# First observation of $\boldsymbol{\gamma}$ rays emitted from excited states south-east of ${ }^{132} \mathrm{Sn}$ : The $\pi g_{9 / 2}^{-1} \otimes v f_{7 / 2}$ multiplet of ${ }^{132} \mathbf{I n}_{83}$ 

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For the first time, the $\gamma$ decay of excited states has been observed in a nucleus situated in the quadrant south-east of doubly magic ${ }^{132} \mathrm{Sn}$, a region in which experimental information so far is limited to ground-state properties. Six $\gamma$ rays with energies of $50,86,103,227,357$, and 602 keV were observed following the $\beta$-delayed neutron emission from ${ }^{133} \mathrm{Cd}_{85}$, populated in the projectile fission of a ${ }^{238} \mathrm{U}$ beam at the Radioactive Isotope Beam Factory at RIKEN within the EURICA project. The new experimental information is compared to the results of a modern realistic shell-model calculation, the first one in this region very far from stability, focusing in particular on the $\pi 0 g_{9 / 2}^{-1} \otimes \nu 1 f_{7 / 2}$ particle-hole multiplet in ${ }^{132} \mathrm{In}_{83}$. In addition, theoretical estimates based on a scaling of the two-body matrix elements for the $\pi h_{11 / 2}^{-1} \otimes \nu g_{9 / 2}$ analog multiplet in ${ }^{208} \mathrm{Tl}_{127}$, one major proton and one major neutron shell above, are presented.

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The region of the chart of nuclides south-east of doubly magic ${ }^{132} \mathrm{Sn}$, i.e., the nuclei in proximity of ${ }^{132} \mathrm{Sn}$ with $Z<50$ and $N>82$, is of great relevance to the description of the rapid

[^0]neutron capture process of nucleosynthesis, in particular after the break-out from the $N=82$ waiting point nuclei. From the nuclear structure point of view, the study of these nuclei, which are the furthest off stability experimentally accessible today, may give important information on the shell evolution and on the underlying driving forces. They actually play a special role within the framework of the shell model, offering


FIG. 1. Experimental status of the $Z \leqslant 50$ and $N \geqslant 82$ region of the nuclear chart with respect to half-lives, masses and excited states (see text for details). The present work reports on the $\gamma$ decay of excited states of ${ }^{132}$ In (red square), populated via $\beta$-delayed neutron emission from ${ }^{133} \mathrm{Cd}$. The numbers for ${ }^{132,133} \mathrm{Cd}$ refer to the number of identified decay chains.
a unique opportunity to test the matrix elements of the effective shell-model Hamiltonian for protons and neutrons, occupying orbitals which are separated by two major shell closures. Despite this twofold importance, this region is still a terra incognita as far as the nuclear structure of these nuclei is concerned as illustrated in Fig. 1. For some $N>82$ In and Cd isotopes, basic ground-state properties such as half-lives, $\mathrm{T}_{1 / 2}$, and $\beta$-delayed neutron emission probabilities, $\mathrm{P}_{n}$, have been measured in $\beta$-decay experiments performed at ISOLDE some years ago [1-3], and very recently knowledge about half-lives was extended significantly in an experiment performed at RIKEN [4]. The first mass measurement for a $Z<50, N>82$ nucleus, namely, ${ }^{131} \mathrm{Cd}$, was presented just a few weeks ago [5]. With respect to excited states, significant progress has been achieved recently along the $Z=50$ and $N=82$ chains of semimagic nuclei using the technique of isomer spectroscopy. The observation of the decay of $6^{+}$and $8^{+}$seniority isomers in ${ }^{136,138} \mathrm{Sn}[6],{ }^{130} \mathrm{Cd}[7]$, and ${ }^{128} \mathrm{Pd}$ [8] enabled the identification of all members of the $\nu 1 f_{7 / 2}^{2}$ and $\pi 0 g_{9 / 2}^{-2}$ multiplets in these nuclei (see Fig. 1). However, in spite of an extensive search for isomers in that region, no excited state decay has been observed so far in a nucleus with $Z<50$ and $N>82$.

