

ELECTRICAL EFFECTS OF GASES ON LEAD TELLURIDE THIN FILMS

by

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Abstract

Interaction of oxygen and atomic hydrogen with thin films of lead telluride was studied by performing in situ Hall measurements. The films were grown in a vacuum of  $\sim 1 \times 10^{-6}$  torr on air-cleaved muscovite mica using a single source evaporation technique. The carrier concentration at room temperature was in the range  $10^{16}$ - $10^{18}$   $\text{cm}^{-3}$  and the values of the Hall mobilities at room temperature ranged from 400-900  $\text{cm}^2 \text{V}^{-1} \text{s}^{-1}$ . The thickness of the films varied from 2000 $\text{\AA}$  to 5000 $\text{\AA}$ .

The effect of oxygen and atomic hydrogen on the electrical properties of the films was examined by continuously monitoring the Hall coefficient,  $R_H$  and the resistivity,  $\rho$  during the gas exposure. Results were interpreted in terms of two models, namely surface adsorption model and diffusion model. Theoretical expressions for  $R_H$  and  $\rho$  were developed for both models in order to compare the experimental and the theoretical  $R_H$  vs  $\rho$  curves. The accuracy of the fit between the two curves was taken as evidence for the validity of the model. The shape of  $R_H$  vs  $\rho$  curve was successfully predicted by the theoretical models under appropriate conditions.

Kinetic studies were also undertaken in an attempt to gain further insight into the mechanisms of gas uptake. In addition, mechanisms of ionisation of H were also considered. Based on the combined evidence of the theoretical models and the kinetic studies, it was proposed that the mechanism of gas uptake was not uniquely defined by the above-mentioned models.

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## CHAPTER 1

### PROPERTIES OF PbTe

#### 1.1 INTRODUCTION

Lead telluride belongs to the lead chalcogenide family where lead sulphide and lead selenide are its other two members. The reason for continued scientific interest in lead chalcogenides is two-fold. Firstly, since lead chalcogenides have relatively small band gaps ( $<0.5$  eV) they are suitable for infra-red detection and, secondly, the possibility of other devices such as thin film transistor based on lead chalcogenides. Properties of lead telluride, PbTe in conjunction with lead sulphide, PbS and lead selenide, PbSe have been reviewed by Scanlon(S1), Putley (P1) and more recently by Ravich et al.(R1) where all three reviews contain exhaustive lists of earlier work. Therefore the purpose of this chapter is to present, briefly, an overview of properties of PbTe.

#### 1.2 CRYSTAL STRUCTURE

Lead telluride has a sodium chloride type face centred cubic structure with Pb occupying (000),  $(a/2 \ a/2 \ 0)$ ,  $(a/2 \ 0 \ a/2)$ ,  $(0 \ a/2 \ a/2)$  and Te occupying  $(a/2 \ a/2 \ a/2)$ ,  $(00a/2)$ ,  $(0 \ a/2 \ 0)$ ,  $(a/2 \ 0 \ 0)$  in the unit cell where  $a$  is the lattice constant. The value of  $a$  given by Dalven (D1) is  $6.462\overset{\circ}{\text{Å}}$  whereas values given by Scanlon (S1) and Ravich et al. (R1) are  $6.46\overset{\circ}{\text{Å}}$  and  $6.50\overset{\circ}{\text{Å}}$  respectively. Bonding in



PbTe is partially ionic and partially covalent, i.e. it is a polar semiconductor.

### 1.3 BAND STRUCTURE

Since PbTe has face centred cubic structure, the first Brillouin zone is a truncated octahedron (K4), as shown in Fig. 1.1. Investigations of optical absorption show that the extrema of the conduction and valence bands lie at the same point in k-space. The constant energy surfaces for valence and conduction bands are ellipsoids centred at L points and strongly elongated along the  $\langle 111 \rangle$  direction as shown in Fig. 1.2. Two principal effective masses may be defined with reference to the axes of the ellipsoid of Fig. 1.2.

$$m_{\ell} = \hbar^2 / \frac{d^2 E}{dk_{\ell}^2} \quad (1.1)$$

$$m_t = \hbar^2 / \frac{d^2 E}{dk_t^2} \quad (1.2)$$

where  $m_{\ell}$  is the longitudinal effective mass and  $m_t$  is the transverse effective mass,  $k_{\ell}$  is a vector perpendicular to  $k_t$  and parallel to (111) direction. The mass anisotropy K is related to  $m_{\ell}$  and  $m_t$  by the following equation

$$K = \frac{m_{\ell}}{m_t} \quad (1.3)$$

Cuff et al. (C1) give the value of K for valence and conduction band to be 14 and 10 respectively at 4<sup>o</sup>K. The other two effective masses pertinent to electrical

