

1 Correlation of gravestone decay and air quality 1960-2010

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12 Highlights

- 13 • Gravestone decay provides a quantitative measure of acid flux
- 14 • Land use strongly correlated with spatial variability in gravestone decay
- 15 • Pronounced increase in deposition efficiency of sulfur dioxide (SO₂) after about 1980

16 Abstract

17 Evaluation of spatial and temporal variability in surface recession of lead-lettered Carrara
18 marble gravestones provides a quantitative measure of acid flux to the stone surfaces and is
19 closely related to local land use and air quality. Correlation of stone decay, land use, and air
20 quality for the period after 1960 when reliable estimates of atmospheric pollution are available
21 is evaluated. Gravestone decay and SO₂ measurements are interpolated spatially using
22 deterministic and geostatistical techniques. A general lack of spatial correlation was identified
23 and therefore a land-use-based technique for correlation of stone decay and air quality is
24 employed. Decadally averaged stone decay is highly correlated with land use averaged spatially
25 over an optimum radius of ≈7 km even though air quality, determined by records from the UK
26 monitoring network, is not highly correlated with gravestone decay. The relationships among
27 stone decay, air-quality, and land use is complicated by the relatively low spatial density of both
28 gravestone decay and air quality data and the fact that air quality data is available only as
29 annual averages and therefore seasonal dependence cannot be evaluated. However, acid
30 deposition calculated from gravestone decay suggests that the deposition efficiency of SO₂ has
31 increased appreciably since 1980 indicating an increase in the SO₂ oxidation process possibly
32 related to reactions with ammonia.

33 **Key Words:** Gravestone decay; acid deposition; air quality; land use, West Midlands;
34 United Kingdom, SO₂ deposition velocity.

35 1. Introduction

36 From the onset of the Industrial Revolution until the environmental revolution of the 1970s
37 Britain was plagued by air pollution from industrial, urban, and residential sources (Sale and
38 Foner, 1993; McCormick, 2013). The largest contributors to air pollution were particulate
39 matter (smoke) and acid in the form of oxides of nitrogen (NO_x) and sulfur (SO_x) compounds,
40 particularly sulfur dioxide (SO_2). (Marsh, 1978; Bricker and Rice, 1993). As early as the 1840s
41 there were efforts to measure air pollution in British cities (Moseley, 2009) and Smith (1876)
42 determined that the burning of coal was the principle source of “acid rain.” It was not until
43 about 1960 that the network was greatly expanded with the establishment of the National
44 Survey, which measured daily smoke and sulfur concentrations at over 500 locations (Moseley,
45 2009). Prior to 1960, air quality measurements were limited in spatial and temporal coverage
46 and often described anecdotally, particularly during severe air quality events. Proxy records
47 have been used to reconstruct air quality; these records include physical descriptions (Allen
48 1966; Allen 1994; Auliciems and Burton, 1973; Fenger, 2009), particulates in lung tissue samples
49 (Hunt et al. 2003) and sediment cores (Kelly and Thornton, 1996), and lake acidification studies
50 (Battarbee and Renberg, 1990; Battarbee et al., 1990). Air quality measurements are of great
51 interest in studies of ambient environmental conditions (Urone and Schroeder, 1969; Eggleston
52 et al., 1992; Leck and Rodhe, 1989; Fenger, 2009), efficacy of environmental regulation, and
53 health related studies of mortality and morbidity related to acute and chronic respiratory
54 ailments (Macfarlane, 1977; Spix et al. 1993; Ito et al. 1993; Greenstone, 2004).

55 A proxy that has been used successfully to evaluate historical trends in acid deposition is
56 surface recession of Carrara marble gravestones (Cooke 1989; Cooke et al., 1995; Dragovich,
57 1991; Inkpen, 1998, 2013; Inkpen and Jackson, 2000; Inkpen et al., 2000, 2001, 2008, in press;
58 Meierding, 1981; Mooers et al., 2016; Mooers and Massman, in press; Thornbush and
59 Thornbush, 2013; Viles, 1996), hereafter referred to as gravestone decay to be consistent with
60 the body of recent literature. Mooers et al. (2016) report on a 120-year record of acid
61 deposition in the West Midlands, UK, reconstructed from lead-lettered marble gravestone
62 decay. Their record is compiled from measurements on nearly 600 lead-lettered marble

63 gravestones and they demonstrate that gravestone decay is a robust measure of acid
64 deposition. However, the correlation between acid deposition and available air quality data is
65 more tenuous (Inkpen, 2013; Inkpen et al., in press) and can be influenced by numerous factors
66 (Wesley and Hicks, 1977; Schaefer et al., 1992). Therefore the goal of this study is to explore the
67 relationship between gravestone decay and air quality. Correlation between air quality (SO₂ and
68 smoke) and gravestone decay would then allow quantitative estimation of air quality for earlier
69 periods of time where lead-lettered marble gravestones are available but atmospheric
70 concentrations of pollutants were not measured.

71 The correlation between surface recession of lead-lettered, Carrara marble gravestones and
72 annually averaged atmospheric SO₂ and smoke measurements in the West Midlands, UK, for
73 the period 1960-2010 is evaluated. The study area includes West Midlands County and
74 surrounding portions of Staffordshire, Worcestershire, and Warwickshire (Figure 1). The
75 industrial and residential development of the area is well documented, there is a large number
76 of cemeteries (Figure 1A) with lead-lettered marble gravestones, and a network of air quality
77 monitoring stations was in place by 1960 (Figure 1B) (Mosley, 2009, 2011). Decadally averaged
78 rates of gravestone decay and measured SO₂ and smoke are interpolated spatially for the
79 period after 1960 and correlation between them is evaluated. Interpolation techniques include
80 deterministic and geostatistical methods; however, because of a high degree of spatial non-
81 stationarity and anisotropy in gravestone decay and limited spatial and temporal coverage of
82 air quality measurements, there is great uncertainty in the interpolated values and correlation
83 between stone decay and air quality is poor.

84 Because acid deposition is directly related to proximity of sources of SO₂ and NO_x, a land-
85 use based approach for correlation of gravestone decay rates with air quality is developed.
86 Sensitivity and optimization analysis were used to determine the optimum radius of influence
87 of land use on gravestone decay and weighting factors for interpolating intermediate values of
88 decay. In addition, if stone decay is assumed to result primarily from deposition of sulfuric acid
89 then stone decay rates are functions of the production rate of sulfuric acid from SO₂ oxidation.
90 The relationship between stone decay and atmospheric concentration is nonlinear, suggesting a

91 marked increase in the efficiency of the oxidation process of SO₂ after about 1980. The aim of
92 this investigation is therefore to determine the efficacy of gravestone decay in spatially and
93 temporally integrating and recording air quality and explore the nonlinearity of the SO₂
94 oxidation process.

95 **2. Methods**

96 Mooers et al. (2016) examined the spatial and temporal pattern of acid deposition over the
97 period 1890-2010 from decay of lead-lettered Carrara marble gravestones. Their dataset
98 includes 1417 individual measurements on 591 tombstones in 33 cemeteries collected between
99 2005 and 2010. The current investigation assesses the correlation of acid deposition and air
100 quality and is more restricted in both space and time. Therefore only the cemeteries within the
101 vicinity of the air quality monitoring network were chosen for analysis (Figure 1A). 21 of the
102 cemeteries reported by Mooers et al. (2016) are used. Additional measurements were taken in
103 July of 2014 to enhance the spatial resolution of gravestone decay over the past 55 years that
104 coincide with air quality monitoring data. 485 inscriptions were measured from 227 tombstones
105 in 10 additional cemeteries with emphasis on post 1950 inscriptions. In addition, Bilston (BIL)
106 Cemetery was revisited and additional data were acquired to constrain post 1950 decay rates.
107 Cemeteries, their locations, and associated data are listed in Table 1.

108 26 air quality monitoring stations lie in the study area; their locations are shown in Figure
109 1B and the annually averaged SO₂ and smoke concentrations for all stations are shown in Figure
110 2. Despite the expansion of the air-quality monitoring network after 1960, there is still a general
111 lack of temporal and spatial continuity of records. The period of record of each monitoring
112 station is highly variable; many stations were only in operation for short periods of time (Table
113 2).

114 **2.1 Gravestone decay measurements**

115 Gravestones were selected for measurement following the criteria of Mooers et al. (2016),
116 which closely follow the criteria of Cooke et al. (1995). Measured gravestones were standing
117 vertically, had planar surfaces, used lead lettering, had limited ornamentation, and contained

118 two or more inscriptions per stone. In addition, inscriptions had to be in chronological order
119 and there had to be visible evidence that the stone had been resurfaced at the location of each
120 new inscription.

121 Surface recession of the marble was measured with the depth probe of a digital caliper
122 (accuracy of 0.01mm and precision of ± 0.02 mm (instrument error)) from the surface of the
123 lead letters to the stone surface. Resting the digital caliper on two neighboring lead letters
124 provided stability in measurement while reducing error associated with tilting of the depth
125 probe. Ten measurements were made along the date line of each inscription without regard to
126 letter or numeral. Decay for that measurement was then calculated as the trimmed mean
127 (Tukey, 1962) with the high and low values omitted. The trimmed mean was used to avoid bias
128 from unusually large or small values that might result from a variety of causes such as poorly
129 set lettering, odd shaped letters that may hold moisture, etc.

130 **2.2 Determination of Decay Rates**

131 Post 1940 gravestone decay data were plotted vs. inscription date. In general, gravestone
132 decay as a function of time is nonlinear (Mooers and Massman, in press; Mooers et al., 2016)
133 and follows a trend similar to SO₂ and smoke (Figure 2). Gravestone decay rates were therefore
134 determined by best-fit least squares regression function, which in most cases was a 2nd order
135 polynomial. In the case of Rycroft Cemetery in Dudley (DUD) a 3rd order polynomial provided a
136 higher correlation coefficient and prevented the function from becoming slightly negative in
137 the most recent decade. Decay rates were then determined as the derivative of the best-fit
138 polynomial at the midpoint of each respective decade.

139 **2.3 Spatial Interpolation of Gravestone Decay**

140 **2.3.1 Variogram analysis and Kriging**

141 Since air quality measurements do not coincide geographically with cemeteries, proper
142 spatial interpolation of gravestone decay is critical for comparison. Variograms of the decadal
143 averaged gravestone decay rates from the 33 measured cemeteries were evaluated for best
144 model fit. Stone decay rate for each decade from 1965-2005 was then gridded in ArcGIS® using

145 Empirical Bayesian Kriging (EBK) at a grid spacing of 200 m. Whereas classical Kriging assumes
146 the estimated semivariogram is the true semivariogram generated from a Gaussian distribution,
147 EBK generates many semivariogram models and removes local trends (Krivourchko, 2012). EBK
148 is particularly well suited for small, moderately non-stationary datasets (Chiles and Delfiner,
149 1999; Pilz and Spöck, 2007). Interpolated decay rates were compared with air quality data.

