# Vehicular Trip Estimation in Urban Areas 

James J. Schuster<br>Graduate Assistant and<br>Harold L. Michael<br>Associate Director<br>Joint Highway Research Project<br>Purdue University

## INTRODUCTION

A standard metropolitan statistical area is defined (except in New England) as a county or a group of contiguous counties which contain at least one city of 50,000 inhabitants or more or "twin cities" with a combined population of at least 50,000 . In addition to the county or counties containing such a city or cities, contiguous counties are included in a standard metropolitan area if, according to certain criteria, they are essentially metropolitan in character and are socially and economically integrated with the central city. In New England, towns and cities rather than cities and counties are the units used in defining standard metropolitan statistical areas (1).*

In 1960 there were 212 standard metropolitan areas in the United States of which 188 had a population less than one million. Table 1 shows the number of these areas in each of four ranges of population.

TABLE 1
Classification of Standard Metropolitan Statistical Areas

| Population Classification | No. of Areas 1960 Census | Percent of Total | Cumulative Percentage |
| :---: | :---: | :---: | :---: |
| 50,000-100,000 |  | 10.38 | 10.38 |
| 100,000-500,000 ... | 137 | 64.62 | 75.00 |
| 500,000-1 million | 39 | 13.68 | 88.68 |
| Over 1 million ....... | 24 | 11.32 | 100.00 |
| Total ............ | 212 | 100.00 |  |

[^0]

Fig. 1. Standard metropolitan statistical areas, 1960.

Of the 180 million people in the United States in 1960, approximately 63 percent lived in those 212 metropolitan areas. The locations of the standard metropolitan statistical areas are shown in Figure 1. The projected population of the United States for 1980 is 245 million people, with 75 percent of them living in urban areas. These urban inhabitants will perform millions of miles of daily travel within the city in which they live, and a major share of it will be made by automobile.

The optimum location and design of urban transportation facilities require a reasonably accurate estimate of the usage of each facility in the design hour of the design year. Good estimates of this usage appear to be possible from a knowledge of the current travel patterns of the city. Consequently many cities have conducted travel pattern studies, commonly known as origin-destination surveys. Such a study provides information on the current travel patterns of an individual city, and techniques are available to project the patterns to a future year. These studies, however, are time-consuming and expensive. Moreover, past studies indicate a similarity of travel patterns in cities of similar size and it is generally acknowledged that travel of urban residents has many similar characteristics.

Synthesis of these travel patterns from characteristics of the city and its inhabitants has been the subject of considerable recent study. Each of these studies, however, has generally been performed in only one city and the resulting techniques have not been entirely satisfactory when applied to another city.

Several of the cities in the standard metropolitan statistical areas have had recent transportation studies, including origin-destination. The possibility existed, therefore, of analyzing the results of several of these studies in the hope that techniques and models for synthesizing the travel patterns of cities of similar size in these areas could be developed.

The purpose of this research was to develop a method for synthesizing urban travel patterns through an evaluation of various factors which affected travel patterns in 14 urban areas.

The study included an investigation of travel pattern characteristics in standard metropolitan statistical areas less than one million population. This population classification was chosen because of the possible homogeneity in the factors affecting transportation facilities. Statistical analyses of data from the 14 cities were made to evaluate correlations in urban travel pattern characteristics. Urban vehicular trip patterns, peak-hour travel and design hour volume, truck trips, and traffic generation of the central business district were among the characteristics investigated.

## STATISTICAL ANALYSIS PROCEDURES

One of the most useful tools available to the planner is statistics. Particularly in the field of trip prediction, the techniques of simple regression, multiple regression, and model evolution are extremely useful. One important statistical measure is the square of the correlation coefficient. This provides a measure of the amount of variability of a dependent variable that is explained by the independent variable or variables. This explained variation $\left(\mathrm{R}^{2}\right)$ is referred to as the coefficient of determination in regression analysis.

The evolution of models from data using multiple regression procedures allows the acquisition of maximum information from collected data. Without the use of a computer, model evolution would be impossible due to the enormous amount of calculation. Two procedures available for evolving a model are the "build-up" and the "tear down." The former method involves finding the simple correlation coefficients among all independent and dependent variables and then selecting the variables to go into the model. Independent variables which do not add enough explained variation of the dependent variable to warrant their inclusion in the model are not included. To examine the amount of additional explained variation, the F-test is generally utilized.

There is more flexibility in the choice of variables to be included in the final model in the "tear-down" method. At first all independent variables are placed in the model. Then subsets, usually consisting of those independent variables which have the largest simple correlations with the dependent variable and the smallest simple correlations with the independent variables, are tested. There may be reason to retain certain variables in the model and this may be accomplished by including them in the subsets. Many subsets are tried, and a comparison is made on the fractional amounts of variation in the dependent variable explained by the independent variables before a model is finally decided (2).

