

**INFRARED OPTICAL PROPERTIES OF  
WURTZITE SEMICONDUCTOR  
HETEROSTRUCTURE WITH ARBITRARY  
CRYSTAL ORIENTATIONS**

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by

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## LIST OF SYMBOLS

$\theta_{xc}$	Angle between the $c$ -axis and the $x$ -axis
$\theta_{yc}$	Angle between the $c$ -axis and the $y$ -axis
$\theta_{zc}$	Angle between the $c$ -axis and the $z$ -axis
$\theta$	Angle of incidence in the medium of incidence for reflectance measurement
$\phi$	Angle of rotation about the surface normal of sample from the laboratory $y$ -axis
$\omega$	Angular frequency
$y_0$	Baseline offset of a peak
$x_0$	Center of the peak
$\varepsilon$	Complex dielectric constant
$q$	Component of the wavevector normal to the interface
$\varepsilon_1$	Dielectric constant of the medium of incidence
$\varepsilon_{\perp} (\parallel)$	Dielectric tensor component in a direction perpendicular (parallel) to the $c$ -axis
$E_c$	Electric field vector for extraordinary mode
$E_o$	Electric field vector for ordinary mode
$e$	Electron charge



$m^*$	Electron effective mass
$m_e$	Electron mass
$\alpha_{l-1}$	Field decay constants along the normal of the interface
$d$	Finite thickness of a thin film
$n$	Free carrier concentration
$\Gamma$	Full width at half maximum intensity
$\Gamma_G$	Gaussian full width at half maximum intensity
$\epsilon_\infty$	High frequency dielectric constant
$\epsilon''$	Imaginary part of dielectric constant
$k_p$	In-plane wavevector component of evanescent wave generated by the ATR prism
$a, c$	Lattice constants
$\gamma_{LO}$	LO phonon damping constant
$\nu_{LO}$	LO phonon mode
$\Gamma_L$	Lorentzian full width at half maximum intensity
$\gamma_{LPP}$	LPP damping constant
$\nu_{LPP}$	LPP mode
$\alpha$	Magnitude of the direction cosine of the $c$ -axis with respect to the $x$ - axis

$\beta$	Magnitude of the direction cosine of the $c$ -axis with respect to the $y$ -axis
$\gamma$	Magnitude of the direction cosine of the $c$ -axis with respect to the $z$ -axis
$(h k l)$	Miller indices
$N_e$	Normalization constant of $E_e$
$N_o$	Normalization constant of $E_o$
$\parallel$	Parallel
$\rho$	Parameter related to the asymmetry of a peak
$\epsilon_o$	Permittivity of free space
$\perp$	Perpendicular
$\varphi$	Phase function
$\gamma_p$	Plasma damping constant
$\nu_{po}, \nu_p$	Plasma mode
$R_p$	p-polarized reflectivity
$r_{pp}$	p-to-p polarized reflectance coefficient
$t_{pp}$	p-to-p polarized transmittance coefficient
$r_{ps}$	p-to-s polarized reflectance coefficient

$t_{ps}$	p-to-s polarized transmittance coefficient
$\epsilon'$	Real part of dielectric constant
$r$	Reflectance coefficient
$n_p$	Refractive index of the ATR prism
$m$	Specific layer between the medium of incidence and substrate
$l$	Specific layer in a multilayer system
$R_s$	s-polarized reflectivity
$r_{sp}$	s-to-p polarized reflectance coefficient
$t_{sp}$	s-to-p polarized transmittance coefficient
$r_{ss}$	s-to-s polarized reflectance coefficient
$t_{ss}$	s-to-s polarized transmittance coefficient
$t$	Time
$\gamma_{TO}$	TO phonon damping constant
$\nu_{TO}$	TO phonon mode
$A$	Total area under the peak from the baseline
$N$	Total number of layers for $N$ -layer system
$c_v$	Velocity of light in a vacuum ( $3 \times 10^8 \text{ ms}^{-1}$ )
$\lambda$	Wavelength

$\nu$	Wavenumber
$K_x$	Wavevector of the polaritons along the $x$ -direction or $x$ -component of wavevector for the incident light wave
$k_{\text{sub}}$	Wavevector of the substrate light line
$k_v$	Wavevector of the vacuum light line
$X_e$	$x$ -component of $E_e$
$X_o$	$x$ -component of $E_o$
$\theta_{hkl}$	XRD diffraction angle
$Y_e$	$y$ -component of $E_e$
$Y_o$	$y$ -component of $E_o$
$Z_e$	$z$ -component of $E_e$
$Z_o$	$z$ -component of $E_o$
$q_e$	$z$ -component of the wavevector for extraordinary mode
$q_1$	$z$ -component of the wavevector for incoming wave
$q_o$	$z$ -component of the wavevector for ordinary mode
$D_x(z)$	$z$ -dependence electric displacement field component along the $x$ - direction
$D_y(z)$	$z$ -dependence electric displacement field component along the $y$ - direction

$D_z(z)$   $z$ -dependence electric displacement field component along the  $z$ -direction

$E_x(z)$   $z$ -dependence electric field component along the  $x$ -direction

$E_y(z)$   $z$ -dependence electric field component along the  $y$ -direction

$E_z(z)$   $z$ -dependence electric field component along the  $z$ -direction

## LIST OF ABBREVIATIONS

AlAs	Aluminium arsenide
AlGaAs	Aluminium gallium arsenide
AlGaN	Aluminum gallium nitride
AlN	Aluminum nitride
As <sub>2</sub>	Arsenic
ATR	Attenuated total reflectance
BN	Boron nitride
BPhP	Bulk phonon polariton
CaF <sub>2</sub>	Calcium fluoride
<i>c</i> -axis	<i>c</i> -plane crystallographic axis, also known as optics axis
CdF <sub>2</sub>	Cadmium fluoride
EM	Electromagnetic
FESEM	Field emission scanning electron microscope
FTIR	Fourier transform infrared
FWHM	Full width at half maximum
GaAs	Gallium arsenide
GaN	Gallium nitride
GaP	Gallium phosphide
GUI	Graphical user interface
IDE	Integrated development environment
InAlN	Indium aluminium nitride
InGaN	Indium gallium nitride
InN	Indium nitride