150 **2.3.2 Land-use-based approach**

151 Initial variogram analysis suggested that gravestone decay exhibits poor spatial correlation,
152 which is likely an artifact of significant variation in air quality over short spatial scales (Hoek et
153 al., 2002, 2008). Therefore a land-use-based approach was devised to spatially interpolate
154 gravestone decay. Land use was organized into three categories; 1.) urban areas with high
155 concentrations of factories, large buildings and heavy automobile traffic, 2.) residential areas
156 with dense housing and moderate automobile traffic and 3.) rural/green space with few
157 residences and light traffic. Land use was digitized from recent aerial photography and
158 converted to a 200 m grid for analysis. Evaluation of air photos back to 1960 indicates that
159 there have been few major changes in land-use classification. Grid cells were assigned a land-
160 use indicator as follows: green space generates essentially no pollution and was assigned a
161 land-use indicator of 0.0 and urban/industrial areas were assigned a land-use indicator of 1.0.
162 The relation between urban/industrial and residential is less clear but the land-use indicator will
163 lie somewhere between 0 and 1 and this value must be determined through optimization.
164 Three parameters were then optimized: the indicator value of residential land use, the radius of
165 influence contributing to acid deposition at any location, and a weighting parameter to
166 determine the influence of proximal versus distal locations within the optimum radius.

167 **2.4.1 Optimization of Parameters**

168 The initial optimization of weighting of the residential land-use and radius of influence were
169 done using inverse distance weighting as it provides easy variation of parameters. In its
170 simplest form, the inverse distance weighting parameter (w) is

$$171 \quad w_i(x) = \frac{1}{d(x,x_i)^p} \quad [1]$$

172 where x is the point where the interpolation is being made, d is the distance between known
173 point x_i and the interpolated point, and p is the power parameter. Typical default value for the
174 power parameter for many applications is 2 (inverse distance squared). Reducing the exponent
175 weighs distant points more heavily. For $p=0$ (zero) there is no decrease in weight with distance
176 and the prediction will be simply an average of the values within the search radius. To conduct
177 the initial sensitivity analysis, values of residential land use were varied from 1.0 to 0.0 in steps
178 of 0.2, radius varied from 1 to 10 km, and the inverse distance weighting parameter was varied
179 from 2 to 0. Land use, integrated for each combination of parameters, was calculated for each
180 cell in the 200 m grid. Integrated land use was then correlated with gravestone decay at each
181 cemetery and correlation coefficients (R^2) determined.

182 Since deterministic methods such as IDW differ in their application from geostatistical and
183 interpolation methods (Zimmerman et al., 1999), several additional techniques of land-use
184 interpolation were employed. These included: ordinary kriging, kernel density, and point
185 density calculations all done within ArcGIS® Geostatistical Analyst® and Spatial Analyst®. For
186 each land-use interpolation method the resulting land-use values at cemeteries were correlated
187 with gravestone decay rate for each decade.

188 **2.4.2 Directional dependence of land-use and gravestone decay rate**

189 The directional dependence of land use on stone decay rate was evaluated by integrating
190 land use within search windows of 90°, 120°, and 180° rotated in 45°, 60°, and 60° degree
191 increments, respectively. For each search window, land-use indicators were calculated at 200 m
192 grid cells using the point density function in ArcGIS® Spatial Analyst®. Calculations were made
193 using optimized parameters for radius and residential land use for each search window. The
194 interpolated land use at each measured cemetery was again correlated with gravestone decay
195 at that point. To evaluate directional trends, rose diagrams were constructed using the mean
196 azimuth of each search window and the correlation coefficient between measured gravestone
197 decay rate and the calculated land-use indicator for each directional search.

198 **2.5 Correlation of gravestone decay rates and measured atmospheric SO₂ and smoke**

199 Two separate sets of interpolated grids of gravestone decay rates were generated. First,
200 decadal averaged decay rates for each cemetery were interpolated spatially using Empirical
201 Bayesian Kriging. Second, the linear least-squares regression equation describing the relation
202 between land use and gravestone decay rate was used to assign decay rates spatially. The
203 interpolated and assigned gravestone decay rates at the location of air quality monitoring
204 stations were then plotted against measured SO₂ and smoke and correlation coefficients (R^2)
205 determined to evaluate the relationship between gravestone decay rates (either spatially
206 interpolated or assigned based on land use) and air quality.

207 **2.6 Evaluation of SO₂ deposition efficiency**

208 Marble gravestone decay is a direct measure of flux density of acid (F) (Mooers and
209 Massman, in press), which, in turn, is determined by the atmospheric concentration of
210 pollutants (C) at height z , and the deposition velocity (v_d) given as

$$211 \quad v_d = \frac{-F}{C_z}. \quad [2]$$

212 SO₂ measurements give us a quantitative measure of the atmospheric concentration. If the
213 stone decay is assumed to result from deposition of sulfuric acid, stone decay rates are a
214 measure of the flux of acid to the stone surface, which is a function of the production rate of
215 sulfuric acid from SO₂ oxidation. It is therefore instructive to plot v_d as a function of time to
216 evaluate temporal changes in deposition velocity (deposition efficiency) of SO₂, which can be
217 affected by a number of factors that influence the correlation of gravestone decay with air
218 quality.

219 Deposition velocities were calculated at the 26 air quality monitoring stations using the
220 mean annual SO₂ concentration and the interpolated gravestone decay rate determined using
221 the optimized land use correlation with gravestone decay. Decay rates were then converted to
222 flux of acid as equivalent SO₂ as

$$223 \quad F = \dot{e}\rho w_i \frac{M(\text{CaCO}_3)}{M(\text{H}_2\text{SO}_4)}, \quad [3]$$

224 where (\dot{e}) is decay rate ($l t^{-1}$), ρ is the density of marble ($M l^{-3}$) (we used 2600 kg m^{-3} , Malaga-Starzec et
225 al., (2006)), w_i is the mass fraction of SO_2 in sulfuric acid (0.65), and $M(\text{CaCO}_3)$ and $M(\text{H}_2\text{SO}_4)$ are the
226 mole weight of calcite (100) and sulfuric acid (98), respectively.

227 **3. Results**

228 **3.1 Decay rates**

229 Gravestone decay for the 33 cemeteries included in this study is shown in Figure 3 for the
230 period 1950 to 2010. There is a great deal of variability in decay among stones within any single
231 cemetery. Mooers et al. (2016) conducted an investigation of the sources of variability of stone
232 decay and concluded that by far the largest variability is inherent to the stone. Differences in
233 the physical setting and local effects influence decay by at most a few percent, therefore the
234 data plotted are uncorrected for environmental variables. Time-dependent decay rates were
235 determined by least squares regression (Figure 3, Table 1) for each location.

236 **3.2 Spatial Interpolation of Gravestone Decay**

237 **3.2.1 Variogram analysis**

238 Variograms of the decadal averaged gravestone decay rates from the 33 cemeteries for
239 each decade are shown in Figure 4A-E. In all cases the nugget is large compared with the sill,
240 particularly for the 1960s – 1980s, which leads to relative equality in kriging weights and
241 interpolated values are simply averages of known points (Webster and Oliver 1992; University
242 of Salzburg 2014). The ranges in all cases are between 5 and 10 km; this distance is similar to
243 the average distance between measured cemeteries, again suggesting a lack of spatial
244 correlation resulting in simply averaging of known points by kriging. Figure 4F shows the
245 spatially interpolated gravestone decay rates for the 1960s using Empirical Bayesian Kriging
246 gridded at 200 m. The interpolated decay rates were then compared with air quality data from
247 the 11 air quality monitoring stations available in the 1960s; the correlation between
248 interpolated gravestone decay (and therefore acid flux) is poor (Figure 4G) and results for
249 other decades are similar.

250 **3.2.2 Land Use and Optimization of Parameters**

251 Digitized land use is shown in Figure 5 and the results of the optimization of parameters for
252 the land-use analysis using IDW are shown in Figure 6 and Table 3. The correlation between
253 land use and gravestone decay was maximized for an effective radius of approximately 7000m
254 (Figure 6A), a residential land-use indicator of 0.0 (Figure 6B), and an IDW power of < 0.25 with
255 the best correlation at a value of 0.0 (Figure 6C). Therefore the best correlation between land
256 use and gravestone decay is achieved using the same indicator for residential area and green
257 space. Within the study area there are essentially no green spaces larger than 2-3 km in
258 diameter (Figure 5), which is less than half of the calculated effective radius of influence (7000
259 m) suggesting that air quality in green spaces is likely no different from, and is controlled by,
260 surrounding urban/industrial or residential areas. An optimum inverse distance weighting
261 power of 0.0 indicates that gravestone decay depends basically on an **average** of the air quality
262 over a 7000 m radius of the surrounding area. This averaging is consistent with the variogram
263 analysis, which suggested little spatial correlation in the gravestone decay measurements
264 among cemeteries.

265 Land use was then interpolated to a 200 m grid using ordinary Kriging, kernel density, point
266 density and inverse distance weighting. Figure 7 shows the correlation between the calculated
267 land-use indicator and gravestone decay rate for the various interpolation techniques for a
268 radius of 7000m and a residential land-use indicator of 0.0. Although there is reasonable
269 correlation between land use and stone decay, 4 cemeteries are considered outliers (BEN, COD,
270 JQK, and WAL). Bentley Cemetery (BEN) has an anomalously low decay rate; it is surrounded by
271 four other cemeteries (WIL, WAL, DAR, and BIL) all of which have significantly higher decay
272 rates and far larger number of measurements (Figure 3). Codsall (COD) is anomalously high for
273 the calculated land use, which is mostly rural farmland. Only the relatively small village of
274 Codsall has significant residential neighborhoods. The reason for the anomalously high
275 calculated decay rate is unclear. Key Hill Cemetery (JQK), located in the Birmingham Jewellery
276 Quarter, has anomalously low stone decay compared to Warstone Lane Cemetery, which is
277 located only 100 m away. The dramatic difference in decay rate is attributed to the continuous
278 tree canopy of 100 to 150-year-old London plane at Key Hill Cemetery, whereas Warstone Lane
279 Cemetery is largely open (Mooers and Massman, in press; Mooers et al. 2016).

280 Rrycroft Cemetery (WAL) in Walsall has a relatively high decay rate relative to the calculated
281 land use. Therefore to evaluate the overall effect of these anomalous decay values on the
282 correlation between land use and gravestone decay, BEN, COD, JQK, and WAL were removed
283 from the analysis and the results are shown in Figures 7B, D, F, and H. Note that correlation
284 coefficients are significantly higher with these four outliers omitted.

285 The highest correlation between the spatially averaged land-use parameter and gravestone
286 decay at measured cemeteries was achieved using point-density analysis and kriging with the
287 omission of the aforementioned four anomalous cemeteries. The point density function simply
288 averages the values within a given radius and kriging, given the poor spatial correlation
289 suggested by variogram analysis, does little more than average the land use over the same
290 radius.

291 Table 4 shows the correlation coefficients of land-use vs. stone decay rates using the point-
292 density calculation for each decade and for radii of 4000 – 12,000 m. Correlation coefficients
293 are high for 1960s – 1980s at a radius of approximately 6-7 km. The correlation between land
294 use and stone decay drops off after 1990 and the radius of highest correlation increases.

