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A 'sliding contact' dynamic force spectroscopy method for interrogating slowly forming polymer crosslinks.

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10 Abstract

11 Dynamic Single Molecule Force Spectroscopy (SMFS), conducted most commonly using 12 AFM, has become a widespread and valuable tool for understanding the kinetics and 13 thermodynamics of fundamental molecular processes such as ligand-receptor interactions and 14 protein unfolding. Where slowly forming bonds are responsible for the primary 15 characteristics of a material, as is the case in crosslinks in some polymer gels, care must be 16 taken to ensure that a fully equilibrated bond has first formed before its rupture can be 17 interpreted. Here we introduce a method, sliding contact force spectroscopy (SCFS), which 18 effectively eliminates the kinetics of bond formation from the measurement of bond rupture. 19 In addition it permits bond rupture measurements in systems where one of the binding 20 partners may be introduced into solution prior to binding without tethering to a surface. 21 Taking as an exemplar of a slowly forming bond the 'eggbox' junction crosslinks between 22 oligoguluronic acid chains (oligoGs) in the commercially important polysaccharide alginate, 23 we show that SCFS measures accurately the equilibrated bond strength of the crosslink when 24 one chain is introduced into the sample solution without tethering to a surface. The results 25 validate the SCFS technique for performing single molecule force spectroscopy experiments, 26 and show that it has advantages in cases where the bond to be studied forms slowly and 27 where tethering of one of the binding partners is impractical.

29 Introduction

28

The nature of the dynamic single molecule force spectroscopy (SMFS) experiment allows inherent variations in individual trajectories of unbinding to be observed directly and in real time, while the kinetics and, more recently, the thermodynamics of the bond rupture can be measured¹. This ability has been widely applied in the study of the rupture of bonds ranging from ligand-receptor interactions to the bonds holding proteins in their folded state. To

 characterise a bond formed between two initially separated binding partners, such as that between a ligand and a receptor, the SMFS experiment typically involves tethering the two binding partners to the two surfaces involved (a substrate and the force transducing probe), typically by a polyethylene glycol (PEG) chain. The two surfaces are then brought together for a short time (typically milliseconds, during which the bond between the ligand and receptor may form) and then separated, whereupon the bond is broken. The record of the force experienced by the probe as it is separated from the substrate constitutes the raw data for the dynamic force spectrum (DFS), which is then constructed from a plot of rupture forces f at (the natural log of) instantaneous loading rates at rupture r. Kinetic and thermodynamic parameters are then extracted from fits to the plot of f vs. $\ln(r)$. For nearly two decades the prevailing model for ligand-receptor interactions measured by SMFS has been the Bell-Evans model², which characterises rupture bonds in terms of k_{off} and x_t , the kinetic off rate and the distance to the transition state barrier, but recently a new model³ has been developed that seamlessly combines the slow and fast loading rate regimes and allows extraction of the thermodynamic parameter ΔG_{bu} , the free energy of unbinding, as well as the values of k_{off} and x_t .

Despite the technique relying on the measurement of bonds formed during short, millisecond-timescale contacts between the two surfaces, measurements of the rate of bond formation are confounded by the influence of probe dynamics and the elasticity of the tethers, so estimates of k_{on} derived from AFM force spectroscopy measurements, while sometimes agreeing with bulk measurements⁴, in other cases differ widely from those reported by other methods, making it difficult to assess whether an equilibrated bond has formed. An example of this is the case of the interaction between the antibiotic vancomycin and its target in Staphylococcus *aureus*, the D-Ala- D-Ala terminus of the bacterial cell wall peptidoglycan precursor⁵. Isothermal calorimetry^{6,7}, affinity capillary electrophoresis⁸ and competitive titration methods⁹ have previously established that the dissociation constant K_D for this interaction is in the range of $1 \times 10^{-6} - 10^{-9}$ M, whereas AFM analysis⁴ produced values of k_{off} and k_{on} of $2x10^{-3}$ s⁻¹ and 5 M⁻¹s⁻¹ respectively, giving a value for K_D of 0.4 mM; a difference of 3-6 orders of magnitude from the range of bulk solution values. Given that typical k_{on} values for ligand-receptor interactions such as vancomycin- D-Ala- D-Ala are of the order of 10^6 or 10^7 $M^{-1}s^{-1}$ rather than the 5 $M^{-1}s^{-1}$ measured by AFM, it is clear that estimates of k_{on} based on AFM data can be inaccurate. Consequences arising from the conditions inherent in

conventional single molecule force spectroscopy therefore include a suboptimal sampling ofslowly formed bonds due to the limited time available for bonds to be formed.

