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2 jets

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31

32 *Abstract*

33 Cleaning by a horizontal water jet, impinging onto a soiled Perspex vertical plate, is  
34 described. The plate, the *substrate*, was coated with PVA or petroleum jelly, the *soil*. The  
35 substrate was either

36 (i) fixed, for batch tests in which the cleaned area, roughly circular, grew with time,  
37 or

38 (ii) the substrate moved vertically up or down in its own plane, the water jet  
39 remaining fixed; this reproduced the effect of a jet moving across a surface for  
40 cleaning, **as found in real tank cleaning operations.**

41 In the batch experiments, growth of the radius  $a$  of the cleaning area is well described, at  
42 early times  $t$ , by  $a^5 - a_0^5 = K^5 (t - t_0)$ ,  $a_0$  being the initial radius of the cleaned area at time  $t_0$ ;  
43  $K$  is a constant. At later times **with petroleum jelly**, the cleaning front reached a maximum  
44 value, when the outward momentum of the radially flowing water film balanced the strength  
45 of **the soil. This maximum value is modelled as a ramp of viscoplastic soil inclined at angle  $\chi$**   
46 **to the substrate surface, where  $\chi$  was found to vary from  $7^\circ$  to  $25^\circ$ .**

47 In the tests of continuous cleaning **of petroleum jelly**, a lengthening cleaned area, of width  $w_c$ ,  
48 was observed on the moving substrate. Near the jet was a stationary clean front, whose shape  
49 looked like half an ellipse. This shape, and the width  $w_c$ , are well described by theory  
50 (Wilson *et al Chem. Eng. Sci.* 2015, **123**, 450–459) using parameters from the above-  
51 mentioned batch experiments. This establishes a good link between batch and continuous  
52 cleaning experiments.

53

54 *Keywords* Cleaning, fluid mechanics, impinging jet, PVA, petroleum jelly, viscoplastic

55

56

57 **Introduction**

58 Cleaning is an important step in any food manufacturing process, whether to clear away  
59 residual material from process equipment at product changeover or to remove fouling  
60 deposits which can affect process operability, product quality or hygienic operation (Fryer  
61 and Asteriadou, 2009). Automated plant makes increasing use of cleaning-in-place (CIP)  
62 operations, wherein material is removed by the action of recirculating rinse washes, cleaning  
63 solutions and disinfectants. Time spent cleaning represents a loss of production, affecting the  
64 financial sustainability of a plant. Cleaning affects the environmental sustainability in terms  
65 of energy consumption (cleaning solutions are frequently heated) and material (provision of  
66 cleaning chemicals and disposal of wastes, as well as neutralisation of acid and alkaline  
67 agents) (Köhler *et al.*, 2015). There is thus a need to optimise the performance of cleaning  
68 operations.

69

70 Much of the research into CIP mechanisms to date has concentrated on enclosed units, *e.g.*  
71 pipes, heat exchangers, where the flow of cleaning solutions is well understood. The food  
72 industry makes extensive use of tanks and similar vessels for storage, mixing, reaction and  
73 heating, for which ‘fill and soak’ cleaning operations take long times and require large  
74 volumes of liquid. Some systems use moving<sup>1</sup> jets of liquid, created by nozzles or lances, to  
75 distribute cleaning solution across the walls of process vessels at higher velocities than in  
76 standard pipe flows so that cleaning is augmented by hydraulic action (Jenssen, 2011). These  
77 can significantly reduce the time to clean a vessel.

78 There has, however, been relatively little work to date on cleaning of surface layers – which  
79 we refer to here as soiling layers – by impinging liquid jets. Meng *et al.* (1998) and Leu *et al.*  
80 (1998) studied the mechanisms of removing surface coatings by high velocity waterjets  
81 (which formed sprays). Burfoot and co-workers (Burfoot and Middleton, 2009; Burfoot *et al.*,  
82 2009) quantified the effectiveness high pressure jets in food cleaning applications. Yeckel  
83 and Middleman (1987) studied and modelled the removal of viscous (oil) films from  
84 horizontal surfaces by a vertical impinging water jet in the region bounded by the hydraulic  
85 jump; in this region the liquid flows outwards in a thin film and subjects the layer to  
86 significant shear forces. Lately, Walker and co-workers (Hsu *et al.*, 2011; Walker *et al.*,

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<sup>1</sup> The terms ‘moving’ and ‘fixed’ in this paper refer to the relative motion of the nozzle. The liquid is in steady continuous flow.

87 2012) have extended this approach and considered the interaction of such jets on layers of  
88 non-Newtonian fluids.

89

90 The knowledge of cleaning mechanisms gained from the above studies is expected to apply to  
91 cases where the soiling material is attached uniformly to a wall, but the flow behaviour of the  
92 liquid changes noticeably as it moves over a vertical (or inclined) wall. When a liquid jet hits  
93 a flat surface, it spreads out radially as a thin, fast moving film (termed the *radial flow zone*,  
94 RFZ) until a point where the thickness of the jet increases abruptly. When the liquid impinges  
95 downwards on a horizontal plate, this change in thickness is called a *hydraulic jump* and the  
96 flow pattern is symmetric. When a jet strikes a vertical wall a similar feature is formed above  
97 the point of impingement, which we call the *film jump*. Beyond the film jump the liquid flows  
98 downwards, moving around the film jump as a *rope* which increases in thickness. These  
99 features are shown in Figure 1(a). Below the point of impingement the liquid flows  
100 downwards as a wide film, bounded by a rope on each side. The film can stay wide or narrow  
101 further downstream, depending on the wetting characteristics of the surface (Aouad *et al.*,  
102 2015). These flow patterns and quantitative models for predicting their dimensions and  
103 behaviour have been studied for jets impinging on stationary walls by Wilson and co-workers  
104 (Wilson *et al.*, 2012; Wang *et al.* 2013a; 2013b; 2015).

105

106 Fouling layers and residues in the food sector are often complex soft solids (Fryer and  
107 Asteriadou, 2009). Knowledge of cleaning mechanisms has been driven by the need to  
108 understand and optimise CIP systems, particularly duct flows (*e.g.* Gillham *et al.*, 1999; Fryer  
109 *et al.* 2006). The removal of soil layers by impinging jets can involve *adhesive* and/or  
110 *cohesive* mechanisms. In the former, the forces imposed by the liquid are sufficient to  
111 overcome the strength of attachment of the layer to the substrate and the layer is peeled off: it  
112 may fragment as part of this process, depending on its strength (*i.e.* the interactions between  
113 elements of the soil). With cohesive removal, the forces imposed by the liquid are sufficient  
114 to fragment the soil, *i.e.* by erosion or delamination. The soil is worn away until the substrate  
115 is reached. Dissolution, enhanced by convective mass transfer, may also occur. Wilson *et al.*  
116 (2014) studied the adhesive removal of soils by fixed impinging jets, where a circular,  
117 cleaned region grows outwards from the point of impingement. They presented a quantitative  
118 model, using results from the hydrodynamic model of Wilson *et al.* (2012), which gave a

119 good description of data obtained for layers of polyvinyl acetate (PVA), Xanthan gum, and  
120 petroleum jelly. They subsequently extended this model (Wilson *et al.*, 2015) to describe the  
121 cleaning action of a liquid jet moving across a soiled plate and were able to predict the shape  
122 of the cleaned front and the trends observed for Xanthan gum layers reported by Köhler *et al.*  
123 (2015).

124

125 This ability to predict the liquid contacting pattern and the shape of the cleaned front (see  
126 Wilson *et al.*, 2015) is critical for detailed simulation of cleaning by impinging jets.  
127 Knowledge of the liquid contacting pattern allows the regions wetted by the cleaning solution  
128 to be identified, as well as the time that the layer is in contact with solution: soaking time and  
129 reaction with a cleaning agent are important factors in the removal of complex soils (Wilson,  
130 2005; Fryer and Asteriadou, 2009). Knowledge of the shape of the cleaned front allows the  
131 area cleaned by a moving jet to be calculated for different trajectories, so that these can be  
132 optimised.

133

134 This paper presents an extension of the above experimental and modelling studies in two  
135 aspects. The first is the use of a new experimental configuration which allows the shape of  
136 the cleaned front and the flow patterns to be determined in real time. In previous studies  
137 (Köhler *et al.*, 2015; Wilson *et al.*, 2015) the jet had to be interrupted in order to determine  
138 the shape of the cleaned front. In the current work, the jet is stationary but the soiled plate is  
139 moved upwards (or downwards) past the jet while being videoed.

140 Moving surfaces and stationary nozzles have been employed by workers such as Gradek *et*  
141 *al.* (2006) to study hydraulic jump behaviour but have not, to the authors' knowledge, been  
142 used to study cleaning, particularly for vertical surfaces. The second aspect is the study of  
143 more complex soils, specifically layers of non-crosslinked PVA and a petroleum jelly. The  
144 influence of layer thickness is here investigated for both materials. The adhesive removal  
145 model of Wilson *et al.* is adapted to describe the removal of the petroleum jelly, which is a  
146 viscoplastic material (Ali *et al.*, 2015).

147 **Models**

148 *Radial flow zone hydrodynamics*

149 In these experiments cleaning is observed within the radial flow zone, where the liquid flows  
150 as a thin fast moving film. Wilson *et al.* (2012) modelled the flow in the RFZ as a Nusselt  
151 film, with the average velocity,  $U$ , at radius  $r$  given by

152 
$$\frac{1}{U} - \frac{1}{U_o} = \frac{10\pi^2 \mu}{3\rho Q^2} [r^3 - r_o^3] \quad [1]$$

153 Here  $U_o$  is the velocity in the impinging jet of radius  $r_o$ ,  $Q$  is the jet volumetric flow rate,  $\rho$  is  
154 the liquid density and  $\mu$  its dynamic viscosity. The momentum in the liquid film per unit  
155 circumferential width,  $M$ , at radius  $r$  is

156 
$$M = \frac{3\rho Q U}{5\pi r} \quad [2]$$

157 They calculated the location of the film jump,  $R$ , from a force balance in which the outward  
158 flow of momentum was balanced by surface tension,  $\gamma$ , acting along the surface and at the  
159 liquid-substrate contact line (with contact angle  $\beta$ ). Assuming that  $U_o \gg U(R)$  and  $R \gg r_o$  gave

160 
$$R = 0.276 \left[ \frac{\rho^2 Q^3}{\mu\gamma(1 - \cos \beta)} \right]^{1/4} \quad [3]$$

161 This result is compared with the experimental data for jets impinging on moving substrates.

162

163 *Cleaning – static jets*

164 Wilson *et al.* (2014) presented a model to describe the adhesive (removal) of soil within the  
165 RFZ by a static jet. Material is removed to leave a circular clean region of radius  $a$ , as shown  
166 in Figure 1(b). The rate of growth of the cleaned region is postulated to be proportional to the  
167 force imposed by the fluid, which is a fraction of the momentum per unit width,  $M$ , at  $a$ :

168 
$$\frac{da}{dt} = k'M \quad [4]$$

169 where  $t$  is time and  $k'$  is a cleaning rate constant, expected to be related to the soil thickness,  
 170  $\delta$ . The influence of initial soil layer thickness on cleaning rate is investigated for layers of  
 171 PVA and petroleum jelly here.

172 The momentum flux per unit width,  $M$ , is estimated using Equations [1] and [2], assuming  
 173 that  $1/U_o$  is small, replacing  $r$  by  $a$  in Equation [1] and assuming  $a \gg r_o$ ; this gives

$$174 \quad \frac{da}{dt} = \frac{3k'm^3}{\pi c} \frac{1}{5a^4} = K^5 \frac{1}{5a^4} \quad [5]$$

175 Here,  $m$  is the mass flow rate,  $c$  is a constant determined by liquid properties ( $c = 10\pi^2\rho\mu/3$ ),  
 176 and  $K$  a flow rate dependent cleaning rate constant. Integrating [5] from the point where a  
 177 circular cleaning front is first observed,  $a_o$ , at time  $t_o$  gives with  $\Delta t = t - t_o$ ,

$$178 \quad a^5 - a_o^5 = K^5(t - t_o) = K^5\Delta t \quad [6]$$

179 Wilson *et al.* (2014) showed that Equation [6] described the evolution of the cleaned front for  
 180 several materials until the radius  $a$  reached the film jump, when Equations [1], [2] and [3] no  
 181 longer apply. In the current work Equation [6] is fitted to data obtained with layers of  
 182 different thickness to determine the effect of  $\delta$  on  $K$  (and hence  $k'$ , where tests are conducted  
 183 using different flow rates).

184

### 185 *Cleaning – moving jets*

186 In this case the nozzle moves relative to the substrate at velocity  $v_{jet}$ . Wilson *et al.* (2015)  
 187 adapted the above static jet cleaning model to allow for relative motion between the substrate  
 188 and the jet, for the case where  $|U_o| \gg |v_{jet}|$ . The shape of the cleaned region is shown  
 189 schematically in Figure 1(c). The jet impinges at point O: ahead of O there is an almost  
 190 parabolic cleaning front centred on O, which extends into the jet wake and leaves a swathe of  
 191 width  $w_c$ . By considering the locus of stationary points directly preceding the jet (the dashed  
 192 line in Figure 1(c)) where the rate of peeling matches that of the approaching foulant, the  
 193 following ODE describing the shape of the cleaning front is obtained:

$$194 \quad \frac{dp}{d\theta} = \frac{1}{5} \frac{K^5}{v_{jet}} \frac{1}{p^3 \sin \theta} - \frac{p}{\tan \theta} \quad [7]$$

195 Here,  $p$  is the radial distance from O to the cleaning front and  $\theta$  the azimuthal angle measured  
 196 anticlockwise from the nozzle traverse direction. Integrating [7] from  $\theta = 0$  to  $180^\circ$  gives the  
 197 shape of the cleaning front: there is a maximum in the half-width at  $\theta = 127^\circ$ , which enabled  
 198 Wilson *et al.* to predict the width of the cleared region downstream of the moving jet, *viz.*

$$\begin{aligned}
 w_c &= 2.94 \left( \frac{K^5}{5} \frac{1}{v_{jet}} \right)^{1/4} \\
 &= 1.97 \frac{K^{5/4}}{v_{jet}^{1/4}}
 \end{aligned}
 \tag{8}$$

200 This result is tested for the moving plate configuration, for petroleum jelly layers.

201

### 202 *Cleaning – viscoplastic soils*

203 Equation [5] predicts that the size of the cleaned region should increase steadily until  $a$   
 204 reaches  $R$ , the limit of the RFZ. Hodgson and Smith (2014) studied the removal of layers of  
 205 petroleum jelly in the apparatus used by Wilson *et al.* (2014) and observed that  $a$  often  
 206 reached a limiting value,  $a_{max}$ , where  $a_{max} < R$ . They attributed this to the viscoplastic nature  
 207 of the soil, wherein a yield stress must be overcome before the material will yield. They  
 208 proposed a quantitative model of this behaviour and the following analysis builds on their  
 209 model.

