocalyx are almost parallel to the x-axis, whereas in figure 3(a) a converging flow from the vessel lumen into the cleft entrance is clearly shown within the glycocalyx. The corresponding



FIGURE 5. Oblique view of the pressure distribution in the (x, y)-plane, for $l_G = 150$ nm, $l_T = 150$ nm and $K_p^C = \infty$ with the other parameters in table 1.

plots in the absence of the glycocalyx are shown in figure 4, for reference. We note from figures 3 and 4 that the pressure gradients are present within the glycocalyx both in the y- and z-directions as well as in the x-direction, which is in marked contrast to the vessel lumen and the tissue space. Figure 4(a) shows that, without the glycocalyx, the streamlines in the vessel lumen extend almost radially from the luminal cleft entrance, similar to those in the tissue space. In comparing the outermost streamlines in figures 3(b) and 4(b), we notice that the flow from the vessel lumen enters the cleft entrance spreading more widely from the x-axis in the presence of the glycocalyx than without the glycocalyx, which will be confirmed below from figure 6.

The streamlines in the cleft shown in figures 3(b) and 4(b) demonstrate how the fluid flow passes through the gap of the junction strand in the mid-plane of the cleft. They are similar downstream of the junction strand, while they show some difference upstream of the junction strand, owing to the presence or absence of the glycocalyx. A close look at the cleft region suggests that a nearly potential-type flow may be realized, since the streamlines and pressure contours seem almost perpendicular to each other (see equation (12)).

Figure 5 shows an oblique view of the pressure distribution in the (x, y)-plane, corresponding to figure 3(b). It is clearly illustrated that the pressure varies mildly in the endothelial glycocalyx except just near the cleft entrance, and most pressure drop occurs in the cleft. The pressure decreases monotonically along the x-axis, while, apart from the gap (y > d), the pressure is almost constant in either region upstream or downstream of the tight junction strand. Across the junction strand, there is an abrupt change in pressure, or pressure jump. The considerable pressure jump across the junction strand was previously reported by Hu & Weinbaum (1999).

Along the cleft entrance at x = 0, the pressure has a minimum at y = 0, and it gradually increases toward an asymptote as y increases from 0. This behaviour of the pressure variation along the y-axis is shown in figure 6(b), and the pressure variation along the z-axis is shown in figure 6(a), for various values of the glycocalyx



FIGURE 6. The pressure profiles at the cleft entrance along the z-axis (a) and the y-axis (b), at $K_p^C = \infty$ for various glycocalyx thicknesses with the other parameters in table 1. The solid curves represent the case of $l_G = 0$, the dotted curves $l_G = 50$ nm, the dash-dotted curves $l_G = 100$ nm, the dashed curves $l_G = 150$ nm, and the dash-double dotted curves $l_G = 400$ nm. The velocity vectors at the cleft entrance along the z-axis (c) and the y-axis (d), at $K_p^C = \infty$ in the absence of the glycocalyx (solid arrows) and in the presence of the glycocalyx with $l_G = 150$ nm (dashed arrows), with the other parameters in table 1. In (c) and (d), the velocity is normalized by the mean velocity in the cleft, $u_0 = J_v L/h$.

thickness. Our computations showed that the depression of the pressure curve near the origin (the centre of the cleft entrance) becomes shallower and narrower as the glycocalyx becomes thinner. Figure 6(b) reveals that, in the limit of $l_G = 0$, i.e. with no glycocalyx, the deviation of the pressure from the asymptotic value is small and it is negligible except in a narrow region corresponding to the opening length of the gap of the junction strand, i.e. $y \leq d$. In figure 6(a), a sharp change in pressure is seen at z = h (= 9 nm), corresponding to the corner of the cleft entrance. In particular, the abrupt increase in pressure there was previously observed for Stokes flow through a periodic infinite-slit array in an unbounded plane wall (Hasimoto 1958).

