

Global parameterization of trimmed NURBS based CAD geometries

Mesh deformation based on CAD model deformation

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WCCM XII, Seoul
25-Jul-2016

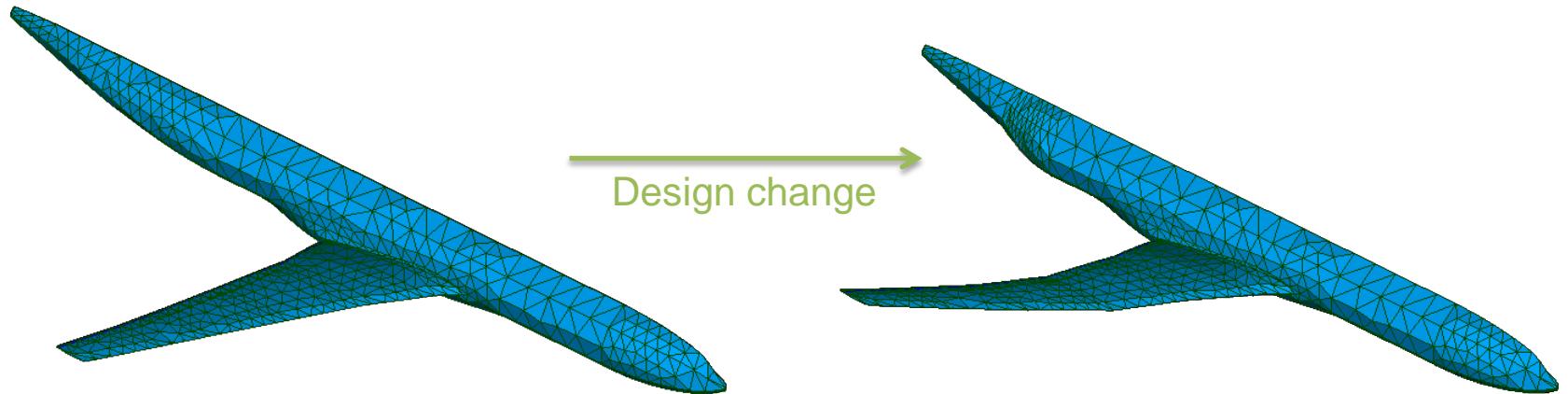
Knowledge for Tomorrow



Motivation