210 At the cleaning front the flow of liquid dislodging the material is assumed to cause yield  
 211 along a flat shear plane inclined to the substrate surface at angle  $\chi$  (see Figure 2). This front  
 212 moves radially outwards with time when the force imposed by the liquid film is sufficient to  
 213 overcome the yield strength. Beyond  $a$  the liquid flows upwards so that a fraction of its  
 214 momentum flux is no longer horizontal and the difference between  $M$  and  $M \cos \chi$  provides  
 215 the driving force for cleaning (see Equation [4]). When the cleaning front reaches  $a_{max}$ , the  
 216 net momentum flux is equal to the force required to overcome the shear yield stress of the  
 217 layer and induce motion. The area of the yielding region for a complete circle of radius  $a_{max}$ ,  
 218 *i.e.* the ramp face, is approximately  $2\pi a_{max} \delta / \sin \chi$ : **the length of the ramp is assumed to be**  
 219 **small compared to  $a_{max}$ .** A force **balance in the horizontal direction** at  $a_{max}$  gives

$$\frac{6}{5} (\dot{m}U - \dot{m}U \cos \chi) = \tau_y \left( \frac{2\pi a_{max} \delta}{\sin \chi} \right) \cos \chi
 \tag{9}$$



221 where  $\tau_y$  is the shear yield stress of the layer; the coefficient 6/5 arises from considering the  
 222 momentum flux due to the parabolic velocity profile in the liquid film, as in Equation [2] (see  
 223 Wilson *et al.*, 2012). Substituting for  $U$  from Equation [1], with  $1/U_0$  and  $r_0$  both small and  $r$   
 224  $= a_{\max}$ , yields

$$225 \quad a_{\max} = \left( \frac{3\dot{m}^3}{5\pi c} \frac{1}{\tau_y \delta} [\tan \chi - \sin \chi] \right)^{1/4} \quad [10]$$

226 An alternative form of Equation [4] is now proposed to describe the rate of cleaning of a  
 227 yield stress material:

$$228 \quad \frac{da}{dt} = k'(M - M_Y) \quad M > M_Y \quad [11a]$$

$$229 \quad \frac{da}{dt} = 0 \quad M \leq M_Y \quad [11b]$$

230 where  $M_Y$  is the momentum flux required to cause yield.

231 By constructing a momentum balance per unit circumferential width in the radial direction,  
 232 the change in fluid momentum can be equated to the force required to yield the material at  
 233 radius  $a$ . With a flat shear plane of area per unit width  $\delta \operatorname{cosec} \chi$  inclined an angle  $\chi$ , this gives  
 234 an expression for  $M_Y$ , viz.

$$235 \quad M_Y - M_Y \cos \chi = \tau_y (\delta \operatorname{cosec} \chi) \cos \chi \quad [12]$$

236 which yields

$$237 \quad M_Y = \frac{\tau_y \delta}{(\tan \chi - \sin \chi)} \quad [13]$$

238 To integrate Equation [11a],  $M$  is obtained from Equation [5], derived from Equation [4];  $M_Y$   
 239 is obtained by substituting  $\tau_y \delta$  from Equation [10] into Equation [13], giving  
 240  $M_Y = 3\dot{m}^3 / 5\pi c a_{\max}^4$ . Combining this with Equations [11a] and [5] gives

$$241 \quad \frac{da}{dt} = k' \frac{3\dot{m}^3}{5\pi c} \frac{1}{a^4} \left( 1 - \left( \frac{a}{a_{\max}} \right)^4 \right) \quad a < a_{\max} \quad [14]$$

$$= \frac{K^5}{5a^4} \left( 1 - \left( \frac{a}{a_{\max}} \right)^4 \right)$$

242 in which  $K$  is a lumped cleaning rate constant. The growth of the cleaned region is given by

243 
$$t - t_o = \frac{5}{K^5} \int_{a_o}^a \frac{a^4}{1 - (a/a_{\max})^4} da \quad [15]$$

244 For the case where  $a = 0$  when  $t = 0$ , Equation [15] yields

245 
$$t = \frac{5}{4} \left( \frac{a_{\max}}{K} \right)^5 \left\{ \ln \left( \frac{1 + a/a_{\max}}{1 - a/a_{\max}} \right) - 4 \left( \frac{a}{a_{\max}} \right) + 2 \tan^{-1} \left( \frac{a}{a_{\max}} \right) \right\} \quad [16]$$

246 For other cases, as observed here, employing a Taylor expansion in  $a/a_{\max}$  and integrating the  
247 above integral gives

248 
$$t - t_o = \left( \frac{a_{\max}}{K} \right)^5 \left\{ \left( \frac{a}{a_{\max}} \right)^5 - \left( \frac{a_o}{a_{\max}} \right)^5 + \frac{1}{9} \left( \frac{a}{a_{\max}} \right)^9 - \frac{1}{9} \left( \frac{a_o}{a_{\max}} \right)^9 + \frac{1}{13} \left( \frac{a}{a_{\max}} \right)^{13} - \frac{1}{13} \left( \frac{a_o}{a_{\max}} \right)^{13} + \dots \right\} \quad [17]$$

249

250 The terms containing  $(a_o/a_{\max})$  are usually negligible. In the early stages of cleaning,  
251 Equation [17] reduces to Equation [6], which was fitted to the data in this linear region to  
252 give  $K$ . With this value of  $K$ ,  $a_{\max}$  was then obtained by fitting Equation [17] to data points  
253 (see Figure 12) over the whole range of  $\Delta t^{0.2}$ . Each value of  $a_{\max}$  then gave  $\chi$  from Equation  
254 [10], using  $\tau_y = 50 \text{ Pa}$  and the measured soil thickness  $\delta$ .

255 Both equations [15] and [17] reduce to Equation [6] when  $a/a_{\max}$  is small. This was the case  
256 for the experiments on removing petroleum jelly with moving jets in this work, so Equation  
257 [8] is used to analyse those data.

258

## 259 **Materials and Methods**

### 260 *Impinging jet apparatus*

261 The apparatus was based on that reported by Wang *et al.* (2013b), see Figure 3. The nozzle  
262 and target were mounted inside a 1.2×1.2×1.7 m high cabinet with Perspex sides which  
263 allowed the jet and substrates being cleaned to be videoed through the walls. Reverse  
264 osmosis (RO) water at room temperature (approximately 20°C) was pumped from a 26 litre  
265 holding tank through a rotameter, control valve and flexible tubing before entering a 150 mm  
266 straight entry section upstream of the nozzle. Brass nozzles with bore diameter,  $d_N$ , of 2, 3  
267 and 4 mm were available: a 2 mm nozzle was used in the cleaning tests reported here. The  
268 nozzle was positioned 60 mm from the target in order to ensure that the jet was coherent. The

269 alignment of the nozzle and target was checked regularly using a square and a digital  
270 inclinometer.

271 An interrupter plate was located between the nozzle and the target in the initial period while  
272 flow was set and stabilised. The plate was then removed to start a cleaning test. After striking  
273 the target, the water drained vertically, fell to the cabinet floor and was either discharged to  
274 drain or recycled if no soil was entrained.

275 Video recordings of jet impingement and cleaning were made using a Nikon D3300 D-SLR  
276 digital camera aligned normal to the target. Images were processed using the NIH ImageJ  
277 software. Transparent graticule tape was located on the reverse (dry) side of target sheets in  
278 order to provide length calibration. Illumination was provided by external 1200 W halogen  
279 lamps or a waterproof IP65 (240V, 36 W) tube light.

280 Targets for static jet cleaning were held in an aluminium frame which could be positioned at  
281 different distances from the nozzle. Sheets (glass or Perspex) of dimensions 360×600×5 mm  
282 (width×height×depth) were coated separately and mounted on the frame using locating  
283 screws.

284 Cleaning by moving jets was studied using the arrangement shown in Figure 3 in which the  
285 nozzle remained stationary and the target was moved upwards or downwards in order to  
286 generate relative motion between the two. This configuration allowed the flow pattern and  
287 cleaning region to be videoed by a stationary camera, and nozzle-motion-induced vibration in  
288 the jet eliminated. A ‘sash window’ system, using a rubber-toothed drive belt connected to a  
289 two-way variable speed motor, provided the vertical motion of the target plate. Cut-off  
290 switches were located on the belt drive to avoid the target exceeding its maximum travel on  
291 the frame. Calibration tests determined that the target plate reached its steady velocity after  
292 an initial 100 mm of travel so cleaning experiments were not started until this acceleration  
293 stage had been completed. This allowed 500 mm of traverse at constant speed, at speeds up to  
294 250 mm s<sup>-1</sup>.

295

#### 296 *Target plate preparation*

297 Soil layers were prepared from two materials on glass or Perspex plates. The uniformity  
298 (flatness and thickness) of the plates was checked using a Moore & Wright deep throat digital  
299 micrometer at 24 different locations on the plate. Two materials were considered for

300 preparing soil layers, namely a water-based PVA glue (ASDA supermarket brand) and  
301 petroleum jelly (Trilanco White Petroleum Jelly, Poulton-le-Flyde, UK). The former interacts  
302 with the cleaning agent (water), undergoing swelling, while the latter is hydrophobic and  
303 does not interact. The PVA tended to pool towards the plate edges when spread over glass so  
304 only Perspex substrates were used in the PVA tests.

305 The rheology of the petroleum jelly was investigated with a Bohlin CV-120 controlled stress  
306 rheometer using sand-blasted 50 mm diameter parallel plates with a 1 mm gap. The  
307 petroleum jelly did not exhibit simple viscoplastic behaviour: steady shear tests indicated a  
308 high viscosity, low-shear plateau marked by a transition to shear thinning at approximately 50  
309 Pa. Oscillatory stress tests were performed at a frequency of 1 Hz and these showed a  
310 transition from elastic to viscous behaviour around 50 Pa. This value was used as the yield  
311 stress for the petroleum jelly in the model calculations. By comparison, the petroleum jelly  
312 product used by Wang (2014) had a yield stress of 12 Pa (see Yang *et al.*, 2012).

313 Even soil layers were prepared by dragging a 340 mm aluminium slider blade over the  
314 surface, leaving a uniform layer of soil in its wake. The clearance between the blade and the  
315 plate was adjusted by a pair of micrometers located behind the drag wheels (see Figure 4), to  
316 give film thickness from 50-2000  $\mu\text{m}$ .

317 PVA layers were applied and left to dry in air at ambient temperature for 24 h. Measurements  
318 of the mass of 120  $\mu\text{m}$  thick layers over time indicated an exponential decrease in mass over  
319 the first 3.5 h, to approximately 21% of the original value. The thickness of the dry PVA  
320 layer was checked using the digital micrometer at 24 locations.

321 Petroleum jelly layers were prepared on Perspex or borosilicate glass plates. The micrometer  
322 could not be used to determine the thickness of the petroleum jelly layers as the material is  
323 soft, so the thickness of the layers was estimated by measuring the mass of jelly applied and  
324 determining its thickness from the area covered and the density, measured separately as  $870$   
325  $\pm 5 \text{ kg m}^{-3}$ . This calculation relies on the substrate being perfectly flat, so a conservative  
326 estimate of its precision, of 50  $\mu\text{m}$ , is quoted. The yield stress of the jelly was measured  
327 previously as 12 Pa at 20°C (Yang *et al.*, 2013).

328 The PVA layers were colourless when dry but turned white and swelled when contacted with  
329 water. The influence of PVA layer thickness on swelling and deformation behaviour was  
330 studied using fluid dynamic gauging (FDG, see Wang and Wilson, 2015), which allows the

331 swelling of a coating immersed in liquid to be monitored in situ and in real time. The layer  
332 thickness is measured by recording the pressure drop in a liquid being sucked through a  
333 nozzle at a given flow rate, the nozzle being located close to the layer surface. FDG  
334 measurements were performed using the automated apparatus described by Wang and Wilson  
335 (2015) with a 1 mm nozzle diameter and RO water at 20°C as the gauging fluid. PVA layers  
336 of various thicknesses were prepared on stainless steel discs and dried as described above.  
337 The loss of mass on drying, and the thickness of the dried layer, were recorded. These  
338 indicated similar behaviour to the layers prepared on Perspex surfaces. Measurements were  
339 recorded for up to an hour following immersion of the sample in the test chamber. It took up  
340 to 60 s to fix the plate and establish the gauging flow, so the initial stage of swelling could  
341 not be monitored.

342

## 343 **Results and Discussion**

### 344 *Film jump location*

345 The location of the film jump and the extent of the rope region, *i.e.* the distances  $R$  and  $R_c$  at  
346 the level of jet impingement (A-A in Figure 1(a)), were measured for coherent jets generated  
347 by all three nozzles ( $d_N = 2, 3, 4$  mm) and different flow rates. The experimental  
348 measurements of  $R$  were in reasonable agreement with the predictions of Equation [3] using  
349 an effective contact angle of 90°, as reported in previous studies (Wang *et al.* 2013b; Wilson  
350 *et al.*, 2014). These results are presented in Supplementary Figure S1 and provide confidence  
351 in using Equation [2] to estimate the local momentum flux.