One element that must be considered in model evolution is the use of the final model. In planning studies it is often necessary to predict future trips from future land use areas. It is necessary to assume that the factors that affect present day trips will also affect future trips if a model evolved from present day trip data is used for trip prediction. Preference may therefore be given to certain variables which are expected to have similar influences today and in the future even though the highest correlation coefficient may not be attained.

The general model evolved through multiple regression is of the following form (2) :

$$
Y_{i}=B_{0}+B_{1} X_{1 i}+B_{2} X_{2 i}+\ldots B_{k} X_{k i}+e_{i}
$$

where:
$Y_{i}=i$ th observed value of the dependent variable
$\mathrm{B}_{0}=$ parameter
$\mathrm{B}_{1}=$ parameter. $\mathrm{i}=1,2, \ldots \mathrm{k}$
$X_{j 1}=$ the ith observation of the j th independent, fixed variable, which could be an interaction such as $X_{1} X_{2}, X_{1}{ }^{2}, X_{2}{ }^{2}$, etc. $\mathrm{j}=1,2, \ldots \mathrm{j} \ldots \mathrm{k}$ and $\mathrm{i}=1,2, \ldots \mathrm{u}$,
The estimating model is of the following form:

$$
y_{i}=b_{o}+b_{1} x_{1 i}+b_{2} x_{2 i}+\ldots b_{k} x_{k i}+e_{i}
$$

Where:
$b_{0}=$ least square estimate of $B_{0}$
$b_{i}=$ least square estimate of $B_{1}$
$\mathrm{e}_{\mathrm{i}}=$ the ith residual.
To use the above models the three basic assumptions outlined below must be made for tests of significance and confidence intervals.
a. The independent variables are fixed and measured without error.
b. For a set of independent variables, the dependent variable is normally and independently distributed.
c. For any set of independent variables the variances of the dependent variables are homogeneous.

## URBAN TRAVEL PATTERN DEVELOPMENT

## General

For the location and design of a transportation facility a knowledge of the volume of vehicles using the facility at the design hour is imperative. The usual procedure for securing an estimate of such volumes is through an analysis of the travel patterns of the city as determined by an origin-destination survey. Such a survey, however, may not be available or possible of completion before the location of a freeway and its interchanges are necessary. It may be possible, furthermore, to develop methods for estimating the travel patterns of a city from travel pattern characteristics in cities of similar size.

To evaluate the possibility of estimating trip patterns of a city in a standard metropolitan statistical area, data were obtained and analyzed from 14 such cities that had completed a transportation study. This study was restricted to cities with a statistical area population of less than one million.

For each of the 14 study cities there were five basic areas, the central business district, the 1960 city area, the 1960 urbanized area, the 1960 standard metropolitan statistical area, and the transportation study area. The organization that performed each transportation study delimited the central business district and the entire transportation study area. In all cases the latter area was larger than the city area and smaller than the standard metropolitan statistical area.

In all cases the 1960 standard metropolitan statistical area contained the largest population. The populations for four of the basic areas for the study cities are listed in Table 2.

TABLE 2
Populations of Fourteen Study Cities

| City | Transportation Study | 1960 |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 1960 | Urbanized | 1960 |
|  |  | SMSA | Area | City |
| Charlotte | 202262 | 272111 | 209551 | 201564 |
| Chattanooga | 241709 | 283169 | 205143 | 130009 |
| Dayton ... | .. 425000 | 694623 | 501664 | 262332 |
| Denver | .. 816700 | 929383 | 803624 | 493887 |
| El Paso | 268968 | 314070 | 277128 | 276687 |
| Huntsville | .. 73260 | 117348 | 74970 | 72365 |
| Nashville | . 357585 | 399743 | 346729 | 170874 |
| New Orleans | .. 855551 | 868480 | 845237 | 627525 |
| Omaha | .. 296449 | 457873 | 389881 | 301598 |
| San Antonio | 586586 | 687151 | 641965 | 587718 |
| Springfield | .. 99020 | 131440 | 90157 | 82723 |
| Toledo | .. 405000 | 456931 | 438283 | 318003 |
| Tucson | .. 242550 | 265660 | 227433 | 212892 |
| Tulsa ..... | .... 240419 | +18974 | 298922 | 261685 |
| Range | .. 73260- | 117348- | 74970- | 72365- |
|  | 855551 | 929383 | 845237 | 627525 |

In the conduct of this research, data used were obtained from the 1960 census and from the 14 transportation studies. Much of the data from the transportation studies used "dwelling unit" as defined by the 1950 census as a basic unit. The data from the 1960 census used "housing unit" as the basic unit. The main difference between these
units was in the treatment of one-room quarters and this had relatively little effect on comparability of the data for large areas.

