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## Scaling of H-mode threshold power and L-H edge conditions with favorable ion grad-B drift in Alcator C-Mod tokamak

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### Abstract

The low-to-high confinement transition (L-H) has been systematically studied in Alcator C-Mod lower single null (favorable ion grad-B drift) plasmas, covering an extensive global plasma parameter space. Plasma density ( $\bar{n}_e$ ), toroidal magnetic field strength ( $B_T$ ), and plasma current ( $I_p$ ) dependence of H-mode threshold power ( $P_{th}$ ) and local plasma edge conditions are investigated. The  $P_{th}$  dependence on density is nonlinear and has a “U-shape”, which is not sensitive to plasma current variation, and affected by  $B_T$  mainly in low densities. The L-H local edge conditions, including the amplitude and gradient scale length of  $T_e$ ,  $n_e$  profiles, are evaluated at times just before L-H and at two radial locations:  $\rho=0.95$  and  $\rho=1.0$ . The behavior of edge conditions at the two locations exhibit a number of major differences in terms of their scaling with global parameters. In all, the scaling of L-H  $P_{th}$  and edge conditions are complex, neither of which can be simply represented by a relation of the type  $\bar{n}_e^x B_T^y I_p^z$ . Local parameters are also evaluated in low power L-mode and compared with the L-H companion. Noticeable differences between L-mode and L-H are mainly observed in  $T_e$  at  $\rho=0.95$  and  $L_n$ ,  $L_T$  near separatrix, while other parameters are found to be not significantly changed. Comparison with resistive-ballooning mode theory yield reasonable good agreement, such that the experimental data at  $\rho=0.95$  fit into the corresponding L-mode and H-mode domains, as well as L-H boundary predicted by theory. A period of improved energy confinement similar to I-mode is identified in a few low density 5.4T discharges prior to L-H transition.

## 1. Introduction

Since the first experimental demonstration of H-mode [1], the low-to-high confinement transition (L-H) studies have attracted considerable research efforts: not only the transition physics per se is of great interest, but also because this subject is closely related to the important issue of predicting required threshold power for H-mode access ( $P_{th}$ ), which is a critical engineering parameter in the design of new tokamaks, e.g. ITER. Early studies were focused on assembling data of  $P_{th}$  from multiple devices into a database and extracting an empirical scaling law with global plasma parameters out of it. These works yielded the international tokamak scaling [2]:

$$P_{th} [MW] = 0.049 \bar{n}_e [10^{20} m^{-3}]^{0.72} B_T [T]^{0.8} S [m^2]^{0.94}$$

, which indicates that the three primary dependencies of  $P_{th}$  are plasma density, strength of toroidal magnetic field, and plasma surface area. Large departures from the scaling law prediction have been constantly discovered: one is the ‘U-shape’-like non-monotonic density scaling seen on several devices (e.g. AUG [3], JET [4], also C-mod [5] as shown later in this paper), where magnitudes of  $P_{th}$  were found to substantially increase below a threshold density, and demonstrate significant divergence from the scaling law. This low density regime has become a concern for ITER, since if ITER is operated there, the scaling law based target design of its required auxiliary heating capability might be insufficient to ensure H-mode access. As a consequence, using the scaling law as a first principle predicting tool may not be reliable enough; the importance of understanding the underlying physics needs to be invoked.

Compared with  $P_{th}$ , threshold plasma edge conditions are considered to be more directly and closely related to L-H physics, hence a comprehensive characterization of them could yield more phenomenological understanding of L-H onset and provide some guidance to experiments. Besides, studying the edge conditions could also help identify the potential L-H ‘critical parameters’ and test their validity. For example,  $T_{e,95}$ , the electron temperature in plasma edge, has been considered as the critical condition for L-H transition and widely investigated in the past. Some earlier works [6][7][8] suggest that  $T_{e,95}$  is generally a good metric: magnitudes in L-mode are distinguishably lower than in H-mode plasmas, and the two domains are usually seen to be clearly divided by the L-H threshold boundary. The dependence of L-H threshold  $T_{e,95}$  on global plasma parameters, e.g.  $\bar{n}_e$ ,  $B_T$ , and  $I_p$  was studied in these works via regression analysis, which led to power law based scaling of the type  $T_{e,95} \sim \bar{n}_e^x B_T^y I_p^z$ . Another important reason for studying threshold plasma conditions is that they can either be directly compared with, or to be used as input variables to test various theoretical models proposed for L-H transition. These comparisons can improve the understanding of the physical mechanism that triggers L-H.

The core of this paper is to examine the plasma density,  $B_T$ , and  $I_p$  dependence of  $P_{th}$  and local plasma edge conditions in standard Alcator C-Mod lower single null plasmas in a broad global parameter space, which will be the themes of section 3 and section 4. Section 2 will briefly discuss experimental conditions and data analysis techniques;

section 5 will show results from the comparisons between resistive-ballooning mode theory and experiments; section 6 will demonstrate the existence of improved energy confinement prior to L-H transition in low density plasmas; section 7 includes conclusions and future work.

## 2. Experimental description and data analysis

### 2.1. Experimental description

The discharges included in this study are all deuterium plasmas and originate from dedicated L-H transition or H-mode pedestal experiments between 2005 and 2010 C-mod experimental campaigns. This large set spans a wide variation of global plasma conditions: line averaged plasma density ( $\bar{n}_e$ ) between  $0.6 \times 10^{20} \text{m}^{-3}$  and  $2.5 \times 10^{20} \text{m}^{-3}$ , toroidal magnetic fields ( $B_T$ ) from 3.5T and 5.4T, and plasma currents ( $I_p$ ) ranging from 0.6MA to 1.4MA. Equilibrium magnetic configurations for these discharges are maintained to be nearly fixed, with  $\kappa \sim 1.7$ ,  $\delta_{\text{upper}} \sim 0.35$ ,  $\delta_{\text{lower}} \sim 0.5$ . All these plasmas were created in lower single null configuration, with ion grad-B drift in the favorable direction for H-mode access. Most low density ( $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ ) plasmas in the set originate from two dedicated L-H transition experiments: one conducted in  $B_T = 5.4\text{T}$  plasmas during 2007 C-mod campaign (later, data from this experiment are displayed in different symbols in order to be distinguished from other 5.4T data), the other one in 2008 campaign with  $B_T / I_p$  operated at 3.5T/0.6MA. In addition to density variation, plasma currents were also scanned at three values (0.6,0.9,1.2MA) in the 2007 experiment. Cryopump, as demanded, was utilized in low density experiment to provide better plasma density control and reduce the edge fuelling sources.

In most scenarios, Ohmic power alone is not sufficient to induce L-H transition. For all quoted discharges, L-H confinement bifurcations were obtained by applying auxiliary heating power, which is solely ICRF, during  $B_T$  and  $I_p$  flattops, i.e. periods in which neither  $B_T$  or  $I_p$  is significantly varied. ICRF antenna frequency on C-Mod can be adjusted between 40 and 80MHz, and was tuned at the value according to the specific operational  $B_T$  to perform on-axis hydrogen fundamental minority heating. Input ICRF power was added in a slow continuous ramp-up pattern, providing a broad range of input power which covers the L-H threshold.

A defined L-H transition is usually discerned by the simultaneous occurrence of the following experimental evidence: an abrupt sharp drop of divertor  $D_\alpha$  emission, a clear break-in-slope rise of line averaged density and confined plasma energy, an enhanced burst of edge electron temperature, and a suppression of plasma turbulence. Accessed H-mode plasmas exhibit prompt formation of both edge temperature and density pedestals following L-H transition. Time histories of some key plasma parameters resolving a typical L-H transition followed by a series of L-H-L transitions are shown by Fig.1.

## 2.2. Diagnostics and data analysis

Some key C-mod diagnostics are needed to provide relevant measurements. Among them, the Thomson scattering (TS) system [9] operated with up to two Nd:YAG lasers each at 30Hz and pulsed alternatively is used as the chief diagnostic for electron temperature ( $T_e$ ) and density ( $n_e$ ) measurements along a vertical chord through the magnetic axis. The spatial resolution of TS measured profiles, when mapped to midplane, is  $\sim$ cm in plasma core and 1~2mm in the plasma edge. Electron cyclotron emission (ECE) diagnostics provide sub ms midplane electron temperature measurements at reduced spatial resolution. Line integrated plasma density is recorded by a multi-chord two-color CW interferometer system. Phase contrast imaging (PCI) and magnetic pick-up coils are used to monitor plasma density and magnetic fluctuations, respectively. For a limited number of discharges, edge impurity (boron) ion temperature ( $T_I$ ) is measured by B<sup>5+</sup> charge exchange recombination spectroscopy. Illustration of measurement locations for these diagnostics relative to a cut of C-Mod poloidal cross section is shown by Fig.2.

The TS measured  $T_e$  and  $n_e$  are mapped to the midplane using the equilibrium reconstruction code EFIT [10]. Then these mapped measurements, combined with the  $T_e$  data collected by ECE and evaluated at the corresponding TS time slices, are fitted into smooth curves to generate global radial profiles of  $T_e$  and  $n_e$ . The edge data, referred to those with  $r > a_0 - 2\text{cm}$ , are fitted utilizing the modified *tanh* function as defined in [11]. Typical examples of edge TS measurements and profile fitting are represented by Fig.3. The included data originate from the last two TS laser pulses before an L-H transition. This figure shows the case of both a high density ( $\bar{n}_e \sim 1.8 \times 10^{20} \text{m}^{-3}$ ) and a low density ( $\bar{n}_e \sim 0.8 \times 10^{20} \text{m}^{-3}$ ) discharge, which is a stringent test for the quality of TS data and profile fitting because of the low  $S/N$ . Although the measurement uncertainties can be larger compared with cases of higher densities, the profile fitting is still quite reliable.

The EFIT returned separatrix radial locations have been routinely used, which for most cases are seen to be reasonably accurate. The uncertainties from EFIT separatrix findings are usually of a few *mm*, thus the induced data scatters need to be taken into account and reduced. In the following sections, the profiles for each included discharges are shifted in the radial direction, so that the EFIT separatrix is aligned with the location of maximum  $d^2P_e/dr^2$ , which is nearly the pedestal foot of electron pressure ( $P_e = n_e T_e$ ) profile in the sense of modified *tanh* function [11]. The required adjustments are seen to be generally minor for most cases, which are found to be within *3mm*. We examined that the general trends discussed in the following sections are not changed by such small shifts. Another approach employed in this study to reduce data scatter is averaging data over a finite radial extent, and using the mean values within the entire region in the evaluation. This method will be employed later (section 4, 5) in assessing local edge plasma conditions, specifically the profile gradient scale lengths.

## 3. H-mode threshold power

H-mode threshold power is characterized by the total power loss to the plasma boundary, which is defined according to [2] as:

$$P_{th} = P_{tot} - dW/dt = P_{OH} + P_{aux} - dW/dt$$

, and assessed at L-H transition times. In the above definition,  $P_{OH}$  is the Ohmic heating power and  $dW/dt$  is the time derivative of plasma stored energy, both are calculated using the EFIT code. ICRF is the sole auxiliary heating source employed in this study, so in this case  $P_{aux} = cP_{RF}$ , where  $P_{RF}$  is the net input ICRF power measured by waveguide couplers, and a numerical factor  $c$  is multiplied to account for the fractional absorption of ICRF power by plasmas. Measured minority ion density concentrations relative to main ion ( $n_H/n_D$ ) for most quoted discharges were about 5%-10%, which is efficient for single pass ICRF power absorption in the hydrogen minority heating scenario [12]. Accurately knowing the value of  $c$  requires dedicated numerical ICRF wave simulation, which is beyond the scope of this study. Some earlier studies [12] proposed a reasonable estimate of  $c$  based on ECE break-in-slope measurements to be about 90% in normal C-mod discharge conditions. For simplicity, we make the assumption that ICRF power launched by antennas are 100% absorbed, thus  $c=1.0$  and  $P_{tot} = P_{OH} + P_{RF}$ . The difference between assuming  $c=1.0$  and  $c=0.9$  can induce some minor discrepancies ( $<0.3\text{MW}$ ) in calculating  $P_{th}$ , but will not change the general conclusions. The net power loss,  $P_{net} = P_{th} - P_{rad,main}$  may be a more appropriate quantity to characterize the H-mode threshold power. Upon an examination, the  $P_{rad,main}$  for the included discharges are mostly about  $0.3\text{MW}$  and essentially independent of density. So the overall trend of  $P_{net}$  is basically differed from that of  $P_{th}$  by an offset.

As shown in Fig.4,  $P_{th}$  in 5.4T exhibits a clear ‘U-shape’, which decreases monotonically with density for  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ , while it increases with density for  $\bar{n}_e > 1.8 \times 10^{20} \text{m}^{-3}$ . In the broad range between the two limits, the  $P_{th}$  exhibits a local minimum, which is close to  $1.5\text{MW}$  and basically invariant with density. The same behavior of  $P_{th}$  in the low density regime ( $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ ) was also reported in a dedicated study of the 2007 experiment [5]. The overall trend with  $\bar{n}_e$  can be nearly represented by a simple analytical function of  $1.5/\bar{n}_e^2 + 0.2\bar{n}_e^{3.5}$ , as shown by the dashed curve on Fig.4. Predictions from the international tokamak scaling (solid line, with  $B_T = 5.4\text{T}$ ,  $S \sim 7.5\text{m}^2$ ) are compared, which is seen to deviate from experimental data at most places, especially for  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$  and  $\bar{n}_e > 2.0 \times 10^{20} \text{m}^{-3}$ , where the scaling law prediction seem to be much lower. Moreover, the plasma density dependence suggested by the scaling law is nearly linear ( $\sim \bar{n}_e^{0.7}$ ), which is completely different than the experimental observation. Although  $I_p$  is varied by a factor of 2 in these discharges, data of  $P_{th}$  exhibit no clear  $I_p$  dependence in the range of  $0.6 \times 10^{20} \text{m}^{-3} < \bar{n}_e < 2.2 \times 10^{20} \text{m}^{-3}$ . It means that  $P_{th}$  is better correlated with plasma density, rather than normalized Greenwald fraction  $\bar{n}_e/n_G$ , where  $n_G [10^{20} \text{m}^{-3}] = I_p [MA]/(\pi a_0 [m]^2)$  is the Greenwald density. In absence of sufficient data,  $I_p$  dependence for  $\bar{n}_e > 2.2 \times 10^{20} \text{m}^{-3}$  is unknown. As previously noted, a similar ‘U-shape’ dependence of  $P_{th}$  on density has also been observed on many devices, e.g. AUG[3], JET[4], etc, suggesting that this feature might be universal, although the values of density at minimum  $P_{th}$  differ, and the underlying physics for these are still not well understood.