352 The effect of substrate motion on the size of the film jump was studied for the configuration  
353 employed in the moving jet cleaning studies (water impinging on Perspex at 20°C,  $d_N = 2$   
354 mm,  $Q = 35$  mL s<sup>-1</sup>;  $Re_{jet} = 21,700$ ) with nozzle liquid velocities up to  $\pm 233$  mm s<sup>-1</sup>. For a  
355 static jet ( $v_{jet} = 0$ ),  $R$  was 46 mm, as shown by the broken line in Figure 5; the diagram also  
356 shows that  $R$  increased a little with  $v_{jet}$  when the plate was moving upwards, *i.e.* the jet  
357 impinged on a region already wetted. Conversely,  $R$  decreased a little when the plate was  
358 moving downwards. With reference to Equation [3], this indicates that the effective contact  
359 angle is affected by the motion of the contact line. A second factor is the relative velocity  
360 between the incoming jet and the target plate, which gives rise to different, non-orthogonal,  
361 angles of impingement for the upward and downwards moving jets. For the present work, the  
362 jet trajectory is always perpendicular to the the plate, whatever the relative values of jet

363 velocity,  $U_o$ , and nozzle travel speed,  $v_{jet}$ . Here,  $U_o \gg v_{jet}$ , so the film velocity in the RFZ was  
364 assumed to be the same as for a stationary jet (when  $v_{jet} = 0$ ). If was comparable with  $U_o$ , a  
365 new RFZ analysis would be needed. Wang *et al.* (2014) studied the effect of angle of  
366 impingement on  $R$ : values below  $90^\circ$  (jet pointing slightly downwards) gave smaller  $R$  owing  
367 to a larger fraction of the flow moving downwards, away from the point of impingement. The  
368 effective angles of impingement, calculated for a plate velocity of  $52 \text{ mm s}^{-1}$ , nozzle diameter  
369 2 mm and flow rate  $35 \text{ mL s}^{-1}$ , were  $89^\circ$  and  $91^\circ$  for downward and upward moving plates,  
370 respectively. With a plate velocity of  $233 \text{ mm s}^{-1}$  the effective angle of impingement was  
371 calculated as  $85.2^\circ$  and  $94.8^\circ$  for downward and upward moving plates, respectively. These  
372 angles are near enough to  $90^\circ$  to justify the assumption of perpendicular impingement.

373

374 The observed reduction in RFZ width with increasing downward plate velocity is  
375 qualitatively consistent with the results presented by Gradeck *et al.* (2006) using a fixed  
376 nozzle and a fast moving belt as the substrate. They employed nozzle velocities (relative to  
377 the belt) of similar magnitude to the average velocity of liquid in the jet, and quantified the  
378 effect of the nozzle motion on the curvature of the hydraulic jump rather than the location of  
379 the jump.

380

381 The rope was noticeably more stable for a downward moving jet, *i.e.* an upwards moving  
382 plate. In this case the flow is passing over a surface which had been previously wetted by  
383 liquid and conditions at the contact line are expected to be related to phenomena affecting the  
384 receding contact angle, such as better wetting (smaller contact angle).

385

### 386 *Cleaning PVA films – static nozzle*

387 Vertical Perspex sheets, each coated with a PVA layer of dry thickness 16-171  $\mu\text{m}$  were  
388 cleaned by a horizontal water jet ( $Re_{jet} = 21,700$ , as above). For all layers, there was an initial  
389 contact time,  $t_c$ , before the jet broke through the soil and cleaning occurred by a peeling  
390 mechanism, sometimes involving ‘fingers’, see Figure 8. The formation of fingers in the RFZ  
391 has been reported previously, by Hsu *et al.* (2011), for water jets impinging perpendicularly  
392 on a layer of viscous liquid coating a solid plate. They observed longer and narrower  
393 fingering for elastic coating fluids (such as semi-dilute polyacrylamide solutions). Their

394 findings are consistent with the present work as the PVA layer will have some elasticity:  
395 quantifying the elasticity of a swelling layer is a challenging topic.

396 Figure 6 shows that the contact time varied randomly with dry layer thickness for  $\delta_{\text{dry}}$  values  
397 less than 75  $\mu\text{m}$ . Above 75  $\mu\text{m}$  there was an approximately linear relationship between  $\delta_{\text{dry}}$   
398 and  $t_c$ . Diffusion of water through the swelling PVA layer to the substrate/layer interface is  
399 thought to delay the onset of peeling; differences in the structure of the layer are also likely to  
400 affect the transition to peeling.

401 The FDG measurements presented in Figure 7 show a similar change in layer swelling  
402 behaviour with dry layer thickness. The data are reported as the swelling ratio,  $S$ , defined as  $S$   
403  $= \delta(t)/\delta_{\text{dry}}$ , where  $\delta$  is measured by FDG and  $\delta_{\text{dry}}$  by micrometer. Each data set shows a  
404 similar pattern, namely an initially rapid increase in thickness followed by a slow approach to  
405 an asymptotic level. Before the asymptote is reached, the thickness increases abruptly,  
406 marking a rupture event due to the stresses imposed by the gauging flow (in these tests, the  
407 maximum shear stress lay in the range 6-20 Pa, see Wang and Wilson (2015)).

408 There are noticeable differences in the amount of swelling (Figure 7) and the time taken for  
409 rupture (Figure 6) as  $\delta_{\text{dry}}$  increases. The maximum swelling ratio is larger (and varies  
410 noticeably) with thinner layers, and rupture occurs earlier. The trend in rupture times reflects  
411 the observed trend in contact times in the cleaning experiments, and the former are plotted on  
412 a secondary axis alongside the  $t_c$  values in Figure 6. The FDG data complement the cleaning  
413 results.

414 The strength of the layer is expected to decrease as the layer swells (reducing the volume  
415 fraction of polymer), and rupture is expected to occur when the force imposed by the gauging  
416 flow exceeds the ability of the layer to resist it. The relationship between swelling ratio and  
417 layer strength is not yet known. A further factor is that cleaning is related to the strength of  
418 adhesion between the layer and the substrate: direct measurement of adhesion strength under  
419 cleaning conditions is difficult.

420 The initial stages of removal rarely featured a uniformly circular region, as assumed by the  
421 model (Equation [4]). Examples of the patterns observed are shown in Figure 8. The time at  
422 which a circular region, radius  $a_0$ , was formed is denoted  $t_0$  (with  $t_0 > t_c$ ) and the subsequent  
423 evolution of the size of the cleaned region was compared with the model. Supplementary  
424 Video 1 shows an example of cleaning of a PVA layer, starting from shortly before the film

425 begins to be removed. There was generally good agreement with the form of the model, as  
426 shown by Figure 9 for two different layer thicknesses. In all cases the experiments were  
427 stopped before the size of the cleaned region,  $a$ , reached the film jump at  $R$ , when Equation  
428 [4] would not apply. The gradient of these loci yields the cleaning rate constant,  $K$  (Equation  
429 [5]). Figure 10 indicates that  $K$  was independent of  $\delta_{\text{dry}}$ , which is expected for a cleaning  
430 mechanism involving peeling at the substrate-layer interface. The initial detachment  
431 behaviour, specifically whether fingering (see Figure 8(a,b)) was observed or not, is indicated  
432 by the symbol shading in Figure 10; there is no systematic influence on  $K$ . Further analysis  
433 indicated that  $K$  was independent of  $t_c$  (data not reported).

434 The values of  $K$  obtained in these tests (average  $9.8 \pm 2.0 \text{ mm s}^{-0.2}$  :  $\delta_{\text{dry}} = 20\text{-}170 \text{ }\mu\text{m}$ ) are  
435 similar to that of  $12 \text{ mm s}^{-0.2}$  reported by Wilson *et al.* (2014) for PVA layers with dry  
436 thickness  $120 \text{ }\mu\text{m}$ . Their PVA glue was a branded product for consumer use, as in these tests.  
437 Detailed composition information was not available. Relating  $K$  (and  $k'$ ) to the properties of  
438 the layer and the substrate is the subject of ongoing work.

439 This work confirms that the modelling approach reported by Wilson *et al.* (2014) can be  
440 applied to materials with time-dependent response to cleaning solutions. In this case, the  
441 PVA layer had to undergo soaking for a given period – related to its thickness – before  
442 removal was observed. The dynamics of the PVA response to cleaning solution reflect  
443 behaviour such as pH-induced swelling and breakdown observed in many food systems. This  
444 time dependency will be important in CIP operations if regions higher up a wall are not  
445 wetted as much as regions below, over which falling films of cleaning solution are likely to  
446 flow continuously. The interaction between soaking and cleaning kinetics and jet hydraulics  
447 **could** be studied using the moving plate apparatus (Figure 3) but was not conducted for the  
448 PVA films in this study.

449

#### 450 *Cleaning petroleum jelly layers – static nozzle*

451 Wilson *et al.* (2014) studied the removal of petroleum jelly layers using a range of nozzle  
452 sizes and flow rates. One nozzle size and flow rate were primarily used in the present work  
453 ( $Q = 35 \text{ mL s}^{-1}$ ,  $d_N = 2 \text{ mm}$ , as in the PVA studies) in order to determine the influence of  
454 layer thickness and to test the modified cleaning model (Equation [15]).

455 Unlike the PVA layers, cleaning started as soon as the petroleum jelly was contacted by the  
456 impinging jet, giving a circular cleaned region (see Figure 11(a) and Supplementary Video



2). Dislodged jelly built up as a rim of spoil around the cleared region and gave rise to noticeable splattering and wayward jetting as this berm of material became thicker. The presence of the rim material did not affect the cleaning rate: this was confirmed by comparing tests at constant flow rate with ones where the flow was stopped momentarily after 20 s, the rim of material removed, and the flow restarted. The same maximum value,  $a_{\max}$ , was reached in each case. This value was always smaller than the size of the RFZ expected for these flow conditions, of 46 mm.

The evolution of the cleaned region radius is plotted for two notionally identical tests in Figure 12, alongside data collected by Wang (2014) for a layer of a different petroleum jelly (on glass), albeit with initial thickness of 200  $\mu\text{m}$ . The difference in behaviour for the notionally identical tests on glass illustrate the variability in the layers arising from the application method.

The data are plotted in the form suggested by Equation [6], with  $a_0$  and  $t_0$  set to zero (cleaning starts instantaneously), *i.e.*  $a \propto t^{1/5}$ . All three data sets follow a linear trend initially but then approach a limiting value asymptotically. Asymptotic behaviour is observed on Perspex and, (with a different asymptote) on glass, which is consistent with this asymptote arising from the viscoplastic nature of the soil. Each data set was fitted to Equation [15], adjusting  $\chi$  (and hence  $a_{\max}$ ) to minimise the sum of squares of the error. The agreement with the fitted model is good, and the transition to asymptotic behaviour is captured reasonably.

Fitting the data to Equation [15] gives estimates of the lumped cleaning rate constant,  $K$ , and the final radius  $a_{\max}$ . The former can also be obtained from the initial linear trend, as shown in Figure 12. The relationship between  $K$  and the soil layer thickness,  $\delta$ , is presented in Figure 13(a), which shows a decrease in  $K$  with increasing soil thickness, particularly for thinner layers. The average value of  $K$  was  $7.2 \pm 1.7 \text{ mm s}^{0.2}$ , which is in reasonable agreement for the value of  $6.1 \text{ mm s}^{0.2}$  reported by Wilson *et al.* (2014) for 250  $\mu\text{m}$  petroleum jelly layers on Perspex cleaned with water at 20°C. The latter study did not explore the asymptotic behaviour observed with petroleum jelly. The  $K$  value of  $7.2 \pm 1.7 \text{ mm s}^{0.2}$  corresponds to a  $k'$  value of  $1.5 \times 10^{-5} \text{ kg}^2 \text{m}^{-4} \text{s}^{-1}$  (Equation [5]).

The Wang (2014) data, for a different petroleum jelly on borosilicate glass, yielded a  $K$  value of  $13.3 \text{ mm s}^{0.2}$ , which is significantly different from the values obtained with Perspex and confirms that the substrate-soil interaction is an important factor in determining the removal rate. The difference follows the trend expected from contact angle measurements: the

489 petroleum jelly is strongly hydrophobic (contact angle  $> 90^\circ$ ) while the glass is more  
490 hydrophilic than Perspex (water contact angles of  $33 \pm 5^\circ$  and  $74 \pm 5^\circ$ , respectively).

491 The effect of layer thickness on cleaning rate is captured indirectly by the shear angle  $\chi$ . The  
492 angle  $\chi$  was calculated from Equation [10] assuming that  $\tau_y = 50 \text{ Pa}$ . The data in Figure 13(b)  
493 show a linear relationship between  $\chi$  and  $K$ . The values of  $\chi$  are relatively modest, at less  
494 than  $30^\circ$ , indicating a gentle ramp at the point of peeling. It is noticeable that the  $\chi$  value  
495 obtained from the Wang (2014) data set, with a different petroleum jelly on glass, differs  
496 from these on Perspex. It was not possible in these experiments to obtain accurate  
497 measurements of the shape of the cleaning front to confirm the assumption of a steady ramp  
498 profile. Both these results (and the correlation between  $K$  and  $\chi$  evident in Figure 13(b))  
499 indicate that the model requires further work, supported by measurements of the cleaning  
500 front employing small, detachable targets. Relaxing the assumption of simple viscoplastic  
501 behaviour for the soil would require detailed simulation of the coupled flow problem between  
502 a mobile soil and the cleaning liquid film.

#### 503 *Cleaning petroleum jelly layers – moving substrate, fixed nozzle*

504 Experiments were performed with petroleum jelly layers of average thicknesses ranging from  
505 295 to 1860  $\mu\text{m}$  on vertical Perspex substrates. The jetting flow was the same as in the  
506 previous sections (water at  $20^\circ\text{C}$ ,  $Q = 35 \text{ mL s}^{-1}$ ,  $d_N = 2 \text{ mm}$ ), with the vertical plate and  
507 substrate moving upwards or downwards, relative to the fixed horizontal cleaning jet, at  
508 velocities ranging from 6 to  $31 \text{ mm s}^{-1}$ .