Also from the theoretical point of view information about the structure of nuclei in the region discussed here is very scarce. While detailed shell-model (SM) calculations have been performed in the past for nuclei situated in the other three quadrants around ${ }^{132} \mathrm{Sn}$, to our knowledge no shellmodel study has been presented yet for the region south-east of ${ }^{132} \mathrm{Sn}$. Obviously the lack of experimental information precludes for the time being the development of empirical interactions. Therefore, the use of effective two-body matrix elements (TBMEs) derived from the bare nucleon-nucleon
$(N N)$ potential within the framework of the many-body theory is the method of choice. In fact, this approach does not require the introduction of any adjustable parameter and is therefore particularly appropriate for investigating the structure of nuclei in unknown regions. Furthermore, it has proved to lead to an accurate description of nuclear structure in various mass regions both close to and far from the valley of stability (see Refs. [9-12] for recent examples).

The aim of the present work was to identify first excited states in the nucleus ${ }^{132} \mathrm{In}$, one proton hole and one neutron particle outside the ${ }^{132} \mathrm{Sn}$ core, and to contrast the experimental findings with the results of first SM calculations for this nucleus. The lowest states in ${ }^{132}$ In are based on the coupling of the proton hole in the $0 g_{9 / 2}$ and the neutron in the $1 f_{7 / 2}$ orbital, forming a multiplet of states in the spin range $I^{\pi}=1^{-}$to $8^{-}$with the $I_{\max }-1$ state, in this case $7^{-}$, being the ground state [13]. We would like to emphasize that this proton-hole, neutron-particle multiplet in ${ }^{132}$ In is a unique study case in the Segrè chart. The corresponding $\pi 0 f_{7 / 2}^{-1} \otimes \nu 1 d_{5 / 2}$ and $\pi 0 d_{5 / 2}^{-1} \otimes \nu 1 p_{3 / 2}$ multiplets in ${ }^{78} \mathrm{Co}$ and ${ }^{42} \mathrm{Al}$, south-east of ${ }^{78} \mathrm{Ni}$ and ${ }^{42} \mathrm{Si}$, i.e., one respectively two $\hbar \omega$ lower, are currently not accessible for experimental studies and the $\pi 0 h_{11 / 2}^{-1} \otimes \nu 1 g_{9 / 2}$ multiplet in ${ }^{208} \mathrm{Tl}$, one $\hbar \omega$ higher, is distorted by the presence of the $2 s_{1 / 2}$ and $1 d_{3 / 2}$ proton orbitals, which are closer to the Fermi level than $0 h_{11 / 2}$.

The experiment was performed at the Radioactive Isotope Beam Factory (RIBF) of the RIKEN Nishina Center. Neutronrich ${ }^{132,133} \mathrm{Cd}$ nuclei were produced following the projectile fission of a $345 \mathrm{MeV} / \mathrm{u}^{238} \mathrm{U}$ beam with an average intensity of about 8 pnA , impinging on a $3-\mathrm{mm}$-thick Be target. The ions of interest were separated from other reaction products and identified on an ion-by-ion basis by the BigRIPS in-flight separator [14]. The particle identification was performed using the $\Delta E$-TOF- $B \rho$ method in which the energy loss $(\Delta E)$, time of flight (TOF), and magnetic rigidity $(B \rho)$ are measured and used to determine the atomic number $Z$ and the mass-to-charge ratio $A / q$ of the fragments. Details about the identification procedure can be found in Ref. [15]. The BigRIPS setting was optimized for the maximum transmission of ${ }^{136} \mathrm{Sn}$. The region of the particle identification plot relevant to the present work is shown in Fig. 2.

After their identification the Cd ions were transported through the ZeroDegree spectrometer (ZDS) and finally implanted into the WAS3ABi (wide-range active silicon strip stopper array for $\beta$ and ion detection) Si array positioned at the focal plane of the ZDS. The WAS3ABi detector $[16,17]$ consists of eight DSSSDs with an area of $60 \times 40 \mathrm{~mm}^{2}$, a thickness of 1 mm , and a segmentation of 40 horizontal and 60 vertical strips each. All decay events detected in WAS3ABi during the first 5 s following a valid implantation signal were stored and correlated offline in space and time with the implanted ions. In total about 8600 decay chains were observed for ${ }^{132} \mathrm{Cd}$ and 640 for ${ }^{133} \mathrm{Cd}$. To detect $\gamma$ radiation emitted in the decay of the implanted radioactive nuclei, 12 large-volume Ge cluster detectors [18] from the former EUROBALL spectrometer [19] were arranged in a close geometry around the WAS3ABi detector. The $\gamma$-ray detection efficiency of this array varies from $16 \%$ at an energy