To reveal the role played by toroidal magnetic field ( $B_T$ ), data from lower  $B_T$  (3.5T, 4.6T) discharges are shown together with portions ( $I_p=0.6-1.0\text{MA}$ ) of 5.4T data on Fig.5. The  $B_T$  dependence of  $P_{th}$  is mainly seen at low density of  $\bar{n}_e < 0.9 \times 10^{20} \text{m}^{-3}$ , where for fixed  $\bar{n}_e$ , values of  $P_{th}$  in lower  $B_T$  are noticeably smaller. However, as  $\bar{n}_e$  is increased above  $1.0 \times 10^{20} \text{m}^{-3}$ , values of  $P_{th}$  from various  $B_T$  at a certain  $\bar{n}_e$  are seen to be close, which suggest that the  $B_T$  dependence diminishes or may even vanish at higher density. The overall density scaling tend to remain ‘U-shape’ in lower  $B_T$ , however, owing to the existence of  $B_T$  effects, the enhancement of  $P_{th}$  in low densities becomes less pronounced. An approximate curve fitting of 3.5T data is shown by the green dashed line in Fig.5. Comparing with the 5.4T one (black dashed line) suggests that the density at minimum  $P_{th}$  varies with  $B_T$ . For  $B_T > 6.0\text{T}$ , the fundamental hydrogen minority heating scenario can not be realized in C-Mod plasmas. To avoid confusion in data interpretation induced by the discrepancies in heating schemes, those data are not included for comparison. Therefore, the density scaling of  $P_{th}$  in high  $B_T$  ( $B_T > 5.4\text{T}$ ) plasmas remains unknown.

In all, the above experimental evidence suggests that the density and  $B_T$  dependence of  $P_{th}$  can not be described by a simple relation of the type  $\bar{n}_e^x B_T^y$ . There are indication that the correlations with the two variables ( $\bar{n}_e, B_T$ ) can be convoluted, for example, the specific  $B_T$  dependence varies with density as already seen. The poor agreement between the scaling law predictions and experimental results reinforce the importance of understanding L-H edge conditions and their relations with H-mode threshold power, eventually aiming at a physics-based reliable prediction capability.

#### 4. Edge plasma conditions

Compared with global threshold power, which could be influenced by many physical and engineering factors (e.g. RF power absorption efficiency, neutrals, wall conditions, energy confinement, etc), plasma conditions either in the edge or scrape-off layer (SOL) region are expected to be more relevant to L-H physics. In this section, characterization of local edge conditions and their scaling with  $\bar{n}_e$ ,  $I_p$  and  $B_T$  are examined both near L-H threshold and in low power L-mode, in order to improve the understanding of the local criteria achieved at (perhaps also required for) L-H transition, and to provide inputs to test various proposed models.

The edge plasma conditions near L-H threshold (still in L-mode) are examined in 4.1 and 4.2. The evaluation is performed in the same set of discharges involved before, using the  $T_e$  and  $n_e$  profiles obtained by fitting into the data from the last two TS pulses prior to L-H, and radially shifted according to the criteria stated earlier in section 2. The edge conditions are assessed at two radial locations of  $\rho=0.95$ , which is approximately at  $a_0-8\text{mm}$  in minor radius, and  $\rho=1.0$ , which is the EFIT separatrix, or equivalently the  $P_e$  ‘pedestal foot’ after the alignment. Here,  $\rho$  is the normalized poloidal flux.

Parameters employed to characterize the local  $T_e$  and  $n_e$  profile shapes are their gradient scale length, normalized to midplane plasma minor radius  $a_0$ , i.e.,  $a_0/L_T=(a_0/T_e)dT_e/dr$  and  $a_0/L_n=(a_0/n_e)dn_e/dr$ . Amplitudes of  $a_0/L_T$  and  $a_0/L_n$  are seen to increase substantially in the narrow region between  $\rho=0.95$  ( $r\sim a_0-8\text{mm}$ ) and  $\rho=1.0$ , as seen from Fig.6.d-e. To reduce data scatter, the means of  $a_0/L_T$  and  $a_0/L_n$  within the two shaded areas (see Fig.6) are used as the values for  $\rho=0.95$  and  $\rho=1.0$ , respectively. Local conditions of  $T_e$  and  $n_e$  are assessed at the two specific locations, which are marked by the two dashed lines in Fig.6. All data are displayed against the  $\bar{n}_e$  evaluated at the corresponding L-H times for each discharge. The error bars shown on some data in Fig.7-10 are estimated utilizing the Monte Carlo profile error analysis technique [13].

Before a detailed examination of the parametric dependence of L-H threshold local edge conditions, some edge profiles are assembled and displayed together in Fig.6 to provide an intuitive sense. Plasmas of the demonstrated profiles cover a parameter space of 2 plasma densities ( $\bar{n}_e\sim 0.7\times 10^{20}\text{m}^{-3}$ ,  $1.0\times 10^{20}\text{m}^{-3}$ ), 2 values of  $B_T$  ( $B_T=3.5\text{T}$ ,  $5.4\text{T}$ ), and 3 plasma currents ( $I_p=0.6$ ,  $0.9$ ,  $1.2\text{MA}$ ). Some features are clearly exhibited by these plots, for example, with similar plasma density (say  $\bar{n}_e\sim 1.0\times 10^{20}\text{m}^{-3}$ ), near separatrix  $T_e$  profiles are maintained approximately identical in shape (see plot of  $a_0/L_T$ ). Progressing radially inward to  $\rho=0.95$ , we see that  $T_e$  profiles with different  $I_p$  (at similar density and  $B_T$ ) clearly diverge, such that the one with higher  $I_p$  becomes much steeper (correspond to larger  $a_0/L_T$ ), hence  $I_p$  dependence of  $T_e$  gradient scale lengths emerge at this location. These observations are also verified below in 4.1 and 4.2, where more characteristics of L-H edge conditions will be demonstrated.

#### 4.1. L-H local conditions at $\rho=0.95$

We start the discussion with focus a on 5.4T data to examine plasma density and  $I_p$  dependence of  $T_{e,95}$  and  $P_{e,95}$  ( $T_e$  and  $P_e$  at  $\rho=0.95$ ) at L-H threshold. First, remarkable enhancement of  $T_{e,95}$  is clearly identified in low densities ( $\bar{n}_e < 1.0 \times 10^{20}\text{m}^{-3}$ ), as shown by Fig.7.a, the manifested trend can be nearly represented by  $\sim 1/\bar{n}_e$  relation. Recall this is also the density range where H-mode  $P_{th}$  exhibit a strong inverse density scaling ( $\sim 1/\bar{n}_e^2$ ) as seen before. However, the  $\sim 1/\bar{n}_e$  dependence of  $T_{e,95}$  is not obeyed in moderate ( $1.0\times 10^{20}\text{m}^{-3} < \bar{n}_e < 1.8\times 10^{20}\text{m}^{-3}$ ) and high ( $\bar{n}_e > 1.8\times 10^{20}\text{m}^{-3}$ ) densities, where we found values of  $T_e$  generally scatter between  $100\text{-}200\text{eV}$  and exhibit no clear trends with  $\bar{n}_e$ . The observed characters of  $T_{e,95}$  at  $\bar{n}_e > 1.0\times 10^{20}\text{m}^{-3}$  are consistent with the result from earlier studies on C-Mod [8], however, the low density branch was not extensively covered in that work. Because  $n_{e,95}$  is well (essentially linearly) correlated with  $\bar{n}_e$  (Fig.7.b), values of  $P_{e,95}$  (Fig.7.c) in the range of  $\bar{n}_e < 1.5\times 10^{20}\text{m}^{-3}$  are maintained close to  $0.1\text{eV}\times 10^{20}\text{m}^{-3}$ , and only exhibit slight variation with density; however, for  $\bar{n}_e > 1.5\times 10^{20}\text{m}^{-3}$ , data of  $P_{e,95}$  manifest a clear prompt rise with density. No clear  $I_p$  dependence has been identified in  $T_e$ ,  $n_e$ , or  $P_e$  at  $\rho=0.95$ .



In Fig.8, data from two lower toroidal fields of  $B_T=3.5\text{T}$  and  $B_T=4.6\text{T}$  are assembled and shown together with portions of 5.4T data to demonstrate the  $B_T$  dependence. We assume that the absence of  $I_p$  dependence on  $T_e$  and  $P_e$  derived from 5.4T data is valid independent of the strength of  $B_T$ . With this assumption, the  $B_T$  dependence of  $T_e$ ,  $n_e$ , and  $P_e$  are investigated by comparing data with different  $B_T$  at similar densities.

The same linear correlation of  $n_{e,95}$  with  $\bar{n}_e$  previously observed in 5.4T data is also followed in cases of lower  $B_T$ . It means that  $n_{e,95}$  is primarily correlated with  $\bar{n}_e$ , and insensitive to either  $I_p$  or  $B_T$  variation. Later it will be shown in 4.2 that this conclusion is also true near the separatrix. The  $B_T$  dependence of  $T_{e,95}$  (Fig.8.a) is more complicated. It is first noticed that for  $\bar{n}_e < 0.9 \times 10^{20} \text{m}^{-3}$  and at fixed  $\bar{n}_e$ , values of  $T_{e,95}$  in lower  $B_T$  (e.g. 3.5T) plasmas are reduced. As  $\bar{n}_e$  increases above  $1.0 \times 10^{20} \text{m}^{-3}$ ,  $T_{e,95}$  is found to be insensitive to  $B_T$ , such that ranges covered by data of different  $B_T$  basically overlap. Consequently, the overall density scaling of  $T_{e,95}$  is affected by  $B_T$  variation: the clear  $\sim 1/\bar{n}_e$  scaling of  $T_{e,95}$  at low density as identified from 5.4T discharges become ambiguous in 3.5T; rather, most 3.5T data as seen are scattered between 100eV and 200eV without showing apparent variation with plasma density. Prior studies done in C-Mod moderate-density ( $\bar{n}_e \sim 1.5 \times 10^{20} \text{m}^{-3}$ ) 8T plasmas [14] suggest a remarkable enhancement of  $T_{e,95}$  compared to 5.4T. This observation casts more questions on the behavior of  $T_{e,95}$  at L-H threshold, which can not be fully answered by this study and requires further investigation. Taken together, these evidence indicate that similar to the circumstance of  $P_{th}$ , the plasma density and/or  $B_T$  dependence of  $T_{e,95}$  can not be simply described by any relation of the type  $\bar{n}_e^x B_T^y$  over an extensive global parameter space.

Fig.9.a-b shows the density scaling of  $T_e$  and  $n_e$  scale lengths in 5.4T plasmas at  $\rho=0.95$ . These plots reveal a notable separation of data with different  $I_p$  in both  $L_T$  and  $L_n$  at fixed density, a feature not seen in either  $T_e$  or  $n_e$  as shown before. For most included data, the magnitudes of  $a_0/L_T$  (Fig.9.a) are found to be approximately proportional to  $I_p$ . However, for  $a_0/L_n$  (Fig.9.b), this proportionality ( $\sim I_p$ ) seems to be mainly identified at  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ . At higher density of  $\bar{n}_e > 1.0 \times 10^{20} \text{m}^{-3}$ ,  $I_p$  dependence of  $a_0/L_n$  tends to be weak or may even vanish. Owing to the existence of  $I_p$  effects, dependence of  $a_0/L_T$  and  $a_0/L_n$  on plasma density can only be examined for some fixed values or a narrow range of plasma currents. Since large portions of  $I_p$  on the plots are concentrated in  $0.8\text{MA} < I_p < 1.0\text{MA}$ , we choose to utilize data with  $I_p$  within this range to elucidate the density dependence. These data suggest a weak inverse correlation of  $a_0/L_T$  with  $\bar{n}_e$ , even for  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ , where  $T_{e,95}$  increase considerably. Therefore at  $\rho=0.95$  with fixed  $I_p$ , shapes of  $T_e$  profiles (i.e.,  $L_T$ ) at L-H seem to be relatively resilient to plasma density variation and maintained similar;  $I_p$ , as indicated, is one primary variable to determine  $T_e$  profile shape at  $\rho=0.95$ . Values of  $a_0/L_n$  at fixed  $I_p$  are found to be close to constant at low density, and decrease monotonically at moderate and high density.

Investigation of  $B_T$  effects on local gradient scale lengths are performed between data of 3.5T/0.6MA and 5.4T/0.6MA. Results are presented in Fig.10. The comparisons have to

be restricted between data with similar  $I_p$ , since it is already known from earlier discussion that gradient scale lengths were highly dependent on  $I_p$ . Similar to that in  $T_{e,95}$ , distinguishable dependence of  $B_T$  on both  $a_0/L_T$  and  $a_0/L_n$  are observed at low density of  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ . Combined with the previously identified  $\sim I_p$  proportionality, it suggests that  $a_0/L_T$  and  $a_0/L_n$  at  $\rho=0.95$  could correlate with  $q_{95}$  ( $q_{95} \sim a_0 B_T / R_0 I_p$ ) at low density. In Fig.11, data of  $\bar{n}_e < 0.9 \times 10^{20} \text{m}^{-3}$  with various  $I_p$  and  $B_T$  are displayed versus  $q_{95}$ , which reveals that  $a_0/L_T$ ,  $a_0/L_n \sim 1/q_{95}$ . Dependence of  $a_0/L_T$  and  $a_0/L_n$  on  $B_T$  is weak at higher densities of  $1.0 \times 10^{20} \text{m}^{-3} < \bar{n}_e < 1.5 \times 10^{20} \text{m}^{-3}$ , and not clear for  $\bar{n}_e > 1.5 \times 10^{20} \text{m}^{-3}$  due to the lack of sufficient 3.5T data.

#### 4.2. L-H local conditions near separatrix

Local conditions near the separatrix, or equivalently the  $P_e$  “pedestal foot” after applying the alignment criteria (see 2.2), are shown by companion with those at  $\rho=0.95$  to highlight similarities and differences in the global scaling between the two locations. Since the nominal lower bound on reliable TS measurements is  $\sim 3 \times 10^{19} \text{m}^{-3}$  [9], only data with local  $n_e$  above this value are included. A glance at Fig.7.d-f and Fig.8.d-f reveals an absence of distinguishable  $I_p$  or  $B_T$  dependence on separatrix  $T_e$  and  $n_e$ . Hence attention is mainly concentrated on the overall plasma density dependence manifested by all data.

First we see values of  $T_{e,sep}$  as shown by Fig.7.d are mainly restricted in the range between 50eV and 100eV, which are consistent with the expectation from the two-point divertor power balance model [15]. The variation of  $T_{e,sep}$  with density is weak, therefore the significant enhancement of  $T_{e,95}$  in low density 5.4T plasmas should not be attributed to a significant elevation of boundary condition,  $T_{e,sep}$ . Later, it will be shown that this is more associated with the alteration of near-separatrix  $T_e$  profile shapes, that is, the appearance of a mild  $T_e$  pedestal. A difference between  $n_{e,sep}$  and  $n_{e,95}$  is that data of  $n_{e,sep}$  at  $\bar{n}_e > 1.5 \times 10^{20} \text{m}^{-3}$  clearly diverge from the linear trend obtained from  $\bar{n}_e < 1.5 \times 10^{20} \text{m}^{-3}$ , whereas a linear scaling was seen to well represent the data trend for  $n_{e,95}$  over the entire density range. Suggested by Fig.7.e, the trend of  $n_{e,sep}$  at high density can be nearly represented by a  $\sim \bar{n}_e^{3.0}$  relation.