IPhP	Interface phonon polariton
IPIPhP	Interface plasmon-phonon polariton
IR	Infrared
IRSE	Infrared spectroscopic ellipsometry
KK	Kramers-Kronig
KRS-5	Thallium iodide bromide
LED	Light-emitting diode
LM	Levenberg-Marquardt
LO	Longitudinal optical
LPP	LO phonon-plasmon coupling
MATLAB	Matrix laboratory
MBE	Molecular beam epitaxy
MFC	Microsoft Foundation Class
MOCVD	Metal-organic chemical vapor deposition
MSVC	Microsoft Visual C++
RF	Radio frequency
Si	Silicon
SiC	Silicon carbide
SPhP	Surface phonon polariton
SPIPhP	Surface plasmon-phonon polariton
TE	Transverse electric
TM	Transverse magnetic
TO	Transverse optical
UV	Ultraviolet
VC++	Visual C++

XRD X-ray diffraction

ZnO Zinc oxide

ZnTe Zinc telluride



**SIFAT-SIFAT OPTIK INFRAMERAH HETEROSTRUKTUR  
SEMIKONDUKTUR WURTZIT DENGAN ORIENTASI HABLUR  
SEMBARANGAN**

**ABSTRAK**

Pergantungan orientasi hablur dengan sifat-sifat optik inframerah (IR) untuk semikonduktor heterostruktur wurtzit heksagon dan substrat yang berkaitan telah dikaji. Pengukuran spektrum pantulan IR terkutub menunjukkan bahawa tindak balas spektrum daripada hablur nilam pukal dan heterostruktur III-nitrida wurtzit yang terdiri daripada lapisan-lapisan yang bersatah kristalografi sembarangan adalah bergantung kepada orientasi sampel. Kecuali sampel yang mempunyai permukaan berorientasi satah-*c*, spektrum pantulan IR terkutub untuk sampel yang dikaji boleh diubahkan dengan memutar sampel pada normal permukaan. Formula pantulan yang mengambil kira kesan orientasi hablur telah digunakan bersama dengan langkah penyesuaian lengkung untuk menganalisis spektrum yang diukur. Parameter-parameter bahan yang penting seperti pemalar dielektrik, mod fonon optik, ketebalan lapisan dan orientasi kristal untuk sampel yang dikaji telah ditentukan secara tidak membina daripada penyesuaian yang terbaik bagi spektrum pantulan IR terkutub eksperimen dan teori. Dengan menggunakan parameter yang diperolehi, simulasi untuk spektrum penyebaran polariton fonon permukaan dan antara muka (SPhP dan IPhP) telah dijalankan dengan mengambil kira kesan-kesan parameter lembapan dan orientasi hablur. Keputusan teori telah menunjukkan bahawa tindak balas SPhP dan IPhP untuk sampel yang mempunyai permukaan berorientasi satah-*a* tanpa kutub atau permukaan berorientasi satah-*r* separa kutub adalah bergantung kepada arah. Sifat-sifat resonan bagi mod SPhP dan IPhP yang diramalkan sangat bersetuju dengan pengukuran pantulan penuh dikecilkan IR terkutub-p.

# INFRARED OPTICAL PROPERTIES OF WURTZITE SEMICONDUCTOR HETEROSTRUCTURE WITH ARBITRARY CRYSTAL ORIENTATIONS

## ABSTRACT

Crystal orientation dependence of the infrared (IR) optical properties of hexagonal wurtzite III-nitride heterostructures and their relevant substrates was investigated. Polarized IR reflectance measurements showed that the spectral responses of bulk sapphire crystals and wurtzite III-nitride heterostructures consisting of layers with arbitrary crystallographic planes depend on sample orientation. Except for sample with  $c$ -plane oriented surface, the polarized IR reflectance spectra of a given sample can be changed by rotating the sample about its surface normal. A reflection formula that considers the effect of crystal orientation was employed with a curve fitting procedure to analyze the measured spectra. Important materials parameters such as the dielectric constant, optical phonon modes, layer thickness and crystal orientation of the studied samples, have been non-destructively determined from the best-fit of experimental and theoretical polarized IR reflectance spectra. Using the obtained parameters, simulations of the surface and interface phonon polaritons (SPhP and IPhP) dispersion spectra have been performed by taking into account the effects of damping parameters and crystal orientation. The theoretical results revealed that the SPhP and IPhP responses of samples with non-polar  $a$ -plane or semi-polar  $r$ -plane oriented surfaces are directionally-dependent. The predicted resonant properties of the SPhP and IPhP modes were in good agreement with the p-polarized IR attenuated total reflectance measurements.

# CHAPTER 1

## INTRODUCTION

### 1.1 Motivation

III-nitride semiconductors, namely, indium nitride (InN), gallium nitride (GaN) and aluminium nitride (AlN) have received continuous interest from optoelectronics research community. The most attractive features of these solid state materials in the area of optoelectronics are their direct bandgaps, i.e., about 0.7 eV for InN (Kuyyalil et al., 2012; Matsuoka et al., 2002), 3.4 eV for GaN (Pankove et al., 1970; Pankove and Schade, 1974) and 6.2 eV for AlN (Yamashita et al., 1979; Yim et al., 1973) at room temperature. Making use of the alloy composition dependence of bandgap, III-nitride-based alloys hold promise for the development of light emitting devices operated in the deep ultraviolet (UV) to near infrared (IR) spectral ranges (Davydov et al., 2002; Iliopoulos et al., 2008; Nepal et al., 2005; Wu et al., 2003a). In 2014, the Nobel Prize for Physics is awarded to Professor Shuji Nakamura, Professor Isamu Akasaki and Professor Hiroshi Amano for their invention of efficient blue light emitting diode (LED) based on III-nitrides (Heber, 2014). The invention of efficient blue LED has paved the way for the generation of bright and energy-saving white light sources for illumination (Nakamura et al., 1991; 2000).

