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Density, molar volume and surface tension of liquid Al-Ti

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24 **Abstract**

25 Al-Ti based alloys are of enormous technical relevance due to their specific properties. For
26 studies in atomic dynamics, surface physics and industrial processing the precise knowledge
27 of the thermophysical properties of the liquid phase is crucial. In the present work, we
28 systematically measure mass density, ρ [gcm^{-3}], and the surface tension, γ [Nm^{-1}], as
29 functions of temperature, T , and compositions of binary Al-Ti melts. Electromagnetic
30 levitation in combination with the optical dilatometry method is used for density
31 measurements and the oscillating drop method for surface tension measurements. It is found
32 that, for all compositions, density and surface tension increase linearly upon decreasing
33 temperature in the liquid phase. Within the Al-Ti system we find the largest values for pure
34 titanium and the smallest for pure aluminum, which amount to $\rho_{(\text{L,Ti})} = 4.12 \pm 0.04 \text{ gcm}^{-3}$ and
35 $\gamma_{(\text{L,Ti})} = 1.56 \pm 0.02 \text{ Nm}^{-1}$ and $\rho_{(\text{L,Al})} = 2.09 \pm 0.01 \text{ gcm}^{-3}$ and $\gamma_{(\text{L,Al})} = 0.87 \pm 0.06 \text{ Nm}^{-1}$,
36 respectively. The data are analyzed concerning the temperature coefficients, ρ_T and γ_T , excess
37 molar volume, V^E , excess surface tension, γ^E , and surface segregation of the surface active
38 component, Al. The results are compared with thermodynamic models. Generally, it is found
39 that Al-Ti is a highly nonideal system.

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46 **Keywords**

47 Al-Ti-alloys, density, surface tension, electromagnetic levitation, Butler model, Chatain
48 model

49 **Table with used symbols**

ρ	mass density (g/cm ³)
ρ_L	mass density at liquidus (g/cm ³ /K)
ρ_T	temperature coefficient of mass density (10 ⁻⁴ g/cm ³ /K)
ρ_i	mass density of component <i>i</i> (g/cm ³)
γ	surface tension (N/m)
γ_L	surface tension at liquidus (N/m)
γ_T	temperature coefficient of surface tension(10 ⁻⁴ N/m/K)
γ_i	surface tension of component <i>i</i> (N/m)
<i>T</i>	temperature (K (°C))
<i>T_L</i>	liquidus temperature (K (°C))
<i>T_{L,Ti}</i>	liquidus temperature of Ti (K (°C))
<i>T_{L,Al}</i>	liquidus temperature of Al (K (°C))
<i>V^E</i>	excess molar volume (cm ³ /mol)
<i>V</i>	molar volume (cm ³)
<i>V_i</i>	molar volume of component <i>i</i>
<i>V^{ideal}</i>	molar volume of an ideal solution (g/cm ³ /mol)
γ^E	excess surface tension (N/m/mol)
γ^{ideal}	surface tension of an ideal solution (N/m/mol)
β	thermal volume expansion coefficient
<i>i, j</i>	chemical species (Al or Ti)
<i>x^B_i</i>	mole fraction of component <i>i</i> in the bulk (at.-%)
<i>X^S_i</i>	mole fraction of component <i>i</i> in the surface (at.-%)
<i>M_i</i>	molar mass of component <i>i</i> (g/mol)
<i>^vV</i>	Redlich-Kister volume parameter of <i>v</i> -th order (cm ³ /mol)
<i>^vC</i>	Redlich-Kister volume parameter of <i>v</i> -th order (cm ³ /mol) at 0 K
<i>^vD</i>	linear temperature coefficient of Redlich-Kister volume parameter of <i>v</i> -th order (10 ⁻⁴ cm ³ /mol/K)
<i>R</i>	universal gas constant (8.314 kJ/K/mol)
<i>A</i>	molar surface area (m ² /mol)
<i>A_i</i>	partial molar surface area of pure liquid <i>i</i> (m ² /mol)
<i>^EG</i>	excess free energy (J /mol)

E_i^B	partial excess free energy of component i in the bulk (kJ/mol)
E_i^S	partial excess free energy of component i in the surface (kJ/mol)
f	geometrical factor
N_{Av}	Avogadro constant ($6.023 \cdot 10^{23} \text{ mol}^{-1}$)
ξ	factor accounting for a reduced coordination number in the surface
k	number of surface layers in the Chatain model
n	index of surface layer in the Chatain model
$x_i^{(n)}$	mole fraction of component i in the n -th surface layer
z	coordination number
z_l	lateral coordination number
z_v	vertical coordination number
$\Phi_{i,j}$	single bond energy for a bond between atoms i and j (J/mol)
ω	regular solution constant (J/mol)
${}^\nu L$	Redlich-Kister coefficient of ν -th order for the free energy (J/mol)
${}^\nu u(T)$	Redlich-Kister coefficient of ν -th order for the surface tension (N/m/mol)
T_P	pyrometer signal (K)
$T_{L,P}$	pyrometer signal at liquidus (K)
Rd	droplet radius (m)
φ	azimuthal angle
a_l	l -th edge curve coefficient
P_l	l -th Legendre polynomial
l	index
V_P	droplet volume in pixel units (pixel ³)
${}^{\text{drop}}V$	real droplet volume (cm ³)
q	scaling factor (cm ³ /pixel ³)
Ω	mean translational frequency (s ⁻¹)
ω_x	translational frequency in x-direction (s ⁻¹)
ω_y	translational frequency in y-direction (s ⁻¹)
ω_z	translational frequency in z-direction (s ⁻¹)
ω_m	surface oscillation frequency of mode m (s ⁻¹)
g	gravitational acceleration (N/m ²)
R_0	radius of the sample with spherical shape (m)
$p_{O_2}^S$	partial pressure of oxygen in the vicinity of the surface (Pa)

K	equilibrium constant (J/mol)
$p_{\text{O}_2}^{\text{Ch}}$	partial pressure of oxygen in the chamber (Pa)
D_{O}	diffusion constant of oxygen in the vapor (m^2/s)
D_{Ox}	diffusion constant of oxide in the vapor (m^2/s)

50 **1. Introduction**

51 *1.1. Al-Ti*

52 The increasing need for more sophisticated materials in various high-temperature applications
53 can potentially be satisfied by using Ti-based intermetallics. Even at elevated temperatures, γ -
54 Al-Ti alloys combine a low density with a high tensile strength. This makes them particularly
55 interesting for applications in the automotive or aerospace industries. For instance, they can
56 be used as turbine blades in aircraft engines or as fuselage materials.

57 In addition, $(\alpha+\beta)$ -TiAl may also be used in medical applications as bone implants, because
58 of their bio-compatibility and corrosion resistance. They also exhibit comparatively low
59 densities and, compared to conventional implants made of Co-Cr- or Fe-based alloys, a small
60 Young modulus of approximately 110 GPa. Compared to the Young-modulus of bones of
61 approximately 25 GPa this is still high so further optimization of the material is necessary.

62 Therefore, developing a profound understanding of the liquid phase is indispensable, as the
63 vast majority of materials are directly produced from the melt by casting [1]. Among the
64 properties relevant in this context, density and surface tension of the liquid phase are of
65 pronounced importance.

66 Density is a fundamental material property. Its knowledge is crucial for casting processes and
67 for determining surface tension from the measured raw data.

68 Surface tension plays a critical role for the castability of an alloy, and for the mould-filling
69 capability. The latter is often problematic in Ti-based alloys. Both properties also reveal
70 interesting academic science as they are strongly affected by processes taking place at the
71 atomic scale.

72 Despite the technical importance of density and surface tension, data on these properties of
73 Ti-based alloys are sparse. The main reason for this is the high chemical reactivity of liquid Ti

74 paired with a large solubility of oxygen. This renders its investigation with conventional
75 techniques extremely difficult. Nevertheless, there are containerbased methods, that have been
76 used to investigate thermophysical properties of pure Ti and binary and multicomponent Al-
77 Ti alloys, including the pendant [2] and sessile drop method [3]. Common methods for the
78 determination of density and surface tension are listed in Table 1. The sessile drop method is
79 applied to calculate the surface tension of a sessile drop, using the equilibrium dependence
80 between the forces of surface tension and gravity. Additionally, density can be obtained from
81 the drop profile by assuming axis-symmetry. When dealing with extremely reactive systems,
82 such as Al-Ti, the difficulty of that method lies in finding an adequate inert substrate material
83 that shows negligible interactions with the sample [2]. In the case of the pendant drop similar
84 theoretical approaches are applied on liquid droplets, which are squeezed through a capillary.
85 The advantage of the pendant drop method is that the contact of the sample with the capillary
86 stays relatively short compared to the substrate contact [3]. Literature data on Ti and
87 industrially used multicomponent alloys, such as $Al_{46}Ti_{46}X_8$, $X=Nb, Ta$ and $Al_6Ti_{90}V_4$, along
88 with their density and surface tension data are published in Refs. [1,4-23].

89 Typically, the main purpose of these investigations is the creation and completing of materials
90 databases. However, if a detailed understanding of the system is envisaged, one must, perform
91 measurements in which the composition is systematically varied [24].

92 The binary system Al-Ti is a good starting point for such investigations. To understand
93 multicomponent systems, their binary basis must firstly be understood. Surprisingly, even for
94 the binary system Al-Ti, data exist only in exceptional cases, such as for $Al_{80}Ti_{20}$ [25].

95 Therefore, the goal of the present work is to deliver systematically measured density and
96 surface tension data on binary liquid Al-Ti alloys. Using electromagnetic levitation avoids
97 pollution of the materials due to reactions with the container walls. Thus, the negative effects
98 of the high chemical reactivity of the material are minimized. However, the interactions with

99 residual gas components of the surrounding environment (gas or vacuum) can still not be
100 excluded. In particular, the role of oxygen needs to be discussed.

101 Density and surface tension measurements using levitation methods have been performed by
102 us in the past on Al-based systems and systems containing Ti, such as Cu-Ti [26, 27], Al-Ni
103 [24,28,29], Al-Cu [30,31], Al-Cu-Ag [32,33], Al-Ag [32,33], Al-Fe [24,28,29], Al-Au
104 [34,35], Al-Si [36,37] and Al-Cu-Si [38]. The formalisms used for the interpretation and
105 discussion of the measured data are described in the following.

106

107 *1.2 Density, molar volume, and thermal expansion*

108 Within a limited temperature interval including the liquidus point, the density $\rho(T)$ of a liquid
109 metal can be considered as a linear function of temperature, T :

$$110 \quad \rho(T) = \rho_L + \rho_T(T - T_L) \quad (1)$$

111 In this Equation, ρ_L is the density at the liquidus temperature, T_L , and ρ_T is the constant
112 temperature coefficient $\partial\rho/\partial T$. The volume expansion coefficient,

113 $\beta = V^{-1}(\partial V/\partial T)$, with V , being the molar volume of the liquid, ρ_T can be expressed as [24]

$$114 \quad \rho_T = -\beta \cdot \rho_L \quad (2)$$

114 For a binary solution of components i ($i = \text{Al, Ti}$), with respective mole fractions x_i^B and
115 molar masses M_i , the molar volume of the solution, $V = \rho^{-1} \sum x_i^B M_i$, is generally represented by
116 [24]:

$$117 \quad V = V^i + V^E, \quad (3)$$

with:

$$118 \quad V^{\text{ideal}} = \sum_{i=\text{Al}}^{\text{Ti}} x_i^B \frac{M_i}{\rho_i} \quad (4)$$

118 Where ρ_i is the density of the pure substance i at temperature T . V^E is the excess volume and
119 the index “B” of the mole fraction marks the amount of element i in the bulk.

120 For $V^E=0$, Eq. (3) reduces to a simple linear combination of the molar volumes of the pure
 121 liquid elements, $V_i=M_i/\rho_i$, and is designated as “ideal”.

122 Generally, V^E depends on the temperature and the mole fraction. A simple expression of V^E is
 123 given by the following Redlich-Kister-type-Ansatz [24]:

$$V^E = x_{Al}^B x_{Ti}^B \left(\sum_{v=0}^{\infty} {}^vV(T) (x_{Al}^B - x_{Ti}^B)^v \right) \quad (5)$$

124 The parameters ${}^vV(T)$ represent the interaction between the elements Al and Ti in the alloy
 125 melt. As a first approximation, these parameters can be assumed to be linear functions of
 126 temperature with parameters ${}^vC = {}^vV(0 \text{ K } (-273.15 \text{ } ^\circ\text{C}))$ and $D^v = \partial {}^vV / \partial T$:

$${}^vV(T) = {}^vC + {}^vDT \quad (6)$$

127

128 1.3 Surface tension

129 As for the density, the surface tension $\gamma(T)$ can be expressed as a linear function of
 130 temperature, provided that the temperature interval considered is sufficiently small:

$$\gamma(T) = \gamma_L + \gamma_T(T - T_L) \quad (7)$$

131 In this equation, γ_L is the surface tension at the liquidus temperature, T_L , and γ_T is the constant
 132 temperature coefficient. In order to quantitatively compare measured surface tension data with
 133 approximated model calculations by Butler [39], the liquid surface is considered as a
 134 monolayer of atoms. The layer is regarded as an individual thermodynamic phase being in
 135 equilibrium with the bulk. If x_i^S is the mole fraction of element i in the surface layer, γ can be
 136 calculated by solving the following set of equations known as the Butler equation [39]:

$$\begin{aligned} \gamma &= \gamma_{Al} + \frac{RT}{A_{Al}} \ln \left(\frac{x_{Al}^S}{x_{Al}^B} \right) + \frac{1}{A_{Al}} \left({}^E G_{Al}^S(T, x_{Al}^S, x_{Ti}^S) - {}^E G_{Al}^B(T, x_{Al}^B, x_{Ti}^B) \right) \\ &= \gamma_{Ti} + \frac{RT}{A_{Ti}} \ln \left(\frac{x_{Ti}^S}{x_{Ti}^B} \right) + \frac{1}{A_{Ti}} \left({}^E G_{Al}^S(T, x_{Al}^S, x_{Ti}^S) - {}^E G_{Al}^B(T, x_{Al}^B, x_{Ti}^B) \right) \end{aligned} \quad (8)$$

137 Here, R is the universal gas constant, and ${}^E G_i^B$ and ${}^E G_i^S$ denote the respective partial excess
 138 free energies of component i in the bulk and in the surface layer. A_i is the partial molar surface

139 area of pure liquid i , approximated by the following expression from the molar volumes of the
 140 pure elements V_i :

$$A_i = fV^{2/3}N_{Av}^{1/3} \quad (9)$$

141 In Eq. (9) N_{Av} is the Avogadro number, and f is a geometrical factor. The value of f depends
 142 on the structures assumed for the surface and the bulk. For liquids, the commonly used value
 143 of 1.09 has recently been regarded as too high [40]. A more reasonable value of $f = 1.0$ has
 144 been proposed by Kaptay [40] which is also used in the present work.