The velocity vectors (u, w) and (u, v) at the cleft entrance normalized by the mean velocity in the cleft, $u_0 = J_v L/h$, are plotted along the z-axis in figures 6(c) and along the y-axis in figure 6(d). The solid arrows represent the velocity vectors in the absence of the glycocalyx, and the dashed arrows in the presence of the glycocalyx with $l_G = 150$ nm. Owing to the normalization of the velocity, larger velocity near the



FIGURE 7. Effect of the glycocalyx thickness on the hydraulic conductivity L_p , L_p^C and L_p^G , with and without cleft-spanning molecules. The solid curves represent L_p , dashed curves L_p^C and dash-dotted curves L_p^G .

centreline (x-axis) with no glycocalyx than that with the glycocalyx indicates that, without the glycocalyx, the fluid flow into the cleft entrance is more concentrated near the x-axis, compared to the case with the glycocalyx, as already noted from figures 3(b) and 4(b). This variation of the velocity profile at the cleft entrance affects the flow structure in the cleft, which results in variations of the hydraulic conductivity with the glycocalyx thickness, as shown below.

With the use of the velocity data obtained and the pressure drop prescribed, the hydraulic conductivity $L_p = J_v/\Delta p$ was calculated, for various parameter values. As seen in figure 5, variations in pressure are very small within the vessel lumen $(-(l_G + l_L) \le x \le -l_G)$ and within the tissue space $(l_C \le x \le l_C + l_T)$, so that Δp is nearly equal to the pressure difference across the surface glycocalyx and the cleft, i.e. $\Delta p \approx \bar{p}(-l_G) - \bar{p}(l_C)$. Here, $\bar{p}(x_0)$ represents the mean pressure averaged over the cross-section at $x = x_0$. Figure 7 shows our predicted values of L_p as a function of the glycocalyx thickness l_G , with and without cleft-spanning molecules. The other parameters are shown in table 1. For $K_p^C = \infty$, the present computations lead to $L_p = 1.75 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$ for $l_G = 150 \text{ nm}$, and $L_p = 1.69 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$ for $l_G = 400 \text{ nm}$. In the presence of the cleft-spanning molecules ($K_p^C = 32.84 \text{ nm}^2$), we had $L_p = 1.01 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$ for $l_G = 400 \text{ nm}$. These values are within the range of the experimental measurements and close to the mean value $1.0 - 1.3 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$ for rat mesentery venules (Adamson *et al.* 2004).

The hydraulic conductivity for the glycocalyx alone is calculated by the ratio of the flow rate and the pressure difference across the glycocalyx, i.e. between its luminal surface and the entrance to the cleft just behind it, such as $L_p^G = J_v/(\bar{p}(-l_G) - \bar{p}(0))$. In this case, $\bar{p}(0)$ represents the mean pressure averaged over the luminal cleft entrance, i.e. $-D \leq y \leq D$ and $-h \leq z \leq h$ at x = 0. Similarly, the hydraulic conductivity for the cleft is given by $L_p^C = J_v/(\bar{p}(0) - \bar{p}(l_C))$. Since we consider a serial pathway of the



FIGURE 8. The distributions of shear stresses exerted by the fluid flow on the surface of the endothelial cell in the cleft at $z = \pm h$, for $l_G = 150$ nm and $K_p^C = \infty$ with the other parameters in table 1. The magnitudes of the shear stresses τ are normalized by $\tau_0 = 3\mu u_0/h$, where u_0 represents the mean velocity in the cleft $u_0 = J_v L/h$.

glycocalyx and the cleft for the fluid flow, we have the relationship:

$$\frac{1}{L_p} = \frac{1}{L_p^G} + \frac{1}{L_p^C},\tag{10}$$

where $(L_p)^{-1}$, $(L_p^G)^{-1}$ and $(L_p^C)^{-1}$ represent the resistance to flow in the vessel wall, the glycocalyx and the cleft, respectively. In figure 7, the variations of L_p^C and L_p^G with the glycocalyx thickness l_G are also plotted. Since the values of L_p^G for the glycocalyx are two orders of magnitude larger than the corresponding values of L_p^C , it is shown that the values of L_p are mainly determined by L_p^C . Our computation predicts that the contributions of the glycocalyx to the total flow resistance are only 3.4% and 4.1% for $l_G = 150 \text{ nm}$ and 400 nm, respectively, if the cleft-spanning molecules are absent ($K_p^C = \infty$). The corresponding values are even smaller if the cleft-spanning molecules are present ($K_p^C = 32.84 \text{ nm}^2$). Comparing the values of the glycocalyx may increase L_p by about 30% for $K_p^C = \infty$, and about 15% for $K_p^C = 32.84 \text{ nm}^2$. This increase in L_p following the removal of the glycocalyx is mostly due to the variation of the flow structure in the cleft, rather than the loss of the flow resistance in the glycocalyx. Figure 7 shows that the values of L_p depend only weakly on the glycocalyx to the flow resistance.