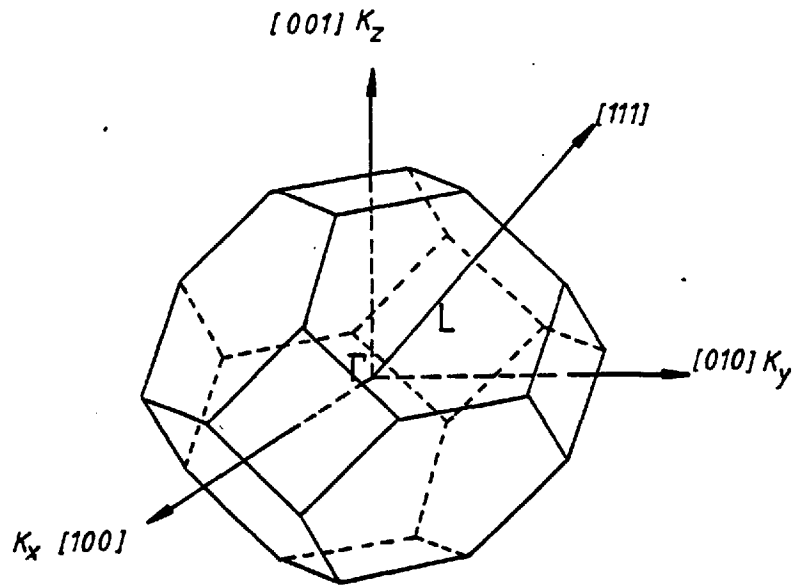


Fig.1.1 1<sup>st</sup> Brillouin zone of PbTe

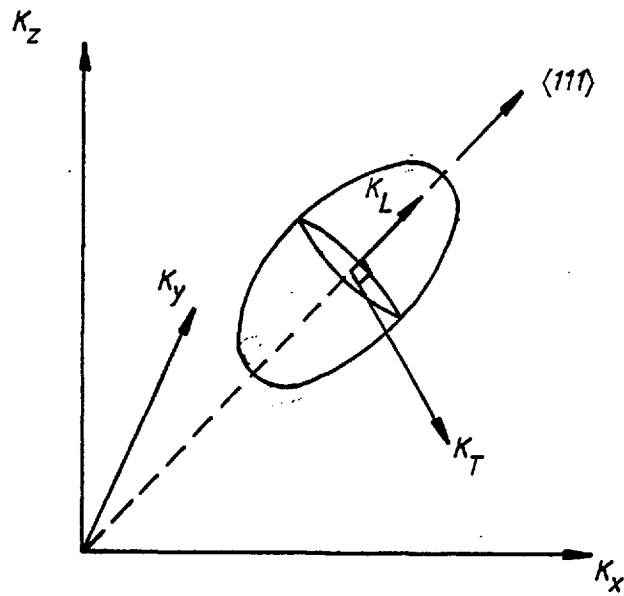


Fig.1.2 Constant energy surfaces

properties are the conductivity effective mass,  $m_c$ , which relates to transport properties and the density of states effective mass,  $m_d$ , which relates to the equilibrium statistics of the carriers. The averaged conductivity effective mass  $m_c$  is related to  $m_l$  and  $m_t$  as follows (D1)

$$m_c = \left( \frac{3m_l m_t}{2m_l + m_t} \right) \quad (1.4)$$

The density of states effective mass,  $m_d$ , can also be related to  $m_l$  and  $m_t$  (C2)

$$m_d = (m_l m_t^2)^{1/3} N_v^{2/3} \quad (1.5)$$

where  $N_v$  is the number of equivalent minima and in the case of the conduction band  $N_v = 4$ . Values of  $m_d$  and  $m_c$  for PbTe (carrier concentration  $10^{18} \text{ cm}^{-3}$ ) at room temperature given by Egerton (E1) are  $m_d = 0.24 m_0$  and  $m_c = 0.09 m_0$  for conduction band and  $m_d = 0.29 m_0$  and  $m_c = 0.11 m_0$  for valence band where  $m_0$  is the mass of free electron.

The band gap deduced from optical absorption experiments performed on epitaxial films of PbTe is 0.31 eV at  $300^\circ\text{K}$  (Z1). It has positive temperature coefficient,  $\frac{dE_g}{dT}$ .

$$E_g = E_{g_0} + \left( \frac{dE_g}{dT} \right) T \quad (1.6)$$

where  $E_{g_0}$  is the band gap at  $0^\circ\text{K}$  and  $\frac{dE_g}{dT} = (4.5 \pm 0.2) \times 10^{-4} \text{ eV K}^{-1}$  (P2) in the temperature range  $25^\circ\text{K} - 300^\circ\text{K}$ .

For narrow band gap semiconductor such as PbTe, non-parabolicity is characteristic and consequence of interband interactions (R3). Non-parabolicity of conduction band and valence band of PbTe has been investigated using two models, namely Kane's model and Cohen's model. Kane (K6) developed dispersion relations for non-parabolic isotropic bands of InSb. In the case of conduction band, he gives the following E vs K relationship

$$E(E + E_g) = E_g \left( \frac{\hbar^2 K^2}{2m_{de}} \right) \quad (1.7)$$

where  $E_g$  is the energy gap,  $\hbar = \frac{h}{2\pi}$ ,  $h$  being Plank's constant,  $m_{de}$  is density of states effective mass of electrons and  $K$  is the wave number. The density of states function for above dispersion equation is given by the following expression (R3)

$$g_c(E) = \frac{1}{2\pi^2} \left( \frac{2m_{de}}{\hbar^2} \right)^{3/2} E^{1/2} \left( 1 + \frac{E}{E_g} \right)^{1/2} \left( 1 + \frac{2E}{E_g} \right) \quad (1.8)$$

where energy zero has been taken at the bottom of the conduction band. By replacing  $E$  with  $(E_v - E)$ , a similar expression for valence band can be obtained. Cohen (C8) extended Kane's model to include non-ellipsoidal energy surfaces and non-parabolicity of the bands for Bi. The dispersion relation in this case becomes (R3),

$$E = \frac{\hbar^2 K_t^2}{2m_{te} \left\{ 1 + \frac{E}{E_g} + \frac{\hbar^2 K_l^2}{2m_{le}} \right\}} + \frac{\hbar^2 K_l^2}{2m_{le}} \quad (1.9)$$

where  $K_t$  and  $K_\ell$  are the transverse and longitudinal wave numbers,  $m_{te}$  and  $m_{\ell e}$  are the transverse and longitudinal principal valence band edge effective masses,  $m_{\ell e}$  is the longitudinal conduction band edge effective mass. Density of states function for conduction band is given by equation (1.10)

$$g_c(E) = \frac{1}{2\pi^2} \left( \frac{2m_{de}}{\hbar^2} \right)^{3/2} E^{1/2} \left\{ 1 + \frac{5E}{3E_g} \left( 1 + \frac{U}{5} \right) \right\} \quad (1.10)$$

where  $U = \frac{m_{\ell e}}{m_{\ell e}}$ . Band (B2) has shown that for lead salts, equations (1.10) and (1.8) may respectively be simplified to the following,

$$g_c(E) \approx \frac{1}{2\pi^2} \left( \frac{2m_{de}}{\hbar^2} \right)^{3/2} E^{1/2} \left( 1 + \frac{2E}{E_g} \right) \quad (1.11)$$

and

$$g_c(E) \approx \frac{1}{2\pi^2} \left( \frac{2m_{de}}{\hbar^2} \right)^{3/2} E^{1/2} \left( 1 + \frac{5E}{2E_g} \right) \quad (1.12)$$

Since expressions for  $g_c(E)$  for non-ellipsoidal energy surfaces and non-parabolic bands and isotropic non-parabolic bands are quite similar, equation (1.8) may be used without incurring a serious error. Equation (1.8) can also be written in reduced energy notation as follows

$$g_c(\epsilon) = \frac{1}{2\pi^2} \left( \frac{2m_{de}kT}{\hbar^2} \right)^{3/2} \epsilon^{1/2} \left( 1 + \frac{\epsilon}{\epsilon_g} \right)^{1/2} \left( 1 + \frac{2\epsilon}{\epsilon_g} \right) \quad (1.13)$$

and similarly for holes,

$$g_v(\epsilon) = \frac{1}{2\pi^2} \left( \frac{2m_d kT}{\hbar^2} \right)^{3/2} (\epsilon + a\epsilon)^{1/2} (1 + 2a\epsilon) \quad (1.14)$$

where

$$\epsilon = \frac{E}{kT}, \text{ non-parabolicity constant } a = \frac{kT}{E_g}, \epsilon_g = \frac{E_g}{kT},$$

$k$  is Boltzmann's constant and  $T$  is the temperature. Similar expressions for  $g_c(\epsilon)$  and  $g_v(\epsilon)$  are also given by Juhasz (J3) for spherical energy surfaces and non-parabolic bands.