145 The main assumption of the Butler model is the approximation of the surface excess free
 146 energy ${}^E G_i^S(T, x_i)$ by ${}^E G_i^S(T, x_i) = \xi {}^E G_i^B(T, x_i)$, where the factor ξ accounts for the reduced
 147 coordination of atoms in the surface layer. It can be approached as the ratio of the respective
 148 coordination numbers of atoms in the surface and the bulk. A constant value of 0.75 was
 149 initially suggested by Tanaka and Iida [41] as default approximation for liquids with unknown
 150 structure. Later, they adjusted this value to 0.83 [42]. In this study, however, we use 0.75 in
 151 order to comply with the Chatain model that is also applied. Solving Eq. (9) yields the surface
 152 tension of the alloy and the concentration in the surface layer, x_i^S .

153 The Butler model may be criticized for its restriction to consider the surface as a phase of a
 154 single monolayer, neglecting concentration gradients perpendicular to the surface. On the
 155 other hand, as shown recently, [43], this phase does not necessarily need to be a mono-layer,
 156 as originally stated by Butler.

157 A different approach is followed by the Chatain model [44, 45] taking into account a
 158 concentration gradient as multiple layers, $n=1 \dots k$, with different compositions, $x_i^{(n)}$, in each
 159 layer, n . The atoms of the liquid are assumed to reside on cubic lattice sites with a
 160 coordination number, $z=12$, in the bulk, and a lateral coordination number, $z_l=6$. The number
 161 of neighboring atoms in an adjacent atom layer is, thus, $z_v=3$. Interactions among atoms take
 162 place only with the nearest neighbors, where, $\Phi_{i,j}$ denotes a single bond energy for a bond

163 between atoms i and j . With this parameter the regular solution constant, ω , can be defined in
 164 Ref. [43] as $\omega = \Phi_{Al,Ti} - 0.5(\Phi_{Al,Al} + \Phi_{Ti,Ti})$. Assuming further that $\gamma_i = -z_v \Phi_{i,i}/2A$, the following
 165 expression is obtained for the surface free energy of a regular solution [43]:

$$\begin{aligned}
 A\gamma &= A\gamma_{Al}x_{Al}^{(1)} + A\gamma_{Ti}x_{Ti}^{(1)} \\
 &- z_v\omega(x_{Ti}^{(1)} - 2x_{Ti}^B x_{Ti}^{(1)} - (x_{Ti}^B)^2) - z_v\omega \sum_{n=1}^k (x_{Ti}^{(n)} - x_{Ti}^B)(x_{Al}^{(n)} - x_{Al}^B) \\
 &- z_v\omega \sum_{n=1}^k (x_{Ti}^{(n)} - x_{Ti}^B)^2 \\
 &+ RT \sum_{n=1}^k \left[x_{Ti}^{(n)} \ln\left(\frac{x_{Ti}^{(n)}}{x_{Ti}^B}\right) + x_{Al}^{(n)} \ln\left(\frac{x_{Al}^{(n)}}{x_{Al}^B}\right) \right]
 \end{aligned} \tag{10}$$

166 The parameters $\Phi_{i,i}$ and ω are related to the surface tension and the excess free energy,
 167 respectively, as follows:

$$\Phi_{i,i} = -A\gamma_i \tag{11}$$

168 And

$$\omega = -\frac{T^2}{z \cdot x_{Al}^B x_{Ti}^B} \frac{\partial}{\partial T} \left(\frac{{}^E G(T)}{T} \right) \tag{12}$$

169 The excess free energy, ${}^E G$, used in Eqs. (8) and (10) is parametrized by a Redlich-Kister
 170 polynomial, as a function of concentration and temperature, with ${}^v L_{Al,Ti}(T)$ being temperature
 171 dependent interaction parameters:

$${}^E G(T, x_{Al}, x_{Ti}) = x_{Al} x_{Ti} \sum_{v=0} {}^v L_{Al,Ti}(T) (x_{Al} - x_{Ti})^v \tag{13}$$

172 For a binary ideal solution, ${}^E G=0$, the following expressing is obtained for its surface tension
 173 γ^{ideal} [46]:

$$\gamma^{ideal}(T) = x_{Al}^S \gamma_{Al}(T) + x_{Ti}^S \gamma_{Ti}(T) \tag{14}$$

174 The deviation from the ideal surface tension, γ^{ideal} , is called excess surface tension, γ^E as:

$$\gamma = \gamma^{ideal} + \gamma^E \tag{15}$$

175 With this formalism, similar that one for the excess molar volume in section 1.2, γ^E may also
 176 be fitted analogously to a second order Redlich-Kister polynomial, with ${}^v u(T)$ being
 177 temperature-dependent interaction parameters:

$$\gamma^E = x_{Al}^B x_{Ti}^B \left(\sum_{v=0}^N {}^v u(T) (x_{Al}^B - x_{Ti}^B)^v \right) \quad (16)$$

178

179 2. Experimental

180 Density and surface tension measurements are conducted in an electromagnetic levitation
 181 chamber described in detail in Ref. [47]. Typically, the alloy samples have diameters of 3 mm
 182 and masses of approximately 0.5 g. Inside the chamber the samples are positioned and melted
 183 by a spatially inhomogeneous electromagnetic field. This field is generated by a coil to which
 184 an alternating current of 100 A is applied with a frequency of approximately 250 kHz.

185 Processing takes place under protective inert gas mixtures of He and Ar (both having a purity
 186 of 99.9999 %). Since, for electromagnetic levitation, positioning and heating are not generally
 187 decoupled, additional temperature control is provided by an adjustable cooling flow of inert
 188 gas, admitted to the samples via a nozzle.

189 The sample temperature, T , is measured using an infrared pyrometer directed to the specimen
 190 from the side. As the effective emissivity is not known in general, the pyrometer signal, T_P ,
 191 needs to be recalibrated with respect to the known liquidus temperature, T_L , and the apparent
 192 liquidus temperature, $T_{L,P}$. The apparent liquidus temperature is identified during the
 193 measurement by a kink in the pyrometer signal that appears, when the melting process is
 194 completed. The recalibration is accomplished using the following relation derived from

195 Wien's law [48]:

$$\frac{1}{T} - \frac{1}{T_P} = \frac{1}{T_L} - \frac{1}{T_{L,P}} \quad (17)$$

196 For metallic liquids, Eq. (17) gives a good approximation for the temperature, provided that
 197 the sample emissivity at the operating wavelength remains constant over the investigated

198 temperature interval [49]. For the pure elements and alloys, values of T_L are shown in
199 Tables 2, 3, 4 and 5 and taken from Ref. [50], using the CALPHAD approach to evaluate
200 thermodynamic data. We have chosen the data as the used model is taking into account recent
201 experimental data and is in close agreement with these data [50]. The phase diagram of the
202 binary system of Al-Ti is shown in Fig. 1, respectively.

203 The preparation of the specific samples is performed by arc-melting the corresponding
204 amounts of Al (99.999 %) and Ti (99.99 %). An ultrasound bath in propanol is used for
205 cleaning and the removal of scales.

206 Finally, all samples are briefly heated up to a temperature of at least T_L+100 K. This produces
207 further purification through evaporation of volatile Al-oxides.

208 The large difference in the melting temperatures of Al, 933 K (660 °C), and Ti, 1941 K (1668
209 °C), presents a challenge for the processing of the liquid alloys, due to the partially intense
210 evaporation of Al. This may cause a shift in the sample mass and its composition. These
211 effects may limit the accuracy of both density and surface tension data. Therefore, the mass
212 loss of each sample is evaluated after each measurement and, in the event that it exceeds 0.1
213 % of the initial sample mass, the results are dismissed.

214

215 *2.1 Density*

216 The optical dilatometry method [30,47,51] is used to measure density and molar volume. This
217 method employs lateral shadow images of the sample captured by a digital charge-coupled
218 device (CCD) camera. The images are analyzed by an edge detection algorithm that
219 determines the radius, Rd , with respect to the drop center and the azimuthal angle φ . The
220 obtained curve, $Rd(\varphi)$, is averaged over 1000 frames in order to eliminate the influence of
221 surface oscillations, and is then fitted by Legendre polynomials of order ≤ 6 , where the
222 brackets $\langle \dots \rangle$ denote averaging:

$$\langle Rd(\varphi) \rangle = \sum_{l=0}^6 a_l P_l(\cos(\varphi)) \quad (18)$$

223 In Eq. (18), P_l is the l -th Legendre polynomial, and a_l are coefficients determined by the fit.

224 The volume is calculated as following, assuming axial symmetry [30] of the droplet in

225 mechanical equilibrium:

$$V_P = \frac{2}{3} \pi \int_0^\pi \langle Rd(\varphi) \rangle^3 \sin(\varphi) d\varphi \quad (19)$$

226 Here, V_P denotes the volume in pixel units. The real droplet volume, ${}^{\text{drop}}V$, is related to the

227 pixel volume, V_P , by a scaling factor, q with ${}^{\text{drop}}V = qV_P$. q is obtained by a calibration

228 procedure described in Ref. [28q]. Finally, the density is calculated with respect to the sample

229 mass, M , by $\rho = M / {}^{\text{drop}}V$. Following this procedure the obtained results are accurate within

230 $\Delta\rho / \rho \leq \pm 1.0\%$ [24,30].

231

232 2.2 Surface tension

233 The oscillating droplet method [47] is applied to determine surface tension. In this method

234 spontaneously self-excited surface oscillations are observed by means of a digital

235 complementary metal oxide semiconductor (CMOS)-camera directed at the sample from

236 above. The camera has a pixel resolution of 400x400, and operates at a frequency of 400 Hz.

237 A series of $2^n = 4196$ frames is recorded for each investigated temperature and, these are

238 then analyzed afterwards with dedicated software that determines the frequency spectra of the

239 sample radii, R , from the image sequences. Under terrestrial conditions i.e. in the case of a

240 non-spherical and slightly rotating droplet the spectrum consists of five distinguished peaks,

241 at frequencies ω_m , corresponding to the surface oscillation modes, with m being a quantum

242 number from, in this case, -2 to +2 [47]. Additionally, the three translational frequencies

243 ω_x , ω_y , ω_z , can be identified from the motion of the droplets' centers of gravity, and thus

244 the mean quadratic translational frequency can be calculated as:

$$\Omega^2 = \frac{1}{3} (\omega_x^2 + \omega_y^2 + \omega_z^2) \quad (20)$$

245 From the five surface oscillations and three translational frequencies, the surface tension, γ , is
246 determined using the sum formula of Cummings and Blackburn [51], where g denotes the
247 gravitational acceleration and R_0 the radius of the sample, which is assumed to be spherical:

$$\gamma = \frac{3M}{160\pi} \sum_{m=-2}^{+2} \omega_m^2 - 1.9\Omega^2 - 0.3 \left(\frac{g}{R_0}\right)^2 \Omega^{-2} \quad (21)$$

248 This procedure allows the precise determination of the surface tension within a margin of $\Delta\gamma/\gamma$
249 $\leq 5.0\%$ [24]

250

251 **3. Results**

252 *3.1 Density*

253 Measured density data are plotted in Fig. 2, versus temperature for liquid samples with Al-
254 mole fractions x_{Al} , ranging from 0 to 100 at.-%. Each measurement is carried out over a broad
255 temperature range, of 150-500 K, including up to 200 K undercooling below the
256 corresponding liquidus temperature. Generally, the temperature range is limited by the
257 nucleation of the solid phase at low temperatures and by mass loss due to evaporation at
258 sufficiently large temperatures.

259 For all compositions, the density, ρ , changes linearly with temperature and with a negative
260 slope, indicating a positive thermal volume expansion coefficient. Moreover, the density
261 changes gradually with x_{Al}^B . Pure Al exhibits the lowest density, and Ti the largest. The
262 density values of the alloys lie within these two extremes.

263 The experimentally obtained values of $\rho(T)$ can be fitted by Eq. (1) with the fits shown in Fig.
264 2 by the solid lines. The obtained values of ρ_L and ρ_T , as well as the volume expansion
265 coefficient, β , calculated from this data via Eq. (2), are listed along with in Tables 2, 3, and 6
266 along with the corresponding liquidus temperatures. Accordingly, Table 2 contains the results
267 for the pure elements and Table 3 contains the results for the alloys.

268 In the case of pure Al, the agreement among the values of ρ_L is around a mean value of 2.30
269 gcm^{-3} , within $\pm 0.02 \text{ gcm}^{-3}$, corresponding to a relative uncertainty of $\pm 0.09 \%$. The values of
270 ρ_T are distributed around a mean of $-2.18 \cdot 10^{-4} \text{ gcm}^{-3}\text{K}^{-1}$, within $\pm 0.32 \cdot 10^{-4} \text{ gcm}^{-3}\text{K}^{-1}$,
271 corresponding to $\pm 15 \%$. In the case of Ti, the average of the individual values of ρ_L amounts
272 to $4.12 (\pm 0.04) \text{ gcm}^{-3}$, corresponding to a relative deviation of 1% . The temperature
273 coefficient of pure Ti scatters around $-2.85 (\pm 1.24) \cdot 10^{-4} \text{ gcm}^{-3}\text{K}^{-1}$ and, hence, within a relative
274 margin of 35% . Generally, it is observed for our measurements that the deviations in ρ_T are
275 in the range of up to 50% , as its precise determination is sensitive to the accuracy of the data
276 points, determined at the margins of the temperature intervals. These are, however, the points
277 that are most exposed to the impact of potential sources of error, such as evaporation at high
278 temperatures, or possible oxide formation, for example at low temperatures.

279 Table 6 contains data for ρ_L and ρ_T , and their mean values selected from literature [4, 35-
280 45,52]. In the case of pure Ti mean values of $4.17 (\pm 0.07) \text{ gcm}^{-3}$, for ρ_L and $-4.18 \cdot 10^{-4}$
281 $(\pm 3.02 \cdot 10^{-4}) \text{ gcm}^{-3}\text{K}^{-1}$, for ρ_T can be found. Thus, the data presented in the present work is in
282 good agreement with the literature and lies within the error for the mean value of pure Ti.
283 Accordingly, for pure Al the mean value of the temperature coefficient of the present work, -
284 $2.85 (\pm 1.24) \cdot 10^{-4} \text{ gcm}^{-3}\text{K}^{-1}$, agrees well with the mean temperature coefficient value of the
285 selected literature data of $-2.91 (\pm 0.5) \cdot 10^{-4} \text{ gcm}^{-3}\text{K}^{-1}$. However, for the mean value of ρ_L for
286 pure Al, the value of the present work, $2.30 (\pm 0.02) \text{ gcm}^{-3}$, is lower and lies beyond the errors
287 bars of the mean value, $2.36 (\pm 0.03) \text{ gcm}^{-3}$, given by literature, see Tabs. 2 and 6. The reason
288 is unclear.

289 In Table 3 the values of ρ_L change gradually with increasing x_{Al}^{B} . Except for $\text{Al}_{40}\text{Ti}_{60}$, $\text{Al}_{60}\text{Ti}_{40}$
290 and $\text{Al}_{90}\text{Ti}_{10}$, all compositions are measured more than once, and, in these cases, the observed
291 scatter in ρ_L and ρ_T is in the same order of magnitude as for the pure elements. For ρ_T this
292 margin is about 40% , which corresponds to the magnitude of the variation among the

293 different values of ρ_T over all compositions. Hence, it is justified to claim that with respect to
294 the experimental accuracy of the data, ρ_T is basically constant with a mean value of -3.83
295 $(\pm 1.6) \cdot 10^{-4} \text{ gcm}^{-3}$. The same holds for β , for which a mean value of $1.18 (\pm 0.5) \cdot 10^{-4} \text{ K}^{-1}$ is
296 found over all compositions.