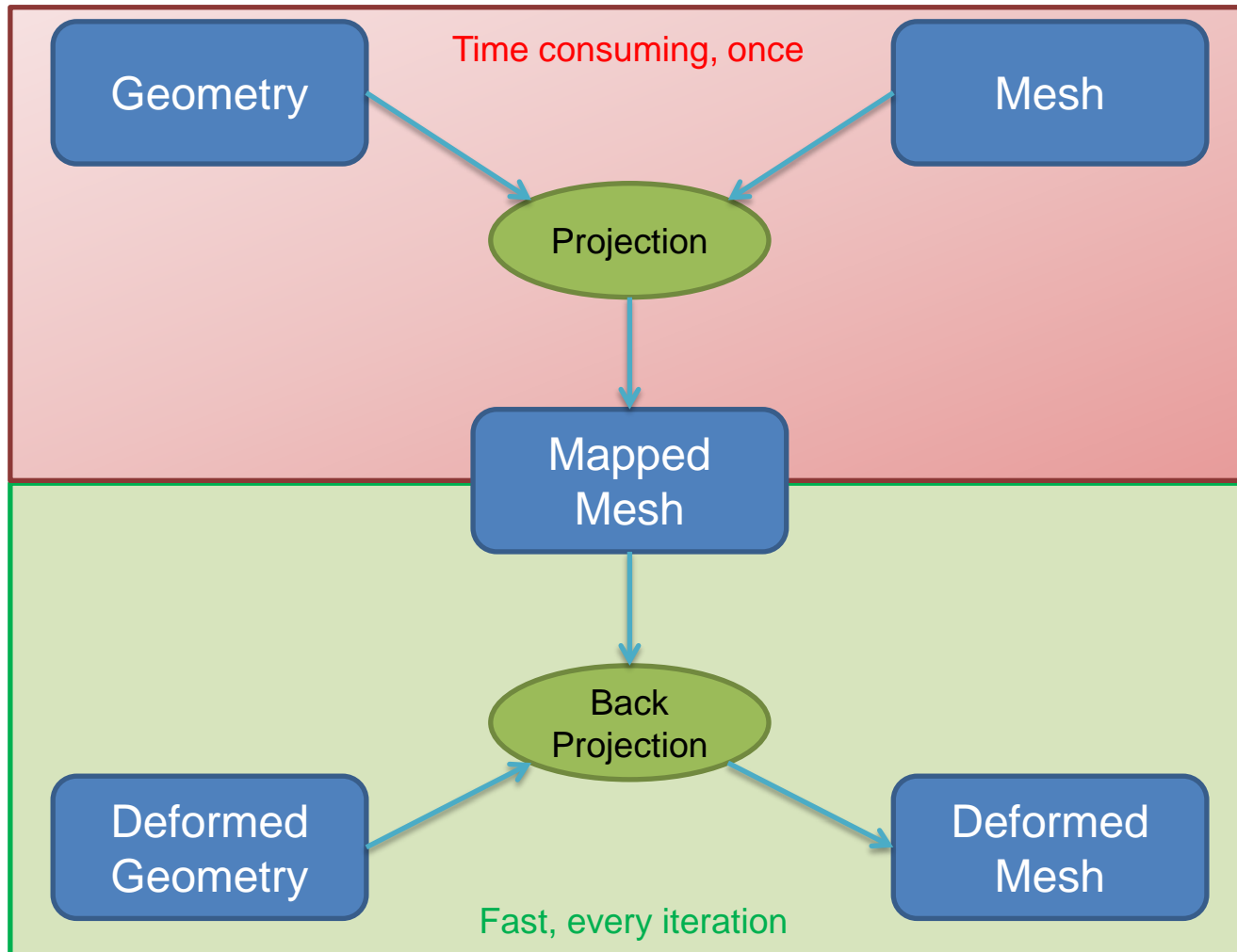
Geometry based mesh deformation

- Fully automatic mesh creation is hard!
- Idea: reuse manually created mesh even for different designs
- Use for gradient based optimization to determine mesh gradient w.r.t design parameters