Non-parabolicity of the conduction band of PbTe in the temperature range 77-300°K was investigated by Zhitinskaya et al (Z2) and Dubrovskaya and Ravich (D2) where these investigators measured the transport coefficients like the thermoelectric power,  $\alpha$ , the Hall coefficient  $R_H$ , electrical conductivity and Nernst-Ettingshausen coefficient as a function of temperature and magnetic field for n-type single crystal PbTe with carrier concentration in the range  $10^{18}$ - $10^{20}$   $\text{cm}^{-3}$ . Dubrovskaya and Ravich (D2) found that both models (Kane's model and Cohen's model) described the energy dependence of density of states for carrier concentration less than  $5 \times 10^{19}$   $\text{cm}^{-3}$  provided suitable values of  $m_d$  and  $E_g$  were chosen whereas Zhitinskaya et al (Z2) noted that the dependence of density of states effective mass on carrier density was described by Kane's model. Stavitskaya et al (S2) measured  $\alpha$ ,  $R_H$  and carrier mobility in the temperature range 100-1000°K for n-type PbTe with

carrier density in  $10^{18}$ - $10^{20}$   $\text{cm}^{-3}$  range and concluded that the experimental data were in good agreement with Kane's model and acoustic scattering.

Valence bands of PbTe have also been investigated in the temperature range 24-450<sup>o</sup>K (A1, K1, C3, D6) and like the conduction band, the principal valence band was also found to be non-parabolic. Existence of a second heavy mass valence band has been proposed by Allgaier (A1), Tauber et al (T2) and Chernik et al (C3) but location of the heavy mass valence band is unknown because this band is always unoccupied at very low temperatures (R3).

#### 1.4 ELECTRICAL PROPERTIES OF PbTe

##### 1.4.1 Single Crystals

Allgaier and Scanlon (A2) measured the mobility of electrons and holes of lead chalcogenides between 4.2<sup>o</sup>K and room temperature where the single crystals were grown by the Bridgman-Stockbargar technique. Some of the earlier work done on the Hall measurements of synthetic crystals of lead chalcogenides is also referenced by Allgaier and Scanlon. In Fig. 1.3, Fig. 1.4 and Fig. 1.5, variation of the Hall coefficient, and the Hall mobility between 4.2<sup>o</sup>K and 295<sup>o</sup>K for PbTe is shown where the data are taken from Allgaier and Scanlon. Carrier concentration at room temperature ranged from  $10^{17}$ - $10^{18}$   $\text{cm}^{-3}$  and resistivity of the samples ranged from 3 m $\Omega$  cm to 24.4 m $\Omega$  cm. The Hall coefficient varied by 10-20% over the entire temperature range. Temperature dependence of the Hall mobility was