297 In addition to ρ_L , ρ_T and β , the Tables 6 and 7 also show the isothermal density calculated
298 from Eq. (1) at $T=1873 \text{ K}$ ($1600 \text{ }^\circ\text{C}$). This temperature is chosen to be in the middle of the
299 total range of temperatures covered by the experiments. As can be seen from the Tables,
300 $\rho(T=1873 \text{ K}$ ($1600 \text{ }^\circ\text{C}$)) decreases monotonically from $\rho_{\text{Ti}}=4.14 (\pm 0.04) \text{ gcm}^{-3}$ to $\rho_{\text{Al}}=2.09$
301 $(\pm 0.01) \text{ gcm}^{-3}$ upon increasing x_{Al}^{B} .

302 In order to elucidate and understand how the density changes with composition, it is indicated
303 not to discuss the mass density but rather the isothermal molar volume, V and its composition
304 dependence. In contrast with mass density, the molar volume is an additive quantity.

305 Moreover, effects originating from the packing and ordering of atoms could be obscured by
306 the mass differences between the pure elements, Al and Ti, if only the mass density is
307 considered.

308 For this reason, the molar volume at 1873 K (1600 K) is plotted in Fig. 3 versus x_{Al}^{B} . For some
309 alloys this temperature lies outside the measured temperature range, due to the
310 aforementioned temperature range boundaries. For these alloys, the density is extrapolated by
311 Eq. (2). This is marked in Fig. 3 by hollow or semi-hollow symbols. The precise location of
312 the phase boundaries is not crucial in this context, as the properties of the stable (or
313 metastable) liquid are of primary interest.

314 As can be seen from Fig. 3, the molar volume, V , generally increases with an increasing mole
315 fraction of respective mean values of the pure elements, x_{Al}^{B} , from $11.54 \text{ cm}^3 \text{ mol}^{-1}$ to 12.92
316 $\text{cm}^3 \text{ mol}^{-1}$.

317 Starting on the left side in Fig. 3, there seems to be the tendency that V slightly decreases for
318 $x_{\text{Al}}^{\text{B}} < 40$ at.-%. However, this tendency is beyond the scatter of the experimental data.
319 Therefore, V can be regarded as practically constant at $\approx 11.5 \text{ cm}^3 \text{ mol}^{-1}$ for $x_{\text{Al}}^{\text{B}} < 70$ at.-%. For
320 $x_{\text{Al}}^{\text{B}} \geq 70$ at.-%, however, V steeply increases with x_{Al}^{B} until its final value is reached at
321 $x_{\text{Al}}^{\text{B}} = 100$ at.-%.

322

323 3.2 Surface tension

324 Surface tension data of the liquid pure elements is plotted versus temperature in Fig. 4 for Al
325 and in Fig. 5 for Ti. In the case of Al, the data shown is published by us previously [24,33].
326 The experimentally obtained values of $\gamma(T)$ follow linear laws and hence, can be fitted by Eq.
327 (7).

328 In the case of pure Ti, the solid squares shown in Fig. 5 represent three individual
329 measurements which are combined to a single curve. For each of these measurements, the
330 obtained fit parameters γ_{L} and γ_{T} are shown in Table 4. From these, arithmetic averages are
331 formed which are shown in Tab. 4 as well, and additionally, in Tab 8. The mean of γ_{L}
332 amounts to $1.56(\pm 0.02) \text{ Nm}^{-1}$. Its' uncertainty corresponds to a relative deviation of $\pm 1.3\%$.
333 The temperature coefficient of pure Ti scatters around $(-1.65(\pm 0.95)) \cdot 10^{-4} \text{ Nm}^{-1} \text{ K}^{-1}$, and hence,
334 within a relative margin of $\pm 58\%$. Generally, it is observed that the deviations in γ_{T} are in the
335 range of up to 58 %, which is larger than the deviations in the surface tension, γ . This is for
336 essentially the same reasons as the increased scatter in ρ_{T} . For comparison, Fig. 5 and Tab. 8
337 also show surface tension data of liquid Ti, or their linear representations, as obtained in
338 literature. Excellent agreement is obviously obtained with the data published by Paradis [53]
339 who measured γ in electrostatic levitation.

340 Fig. 4 shows two sets of experimental surface tension data of liquid Al. The hollow circles
341 represent data that has been measured by Kolland [35] whereas no particular attention was

342 paid to the oxygen partial pressure. It has been concluded in Ref. [35] that this result
 343 corresponds to a case where the surface contains a significant amount of dissolved oxygen.
 344 Fitting Eq. (7) to this data yields $\gamma_L=0.87 \text{ Nm}^{-1}$ and $\gamma_T=-1.46 \cdot 10^{-4} \text{ Nm}^{-1} \text{ K}^{-1}$. This is roughly 5 %
 345 larger than data reported by Molina [54] for an oxygen saturated liquid surface, see Fig. 4.
 346 The solid squares in Fig. 4 represent the measurement of Kobatake [37] where the oxygen
 347 partial pressure was controlled (10^{-1} Pa) using an oxygen sensing and control system (OSC).
 348 The obtained curve is in good agreement with the results of Molina who presented in his
 349 study [54] also surface tension data for an oxygen free Al surface. In Fig. 4, the results of
 350 Kobatake even overestimate the data of Molina slightly. Fitting Eq. (7) to the data of
 351 Kobatake [37] yields $\gamma_L=0.98 \text{ Nm}^{-1}$ and $\gamma_T=-2.71 \cdot 10^{-4} \text{ Nm}^{-1} \text{ K}^{-1}$. For Al, the parameters γ_L and
 352 γ_T are listed in Table 4. Detailed discussions of the surface tension of liquid Al are further
 353 presented in refs. [35,37].
 354 Figure 6 shows plots of γ versus temperature for the liquid alloy samples. For the sake of
 355 completeness and in order to be able to make visual comparisons, the figure also shows the
 356 data for pure Ti and representations of the data of pure Al taken from refs. [35,37].
 357 The Al-mole fraction, x_{Al}^{B} , ranges from 0 to 100 at.-% in Fig. 6. Each measurement is carried
 358 out over a broad temperature range of 100-250 K, including up to 200 K undercooling below
 359 the corresponding liquidus temperature. Corresponding to the density, surface tension
 360 measurements are restricted by the same temperature range boundaries.
 361 For all compositions it is found again that γ linearly declines with temperature. Moreover, γ
 362 changes gradually with x_{Al}^{B} , and exhibits an increase from the lowest values for pure Al, to
 363 the highest γ for pure Ti.
 364 The individual fits of Eq. (7) are shown in Fig. 6 by the solid lines. The obtained values of γ_L
 365 and γ_T are listed in Tab. 5 for the alloy system, together with the corresponding liquidus
 366 temperatures T_L .

367 As shown in Tab. 5, the values of γ_L change gradually with increasing x_{Al}^B . For multiple data
368 of the same alloys, the observed scatter for γ_L and γ_T ranges in the same order of magnitude as
369 for the pure elements. In particular, for γ_T , the margin for all compositions is around 55 %.
370 That agrees well with the magnitude of variation among the γ_T data of each compositions of
371 20-60 %. Hence, it is justified to claim that, with respect to the experimental accuracy of the
372 data, γ_T is essentially constant, with a mean value of $(-2.51(\pm 1.37)) \cdot 10^{-4} \text{Nm}^{-1} \text{K}^{-1}$.
373 In addition, Tables 4 and 5 show the isothermal surface tension calculated from Eq. (7) at
374 $T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$), chosen from the middle of the total range of temperatures covered by
375 the experiments. As can be seen from the Tables, $\gamma(T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$)) decreases
376 monotonically from $\gamma_{Ti}=1.56(\pm 0.02) \text{ Nm}^{-1}$ to $\gamma_{Al}=0.71(\pm 0.01) \text{ Nm}^{-1}$ upon increasing x_{Al}^B . In
377 Fig. 7 the surface tension at $T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$) is plotted versus x_{Al}^B . Analogously to the
378 density data, the extrapolated value for $\gamma(T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$)) partially outliers the measured
379 temperature range for some alloys, which is negligible in the context. Starting on the left side
380 in Fig. 7, $\gamma(T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$)) decreases with concentration for component $x_{Al}^B < 20 \text{ at.-%}$.
381 There appears to be the tendency that $\gamma(T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$)) does not decrease, and is
382 approximately constant for $20 \text{ at.-%} \leq x_{Al}^B \leq 30 \text{ at.-%}$. However, this tendency is beyond the
383 scatter of the experimental data. For $x_{Al}^B > 30 \text{ at.-%}$, $\gamma(T=1950 \text{ K}$ ($1677 \text{ }^\circ\text{C}$)) steeply decreases
384 with x_{Al}^B , and exhibits a concave shape until its final value is reached at $x_{Al}^B = 100 \text{ at.-%}$.

385

386 4. Discussion

387 4.1. Density

388 In addition to the experimental data, the calculated ideal molar volumes, V^{ideal} , at $T=1873 \text{ K}$
389 ($1600 \text{ }^\circ\text{C}$), are plotted versus the bulk Al concentration in Fig. 3. Accordingly, the molar
390 volumes of the pure components used for the calculation are assessed from the averaged
391 density values at $T=1950 \text{ K}$, with $\rho_{Al} = 2.09 \text{ gcm}^{-3}$ and $\rho_{Ti} = 4.14 \text{ gcm}^{-3}$. The deviation

392 between the measured molar volume, V , and the ideal molar volume, V^{ideal} , corresponds to the
 393 excess molar volume, V^E Eq. (4). In Fig. 3, $V(x_{\text{Al}}^{\text{B}})$ is fitted by a Redlich-Kister polynomial of
 394 zeroth ($N = 0$) and first ($N = 1$) order. The fitted, temperature-dependent excess parameters,
 395 0V and 1V , are listed in Tab. 7. Regarding V^{ideal} and V , the fits exhibit a negative deviation, and
 396 hence, the excess volume is negative. For a fitted excess molar volume with $N=0$ in Eq. (4),
 397 the molar volume shows a concave shape, with the maximum negative excess molar volume
 398 for an Al concentration, $x_{\text{Al}}^{\text{B}} \approx 20$ at.-% of around $-0.37 \cdot 10^{-6} \text{m}^3 \text{mol}^{-1}$. Starting from the left
 399 side for a fit with $N=0$ in Eq. (4), V slightly increases for $x_{\text{Al}}^{\text{B}} < 16$ at.-%, and shows a minor
 400 local maximum at $x_{\text{Al}}^{\text{B}} = 16$ at.-%. For $16 \text{ at.-%} < x_{\text{Al}}^{\text{B}} < 67 \text{ at.-%}$, V slightly decreases with a
 401 maximum negative excess molar volume, $V^E \approx -0.8 \cdot 10^{-6} \text{m}^3 \text{mol}^{-1}$, for $x_{\text{Al}}^{\text{B}} = 67 \text{ at.-%}$. For $x_{\text{Al}}^{\text{B}} \geq$
 402 67 at.-% , V steeply increases with increasing Al concentration, until its final value is reached
 403 at $x_{\text{Al}}^{\text{B}}=100 \text{ at.-%}$. In contrast to V^i , both fits are in good agreement with the data.
 404 Consequently, it can be said that, referring to the density and molar volume, Al-Ti is a highly
 405 nonideal system, showing significant negative excess volumes.
 406 However, the fit of first order reproduces the data and its trend more accurately. Thus, we
 407 suggest, in the case of binary Al-Ti, two fit parameters, 0V and 1V , are needed to describe the
 408 excess molar volume. This is in accordance with other binary Ti-containing systems, where
 409 two fit parameters are used to fit the data qualitatively and quantitatively well; for example, in
 410 the case of Cu-Ti [26, 27]. However, a positive excess volume has been found in the case of
 411 Cu-Ti. Negative excess molar volumes have been found in other Al-containing systems such
 412 as Al-Fe [28], Al-Ag [30], Al-Cu [20] and Al-Ni [28], hence, the results are in good
 413 agreement with literature data, for example, with the investigations by Peng et al. for the Al-
 414 Au system [34]. Density measurements and molecular dynamics (MD) simulations in that
 415 system suggest that the nonideal mixing behavior occurs due to the apparent decreasing
 416 atomic radii of the Al atoms. This leads to a shrunken close packing, especially of the Al-Al

417 pairs [34]. Taking this into account, similar processes in the Al-Ti system are likely, but
418 further investigations, e.g. MD simulations, experiments with neutron or X-ray scattering are
419 required to confirm this.

420 Fig. 8 shows plotted and fitted isothermal excess molar volumes, V^E , as a function of the Al
421 concentration, x_{Al}^B , for different temperatures ($T = 1473$ K (1200 °C), 1673 K (1400 °C), and
422 1873 K (1600 °C)). Corresponding to its definition, the excess molar volume for the pure
423 elements Al and Ti equals zero. For all temperatures, the values show a concave shape.
424 Starting from the left side, V^E decreases until its maximum negative values of around $V^E \approx -$
425 $0.80-1.05 \cdot 10^{-6} \text{ m}^3 \text{ mol}^{-1}$ for $x_{Al}^B \approx 60-70$ at.-%. Accordingly, the maximum negative excess
426 molar volumes decrease with increasing temperatures, while their values also shift to higher
427 Al concentrations. This shift indicates, that a more efficient packing and interaction occur for
428 lower temperatures, as pronounced atomic mobility and dynamics at higher temperatures
429 suppress those interactions and entropy becomes dominant.

430

431 4.2 The role of oxygen

432 Due to high affinity of oxygen to both elements, Al and Ti, the impact of potentially existing
433 traces of oxygen on the surface tension needs to be discussed.

434 In the case of pure liquid Al, the effect is demonstrated in Fig. 4. In the case of Kobatake's
435 measurement, the oxygen partial pressure in the chamber $p^{\text{Ch}}_{\text{O}_2}$ was adjusted at roughly 10^{-1}
436 Pa. This is far above the equilibrium partial pressure, 10^{-25} Pa, for Al_2O_3 formation [55].

437 However, it has been argued by Eustathopoulos [56] that the evaporation of volatile Al_2O
438 effectively lowers the oxygen partial pressure $p^{\text{S}}_{\text{O}_2}$ in the vicinity of the surface. This can be
439 described by the following equation:

$$440 \quad p^{\text{S}}_{\text{O}_2} = \{(2D_{\text{O}}/D_{\text{Ox}})p^{\text{Ch}}_{\text{O}_2}/K\}^2 \approx (p^{\text{Ch}}_{\text{O}_2}/K)^2 \quad (22)$$

441 where K is the equilibrium constant of the reaction and D_{O} and D_{Ox} indicate the diffusion
442 coefficients of oxygen and the oxide in the vapor, respectively. In the case of pure Al, the

443 effective partial pressure of the sample, $p_{\text{O}_2}^S$, can be estimated as 10^{-26} Pa, which is well
444 below the equilibrium pressure and the surface tension measured by Kobatake for liquid Al
445 can be regarded as reliable.

