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Engineering Tool for Temperature, Electric Field and Dose Rate Dependence of High Resistivity Spacecraft Materials

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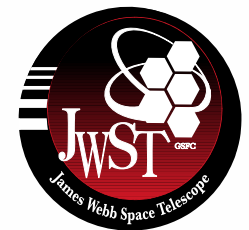
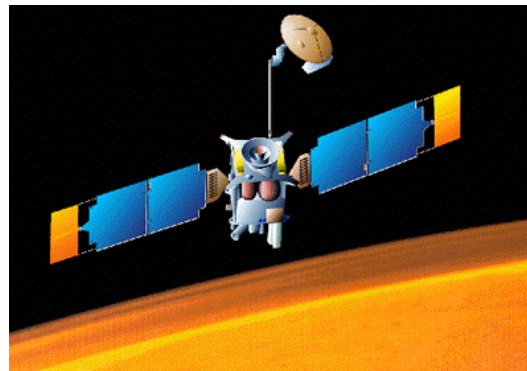
Engineering Tool for Temperature, Electric Field and Dose Rate Dependence of Low Conductivity Spacecraft Materials

JR Dennison, Alec Sim, Jerilyn Brunson, Jodie Gillespie, Steven Hart, Justin Dekany, Charles Sim, and Dan Arnfield

*Materials Physics Group
Utah State University*

Study Support by NASA JWST Project

UtahState
UNIVERSITY



**AIAA Aerospace Sciences Meeting
January, 2009**

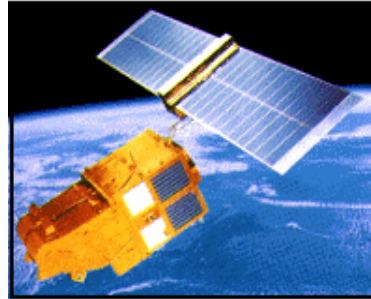
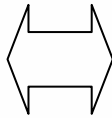
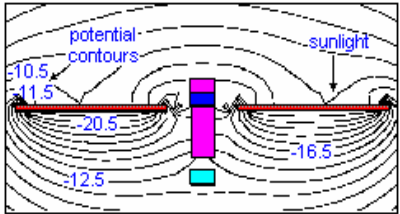
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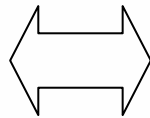
JR Dennison
Jon Abbott
Jennifer Albrecht
Jeri Brunson
Kathryn Chapman
Jodie Corbridge
Steve Hart
Josh Hodges
Ryan Hoffmann
Jake Knight
David Oliphant
Tony Thomas



Surface Voltages Predicted by Spacecraft Charging Models



SEE Handbook or NASCAP predicts on-orbit spacecraft charging in GEO and LEO environments



Materials Research



NASCAP Upgrades



craft Charging Handbook - Microsoft Internet Explorer

Address: D:\SEEHandbook\program\HomePage\Home.htm

INTERACTIVE SPACECRAFT CHARGING HANDBOOK

Plot: Potential vs. Time

Surface Charging: Three Dimensional

Potential [V] vs. time [s] graph showing Max, Min, and Chassis potential over 4000 seconds.

3D visualization of a cube with colored surfaces representing potential distribution.

Spacecraft Name: Wcube

Eclipse Environment: Worst_Case

GEO Location:	Material:	DPoill	Tungston
Longitude: 1	Color: Red	0	0
Universal Time: Year 2000 Day 272	Sunlit Area (m ²)	9.33	14.7
H: 0 M: 00 S: 00	Dark Area (m ²)	2.508e-7	2.568e-7
Sun Direction: 0.0 0.0 1.0	Max. Potential (kV)	2.569e-7	2.568e-7
Details:	Max. Differential (kV)	2.0430e-9	0
	Min. Differential (kV)	1.4857e-10	0
	Initial Current (A)	-9.80e-6	9.81e-6
	Final Current (A)	-9.80e-6	9.80e-6

Typical SEE Handbook Simulation

USU Resistivity Engineering Tool Inputs

Mathcad - [USU Resistivity Engineering Tool Ver. 1-3]

File Edit View Insert Format Tools Symbolics Window Help

My Site Normal Arial 10 B I U

USU Resistivity Calculator Engineering Tool

1-24-08 Ver. 1.2
JR Dennison

This Mathcad worksheet calculates the resistivity of JWST spacecraft materials as a function of electric field (E), temperature (T), and adsorbed dose rate (D) based on parameterized, analytic functions used to model an extensive data set taken by the Utah State University Materials Physics Group.

All input required for each material and run are highlighted in yellow.

Physical Constants and Units

Select Material from pull down box:

Mat_{num} = 2

Material

Enter T, E and D to evaluate resistivity at:

$E_{ev} := 10^6 \cdot V \cdot m^{-1}$

$T_{ev} := 350 \cdot K$

$D_{ev} := 0.03 \cdot Rad \cdot sec^{-1}$

Enter sample thickness:

$d_{ev} := 25 \cdot \mu m$

Electric Field

Temperature

Dose Rate

Sample Thickness

Input data from Excel file

List Materials Related Properties Used in Resistivity Calculations

Material name:	Material_name = "Kapton HN (Kapton)"	
Relative dielectric constant:	$\epsilon_r := 3.400$	Density: $\rho_{den} = 1.42 \cdot gm \cdot cm^{-3}$
Electrostatic breakdown field strength and voltage:	$E_{esd} = 2.700 \times 10^8 \cdot V \cdot m^{-1}$	$V_{esd} := E_{esd} \cdot d_{ev} = 6750 \cdot V$
Fraction of breakdown voltage applied:	$E_{ev} \cdot E_{esd}^{-1} = 0.37 \%$	

These materials properties can be adjusted by enabling the Mathcad statements below.

Density: $\rho_{den} := 1.42 \cdot gm \cdot cm^{-3}$

Relative dielectric constant: $\epsilon_r := 3.4$

Electrostatic breakdown field strength: $E_{esd} := 2 \cdot 10^8 \cdot V \cdot m^{-1}$

Density

Dielectric Constant

ESD Strength

Expand for details of Total Conductivity parameters and model definition

Press F1 for help. AUTO Page 1

USU Resistivity Engineering Tool Inputs

Resistivity Database Master Parameter List

Excel File

Material Index	Material	Thermally Activated Hopping Conductivity				Variable Range Hopping Conductivity			Radiation Induced Conductivity			T_{cr} (low E) (K)	Materials			
		σ_{TAHo}	T_A	E_A	γ_{PF}	σ_{VRHo}	T_o	E_o	k_o	k_I	Δ_I		d	ρ_{den}	ϵ_r	E_{esd}
		($\Omega \cdot \text{cm}$) ⁻¹	(K)	(V·m ⁻¹)	unitless	($\Omega \cdot \text{cm}$) ⁻¹	(K)	(V·m ⁻¹)	(Rad·sec ⁻¹ · $\Omega \cdot \text{cm}$) ⁻¹	unitless	(K ⁻¹)	(K)	(μm)	(g/cm ³)	(-)	(V/m)
1	LDPE	8.00E-08	8866.00	9.52E+08	0.00	1.00E-10	1.03E+08	6.85E+13	3.33E-18	23.00	-3.50E-03	268.00	27.40	0.92	2.26	2.90E+08
2	Kapton HN (Kapton)	2.50E-19	650.00	1.50E+08	0.00	1.00E-40	1.00E+08	1.00E+13	5.00E-18	5.00	0.00E+00	235.00	50.30	1.42	3.40	2.70E+08
3	Kapton E	1.10E-17	1800.00	3.80E+08	0.00	1.00E-40	1.00E+07	1.00E+13	6.00E-18	5.00	0.00E+00	235.00	50.80	1.46	3.10	4.30E+08
4	Kapton FN (616)	1.00E-18	1225.00	2.60E+08	0.00	1.00E-40	1.00E+08	1.00E+13	5.50E-18	5.00	0.00E+00	235.00	28.40	1.53	3.10	2.00E+08
5	PFA (Teflon)	3.00E-01	14000.00	5.00E+80	0.00	1.00E-40	1.00E+08	1.00E+13	4.50E-18	8.00	0.00E+00	235.00	24.10	2.15	2.10	2.60E+08
6	FEP (Teflon)	3.00E-01	14000.00	5.00E+80	0.00	1.00E-40	1.00E+08	1.00E+13	4.50E-18	8.00	0.00E+00	235.00	26.70	2.15	2.00	1.70E+08
7	PTFE (Teflon)	3.00E-01	14000.00	5.00E+80	0.00	1.00E-40	1.00E+08	1.00E+13	4.50E-18	8.00	0.00E+00	235.00	72.90	2.16	2.10	1.20E+08
8	ePTFE (Gortex)	3.00E-01	14000.00	5.00E+80	0.00	1.00E-40	1.00E+08	1.00E+13	4.50E-18	8.00	0.00E+00	235.00	78.20	0.65	1.30	4.30E+07
9	ETFE (Tefzel)	3.00E-01	14000.00	5.00E+80	0.00	1.00E-40	1.00E+08	1.00E+13	4.50E-18	8.00	0.00E+00	235.00	53.10	1.70	2.70	2.40E+08

USU Resistivity Engineering Tool Outputs

Total Resistivity and resistivity contributions from each mechanism:

TOTAL:

$$\rho_{\text{Tot}} := \sigma_{\text{Tot}}(E_{\text{ev}}, T_{\text{ev}}, D_{\text{ev}}, \sigma_{\text{TAH0}}, E_{\text{A}}, T_{\text{A}}, \gamma_{\text{PF}}, \epsilon_r, \sigma_{\text{VRH0}}, E_{\text{O}}, T_{\text{O}}, k_0, k_1, \Delta_1)^{-1} = 8.159 \times 10^{15} \cdot \Omega \cdot \text{cm}$$

TAH: $\rho_{\text{TAH}} := \sigma_{\text{TAH_PF2}}(E_{\text{ev}}, T_{\text{ev}}, \sigma_{\text{TAH0}}, E_{\text{A}}, T_{\text{A}}, \gamma_{\text{PF}}, \epsilon_r)^{-1} = 5.813 \times 10^{16} \cdot \Omega \cdot \text{cm}$

VRH: $\rho_{\text{VRH}} := \sigma_{\text{VRH2}}(E_{\text{ev}}, T_{\text{ev}}, \sigma_{\text{VRH0}}, E_{\text{O}}, T_{\text{O}})^{-1} = 5.549 \times 10^{18} \cdot \Omega \cdot \text{cm}$

RIC: $\rho_{\text{RIC}} := \sigma_{\text{RIC}}(T_{\text{ev}}, D_{\text{ev}}, k_0, k_1, T_{\text{cr}}, \Delta_1)^{-1} = 9.507 \times 10^{15} \cdot \Omega \cdot \text{cm}$