Characterizations of local gradient scale lengths near separatrix are illustrated by Fig.9.c-d and Fig.10.c-d. Unlike the case of  $\rho=0.95$ , either  $I_p$  no  $B_T$  effects on  $a_0/L_T$  could not be explicitly identified over the entire density range, yet a strong  $\sim 1/\bar{n}_e$  overall correlation between  $a_0/L_T$  and density is clearly manifested. This evidence suggests that  $T_e$  profile shape ( $a_0/L_T$ ) near separatrix is primarily sensitive to plasma density variation. Also, the strong increase of  $a_0/L_T$  at  $\rho=1.0$  could be a main reason for the dramatic enhancement of  $T_{e,95}$  in low densities at 5.4T, rather than  $T_{e,sep}$ , which is only slightly varied. In some very low density ( $\bar{n}_e < 0.8 \times 10^{20} \text{m}^{-3}$ ) plasmas with values of  $a_0/L_T$  near  $\rho=1.0$  much exceeding those at  $\rho=0.95$ , even a mild  $T_e$  pedestal can form, e.g. the cases shown in yellow and green on Fig.6. Similar to  $a_0/L_T$ , apparent  $I_p$  dependence on  $a_0/L_n$  at  $\rho=1.0$  is also absent. Dependence of  $a_0/L_n$  on plasma density at moderate and high density is demonstrated in Fig.9.d and Fig.10.d. Both figures show that  $a_0/L_n$  generally decreases with density. Unlike the case of  $a_0/L_T$ , the role of  $B_T$  on  $a_0/L_n$  is distinguishable: for fixed density,  $a_0/L_n$

is reduced at lower  $B_T$ . Similar asymmetry was also observed previously between the  $B_T$  dependence of  $T_{e,95}$  and  $n_{e,95}$ .

#### 4.3. Relation with low power L-mode

Comparing edge conditions at L-H with those in low power L-mode (for simplicity, ‘L-mode’ in 4.3 and 4.4) is of particular importance in revealing what edge parameters are significantly changed during the course of plasma evolution from L-mode to L-H, and via what mechanisms these modification are achieved, which could further help identify the potential triggers for confinement bifurcation. Edge plasma conditions in L-mode are calculated in the same set of discharges involved in 4.1 and 4.2, using the  $T_e$  and  $n_e$  profiles obtained by fitting into the TS measurements within the first 50ms of  $I_p$  flattop for each discharge. The same spatial averaging of edge parameters used in section 4 is adopted. These data are mostly from Ohmic plasmas, but mixed with a small number of low-power (<0.5MW) ICRF ones.

Fig.12 reveals that L-mode  $T_{e,95}$  are mainly scattered between 100eV and 200eV, and do not exhibit clear correlation with plasma density. Compared with  $T_{e,95}$  at L-H, the values of L-mode  $T_{e,95}$  (Fig.12.a) in most 5.4T plasmas are found to be lower. The divergence is especially clear for  $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ , where the data there suggest that significant increase of  $T_{e,95}$  from the L-mode level is required in order to access H-mode. However, for most 3.5T and some 5.4T (those with moderate of  $1.0 \times 10^{20} \text{m}^{-3} < \bar{n}_e < 1.5 \times 10^{20} \text{m}^{-3}$ , i.e. near the minimum of  $P_{th}$ ) plasmas, the values of  $T_{e,95}$  in L-mode and at L-H are seen to be comparable, which could suggest that  $T_{e,95}$  in these cases might not very likely be the “critical” parameter need to be achieved for L-H transition. Unlike  $T_{e,95}$ , the  $n_{e,95}$ ,  $T_{e,sep}$  and  $n_{e,sep}$  in L-mode are not dramatically different than L-H. The values of  $a_0/L_T$  and  $a_0/L_n$  at  $\rho=1.0$  (Fig.13.a-b) in L-mode are generally lower than what they are at L-H. By contrast, data of both  $L_T$  and  $L_n$  at  $\rho=0.95$  exhibit no significant overall divergence between L-mode and L-H.

#### 4.4. Relation with SOL-divertor physics

As shown by Fig.14, the large scatters in data of  $a_0/L_T$  at  $\rho=0.95$  for both L-mode and L-H induced by  $I_p$  and  $B_T$  variation can be reduced if these data are re-organized with respect to the dimensionless parameter  $\bar{n}_e/n_G$ . Reduced data scatter are also observed in  $a_0/L_p = a_0/L_T + a_0/L_n$  over all densities since  $a_0/L_T \gg a_0/L_n$ . The overall trend of  $a_0/L_T$  and  $a_0/L_p$  is basically the same: they generally increase towards lower values of  $\bar{n}_e/n_G$ , which are guided by the dash lines on Fig.14. Differences between L-mode and L-H could exist mainly in the high-recycling regime ( $0.19 < \bar{n}_e/n_G < 0.31$ ), such that at fixed  $\bar{n}_e/n_G$ , values of  $a_0/L_p$  (also  $a_0/L_T$ ) at L-H seem to be generally larger than in L-mode.

Early studies by LaBombard [16] discovered similar correlation between  $L_p$  and  $\bar{n}_e/n_G$  in the near SOL ( $a_0 < r < a_0 + 5\text{mm}$ ) region in Ohmic plasmas, and connect this feature with the potential role of electromagnetic drift wave turbulence on edge profile regulation.

Based on results shown in Fig.14, a similar scaling with  $\bar{n}_e/n_G$  applies at  $\rho=0.95$  for  $a_0/L_p$  (also  $a_0/L_T$  since  $a_0/L_p \sim a_0/L_T$ ) in L-mode and at L-H. Curiously, the scale lengths at  $\rho=1.0$  depend on  $\bar{n}_e$ , rather than the normalized Greenwald fraction. It is as if that at both  $\rho=0.95$  and in the near SOL, plasma profiles are influenced by similar cross-field transport mechanism, and “pivoted” about the near separatrix location --an implication that the entire plasma edge and near SOL regimes should be studied as an integrated physical system.

## 5. Comparison with theory

A handful of theoretical models have been proposed in attempt to explain L-H transition, most of which can be found in the comprehensive review article by Connor and Wilson [17]. Rather than validating each of these models, we focus on testing a specific one based on a series of preceding works by Rogers, Drake and Zeiler (RDZ) [18][19][20]. This model relies on the suppression of resistive-ballooning mode turbulence as the mechanism for L-H transition. In this section, we aim at a comprehensive examination from experiment on the validity of RDZ model in predicting: (1) L-H transition threshold; (2) L-mode and H-mode operational domains. It is worthwhile to mention that similar comparisons were conducted before on Alcator C-Mod [8] in moderate densities, normal and high  $B_T$  (5T, 8T) plasmas, where encouraging agreement between theory and experiments have been found. Results shown below will extend this comparison into a broader parameter space, which covers a wide range of densities ( $\bar{n}_e=0.6-2.1 \times 10^{20} \text{m}^{-3}$ ), three magnetic fields ( $B_T=3.5\text{T}, 4.6\text{T}, 5.4\text{T}$ ), and more plasma currents ( $I_p=0.6-1.2\text{MA}$ ).

The RDZ model indicates that the L-mode to H-mode confinement bifurcation is triggered when the critical conditions for suppressing resistive-ballooning mode instabilities induced particle and thermal transport are reached. The model relies on two dimensionless parameters to characterize mode stability and induced transport: the MHD ballooning parameter  $\alpha_{MHD} (\sim q^2 R d\beta / dr)$ , and the diamagnetic parameter  $\alpha_{dia} (\sim 1 / \sqrt{q v_*})$ , where  $v_* \propto Z_{eff} q n_e / T_e^2$ ). Based on a number of three-dimensional nonlinear numerical simulations [18] performed previously in shifted-circle equilibrium magnetic geometry, an approximate L-H threshold boundary was obtained. As shown in Fig.15 by dashed lines, this boundary is in ‘L’ shape, with the two ‘arms’ being  $\alpha_{MHD} \sim 0.5$  and  $\alpha_{dia} \sim 0.6$ , respectively. H-modes are predicted to emerge in the space upper and right to the L-H boundary on the  $\alpha_{MHD} - \alpha_{dia}$  diagram, while L-mode are expected to stay in the remaining areas.

To experimentally examine the model predicted L-H threshold boundary, values of  $\alpha_{MHD}$  and  $\alpha_{dia}$  at L-H are evaluated for all discharges included earlier in this study at two radial locations of  $\rho=0.95$  (Fig.15.a) and  $\rho=1.0$  (Fig.15.c), staying in the same analysis scheme introduced in section 4. The assumption  $T_e \sim T_i$  is applied here, thus  $\alpha_{MHD} \sim 2\alpha_e$ . This assumption is generally true in the high collisional C-Mod plasma edge, even at low

density, which is verified by the charge exchange  $T_i$  measurements. Same calculation are performed in low power L-mode (i.e., calculated from the first 50ms of  $I_p$  flattop, same as in 4.3) at  $\rho=0.95$ , and shown in Fig.15.b. It is noticed from Fig.15.a that the L-H data at  $\rho=0.95$  are distributed close to the theory predicted boundary, which shows promising agreement. Compared with L-H, most data in low power L-mode are seen to be systematically lower in  $\alpha_{MHD}$ , staying below the  $\alpha_{MHD}=0.5$ . The increase of  $\alpha_{MHD}$  is observed to be especially pronounced for  $\alpha_{dia}\sim 0.6$ . According to the results from 4.3, the enhancement of  $\alpha_{MHD}$  (i.e. pressure gradients if  $I_p$  is fixed) are primarily achieved by the promotion of  $T_{e,95}$ , although in some cases, for example in the high-recycling regime, the increase of  $a_0/L_p$  (see Fig.14.c, Fig.14.f) may contribute as well. Also note that at  $\rho=0.95$ , the domain where low density data ( $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$  at L-H, open triangles on Fig.15.a) emerge on the diagram overlaps with that of the higher density ones, which implies that the local “bifurcation criteria” for L-H transition at different densities could be uniform, although the required heating power can vary strongly. Fig.15.d. shows that most L-mode and H-mode data largely appear in their corresponding domains as predicted by theory.

Although Fig.15.b suggests that the values of  $\alpha_{dia}$  at  $\rho=0.95$  in L-mode and at L-H are not remarkably different, the plasma evolution towards L-H, which is represented by the traces (those connected lines in Fig.16) on the  $\alpha_{MHD} - \alpha_{dia}$  diagram, could be different at various  $\alpha_{dia}$ . We take three discharges with  $B_T=5.4\text{T}$ ,  $I_p=0.8\sim 1.0\text{MA}$ , at low ( $\bar{n}_e=0.6 \times 10^{20} \text{m}^{-3}$ ), intermediate ( $\bar{n}_e=1.7 \times 10^{20} \text{m}^{-3}$ ), and high ( $\bar{n}_e=2.1 \times 10^{20} \text{m}^{-3}$ ) density, to demonstrate the difference, as shown in Fig.16. Comparing the three plots, it is noticed that L-mode data in the low density (Fig.16.a) case mainly range between  $\alpha_{dia}=1.0$  and  $\alpha_{dia}=2.0$  as it progressively pass the L-H boundary of  $\alpha_{MHD}=0.5$ . By contrast, in the intermediate density (Fig.16.b) case, the direction of the traces is essentially vertical towards the ideal MHD stability boundary for confinement bifurcation:  $\alpha_{MHD}=1.0$  [17], meanwhile remains closely aligned with  $\alpha_{dia}=0.6$  horizontally. Owing to its high collisionality, L-modes in the high density (Fig.16.c) case emerge in the region left to  $\alpha_{dia}=0.6$  and lower than  $\alpha_{MHD}=0.5$ , so the direction of plasma evolution to L-H on the diagram is primarily upward right, which is a process of simultaneous promotion of  $\alpha_{MHD}$  and  $\alpha_{dia}$ . Interestingly, the scenario in the low density case is akin to the conditions required for nonlinear Kelvin-Holmholz poloidal shear flow to be generated, sustained, and ultimately trigger L-H, that is  $\alpha_{dia}\sim 1.0$ ,  $\alpha_{MHD} < \sim 0.5$  [17][18].

Shown by Fig.15.c, data near separatrix ( $\rho=1.0$ ) are mainly concentrated in the area lower and left relative to the predicted L-H threshold boundary on the  $\alpha_{MHD} - \alpha_{dia}$  diagram (i.e.,  $\alpha_{MHD} < 0.5$ ,  $\alpha_{dia} < 1.5$ ), which is the result of higher collisionality ( $\alpha_{dia}\sim 1/\nu_*$ ) and lower pressure near separatrix than  $\rho=0.95$ . So the resistive-ballooning mode turbulence near the separatrix might not be sufficiently suppressed to trigger L-H confinement bifurcation.

The above comparisons yield reasonably good agreements between theory and experiments, and have suggested a potential role of resistive-ballooning mode turbulence on L-H transition. However, these results provide no clues on the relation between the RDZ model and the observed edge conditions, e.g.  $T_{e,95}$ , or required H-mode threshold power. Neither can we directly prove the existence of resistive-ballooning mode until the

characters of edge fluctuations are well diagnosed and studied. Assessing the agreement between C-Mod data and other propose models is the subject of ongoing works.

## 6. Enhanced energy confinement before L-H at low density

In a few low density discharges ( $\bar{n}_e \sim 0.6 \times 10^{20} \text{ m}^{-3}$ ,  $I_p = 0.9 \text{ MA}$ ,  $B_T = 5.4 \text{ T}$ ), an improved energy confinement phase was discovered before L-H transition. Time histories of some key plasma parameters for one such case are shown in Fig.17. This confinement phase share several common features with the I-mode regime [21], including (1) the appearance of substantial electromagnetic fluctuations in the intermediate frequency range with signature frequencies  $\sim 250 \text{ KHz}$  and detected by both magnetic pick-up coils and PCI; (2) steady and continuous improvement of plasma energy confinement indicated by  $H_{98}$  reaching H-mode level of above 1.0, but without clear H-mode transition during this course (L-H at 1.24 sec); (3) low edge neoclassical collisionality (see for example [21]), namely,  $\nu_{* \text{ neo}} \sim 0.5$ ; (4) appearance of a mild temperature (both  $T_e$  and  $T_i$ , see Fig.18) pedestal while the electron density profile retains an L-mode shape. Despite the low collisionality, Fig.18 indicates that electron and ion temperature in plasma edge are still well coupled, such that  $T_e \sim T_i$ .