> In many cases studied, the high k_{on} typical for ligand-receptor interactions allows us to assume that fully equilibrated bonds form during the tens of milliseconds that probe and substrate are close together during a force spectroscopy cycle. However, an example of an important interaction for which the limited time for bond formation may affect SMFS measurements is the calcium-mediated 'eggbox' junction, crosslinking between sequences of oligoguluronic acids (oligoGs), that is primarily responsible for alginate gelation. Each unit of an eggbox junction consists of a calcium ion-mediated interaction between pairs of guluronic acids (gulA) on opposing chains of alginate in a 2:1:2 gulA:Ca²⁺:gulA complex (Figure 1a). Consecutive sequences of these interactions constitute the eggbox junction, forming a crosslink in the network. The rheology of polymer gels is strongly influenced by long timescale relaxation processes that occur following formation and deformation of the gel¹¹⁻¹³. These relaxation processes, which can take hours to complete, involve the breaking and reforming of the interactions underpinning these crosslinks to resolve internal stresses arising from the deformation. Recently¹⁴ we showed that even at the level of individual crosslinks, in oligoGs as short as 16 units, times of several hundred milliseconds were required for the crosslinks to reach their equilibrated, full strength. This poses a problem for the study of crosslinking at the molecular level using techniques such as atomic force microscopy (AFM)-based single molecule dynamic force spectroscopy (SMFS) since as dwell times of the probe at the substrate increase, the incidence of multiple and non-specific interactions increase, potentially obscuring the specific interactions of interest and leading to inaccurate measurements. Recently this problem was shown to be especially acute for binding partners coupled to long tethers¹⁵. Conversely, the use of long tethers make the identification of single bond ruptures possible on the basis of the apparent Kuhn length of the PEG tether¹⁶. Indeed, in the study described above we were unable to extend the analysis of the bond rupture beyond 500 ms due to the paucity of reliable specific, single bond ruptures at longer dwell times. A single molecule method that allows the accurate measurement of the strength of equilibrated crosslinks within polymer chains is, therefore, lacking.

An alternative iteration of dynamic force spectroscopy may be called 'sliding contact'
(dynamic) force spectroscopy (hereafter SCFS). The SCFS method (Figure 1b) introduces a
'sliding contact' between the AFM probe and the substrate, formed by a (pseudo)rotaxane¹⁷.

A rotaxane consists of a macrocyclic 'bead' threaded onto a polymer axis, with 'stations' or 'stoppers' along the axis that interact with the bead or stop it from sliding off the end of the polymer axis (the presence or absence of stoppers distinguishes a rotaxane from a pseudorotaxane)¹⁸. In SCFS, the polymer axis will be the polymer of interest conjugated to a poly(ethylene glycol) (PEG) polymer, on to which a bead (α -cyclodextrin (CD), with a tether terminating in a reactive group recognised by the AFM probe) is threaded. The spontaneous formation of polyrotaxanes between PEG and α -CD is well known^{17,18}, whereby the PEG threads into the pore of the α -CD. The PEG is grafted to a substrate suitable for SMFS that acts as a stopper, and the AFM probe is brought into contact with the substrate and retracted, as in a conventional SMFS experiment. When a bond is formed between the AFM probe and the tether on the CD and the probe retracts, the CD is forced to slide along the polymer axis, encountering resistance to sliding in proportion to the strength of the interaction between the CD bead and the polymer axis, station or stopper it encounters. This change in resistance will be recorded in the force vs. separation spectrum in the same way as other changes in force (such as polymer stretching and bond rupture) are in conventional DFS. In the present work, the complex formed by the two guluronic acid oligomers and Ca^{2+} ions represents a station and the process that occurs when the CD bead encounters this complex is sketched in figure 1c. A similar dynamic force spectrum can be constructed and the same models used to fit the data and characterise the sliding of the CD over a station or stopper. Iterations of this approach have been used to manipulate α-CD beads forming a polyrotaxane with PEG back and forth along the PEG axle¹⁹, and to measure the force required to drive a bead between two stations in a rotaxane^{20,21}. It has also been considered as a potential sequencing tool for DNA and other polymers²²⁻²⁵.