▶ Expand for more complete listing of resistivities and related values

Scope of USU Experimental Studies

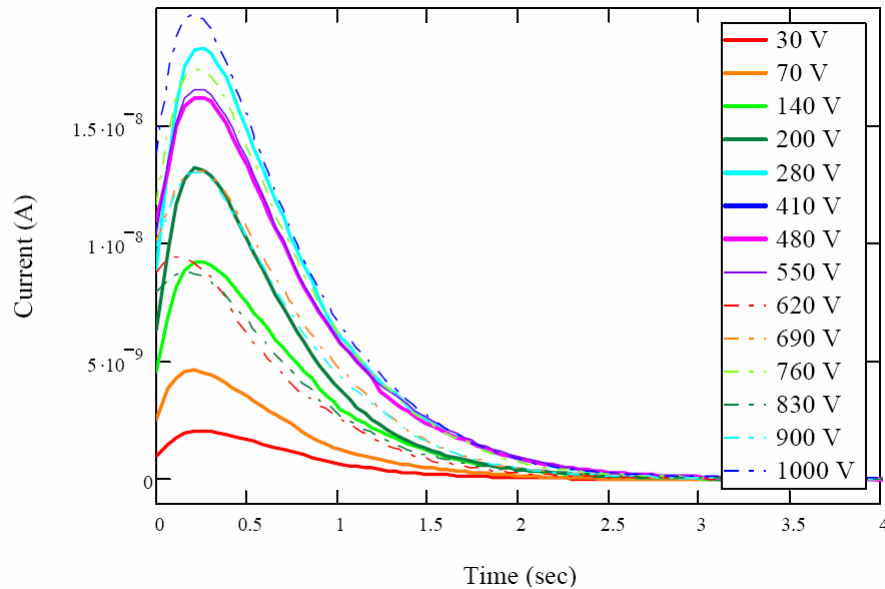
Determine the resistivity and related materials properties of critical JWST materials over the appropriate range of environmental conditions:

- **Temperature:** ~100 K to 365 K
- **Electric field:** low to breakdown field ($\sim 3 \times 10^8$ V/m)
- **Radiation dose:** low dose to ~ 10 rad/sec

Appropriate theory has been used to obtain parametric fits to the data and, where necessary, extend the data to experimentally inaccessible regions.

Validity and range of the theories were determined.

Transient Currents



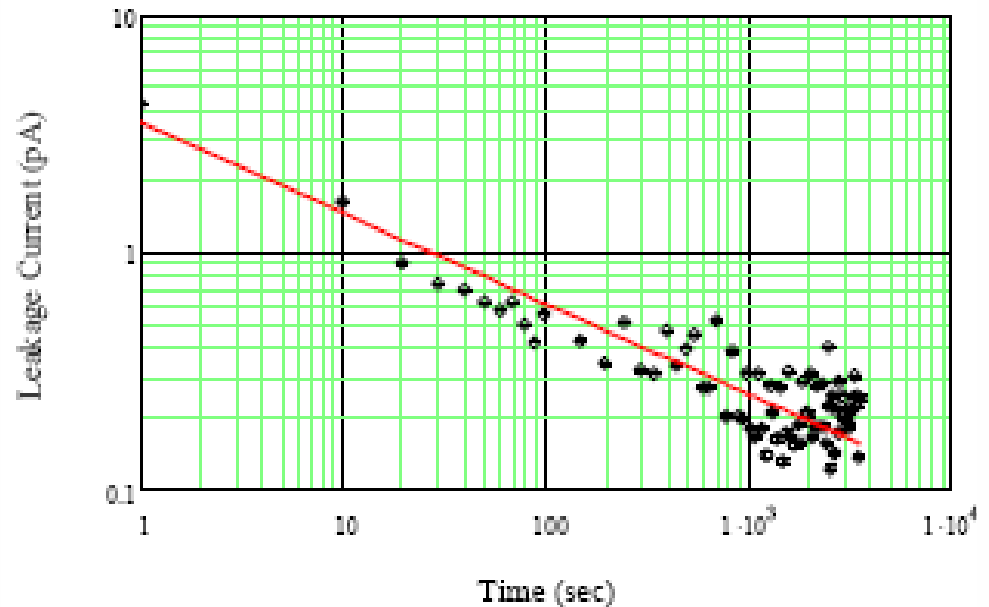
Polarization

$$\sigma_P(t) = \left[\epsilon_o (\epsilon_r^\infty - \epsilon_r^o) / \tau_P \right] e^{-t/\tau_P}$$

Temporal changes in current as sample comes to equilibrium are not considered in this study.

Polarization Current (short term—10 s to a few hrs)

Diffusion Current (long term—10 min to a few days)



Space Charge Diffusion

$$\sigma_{diff}(t) = (q_c D_o / E) \frac{\partial p(t)}{\partial z}$$

RIC Measurements

- Designed and built an entirely new test system
- Characterized instrumentation and methods
- Used standard model for RIC, augmented with T-dependent k and Δ
- Determined k and Δ for JWST materials over range of dose rates encountered by JWST
 - Measurements made from ~ 0.01 to ~ 10 rad/s
- Determined T dependence of k and Δ for JWST materials
 - Measurements made from ~ 105 K to ~ 335 K

Electrostatic Breakdown (ESD) Measurements

- Extensive room T measurements (5-20 per material)
 - Limited studies completed at $T < T_{rm}$, down to ~ 140 K.
 - Limited studies completed on endurance (ramp rate) testing
-
- Breakdown fields were mid- 10^7 V/m to mid- 10^8 V/m for all materials, except ePTFE.
 - Typical results have 10% to 30% variation in V_{esd} .
 - Typically measured results 10-25% higher than manufacturer's values. Attributed to slower ramp rate and dry samples.
 - Found modest dependence on ramp rate.

Conductivity Mechanisms

Engineering tool considers three conductivity mechanisms.

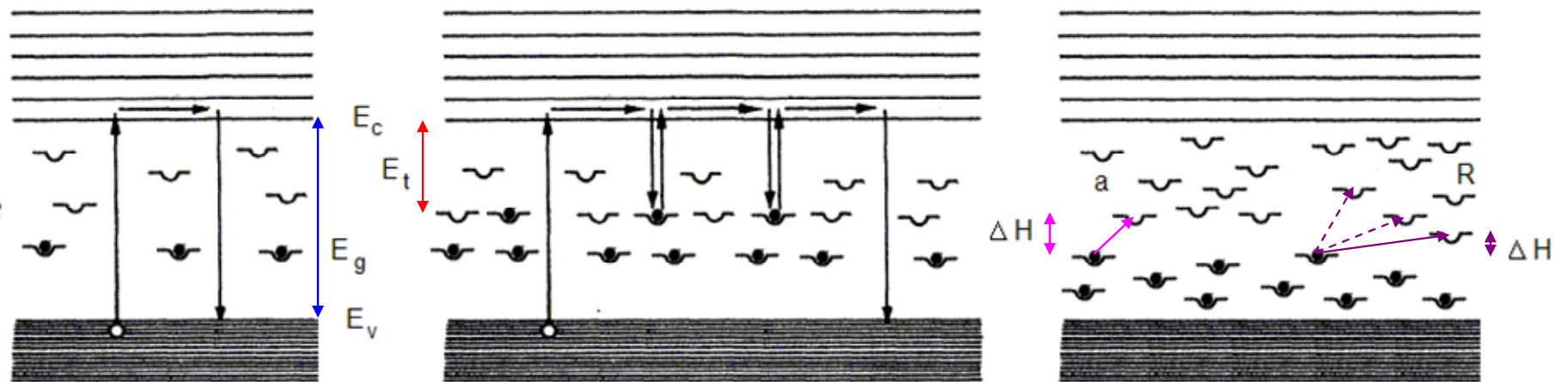
TAH and VRH depend on F and T

RIC depends on D and T

$$\sigma_{Total}(F, T, \dot{D}) = \sigma_{TAH}(F, T) + \sigma_{VRH}(F, T) + \sigma_{RIC}(\dot{D}, T)$$

Conduction Models

Model: T and E Dependence of DC Conductivity



Intrinsic SC

RIC

TAH

VRH

Thermally Activated Hopping Conductivity

TAH theory is based on thermally assisted quantum tunneling from adjacent trap sites of a single well depth and separation.

An E-field favors one direction of motion over another, leading to sinh behavior:

$$\sigma_{TAH}(F, T) = \left[\frac{2N(T)v_{TAH} a q_e}{F} \right] \exp\left[\frac{-\Delta H}{k_B T} \right] \sinh\left[\frac{a q_e F}{k_B T} \right] = \left\{ \sigma_{TAHo}(T) \left(\frac{T_A}{T} \right) Z_A(\beta_A) \exp\left(-\frac{T_A}{T} \right) \right\}$$

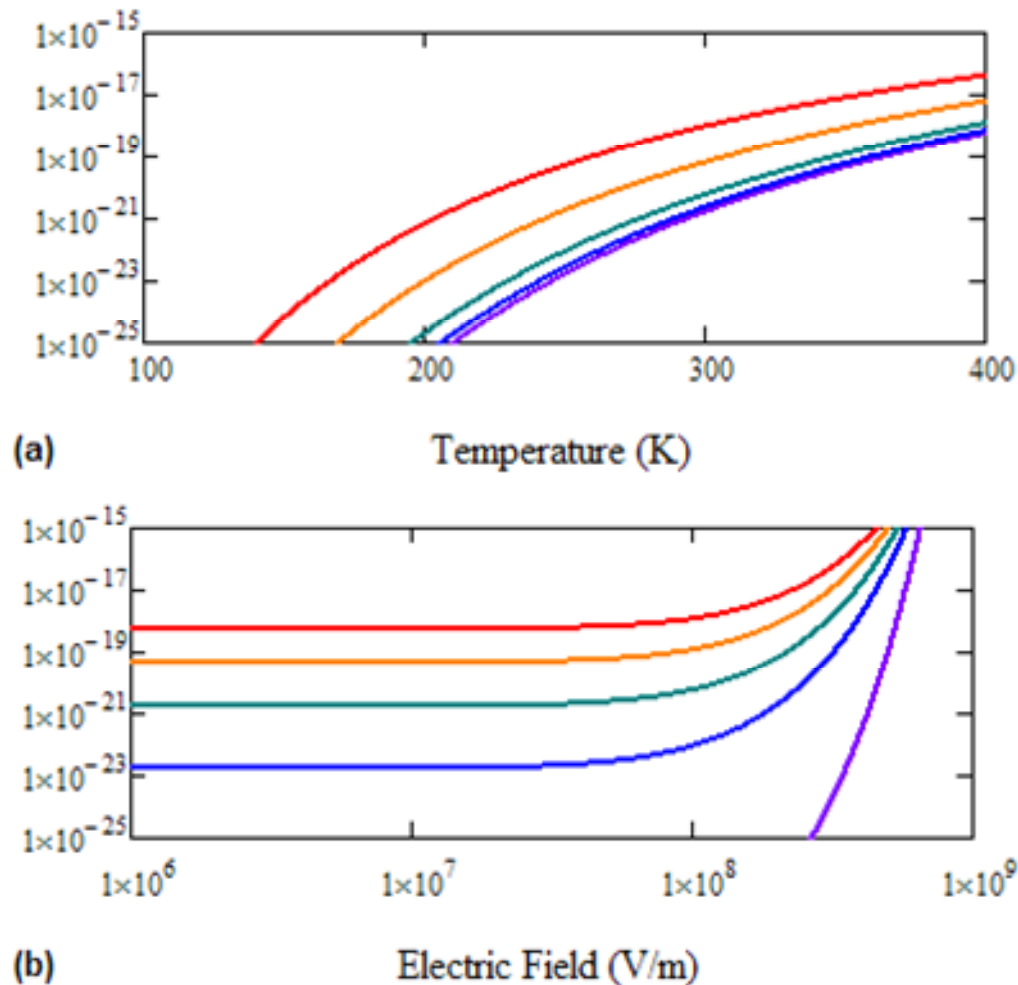
$$\beta_A \equiv 4F T_A / 3 F_A T = q_e F a / k_B T \quad \text{with} \quad Z_A(\beta_A) \equiv \frac{1}{\beta_A} \sinh(\beta_A)$$