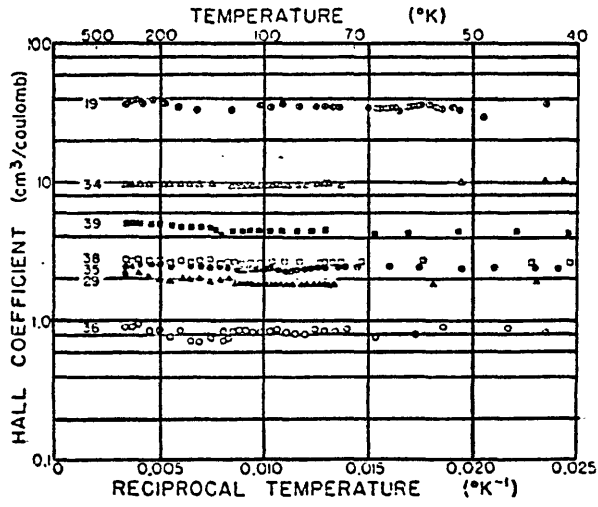


Fig.1.3  $R_H$  versus Temperature

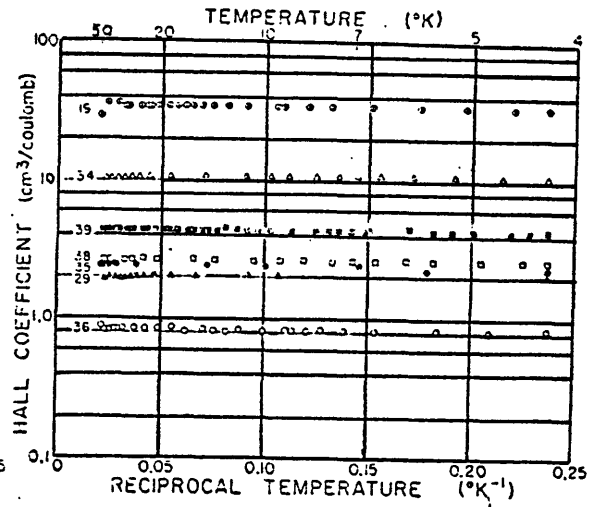


Fig.1.4  $R_H$  versus Temperature

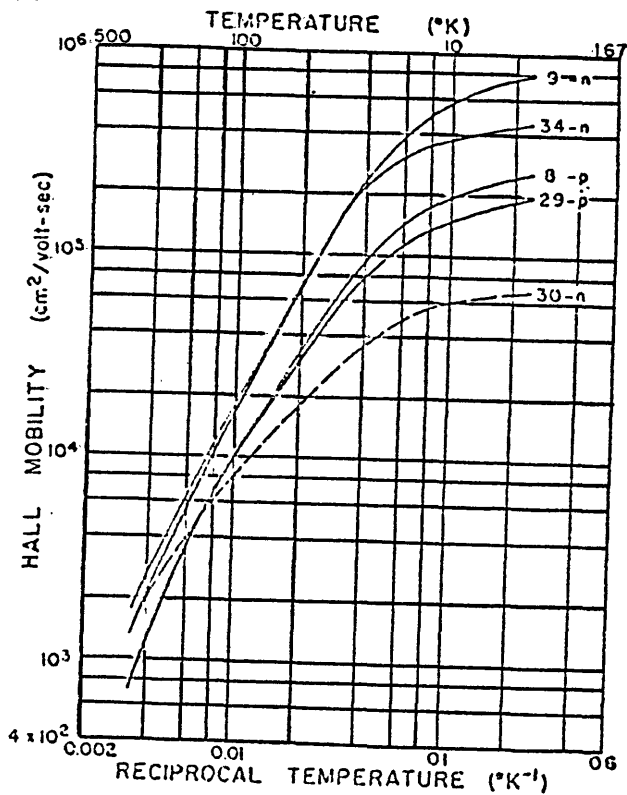


Fig.1.5  $\mu_H$  versus Temperature

Key

- n-type natural PbS
- n-type PbS
- ◐ p-type PbS
- ◑ n-type PbSe
- ◒ p-type PbSe
- ◓ n-type PbTe
- ◔ p-type PbTe

[Data from Allgaier and Scanlon (A2)]



described by a power law,

$$\mu_H \propto T^{-s} \quad (1.15)$$

where the averaged value of  $s$  between  $100^\circ\text{K}$ - $295^\circ\text{K}$  was in the range 2.2-2.4. Low temperature mobilities at  $4.2^\circ\text{K}$  were sometimes as high as  $8 \times 10^5 \text{ cm}^2/\text{vs}$ , where the unimportance of ionised impurity scattering was attributed to high static dielectric constant. (Kanai and Shohno (K2) who measured the capacitance of junction diodes of PbTe suggested a value of static dielectric constant of  $\sim 420$  at  $77^\circ\text{K}$ .) Furthermore, temperature dependence of  $\mu_H$  was the same for n-type and p-type single crystals. Putley (P1) when reviewing the transport properties of lead chalcogenides found, (i) complete absence of discrete impurity levels and (ii) no evidence for ionised impurity scattering even in very impure material at  $4^\circ\text{K}$ .

An explanation of temperature dependence of mobility was put forward by Allgaier and Houston (A3) where they proposed that the combined effect of one phonon acoustic scattering and a temperature dependent carrier effective mass was responsible for the power law. For classical statistics (D1),

$$\mu \propto m^{-5/2} T^{-3/2} \quad (1.16)$$

Therefore,  $m \propto T^{0.4}$  for pure samples to give  $\mu \propto T^{-2.5}$ .

#### 1.4.2 Thin Films

Electrical properties of epitaxial thin films of lead chalcogenides grown on alkali halides were reviewed by Zemel (Z3). However, glass and mica were also used as substrates during some of the earlier investigations of photoconductivity and electrical properties of lead telluride (S3, M1). Fig. 1.6 and Fig. 1.7 show the temperature dependence of the Hall coefficient and mobility for PbTe films. Two points are worth noting.

- (i) High mobilities are maintained even at liquid nitrogen temperatures.
- (ii) Around room temperature, the power law  $\mu \propto T^{-s}$  is obeyed where  $s \sim 2.5$ .

Both of these features are in common with bulk single crystals.

Using mobility as a criterion of film quality, quality of thin film materials is usually much inferior to that of equivalent bulk material especially when the films are grown in a conventional vacuum system (open source, pressure  $\sim 10^{-6}$  torr). However, one of the techniques which has contributed significantly to the preparation of thin films with bulk-like properties is the hot wall technique (HWT). A recent review of HWT is given by Lopez-Otero (L1) where he defines HWT as the technique of vacuum film deposition, the main characteristic being the growth of epitaxial layers under conditions as near

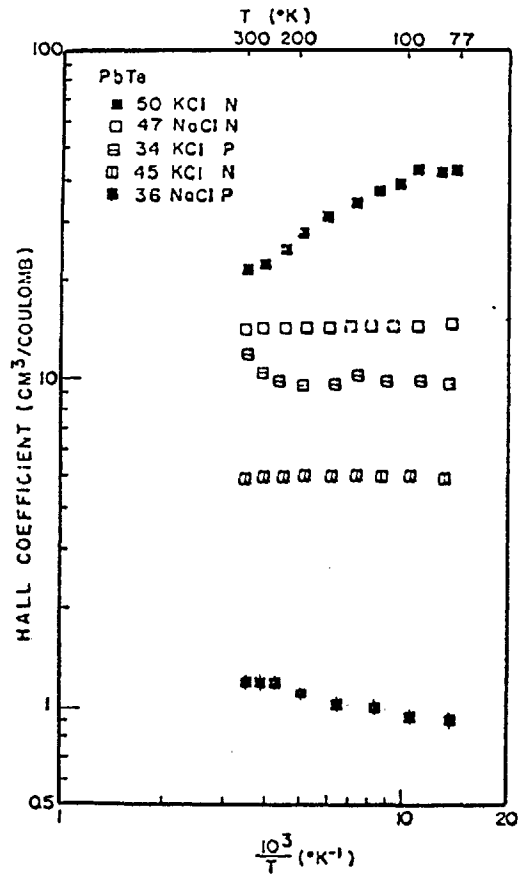


Fig.1.6  $R_H$  versus Temperature (Z1)

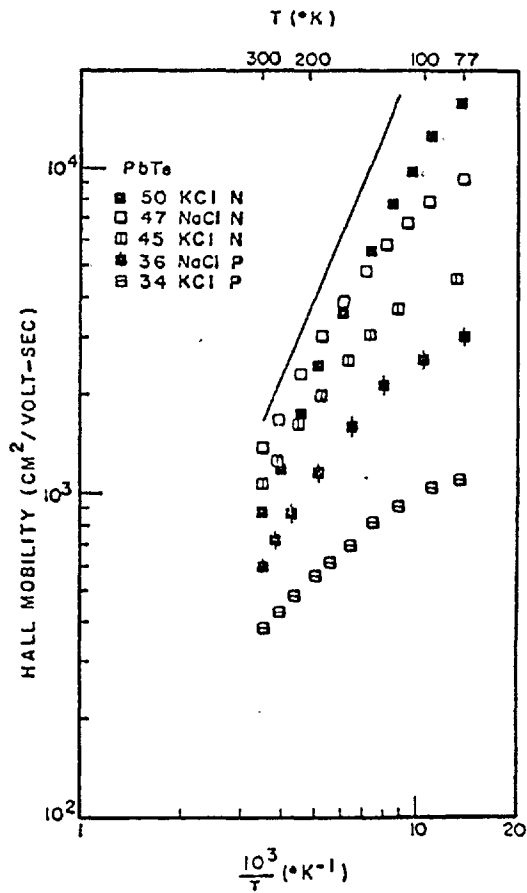


Fig.1.7  $\mu_H$  versus Temperature (Z1)