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4 5 6 7 8 9 10 11 12 13 14 15 16 17	127	Figure 1 (a) Structure of the 'eagbor' junction zone between two pairs of guluronic acid
	120	sequences and a divalent metal cation such as calcium (b) diagram showing the analogy
	12)	between a conventional rotayane (left) and the sliding contact pseudorotayane (right). The
	130	common features (stations, head, axis) are labelled in each (c) Illustration of the proposed
	131	machanism of unzipping of an agabax junction by sliding contact force spectroscopy (i) A
	132	mechanism of unzipping of an eggoox function by straing contact force spectroscopy. (i) A
	133	cyclodexirin macrocycle forms a pseudorolaxane with the FEG portion of a FEG-guiuronic
	134	acia conjugate; (ii) an AFM probe binds to a tether on the cyclodextrin; (iii) the AFM probe
18 19	135	retracts, pulling the tethered cyclodextrin along the conjugate; (iv) any guluronic acid
19 20 21 22 23 24 25 26 27 28 29	136	oligomers bound to the conjugate are displaced by the cyclodextrin as it slides along.
	137	
	138	While SCFS offers the opportunity to measure the difference in interaction between the
	139	sliding CD and the monomers in the polymer axle during sliding, the CD may also be used as
	140	a molecular 'zipper' to unzip molecules bound to sites incorporated into the polymer. From
	141	the point of view of addressing the eggbox junction zone in alginate, crosslinking between
30 31	142	the oligoG conjugated to the PEG (and along which the CD is driven by the AFM probe) and
32	143	untethered oligoG that has bound to it may be treated as a kind of stopper, in that the CD pore
33 34	144	is too small to accomodate both strands and so proceeds by unzipping the interaction between
35 36	145	the conjugated and untethered oligoG. This application of SCFS offers an alternative that
37 38	146	potentially addresses several drawbacks of conventional DFS, including those highlighted
39	147	above. Firstly, because the AFM probe is functionalised to pick up a tether attached to the
40 41	148	functionalised CD and does not need to form the bond to be broken during the approach cycle
42 43	149	of the experiment, SCFS offers the freedom to allow the bond of interest to be formed under
44	150	ideal conditions and timescales. Secondly, once the CD has been picked up by the AFM
45 46	151	probe, the retraction of the probe drives the CD along the polymer, so the direction of the
47 48	152	unzipping action is controlled by the sequence and orientation of crosslinking sites along the
49 50	153	polymer. Thirdly, only one of the binding partners needs to be tethered to the substrate,
51 52	154	allowing the probing of interactions between a tethered and a free binding partner, removing
52 53	155	a source of potential distortion of the interaction between the binding partners.
54 55	156	
56 57	157	Here we show that SCFS can be used to (i) break bonds formed between an untethered
58	158	oligoguluronic acid chain (oligoG) and its tethered counterpart in the presence of free Ca^{2+} .
59 60	159	(ii) consider the effects the controlled direction of sliding has on the runture of the bond and
	160	(iii) establish the value of the free energy of unbinding $\Lambda G_{L_{a}}$ of fully equilibrated crosslinks
	100	(in) company of the value of the free energy of unoniting 2000 of funly equilibrated elossinity

between the two oligomers, where binding is estimated to take on the order of seconds to reach full strength. We thereby aim to establish this method as a viable one for measuring the equilibrated bond strength of slowly forming bonds at the single molecule level. **Experimental** OligoG conjugation, rotaxane formation and immobilisation Conjugates between purified oligoGs with n = 6, 10 and 16-18 guluronic acid monomers and PEG were prepared as described previously¹⁴. Briefly, oligoGs were end-functionalised with Boc-NH-PEG-NH₂ (an amine-terminated poly(ethylene glycol) (PEG) with a tert-butoxycarbonyl (Boc) protecting group) using a reductive amination method²⁶ previously demonstrated for covalently linking polysaccharides to AFM probes and substrates²⁷. The deprotected amine group on the oligoG-PEG conjugate was coupled to a N-hydroxysuccinimide-PEG-maleimide (NHS-PEG-Mal) and this conjugate was coupled to a mica surface functionalised with thiol groups following a method previously used to functionalise silica beads²⁸. α -cvclodextrins were modified with a bisamine-terminated PPG-PEG-PPG tether as described previously²³. Briefly, aldehyde groups were created on the cyclodextrins by treatment with Dess-Martin periodinane and bis(2-aminopropyl) polypropylene oxide-polyethylene oxide block copolymer was coupled to the aldehyde in a Schiff base reaction. 0.4% w/w of each PEG-oligoG conjugate was mixed with a 1:1 mole equivalent of amino-functionalized α -CD for 24 hours, and deposited onto template-stripped gold from water for 24 hours. Untethered oligoGs were used as isolated after purification. AFM probes (MLCT silicon nitride from Veeco Instruments, Santa Barbara, CA, USA) with nominal spring constants of 10 and 20 pN/nm were silanised with thiol-terminated alkylsilane and then further functionalised with NHS-PEG-Mal as described above. **AFM force spectroscopy experiments** Force spectroscopy experiments were carried out using a JPK Nanowizard III (JPK, Berlin, Germany) in buffered aqueous solution. Spring constants (calibrated using the method built in to the JPK AFM and based on the method devised by Hutter & Bechhoefer²⁹) ranged from 13.3 to 40.4pN/nm. Experiments were conducted in 20mM MOPS (3-morpholinopropane-1-sulfonic acid), with the addition of 2 mM CaCl₂ and/or 20 mM EDTA as described. Force