In addition to the many variables that were obtained from the census and the transportation studies, many interactions were used in evolving the various models. Interaction is the differential response of one factor in combination with varying levels of a second factor applied simultaneously, that is, interaction is an additional effect due to the combined influence of two or more factors (3).

## Total Vehicle Trips in a Study Area

Total vehicle trips in a study area are comprised of both the internal and external one-way movements. An internal trip has both the origin and the destination within the confines of the delimited study area and includes interzonal trips and intrazonal trips. An external trip may have one or both ends of the trip outside the study area and includes external-internal trips (called local trips in this study) and through trips.

It would be erroneous to compare only the internal trips among the 14 locations because of the variability that exists in the delimiting of the study area. It is obvious that the number of internal trips will increase as the transportation area increases. The percent of total vehicle trips that were internal trips ranged from 75.2 to 96.3 .

The model evolved for this analysis was;

$$
\begin{array}{r}
\mathrm{Y}=+142010+1.53441 \mathrm{X}_{1} \\
-8731.8 \mathrm{X}_{2} \tag{I}
\end{array}
$$

where:
$Y=$ total number of vehicle trips per day in a study area
$\mathrm{X}_{1}=$ transportation study population
$X_{2}=$ percent of employed persons using public transportation to work.

The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 96.9 percent with a sample size of 14 .

## Effect of Study Population and Area

The ratios of external vehicle trips to total vehicle trips and local vehicle trips to internal vehicle trips vary with the size of the transportation study population and area, as shown in Figures 2 and 3.

The lines shown are least square fits of data obtained from the 14 study areas. It is easily seen that as the area increases, population increases,


Fig. 2. Relation of external trips and transportation study population.


Fig. 3. Relation of external trips and transportation study area.
with the effect that fewer trips are included in the external portion of the survey.

It was desired to know if the ratio of external trips and local trips to total trips could be estimated from the factors of population and area. The following models were evolved for this purpose:

$$
\begin{align*}
Y= & 0.4126+10^{-10}\left[0.0242 X_{1} X_{2}{ }^{2}-4644.2 X_{1}-11351\right. \\
& \left.X_{2}{ }^{2}+452.1\left(X_{1} / X_{2}\right)^{2}-1576380\left(X_{1} / X_{2}\right)\right] \tag{II}
\end{align*}
$$

where:

$$
\begin{aligned}
\mathrm{Y}= & \text { ratio of external vehicle trips per day to total vehicle } \\
& \text { trips per day } \\
\mathrm{X}_{1}= & \text { transportation study population } \\
\mathrm{X}_{2}= & \text { transportation study area in square miles }
\end{aligned}
$$

and :

$$
\begin{align*}
\mathrm{Y}= & +0.545+10^{-7}\left[-0.02687 \mathrm{X}_{1} \mathrm{X}_{2}-17.4 \mathrm{X}_{2}{ }^{2}\right. \\
& +7.00\left(10^{-5}\right) \mathrm{X}_{1} \mathrm{X}_{2}^{2}+0.656\left(\mathrm{X}_{1} / \mathrm{X}_{2}\right)^{2}-2774 \\
& \left.\left(X_{1} / X_{2}\right)\right] \tag{III}
\end{align*}
$$

where:

$$
\begin{aligned}
\mathrm{Y}= & \text { ratio of local vehicle trips per day to internal vehicle } \\
& \text { trips per day } \\
X_{1}= & \text { transportation study population } \\
X_{2}= & \text { transportation study area in square miles }
\end{aligned}
$$

The amounts of variability ( $\mathrm{R}^{2}$ ) explained by these models are 87.5 percent and 85.8 percent, respectively, with a sample size of 14 .

## Central Business District

The central business district is the largest traffic generator when considering vehicle trip-ends per square mile as a measure of generation. For the central business districts and the next largest generators, the number of vehicle trip-ends per square mile and the ratio of the two are shown in Table 3 for the 14 cities.