Electron temperature and density profiles from the steady state period with well-established coherent fluctuations are compared with those in L-mode and H-mode, and shown by Fig.18. In general,  $T_e$  profile is similar to its H-mode companion but distinct with the one in L-mode: both support an edge pedestal, and the central  $T_e$  are comparable, which is  $4 \sim 4.5 \text{ KeV}$ . The width of  $T_e$  pedestal (radial extension from pedestal top to bottom) is about 1.5cm, a little broader than that in the subsequent H-mode, which is about 1cm wide. Inside the pedestal, the two profiles are nearly identical. On the other hand, the density profile is found to remain in L-mode shape, perhaps slightly more peaked, but clearly without the formation of a steep density pedestal as in the H-mode scenario. Most of these properties are consistent with the typical I-mode profile characters, which have been described in [21].

Despite these similarities, this confinement phase differs from typical I-modes in certain aspects of first, these low-density discharges were created in standard lower single null magnetic topology ( $\kappa \sim 1.66$ ,  $\delta_{\text{upper}} \sim 0.35$ ,  $\delta_{\text{lower}} \sim 0.53$ ) with ion grad-B drift in the favorable direction (i.e., pointing towards X-point), whereas most I-modes [21] are achieved either with unfavorable ion grad-B drift, or with favorable drift and atypical shaping. Because the H-mode threshold power is significantly enhanced at low density, an operation window exists for the enhanced confinement prior to H-mode transition. Similarly, I-mode access with unfavorable grad-B drift is allowed because  $P_{th}$  is much higher than in the favorable grad-B direction. There are two major differences between the intermediate frequency fluctuations (250KHz mode) and the commonly seen weakly coherent modes (WCM) in normal I-mode plasmas. One is that the bandwidth of the 250KHz mode is narrower ( $\sim 30 \text{ KHz}$ ) compared to those of WCM, which are typically  $50 \sim 100 \text{ KHz}$  [21]. Another one is that the toroidal mode number, inferred by correlating

magnetic pick-up coils measurements at several different toroidal locations, is indicated to be low for the 250KHz mode, such that  $n < 5$ ; however, for standard WCM,  $n$  is typically above 10 [21].

Nevertheless, this confinement phase serves the same purpose as I-mode in combining the merit of H-mode on improving energy confinement, and of L-mode on maintaining right amount particle transport to avoid impurity accumulation.

## 7. Conclusion and future work

To summarize, plasma density, toroidal magnetic field strength, and plasma current dependence of H-mode threshold power ( $P_{th}$ ) and local plasma edge conditions at L-H have been experimentally studied in Alcator C-Mod plasmas with favorable ion grad-B drift. Plasma density dependence of  $P_{th}$  was found to be ‘U-shaped’, which is similar to earlier observations on AUG, COMPASS, JET, JT-60, etc. Toroidal field dependence of  $P_{th}$  over the range of  $3.5T < B_T < 5.4T$  was found to depend on density: it is clearly identified at low density but becomes weak or may even vanish at moderate and high density. Despite a factor of 2 variations of plasma currents, no distinguishable  $I_p$  dependence of  $P_{th}$  was identified. For the few 5.4T discharges with lowest densities, an improved energy confinement emerged prior to L-H transition.

Local plasma edge conditions at L-H were characterized at two radial locations:  $\rho=0.95$  and  $\rho=1.0$  (near separatrix). At  $\rho=0.95$ ,  $T_{e,95}$  in 5.4T display a strong  $\sim 1/\bar{n}_e$  scaling at low densities, while weak or no density dependence is found at high density. Effects of  $B_T$  on  $T_{e,95}$  are mainly manifested at low density, such that for fixed  $\bar{n}_e$ ,  $T_{e,95}$  is lower for reduced  $B_T$ , however, the  $I_p$  dependence of  $T_{e,95}$  is absent. It is found that  $n_{e,95}$  is almost linearly correlated with plasma density, and is insensitive to either  $B_T$  or  $I_p$  variation. However, both  $I_p$  and  $B_T$  dependence were clearly identified in  $a_0/L_T$  and  $a_0/L_n$ , and it is likely that the proportionality is  $\sim 1/q_{95}$  at low density. Near the separatrix, both  $T_{e,sep}$  and  $n_{e,sep}$  exhibit no  $I_p$  or  $B_T$  dependence. The density dependence of  $T_{e,sep}$  is also weak even at low density;  $n_{e,sep}$  diverge from linear scaling at high density. A strong  $\sim 1/\bar{n}_e$  overall density scaling is identified in separatrix  $a_0/L_T$ , while both  $I_p$  and  $B_T$  dependence tend to be weak. The separatrix  $a_0/L_n$  is lower at reduced  $B_T$ , whereas  $I_p$  basically exerts no effect on separatrix  $a_0/L_n$ . Local conditions at L-H were also compared with those in low power L-mode, where distinct difference in the magnitudes of  $T_{e,95}$  were found between the two cases in most 5.4T plasmas. Yet for moderate density 5.4T and most 3.5T plasmas, the values of  $T_{e,95}$  in L-mode and at L-H are comparable. Amplitudes of  $a_0/L_T$  and  $a_0/L_n$  near separatrix at L-H seem to be larger than L-mode. Other parameters are not significantly different between the two cases.

Calculated local edge conditions have been used as inputs to test the resistive-ballooning mode theory (RDZ model). For  $\rho=0.95$ , data at L-H as shown on  $\alpha_{MHD} - \alpha_{dia}$  diagram are found to be distributed close to the theory predicted L-H boundary, while compared to L-H, values of  $\alpha_{MHD}$  in L-mode seem to be systematically lower and well below the  $\alpha_{MHD}$

$\sim 0.5$  boundary. In addition, data in L-mode and H-mode largely fall into their corresponding theory predicted domains on the diagram. Inside and near separatrix, data both in L-mode and at L-H are mostly scattered in the area of  $\alpha_{MHD} < 0.5$  and  $\alpha_{dia} < 0.6$ , which is away from the theoretical boundary, and are not significantly changed from L-mode to L-H.

Future work will aim at better understanding of the physics of  $P_{th}$  and the correlation between  $P_{th}$  and local edge conditions, at resolving the evolution of edge conditions from L-mode to L-H in a finer time scale by employing improved time resolution diagnostics capability, at identifying the timing and triggers of L-H transition in various global plasma conditions, at looking for the differences and similarity between L-H and I-H transition, at searching for other major “hidden variables” in  $P_{th}$ , etc.

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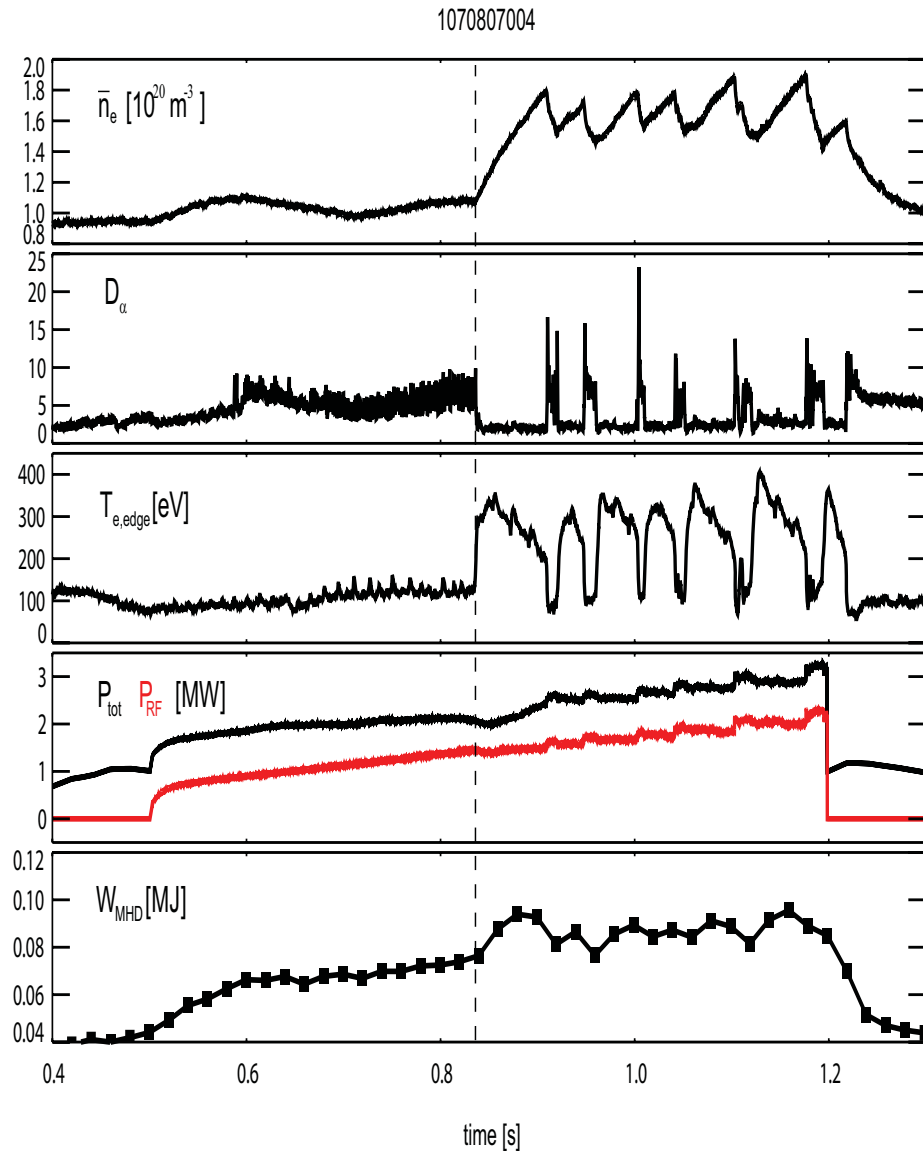


Fig.1. Time histories of some plasma parameters for a transition from L-mode to H-mode on C-Mod. The L-H transition is marked by the dashed line on these plots.

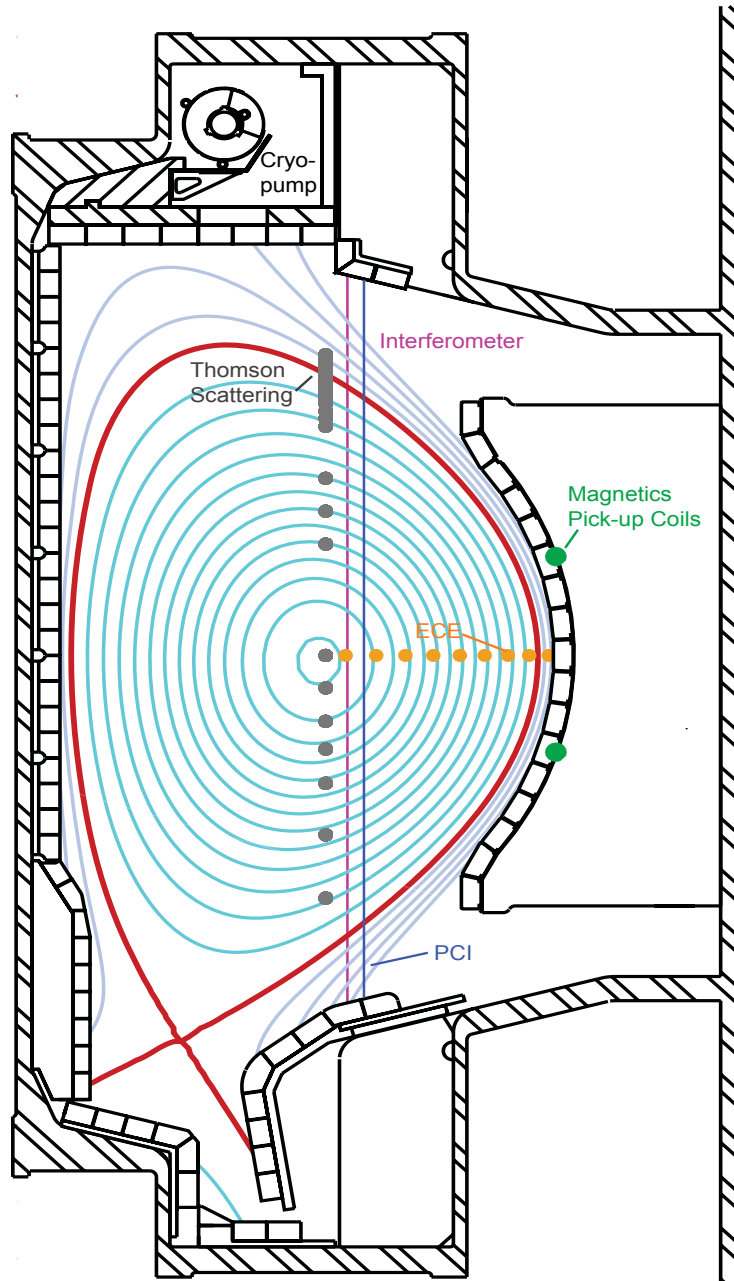


Fig.2. Illustration of standard lower single null equilibrium magnetic geometry on a poloidal cross section of Alcator C-Mod. Measurement locations of some key C-Mod diagnostics are displayed on the same plot.