446 In the case of pure Ti, the situation is more complicated. A detailed thermodynamic analysis
447 on oxygen in liquid Ti performed by Belyanchikov [57] shows that there are no volatile
448 oxides in this system. Ti can reduce liquid Al and consequently capture all oxygen from Al if,
449 as in the present work, liquid Al-Ti is investigated. Belyanchikov [57] furthermore showed
450 that Ti can practically not be reduced by any of the strongest deoxidizers known, i.e. Ba, Be,
451 Ca, Ce, Hf, La, Mg, Sr, Zr, and Fe. The oxygen content of one of the solidified Ti samples
452 was determined in a LECO analysis after the levitation run. It was found that its oxygen
453 concentration was approx. 0.15 %. This value agrees with the maximum solubility of oxygen
454 in liquid Ti predicted by Belyanchikov [57] under the assumption that Ti is in contact with an
455 oxide.

456 On the other hand, Paradis argued in his work that his surface tension data on pure and
457 oxygen-free liquid Ti should be correct, because pronounced evaporation of liquid Ti might
458 induce a self-purification process of the sample [53]. It is evident that both datasets of the
459 surface tension of liquid Ti, the one of Paradis and of the present work, belong to the highest
460 values obtained in Fig. 5. Most of the other data, including the one measured by Amore [27],
461 are lower. This fact indicates that oxygen, if dissolved in the liquid Ti samples, does not play
462 a significant role in the case of the present work.

463

464 *4.3 Surface tension*

465 A comparison of the experimental data and model calculations for the isothermal surface
466 tension, $\gamma(T=1950 \text{ K (1677 } ^\circ\text{C)})$, is shown in Fig. 7. The data are fitted by a Redlich-Kister
467 type polynomial of first (N=1) order. The corresponding fit parameters, ${}^0u(T=1950 \text{ K (1677$
468 $^\circ\text{C)})$ and ${}^1u(T=1950 \text{ K (1677 } ^\circ\text{C)})$, for the excess surface tension of the measured data are

469 listed in Tab. 7. The fit is in good agreement with the data and lies within the error bars for all
470 Al concentrations. Generally, the fit follows the curvature of the data, except for 10 at.-% <
471 $x_{\text{Al}}^{\text{B}} < 30$ at.-%, where it does not reproduce the kink, and slightly overestimates the surface
472 tension.

473 The model for an ideal solution, following Eq. (15), exhibits a concave shape, with its highest
474 values for pure Ti and lowest values for pure Al. The model does not reproduce the data
475 qualitatively, and underestimates the values for all alloys except for $\text{Al}_{90}\text{Ti}_{10}$. Hence, the
476 model fails to describe the data correctly and Al-Ti does not show ideal solution behaviour,
477 analogously to density, excess free energy and other Al- and Ti-based alloys.

478 A far better agreement is obtained for the calculations by the Butler model, Eq. (9) with the
479 temperature dependent interaction parameters, ${}^{\text{V}}L_{\text{Al,Ti}}(T)$, listed in Tab. 7 and Chatain model
480 [44,45] for subregular nonideal solutions. The surface tension and its concentration
481 dependence are predicted qualitatively with both models, showing positive excess values,
482 regarding the ideal solution. The Butler model shows a good agreement, in particular for 25
483 at.-% $\geq x_{\text{Al}}^{\text{B}} \geq 50$ at.-%. In this interval the model follows the curvature of the data and lies
484 within all error bars. Nevertheless, for 25 at.-% < $x_{\text{Al}}^{\text{B}} < 50$ at.-% the Butler model
485 underestimates the data by 5-16 % and does not reproduce the kink, shown by the data for
486 those concentrations. On the other hand, the calculations of the Chatain model [44,45]
487 reproduce the kink for an Al concentration around 25-50 at.-%, but overestimate $\gamma(T=1950 \text{ K}$
488 $(1677 \text{ }^{\circ}\text{C}))$ for 40 at.-% < $x_{\text{Al}}^{\text{B}} < 70$ at.-% by 5-12 %. Although the Chatain model lies within
489 the error bars for Al concentrations greater than 70 at.-%, the model predicts a negative kink
490 in this interval, while the data follows a minor a positive kink.

491 Overall, it is suggested that the Butler model for nonideal solutions reproduces the data most
492 accurately in the Al-Ti system. Usually, the ideal solution fails to predict experimental data
493 correctly, as for most systems, the excess free energy, ${}^{\text{E}}G \neq 0$. For ideal solutions only the
494 surface segregation of the surface active component is taken into account e.g. Al in the case of

495 Al-Ti but other inter-atomic effects are neglected. Surface segregation can be understood as a
496 process of energy minimization, in order to minimize the energy of the system, G_{tot} , the
497 component with the smaller surface tension becomes enriched in the surface layer. For alloys
498 with $E^{\text{G}} > 0$, the surface segregation becomes enhanced, while for alloys with $E^{\text{G}} < 0$, the
499 surface segregation of Al is suppressed, due to interatomic attractions. The latter is found for
500 many Al-systems, such as Al-Cu, Al-Ni, Al-Fe and Al-Au, as reported by Brillo et al. [24],
501 and leads to an increased surface tension, compared to the ideal system, as in the case of Al-
502 Ti.

503 The suppressed Al surface segregation of the nonideal solution, in comparison with the ideal
504 solution is also calculated with the Butler model [39] for a monolayer, and the Chatain model
505 [44, 45] for multiple layers, displayed in Fig. 9. Here, the Al-content of the surface is plotted
506 against the Al-content of the bulk. For all models a general Al segregation is evident in an
507 enriched Al-content in the surface versus the bulk. Compared to the ideal solution, for $x_{\text{Al}}^{\text{B}} \leq$
508 60 at.-% the concentration of the top layer is relatively depleted by Al, by up to 40 % for the
509 Butler model and up to 60 % for the Chatain model. For Al concentrations higher than 60 at.-
510 % for the Butler model, and 80 at.-% for the Chatain model, no further suppression of the
511 segregation is predicted by the models.

512 As can be seen in Figs. 9 and 10, the Chatain model gives highly fluctuating values of Al
513 enrichment and depletion for the uppermost layers. Fig. 10 shows the concentration, $x_{\text{Al}}(n)$, of
514 each layer plotted against the layer number, n , for $\text{Al}_{50}\text{Au}_{50}$, at $T=1700$ K (1427 °C), $T=1950$
515 K (1677 °C). While, with respect to the bulk, the first layer exhibits an enrichment of Al of
516 around 25 %, the second layer shows a depletion of Al of around 10 %. This oscillating
517 behaviour continues for both temperatures in the figure, until, in the layer, $n=6$, the bulk
518 composition is reached. Such concentration oscillations are called chemical layering. In this
519 mechanism the segregation of one component to the surface leads to an excess of the other
520 component in the following layer. Due to the negative excess free energy, the other

521 component is then favored in the second layer. Chemical layering has been observed in
 522 several systems with negative excess free energy; for example in the cases of Al-Ni [29], Al-
 523 Cu [31] and Al-Au [35]. For $T=1700$ K (1427 °C), the chemical layering is slightly more
 524 pronounced than for $T=1950$ K (1677 °C), due to the minor atomic dynamics at low
 525 temperatures and, thus, enhanced interactions between atoms.

526 The values for the temperature coefficient, γ_T , experimentally obtained, and the values
 527 calculated by the Chatain and Butler model, are plotted in Fig. 11. As γ_T was assumed to be
 528 constant, with a mean value of $-2.51(\pm 1.37) 10^{-4} \cdot \text{Nm}^{-1} \text{K}^{-1}$, the Butler model, with a mean
 529 value of $-2.14(\pm 0.89) 10^{-4} \cdot \text{Nm}^{-1} \text{K}^{-1}$, is, regarding the temperature coefficient, also in better
 530 agreement with the data than the Chatain model with a mean value of $-1.50(\pm 0.21) 10^{-4} \cdot \text{Nm}^{-1} \text{K}^{-1}$. Starting on the left side in Fig. 11, there appears to be the tendency for γ_T to slightly
 531 decrease for $x_{\text{Al}}^{\text{B}} < 40$ at.-% and increases for higher Al concentrations, which corresponds to
 532 the Butler model. However, this tendency is beyond the scatter of the experimental data.

533 The measured values and the values calculated from the Chatain and Butler model of the
 534 excess surface tension, γ^{E} , using Eq. (18), evaluated at a fixed temperature, $T=1950$ K (1677
 535 °C), are shown in Fig. 12. The corresponding fit parameters, ${}^0u_{i,j}$ and ${}^1u_{i,j}$, for the excess
 536 surface tension of the measured data are listed in Tab. 7. The highest excess surface tension is
 537 found for $x_{\text{Al}}^{\text{B}} \leq 40$ at.-%, which amounts to 0.28 Nm^{-1} , while for higher Al concentrations the
 538 excess surface tension is significantly smaller, at around 0.1 Nm^{-1} . As seen in Fig. 7, both
 539 models are in good agreement with the surface tension, and the excess surface tension data,
 540 respectively. The Butler model underestimates the data, especially for $x_{\text{Al}}^{\text{B}} \leq 40$ at.-%, but
 541 reproduces the data within the error bars. The Chatain model overestimates the data, except
 542 for $x_{\text{Al}}^{\text{B}} > 80$ at.-%, and lies within the error bars, except for $x_{\text{Al}}^{\text{B}} \approx 50-60$ at.-%. Qualitatively,
 543 the Chatain model appears to reproduce the data more accurately for $x_{\text{Al}}^{\text{B}} \leq 40$ at.-%, while
 544 the Butler model appears more accurate for $x_{\text{Al}}^{\text{B}} > 40$ at.-%. The data and the Butler model

546 could indicate that a pronounced suppression of Al segregation only occurs up to a certain Al
547 concentration, of around 40 at.-%.

548 In Fig. 13 the isothermal surface tension data of the binary Al-Ti system, at $T=1950$ K (1677
549 °C), and literature surface data of pure Titanium and, some industrially used, multicomponent
550 alloys at equivalent temperatures, are plotted versus the Al concentration. As mentioned
551 above, multicomponent alloys on the basis of Al-Ti are of particular technical importance,
552 while data on their properties are sparse. As can be seen in Fig. 13, the surface tension data of
553 the binary system and the multicomponent alloys are in good agreement with deviations up to
554 10 %, in the case of $\text{Al}_6\text{Ti}_{90}\text{V}_4$, reported by Egry et al. [59]. Those deviations lie within the
555 same range of order as the relative uncertainties for the data of the pure e.g. 8 % for Ti, and
556 binary components e.g. 24 % for $\text{Al}_{80}\text{Ti}_{20}$, reported by Novacovic et al. [25] and in the present
557 work. Therefore, the data that are presented in the present work do not only fill the database
558 for thermophysical properties of binary Al-Ti alloys, but also established a good starting point
559 for investigations and processing of industrially used Al-Ti-based alloys with multiple
560 components.

561 Oxygen adsorption at the surface of the sample can produce a reduction in the surface tension.
562 The electromagnetic levitation technique is a generally clean method which avoids contact
563 between the liquid alloy and a container. Although it does not avoid contact with the gas
564 phase, an oxygen-reduced sample surface can still be achieved as discussed above. For the
565 surface tension of pure Ti, no comparable results for measurements under oxygen reduced
566 atmosphere are available. Anyhow, the mean value of the surface tension value for pure Ti of
567 this work is higher than the mean value of the cited literature data. That indicates that our
568 measurements are averagely and comparatively less affected by oxygen impurities.
569 For future works an extend study on the dependence of the surface tension on the oxygen
570 partial pressure of Al-Ti alloys would be of great value and interest. Such a study is presently
571 being carried out by us.

572 **5. Summary**

573 Density and surface tension of binary Al-Ti-alloys are measured over a broad temperature and
574 composition range. It is found that, for all compositions, the density and surface tensions
575 increase linearly upon decreasing temperatures. The data are analyzed concerning the
576 temperature coefficients, excess molar volume, excess surface tension and surface
577 segregation. Generally, Al-Ti is a highly nonideal system. Significantly highly negative
578 values are found for the excess molar volume, which is in good agreement with other binary
579 Ti-containing systems. Referring to the Al-Au system [34], shrunk Al radii are suggested to
580 mainly trigger that mechanism, but further investigations are needed to verify this hypothesis.
581 Concerning the surface tension, a highly nonideal behaviour could also be observed, with
582 positive values for the excess surface tension. The results correspond well with the predictions
583 of the Butler [39] and the Chatain model [44, 45] for nonideal solutions with excess free
584 energy, $^E G \neq 0$. For nonideal solutions the models not only take the surface segregation of the
585 surface active component, Al, into account, but also the suppression of the latter, due to
586 interatomic attractions. Both mechanisms can be distinguished in the Al-Ti-system,
587 coinciding with other Al-systems, reported by Brillo [24].
588 Overall, the nonideal behaviour for all investigated properties of the Al-Ti-system is more
589 distinct for relatively low temperatures, due to the minor atomic dynamics and thus, enhanced
590 interactions between atoms.
591 Multicomponent Al-Ti-based alloys - rather than binary Al-Ti-alloys - are of primary interest
592 for various high temperature applications; however data on their properties are sparse. Before
593 investigating partly highly complicated multi-component systems, it is an useful if not
594 necessary approach to start with measurement in the binary system. In this work we could
595 show that the data of the binary and multiple component systems are in very good agreement
596 (Fig. 13). Therefore, we suggest that the data of the binary Al-Ti-system, presented in this

597 work, is not only interesting as fundamental research results, but may also be sufficient for
598 many applications with multi-component Al-Ti-alloys.

599

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604 study and for his valuable suggestions.

605

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694 **Figure captions:**

695

696 **Fig. 1:** Scheme of the phase diagram of **Al-Ti** according to the thermodynamic description of
697 Witusiewicz et al. using the CALPHAD approach [50]. For the sake of clarity, details at low
698 temperature have been omitted.

699 **Fig. 2:** Measured density, ρ , of liquid Al-Ti (symbols) and their linear fits (lines) versus
700 temperature, T , following Eq. (1). For the pure elements the fits for the mean values of all
701 measurements of Al and Ti are shown. The inset shows a magnified portion of the figure for
702 Al-mole fractions x_{Al}^B , ranging from 10 to 50 at.-%.

703 **Fig. 3:** Molar volumes in dependence of the mole fraction, x_{Al}^B of measurements at $T=1873$ K
704 (solid circles), molar volumes extrapolated to a temperature range below (hollow circles) and
705 above (half-solid circles) measurement conditions. The lines show the ideal molar volumes
706 (dotted line) and fitted molar volumes with one fit parameter, 0V , (solid line) and two fit
707 parameters, 0V and 1V , (dashed-dotted-dotted line), following Eq. (4, 5).

708 **Fig 4:** Surface tension of pure liquid Al as function of temperature. The circles denote data
709 measured by Kolland [35] and the squares data measured by Kobatake [36] under oxygen
710 reduced conditions. The solid and the dashed-dotted lines represent corresponding fits to this
711 data. For comparison, representations of the surface tension data of Molina [54] are shown by
712 the dashed and dotted lines.