295 **3.2.3 Directional dependence of land use on gravestone decay**

296 The correlation between interpolated land use and gravestone decay rate for the
297 directionally dependent search patterns are shown in Table 5 and Figure 8. Once again
298 omitting BEN, COD, WAL, and JQK from the analysis improves the correlation for the reason
299 stated above. Note that the wider the search pattern the better the correlation between land
300 use and stone decay (Table 5). The correlation coefficients for gravestone decay and land use
301 for each of directional searches are shown in Table 5. Although the correlation coefficients are
302 not as high as the omnidirectional calculation there is a clear directional trend. The highest
303 correlation of land use and gravestone decay for the 1960s and 1970s is south and southwest.
304 From the 1980s to the 2000s the correlation coefficients decrease as the directional
305 dependence of stone decay rate shifts to westerly and then nearly to the north. This change in
306 directional trend coincides with improving air quality and the increase in effective radius of
307 influence contributing acid and changing deposition efficiency of SO₂.

308 3. 3 Correlation of land use and air quality

309 The correlation of gravestone decay rate and optimized land use suggests that interpolated
310 land use may be used as a proxy for acid deposition and the relationship between land use and
311 air quality can be evaluated. The decadal averaged SO₂ and smoke concentrations for 23
312 monitoring stations are shown in Table 6. The correlation of land use (calculated using the
313 point density function, a radius of 7 km, a residential land-use indicator of 0.0) and SO₂ and
314 smoke for the 1960s-1980s is shown in Figure 9. Trends are clearly evident for the 1960s and
315 1970s even though R² values are relatively low. By the 1980s, there is little correlation between
316 land use and SO₂ and smoke.

317 3.4 Evaluation of SO₂ deposition efficiency

318 Figure 10 shows the calculated deposition velocities for all air quality monitoring locations for
319 all years (Figure 10). Five-year and ten-year moving averages are also plotted to remove high-
320 frequency variation. Note that after about 1980 there is an increasing trend in the deposition
321 velocity indicating an increase in the efficiency of SO₂ oxidation to sulfuric acid. SO₂ emissions in
322 Europe have decreased substantially since 1980, which has been reflected in large reductions in
323 airborne concentrations of SO₂ (Vestreng et al., 2007). Jones and Harrison (2011) used data
324 from the European Monitoring and Evaluation Programme (EMEP) to examine relationships
325 between SO₂ and sulfate in rural air. The data from all countries examined could be fit to a
326 curvilinear relationship:

$$327 \quad \chi[\text{SO}_4^{2-}] = a \cdot \chi[\text{SO}_2]^b + c \quad [4]$$

328 where $\chi[\text{SO}_4^{2-}]$ and $[\text{SO}_2]$ are airborne concentrations, and a, b and c are constants. As b takes
329 values of typically around 0.6, the percentage reduction in SO₄²⁻ is less than proportionate for a
330 given reduction in SO₂. Hidy et al. (2014) examined measured concentrations from sites in the
331 southeastern United States; between 1999 and 2013, average SO₂ concentrations fell by
332 approximately 84%, while SO₄²⁻ over the same period fell by only 60%. The trend seen in Figure
333 10 of higher sulfuric acid production efficiency at lower concentrations of SO₂ in more recent
334 years is consistent with this pattern.

335 **4.0 Discussion and Conclusions**

336 Gravestone decay has been shown to serve as an excellent proxy for acid deposition (Mooers et
337 al., 2016; Inkpen, 1998, 2013; Cooke, 1989, Cooke et al., 1995). In addition, the results of this
338 investigation suggest that gravestone decay exhibits a high degree of correlation with
339 interpolated land use (Figure 7), which when integrated over some optimal area essentially
340 determines the pollution sources and therefore the acid flux. The correlation between
341 interpolated land use and air quality, however, is rather poor (Figure 9) and the reasons for the
342 poor correlation are difficult to determine. The paucity of measurements of SO₂ and smoke
343 and the lack of spatial and temporal continuity of the records all contribute to poor correlation.
344 In addition, SO₂ data are annual averages and gravestone decay may well be sensitive to
345 seasonal variations or even short-term extreme events that are not represented in the available
346 data. Correlation between gravestone decay and measured SO₂ and smoke concentrations (air
347 quality) is suggested by their similar exponential trends (Figures 2 and 3). Although spatial
348 interpolation procedures can be used to determine intermediate values of gravestone decay,
349 variogram analysis indicates that there is a lack of spatial correlation particularly prior to about
350 1980. Local factors, likely related to land use (or possibly even microclimatic effects), therefore
351 appear to overwhelm the spatial continuum. The land-use approach of spatial interpolation is
352 therefore at least as good as other methods even though the correlation with annually
353 averaged annual air-quality data is rather poor.

354 By about 1980 there was a dramatic turnaround in air quality (Mosley, 2009; 2011) that is
355 evident in both the SO₂ and smoke data (Figure 2) and is well documented in decreasing
356 gravestone decay rates (Mooers et al., 2016) and therefore acid flux. At this time there is a
357 change in the directional dependence of gravestone decay on land use (Figure 8) and an
358 increase in the optimum radius of influence of land use on gravestone decay rates (Tables 3 and
359 4). Also at this time there appears to be a marked increase in the efficiency of the SO₂ oxidation
360 process (Figure 10). The most probable explanation for the increased deposition efficiency is
361 non-linearity in the SO₂ conversion to sulfate, which is seen in both field measurement data
362 (Jones and Harrison, 2011; Hidy et al., 2014) and numerical model results (Harrison et al., 2013).

363 An alternative explanation of Figure 10, which needs to be considered, is that increased
364 emissions of nitrogen oxides have led to increased concentrations of nitric acid and higher
365 decay rates. However, UK emission statistics for NO_x show a peak in 1990 with continual
366 decrease until 2013 (National Atmospheric Emissions Inventory, 2016), suggesting that decay
367 due to nitric acid cannot explain the observed trends.

368 As sulfuric acid production falls in response to decreased SO₂ concentrations, so the extent of
369 neutralization by ammonia is likely to increase, hence reducing sulfate acidity and working in
370 the opposite sense to Figure 10. An alternative role for ammonia is in enhancing the deposition
371 efficiency of SO₂ through co-deposition (Erisman and Wyers, 1993). This is expected to
372 enhance SO₂ deposition efficiency at lower concentrations, and if followed by oxidation of the
373 SO₂ leads to enhanced sulfate concentrations, although not necessarily to sulfuric acid.

374 As overall air quality improves four trends are evident; 1) the correlation between interpolated
375 land use and stone decay becomes less (Table 4), 2) the effective radius of influence of land use
376 on local air quality increases (Table 4), 3) the directional dependence of land use on local air
377 quality changes from southerly to westerly to northerly, and 4) the efficiency of stone decay
378 increases as SO₂ concentrations fall. These trends are consistent with greatly reduced contrast
379 in air quality among different land-use types. The reason for the change in directional trend
380 from south to north over 50 years is unclear, but possibly related to industrial decline in the
381 Midlands over this time (Spencer et al., 1986).

382 Finally, interpolated land use and the correlation with SO₂ and smoke can be used to estimate
383 average air quality over the study area for each decade (Figure 11). The improvement in air
384 quality is quite dramatic, particularly between the 1960s and the 1980s. After about the mid-
385 1980s air quality is relatively uniform spatially in the West Midlands and the correlation with
386 land use is significantly lower.

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Figure 1. West Midlands County, UK, showing the locations of cemeteries (A) and air-quality monitoring stations (B).

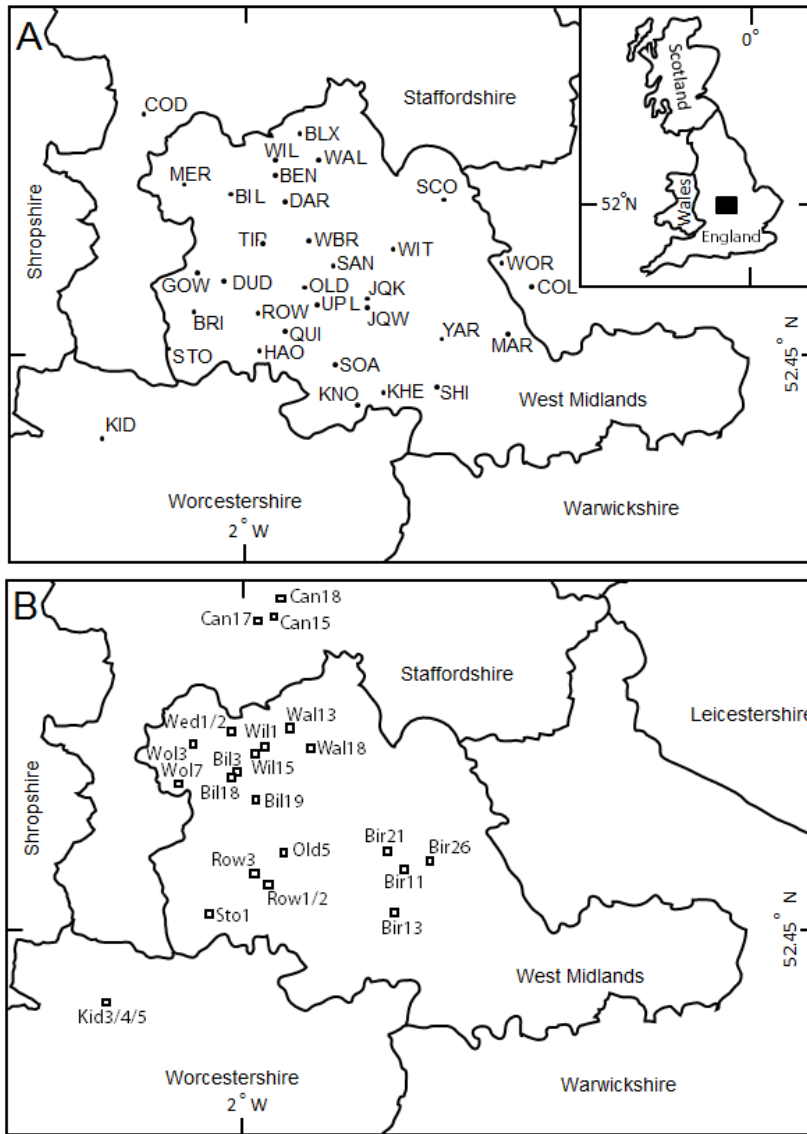


Figure 2. SO₂ and smoke concentrations from all stations for the period 1960 to 2005, the period of available record. Each data point represents a one-year average of SO₂ or smoke for the 23 stations listed in Table 2.