Apart from lighting applications, III-nitrides are versatile materials for the production of durable electronic devices, sensors and solar cell. With wide bandgaps, strong chemical bonds and thermal stabilities, GaN and AlN possess outstanding device performance, which goes beyond the typical semiconductor materials [such as silicon (Si) and gallium arsenide (GaAs)] that can handle. It have been demonstrated

that transistors and various sensors fabricated based on GaN and AlN can operate at high power, high temperature, resist radiation damage and withstand caustic environment (Lin et al., 2010; Pearton et al., 2004; Son et al., 2010; Turner et al., 1994). On the other hand, the narrow bandgap of InN can be adapted to fabricate solar cell. The efficiency of a solar cell varies as a function of bandgap. Theoretically, the maximum efficiency of a solar cell assuming a single p-n junction is around 33.7 % with bandgap of 1.34 eV, which is known as Shockley-Queisser limit (Shockley and Queisser, 1961). Through fabrication of In-rich InGaN or InAlN ternary alloy, efficient solar cell that has better performance than the conventional Si-based solar cell can be realized (Jani et al., 2007; Wu et al., 2003b; Yamamoto et al., 2010). Besides, InN is of great scientific interest for terahertz applications due to its small electron effective mass, large electron mobility and high peak electron velocity (Ascázubi et al., 2004; Hwang et al., 2010).

III-nitrides can crystallize in three types of structural phases, namely, wurtzite, zincblende and rock-salt. Under normal ambient conditions, III-nitrides preferentially crystallize in the wurtzite structure. Zincblende III-nitrides are thermodynamically metastable. To fabricate zincblende III-nitrides, epitaxial technique with special growth conditions and substrate with specific crystal symmetry are required (Daudin et al., 1998; Hu et al., 2004; Miyoshi et al., 1992). Formations of III-nitrides in the rocksalt structure only occur under high pressure condition. The structural phase transition from wurtzite to rock salt structure for InN, AlN and GaN have been experimentally observed under high pressure conditions at 12.1GPa, 22.9GPa and 52.2GPa, respectively (Ueno et al., 1992; 1994). Because of the reproducibility of high quality wurtzite III-nitrides, most experimental studies were conducted for wurtzite case.

Wurtzite III-nitrides belong to the hexagonal crystal system and are conventionally grown in polar *c*-plane orientation. The spontaneous polarization field inside the *c*-plane wurtzite semiconductor is an advantage for certain device applications (Li et al., 2001; Shi et al., 2013; Woodward et al., 2012). However, it is a drawback for electroluminescent devices. The strong internal polarization field gives rise to the quantum confined Stark effect, which reduces the carrier recombination transition rate and red-shifts the emission wavelength. This leads to a reduction in the efficiency of light emitting devices (Kuokstis et al., 2002; Leroux et al., 1998; Miller et al., 1984). There is an upsurge of research on the wurtzite semiconductors in non-polar and semi-polar orientations (Huang et al., 2012; Kucharski et al., 2012; Paduano et al., 2013). The motivation is that the piezoelectric and polarization field strengths are insignificant in non-polar wurtzite semiconductors or can be significantly reduced in semi-polar wurtzite semiconductors (Farrell et al., 2012; Paskova, 2008), hence overcome the disadvantages of polar wurtzite semiconductors in lighting applications. Several reports revealed that non-polar and semi-polar wurtzite semiconductors have better photoluminescence characteristics than polar wurtzite semiconductors (Aggarwal et al., 2010; Bae et al., 2011; Ng, 2002).

Since the proof of the minimal internal polarization field strength is beneficial to lighting applications, numerous works have been done to look for growth methods and optimum growth conditions of non-polar wurtzite III-nitride thin films (Moram et al., 2009; Okada et al., 2009; Sun et al., 2009; Wu et al., 2008). Nevertheless, the properties of non-polar wurtzite III-nitrides are less well understood than those of the polar III-nitrides due to the difficulties in obtaining high quality samples. The planar anisotropic nature of the growth mode can easily lead to an epitaxial layer with high

density of crystalline defects (Ajagunna et al., 2010; Fang et al., 2011; Wang et al., 2004). Fortunately, with recent advances in crystal growth, high quality non-polar wurtzite III-nitrides thin films are reproducible using epitaxy technology such as molecular beam epitaxy (MBE) (Ajagunna et al., 2010; Lo et al., 2015) and metal-organic chemical vapor deposition (MOCVD) (Chiang et al., 2011). The availability of high quality samples offers opportunities for reliable experimental characterization of the properties of non-polar wurtzite III-nitrides.

A structure built up with at least two different materials in junction contact is known as heterostructure (Agostini and Lamberti, 2011). Integration of III-nitrides with other materials into heterostructure is a key step to realize III-nitride-based device applications. Despite extensive research on the growth of non-polar wurtzite III-nitride thin films, investigations of the effects of crystal orientation on the optical properties of wurtzite III-nitride heterostructures, in particular, in IR spectral region, are still scant up to date. Many related material researchers, especially for those doing fabrication works, are not familiar with the crystal orientation dependence of IR optical responses of wurtzite semiconductor heterostructure and the associated characterization procedure.

In semiconductor device fabrication, there are layers that are intentionally grown or deposited. Meanwhile, accumulation layers and oxide layers may exist at the surface and interfaces. In all these cases, the lattice dynamics as well as the other properties related to the surface and interface regions might be altered (Chen et al., 1990; Kim and Stroscio, 1990; Lassnig and Zawadzki, 1984). A deep understanding of optical phonon responses at the surface and interfaces in semiconductor heterostructure is thus insightful for the design of optoelectronics devices. Due to the dissimilar distribution of polarization charges at the surface and interfaces as

compared to the bulk region, the optical properties of the surface and interfaces are generally different from the bulk region. The existence of the interfaces in semiconductor heterostructure has great impact on some important fundamental properties, especially the electron transport and optical phonon properties (Hsu and Walukiewicz, 1998; Kim and Stroscio, 1990; Wendler et al., 1990).

For a multilayer system consisting of layers having negative dielectric functions in the IR spectral region, surface and interface phonon polaritons (SPhP and IPhP) exist at the surface and interfaces of the system (Agranovich and Mills, 1982; Albuquerque and Cottam, 2004; Mills and Maradudin, 1973). The SPhP and IPhP modes have great potential and adaptability in modern device applications due to their abilities in mediating thermal energy transfer and the sensitive resonant properties. Through manipulating the properties of the SPhP modes, modern devices such as near field surface enhanced spectroscopy (Anderson, 2005; Huber et al., 2005), high density optical data storage device (Ocelic and Hillenbrand, 2004), thermo-photovoltaic energy conversion system (Laroche et al., 2006; Narayanaswamy and Chen, 2003; Shen et al., 2009) and antenna sensors (Kim and Cheng, 2010) have been designed. Since wurtzite III-nitrides possess negative dielectric functions in the IR spectral region, SPhP and IPhP modes exist in its heterostructure system. To explore new application possibility of the SPhP and IPhP based on wurtzite III-nitrides, a prior understanding of the factors which influence the SPhP and IPhP responses of wurtzite III-nitride heterostructures, is thus the prerequisite. Nevertheless, there is lack of investigation of the IR absorptions by the SPhP and IPhP modes of wurtzite III-nitride heterostructures consisting of layers with non-polar and semi-polar planes.