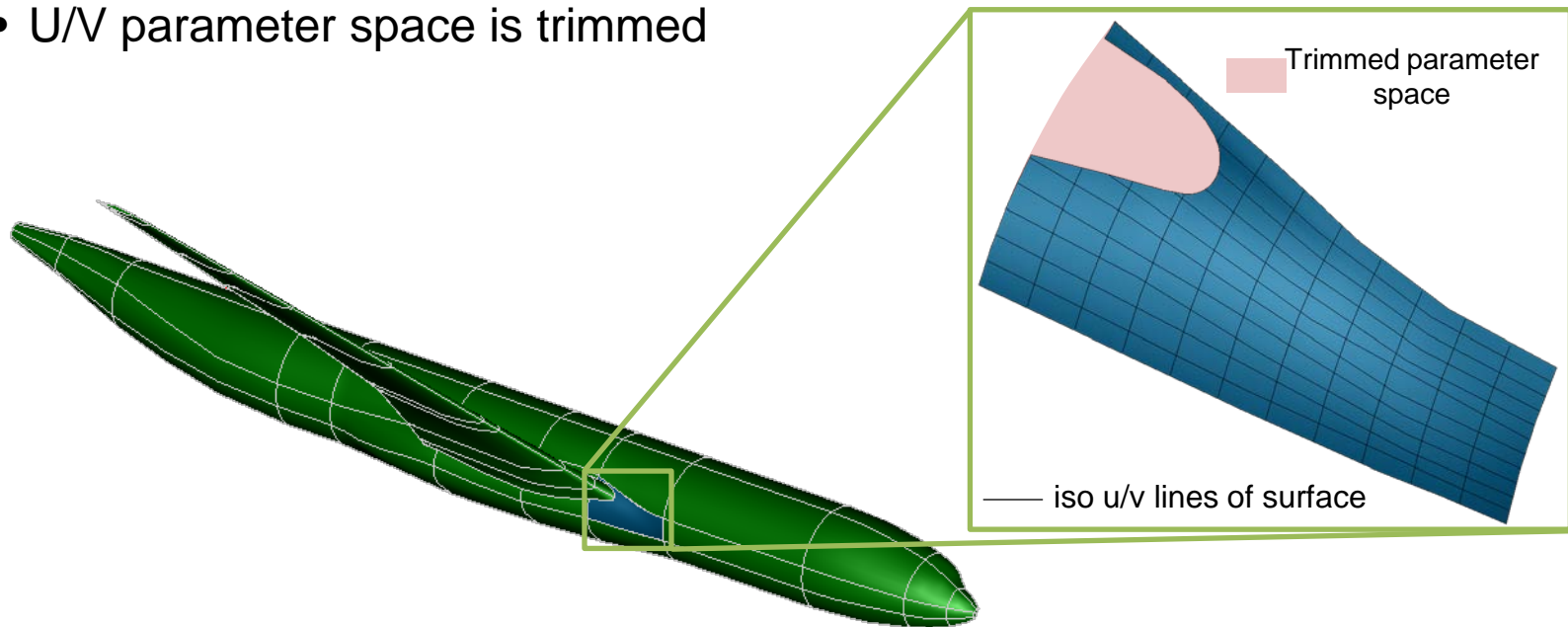
Geometry based mesh deformation

General idea



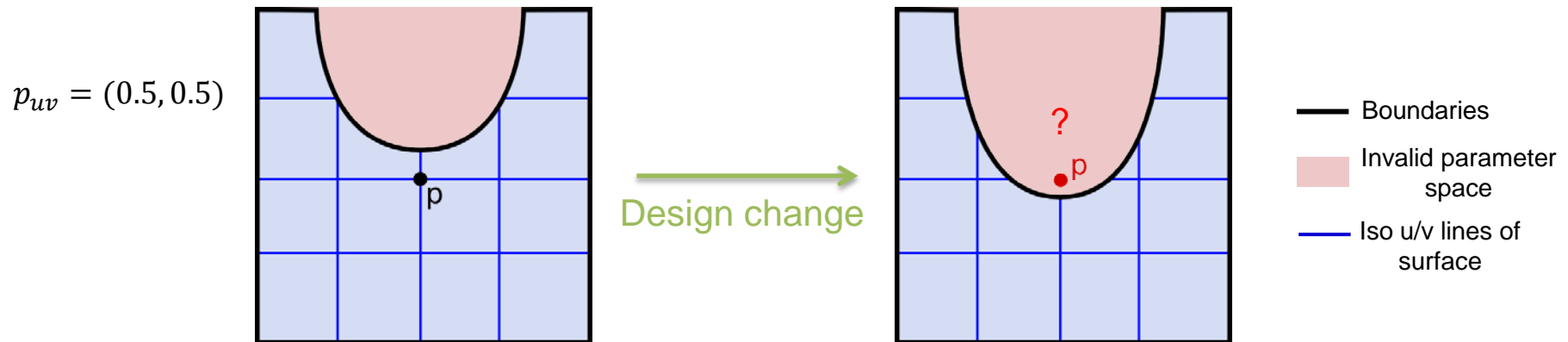
Trimmed NURBS based geometries

- Consists of many panels
- Each panel is a trimmed NURBS
- U/V parameter space is trimmed