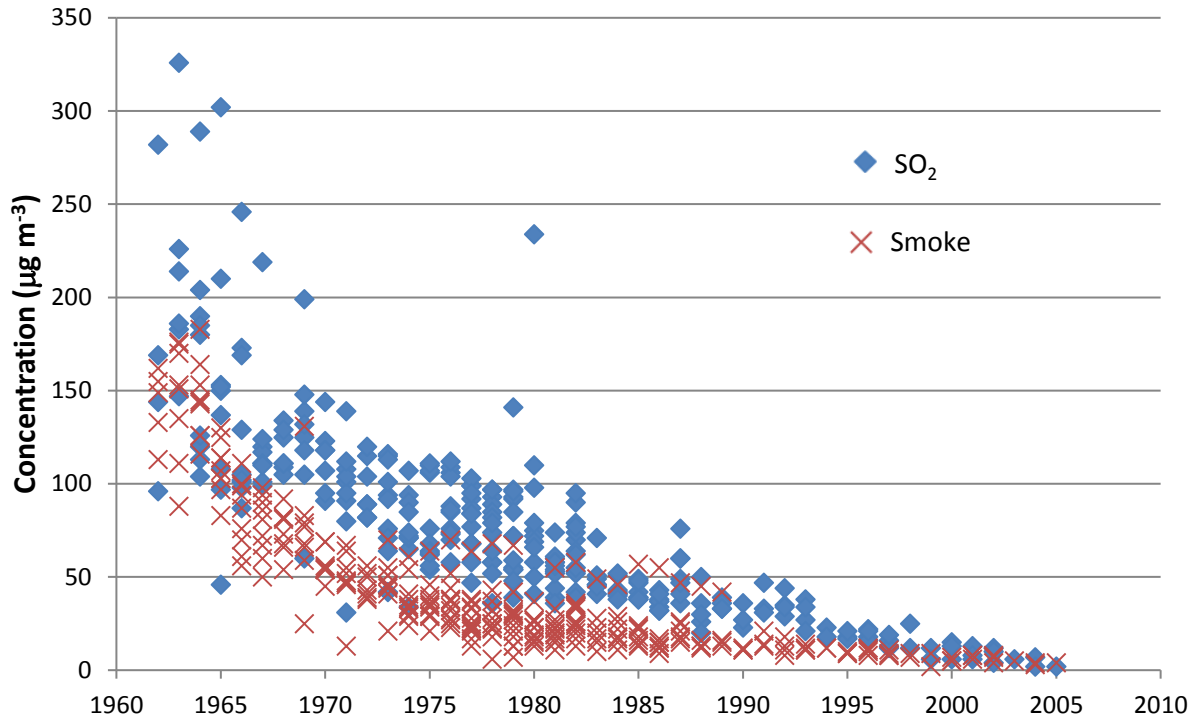


Figure 3. Gravestone decay for 33 cemeteries in the West Midlands and surrounding area. Each point represents stone decay on a single inscription. Values are the average of 10 measurements on the date line of the inscription with the high and low values removed (trimmed mean). Data are plotted as years before 2010 so that regression equations pass through the graph origin.

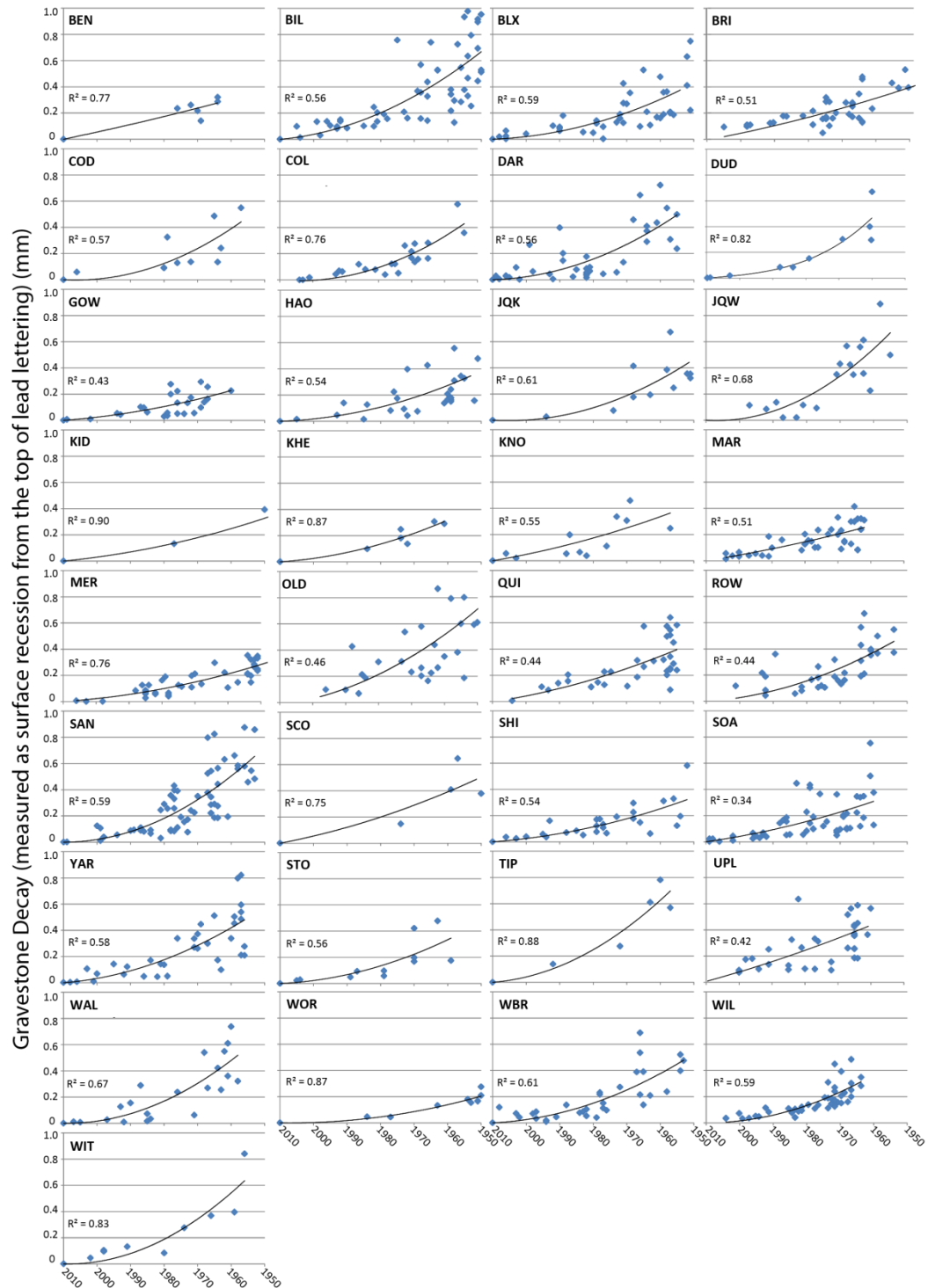


Figure 4. A-E) variograms of the gravestone decay rate for the 1960s – 2000s, respectively; F) results of Empirical Bayesian Kriging of decay rates, and G) correlation of interpolated gravestone decay rate and SO₂ concentrations at air quality monitoring locations.

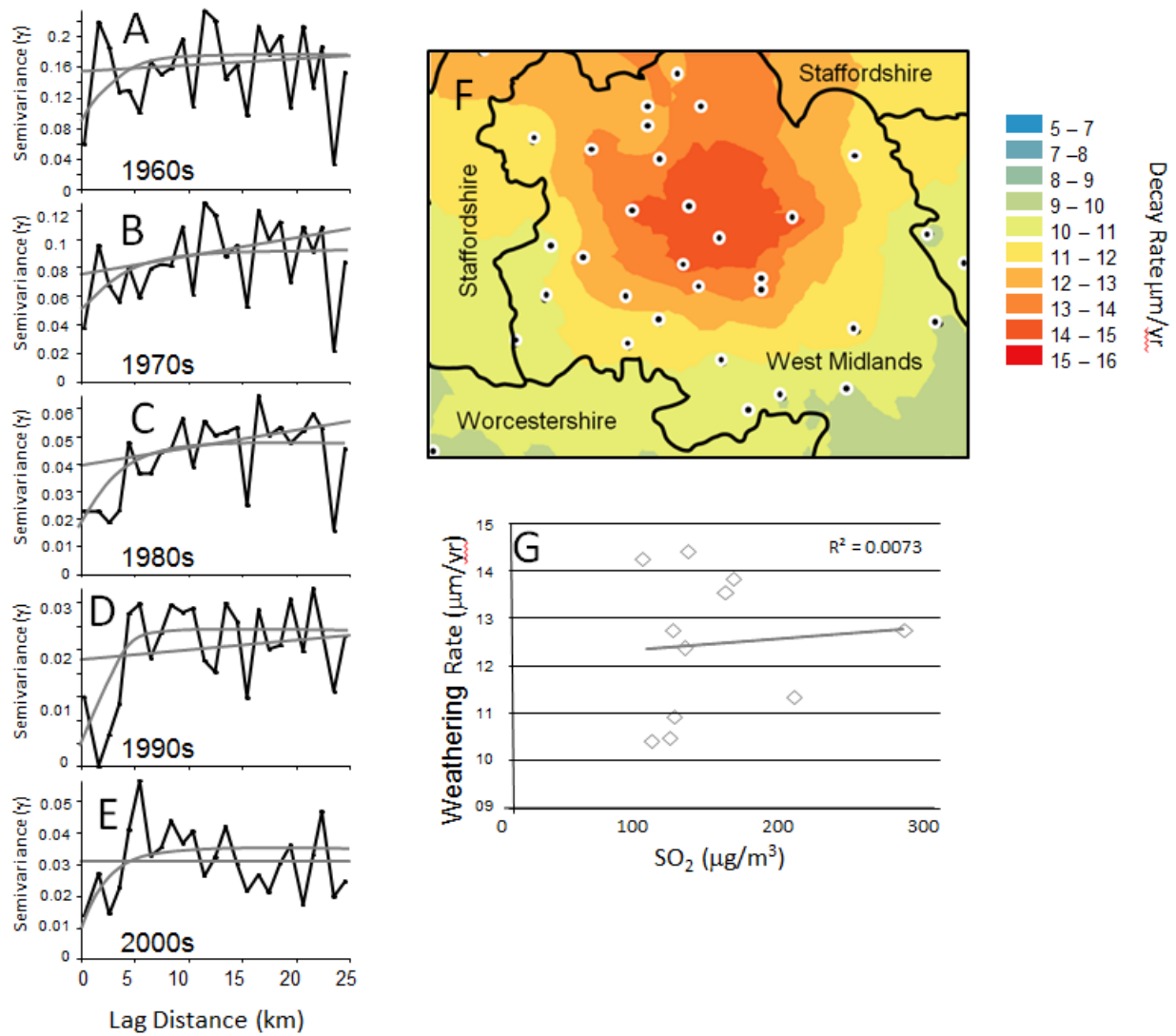


Figure 5. Land use digitized from recent aerial photography.