Reduced fitting parameters

$$\sigma_{TAHo}(T) \equiv 2 N(T) v_{TAH} q_e^2 a^2, \quad T_A \equiv \Delta H / k_B \quad \text{and} \quad F_A \equiv 4\Delta H / 3 q_e a$$

TAH Dependence on E and T

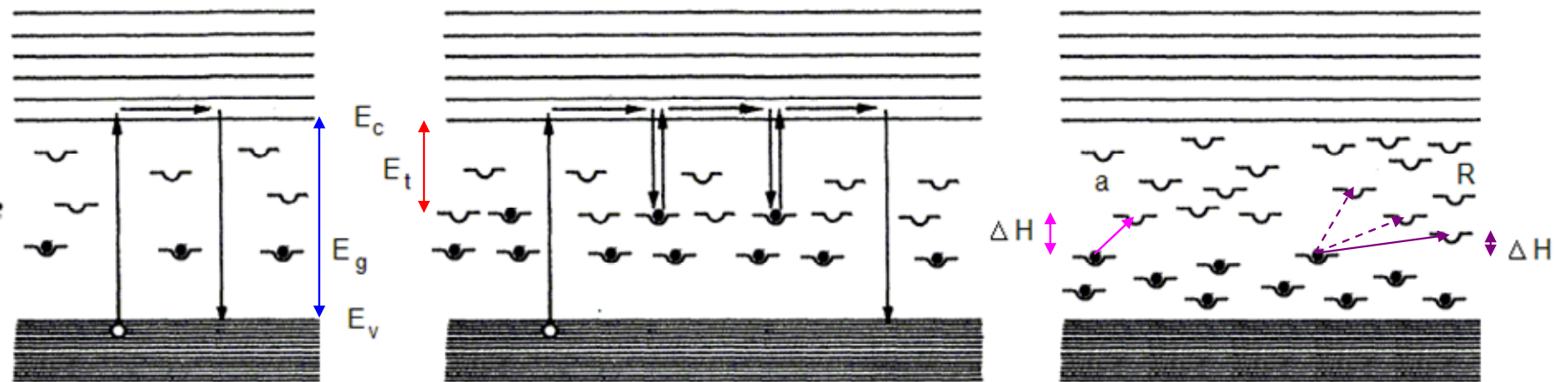
Thermally Activated Hopping
Conductivity



Temperature and electric field dependence of thermally activated hopping conductivity. (a) Temperature dependence with electric fields of $1 \cdot 10^7$ V/m (purple), $5 \cdot 10^7$ V/m (blue), $1 \cdot 10^8$ V/m (green), $2 \cdot 10^8$ V/m (orange) and $3 \cdot 10^8$ V/m (red). **(b)** Electric field dependence with temperatures of 150 K (purple), 250 K (blue), 300 K (green), 350 K (orange) and 400 K (red). Curves are based on Eq. (2). To approximately match LDPE data we have set $\sigma_{TAHo} = 1.4 \cdot 10^{-10}$ ($\Omega\text{-cm}$)-1 and $FA = 9.5 \cdot 10^8$ V/m for $TA = 6626$ K. $FESD$ is $\sim 3 \cdot 10^8$ V/m.

Conduction Models

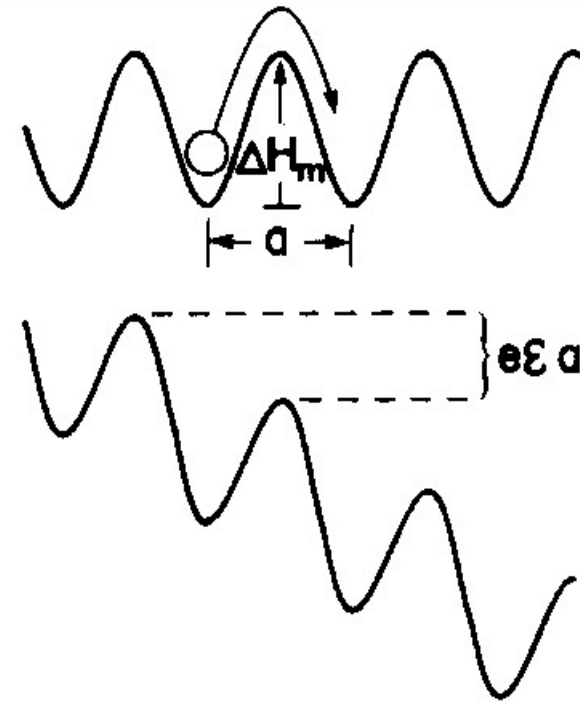
Model: T and E Dependence of DC Conductivity



TAH

Theory of Thermally Activated Hopping Conductivity

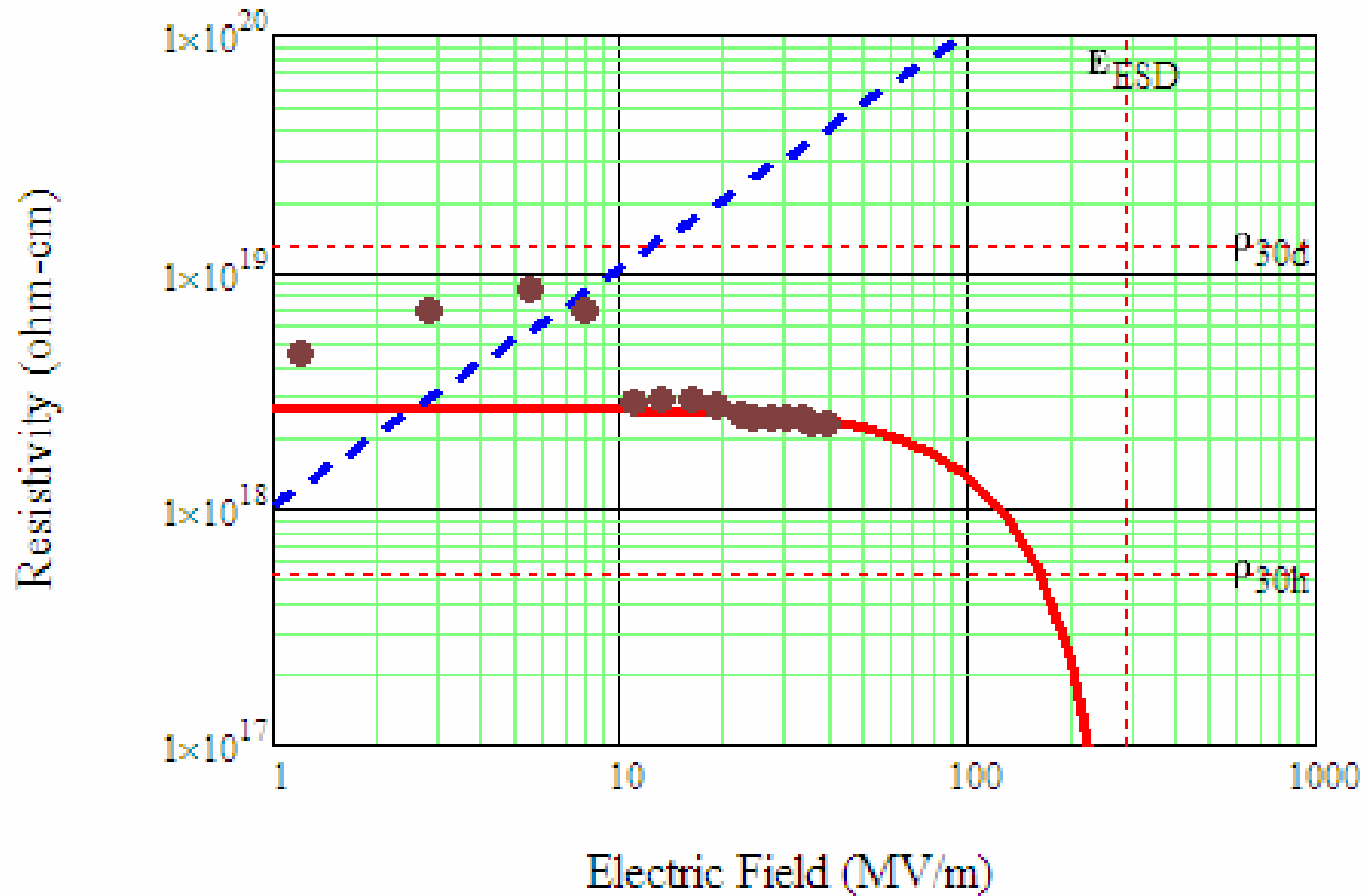
Theory of thermal assisted hopping conductivity provides a model for the temperature and electric field dependence of the conductivity of polymers:



$$\sigma_{TAH}(F, T) = \left[\frac{2N(T)v_{TAH} a q_e}{F} \right] \exp\left[\frac{-\Delta H}{k_B T} \right] \sinh\left[\frac{a q_e F}{k_B T} \right] = \left\{ \sigma_{TAHo}(T) \left(\frac{T_A}{T} \right) Z_A(\beta_A) \exp\left(-\frac{T_A}{T} \right) \right\}$$

$$\sigma_{TAHo}(T) \equiv 2 N(T) v_{TAH} q_e^2 a^2, \quad T_A \equiv \Delta H / k_B \quad \text{and} \quad F_A \equiv 4\Delta H / 3q_e a$$

E-field Dependence of TAH



Note divergence at E_{ESD}

Variable Range Hopping Conductivity

Variable range hopping model of Mott and Davis (as extended by Huges and Apsley for E-field dependence), allows hopping at a range of distances over a distribution of trap energy states:

Theory leads to “ $T^{1/4}$ ” behavior

$$\sigma_{VRH}(F, T) = \left\{ \sigma_{VRHo}(T) \left(\frac{T_V}{T} \right)^{1/4} Z_{V1}(\beta_V) \exp \left[\left(-\frac{T_V}{T} \right)^{1/4} Z_{V2}(\beta_V) \right] \right\}$$

$$\beta_V \equiv 4FT_V / 3F_V T = q_e F (2\alpha)^{-1} / k_B T$$

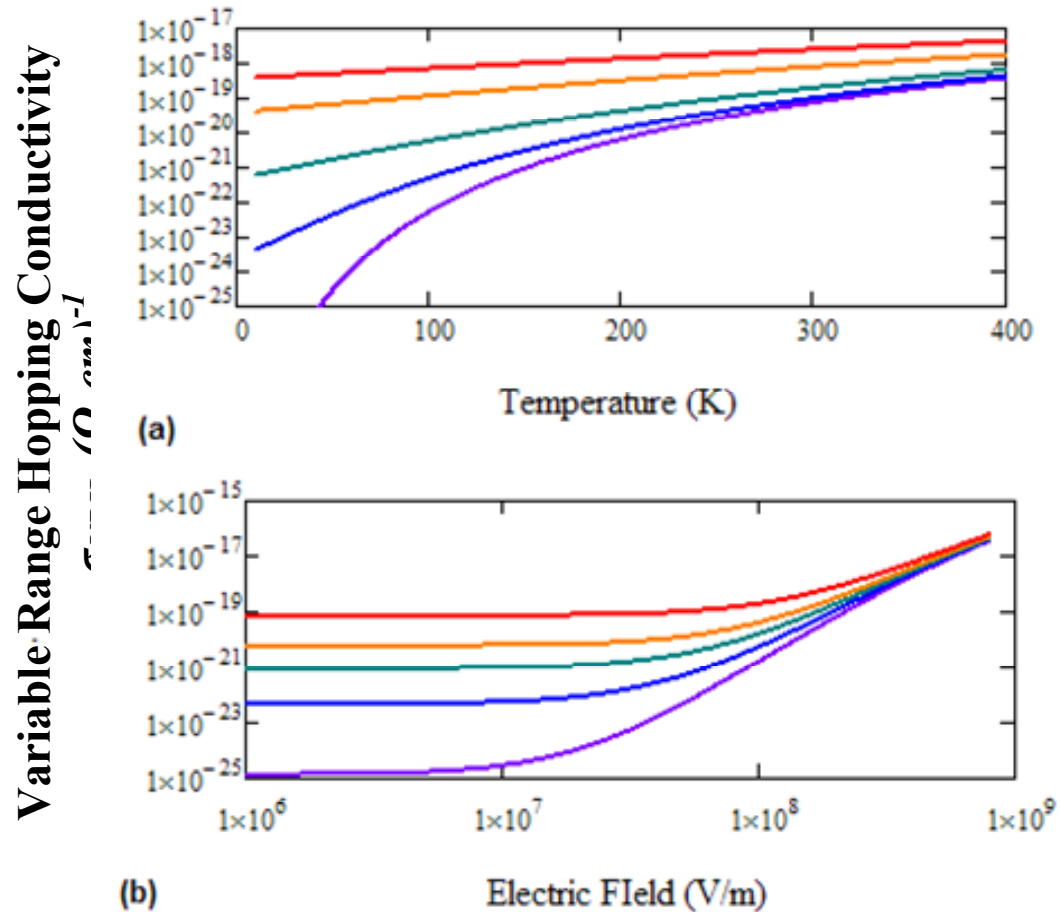
$$Z_{V1}(\beta_V) \equiv [2/Z_{Vo}(\beta_V)]^{1/4} \quad \text{and} \quad Z_{V2}(\beta_V) \equiv \left(\frac{-1}{2\beta_V} \right) \cdot \left[1 + \frac{Z_{Vo}(\beta_V)}{Z_{Vo}(\beta_V) - \frac{3}{2}\beta_V} \right] \cdot Z_{V1}(\beta) \cdot \left[\frac{\frac{3 + \beta_V}{24 \cdot (1 + \beta_V)^3} - \frac{1}{8} - \frac{\beta_V}{3}}{\frac{2 + \beta_V}{6 \cdot (1 + \beta_V)^2} + \frac{1}{3} + \frac{\beta_V}{2}} \right]$$

$$\text{with } Z_{Vo}(\beta_V) \equiv \frac{\left(1 + \frac{\beta_V}{2} \right)}{(1 + \beta_V)^2} + \left(1 + \frac{3}{2}\beta_V \right)$$

Reduced fitting parameters

$$\text{with } \sigma_{VRHo}(T) = 2 N_{E_F} v_{VRH} q_e^2 / (2\alpha)^2, \quad T_V \equiv 3(2\alpha)^3 / N_{E_F} \pi k_B \quad \text{and} \quad F_V \equiv 4(2\alpha)^4 / N_{E_F} \pi q_e$$

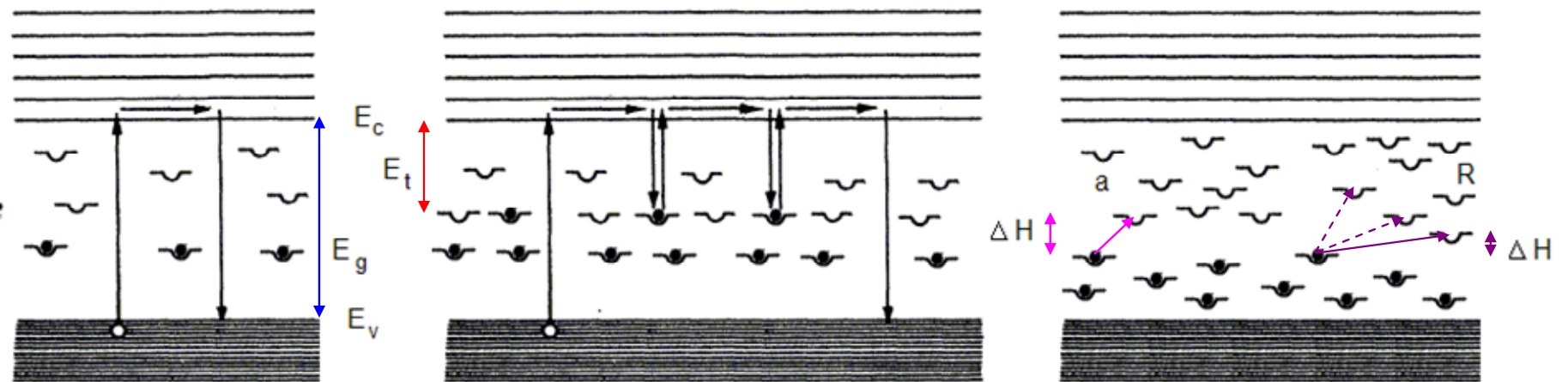
VRH Dependence on E and T



Temperature and electric field dependence of variable range hopping conductivity. (a) Temperature dependence with electric fields of $1 \cdot 10^7$ V/m (purple), $5 \cdot 10^7$ V/m (blue), $1 \cdot 10^8$ V/m (green), $2 \cdot 10^8$ V/m (orange) and $3 \cdot 10^8$ V/m (red). (b) Electric field dependence with temperatures of 50 K (purple), 100 K (blue), 150 K (green), 200 K (orange) and 300 K (red). Curves are based on Eq. (4). To approximately match LDPE data we have set $\sigma_{VRHo} = 1.0 \cdot 10^{-10}$ $(\Omega \text{ cm})^{-1}$ and $FV = 6.9 \cdot 10^{13}$ V/m for $TV = 1.0 \cdot 10^8$ K.

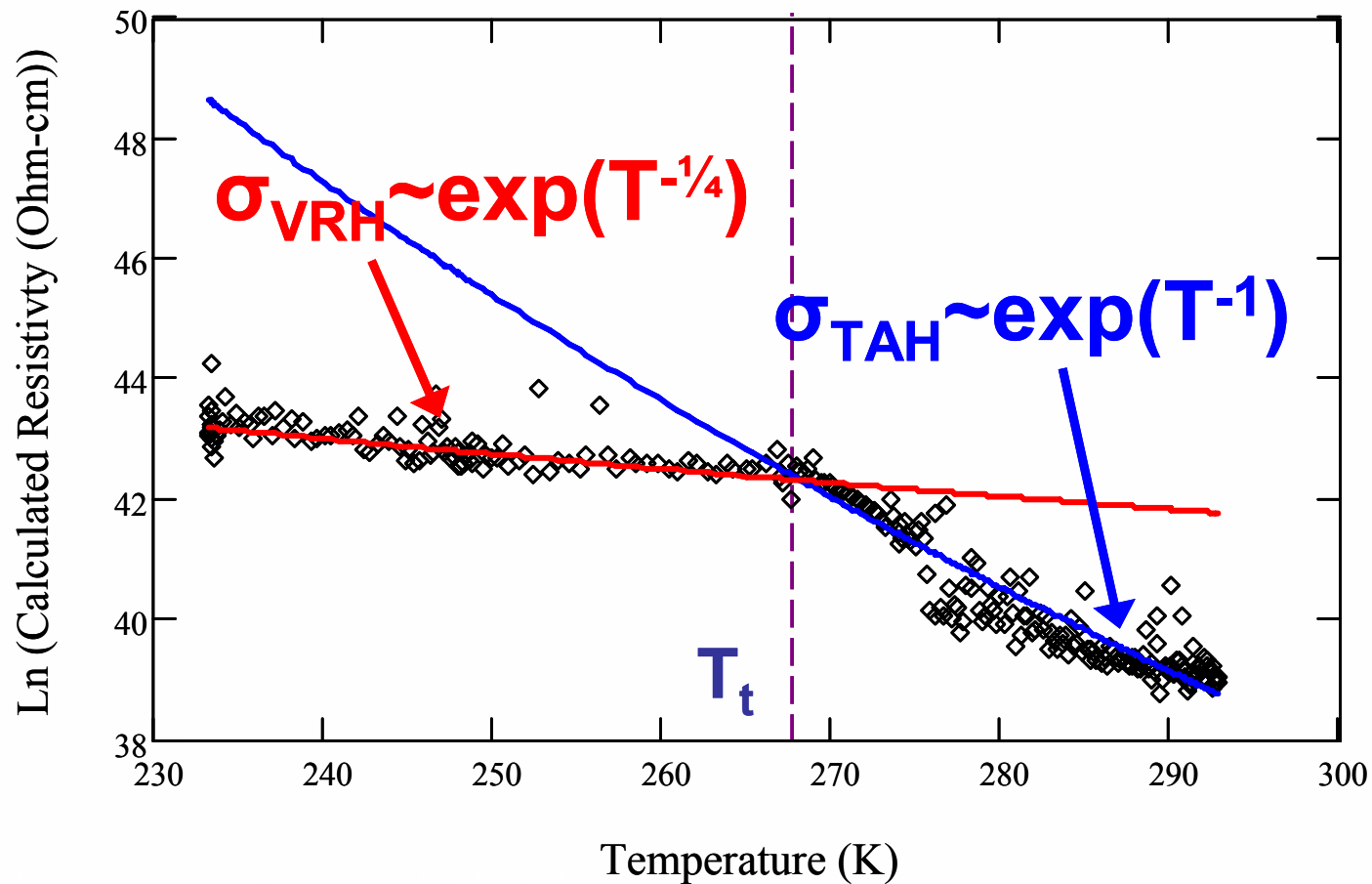
Conduction Models

Model: T and E Dependence of DC Conductivity



VRH

Temperature Dependence of TAH and VRH



Note change in slope for transition from TAH to VRH.