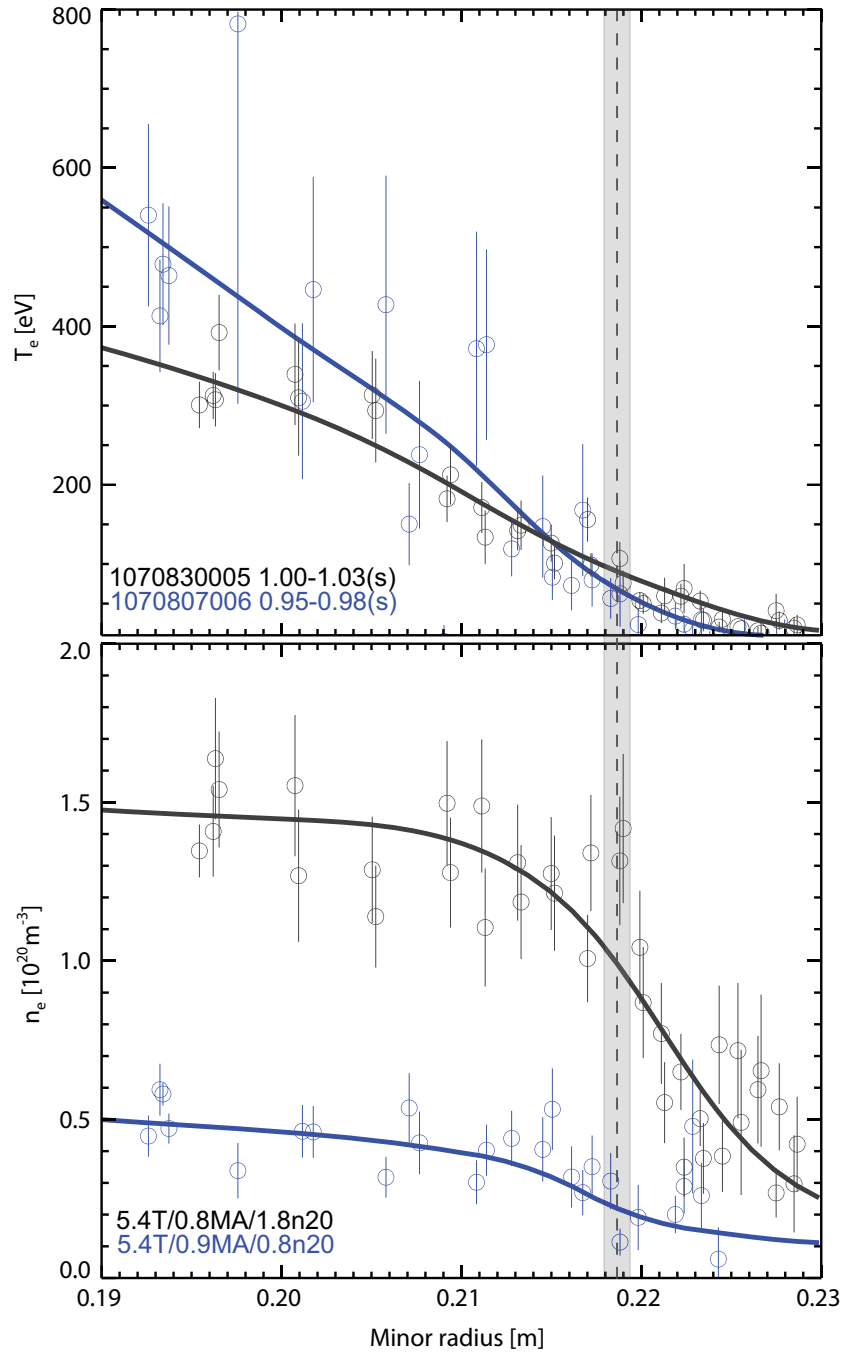


Fig.3. Thomson scattering measurements (open circles) of  $n_e$  and  $T_e$  in the edge region of a low ( $\bar{n}_e=0.8 \times 10^{20} \text{m}^{-3}$ , blue) and moderate ( $\bar{n}_e=1.8 \times 10^{20} \text{m}^{-3}$ , black) density discharge. The presented data are from the last two TS laser pulses, which is within  $\sim 30$ ms prior to L-H transition. Shown in solid lines are curve fitting to these data. The dashed line and shaded bar represent the approximate radial location of EFIT separatrix location.

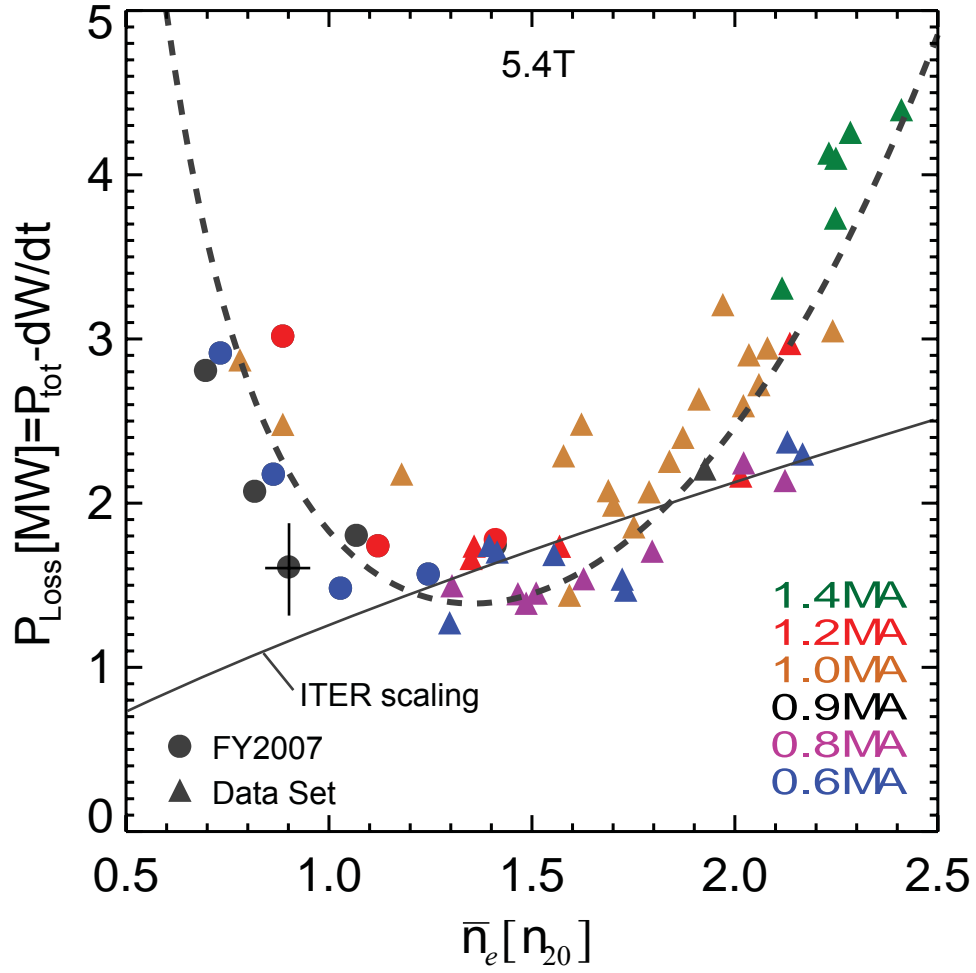


Fig.4. H-mode threshold power ( $P_{th}$ ) in 5.4T plasmas versus line averaged density. Data from the dedicated low density L-H experiment in 2007 C-Mod campaign are shown by solid circles. Plot in dashed line is an approximate curve fitting to these data. The international tokamak scaling is shown as the solid line on the same plot.

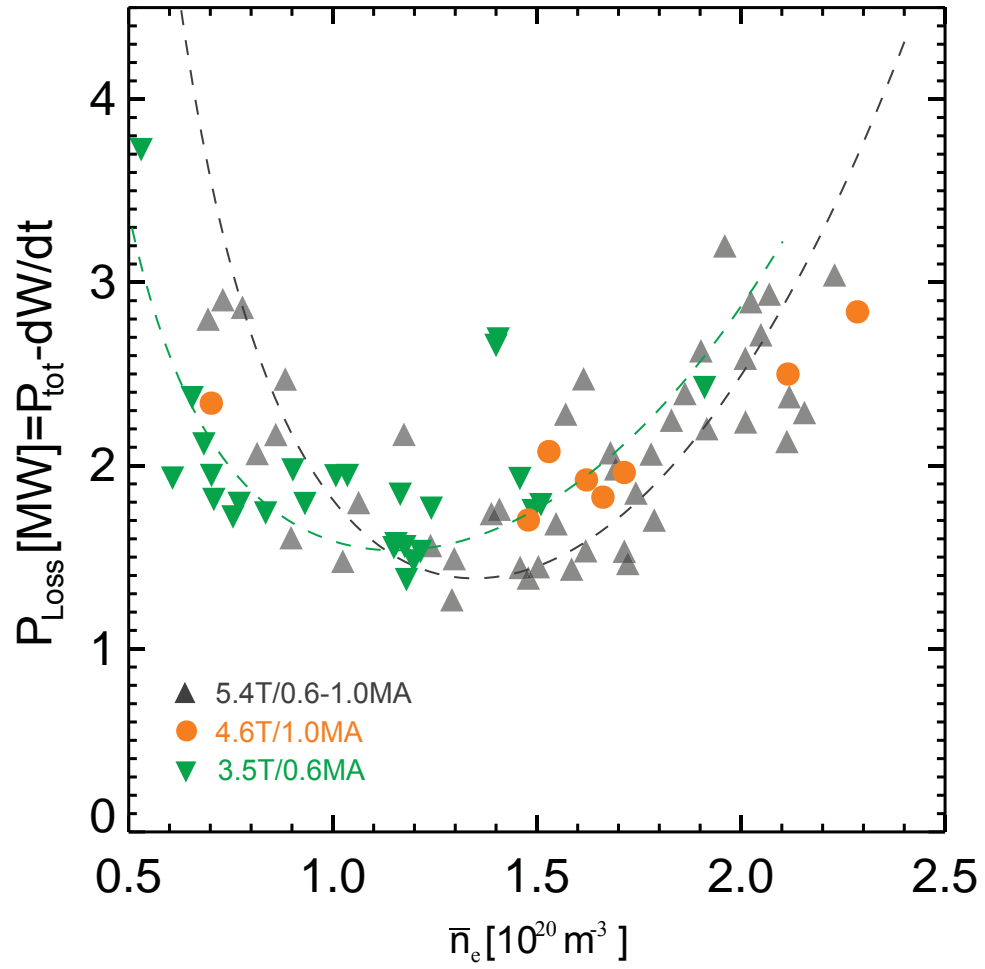


Fig.5. Data of  $P_{th}$  from lower  $B_T$  (3.5T, 4.6T) plasmas versus line averaged density are displayed together with portions of 5.4T data. The dashed line is the same curve fitting to 5.4T data as in Fig.4.

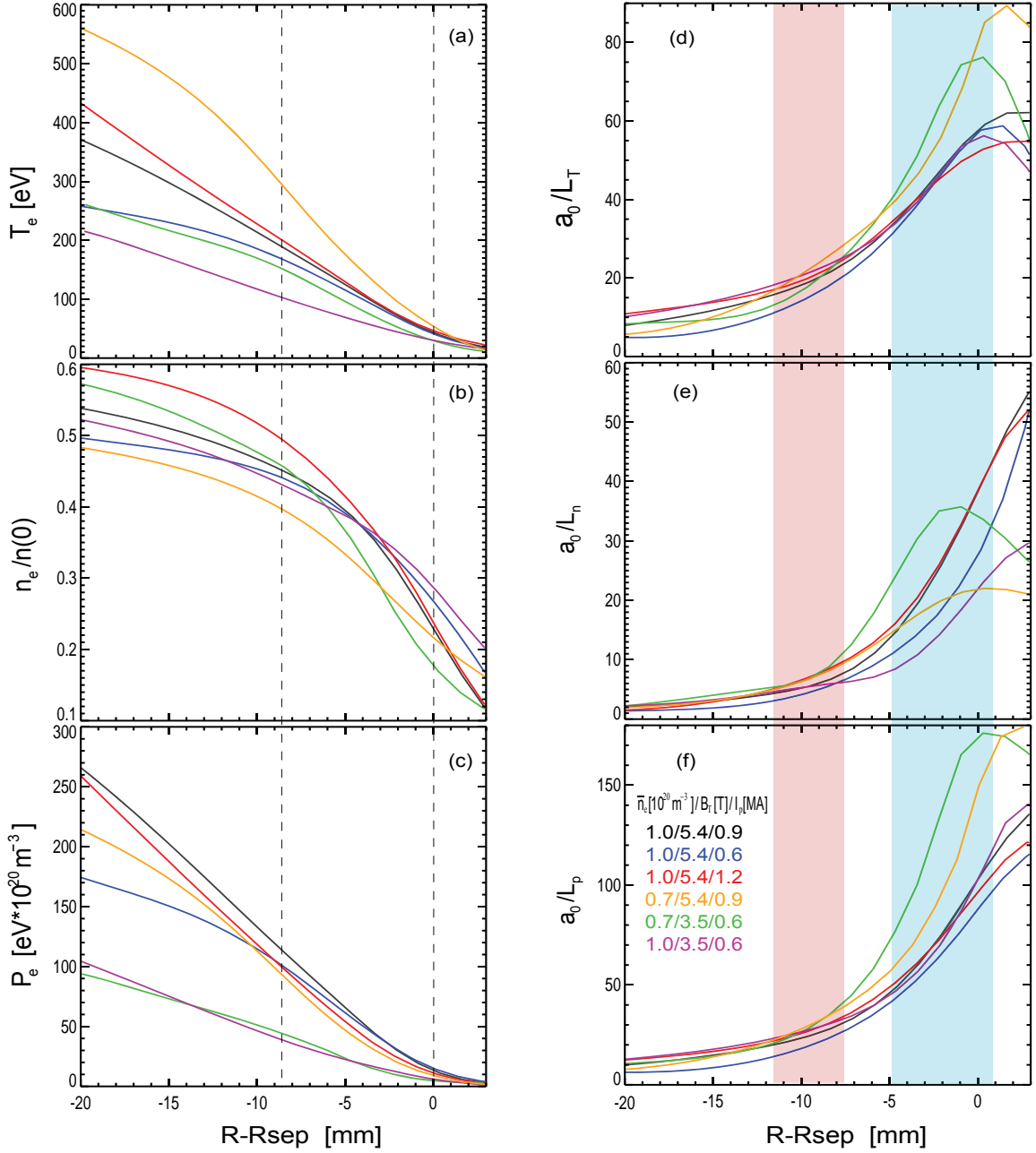


Fig.6. Composite edge profiles preceding L-H from some low density ( $\bar{n}_e < 1.0 \times 10^{20} \text{m}^{-3}$ ) plasmas. The  $T_e$  and  $n_e$  profiles are obtained by fitting into the TS measurements from the last two laser pulses prior to L-H. Profiles of  $a_0/L_T$  and  $a_0/L_n$  are derived from the corresponding  $T_e$  and  $n_e$  profiles, respectively. Dashed lines represent the EFIT separatrix and the approximate midplane radial location of  $\rho=0.95$  flux surface. Shaded areas (right) are regions for spatial averaging in evaluating  $a_0/L_T$ ,  $a_0/L_n$ . These profiles have been shifted in the radial direction relative to the original ones, in order to align the location of maximum  $d^2 P_e / dr^2$  (nearly the  $P_e$  pedestal foot) for each case with the EFIT separatrix.