The trimmed NURBS parameterization problem

- Trimmed NURBS:
 - Parameter space of surface trimmed by boundary curves

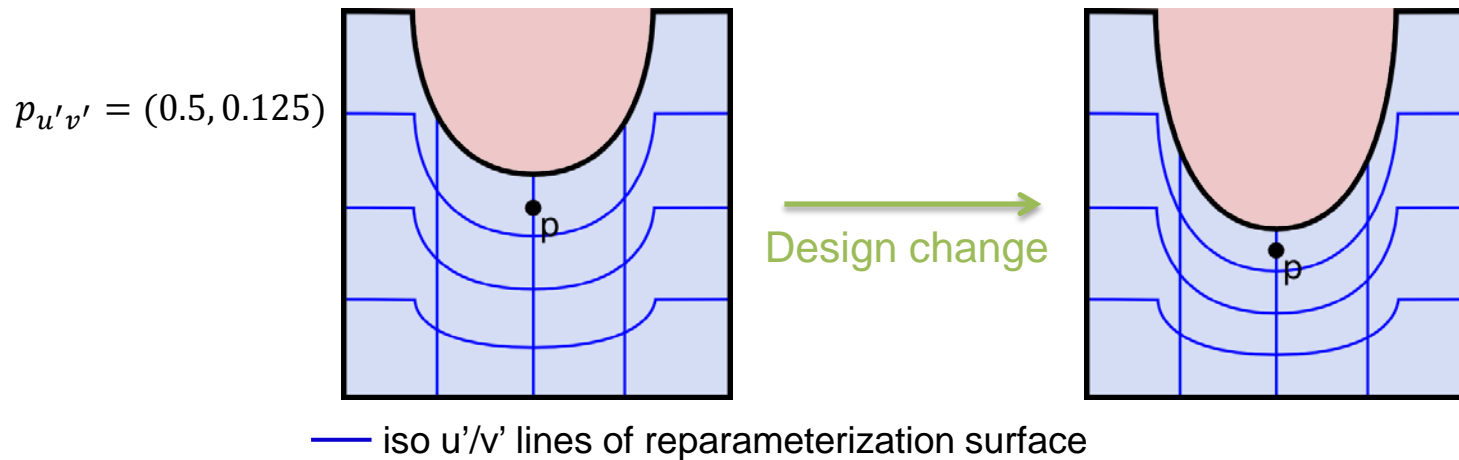


- Mesh points get lost / are outside panel after design change
 - u/v surface coordinates no good choice for mapping



Solution: reparameterization of the parameter space

- Create 2D reparameterization surface that respects boundaries

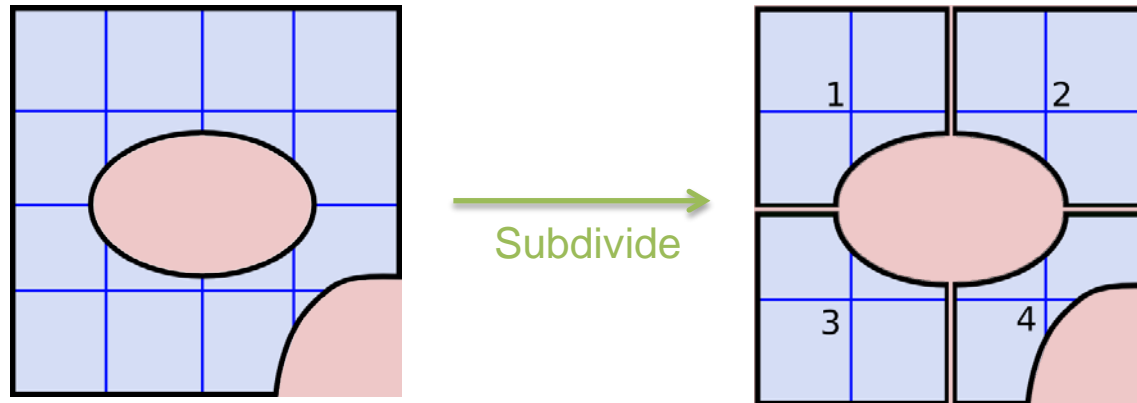


- No loss of mesh points anymore
- Next problem: what to do with holes or complicated boundaries?