This occurs near a beta structural phase transition.

Fit for RIC

Basic theory for RIC follows from the Rose, Fowler, Vaisenberg for radiation assisted thermal hopping from a distribution of multiple trap sites

The key power law relation has T dependant coefficients k_{RIC} and Δ

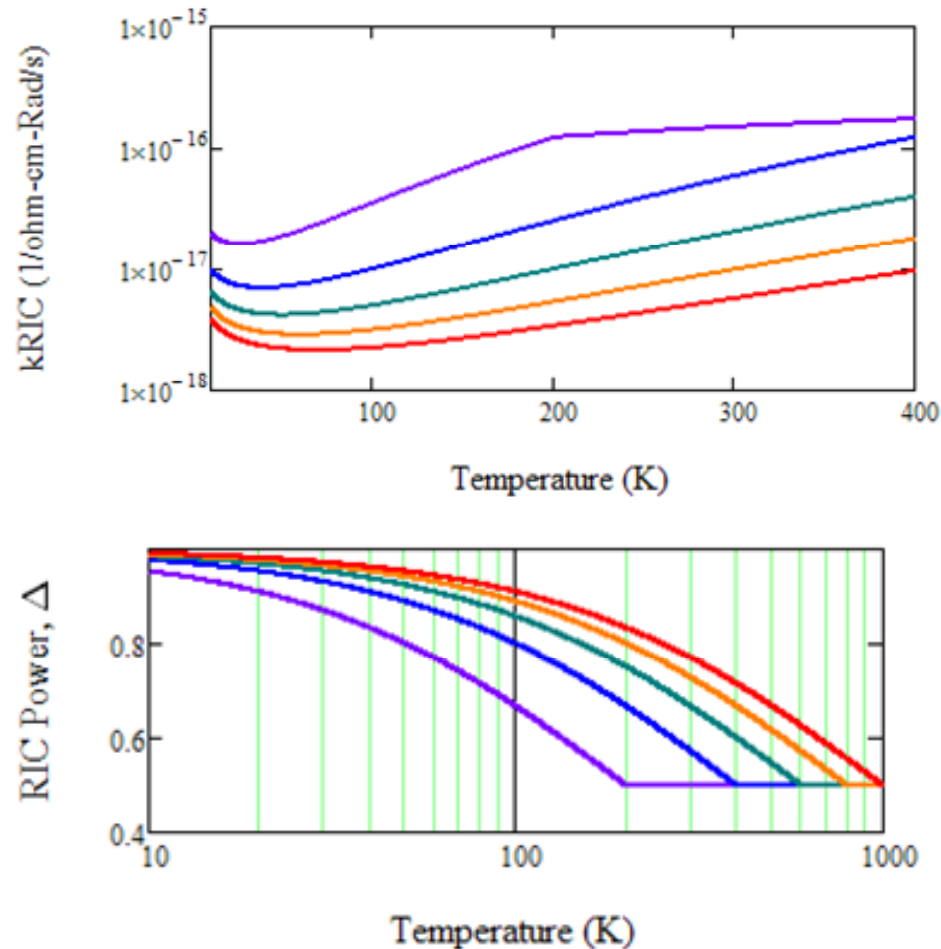
$$\sigma_{RIC}(\dot{D}) = k_{RIC}(T) \dot{D}^{\Delta(T)}$$

$$\Delta(T) = [1 + T/T_{RIC}]^{-1}$$

$$k_{RIC}(T) = q_e \mu_o \left[\left(\frac{\rho_m}{s \Sigma n_o T_{RIC}} \right) \left(\frac{m_e^*}{3k_B T} \right)^{1/2} \right]^{\Delta(T)} \left[2 \left(\frac{\sqrt{m_e^* m_h^*} k_B T}{2\pi \hbar^2} \right)^{3/2} \right]^{1-\Delta(T)} = k_{RICo} \cdot k_{RIC1}^{\Delta(T/T_{RIC})} [T/T_{RIC}]^{3/2-2\Delta(T/T_{RIC})}$$

$$\text{with } k_{RICo} \equiv \left[\frac{q_e \mu_o}{\pi \sqrt{2\pi} \hbar^3} (m_e^* m_h^*)^{3/4} (k_B T_{RIC})^{3/2} \right] \text{ and } k_{RIC1} \equiv \left[\left(\frac{\pi \sqrt{2\pi} \rho_m k_B \hbar^3}{\sqrt{3} s \Sigma n_o} \right) \left(\frac{\sqrt{m_e^*}}{(m_e^* m_h^*)^{3/4}} \right) (k_B T_{RIC})^{-3} \right]$$

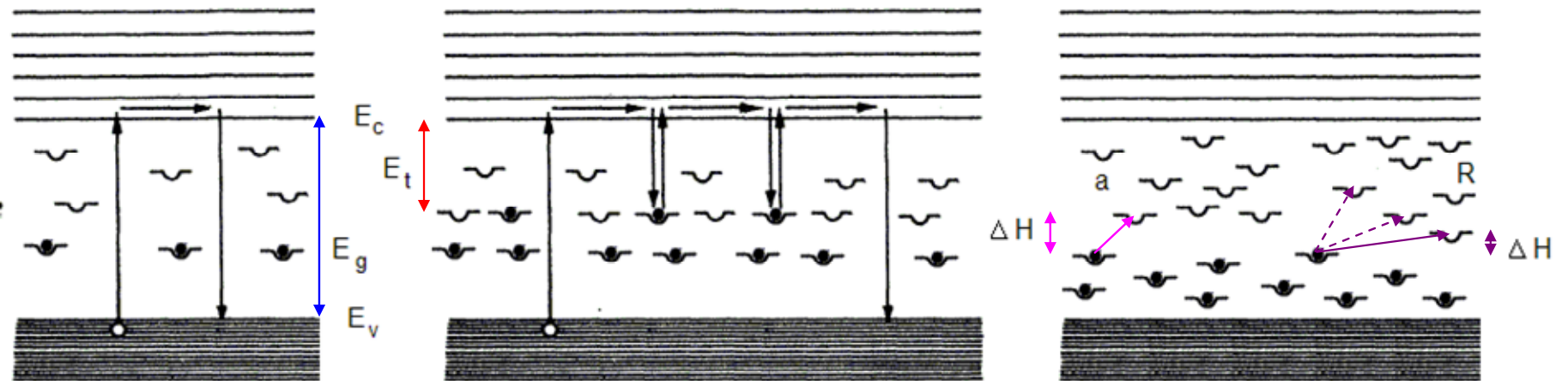
RIC Dependence on D and T



Temperature dependence of the RIC parameters. (a) Proportionality constant, $kRIC$, based on Eq. (8). (b) RIC power, Δ , based on Eq. (7). Values shown are for TRIC set to 200 K (purple), 400 K (blue), 600 K (green), 800 K (orange) and 1000 K (red). To approximately match LDPE data we have set $kRIC_0 = 1.8 \cdot 10^{-14}$ ($\Omega\text{-cm-Rad/sec}$)-1 and $kRIC_1 = 4.6 \cdot 10^{-5}$ for TRIC=600 K.

Conduction Models

Model: T and E Dependence of DC Conductivity

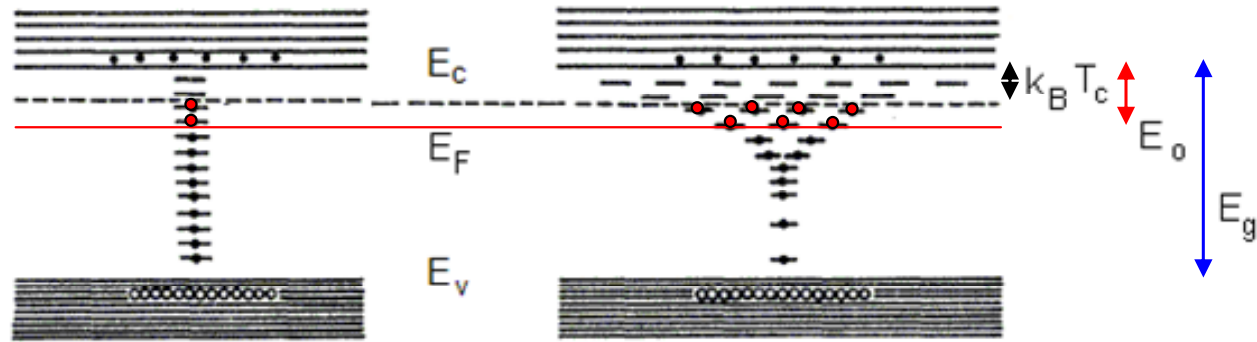


RIC

What IS Radiation Induced Conductivity (RIC)

Theoretical Model: T and D Dependence of RIC

- conduction electrons
- holes
- empty traps
- filled traps
- radiation filled traps