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curves were collected in arrays of 32×32 data points over areas of $2 \times 2 \mu m^2$ at a relative setpoint of 0.2 nN. The z-length was 200 nm, the approach and retract speeds were set at 500 nm.s⁻¹ and data was collected at a rate of 2048 samples.s⁻¹. Force curves were exported and analysed using JPK's data processing software (JPK instruments, DE, ver. 4.2.23). For single chain sliding experiments events with total length in the interval 10-30 nm were selected and terminal plateau length was identified and measured using the JPK software, while for the unzipping experiments, the unbinding events (occurring at a frequency of <10% in all cases) were fitted with an extended freely-jointed chain model and those events with fitted contour lengths in the interval 10-40 nm were selected for analysis using the Friddle- Noy-De Yoreo (F-N-Y) model^{1,3} for the forced rupture of bonds using OriginProTM (OriginLab, ver. 8.0724). In equation 1, the F-N-Y model recognises that rebinding at slow loading rates represents an equilibrated situation, reflected by the equilibrium force f_{eq} , and also reflects the Bell-Evans f $\sim \ln(r)$ relation² in the high loading rate regime. Besides estimating the values of the kinetic parameters x_t and k_{off} (equation 2) in common with the Bell-Evans model, the F-N-Y model allows the estimation of the free energy of unbinding ΔG_{bu} for the single molecule interaction from the values of f_{eq} and k_{eff} , the effective spring constant (equation 3).

211 Equation 1.

$$\langle f \rangle = f_{eq} + f_\beta \cdot ln \left(1 + e^{-0.577} \cdot \frac{r}{f_\beta k_u(f)} \right)$$

213 Equation 2.

$$k_{off} = \frac{k_u(f)}{exp\left[\frac{f - 1/2 k_{eff} \cdot x_t}{f_\beta}\right]}$$

Equation 3.

$$\Delta G_{bu} = \frac{\left(f_{eq}\right)^2}{2k_{eff}}$$

5 216

Here $\langle f \rangle$ is the most probable rupture force for events at a certain value of loading rate *r*; f_{eq} is the mean force required to irreversibly separate the binding pair (the 'equilibrium force'); $f_{\beta} = k_{\rm B}T/x_{\rm t}$ is the thermal force where $x_{\rm t}$ is the distance to the energy barrier, $k_{\rm B}$ the Boltzmann

constant and T the temperature in Kelvin; $k_u(f)$ is the unbinding rate at a given force f; k_{eff} is the effective spring constant, $k_{\text{eff}}^{-1} = k_{\text{cantilever}}^{-1} + k_{\text{linker}}^{-1}$. The most probable rupture forces (f) were calculated for intervals based on the loading rate r, with the number of datapoints n per interval ranging from 10 to 30, so that the maximum error bars on the value of the most probable rupture force (f) in each interval did not exceed 10 pN. DFS (plots of (f) vs. $\ln(r)$) for both sets of experiments were then constructed and the values for the parameters f_{eq} , x_t , k_{off} and ΔG_{bu} were extracted from fits of the F-N-Y model to the DFS for each oligoG. The F-N-Y model has been used recently to determine the length of the minimum sequence of guluronic acids to form a strong, stable calcium-mediated 'eggbox' junction¹⁴. **Results and Discussion** In the SCFS experiment, untethered oligoG was allowed to bind in the presence of CaCl₂ to oligoG tethered to the surface by PEG, as in the conventional SMFS experiment¹⁴, but with the addition of α -CD which was threaded over the PEG polymer to form a pseudorotaxane prior to binding the polymer to the surface. A tether on the α -CD was terminated with an amine group and an AFM probe was functionalised with another PEG spacer, this time terminated with a succinimide group. Previously²³ we have shown that at neutral pH a strong bond was rapidly formed between the amine and succinimide groups, and this bond allowed the AFM probe to manipulate the α -CD along the polymer chain and over the oligoG. Firstly, in order to confirm that we were observing the pickup and sliding of the CD, we characterised the length of the plateau in force caused by sliding the CD along individual strands of 6-, 10- and 16-18-mer (2-, 4- and 8-Ca²⁺) oligoGs. The force spectra collected do not show the sharp increase in force prior to the terminating rupture point that is typically observed for single molecule stretches in conventional force spectroscopy. Instead, the stretching events start with the force increasing to approximately 40-70 pN, forming a plateau at this force for some distance, before abruptly terminating, with the recorded force returning to zero. Examples of these force spectra are presented in Figure 2a. The length of the plateau region can be determined in the AFM software, and we see the lengths of the three oligomers reflected in the lengths of the plateaus, as presented in Figure 2b. The experimentally observed plateau lengths are close to the expected lengths of oligoGs of 6, 10 and 16-18 monomers, based on a per monomer length for guluronic acid of 0.435 nm^{30} (Figure 2c).



Figure 2: (a) examples of force curves from the different oligoG experiments: curves 1 and 2
are from the 16-18-mer oligoGs, curves 3 and 4 are from the 10-mer oligoGs and curves 5
and 6 are from the 6-mer oligoGs ; (b) distribution of plateau lengths for the 3 oligomers; (c)
comparison of mean observed length to expected oligomer length for the 3 oligomers; (d)
DFS for sliding CD ring along the 3 oligomers. The scale of the x-axis is the natural
logarithm of the loading rate r (in pN/s), divided by 1 pN/s.