The fluid stresses exerted on the endothelial surface were calculated by using the velocity data. Figure 8 shows a representative example of the shear stress distribution on the surface of the intercellular cleft (at $z = \pm h$) for $l_G = 150$ nm. Here, the magnitudes of the wall shear stress $\tau = \mu \sqrt{(\partial u/\partial z)^2 + (\partial v/\partial z)^2}|_{z=\pm h}$ are normalized by the wall shear stress exerted by the plane Poiseuille flow between two parallel plates with separation distance 2h, i.e. $\tau_0 = 3\mu u_0/h$. For a representative flow rate $J_v = 10^{-8} \text{ m s}^{-1}$, we have $u_0 = 5.6 \times 10^{-6} \text{ m s}^{-1}$ and $\tau_0 = 1.28$ Pa, for h = 9 nm.

The luminal surface of the endothelial cell is continuously exposed to the shear stress of blood flow which is of the order of 1-2 Pa for postcapillary venules (Lipowsky 1995), that may be actually transmitted via the glycocalyx to the cytoskeleton of the endothelial cell (Smith et al. 2003; Long et al. 2004). Comparing with this value, we see from figure 8 that the wall shear stresses exerted on the cleft surface of the endothelial cell are extremely high. The shear stresses are concentrated in the gap region, especially near its ends $(l_J \leq x \leq l_J + \delta \text{ and } |y| \sim d)$. This is caused by the velocity profile in the gap region, having a minimum at the gap centre, and a maximum near the gap edge with a sharp decline to 0 at the edge to satisfy the no-slip condition. This characteristic velocity profile was previously reported by Zeng & Weinbaum (1994), where they analysed a Stokes flow through a parallel-walled channel obstructed by a thin planar barrier with a periodically spaced rectangular orifice. It was reported that for moderate and large ratios of channel height to orifice width (= h/d in the present study), the velocity profile in the orifice has the maximum at its centre, just like the Poiseuille flow, whereas a decrease in the ratio shifts the peak position toward the edge of the orifice. Apparently, the present geometry corresponds to the latter, since $h/d = 0.0571 \ll 1$ (see table 1).

It is increasingly recognized that the endothelial glycocalyx serves a critical role in the transmission of the fluid shear stress to the actin cytoskeleton and in the initiation of intracellular signalling (Thi *et al.* 2004; Weinbaum, Tarbell & Damiano 2007). Although the role of the fluid shear stresses in the cleft is not clear, the concentrated shear stresses shown in figure 8 suggest that they may have some effect on the tight junction itself, such as modulating the opening of the endothelial cell, the present study shows that the fluid filtration between the vessel lumen and the tissue space may exert the much smaller shear stresses on the luminal side $(x = l_C)$ than those on the cleft surface $(z = \pm h)$.

It may be interesting to estimate how much of the pressure force applied to the cleft, $\Delta p(2h)(2D)$, is taken up by shear stresses on the cleft surface. The integrations of the x-component of the stresses over the cleft surface and the junction strand surface show that most pressure force (approximately 90%) acts on the tight junction strand, and the remainder of the force is taken up by the shear stress exerted on the cleft surface. This may be anticipated from figure 5, where the pressure on the upstream-side of the tight junction strand is nearly equal to the most upstream pressure (= 0) and the pressure on its downstream-side is close to the most downstream pressure (= $-\Delta p$), resulting in the force exerted on the tight junction strand being $\Delta p(2h)(2D - 2d)$. Accordingly, the fraction of the pressure force taken up by the pressure difference across the tight junction strand is roughly estimated to be $(2D - 2d)/2D \sim 0.9$, sinced/D = 0.0877 (see Table 1). If we substitute the pressure difference $\Delta p = 10 \text{ cmH}_2\text{O}$ and the cleft width 2h = 18 nm, then the corresponding force on the tight junction strand per unit length along the strand is approximately $\Delta p(2h) = 1.8 \times 10^{-5} \text{ N m}^{-1}$.

