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# Measurement of Nucleon-Nucleon Elastic Scattering at Small Angles using the ANKE spectrometer 

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# Measurement of Nucleon-Nucleon Elastic Scattering at Small Angles using the ANKE spectrometer 

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## Abstract

A fundamental understanding of the nucleon-nucleon (NN) interaction is one of the ultimate goals of nuclear and hadron physics. Apart from their intrinsic importance for the study of nuclear forces, NN elastic scattering data are necessary, for example, in the modelling of meson production and other nuclear reactions at intermediate energies.

Quantum chromodynamics, the theory of strong interactions, is not able to determine the NN interaction from first principles because of its non-perturbative nature at intermediate energies (the coupling constants are too strong). Hence, phenomenological approaches are necessary to describe the NN interaction. Partial wave analyses (PWA), such as the ones regularly performed by the SAID (Scattering Analysis Interactive Dial-in) group, have proved to be truly invaluable tools over many years for researchers in this area. These analyses rely on the quantity and quality of the experimental measurements of various proton-proton $(p p)$ and proton-neutron ( $p n$ ) scattering observables at different energies over the full angular ranges.

The goal of many experiments conducted at Cooler Synchrotron (COSY) has been to provide PWA with the precision measurements of NN observables that are essential for these analyses. The experiments presented in this thesis have been carried out within the ANKE collaboration at COSY-Jülich, Germany. Data were obtained using polarised or unpolarised proton beams with kinetic energies from 0.8 GeV up to 2.8 GeV and unpolarised hydrogen or deuterium cluster-jet targets. The detection system of the ANKE spectrometer is the ideal set-up for carrying out refined measurements at the small scattering angles that had not previously been investigated.

The thesis comprises the measurements of the analysing power $A_{y}$ and differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering, and preliminary results for the analysing power $A_{y}$ in the $p n$ quasi-free elastic scattering. These new data close an important gap in the NN database at scattering angles up to $30^{\circ}$ and energies up to 2.8 GeV .

The results obtained are compared to the predictions from the SAID PWA published in 2007 that were based on data from earlier experiments. The impact of the present results is demonstrated by the significant changes in the low partial waves of the updated SAID PWA, which includes the new ANKE measurements as well as the existing global data.

## Zusammenfassung

Ein fundamentales Verständnis der Nukleon-Nukleon (NN) Wechselwirkung ist eines der wichtigsten Ziele der Kern- und Hadronenphysik. Neben ihrer zentralen Bedeutung für die Erforschung der Kernkräfte, sind Daten für elastische NN Streuung erforderlich, zum Beispiel bei der Modellierung von Mesonproduktion und anderen Kernreaktionen bei mittleren Energien.

Die Theorie der starken Wechselwirkung, Quantenchromodynamik, ist nicht in der Lage, die NN Wechselwirkung ab initio zu bestimmen, wegen der nichtstörungstheoretischen Natur bei mittleren Energien (die Kopplungskonstante ist zu stark). Daher sind phänomenologische Ansätze notwendig, die NN Wechselwirkung zu beschreiben. Partialwellenanalysen (PWA), z.B. jene, die regelmäßig von der SAID (Scattering Anlysis Interactive Dial-in) Gruppe durchgeführt werden, haben sich als wirklich wertvolle Werkzeuge für Forscher in diesem Bereich erwiesen. Eine solche Analyse hängt stark ab von der Quantität und Qualität der experimentellen Messungen verschiedener Observablen von Proton-Proton ( $p p$ ) und Proton-Neutron ( $p n$ ) Streuung bei verschiedenen Energien und über den gesamten Winkelbereich.

Das Ziel vieler Experimente, die am Cooler Synchrotron (COSY) durchgeführt werden, ist, PWA mit den grundlegenden Präzisionsmessungen von NN Observablen zur Verfügung zu stellen. Die Experimente dieser Arbeit wurden an COSYJülich von der ANKE Kollaboration durchgeführt. Für die Messungen wurden polarisierte oder unpolarisierte Protonenstrahlen und unpolarisierter Wasserstoff oder Deuterium als Clusterjet-Target benutzt. Das Detektionssystem des ANKESpektrometer ist die ideale Einrichtung für präzise Messungen bei kleinen Streuwinkeln, die bisher nicht untersucht worden sind.

Die Dissertation beinhaltet die Messungen der Analysierstärke $A_{y}$ und differentiellen Wirkungsquerschnitte $d \sigma / d \Omega$ in der $p p$ elastischen Streuung und die vorläufigen Ergebnisse für die Analysierstärke $A_{y}$ in $p n$ quasi-freier elastischer Streuung. Diese neuen genauen Daten schließen eine wichtige Lücke in der NN Datenbank bei kleinen Streuwinkeln bis zu $30^{\circ}$ und Energien bis zu 2.8 GeV .

Die erhaltenen Ergebnisse werden verglichen mit den SAID 2007 PWA, die auf Daten aus früheren Experimenten beruhen. Die Auswirkungen der vorliegenden Ergebnisse in Gestalt von signifikanten Veränderungen in den niedrigen Partialwellen der aktualisierten SAID PWA werden demonstriert.

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 sбscmotol - PWA) Usäys mjonon. SAID (Scattering Analysis Interactive Dial-in)

























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To my wonderful parents,
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## Abbreviations

| SM | Standard Model |
| :--- | :--- |
| PSA | Phase Shift Analysis |
| PWA | Partial Wave Analysis |
| QCD | Quantum ChromoDynamics |
| SAID | Scattering Analysis Interactive Dial-in |
| COSY | COoler SYnchroton |
| ANKE | Apparatus for Studies of Nucleon and Kaon Ejectiles |
| EDDA | Excitation Function Data Acquisition |
|  | Designed for Analysis of Phase Shifts |
| STT | Silicon Tracking Telescope |
| FD | Forward Detector |
| MWPC | MultiWire Proportional Chamber |
| MWDC | MultiWire Drift Chamber |
| LEP | Low Energy Polarimeter |
| BCT | Beam Current Transformer |
| RF | Radio Frequency |
| PM | PhotoMultiplier |
| ANL | Argonne National Laboratory |
| LNPI | Leningrad Nuclear Physics Institute |

## Chapter 1

## Introduction

What are the fundamental blocks of matter? How did the universe evolve just after the Big Bang? What are the mechanisms behind the various interactions? There is a wealth of fundamental questions with profound significance for our understanding of Nature and the structure of matter of which we and our universe are composed. Answering many of these questions lies at the heart of nuclear science.

One of the key moments for nuclear physics was the Geiger-Marsden experiment (also known as the Rutherford gold foil experiment) that showed how profoundly our understanding of the matter can be changed via a simple scattering experiment. Since then many increasingly sophisticated scattering experiments have been performed and we have learned a lot about the fundamental particles, but there are still many questions that we need to seek answer to.

The first two sections of this chapter will provide a short overview of the structure of matter, as we understand it today, and a short historical overwiew of our insight into the structure of the nucleon. The following sections describe the importance of the nucleon-nucleon scattering in general and the motivation of the experimental investigations, described in this dissertation.

### 1.1 Structure of matter

Our perception of the structure of matter has changed many times during the history and most rapidly since the end of the $19^{\text {th }}$ century, when atoms were still thought to be the most basic, indivisible building blocks of matter, to the latter
half of the $20^{\text {th }}$ century, when all known subatomic particles were organised within the Standard Model (SM).


Figure 1.1: The Standard Model of elementary particles (schematic depiction), with the three generations of matter in the first three columns, gauge bosons in the fourth column, and the Higgs boson in the fifth [1].

The Standard Model (SM) is the quantum field theory that describes all different kinds of interactions (except gravity, for which a quantum field theoretical description has not been achieved yet) and classifies the elementary particles. The elementary particles constituting the ordinary matter are the fundamental fermions (half-integer spin particles), namely quarks and leptons; the gauge bosons (integerspin particles) mediate forces, while Higgs boson is responsible for the intrinsic mass of particles. The schematic depiction of SM elementary particles, with the three generations of matter, the Higgs and gauge bosons, is given in Figure 1.1.

The four fundamental forces are: the gravitational, electromagnetic, weak and strong forces. Even though weak and strong interactions are short ranged and hence were left unnoticed for a long time, nowadays we know their important role in the existence of matter. The weak force is involved in radioactivity, causing unstable atomic nuclei to decay, and plays important role in powering the sun's thermonuclear process. The strong interaction is responsible for holding quarks together, and consequently binding protons and neutrons into stable nuclei.

### 1.1.1 Structure of the nucleon: historical overview

Nucleons (protons and neutrons) are the lowest-energy bound states of quarks and gluons. They represent the simplest form of observable matter and comprise more than $99 \%$ of the mass of the visible universe. Most of these nucleons are in the core of atoms, the same atoms that everything we see on the daily basis is made from, including ourselves. So it comes as no surprise that nucleons have been studied with such a scrutiny during the last century.

Rutherford has started to use the word "proton" for the hydrogen nuclei after the first reported nuclear reaction ${ }^{14} N+\alpha \rightarrow{ }^{17} O+p$ was observed and protons were identified as part of all nuclei. However, it was only after the discovery of neutron by James Chadwick in 1932 that the basic structure of nuclei and nuclear isotopes could be understood. Nevertheless, the nucleons were thought to be elementary particles not for long: already in 1933 first glimpse of an internal structure of the nucleon was observed, when magnetic moments of protons and neutrons were measured. In 1964 Gell-Mann [2] and, independently, Zweig [3] proposed a theory that nucleons are composed of point like particles called quarks. These quarks were postulated to have spin $-1 / 2$, a fractional electric charge, and came in different types called flavours. Soon after the electron scattering experiment that showed that nucleons are indeed composed of quarks took place at the Stanford Linear Accelerator Centre (SLAC) [4, 5]. Combinations of different flavours of quarks comprise baryons (built up from three quarks) and mesons (a quark and an antiquark). These two groups of particles are categorized as hadrons.

Quantum Chromodynamics (QCD), the gauge field theory of the strong interaction, describes the interaction of quarks through the exchange of massless vector gauge bosons, the gluons. QCD follows the formalism of Quantum Electrodynamics (QED), which has a coupling constant $a$ that describes the strength of the electromagnetic interaction. The underlying $\mathrm{SU}(3)$ gauge structure, rather than the simple $\mathrm{U}(1)$ of QED, implies many analogies, but also basic new features. The carriers of the strong force are 8 massless gluons in analogy to the photon for the electromagnetic force. An important new aspect is that the gluons, carrying a new quantum number called colour, can interact with each other.

As a consequence of the gluon self-coupling, QCD implies that the coupling strength $\alpha_{s}$, the analogue to the fine structure constant $\alpha$ in QED, becomes large at large distances, or equivalently, at low momentum transfers. Therefore, QCD provides a qualitative reason for the observation that quarks do not appear as free particles
but only exist as bound states of quarks, forming hadrons. Quarks carry one out of three different colour charges: red, blue and green, while hadrons are colourless bound states. The gluons also carry the colour charge and therefore can interact with each other.

QCD does not predict the actual value of $\alpha_{s}$. For large momentum transfers Q, however, it determines the functional form of the energy dependence of $\alpha_{s}$, illustrated in Figure 1.2. While an increasingly large coupling at small energy scales leads to the confinement of quarks and gluons inside hadrons, the coupling becomes small at high-energy or short-distance reactions; quarks and gluons are said to be asymptotically free [6].


Figure 1.2: The value of the "running" coupling constant $\alpha_{s}$, as a function of the energy scale E. The curve that slopes downwards is a prediction of the asymptomatic freedom in QCD, while the empty circles show the measurements that have been made [7].

At high energies a perturbative approach can be taken in the mathematical description of the interactions, with $\alpha_{s}$ as the expansion parameter. This kinematic regime is called perturbative QCD or just pQCD, and theoretical predictions can be well tested by experiments. However at lower energies the coupling constant becomes larger, and perturbative calculations no longer work. Therefore the force description in this energy range relies on the phenomenological approach. The experimental data of high quality and precision at low and intermediate energy are necessary for the full understanding of the strong interaction.

### 1.2 Nucleon-nucleon scattering

The nucleon-nucleon (NN) interaction is the prototype for the action of the nuclear forces. Data on NN scattering are necessary ingredients, not only for the understanding of nuclear forces, but also for the description of meson production and other nuclear reactions at intermediate energies.

The scattering amplitudes for the complete description of the NN interaction can be reconstructed from the phase shift analysis (PSA). It has proved to be a truly invaluable tool over many years for researchers working in this area. For an interpretation of the results obtained in this work, they will be compared to the most recently published $[8]$ and modified calculations from the SAID (Scattering Analysis Interactive Dial-in) partial wave analysis (PWA) [9, 10]. The SAID facility is based at George Washington University, Washington DC, USA. It maintains a database which contains the world data on NN scattering among other reactions, and provides predictions from PWA of the data. Such an analysis is based on the measurement of various NN scattering observables at different energies over the full angular range.

Unpolarised experiments provide information only about the averaged spin effects. This means that a certain amount of information is being lost. Since strong interaction is spin-dependent, it is crucial to conduct polarised experiments to separate the spin-specific parts of interaction. The polarised experiments provide additional information on reaction mechanisms, indespensable for the partial wave analysis.

### 1.2.1 EDDA's legacy

It should be pointed out that the COSY-EDDA collaboration (Excitation function Data acquisition Designed for Analysis of phase shifts) have provided a perfect example of how polarised data have completely revolutionised partial wave analysis.

The data on the differential cross section in $p p$ elastic scattering [11] were taken in a continuous ramp of the proton beam energy from 0.24 to 2.58 GeV using the $\mathrm{CH}_{2}$ fibre target. Prior to the EDDA measurements, SAID solution was only valid up to 1.6 GeV . With more than 2000 points EDDA data completely dominated the SAID database above about 1 GeV .

EDDA collaboration has also made contributions in spin-dependent measurements: the data points were produced for the proton analysing power using the unpolarised
beam between 0.44 and 2.49 GeV incident on a polarised hydrogen target [12, 13]. In addition, $p p$ spin correlations were studied in the same energy range [14]. However, due to the design of the EDDA detector, the experiments only extended over the central region of centre-of-mass (c.m.) angles, $30^{\circ} \lesssim \theta_{c m} \lesssim 150^{\circ}$.

### 1.3 Synopsis of the thesis work

Many accelerators around the world included the NN study into their research program, however even after many years of studies, there are still many gaps in our knowledge. As one can see in the Figure 1.3, even in the data base of the most basic reaction of proton-proton elastic scattering, there has been a significant gap at the small angles $\left(\theta_{c m}<30^{\circ}\right)$ above 1 GeV . The situation is much worse for the isoscalar $I=0$ case of proton-neutron scattering (Figure 1.4).


Figure 1.3: Abundance plots of c.m. scattering angle $\left(\theta_{c m}\right)$ versus beam kinetic energy ( $T_{l a b}$ ) for experiments on the analysing power $A_{y}$ (left) and for crosssection $d \sigma / d \Omega$ (right) in proton-proton elastic scattering [15].

The precision data at small angles have a potential to significantly influence PSA. Adding to the NN scattering data base was one of the major priorities of the ANKE collaboration. This thesis comprises data gathered over three ANKE experiments, dedicated to the understanding of NN scattering:

- the proton-proton elastic scattering studies
- analysing power $A_{y}$ in proton-proton elastic scattering using unpolarised hydrogen cluster target and polarised proton beam at six energies between 0.796 and 2.4 GeV ;


Figure 1.4: Abundance plot of c.m. scattering angle $\left(\theta_{c m}\right)$ versus beam kinetic energy $\left(T_{l a b}\right)$ for experiments on the analysing power $A_{y}$ in proton-neutron scattering [15].

- unpolarised differential cross sections $d \sigma / d \Omega$ at eight beam kinetic energies between 1.0 and 2.8 GeV .
- The proton-neutron quasi-elastic scattering study
- analysing power $A_{y}$ using unpolarised deuterium cluster target and polarised proton beam at six energies between 0.796 and 2.4 GeV .

While high-quality $p p$ data from ANKE close a very important gap at small angles, proton-neutron $(p n)$ data are a crucial contribution to the very incomplete $p n$ data base.

The outline of the remainder of this thesis is as follows: Chapter 2 describes the common formalism of the polarised experiments, on which the following chapters will be based. In Chapter 3 the experimental setup for the ANKE experiments is introduced. Chapter 4 gives a detailed description of the data analysis and obtained results for the analysing power in $\vec{p} p$ elastic scattering. In Chapter 5 the specifics of the cross section measurements in $p p$ elastic scattering are described. Chapter 6 presents the data analysis performed on proton-neutron quasi elastic scattering and preliminary results. The concluding remarks are presented in Chapter 7.

## Chapter 2

## Formalism in polarised experiments

Polarisation physics represents the section of physics devoted to investigate the statistical and dynamical characteristics of processes associated with spin, which is one of the fundamental characteristics of elementary particles and nuclei. The spin is a tool to investigate and test fundamental questions. Performing the unpolarised cross section measurements for non-zero spin particles implies that in the description and experimentally there is summing over initial-channel and averaging over final-channel spin states. This means that a certain amount of information is being lost.

In this chapter a short overview of the formalism necessary to investigate the spinspecific parts of nucleon-nucleon (NN) interaction is given. Namely, important aspects of polarised experiments necessary to extract the spin observables, and a method to reduce the systematic errors. Within this thesis, only interactions of $1 / 2$ spin particles are studied, hence only this simple case of $1 / 2$ spin particle scattering is described in the following.

### 2.1 Polarisation formalism

Quantum mechanics deals with statistical statements about the result of measurements on an ensemble of states (particles, beams, targets). In other words: by giving an expectation value of operators it provides probability amplitudes for the result of a measurement on an ensemble.

There are two limiting cases. One is the pure state, that is our knowledge of the system is complete, e.g. when all members of an ensemble are in the same spin
state. A special case is the spin state of a single particle, which is always completely polarised. In general, our knowledge of a system is incomplete and can only be described by superposition of such pure states, weighted with the probability of their occurrence in this superposition. Such a state is called a mixed state. The appropriate and also practical description of such states is by using the density operator $\rho$ :

$$
\begin{equation*}
\rho=\sum_{i} p_{i}\left|\psi^{i}\right\rangle\left\langle\psi^{i}\right|, \tag{2.1}
\end{equation*}
$$

where $p_{i}$ is the probability of finding the ensemble in a quantum mechanical state characterised by $\left|\psi^{i}\right\rangle$. A pure state is represented by the density matrix:

$$
\rho=\left(\begin{array}{ll}
1 & 0  \tag{2.2}\\
0 & 0
\end{array}\right) .
$$

A completely unpolarised beam with all spin substates equally occupied has the density matrix

$$
\rho=1 / 2\left(\begin{array}{ll}
1 & 0  \tag{2.3}\\
0 & 1
\end{array}\right)=1 / 2\left[\left(\begin{array}{ll}
1 & 0 \\
0 & 0
\end{array}\right)+\left(\begin{array}{ll}
0 & 0 \\
0 & 1
\end{array}\right)\right] .
$$

This corresponds to superposition of pure states with equal weights of $1 / 2$. A general beam can be interpreted as a superposition of the two pure states defined with respect to the quantization axis with the contributions $N_{+}$and $N_{-}$:

$$
\rho=N_{+}\left(\begin{array}{ll}
1 & 0  \tag{2.4}\\
0 & 0
\end{array}\right)+N_{-}\left(\begin{array}{ll}
0 & 0 \\
0 & 1
\end{array}\right)=\left(\begin{array}{cc}
N_{+} & 0 \\
0 & N_{-}
\end{array}\right) .
$$

The vector polarisation of a spin $1 / 2$ system has form:

$$
\begin{equation*}
P=\frac{N_{+}-N_{-}}{N_{+}+N_{-}} \tag{2.5}
\end{equation*}
$$

### 2.1.1 $\operatorname{Spin}$ structure $1 / 2+1 / 2 \rightarrow 1 / 2+1 / 2$

Formalism of elastic scattering of the systems with spin structure $1 / 2+1 / 2 \rightarrow$ $1 / 2+1 / 2$, including the NN scattering, is described in detail in References [16] and [17]. In principle, there are 255 possible polarisation observables for this spin system + unpolarised differential cross section. However, for elastic scattering, parity conservation and time-reversal invariance will reduce this number to 25 for identical particles, for example $p p$ scattering, and to 36 linearly independent
experiments for non-identical particles, such as $p n$ scattering. Nucleon-nucleon scattering matrix $M$ is presented as

$$
\begin{array}{r}
M\left(k_{f}, k_{i}\right)=\frac{1}{2}\left\{(a+b)+(a-b)\left(\sigma_{\mathbf{1}}, \mathbf{n}\right)\left(\sigma_{\mathbf{2}}, \mathbf{n}\right)+\right.  \tag{2.6}\\
\left.+(c+d)\left(\sigma_{\mathbf{1}}, \mathbf{m}\right)\left(\sigma_{\mathbf{2}}, \mathbf{m}\right)+(\mathbf{c}-\mathbf{d})\left(\sigma_{\mathbf{1}}, \mathbf{l}\right)\left(\sigma_{\mathbf{2}}, \mathbf{l}\right)+\mathbf{e}\left(\sigma_{\mathbf{1}}+\sigma_{\mathbf{2}}, \mathbf{n}\right)\right\}
\end{array}
$$

here the amplitudes $a, b, c, d$, and $e$ are complex functions of two variables: energy in c.m. and the scattering angle. $\mathbf{l}, \mathbf{m}$, and $\mathbf{n}$ are the c.m. basis vectors:

$$
\begin{equation*}
\mathbf{l}=\frac{\mathbf{k}_{\mathbf{f}}+\mathbf{k}_{\mathbf{i}}}{\left|\mathbf{k}_{\mathbf{f}}+\mathbf{k}_{\mathbf{i}}\right|}, \mathbf{m}=\frac{\mathbf{k}_{\mathbf{f}}-\mathbf{k}_{\mathbf{i}}}{\left|\mathbf{k}_{\mathbf{f}}-\mathbf{k}_{\mathbf{i}}\right|}, \mathbf{n}=\frac{\mathbf{k}_{\mathbf{f}} \times \mathbf{k}_{\mathbf{i}}}{\left|\mathbf{k}_{\mathbf{f}} \times \mathbf{k}_{\mathbf{i}}\right|} . \tag{2.7}
\end{equation*}
$$

whereas $\sigma_{1}$ and $\sigma_{\mathbf{2}}$ are Pauli matrices. After considering parity conservation, timereversal invariance and the Pauli principle, there are $N=5$ invariant, independent complex amplitudes in $p p$ scattering, and $N=6$ in $n p$ scattering. Thus in a complete experiment $2 N-1$ real quantities have to be measured by at least as many independent experiments: 9 for $p p$ and 11 for $n p$ [18].

### 2.1.2 Coordinate system

For polarised experiments the appropriate definition of coordinate system is very important. In unpolarised reactions incoming and outgoing particle momenta define the scattering plane. A polarisation vector adds another direction, introducing an azimuthal dependence of observables. Suitable coordinate systems have been agreed upon in two international conventions on polarisation phenomena in nuclear reactions, in Basel [19] and in Madison [20]. A cartesian coordinate system is formed with z along the incident beam momentum $\mathbf{k}_{\mathbf{i}}, y$ along $\mathbf{k}_{\mathbf{i}} \times \mathbf{k}_{\mathbf{f}}$ where $\mathbf{k}_{\mathbf{f}}$ is the scattered particle momentum, and $x$ such as to define a right-handed coordinate system. Let's define $\mathbf{i}, \mathbf{j}$ and $\mathbf{k}$ unit vectors pointing along the $x, y$ and $z$ coordinate axes respectively. So, $\mathbf{k}=\mathbf{k}_{\mathbf{i}} / k_{i}, \mathbf{j} \|\left(\mathbf{k}_{\mathbf{i}} \times \mathbf{k}_{\mathbf{f}}\right)$, and $\mathbf{i} \|(\mathbf{k} \times \mathbf{j})$.