In order to accurately measure rupture forces when the sliding contact 'unzips' the interaction between the oligoGs, we must take into account the force required to slide the cyclodextrin ring over the oligosaccharide chain. The dynamic force spectrum resulting from a plot of f vs. $\ln(r)$ for these experiments reveals that the three oligomers all show similar behaviour – indeed, the DFS for each oligomer can be superimposed on each other and overlap extensively, each spectrum showing an almost flat dependence of f on $\ln(r)$ (Figure 2d). Within the paradigm of the F-N-Y model, a flat dependence of f on $\ln(r)$ reflects the equilibrium condition, where the rates of unbinding and rebinding (here taken to mean sliding on to or off the next monomer in the chain) exceed the rate of loading r on the bond. This

means that fits to the F-N-Y model cannot produce reliable values for the kinetic parameters $x_{\rm t}$ and $k_{\rm off}$ but that we can estimate the value of f_{eq} (and hence $\Delta G_{\rm bu}$) for the sliding interaction of the cyclodextrin ring along the polymer strand directly from the most probable plateau force across each spectrum. It is however more difficult to accurately measure the loading rate r in the transition to these relatively low force plateau events, which impacts on the reliability of the DFS and subsequent fits. Reassurance that the force f is independent of rcomes from the observation that the range of f observed is relatively narrow, similar to the background thermal noise level of ± 15 pN, as would be expected when f is not changing. Thus, applying the F-N-Y model to extract the value of f_{eq} produces values of 43±11, 44±8 and 54±12 pN for the 6-, 10- and 16-18-mer oligoGs respectively, and these values overlap with the mean rupture forces across each dataset. The unbinding energies ΔG_{bu} derived from these values reflect the energy required to thread the cyclodextrin on to, and off, a monosaccharide within the oligoG, a process that occurs for each monomer in the oligomer, producing the observed plateau. Thus, when the values of k_{eff} ($k_{cantilever} = 14, 13$ and 25 pN.nm⁻¹ and $k_{\text{linker}} = 67 \text{ pN.m}^{-1}$)¹ are considered, the energies ΔG_{bu} required to slide the cyclodextrin over individual monomers in the oligoGs are found to be similar to each other, at 47, 50 and 48 kJ/mol for the 6-, 10- and 16-18-mer oligoGs respectively.

Having established the energy required to slide the cyclodextrin ring along the oligomer chain, we can use this approach to unzip specific bonds formed between components of the threaded oligomer and molecules that are introduced into the sample space without tethering to the substrate or AFM probe. Here, the experiment is conducted as just described but untethered oligoGs and calcium ions are injected into the sample space, so that bonds formed between tethered and untethered molecules could be interrogated. The 10-mer oligoG is expected to crosslink a maximum of 4 Ca^{2+} ions (because the tethered oligoG effectively loses one monomer during conjugation to the PEG¹⁴), and the 16-18-mer oligoG up to 8 Ca^{2+} ions. When we carry out these experiments, we observe new interactions in addition to the single chain sliding events already characterised. Addition of EDTA effectively abolishes these interactions and we subsequently only observe single chain sliding events, as described above. Depending on the oligomer under consideration, we observe different behaviour, as depicted in Figure 3a. In particular we see, in the two shortest oligoGs, some events that more closely resemble conventional single molecule rupture events, and which have recently been described in the alginate system¹⁴: sharp ruptures at higher forces that return rapidly to zero force after the rupture. In contrast, in the 16-18-mer oligoG we observe that once the force



 Figure 3. (a) examples of force curves showing the rupture of crosslinks between oligoGs. 1 and 2 show ruptures between 16-18-mer oligoGs; 3 and 4 show ruptures between 10-mer oligoGs and 5 and 6 show ruptures between 6-mer oligoGs. 1 and 2 are examples of dual rupture events: a 'sawtooth' double rupture in curve 1 (distance between events = 3.6 nm) and a plateau in curve 2 (distance between events = 4.1 nm). (b) histograms of rupture forces for (top) 6-mer (middle) 10-mer and (bottom) 16-18-mer oligoGs. (c) dynamic force spectra for all data for the three oligomers. The scale of the x-axis is the natural logarithm of the loading rate r (in pN/s) divided by 1 pN/s. (d) DFS for the three oligomer fractions, split into groups according to the force histogram and DFS presented in figure 3b and c. Solid lines are fits to the unzipping data for 6-mer (Δ), 10-mer (\Box) and 16-18-mer (**0**) oligoGs, dashed lines are fits to the sliding data for the three oligomers and dotted lines are extrapolations to the value of f_{eq} in each case. (e) comparison of force curves from SMFS (black) and SCFS (grey) experiments, highlighting the increased force signal originating from the sliding of the *CD* ring along the *PEG* chain. (f) distribution of distances between first and second rupture events in the 16-18-mer oligoG SCFS experiment. (force curve 1. in figure 3a) and sometimes resembles a plateau (force curve 2. in figure 3a). The existence of these dual events was confirmed by fitting a second freely-jointed chain stretch to the data, and the zoomed spectra in figure 3a show that the data for the two curves are fit by two freely jointed chains each, using the same Kuhn length (0.70 and 0.76 nm) but

separated by 3.6 and 4.1 nm respectively. There is a continuum of responses observed following the first rupture in these cases, so distinguishing sawtooth and rupture events is difficult to achieve. As exemplars of this transition, curve 1 is identified as a sawtooth event by the drop in force immediately following the first rupture (33 pN), before the force increases again prior to the second rupture while curve 2 is identified as a plateau event because the force only drops a small amount (16 pN) before reaching a plateau force which is terminated by a brief increase in force. In all cases, these events occur alongside events that resemble those seen in the single chain sliding experiments as presented in Figure 2a. Figure 3b shows histograms of the rupture forces and Figure 3c shows plots of force vs ln(r) for the three oligomers studied, while the DFS derived from this data is shown in Figure 3d.