The trimmed NURBS parameterization problem

- Panels with complicated boundaries can not be reparameterized with one surface!



- Solution: subdivision of the panel into multiple sub-surfaces
- Reparameterize each sub-surface



Projection / Back projection

- **Projection:**

$$\vec{P} \in \mathbb{R}^3 \rightarrow i, j, u', v'$$

with:

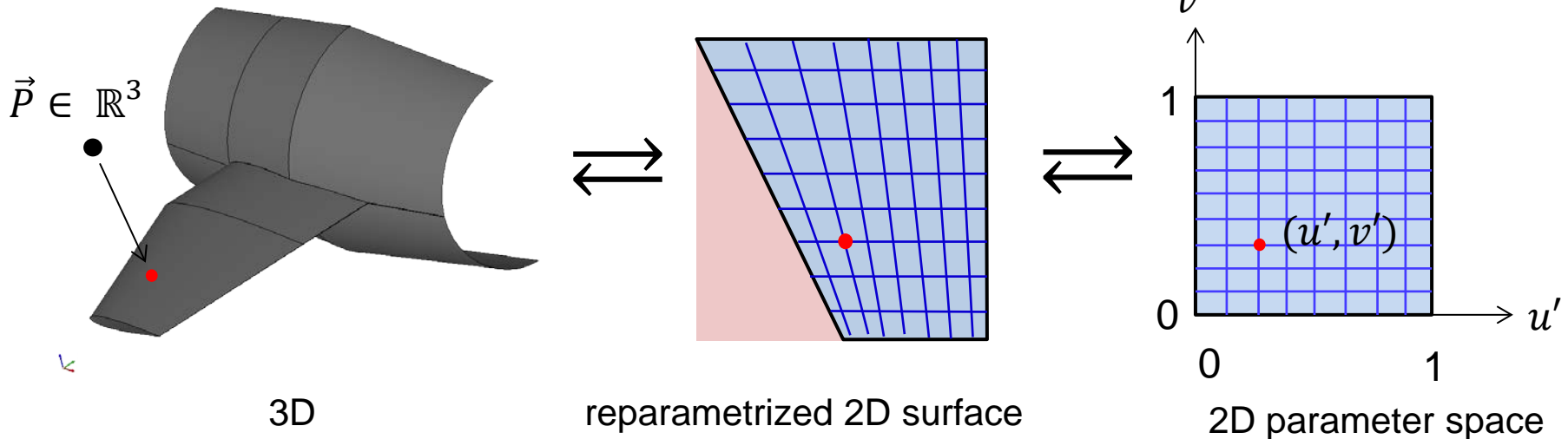
i : panel index

j : sub-surface index

$u', v' \in [0,1]$

- **Back projection:**

$$i, j, u', v' \rightarrow \vec{P} \in \mathbb{R}^3$$

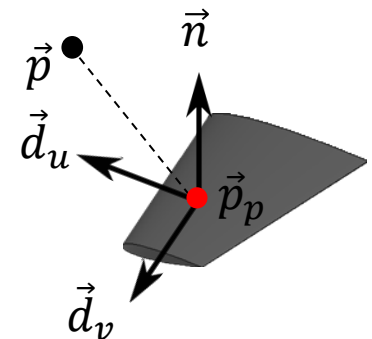


Improvement: Exact back projection

- Motivation:
 - Geometry changes are very small for finite differences
 - Mesh points may not exactly lie on the original geometry
- Requirement: Invariant geometries should result in exactly the same mesh
- Solution:
 1. Project point \vec{p} onto surface
 2. Create local coordinate system (CS) from $\vec{d}_u, \vec{d}_v, \vec{n} = \vec{d}_u \times \vec{d}_v$
 3. Store also the deviation of projected point \vec{p}_p in the local CS