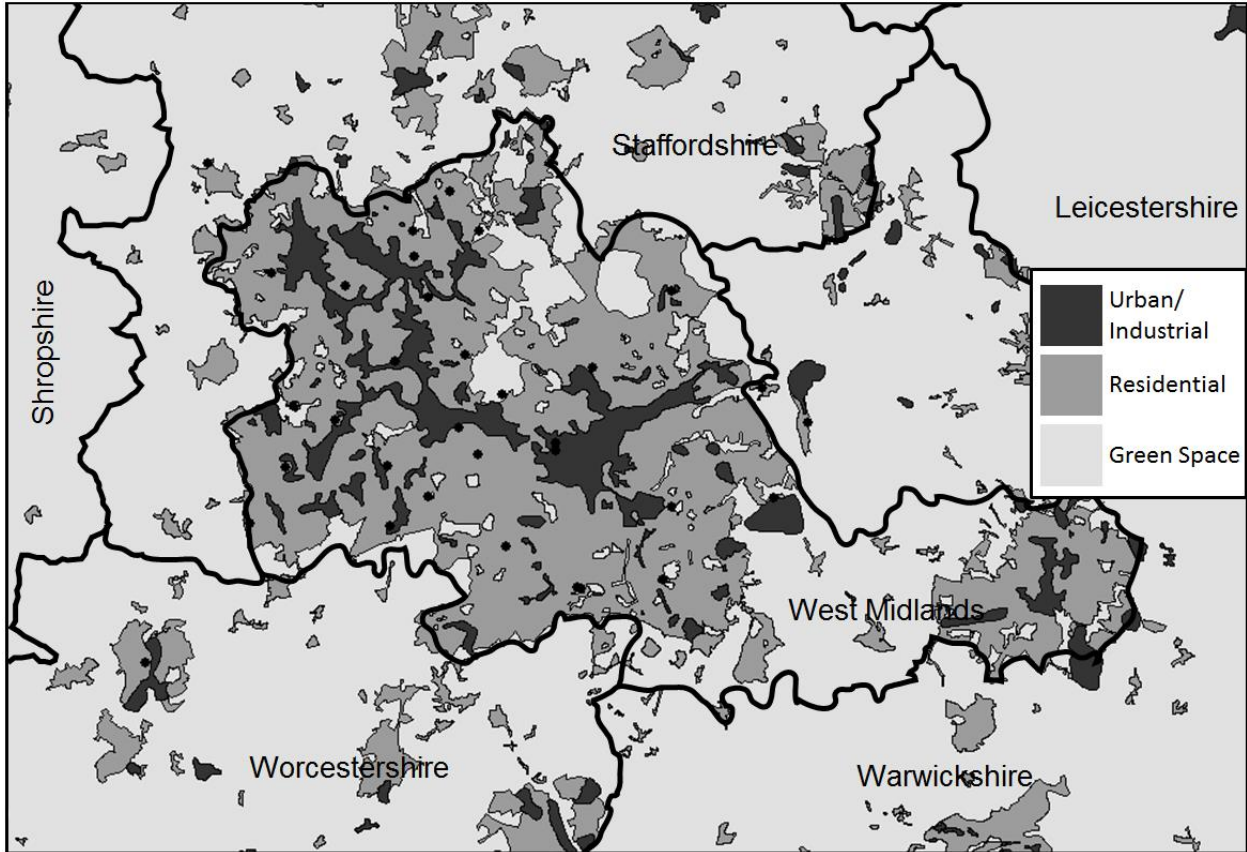


Figure 6. IDW optimization; A) radius, B) residential land-use indicator, and C) inverse-distance weighting factor.

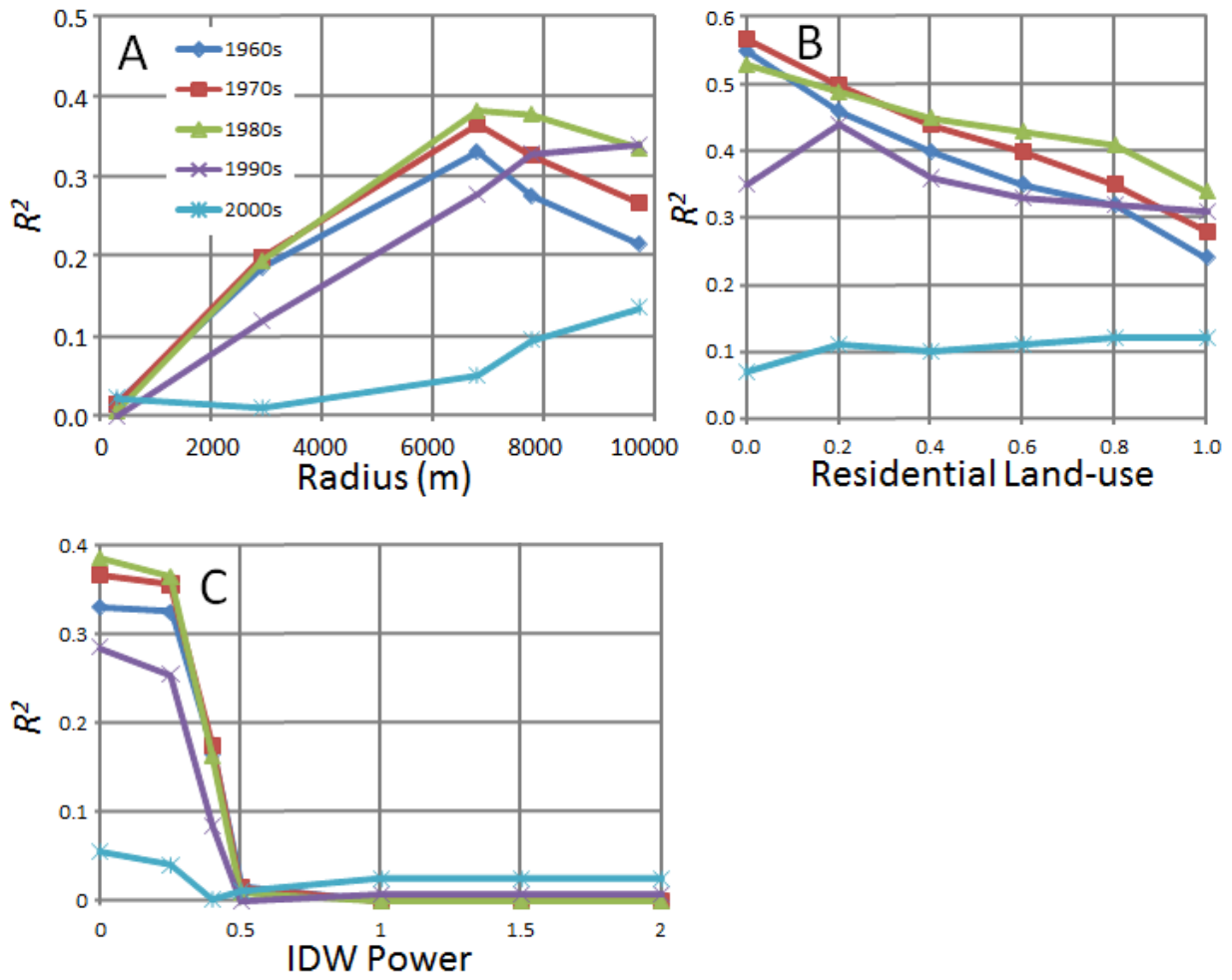


Figure 7. Relationship between Interpolated land use and gravestone decay rate for 33 cemeteries. Land-use interpolation by Kriging (A, B), Kernel Density (C,D), Point Density (E,F), and IDW (G,H). For each method of interpolation the correlation coefficient is greatly improved by omitting the four anomalous cemeteries as described in the text (B, D, F, and H).

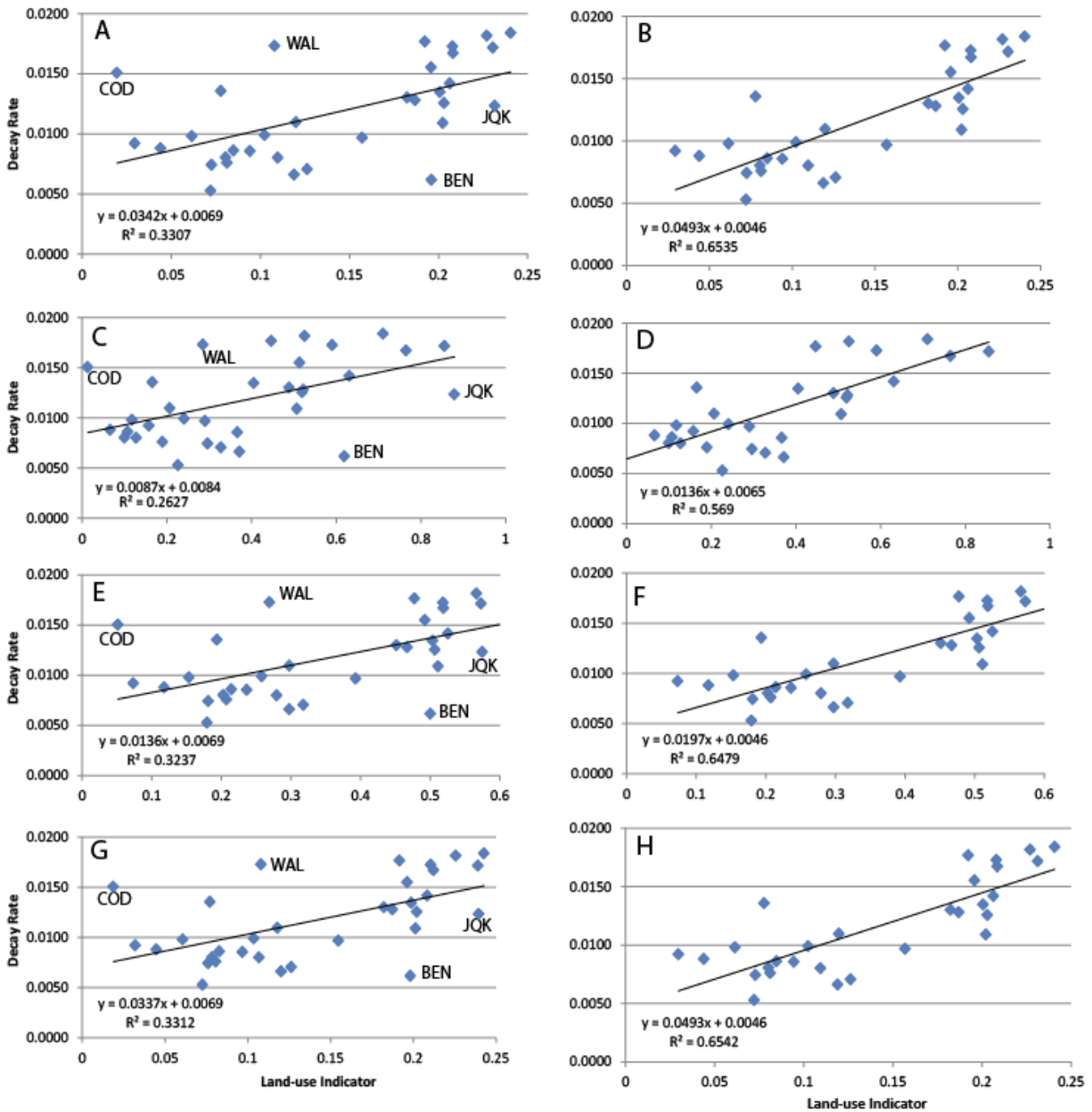


Figure 8. Rose diagrams of directional dependence of land use on gravestone weathering rate. Diagrams were constructed from the directional searches using the mean azimuth of each search and the correlation coefficient for that search window between gravestone weathering and the interpolated land-use indicator.