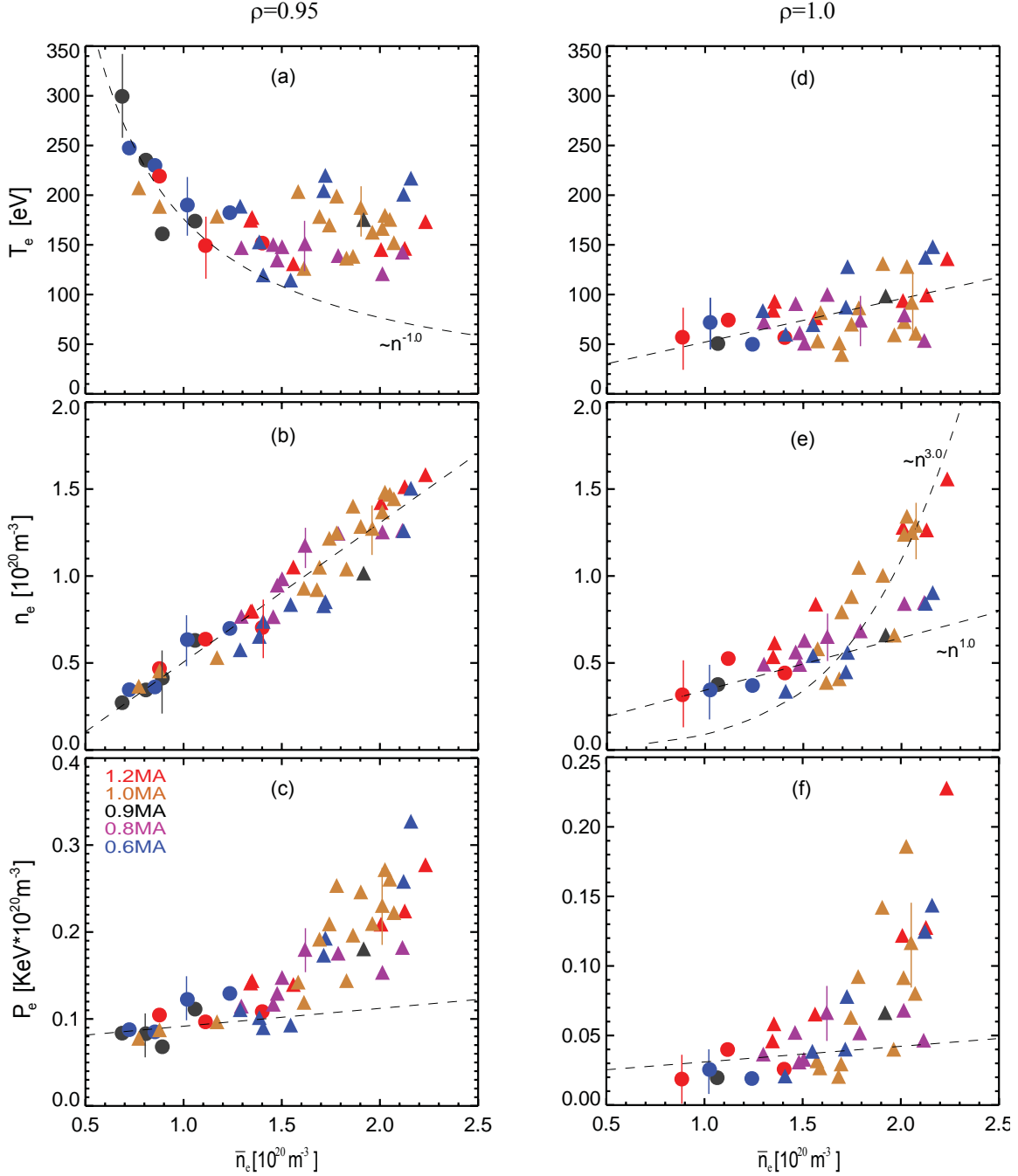


Fig.7. L-H threshold  $T_e$ ,  $n_e$ , and  $P_e$  from 5.4T plasmas versus  $\bar{n}_e$  at  $\rho=0.95$  (left) and  $\rho=1.0$  (right). Data are evaluated at the dashed lines in Fig.6 of the  $T_e$  and  $n_e$  profiles obtained by fitting into the TS data from the last two laser pulses prior to L-H. Symbol coding is identical to Fig.4. Dashed lines (except the  $\sim \bar{n}_e^{3.0}$  one in the plot of  $n_e$  at  $\rho=1.0$ ) are intended to guide the trends at low and moderate densities ( $\bar{n}_e < 1.5 \times 10^{20} \text{ m}^{-3}$ ). Only data with local  $n_e$  above  $\sim 3 \times 10^{19} \text{ m}^{-3}$  are included, since this is the lower limit for reliable TS density measurements on C-Mod.



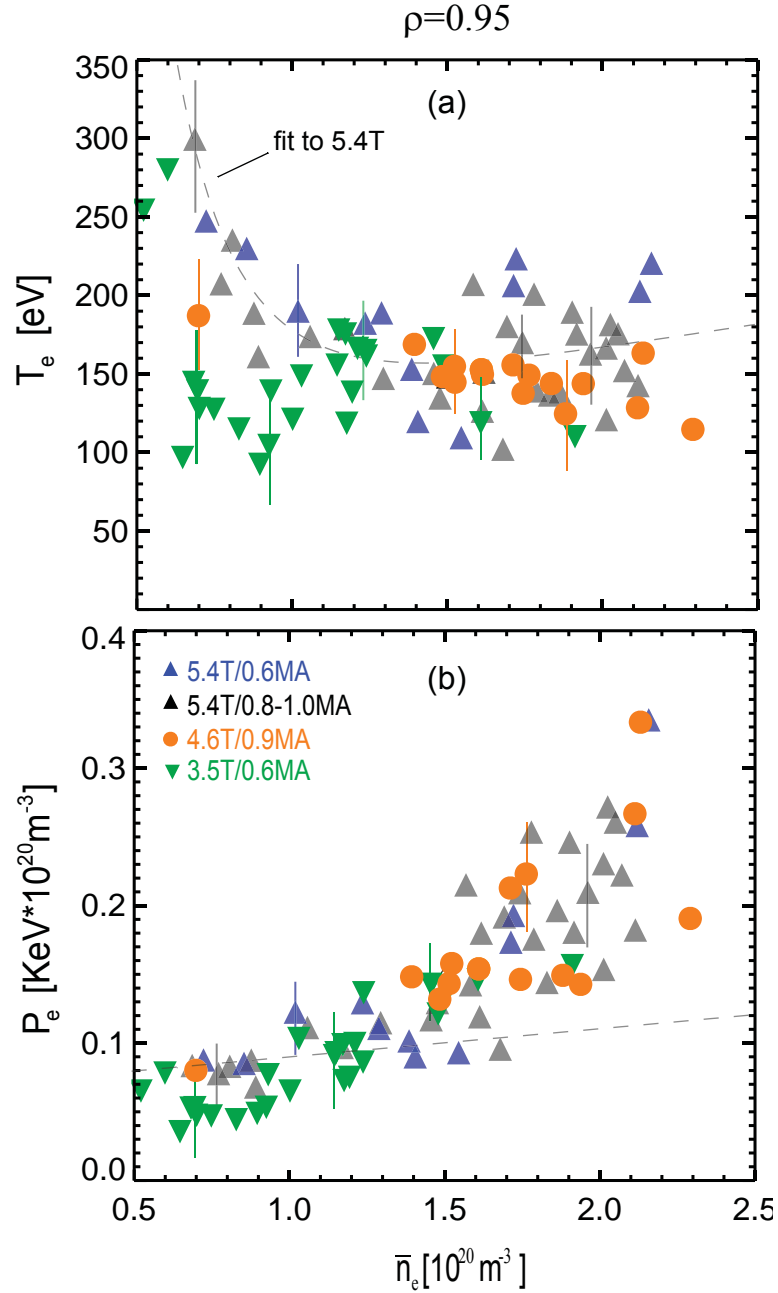


Fig.8. L-H threshold (a)  $T_e$  and (b)  $P_e$  from lower  $B_T$  (3.5T,4.6T) plasmas along with portions of 5.4T data versus  $\bar{n}_e$  at  $\rho=0.95$ . The dashed line in  $P_e$  is taken from Fig.7, which is intended to guide the trend of 5.4T data in low and moderate density ( $\bar{n}_e < 1.5 \times 10^{20} \text{ m}^{-3}$ ).

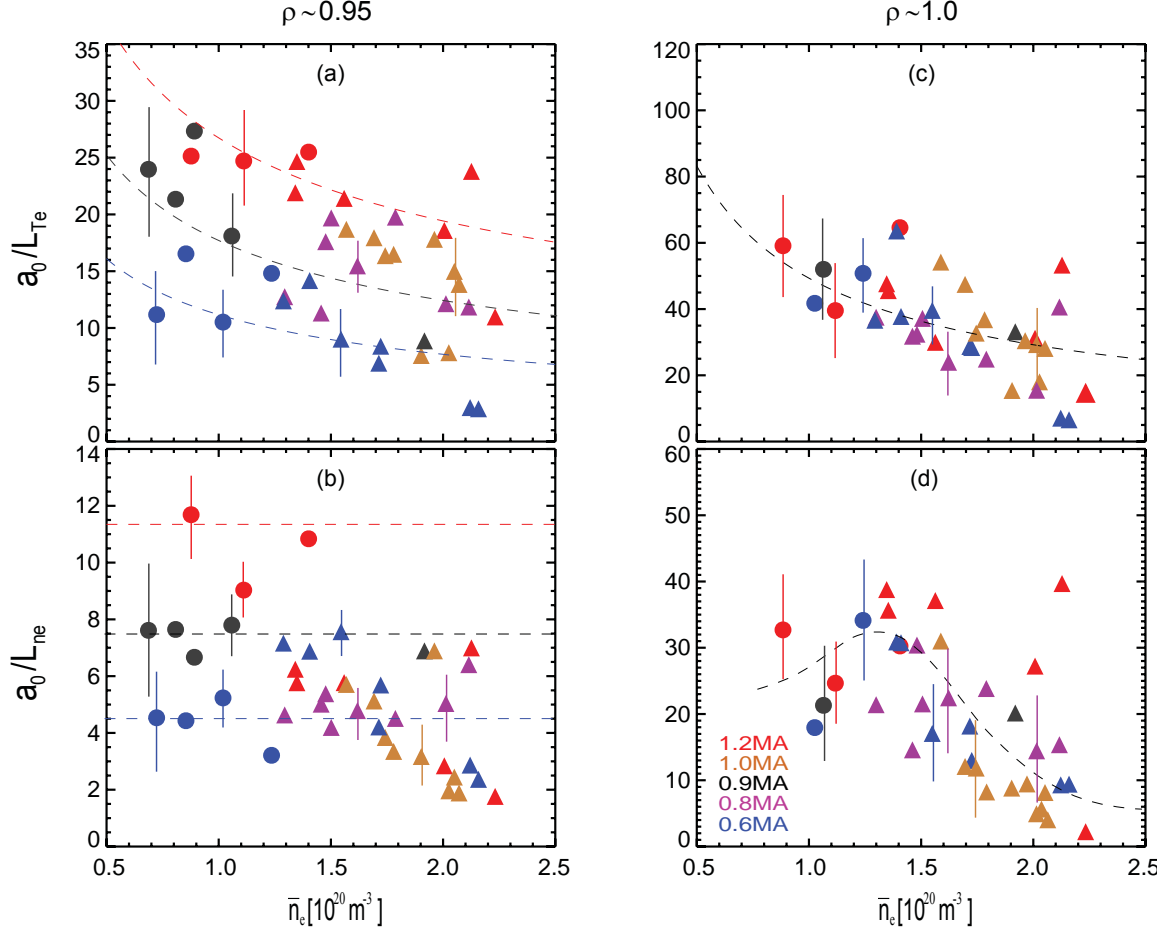


Fig.9. L-H threshold  $a_0/L_T$ ,  $a_0/L_n$  from 5.4T plasmas versus  $\bar{n}_e$  at  $\rho=0.95$  (a-b) and  $\rho=1.0$  (c-d). Data are calculated using the  $T_e$  and  $n_e$  profiles obtained by fitting into the TS data from the last two laser pulses prior to L-H, and averaged within the shaded layers in Fig.6. Symbol coding is identical to Fig.4. Dashed lines in (a) and (b) are intended to guide the trends of 5.4T data at low and moderate density ( $\bar{n}_e < 1.5 \times 10^{20} \text{ m}^{-3}$ ). Dashed lines in (c) and (d) are intended to guide the data trend over the entire density. Some low density data have been intentionally excluded from (d) for the same reason as stated in Fig.7.

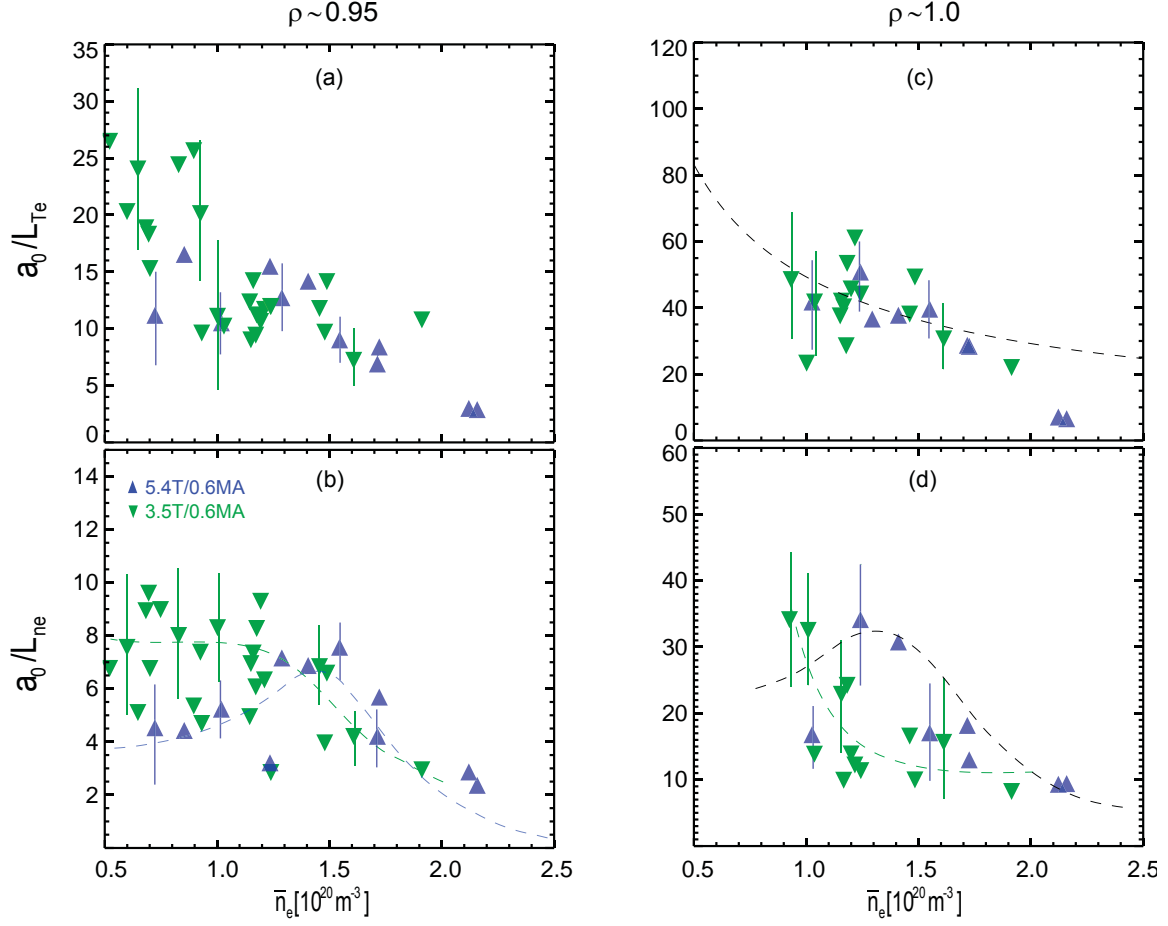


Fig.10. L-H threshold  $a_0/L_T$ ,  $a_0/L_n$  from 3.5T/0.6MA plasmas along with 5.4T/0.6MA data versus  $\bar{n}_e$  at  $\rho=0.95$  (a-b) and  $\rho=1.0$  (c-d). Data are calculated using the  $T_e$  and  $n_e$  profiles obtained by fitting into the TS data from the last two laser pulses prior to L-H, and averaged within the shaded layers in Fig.6. Dashed lines are intended to guide the data trends in 5.4T (blue), 3.5T (green), or both (black).