713 **Fig. 5:** Surface tension of liquid Ti (solid symbols) versus temperature. For comparison, data
714 of various authors are shown as well (hollow symbols). The long dashed line represents our
715 previous results determined in EML [27] and the results obtained by Paradis [53] using
716 electrostatic levitation are represented by the dashed-double-dotted line.

717 **Fig. 6:** Literature surface tension, γ , of liquid Al [24, 35] and measured surface tension of
718 liquid Al-Ti (symbols) and their linear fits (lines) in dependence of temperature, T , following

719 Eq. (8). The inset shows a magnified portion of the figure for Al-mole fractions x_{Al}^{B} , ranging
720 from 0 to 40 at.-%.

721 **Fig. 7:** Isothermal surface tension γ of measured liquid Al-Ti and literature data for pure
722 liquid Al, in dependence of the bulk mole fraction x_{Al}^{B} at 1950 K (1677 °C). The squares
723 show the extrapolated measured surface tension data, the lines represent the data fit with two
724 fit parameter, 0u and 1u , (dashed-dotted-dotted line) following Eq. (21), surface tension values
725 calculated with the Butler model [39] for subregular solutions with ideal (dotted line) and
726 nonideal mixing behaviour (dashed line) and the Chatain model [44,45] for subregular
727 solutions (solid line), as described in the text.

728 **Fig. 8:** Fitted excess molar volumes, V^{E} (Eq. 15), of first order fits ($N = 1$) at $T=1473$ K
729 (1200 °C) (dotted line), 1673 K (1400 °C) (dashed line) and 1873 K (1600 °C) (solid line).

730 **Fig 9:** Calculated surface mole fraction x_{Al}^{S} as a function of the bulk mole fraction x_{Al}^{B} at
731 $T=1950$ K (1677 °C) using the ideal (dotted line) and nonideal (dashed line) subregular
732 solution model by Butler [39] and by Chatain [44,45] (solid lines) for different layers, where
733 layer “1” denotes the layer at the surface. The layer numbers increase with their distance to
734 the surface.

735 **Fig 10:** Calculated surface mole fraction $x_{\text{Al}}^{(\text{n})}$ as a function of the bulk mole fraction x_{Al}^{B} at
736 $T=1700$ K (1477 °C) (triangles) and $T=1950$ K (1677 °C) (squares) using the nonideal
737 subregular solution model by Chatain [44, 45] for different layers, where the layer numbers
738 increase with their distance to the surface.

739 **Fig 11:** Temperature coefficient values γ_{T} (Eq. (8) in dependence of the bulk mole fraction
740 x_{Al}^{B} of measured data at 1950 K (1677 °C), represented by the squares. The lines represent the
741 calculated temperature coefficient values for the nonideal subregular solution model by Butler
742 [39] (dashed line) and by Chatain [44, 45] (solid line).

743 **Fig 12:** Isothermal excess surface tension γ^E of liquid Al-Ti as a function of the bulk mole
744 fraction x_{Al}^B at $T=1950$ K (1677 °C). The symbols show the extrapolated measured surface
745 tension data subtracted by the calculated surface tension values of the Butler [39] (squares)
746 and Chatain [44, 45] (triangles) model for ideal subregular solutions. The lines represent
747 excess surface tension γ^E , (Eq. (20)), values calculated as the difference between the Butler
748 (dashed line) and Chatain (solid line) model for ideal and nonideal subregular solutions.

749 **Fig. 13:** Surface tension γ of liquid Al-Ti in dependence of the bulk mole fraction x_{Al}^B of
750 measured data at 1950 K (1677 °C) and of Ti and industrially used Al-Ti-based alloys at
751 similar temperatures: Tiele [20], Allen [21], Amore [27], Arkhipkin [16], Paradis [17,52]
752 Kuppermann [23] Man [19], Nowak [60] Novakovic [25] and Egry [1,59].

753

754 **Table captions:**

755

756 **Table 1:** Key of methods for the density and surface tension data, selected from literature and
757 as used in the tables 2 and 7. The key R, meaning "recommended", species that the listed
758 value is obtained from a literature review.

759 **Table 2:** Parameters T_L , ρ_L , and ρ_T and the interpolated density $\rho(T=1873 \text{ K (1600 } ^\circ\text{C)})$ and
760 its mean values in bold font of pure liquid Al and Ti.

761 **Table 3:** Parameters T_L , ρ_L , and ρ_T and the extrapolated density $\rho(T=1873 \text{ K (1600 } ^\circ\text{C)})$ of
762 the investigated liquid alloys $\text{Al}_x\text{Ti}_{100-x}$.

763 **Table 4:** Parameters γ_L , and γ_T and the extrapolated isothermal surface tension $\gamma(T=1950 \text{ K}$
764 $(1677 ^\circ\text{C)})$ and its mean values in bold font for liquid Ti measured in this work and the
765 selected data from literature for liquid Al used for the models and the references, respectively.

766 **Table 5:** Parameters γ_L , and γ_T and the interpolated surface tension $\gamma(T=1950 \text{ K (1677 } ^\circ\text{C)})$ of
767 the investigated liquid alloys $\text{Al}_x\text{Ti}_{100-x}$.

768 **Table 6:** Parameters T_L and ρ_L and its mean values in bold font for the density of pure Al and
769 Ti selected from literature. The methods and references are specified in the fourth and fifth
770 column and the method key can be found in Tab. 3.

771 **Table 7:** Coefficients ${}^vV(T)$ of Redlich-Kister type polynomial fit, following Eq. (5) for fitted
772 excess molar volumes, V^E , temperature dependent parameters vL used for the calculations of
773 the subregular solution models by Butler and by Chatain (Eq. (15) and coefficients ${}^vu(T)$ of

774 **Table 8:** Compilation of surface tension values γ_L and γ_T and the corresponding references
775 and methods for liquid Titanium. The method key is listed in Tab. 3, respectively. Redlich-
776 Kister type polynomial fit following Eq. (21) for fitted excess surface tension, γ^E .

Table 1

Key	Method
CR	Rise method
DC	Draining crucible
ESL	Electro static
DW	Drop weight
PW	Pendant wire
EML	Electro magnetic
OD	Oscillating drop
PD	Pendant drop
A	Archimedian methods
BP	Bubble Pressure
SD	Sessile drop
G	γ -Absorption dilatometry
EW	Exploding wire
R	Recommended from literature review

Table 2

Composition	T_L (K (°C))	ρ_L (gcm ⁻³)	ρ_T (10 ⁻⁴ gcm ⁻³ K ⁻¹)	$\rho(T=1873K$ (1600 °C)) (g/cm ³)
Ti	1941 (1668)	4.14	-1.48	4.15
Ti	1941 (1668)	4.15	-4.4	4.18
Ti	1941 (1668)	4.06	-3.14	4.08
Ti	1941 (1668)	4.13	-2.38	4.14
Ti	1941 (1668)	4.12±0.04	-2.85±1.23	4.14±0.04
Al	933 (660)	2.32	-2.52	2.08
Al	933 (660)	2.28	-1.88	2.10
Al	933 (660)	2.29	-2.14	2.09
Al	933 (660)	2.30±0.02	-2.18±0.32	2.09±0.01

Table 3

Composition	T_L (K (°C))	ρ_L (gcm ⁻³)	ρ_T (10 ⁻⁴ gcm ⁻³ K ⁻¹)	$\rho(T=1873$ K (1600 °C)) (g/cm ³)
Al ₁₀ Ti ₉₀	1962 (1689)	3.91	-4.98	3.96
Al ₁₀ Ti ₉₀	1962 (1689)	3.82	-2.78	3.84
Al ₂₀ Ti ₈₀	1948 (1675)	3.63	-3.91	3.66
Al ₂₀ Ti ₈₀	1948 (1675)	3.67	-3.17	3.69
Al ₂₅ Ti ₇₅	1941 (1668)	3.69	-5.49	3.73
Al ₂₅ Ti ₇₅	1941 (1668)	3.65	-3.37	3.67
Al ₂₅ Ti ₇₅	1941 (1668)	3.61	-5.53	3.65
Al ₃₀ Ti ₇₀	1915 (1642)	3.52	-7.57	3.55
Al ₃₀ Ti ₇₀	1915 (1642)	3.53	-3.2	3.54
Al ₄₀ Ti ₆₀	1853 (1580)	3.37	-1.18	3.36
Al ₅₀ Ti ₅₀	1757 (1484)	3.34	-4.91	3.36
Al ₅₀ Ti ₅₀	1757 (1484)	3.38	-4.51	3.32
Al ₆₀ Ti ₄₀	1721 (1448)	3.13	-5.56	3.04
Al ₇₀ Ti ₃₀	1689 (1416)	2.91	-3.53	2.85
Al ₇₀ Ti ₃₀	1689 (1416)	2.88	-3.37	2.82
Al ₈₀ Ti ₂₀	1654 (1381)	2.69	-5.82	2.57
Al ₈₀ Ti ₂₀	1654 (1381)	2.69	-5.58	2.57
Al ₉₀ Ti ₁₀	1562 (1289)	2.46	-3.41	2.36

Table 4

Element	T_L (K (°C))	γ_L (Nm ⁻¹)	γ_T (10 ⁻⁴ Nm ⁻¹ K ⁻¹)	$\gamma(T=1950$ K (1677 °C)) (Nm ⁻¹)	Reference
Ti	1941 (1668)	1.56	-0.62	1.56	Present work
Ti	1941 (1668)	1.58	-2.49	1.57	Present work
Ti	1941 (1668)	1.54	-1.85	1.54	Present work
Ti	1941 (1668)	1.56±0.02	-1.65±0.95	1.55±0.02	
Al	933 (660)	0.98	-2.71	0.70	[37]
Al	933 (660)	0.87	-1.46	0.72	[35]
Al	933 (660)	0.92±0.08	-2.09±0.88	0.71±0.02	

Table 5

Composition	T_L (K (°C))	γ_L (Nm ⁻¹)	γ_T (10 ⁻⁴ Nm ⁻¹ K ⁻¹)	$\gamma(T=1950 \text{ K (1677 °C)})$ (Nm ⁻¹)
Al ₁₀ Ti ₉₀	1962 (1689)	1.52	-4.34	1.53
Al ₁₀ Ti ₉₀	1962 (1689)	1.46	-5.81	1.47
Al ₂₀ Ti ₈₀	1948 (1675)	1.35	-3.29	1.35
Al ₂₀ Ti ₈₀	1948 (1675)	1.28	-2.18	1.28
Al ₂₅ Ti ₇₅	1941 (1668)	1.30	-2.42	1.30
Al ₂₅ Ti ₇₅	1941 (1668)	1.36	-3.38	1.36
Al ₃₀ Ti ₇₀	1915 (1642)	1.34	-3.38	1.33
Al ₃₀ Ti ₇₀	1915 (1642)	1.33	-4.24	1.31
Al ₄₀ Ti ₆₀	1853 (1580)	1.24	-1.79	1.23
Al ₅₀ Ti ₅₀	1757 (1484)	1.07	-2.86	1.01
Al ₆₀ Ti ₄₀	1721 (1448)	0.96	-0.68	0.95
Al ₇₀ Ti ₃₀	1689 (1416)	0.94	-1.80	0.89
Al ₈₀ Ti ₂₀	1654 (1381)	0.92	-1.61	0.88
Al ₉₀ Ti ₁₀	1562 (1289)	0.89	-3.14	0.77
Al ₉₀ Ti ₁₀	1562 (1289)	0.81	-0.23	0.80

Table 6

Composition	ρ_L (gcm ⁻³)	ρ_T (10 ⁻⁴ gcm ⁻³ K ⁻¹)	Reference	Method
Al	2.37	-2.6	[35]	A
Al	2.39	-3.9	[36]	BP
Al	2.37	-2.6	[37]	SD
Al	2.38	-3.3	[38]	SD
Al	2.37	-3.1	[39]	G
Al	2.38	-2.3	[40]	G
Al	2.38	-2.3	[41]	R
Al	2.37	-3.1	[42]	R
Al	2.36	-3.3	[4]	EML
Al	2.36	-3.0	[4]	EML
Al	2.29	-2.5	[4]	EML
Al	2.36±0.03	-2.91±0.50		
Ti	4.17	-2.2	[43]	ESL
Ti	4.10	-9.9	[44]	ESL
Ti	4.21	-5.1	[52]	ESL
Ti	4.14	-2.25	[41]	R
Ti	4.29	-2.3	[45]	WE
Ti	4.1	-3.3	[4]	EML
Ti	4.17±0.07	-4.18±3.02		

Table 7

ν	${}^{\nu}V(T)$ ($\text{m}^3\text{mol}^{-1}$)	${}^{\nu}L$ (Jmol^{-1})	${}^{\nu}u(T)$ ($\text{Nm}^{-1}\text{mol}^{-1}$)
0	$0.00247T-6.55516$	$41.972T-118048$	$-0.00136T+2.8091$
1	$-0.001T+4.3711$	$19.704T-23613$	$-2.18327 \cdot 10^{-4}T+0.21604$
2		$-13.844T+34757$	

Table 8

γ_L ($10^{-4} \text{ Nm}^{-1}\text{K}^{-1}$)	γ_T ($10^{-4} \text{ Nm}^{-1}\text{K}^{-1}$)	$T(\text{K } (^\circ\text{C}))$	Reference	Method
1.51	-	1940 (1667)	Elyutin et al. [15]	CR
1.41	-	1941 (1668)	Arkhipkin et al. [16]	DC
1.557	-0.156	1943 (1670)	Paradis et al. [17,52]	ESL
1.525	-	1943 (1670)	Vinet et al. [18]	DW/PW
1.475	-	1943 (1670)	Man et al. [19]	PD
1.49	-0.17	1943 (1670)	Brillo et al. [27]	EML-OD
1.588	-	1953 (1680)	Tiele et al. [20]	DW
1.65	-	1953 (1680)	Allen et al. [21]	PD
1.39	-	1953 (1680)	Peterson et al. [22]	PD
1.675	-	1953 (1680)	Kupperman et al. [23]	Levitation
1.58	-2.49	1941 (1668)	Present work	EML-OD
1.54	-1.85	1941 (1668)	Present work	EML-OD
1.56	-0.62	1941 (1668)	Present work	EML-OD