509 As the jet passed over the soil, cleaning occurred immediately within the RFZ (see Figure  
510 11(b) and Supplementary Video 3). The cleaning front was elliptical, as reported by Wilson  
511 *et al.* (2015), creating a cleared region of width  $w_c$  (see Figure 11(b)). This photograph also  
512 shows that a film jump was not observed in these tests as the berm of spoil deflected the  
513 water film away from the surface, giving splashback and secondary jetting. The cleaning  
514 front appeared to be more stable when the plate was moving downwards rather than upwards,  
515 which was accredited to the jet flowing into undisturbed soil. When the plate moved upwards,  
516 the soil had been in contact with the draining film prior to being washed by the jet.

517 The model of Wilson *et al.* (2015) (Equation [7]) was found to predict the shape of the  
518 cleaning front very well. Figure 14 compares the shape of the front extracted from  
519 photographs for several cases with the profile obtained by integrating Equation [7]. The

520 results are presented in dimensionless form, scaled by  $a_x$ , the shortest distance from the  
521 impingement point to the cleaning front (see Figure 1(c)). The agreement with the predicted  
522 profile for upward moving jets is excellent, while there is more scatter with the downward  
523 moving jets, as mentioned above. The width of the cleaned region,  $w_c$ , was also less uniform  
524 when the jet was moving downwards, which could be due to the boundary of the RFZ  
525 buffeting the sides of the cleaned region as the nozzle descended.

526 Equation [8] indicates that  $w_c$  should be proportional to  $v_{\text{jet}}^{-1/4}$ . The data collected for two  
527 layer thicknesses are plotted in this form in Figure 15 and confirm this behaviour (as did data  
528 for other soil thicknesses, data not reported). These results confirm the generality of the  
529 Wilson *et al.* (2015) model, as it was developed to describe adhesive removal (peeling) of  
530 **Xanthan** gum layers.

531 Equation [8] is based on Equation [5], *i.e.* it does not consider the asymptotic behaviour  
532 resulting from the viscoplastic nature of the layer. Inspection of Figure 12 suggests that  
533 Equation [5] gives a reasonable description of petroleum layer behaviour when the radius of  
534 the cleaning front, which can be related to  $w_c/2$ , is less than  $3a_{\text{max}}/4$ . The values of  $w_c$  in  
535 Figure 15 (and the other data sets) all fitted this criterion so Equation [8] is expected to apply  
536 here.

537 Each datum in Figure 15 yields a value of  $K$  and these are compared with the values obtained  
538 for the static nozzle tests in Figure 16. There is excellent agreement between the two sets of  
539 results: both exhibit the decreasing trend with layer thickness discussed in the previous  
540 section. No further analysis of the shear plane shape is offered here. This result confirms that  
541 measurements made with the static nozzle can be used to predict the performance of moving  
542 jets, for both upwards and downwards cases.

543 **velocities employed in these studies are low compared with those employed in industrial**  
544 **practice.**

545

## 546 **Conclusions**

547 For batch cleaning by a horizontal water jet impinging on a vertical soiled surface, the growth  
548 of the radius  $a$  of the clean area **for both soils considered here** is well described, in the early  
549 stage of cleaning, by  $a^5 - a_0^5 = K^5 (t - t_0)$ ; thus  $(a^5 - a_0^5)^{0.2}$  is linearly related to  $\Delta t^{0.2} = (t -$   
550  $t_0)^{0.2}$ . The time  $t_0$  is when a clean area, of radius  $a_0$ , is first formed by the impinging jet. **With**

551 the PVA soils, this time is related to swelling (and softening) of the layer, as demonstrated by  
552 separate fluid dynamic gauging tests. The initial removal of PVA layers was often, but not  
553 always, accompanied by fingering.

554 The value of the cleaning rate constant,  $K$ , was independent of dry layer thickness for the  
555 PVA soils, which is consistent with a peeling mechanism.

556 In contrast,  $K$  decreased with layer thickness for the petroleum jelly. With this soil, the  
557 radius,  $a$ , of the clean area approaches an asymptote  $a_{max}$ , when the radial momentum of the  
558 cleaning water film, formed by the jet impinging on the substrate, balances the adhesive  
559 strength of the soil on the substrate. The soil is modelled as forming a ramp at radius  $a_{max}$   
560 which deflects the radial flow of cleaning water at angle  $\chi$  to the substrate. The angle  $\chi$  is  
561 calculated from  $a_{max}$  together with the soil thickness  $\delta$  and its shear strength  $\tau_y$ , measured  
562 separately. The angle  $\chi$  is found to be of order 7 – 25 degrees;  $\chi$  is linearly related to  $K$ .

563 Continuous cleaning was studied by moving the vertical soiled surface up or down relative to  
564 the horizontal cleaning jet, which was fixed. This simulated industrial cleaning where a jet  
565 moves over a soiled surface. The jet velocities and the nozzle velocities studied in these  
566 experiments are low compared to those employed in industrial practice: scale-up to industrial  
567 operating conditions represents an area for future work.

568 With the moving soiled plate, a cleaned strip, of width  $w_c$ , is formed; the clean strip is below  
569 the jet when the plate moves down, above the jet when the plate moves up. A cleaned front,  
570 of nearly semi-elliptical shape, is formed near the jet; the clean bit starts at distance  $a_x$  from  
571 the jet, above the jet with the plate moving down, below the jet when the plate moves up.

572 The width  $w_c$ , the distance  $a_x$  and the shape of the above-mentioned front are well predicted  
573 by the differential equation [7], using the parameter  $K$  from the batch experiments and the  
574 velocity  $v_{jet}$  of the substrate. In this way, the batch and continuous experiments are well  
575 linked; results from a batch experiment can be used to predict the behaviour of a continuous  
576 experiment where the cleaning jet moves parallel to the soiled plate.

577

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654 **Nomenclature**

**Roman**

$a$	radial location of cleaning front	m
$a_0$	radius when cleaning front is first seen	m
$a_x$	radial location of cleaning front on jet path	m
$a_{\max}$	radial location of cleaning front, limiting value	m
$c$	lumped parameter, Equation [5]	$\text{kg}^2 \text{m}^{-4} \text{s}^{-1}$
$d_N$	nozzle throat diameter	m
$k'$	cleaning rate constant	$\text{m s kg}^{-1}$
$K$	lumped cleaning rate parameter, Equation [5]	$\text{m s}^{-0.2}$
$M$	momentum flux per unit width	$\text{kg s}^{-2}$
$M_y$	momentum flux per unit width to overcome yield stress	$\text{kg s}^{-2}$
$\dot{m}$	mass flow rate in jet	$\text{kg s}^{-1}$
$\rho$	radial distance to cleaning front, Equation [7]	m
$Q$	volumetric flow rate	$\text{m}^3 \text{s}^{-1}$
$R^2$	correlation coefficient	-
$r$	radial co-ordinate	m
$r_0$	jet radius	m
$R$	radius of hydraulic jump	m
$Re_{\text{jet}}$	jet Reynolds number, defined $Re_{\text{jet}} = \rho U_0 d_N / \mu$	-
$S$	swelling ratio, $S = \delta(t) / \delta_{\text{dry}}$	-
$t$	time	s
$\Delta t$	total time after cleaning front is first seen, $= t - t_0$	s
$t_c$	contact time of soil and water before jet breakthrough and	s

cleaning starts

$t_o$	time at which cleaning front, radius $a_o$ , is first seen	s
$U$	mean velocity in film	$\text{m s}^{-1}$
$U_o$	jet and initial film mean velocity	$\text{m s}^{-1}$
$v_{\text{jet}}$	nozzle traverse speed (plate velocity with stationary jet)	$\text{m s}^{-1}$
$w_c$	width of cleaned region	m

655

### Greek

$\beta$	contact angle	°
$\delta$	thickness of layer	m
$\delta_{\text{dry}}$	thickness of dry layer, measured by micrometer	m
$\gamma$	surface tension (liquid/vapour)	$\text{N m}^{-1}$
$\mu$	dynamic viscosity	$\text{Pa s}$
$\theta$	azimuthal angle	°
$\chi$	slope of yield plane	°
$\rho$	density	$\text{kg m}^{-3}$
$\tau_y$	shear yield stress	Pa

656

### 657 **Acronyms** 658

659	CIP	cleaning in place
660	FDG	fluid dynamic gauging
661	PVA	polyvinylalcohol
662	RFZ	radial flow zone
663	RO	reverse osmosis



## Figure captions

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Figure 2 Proposed model for cleaning of a viscoplastic soil layer of thickness  $\delta$ .

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Figure 5 Effect of nozzle-substrate motion on the film jump. Clean Perspex plate,  $d_N = 2$  mm,  $Q = 35$  mL s<sup>-1</sup>. (a) Dimension  $R$ , measured at level of impingement. **The  $v_{jet}$  error bars show the standard error in measurements of the steady plate velocity**; (b) Photographs of impingement region for plate moving (i) downwards and (ii) upwards,  $v_{jet} = 52$  mm s<sup>-1</sup>.

Figure 6 Effect of initial PVA layer thickness  $\delta_{dry}$  on initial contact time (left hand axis) before jet breakthrough was observed, and rupture time measured by FDG tests (Figure 7, right hand axis). ‘Fingering’, see Figure 8, was sometimes observed. Dashed locus shows linear relationship between  $t_c$  and  $\delta$  for  $\delta > 75$   $\mu$ m. **The error bars for  $\delta_{dry}$  indicate the range in the thickness values measured across the plate.**

Figure 7 Swelling ratio,  $S = \delta(t)/\delta_{dry}$ , describing swelling behaviour of PVA layers measured in RO water at 20°C by fluid dynamic gauging. Points marked R indicate where the layer was disrupted by the gauging flow: subsequent data were discarded. The small steps in each profile are related to changes in FDG nozzle position. The precision of the FDG measurements is  $\pm 10$   $\mu$ m and the steps lie within this range.

Figure 8 Photographs showing different removal patterns observed with PVA layers. (a) **fingers**, (b) **annulus of uncleaned material**, both for  $\delta_{dry} = 105 \pm 20$   $\mu$ m; (c) **evolution of initially asymmetric cleared region to a circular one**;  $\delta_{dry} = 43 \pm 22$   $\mu$ m.

Figure 9 Growth of cleared region for two different PVA layer thicknesses. Data are plotted in the form suggested by Equation [6] so that the gradient gives the value of  $K$ . Symbols – experimental measurements; loci – fitted trend lines.  $R^2$  is the regression coefficient.

Figure 10 Effect of dry PVA layer thickness on  $K$ . Dashed locus shows mean value of  $K$ .

Figure 11 Cleaning of petroleum jelly layers with (a) static nozzle and (b) plate moving downwards; nozzle static. Perspex sheets. Experimental conditions:  $d_N = 2$  mm,  $Q = 35$  mL s<sup>-1</sup>; (a)  $\delta = 375$   $\mu$ m; (b)  $\delta = 645$   $\mu$ m,  $v_{jet} = 7.3$  mm s<sup>-1</sup>.

Figure 12 Evolution of size of cleared region for petroleum jelly layers with static jet,  $d_N = 2$  mm,  $Q = 35$  mL s<sup>-1</sup>. Symbols: circles, diamonds, this work, Perspex substrate,  $\delta = 470 \pm 50$   $\mu$ m; triangles, glass substrate,  $\delta = 200 \pm 30$   $\mu$ m, reported by Wang (2014). Solid

loci show fit of initial data (solid symbols) to Equation [6]; dashed loci show fit for all data in a series to Equation [17]. Horizontal dot-dashed loci show  $a_{\max}$ .

Figure 13 Effect of petroleum jelly layer thickness on cleaning model parameters. (a)  $K$  values, extracted from initial stages of cleaning (see Figure 12). Open circle, open triangle – mean values of  $K$  reported by Wilson *et al.* (2014) and Wang (2014), respectively, for a different petroleum jelly. PVA values (Figure 10) included for comparison. (b) Relationship between  $\chi$  and  $K$ , calculated from  $a_{\max}$  using Equation [10] and measured values of  $\dot{m}$ ,  $\delta$  and  $c$ : solid circles – this work, Perspex substrate,  $\tau_y = 50$  Pa; triangle, Wang (2014), glass substrate (see Figure 12),  $\tau_y = 12$  Pa

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Figure 16 Effect of petroleum jelly layer thickness on  $K$  obtained from moving jet experiments. Static nozzle results (Figure 13(a)) plotted for comparison.

## Supplementary Materials

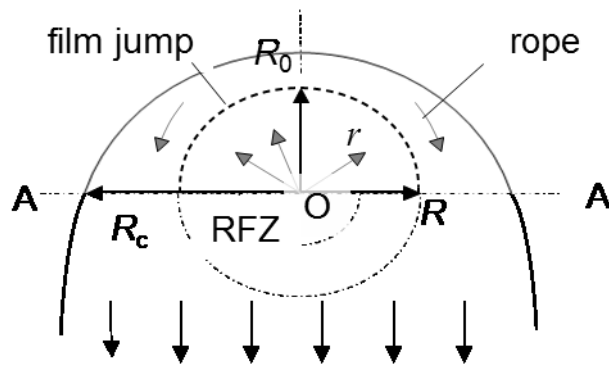
Supplementary Figure S1: Effect of jet flow rate on RFZ radius with jet flow rate for different nozzle diameters (a)  $d_N = 2$  mm, (b)  $d_N = 3$  mm, (c)  $d_N = 4$  mm on (i) Perspex and (ii) glass.  $x$ -axis error bars are too small to plot. Eq. [3] is plotted using the measured advancing contact angles (solid) and an effective contact angle of  $90^\circ$  (dashed).