## Vehicle Trips to and from the Central Business District

The internal and external vehicle trips per day to and from the central business district consist of those trips that had either their origin or destination in that particular zone. These trips had an average of 73,556 and ranged from 22,855 in Huntsville to 119,640 in New Orleans. The following model was evolved:

$$
\begin{align*}
Y= & -39570+0.04948 X_{1}+41335 X_{2} \\
& -1443.9 X_{3}+1492.0 X_{4}+28.755 X_{5} \tag{IV}
\end{align*}
$$

'TABLE 3
Traffic Generating Characteristics of the Central Business District

| City | Trip Ends per mi ${ }^{2}$ | Largest Generator Outside CBD <br> Trip Ends per mi ${ }^{2}$ | Ratio of CBD to Next Largest Generator |
| :---: | :---: | :---: | :---: |
| Charlotte ............ | 142055 | 18866 | 7.53 |
| Dayton ............... | $20734+$ | 101539 | 2.04 |
| Denver ............... | 250269 | 39196 | 6.39 |
| El Paso ............. | 355974 | 30349 | 11.73 |
| Huntsville .......... | 201058 | 14990 | 13.41 |
| New Orleans ...... | 213901 | 44730 | 4.78 |
| Omaha ............... | 203101 | 48438 | 4.19 |
| San Antonio ........ | 298055 | 34471 | 8.65 |
| Springfield .......... | 312319 | 43222 | 7.23 |
| Toledo .............. | 261387 | 17498 | 14.94 |
| Tucson ............... | 229446 | 53747 | 4.27 |
| Tulsa | 241870 | 86236 | 2.80 |
| Range .......... | $\begin{array}{r} 142055- \\ 35597+ \end{array}$ | $\begin{aligned} & 14990- \\ & 101539 \end{aligned}$ | $\begin{aligned} & 2.04- \\ & 14.94 \end{aligned}$ |

where:
$\mathrm{Y}=$ vehicle trips to and from the central business district per day
$\mathrm{X}_{1}=$ transportation study population
$X_{2}=$ area of the central business district in square miles
$\mathrm{X}_{3}=$ percent of employed persons using public transportation to work
$\mathrm{X}_{4}=$ percent of employed persons who had white collar occupations
$\mathrm{X}_{5}=$ the interaction of the area of the central business district by the transportation study population density.
The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 94.4 percent with a sample size of 14 .

For the 14 locations there was an average of 13.36 percent of the total vehicle trips that had an origin or destination in the central business district and the range was from 7.80 percent in Toledo to 20.27 percent in Tulsa. The relationship between the daily vehicle trips to
and from the central business district and the daily total vehicle trips in a study area is shown in Figure 4.


Fig. 4. Relation between vehicle trips to and from CBD and total vehicle trips.

## Intrazonal Central Business District Vehicle Trips

The intrazonal central business district vehicle trips are those movements that have both their origin and destination within that particular delimited zone. The lengths of these trips are necessarily very short due
to the small area of the district, which was less than one square mile for all the study locations.

These daily trips ranged from 1,790 in Tucson to 13,976 in New Orleans and the following model was evolved:

$$
\begin{align*}
\mathrm{Y}= & +5790+6406.7 \mathrm{X}_{1}+0.8432 \mathrm{X}_{2} \\
& -1.18459 \mathrm{X}_{3}-0.00017 \mathrm{X}_{4}+0.01909 \mathrm{X}_{5} \tag{V}
\end{align*}
$$

where:
$\mathrm{Y}=$ intrazonal central business district trips per day
$\mathrm{X}_{1}=$ area of the central business district in square miles
$\mathrm{X}_{2}=$ transportation study population density
$X_{3}=$ median family income for the standard metropolitan statistical area
$\mathrm{X}_{4}=$ interaction of transportation study population by the percent of employed persons using public transportation to work
$\mathrm{X}_{5}=$ interaction of the transportation study population by the area of the central business district.
The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 98.5 percent with a sample size of 14 .

## Study Zones

For the evolution of models for the number of vehicle trips per day attracted to and generated by a zone, the number of vehicle trips per day in both directions between a zone and the central business district, and the number of interzonal vehicle trips per day, 75 study zones, excluding the central business district, were chosen from 13 study cities. These were chosen on the basis of being representative of the entire study area.

Analyses, therefore, were made on the vehicle trips attracted to and generated by 75 zones, the vehicle trips in both directions between those 75 zones and their respective central business districts, and the interzonal vehicle trips within the cities. The resulting number of interchanges was 269.