4. Discussion

4.1. Comparison to previous model studies

As noted in §1, Fu *et al.* (1994) combined the endothelial surface glycocalyx and the cleft-spanning molecules in their model, and treated the entire matrix layer as if it existed in the entrance region of the wide part of the cleft. In the entrance matrix layer, they assumed a regular array of fine fibres with radius $r_f = 0.6$ nm

and spacing $\Delta = 7$ nm, corresponding to GAG side-chains. The Darcy permeability is estimated to be $K_p = 7.08 \text{ nm}^2$ from (4). It was shown that the matrix layer of ordered periodic structure with about 100 nm thickness could be compatible with experimental observations for frog mesentery capillaries, $L_p = 2.0 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$. With the glycocalyx covering the entire endothelial surface, Weinbaum and colleagues used the quasi-one-dimensional flow approximation within the glycocalyx and obtained the measured L_p when the glycocalyx thickness is 150 nm and $r_f = 0.6$ nm, $\Delta = 7$ nm (Hu & Weinbaum 1999; Hu *et al.* 2000; Weinbaum *et al.* 2003). Using $r_f = 6$ nm, $\Delta = 8$ nm for core proteins and the same geometry with the current study for the rat mesentery microvessels, Adamson *et al.* (2004) predicted that L_p is equal to 1.24×10^{-7} cm (cmH₂O)⁻¹ s⁻¹ for $l_G = 150$ nm in the presence of the cleftspanning molecules, and about twice of this value in the absence of the cleft-spanning molecules. Quite recently, Zhang *et al.* (2006) have indicated that the quasi-onedimensional flow approximation in the glycocalyx with the use of $K_p^G = 9.24$ nm² provides $L_p = 1.3 \times 10^{-7}$ cm (cmH₂O)⁻¹ s⁻¹ for $l_G = 150$ nm for the same structural parameters as the present study, free of any microstructure in the cleft.

The difference of the present study from these previous estimates results mainly from the three-dimensional flow structures in the glycocalyx (see figure 3), in spite of using comparable values of the Darcy permeability for the glycocalyx. The one-dimensional flow approximation is suitable in the y-direction, whereas it is inappropriate in the zdirection, as shown in figure 3(a). The converging flow into the luminal cleft entrance in the z-direction may markedly increase the flow rate for a given pressure difference across the glycocalyx. Under the quasi-one-dimensional flow approximation, Zhang et al. (2006) showed that along the x-axis, about half of the pressure drop occurs across the glycocalyx and half occurs in the cleft, for $l_G = 150 \text{ nm}$ and $K_p^G = 9.24 \text{ nm}^2$. It was also shown that the pressure drop across the glycocalyx averaged over the entire cleft length is 10% of the total pressure drop across the endothelial cell. In comparison, the present study predicts for the same parameter values except $K_p^{G_{\parallel}} = 6.10 \text{ nm}^2$ and $K_p^{G_{\perp}} = 3.16 \text{ nm}^2$ that about 30% of the pressure drop occurs across the glycocalyx along the x-axis (see dashed curves in figure 6), and the pressure drop across the glycocalyx averaged over the entire cleft length is only 3 % of the total pressure drop. The present study suggests much smaller contribution of the surface glycocalyx to the hydraulic conductivity than the previous estimates, primarily owing to substantial spreading of the flow within the glycocalyx.

4.2. Effects of the Darcy permeability of the glycocalyx on the hydraulic conductivity

If one-dimensional flow is assumed in the glycocalyx flowing directly into the cleft entrance with no spreading, the Darcy law provides the pressure drop across the glycocalyx thickness as $\Delta p^G = \mu U l_G / K_p^G$, where U is the velocity of the onedimensional flow. If we further assume that the flow is uniform, i.e. U is constant along the length of the cleft entrance, then the velocity U is related to the fluid flux per unit area of the endothelial luminal surface J_v as $U = J_v / (2hA)$. Thus, L_p^G for the uniform one-dimensional flow is represented by $L_p^G = J_v / \Delta p^G = K_p^G 2hA / \mu l_G$. Using this value, we here introduce a correction factor C^G , corresponding to (1) for the cleft, which represents the hydraulic conductivity for the glycocalyx relative to the value obtained by the one-dimensional flow approximation:

$$L_p^{G(1)} = A K_p^G \frac{2h}{\mu l_G}, \quad L_p^{G(3)} = C^G L_p^{G(1)}.$$
 (11)



FIGURE 9. (a) Correction factor C^G in (11) as a function of the isotropic Darcy permeability of the glycocalyx K_p^G , at $l_G = 150$ nm (solid curve) and 400 nm (dashed curve) for $K_p^C = \infty$ with the other parameters in table 1. (b) Hydraulic conductivity L_p as a function of the isotropic Darcy permeability of the glycocalyx K_p^G , at $l_G = 150$ nm (solid curve) and 400 nm (dashed curve) for $K_p^C = \infty$ with the other parameters in table 1. In (a) and (b), the filled circles and open circles represent the corresponding values for $K_p^{G_{\parallel}} = 6.10$ nm² and $K_p^{G_{\perp}} = 3.16$ nm², when isotropic $K_p^G = 4.9$ nm² and 4.8 nm² are substituted into (11), respectively.