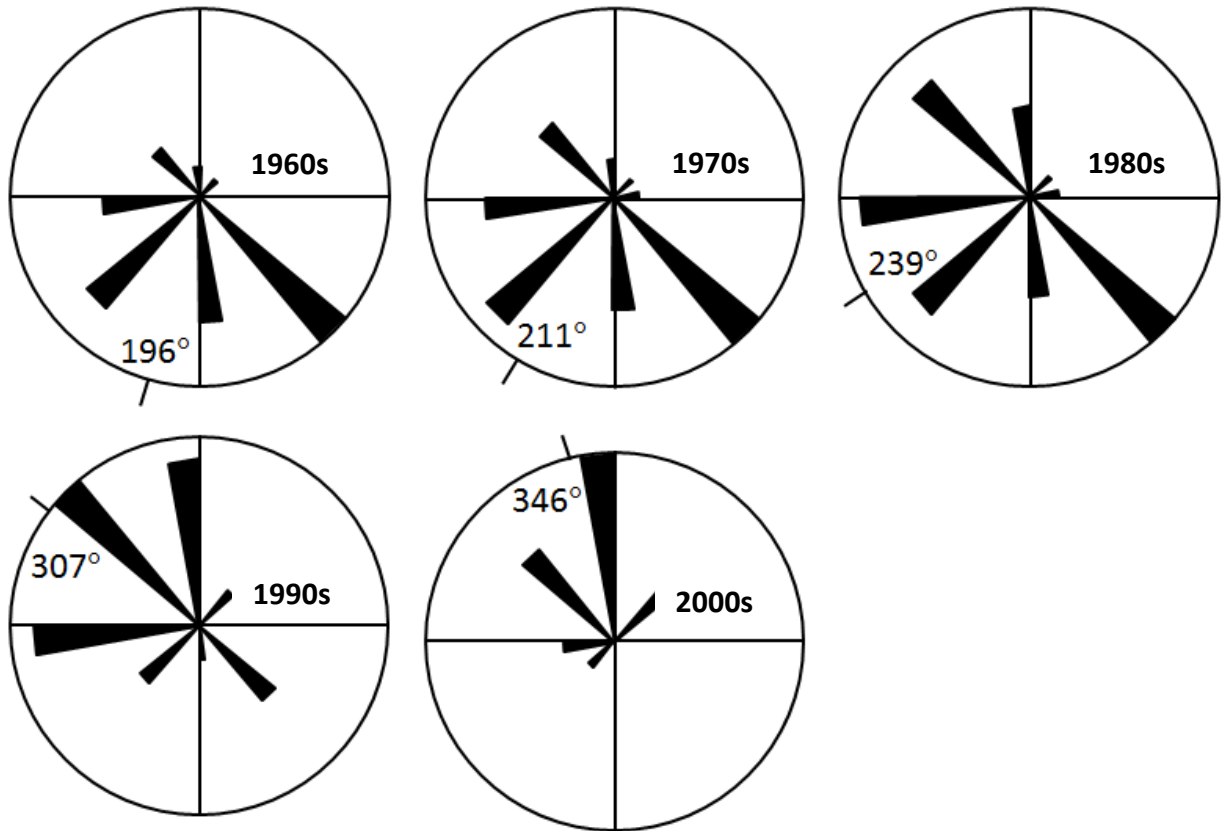


Figure 9. Correlation between land-use indicator and SO₂ and smoke concentrations for the 1960s (A, B), 1970s (C, D), and the 1980s (E, F).

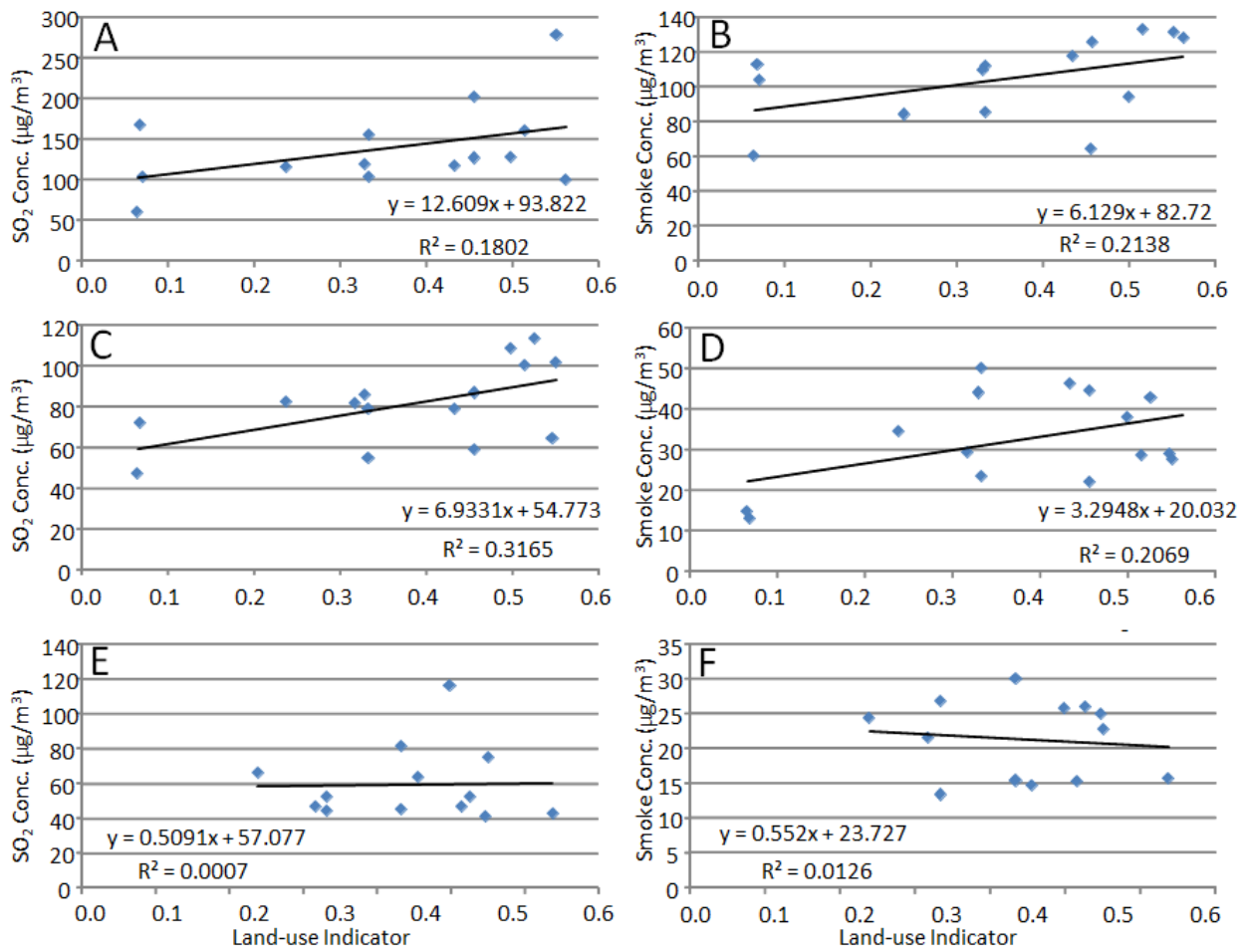


Figure 10. Surrogate deposition velocity (F/C_2) as a function of year of measurement. Blue diamonds are all data, red squares are 5-year and green triangles are 10-year moving averages. Trend line was calculated from all data points using a third-order polynomial least-squares regression.

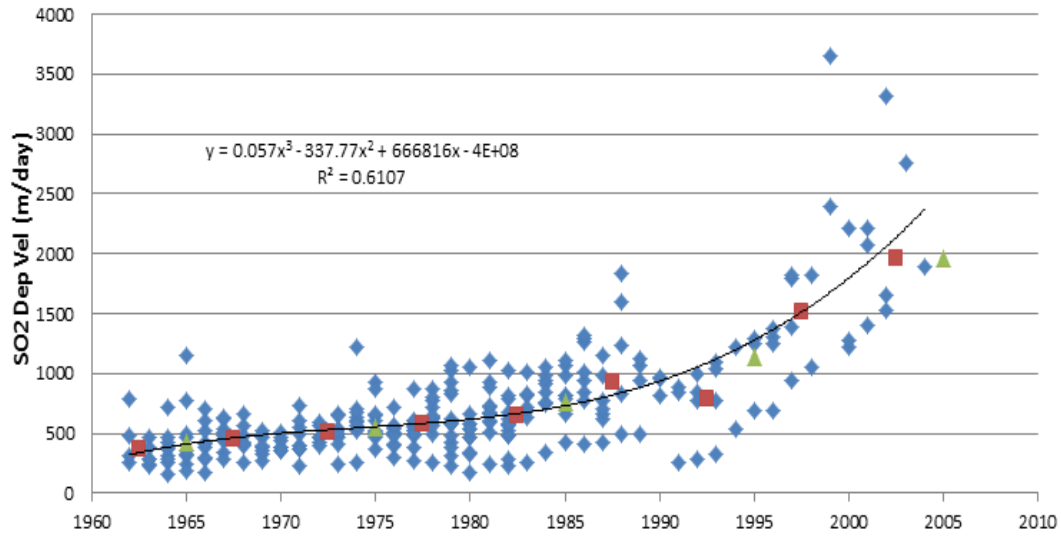
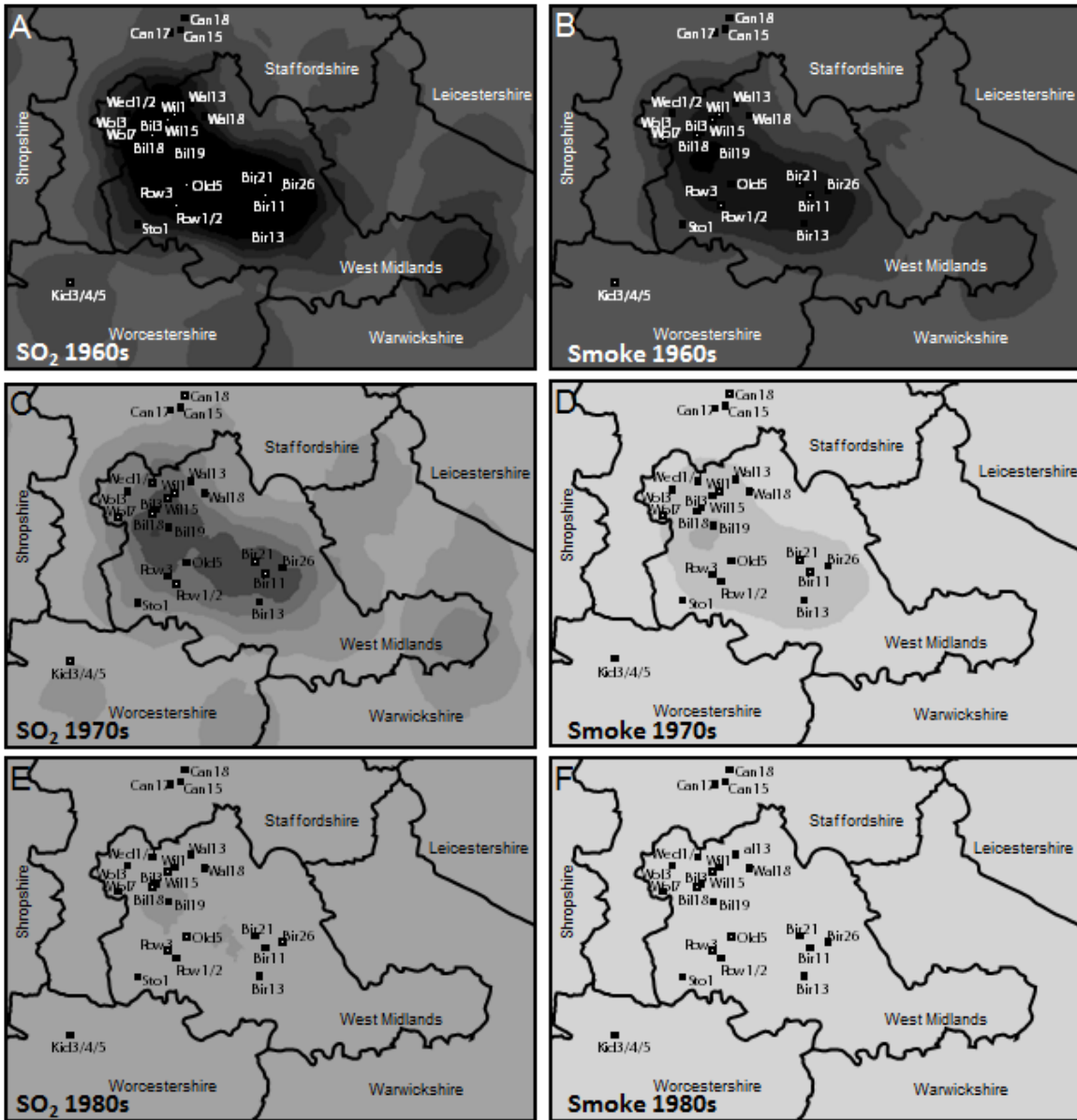
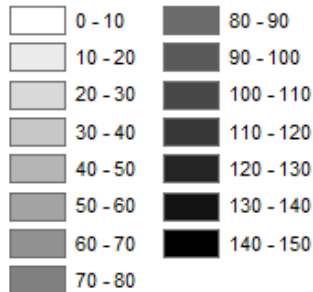