## Zonal Vehicle Trips

For the 75 study zones a model was evolved for the total number of vehicle trips per day attracted and generated by a zone. Total trips consisted of internal trips, external trips, and intrazonal trips. The following model was evolved:

$$
\begin{align*}
\mathrm{Y}= & -7655-1326.4 \mathrm{X}_{1}+5.0602 \mathrm{X}_{2} \\
& -0.01714 \mathrm{X}_{3}+43.416 \mathrm{X}_{4} \\
& +7.2513 \mathrm{X}_{5}+2.07\left(10^{-6}\right) \mathrm{X}_{6} \tag{VI}
\end{align*}
$$

where:
$\mathrm{Y}=$ total number of vehicle trips per day attracted and generated by a zone
$\mathrm{X}_{1}=$ straight line distance in miles from the centroid of the central business district to the centroid of the study zone
$X_{2}=$ number of passenger cars owned in the study zone
$X_{\mathbf{3}}=$ population of the entire transportation study area
$X_{4}=$ transportation study area in square miles
$\mathrm{X}_{5}=$ transportation study density in persons per square mile
$X_{6}=$ three factor interaction of percent of population that are workers in a study zone by the number of people that are in the study zone by the number of cars that are in the study zone.
The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 91.0 percent with a sample size of 75 .

## Zone-Central Business District Trips

A model for the number of vehicle trips per day in both directions between each of the 75 study zones and its respective central business district was evolved for the study cities. The following model was evolved:

$$
\begin{align*}
Y= & +498+0.46257 X_{1}-96.700 X_{2}+0.68270 X_{3} \\
& +0.01331 X_{4} \\
& -0.01967 X_{5}-0.00300 X_{6}+0.001767 X_{7} \tag{VII}
\end{align*}
$$

where:
$\mathrm{Y}=$ number of vehicle trips per day in both directions between a zone and its central business district
$X_{1}=$ population of the study zone
$\mathrm{X}_{2}=$ straight line distance in miles from the centroid of the central business district to the centroid of the study zone
$\mathrm{X}_{3}=$ number of passenger cars owned in the study zone
$X_{4}=$ two factor interaction of percent of population that are workers in the study zone by the number of people that are in the study zone
$\mathrm{X}_{5}=$ two factor interaction of percent of employed persons who had white collar occupations for the standard metropolitan statistical area by the population of the study zone
$X_{0}=$ three factor interaction of the straight line distance in miles from the centroid of the central business district to the centroid of the study zone by the percent of population that are workers in the study zone by the population of the study zone
$X_{7}=$ three factor interaction of the straight line distance in miles from the centroid of the central business district to the centroid of the study zone by the percent of employed persons who had white collar occupations for the standard metropolitan statistical area by the population of the study zone.

The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 91.7 percent with a sample size of 75 .

Some investigators have related the independent variable of the above model, the number of vehicle trips per day between a zone and the central business district, to the total number of vehicle trips per day attracted and generated by the zone. This relationship for the 75 zones used in this research is shown in Figure 5. The $\mathrm{R}^{2}$ for this relationship for the study zones was 75.4 percent, while that for the evolved model was 91.7 percent.

## Interzonal Vehicle Trips

A model for the number of vehicle trips per day in both directions for the zonal interchanges between the non-CBD zones in the study cities was evolved. The following model was evolved:

$$
\begin{align*}
\mathrm{Y}= & 796.2-0.108+\mathrm{X}_{1}-0.04275 \mathrm{X}_{2}-133.7 \mathrm{X}_{3}- \\
& 6.223 \mathrm{X}_{4} \\
& +15.29\left(10^{-4}\right) \mathrm{X}_{5}+20.84\left(10^{-4}\right) \mathrm{X}_{6}-0.7401 \\
& \left(10^{-2}\right) \mathrm{X}_{7} \\
& +0.1018\left(10^{-4}\right) \mathrm{X}_{8}-0.5256\left(10^{-5}\right) \mathrm{X}_{9}+0.7234 \\
& \left(10^{-3}\right) \mathrm{X}_{10} \\
+ & 52.37\left(10^{-6}\right) \mathrm{X}_{11}+1.262 \mathrm{X}_{12}-11.10\left(10^{-10}\right) \\
& \mathrm{X}_{13}-3.564\left(10^{-14}\right) \mathrm{X}_{14} \\
& -8.876\left(10^{-10}\right) \mathrm{X}_{15}-0.3867\left(10^{-11}\right) \mathrm{X}_{16}+ \\
& 0.1507\left(10^{-6}\right) \mathrm{X}_{17} \\
- & 0.1886\left(10^{-6}\right) \mathrm{X}_{18}+1.443 \mathrm{X}_{19}-0.1514 \mathrm{X}_{20}
\end{align*}
$$

where:
$Y=$ number of vehicle trips per day in both directions for zonal interchanges between non-CBD zones.
$X_{1}=$ number of cars owned in the smaller populated zone.
$X_{2}=$ number of cars owned in the larger populated zone.
$\mathrm{X}_{3}=$ distance in miles between the centroids of the two zones.
$\mathrm{X}_{4}=$ angle in degrees between centroid of zone i and centroid of zone $j$ with the vertex at the centroid of the central business district.