For $l_G = 150 \text{ nm}$ or 400 nm, we have $L_p^{G(1)} = 5.5 \text{ or } 2.1 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$, respectively, when $K_p^G = 3.16 \text{ nm}^2$ and $A = 10^{-1} \mu \text{m}^{-1}$. For $K_p^G = 6.10 \text{ nm}^2$, the corresponding values are $L_p^{G(1)} = 10.6 \text{ or } 4.0 \times 10^{-7} \text{ cm} (\text{cmH}_2\text{O})^{-1} \text{ s}^{-1}$. Assuming isotropic $K_p^G (= K_p^{G_H} = K_p^{G_\perp})$, we have used the present model to compute the hydraulic conductivity for the glycocalyx $L_p^{G(3)}$ as well as that for the microvessel wall L_p , and the obtained values of C^G and L_p are plotted as functions of K_p^G , in figures 9(*a*) and 9(*b*), respectively.

Figure 9(*a*) shows that $C^G \approx 6-7$ for $l_G = 150$ nm in a rather wide range of K_p^G from 0.1 nm² to almost 10 nm², and $C^G \approx 13-14$ in the same range of K_p^G for $l_G = 400$ nm. For an anisotropic case such as $K_p^{G_{//}} = 6.10$ nm² and $K_p^{G_{\perp}} = 3.16$ nm², the correction factors C^G for $l_G = 150$ nm and 400 nm are found to lie on the corresponding solid and dashed curves, respectively, if we adopt an isotropic value of $K_p^G = 4.9$ and 4.8 nm² in the evaluation of $L_p^{G(1)}$ by (11).

Figure 9(b) shows our predicted values of L_p for the vessel wall with the variation of isotropic K_p^G , at $l_G = 150$ nm and 400 nm. We note that the solid and dashed curves are comparable, indicating that the values of L_p are almost independent of the glycocalyx thickness, as already seen in figure 7. When the value of K_p^G is increased from 0.1 nm² to 100 nm² by three orders of magnitude, figure 9(b) indicates that the subsequent increase in L_p is relatively small, ranging from almost 0.4×10^{-7} cm (cmH₂O)⁻¹ s⁻¹ to about 2×10^{-7} cm (cmH₂O)⁻¹ s⁻¹.

No direct measurements have been made of the Darcy permeability for the endothelial surface glycocalyx. The values in table 1, $K_p^{G_{\parallel}} = 6.10 \text{ nm}^2$ and $K_p^{G_{\perp}} = 3.16 \text{ nm}^2$, were determined based on the detailed structural measurements which proposed regular arrangements of core proteins with $r_f = 6 \text{ nm}$ and $\Delta = 8 \text{ nm}$ (Squire *et al.* 2001; Weinbaum et al. 2003). For the core protein geometry adopted in the present study, Sugihara-Seki (2006) made a fluid-mechanical analysis on the motion of a solute between regularly arranged core proteins and estimated the reflection coefficient. The predicted values of the reflection coefficient for various sized solutes are close to experimental measurements, accounting satisfactorily for the observed molecular filtering. For example, the reflection coefficient to solutes corresponding to serum albumin with Stokes radius = 3.6 nm is predicted to be as high as 0.8. This estimate explains the experimental measurements much better than previous analyses. Zhang et al. (2006) also reached a similar conclusion using the same geometry of the core proteins. Experimental studies have shown that, despite large variations of L_p depending on types of microvessels, various microvessels with fenestrated or continuous endothelium exhibit similar values of the reflection coefficient. This similarity in size selectivity of different types of microvessel walls can be explained well by an idea of the fibre matrix theory that the glycocalyx forms the primary molecular sieve for plasma proteins (Curry & Michel 1980). Thus, the accordance of the reflection coefficient obtained from the present model with experimental observations may lend support to the present model structures adopted for the glycocalyx.