To contribute an understanding of the crystal orientation dependence of the SPhP and IPhP responses, the SPhP and IPhP characteristics of wurtzite III-nitride heterostructures and their relevant substrates with different crystal orientations, will be carried out. Information about the layered structures, specifically the crystal orientation, layer thickness and the IR dielectric tensor components are the basis for the theoretical study of the SPhP and IPhP modes. Therefore, attention is also paid to the characterization technique and the associated procedure for the determination of the crystal orientation, layer thickness and IR dielectric tensor components of the studied samples. Apart from wurtzite III-nitrides, the SPhP and IPhP characteristics of a wurtzite *c*-plane zinc oxide (ZnO) thin film on silicon carbide (6H-SiC) substrate are investigated. It is worth to highlight here that the IR optical properties of wurtzite ZnO and 6H-SiC are analogous to that of wurtzite III-nitrides. As compared to the wurtzite III-nitride samples, however, the wurtzite ZnO sample used in this work possesses a simpler layered structure (i.e., the system has a least number of layers and the free carriers' plasma response is negligible), which is convenient for testing the theoretical model presented in this dissertation.

## **1.2 Objectives and scope of work**

This dissertation focuses primarily on the investigations of the IR optical properties of wurtzite semiconductor heterostructure with arbitrary crystal orientation. Oblique-incidence polarized IR reflectance and attenuated total reflectance (ATR) are the main experimental techniques used in this project. The early parts of the dissertation are mainly dealing with the theoretical and computational works. First, the reflection formula that is applicable to wurtzite semiconductor heterostructure with arbitrary crystal orientation was derived. Based on the reflection formula and



appropriate dielectric function models for the studied materials, software for calculating the reflectivity was developed. The software can be used to simulate the polarized IR reflectance and ATR spectra of multilayer system consisting of arbitrary oriented hexagonal and/or cubic structured layers.

The latter works are to apply the simulation software for characterizations of wurtzite III-nitride heterostructures with arbitrary crystal orientations. The initial work is the determination of material parameters of various samples using the polarized IR reflectance measurements. The material parameters deduced include the dielectric constant, optical phonon modes, layer thickness and crystal orientation. Through some mathematical manipulations on the reflection formula, the dispersion spectra of the SPhP and IPhP modes of the studied system can be simulated, hence predict the crystal orientation dependence of the SPhP and IPhP responses. The ultimate goal is to verify the theoretical predictions of the SPhP and IPhP modes of the studied samples with the p-polarized IR ATR measurements.

### **1.3 Originality of the research**

For the first time, the SPhP and IPhP responses of wurtzite III-nitride heterostructure consisting of layers with non-polar and semi-polar planes are reported. Since sapphire crystal is the main substrate for the growth of wurtzite III-nitride heterostructure, the SPhP responses of sapphire crystals with differently oriented surfaces are also investigated. A method has been proposed to calculate the SPhP and IPhP dispersion curves/spectra taking into account the effects of crystal orientation and damping parameters. The validity of the method has been tested experimentally with the p-polarized IR ATR measurements of various samples.

To simulate the polarized IR reflectance and ATR spectra, a reflection formula has been derived in the form of 4×4 transfer matrix following Lekner's approaches (Lekner, 1991, 1992, 1994). However, the formula has been rewritten into a more concise form so that the formula is numerically stable and efficient for computation. Considering the reflection formula for arbitrary oriented hexagonal crystal system is not often applied as compared to the conventional reflection formula that is specific for polar *c*-plane orientation (Barker Jr and Ilegems, 1973; Cadman and Sadowski, 1978; Dumelow and Tilley, 1993), detailed calculation procedure including the numerical tricks are included in this dissertation. Apart from that, the polarized IR reflectance responses of bulk-like free standing zincblende GaN and zincblende GaN thin films have been investigated for complementary information. Additional resonant features, which have not been predicted from theory, have been detected in the first derivative of the polarized IR reflectance spectra measured at high angles of incidence.

#### **1.4 Organization of the dissertation**

After a brief introduction in this chapter, various IR spectroscopic techniques for material characterization, the highlight of IR reflectance spectroscopy for characterization of semiconductors and the history of research on the SPhP and IPhP modes of wurtzite semiconductor heterostructures are reviewed in chapter 2. The early sections of chapter 3 present the theoretical models for the calculations of dielectric tensor components and reflectivity for wurtzite semiconductor heterostructure with arbitrary crystal orientation. The end of chapter 3 describes the method for the simulation of the SPhP and IPhP dispersion curves/spectra. Chapter 4 elucidates the details of the samples and measurements used in this work, followed

by the details of software implementation and curve fitting algorithm. Chapters 5 and 6 illustrate the main results of the dissertation. For clarity of discussion, the early section of chapter 5 presents the polarized IR reflectance studies of the samples with zincblende structure. After that, the discussions are directed to the polarized IR reflectance studies of wurtzite semiconductor heterostructures and their relevant substrates consisting of layers with arbitrary crystallographic planes. In chapter 6, the orientation dependence of the SPhP and IPhP responses of wurtzite semiconductor heterostructures and their relevant substrates are presented. Finally, chapter 7 summarizes the important findings of this dissertation and suggests a few possible directions for future research.

## **CHAPTER 2**

### **LITERATURE REVIEW**

#### **2.1 Introduction**

Prior to the fabrication of semiconductor devices, a number of measuring tools are usually required to characterize the fundamental properties of raw materials to ensure a consistently high quality product. For examples, scanning electron microscope is used to investigate the surface morphology and to measure the individual layer thickness of semiconductor heterostructures. Secondary ion mass spectrometry, Hall-effect and capacitance-voltage probes are used to determine the electrical properties of semiconductor layers. However, these techniques cannot be flexibly applied in certain cases such as the manufacturing process monitoring due to the contamination or damage to the sample. To avoid the contamination or damage to the sample, complementary optical techniques such as Raman scattering, UV-visible and IR spectroscopies have been applied widely for non-destructive characterization of semiconductors.