Figure 11. Predicted SO₂ and smoke concentrations based on land-use/air quality correlations in Figure 9 for the 1960s through 1980s.



SO₂ (µg/m³)



Smoke (µg/m³)

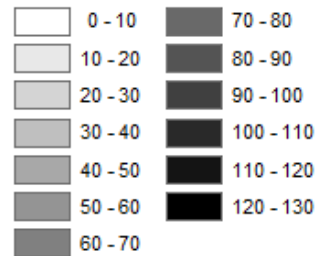


Table 1. List of cemeteries visited during this investigation. Locations are given in UTM Zone 30. Gravestone decay vs. age for each cemetery was fitted with a non-linear polynomial regression and the equation and R2 value are tabulated. For each decade 1960-2010 mean decay rates were calculated at the derivative of the regression equation for the midpoint year and are given in $\mu\text{m}/\text{yr}$.

Identifier	Cemetery Name	Easting	Northing	Neighborhood	Function	R2	Y2000s	Y1990s	Y1980s	Y1970s	Y1960s
BEN	Bentley Cemetery	565735	5826699	Bentley	$y = 1.51\text{E-}05 X^2 + 5.32\text{E-}03 X + 0$	$R^2 = 0.77$	0.0041	0.0046	0.0051	0.0057	0.0062
BIL	Bilston Cemetery	561866	5825044	Bilston	$y = 1.47\text{E-}04 X^2 + 2.34\text{E-}03 X + 0$	$R^2 = 0.55$	0.0050	0.0079	0.0108	0.0138	0.0167
BLX	Bloxwich Cemetery	567804	5830398	Bloxwich	$y = 1.02\text{E-}04 X^2 + 9.82\text{E-}04 X + 0$	$R^2 = 0.59$	0.0028	0.0049	0.0069	0.0089	0.0110
BRI	Brierly Cemetery	558519	5814794	Brierly	$y = 9.36\text{E-}05 X^2 - 6.09\text{E-}04 X + 0$	$R^2 = 0.53$	0.0011	0.0029	0.0048	0.0067	0.0086
COD	Saint Nicholas Churchyard	554119	5831975	Codsall	$y = 1.82\text{E-}04 X^2 - .28\text{E-}03 X + 0$	$R^2 = 0.57$	0.0005	0.0042	0.0078	0.0114	0.0151
COL	Coleshill Parish Church/Cemetery	588007	5817313	Coleshill	$y = 1.73\text{E-}04 X^2 - 2.02\text{E-}03 X + 0$	$R^2 = 0.76$	0.0000	0.0032	0.0066	0.0101	0.0136
DAR	Fallings Heath Cemetery	566570	5824432	Darlston	$y = 1.48\text{E-}04 X^2 + 8.28\text{E-}04 X + 0$	$R^2 = 0.56$	0.0023	0.0053	0.0082	0.0112	0.0142
DUD	Scot's Green Cemetery	561285	5817504	Dudley	$y = 3.24\text{E-}06 X^3 - 03\text{E-}05 X^2 + 0.002 X + 0$	$R^2 = 0.82$	0.0014	0.0024	0.0051	0.0094	0.0155
GOW	Gornal Woods Cemetery	558912	5818302	Gornal Woods	$y = 5.22\text{E-}05 X^2 + 1.94\text{E-}03 X + 0$	$R^2 = 0.43$	0.0029	0.0039	0.0050	0.0060	0.0071
HAO	Halesowen Cemetery	564377	5811518	Halesowen	$y = 9.26\text{E-}05 X^2 + 21\text{E-}04 X + 0$	$R^2 = 0.54$	0.0025	0.0043	0.0062	0.0080	0.0099
JQK	Key Hill Cemetery	573743	5816222	Jewellery Quarter	$y = 1.52\text{E-}04 X^2 - 1.40\text{E-}03 X + 0$	$R^2 = 0.61$	0.0001	0.0032	0.0062	0.0093	0.0123
JQW	Warstone Lane Cemetery	573730	5815781	Jewellery Quarter	$y = 2.48\text{E-}04 X^2 - 1.49\text{E-}03 X + 0$	$R^2 = 0.68$	0.0011	0.0051	0.0091	0.0132	0.0172
KID	Kidderminster Cemetery	550592	5803814	Kidderminster	$y = 4.95\text{E-}05 X^2 + 2.47\text{E-}03 X + 0$	$R^2 = 0.90$	0.0015	0.0034	0.0054	0.0073	0.0092
KHE	Brandwood End Cemetery	574978	5808054	Kings Heath	$y = 9.29\text{E-}05 X^2 + 1.74\text{E-}03 X + 0$	$R^2 = 0.87$	0.0009	0.0028	0.0048	0.0067	0.0086
KNO	Saint Nicholas Cemetery	575167	5807964	Kings Norton	$y = 4.72\text{E-}05 X^2 + 4.37\text{E-}03 X + 0$	$R^2 = 0.55$	0.0030	0.0043	0.0055	0.0068	0.0080
MAR	Marston Green Burial Grounds	586086	5813062	Marston Green	$y = 2.54\text{E-}05 X^2 + 4.08\text{E-}03 X + 0$	$R^2 = 0.51$	0.0048	0.0045	0.0049	0.0058	0.0074
MER	Merridale Cemetery	557690	5825788	Merridale	$y = 4.98\text{E-}05 X^2 + 1.73\text{E-}03 X + 0$	$R^2 = 0.76$	0.0026	0.0036	0.0046	0.0056	0.0066
OLD	Olbury Cemetery	568314	5817067	Oldbury	$y = 1.48\text{E-}04 X^2 + 2.74\text{E-}03 X + 0$	$R^2 = 0.46$	0.0054	0.0084	0.0113	0.0143	0.0173
QUI	Quinton Cemetery	566553	5813148	Quinton	$y = 5.76\text{E-}05 X^2 + 4.03\text{E-}03 X + 0$	$R^2 = 0.44$	0.0051	0.0062	0.0074	0.0085	0.0097
ROW	Rowley Regis Cemetery	564247	5814857	Rowley Regis	$y = 1.10\text{E-}04 X^2 + 2.04\text{E-}03 X + 0$	$R^2 = 0.44$	0.0040	0.0062	0.0084	0.0106	0.0128
SAN	Handsworth Cemetery	570750	5818928	Sandwell	$y = 2.02\text{E-}04 X^2 + 1.85\text{E-}05 X + 0$	$R^2 = 0.59$	0.0020	0.0061	0.0101	0.0141	0.0182
SCO	Sutton Coldfield Cemetery	580327	5824737	Sutton Coldfield	$y = 5.85\text{E-}05 X^2 + 4.90\text{E-}03 X + 0$	$R^2 = 0.75$	0.0033	0.0047	0.0061	0.0074	0.0088
SHI	Robin Hood Cemetery and Crematorium	579776	5808467	Shirley	$y = 6.34\text{E-}05 X^2 + 1.88\text{E-}03 X + 0$	$R^2 = 0.54$	0.0025	0.0038	0.0050	0.0063	0.0076
SOA	Lodge Hill Cemetery and Crematorium	570966	5810346	Selly Oak	$y = 5.07\text{E-}05 X^2 + 3.65\text{E-}03 X + 0$	$R^2 = 0.34$	0.0040	0.0050	0.0060	0.0070	0.0080
YAR	South Yardley Cemetery and Crematorium	580324	5812585	South Yardley	$y = 1.27\text{E-}04 X^2 + 2.05\text{E-}03 X + 0$	$R^2 = 0.58$	0.0033	0.0059	0.0084	0.0109	0.0135
STO	Stourbridge Crematorium	556494	5811652	Stourbridge	$y = 1.10\text{E-}04 X^2 + 1.18\text{E-}03 X + 0$	$R^2 = 0.56$	0.0008	0.0031	0.0053	0.0076	0.0098
TIP	Tipton Cemetery	564697	5820810	Tipton	$y = 2.11\text{E-}04 X^2 + 1.97\text{E-}03 X + 0$	$R^2 = 0.88$	0.0014	0.0057	0.0099	0.0141	0.0184
UPL	Uplands Cemetery	569384	5815531	Uplands	$y = 3.94\text{E-}05 X^2 + 7.03\text{E-}03 X + 0$	$R^2 = 0.42$	0.0077	0.0085	0.0093	0.0101	0.0109
WAL	Ryecroft Cemetery	569438	5828132	Walsall	$y = 1.96\text{E-}04 X^2 - 3.38\text{E-}04 X + 0$	$R^2 = 0.69$	0.0016	0.0055	0.0095	0.0134	0.0173
WOR	Saint Peter and Saint Paul Parish Church	585444	5819309	Water Orton	$y = 6.28\text{E-}05 X^2 - 3.71\text{E-}04 X + 0$	$R^2 = 0.87$	0.0003	0.0015	0.0028	0.0040	0.0053
WBR	Heath Lane Cemetery	568630	5821123	West Bromwich	$y = 1.26\text{E-}04 X^2 + 1.24\text{E-}03 X + 0$	$R^2 = 0.61$	0.0025	0.0050	0.0075	0.0100	0.0126
WIL	Willenhall Cemetery	565666	5828171	Willenhall	$y = 1.40\text{E-}04 X^2 + 3.64\text{E-}04 X + 0$	$R^2 = 0.59$	0.0018	0.0046	0.0074	0.0102	0.0130
WIT	Witton Cemetery	575877	5820467	Witton	$y = 2.28\text{E-}04 X^2 - 5.44\text{E-}04 X + 0$	$R^2 = 0.83$	0.0007	0.0049	0.0092	0.0134	0.0177

Table2. Name and location of air-quality monitoring stations active within the study area, their location (UTM), and period of record.

