

NUMERICAL PREDICTION OF LAMINAR NANOFLUID
FLOW IN RECTANGULAR MICROCHANNEL

SAIDU BELLO ABUBAKAR

UNIVERSITI TEKNOLOGI MALAYSIA

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SAIDU BELLO ABUBAKAR

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Dedicated to my late father

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First and foremost praise is to Allah, the Almighty, on whom ultimately we depend for sustenance and guidance. May His blessings and peace be upon His beloved servant prophet Muhammad (SAW), his household, the four rightly guided companions, other companions and the entire Muslims Ummah.

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ABSTRACT

Numerical simulation of laminar nanofluid flow in Three-dimensional (3D) straight rectangular microchannel heat sink is carried out. In this study the behavior and effect of using pure water and $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ as working fluids in the microchannel are examined. $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ with volume fraction range of 0.4% - 0.8% are used in this simulation to evaluate the cooling performance of microchannel heat sink. Fluent, a Computational Fluid Dynamic (CFD) is used as the solver of simulation. A rectangular microchannel with hydraulic diameter of 86 μm and length of 10mm under the boundary condition of constant heat flux and uniform inlet velocity is set on this analysis. The Results of present work show that using $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ as coolant resulted in to higher efficiency of heat transfer in microchannel heat sink in comparison to Pure water. However, using $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ with 0.8% volume fraction provide a high heat transfer enhancement of 30% as compared to 0.4% and 0.6% volume fractions of the same $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$. Numerical results show that increasing the thermal conductivity of working fluid can enhanced heat transfer. Therefore, it is equally important to note that the presence of nanoparticles could enhance the cooling of MCHS. Meanwhile, higher Nusselt number is found as fluid enters the channel inlet. This could be anticipated as a result of the development of thermal entry region at the channel and the values of Nusselt number tend to stabilize after fully develop region has been achieved.

ABSTRAK

Kajian simulasi berkaitan pengaliran aliran nano (lamina) berdimensi segi empat tepat menerusi penyerap haba saluran mikro dalam Tiga Dimensi (3D) dilakukan. Perubahan dan kesan ketika penggunaan air tulen (suling) dan $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ (bendalir kerja) di dalam saluran mikro ini akan dikaji. Simulasi ini akan mengkaji prestasi penyejukan penyerap haba saluran mikro dengan menggunakan $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ pada julat yang kecil, iaitu diantara 0.4% - 0.8%. Perisian Fluent, Computational Fluid Dynamic (CFD) akan digunakan untuk menjalankan simulasi ini. Analisis ini akan dilakukan pada saluran mikro segi empat tepat dengan dimensi, 86 μm diameter hidraulik dan 10mm panjang pada keadaan sempadan fluks haba yang berterusan dengan halaju seragam. Hasil daripada kajian terkini berkaitan penyerap haba saluran menunjukkan penggunaan $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ sebagai penyejuk akan memberi kesan kecekapan yang lebih tinggi berbanding air tulen (suling) dari segi pemindahan haba. Walau bagaimanapun, penggunaan $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ 0.8% pecahan isipadu akan memberi peningkatan pemindahan haba yang tinggi iaitu sebanyak 30% berbanding 0.4% dan 0.6% pada pecahan jumlah yang sama. Keputusan berangka menunjukkan bahawa peningkatan kekonduksian haba bendalir kerja boleh meningkatkan pemindahan haba. Oleh itu, adalah mustahak untuk mengambil kira kehadiran partikel-partikel nano yang boleh meningkatkan penyejukan MCHS. Sementara itu, bilangan Nusselt yang lebih tinggi telah ditemui ketika bendalir mengalir pada saluran masuk terusan. Ini dapat dijangkakan akibat

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LIST OF ABBREVIATIONS

3D	Three Dimensional
Fe ₃ O ₂ -H ₂ O	Ferrofluid
H ₂ O	Pure water
CAD	Computer Aided Design
CFD	Computational Fluid Dynamic
EG	Ethylene glycol
EO	Engine oil
FVM	Finite Volume Method
GAMBIT	Geometry and Mesh Building Intelligent Toolkit
IC	Integrated Circuit
MCHS	Microchannel heat sinks
VEROS	vacuum evaporation onto a Running oil substrate
VSLI	very large scale integrated

LIST OF SYMBOLS

A	Area
C_p	Specific heat capacity
D_h	Hydraulic Diameter
h	Heat transfer coefficient
H	Height of the microchannel heat sink
H_{ch}	Height of the channel
H_{w1}	Height from bottom surface
H_{w2}	Height from the top Surface
L	Hydraulic length
K	Thermal conductivity
k_{bf}	Thermal conductivity of base fluid
k_p	Thermal conductivity of solid nanoparticle
k_s	Solid thermal conductivity
Nu	Nusselt Number
q''	Heat Flux
Re	Reynolds Number
T	Temperature
T_{in}	Inlet temperature
$V (u,v,w)$	Velocity
W	Microchannel heat sink width
W_{ch}	Channel width
$W_{w1/w2}$	Channel thicknes
Φ	Volume fraction of nanoparticles