The unit vector pointing along the spin quantization axis is denoted by $\mathbf{S}$; its direction is defined in terms of $\beta$, the angle between $\mathbf{S}$ and beam direction, and $\phi$, the angle between its projection on $x y$ plane and the $y$ axis. In this system, the scattering is always in the $x z$ plane, and the momentum vector of the scattered particle lies in the $x z$ half-plane with positive $x$. The so-called "up" direction is defined by the transverse component of the spin quantization axis: $\mathbf{S}_{\perp}=\mathbf{S}-(\mathbf{S} \cdot \mathbf{k}) \mathbf{k}$. Hence, according to an observer who is looking along the beam direction and is aligned


Figure 2.1: Madison convention for the definition of the coordinate system in the polarised experiments. The $z$ axis is along the incident beam momentum, while the scattering is in the $x z$ plane. The spin quantization axis $\mathbf{S}$ is defined in terms of $\beta$, the angle between $\mathbf{S}$ and beam direction, $z$-axis, and $\phi$, the angle between its projection on $x y$ plane and the $y$ axis.
with the "up" direction, the scattering (positive $x$ half-plane of $x z$ plane) is to the left, if the $y$ axis is along $\mathbf{S}_{\perp}\left(\phi=0^{\circ}\right)$. Correspondingly, if $\phi=180^{\circ}, \phi=270^{\circ}$ and $\phi=90^{\circ}$, then the scattering is to the right, up and down, respectively.

### 2.2 Spin observables

Although the spin observables depend only on a polar angle, the cross section including these observables generally exhibit also a dependence on the azimuthal angle. This dependence enters via the need to introduce a coordinate system in which the detector positions, as well as the polarisation direction, have to be described. The cross section for a polarised beam of spin $1 / 2$ particles is

$$
\begin{equation*}
\sigma(\theta, \phi)=\sigma_{0}(\theta)\left[1+P_{y} A_{y}(\theta)\right] \tag{2.8}
\end{equation*}
$$

where $\sigma_{0}(\theta)$ is the cross section for the scattering of an unpolarised beam at the scattering angle $\theta, A_{y}(\theta)$ is the analysing power of the reaction at the same angle and $P_{y}$ is the $y$ component of the beam polarisation:

$$
\begin{equation*}
P_{y}=\mathbf{P} \cdot \mathbf{j} \equiv \mathbf{P} \sin \beta \cos \phi \equiv \mathbf{P}_{\perp} \mathbf{\operatorname { c o s }} \phi, \tag{2.9}
\end{equation*}
$$

where $\mathbf{P}$ is the beam polarisation, $\mathbf{j}$ is unit vector along the $y$ axis, and $P_{\perp}$ is the component of beam polarisation perpendicular to its direction of motion. Since in
our experiment we have a transversely polarised beam, we assume $\beta \approx 90^{\circ}$. Hence the difference between $P_{\perp}$ and $P$ is neglected, and we set $P_{\perp} \equiv P$.
The Madison convention implies that for spin $1 / 2$ particles the polarisation should be counted positive in the direction $\left(\mathbf{k}_{\mathbf{i}} \times \mathbf{k}_{\mathbf{f}}\right)$. Assuming a positive analysing power, this positive polarisation yields a positive left-right (L-R) asymmetry.

### 2.3 Cross-ratio method

Many sources of systematic uncertainties in the determination of the analysing power $A_{y}$ can be neglected in the first order in case of left-right symmetrical arrangement of the detection system [21]. Let us consider symmetric two detector system, depicted in Figure 2.2. The actual number of counts recorded in a detector is

$$
\begin{equation*}
N(\theta, \phi)=n N_{t} \Omega E \sigma(\theta, \phi), \tag{2.10}
\end{equation*}
$$

where $n$ is the number of particles incident on the target, $N_{t}$ is the number of target nuclei per cubic centimetre, $\Omega$ is a geometrical factor, defined by the detector, i.e. the solid angle subtended by the detector, and E is the detector efficiency. It is allowed that the solid angle factor, as well as the efficiency of detector 1 are different from those of detector 2. Therefore, Equation 2.10 for each detector will look like

$$
\begin{align*}
& N_{1}(\theta, \phi)=n N_{t} \Omega_{1} E_{1} \sigma_{0}(\theta)\left[1+P_{y} A_{y}(\theta) \cos \phi\right],  \tag{2.11}\\
& N_{2}(\theta, \phi)=n N_{t} \Omega_{1} E_{2} \sigma_{0}(\theta)\left[1+P_{y} A_{y}(\theta) \cos \phi\right] . \tag{2.12}
\end{align*}
$$

In Figure 2.2 beam polarisation direction "up" is depicted coming out of paper in red. In this case, detector 1 detects particles, that are scattered to the "left" ( $\phi=0^{\circ}$ ) and detector 2 gets particles that are scattered to the "right" $\left(\phi=180^{\circ}\right)$. Therefore,

$$
\begin{align*}
\left.N_{1}(\theta, 0)\right) & \equiv N_{1}^{\uparrow}  \tag{2.13}\\
N_{2}(\theta, \pi) & \equiv L_{1}=n N_{t} \Omega_{1} E_{1} \sigma_{0}(\theta)\left[1+P_{y} A_{y}(\theta)\right]  \tag{2.14}\\
& \equiv R_{2}=n N_{t} \Omega_{1} E_{2} \sigma_{0}(\theta)\left[1-P_{y} A_{y}(\theta)\right] .
\end{align*}
$$

If we now "flip" the polarisation $\mathbf{P} \rightarrow-\mathbf{P}$, the spin direction will be going into the paper (depicted in green). This is referred to as beam polarisation "down", and in


Figure 2.2: The idealistic symmetric arrangement of the two-detector system.. The two cases of beam polarisation are shown: "up" in red and "down" in green. The corresponding counts of particles scattered to the detectors are described in text.
this case detector 1 will be on the right and detector 2 on the left side.

$$
\begin{gather*}
N_{1}(\theta, \pi) \equiv N_{1}^{\downarrow} \equiv R_{1}=n^{\prime} N_{t}^{\prime} \Omega_{1} E_{1} \sigma_{0}(\theta)\left[1-P_{y} A_{y}(\theta)\right]  \tag{2.15}\\
N_{2}(\theta, 0) \equiv N_{2}^{\downarrow} \equiv L_{2}=n^{\prime} N_{t}^{\prime} \Omega_{1} E_{2} \sigma_{0}(\theta)\left[1+P_{y} A_{y}(\theta)\right] . \tag{2.16}
\end{gather*}
$$

Primes are used to indicate that the integrated charge and the effective target thickness may be not the same for the two runs. We can form geometrical means of number of particles scattered to the left $L \equiv \sqrt{L_{1} L_{2}}$ and particles scattered to the right $R \equiv \sqrt{R_{1} R_{2}}$.

$$
\begin{align*}
& L=\left[n n^{\prime} N N^{\prime} \Omega_{1} \Omega_{2} E_{1} E_{2}\right]^{\frac{1}{2}} \sigma_{0}\left[1+P A_{y}(\theta)\right],  \tag{2.17}\\
& R=\left[n n^{\prime} N N^{\prime} \Omega_{1} \Omega_{2} E_{1} E_{2}\right]^{\frac{1}{2}} \sigma_{0}\left[1-P A_{y}(\theta)\right] . \tag{2.18}
\end{align*}
$$

We can solve for $P A_{y}(\theta)$ and get the left-right assymetry $\varepsilon$

$$
\begin{equation*}
\varepsilon=\frac{L-R}{L+R}=\frac{2 P A_{y}\left[n n^{\prime} N N^{\prime} \Omega_{1} \Omega_{2} E_{1} E_{2}\right]^{\frac{1}{2}} \sigma_{0}}{2\left[n n^{\prime} N N^{\prime} \Omega_{1} \Omega_{2} E_{1} E_{2}\right]^{\frac{1}{2}} \sigma_{0}}=P A_{y}(\theta), \tag{2.19}
\end{equation*}
$$

which is independent of the relative detector efficiencies $\left(E_{1}, E_{2}\right)$, solid angles $\left(\Omega_{1}, \Omega_{2}\right)$, relative integrated charge ( $n n^{\prime}$ ) and target thickness variations. ( $N N^{\prime}$ ). $n$ and $N$, quantities common to the two channels, can be averaged over the data acquisition time (in one run), while $E$ and $\Omega$, quantities different in the two channels, must not vary with time [21]. We can define the geometric mean of the
number of particles detected by detector 1 in two runs as $N_{1}$ :

$$
\begin{equation*}
N_{1} \equiv \sqrt{L_{1} R_{1}}=\Omega_{1} E_{1} \sigma_{0}(\theta) N N^{\prime} n n^{\prime}\left[1-\left(P A_{y}\right)^{2}\right]^{\frac{1}{2}} \tag{2.20}
\end{equation*}
$$

and for particles detected by detector 2 we have

$$
\begin{equation*}
N_{2} \equiv \sqrt{L_{2} R_{2}}=\Omega_{2} E_{2} \sigma_{0}(\theta) N N^{\prime} n n^{\prime}\left[1-\left(P A_{y}\right)^{2}\right]^{\frac{1}{2}} . \tag{2.21}
\end{equation*}
$$

Monitoring on the ratio

$$
\begin{equation*}
\frac{N_{1}}{N_{2}}=\frac{\Omega_{1} E_{1}}{\Omega_{2} E_{2}} \tag{2.22}
\end{equation*}
$$

provides the check on the performance of the apparatus; this variable is required to be constant in time if the asymmetry determination is to be accurate. The statistical error associated with a measurement of the asymmetry $\varepsilon$ is given by the means of geometrical means $L$ and $R$ :

$$
\begin{equation*}
\delta \varepsilon=\sqrt{\frac{1-\varepsilon^{2}}{L+R}} \tag{2.23}
\end{equation*}
$$

## Chapter 3

## Experimental setup

All the results presented in this thesis, have been obtained using the data gathered at the ANKE spectrometer at COSY-Jülich. COSY facility with the polarised ion source are introduced in the Sections 3.1 and 3.1.1. Even though the COSY facility includes many experimental possibilities, this chapter includes the description of only those experimental equipments that have been actively used in the described experiments. Namely, the EDDA polarimeter and ANKE spectrometer are discussed in Sections 3.2 and 3.3 respectively. Finally, an overview of the different experimental conditions, under which the present data have been acquired, is given in Section 3.4.

### 3.1 COSY facility

The COSY accelerator and storage ring, shown schematically in Figure 3.1, serves the quests of the fundamental research in the Institute of Nuclear Physics of Jülich research centre (Forschungszentrum Jülich). The name COoler SYnchrotron (COSY) refers to the two phase space cooling mechanisms integrated in the ring. A beam with a momentum below $0.6 \mathrm{GeV} / \mathrm{c}$ can be cooled with the electron cooler [22, 23]. The stochastic cooler is used to manipulate the beam above a momentum of $1.5 \mathrm{GeV} / \mathrm{c}$ [24]. The acceleration process of the COSY beam consists of several stages. Negative ion sources can produce unpolarised and polarised hydrogen and deuterium ions, which are then accelerated by JULIC cyclotron up to $300 \mathrm{MeV} / c$ for $H^{-}$and up to $600 \mathrm{MeV} / c$ for $D^{-}$. These pre-accelerated ions are stripped off their electrons and the remaining protons or deuterons are injected in COSY ring with 183.4 m circumference, here particles can be accelerated and
stored at any momentum in the range from $300 \mathrm{MeV} / c$ to $3.65 \mathrm{GeV} / c$ [25]. At the injection beamline, the Low Energy Polarimeter (LEP) can provide a polarisation measurement of the beam generated by the polarised ion source.


Figure 3.1: The COSY accelerator facility at Forschungszentrum Jülich. The positions of the ANKE spectrometer and the EDDA polarimeter at the ring are shown. In the bottom of the figure the sources providing polarised and unpolarised protons (or deuterons), the cyclotron that accelerates the particles to the injection energy and the Low Energy (LE) Polarimeter can be seen.

Transversely polarised proton beams are available with intensities up to $1 \cdot 10^{10}$ particles with a polarisation up to $70 \%$. For deuterons an intensity of $3 \cdot 10^{10}$ with vector and tensor polarisation of more than $70 \%$ and $50 \%$ were achieved respectively. The two 40 m long straight sections are designed to serve the internal experiments. Figure 3.1 demonstrates the COSY accelerator facility with the
positions of the ANKE spectrometer and the EDDA polarimeter, used during the experiments that are subject of this thesis.

### 3.1.1 Polarised ion source at COSY

The polarised ion source at COSY consists of three groups of components: the pulsed atomic beam source, the caesium beam source, and the charge-exchange and extraction region [26]. The schematic layout of the setup is shown in Figure 3.2. The use of atomic hydrogen allows one to take advantage of the large magnetic moment of the electron. The nuclear spin, in turn, is affected by its coupling to the electron [27].


Figure 3.2: Setup of the polarised ion source at COSY [28]. The negatively charged ions are produced in a charge exchange process between a neutral nuclear polarised hydrogen beam and a fast neutral cesium beam.

The neutral polarised hydrogen $H^{0}$ beam is produced in the atomic beam source, consisting of RF dissociator and a sextupole separation magnet. First, the gas molecules are dissociated in a RF discharge (300-400 W) and a high degree of dissociation is maintained by adding small amounts of nitrogen and oxygen that reduces surface and volume recombination. The atoms are cooled to about 30 K by passing through an aluminium nozzle of 20 mm length and 3 mm diameter. By slowing down the atoms, the acceptance of the hexapole system and dwell time in the charge-exchange are increased. The first sextupole magnet produces electron state polarisation by defocusing atoms with the electron spin state $m_{j}=-1 / 2$. Remaining beam of atoms with $m_{j}=+1 / 2$ is then focused by the second sextupole
magnet. The nuclear polarisation is provided by two RF transitions switching between the hyperfine substates of the hydrogen atoms [29].

Afterwards, the atomic $\vec{H}^{0}$ beam with now high nuclear polarisation collides with the fast neutral caesium (Cs) beam. Thanks to the significantly higher electronegativity, a hydrogen atom acquires an additional electron from a caesium atom, and becomes negatively charged, according to

$$
\begin{equation*}
\vec{H}^{0}+C s^{0} \longrightarrow \vec{H}^{-}+C s^{+} \tag{3.1}
\end{equation*}
$$

The fast $\mathrm{Cs}^{0}$ beam, needed for the abovementioned reaction, is produced in two steps. First, Cs vapor is thermally ionized on a hot $\left(1200^{\circ}\right)$ porous tungsten surface at an appropriate beam potential of about $40-60 \mathrm{kV}$, where the cross section for the charge-exchange reaction has its maximum. Second, the beam is focused by a quadropole triplet to a neutraliser that consists of caesium oven, a cell filled with caesium vapour, and a magnetically driven flapper valve between the oven and the cell. The remaining $\mathrm{Cs}^{+}$beam is deflected in front of the solenoid into a Faraday cup, while the fat neutralised caesium atoms enter the charge-exchange region. A neutraliser efficiency is typically over $90 \%$.

In the charge exchange region the nuclear polarisation is preserved by the longitudinal magnetic field. A small electrostatic gradient field guides the very slow $H^{-}$ions to the extraction orifice, where they are deflected by a $90^{\circ}$ electrostatic toroidal deflector into the injection beamline of the cyclotron. In the final stage, a Wien filter separates the $H^{-}$ions from electrons and other background. The Wien filter is rotatable around the beam axis, providing any orientation of the polarisation vector. In order to avoid the polarisation loss during the acceleration, spin orientation parallel to that of cyclotron magnetic field is chosen[30].

### 3.1.2 Depolarising resonances at COSY

This section is dedicated to the description of the difficulties in the acceleration of the polarised proton beam. For an ideal planar closed-loop accelerator with a vertical guide field, the particle spin vector precesses around the vertical axis. In this way the vertical beam polarisation is preserved. The spin motion in an external electromagnetic field is governed by the Thomas-BMT equation, leading to a spin tune $\nu_{s p}=\gamma G$, which describes the number of spin precessions of the central beam per revolution in the ring. $G$ is the anomalous magnetic moment of
the particle ( $G=1.7928$ for protons, -0.1423 for deuterons), and $\gamma=E / m$ is the Lorentz factor. During the acceleration of a vertically polarised beam, depolarising resonances are crossed if the precession frequency of the spin $\gamma G$ is equal to the frequency of the encountered spin-perturbing magnetic fields. In a strong-focusing synchrotron like COSY, two different types of strong depolarising resonances are excited, namely imperfection resonances caused by magnetic field errors and misalignments of the magnets, and intrinsic resonances excited by horizontal fields due to the vertical focusing [31].

In the momentum range of COSY, five imperfection resonances have to be crossed for protons. The existing correction dipoles of COSY are utilised to overcome all imperfection resonances by exciting adiabatic spin flips without polarisation losses. The number of intrinsic resonances depends on the superperiodicity of the lattice. The magnetic structure of COSY allows one to choose a superperiodicity of $P=2$ or 6 . A tune-jump system consisting of two fast quadrupoles has been developed especially to handle intrinsic resonances at COSY [32].

The imperfection resonances for protons in the momentum range of COSY are listed in Table 3.1. They are crossed during acceleration, if the number of spin precessions per revolution of the particles in the ring is an integer $(\gamma G=k, k$ is integer). The resonance strength depends on the vertical closed orbit deviation.

| $\gamma G$ | $T_{p}$ <br> GeV | $p$ <br> $\mathrm{GeV} / c$ | $y_{c o}^{r m s}$ <br> mm | $\epsilon_{r}$ <br> $10^{-3}$ | $P_{f} / P_{i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 0.1084 | 0.4638 | 2.3 | 0.95 | -1.00 |
| 3 | 0.6318 | 1.2587 | 1.8 | 0.61 | -0.88 |
| 4 | 1.1551 | 1.8712 | 1.6 | 0.96 | -1.00 |
| 5 | 1.6785 | 2.4426 | 1.6 | 0.90 | -1.00 |
| 6 | 2.2018 | 2.9964 | 1.4 | 0.46 | -0.58 |

Table 3.1: Resonance strength $\epsilon_{r}$ and the ratio of preserved polarisation $P_{f} / P_{i}$ at imperfection resonances for a typical vertical orbit deviation $y_{c o}^{r m s}$, without considering synchrotron oscillation.

A spin flip occurs at all resonances if synchrotron oscillations are not considered. However, the influence of synchrotron oscillation during resonance crossing cannot be neglected. After the first imperfection resonance, the calculated polarisation with a momentum spread of $\Delta p / p=1 \times 10^{-3}$ and a synchrotron frequency of $f_{\text {syn }}=450 \mathrm{~Hz}$ is about $P_{f} / P_{i} \approx-0.85$. The resonance strength of the first imperfection resonance has to be enhanced to $\epsilon_{r}=1.6 \times 10^{-3}$ to excite spin flips with polarisation losses of less than $1 \%$. At the other imperfection resonances the effect
of synchrotron oscillation is smaller, due to the lower momentum spread at higher energies. Vertical correction dipoles or a partial Siberian snake could be used to preserve polarisation at imperfection resonances by exciting adiabatic spin flips. Simulations indicate that an excitation of the vertical orbit with existing correction dipoles by 1 mrad is sufficient to adiabatically flip the spin at all imperfection resonances. In addition, the solenoids of the electron-cooler system inside COSY are available for use as a partial snake. They are able to rotate the spin around the longitudinal axis by about $8^{\circ}$ at the maximum momentum of COSY. A rotation angle of less than $1^{\circ}$ of the spin around the longitudinal axis already leads to a spin flip without polarisation losses at all five imperfection resonances [33]. The number of intrinsic resonances depends on the superperiodicity $P$ of the lattice, which is given by the number of identical periods in the accelerator. The COSY ring consists of two $180^{\circ}$ arc sections connected by straight sections. The straight sections can be tuned as telescopes with 1:1 imaging, giving a $2 \pi$ betatron phase advance. In this case the straight sections are optically transparent and the arcs contribute to the strength of intrinsic resonances. One then obtains for the resonance condition $\gamma G=k \times P \pm\left(Q_{y}-2\right)$, where $k$ is an integer and $Q_{y}$ is the vertical betatron tune. The magnetic structure in the arcs allows adjustment of the superperiodicity to $P=2$ or 6 . The corresponding intrinsic resonances in the momentum range of COSY are listed in Table 3.2.

| $P$ | $\gamma G$ | $T_{p}$ <br> MeV | $p$ <br> $\mathrm{MeV} / c$ | $\epsilon_{r}$ <br> $10^{-3}$ |
| :---: | :---: | :---: | :---: | :---: |
| 2 | $6-Q_{y}$ | 312.4 | 826.9 | 0.26 |
| 2 | $0+Q_{y}$ | 950.7 | 1639.3 | 0.21 |
| 2,6 | $8-Q_{y}$ | 1358.8 | 2096.5 | 1.57 |
| 2 | $2+Q_{y}$ | 1997.1 | 2781.2 | 0.53 |
| 2 | $10-Q_{y}$ | 2405.2 | 3208.9 | 0.25 |

Table 3.2: Resonance strength $\epsilon_{r}$ of intrinsic resonances for a normalized emittance of $1 \pi \mathrm{~mm}$ mrad and vertical betatron tune of $Q_{y}=3.61$ for different superperiodicities $P$.

### 3.2 EDDA polarimeter

Even though the polarisation of the beam is measured at the injection via Low Energy Polarimeter (LEP), it is important to control the polarisation of the beam after it goes through all the depolarisation resonances and reaches the flattop (constant kinetic energy). This was achieved via EDDA measurements during the last 20 seconds at the end of the every cycle.

The EDDA experiment was initially conceived to provide high precision $p p$ elastic scattering data in the COSY energy range ( $0.5-2.5 \mathrm{GeV}$ ), but later has been modified to be used as the internal polarimeter. The EDDA-polarimeter is comprised of the $7 \mu m$ diameter carbon fibre target and $2 \times 29$ semi-ring scintillators that intercept protons within the polar angle range from $11.1^{\circ}$ to $42.7^{\circ}$ in the laboratory coordinate system (Appendix A) [12].


Figure 3.3: The schematic layout of the full EDDA detector setup (left) and photo (right) of the EDDA polarimeter.

The outside layer consists of a series of rings that wrap around the bars and each intercepts a narrow range of scattering angles from the target. The stripped-down version of the EDDA detector used as a polarimeter at COSY does not include the bars. It was calibrated during the EDDA data-taking periods against the full detector setup. As demonstrated in Figure 3.3, the rings (R) are split into left and right halves. Each half is connected to a light guide and single photomultiplier tube. The triggers are generated for each of the solid semiring-shaped scintillators, signal from which were counted in the so-called scalers. The time-marking system uses a precise clock to provide time for each event trigger. These times are stored and passed to the event processing software. The scaler rates are then read out separately for each ring and the two spin directions, and making use of the cross-ratio method, and known ring effective analysing powers [34], the beam polarisation is calculated. See the details in Section 4.1.