as possible to thermodynamic equilibrium. The salient feature of HWT is the use of a hot wall which both encloses and directs the vapour from source to substrate. This also avoids the loss of evaporating material and reduces the difference between substrate and source temperatures to a minimum. In order to illustrate the effectiveness of HWT to produce films with bulk-like properties, in Fig. 1.8 the Hall mobility versus temperature is plotted for PbTe films grown by conventional vacuum system (Egerton (E1)) and HWT (Lopez-Otero (L2) and Dhere (D3)). Also shown on the graph is the plot  $\mu_H$  vs T for n-type single crystals from Allgaier and Scanlon (A2). Even though Egerton's films were thin ( $\sim 3000\text{\AA}$ ) and grown on mica and films grown by Lopez-Otero and Dhere were thicker and grown on alkali halides, it is clear from Fig. 1.8 that films produced using HWT have essentially bulk-like mobilities. Another advantage of HWT is that it affords control over the carrier concentration which is not possible with a conventional vacuum system.

### 1.5 GASEOUS AMBIENT EFFECTS

Most of the early work regarding the effect of gases on the electrical properties of lead chalcogenides was concerned with the problem of photoconductivity. For instance, the effect of oxygen on polycrystalline films of PbTe and PbSe grown on glass substrate was investigated by Bode and Levinstein (B1), Jones (J1) and Yasuoka (Y1).

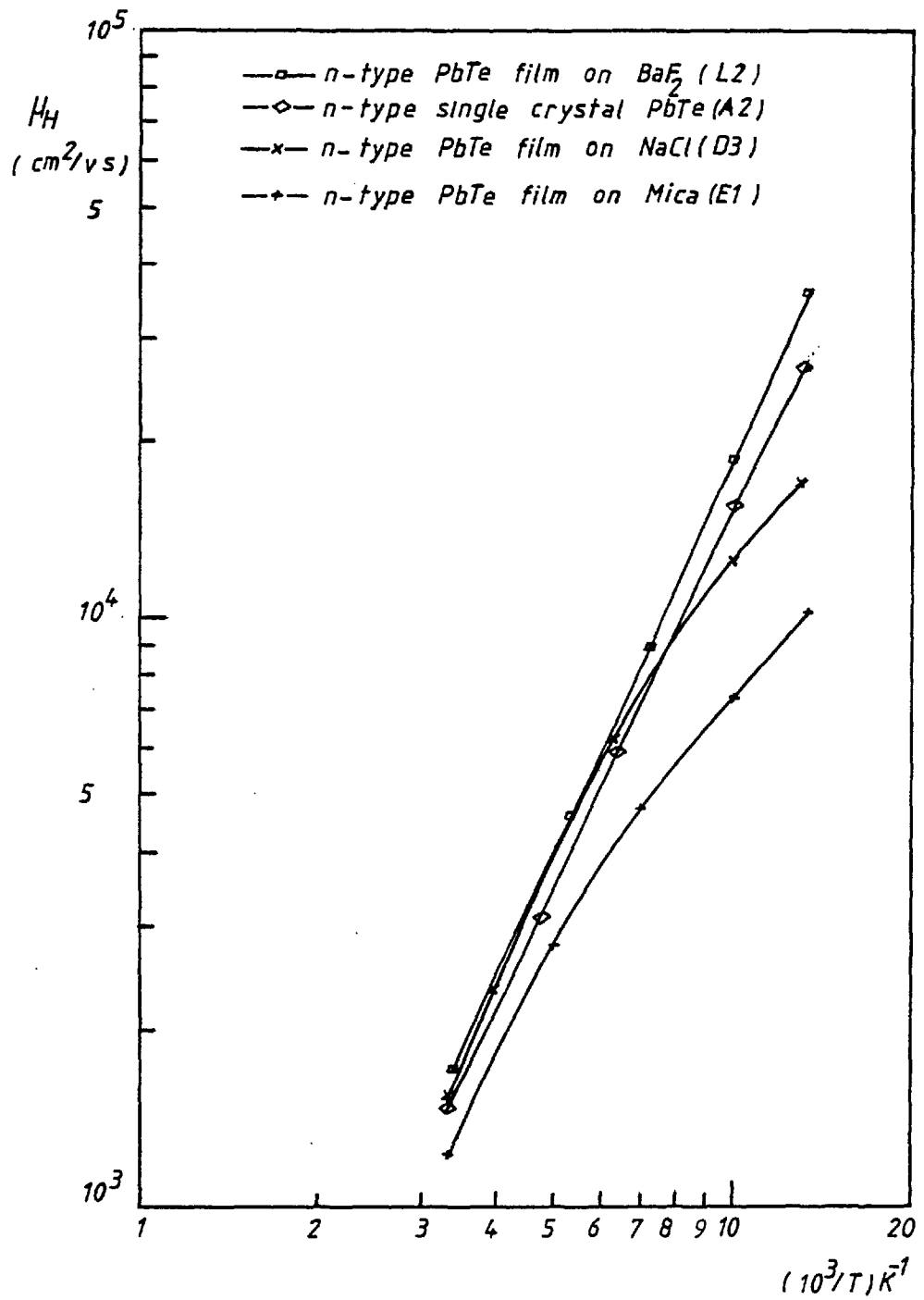


Fig.1.8  $\mu_H$  versus Temperature

These workers noted that oxygenated films became photoconductive.

Interaction of  $O_2$  with epitaxial PbSe films grown on NaCl substrate was first investigated by Brodsky and Zemel (B3). The effect of oxygen on epitaxial thin films of lead telluride grown on mica was investigated by Egerton and Juhasz (E2). Later on, Zemel and co-workers (M2, Y2) used alkali halides as substrates for their epitaxial thin films of lead selenide and gaseous ambient experiments. Interaction of oxygen and atomic hydrogen with  $Pb_{1-x}Sn_xTe$  alloy has also been investigated (B2,H1). A review of gas effects of lead chalcogenides films is given by Zemel (Z4).