Uniform Trap Density

$$\Delta(T) \rightarrow 1$$

$$k(T) \rightarrow k_{RIC0}$$

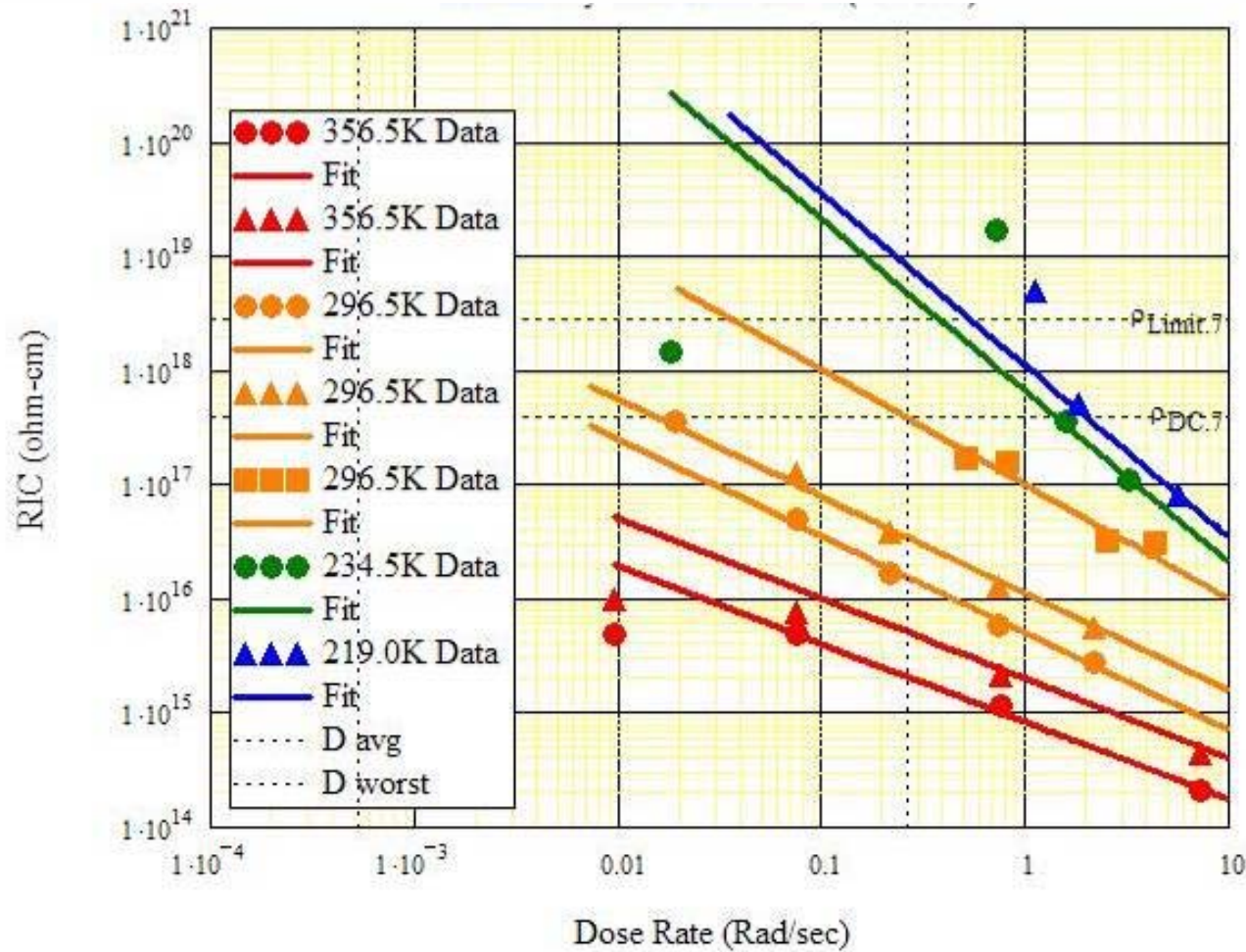
Exponential Trap Density

$$\Delta(T) \rightarrow \frac{T_c}{T + T_c}$$

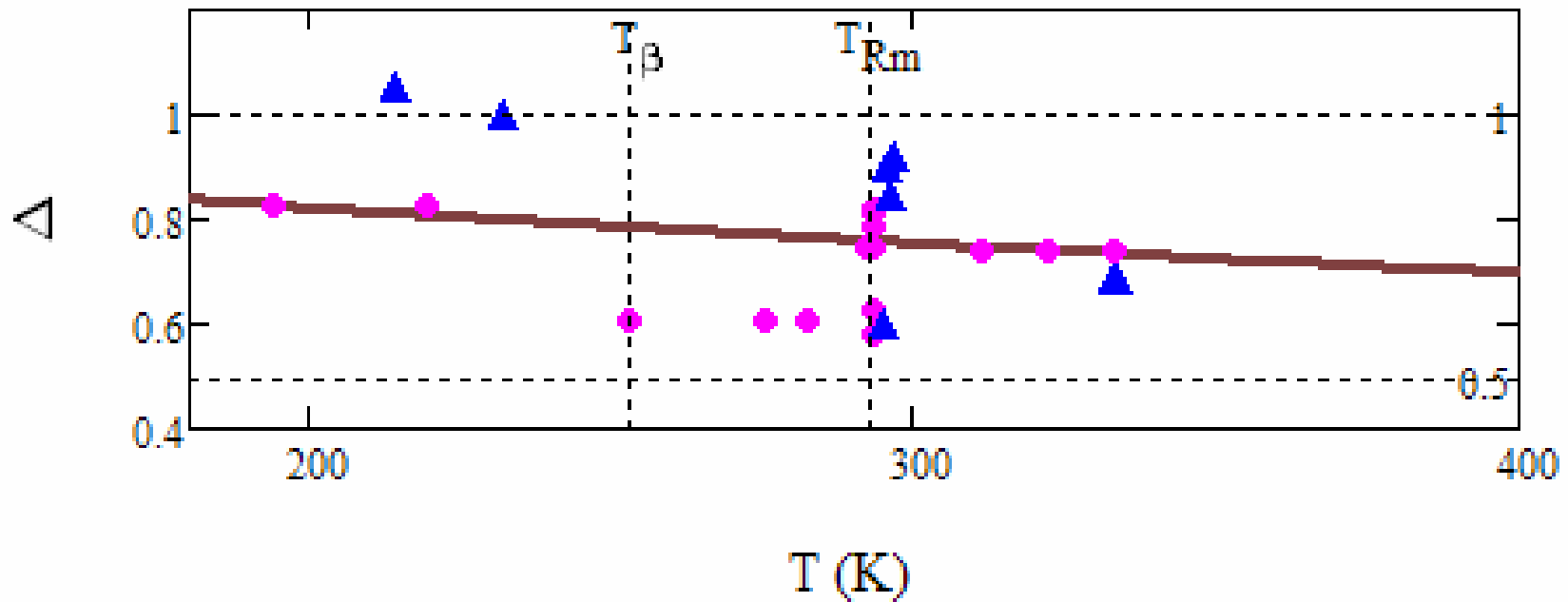
$$k(T) \rightarrow k_{RIC1} \left[2 \left(\frac{m_e k_B T}{2\pi \hbar^2} \right)^{3/2} \left(\frac{m_e^* m_h^*}{m_e m_e} \right)^{3/4} \right] \frac{T}{T + T_c}$$