There may be several factors affecting the value of K_p^G , which was estimated based on the regular arrangement of core proteins. Although we have assumed a rigid structure of the core proteins, resulting in constant values of K_p^G , the flexible property of the glycocalyx as well as the adsorption of plasma proteins may induce a local variation in solid-volume fraction in the glycocalyx, which may alter its permeability property. In addition, surface charges on the molecular filaments of the glycocalyx (Vink & Duling 2000; Damiano & Stace 2002) and a possible presence of interconnecting molecules between core proteins would also affect K_p^G .

Among these factors, we here briefly consider the effect of the possible presence of the apical layer at the luminal surface of the core-protein layer on the hydraulic conductivity. As a preliminary study to examine this effect, we modify the present model to include the apical layer, in such a way that the space of the vessel lumen $(-(l_G + l_L) < x < -l_G)$ is replaced by the apical layer with a Darcy permeability K_p^A , allowing its variation independent of K_p^G . For the apical layer thickness $l_L = 300$ nm and $l_G = 150$ nm, i.e. total thickness of the endothelial surface layer being 450 nm, our computation showed that a decrease in K_p^A from 10 nm² to 0.1 nm² reduces L_p from 1.71×10^{-7} cm (cmH₂O)⁻¹ s⁻¹ to 1.28×10^{-7} cm (cmH₂O)⁻¹ s⁻¹, when $K_p^{G_{\parallel}} = 6.10$ nm² and $K_p^{G_{\perp}} = 3.16$ nm². These values are not much different from our obtained value of $L_p = 1.75 \times 10^{-7}$ cm (cmH₂O)⁻¹ s⁻¹ in the presence of the core-protein layer alone without the apical layer. Thus, it is suggested that the effect of the apical layer on the hydraulic conductivity could be minor when the Darcy permeability of the apical layer is comparable or larger than that of the core-protein layer. Even when $K_p^A = 1$ nm², the contribution of the endothelial surface layer with thickness 450 nm to the whole resistance is predicted to be about 6 %.

4.3. Effects of the glycocalyx removal on the hydraulic conductivity

Adamson (1990) demonstrated that enzymatic removal of the surface glycocalyx, using pronase, increased the hydraulic conductivity of frog mesentery capillaries from 2.0×10^{-7} cm (cmH₂O)⁻¹ s⁻¹ to 4.9×10^{-7} cm (cmH₂O)⁻¹ s⁻¹ by 2.5-fold. This is the only experiment which tried to isolate the contribution of the surface glycocalyx from the whole vessel wall. It is not clear to what extent pronase perfusion degraded the glycocalyx, or affected structures of the cleft and the tight junction strand. However, if we postulate here that the glycocalyx was completely removed with no effect on the

cleft and tight junction structures, then this *in vivo* experiment implies that there is a 2.5 times difference between the values of L_p with and without the glycocalyx. In the present analysis, in contrast, a comparison of the L_p values at $l_G = 0$ and $l_G > 150$ nm in figure 7 suggests that the removal of the glycocalyx would enhance L_p by about 30% at $K_p^C = \infty$. The reason of this discrepancy is not apparent. One cause may be the values of the Darcy permeability for the glycocalyx adopted.

Here, we examine the possibility of adopting a value of K_p^G which would be pertinent to the *in vivo* experiment, focusing on the y-intercept of the L_p curve in figure 7, i.e. $L_p = 2.28 \times 10^{-7}$ cm (cmH₂O)⁻¹ s⁻¹ at $l_G = 0$. To achieve a 2.5 times smaller value of this, i.e. $L_p = 0.9 \times 10^{-7}$ cm (cmH₂O)⁻¹ s⁻¹ in the presence of the glycocalyx, we know from figure 9(b) that $K_p^G \approx 0.6 \text{ nm}^2$. In other words, if we adopted $K_p^G = 0.6 \text{ nm}^2$ instead of $K_p^{G_{//}} = 6.10 \text{ nm}^2$ and $K_p^{G_{\perp}} = 3.16 \text{ nm}^2$, our analysis suggests that the removal of the glycocalyx would increase L_p by 2.5 times. However, this value of K_p^G is far too small to account for experimental measurements of the reflection coefficient to solutes. Actually, for $K_p^G = 0.6 \text{ nm}^2$, equation (3) provides the spacing between adjacent fibre surfaces as $\Delta = 3.9 \text{ nm}$ and 2.7 nm for the fibre radius $r_f = 6 \text{ nm}$ and 0.6 nm, respectively. Similarly, (5) yields $\Delta = 3.1 \text{ nm}$ and 2.0 nm for $r_f = 6 \text{ nm}$ and 0.6 nm, respectively. These values are even smaller than a half of $\Delta = 8 \text{ nm}$ observed by Squire *et al.* (2001) and adopted in the present study. Apparently, they are too small for serum albumin (radius = 3.6 nm) to pass through the spacing. The resulting values of the reflection coefficient would be close to unity for the solute with radius larger than at least 2 nm, which seems inconsistent with measurements of the reflection coefficient (Michel & Curry 1999).