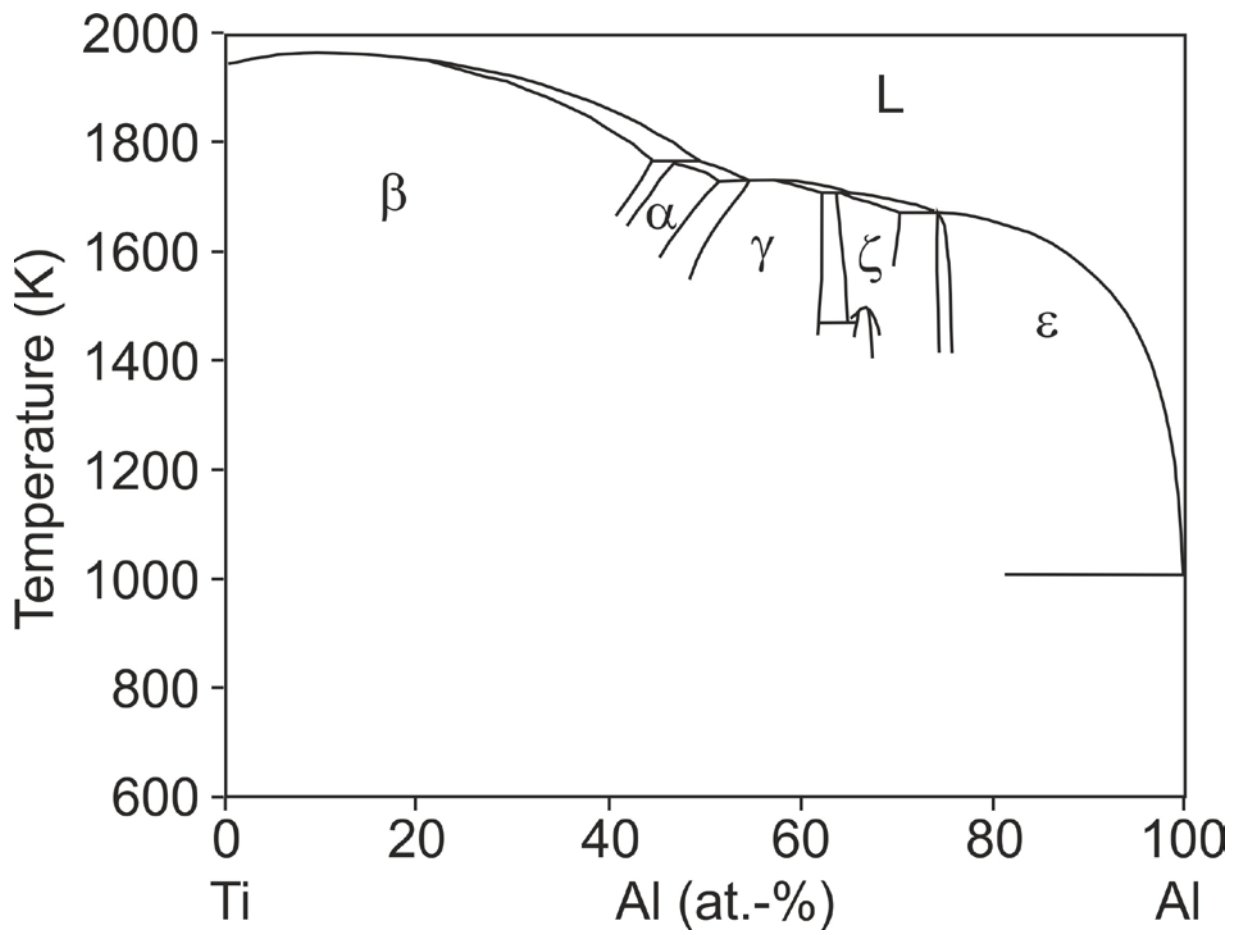


Figure 1

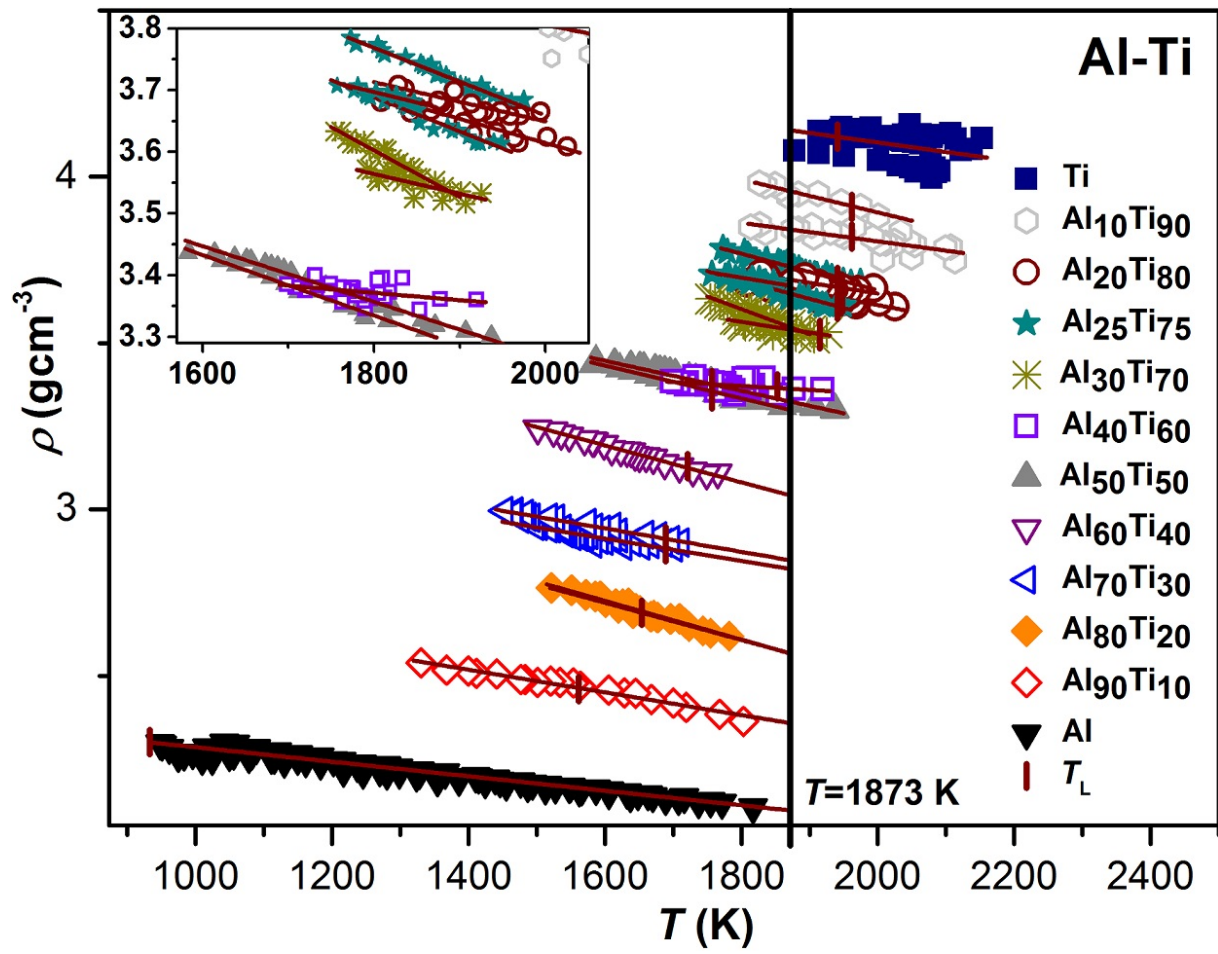


Figure 2

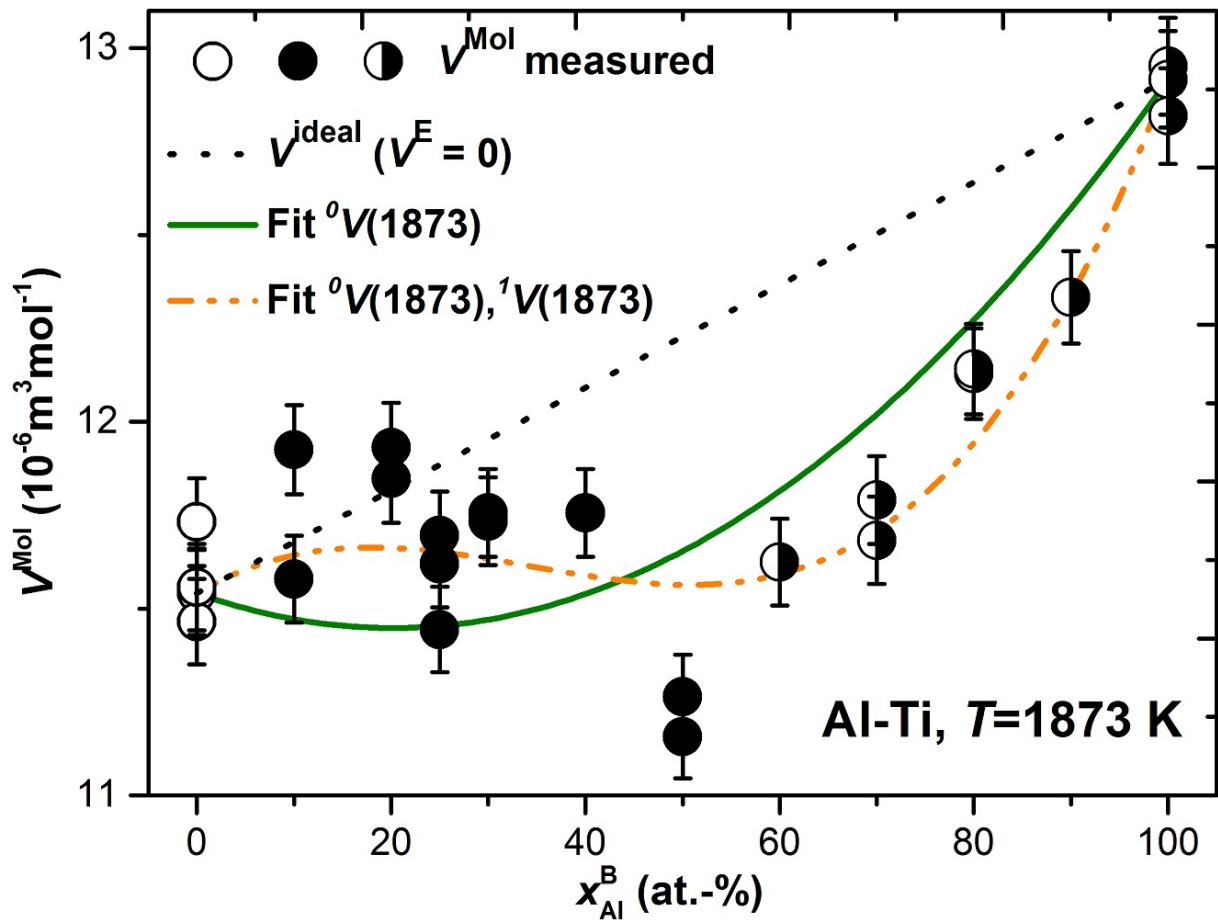


Figure 3

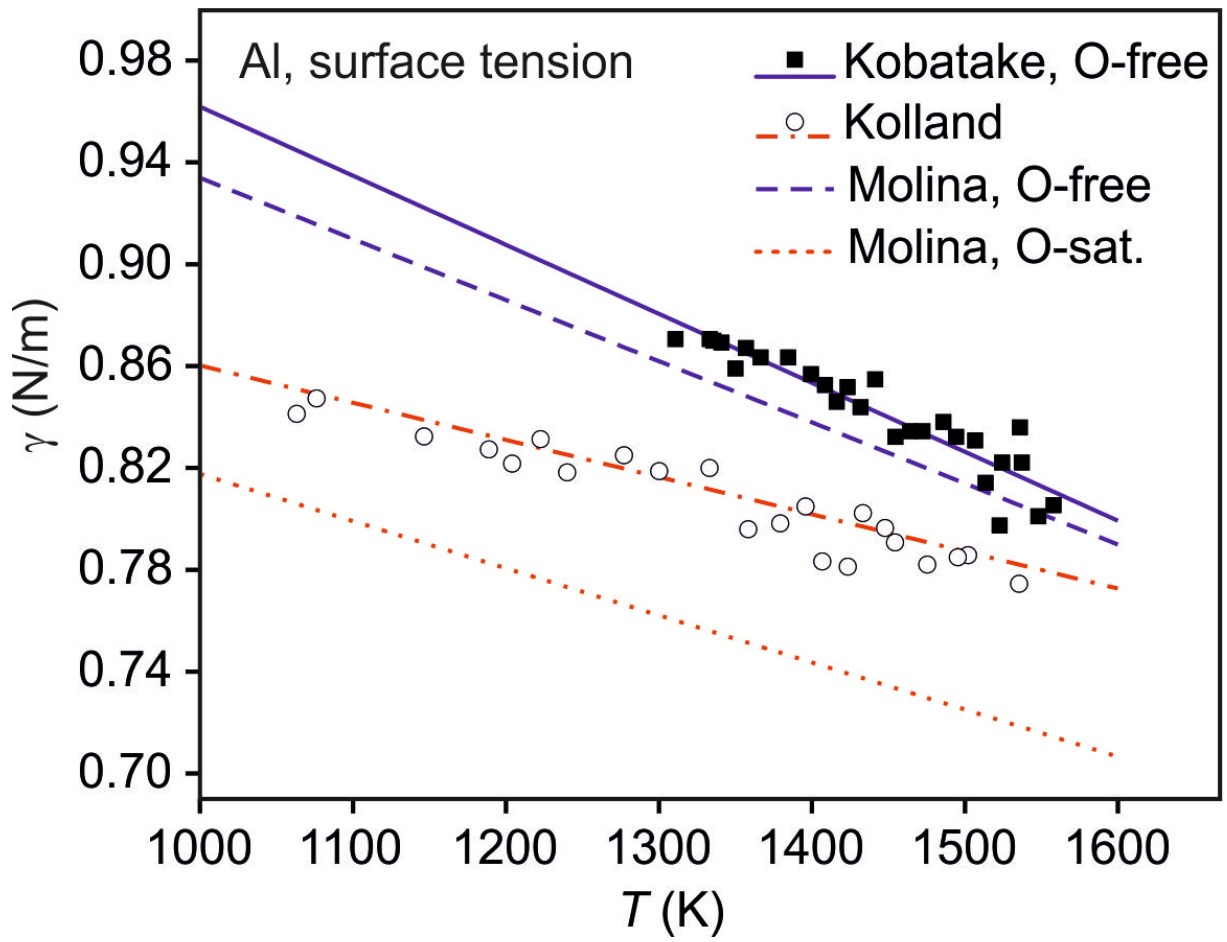


Figure 4