FIG. 2. Partial particle identification plot showing all events according to the reconstructed values of the atomic mass $Z$ and the mass-to-charge ratio $A / q$. Note the clear separation between the fully stripped (i.e., $q=Z$ ) ${ }^{132,133} \mathrm{Cd}$ ions and the hydrogen-like ${ }^{129,130} \mathrm{Cd}$ ions $(q=Z-1)$.
of 100 keV to $7 \%$ at 1 MeV . Note that no add-back of signals registered in neighboring Ge crystals has been applied in the present work.

In Ref. [1] a $\log f t$ value of 5.4 was estimated for the first-forbidden decay $\nu 1 f_{7 / 2} \rightarrow \pi 0 g_{9 / 2}$ from the $0^{+}$ground state of ${ }^{132} \mathrm{Cd}$ (with configuration $\pi g_{9 / 2}^{-2} \otimes v f_{7 / 2}^{2}$ ) to the $1^{-}$ member of the $\pi g_{9 / 2}^{-1} \otimes v f_{7 / 2}$ multiplet in ${ }^{132}$ In, the only significant decay branch populating excited states in ${ }^{132} \mathrm{In}$ below the neutron separation energy ( $P_{n}=60 \% \pm 15 \%$ [1]). For this $\log f t$ value the $1^{-}$state is expected to be populated in $20-30 \%$ of all ${ }^{132} \mathrm{Cd}$ decays. Consequently, taking into account the 8600 observed decays and the $\gamma$ efficiencies quoted above, a few hundred counts are expected for the $\gamma$ transitions connecting this $1^{-}$state to the $7^{-}$ground state. However, as discussed in Ref. [20], no distinct $\gamma$ rays were observed in the energy range below 900 keV in prompt coincidence with the decay of ${ }^{132} \mathrm{Cd}$ ions implanted into WAS3ABi, possibly indicating a larger $\beta$-delayed neutron emission probability as reported in the literature. In contrast, a number of low-energy $\gamma$ rays are observed following the 640 recorded decays of ${ }^{133} \mathrm{Cd}$ ions. Since a " $P_{n}$ value close to $100 \%$ " was reported for ${ }^{133} \mathrm{Cd}$ in Ref. [3], these $\gamma$ rays are assumed to be emitted from excited states in ${ }^{132} \mathrm{In}$.

Figure 3(a) shows the spectrum of $\gamma$ rays observed in prompt coincidence with $\beta$-decay events registered within the first 200 ms after the implantation of an identified ${ }^{133} \mathrm{Cd}$ ion into WAS3ABi. Five lines at energies of $50,103,227,357$, and 602 keV are clearly visible in this spectrum and there are indications for at least one additional line in the range between 50 and 100 keV . In order to reduce the low-energy background in this spectrum, we considered in the next step only those events in which only one of the seven crystals in a Ge cluster detector registered an energy deposition. This condition, which


FIG. 3. $\gamma$-ray spectra in prompt coincidence with decay events during the first 200 ms after the implantation of a ${ }^{133} \mathrm{Cd}$ ion into WAS3ABi. (a) Without further condition, (b) requiring multiplicity one in the composite Ge detector, and (c) applying in addition a strict spatial correlation discussed in detail in the text.
favors photopeak events over signals belonging to Compton scattered $\gamma$ rays, resulted in the $\gamma$-ray spectrum shown in Fig. 3(b). To further clean up the spectrum a very strict spatial correlation between the implantation and the decay is required. Figure 3(c) is obtained when only those events are considered in which the decay took place either in the Si detector in which the ion was implanted or in the one in front or behind. Furthermore, in the plane perpendicular to the beam axis, the decay had to occur within 1 mm of the implantation position in both the vertical and the horizontal directions. The background is now significantly reduced as compared to Fig. 3(a), in particular in the low-energy region. In addition to the five lines listed above there is now clear evidence of the existence of a sixth line at an energy of 86 keV . The statistics accumulated in the present experiment are very limited (see Fig. 3) so that unfortunately no conclusive $\gamma \gamma$ coincidence information could be obtained.