Supplementary Video 1 Cleaning of PVA layer ( $\delta = 93$   $\mu\text{m}$ ) on Perspex, static nozzle ( $d_N = 2$  mm,  $\dot{m} = 35$   $\text{g s}^{-1}$ )

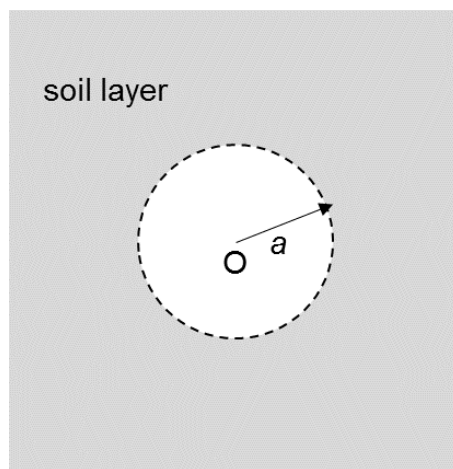
Supplementary Video 2 Cleaning of petroleum jelly layer ( $\delta = 136$   $\mu\text{m}$ ) on Perspex, static nozzle ( $d_N = 2$  mm,  $\dot{m} = 35$   $\text{g s}^{-1}$ )

Supplementary Video 3 Cleaning of petroleum jelly layer ( $\delta = 645$   $\mu\text{m}$ ) on Perspex, moving nozzle ( $d_N = 2$  mm,  $v = 7.3$   $\text{mm s}^{-1}$ ,  $\dot{m} = 35$   $\text{g s}^{-1}$ )

(a)



(b)



(c)

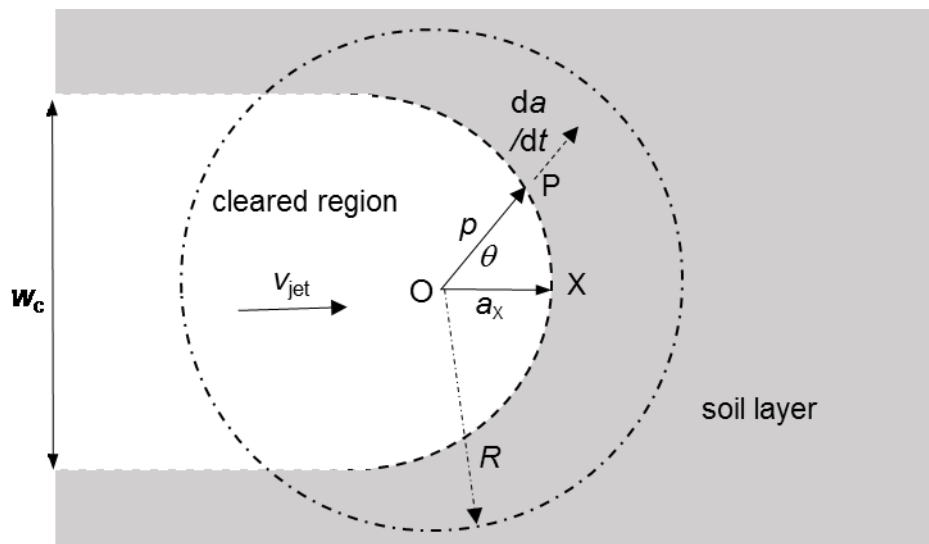


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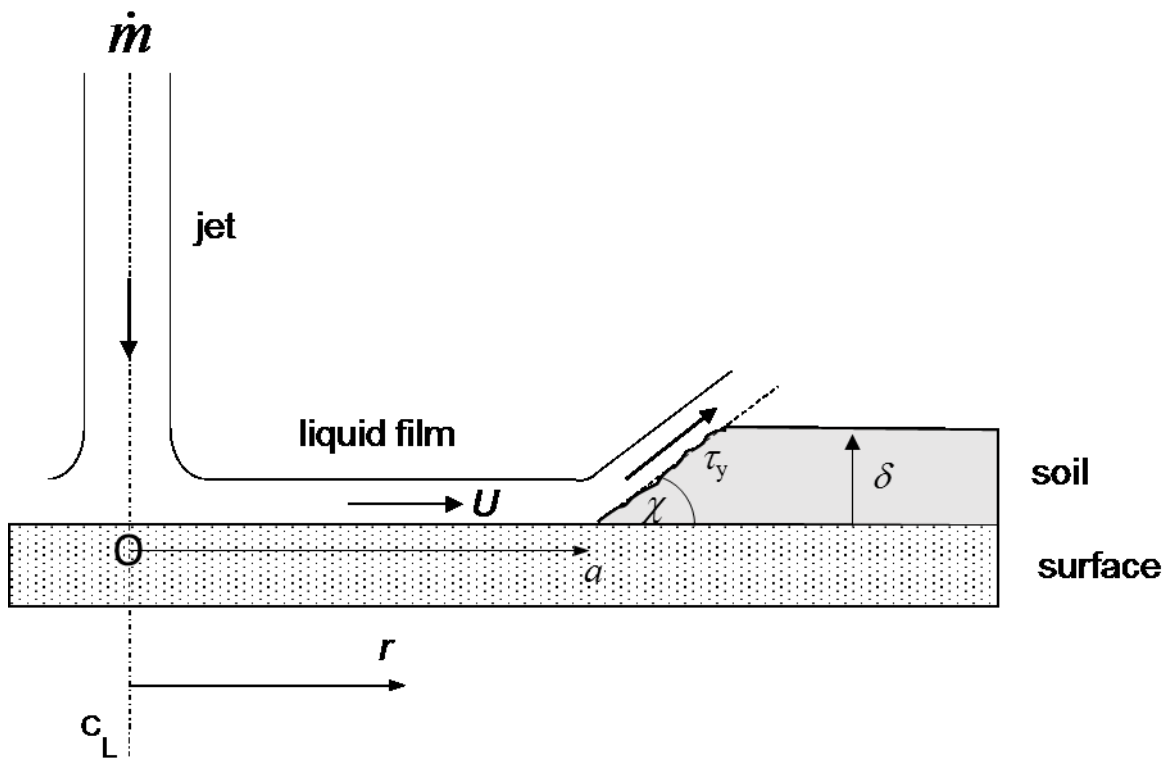
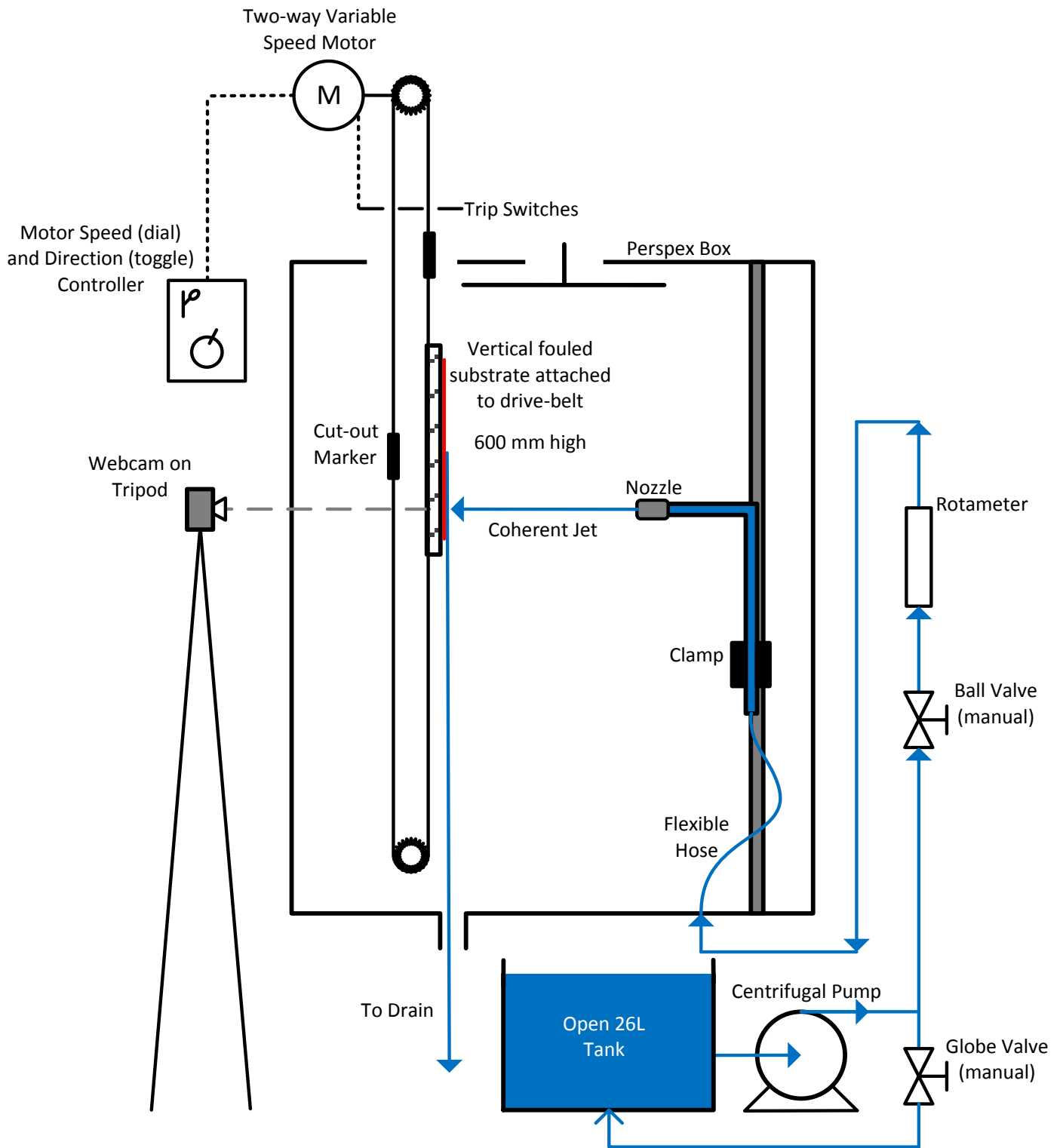
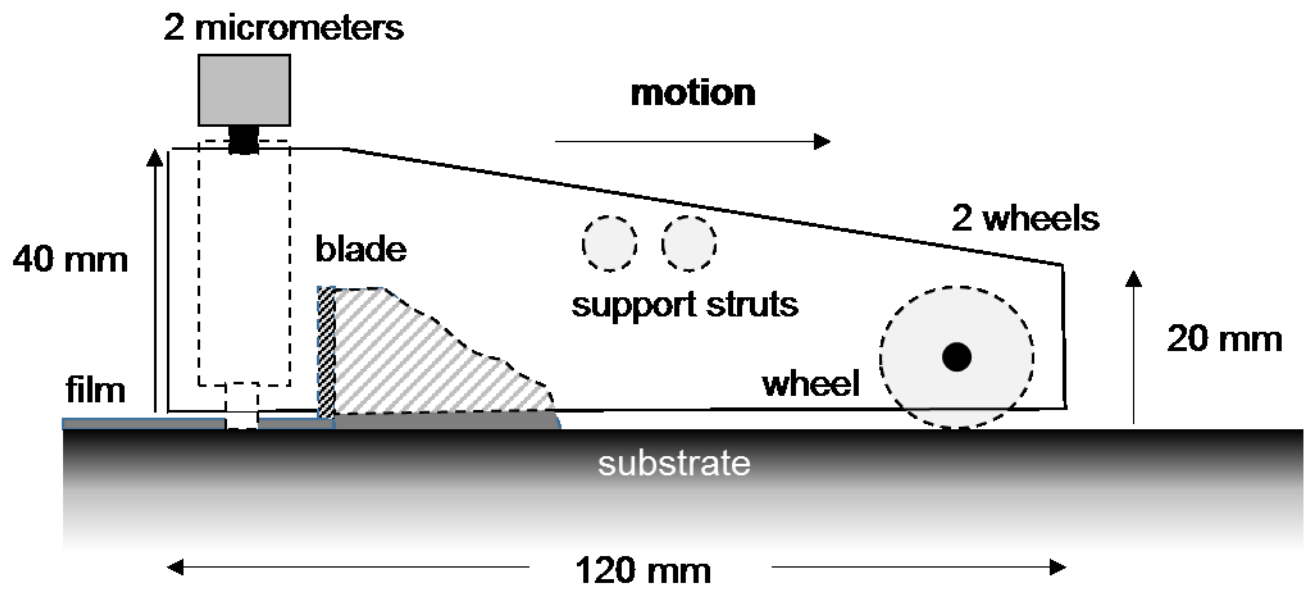


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(a)



(b)

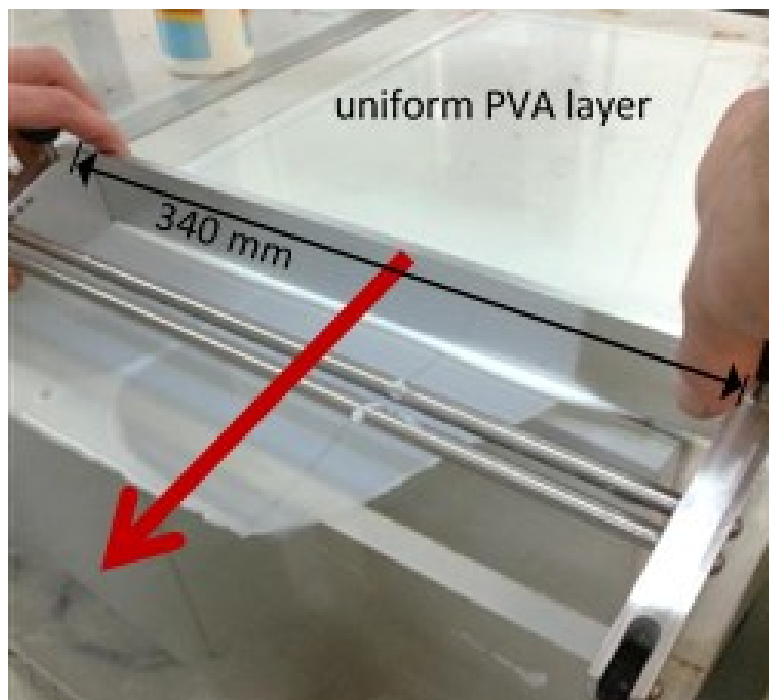
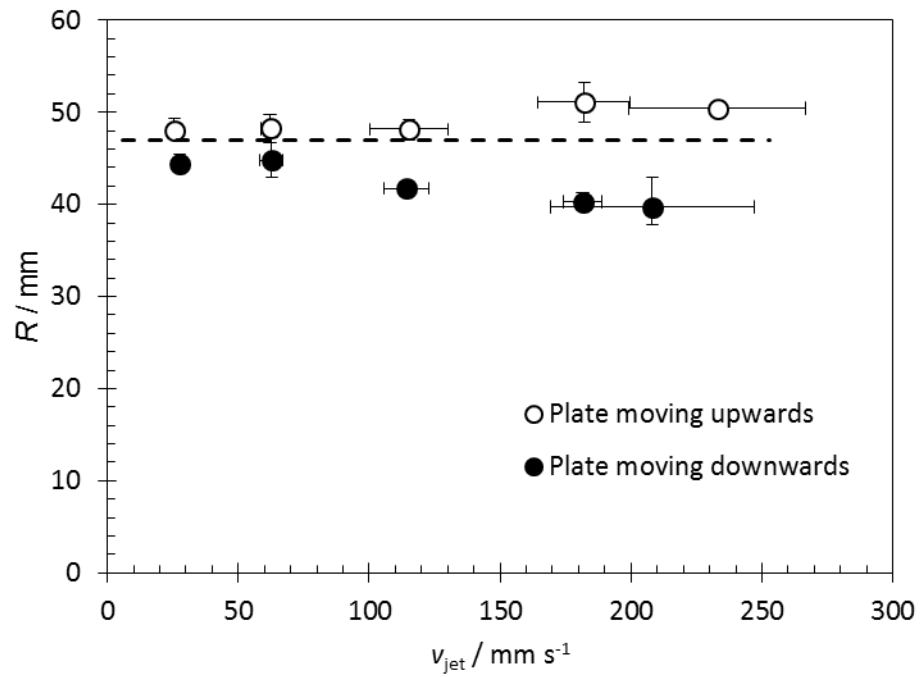