Closely allied to the gaseous ambient effects has been the development of hydrogen sensitive MOS, field effect transistor by Lundström et al (L3,L4). They used a thin film of palladium Pd as the gate electrode on an n-channel MOST. With this structure, they were able to detect with ease 40 ppm hydrogen gas in air. Shivaraman (S4) used a similar structure to detect  $H_2S$ . In such a structure, Pd-gate acts as a catalyst for the dissociation of  $H_2$  or  $H_2S$  and atomic hydrogen thus produced is partially dissolved in Pd and partially adsorbed onto the Pd-SiO<sub>2</sub> interface. This gives rise to changes in the work function difference between the metal and the semiconductor which is equal to a change in threshold voltage of the transistor (S4). Steele and MacIver (S5) used the observation that the height of a Schottky barrier produced at metal and cadmium sulphide, CdS contact was strongly dependent on the metal

work function, to fabricate a hydrogen detector. They evaporated Pd dots ( $800\text{\AA}$  in thickness) onto indium doped single crystal of CdS and measured the dark I-V characteristics of Pd-CdS diodes when exposed to a gas mixture containing hydrogen. In a recent review, Zemel (Z5) has discussed further the possibilities of chemically sensitive semiconductor devices.

#### 1.6 AIM OF PRESENT STUDY AND LAYOUT OF THE THESIS

The aim of the present investigation of interaction of atomic hydrogen and oxygen with epitaxial thin films of PbTe is to gain a clearer insight into the mechanisms of gas uptake. Layout of the thesis is as follows.

In chapter 2, description of the vacuum system used to prepare thin films of PbTe will be given. Results of x-ray diffraction and transmission electron microscopy studies will also be presented. Chapter 3 deals with the Hall measurements and the discussion of temperature dependence of the Hall mobility.

Chapters 4 and 5 are the major chapters of the thesis and these deal with the gaseous ambient experiments. Results are discussed in terms of two theoretical models - surface adsorption model and the diffusion model. Critical examination and extension of these models will be presented in chapter 4. Results of kinetic studies will be presented and discussed in chapter 5. In chapter 6, main conclusions reached during the present study will be given together with some suggestions for future work.

CHAPTER 2FILM PREPARATION2.1 INTRODUCTION

A single source evaporation technique was used to produce thin films of lead telluride <sup>(E1,B2,H1).</sup> Details of the vacuum system employed to produce these films will be described in this chapter. Results of x-ray diffraction and electron microscopy studies will also be presented.

2.2 VACUUM SYSTEM

A glass chamber (12" in diameter, 12" in height) was evacuated by a water-cooled oil diffusion pump. The diffusion pump (6" in diameter and filled with silicone MS 704 oil) was backed by a mechanical rotary pump. A liquid nitrogen trap was inserted in between the diffusion pump and the high vacuum valve (baffle valve) to prevent back streaming of the diffusion pump oil and to reduce the partial pressure of condensable gases. The top end of the glass chamber was sealed by a Viton gasket with a top plate. Similarly, a base plate sealed the lower end of the chamber. Electrical leadthroughs were passed through both plates for supplying current to various heaters. A schematic diagram of the evaporation chamber is shown in Fig. 2.1.