Fig. 5. Relation between CBD trips and total trips for study zones.
$X_{5}=$ two factor interaction of the population of the smaller populated zone by the percent of population under 34 years that are enrolled in school for that zone. This is a measure of the school enrollment for that zone.
$X_{6}=$ two factor interaction of the population of the smaller populated zone by the percent of workers in that zone. This is a measure of the number of workers in that zone.
$X_{\mathbf{7}}=$ two factor interaction of the population of the smaller populated zone by the straight line distance in miles between the centroids of the two zones.
$\mathrm{X}_{8}=$ two factor interaction of the population of the larger populated zone by the percent of population under 34 years that are enrolled in school for that zone. This is a measure of the school enrollment for that zone.
$\mathrm{X}_{9}=$ two factor interaction of the population of the larger populated zone by the percent of workers in that zone. This is a measure of the number of workers in that zone.
$X_{10}=$ two factor interaction of the population of the larger populated zone by the straight line distance in miles between the centroids of the two zones.
$X_{11}=$ two factor interaction of the number of passenger cars owned in one zone by the number of passenger cars owned in the other zone.
$X_{12}=$ two factor interaction of the distance in miles between the centroids of the two zones by the angle in degrees between the two zones with the vertex at the central business district.
$X_{13}=$ four factor interaction of population of a zone by percent of population under 34 years that are enrolled in school in that zone by population of the other zone by percent of population under 34 years that are enrolled in school of the other zone. This is a measure of the two factor interaction of school enrollment by school enrollment.
$X_{14}=$ four factor interaction of population of a zone by median income of families in that zone by population of the other zone by median income of families in the other zone.
$X_{15}=$ four factor interaction of population of a zone by percent of workers in that zone by population of the other zone by percent of workers in the other zone. This is a measure of the two factor interaction of workers by workers.
$X_{16}=$ three factor interaction of population of a zone by population of the other zone by transportation study population.
$\mathrm{X}_{17}=$ three factor interaction of population of a zone by population of the other zone by percent using public transportation to work for the standard metropolitan statistical area.
$\mathrm{X}_{18}=$ three factor interaction of population of a zone by population of the other zone by the straight line distance in miles between the centroids of the two zones.
$\mathrm{X}_{19}=$ three factor interaction of the straight line distance in miles between the zone and the central business district, between the other zone and the central business district and between the two zones.
$\mathrm{X}_{20}=$ three factor interaction of the straight line distances in miles from the centroid of the zone to the central business district by the distance from the other zone to the central business district by the angle in degrees between the two zones with the vertex at the central business district.
$X_{21}=$ two factor interaction of the population of the smaller zone by the percent of workers in that zone divided by the two factor interaction of the population of the larger zone by the percent of workers in that zone. This is a measure of the ratio of workers between two zones.

The amount of variability ( $\mathrm{R}^{2}$ ) explained by this model is 70.0 percent with a sample size of 269 .

## DESIGN HOUR TRAFFIC VOLUME

Since a transportation facility should operate efficiently most of the time, the period of greatest interest is that of peak-hour travel. A relationship, therefore, between average daily traffic and peak-hour travel is desired.

The hourly variations in vehicle traffic volumes for 16 of the daily hours were available for seven of the 14 study cities. All of the locations were quite similar in pattern as is shown in Figure 6. For all cities the evening peak was the highest and it occurred between 4 p.m. and 6 p.m. The mean for this primary peak was 8.8 percent with a range from 8.3 to 9.3 percent. The secondary peak, which occurred between 7 a.m. and 9 a.m. for all locations, had a mean of 7.1 percent and a range from 6.0 to 8.4 percent.

The hourly traffic variation for all large urban areas may be quite similar, as Figure 7, which shows the hourly average of the seven cities (all of which had less than one million population), does not indicate a


Fig. 6. Hourly variations in traffic flow for 7 cities.
significant variation for the Detroit area, which has approximately four million people. The evening peaks are quite similar, even though the peak hour extends over a longer period of time in Detroit, 3 to 6 p.m.

Thus it appears that the average peak hour traffic volume for a facility could be estimated quite reliably from the average daily traffic


Fig. 7. Comparison of mean hourly variations in traffic flow with Detroit.
volume of that facility by the use of the mean percentage of 8.8 for the peak hour.