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(a)



(b)

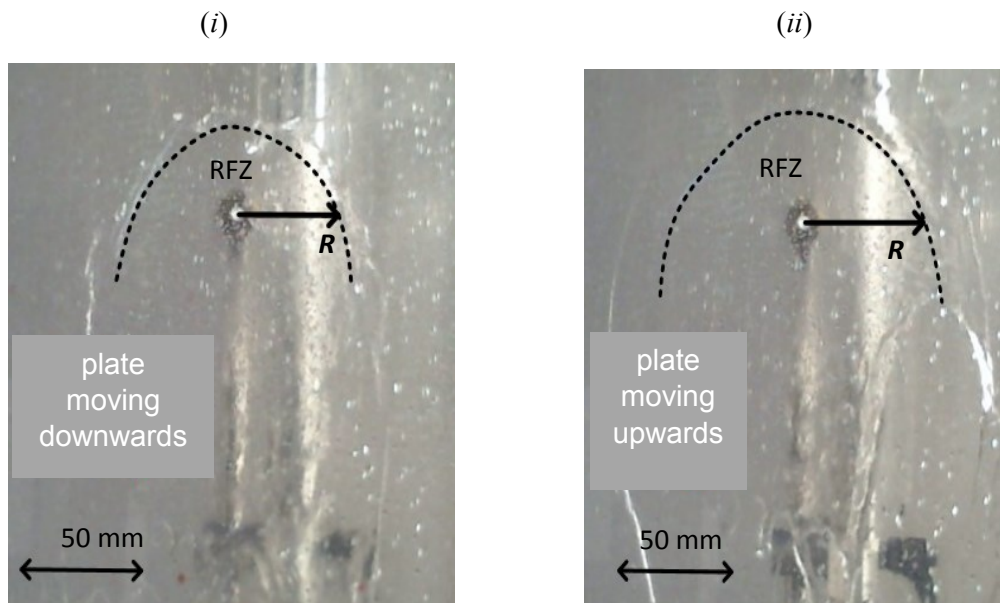


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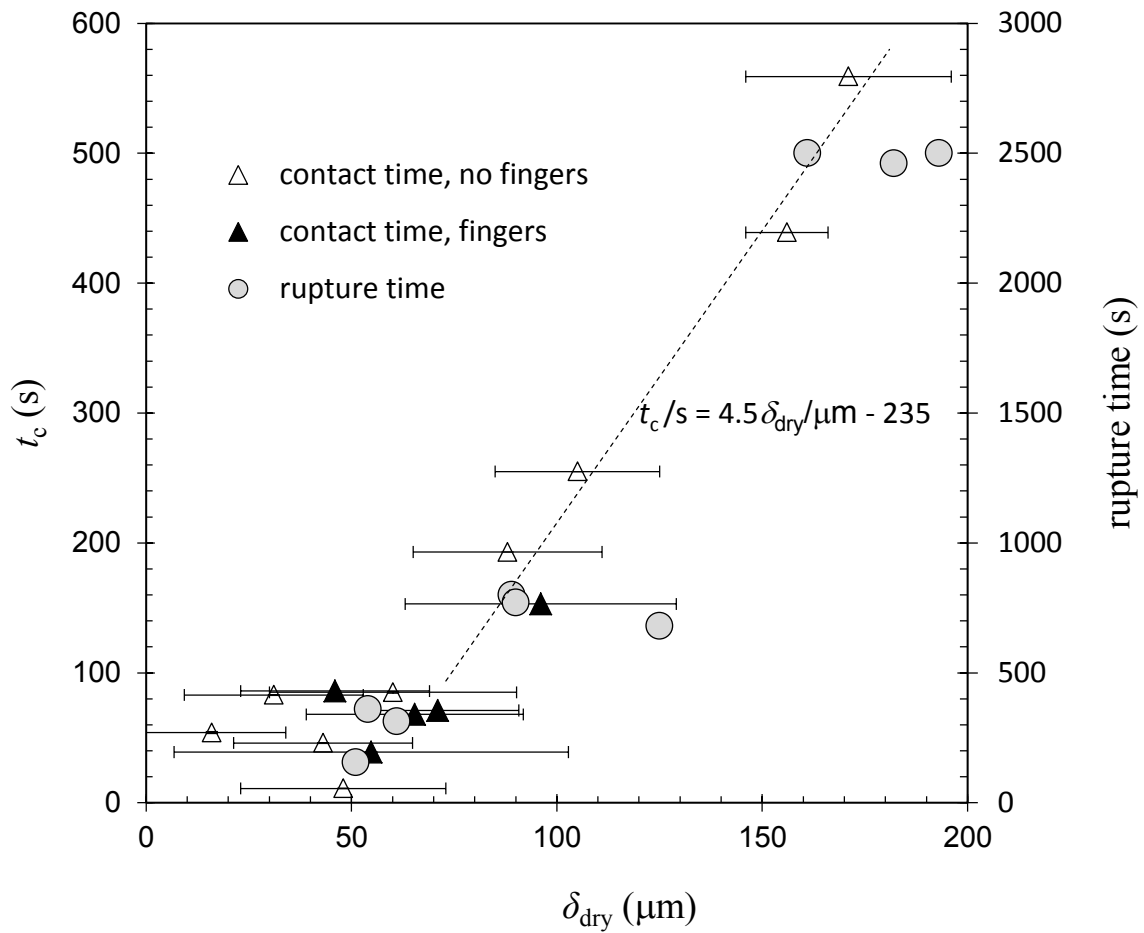


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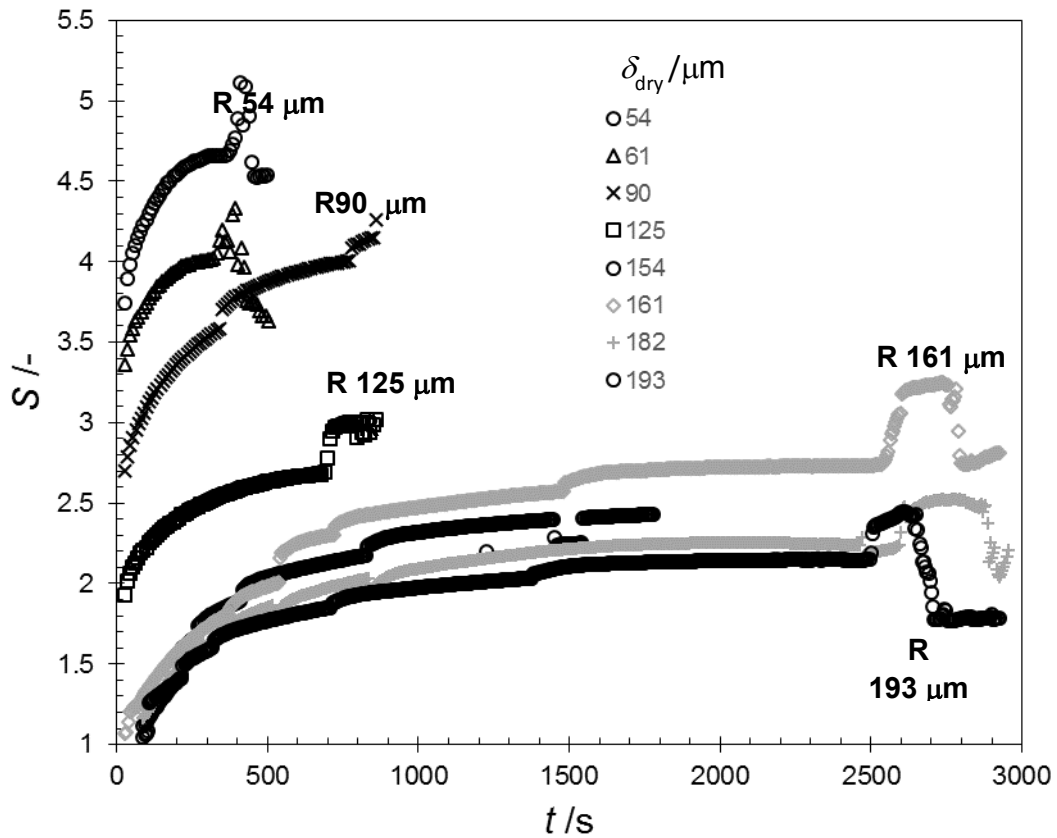


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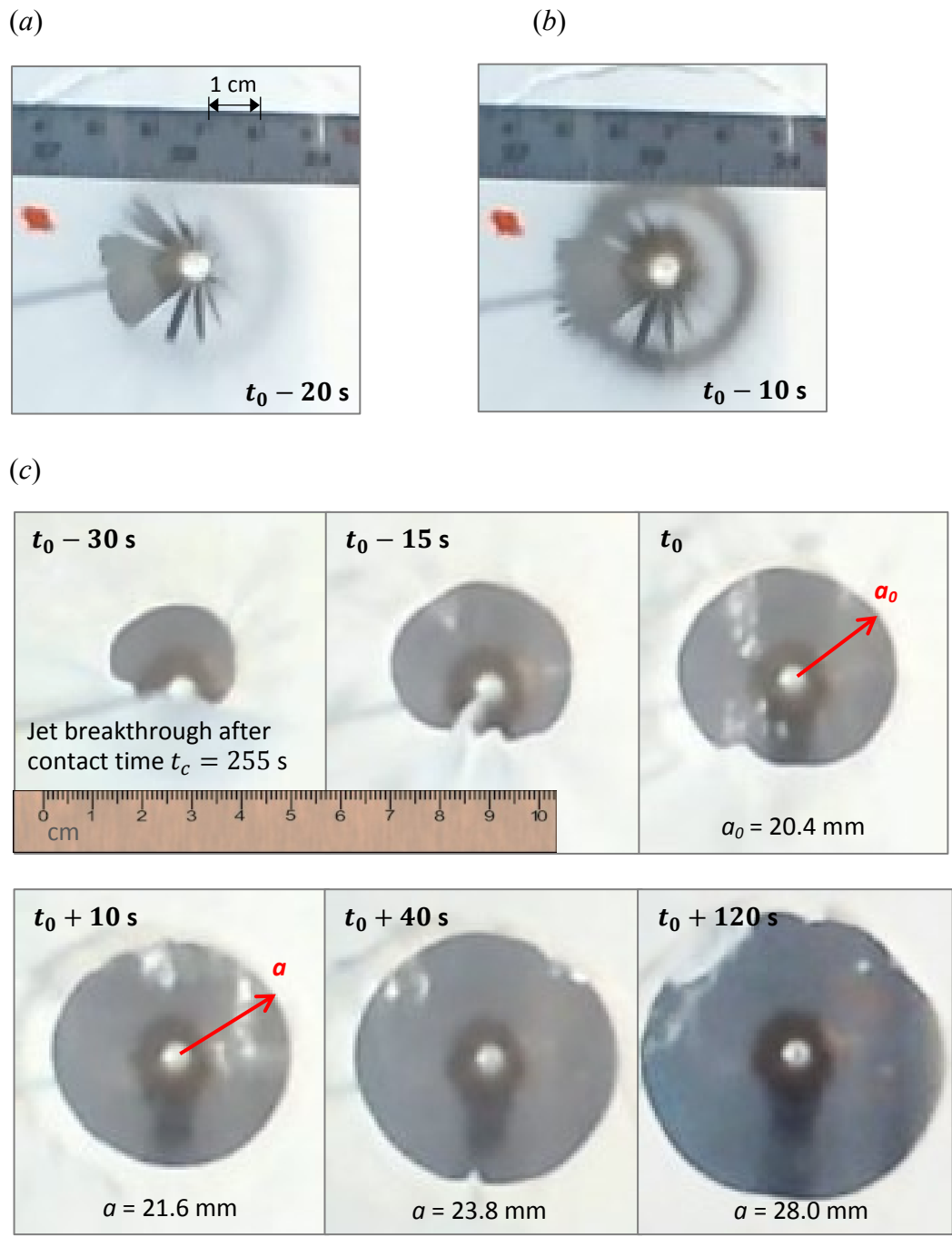