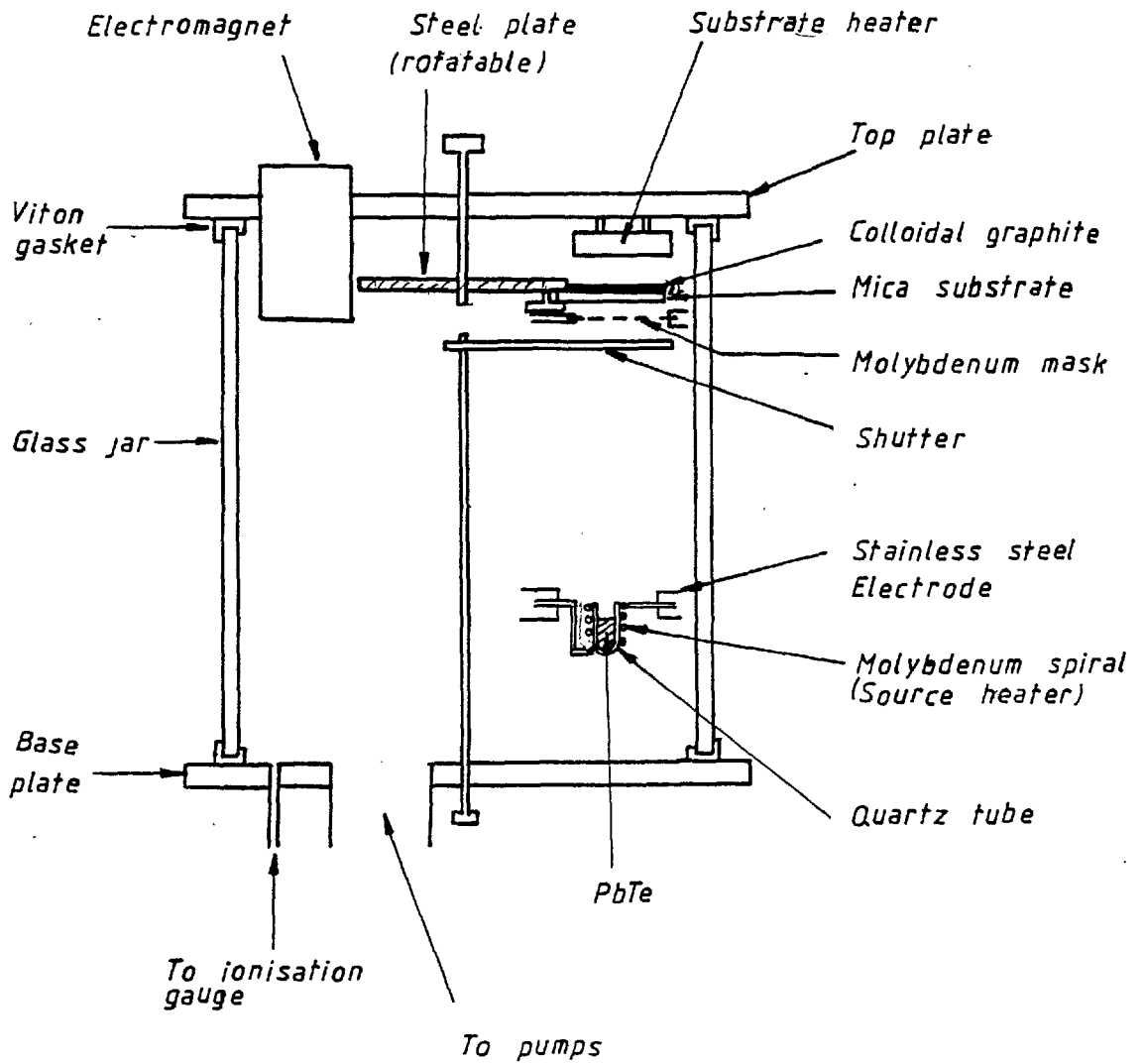
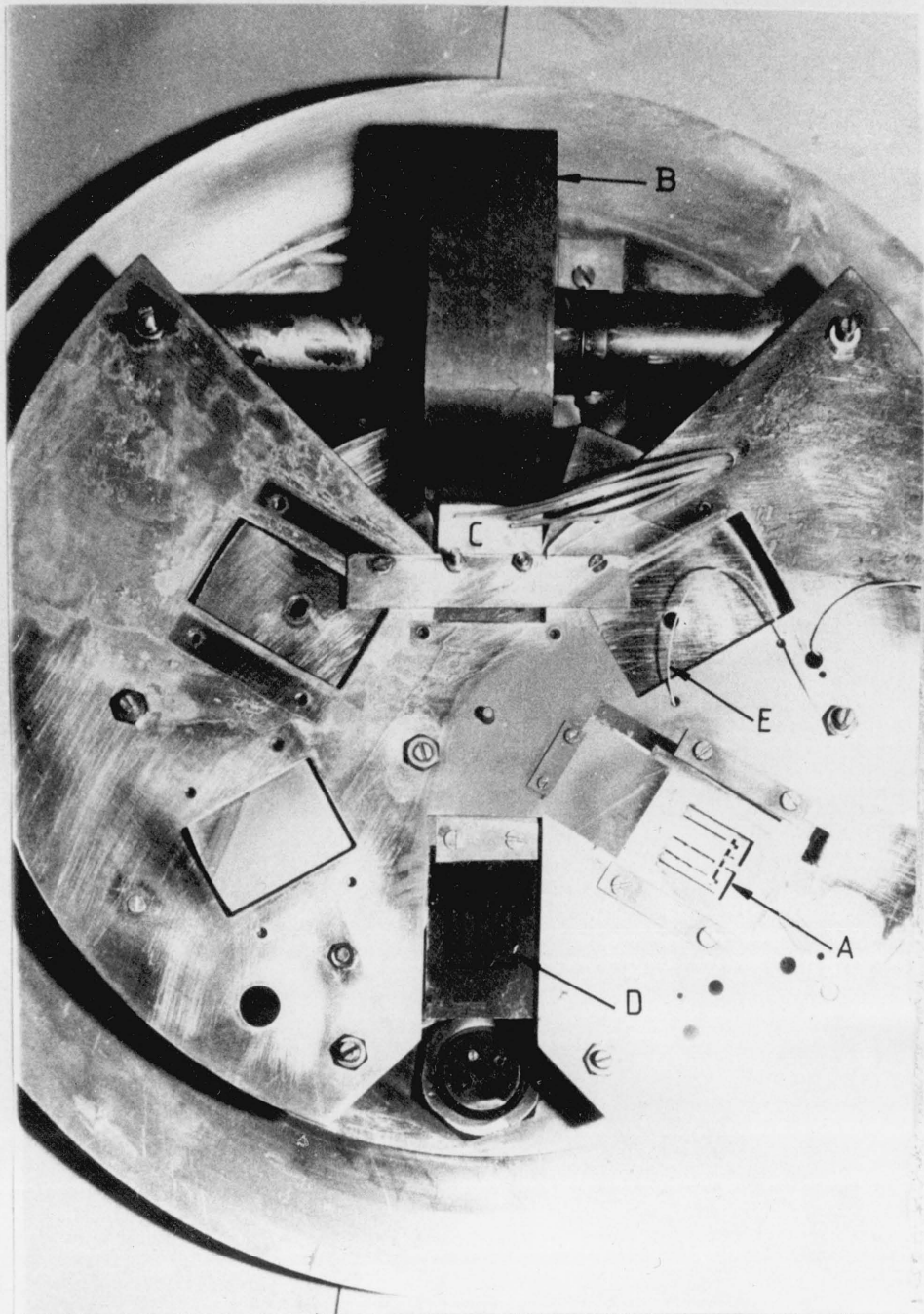


Fig. 2.1 Evaporation Chamber (Schematic)

The top plate consisted of two stainless steel plates where one of the plates could be rotated. A molybdenum mask<sup>was</sup> used to evaporate the films in standard Hall shape and the pressure contacts were mounted on the fixed plate whereas the substrate was mounted on the rotatable plate. The electromagnet and the substrate heater were fixed to the top plate. Fig. 2.2 shows the top plate assembly. The substrate heater consisted of a 5 thou. molybdenum wire threaded through alumina tubes to ensure uniform heating. A double radiation shield of molybdenum sheet was used to prevent upward radiation. The substrate heater was clamped to the top plate so that it was 1 cm above the substrate. The evaporation mask was clamped 5 mm below the substrate. Once the film was deposited, it was allowed to cool down to room temperature and then the film was rotated so that it was situated in between the poles of the electromagnet where pressure contacts to the film were made. In this way, it was possible to carry out the Hall measurements without breaking the vacuum seal.

The source material was contained in a small quartz tube sealed at one end. The tube was 3 cm in length and its outside diameter was 6 mm. It was heated by passing current through a molybdenum wire wound in a spiral around the entire length of the tube. The distance from top of the source assembly to substrate was about 12 cm. Typically, 10-11 amps were passed through the source heater to deposit the film.



Key

- A Film Mask
- B Electromagnet
- C Pressure Contacts
- D PbTe Film
- E Thermocouple

Fig. 2.2 Top Plate Assembly

To atomise hydrogen for gaseous ambient experiments (chapters 4 and 5), a tungsten filament (8 thou. in diameter) was also incorporated into the vacuum chamber - where the stainless steel electrodes for this heater and the source heater were passed through the base plate. Flexible stainless steel tubing was used to conduct hydrogen gas into the vacuum system where its flow was controlled by a needle leak valve. A separate needle leak valve was used to control the flow of air into the system. Pressure inside the vacuum chamber was measured by a Mullard 10G12 ion gauge.