### 3.3 ANKE spectrometer

The Apparatus for Studies of Nucleon and Kaon Ejectiles (ANKE) is an internal experiment in one of the straight section of COSY. It consists of the magnetic system (three dipole magnets), unpolarised hydrogen or deuteron cluster-jet target, and different detection systems, from which we have mostly used for this experiment only Forward Detector (FD) and Silicon Tracking Telescopes (STTs). In Figure 3.4 only those parts of the spectrometer are shown that are relevant for this experiment.


Figure 3.4: The ANKE spectrometer setup (top view), showing the positions of the hydrogen cluster-jet target, the silicon tracking telescopes (STT), and the forward detector (FD).

The main purpose of the ANKE magnetic system is to separate the ejectiles from the circulating COSY beam in order to identify them and analyse their momentum. The first dipole magnet D1 deflects the circulating beam by an angle $\alpha$ off its straight path onto the target; the spectrometer dipole magnet D2 (beam deflection $-2 \alpha)$ separates the produced particles from the beam for momentum analysis; finally D3, identical to D1, leads the unscattered beam particles back onto the normal orbit [35]. The deflection angle of the beam can be adjusted to optimise the magnetic field up to 1.56 T independent of the COSY beam momentum.

### 3.3.1 Unpolarised cluster-jet target

For the ANKE experiments target with thickness of $10^{13}$ to $10^{15} \mathrm{atoms} / \mathrm{cm}^{2}$ is typically used. For experiments that require unpolarised targets, it is provided by
cluster-jet target device, shown in Figure 3.5. It consists of three main parts: the cluster-jet source, the scattering chamber, and the cluster-jet beam dump [36].


Figure 3.5: The cluster-jet target installed at ANKE.
Figure 3.6 illustrates the schematic overview of the cluster production process. The hydrogen or deuterion gas at pressures of 18 bar is cooled down to temperatures of $20-30 \mathrm{~K}$ and pressed through a Laval nozzle. Adiabatic expansion of the cooled beam further cools down the beam and the oversaturated gas spontaneously condensates to clusters with typical size of $10^{3}-10^{4}$ atoms. Even though the chosen temperature, pressure and nozzle geometry have already been optimized, only a small part of used gas forms clusters. Hence the skimmer (an opening of $700 \mu \mathrm{~m}$ ) is used to separate the cluster jet from the surrounding gas. The final shape of the cluster jet is defined by a second opening, collimator. Finally, the cluster beam is separated from the residual gas by a skimmer.

The scattering (analysing) chamber is equipped with a scanning rod with a thickness of 1.0 mm which is controlled by a stepper-motor and can be positioned in


Figure 3.6: Cluster production process in a Laval-nozzle. The cluster-jet beam is extracted and shaped using the skimmer. Note the exaggerated scale, the opening of the skimmer is only $700 \mu \mathrm{~m}$.
units of $1 / 24 \mathrm{~mm}$. When the rod is placed inside the cluster beam, a part of the beam is stopped and converted into a gas load which can be recorded by an ionization vacuum meter. In that way information on the cluster beam size and position can be obtained. Furthermore, if the rod is places at a fixed position inside the cluster beam, this system allows the density of the beam to be monitored.

The part of the cluster-jet beam, which does not interact with the COSY beam, is collected in the beam dump. It consists of three cryopumps and one turbo molecular pump mounted at the end.

### 3.3.2 Forward Detector (FD)

Forward Detector (FD) is located in the gap of 1.6 m between the D2 and D3 dipole magnets. The closeness of the FD part to the COSY beam pipe introduces the requirement for the system to operate at rather high counting rates of $10^{5} \mathrm{~s}^{-1}$ and more.

The FD comprises two multiwire proportional (MWPC) and one drift chamber (MWDC) as well as a two-plane scintillation hodoscope. The information from MWPC and MWDC chambers are used for track reconstruction at ANKE. The existence of the strong magnetic field of the D 2 ensures a good spatial separation of tracks with different mass-to-charge ( $m / q$ ) ratio. Using the hit information from different layers of the MWPC and MWDC and the geometrical position of the target, tracks are found from the overall fit procedure. Details on the trackfinding algorithm and the track-reconstruction software can be found in [37] [38].

The MWPCs have four wire planes each, with two horizontally (X) and two vertically ( Y ) aligned wires as well as two-strip planes, which are inclined by $\pm 30^{\circ}$ with respect to the wires. High spatial resolution of less than 1 mm is required from the Multiwire Proportional Chambers (MWPCs), in order to achieve momentum resolution of about $1 \%$, which is essential for distinguishing proton-proton pairs with low excitation energy.

The forward hodoscope is composed of two planes of vertically aligned scintillators from polystyrene. The first and second planes contain 8 and 9 scintillators, respectively. In each plane, counters that are placed close to the COSY beam pipe, have smaller thickness ( 15 mm ) and width (varying between 40 and 60 mm ), compared to those responsible for lower momentum region ( 20 mm thick, 80 mm wide). The height of all scintillators is 360 mm . Each of the scintillators is read out by two photomultiplier tubes placed on both ends. They provide timing as well as the amplitude signal. The timing signal can be used to form a trigger and also to measure the differences of the arrival times of particle pairs. A typical time resolution for events with two registered particles is around 0.5 ns . The amplitude signal from photomultipliers provides information about the energy loss in the scintillator, which can be measured with $10 \%$ accuracy [39].

### 3.3.3 Silicon Tracking Telescopes (STT)

Two Silicon Tracking Telescopes are placed inside the vacuum chamber in a $\phi$ symmetric (left-right) arrangement close to the beam-target overlap (schematically shown in Figure 3.4). Each STT consists of three individual double-sided silicon strip detectors of different thickness. The basic configuration has a $65 \mu \mathrm{~m}$ first layer, a $300 \mu \mathrm{~m}$ second layer and to ensure stopping of protons with kinetic energy up to 40 MeV , a third layer of $5100 \mu \mathrm{~m}$ thickness. The first layer is placed 28 mm from the centre of the beam pipe. The distance between the two first layers is set to 20 mm . The photograph of the STT detectors, along with the cooling system and front-end read-out electronics, is given in Figure 3.7.

Measuring the energy losses in the individual layers of the telescope allows the identification of stopped particle by the $\Delta E / E$ method. From the Bethe-Bloch formula, it can be seen that the energy loss in matter depends on the charge ze and the velocity of the incident particle $v=\beta c$.

$$
\begin{equation*}
-\frac{d E}{d x}=\frac{4 \pi}{m_{e} c^{2}} \frac{n z^{2}}{\beta^{2}}\left(\frac{e^{2}}{4 \pi \varepsilon_{0}}\right)^{2}\left[\ln \left(\frac{2 m_{e} c^{2} \beta^{2}}{I\left(1-\beta^{2}\right)}\right)-\beta^{2}\right], \tag{3.2}
\end{equation*}
$$



Figure 3.7: Photo of a Silicon Tracking Telescope (STT), including the cooling system and read-out electronics.
where $E$ is energy of the particle; $x$ is the distance travelled by the particle; and $m_{e}$ is mass of the electron; $n$ is electron density of the target; $I$ is the mean ionisation energy of the target; while $\varepsilon_{0}$ is the vacuum permittivity.

Therefore, these energy losses in the layers are specific to the particle type. Ratio of energy losses with the total energy of the particle is used to identify the particles. The minimum energy of a reconstructed particle is given by the thickness of the most inner layer. It will be detected as soon as it passes through the inner layer and in the second layer [40]. This corresponds to minimum energy of 2.5 MeV for protons. The setup was built in a $\phi$-symmetric (left-right) arrangement to make use of the cross-ratio method. This configuration fulfils the requirement of particle identification together with a precise energy determination (1-5\%) and tracking with vertex resolution of 1 mm over a wide range. The time resolution of the setup is less than 1 ns.

### 3.4 Experimental conditions

This thesis comprises data gathered over three dedicated experiments.

- Objective: analysing power $A_{y}(\theta)$ in proton-proton elastic scattering
- Beam: polarised proton beam;
- Target: unpolarised hydrogen cluster target;
- Data gathered by: EDDA, ANKE STT, ANKE FD;
- Beam Energies: $T_{p}=0.796,1.6,1.8,1.965,2.157$, and 2.368 GeV ;
- Angular range: $4^{\circ}-30^{\circ}$.
- Objective: unpolarised differential cross section in proton-proton elastic scattering $d \sigma / d \Omega$
- Beam: unpolarised proton beam;
- Target: unpolarised hydrogen cluster target;
- Data gathered by: ANKE FD, Schottky spectrum analyser;
- Beam Energies: $T_{p}=1.0,1.6,1.8,2.0,2.2,2.4,2.6$, and 2.8 GeV ;
- Angular range: $12^{\circ}-30^{\circ}$.
- Objective: analysing power $A_{y}(\theta)$ in proton-neutron quasi-free elastic scattering
- Beam: polarised proton beam;
- Target: unpolarised deuterium cluster target;
- Data gathered by: EDDA, ANKE STT, ANKE FD;
- Beam Energies: $T_{p}=0.796,1.6,1.8,1.965,2.157$, and 2.368 GeV ;
- Angular range: $13^{\circ}-30^{\circ}$.


## Chapter 4

## Analysing power in proton-proton elastic scattering

The investigations of the analysing power $A_{y}$ in proton-proton ( $\overrightarrow{p p}$ ) elastic scattering were motivated by the lack of experimental data at small angles above 1 GeV (Figure 1.3). The $\vec{p} p$ experiment at ANKE was carried out using polarised proton beam at six energies, $T_{p}=0.796,1.6,1.8,1.965,2.157$, and 2.368 GeV . The determination of the analysing power $A_{y}(\theta)$ as the function of the scattering polar angle requires the measurement of the scattered particles asymmetry $\varepsilon(\theta)$ and the beam polarisation value $P$ :

$$
\begin{equation*}
\varepsilon(\theta) \propto P A_{y}(\theta) \tag{4.1}
\end{equation*}
$$

While asymmetry $\varepsilon(\theta)$ was calculated using the ANKE detection systems (STT and FD), the beam polarisation $P$ was measured using the EDDA detector. The beam polarisation mode was changed every subsequent cycle to take the maximum advantage of the cross-ratio method, described in Section 2.3. Cycles of 180 s or 300 s duration were used for each spin mode, with the last 20 s of each cycle being reserved for the measurement of the beam polarisation with the EDDA detector. The details on the beam polarisation measurement are provided in Section 4.1, while the asymmetry determination using the STT and FD are given in Section 4.2. Finally, the results of the analysing power in $\vec{p} p$ elastic scattering are discussed in Section 4.4.

### 4.1 Beam polarisation measurement using EDDA

The absolute values of the beam polarisations were measured by the EDDA polarimeter for the first time in the ANKE beam time in 2013. The EDDA carbon fibre target was moved into the beam for the last 20 seconds of every cycle, and scaler counts were recorded. The carbon target effectively consumes all the beam, hence it could not be used before the ANKE measurement of asymmetry in a cycle.

Originally, the EDDA detector was equipped with a polarised atomic hydrogen target, and had been used to measure the $p \vec{p}$ analysing power over almost the whole COSY energy range [12] [13]. By studying further the scattering of polarised protons on C and $\mathrm{CH}_{2}$ targets, it was possible to deduce the quasi-free analysing power of the carbon.

The beam polarisation in our experiment has been determined based on the asymmetry $\varepsilon\left(\theta_{\text {lab }}\right)$ and effective carbon analysing powers $A_{n}^{e f f}(C)$ in quasi-elastic scattering of the protons on carbon-bound nuclear protons. These effective analysing power values were taken from the dedicated studies in 2000 at EDDA-COSY [34].

The asymmetry term $\varepsilon\left(\theta_{l a b}\right)$ was calculated via the cross-ratio method (Equation 2.19), using the rates in the semi-rings placed to the left and right of the beam. It was possible to compare left and right count rates for each polar angle $\theta_{l a b}$ range, corresponding to the semi-ring (Appendix A), while averaging over azimuthal angle $\phi$ range. Thus, the asymmetry term for each polar angle range has form:

$$
\begin{equation*}
\left\langle\varepsilon\left(\theta_{l a b}\right)\right\rangle=\left\langle P A_{y}\left(\theta_{l a b}\right) \cos \phi\right\rangle \approx \frac{2}{\pi} P A_{y}\left(\theta_{l a b}\right) . \tag{4.2}
\end{equation*}
$$

We can deduce the beam polarisation $P$ from $\varepsilon\left(\theta_{\text {lab }}\right)$ in an EDDA ring:

$$
\begin{equation*}
P_{\theta_{l a b}} \approx \frac{\varepsilon\left(\theta_{l a b}\right)}{A_{e f f}\left(\theta_{l a b}\right)}, \tag{4.3}
\end{equation*}
$$

where $A_{\text {eff }}$ is the effective analysing power, values for which are taken from [34]

$$
\begin{equation*}
A_{e f f}\left(\theta_{l a b}\right)=\frac{2}{\pi} A_{y}\left(\theta_{l a b}\right) \tag{4.4}
\end{equation*}
$$

The polarisation values calculated from the count asymmetry in every ring are shown in Figure 4.1 as the function of the corresponding scattering polar angle in the laboratory coordinate system. The beam polarisation $P$, obviously, does not
depend of the scattering angle $\theta_{\text {lab }}$, at which we are performing the measurement. In order to decrease the statistical uncertainty of $P$ we take advantage of this independence and form the weighted average of all $P_{\theta_{l a b}}$ as a final result for $P$.


Figure 4.1: The polarisation values, calculated ring by ring, are shown versus corresponding laboratory polar angles (according to Appendix A). The sample plots are shown for beam kinetic energies $T_{p}=1.8 \mathrm{GeV}$ and $T_{p}=2.157 \mathrm{GeV}$.

The weighted averages over time and polar angle of the beam polarisations determined at the six energies are given in Table 4.1. The changes in sign reflect the number of spin flips required to pass through the imperfection resonances, described in detail in Section 3.1.2. It should be noted that each of the six beams was prepared independently and, for this reason, the magnitude of the polarisation may not decrease monotonically as more resonances are crossed.

| $T_{p}(\mathrm{GeV})$ | 0.796 | 1.6 | 1.8 | 1.965 | 2.157 | 2.368 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $P$ | 0.554 | 0.504 | -0.508 | -0.429 | -0.501 | 0.435 |
| $\Delta P$ | $\pm 0.008$ | $\pm 0.003$ | $\pm 0.011$ | $\pm 0.008$ | $\pm 0.010$ | $\pm 0.015$ |

Table 4.1: The values of the mean polarisations $P$ determined with the EDDA polarimeter averaged over all the data at the beam energy $T_{p}$. Only statistical errors are given in the table.

Consistent results were achieved with the EDDA polarimeter after the short (180 s) and long ( 300 s ) cycles. As expected, it implies that beam polarisation is not lost at flattop (constant beam energy) over a COSY cycle. However, due to the nonzero dispersion combined with the energy loss of the beam caused by its passage through the target, the settings at the three lowest energies gradually degrade slightly. This effect was taken into account in the analysis.

### 4.1.1 Beam polarisation uncertainty

The variation of the beam polarisation values among the cycles at any given energy was checked using EDDA with various selections and combinations of the cycles. All the studies yield the consistent results within the uncertainties at every given energy. The variation of the beam polarisation values was also checked with the asymmetry of the counts in the STT in various cycles and found to be around 0.04 (RMS).

Besides the statitical errors, shown in Table 4.1, the uncertainty of the effective carbon analysing powers should be taken into account. In the studies of the $\mathrm{CH}_{2}$ and C targets for the fast beam polarisation, the systematic error for the $A_{\text {eff }}$, unfortunately, could be estimated only very roughly from the change of polarisation values during the calibration procedure. Unlike $\mathrm{CH}_{2}$ target, C target is free of additional systematic errors occuring due to the aging of the target (loss of hydrogen ions in the interaction with beam protons). The value for the systematic uncertainty of the carbon effective analysing powers was estimated in [34] to be $3 \%$.

### 4.2 Asymmetry measurement using ANKE

### 4.2.1 Event selection by STT

The analysis of the scattered particles, detected in the STT, is based on the software, developed mainly by G. Macharshvili. It includes the codes for reconstructing tracks, using energy deposited in the layers of the STT as well as the neural network method, and is described in detail in Reference [41].

Tracks were reconstructed starting from the hits in the second layer. The STT trigger requested a minimum energy deposit in the second layer of either telescope. Combinations of these hits with the hits in the first layer have been considered. If the reconstructed track hits the inside the ellipse of beam-target overlay in the $z y$ plane (at $x=0$ ), then it is stored.

In general, the hit from the third layer is also added to the reconstructed track in case it is inside the $20^{\circ}$ cone along the track with the apex at the second layer hit. The cone opening angle corresponds to the maximum angle of multiple scattering.

The third layer hit does not change a track geometry, it is used only to fulfil the energy deposit information.

In some cases a possible track might be missing a hit in the first or second layer due to possible vicinity to the energy threshold or inactive segments. In order to increase the efficiency of the track reconstruction, in these cases energy deposits for the first or second layers were added to the energy loss sum in the correspondence to the missing hit, assuming $\Delta E_{2}=5 \Delta E_{1}$ or $\Delta E_{1}=0.2 \Delta E_{2}$ [42].

The greater precision in the angle of the recoiling proton is achieved by deducing it from the energy measured in the telescope rather than from a direct angular measurement. The Figure 4.2 demonstrates the difference between the angle reconstructed from the energy of the scattered particle and directly measured scattering angle of the track. Even though it is not possible to judge directly from Figure 4.2 the contribution of each angle to the distribution, the simulation shows that about $80 \%$ of the width of the distribution comes from the directly measured scattering angle of the track.


Figure 4.2: Difference between the directly measured angle of the track $\theta$ and the angle reconstructed from the energy $\theta(E)$. The example plot is shown at $T_{p}$ $=2.368 \mathrm{GeV}$.

The protons with energies below 30 MeV were completely stopped in three layers of the STT. Furthermore, it is also possible to deduce the energy of punch-through protons up to 90 MeV . Thus expanding considerably the angular coverage of the telescope. For this purpose, the kinetic energy of these energetic protons was defined through a comparison of the angles and energy deposits in all three layers with simulated data using a neural network approach. The relative uncertainty
was defined during the network training procedure [43] and is equal to $2 \%$ at 30 MeV and $4 \%$ at 90 MeV .

There is very little ambiguity in the isolation of the proton peak in the missing mass spectra of the selected STT events (Figure 4.3).


Figure 4.3: Missing mass $M_{X}(p p \rightarrow p X)$ spectrum obtained for the beam energy of $T_{p}=1.6 \mathrm{GeV}$, showing the clear proton peak when detecting one proton in the STT.

### 4.2.2 Asymmetry measurement using STT

The left-right symmetry of ANKE STTs, along with the reversal of the beam polarisation every subsequent cycle allowed us to use the cross-ratio method, described in the Section 2.3. The left-right asymmetry of the protons scattered to the STTs in each polar angle interval is calculated as

$$
\begin{equation*}
\varepsilon(\theta)=\frac{L(\theta)-R(\theta)}{L(\theta)+R(\theta)} \tag{4.5}
\end{equation*}
$$

where $L(\theta)$ and $R(\theta)$ are the geometrical means of number of particles scattered in the given polar angle interval to the left $L=\sqrt{N_{1}^{\uparrow} N_{2}^{\downarrow}}$ and to the right $R=\sqrt{N_{1}^{\downarrow} N_{2}^{\uparrow}}$ in respect to the beam polarisation (Figure 2.2). As was shown previously, the scattering asymmetry is related to the analysing power $A_{y}(\theta)$ for each value of the scattering angle $\theta$ through

$$
\begin{equation*}
\varepsilon(\theta)=A_{y}(\theta) P\langle\cos \phi\rangle . \tag{4.6}
\end{equation*}
$$

The $\phi$ acceptances for the left and right STTs differ only slightly: $\langle\cos \phi\rangle_{1}=$ $0.9663 \pm 0.0005$ and $\langle\cos \phi\rangle_{2}=0.9670 \pm 0.0003$. The simulation showed that even larger difference between $\langle\cos \phi\rangle_{1}$ and $\langle\cos \phi\rangle_{2}$ would not affect the measured asymmetry. Therefore, we assume that $\phi$ acceptances of the detectors are the same and in our calculations $\langle\cos \phi\rangle \approx 0.9666$ can be used.

### 4.2.3 Event selection by FD

Scattered particles, which pass through the vacuum chamber of the D2 magnet and leave it through the forward exit window, are detected in the FD. The analysis is based on the software, developed mainly by S . Dymov. It includes the codes for finding tracks and reconstructing particle momenta and is described in detail in Reference [37].

The precision of the momentum and angle reconstruction is directly related to the accuracy of the ANKE geometry measurement. Positions and sizes of various parts of the ANKE spectrometer are well defined and fixed, but there are some parameters in the track reconstruction software that change from one experiment to another and it is not possible to measure them directly with enough precision. Uncertainties in these parameters shift the reconstructed particle momenta and consequently result in shifts in the missing mass spectra. Therefore, these parameters should be calibrated for every experiment individually.

The setup parameters are adjusted using the kinematics of different reactions. For every iteration of the fitted parameters, the program reconstructs tracks from scratch and looks at the displacement of the missing masses from their nominal values for every reaction. After the geometry adjustment, the hit coordinates and the time of flight are used for the final track reconstruction. The energy loss cut for elastic proton identification is relevant only at the 0.796 GeV beam energy, where the forward going deuterons from the $p p \rightarrow d \pi^{+}$have the momenta close to that of the $p p$ elastic protons. After the applied cuts the admixture of those deuterons does not exceed $0.02 \%$.

The number of elastic protons was determined from the missing mass spectra after subtracting a linear background from the peak in each angular bin. Typical missing mass spectrum is shown in Figure 4.4.

The setup acceptance was defined from GEANT simulation, followed by the same track and momentum reconstruction procedures that were applied to the data.


Figure 4.4: Missing mass $M_{X}(p p \rightarrow p X)$ spectrum obtained from the particles detected in the forward detector at the beam kinetic energy of 1.6 GeV .

Although the final results were obtained without further restriction on the $\phi$ range, estimations done with several $\phi$ cuts showed no change beyond the statistical fluctuations. The angular acceptance at $T_{p}=1.6 \mathrm{GeV}$ is shown in Fig. 4.5 and it looks rather similar at the other energies [44].


Figure 4.5: Forward detector angular acceptance for $p p \rightarrow p p$ at the beam kinetic energy of 1.6 GeV .

### 4.2.4 Asymmetry measurement using FD

The absence of the left-right symmetry in the Forward Detector does not permit the use of the cross-ratio method to determine the asymmetry. Therefore, the
analysing power can only be defined from the asymmetry of the count rates for the two states of the beam polarisation. In this case the asymmetry is introduced as

$$
\begin{equation*}
\varepsilon(\theta)=\frac{N_{\uparrow}(\theta) / L_{\uparrow}-N_{\downarrow}(\theta) / L_{\downarrow}}{N_{\uparrow}(\theta) / L_{\uparrow}+N_{\downarrow}(\theta) / L_{\downarrow}} \tag{4.7}
\end{equation*}
$$

in terms of the luminosity-normalised numbers of counts for the two orientations of the beam polarisation $N_{\uparrow}(\theta) / L_{\uparrow}$ and $N_{\downarrow}(\theta) / L_{\downarrow}$, or

$$
\begin{equation*}
\varepsilon(\theta)=\frac{N_{\uparrow}(\theta)-N_{\downarrow}(\theta) / L_{\text {rel }}}{N_{\uparrow}(\theta)+N_{\downarrow}(\theta) / L_{r e l}} \tag{4.8}
\end{equation*}
$$

in terms of the relative luminosity factors $L_{r e l}=L_{\uparrow} / L_{\downarrow}$. These factors were fixed by comparing the rates of charged particle production in angular regions where the beam polarisation could play no part [45].