Identifier	Site Name (site code)	UTM30 Easting	UTM30 Northing	Start Date	End Date	Address
Bil3	BILSTON 3 (330003)	562677	5824589	4/1/1943	4/6/1970	23 WELLINGTON RD, Wolverhampton
Bil18	BILSTON 18 (330018)	562183	5824182	4/4/1978	4/2/1984	ST EDWARDS NURSERY SCHOOL, Wolverhampton
Bil19	BILSTON 19 (330019)	564311	5822211	3/29/1983	3/28/1988	ERNEST BOLD COURT WOLVERHAMPTON ST, Wolverhampton
Bir11	BIRMINGHAM 11 (355011)	577095	5816387	4/3/1962	3/31/1969	CENTRAL LAB, NECHELLS, Birmingham
Bir13	BIRMINGHAM 13 (355013)	576450	5812377	4/3/1962	3/31/1969	CONGREGATIONAL CHURCH, LADYPOOL RD, SPARKBROOK, Birmingham
Bir21	BIRMINGHAM 21 (355021)	575774	5817869	3/28/1972	3/29/1982	ASTON HALL, ASTON PARK, Birmingham
Bir26	BIRMINGHAM 26 (355026)	579387	5817019	4/1/1975	4/3/1995	INGLETON RD JUN & INF SCHOOL, Birmingham
Can15	CANNOCK 15 (530015)	565790	5838135	4/5/1966	4/2/1973	HEALTH DEPT, CHURCH ST, Cannock Chase
Can17	CANNOCK 17 (530017)	564396	5837716	3/28/1972	3/30/1981	LONGFORD COURT, BIDEFORD WAY, Cannock Chase
Can18	CANNOCK 18 (530018)	566470	5839645	4/1/1980	3/30/1998	ARTHUR ST, CHADSMOOR, Cannock Chase
Kid3	KIDDERMINSTER 3 (1680003)	551255	5804326	4/4/1961	4/4/1966	P.H.DEPT, VICAR ST, Wyre Forest
Kid4	KIDDERMINSTER 4 (1680004)	551153	5804525	4/4/1967	4/2/1979	5-9 CHURCH ST, Wyre Forest
Kid5	KIDDERMINSTER 5 (1680005)	551154	5804425	4/3/1979	3/30/1981	26 VICAR ST, Wyre Forest
Old5	OLDBURY 5 (2460005)	566876	5817545	4/1/1958	3/29/1999	MUNICIPAL BUILDINGS, FLASH RD, Sandwell
Row1	ROWLEY REGIS 1 (2752501)	565513	5814826	4/4/1967	3/29/1976	BRITANNIA ROAD SCHOOL, BLACKHEATH, Sandwell
Row2	ROWLEY REGIS 2 (2752502)	565513	5814826	4/1/1975	3/29/1982	CORRIDOR, BRITANNIA RD SCH, BLACKHEATH, Sandwell
Row3	ROWLEY REGIS 3 (2752503)	564299	5815809	3/31/1998	Present	SPRINGFIELD SCHOOL DOULTON ROAD ROWLEY REGIS, Sandwell
Sto1	STOURBRIDGE 1 (3110001)	560246	5812353	4/1/1951	3/29/1982	LYE CLINIC, ORCHARD LANE, Dudley
Wal13	WALSALL 13 (3380013)	567225	5828453	4/4/1961	3/28/1988	BEECHDALE CLINIC, STEPHENSON SQ, LEAMORE, Walsall
Wal18	WALSALL 18 (3380018)	569150	5826679	3/30/1976	Present	ENV. HEALTH DEPT, CIVIC CENTRE, DARWALL ST, Walsall
Wed1	WEDNESFIELD 1 (3470001)	562229	5828084	4/1/1952	3/29/1982	HEALTH CENTRE, HIGH ST, Wolverhampton
Wed2	WEDNESFIELD 2 (3470002)	562329	5828085	3/30/1982	Present	COUNCIL OFFICES, ALFRED SQUIRE RD, Wolverhampton
Wil1	WILLENHALL 1 (3620001)	565047	5826822	4/1/1948	4/6/1970	ALBION WORKS (HARPERS), Walsall
Wil15	WILLENHALL 15 (3620015)	564255	5826211	4/1/1969	3/30/1987	COUNCIL OFFICE, Walsall
Wol3	WOLVERHAMPTON 3 (3660003)	558844	5826936	4/1/1948	3/31/1980	HEALTH OFFICES 57 WATERLOO RD, Wolverhampton
Wol7	WOLVERHAMPTON 7 (3660007)	557590	5823618	4/2/1963	3/30/1987	PENN SCHOOL, MANOR RD, Wolverhampton

Table 3. Results of optimization of parameters, radius, residential land-use indicator, and inverse distance weighting (IDW) power. Maximum values in bold.

	Radius	1960s	1970s	1980s	1990s	2000s
Radius	300	0.02	0.01	0.01	0.00	0.02
	3000	0.19	0.20	0.19	0.12	0.01
	7000	0.33	0.37	0.38	0.28	0.05
	8000	0.28	0.33	0.38	0.33	0.10
	10000	0.22	0.27	0.34	0.34	0.14

	Land Use	1960s	1970s	1980s	1990s	2000s
Residential Land-use	1.0	0.24	0.28	0.34	0.31	0.12
	0.8	0.32	0.35	0.41	0.32	0.12
	0.6	0.35	0.40	0.43	0.33	0.11
	0.4	0.40	0.44	0.45	0.36	0.10
	0.2	0.46	0.50	0.49	0.44	0.11
	0.0	0.55	0.57	0.53	0.35	0.07

	IDW	1960s	1970s	1980s	1990s	2000s
IDW Power	2.00	0.00	0.00	0.00	0.01	0.03
	1.50	0.00	0.00	0.00	0.01	0.03
	1.00	0.00	0.00	0.00	0.01	0.03
	0.50	0.02	0.02	0.01	0.00	0.01
	0.40	0.17	0.18	0.16	0.09	0.00
	0.25	0.33	0.36	0.37	0.26	0.04
	0.00	0.33	0.37	0.39	0.29	0.06

Table 4. Correlation coefficients for land-use using the point-density calculation vs. average decadal gravestone stone decay rate for radii of 4000 – 12000 m. Maximum values in bold/italic

Residential Value 0.2						
Resid. Ind.	Radius	1960s	1970s	1980s	1990s	2000s
0.2	4000	0.45	0.48	0.47	0.32	0.06
0.2	6000	0.56	0.60	0.59	0.40	0.07
0.2	7000	0.53	0.58	0.59	0.43	0.10
0.2	8000	0.45	0.51	0.55	0.44	0.12
0.2	10000	0.37	0.44	0.49	0.43	0.14
0.2	12000	0.34	0.42	0.48	0.42	0.14

Residential Value 0.0						
Resid. Ind.	Radius	1960s	1970s	1980s	1990s	2000s
0.0	4000	0.45	0.45	0.40	0.23	0.02
0.0	6000	0.65	0.66	0.60	0.34	0.03
0.0	7000	0.65	0.68	0.65	0.41	0.06
0.0	8000	0.52	0.58	0.60	0.45	0.10
0.0	10000	0.38	0.44	0.48	0.41	0.14
0.0	12000	0.33	0.40	0.46	0.40	0.14

Table 5. Correlation coefficients for gravestone decay and land use for each directional search window. Maximum values in bold/italic with near maximum values in grey.

Azimuth	1960s	1970s	1980s	1990s	2000s
0	0.01	0.02	0.05	0.12	0.14
45	0.00	0.00	0.00	0.01	0.05
90	0.13	0.14	0.14	0.12	0.04
135	0.39	0.38	0.33	0.16	0.00
180	0.33	0.26	0.14	0.01	0.06
225	0.31	0.27	0.18	0.03	0.03
270	0.32	0.39	0.44	0.34	0.06
315	0.15	0.23	0.33	0.39	0.19
0	0.10	0.16	0.26	0.33	0.20
45	0.00	0.00	0.01	0.04	0.09
135	0.45	0.41	0.29	0.09	0.01
135	0.15	0.15	0.14	0.11	0.03
225	0.31	0.27	0.18	0.03	0.03
270	0.36	0.44	0.51	0.41	0.09
0	0.08	0.12	0.19	0.27	0.20
45	0.12	0.13	0.15	0.15	0.08
135	0.35	0.31	0.23	0.09	0.00
180	0.52	0.49	0.37	0.13	0.01
225	0.46	0.49	0.45	0.24	0.01
315	0.29	0.37	0.46	0.43	0.14

Table 6. Mean decadal SO₂ and smoke concentrations (µg/m³) for 23 air-quality monitoring stations in the study area. Interpolated land-use indicator determined by point-density function.

site_name	Land Use Indicator	1960s		1970s		1980s	
		SO2	Smoke	SO2	Smoke	SO2	Smoke
BILSTON 3	0.56	99.00	128.00	-	-	-	-
BILSTON 18	0.55	-	-	64.50	29.00	40.67	25.00
BILSTON 19	0.64	-	-	-	-	42.60	15.60
BIRMINGHAM 11	0.55	277.33	131.17	-	-	-	-
BIRMINGHAM 13	0.46	202.40	125.20	-	-	-	-
BIRMINGHAM 21	0.55	-	-	101.86	27.57	75.00	22.67
BIRMINGHAM 26	0.52	-	-	100.00	28.60	46.50	15.30
CANNOCK 15	0.07	103.50	103.50	-	-	-	-
CANNOCK 17	0.07	-	-	88.33	65.50	54.13	50.88
CANNOCK 18	0.06	-	-	-	-	-	-
KIDDERMINSTER 3	0.07	167.33	112.75	-	-	-	-
KIDDERMINSTER 4	0.06	60.00	60.00	47.14	14.86	-	-
KIDDERMINSTER 5	0.07	-	-	72.00	13.00	-	-
OLDBURY 5	0.50	127.71	94.29	108.70	37.90	116.00	25.67
ROWLEY REGIS 1	0.46	126.33	64.00	86.80	44.40	-	-
ROWLEY REGIS 2	0.46	-	-	58.80	22.00	63.33	14.67
ROWLEY REGIS 3	0.50	-	-	-	-	-	-
STOURBRIDGE 1	0.24	115.33	84.00	82.13	34.44	66.00	24.33
WALSALL 13	0.33	155.50	111.63	78.60	50.00	44.22	26.78
WALSALL 18	0.32	-	-	81.33	29.33	46.44	21.56
WEDNESFIELD 1	0.43	117.50	117.50	79.00	46.20	81.00	30.00
WEDNESFIELD 2	0.43	-	-	-	-	44.75	15.38
WILLENHALL 1	0.52	159.67	132.75	-	-	-	-
WILLENHALL 15	0.53	-	-	113.40	42.70	52.50	26.00
WOLVERHAMPTON 3	0.33	118.71	109.43	85.50	43.90	-	-
WOLVERHAMPTON 7	0.33	102.67	85.00	54.83	23.33	52.63	13.38