In each case, then, the events fall into two groups, those with sharp rupture events (which
may be followed by a plateau or second rupture) and those with only plateaus. In each case
the latter group both resembles in form and in force the single chain sliding DFS while the

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former group, at higher forces, constitutes a new type of event well separated from the single chain sliding events. These clusters reflect the types of event discussed above, suggesting that the two types of event can be identified as instances where unterthered oligoG bound to the tethered oligoG has been 'unzipped' by the action of the cyclodextrin ring sliding along the tethered chain (the 'unzipping' group), and instances where no untethered oligoG has bound to the tethered chain and the cyclodextrin slide freely along and off, as it does in the absence of untethered oligoG (the 'sliding' group). By comparing the numbers of the two types of event we can estimate the extent of binding of the untethered oligoG to the tethered oligoG, and in these cases we observe unzipping in 81, 76 and 52% of observed events for the 6-, 10-and 16-18-mer oligoGs respectively. The existence of the sliding group of events reveals that binding between the oligoGs is not 100% efficient, even when minutes are allowed for binding to occur. In the 6-mer oligoG the forces measured in the unzipping group are significantly lower than those in the unzipping groups for the two longer oligoGs. This distribution of forces for the three oligomers bears out the conclusion of our previous work¹⁴, where we showed (at long interaction times) that Ca^{2+} -mediated crosslinks between short oligoGs ruptured at lower forces than those between oligoGs of 10 monomers or more.

The DFS for the unzipping groups each show evidence that the data encompass the transition between the equilibrium and non-equilibrium states and can be fit by the F-N-Y model, allowing the estimation of the parameters x_t , k_{off} and f_{eq} (and hence ΔG_{bu}). This finding is, on first consideration, surprising: we have established that this is a slowly forming bond so we do not expect to find a fast rebinding rate during its rupture. It has been proposed³¹ that the slow binding kinetics of elastic polyelectrolyte crosslinks such as the eggbox junction arise from the time taken for the polymeric strands to align and form the initial crosslinks in coordination with the Ca^{2+} ions. In the situation arising during the sliding of the CD ring along the oligoG chain and the consequent rupture of the crosslink, all components of the crosslink remain close together so rebinding may occur rapidly. The rate-limiting step in bond formation is then the initial rearrangement of the polyelectrolyte chains, which is not significantly perturbed in the time it takes for the CD ring to move forward: indeed, the size and stiffness of the polymer chains that limit the bond formation rate in the first instance may also be the factors driving rapid rebinding immediately following unbinding. Conversely, the sliding groups show little dependence of f on r, so only f_{eq} (and ΔG_{bu}) may be measured.

To accurately characterise the rupture we must deconvolute the force required simply to slide the cyclodextrin along the tethered oligoG from the force required to unzip the bound untethered oligoG. Since both processes occur simultaneously the overall force observed consists of the sum of these two forces, so the value of f_{eq} for the unzipping process is obtained by subtracting the value of f_{eq} for the single chain sliding event from the overall f_{eq} observed for the interaction at low loading rates and derived from the DFS shown in Figure 3d. The resulting force we call the excess f_{eq} , and the free energy calculated from it is the excess ΔG_{bu} .

Table 1. Values of parameters from fits of the data for the sliding and unzipping events for the three oligomers to the F-N-Y model. Values are given as mean \pm SD.

OligoG	$f_{\rm eq}({\rm pN})$	$\operatorname{Excess} f_{\operatorname{eq}}$	Excess ΔG_{bu}	x _t (nm)	$k_{off}(s^{-1})$
interaction		(pN)	(kJ/mol)		
6 sliding	44±6	n.d.	n.d.	n.d.	n.d.
6 unzipping	58±12	20±12	10.3±6.1	0.08±0.03	21.3±12.6
10 sliding	43±7	n.d.	n.d.	n.d.	n.d.
10 unzipping	112±23	68±24	125±30	0.12±0.05	2.1±1.8
16 sliding	51±9	n.d.	n.d.	n.d.	n.d.
16 unzipping	141±31	87±26	125±33	0.10±0.04	7.2±6.1