The emphasis of this dissertation is on the case studies of IR spectroscopy for characterization of IR optical parameters, SPhP and IPhP responses of wurtzite semiconductor heterostructure with arbitrary crystal orientation. To exemplify the importance of the research topic and to ease the discussions in the latter chapters, this chapter briefly describes the common IR spectroscopic techniques, followed by the highlight of IR reflectance spectroscopy for characterization of semiconductors. Subsequently, the fundamentals, history and relevant studies of the SPhP and IPhP characteristics of wurtzite semiconductor heterostructures are reviewed.

## 2.2 IR spectroscopic techniques for material characterization

When a light wave interacts with a material, the incident light can be reflected at the surface, the light passing through the surface can be scattered or absorbed while the remaining light which leaves the material is the transmitted light. The wave theory of light is established when Maxwell developed his theory of electromagnetic (EM) radiation and showed that light that is perceived by human eyes (i.e., visible light) was only a small portion of EM spectrum (Tilley, 2010). EM spectrum categorizes EM radiations by wavelength into radio wave, microwave, terahertz, IR, visible, UV, X-rays and gamma rays, as illustrated in Figure 2.1. Spectroscopy is a tool that is developed based on interaction between EM radiation and matter. The term “spectroscopy” refers to the measurement of radiation responses of a material as a function of wavelength, energy, frequency or wavenumber (Band, 2006).

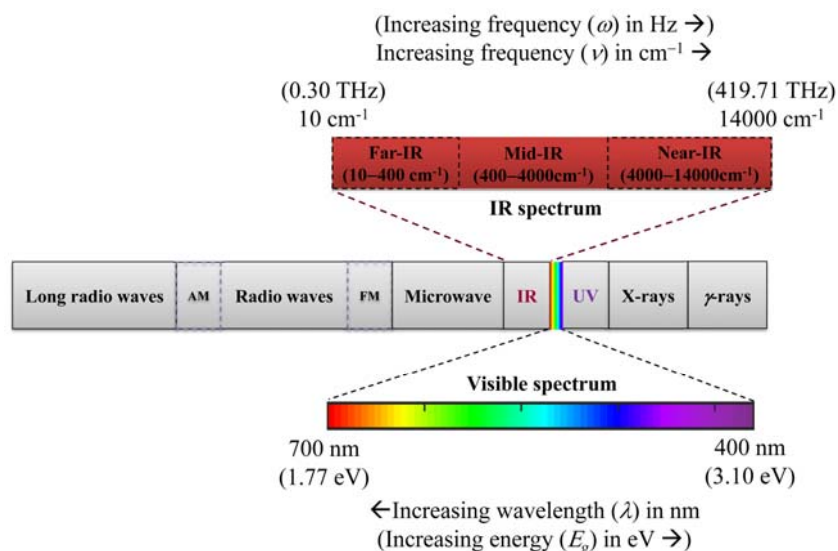


Fig. 2.1: The EM spectrum. The EM radiation that is perceived by human eyes is called visible light, occupies wavelength region from 400–700 nm.

A spectroscopy that deals with the IR radiation is known as IR spectroscopy. The spectrum measured by IR spectroscopy is represented by a plot of IR intensity versus wavenumber scale ( $\text{cm}^{-1}$ ), where the wavenumber is directly proportional to the frequency and energy. IR spectrum can be further divided into far-, mid- and near-IR sub-regions, corresponding to the wavenumber regions of 10–400  $\text{cm}^{-1}$ , 400–4000  $\text{cm}^{-1}$  and 4000–14000  $\text{cm}^{-1}$ , respectively. The far-IR region provides information about the vibrations of molecules containing heavy atoms, molecular skeleton vibrations, molecular torsions and crystal lattice vibrations. The mid-IR region provides information about the fundamental vibrations and associated with the rotational-vibrational structure whereas, the near-IR region provides information about the excitation of overtone or harmonic vibration (Sun, 2009). Because different compounds have different combination of atoms and associated with unique vibration frequencies, IR spectrum can be exploited to deduce sample identity.

The development of IR spectroscopic techniques lies on the basis of transmission and reflection phenomena. Transmittance spectroscopy is the oldest and simplest method. When a light wave propagates across a finite length absorbing medium, one may be interested in the portion of light that is either be absorbed or passes through the medium. The transmittance refers to the relative amount of the light that passes through the medium, whereas the absorbance refers to the amount of light dissipated in the medium (Tkachenko, 2006). Although operation of transmittance spectroscopy is simple, however, the user often needs to prepare the sample into the forms of pellet, mull, film, etc. before the transmittance measurement can be made. The sample preparation for transmittance spectroscopy requires expertise and is time consuming (Griffiths and De Haseth, 2007; Smith, 2011). To investigate the sample that is difficult to analyze by the transmittance technique,

reflectance spectroscopy is a preferential option. The reflectance refers to the fraction of light that is reflected from the surface of the sample. Reflectance spectroscopy can be further classified into two types, namely, external reflectance and internal reflectance measurements. In external reflectance measurement, the medium of incidence is a vacuum. If the light beam is reflected from a smooth surface, the reflection is said to be specular and the angle of reflectance equals to the angle of incidence. If the surface is rough, reflection occurs in random direction so-called diffuse reflection. In internal reflectance measurement (also known as ATR), the medium of incidence is a prism. Total internal reflection phenomenon occurs when the angle of incidence at the interface between the sample and prism is greater than the critical angle (Griffiths and De Haseth, 2007; Kortüm, 2012; Otto, 1975). Apart from the transmittance and reflectance techniques, ellipsometry is another popular setup of IR spectroscopy. Ellipsometry measures the change in polarization as light reflects or transmits from a material structure, where the change in polarization is quantified by the amplitude ratio and the phase difference (Tompkins and Irene, 2005).

In principle, the selection of which spectroscopic techniques for sample characterization depends on the nature of the sample and the kind of information demanded by the user. Specifically, this project utilized the specular reflectance and ATR techniques for sample characterization. Ellipsometry and transmittance cases are outside the scope of this dissertation.