To compare these six observed $\gamma$ rays with theoretical predictions, a realistic effective interaction was derived for the first time for nuclei in the quadrant south-east of ${ }^{132} \mathrm{Sn}$. We take ${ }^{132} \mathrm{Sn}$ as closed core and consider a model space spanned by the four $0 f_{5 / 2}, 1 p_{3 / 2}, 1 p_{1 / 2}, 0 g_{9 / 2}$ proton-hole orbitals and the $\operatorname{six} 1 f_{7 / 2}, 2 p_{3 / 2}, 2 p_{1 / 2}, 0 h_{9 / 2}, 1 f_{5 / 2}, 0 i_{13 / 2}$ neutron orbitals. The adopted values of the neutron single-particle and proton single-hole energies are taken from the experimental spectra of ${ }^{133} \mathrm{Sn}[21,22]$ and ${ }^{131} \mathrm{In}$ [20], respectively, except those of the $\nu 0 i_{13 / 2}$ and the $\pi 0 f_{5 / 2}^{-1}$ orbitals, whose corresponding states have not yet been observed. The energies of these two orbitals are from Refs. [23] and [20], respectively. The two-body effective interaction is derived within the framework of the $\hat{Q}$-box folded diagram expansion [24] starting from the


FIG. 4. Lowest particle-hole and, respectively, particle-particle multiplets in (a) ${ }^{132} \mathrm{In}$ and (b) ${ }^{134} \mathrm{Sb}$. Filled circles correspond to negative-parity and open circles to positive-parity states. Results of SM calculations using realistic effective interactions are shown in black (for ${ }^{134} \mathrm{Sb}$ from Ref. [28]), while SM estimates based on a scaling of TBMEs from the ${ }^{208} \mathrm{~Pb}$ region are given in green. Experimentally proposed states are represented by red dots (for ${ }^{134} \mathrm{Sb}$ from Ref. [29]). For ${ }^{132}$ In, the dashed red line represents the level energies obtained assuming that the six $\gamma$ rays observed in the present experiment form a cascade from the $1^{-}$state to the $7^{-}$ground state while the full red line results from the assumption that one low-energy transition escaped observation (see text for details).
high-precision CD-Bonn $N N$ potential [25], renormalized by means of the $V_{\text {low }-k}$ approach [24] with a cutoff momentum $\Lambda=2.2 \mathrm{fm}^{-1}$. The $\hat{Q}$ box is obtained by including diagrams up to second order in $V_{\text {low-k }}$, which are computed within the harmonic-oscillator basis with $\hbar \omega=7.88 \mathrm{MeV}$. It is worth pointing out that the neutron-proton effective interaction has been explicitly derived in the particle-hole formalism as described in Ref. [26]. All calculations are performed with the OXBASH shell-model code [27]. The four multiplets calculated at lowest excitation energy in the proton-hole, neutron-particle nucleus ${ }^{132}$ In are shown in Fig. 4(a). As expected, the members of the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ multiplet form the negative-parity yrast sequence while the $\pi p_{1 / 2}^{-1} \otimes \nu f_{7 / 2}$ configuration at energies slightly above 500 keV is the lowest positive-parity one. The second excited $3^{-}-6^{-}$states, belonging to the $\pi g_{9 / 2}^{-1} \otimes \nu p_{3 / 2}$ configuration, are positioned about $0.75-1.0 \mathrm{MeV}$ above the yrast line. Finally, the $\pi p_{3 / 2}^{-1} \otimes v f_{7 / 2}$ multiplet is predicted at excitation energies around 1.5 MeV .