Table 1 presents the values of the derived parameters. Of particular note in this data is the fact that the values of excess ΔG_{bu} for the 10-mer and the 16-18-mer are similar, at 125 kJ/mol. Assuming, for the 10-mer oligoG interaction, 4 Ca²⁺ ions are involved, this value corresponds to 31 kJ/mol per Ca^{2+} ion, in close agreement with the value measured using conventional SMFS at long dwell times $(36 \text{ kJ/mol/ Ca}^{2+})^{13}$ and falling within the range of values measured³² or calculated from simulations^{33,34} (25-60 kJ/mol/ Ca^{2+}). The calculated values for excess ΔG_{bu} for the 10-mer and the 16-18-mer are similar even though the values of excess f_{eq} differ, because accurate calculation of the free energy of unbinding requires the effective spring constant of the cantilever and polymer tethers^{1,3}, and in the case of the experiments conducted here the cantilever spring constants for the 10-mer and 16-18-mer experiments were 13 and 25 pN/nm respectively. The excess ΔG_{bu} for the 6-mer is much smaller at 10 kJ/mol, similar to the value obtained from conventional SMFS¹⁴. Values for the kinetic off-rate, k_{off} , for the two longest oligomers are also similar to each other (2.1±1.8 and $7.2\pm6.1 \text{ s}^{-1}$ for the 10-mer and the 16-18-mer respectively) but much higher (21.3 s⁻¹) for the

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6-mer. Values of x_t for the three oligomers are similar to each other, at about 1 Ångström, a value that reflects the distance the crosslink must be distorted before it ruptures. A key observation is that the range of forces observed is narrower for the sliding contact experiment than was recorded in the conventional SMFS experiment¹⁴: in the previous SMFS work, franged from 50-70 pN up to 250 and 450 pN for the 10-mer and 16-18-mers over 3 decades of loading rate, whereas in the present study the range of forces differs by less than 100 pN over a similar range of loading rates (Figures 3b-d). This observation suggests that at the range of loading rates achieved in this experiment the bond remained close to the equilibrium regime where rapid rebinding is possible, only being taken away from this regime at the highest loading rates. This reflects the processive nature of the rupture event in the sliding contact experiment. Instead of tension being applied along the whole crosslink, as it is when the oligomers are pulled apart in conventional SMFS, in the sliding contact experiment the crosslink is addressed one monomer at a time. Thus, for both the 10-mer and the 16-18-mer, the initial unzipping event was identical and reflects the same initial opening up of the crosslink, which is much stronger than the opening of the crosslink between 6-mer oligoGs. Further evidence that the group of force curves we have identified as unzipping events reflect the interaction of the CD ring with the oligoG crosslink comes from a comparison with force curves obtained in the conventional oligomer separation SMFS experiment¹⁴, as depicted in Figure 3e. Here, at positions prior to the increase in force that precedes crosslink rupture, we observe that the force recorded in the SCFS experiment is higher and more plateau-like than the corresponding SMFS experiment. This is due to the sliding of the CD ring along the PEG chain, a feature previously observed in other SCFS experiments²³.

We can therefore conclude that the state or number of crosslinked monomers downstream of the first influences the force required to rupture the crosslink, just as it does in conventional SMFS, despite the different way in which the tension is applied to the junction. Thus the junction is not unzipped one monomer at a time, but the first monomer is stabilised in the crosslink by its downstream neighbours, so that the 4 Ca^{2+} crosslink fails as a single unit (again, as it does in conventional SMFS). In the case of the 10-mer, the initial opening of the junction is sufficient to destabilise the rest of the junction so a sharp rupture is observed. This reflects the fact that the minimum strong crosslink requires 4 Ca²⁺ ions, and that crosslinks involving fewer Ca^{2+} ions fail at lower forces. In the 16-18-mer oligoG the junction is long enough that the opening of the initial 4 Ca²⁺ crosslink does not destabilise the entire junction, since more than 4 Ca^{2+} ions remain in the crosslink, so a second rupture event (or a plateau in

force) is observed as the cyclodextrin ring slides along the chain, unzipping interactions until destabilisation occurs. Plateaus, rather than a 'sawtooth' profile, would be expected to be observed when the CD ring encounters the next crosslinked sequence before the polymer chain has had time to relax and release the tension on the CD, or when the freed end of the oligoG remains to obstruct the CD as it passes along the tethered chain, whereas sawtooth profiles of double ruptures would be expected to be observed in cases where the freed chain happens to move away from the sliding CD. Figure 3a shows examples of sawtooth and rupture events. Figure 3f shows the distribution of the distances between the first and subsequent rupture events (and the lengths of plateaus) following initial rupture in the 16-18-mer, which has a peak at 3-4 nm. This value is close to the difference in length between the 10-mer and 16-18-mer oligoGs presented in Figures 2b and c (3.9 nm for the 10-mer and 7.0 nm for the 16-18-mer) and so reflects a situation in which, after disrupting 8 or so monomers taking part in the initial crosslink, the CD ring must slide along the polymer chain to address the remaining interacting monomers. This model thus requires cooperativity across several monomers. Voulgarakis et al²² considered the applicability of a sliding contact force spectroscopy technique such as the one realised here as a method for sequencing DNA, using the CD ring to rupture the interactions between basepairs with the different forces required to rupture A-T and G-C interactions used as the basis for reconstructing the sequence. In this work they simulated the sliding contact experiment and found that the basepair interactions tended to rupture in bursts rather than individually, and that the force required to rupture an individual basepair depended on the identity of the next 5 or so basepairs in the sequence. Thus we can expect the number of consecutive Ca^{2+} mediated interacting monomers in the eggbox junction to determine the force required to unzip it, while the much lower temporal resolution of the AFM experiment in comparison to the simulation means that we would observe such rapid bursts of rupture events as a single event. Figure 4 illustrates the proposed progress of the rupture events in conventional SMFS and SCFS, highlighting the different ways in which the crosslink is addressed and ruptured. Finally it may be noted that rotaxanes formed between CD beads and PEG axes can accommodate multiple beads on a single axis¹⁸. This is likely to occur in the SCFS eperiment too and may result in the AFM probe dragging a 'train' of CD beads along the oligomer. The first bead in the train will induce the rupture of any eggbox junctions and the rest of the beads will then slide along and off the chain, potentially yielding subtle differences in the resulting force curves that we have not been able to differentiate from the single bead case.