The average peak hour volume, however, is not normally the one used for design purposes. The peak-hour volume representative of the thirtieth highest hourly volume of the year is the generally accepted criterion. Exception may be necessary in those areas or locations where concentrated recreational or other travel during some seasons of the year results in a distribution of traffic volume of such nature that a sufficient number of hourly volumes are so much greater than the thirtieth highest hourly volume that they cannot be tolerated and a higher value must be considered in design (4).

The typical daily and monthly variations in addition to the hourly variations were available for Chattanooga, Nashville, New Orleans, and Tucson. These two variations are illustrated in Figures 8 and 9. For all four cities the lowest and highest daily variations occurred on Sunday and Friday respectively, but there was a wide range of values. The two Tennessee cities had the lowest monthly variations in February and the highest in June, while Tucson had the highest in February and lowest


Fig. 8. Daily variations in traffic flow.


Fig. 9. Monthly variations in traffic flow.
in July. New Orleans had a peak in January and the lowest percent occurred in March.

Using the hourly, daily, and monthly variations in these four cities, a computer program was written for the estimation of the percent of daily traffic which traveled during 2,016 hours of the year in each of the four cities. The equation for this program was

$$
\mathrm{C}_{\mathrm{ijk}}=\mathrm{H}_{\mathrm{i}} \times \mathrm{D}_{\mathrm{j}} \times \mathrm{M}_{\mathrm{k}}
$$

Where:
$\mathrm{C}_{\mathrm{ijk}}=$ percent of hourly traffic divided by the annual average daily traffic for the ith hour of the j th day in the kth month.
$\mathrm{H}_{\mathrm{i}}=$ percent of hourly traffic for the $i$ th hour, $\mathrm{i}=1,2, \ldots 24$.
$\mathrm{D}_{\mathrm{j}}=$ daily factor for the jth day, obtained by dividing the volume of traffic on the jth day by the average daily volume, $\mathrm{j}=1,2, \ldots 7$.
$\mathrm{M}_{\mathrm{k}}=$ monthly factor for the kth month, obtained by dividing the volume of traffic in the kth month by the average monthly volume, $\mathrm{k}=1,2, \ldots 12$.
Except for a few special events which might have had unusually high volumes of traffic in these cities, the values obtained from the
equation are representative of all hours of the year because the weekly variations in traffic within one month (which were not included) are small and generally not enumerated in a volume count program.

The analysis made on the data from the four cities is summarized in Table 4, which also shows the average values from the "Highway

TABLE 4
Hourly Percent of Average Daily Traffic

|  | Highest | 10th | 20th | 30 th | 50th | 100th | 180th | Lowest |
| :--- | :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Chattanooga | 10.0 | 9.8 | 9.5 | 9.4 | 9.2 | 9.0 | 8.7 | 0.3 |
| Nashville | 10.6 | 10.5 | 10.3 | 10.1 | 9.9 | 9.7 | 9.4 | 0.5 |
| New Orleans | 10.1 | 9.8 | 9.6 | 9.5 | 9.5 | 9.3 | 9.1 | 0.3 |
| Tucson | 9.8 | 9.8 | 9.7 | 9.3 | 9.1 | 8.9 | 8.6 | 0.3 |
| Mean | 10.1 | 10.0 | 9.8 | 9.6 | 9.4 | 9.2 | 9.0 | 0.4 |
| Highway <br> $\quad$Capacity <br> Manual $^{1}$ | 12.4 | 10.9 | 10.5 | 10.2 | 9.5 | N.A. ${ }^{2}$ | N.A. | N.A. |

1 Average for 38 locations in 8 cities.
2 N.A.-Not Available.

Capacity Manual" for 38 locations in eight cities (5). It is interesting to note the small difference in percentages for the highest 100 hours in each of the four cities. Close agreement between their means and the means from the manual exists, with the largest difference occurring at the highest hour. The values from the four cities are also in agreement with the suggested values of the American Association of State Highway Officials, which are 7 to 18 percent of the average daily traffic with a mean of 11 percent. Table 4 also verifies the characteristic that the fluctuation in peak-hour volumes from day-to-day in any one year is relatively small on urban arterials (4). From these observations, a value of ten percent of the average daily traffic should be a good estimate for the design hour volume in an urban area within a standard metropolitan statistical area.

This relation between the design hour volume (30th highest hour) and average daily traffic on urban facilities is lower than on rural facilities, as is illustrated in Figure 10, which shows the curves for the mean of the study cities, the average for 167 main rural highway locations in 48 states (6), and an urban through route from the Connecticut State Highway Department (7).


Fig. 10. Relation between peak-hour and average daily traffic volumes.