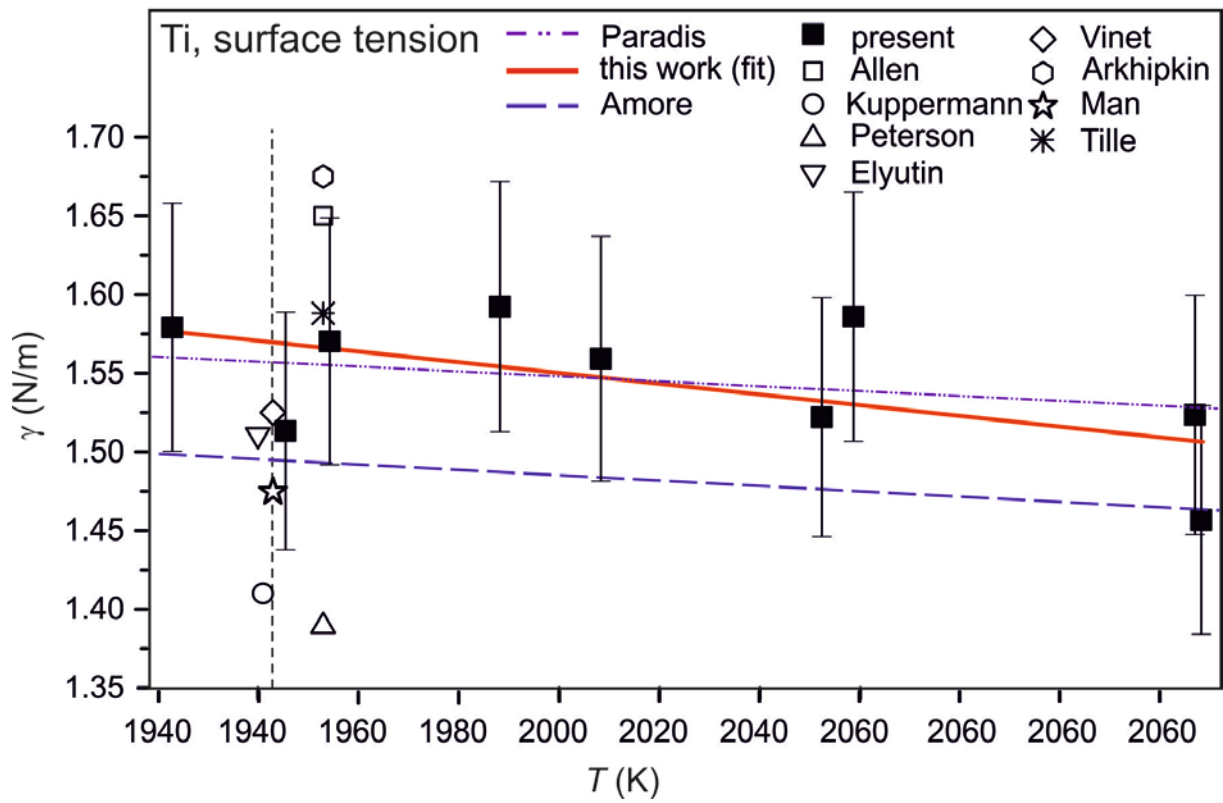


Figure 5

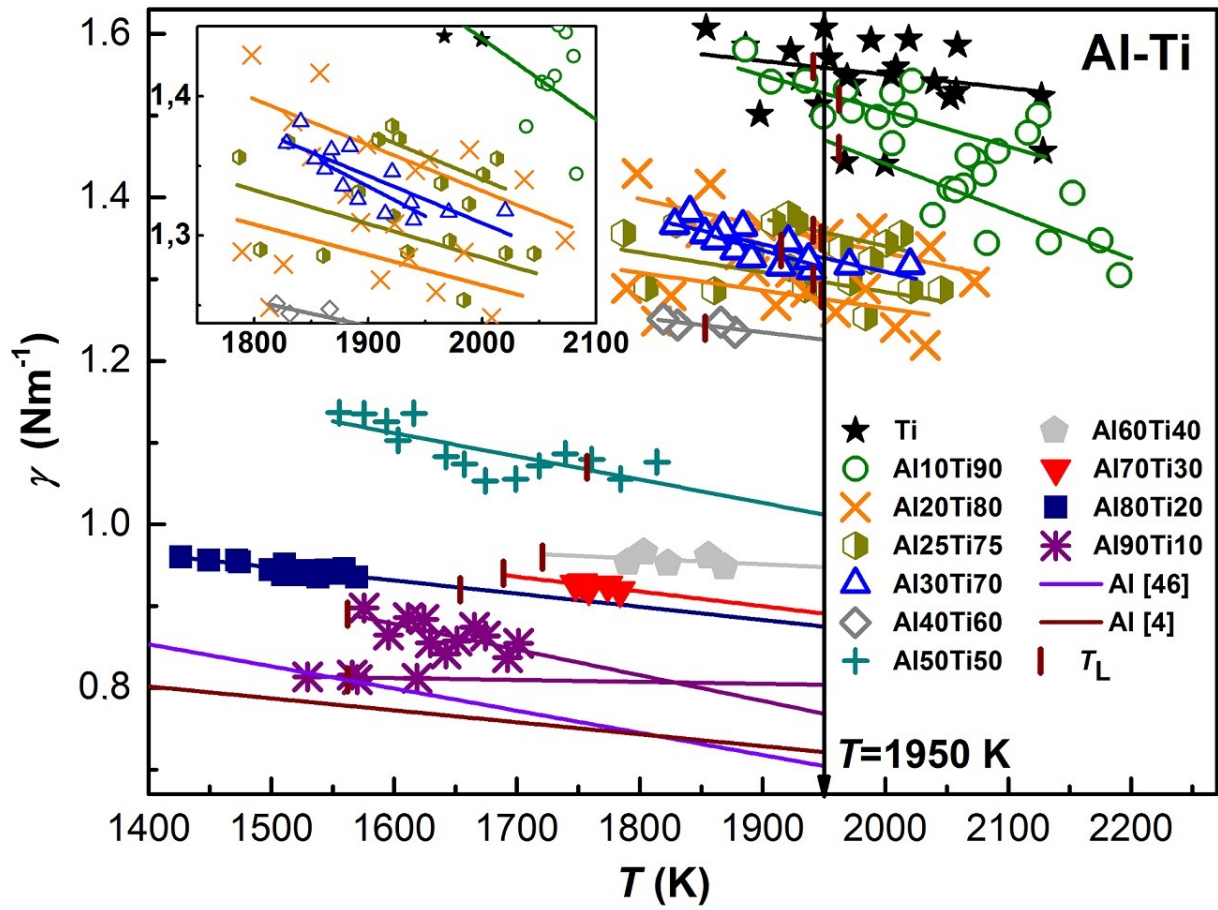


Figure 6

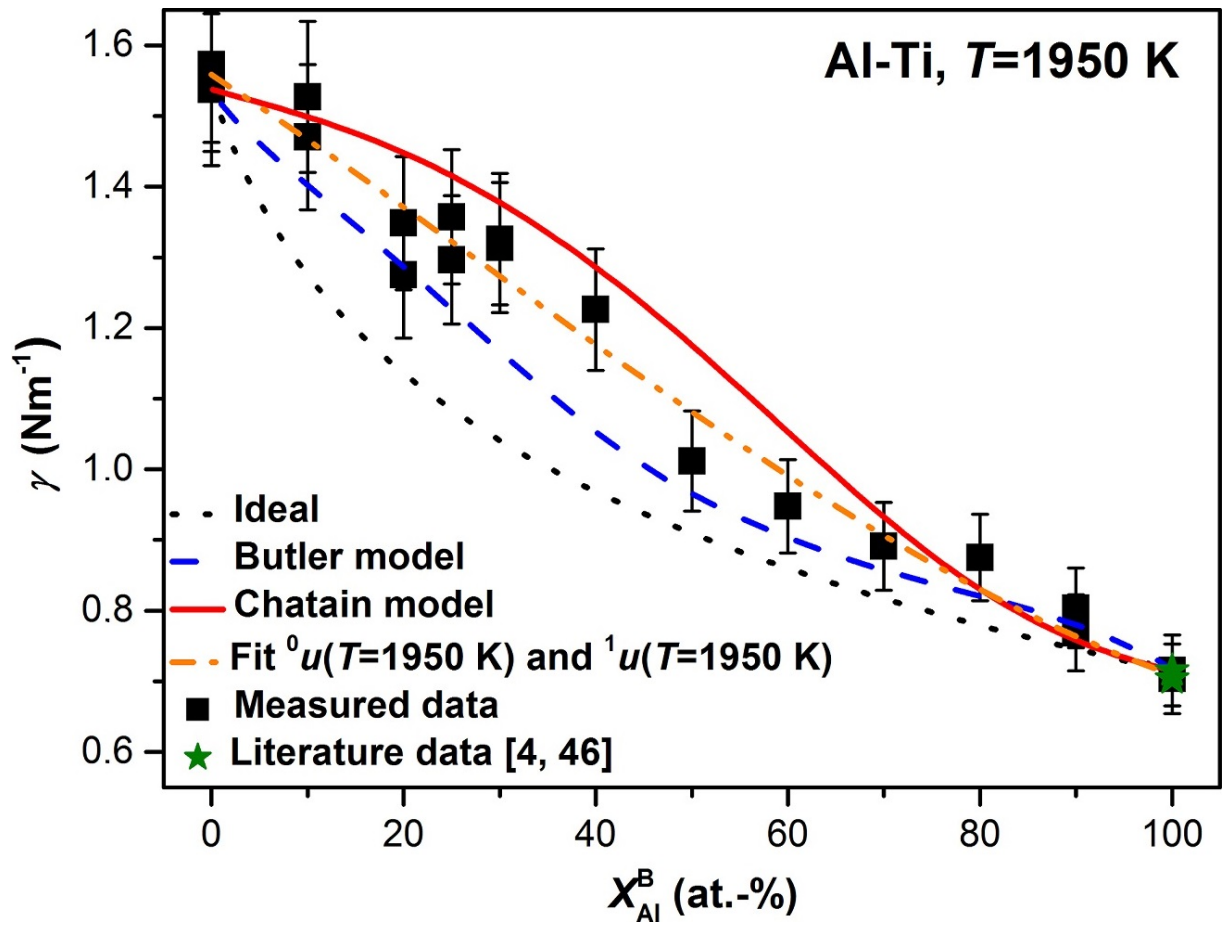


Figure 7

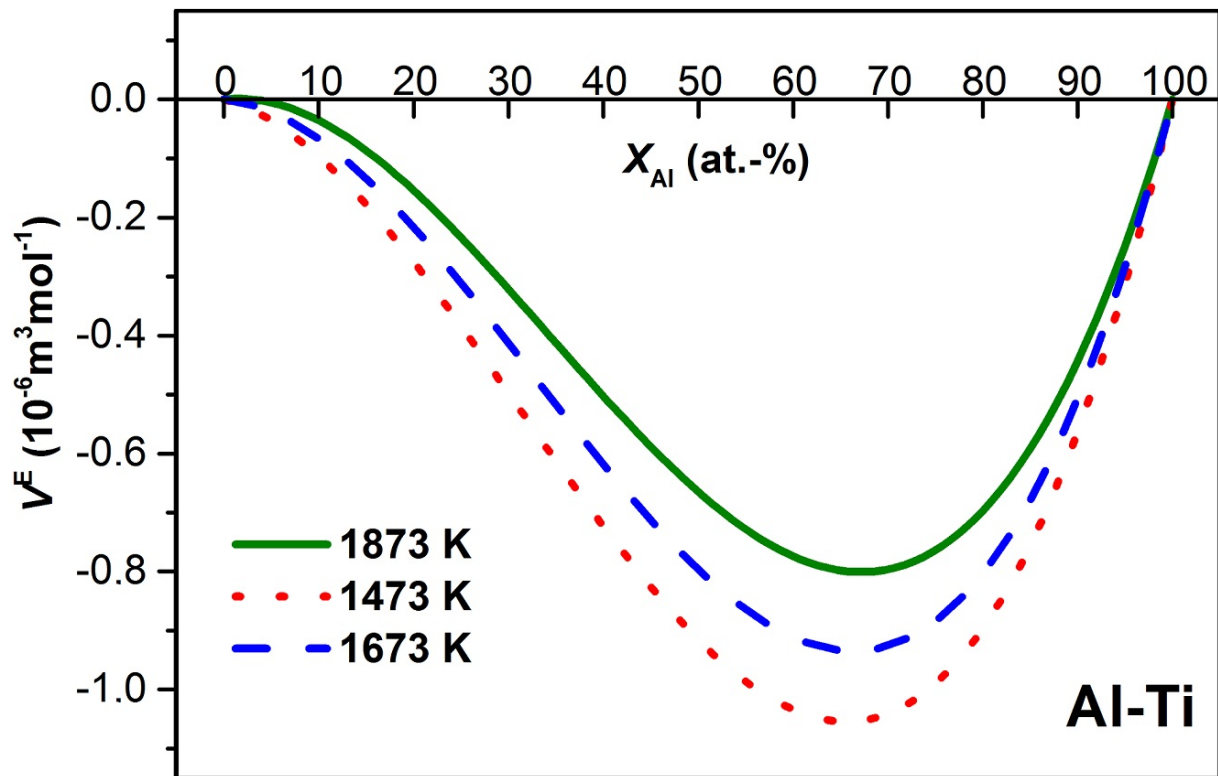


Figure 8

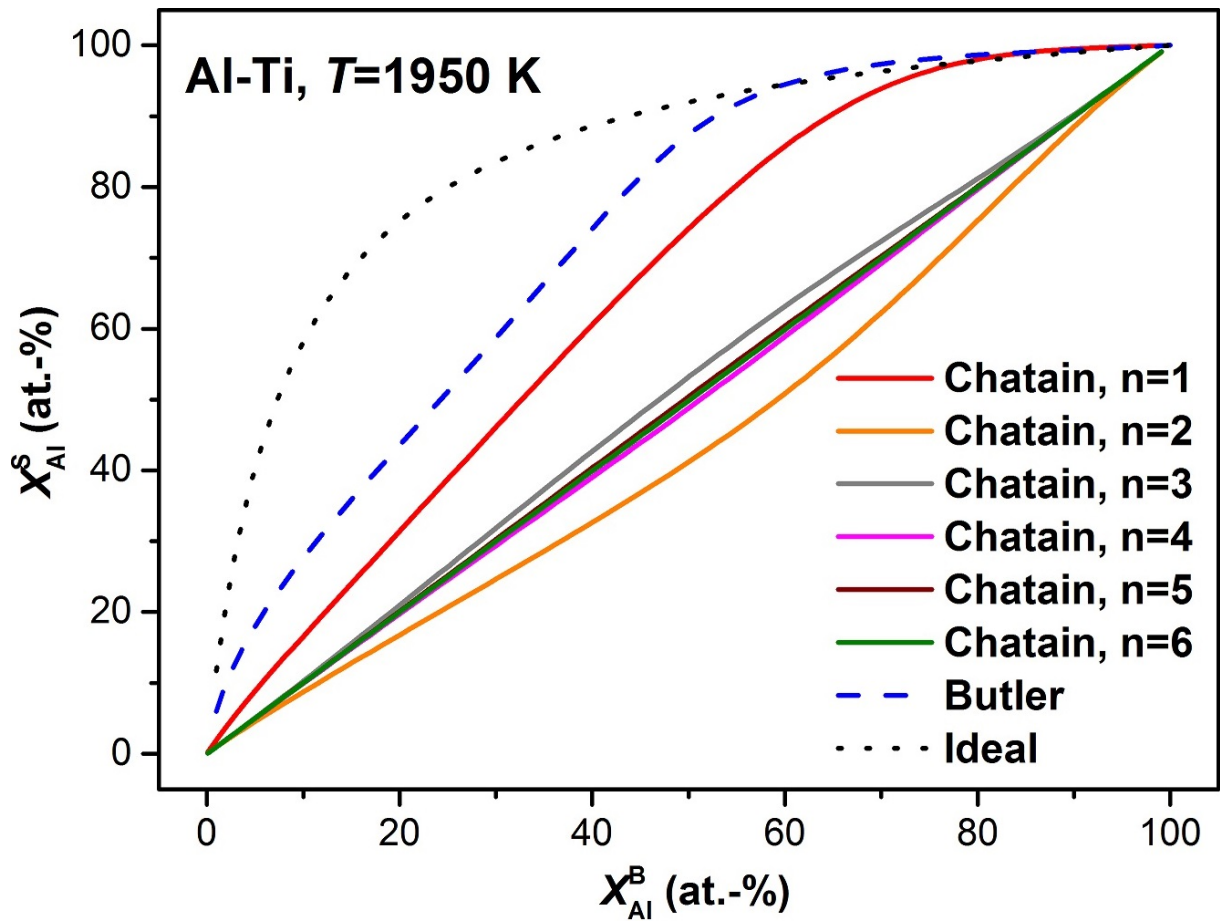