471 Figure 4. sketches of the arrangements of oligomers, Ca2+ ions and CD rings during (a)
472 SMFS of 10-mer oligoG, (b) SCFS of 10-mer oligoG and (c) SCFS of 16-18-mer oligoG.
473 Arrows depict the point of contact of the force transducer and the direction in which force is
474 applied in each case. (d-f) force curves corresponding to (a-c) above, with the steps (i) – (vii)
475 highlighted in each case.

477 Conclusions

43 478

Single molecule force spectroscopy remains a powerful tool for measuring the strength of individual bonds between molecules brought together transiently. The timescale of the SMFS experiment is expected to be sufficient for many interactions between small molecules to reach equilibrium during the time that the two molecules are close enough to each other to interact. However, particularly in the case of crosslinking interactions between polymers, times in excess of 1 second may be required for the crosslink to reach its fully equilibrated state. Here we have shown, using the example of the Ca^{2+} -mediated crosslink between oligomers of guluronic acid, that an alternative iteration of single molecule force spectroscopy may be used to accurately measure the free energy of unbinding of slowly forming bonds after they have reached equilibrium. We explore the mechanics of the rupture

event caused by unzipping the crosslink with the CD ring and show that we are able to achieve the predicted advantages that this approach holds over conventional SMFS, namely the lack of tethering of the binding partner to the AFM probe and control over the direction in which the bond is attacked. The results allow us to set a value for the free energy required to rupture the minimum Ca^{2+} -mediated crosslink between oligoguluronic acid chains, an interaction that governs the properties of the important polysaccharide alginate, of 125 kJ/mol. References Noy, A.; Friddle, R. W. Practical single molecule force spectroscopy: how to (1)determine fundamental thermodynamic parameters of intermolecular bonds with an atomic force microscope. Methods 2013, 60 (2), 142-150. Evans, E. Probing the relation between force - Lifetime - and chemistry in single (2)molecular bonds. Annu Rev Bioph Biom 2001, 30, 105–128. (3) Friddle, R. W.; Nov, A.; De Yoreo, J. J. Interpreting the widespread nonlinear force spectra of intermolecular bonds. Proceedings of the National Academy of Sciences 2012, 109 (34), 13573–13578. Coppari, E.; Santini, S.; Bizzarri, A. R.; Cannistraro, S. Kinetics and binding (4) geometries of the complex between β 2-microglobulin and its antibody: An AFM and SPR study. Biophys. Chem. 2016, 211, 19-27. (5) Gilbert, Y.; Deghorain, M.; Wang, L.; Xu, B.; Pollheimer, P. D.; Gruber, H. J.; Errington, J.; Hallet, B.; Haulot, X.; Verbelen, C.; Hols, P.; Dufrene, Y. F. Single-Molecule Force Spectroscopy and Imaging of the Vancomycin/ d-Ala- d-Ala Interaction. Nano Lett 2007, 7 (3), 796-801. Rao, J.; Lahiri, J.; Isaacs, L.; Weis, R. M.; Whitesides, G. M. A Trivalent System (6) from Vancomycin·d-Ala-d-Ala with Higher Affinity Than Avidin·Biotin. Science 1998, 280 (5364), 708–711. Jianghong Rao; Joydeep Lahiri; Robert M Weis, A.; Whitesides, G. M. Design, (7)Synthesis, and Characterization of a High-Affinity Trivalent System Derived from Vancomycin and l-Lys-d-Ala-d-Ala; J. Am. Chem. Soc., 2000; Vol. 122, pp 2698-2710. Rao, J.; Whitesides, G. M. Tight Binding of a Dimeric Derivative of Vancomycin (8) with Dimeric 1-Lys-d-Ala-d-Ala; J. Am. Chem. Soc., 1997; Vol. 119, pp 10286-10290.

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