Unpublished studies (J. Tarbell, personal communication), in which heparinase III instead of pronase has been used to remove the surface glycocalyx in cultured bovine aortic endothelial cell (BAEC) monolayers show only a 38% increase in the hydraulic conductivity and a 260% increase for pronase digestion similar to the *in vivo* study by Adamson (1990). Heparinase is known to degrade selectively heparin sulfate of the glycocalyx (Pahakis *et al.* 2007). An application of pronase with higher concentration (0.125 mg ml^{-1}) greatly enhanced the hydraulic conductivity of BAEC monolayers. These results suggest some effects of this non-specific enzyme on the tight junction structure, although there is a possibility that the cell-surface chemistry in cultured cells *in vitro* may be different from the glycocalyx *in vivo*. Future detailed experimental studies using various enzymes are expected to clarify the contribution of the surface glycocalyx to the hydraulic conductivity of microvessel walls *in vivo*.

4.4. The correction factory for the hydraulic conductivity of the clef

For the flow in the cleft, all previous model studies starting with Tsay *et al.* (1989) including Adamson *et al.* (2004) adopted a two-dimensional approximation, where the flow is equivalent to the classical Hele-Shaw flow of a Newtonian fluid in the absence of the cleft-spanning molecules. In the two-dimensional flow analyses, the velocity (u, v) in the cleft is expressed as $u(x, y, z) = u^*(x, y)(1 - z^2/h^2)$ and $v(x, y, z) = v^*(x, y)(1 - z^2/h^2)$, which satisfy the no-slip condition at $z = \pm h$. The velocity in the cleft mid-plane, (u^*, v^*) , is linearly related to the local gradient in the averaged pressure $p^*(x, y)$ as

where K is a constant such that

$$K = \begin{cases} \frac{h^2/3\mu}{\mu} & \text{no cleft-spanning molecules,} \\ \frac{K_p}{\mu} \left\{ 1 - \frac{\sqrt{K_p}}{h} \tanh\left(\frac{h}{\sqrt{K_p}}\right) \right\} & \text{Brinkman flow,} \end{cases}$$
(13*a*, *b*)

(Phillips, Parker & Wang 1994). A combination of (12) with the continuity equation leads to the two-dimensional Laplace equation for the pressure:

$$\nabla^2 p^* = 0. \tag{14}$$

Phillips *et al.* (1994) solved (14) analytically in the domain of $0 \le x \le l_c$ subject to the boundary conditions of the uniform constant pressures at the cleft entrance and exit, together with the no-penetrating condition on the surface of the tight junction:

$$p^* = 1$$
 on $x = 0$, $p^* = 0$ on $x = l_C$, $\partial p^* / \partial x = 0$ on $x = (l_J + \delta/2)_{\pm}$, $|y| \ge d$. (15)

In this analysis, the thickness of the tight junction is neglected and $()_{\pm}$ represents the luminal and abluminal sides of the tight junction strand.

The solutions of this analysis were summarized in terms of the correction factor C, which represents the flow rate of the two-dimensional flow relative to a onedimensional flow through a rectangular cross-section of the gap of the tight junction, for a given pressure drop (Adamson & Michel 1993). By substituting f = d/D in (1), we have for the flow of a Newtonian fluid in the absence of the cleft-spanning molecules,

$$L_p^{C(1)} = \frac{2Ah^3d}{3\mu l_C D}, \quad L_p^{C(2)} = CL_p^{C(1)}.$$
 (16)