### **2.3 Relation between IR dielectric function and IR reflectance spectrum of semiconductors**

To comprehensively understand the physical properties of a material on the theoretical basis of solid state physics, one may calculate the band structure of the material. The theory of band structure such as density functional theory has been frequently employed to explain the electronic, magnetic and optical properties of semiconductor materials. Useful information such as electrical conductivity, resistivity, vibrational modes, optical absorption, etc. can be predicted theoretically (Adachi, 2012; Persson et al., 2001; Vogel et al., 1997). On the other hand, to understanding the physical properties of a material experimentally, it is useful to apply spectroscopic techniques making use of the light interaction with material, which is the focus in this dissertation.

For any spectral region including the IR, the reflectance of a non-magnetic semiconductor is related to its dielectric constant (or the refractive index). The dielectric constant varies as a function of frequency, so called dielectric function. Numerically, the reflectance is an absolute value, whereas the dielectric function is a complex value that consists of imaginary part [i.e.,  $\epsilon(\nu) = \epsilon'(\nu) + i\epsilon''(\nu)$ , where  $\nu$  is wavenumber]. Investigation of the dielectric function is meaningful because the dielectric function is closely related to many fundamental properties such as electronic and optical properties. However, the reflectance measurement does not directly give user information about the dielectric function. A mathematical analysis, called Kramers-Kronig (KK) relations can be complementary applied to extract both  $\epsilon'(\nu)$  and  $\epsilon''(\nu)$  from the measured reflectance spectrum (Berreman, 1967; Grosse and Offermann, 1991; Hopfe et al., 1992; Lucarini, 2005; Querry and Holland, 1974).



Using the KK relations, the reflectance coefficient as a function of  $\nu$ , which is a complex value, can be retrieved, as shown in Eqs. (2.1)–(2.2) (Berreman, 1967):

$$r(\nu) = \sqrt{R(\nu)} \exp(i\varphi(\nu)), \quad (2.1)$$

$$\varphi(\nu) = \frac{\nu}{\pi} \int_0^{\infty} \frac{\ln R(\nu') - \ln R(\nu)}{\nu^2 - \nu'^2} d\nu', \quad (2.2)$$

where  $R(\nu)$  is the measured reflectance and  $\varphi(\nu)$  is the phase function. Once  $r(\nu)$  is obtained,  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$  can be simply derived from the formula of the reflectance coefficient for the system of study. For a normal-incidence reflectance measurement on a simple cubic crystal,  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$  can be calculated using (Lekner, 1987):

$$\varepsilon(\nu) = \left( \frac{1-r(\nu)}{1+r(\nu)} \right)^2. \quad (2.3)$$

Despite the exceptional ability of KK relations,  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$  deduced from the KK relations may suffer from numerical errors if the numerical procedure of KK relations is not implemented properly. Besides, application of KK relations on the studies of anisotropic crystals such as the wurtzite crystal is problematic. This is because more than one set of dielectric tensor components [i.e., more than one set of  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$ ] may be involved in the formula of the reflectance coefficients for anisotropic crystals, leading to undeterminable parameters (Berreman, 1972; Lekner, 1991). Instead of using the KK relations, one can obtain  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$  using the standard model of dielectric function derived theoretically. Given that the dielectric function of the sample is known, the theoretical reflectance spectrum can be simulated. The best fit of experimental and theoretical spectra with acceptable

tolerance level gives reliable  $\varepsilon'(\nu)$  and  $\varepsilon''(\nu)$ . Moreover, material parameters involved in the calculation of the dielectric function can be simultaneously determined.

To analyze the IR reflectance spectrum of semiconductor, several handy dielectric function models have been developed since a few decades ago. Examples of well-known IR dielectric function models include Drude model (Bustarret et al., 1992), classical harmonic oscillator model (Born, 1959; Kroon, 2007), four-parameter semi-quantum model, which is also known as Gervais's oscillator model (Gervais and Piriou, 1974) and Kukharskii's model (Kukharskii, 1973). The mathematical descriptions of the mentioned dielectric function models will be discussed in Chapter 3. Attribute to the practicality of these established models, valuable information such as the free carrier concentration, mobility, optical phonon frequencies and crystalline quality of semiconductor can be quantitatively deduced from the IR reflectance measurement (Dumelow et al., 1993; Lee et al., 2011b; Misiewicz et al., 1994; Mutschke et al., 1999; Narita et al., 2004). The capability of IR reflectance spectroscopy to determine materials properties makes it holds promise for characterization of semiconductors up till now.

#### **2.4 Surface and interface phonon polaritons (SPhP and IPhP) phenomena**

A material having a negative dielectric function is known as a surface-active medium, which supports the surface mode when it attaches with a surface-inactive medium having a positive dielectric function. SPhP is one type of surface modes resulted from the coupling of IR photon under the p-polarization [transverse magnetic (TM)] field with the phonon localized near the surface of a surface-active medium. The SPhP mode travels along a direction perpendicular to the surface normal and its amplitude attenuates exponentially from the surface to bulk

(Albuquerque and Cottam, 2004; Cottam and Tilley, 1989). In a multilayer system consists of surface-active media, polarization charges exist at both the surface and interfaces. The dissimilar restoring forces of atoms and dissimilar lattice vibrations at the heterointerfaces lead to the existence of both the SPhP and IPhP modes (Agranovich and Mills, 1982; Mills and Maradudin, 1973).

In implementing process of relevant application based on the SPhP or IPhP mode, understanding the elementary factors that significantly influence the SPhP and IPhP modes would be an advantage. Generally, the SPhP and IPhP characteristics of a semiconductor heterostructure can be predicted by simulating the SPhP and IPhP dispersion curves using the corresponding dispersion relation (Borstel and Falge, 1977; Dumelow et al., 1993; Lee et al., 2011a; Mills and Maradudin, 1973). The dispersion relation of the SPhP and IPhP modes in a system with a given number of thin layers can be deduced from the boundary problems of Maxwell's EM wave equations. Formal derivation principle of the dispersion relation of the SPhP and IPhP modes can be referred to works done by Mills and Maradudin (1973), Dumelow et al. (1993), Hamilton et al. (1996) and Lee et al (2011a).