Figure 9

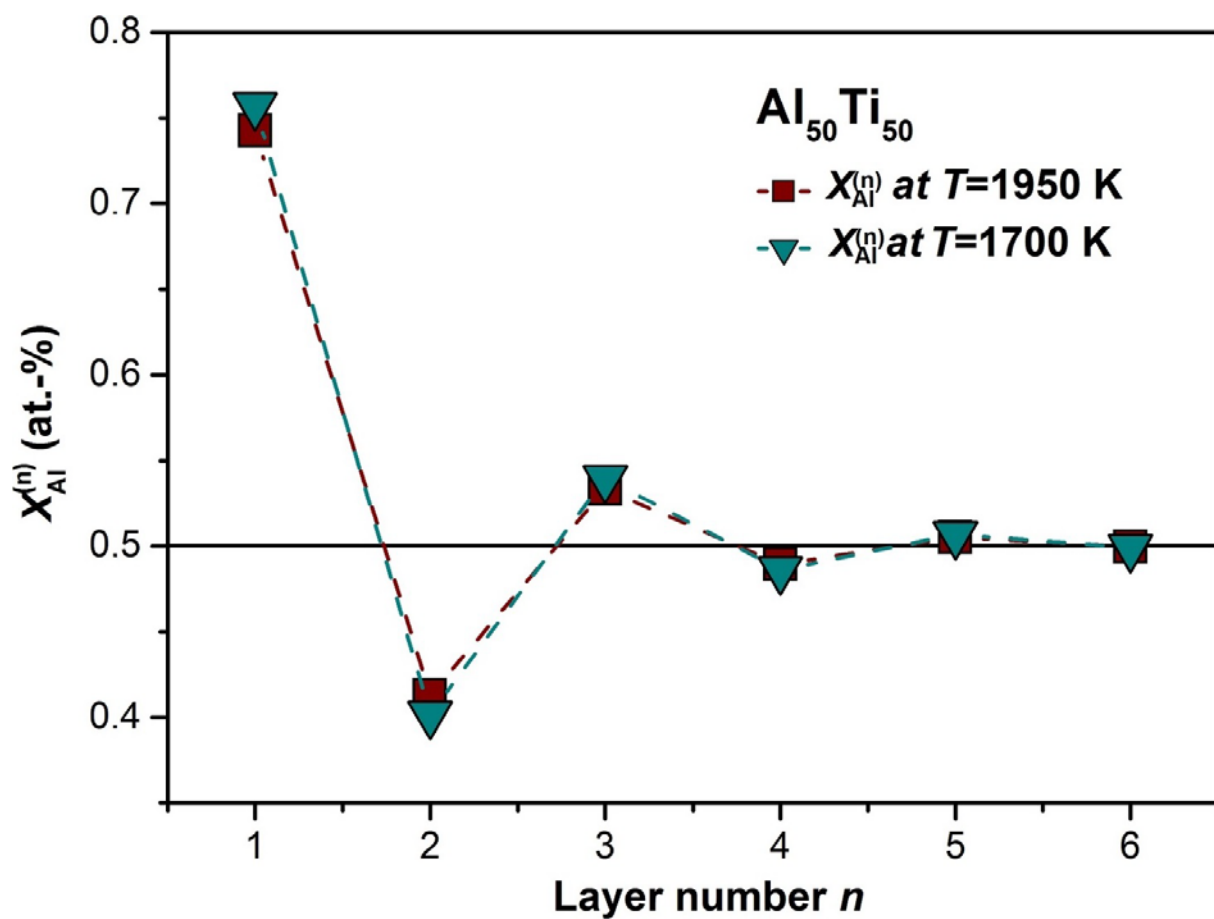


Figure 10

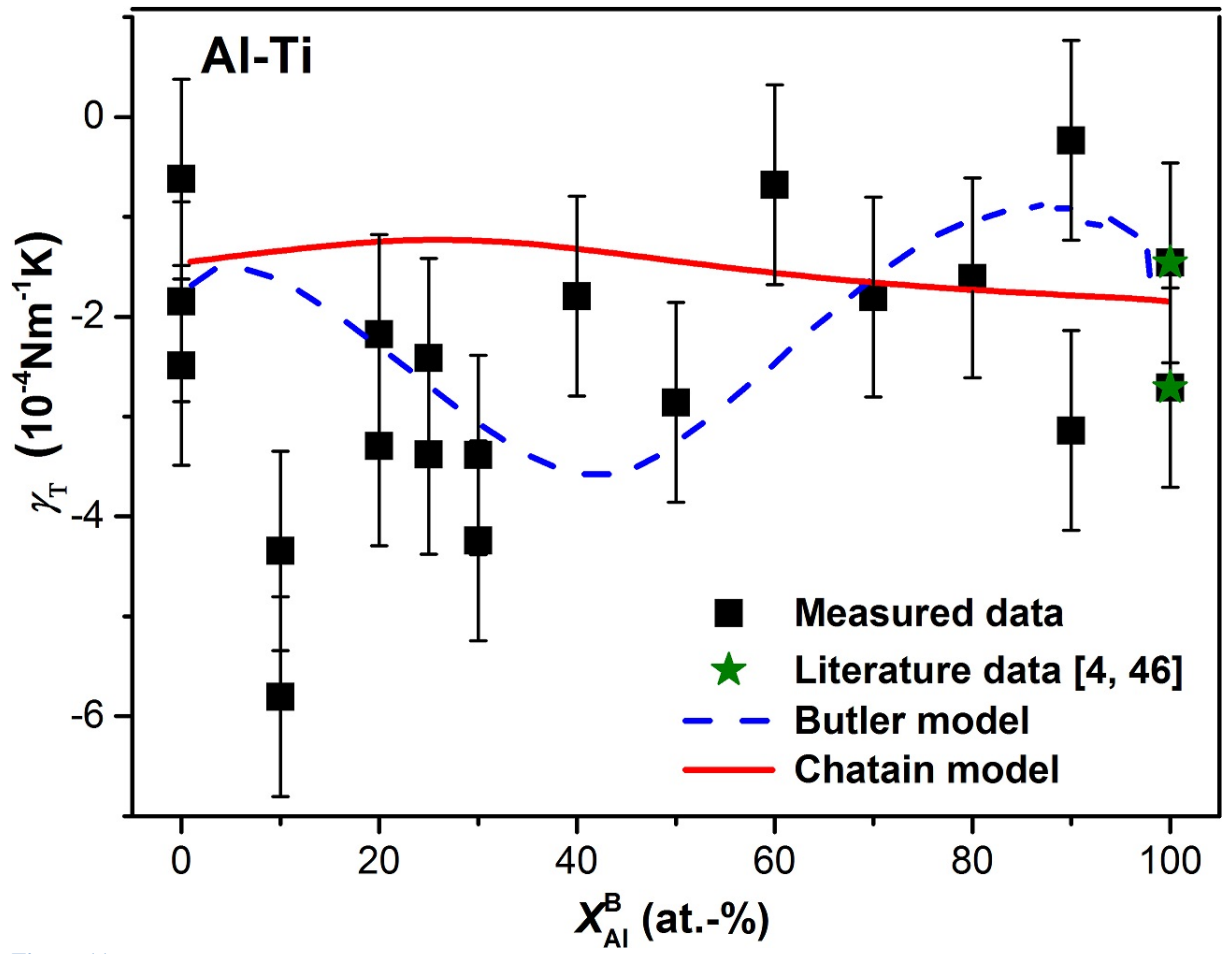


Figure 11

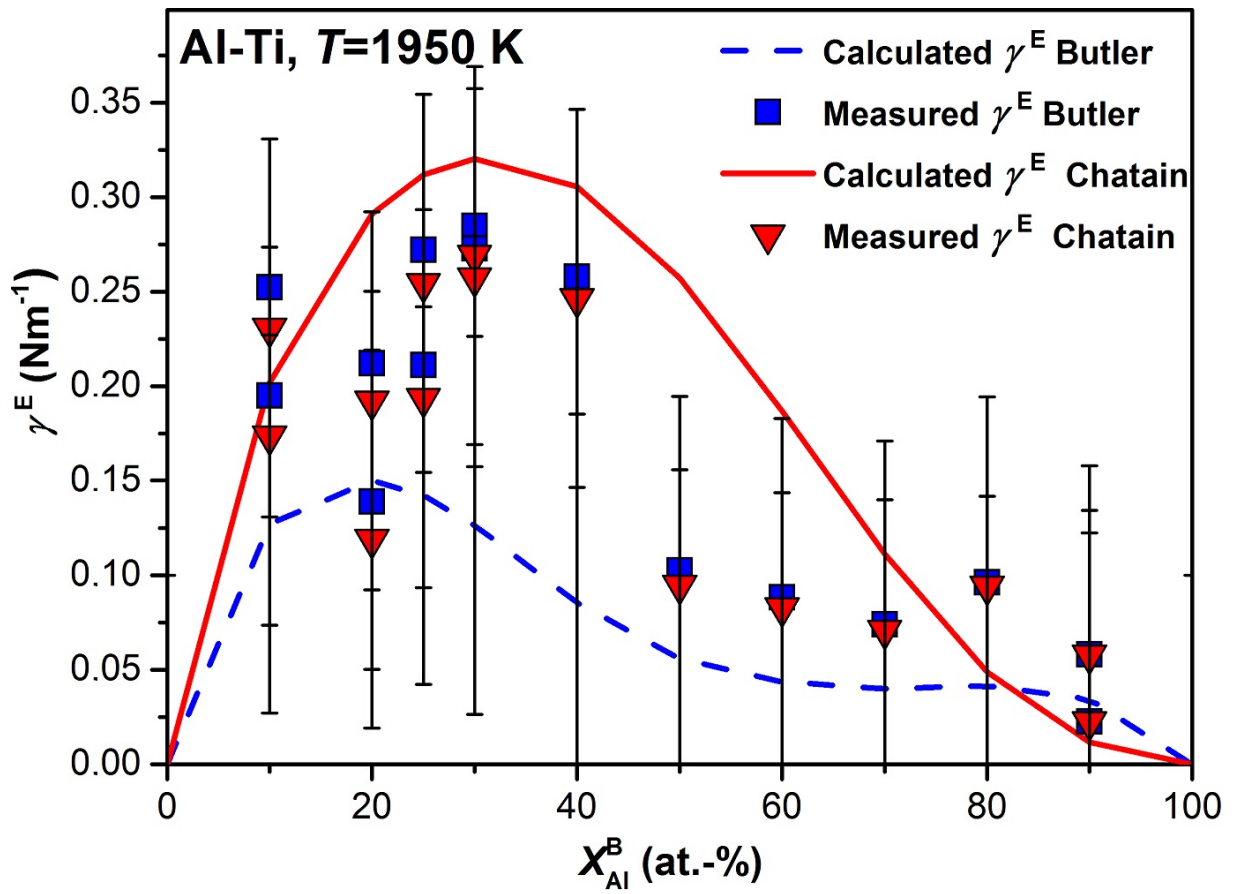


Figure 12

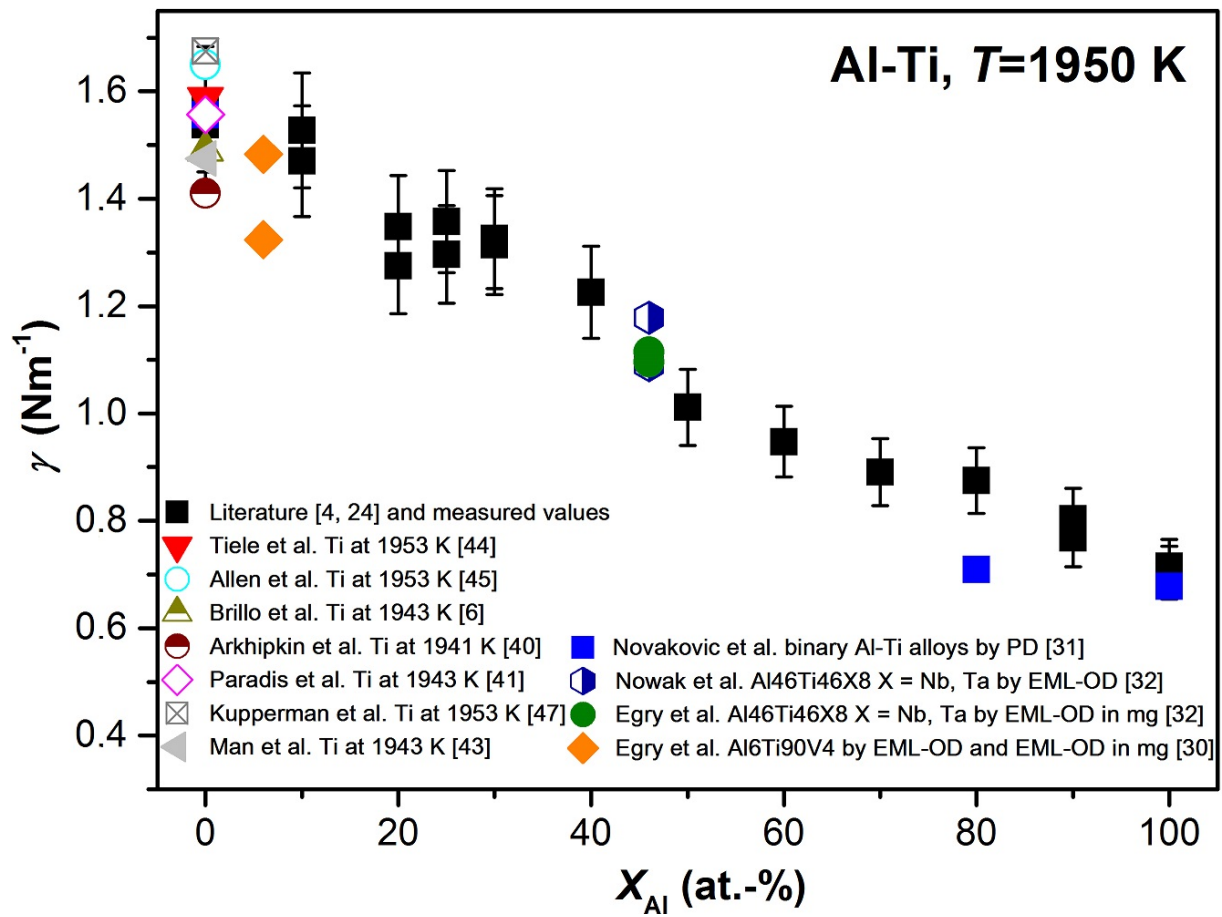


Figure 13