The luminosity calibration data, which corresponded generally to the inelastic events involving pion production, were selected by applying cuts either on the small polar angles $\theta$ or on the azimuthal angle $\phi$ near $\pm 90^{\circ}$. In Figure. 4.6 three groups of events with the decreasing level of cut tightness are shown:
i) $\theta<0.5^{\circ},||\phi|-90|<5^{\circ}$
ii) $\theta<1^{\circ}$, $||\phi|-90|<10^{\circ}$
iii) $\theta<2^{\circ},||\phi|-90|<20^{\circ}$.


Figure 4.6: Relative luminosities obtained with various angular cuts (shown at horizontal axis) at $T_{p}=1.8 \mathrm{GeV}$. Only a small section of the vertical scale is shown to emphasise the small differences.

Figure. 4.6 illustrates the relative luminosities at the sample energy $T_{p}=1.8$ GeV , but the distributions look similar at the other energies. Luminosity ratios in the three group of cuts are consistent within the statistical uncertainty. For the calculation of the asymmetry, the average value of the relative luminosity factors, gained from the abovementioned cuts, was used as the normalisation factor in Equation 4.8.

### 4.3 Sources of the systematic uncertainties

The cross-ratio method allows one to eliminate first order systematic errors that arise from misalignments between the left and right STTs. Other systematic errors for the asymmetry obtained using the STT, such as those arising from differences in the magnitudes of the up and down polarisations, also cancel in the first order. Nevertheless, the systematic uncertainties of the STT data were investigated further to the higher order by varying all the inputs to the reasonable levels, and observing the possible change in the asymmetry. The data gained using the FD lack these advantages and rely on the correct normalisation with the relative luminosities. The three groups of angular cuts, described previously, yielded consistent results within statistical errors. As a result, it is estimated the systematic uncertainty of $A_{y}$ due to the normalisation procedure does not exceed $0.3 \%$.

### 4.3.1 Difference in polarisation values for two polarisation modes

Low Energy Polarimeter (LEP) measurements showed that at the injection into the COSY ring, the polarisation magnitudes for polarisation modes "up" and "down" are less than statistical uncertainty of $1 \%$. After the acceleration the difference between the values for two modes may be larger. However, even assuming $\left|P_{\uparrow}-P_{\downarrow}\right|=0.1$, the correction term for the asymmetry measured using the STT is less than $5 \cdot 10^{-4}$ and can be ignored. The difference between the polarisation magnitudes is potentially more serious for the FD analysis, the same assumption of $\left|P_{\uparrow}-P_{\downarrow}\right|=0.1$ could induce the relative errors in $A_{y}$ of up to $2.5 \%$. However, it should be noted that in the overlap regions of the STT and FD data any disagreements between the determinations of the asymmetries in the two systems are on the $1 \%$ level and this puts a much tighter constraint on possible $\left|P_{\uparrow}-P_{\downarrow}\right|$ differences.

### 4.3.2 Polar angle accuracy

Misalignment of the left and right STT detectors, i.e. the difference in the angles $\theta_{1}$ and $\theta_{2}$ measured at two telescopes, may raise the fake asymmetry. Assuming $\left|\theta_{1}-\theta_{2}\right| \simeq(0.5 \pm 1.0)^{\circ}$ for each $\theta$ bin, estimated from $\theta-\theta(E)$ distribution variance (Figure 4.2), the upper limit for the systematic error induced by the STT detectors misalignment is $1.5 \cdot 10^{-3}$ at the beam kinetic energy of $T_{p}=0.796 \mathrm{GeV}$ and by factor of 2 smaller at the higher energies.

One can estimate the precision of the measured scattering angle at the FD indirectly from the $p p \rightarrow d \pi^{+}$reaction. The simultaneous measurement of the deuteron and pion in the FD showed that the precision of the horizontal transverse momentum $\Delta P_{x}$ is less than $1.5 \mathrm{MeV} / c$. This corresponds to the systematic deviation in the laboratory angles from those expected for these kinematics $\Delta \theta_{l a b}<0.07^{\circ}$. If this is valid also for $p p$ elastic scattering it would suggest that the c.m. scattering angles were defined with a precision of better than $0.15^{\circ}$.

In cases, where one of the protons from an elastic scattering event is detected in the FD and the other in the STT, it is possible to compare directly the scattering angle measured in the two systems. Figure 4.7 shows the difference of the results of the $\theta_{c m}^{S T T}$ calculated from the energy deposited in the STT layers and $\theta_{c m}^{F D}$ reconstructed from the track in the FD.

In general, the $\theta_{c m}^{S T T}$ angle is larger than $\theta_{c m}^{F D}$, with the difference being typically $\approx 0.3^{\circ}$, as seen for $T_{p}=0.796 \mathrm{GeV}$ (left panel) and $T_{p}=2.157 \mathrm{GeV}$ (right panel). It is not possible to judge which detector is responsible for this difference which is, however, small compared with the $\theta_{c m}$ bin widths of $1.0^{\circ}$ (FD) and $1.2^{\circ}$ (STT) used for the final values of $A_{y}$.


Figure 4.7: Difference between the scattering angles reconstructed using the FD $\theta_{c m}^{F D}$ and STT $\theta_{c m}^{S T T}$. Example plots are shown for $T_{p}=0.796 \mathrm{GeV}$ (left panel) and $T_{p}=2.157 \mathrm{GeV}$ (right panel).

To estimate the impact of the angular deviation onto $A_{y}$, for each energy we approximated the reconstructed $A_{y}$ dependence with a parabola. Then, one can calculate the relative change of $A_{y}$ occurring due to the constant shift in angle $\delta A_{y}=\left(A_{y}(\theta)-A_{y}(\theta+\delta \theta)\right) / A_{y}(\theta)$ (Figure 4.8). The maximal error of $2.5 \%$ is obtained at $T_{p}=0.796 \mathrm{GeV}$. At higher energies the possible systematic error is much smaller, e.g., at $T_{p}=2.368 \mathrm{GeV}$, shown in the right panel of Figure 4.8, it is less than $1.2 \%$.


Figure 4.8: Systematic error due to the possible maximum shift of the scattering angle. Example plots are shown for the beam kinetic energies $T_{p}=0.796$ GeV (left panel) and $T_{p}=2.368 \mathrm{GeV}$ (right panel).

### 4.3.3 Detector efficiencies stability

Another factor that could affect the asymmetry measured using the STTs is an instability of two detectors efficiencies in time. To be more precise, the ratio of the efficiencies of the two telescopes $r=E_{1} / E_{2}$ should be constant to avoid the fake asymmetry. Let us introduce the instability factor $r_{\uparrow} / r_{\downarrow}$ that should be equal to 1 , in case the efficiencies ratios are the same for the both beam polarisation modes.

The angular dependence of typical average ratio $r_{\uparrow} / r_{\downarrow}$ at the beam energies of $T_{p}$ $=0.796 \mathrm{GeV}$ and 1.8 GeV are shown in Figure 4.9. In almost all the cases the fitted constants are indeed close to 1 (with $\chi^{2} / n d f \simeq 1$ ).

The uncertainty of the fitted constant can be interpreted as the systematic uncertainty induced by the detector instability, i.e.

$$
\begin{equation*}
\Delta A_{y}(\theta) \approx\left(1-r_{\uparrow} / r_{\downarrow}\right) A_{y}(\theta) \equiv c(\theta) A_{y}(\theta) \tag{4.9}
\end{equation*}
$$



Figure 4.9: The angular dependences of the instability factor $r_{\uparrow} / r_{\downarrow}$ at the beam energies of $T_{p}=0.796 \mathrm{GeV}$ (left panel) and $T_{p}=1.8 \mathrm{GeV}$ (right panel).

The STT detector efficiency instability correction, which was studied at all energies, does not exceed the $|c|=1.3 \%$ that was found at 1.8 GeV . The relevant corrections of the analysing power $c(\theta) A_{y}(\theta)$ were added for each angular bin of the analysing power, obtained from the STT data set.

In order to simulate the maximum possible systematic error, induced by the STT detectors inefficiencies, $c=1-r_{\uparrow} / r_{\downarrow}=0.2$ was introduced into the simulation. After the correction factor was applied, the angular dependence of the systematic uncertainty has been simulated once more, and the obtained systematic uncertainties were typically of the order $10^{-3}$ that is one order smaller than prior to the correction.

The efficiency for registering events in the FD were studied by using events where both the fast and recoil protons were measured in the FD and STT, respectively. The efficiencies obtained per cycle are shown in Figure 4.10, summarised separately for the two beam polarisation modes. This value is expected to be lower than $100 \%$ due to a small fraction of misidentified protons in the STT, as well as the possibility of multiple particles recorded in the STT or FD within a single trigger. There is also a small inefficiency of the FD trigger ( $\lesssim 1 \%$ ) and a loss of particles because of the large angle scattering or interaction with the detector material.

Most importantly, the difference of the efficiencies between the two polarisation modes is of less than $10^{-3}$ that is within the statistical uncertainties.


Figure 4.10: Efficiencies of the elastic event reconstruction using the FD in the cycles with the beam polarisation mode up (left panel) and beam polarisation mode down (right panel).

### 4.3.3.1 Summary on systematic uncertainties

The overall systematic uncertainty in $A_{y}$ arising from asymmetry measurement using the STT does not exceed $0.3 \%$. The dominant systematic error is, hence, that arising from the determination of the beam polarisation in the EDDA polarimeter, which was estimated to be $3 \%$ [34]. For the FD data there is, in addition, a possible contribution associated with the assumption of equal up and down polarisations so that in this case we would cautiously assume a $5 \%$ systematic uncertainty. To these figures must be added the statistical uncertainty in the determinations of the beam polarisations at the six energies shown in Table 4.1.

### 4.4 Results and discussion

The results of all the ANKE measurements of $A_{y}\left(\theta_{c m}\right)$ for $\vec{p} p$ elastic scattering are shown for the six energies in Figure 4.11. For the final results, only those cycles were used that contained good quality data in all the detectors: FD and STT, as well as the EDDA polarimeter.

The agreement between the STT and FD data, which involved completely independent measurements of the final state, is remarkably good. The individual deviations generally lie within the statistical uncertainties and the average Over the angular overlap regions is $A_{y}(F D) / A_{y}(S T T)=1.00 \pm 0.01$. At beam energies close to 0.796 GeV there are many measurements of the $p p$ analysing power and, in general, they are in good mutual agreement, as they are with the new ANKE data.


Figure 4.11: Comparison of the ANKE measurements of the proton analysing power in $\vec{p} p$ elastic scattering using the STT (red filled circles) and the FD (blue filled triangles) systems with the curves corresponding to the SAID 2007 (solid black line) [8] and the revised fit (dashed red) solutions. Only statistical errors are shown so that the systematic uncertainties arising, for example, from the calibration of the EDDA polarimeter have not been included. Also shown are selected results from EDDA (black crosses) [13] at the energies different by no more than 7 MeV and, at 0.796 GeV , LAMPF [46-48], and SATURNE [49] (black open symbols).

This reinforces the confidence in the use of the EDDA polarimeter. At 1.6 GeV and above there are far fewer experimental measurements and, for clarity, we only show the EDDA data at neighbouring energies though, at the highest energy, the statistical fluctuations are significant [13].

The SAID 2007 solution [8], shown by the solid black line in Figure 4.11, describes the bulk of the $\approx 0.796 \mathrm{GeV}$ data very well indeed. However, at higher energies the ANKE data deviate significantly from the predictions of the 2007 solution. Moreover, the shapes of the ANKE data seem very different from these predictions, rising much more steeply at small angles. Therefore, these discrepancies cannot be due to a simple miscalibration of the EDDA polarimeter, for example, which would change the overall magnitude of $A_{y}(\theta)$ but not its angular dependence [50].

The ANKE analysing power data have been added to the world data set and searches made for an updated partial wave solution. To allow for possible systematic effects, the SAID fitting procedure introduces a scale factor $N$ into any
data set and determines its value, as well as the $p p$ phases and inelasticities, by minimising an overall $\chi^{2}$ for the complete data set. When this is done, the average value of $\chi^{2}$ per degree of freedom found for the ANKE STT data is 1.6 and slightly larger for the FD results. The new fits, which lead to the red dashed curves in Figure 4.11, correspond to significant changes at the higher energies to the parameters of the lower partial waves, with the biggest changes up to $60 \%$ in ${ }^{3} F_{2}$ and ${ }^{3} F_{4}$ (Figure 4.12).


Figure 4.12: Energy-dependent phase shift analysis parameters: $\delta$ phase shift and $\rho\left(\cos \rho=\eta\right.$, where $\eta$ is the absorption parameter) for ${ }^{3} F_{2}$ and ${ }^{3} F_{4}$ partial waves from the 2014 SAID solution, in comparison with the older solution from 2007.

The values of the normalisation factors $N$ reported in Table 4.2 have an average of $\langle N\rangle=1.00 \pm 0.02$ for the STT data. These factors, which would effectively multiply the beam polarisations, have not been applied in Figure 4.11. The deviations of the individual values of $N$ from unity might seem to be greater at the higher energies. They are somewhat larger than what one would expect on the basis of the quoted uncertainties in the EDDA polarimeter, being around $5 \%$ rather than the $3 \%$ estimate [34]. It should be stressed that the introduction of the scale factor $N$ does not change the shape of a distribution and, even in cases where a value close to one is found, this does not mean that the fit reproduces perfectly the data. A clear example of this is to be found in the larger angle data at 1.6 GeV shown in Figure 4.11.

| $T_{p}(\mathrm{GeV})$ | 0.796 | 1.6 | 1.8 | 1.965 | 2.157 | 2.368 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $N$ | 1.00 | 1.00 | 0.99 | 1.09 | 1.01 | 0.93 |

Table 4.2: The normalisation factors $N$ obtained in a partial wave fit [51] to the current STT data.

### 4.5 Conclusion

We have measured the analysing power in $\overrightarrow{p p}$ elastic scattering at 0.796 GeV and at five energies from 1.6 GeV up to 2.4 GeV using both the silicon tracking telescopes and the forward detector. The consistency between these two independent measurements of the final protons is striking so that the only major systematic uncertainty is the few percent associated with the calibration of the EDDA polarimeter. Though the overall uncertainties are slightly larger for the FD data, these results are important because they extend the coverage to slightly larger scattering angles.

In the small angle range accessible to ANKE, the new data are consistent with older measurements around 0.796 GeV and also with the 2007 SAID predictions at this energy [9]. At higher energies the ANKE results lie significantly above the 2007 solution near the forward direction and also display a different angular dependence. By adjusting some of the phases and inelasticities in the low partial waves by up to $60 \%$, the new SAID solution [51] was obtained that provides a much better description of the new ANKE $A_{y}$ data.

## Chapter 5

## Cross section in proton-proton elastic scattering

As was shown in the introduction (Figure 1.3), there are relatively few measurements of $p p$ elastic scattering for beam energies above about 1 GeV in the angular range between $10^{\circ}$ and $30^{\circ}$. This falls between the region of major Coulomb effects and the larger angles where the EDDA collaboration has contributed extensively. This lack of information on the differential cross section and the analysing power inevitably leads to ambiguities in any $p p$ PWA at high energies. To address this gap in our knowledge, ANKE collaboration has carried out the studies of the $p p$ analysing power, presented in the previous chapter, and differential cross section, which is discussed here.

The differential cross section $d \sigma / d \Omega$ measurements were performed using the ANKE unpolarised hydrogen cluster-jet target and the unpolarised proton beam at eight kinetic energies $T_{p}=1.0,1.6,1.8,2.0,2.2,2.4,2.6,2.8 \mathrm{GeV}$ for center-of-mass angles in the range from $12^{\circ}-16^{\circ}$ to $25^{\circ}-30^{\circ}$, depending on the energy. As was the case for the analysing power $A_{y}$, the present studies of $d \sigma / d \Omega$ were carried out using the ANKE spectrometer. However, for $d \sigma / d \Omega$ investigations only forward detection system was used to detect fast protons from elastic $p p$ scattering.

In general, the cross section $\sigma$ for a given physical process is given in terms of the corresponding counting rate $R$ and the luminosity $L$ through:

$$
\begin{equation*}
\sigma=\frac{R}{L} . \tag{5.1}
\end{equation*}
$$

The biggest challenge is to establish the beam-taget luminosity at the few percent level, because the overlap of the beam and target can not be deduced with such precision from macroscopic measurements. The details on the luminosity determination are provided in Section 5.1, while the count rate analysis using FD is shortly described in Section 5.2. Finally, the results of the differential cross section in $p p$ elastic scattering are discussed in Section 5.4.

### 5.1 Luminosity determination

The knowledge of the luminosity is the crucial element of cross section measurement. The ANKE collaboration and the COSY machine crew have jointly developed a very accurate method for determining the absolute luminosity in an experiment at an internal target position. The technique relies on measuring the energy losses due to the electromagnetic interactions of the beam as it passes repeatedly through the thin target and measuring the shift of the revolution frequency by studying the Schottky spectrum [52]. In order to extract the cross section of any reaction, the absolute value of the luminosity must be determined. For the fixed target experiments, luminosity is completely defined by:

$$
\begin{equation*}
L=n_{B} \times n_{T}, \tag{5.2}
\end{equation*}
$$

where $n_{B}$ is the particle current of the incident beam and $n_{T}$ is the effective target thickness, expressed as an areal density. The measurement of the beam intensity $n_{B}$ is performed via the high precision Beam Current Transformer (BCT) (Section 5.1.1). The effective target density $n_{T}$ is determined via the measurement of the beam revolution frequency shift caused by the electromagnetic interaction between the beam and target particles (Section 5.1.2).

### 5.1.1 Beam intensity measurement

The particle current of the incident beam $n_{B}$ was deduced from the calibrated Beam Current Transformer signal. The amplitude of the BCT signal is proportional to the COSY beam current, $I_{b}=n_{B} e=N f e$, where $N$ is number of particles in the beam, $f$ is revolution frequency, and $e$ is particle charge.

To avoid the effects from stray magnetic fields, the BCT is mounted in field-free region of the ring and, in addition, is magnetically shielded.


Figure 5.1: Beam Current Transformer (BCT) typical raw signal, recorded during the experiment.

The raw BCT signal (Figure 5.1) was calibrated with a current-carrying wire placed between the beam tube and ferrite core of the BCT. The result of the calibration, applying a current from a high precision source, is given in Figure 5.2 and it does not depend on the energy of the beam.


Figure 5.2: BCT signal vs. current $I$ in the calibration wire.

In the given experiment, the BCT signal was recorded directly to the ANKE data stream. The measurements were carried out every second over the 300 s cycle and then averaged. The final results are accurate to better than $10^{-3}$, and hence, can be neglected in comparison with target density uncertainties that will be discussed in the following.

### 5.1.2 Target density determination

When a charged particle passes through the matter, it loses energy through electromagnetic interaction. In the storage ring an uncooled beam passes a thin target a very large number of times. The energy loss, which is proportional to the target thickness, builds up steadily in time and causes a shift in the revolution frequency $f_{0}$. This shift can be determined by studying the Schottky power spectrum of the beam [53].

The energy loss $\delta T$ per single passage through the target, divided by the mass stopping power $S_{m}=\frac{d E}{d x} \frac{1}{\rho}$ and the mass $m$ of the target atom, yields the number of target atoms per unit area that interact with the beam:

$$
\begin{equation*}
n_{T}=\frac{\delta T}{S_{m} m} \tag{5.3}
\end{equation*}
$$

Over a small period of time the beam makes $f_{o} \Delta t$ traversals with the corresponding energy loss $\Delta T$. Hence, Equation 5.3 maybe written in terms of energy loss, as

$$
\begin{equation*}
n_{T}=\frac{\Delta T}{f_{0} S_{m} m \Delta t} \tag{5.4}
\end{equation*}
$$

or applying logarithmic differentiation, in terms of change in the beam momentum as

$$
\begin{equation*}
n_{T}=\frac{1+\gamma}{\gamma} \frac{T_{0} \Delta p}{f_{0} S_{m} m p_{0} \Delta t} . \tag{5.5}
\end{equation*}
$$

$T_{0}$ and $p_{0}$ are the initial values of the beam kinetic energy and momentum and $\gamma$ is the Lorentz factor.

The fractional change in the revolution frequency is proportional to that in the momentum through the so-called frequency-slip parameter $\eta$ :

$$
\begin{equation*}
\frac{\Delta f}{f_{0}}=\eta \frac{\Delta p}{p_{0}} . \tag{5.6}
\end{equation*}
$$

Putting the expressions 5.5 and 5.6 together, we obtain

$$
\begin{equation*}
n_{T}=\left(\frac{1+\gamma}{\gamma}\right) \frac{1}{\eta} \frac{1}{S_{m} m} \frac{T_{0}}{f_{0}^{2}} \frac{d f}{d t} . \tag{5.7}
\end{equation*}
$$

The stopping power $S_{m}$ and mass of the target atoms are well known and easily accessible at NIST-PML data base [54]. The initial values of frequency and energy of the beam, as well as the Lorenz factor are routinely measured for every
experiment at COSY. Therefore, once the frequency-slip parameter $\eta$ is known, $n_{T}$ can be deduced by measuring the beam revolution frequency shift $d f / d t$ during the data taking.

The frequency-slip paremeter $\eta$ can be expressed in terms of $\alpha$, the so-called momentum compaction factor, which is constant for a given lattice settings of the accelerator:

$$
\begin{equation*}
\eta=\frac{1}{\gamma^{2}}-\alpha \tag{5.8}
\end{equation*}
$$

The $\eta$ parameter determines the direction of the frequency change during the machine cycle. The revolution frequency depends on the particle speed $\beta c$ and the orbit length $L$ through $f=\beta c / L$, where due to dispersion, $L$ is also a function of the momentum. Using the definition of the momentum compaction factor $\alpha=$ $(d L / L) /(d p / p)$, we obtain

$$
\begin{equation*}
\frac{d f}{f}=\left(\frac{1}{\gamma^{2}}-\alpha\right) \frac{d p}{p} \tag{5.9}
\end{equation*}
$$

An estimate of $\alpha$, which is constant for a given lattice setting, may be done by a computer simulation of the accelerator, but greater precision is achieved by a direct measurement, as will be described later.

### 5.1.2.1 Schottky noise

The beam in the synchrotron consists of a finite number of charged particles. A current created by these charge carriers has some statistical fluctuation, that were investigated first by W. Schottky [55].

The current fluctuations induce a voltage signal at a beam pick-up. The Fourier analysis of this voltage signal by a spectrum analyser delivers frequency distribution around the harmonics of the revolution frequency. The frequencies of COSY were measured with the existing Schottky pick-up of stochastic cooling system, which is optimized to operate in GHz region. The harmonic number 1000 of COSY revolution frequency was measured with a spectrum analyser. Schottky noise current is proportional to the square root of number of particles in the ring. Therefore, the amplitudes of the measured distribution are squared to give the Schottky power spectra, which are representative of the momentum spread of the beam.