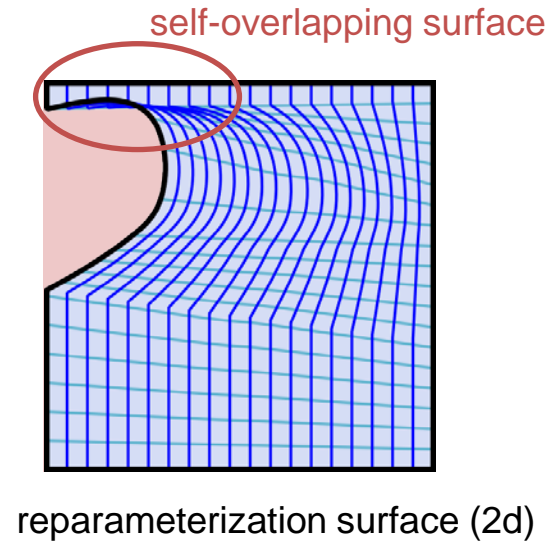
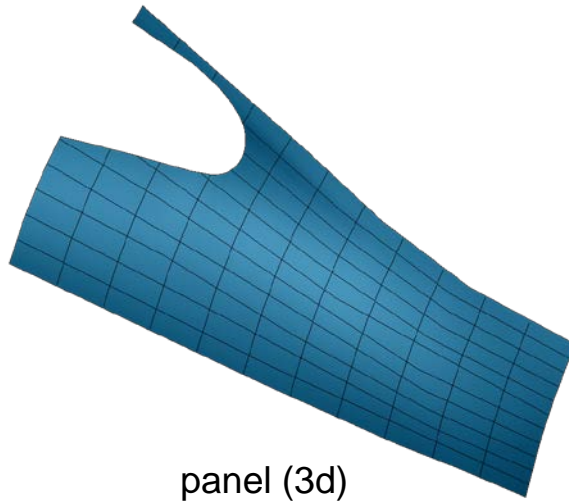
$$\vec{p} - \vec{p}_p = dn \cdot \vec{n} + du \cdot \vec{d}_u + dv \cdot \vec{d}_v$$

- (Back)Projection: $\vec{P} \in \mathbb{R}^3 \leftrightarrow i, j, u', v', dn, du, dv$



Uniqueness of projection

- Reparameterization surfaces can self-overlap



- Issue: Projection is not unique → multiple solutions !
- Resulting mesh might be invalid



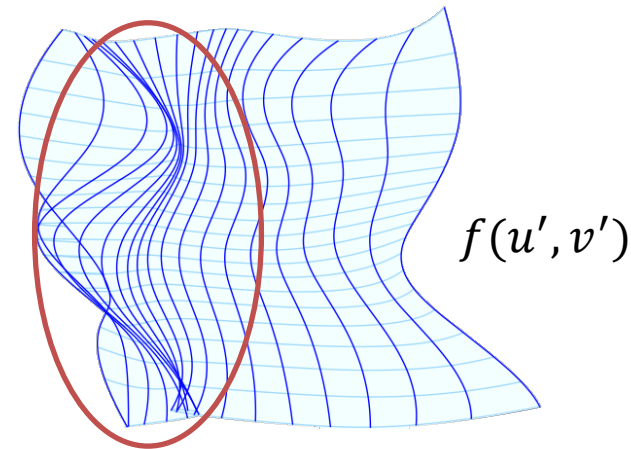
Uniqueness of projection

Invertibility of reparameterization surfaces

- Reparameterization surface $f(u', v') \rightarrow (u, v)$ must be invertible

➤ there must exist inverse function f' , with

$f'(u, v) \rightarrow (u', v')$, $u', v' \in [0, 1]$, u, v inside trimmed parameter space



- If invertible, projection is unique 🙌

- How to check existence of $f'(u, v)$?