For a two-layer system, the dispersion relation of the SPhP mode can conveniently be derived in a form in which the wavevector component along the interface is explicitly expressed as a function of frequency. For example, the dispersion relation of the SPhP mode for a two-layer system, where the layers are treated to be isotropic, can be expressed as (Borstel and Falge, 1977):

$$K_x = (2\pi\nu) \sqrt{\frac{\epsilon_1 \epsilon_2}{\epsilon_1 + \epsilon_2}}, \quad (2.4)$$

where  $K_x$  is the wavevector of the SPhP travels along the  $x$ -direction. The symbol  $\varepsilon$  represents the dielectric function and the associated subscript represents the layer sequence of the attached media.

For a multilayer system in which the total number of layers is greater than two, however, it is impossible to derive the dispersion relation in an explicit form. Therefore, the dispersion relation of the SPhP and IPhP modes for multilayer system is restricted to an implicit form (Bah et al., 1995; Mills and Maradudin, 1973; Nakayama et al., 1988; Ng et al., 2009b). An example of the dispersion relation of the SPhP and IPhP modes for a three-layer system, where the layers are treated to be isotropic, is given by (Lee et al., 2011b):

$$(\alpha_1\varepsilon_1 + \alpha_0\varepsilon_2)(\alpha_1\varepsilon_3 + \alpha_2\varepsilon_2) - (\alpha_1\varepsilon_1 - \alpha_0\varepsilon_2)(\alpha_1\varepsilon_3 - \alpha_2\varepsilon_2)\exp(-2\alpha_1d) = 0, \quad (2.5)$$

where  $\alpha_{l-1} = [K_x^2 - \varepsilon_l(2\pi\nu)^2]^{1/2}$  and  $l = 1, 2$ , or  $3$ . From Eq. (2.5), it is clear that the implicit dispersion relation of the SPhP and IPhP modes for multilayer system is a transcendental equation, which cannot be solved algebraically. However, solutions of implicit equation, defined within a specified tolerance level, can be evaluated numerically by means of standard numerical root finding procedure.

To reduce the complexity in root finding for implicit equation and to obtain the numerical solutions in the lossless limit, an ideal assumption, namely zero damping, is usually taken (Borstel and Falge, 1977; Dumelow et al., 1990a; Lee et al., 2011d; Marschall and Fischer, 1972; Nakayama et al., 1988). Nevertheless, under certain circumstance, this ideal assumption will result in loss of information in the SPhP and IPhP dispersion curves, hence restricts the prediction of the SPhP and IPhP responses of the studied material (Lee et al., 2011b; Ng et al., 2012). Moreover, the ignorance of damping parameters is expected to induce a discrepancy between the

experimental and theoretical results. Consequently, one subject of interest in this dissertation is to propose a method to calculate the SPhP and IPhP dispersion curves taking into account the effects of damping parameters. The method is described in Chapter 3.

## **2.5 Overview of research on the SPhP and IPhP modes**

Studies of the SPhP and IPhP phenomena have been started since a few decades ago. Early investigations of the SPhP and IPhP phenomena were mostly conducted on the cubic crystal system. For instances, Marschall and Fischer (1972) studied the SPhP mode in gallium phosphide (GaP) crystal. Bryksin et al. (1972; 1974) studied the SPhP modes in calcium fluoride ( $\text{CaF}_2$ ), cadmium fluoride ( $\text{CdF}_2$ ) and several alkali halide crystals. Watanabe et al. (1983) investigated the SPhP mode in zinc telluride (ZnTe) slab. Nakayama et al. (1988; 1990) investigated the SPhP and IPhP modes in GaAs/aluminium arsenide (AlAs) heterostructure on GaAs substrate. Investigations of the SPhP and IPhP modes have also been done on more sophisticated systems such as GaAs/AlAs superlattices (Dumelow et al., 1990b), gratings of GaP thin slabs (Watanabe et al., 1989) and GaAs/AlGaAs multiple quantum well structure (El-Gohary et al., 1989).

Latterly, investigations of the SPhP and IPhP modes were mostly conducted on the hexagonal crystal system, specifically the wurtzite crystal. The SPhP and IPhP modes in the hexagonal crystal system may reveal distinct behaviours as compared to the cubic crystal system. For instance, the virtual SPhP mode may exist in the hexagonal crystal, however, the virtual SPhP mode is always absent in the cubic crystal (Falge and Otto, 1973; Hartstein et al., 1973). Considerable efforts have been done to elucidate the SPhP and IPhP characteristics of ZnO, III-nitrides and their

alloy systems. For instances, Kuroda et al. (2005) studied the SPhP and IPhP modes in wurtzite GaN thin film on sapphire substrate. Zhang and Shi (2009) studied the SPhP and IPhP modes in AlGaN thin film. Valcheva et al. (2009) investigated the SPhP and IPhP modes in InN/AlN heterostructure on sapphire substrate. A number of investigations have been carried out by the research group of Ng et al. on the SPhP and IPhP modes in ZnO and III-nitride-based semiconductor systems (Lee et al., 2011a; 2011b; 2011c; 2011d; Ng et al., 2007; 2008, 2009a; 2010a; 2010b).

Up-to-date, the research trend of the SPhP and IPhP modes is directed toward the exploitation of the SPhP and IPhP characteristics of advanced materials and structures, new characterization technique of the SPhP and IPhP modes and novel device applications based on the SPhP and IPhP modes. For instances, Yan and Bao (2014) theoretically investigated the quasi-one-dimensional rectangular quantum well wire systems consisting of ternary mixed crystals. Kazantsev and Ryssel (2013) demonstrated the mapping of SPhP resonance of a SiC crystal in mid-IR region using apertureless scanning near-field microscope. Dai et al. (2014) applied the IR nano-imaging technique to investigate the properties of SPhP mode in an atomically thin van der Waals crystal, hexagonal boron nitride (BN). Competitive efforts have been done to adapt the resonant behaviour of the SPhP and IPhP modes for near-field radiative heat transfer applications (Biehs et al., 2013; Francoeur et al., 2011; Messina and Ben-Abdallah, 2013).