Figure 5.3: Schottky power spectra for $T_{p}=1.0 \mathrm{GeV}$ (a) and $T_{p}=2.0 \mathrm{GeV}$ (b) obtained during one 300 s cycle and scaled to harmonic number 1 . The mean frequencies are indicated by the vertical (red) lines.

The Schottky signals were recorded every 10 s with a 189 ms sweep time, resulting in effectively instantaneous spectra. For ease of representation, only the results from every 60 seconds are shown in Figure 5.3.

We estimate the background from both sides of the spectra, assuming that the background noise associated with a spectrum analyser is flat. After subtracting the background noise from the original Schottky spectrum, we can evaluate the mean frequency $f$ of the beam at any instantaneous measurement. The centroids of the distributions, are indicated by the vertical red lines in Figure 5.3.

### 5.1.2.2 Frequency shift

The mean frequencies of the beam as the function of time $t$ over the 300 s cycle are presented in Figure 5.4. It must be noted that the direction of the frequency change is actually different at low and high energies, depending on the lattice settings of the accelerator. The point of transition, where $d f$ changes its sign,



Figure 5.4: Typical mean frequency shift derived from the Schottky power spectra of the type illustrated in Figure 5.3 for $T_{p}=1.0 \mathrm{GeV}$ (left panel) and $T_{p}=2.0 \mathrm{GeV}$ (right panel).
occurs when $\alpha=1 / \gamma_{t r}^{2}$. Consequently, near the transition point $\eta$ is small and this is the principal restriction on the applicability of the Schottky method. For COSY proton beam the transition occurs for $T_{p} \approx 1.3 \mathrm{GeV}$, for this reason the experiments were not conducted between 1.0 GeV and 1.6 GeV . As one can see, an average frequency shift in the cycle, which is comparable to the spectra width, is negative for 1.0 GeV and positive for 2.0 GeV . For this reason, the example energies in Figures 5.3-5.5 were chosen from both sides of the transition point.


Figure 5.5: Average frequency shifts within the cycle duration, measured by the new (blue) and old (green) spectrum analysers at $T_{p}=1.0$ and $T_{p}=2.0$ GeV .

The frequency change $d f / d t$ should not be time dependent, if beam-target overlap and the target density are constant during the cycle. Hence, by checking $d f / d t$ dependence on time within the cycle via averaging many cycles, one can check the stability of the effective target density, which also accounts for beam-target overlap.

In order to avoid the systematic effects, asociated with the COSY magnets slowly reaching the nominal field, it was decided to cut off the data from first 60 seconds
of data taking in every cycle. The frequency shifts were calculated independently, splitting the data from the useful cycle length into three parts. As demonstrated in Figure 5.5, $d f / d t$ values did not show any evidence of time dependency apart from the statistical fluctuations.

### 5.1.2.3 COSY rest gas

A small frequency shift is produced by the interaction of the beam with the residual gas in the COSY ring. Besides, the ANKE target produces additional increase of the vacuum pressure in the vicinity of the target. In order to account for these systematic effects, dedicated cycles were developed, where the ANKE cluster target was switched on, but the beam was steered away from it.

Even though these measurements already account for both effects, the separate cycles with target switched off, were performed, to estimate the pure effect of the residual gas, and to check that the beam was successfully steered away from the target. Figure 5.6 shows an example of these measurements at 1 GeV . As one can see, the effects from the ANKE target and residual gas together, as well as residual gas only are small, but distinguishable.


Figure 5.6: Example of frequency shift caused by the background when the target is on $\left(\frac{d f}{d t}\right)_{A N K E+C O S Y}$ (left) and when the target is off $\left(\frac{d f}{d t}\right)_{C O S Y}$ (right) compared to the total frequency shift $\left(\frac{d f}{d t}\right)_{t o t}$ with the beam incident on the target (middle).

Finally, the frequency shift caused purely by beam-target interaction is calculated as:

$$
\begin{equation*}
\left(\frac{d f}{d t}\right)_{t a r}=\left(\frac{d f}{d t}\right)_{t o t}-\left(\frac{d f}{d t}\right)_{A N K E+C O S Y} \tag{5.10}
\end{equation*}
$$

where $\left(\frac{d f}{d t}\right)_{t o t}$ is the total frequency shift during the measurement discussed in the previous section, and $\left(\frac{d f}{d t}\right)_{A N K E+C O S Y}$ is the frequency shift caused by the residual gas of the COSY ring and effect from the ANKE cluster target. The corresponding uncertainties of the background measurement have been accounted for in the systematic errors summary (see details in Table 5.1).

### 5.1.2.4 Momentum compaction factor

After determining $d f / d t$, only momentum compaction factor $\alpha$ is needed to finalise the calculation of the target density $n_{t}$ at all the beam energies, according to Equation 5.7 and 5.8. The $\alpha$ measurements at COSY were performed in the dedicated cycles with the target switched off by adjusting the strength of the COSY bending magnets by few parts per thousand (which lays within the accelerator acceptance) and measuring the relative change in the beam revolution frequency $\Delta f / f_{0}$. The dependence between $\Delta B / B_{0}$ and $\Delta f / f_{0}$ is plotted in Figure 5.7.


Figure 5.7: Variation of the relative change in the mean beam revolution frequency $\Delta f / f_{0}$ with the relative change in the field strength in the bending magnets $\Delta B / B_{0}$. The fit defines the momentum compaction factor $\alpha$. The example is shown for $T_{p}=2.0 \mathrm{GeV}$.

If the changes are not very large there is a linear relationship between the relative revolution frequency shift $\Delta f / f_{0}$ and the relative change in the field $\Delta B / B_{0}$,
expressed as following:

$$
\begin{equation*}
\frac{\Delta f}{f_{0}}=\alpha \frac{\Delta B}{B_{0}} \tag{5.11}
\end{equation*}
$$

Larger values of $\Delta B / B_{0}$ and $\Delta f / f_{0}$ require higher order terms in Equation 5.11. For the purposes of this experiment, $\left|\Delta B / B_{0}\right|<1 \%$ range was fitted with polynomial of second order.

### 5.1.2.5 Luminosity summary

The luminosity measurements defined by the effective target density $n_{T}$ and beam current $n_{B}$ are summarised for all eight energies of the experiment in Figure 5.8.


Figure 5.8: The luminosity measured in every cycle during the experiment.

Every point stands for the average luminosity in the cycle. As seen, the luminosity may vary from cycle to cycle rather significantly even at the fixed beam energy, which is mainly due to the COSY beam intensity variations. This does not concern the reliability of the final results, because the target density is determined for each cycle independently.

### 5.2 Event selection by FD

In order to determine cross section, besides luminosity counting rate $R$ (Equation 5.2) of $p p$ elastic scattering events must be measured. The events were selected by detecting a single fast proton in the Forward Detector (FD). The analysis of $p p$ elastic scattering data from the FD has been already discussed in the previous chapter. Therefore, in this section only the specifics of the cross section analysis will be discussed.

The trigger for the data acquistion system was initiated by a signal produced by the proton in either of two hodoscopes of FD, placed one behind the other. This, together with a high efficiency of scintillation counter, reduced the trigger inefficiency to the $10^{-4}$.

The counter efficiency was studied by analysing the signal amplitude as a function of the vertical hit coordinate for the selected $p p$ elastic events. Two kinds of angular acceptance cuts were applied: the equal $|\phi|<10^{\circ}$ cut for all polar angles, and $\left|Y_{\text {track }}\right|<10 \mathrm{~cm}$ cut on the vertical coordinate in the D 2 exit window. No sign of the amplitude falling below the threshold was observed, except for the first (closest to the beam pipe) counters in each hodoscope wall. The efficiency of each of MWPC's planes exceeds $97 \%$ [56].

The selected events produced a prominent peak in the missing mass spectrum, with a background of only $1-2 \%$. A small contribution from the $p p \rightarrow d \pi^{+}$reaction to the peak region at 1 GeV was subtracted on the basis of the energy-loss information.

The setup parameters were adjusted in a geometry tuning procedure, with the use of the exclusive $p p \rightarrow p p, p p \rightarrow p n \pi^{+}, p p \rightarrow p p \pi^{0}$, and $p p \rightarrow d \pi^{+}$reactions. In the last case, both the $d$ and $\pi^{+}$were detected in the FD simultaneously and this gave valuable information on the systematic uncertainty of the transverse momentum reconstruction. These showed that any systematic shift in the determination of the c.m. angle in $p p$ elastic scattering was less than $0.15^{\circ}$, which would correspond to a $0.5 \%$ change in the differential cross section.

### 5.3 Systematic uncertainties

Table 5.1 lists identified contributions to the total systematic uncertainty of cross section at different proton beam energies $T_{p}$. $\mathrm{E}_{1}$ reflects the statistical and systematic effects in the determination of the Schottky $\eta$ parameter. $\mathrm{E}_{2}$ arises from the rest gas effect (including direct measurement errors as well as possible instabilities). $\mathrm{E}_{3}$ is a measure of the density instability through the 300 s cycle. In addition, the $1.5 \%$ accuracy of the stopping powers (taken from the NIST database [54]) and an estimate of the $1.5 \%$ precision of the analysis of data taken with the FD have to be taken into account. These contributions have been added in quadrature to give the total percentage uncertainty, shown in the last column of Table 5.1. No single contribution is dominant, which means that it would be hard to reduce the systematic error to much below the $2.5-3.5 \%$ total uncertainty quoted in the table [57].

| $T_{p}$ <br> GeV | $\mathrm{E}_{1}$ frequency-slip <br> parameter [\%] | $\mathrm{E}_{2}$ residual <br> gas [\%] | $\mathrm{E}_{3}$ target density <br> instability $[\%]$ | Total <br> $[\%]$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | 1.6 | 0.7 | 0.7 | 2.8 |
| 1.6 | 1.2 | 1.9 | 1.4 | 3.4 |
| 1.8 | 1.3 | 1.6 | 1.6 | 3.4 |
| 2.0 | 0.8 | 1.9 | 1.8 | 3.5 |
| 2.2 | 0.3 | 1.0 | 1.0 | 2.6 |
| 2.4 | 0.4 | 1.5 | 1.6 | 3.1 |
| 2.6 | 0.4 | 1.5 | 1.5 | 3.0 |
| 2.8 | 0.9 | 1.2 | 0.5 | 2.6 |

TABLE 5.1: Percentage contributions to the total systematic uncertainty at different proton beam energies $T_{p}$. $\mathrm{E}_{1}$ reflects the statistical and systematic effects in the determination of the Schottky $\eta$ parameter. $\mathrm{E}_{2}$ arises from the rest gas effect (including direct measurement errors as well as possible instabilities). $\mathrm{E}_{3}$ is a measure of the density instability through the 300 s cycle. These contributions have been added in quadrature together with the accuracy of the stopping powers and the precision of the FD analysis to give the total percentage uncertainty in the last column.

### 5.4 Results and discussion

The numerical values of the measured cross section as the function of the polar angle and the function of the four-momentum transfer $t$ are summarised in Appendix C. The variation of the obtained ANKE data can be seen most clearly in the differential cross section with respect to the four-momentum transfer $t$ and these
results are shown in Figure 5.9. Also shown are exponential fits to the measured data made on the basis of

$$
\begin{equation*}
\frac{\mathrm{d} \sigma}{\mathrm{~d} t}=A \exp \left(-B|t|+C|t|^{2}\right) \tag{5.12}
\end{equation*}
$$

where the values of the resulting parameters are given in Table 5.2.


Figure 5.9: Combined ANKE data set of differential cross sections with respect to the four-momentum transfer $t$ compared to fits made on the basis of Equation 5.12. Systematic errors are not shown. The correct values are shown at 1.0 GeV but, for clarity of presentation, the other data are scaled down sequentially in energy by factors of 1.2 . The true numerical values of the cross section and fit parameters are given in Appendix C and Table 5.2, accordingly.

Taking $C=0$ at 1 GeV would change the value extracted from the fit by less than $1 \%$, though this parameter becomes more important at higher energies where the $t$ range is larger. This empirical representation of the measured data may prove helpful when the results are used in the normalisation of other experimental measurements.

### 5.4.1 Comparison with LNPI results at 1 GeV

There are very few data sets of absolute cross sections at small angles to which the ANKE results can be compared. In the vicinity of 1 GeV there are two measurements that were made with the IKAR recoil detector in the Leningrad Nuclear Physics Institute (LNPI). In the first of these at 992 MeV , IKAR used a hydrogen target [58]. In the second at 991 MeV a methane target was used, though the prime purpose of this experiment was to show that such a target gave consistent results and so could be used with a neutron beam [59].


Figure 5.10: Differential cross section for $p p$ elastic scattering. The ANKE data at $T_{p}=1 \mathrm{GeV}$ with statistical errors (blue squares) are compared to the IKAR (LNPI) hydrogen data at 992 MeV (green circles) [58] scaled by a factor of 1.085 and methane results at 991 MeV (red triangles) [60] scaled by a factor of 1.04. At very small values of $|t|$ there is a rise caused mainly by Coulomb-nuclear interference.

The ratio of the IKAR hydrogen values [58] to the fit of the ANKE 1 GeV data over the common range of angles is $0.920 \pm 0.005$. In order to compare the shapes of these data sets, the LNPI results have been scaled by a factor of 1.085 before being plotted in Figure 5.10. The scaling factor is significant in view of the $2 \%$ and $2.8 \%$ absolute normalisations reported for the IKAR and ANKE experiments, respectively.

### 5.4.2 Comparison with ANL results at 2.0 and 2.8 GeV

Data are also available from the Argonne National Laboratory (ANL) in our angular range at 2.2 and $2.83 \mathrm{GeV}[61]$ and these values are plotted together with our
measurements in Figure 5.11. The ANL data sets agree with our 2.2 and 2.8 GeV results to within $1 \%$. However, the absolute normalisation claimed for these data was $4 \%$ [61] so that it is not possible to draw completely firm conclusions from this comparison.


Figure 5.11: The ANKE $p p$ differential cross section data at 2.2 GeV (closed blue circles) and 2.8 GeV (closed blue triangles) compared to the ANL results [61] at 2.2 GeV (open red circles) and 2.83 GeV (open red triangles). Systematic errors are not shown. For presentational purposes, both higher energy data sets have been scaled downwards by a common factor of 1.5

### 5.4.3 Impact on the SAID solution

The results obtained at ANKE could clearly have an impact on the current partial wave solutions. This is demonstrated in Figure 5.12, where the ANKE cross sections at $1.0,2.0$, and 2.8 GeV are compared to both the SAID 2007 solution [9] and a modified one [51] that takes the present data at all eight energies into account. Scaling factors in the partial wave analysis, consistent with the overall uncertainties given in Table 5.1, have been included in the figure. The major changes introduced by the new partial wave solution are in the ${ }^{1} S_{0}$ and ${ }^{1} D_{2}$ waves.

The precise EDDA measurements were undertaken for c.m. angles of $35^{\circ}$ and above whereas the ANKE data finish well below this and the gap looks even bigger in terms of the momentum-transfer variable $t$. Nevertheless, the modified SAID solution shown in Figure 5.12 fits the ANKE 1 GeV cross section reduced by $3 \%$ and describes also the EDDA data at 1.0144 GeV [62]. Such a $3 \%$ reduction in the


Figure 5.12: Scaled ANKE proton-proton elastic differential cross sections at $1.0,2.0$, and 2.8 GeV with statistical errors compared to the SAID 2007 solution [9] and a modified ("new") partial wave solution where the ANKE data have been taken into account. For presentational reasons the 2.0 and 2.8 GeV data and curves have been reduced by factors of 0.5 and 0.25 , respectively. The best agreement with the new partial wave data was achieved by scaling the ANKE data with factors $0.97,0.96$, and 1.03 at the three energies. Such factors are within the uncertainties given in Table 5.1.

ANKE normalisation at this energy is consistent with the results of a combined fit of (Equation 5.12) to the EDDA and the Coulomb-corrected ANKE data.

In the forward direction the number of proton-proton elastic scattering amplitude reduces from five to three and the imaginary parts of these amplitudes are determined completely by the spin-averaged and spin-dependent total cross sections with the help of the generalised optical theorem. The corresponding real parts have been estimated from forward dispersion relations, where these total cross sections provide the necessary input [63]. All the terms contribute positively to the value of $A(G K)$ and, using the optical theorem, the lower bound,

$$
\begin{equation*}
A \geq\left(\sigma_{\mathrm{tot}}\right)^{2} / 16 \pi, \tag{5.13}
\end{equation*}
$$

is obtained by taking the $p p$ spin-averaged total cross section $\sigma_{\text {tot }}$. This lower bound and the full Grein and Kroll estimates for $A$ [63] are both shown in Figure 5.13 where, for consistency, the same values of $\sigma_{\text {tot }}$ were used in the two calculations [57].

| $T_{p}$ <br> GeV | $A$ <br> $\frac{\mathrm{mb}}{(\mathrm{GeV} / \mathrm{c})^{2}}$ | $B$ <br> $(\mathrm{GeV} / c)^{-2}$ | $C$ <br> $(\mathrm{GeV} / c)^{-4}$ | $A($ Corr. $)$ <br> $\frac{\mathrm{mb}}{(\mathrm{GeV} / c)^{2}}$ | $A(\mathrm{GK})$ <br> $\frac{\mathrm{mb}}{(\mathrm{GeV} / c)^{2}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1.0 | $136.4 \pm 1.3 \pm 3.8$ | $6.7 \pm 0.4$ | $4.0 \pm 3.8$ | $136.7 \pm 3.8$ | 135.2 |
| 1.6 | $131.7 \pm 1.9 \pm 4.5$ | $7.4 \pm 0.3$ | $2.7 \pm 1.7$ | $131.1 \pm 4.5$ | 128.9 |
| 1.8 | $128.6 \pm 1.7 \pm 4.4$ | $7.6 \pm 0.2$ | $3.4 \pm 1.0$ | $127.6 \pm 4.3$ | 125.7 |
| 2.0 | $127.3 \pm 1.7 \pm 4.5$ | $7.7 \pm 0.2$ | $2.5 \pm 0.8$ | $124.0 \pm 4.3$ | 123.1 |
| 2.2 | $117.2 \pm 1.8 \pm 3.0$ | $7.6 \pm 0.2$ | $1.4 \pm 0.7$ | $113.1 \pm 2.9$ | 120.9 |
| 2.4 | $119.2 \pm 1.8 \pm 3.7$ | $8.0 \pm 0.2$ | $2.7 \pm 0.5$ | $112.8 \pm 3.5$ | 118.5 |
| 2.6 | $111.9 \pm 1.7 \pm 3.4$ | $7.8 \pm 0.2$ | $2.0 \pm 0.4$ | $108.8 \pm 3.3$ | 116.0 |
| 2.8 | $108.5 \pm 1.8 \pm 2.8$ | $8.1 \pm 0.2$ | $2.4 \pm 0.4$ | $105.0 \pm 2.7$ | 113.6 |

Table 5.2: Parameters of the fits of Equation 5.12 to the differential cross sections measured in this experiment. In addition to the statistical errors shown, the second uncertainty in the value of $A$ in the second column represents the combined systematic effects summarised in Table 5.1. The corrected values of the forward cross section, $A$ (Corr.), were obtained using the SAID fit discussed in the text, the associated error bars being purely the systematic ones listed in Table 5.1. These values, which were not subjected to the SAID normalisation factors applied in Figure 5.12, may be compared with those of $A(\mathrm{GK})$, which were determined using the Grein and Kroll forward amplitudes [63].

The 992 MeV IKAR data of Figure 5.10 show a significant rise at small $|t|$ that is a reflection of Coulomb distortion of the strong interaction cross section and this was taken into account through the introduction of explicit corrections [58]. The corrected data were then extrapolated to the forward direction $(t=0)$, using a simple exponential function, which would correspond (Equation 5.12) with $C=0$. The resulting points at all the energies studied are generally about $10 \%$ below the Grein and Kroll predictions [63] and would therefore correspond to smaller real parts of the spin-dependent amplitudes. The extrapolation does, of course, depend upon the Coulomb-corrected data following the exponential fit down to $t=0$.

Though the ANKE data do not probe such small $|t|$ values as IKAR LNPI [58], and are therefore less sensitive to Coulomb distortions, these effects cannot be neglected since they contribute between about $1.5 \%$ and $4.5 \%$ at 1.0 GeV though less at higher energies.

It is seen in Figure 5.12 that modified SAID solutions describe well the ANKE measurements at three typical energies and the same is true also at the energies not shown. After fitting the ANKE measurements, there is a facility in the SAID


Figure 5.13: The predictions of Grein and Kroll [63] for the values of the forward $p p$ elastic differential cross section (solid line), the corresponding lower limit provided by the spin-independent optical theorem (Equation 5.13) being indicated by the dashed line. The extrapolated ANKE data, corresponding to the $A$ (Corr.) parameter of Table 5.2, are shown with their quoted errors by the (blue) circles, whereas the (red) squares are the published IKAR values [58].
program for switching off the Coulomb interaction without adjusting the partial wave amplitudes [9] and this allows a robust extrapolation of the Coulomb-free cross section to the forward direction. The approach has the advantage that it includes some of the minor Coulomb effects that are contained in the SAID program [64][65]. It takes into account the phase variations present in the partial wave analysis and also the deviations from exponential behaviour for very small momentum transfers, $|t| \lesssim m_{\pi^{0}}^{2}=0.018(\mathrm{GeV} / c)^{2}$, that are linked to pion exchange. The values for $A$ (Corr.) at $t=0$ produced in this way are given in Table 5.2 and shown in Figure 5.13. The error bars are purely the systematic uncertainties listed in Table 5.1 and any errors in the angular dependence of the SAID predictions are neglected.

The corrections obtained using the SAID program with and without the Coulomb interaction at 1 GeV are a little larger than those found by the LNPI group using an explicit Coulomb formula [58], in part due to the different relative real parts of the $p p$ amplitude in the two calculations.

The agreement of the ANKE data with the theoretical curve in Figure 5.13 is encouraging and would be even slightly better if the normalisation factors found in the fits to the cross sections in Figure 5.12 were implemented. Nevertheless,
the extrapolated values generally fall a little below the predictions at the higher energies.

### 5.5 Conclusion

In summary, we have measured the differential cross sections for proton-proton elastic scattering at eight energies between 1.0 and 2.8 GeV in a c.m. angular domain between about $12^{\circ}-16^{\circ}$ to $25^{\circ}-30^{\circ}$, depending on the energy. Absolute normalisation of typically $3 \%$ were achieved by measuring the energy loss of the beam as it traversed the target. After taking the Coulomb distortions into account, the extrapolations to the forward direction, are broadly compatible with the predictions of forward dispersion relations.

Although our results are completely consistent with ANL measurements at 2.2 and 2.83 GeV [61], the published IKAR values [58] are lower than ours at 1 GeV by about $8 \%$, though this would be reduced to about $5 \%$ if one accepts the renormalisation factor from the SAID fit shown in Figure 5.12.


Figure 5.14: Energy-dependent phase shift analysis parameters: $\delta$ phase shift and $\rho\left(\cos \rho=\eta\right.$, where $\eta$ is the absorption parameter) for ${ }^{1} S_{0}$ and ${ }^{1} D_{2}$ partial waves from the 2015 SAID solution [51], in comparison with the older solution from 2007 [8].