Greek Symbols

ρ	Density
μ	Kinematic Viscosity
ϕ	Particle volume fraction

Subscripts

b_f	Base fluid
f	Fluid
in	Inlet
nf	Nanofluid
s	Solid nanoparticle

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CHAPTER 1

INTRODUCTION

1.1 Background of Study

The severe need by user for greater IC speeds, functionality and minimization has fuelled an extraordinary acceleration in chip power dissipation. Amongst all the problems facing by the chip and computer designers is none other than more burning than the soaring levels of power flowing through the integrated circuits. Thermal demands are continuously on the rise. Increasing process speeds (up to 2.5 GHz), decreasing product sizes and styling requirements cause higher and higher heat loads on the products and consequently thermal management is becoming a critical bottleneck to system performance. The National Electronic Technology Roadmap, 1997 has acknowledge the expectation that the Moore' law improvements in the semiconductor technology will continue into the second decade of the 21st century [1]. Due to these enhancements, the chip level heat fluxes have gone up tremendously.

The heat dissipated by silicon chips has increased from 10-15 W/cm² in the year 2000 to 100 W/cm² in the year 2006. High heat fluxes of the order of 10²-10³ W/cm² are also found in opto-electronic equipment, high performance super computers, power devices, electric vehicles and advanced military avionics[2]. As now the thermal design power of the last versions of processors for high performance calculation is about 100-130 W/cm².

These significant developments of power of microprocessors and other electronic components by simultaneous reduction of their surface area contribute to critically high the heat flux generation. An increase in the heating density of these components has been a serious problem affecting the performances and reliability of the electrical devices. The advance cooling technology using microchannels were proposed by [3] for cooling very large scale integrated (VLSI) circuitry. The concept of microchannel heat sink applied in cooling system is important due to high-density electronics packaging requires new advancement in thermal management.

Cooling becomes one of the top technical challenges facing high-tech industries. Since conventional methods of cooling such as forced convection air cooling fails to dissipate away the astronomical volumetric heats from the very small surfaces of electronic chips and circuits, new solution need to be present to overcome these matter. The small physical size of electronic equipment and limitations of air cooling systems have caused an increase of interest in high-performance liquid cooling systems. A liquid coolant is pumped through the microchannels of the heat sink so as to extract the heat from the source such as electronic chip on which it is mounted. In most cases, water is used as a coolant. But water is well known as heat transfer fluids which have low thermal conductivity that greatly limits the heat exchange efficiency. Other base fluids like engine oil and ethylene glycol also have low thermal conductivity.

Promising result was obtained if using nanofluids as a coolant. Nanofluids can be used to improve heat transfer and energy efficiency by addition of solid phase into the base fluid. Nanofluids can be considered to be next generation heat transfer fluids as they offer exciting new possibilities to enhance heat transfer compared to pure liquids. Nanofluids are expected to have superior properties compared to conventional heat transfer fluid.

1.2 Problem Statement

The use of nanofluids as a coolant for microchannel heat sink on semiconductor and electrical field is found out more effective and researches on this application are increasing from time to time. Before nanofluids were first discovered, most of the researches focus on conventional methods of cooling such as forced convection air-cooling and using fin to dissipate away the excessive heats from the microchannel heat sink. Most of the researches focused on the material properties of microchannel heat sink can enhance the heat transfer. There are a few journals and papers discuss about heat transfer mechanism and research on material properties of the microchannel using $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$. This study will focus on heat transfer enhancement Using $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$ in Microchannel.

1.3 Objectives of the Study

Before the research is carried out the objectives of the study has to be defined. However the main objectives regarding this simulation study are:

1. To study the fluid behaviour along the rectangular microchannel
2. To analyse the heat transfer performance in microchannel using $\text{Fe}_3\text{O}_4\text{-H}_2\text{O}$

1.4 Scope of the Project

To achieve the stated Objectives above the scope of this study are limited to the following:

1. The mode of heat transfer is internal forced convection

2. The working fluids in microchannel heat sink consist of pure water and Fe_3O_4 . Using volume fractions 0.4% - 8%
3. Fluid flow and heat transfer are in steady state.
4. Fluid is in single phase and incompressible flows are investigated.
5. The microchannel is in constant diameter, constant shape design and constant heat flux applied.
6. The study covered laminar flow only.
7. The simulation is conducted using FLUENT.

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