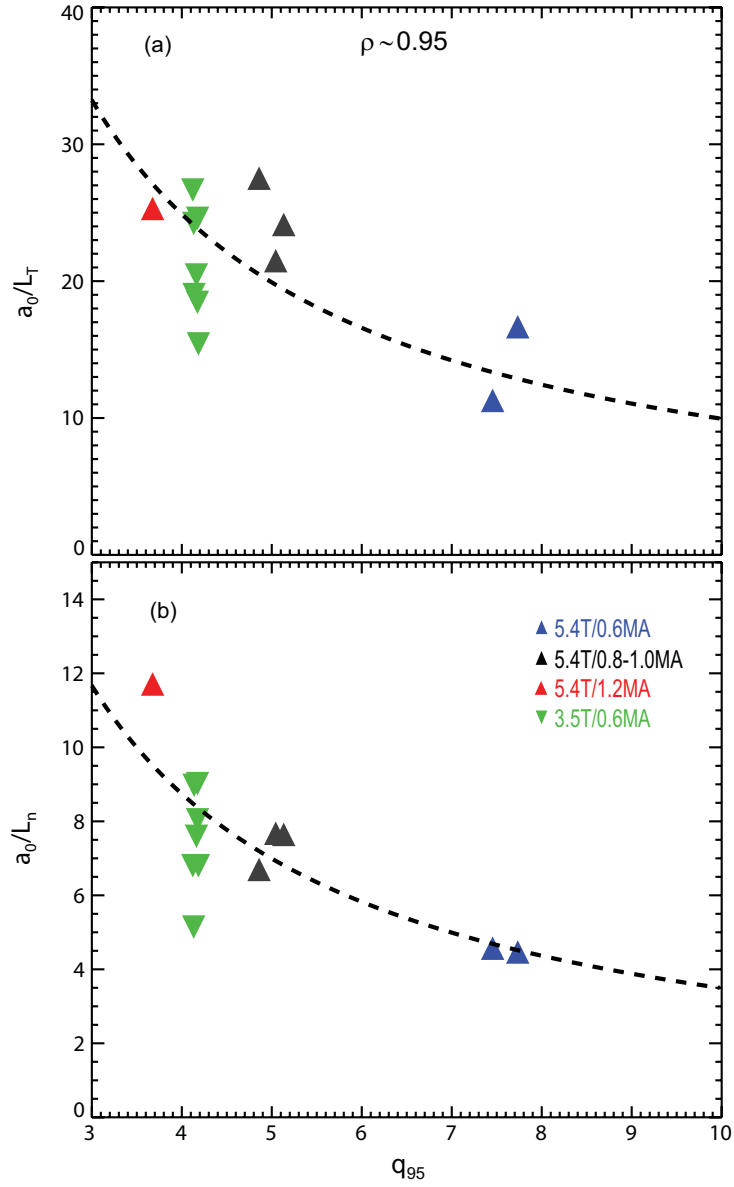


Fig.11. Data of  $a_0/L_{Te}$ ,  $a_0/Ln_e$ , with  $\bar{n}_e < 0.9 \times 10^{20} \text{ m}^{-3}$  are displayed as a function of  $q_{95}$ . The data are found to approximately follow the  $\sim 1/q_{95}$  relation, which are guided by the dashed lines on each plot.

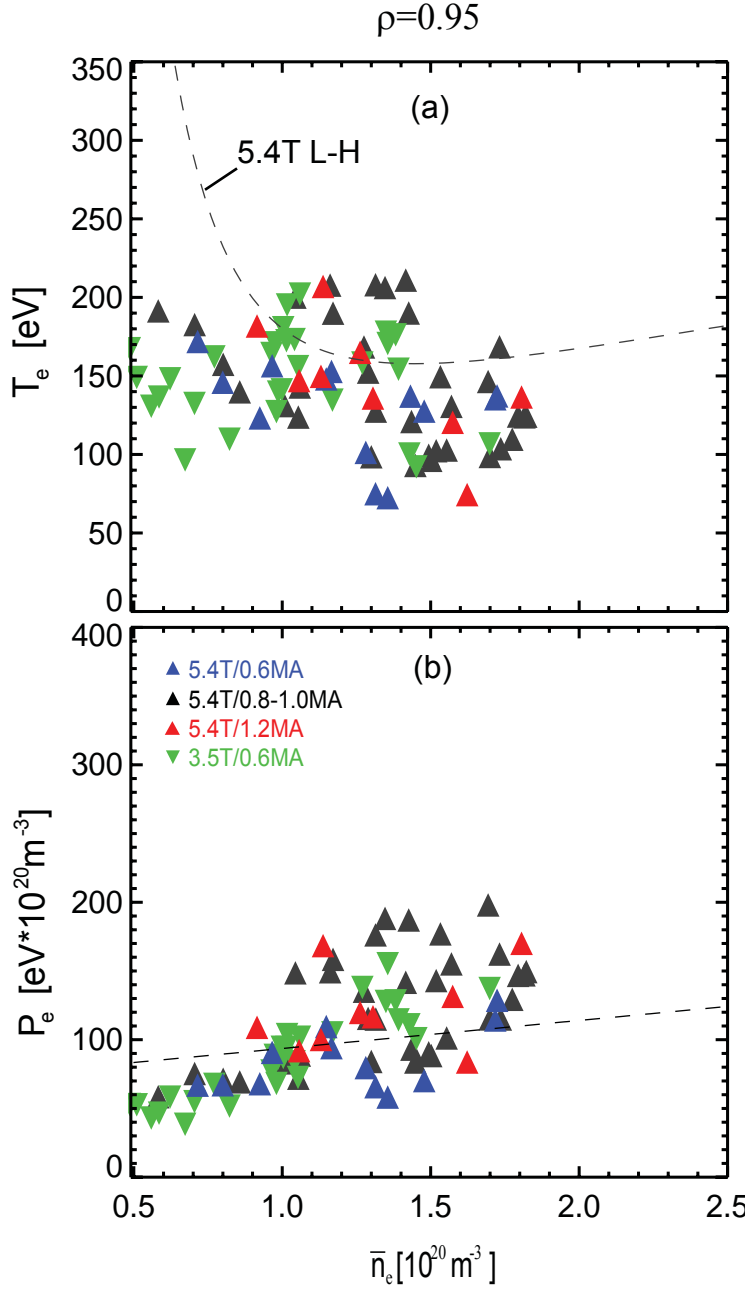


Fig.12. (a)  $T_e$  and (b)  $P_e$  in low power L-mode plasmas, versus  $\bar{n}_e$  at  $\rho=0.95$ . Data are evaluated at the dashed lines in Fig.6 using  $T_e$  and  $n_e$  profiles obtained by fitting into TS data within the first 50ms of  $I_p$  flattop. Dashed lines are taken from Fig.8.

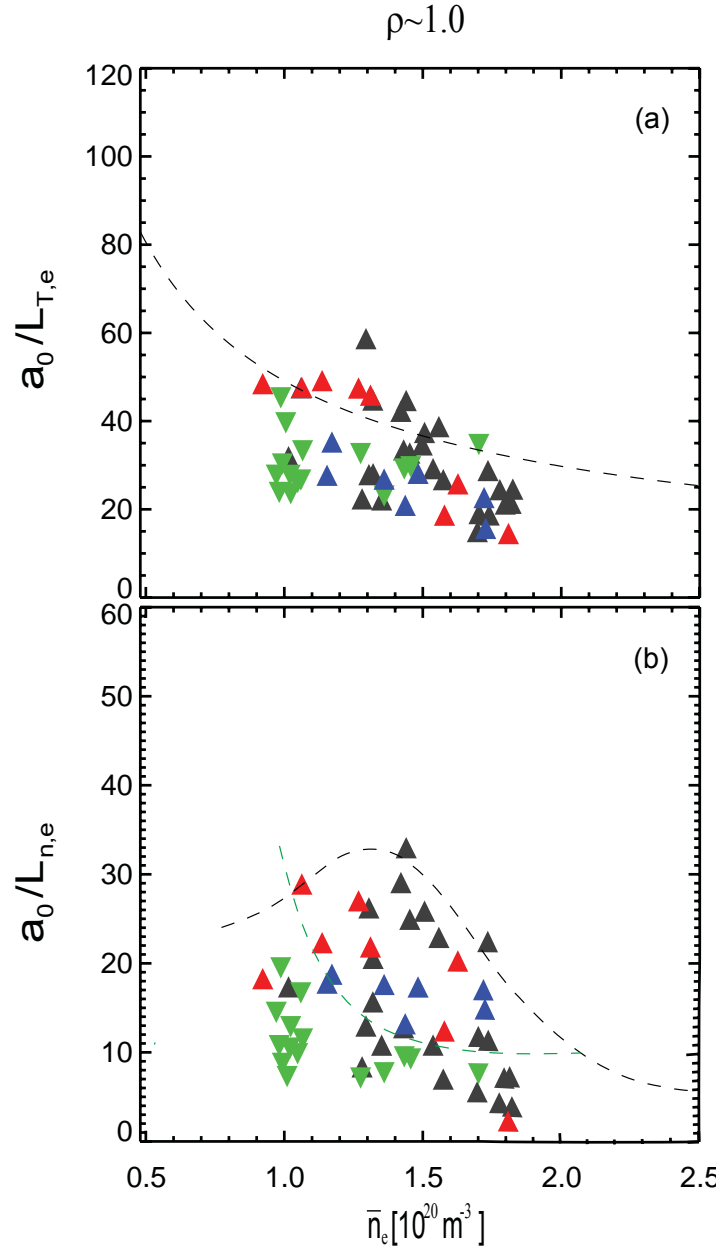


Fig.13.  $a_0/L_T$ ,  $a_0/L_n$  in low power L-mode plasmas, versus  $\bar{n}_e$  at  $\rho=1.0$ . Data are calculated using the  $T_e$  and  $n_e$  profiles obtained by fitting into the TS data from the first 50ms of  $I_p$  flattop, and averaged within the shaded layers in Fig.6. Dashed lines are taken from in Fig.10, which approximately guide the data trends at L-H.

$\rho \sim 0.95$

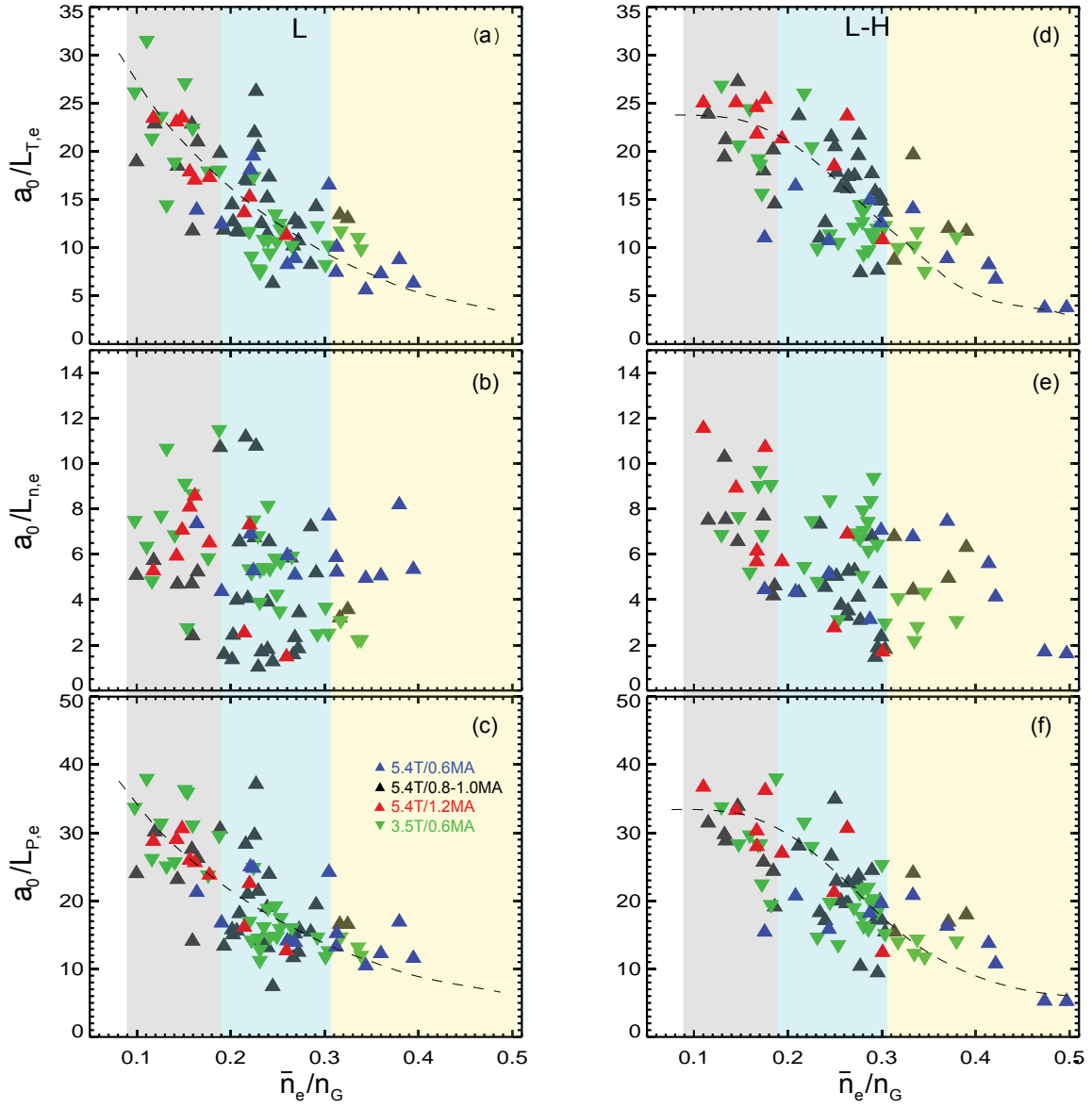


Fig.14. Illustration of  $a_0/L_T$ ,  $a_0/L_n$ ,  $a_0/L_p$  in low power L-mode plasmas, versus  $\bar{n}_e/n_G$  at  $\rho=0.95$ , in low power L-mode (left) and at L-H (right). Dash lines are intended to guide the data trends. Shaded areas represent sheath-limited (gray), high-recycling (cyan), and detachment (yellow) regime, respectively.