In the Appendix to Adamson & Michel (1993), Parker *et al.* plotted *C* as a function of the cleft geometry. Correspondingly, we have computed $C^* = L_p^C/L_p^{C(1)}$, where L_p^C represents the hydraulic conductivity for the three-dimensional Newtonian flow in the present study, with $K_p^C = \infty$. In figure 10, we plotted *C* and *C** as a function of the junction position from the luminal cleft entrance relative to the cleft depth, $\nu = (l_J + \delta/2)/l_C$, for various gap lengths relative to the gap separation, d/D. The cleft geometry in table 1 corresponds to $\nu = 0.181$ and d/D = 0.0877. The *C** curves in figure 10 represent the cases of $K_p^{G_{\parallel}} = 6.10 \text{ nm}^2$, $K_p^{G_{\perp}} = 3.16 \text{ nm}^2$, and $K_p^T = 190 \text{ nm}^2$. This asymmetry of the up- and down-stream values of the Darcy permeability reflects in the asymmetry of the *C** curves with respect to the centreline $\nu = 0.5$, while the solid curves of *C* are symmetric owing to the symmetric boundary condition (15).

Similarly, the correction factor, $C^{**} = L_p^C / L_p^{C(1)}$, can be defined for the Brinkman flow with the use of the following $L_p^{C(1)}$:

$$L_p^{C(1)} = \frac{2AhK_p \left\{ 1 - \frac{\sqrt{K_p}}{h} \tanh\left(\frac{h}{\sqrt{K_p}}\right) \right\}}{\mu l_C} \frac{d}{D}.$$
 (17)

This expression is easily obtained from (13). In figure 10, C^{**} for the Brinkman flow with $K_p^C = 32.84 \text{ nm}^2$ is also plotted by dash-dotted curves, for $K_p^{G_{\parallel}} = 6.10 \text{ nm}^2$, $K_p^{G_{\perp}} = 3.16 \text{ nm}^2$ and $K_p^T = 190 \text{ nm}^2$. Figure 10 clearly demonstrates that the L_p^C values for the three-dimensional flow are distinctly different from those for one-dimensional or two-dimensional flows, especially for small values of d/D, although the flow in the cleft shown by the streamlines and the pressure contours in figures 3 and 4



FIGURE 10. Correction factor C(solid curves), C^* (dotted curves) and C^{**} (dash-dotted curves) vs. relative junction position $v = (l_J + \delta/2)/l_C$, for relative gap length d/D = 0.02, 0.08774 and 0.2, or 2d = 71.8 nm, 315 nm, and 718 nm at 2D = 3590 nm.

ressembles the two-dimensional potential flow. Generally, C^* and C^{**} are smaller than the corresponding values of C, because the three-dimensional flow has a larger resistance to flow owing to the no-slip condition on the surface of the tight junction strand. For d/D = 0.2, the values of C^* and C^{**} are as low as unity, which may be attributed to non-uniform pressure distributions at the cleft entrance and exit, whose mean pressures, not the local pressures in the region $|y| \leq d$, are used to evaluate L_p^C in the present analysis (see figures 5 and 6). For the parameter values shown in table 1, C = 1.74, $C^* = 1.21$ and $C^{**} = 1.36$, which are considerably different from each other.

The present method of analysis on the three-dimensional flow will be useful in examining the coupled movement of water and solutes in the cleft, which is closely related to the revised Starling principle proposed by Michel (1997) and Weinbaum (1998). The water flow though the gap of the tight junction strand is expected to affect significantly the back diffusion of solute from the tissue into the luminal side of the cleft, as noted in §1. This issue is left for a future study.

5. Concluding remarks

Using a mathematical model for steady fluid flow through a serial pathway consisting of the endothelial surface glycocalyx and the endothelial intercellular cleft with junction strands and their discontinuous gaps, we analysed three-dimensional flow of the fluid across the microvessel wall and estimated the hydraulic conductivity. If the values of the Darcy permeability for the glycocalyx are determined based on the regular arrangements of fibres with $r_f = 6$ nm and $\Delta = 8$ nm, then the present study predicts the hydraulic conductivity close to the experimental measurements for rat mesentery microvessels. A key conclusion may be that the endothelial surface

glycocalyx could have a much smaller contribution to the flow resistance than does the intercellular cleft. If further information regarding the ultrastructure and composition of the fibre matrices in the glycocalyx as well as the cleft structures becomes available, this idealized model could be improved to provide a more realistic description of the water flow across the microvessel wall.

The authors thank Drs J. Tarbell and S. Weinbaum for providing unpublished experimental data (J. T.) and valuable comments (S. W.). This research was supported in part by Grants-in-Aid for Scientific Research (B) 16360093 and 19360090.

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