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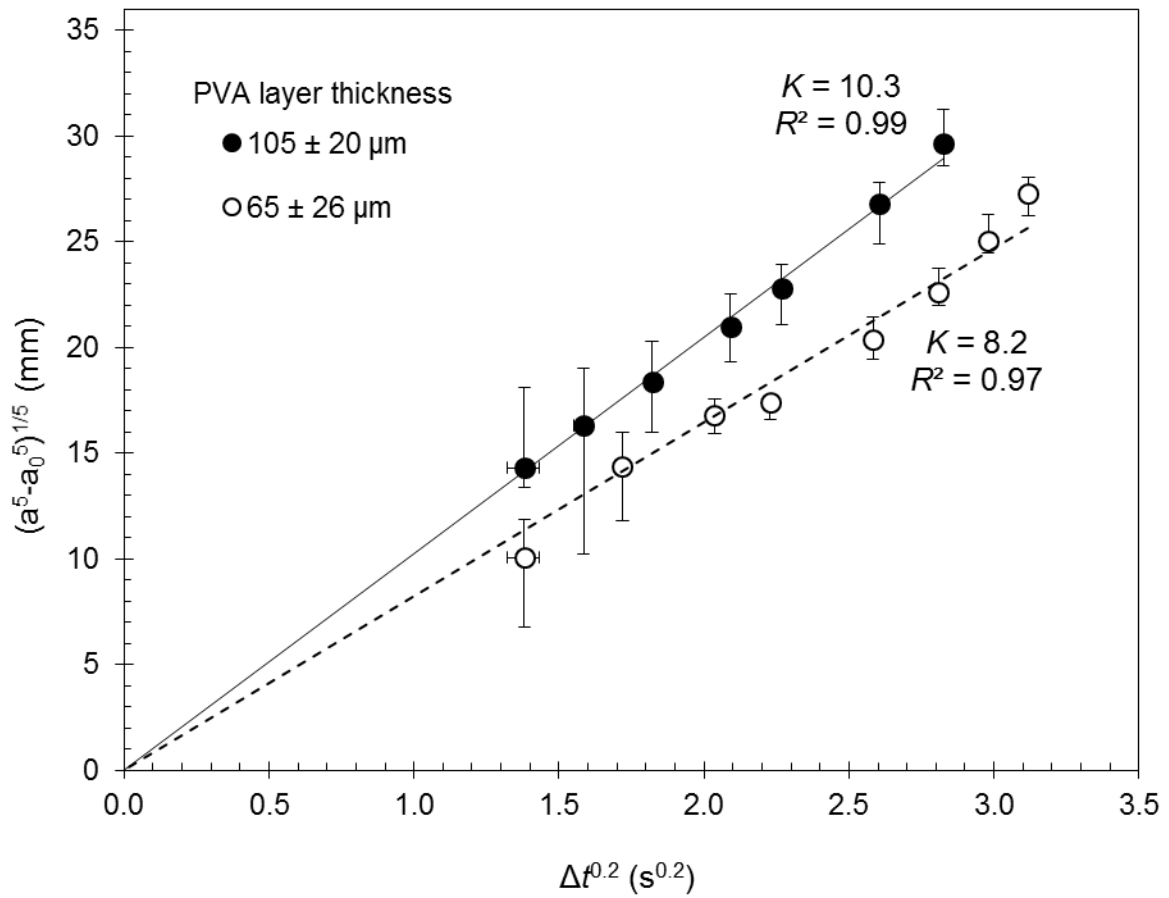


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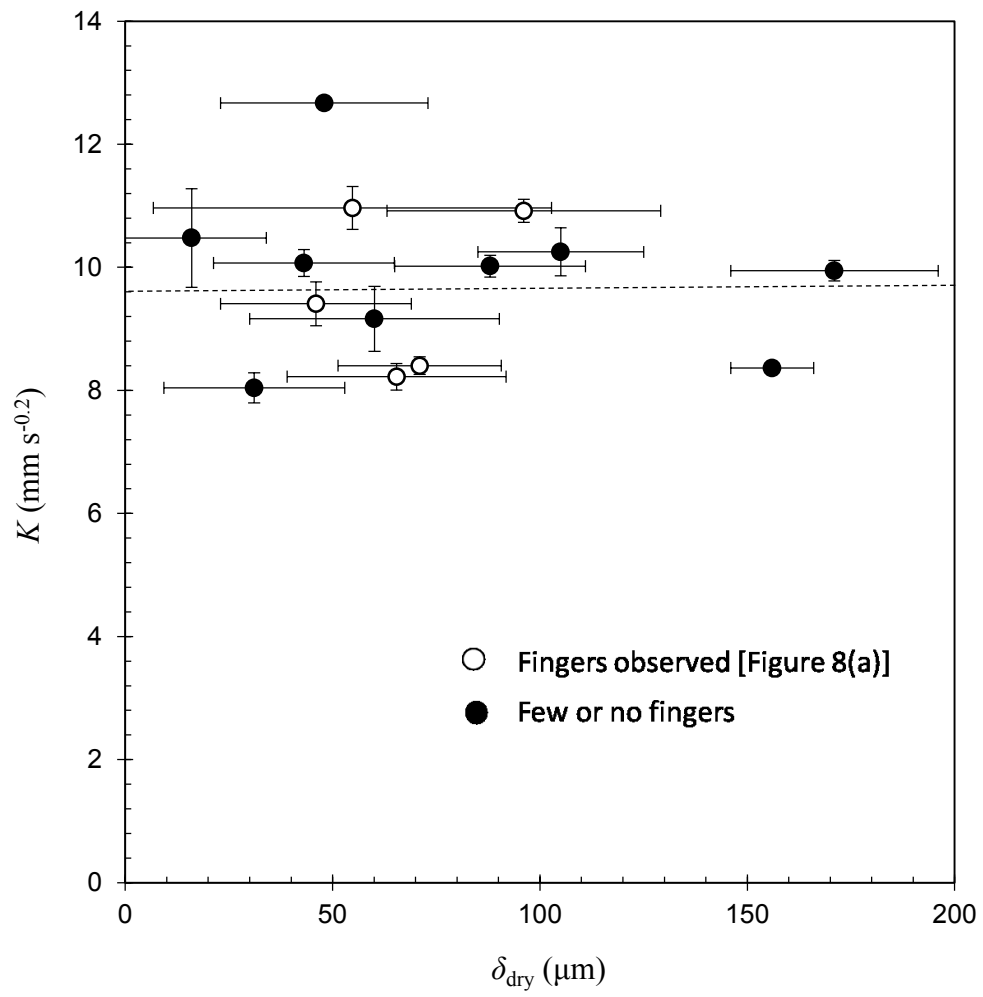


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(a)



(b)



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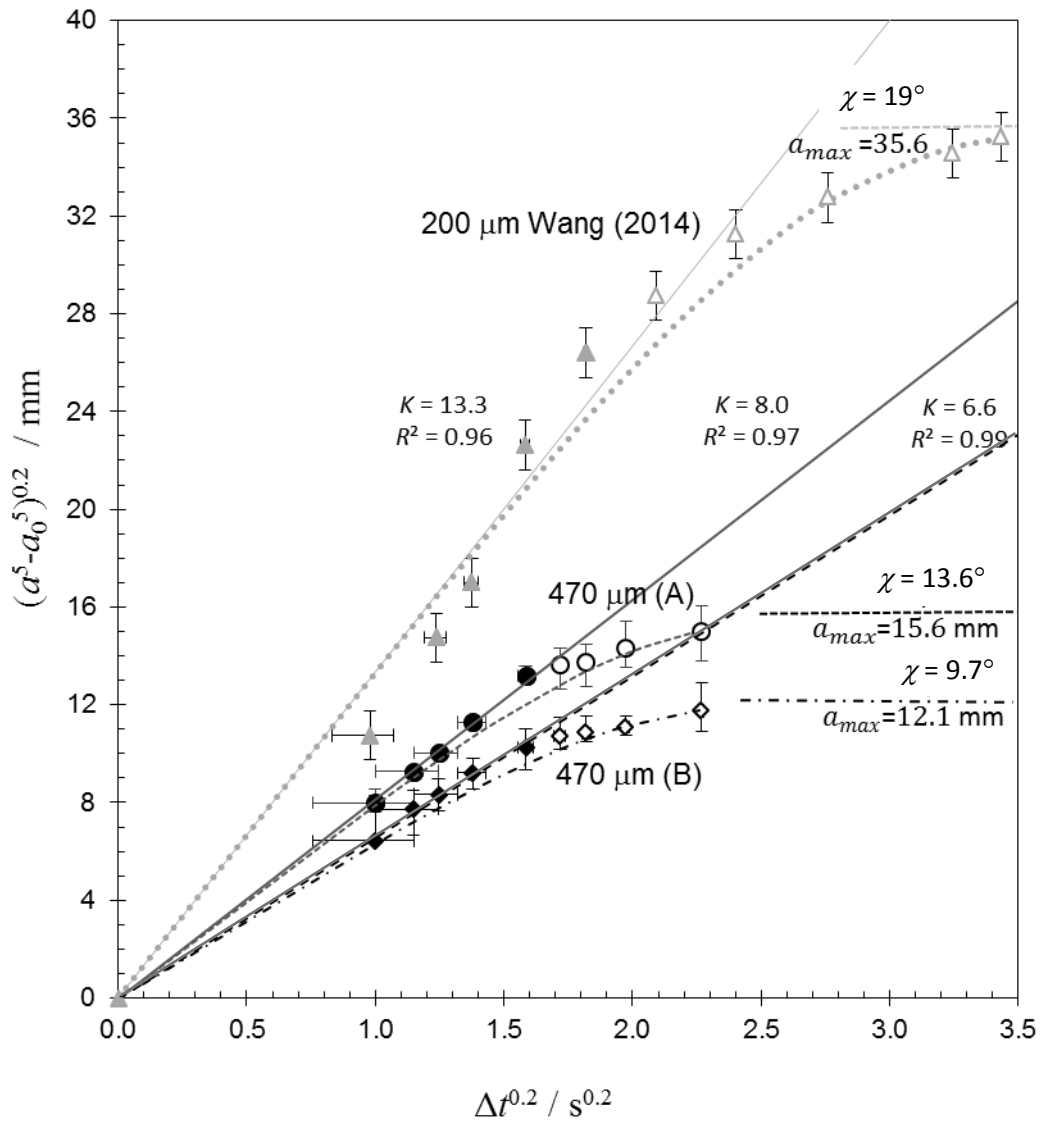


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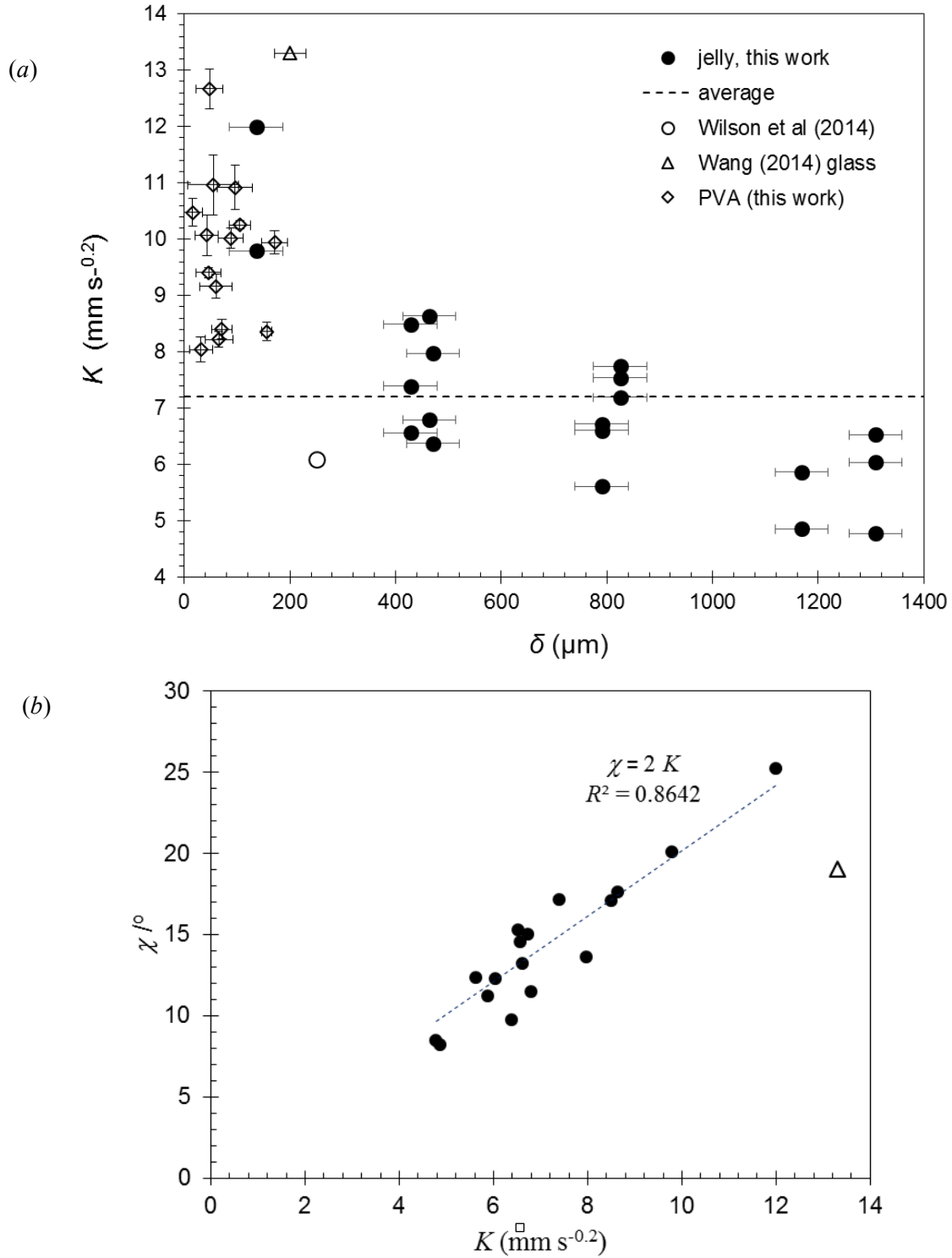