Despite numerous works have been carried out to comprehend the fundamentals and to exploit potential applications of the SPhP and IPhP modes, there is lack of investigation of the SPhP and IPhP modes in wurtzite semiconductor heterostructures consisting of layers with non-polar and semi-polar planes. Previous investigations of the SPhP and IPhP modes in wurtzite semiconductors were almost

conducted on non-polar *c*-plane samples in which the effect of crystal orientation is trivial (Lee et al., 2011b; Ng et al., 2009b; Torii et al., 2000; Valcheva et al., 2009; Zhang and Shi, 2009). In fact, for a material that does not crystallizes in a cubic structure, the dielectric function strongly depends on the crystal orientation (Bickermann et al., 2005; Engelbrecht and Helbig, 1993; Kazan et al., 2009; Lekner, 1991). In view of the dielectric function is the key parameter to determine the SPhP and IPhP modes, the SPhP and IPhP modes in non-cubic crystal system should undergo changes as crystal orientation varies. To gain an insight into the effects of crystal orientation on the SPhP and IPhP modes, in-depth investigations of the SPhP and IPhP responses of wurtzite III-nitride heterostructures and their relevant substrates with different crystal orientations, are therefore highly demanded.

## **2.6 Summary**

In brief, the descriptions of common IR spectroscopic techniques, the capability of IR reflectance spectroscopy for characterization of semiconductors, and the fundamentals of the SPhP and IPhP phenomena have been reviewed. The history and important issues arose in previous studies as well as the current trend of research on the SPhP and IPhP modes have also been discussed. Throughout this chapter, a general impression of the role of research in the SPhP and IPhP modes has been illustrated.

## CHAPTER 3

### THEORETICAL MODEL

#### 3.1 Introduction

In this chapter, the theoretical models used for the simulation of oblique incidence polarized IR reflectance and ATR spectra of multilayer system consisting of arbitrary oriented hexagonal and/or cubic structured layers is introduced. To have a clear depiction of the theory of reflection, the step-by-step derivation principle of the reflection formula is discussed. Subsequently, method for the simulation of the SPhP and IPhP dispersion curves/spectra taking into account the effects of damping and crystal orientation is presented. To realize all these simulations, the initial approach is to calculate the dielectric tensor components of the studied samples, as described in the latter section.

#### 3.2 IR dielectric function models for semiconductor

This section presents the conventional IR dielectric function models used for describing the IR optical properties of semiconductors. For a doped semiconductor with no IR-active vibrational mode or noble metal, the IR dielectric function can be simply described by the Drude model (Ordal et al., 1983):

$$\varepsilon(\nu) = \varepsilon_{\infty} - \frac{\nu_{po}^2}{\nu^2 + i\nu\gamma_p}, \quad (3.1)$$



where  $\epsilon_\infty$  is the high-frequency dielectric constant,  $\nu_{po}$  is the wavenumber of plasma mode (also known as the plasmon) and  $\gamma_p$  is the plasma damping constant. Occasionally, a similar but slightly different form of the Drude model can be found in the literature (Cleary et al., 2010; Peter and Cardona, 2010):

$$\epsilon(\nu) = \epsilon_\infty - \frac{\epsilon_\infty \nu_p^2}{\nu^2 + i\nu\gamma_p} . \quad (3.2)$$

Numerically,  $\nu_{po}$  in Eq. (3.1) is different as compared to that of  $\nu_p$  in Eq. (3.2). The relationship between  $\nu_{po}$  and  $\nu_p$  is given by  $\nu_p^2 = \nu_{po}^2/\epsilon_\infty$ . However, same name (i.e., plasma mode) is conventionally used to define both  $\nu_{po}$  and  $\nu_p$ , therefore, additional care must be taken in this regard. In particular, the equations used by  $\nu_{po}$  and  $\nu_p$  for the estimation of carrier concentration  $n$ , are different. For Eq. (3.1),  $\nu_{po}$  is related to  $n$  using (Ordal et al., 1983):

$$\nu_{po}^2 = \frac{4\pi e^2 n}{m^*} , \quad (3.3)$$

where  $e$  is the electron charge and  $m^*$  is the electron effective mass (i.e.,  $m^* = \text{effective mass ratio} \times m_e$ ) and  $m_e$  is the electron mass. The permittivity of free space  $\epsilon_0$  is equivalent to  $1/4\pi$  in Gaussian unit. Combining Eq. (3.3) with the expressions  $\nu_p^2 = \nu_{po}^2/\epsilon_\infty$  and  $\epsilon_0 = 1/4\pi$  gives the relation between  $\nu_p$  and  $n$  (Peter and Cardona, 2010):

$$\nu_p^2 = \frac{ne^2}{\epsilon_0 \epsilon_\infty m^*} . \quad (3.4)$$

For an undoped semiconductor or insulator, the IR dielectric function can be described by a classical damped harmonic oscillator model (Born, 1959):

$$\varepsilon(\nu) = \varepsilon_\infty + \sum_g^G \frac{\rho_g \nu_{\text{TO}g}^2}{\nu_{\text{TO}g}^2 - \nu^2 - i\nu\gamma_{\text{TO}g}}, \quad (3.5)$$

where  $\nu_{\text{TO}}$  is the wavenumber of the TO phonon mode,  $\gamma_{\text{TO}}$  is the TO phonon damping constant, and  $\rho$  is the dipole strength.  $G$  and  $g$  are the total number of vibrational modes and the index corresponding to a specific vibrational mode, respectively. The classical damped harmonic oscillator model assumes that the decay mechanism of each LO phonon is tied to that of TO phonon. Gervais and Piriou (1973) have rewritten the oscillator model into a factorized form, named as the four-parameter semi-quantum model (also known as Gervais's oscillator model). The Gervais's oscillator model assumes that the TO and LO phonon damping constants are independent of each other, as given by (Gervais and Piriou, 1974):

$$\varepsilon(\nu) = \varepsilon_\infty \prod_{g=1}^G \left( \frac{\nu_{\text{LO}g}^2 - \nu^2 - i\nu\gamma_{\text{LO}g}}{\nu_{\text{TO}g}^2 - \nu^2 - i\nu\gamma_{\text{TO}g}} \right), \quad (3.6)$$

where  $\nu_{\text{LO}}$  is the wavenumber of the LO phonon mode and  $\gamma_{\text{LO}}$  is the LO phonon damping constant. Eq. (3.6) is applied with a constraint equation, namely, Lowndes's condition  $\sum_g^G (\gamma_{\text{LO}g} - \gamma_{\text{TO}g}) > 0$  to keep the physical meaning of  $\varepsilon(\nu)$  so that the extinction coefficient is always positive [i.e.,  $\varepsilon''(\nu) > 0$ ] (Schubert, 2004).

For a doped semiconductor with IR-active vibrational modes, the IR dielectric function is simply a combination of the oscillator model and the Drude model that is (Dumelow et al., 1993):