$$\sigma_{RIC}(T, D) = k_{RIC}(T) \cdot D^{\Delta(T)}$$

Comparison of RIC at Various T

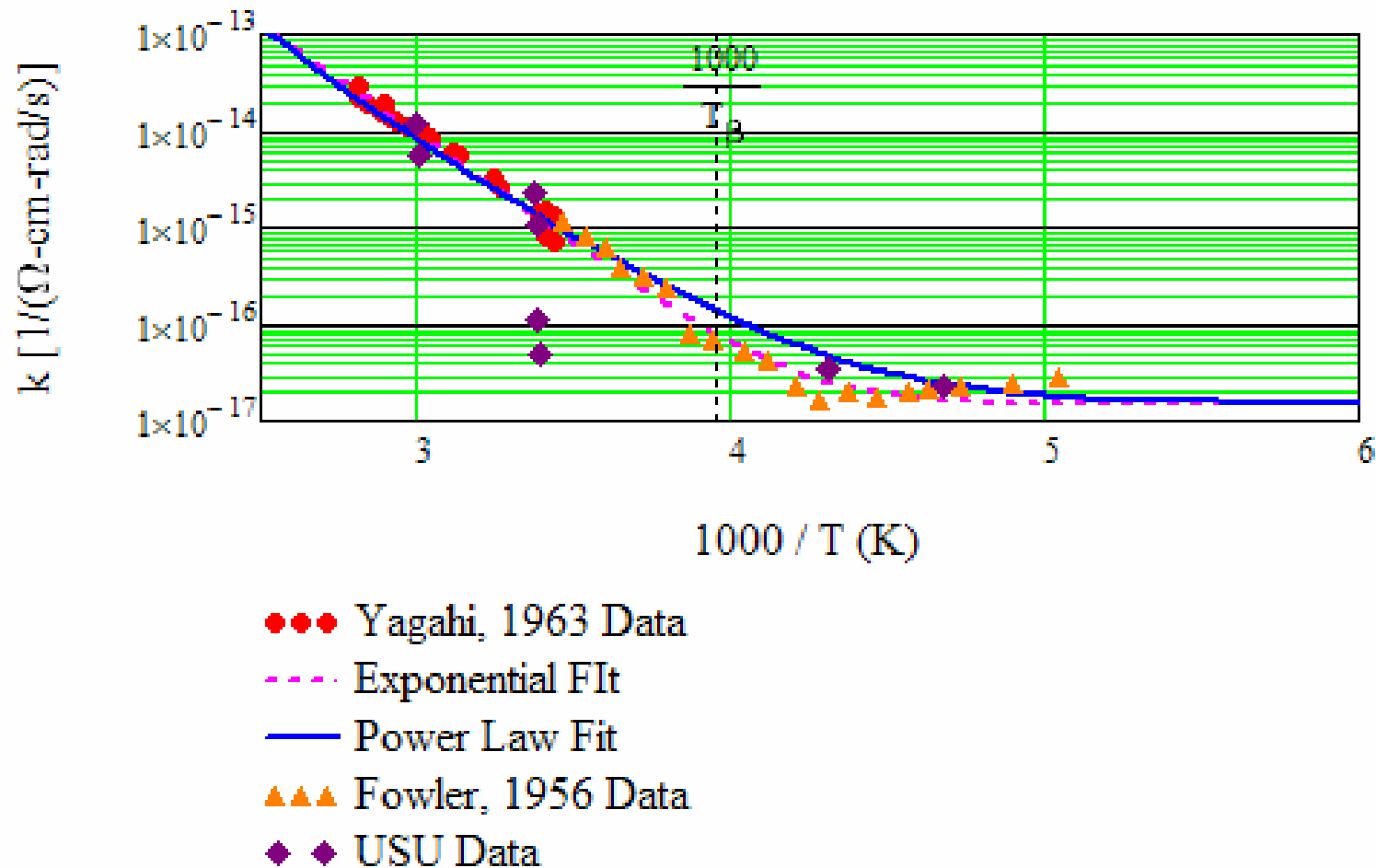


Comparison of RIC at Various T

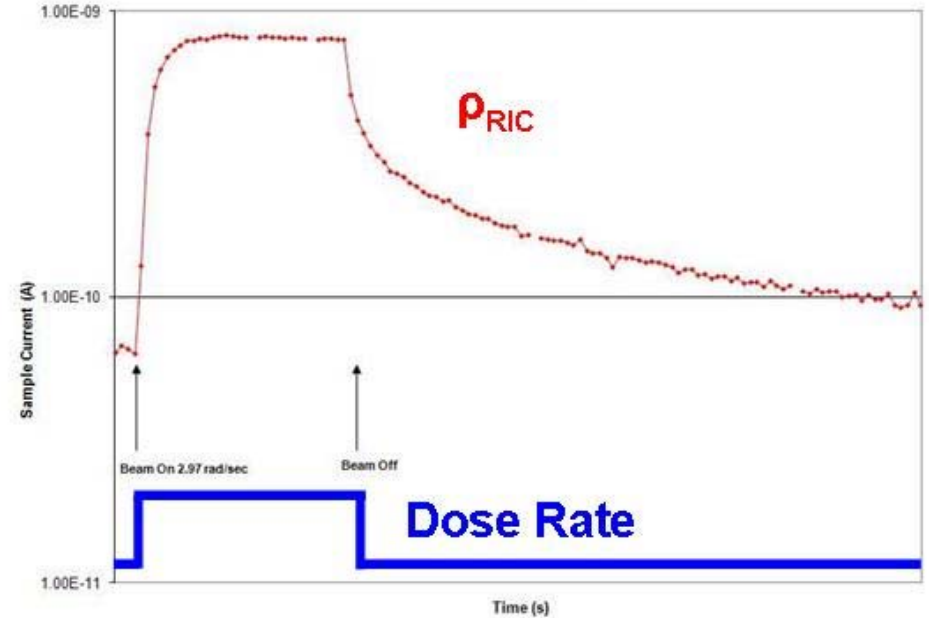
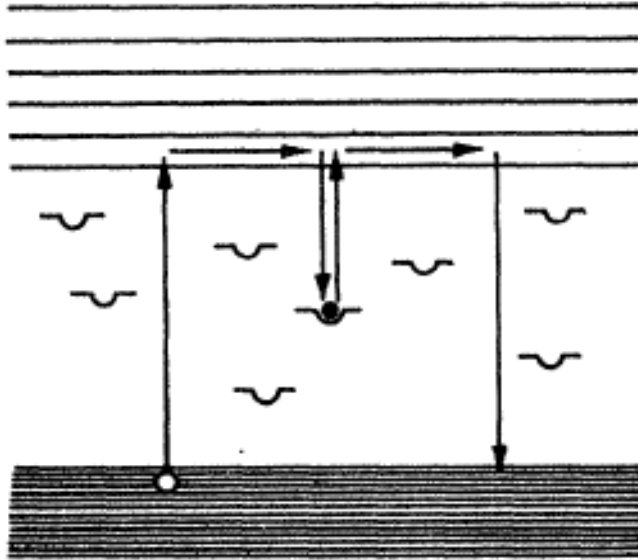


- Fit to Delta at RT
- Other Data Sets
- ▲▲ USU Data

Comparison of RIC at Various T



Time Behavior of RIC



Dose Dependant RIC

$$\sigma_{RIC}(\dot{D}) = k_{RIC} \cdot \dot{D}^{\Delta}$$

Persistent RIC

$$\sigma_{RIC}(t) = \sigma_{RIC_0} (1 + t/\tau_{trap})^{-1}$$

In real time, when the radiation is turned on, a finite period is required for the measured conductivity to approach the radiation induced conductivity.

Similarly, when the radiation is turned off, the measured conductivity also takes a finite amount of time to decay down to the material's initial conductivity.

Electrostatic Breakdown Theory

Based on the thermodynamic model for ESD

From an expression for bond disruption, from an expression for charge mobility similar to the TAH model, we get

$$1 = \left(\frac{k_B T}{h/t_{en}} \right) \exp \left[\frac{-\Delta G}{k_B T} \right] \sinh \left[\frac{q_e F_{ESD} \lambda}{k_B T} \right] = \left(\frac{k_B T}{h/t_{en}} \right) \left(\frac{\frac{3}{4} F_{ESD}}{F_{A'}} \right) \left[\frac{T_{A'}}{T} Z_{A'}(\beta_{A'}) \exp \left[\frac{-T_{A'}}{T} \right] \right]$$

Reduced fitting parameters

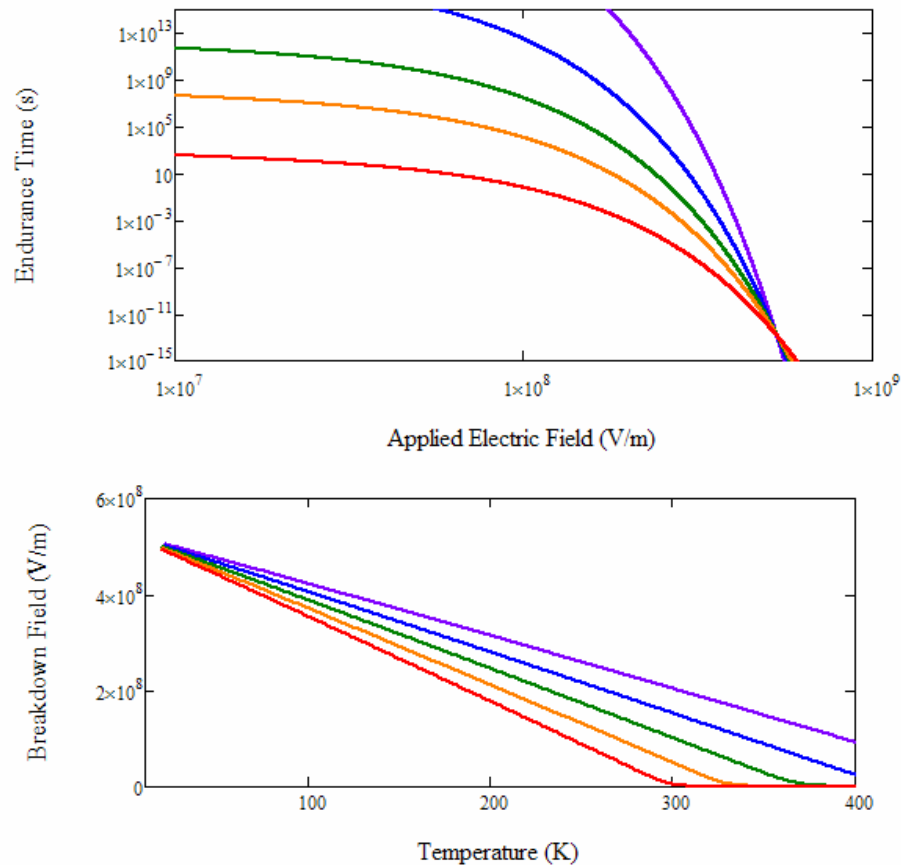
$$\text{with } \beta_{A'} \equiv 4F_{ESD} T_{A'} / 3 F_{A'} T = q_e F_{ESD} \lambda / k_B T$$

$$T_{A'} \equiv \Delta G / k_B \quad \text{and} \quad F_{A'} \equiv \Delta G / \frac{3}{4} q_e \lambda \rightarrow \frac{3}{4} F_{ESD}$$

Finally, an expression for breakdown field strength in terms of endurance time and the fitting parameters:

$$F_{ESD} = \left[\frac{k_B T}{q_e \left(\frac{3}{4} \lambda \right)} \right] \operatorname{csc} h^{-1} \left[\left(\frac{h/t_{en}}{k_B T} \right) \exp \left(\frac{-\Delta G}{k_B T} \right) \right] = \left(\frac{3}{4} F_{A'} \frac{T}{T_{A'}} \right) \operatorname{csc} h^{-1} \left[\left(\frac{h/t_{en}}{k_B T} \right) \exp \left(\frac{-T_{A'}}{T} \right) \right]$$

ESD Dependence on Endurance Time



Temperature dependence of the electrostatic field breakdown strength. (a) *Endurance, or time to breakdown, a function of applied electric field, based on Eq. (9). Curves shown are for temperature set to 150 K (purple), 200 K (blue), 250 K (green), 300 K (orange) and 400 K (red).* (b) *Breakdown field strength as a function of temperature, based on Eq. (10). Curves shown are endurance times set to 100 s (purple), 102 s (blue), 104 s or 2.8 hr (green), 106 s or 11.6 days (orange) and 108 s or 3.2 yr (red). To approximately match LDPE data, we have set $FESD=9.5 \cdot 10^8$ V/m and $\Delta G'=1.22$ eV.*

Representative Fitting Parameters for LDPE

*Based on the best overall fits to the full data set,
Using the equations above, we estimate the
fitting parameters to be:*

$$\sigma_{TAHo} = 8.0 \cdot 10^{-8} (\Omega\text{-cm})^{-1}$$

$$E_A = 9.5 \cdot 10^8 \text{ V/m}$$

$$T_A = 8.9 \cdot 10^3 \text{ K}$$

$$k_{RICo} = 1.8 \cdot 10^{-14} (\Omega\text{-cm-Rad/sec})^{-1}$$

$$k_{RIC1} = 4.6 \cdot 10^{-5}$$

$$T_{RIC} = 600 \text{ K}$$

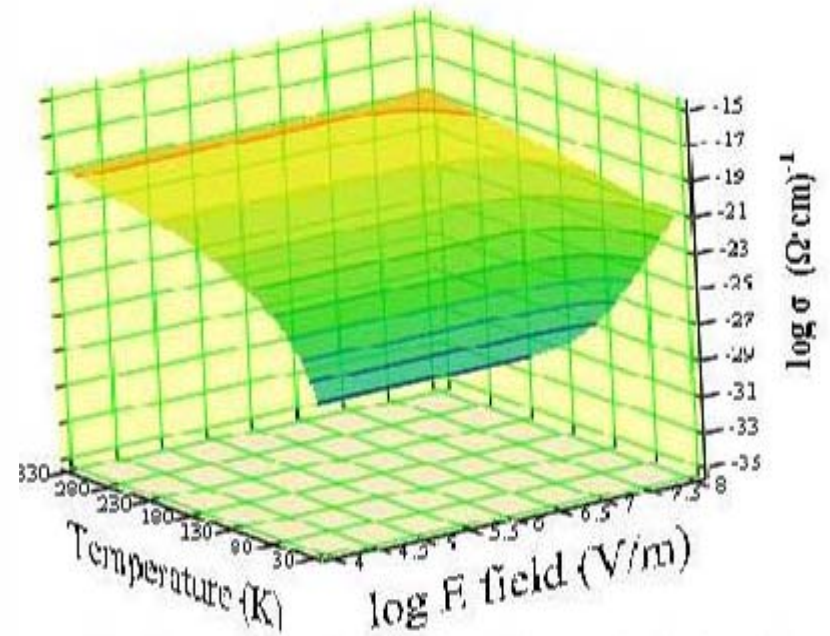
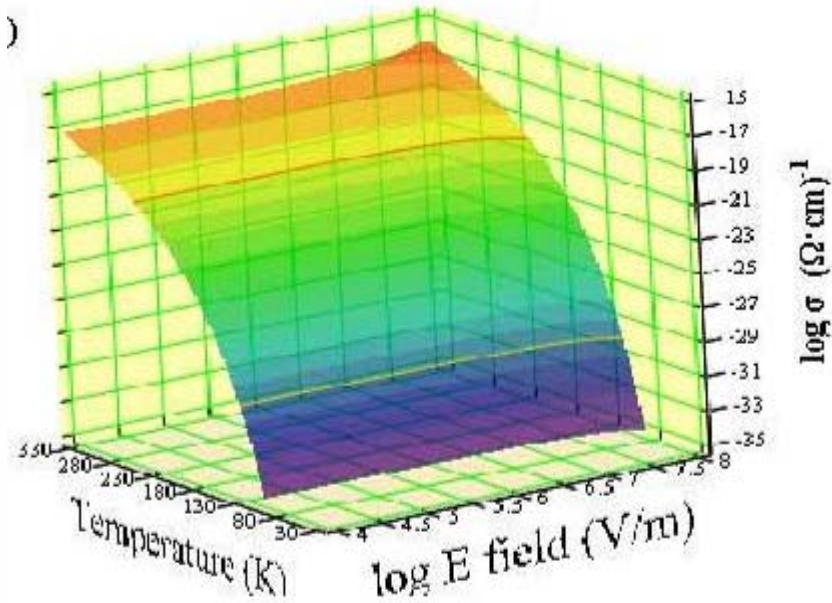
$$\sigma_{VRHo} = 1.0 \cdot 10^{-10} (\Omega\text{-cm})^{-1}$$