The new ANKE data have a significant influence on a partial wave analysis of the $p p$ elastic scattering. In the modified SAID solution, the ${ }^{1} S_{0}$ and ${ }^{1} D_{2}$ waves in particular significantly change at high energies (Figure 5.14). On a more practical level, the measurements will also be a valuable tool in the normalisation of other experiments.

## Chapter 6

## Analysing power in proton-neutron quasi-free elastic scattering

The analysing power $A_{y}$ in $\vec{p} n$ quasi-free elastic scattering has been measured at small angles at COSY-ANKE using polarised proton beam at 0.796 GeV and five other beam energies between 1.6 and 2.4 GeV incident on the unpolarised deuteron cluster-jet target. The use of deuterium as an effective neutron target is possible because of the small binding energy of the deuteron (about 2.2 MeV ). Consideration of the quasi-free elastic scattering is based on the assumption that the incoming particle is being scattered by only one of two nucleons in the deuteron, while no momentum is transferred to the second nucleon (this nucleon acts as a spectator). In general, the quasi-free scattering is considered to be realized when the momentum transfer from a beam particle to a scattered one $\left(P_{t}\right)$ is large enough as compared with the spectator particle momentum $\left(P_{s p}\right)$. Unfortunately, no neutron detection system is available at ANKE-COSY, and hence, no direct measurement of the scattered neutron is possible. The asymmetries of $\vec{p} n$ quasifree elastic scattering were obtained from the coincidence events, where the fast proton is detected in the ANKE Forward Detector (FD) and the slow spectator proton in a silicon tracking telescope (STT).

This chapter will describe the details of the analysis, unique for the $\overrightarrow{p n}$ quasi-free elastic scattering studies at ANKE.

### 6.1 Beam polarisation

Similar to $\vec{p} p$ elastic scattering experiment, in $\vec{p} d$ measurements the beam polarisation was reversed every subsequent cycle. For each polarisation mode cycles of 180 s or 300 s duration were used, with the last 20 s of each cycle being reserved for the measurement of the beam polarisation with the EDDA detector. The measurement of the proton beam polarisation for the runs with deuteron target followed the same steps as for $\vec{p} p$ ANKE experiment, discussed in Section 4.1.

The weighted averages of the beam polarisations determined over all data at six beam energies are given in Table 6.1. The changes in sign reflect the number of spin flips required to pass through the imperfection resonances, described in detail in Section 3.1.2. The COSY settings for each of the six kinetic energies of the beam were prepared independently and, for this reason, the magnitude of the polarisation may not decrease monotonically with increasing value of the beam energy.

| $T_{p}(\mathrm{GeV})$ | 0.796 | 1.6 | 1.8 | 1.965 | 2.157 | 2.368 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $P$ | 0.511 | 0.378 | -0.508 | -0.476 | -0.513 | 0.501 |
| $\Delta P$ | $\pm 0.001$ | $\pm 0.001$ | $\pm 0.003$ | $\pm 0.005$ | $\pm 0.005$ | $\pm 0.004$ |

Table 6.1: The values of the mean polarisations $P$ determined with the EDDA polarimeter averaged over all the data at the beam energy $T_{p}$. Only statistical errors are given in the table.

The variation of the beam polarisation values among the cycles at any given energy was checked using EDDA with various selections and combinations of the cycles. All the studies yield the consistent results within the uncertainties at any given energy.

### 6.2 Event selection

Neutron detection is not possible using the ANKE detection system. Therefore, in order to select quasi-free elastic scattering events in the ANKE experiment one proton is measured in the STT in coincidence with the fast proton detected in the FD. The PLUTO simulation [66] has been performed to estimate the rate of $p p$ and $p n$ quasi-free scattering within the acceptance of the ANKE detectors. Figure 6.1 shows the expected counts of $p d \rightarrow p p n_{s p}$ and $p d \rightarrow p n p_{s p}$ reactions at ANKE. The example is shown for beam kinetic energy $T_{p}=0.796 \mathrm{GeV}$.


Figure 6.1: The acceptance $p d \rightarrow p p n_{s p}$ (black histograms) and $p d \rightarrow p n p_{s p}$ (red histograms) reactions simulated in the framework of spectator model at $T_{p}$ $=0.796 \mathrm{GeV}$. Coincidence events, where one proton is detected in the FD and other one in the STT1 (left panel) or in the STT2 (right panel) are depicted.

The simulation has demostrated that the $p p$ quasi-elastic scattering is kinematically suppressed in the STT2 due to the FD being an one-arm detector. Therefore, all the coincidence events of the protons detected in the STT2 and the FD are assumed to belong to $p n$ quasi-free elastic scattering. Namely, the proton detected in the STT2 is assumed to be "spectator" one, whereas the particle detected in the FD is regarded as a proton, scattered elastically on a quasi-free neutron.

The proton momentum reconstruction in the STT and the FD followed the same steps as described in Chapter 4. The STTs detect particles with energy threshold of 2 MeV , corresponding to the proton momentum $P_{p}>70 \mathrm{MeV} / \mathrm{c}$ [67]. This momentum of spectator proton should be smaller than momentum transfer for the spectator model to be applicable. The careful handling of the data within the spectator model scenario is discussed in greater detail in Section 6.5.

The quasi-free $p n$ elastic scattering events are identified through the evaluation of the missing mass in the $p d \rightarrow p p X$ reaction. As can be seen from the typical example shown in Figure 6.2, at a beam energy of 2.157 GeV , the missing mass peak is well positioned at the neutron mass. The upper limit of the background estimation (details in Section. 6.4) is small compared with the statistical errors of the analysing power.


Figure 6.2: Missing-mass $M_{X}(p p \rightarrow p p X)$ spectra obtained for a beam energy of $T_{p}=2.157 \mathrm{GeV}$. The peak is consistent with the neutron mass value.

### 6.3 Asymmetry determination

Since the FD is a single-arm detector, the analysing power for the quasi-free elastic scattering has to be calculated from the simple asymmetries of counts corresponding to different orientations of the beam polarisation. The deuterium cluster target was unfortunately not very stable during this experiment causing large variation of the luminosity (beam-target overlap). Hence, the dedicated normalisation procedure had to be prepared.

In this case, the asymmetry is introduced in terms of normalised numbers of counts for the two orientations of the beam polarisation:

$$
\begin{equation*}
\varepsilon(\theta)=\frac{N^{\uparrow}(\theta) / N_{\text {norm }}^{\uparrow}-N^{\downarrow}(\theta) / N_{\text {norm }}^{\downarrow}}{N^{\uparrow}(\theta) / N_{\text {norm }}^{\uparrow}+N^{\downarrow}(\theta) / N_{\text {norm }}^{\downarrow}} . \tag{6.1}
\end{equation*}
$$

As was discussed in Chapter 5, the normalisation factor must be chosen in such a way, that it does not depend on the beam polarisation. For the given analysis, normalisation factor $N_{\text {norm }}=k N_{d 1}+N_{d 2}$ was constructed from the number of deuterons detected in the STT1 $\left(N_{d 1}\right)$ and the $\operatorname{STT} 2\left(N_{d 2}\right)$. The polarisation influence can be cancelled in the $N_{\text {norm }}$, if one requires

$$
\begin{equation*}
\frac{k N_{d 1}^{\uparrow}-N_{d 2}^{\uparrow}}{k N_{d 1}^{\uparrow}+N_{d 2}^{\uparrow}}=\frac{N_{d 2}^{\downarrow}-k N_{d 1}^{\downarrow}}{N_{d 2}^{\downarrow}+k N_{d 1}^{\downarrow}} . \tag{6.2}
\end{equation*}
$$

The equalising coefficient $k$ is, hence, determined as

$$
\begin{equation*}
k=\sqrt{\frac{1}{\left(N_{d 1}^{\uparrow} / N_{d 2}^{\uparrow}\right)\left(N_{d 1}^{\downarrow} / N_{d 2}^{\downarrow}\right)}}=\sqrt{\frac{N_{d 2}^{\downarrow} N_{d 2}^{\uparrow}}{N_{d 1}^{\uparrow} N_{d 1}^{\downarrow}}}=\frac{N_{2}}{N_{1}} . \tag{6.3}
\end{equation*}
$$

This approach is based on the several assumptions, including acceptance stability, equality of polarisation values for two modes $\left|P_{\uparrow}\right|=\left|P_{\downarrow}\right|$, and constant ratio of dead times for the different triggers.

### 6.3.1 Normalisation via proton-deuteron elastic scattering

It was possible to check the proposed normalisation procedure by comparison with proton-deuteron elastic scattering asymmetry obtained via the cross-ratio method. As was explained in Chapters 2 and 4, the cross-ratio method provides precision results without the first order systematic uncertainties. The cross-ratio asymmetry was measured using stopped deuterons that were identified in the STTs. Similar to $\vec{p} p$ analysis, the angles of the stopped deuterons were deduced from the energy deposits measured in the three layers of the STT rather than from a direct angular measurement.


Figure 6.3: Comparison of the $\vec{p} d$ elastic scattering asymmetries $\varepsilon\left(\theta_{c m}\right)$ at $T_{p}=1.965 \mathrm{GeV}$ obtained in two different ways: blue triangles stand for the cross-ratio method; red squares correspond to the simple left-right asymmetry, using the normalisation procedure decribed in the text.

We have calculated the left-right asymmetry of the deuterons scattered to the STTs in each polar angular interval as

$$
\begin{equation*}
\varepsilon(\theta)=\frac{L(\theta)-R(\theta)}{L(\theta)+R(\theta)} \tag{6.4}
\end{equation*}
$$

from the geometrical means of number of particles scattered in the given polar angle interval to the left $L$ and particles scattered in the same angle interval, but to the right $R$ in respect to the beam polarisation. The results for the asymmetry calculated via the cross-ratio method are compared to the simple left-right asymmetry calculated using the new normalisation procedure in Figure 6.3. The good agreement of the asymmetries shown in Figure 6.3 confirms the validity of the proposed normalisation procedure.

Using the polarisation values from Table 6.1, the analysing power $A_{y}$ in protondeuteron elastic scattering was obtained at all six energies. The ANKE data at 0.796 GeV agree with SATURNE measurements [68] within the systematic error bars. Besides providing the normalisation check, these data, summarised in the Figure 6.4 and Appendix D, can be used independently for polarimetry in other experiments.


Figure 6.4: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} d$ elastic scattering (colored filled circles), along with the existing experimental data from SATURNE (black circles) at $T_{p}=0.796 \mathrm{GeV}[68]$. Shown values include statistical errors only.

### 6.4 Background correction

As seen in Figure 6.2, there is some background under neutron peak in the missing mass distribution. In case the background does not depend on the beam polarisation, the true value of the asymmetry $\varepsilon_{\text {true }}$ can be calculated as

$$
\begin{equation*}
\varepsilon_{\text {true }}=\varepsilon_{\text {meas }}\left(1+N_{b g} / N_{0}\right) \equiv \varepsilon_{\text {meas }}\left(1+k_{b g}\right), \tag{6.5}
\end{equation*}
$$

where $N_{b g}$ is the background count within the chosen range of kinematic variables, and $N_{0}$ is the count related to the unpolarised cross section within the same range.


Figure 6.5: The difference of normalised missing mass distributions for two polarisation modes at 1.8 GeV .

To check the validity of the background correction via Equation 6.5, the difference of missing mass distributions for different beam polarisation orientations was studied (Figure 6.5). The missing mass spectra for every cycle were normalised by number of elastic deuterons $\left(N_{\text {norm }}\right)$. Then all normalised distributions obtained at the same beam polarisation mode were summed up with the proper error recalculation. The number of the selected cycles with the beam polarisation up ( $\uparrow$ ) and the beam polarisation down $(\downarrow)$ may not necessary be the same. Hence, the further correction for the number of cycles should be undertaken for the final difference of missing mass spectra. As seen in Figure 6.5, contributions of the unpolarised counts are indeed cancelled in such a distribution. The difference of neutron peaks can be fitted by Gaussian, with no background in the vicinity. Similar figures at other energies prove that there is no polarised background and Equation 6.5 can be used for the asymmetry correction.

The true asymmetry should not change among various $M_{x}$ ranges within the neutron peak, hence it should be possible to roughly estimate the background effect from comparison of the measured asymmetry for different $M_{x}$ ranges. The large statistical errors, however, do not allow to estimate only very roughly the upper limit of $k_{b g}$ to be 0.05-0.07 within the $\pm 2 \sigma$ range.

For more precise estimation on $k_{b g}$, two background shape hypotheses were investigated: polynomial (Figure 6.6 left panel) and polynomial + Gaussian (Figure 6.6 right panel). The sum of normalised missing mass spectra at 1.8 GeV , fit with Gaussian (centered at neutron mass) and background of different shapes, are shown in Figure 6.6 by black curve. Red dashed curves represent the polynomial approximation for the background, the green dashed curve represents the polynomial + Gaussian (mean value of $m_{x} \approx 0.86 \mathrm{GeV} / c^{2}$ ). The polynomial background does not describe well the tail on the left side of the neutron peak, but the central part of the n-peak is described very well within the $1.5-2 \sigma$. Hence, even if we consider an additional Gaussian, that helps to describe the left side of the peak, the contribution to the central part is negligible. As a result, both background shapes would give close values of $k_{b g}$ of 0.03 for polynomial, and 0.026 for polynomial + Gaussian shapes.


Figure 6.6: The sum of normalised missing mass spectra at 1.8 GeV (blue points), fit with Gaussian and background of different shapes (black curve). Red dashed curves represent the polynomial approximation for the background, the green dashed curve represents the polynomial + Gaussian with $m_{x} \approx 0.86$ $\mathrm{GeV} / c^{2}$.

### 6.5 Validity of spectator model

The analysis in the first approximation, when all the coincidence events of protons detected in the FD and in the STT2 are assumed to belong to $p n$ quasi-free elastic
scattering, yields the results that are consistent with the existing SAID solution and experimental data at 0.796 GeV . However, the Figure 6.7 shows that the acceptance of the ANKE detection systems in terms of the $P_{s p} / P_{t}$ ratio spans from 0.3 up to 1.6 , where spectator model is not supposed to be valid. Indeed,


Figure 6.7: The ANKE acceptance in terms of the $P_{s p} / P_{t}$ ratio dependence on the c.m. scattering angle $\theta_{c m}$ at the beam energy of $T_{p}=0.796 \mathrm{GeV}$.
the more careful analysis showed the dependence of the analysing power on the $P_{s p} / P_{t}$ ratio. It is seen from Figure 6.8 that at least $P_{s p} / P_{t}<0.6$ cut is necessary for the analysis at $T_{p}=0.796 \mathrm{GeV}$. Therefore, the careful handling of the data within the spectator model scenario is necessary.

The following studies on this matter have shown that to separate quasi-free scattering another cut of $P_{t}<200 \mathrm{MeV} / c$ is necessary. The underlying reasons are not entirely clear yet and the investigations are undergoing.

### 6.5.1 Quasi-free elastic proton-proton scattering

The analysing power in proton-proton elastic scattering offers an interesting possibility for the study of the applicability of the spectator model cuts applied for proton-neutron quasi-free elastic scattering. Namely, we can identify the quasi-free $\vec{p} p$ elastic scattering via detecting the slow proton in the STT and the fast proton in the FD. It should be noted that detecting both scattered protons in the STT and FD allows to get closer to the spectator model, because there is no $P_{s p}<70$ $\mathrm{MeV} / c$ limit anymore. However, applying the same cuts as towards $\vec{p} n$ quasi-free elastic scattering, we can compare the analysing power $A_{y}$ in quasi-free $\overrightarrow{p p}$ to the


Figure 6.8: Analysing power $A_{y}$ dependence on the $P_{s p} / P_{t}$ ratio at the kinetic beam energy $T_{p}=0.796 \mathrm{GeV}$. The black horizontal line shows the $A_{y}$ values expected from SAID 2007 solution.
$A_{y}$ obtained in free $\overrightarrow{p p}$ elastic scattering (Chapter 4). The results are shown in Figure 6.9 at 0.796 GeV (upper panel) and 1.6 GeV (lower panel). At higher energies the $A_{y}$ values could not be retrieved in the acceptance of the ANKE setup.

The points in red depict the result of the analysis without any cuts on the $P_{s p} / P_{t}$ ratio. The green triangles are the result of the same cut procedure $\left(P_{s p} / P_{t}<0.5\right.$ and $P_{t}>200 \mathrm{MeV} / \mathrm{c}$ ) as for $p n$ analysis. Finally, blue empty symbols show the $p p$ elastic data: circles stand for data obtained from STT and squares - from FD.

The analysis of the quasi-free $\vec{p} p$ elastic events proves the justification of the applied cuts within this work. However, the reasons underneath the cuts are not completely understood and are still to be studied in detail. This demonstrates that $p n$ data at 0.796 GeV in the angular range between $18^{\circ}$ and $23^{\circ}$ indeed correspond to the quasi-free scattering within the applied cuts. The higher energies are influenced much less by the applied cuts, because already for 1.6 GeV the transfer momentum is higher than $180 \mathrm{MeV} / c$.

### 6.6 Results and discussion

The results of the $A_{y}$ measurements at ANKE for $p n$ quasi-elastic scattering are shown in Figure 6.10. The SAID 2007 solution [8], which is only valid up to


Figure 6.9: Analysing power in $\vec{p} p$ quasi-free elastic scattering without any cuts (red points), with the same cuts as for $\vec{p} n$ quasi-free elastic scattering (green triangles), compared to the analysing power obtained from free proton-proton elastic scattering at ANKE: FD (blue empty squares) and STT (blue empty circles). The results are shown at $T_{p}=0.796 \mathrm{GeV}$ (upper panel) and $T_{p}=1.6$ GeV (lower panel).
1.3 GeV kinetic energy, is shown by the solid black line at the $T_{p}=0.796 \mathrm{GeV}$ in Figure 6.10. This energy was specifically chosen for the comparison with the existing data [69-72] and SAID solution [8]. After the appropriate cuts, that ensure the quasi-free elastic scattering, the analysing power in proton-neutron quasi-free elastic scattering could have been obtained. The agreement between the new ANKE data and other existing data at 0.796 GeV and also with the SAID 2007 prediction is very good.

The higher energies, which were the main purpose of this experiment, have even


Figure 6.10: ANKE measurements of the analysing power $A_{y}\left(\theta_{c m}\right)$ in $\overrightarrow{p n}$ quasielastic scattering. Upper panel: the ANKE results (red filled circles) at 0.796 GeV are compared with the curves corresponding to the SAID 2007 prediction (solid black line) [9] and other existing measurements (black open symbols) [6972]. Middle panel: the preliminary SAID solution for the analysing power in $p n$ quasi-free elastic scattering at beam kinetic energy $T_{p}=1.6 \mathrm{GeV}$ is shown in red dashed curve along with the ANKE (red filled circles) and SATURNE (black empty squares) measurements at this energy. Lower panel: ANKE data at four higher energies (filled circles) and the results from Argonne National Laboratory at 2.2 GeV energy [73, 74] (black open symbols). The data at lower panel are scaled for the ease of presentation. Only statistical errors are shown.
better acceptance towards the proton-neutron quasi-free elastic scattering, resulting in the precision data in the non-explored angular and energy region. Results for the higher energies presented in Figure 6.10 were obtained using the data with the cut of $P_{s p} / P_{t}<0.4$. This cut does not drastically decrease the available statistics because the FD acceptance for larger $P_{s p} / P_{t}$ ratio is small. At 1.6 GeV
the loss of statistics due to the limit on the $P_{s p} / P_{t}$ is about $25 \%$, and it goes down with increasing of beam energy. Excluding the 1.6 GeV beam energy, presented results involve more than $95 \%$ of the total available statistics we have collected.

Another confirmation of the high quality of the obtained data is an overlap with the existing data from Argonne National Laboratory (ANL) at 2.2 GeV [73, 74]. The ANKE data points are in a good agreement with ANL data in the overlapping region, and reasonably continue the angular dependence at the smaller angles.

In Figure 6.10 (lower panel) all the results obtained at ANKE at higher energies are summarised. The absolute values are shown at 2.368 GeV , but for clarity of presentation, the other data are scaled up sequentially with the decreasing energy. The scaling factors are given in the legend. The systematic errors, not shown in the figure, include the uncertainties of the determination of the beam polarisation in the EDDA polarimeter.

Using our and other recent data (including WASA-COSY experimental measurements at 1.3 GeV ) the SAID group was able to provide the preliminary solution for $p n$ quasi-elastic scattering at 1.6 GeV (shown by red dashed curve in Figure 6.10 middle panel), extending the PWA range from previously published 1.3 GeV .

### 6.7 Conclusion

We have measured the analysing power in the proton-neutron quasi-free elastic scattering using proton polarised beam at six energies $T_{p}=0.796,1.6,1.8,1.965$, $2.157,2.368 \mathrm{GeV}$ and deuteron unpolarised target. It was possible to show that spectator model could be used in the given experiment.

The ANKE measurements of the analysing power in the proton-neutron quasi-free elastic scattering at beam kinetic energy of 0.796 GeV are consistent with the older experimental data and SAID solution. Furthermore, it was possible to compare the new ANKE measurements with the ANL data at 2.157 GeV , resulting in a good agreement. This further proves the quality of the data at small angles at 5 new energies in the range from 1.6 to 2.4 GeV . This is an important input in the very scarce $p n$ quasi-free elastic scattering data base. Consequently, increasing of the energy range of SAID PWA for $p n$ up to 1.6 GeV has been possible. The shown curve is still only preliminary, the corresponding publication is being prepared for the submission [51]. ANKE data can further aid the SAID analysis by extracting the differential cross-section values in $p n$ quasi-free elastic scattering.

## Chapter 7

## Summary and outlook

This dissertation presents three sets of nucleon-nucleon (NN) scattering data at small angles, including precision data for the analysing power $A_{y}(\theta)$ and the unpolarised differential cross section $d \sigma / d \Omega(\theta)$ in proton-proton $(p p)$ elastic scattering, and the first data set on the analysing power $A_{y}(\theta)$ in proton-neutron ( $p n$ ) quasifree elastic scattering. These studies, motivated by the lack of experimental data for Partial Wave Analysis (PWA) of NN scattering, provide consistent results and form together an important part of the NN studies programme at the Cooler Synchrotron (COSY) in Jülich.

The determination of the analysing power in $\overrightarrow{p p}$ elastic scattering, which relied on the use of the EDDA polarimeter for the absolute measurement of the beam polarisation, provided an interesting opportunity for working with the combination of the ANKE Silicon Tracking Telescopes (STT) and Forward Detector (FD) in the study of small angle scattering. The independent analyses of data gathered with the STT and FD, not only yielded great consistency and increased the angular coverage, but also provided a unique opportunity to study possible sources of systematic uncertainties in great detail. It was concluded that the only significant systematic uncertainty is the $3-5 \%$ associated with the EDDA polarimeter. The proton beam kinetic energy of 0.796 GeV was specially chosen for the control studies of the analysing power. The ANKE results at this energy are in striking agreement with world data (SATURNE, ANL and others) and also with the SAID 2007 solution. This reinforced our confidence in the results obtained using the ANKE asymmetry measurements together with the EDDA beam polarimetry values.

At five higher energies, $T_{p}=1.6,1.8,1.965,2.157$, and 2.368 GeV , the analysing power values were measured for the first time at small angles. The comparison with the current SAID analysis showed significant discrepancies. Not only did the ANKE values lie significantly above the SAID prediction, but the angular dependence was also markedly different from that expected. The SAID group subsequently analysed the world data, this time including the ANKE analysing power measurements, and obtained a modified PWA solution that describes the data significantly better. This led to changes in the lower partial waves (e.g., ${ }^{3} F_{2}$ and ${ }^{3} F_{4}$ ) by up to $60 \%$ at the higher energies.