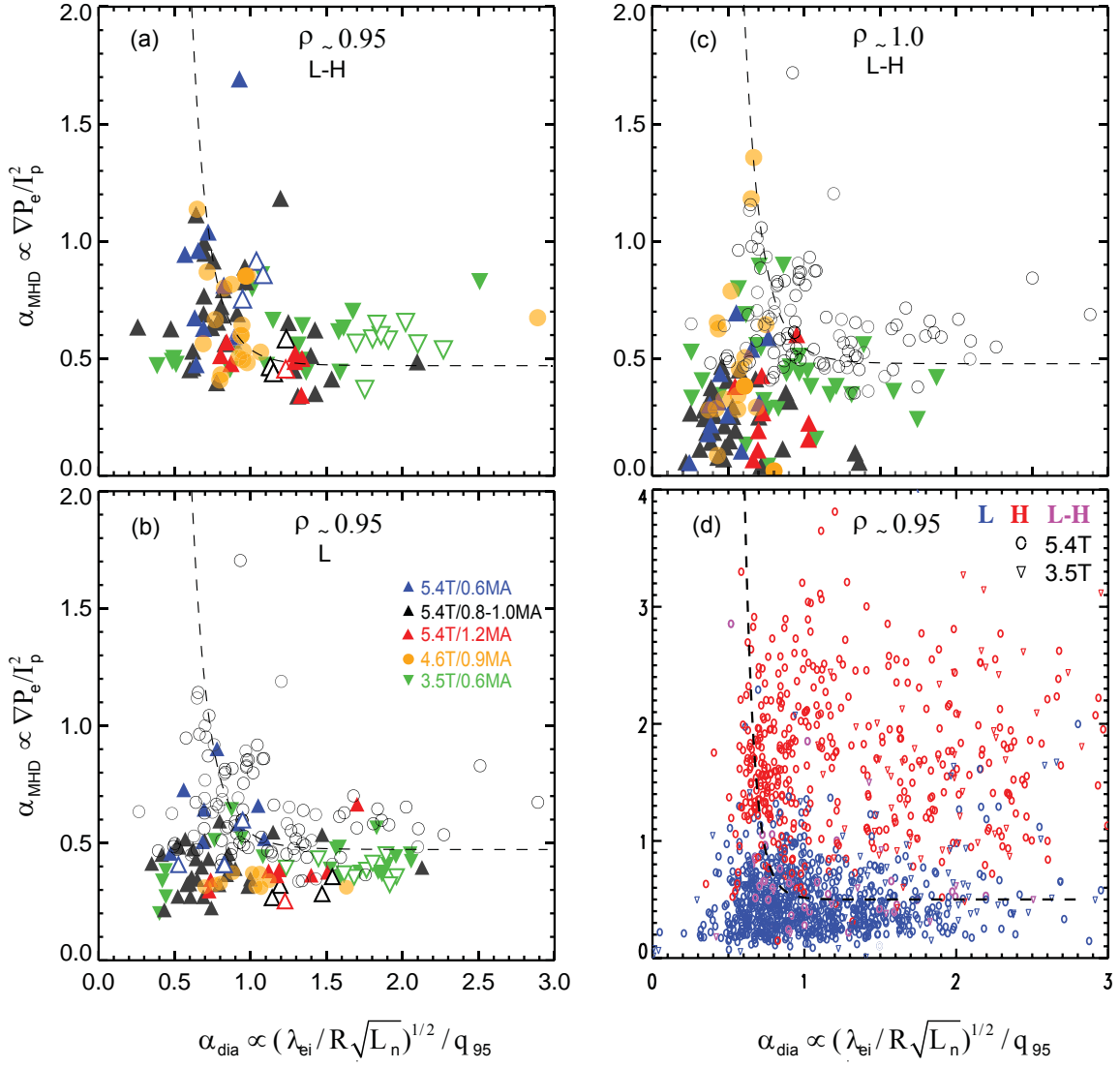


Fig.15. Plot of  $\alpha_{MHD}-\alpha_{dia}$  of (a) L-H at  $\rho=0.95$  (b) Low-power L-mode at  $\rho=0.95$  (c) L-H at  $\rho=0.95$  (d) L-mode, L-H (last two points prior to transition), and H-mode at each TS pulse in 5.4T and 3.5T plasmas. Data from (a) are over plotted on (b) and (c) by open circles. Low density data of  $\bar{n}_e < 1.0 \times 10^{20} \text{ m}^{-3}$  at L-H are shown in open triangles on (a) and (b). Theory (RDZ model) predicted L-H boundary is shown by dashed line on each plot. The density coverage is  $0.6 \times 10^{20} \text{ m}^{-3} < \bar{n}_e < 2.1 \times 10^{20} \text{ m}^{-3}$ .



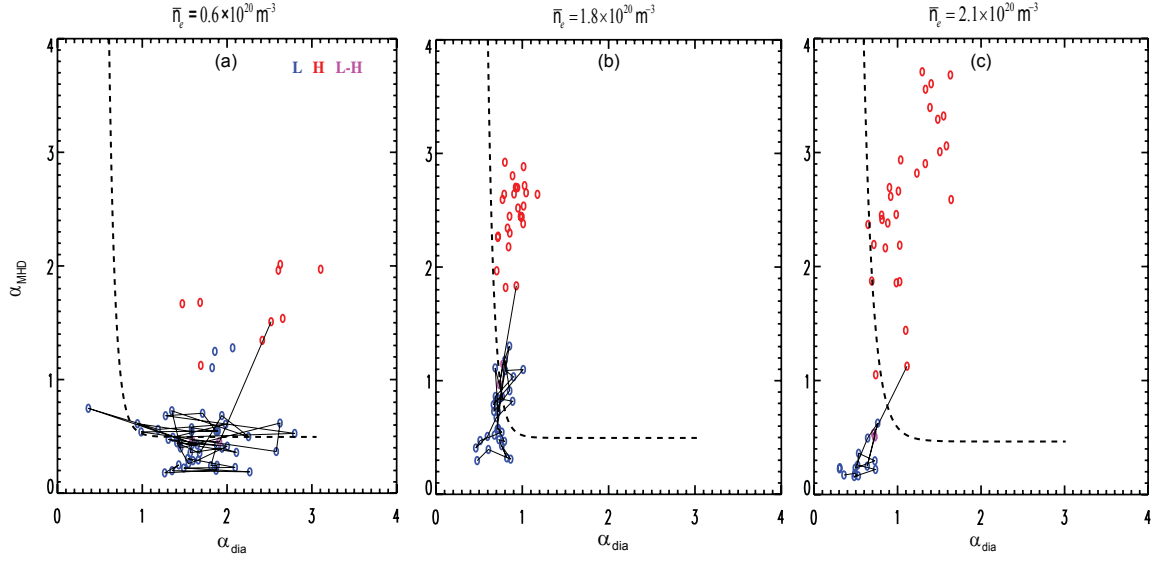


Fig.16. Comparison of time evolution of plasma states on  $\alpha_{MHD}$ - $\alpha_{dia}$  diagram from L-mode to H-mode at three different plasma densities: (a)  $\bar{n}_e = 0.6 \times 10^{20} \text{ m}^{-3}$  (b)  $\bar{n}_e = 1.8 \times 10^{20} \text{ m}^{-3}$  (c)  $\bar{n}_e = 2.1 \times 10^{20} \text{ m}^{-3}$ . Each point represents a TS pulse.

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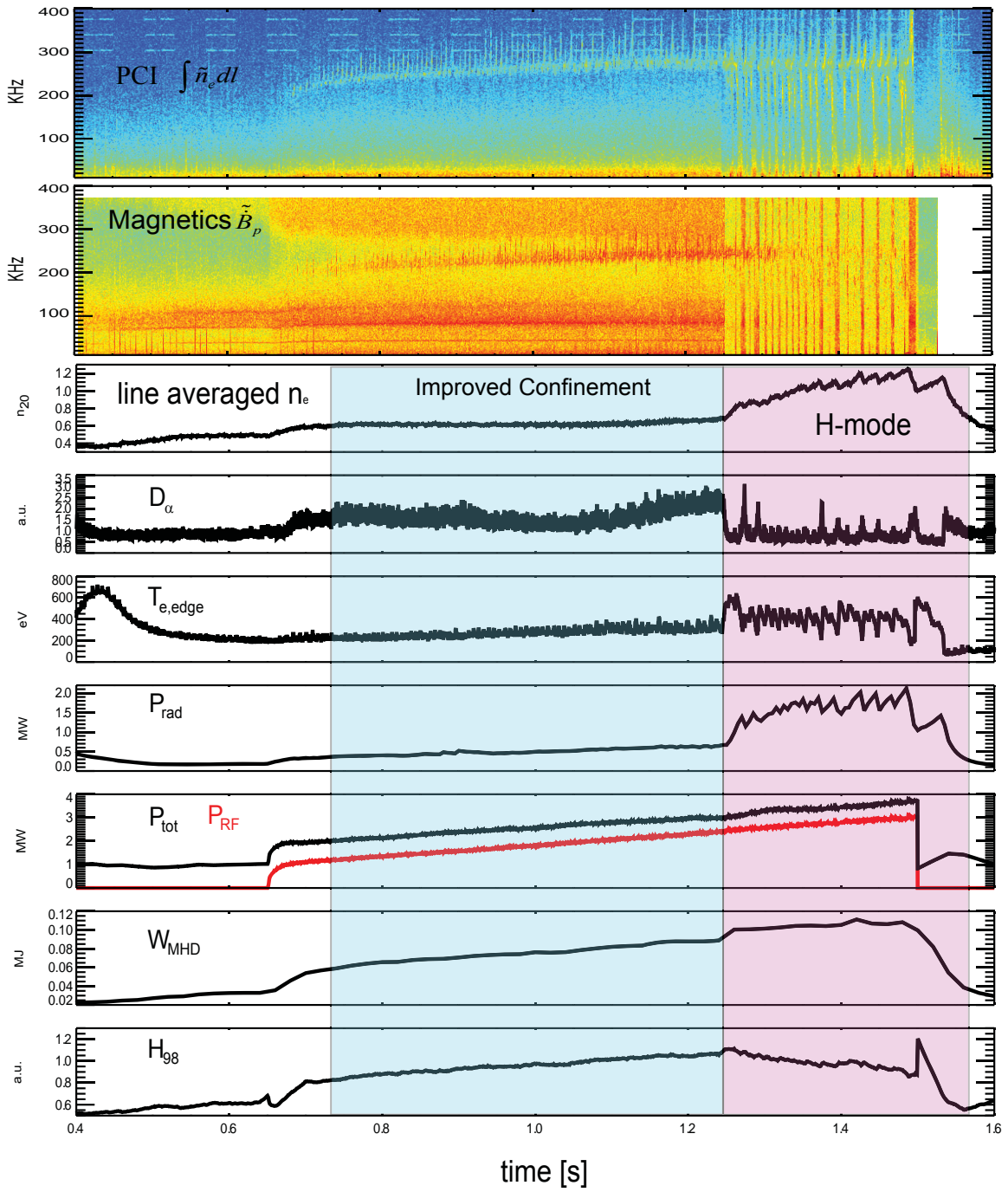


Fig.17. Time histories of global plasma parameters and plasma fluctuations in a low density discharge. Improved confinement phase lasted from 0.7s to 1.24s. H-mode was accessed at 1.24s.

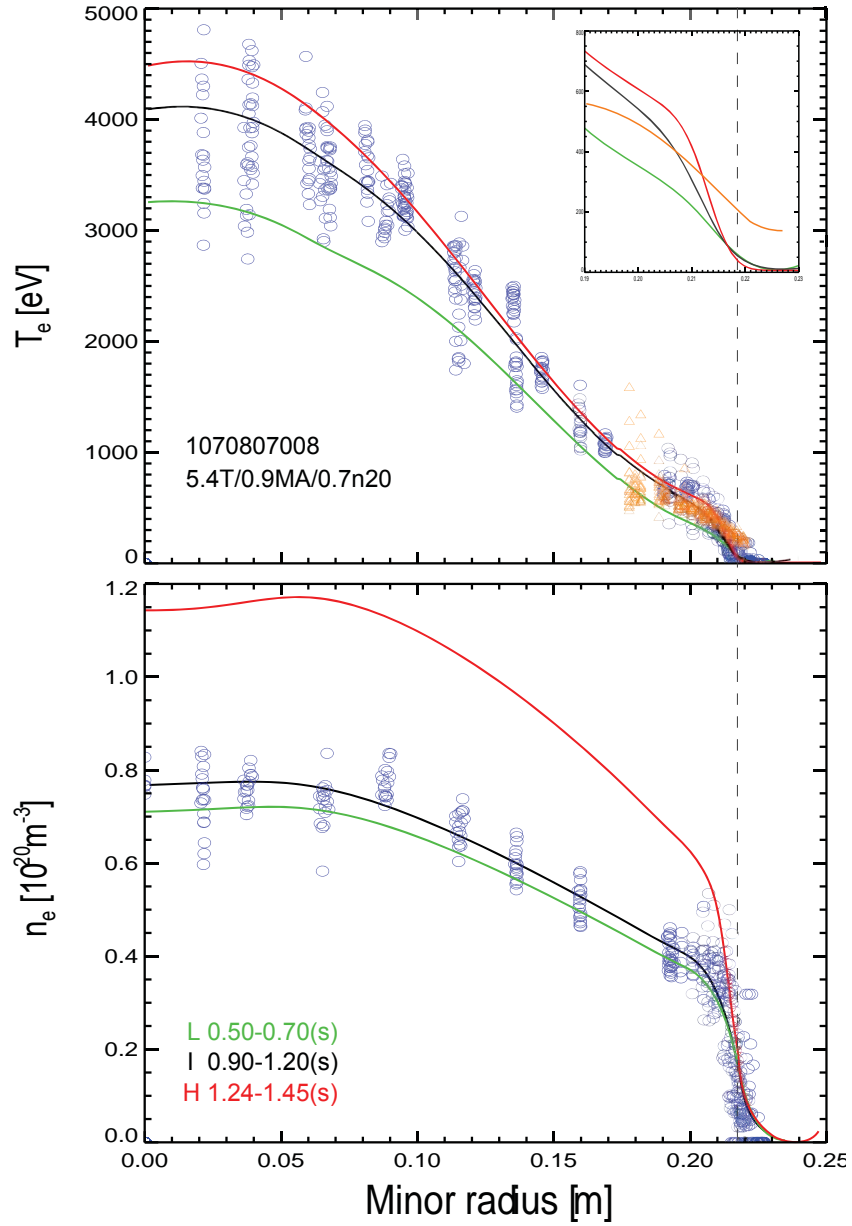


Fig.18. Time averaged  $T_e$  (top) and  $n_e$  (bottom) profiles in L-mode (green), Improved confinement (black) and H-mode (red) plasmas. TS measurements in the improved confinement phase are shown in blue open circles. The  $B^{5+}$  impurity ion temperature ( $T_I$ ) measurements from charge exchange recombination spectroscopy in the same time period are represented by yellow triangles in the top panel.