For a start, we assume in the following that the six observed $\gamma$ rays correspond to the expected cascade of $M 1$ transitions from the $1^{-}$member of the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ multiplet down to the $7^{-}$ground state. This assumption is based on the observation made in several experimental studies [29-32] that, due to the $E^{5}$ dependence of $\beta$ decay, $\beta$-delayed neutron emission tends to populate states at low excitation energy in the daughter nucleus. For example, in the decay of the (7/2-) ground state of ${ }^{135} \mathrm{Sn}$ via neutron emission to excited states in ${ }^{134} \mathrm{Sb}$ [29], a case which is very similar to the one discussed here with respect to the relative excitation energies of different configurations in the daughter nucleus as shown in Fig. 4(b), primarily the members of the $\pi g_{7 / 2} \otimes \nu f_{7 / 2}$
multiplet are populated. The $1^{-}$and $2^{-}$states with excitation energies around 900 keV , which belong to the $\pi d_{5 / 2} \otimes \nu f_{7 / 2}$ configuration, receive at most $6 \%$ of the total feeding [29]. The resulting excitation energies, assuming that all six observed transitions connect states of the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ multiplet and ordering them according to their energies, are compared to the results of the SM calculations in Fig. 4(a). In this scenario, the experimental energies are systematically higher than the calculated ones, leading to a total energy spread which is twice as large as theoretically predicted. The average difference between experimental and calculated excitation energies is $\approx 300 \mathrm{keV}$, which corresponds to roughly $50 \%$ of the SM energy spread.

Realistic SM calculations using the same approach as described above have been reported in the past for a number of proton-particle, neutron-hole multiplets, namely, the $\pi g_{9 / 2} \otimes \nu g_{9 / 2}^{-1}$, the $\pi g_{7 / 2} \otimes \nu d_{3 / 2}^{-1}$ and the $\pi h_{9 / 2} \otimes \nu f_{5 / 2}^{-1}$ states in ${ }^{90} \mathrm{Nb}_{49},{ }^{132} \mathrm{Sb}_{81}$, and ${ }^{208} \mathrm{Bi}_{125}$ [26,33-35], respectively, and also for the particle-particle nuclei ${ }^{210} \mathrm{Bi}$ [36] and ${ }^{134} \mathrm{Sb}$ [28]. For ${ }^{134} \mathrm{Sb}$, the results of SM calculations are included in Fig. 4(b). These calculations very nicely reproduce the shape of the $\pi g_{7 / 2} \otimes \nu f_{7 / 2}$ multiplet, only slightly overestimating the spread in energy, and also agree with experiment for the excitation energies of the $1^{-}$and $2^{-}$members of the $\pi d_{5 / 2} \otimes \nu f_{7 / 2}$ configuration. In all the cases listed above, the agreement is of comparable quality and the average difference between experimental and calculated level energies amounts to less than $10 \%$ of the SM energy spread of the respective multiplet. In view of this consistently obtained good agreement between experiment and SM calculations for a significant number of cases, the comparison shown in Fig. 4(a) seems to disprove our original assumption that the six observed $\gamma$ transitions form a single cascade. From the experimental side it can of course not be excluded that one or more low-energy transitions escaped observation. For example, the calculated energy for the $5^{-} \rightarrow 6^{-}$transition is only 6 keV . Assuming that one of the lowest transitions within the multiplet is unobserved and adopting an energy of $25 \pm 25 \mathrm{keV}$ for this transition, excitation energy ranges can be estimated for all states of the multiplet as shown in Fig. 4(a). Note that in this scenario the $602 \mathrm{keV} \gamma$ ray would correspond to the decay of a higher lying excited state, belonging to either the $\pi p_{1 / 2}^{-1} \otimes \nu f_{7 / 2}$ or the $\pi g_{9 / 2}^{-1} \otimes v p_{3 / 2}$ multiplet. The resulting excitation energies are now much closer to the SM predictions and the average difference drops to 80 keV , i.e., $12 \%$ of the SM energy spread, comparable to that found in all other cases studied so far. It therefore seems likely that one of the low-energy transitions within the multiplet indeed escaped observation.

Besides the realistic SM calculations discussed above there is an alternative theoretical approach to studying nuclei with only a few nucleons or holes outside the doubly magic ${ }^{132} \mathrm{Sn}$ core. It is based on the known similarities between the nuclear structure properties of nuclei in the ${ }^{132} \mathrm{Sn}$ and ${ }^{208} \mathrm{~Pb}$ regions [37,38]. As was recognized already more than 30 years ago by Blomqvist [37], every proton or neutron single-particle state in the ${ }^{132} \mathrm{Sn}$ region with quantum numbers $(n, l, j)$ has its analog state in the ${ }^{208} \mathrm{~Pb}$ region, one harmonic oscillator shell higher, with quantum numbers $(n, l+1, j+1)$.