Values of the unpolarised differential cross sections were obtained at eight proton beam energies, namely $T_{p}=1.0,1.6,1.8,2.0,2.2,2.4,2.6$, and 2.8 GeV . While the procedure for identifying $p p$ elastic scattering using the FD was very similar to that for the analysing power experiment, the most complex part of the cross section analysis was the determination of the absolute luminosity. An accuracy of about $3 \%$ was achieved via the Schottky method, which measured the energy loss of the beam as it traversed the target. After taking Coulomb distortions into account, the values of the cross sections extrapolated to the forward direction are broadly compatible with the predictions of the forward dispersion relations. In addition, our results are completely consistent with ANL measurements at 2.2 and 2.83 GeV .

The precise ANKE values of the observables in $p p$ elastic scattering have provided the SAID data base and PWA with significant new input, resulting in important changes in the low partial waves. Most surprisingly, the ${ }^{1} S_{0}$ and ${ }^{1} D_{2}$ waves changed compared to the SAID 2007 solution.

In order to investigate $\vec{p} n$ quasi-free elastic scattering, experiments with polarised proton beams and an unpolarised deuterium cluster-jet target were carried out at six energies. The polarisation of the proton beam was determined using the EDDA polarimeter while the asymmetry was measured via the coincidence of events where the fast proton was detected in the FD and spectator proton in the STT. It was shown that the spectator model could be used to extract pn quasi-free elastic scattering at all the energies studied.

Quasi-free $\vec{p} p$ elastic scattering could also be identified at $T_{p}=0.796$ and 1.6 GeV using the same analysis cuts as for $\vec{p} n$. The agreement of the analysing powers in $\overrightarrow{p p}$ quasi-free elastic scattering and free $\vec{p} p$ elastic scattering further confirmed the correctness of the analysis. The procedure for the asymmetry calculation was also checked by comparing the asymmetry obtained for $p d$ elastic scattering with the developed normalisation procedure to that found using the cross-ratio method.

The analysing powers in $\vec{p} d$ elastic scattering can then also be used for polarimetry in other experiments.

The measurements of the analysing power $A_{y}(\theta)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}=1.6,1.8,1.965,2.157$ and 2.368 GeV were performed for the first time at such small scattering angles. There is also good agreement in the overlap region with the existing experimental data at 0.796 GeV and 2.157 GeV . The SAID group modified the $I=0$ partial wave analysis, increasing the upper limit of the solution validity from 1.3 GeV up to 1.6 GeV . Nevertheless, more $\vec{p} n$ scattering data are necessary in order to establish a reliable PWA at higher energies. It is planned to extract the differential cross section of $p n$ quasi-free elastic scattering from these ANKE data.

In summary, the results presented in this dissertation are in a good agreement with the existing world data where these exist. However, the ANKE data fill in many holes in the angular and energy coverage of NN elastic scattering observables and these results are having a significant impact on the partial wave analysis.

## Appendices

## Appendix A

## Angular ranges of EDDA semi-rings

| Ring Number | $\Delta \theta_{\text {lab }}$ |
| :---: | :---: |
| 14 | $42.7^{\circ} \ldots 36.9^{\circ}$ |
| 15 | $39.8^{\circ} \ldots 34.1^{\circ}$ |
| 16 | $36.9^{\circ} \ldots 31.5^{\circ}$ |
| 17 | $34.1^{\circ} \ldots 28.9^{\circ}$ |
| 18 | $31.5^{\circ} \ldots 26.5^{\circ}$ |
| 19 | $28.9^{\circ} \ldots 24.2^{\circ}$ |
| 20 | $26.5^{\circ} \ldots 22.1^{\circ}$ |
| 21 | $24.2^{\circ} \ldots 20.1^{\circ}$ |
| 22 | $22.1^{\circ} \ldots 18.3^{\circ}$ |
| 23 | $20.1^{\circ} \ldots 16.6^{\circ}$ |
| 24 | $18.3^{\circ} \ldots 15.0^{\circ}$ |
| 25 | $16.6^{\circ} \ldots 13.6^{\circ}$ |
| 26 | $15.0^{\circ} \ldots 12.3^{\circ}$ |
| 27 | $13.6^{\circ} \ldots 11.1^{\circ}$ |
| 28 | $12.3^{\circ} \ldots 10.1^{\circ}$ |
| 29 | $11.1^{\circ} \ldots 9.9^{\circ}$ |

Table A.1: Laboratory angle ranges, corresponding to EDDA rings, in the coordinate system, associated with the detector.

## Appendix B

## Numerical values of $A_{y}$ in $\overrightarrow{p p}$ elastic scattering

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 0.796 | 6.6 | 0.1701 | 0.0112 |
| 0.796 | 7.8 | 0.1806 | 0.006 |
| 0.796 | 9.0 | 0.2108 | 0.0047 |
| 0.796 | 10.2 | 0.2326 | 0.0042 |
| 0.796 | 11.4 | 0.2505 | 0.0042 |
| 0.796 | 12.6 | 0.2682 | 0.004 |
| 0.796 | 13.8 | 0.2897 | 0.004 |
| 0.796 | 15.0 | 0.3088 | 0.0038 |
| 0.796 | 16.2 | 0.3188 | 0.0038 |
| 0.796 | 17.4 | 0.3377 | 0.0038 |
| 0.796 | 18.6 | 0.3506 | 0.0038 |
| 0.796 | 19.8 | 0.3688 | 0.004 |
| 0.796 | 21.0 | 0.3789 | 0.0042 |
| 0.796 | 22.2 | 0.4022 | 0.0042 |
| 0.796 | 23.4 | 0.4049 | 0.0045 |
| 0.796 | 24.6 | 0.4152 | 0.0054 |
| 0.796 | 25.8 | 0.4336 | 0.0052 |
| 0.796 | 27.0 | 0.4414 | 0.0058 |
| 0.796 | 28.8 | 0.4466 | 0.0059 |
| 0.796 | 31.2 | 0.4651 | 0.0137 |

Table B.1: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=0.796 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.6 | 4.2 | 0.1025 | 0.0124 |
| 1.6 | 5.4 | 0.1124 | 0.0034 |
| 1.6 | 6.6 | 0.1282 | 0.0028 |
| 1.6 | 7.8 | 0.1456 | 0.0024 |
| 1.6 | 9.0 | 0.1578 | 0.0022 |
| 1.6 | 10.2 | 0.1711 | 0.002 |
| 1.6 | 11.4 | 0.1908 | 0.002 |
| 1.6 | 12.6 | 0.2044 | 0.002 |
| 1.6 | 13.8 | 0.2179 | 0.002 |
| 1.6 | 15.0 | 0.2291 | 0.002 |
| 1.6 | 16.2 | 0.2457 | 0.0018 |
| 1.6 | 17.4 | 0.2528 | 0.002 |
| 1.6 | 18.6 | 0.2609 | 0.002 |
| 1.6 | 19.8 | 0.2694 | 0.002 |
| 1.6 | 21.0 | 0.2836 | 0.0026 |
| 1.6 | 22.2 | 0.2878 | 0.0034 |
| 1.6 | 23.4 | 0.3016 | 0.0043 |
| 1.6 | 25.2 | 0.3081 | 0.0041 |

Table B.2: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=1.6 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.8 | 5.4 | 0.1106 | 0.0052 |
| 1.8 | 6.6 | 0.1278 | 0.0042 |
| 1.8 | 7.8 | 0.1405 | 0.004 |
| 1.8 | 9.0 | 0.1544 | 0.0036 |
| 1.8 | 10.2 | 0.172 | 0.0034 |
| 1.8 | 11.4 | 0.182 | 0.0034 |
| 1.8 | 12.6 | 0.1964 | 0.0034 |
| 1.8 | 13.8 | 0.2122 | 0.0034 |
| 1.8 | 15.0 | 0.2166 | 0.0034 |
| 1.8 | 16.2 | 0.2297 | 0.0031 |
| 1.8 | 17.4 | 0.2426 | 0.0035 |
| 1.8 | 18.6 | 0.2473 | 0.004 |
| 1.8 | 19.8 | 0.2584 | 0.0048 |
| 1.8 | 21.0 | 0.2656 | 0.0057 |
| 1.8 | 22.2 | 0.2707 | 0.0067 |
| 1.8 | 23.4 | 0.2719 | 0.0076 |
| 1.8 | 24.6 | 0.2776 | 0.0086 |
| 1.8 | 25.8 | 0.2822 | 0.0113 |

Table B.3: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=1.8 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.965 | 4.2 | 0.1034 | 0.0068 |
| 1.965 | 5.4 | 0.1102 | 0.0037 |
| 1.965 | 6.6 | 0.1393 | 0.0033 |
| 1.965 | 7.8 | 0.1571 | 0.0033 |
| 1.965 | 9.0 | 0.1781 | 0.003 |
| 1.965 | 10.2 | 0.1895 | 0.0028 |
| 1.965 | 11.4 | 0.1991 | 0.0028 |
| 1.965 | 12.6 | 0.2156 | 0.0028 |
| 1.965 | 13.8 | 0.2299 | 0.0026 |
| 1.965 | 15.0 | 0.2357 | 0.0026 |
| 1.965 | 16.2 | 0.2499 | 0.0026 |
| 1.965 | 17.4 | 0.2649 | 0.0026 |
| 1.965 | 18.6 | 0.2723 | 0.0028 |
| 1.965 | 19.8 | 0.2805 | 0.0035 |
| 1.965 | 21.0 | 0.2933 | 0.0042 |
| 1.965 | 22.2 | 0.2973 | 0.0047 |
| 1.965 | 23.4 | 0.3127 | 0.0056 |

Table B.4: Analysing power $A_{y}$ in $\overrightarrow{p p}$ elastic scattering at $T_{p}=1.965 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.157 | 4.2 | 0.085 | 0.0044 |
| 2.157 | 5.4 | 0.0984 | 0.0028 |
| 2.157 | 6.6 | 0.1235 | 0.0026 |
| 2.157 | 7.8 | 0.1325 | 0.0024 |
| 2.157 | 9.0 | 0.1484 | 0.0024 |
| 2.157 | 10.2 | 0.1632 | 0.0022 |
| 2.157 | 11.4 | 0.1726 | 0.0022 |
| 2.157 | 12.6 | 0.1868 | 0.002 |
| 2.157 | 13.8 | 0.1913 | 0.002 |
| 2.157 | 15.0 | 0.2011 | 0.0022 |
| 2.157 | 16.2 | 0.2113 | 0.002 |
| 2.157 | 17.4 | 0.2201 | 0.0022 |
| 2.157 | 18.6 | 0.2304 | 0.0026 |
| 2.157 | 19.8 | 0.2342 | 0.0032 |
| 2.157 | 21.0 | 0.2446 | 0.0036 |
| 2.157 | 22.2 | 0.2508 | 0.0042 |
| 2.157 | 23.4 | 0.2544 | 0.0112 |

Table B.5: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=2.157 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.368 | 4.2 | 0.0757 | 0.0044 |
| 2.368 | 5.4 | 0.0911 | 0.003 |
| 2.368 | 6.6 | 0.1036 | 0.0028 |
| 2.368 | 7.8 | 0.1183 | 0.0028 |
| 2.368 | 9.0 | 0.1289 | 0.0028 |
| 2.368 | 10.2 | 0.1353 | 0.0025 |
| 2.368 | 11.4 | 0.1507 | 0.0025 |
| 2.368 | 12.6 | 0.157 | 0.0023 |
| 2.368 | 13.8 | 0.1682 | 0.0025 |
| 2.368 | 15.0 | 0.1733 | 0.0023 |
| 2.368 | 16.2 | 0.1825 | 0.0023 |
| 2.368 | 17.4 | 0.1878 | 0.0028 |
| 2.368 | 18.6 | 0.1945 | 0.0035 |
| 2.368 | 19.8 | 0.2037 | 0.0039 |
| 2.368 | 21.0 | 0.2007 | 0.0044 |
| 2.368 | 22.2 | 0.2046 | 0.0099 |

Table B.6: Analysing power $A_{y}$ in $\overrightarrow{p p}$ elastic scattering at $T_{p}=2.368 \mathrm{GeV}$, calculated from STT data.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 0.796 | 14.5 | 0.3065 | 0.0045 |
| 0.796 | 15.5 | 0.3241 | 0.0046 |
| 0.796 | 16.5 | 0.3331 | 0.0047 |
| 0.796 | 17.5 | 0.3445 | 0.0048 |
| 0.796 | 18.5 | 0.3659 | 0.0048 |
| 0.796 | 19.5 | 0.373 | 0.0049 |
| 0.796 | 20.5 | 0.385 | 0.0051 |
| 0.796 | 21.5 | 0.3908 | 0.0052 |
| 0.796 | 22.5 | 0.4055 | 0.0056 |
| 0.796 | 23.5 | 0.4124 | 0.0078 |

Table B.7: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=0.796 \mathrm{GeV}$, calculated from FD data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.6 | 11.5 | 0.1873 | 0.0085 |
| 1.6 | 12.5 | 0.1988 | 0.0031 |
| 1.6 | 13.5 | 0.2101 | 0.0026 |
| 1.6 | 14.5 | 0.223 | 0.0024 |
| 1.6 | 15.5 | 0.2373 | 0.0025 |
| 1.6 | 16.5 | 0.2448 | 0.0025 |
| 1.6 | 17.5 | 0.2566 | 0.0026 |
| 1.6 | 18.5 | 0.2604 | 0.0027 |
| 1.6 | 19.5 | 0.2723 | 0.0028 |
| 1.6 | 20.5 | 0.2756 | 0.003 |
| 1.6 | 21.5 | 0.2844 | 0.003 |
| 1.6 | 22.5 | 0.2941 | 0.0031 |
| 1.6 | 23.5 | 0.2991 | 0.0033 |
| 1.6 | 24.5 | 0.3012 | 0.0034 |
| 1.6 | 25.5 | 0.3076 | 0.0036 |
| 1.6 | 26.5 | 0.3168 | 0.0054 |

TABLE B.8: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=1.6 \mathrm{GeV}$, calculated from FD data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.8 | 12.5 | 0.194 | 0.006 |
| 1.8 | 13.5 | 0.2067 | 0.0048 |
| 1.8 | 14.5 | 0.2231 | 0.0045 |
| 1.8 | 15.5 | 0.2281 | 0.0045 |
| 1.8 | 16.5 | 0.2418 | 0.0045 |
| 1.8 | 17.5 | 0.2451 | 0.0046 |
| 1.8 | 18.5 | 0.2591 | 0.0047 |
| 1.8 | 19.5 | 0.2634 | 0.0048 |
| 1.8 | 20.5 | 0.269 | 0.005 |
| 1.8 | 21.5 | 0.2784 | 0.0053 |
| 1.8 | 22.5 | 0.28 | 0.0057 |
| 1.8 | 23.5 | 0.2889 | 0.0063 |
| 1.8 | 24.5 | 0.2822 | 0.0068 |
| 1.8 | 25.5 | 0.2902 | 0.0069 |
| 1.8 | 26.5 | 0.2935 | 0.0072 |

Table B.9: Analysing power $A_{y}$ in $\overrightarrow{p p}$ elastic scattering at $T_{p}=1.8 \mathrm{GeV}$, calculated from FD data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.965 | 12.5 | 0.2154 | 0.0062 |
| 1.965 | 13.5 | 0.2323 | 0.0034 |
| 1.965 | 14.5 | 0.2337 | 0.0028 |
| 1.965 | 15.5 | 0.2468 | 0.0028 |
| 1.965 | 16.5 | 0.256 | 0.0029 |
| 1.965 | 17.5 | 0.2636 | 0.003 |
| 1.965 | 18.5 | 0.2749 | 0.0031 |
| 1.965 | 19.5 | 0.2789 | 0.0032 |
| 1.965 | 20.5 | 0.2835 | 0.0033 |
| 1.965 | 21.5 | 0.2926 | 0.0034 |
| 1.965 | 22.5 | 0.3001 | 0.0036 |
| 1.965 | 23.5 | 0.3098 | 0.004 |
| 1.965 | 24.5 | 0.3142 | 0.0041 |
| 1.965 | 25.5 | 0.3126 | 0.0042 |
| 1.965 | 26.5 | 0.3185 | 0.0045 |

Table B.10: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=1.965 \mathrm{GeV}$, calculated from FD data.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.157 | 13.5 | 0.1874 | 0.0026 |
| 2.157 | 14.5 | 0.1998 | 0.0021 |
| 2.157 | 15.5 | 0.2066 | 0.002 |
| 2.157 | 16.5 | 0.2137 | 0.002 |
| 2.157 | 17.5 | 0.2226 | 0.0021 |
| 2.157 | 18.5 | 0.2265 | 0.0022 |
| 2.157 | 19.5 | 0.2302 | 0.0023 |
| 2.157 | 20.5 | 0.2373 | 0.0024 |
| 2.157 | 21.5 | 0.2438 | 0.0025 |
| 2.157 | 22.5 | 0.242 | 0.0026 |
| 2.157 | 23.5 | 0.2548 | 0.0028 |
| 2.157 | 24.5 | 0.2487 | 0.003 |
| 2.157 | 25.5 | 0.2559 | 0.0032 |
| 2.157 | 26.5 | 0.2637 | 0.0035 |
| 2.157 | 27.5 | 0.2639 | 0.0036 |

Table B.11: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=2.157 \mathrm{GeV}$, calculated from FD data.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.368 | 13.5 | 0.1641 | 0.0033 |
| 2.368 | 14.5 | 0.1764 | 0.0024 |
| 2.368 | 15.5 | 0.1743 | 0.0023 |
| 2.368 | 16.5 | 0.1865 | 0.0023 |
| 2.368 | 17.5 | 0.1916 | 0.0024 |
| 2.368 | 18.5 | 0.1966 | 0.0025 |
| 2.368 | 19.5 | 0.2018 | 0.0026 |
| 2.368 | 20.5 | 0.206 | 0.0028 |
| 2.368 | 21.5 | 0.2066 | 0.0029 |
| 2.368 | 22.5 | 0.2157 | 0.003 |
| 2.368 | 23.5 | 0.2195 | 0.0033 |
| 2.368 | 24.5 | 0.2147 | 0.0035 |
| 2.368 | 25.5 | 0.2135 | 0.0037 |
| 2.368 | 26.5 | 0.2215 | 0.004 |
| 2.368 | 27.5 | 0.2237 | 0.0043 |
| 2.368 | 28.5 | 0.2209 | 0.0046 |

Table B.12: Analysing power $A_{y}$ in $\vec{p} p$ elastic scattering at $T_{p}=2.368 \mathrm{GeV}$, calculated from FD data.

## Appendix C

## Numerical values of $d \sigma / d \Omega$ in $p p$ elastic scattering

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | 12.25 | 17.72 | 0.02136 | 118.7 |
| 1.0 | 12.75 | 17.64 | 0.02314 | 118.1 |
| 1.0 | 13.25 | 17.36 | 0.02498 | 116.2 |
| 1.0 | 13.75 | 16.98 | 0.02689 | 113.7 |
| 1.0 | 14.25 | 16.78 | 0.02887 | 112.4 |
| 1.0 | 14.75 | 16.49 | 0.03092 | 110.5 |
| 1.0 | 15.25 | 16.41 | 0.03304 | 109.9 |
| 1.0 | 15.75 | 16.18 | 0.03523 | 108.4 |
| 1.0 | 16.25 | 15.87 | 0.03748 | 106.2 |
| 1.0 | 16.75 | 15.67 | 0.03981 | 105.0 |
| 1.0 | 17.25 | 15.47 | 0.04220 | 103.6 |
| 1.0 | 17.75 | 15.17 | 0.04467 | 101.6 |

Table C.1: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=1.0 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.0 | 18.25 | 14.98 | 0.04720 | 100.3 |
| 1.0 | 18.75 | 14.71 | 0.04979 | 98.50 |
| 1.0 | 19.25 | 14.55 | 0.05246 | 97.44 |
| 1.0 | 19.75 | 14.39 | 0.05519 | 96.33 |
| 1.0 | 20.25 | 14.03 | 0.05799 | 93.96 |
| 1.0 | 20.75 | 13.66 | 0.06086 | 91.50 |
| 1.0 | 21.25 | 13.45 | 0.06380 | 90.08 |
| 1.0 | 21.75 | 13.38 | 0.06680 | 89.60 |
| 1.0 | 22.25 | 12.94 | 0.06986 | 86.66 |
| 1.0 | 22.75 | 12.88 | 0.07300 | 86.28 |
| 1.0 | 23.25 | 12.53 | 0.07620 | 83.89 |
| 1.0 | 23.75 | 12.32 | 0.07946 | 82.48 |
| 1.0 | 24.25 | 11.90 | 0.08279 | 79.70 |

Table C.2: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=1.0 \mathrm{GeV}$ (continuation).