Uniqueness of projection

Invertibility criterion

- Jacobi determinant (i.e. Z-component of normal vector) must not be negative, i.e.

$$\det J(u', v') \stackrel{\text{def}}{=} \left[\frac{\partial}{\partial u'} f(u', v') \times \frac{\partial}{\partial v'} f(u', v') \right]_z \geq 0, \forall u', v' \in [0, 1]$$

- Jacobi determinant of Bezier patch is 1d Bezier surface:

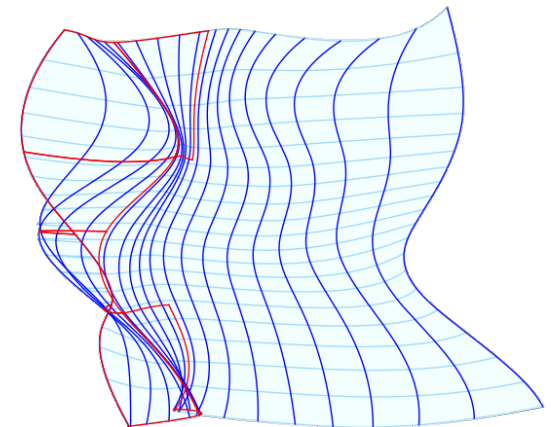
- control points T_{pq} can be computed according to *, eq. (11)

- Convex hull property: $\det J(u', v') \geq 0$, if $T_{pq} > 0$

➤ Split reparameterization surface f into Bezier patches

➤ Inspect control points for positivity

- But: false positives possible!



Non-invertible Bezier patches

*Lin, Hongwei et al. 2007: Generating strictly non-self-overlapping structured quadrilateral grids

Implementation details

- Written in C++ as a library
- Library offers functions to
 - Perform projection and back-projection of points
 - Import CAD models (IGES, Step, BREP)
 - Check invertibility of each sub-surface
 - Distribute the geometry to each node of a cluster
 - Compare the topology of two CAD models
- Uses the OpenCASCADE Technology* CAD library