Furthermore, the matrix elements of the effective interactions in the ${ }^{132} \mathrm{Sn}$ and ${ }^{208} \mathrm{~Pb}$ regions are expected to be proportional to each other. In several studies [29,39,40] unknown two-body matrix elements in the ${ }^{132} \mathrm{Sn}$ region were derived from the interaction designed by Warburton for nuclei in the ${ }^{208} \mathrm{~Pb}$ region [41]. In all these cases, using the prescription given in Ref. [37], the interaction strengths were scaled up by a factor of $(208 / 132)^{1 / 3}$ corresponding to the mass dependence of a finite-range interaction in an oscillator basis. Here, we followed the same procedure to calculate the states belonging to the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ configuration in ${ }^{132}$ In from the TBME for the $\pi h_{11 / 2}^{-1} \otimes \nu g_{9 / 2}$ multiplet in ${ }^{208} \mathrm{Tl}$ [41]. Note that no configuration mixing was considered. The resulting energies are shown in green in Fig. 4(a). As for the realistic SM interaction, a much better agreement with experiment is obtained assuming that one low-energy transition escaped observation. In this case the multiplet is perfectly reproduced by the theory in the spin range $2-7$, only the $1^{-}$state is predicted too high in energy (about 300 keV ). Note that the estimate obtained in the same way for the $\pi g_{7 / 2} \otimes \nu f_{7 / 2}$ multiplet in ${ }^{134} \mathrm{Sb}$, inferred from the TBME for the $\pi h_{9 / 2} \otimes$ $\nu g_{9 / 2}$ configuration in ${ }^{210} \mathrm{Bi}$, yields excellent agreement with experiment as shown in Fig. 4(b). In contrast to the particleparticle multiplet in ${ }^{134} \mathrm{Sb}$, the $\pi g_{9 / 2}^{-1} \otimes v f_{7 / 2}$ hole-particle configuration in ${ }^{132}$ In exhibits negligible odd-even staggering which supports the chosen $\gamma$-ray sequence in descending order.

To summarize the above discussion: Assuming that the six $\gamma$ rays observed following $\beta$-delayed neutron emission from ${ }^{133} \mathrm{Cd}$ in the present work form a cascade of $M 1$ transitions between the members of the multiplet expected to be lowest in ${ }^{132}$ In, namely, the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ configuration, the experimental $1^{-}-7^{-}$energy spread is strongly underestimated by both the SM calculation employing a modern realistic effective interaction and the estimate based on a $A^{-1 / 3}$ mass scaling of TBME designed for nuclei in the ${ }^{208} \mathrm{~Pb}$ region. On the other hand, considering the possibility that one of the low-energy transitions within the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ multiplet escaped observation, a much better agreement between the experimental excitation energies and the two different theoretical approaches is obtained. More precisely, the quality of the results obtained from the realistic SM calculation is in this case of the same order as found for several other particle-hole and particle-particle multiplets in different mass regions.

In conclusion, in the present work we reported on the very first observation of $\gamma$ decays from excited states of a nucleus situated in the quadrant south-east of ${ }^{132} \mathrm{Sn}$, namely, its one proton-hole, one neutron neighbor ${ }^{132} \mathrm{In}$. On the theoretical side, we presented the first shell-model calculation considering neutrons in the $N=82-126$ and proton holes in the $Z=28-50$ major shells. The TBME were derived from the $N N$ potential within the framework of the many-body theory. The comparison between experiment and theory suggests that at least four of the six observed transitions connect members of the $\pi g_{9 / 2}^{-1} \otimes \nu f_{7 / 2}$ multiplet, while at least one more likely corresponds to the decay of an excited state belonging to another configuration. The present work constitutes an important first step toward the exploration of the nuclear structure in a region of the nuclear chart, which, although crucial for nucleosynthesis processes, is presently still a terra incognita as far as excited state properties are concerned. With the steadily increasing beam intensities provided by radioactive ion beam facilities around the world it is to be expected that more comprehensive experimental information, for ${ }^{132} \mathrm{In}$ as well as other nuclei in the region, will soon become available. This will allow one to ascertain the capability of different nuclear models to provide reliable predictions for physical quantities in regions of the isotope chart which will remain unaccessible for experimental studies.

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