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.6 | 13.75 | 23.17 | 0.04302 | 96.98 |
| 1.6 | 14.25 | 22.58 | 0.04619 | 94.51 |
| 1.6 | 14.75 | 21.91 | 0.04947 | 91.70 |
| 1.6 | 15.25 | 21.45 | 0.05286 | 89.76 |
| 1.6 | 15.75 | 20.59 | 0.05636 | 86.18 |
| 1.6 | 16.25 | 20.59 | 0.05997 | 86.18 |
| 1.6 | 16.75 | 19.95 | 0.06370 | 83.51 |
| 1.6 | 17.25 | 19.18 | 0.06753 | 80.27 |
| 1.6 | 17.75 | 19.01 | 0.07147 | 79.58 |
| 1.6 | 18.25 | 18.49 | 0.07551 | 77.38 |
| 1.6 | 18.75 | 17.69 | 0.07967 | 74.05 |
| 1.6 | 19.25 | 17.33 | 0.08394 | 72.53 |
| 1.6 | 19.75 | 16.83 | 0.08831 | 70.43 |
| 1.6 | 20.25 | 16.18 | 0.09279 | 67.72 |
| 1.6 | 20.75 | 15.88 | 0.09738 | 66.47 |
| 1.6 | 21.25 | 15.33 | 0.1021 | 64.16 |
| 1.6 | 21.75 | 14.68 | 0.1069 | 61.43 |
| 1.6 | 22.25 | 14.38 | 0.1118 | 60.16 |
| 1.6 | 22.75 | 13.79 | 0.1168 | 57.72 |
| 1.6 | 23.25 | 13.20 | 0.1219 | 55.26 |
| 1.6 | 23.75 | 12.90 | 0.1271 | 53.98 |
| 1.6 | 24.25 | 12.23 | 0.1325 | 51.18 |
| 1.6 | 24.75 | 12.18 | 0.1379 | 50.99 |
| 1.6 | 25.25 | 11.54 | 0.1434 | 48.32 |
| 1.6 | 25.75 | 11.07 | 0.1491 | 46.33 |
| 1.6 | 26.25 | 10.81 | 0.1548 | 45.26 |

Table C.3: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=1.6 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 1.8 | 14.25 | 23.43 | 0.05197 | 87.16 |
| 1.8 | 14.75 | 22.97 | 0.05566 | 85.47 |
| 1.8 | 15.25 | 22.17 | 0.05947 | 82.47 |
| 1.8 | 15.75 | 21.62 | 0.06341 | 80.42 |
| 1.8 | 16.25 | 20.78 | 0.06747 | 77.31 |
| 1.8 | 16.75 | 20.39 | 0.07166 | 75.86 |
| 1.8 | 17.25 | 19.83 | 0.07597 | 73.78 |
| 1.8 | 17.75 | 19.24 | 0.08040 | 71.56 |
| 1.8 | 18.25 | 18.56 | 0.08495 | 69.05 |
| 1.8 | 18.75 | 17.96 | 0.08963 | 66.81 |
| 1.8 | 19.25 | 17.40 | 0.09443 | 64.73 |
| 1.8 | 19.75 | 16.70 | 0.09935 | 62.14 |
| 1.8 | 20.25 | 16.04 | 0.1044 | 59.67 |
| 1.8 | 20.75 | 15.83 | 0.1095 | 58.90 |
| 1.8 | 21.25 | 15.07 | 0.1148 | 56.08 |
| 1.8 | 21.75 | 14.36 | 0.1202 | 53.43 |
| 1.8 | 22.25 | 14.21 | 0.1258 | 52.87 |
| 1.8 | 22.75 | 13.59 | 0.1314 | 50.56 |
| 1.8 | 23.25 | 12.84 | 0.1372 | 47.77 |
| 1.8 | 23.75 | 12.34 | 0.1430 | 45.89 |
| 1.8 | 24.25 | 11.95 | 0.1490 | 44.45 |
| 1.8 | 24.75 | 11.60 | 0.1551 | 43.16 |
| 1.8 | 25.25 | 11.05 | 0.1614 | 41.09 |
| 1.8 | 25.75 | 10.48 | 0.1677 | 39.00 |
| 1.8 | 26.25 | 10.18 | 0.1742 | 37.86 |
| 1.8 | 26.75 | 9.678 | 0.1807 | 36.01 |
| 1.8 | 27.25 | 9.457 | 0.1874 | 35.18 |

Table C.4: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=1.8 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.0 | 14.25 | 24.5061 | 0.0577396 | 82.05 |
| 2.0 | 14.75 | 23.87 | 0.06184 | 79.94 |
| 2.0 | 15.25 | 23.17 | 0.06608 | 77.57 |
| 2.0 | 15.75 | 22.55 | 0.07045 | 75.5 |
| 2.0 | 16.25 | 21.67 | 0.07497 | 72.57 |
| 2.0 | 16.75 | 20.83 | 0.07962 | 69.75 |
| 2.0 | 17.25 | 20.43 | 0.08441 | 68.42 |
| 2.0 | 17.75 | 19.58 | 0.08933 | 65.56 |
| 2.0 | 18.25 | 18.83 | 0.09439 | 63.05 |
| 2.0 | 18.75 | 18.18 | 0.09959 | 60.86 |
| 2.0 | 19.25 | 17.51 | 0.1049 | 58.63 |
| 2.0 | 19.75 | 17.01 | 0.1104 | 56.97 |
| 2.0 | 20.25 | 16.18 | 0.116. | 54.19 |
| 2.0 | 20.75 | 15.3. | 0.1217 | 51.24 |
| 2.0 | 21.25 | 15.04 | 0.1276 | 50.36 |
| 2.0 | 21.75 | 14.38 | 0.1336 | 48.15 |
| 2.0 | 22.25 | 13.43 | 0.1397 | 44.98 |
| 2.0 | 22.75 | 13.21 | 0.146. | 44.23 |
| 2.0 | 23.25 | 12.67 | 0.1524 | 42.44 |
| 2.0 | 23.75 | 12.01 | 0.1589 | 40.20 |
| 2.0 | 24.25 | 11.35 | 0.1656 | 38.00 |
| 2.0 | 24.75 | 10.74 | 0.1724 | 35.95 |
| 2.0 | 25.25 | 10.47 | 0.1793 | 35.04 |
| 2.0 | 25.75 | 9.949 | 0.1863 | 33.31 |
| 2.0 | 26.25 | 9.499 | 0.1935 | 31.8. |
| 2.0 | 26.75 | 9.036 | 0.2008 | 30.26 |
| 2.0 | 27.25 | 8.484 | 0.2083 | 28.41 |
| 2.0 | 27.75 | 8.287 | 0.2158 | 27.75 |

Table C.5: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=2.0 \mathrm{GeV}$

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.2 | 14.75 | 23.17 | 0.06802 | 70.54 |
| 2.2 | 15.25 | 22.33 | 0.07269 | 67.98 |
| 2.2 | 15.75 | 21.87 | 0.07750 | 66.58 |
| 2.2 | 16.25 | 20.74 | 0.08247 | 63.14 |
| 2.2 | 16.75 | 19.87 | 0.08758 | 60.47 |
| 2.2 | 17.25 | 19.26 | 0.09285 | 58.64 |
| 2.2 | 17.75 | 18.35 | 0.09826 | 55.87 |
| 2.2 | 18.25 | 17.89 | 0.1038 | 54.46 |
| 2.2 | 18.75 | 17.12 | 0.1095 | 52.12 |
| 2.2 | 19.25 | 16.26 | 0.1154 | 49.51 |
| 2.2 | 19.75 | 15.69 | 0.1214 | 47.76 |
| 2.2 | 20.25 | 14.89 | 0.1276 | 45.32 |
| 2.2 | 20.75 | 13.91 | 0.1339 | 42.33 |
| 2.2 | 21.25 | 13.76 | 0.1403 | 41.89 |
| 2.2 | 21.75 | 13.03 | 0.1470 | 39.67 |
| 2.2 | 22.25 | 12.35 | 0.1537 | 37.58 |
| 2.2 | 22.75 | 11.87 | 0.1606 | 36.13 |
| 2.2 | 23.25 | 11.11 | 0.1676 | 33.81 |
| 2.2 | 23.75 | 10.81 | 0.1748 | 32.89 |
| 2.2 | 24.25 | 10.24 | 0.1821 | 31.18 |
| 2.2 | 24.75 | 9.573 | 0.1896 | 29.14 |
| 2.2 | 25.25 | 9.204 | 0.1972 | 28.02 |
| 2.2 | 25.75 | 8.527 | 0.2050 | 25.96 |
| 2.2 | 26.25 | 8.194 | 0.2129 | 24.94 |
| 2.2 | 26.75 | 7.755 | 0.2209 | 23.60 |
| 2.2 | 27.25 | 7.201 | 0.2291 | 21.92 |
| 2.2 | 27.75 | 6.867 | 0.2374 | 20.90 |
| 2.2 | 28.25 | 6.436 | 0.2459 | 19.59 |

TABLE C.6: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=2.2 \mathrm{GeV}$

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.4 | 15.25 | 23.11 | 0.0793 | 64.50 |
| 2.4 | 15.75 | 21.91 | 0.0846 | 61.14 |
| 2.4 | 16.25 | 21.35 | 0.08996 | 59.56 |
| 2.4 | 16.75 | 20.35 | 0.09554 | 56.77 |
| 2.4 | 17.25 | 19.15 | 0.1013 | 53.42 |
| 2.4 | 17.75 | 18.60 | 0.1072 | 51.89 |
| 2.4 | 18.25 | 17.77 | 0.1133 | 49.57 |
| 2.4 | 18.75 | 17.06 | 0.1195 | 47.61 |
| 2.4 | 19.25 | 16.23 | 0.1259 | 45.29 |
| 2.4 | 19.75 | 15.30 | 0.1325 | 42.68 |
| 2.4 | 20.25 | 14.93 | 0.1392 | 41.67 |
| 2.4 | 20.75 | 14.17 | 0.1461 | 39.52 |
| 2.4 | 21.25 | 13.12 | 0.1531 | 36.62 |
| 2.4 | 21.75 | 12.76 | 0.1603 | 35.61 |
| 2.4 | 22.25 | 11.87 | 0.1677 | 33.12 |
| 2.4 | 22.75 | 11.45 | 0.1752 | 31.95 |
| 2.4 | 23.25 | 10.81 | 0.1829 | 30.17 |
| 2.4 | 23.75 | 10.16 | 0.1907 | 28.33 |
| 2.4 | 24.25 | 9.786 | 0.1987 | 27.31 |
| 2.4 | 24.75 | 9.043 | 0.2068 | 25.23 |
| 2.4 | 25.25 | 8.573 | 0.2152 | 23.92 |
| 2.4 | 25.75 | 8.060 | 0.2236 | 22.49 |
| 2.4 | 26.25 | 7.604 | 0.2322 | 21.22 |
| 2.4 | 26.75 | 7.213 | 0.2410 | 20.12 |
| 2.4 | 27.25 | 6.702 | 0.2499 | 18.70 |
| 2.4 | 27.75 | 6.441 | 0.2590 | 17.97 |
| 2.4 | 28.25 | 5.983 | 0.2682 | 16.70 |
| 2.4 | 28.75 | 5.671 | 0.2776 | 15.82 |
| 2.4 | 29.25 | 5.392 | 0.2871 | 15.05 |

Table C.7: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=2.4 \mathrm{GeV}$

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / d t$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.6 | 15.75 | 21.58 | 0.0916 | 55.57 |
| 2.6 | 16.25 | 20.63 | 0.0975 | 53.12 |
| 2.6 | 16.75 | 19.82 | 0.1035 | 51.06 |
| 2.6 | 17.25 | 18.88 | 0.1097 | 48.64 |
| 2.6 | 17.75 | 17.61 | 0.1161 | 45.36 |
| 2.6 | 18.25 | 17.24 | 0.1227 | 44.40 |
| 2.6 | 18.75 | 16.35 | 0.1295 | 42.11 |
| 2.6 | 19.25 | 15.56 | 0.1364 | 40.08 |
| 2.6 | 19.75 | 14.83 | 0.1435 | 38.20 |
| 2.6 | 20.25 | 13.85 | 0.1508 | 35.66 |
| 2.6 | 20.75 | 13.41 | 0.1582 | 34.54 |
| 2.6 | 21.25 | 12.50 | 0.1659 | 32.18 |
| 2.6 | 21.75 | 11.79 | 0.1737 | 30.36 |
| 2.6 | 22.25 | 11.26 | 0.1816 | 29.00 |
| 2.6 | 22.75 | 10.45 | 0.1898 | 26.92 |
| 2.6 | 23.25 | 10.04 | 0.1981 | 25.86 |
| 2.6 | 23.75 | 9.354 | 0.2066 | 24.09 |
| 2.6 | 24.25 | 8.864 | 0.2153 | 22.83 |
| 2.6 | 24.75 | 8.381 | 0.2241 | 21.59 |
| 2.6 | 25.25 | 7.735 | 0.2331 | 19.92 |
| 2.6 | 25.75 | 7.377 | 0.2422 | 19.00 |
| 2.6 | 26.25 | 6.740 | 0.2516 | 17.36 |
| 2.6 | 26.75 | 6.518 | 0.2611 | 16.79 |
| 2.6 | 27.25 | 6.064 | 0.2707 | 15.62 |
| 2.6 | 27.75 | 5.608 | 0.2806 | 14.44 |
| 2.6 | 28.25 | 5.324 | 0.2906 | 13.71 |
| 2.6 | 28.75 | 4.88 | 0.3007 | 12.57 |
| 2.6 | 29.25 | 4.615 | 0.311 | 11.89 |
| 2.6 | 29.75 | 4.348 | 0.3215 | 11.20 |

Table C.8: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=2.6 \mathrm{GeV}$

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $d \sigma / d \Omega\left(\theta_{c m}\right)$ <br> $[\mathrm{mb}]$ | $-t$ <br> $(\mathrm{GeV} / \mathrm{c})^{2}$ | $d \sigma / \mathrm{dt}$ <br> $\left[\mathrm{mb} /(\mathrm{GeV} / \mathrm{c})^{2}\right]$ |
| :---: | :---: | :---: | :---: | :---: |
| 2.8 | 16.25 | 20.12 | 0.1049 | 48.13 |
| 2.8 | 16.75 | 19.10 | 0.1115 | 45.67 |
| 2.8 | 17.25 | 17.84 | 0.1182 | 42.66 |
| 2.8 | 17.75 | 17.11 | 0.1251 | 40.93 |
| 2.8 | 18.25 | 16.16 | 0.1321 | 38.65 |
| 2.8 | 18.75 | 15.48 | 0.1394 | 37.01 |
| 2.8 | 19.25 | 14.56 | 0.1469 | 34.83 |
| 2.8 | 19.75 | 13.71 | 0.1545 | 32.80 |
| 2.8 | 20.25 | 13.07 | 0.1624 | 31.26 |
| 2.8 | 20.75 | 12.17 | 0.1704 | 29.11 |
| 2.8 | 21.25 | 11.81 | 0.1786 | 28.24 |
| 2.8 | 21.75 | 10.89 | 0.1870 | 26.04 |
| 2.8 | 22.25 | 10.09 | 0.1956 | 24.13 |
| 2.8 | 22.75 | 9.771 | 0.2044 | 23.37 |
| 2.8 | 23.25 | 8.991 | 0.2133 | 21.50 |
| 2.8 | 23.75 | 8.505 | 0.2225 | 20.34 |
| 2.8 | 24.25 | 7.938 | 0.2318 | 18.98 |
| 2.8 | 24.75 | 7.452 | 0.2413 | 17.82 |
| 2.8 | 25.25 | 7.020 | 0.2510 | 16.79 |
| 2.8 | 25.75 | 6.449 | 0.2609 | 15.42 |
| 2.8 | 26.25 | 6.015 | 0.2709 | 14.39 |
| 2.8 | 26.75 | 5.586 | 0.2812 | 13.36 |
| 2.8 | 27.25 | 5.278 | 0.2916 | 12.62 |
| 2.8 | 27.75 | 4.915 | 0.3022 | 11.76 |
| 2.8 | 28.25 | 4.633 | 0.3129 | 11.08 |
| 2.8 | 28.75 | 4.251 | 0.3239 | 10.17 |
| 2.8 | 29.25 | 3.900 | 0.3350 | 9.326 |
| 2.8 | 29.75 | 3.749 | 0.3463 | 8.966 |
| 2.8 | 30.25 | 3.425 | 0.3577 | 8.191 |

Table C.9: Unpolarised differential cross section $d \sigma / d \Omega$ in $p p$ elastic scattering at $T_{p}=2.8 \mathrm{GeV}$

## Appendix D

## Numerical values of $A_{y}$ in $\vec{p} d$ elastic scattering

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 0.796 | 7.5 | 0.2573 | 0.0116 |
| 0.796 | 8.5 | 0.2680 | 0.0040 |
| 0.796 | 9.5 | 0.2929 | 0.0032 |
| 0.796 | 10.5 | 0.3156 | 0.0029 |
| 0.796 | 11.5 | 0.3401 | 0.0029 |
| 0.796 | 12.5 | 0.3582 | 0.0028 |
| 0.796 | 13.5 | 0.3778 | 0.0024 |
| 0.796 | 14.5 | 0.3923 | 0.0027 |
| 0.796 | 15.5 | 0.4099 | 0.0029 |
| 0.796 | 16.5 | 0.4153 | 0.0031 |
| 0.796 | 17.5 | 0.4226 | 0.0034 |
| 0.796 | 18.5 | 0.4253 | 0.0037 |
| 0.796 | 19.5 | 0.4272 | 0.0040 |
| 0.796 | 20.5 | 0.4335 | 0.0044 |
| 0.796 | 21.5 | 0.4340 | 0.0049 |
| 0.796 | 22.5 | 0.4304 | 0.0057 |
| 0.796 | 23.5 | 0.4252 | 0.0066 |
| 0.796 | 24.5 | 0.4112 | 0.0076 |
| 0.796 | 25.5 | 0.4054 | 0.0090 |
| 0.796 | 26.5 | 0.4242 | 0.0110 |
| 0.796 | 27.5 | 0.3984 | 0.0164 |
| 0.796 | 28.5 | 0.4055 | 0.0904 |

Table D.1: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=0.796 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.6 | 5.5 | 0.1153 | 0.0031 |
| 1.6 | 6.5 | 0.1056 | 0.0016 |
| 1.6 | 7.5 | 0.1267 | 0.0013 |
| 1.6 | 8.5 | 0.1390 | 0.0014 |
| 1.6 | 9.5 | 0.1463 | 0.0013 |
| 1.6 | 10.5 | 0.1561 | 0.0015 |
| 1.6 | 11.5 | 0.1674 | 0.0016 |
| 1.6 | 12.5 | 0.1694 | 0.0018 |
| 1.6 | 13.5 | 0.1790 | 0.0021 |
| 1.6 | 14.5 | 0.1815 | 0.0024 |
| 1.6 | 15.5 | 0.1736 | 0.0027 |
| 1.6 | 16.5 | 0.1840 | 0.0032 |
| 1.6 | 17.5 | 0.1719 | 0.0038 |
| 1.6 | 18.5 | 0.1877 | 0.0046 |
| 1.6 | 19.5 | 0.1925 | 0.0100 |

Table D.2: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=1.6 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.8 | 5.5 | 0.1227 | 0.0017 |
| 1.8 | 6.5 | 0.1324 | 0.0012 |
| 1.8 | 7.5 | 0.1430 | 0.0010 |
| 1.8 | 8.5 | 0.1538 | 0.0009 |
| 1.8 | 9.5 | 0.1647 | 0.0009 |
| 1.8 | 10.5 | 0.1807 | 0.0011 |
| 1.8 | 11.5 | 0.1855 | 0.0012 |
| 1.8 | 12.5 | 0.1909 | 0.0014 |
| 1.8 | 13.5 | 0.1997 | 0.0016 |
| 1.8 | 14.5 | 0.2067 | 0.0019 |
| 1.8 | 15.5 | 0.2018 | 0.0022 |
| 1.8 | 16.5 | 0.1969 | 0.0027 |
| 1.8 | 17.5 | 0.1970 | 0.0037 |

Table D.3: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=1.8 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.965 | 4.5 | 0.1003 | 0.0110 |
| 1.965 | 5.5 | 0.0968 | 0.0024 |
| 1.965 | 6.5 | 0.1077 | 0.0019 |
| 1.965 | 7.5 | 0.1230 | 0.0017 |
| 1.965 | 8.5 | 0.1324 | 0.0014 |
| 1.965 | 9.5 | 0.1410 | 0.0016 |
| 1.965 | 10.5 | 0.1524 | 0.0018 |
| 1.965 | 11.5 | 0.1616 | 0.0020 |
| 1.965 | 12.5 | 0.1645 | 0.0023 |
| 1.965 | 13.5 | 0.1665 | 0.0027 |
| 1.965 | 14.5 | 0.1738 | 0.0032 |
| 1.965 | 15.5 | 0.1601 | 0.0039 |
| 1.965 | 16.5 | 0.1620 | 0.0049 |
| 1.965 | 17.5 | 0.1560 | 0.0127 |

TABLE D.4: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=1.965 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.157 | 4.5 | 0.0862 | 0.0074 |
| 2.157 | 5.5 | 0.0922 | 0.0028 |
| 2.157 | 6.5 | 0.1053 | 0.0024 |
| 2.157 | 7.5 | 0.1127 | 0.0020 |
| 2.157 | 8.5 | 0.1264 | 0.0019 |
| 2.157 | 9.5 | 0.1330 | 0.0022 |
| 2.157 | 10.5 | 0.1415 | 0.0025 |
| 2.157 | 11.5 | 0.1487 | 0.0029 |
| 2.157 | 12.5 | 0.1550 | 0.0033 |
| 2.157 | 13.5 | 0.1606 | 0.0039 |
| 2.157 | 14.5 | 0.1603 | 0.0047 |
| 2.157 | 15.5 | 0.1532 | 0.0059 |
| 2.157 | 16.5 | 0.1500 | 0.0107 |

TABLE D.5: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=2.157 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.368 | 4.5 | 0.0821 | 0.0045 |
| 2.368 | 5.5 | 0.0910 | 0.0023 |
| 2.368 | 6.5 | 0.0993 | 0.0021 |
| 2.368 | 7.5 | 0.1132 | 0.0017 |
| 2.368 | 8.5 | 0.1179 | 0.0018 |
| 2.368 | 9.5 | 0.1248 | 0.0020 |
| 2.368 | 10.5 | 0.1319 | 0.0024 |
| 2.368 | 11.5 | 0.1355 | 0.0028 |
| 2.368 | 12.5 | 0.1430 | 0.0033 |
| 2.368 | 13.5 | 0.1474 | 0.0040 |
| 2.368 | 14.5 | 0.1357 | 0.0050 |
| 2.368 | 15.5 | 0.1333 | 0.0082 |
| 2.368 | 16.5 | 0.1498 | 0.0107 |

Table D.6: Analysing power $A_{y}$ in $\vec{p} d$ elastic scattering at $T_{p}=2.368 \mathrm{GeV}$.

## Appendix E

## Numerical values of $A_{y}$ in $\vec{p} n$ quasi-free elastic scattering

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 0.796 | 18 | 0.270 | 0.018 |
| 0.796 | 20 | 0.290 | 0.018 |
| 0.796 | 22 | 0.278 | 0.016 |
| 0.796 | 24 | 0.328 | 0.022 |

Table E.1: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}$ $=0.796 \mathrm{GeV}$.

| $T_{p}$ <br> $[\mathrm{GeV}]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.6 | 14 | 0.137 | 0.018 |
| 1.6 | 17 | 0.151 | 0.015 |
| 1.6 | 20 | 0.153 | 0.015 |
| 1.6 | 23 | 0.170 | 0.016 |
| 1.6 | 26 | 0.169 | 0.018 |

TABLE E.2: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}$ $=1.6 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.8 | 13.5 | 0.125 | 0.011 |
| 1.8 | 16.5 | 0.145 | 0.008 |
| 1.8 | 19.5 | 0.152 | 0.008 |
| 1.8 | 22.5 | 0.148 | 0.009 |
| 1.8 | 25.5 | 0.158 | 0.010 |

Table E.3: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}$ $=1.8 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 1.965 | 13.5 | 0.108 | 0.016 |
| 1.965 | 16.5 | 0.119 | 0.011 |
| 1.965 | 19.5 | 0.138 | 0.011 |
| 1.965 | 22.5 | 0.112 | 0.012 |
| 1.965 | 25.5 | 0.141 | 0.013 |
| 1.965 | 28.5 | 0.127 | 0.022 |

Table E.4: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}$ $=1.965 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.157 | 14 | 0.091 | 0.016 |
| 2.157 | 17 | 0.103 | 0.013 |
| 2.157 | 20 | 0.111 | 0.013 |
| 2.157 | 23 | 0.143 | 0.014 |
| 2.157 | 26 | 0.115 | 0.017 |
| 2.157 | 29 | 0.141 | 0.026 |

TABLE E.5: Analysing power $A_{y}\left(\theta_{c m}\right)$ in $\vec{p} n$ quasi-free elastic scattering at $T_{p}$ $=2157 \mathrm{GeV}$.

| $T_{p}$ <br> $[G e V]$ | $\theta_{c m}$ <br> $\left[{ }^{\circ}\right]$ | $A_{y}\left(\theta_{c m}\right)$ | $\Delta A_{y}\left(\theta_{c m}\right)$ |
| :---: | :---: | :---: | :---: |
| 2.368 | 17 | 0.085 | 0.011 |
| 2.368 | 20 | 0.102 | 0.012 |
| 2.368 | 23 | 0.102 | 0.013 |
| 2.368 | 26 | 0.122 | 0.016 |
| 2.368 | 29 | 0.100 | 0.021 |

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## Publikationen

## mit Daten aus der vorliegenden Dissertation

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