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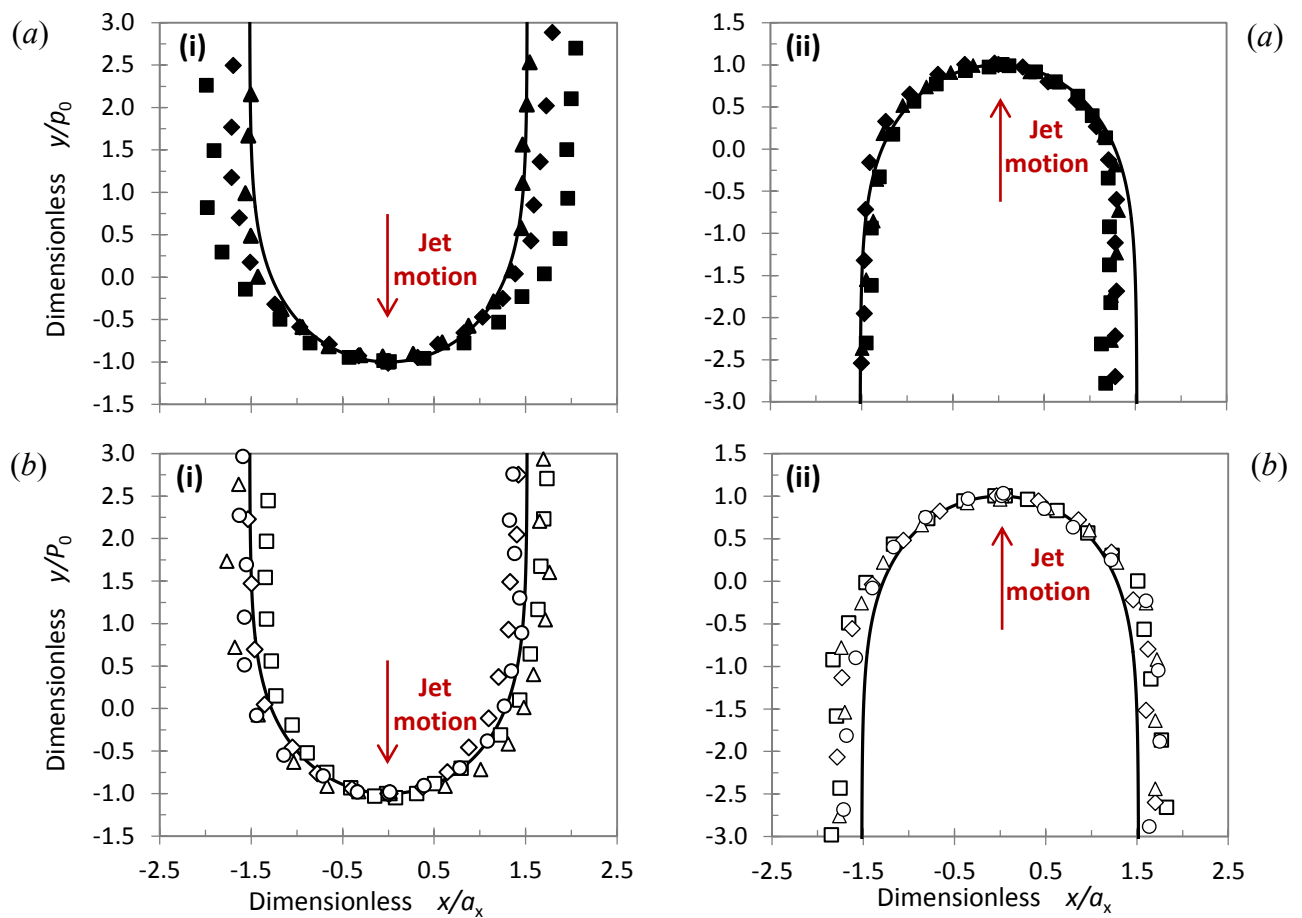


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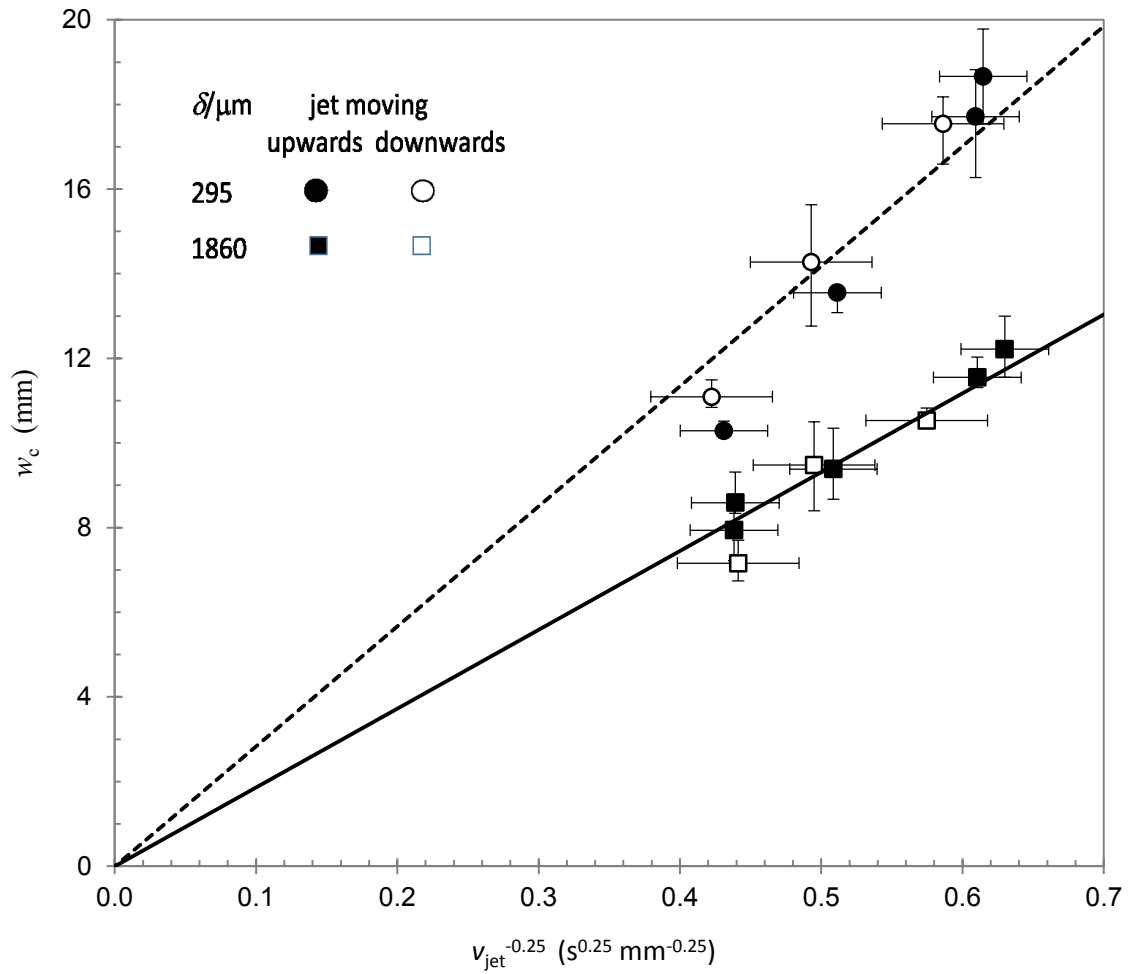


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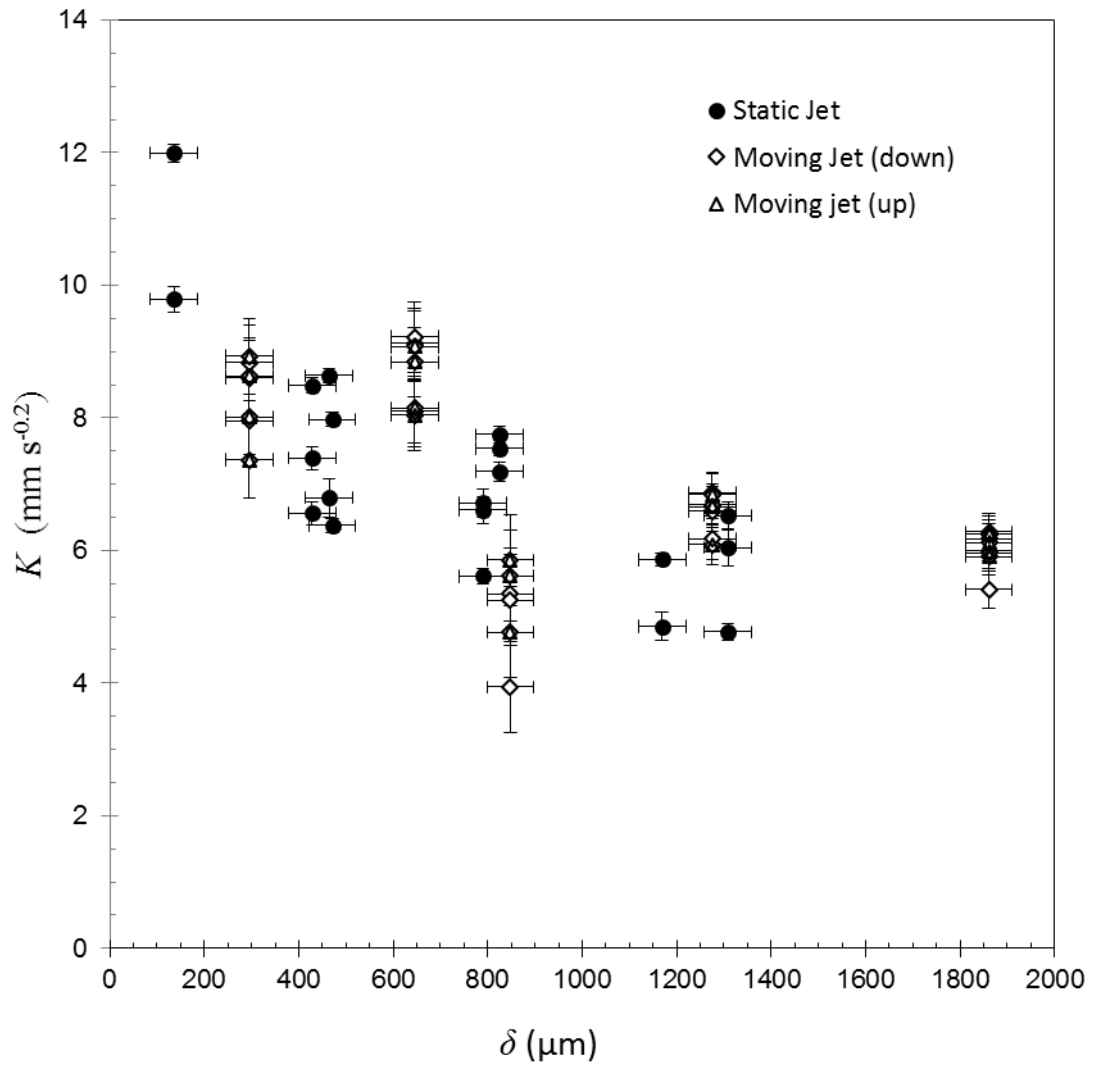
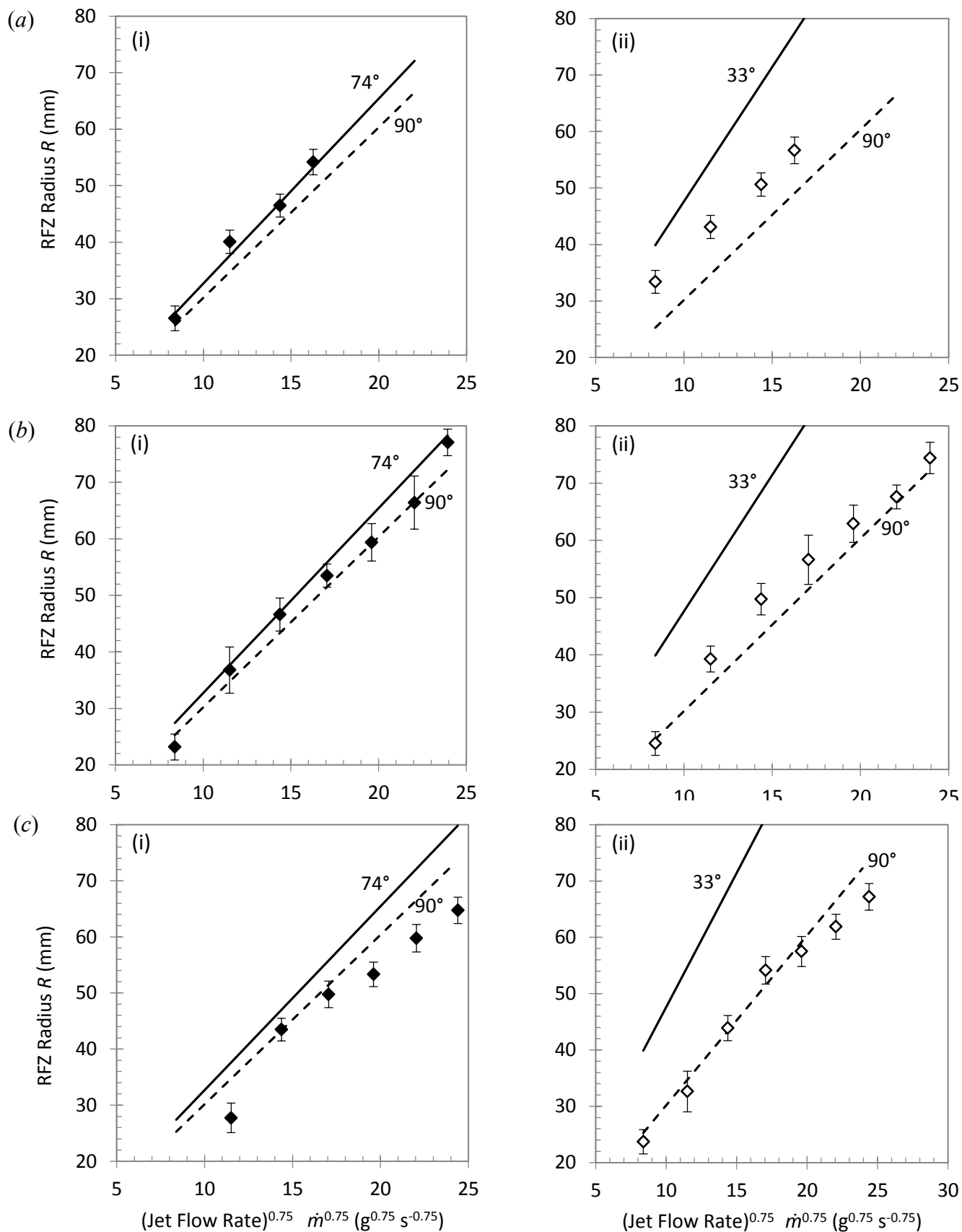


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