$$E_V = 6.9 \cdot 10^{13} \text{ V/m}$$

$$T_V = 1.0 \cdot 10^8 \text{ K}$$

$$\Delta G, \text{ of } 1.2 \text{ eV}$$

Individual Conductivity Components

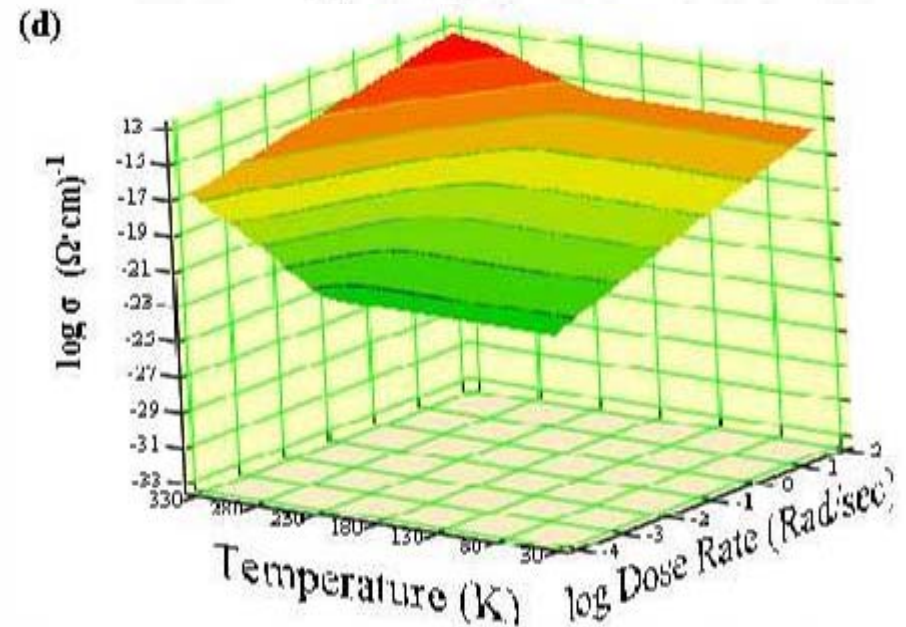


LDPE Data

TAH

VRH

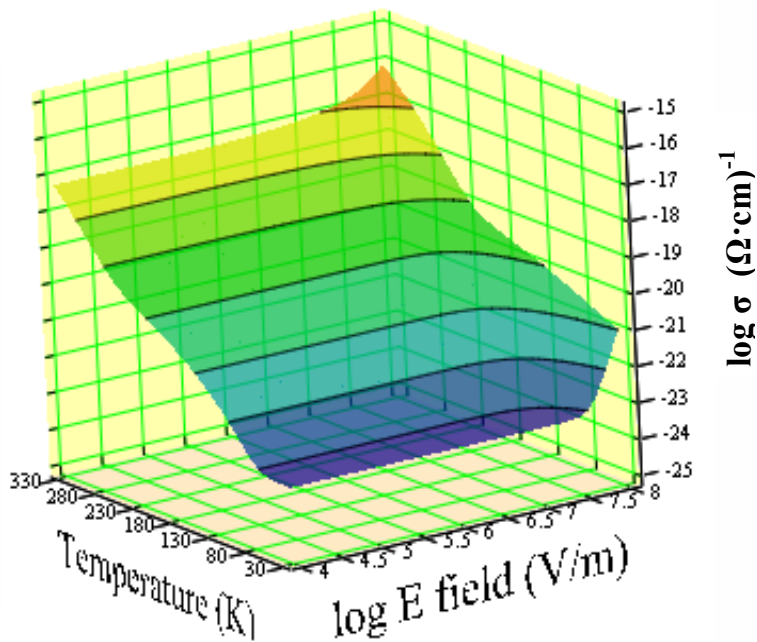
RIC



Constant Voltage Resistivity Fits--LDPE

(a)

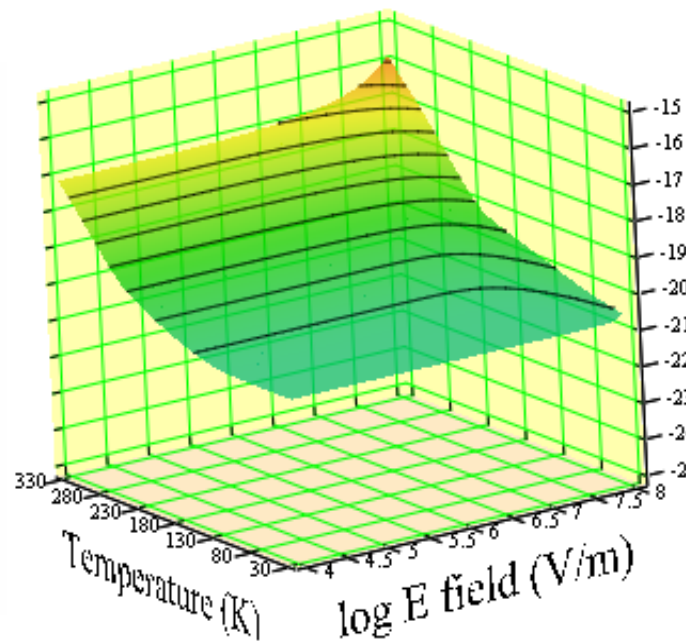
Low dose rate



(b)

Average L2 Dose Rate

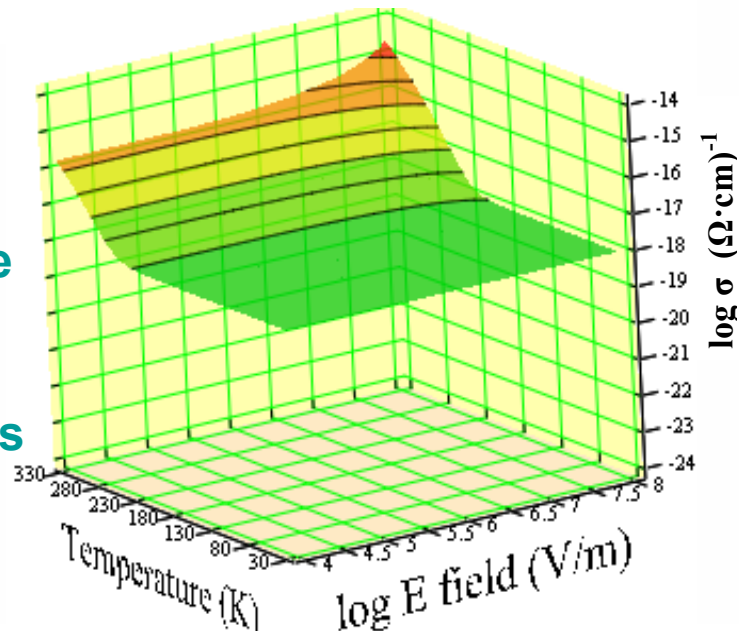
5 mRad/s



(c)

Worst Case L2 Dose Rate

0.2 Rad/s



(d)

High Dose Rate

10 Rad/s

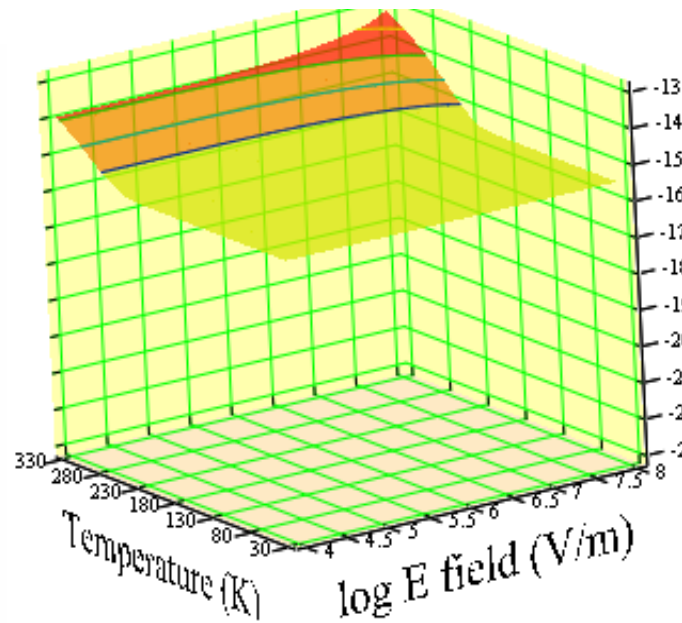


Figure . Total conductivity as a function of temperature and E-field for various absorbed dose rates. E-field and conductivity are logarithmic. (a) Low absorbed dose rate of 10^{-6} Rad \cdot sec⁻¹. (b) Approximate average L2 absorbed dose rate of $5.4 \cdot 10^{-4}$ Rad \cdot sec⁻¹. (c) Approximate worst case (storm) L2 absorbed dose rate of $2.7 \cdot 10^{-1}$ Rad \cdot sec⁻¹. (d) High absorbed dose rate of 10^{+2} Rad \cdot sec⁻¹.

Summary

- **Extensive Resistivity measurements made.**
- **Physics-based parameterized models determined from literature.**
- **New Engineering tool developed.**
 - **Tool capabilities are being updated.**
 - **Hopefully more materials will be added.**
 - **Looking for mechanism to distribute information.**