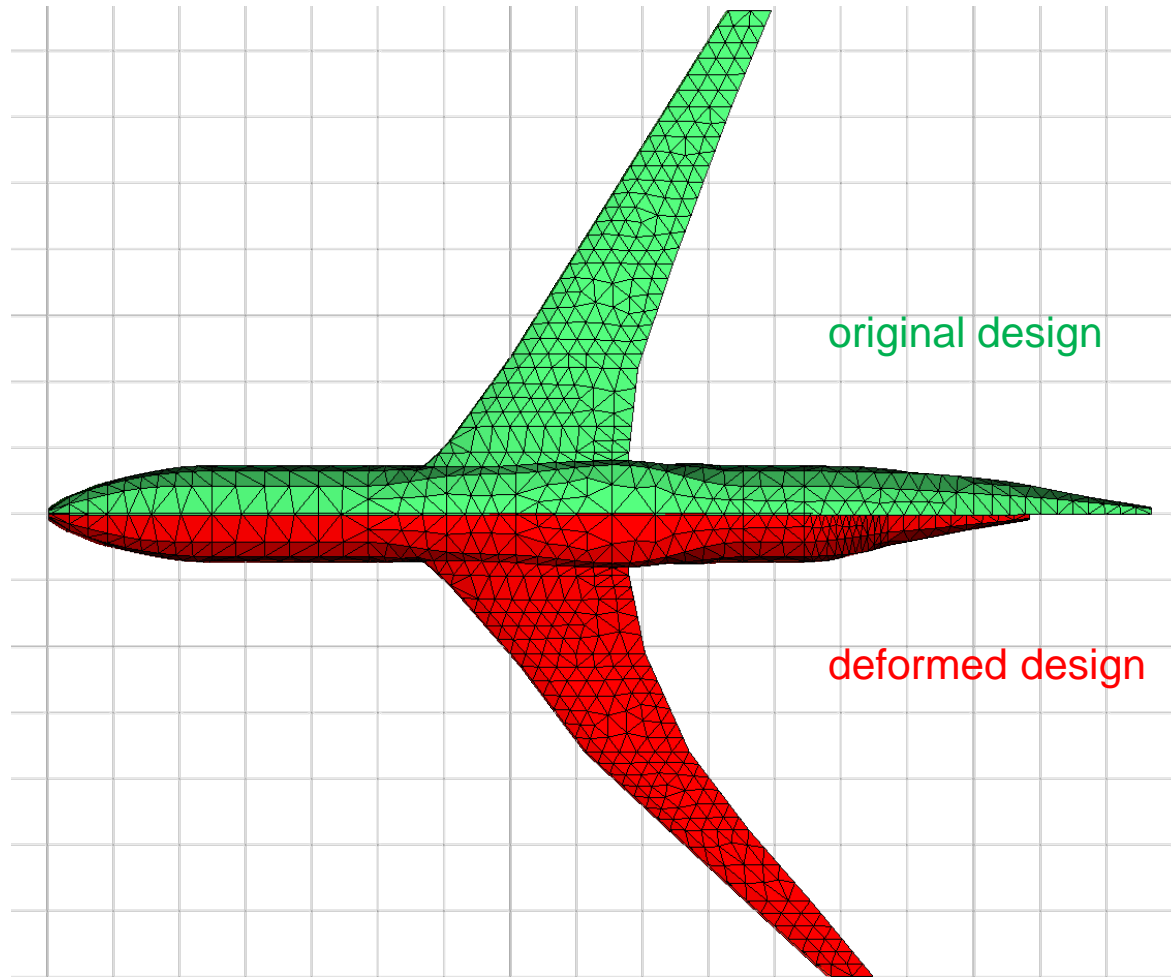


Results

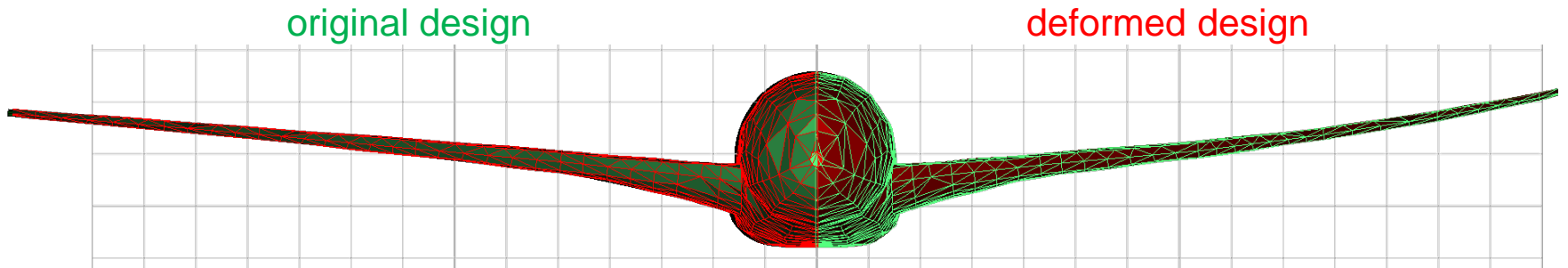
- Algorithm currently used at Airbus D&S for FEM based structural analysis
- Currently used in DLR for CFD simulations with structured meshes in the DLR internal project VicToria*:
 - Adjoint CFD solver TAU requires mesh gradients (i.e. how does the mesh change with some design parameter change)
 - This method suitable to compute the gradients
- Method not suitable for large design changes:
 - Topology of panels and boundaries must not change!



Results



Results



Summary + Outlook



Questions



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