## SOME IMPORTANT VARIATIONS

IN DESIGN HOUR VOLUMES
The volume of traffic during the design hour is that volume in the design year for which sufficient capacity should be provided. The capacities required for a freeway and its interchange ramps, however, are vitally affected by the number of trucks in the design hour volume and in the distribution of the direction of travel during the design hour.

Average daily traffic volume consists of passenger cars and trucks. Light delivery trucks, such as panels and pickups, are normally considered as passenger cars. Trucks include all buses, single-unit trucks, and truck combinations, that is, vehicles with dual tires on the rear axle or those having 9,000 pounds or greater gross vehicle weight rating. Truck trips during the design hour often are considered as a percentage of total vehicular traffic and are referred to by the letter $T$ (4).

Average daily truck trips averaged 16.20 percent of the total vehicular trips for the 14 study cities and ranged from 7.39 percent in Huntsville to 25.98 percent in New Orleans. A regression analysis relating truck trips to total vehicle trips for all the cities was made and the relation is given below.

$$
\begin{equation*}
Y=-19900.5+0.20631 X \tag{IX}
\end{equation*}
$$

where:
$\mathrm{Y}=$ truck trips per day in the study area
$X=$ total vehicle trips per day in the study area
The relationship between truck trips and total vehicle trips is shown in Figure 11.

The hourly variations in truck volumes varied considerably from the hourly variations in total vehicular volumes for the four cities for which these variations were available, as is shown in Figure 12. None of the four cities had the truck peak hours occurring from 4 p.m. to 6 p.m., which were the peak hours for total vehicle trips, but had peaks


Fig. 11. Relation between truck trips and total vehicle trips.


Fig. 12. Hourly variation in truck volumes (percent).
beginning at 8 a.m., 9 a.m., 10 a.m., and 2 p.m. The mean percent of trucks traveling during the peak hour of total travel (4-6 p.m.) was 7.2 percent of total truck trips.

A value for the percent of total vehicle trips that are truck trips at the design hour may be estimated from the equation below.

$$
\mathrm{T}=\frac{\mathrm{K}_{\mathrm{T}} \mathrm{AD}^{\text {Trucks }}}{\mathrm{K} \mathrm{ADT}} \times 100
$$

where:
T $\quad=$ percent of total vehicles that are trucks at the design hour.
$\mathrm{K}_{\mathrm{T}} \quad=$ percent of truck trips at the design hour.
$\mathrm{K} \quad=$ percent of total trips at the design hour.
$\mathrm{ADT}_{\text {Trucks }}=$ average daily traffic of trucks at the design year.
ADT $\quad=$ average daily traffic of vehicles at the design year.
$\mathrm{K}_{\mathrm{T}}$ was found to have a mean value of 7.2 for the four cities of this study which had this information available. A good value for K was previously shown to be 10.0 percent. The use of these values will permit an estimation of $T$ which should be adequate for the determination of capacity requirements during the design hour.

The second factor previously mentioned as important in the determination of capacity requirements was directional distribution of traffic volume during the design hour. Considerable research on this factor has indicated that rarely is traffic evenly distributed during the design hour, although this situation may be approached in and near the central business area (5). The amount of traffic flowing in the direction of heavier movement in urban areas has normally been found to range from 55 percent near the central business district to 60 percent in intermediate areas to 65 percent in outlying areas (5).

## Conclusions

These conclusions are applicable to major urban areas of standard metropolitan statistical areas of less than one million population.
A. The following travel pattern elements or characteristics can be reliably estimated for a transportation study area by use of the indicated models developed in this research.

1. The total number of vehicle trips per day-Model I.
2. The ratio of external vehicle trips per day to total vehicle trips per day-Model II.
3. The ratio of local vehicle trips per day to internal vehicle trips per day-Model III.
4. The number of vehicle trips per day to and from the central business district-Model IV.
5. The number of intrazonal central business district vehicle trips per day-Model V.
6. The total number of vehicle trips per day attracted and generated by each zone-Model VI.
7. The number of vehicle trips per day between a zone and the central business district--Model VII.
8. The number of interzonal vehicle trips per day between two zones, excluding the central business district-Model VIII.
B. The central business district is the largest generator of trips within the transportation study area.
C. The number of truck trips per day in a transportation study area can be reliably estimated by the use of Model IX.
D. A good estimate of the design hour volume (30th highest hour) is ten (10) percent of the average daily traffic volume.
Models for trip prediction will not supplant all field studies in urban areas but models are a tool that can assist in the understanding of urban
transportation problems. It is imperative that continuing studies of travel characteristics be made so that travel patterns in urban areas can be thoroughly understood by the transportation planner.

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[^0]:    * Numbers in parentheses refer to entries in the list of references at the end.