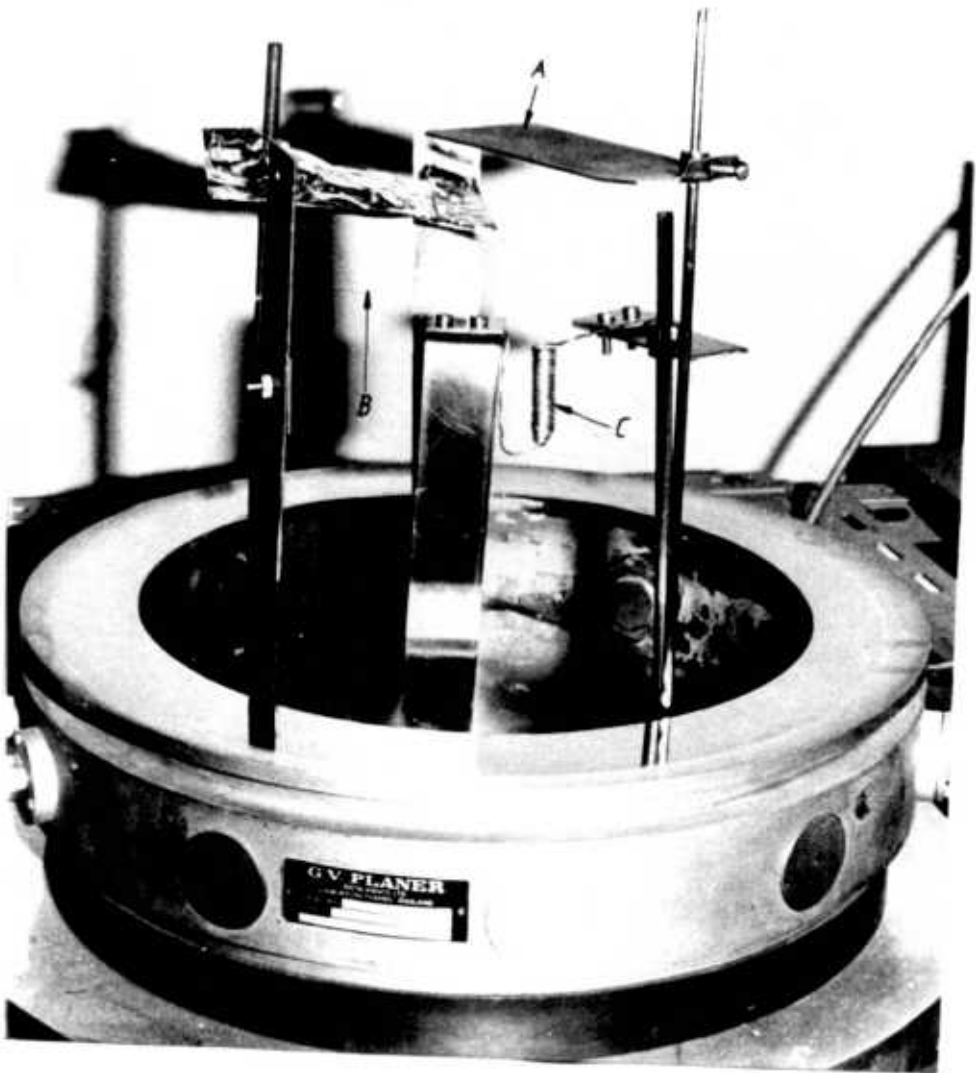
### 2.3 EVAPORATION PROCEDURE

Prior to each evaporation, the source tube was etched in concentrated  $\text{HNO}_3$  for about one hour and then thoroughly rinsed with distilled water. If the remains of the previous evaporation still persisted, the tube was heated in vacuum until all such remains sublimed. A fresh change of about 400 mgm of crushed source material was placed in the quartz tube. The source material was p-type<sup>†</sup> single crystal  $\text{PbTe}^*$ . Mass spectrometric analysis (excluding Be, Li, He, D, H) carried out by Analytical Services Laboratory of Imperial College showed that the following impurities were present.

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\*The author is indebted to Dr. Mino Green for supplying the source material.

†  $\rho = 6 \text{ m}\Omega\text{.cm}$ , Seebeck coefficient at room temp. =  $286 \mu\text{V}^\circ\text{C}^{-1}$ .



*Key*

- C*      *Source Heater*
- B*      *Filament For Atomizing Hydrogen*
- A*      *Shutter*

Fig. 2.3

Element	Quantity (ppm wt. for wt.)
Au, K, C, Si, Na	< 1
Fe	1.1
Ca	1.6

Muscovite mica was used as substrate for most of the films because it was a large area single crystal substrate, atomically flat, electrically insulating and chemically inert (G1). Furthermore, it was readily available. One face of mica substrate was coated with colloidal graphite to maximise the absorption of radiation from the substrate heater (B2, P3). The substrate (1½" x 1) was then cleaved to about 2 thou. thickness and mounted in the top plate with the freshly cleaved face facing the source heater. The glass chamber was evacuated and when the system was left pumping over night, the pressure inside the chamber was  $\sim 1 \times 10^{-6}$  torr. The substrate heater was switched on to heat the substrate up to 275°C for one hour before cooling it down to the temperature of film deposition. When the substrate temperature had stabilised, liquid nitrogen was poured into the trap and the system was left pumping for a further 90 minutes. Leaving air-cleaved mica at 200°C in vacuum of  $\sim 2 \times 10^{-6}$  torr has been suggested by Ota (O1) as an effective method of cleaning the substrate.

In a separate experiment, the substrate heater was calibrated by embedding an iron-constantan thermocouple in colloidal graphite on the front face (i.e. on the face where PbTe film was to be deposited) of mica. The calibration curve shown in Fig. 2.4 was used to determine the substrate temperature. The films were deposited in the temperature range 150-250°C. When a working pressure of  $\sim 1 \times 10^{-6}$  torr was reached, the source heater was switched on making sure that the shutter was covering the substrate. The source tube heated up slowly to typically 700°C and more volatile impurities were sublimed for about 1 minute while the shutter was still masking the substrate. The shutter was then removed and the film was deposited. A typical evaporation run lasted for 15 minutes. The ionisation gauge was kept 'off' during the evaporation run and used sparingly throughout the pump down to prevent production of unwanted atomic hydrogen (see chapter 4). Periodically, all nuts, screws and electrodes inside the vacuum chamber were scrubbed clean, washed in distilled water, washed in dilute HNO<sub>3</sub> and finally rinsed in distilled water.

#### 2.4 FILM THICKNESS MEASUREMENT

The thickness of the film was measured by multiple beam interference method (B12). A sodium lamp was used as a source of monochromatic light ( $\lambda/2 = 2946\overset{\circ}{\text{A}}$ ). A thin film of Al or Ag was evaporated onto PbTe film at room temperature (in a different vacuum system) to obtain a

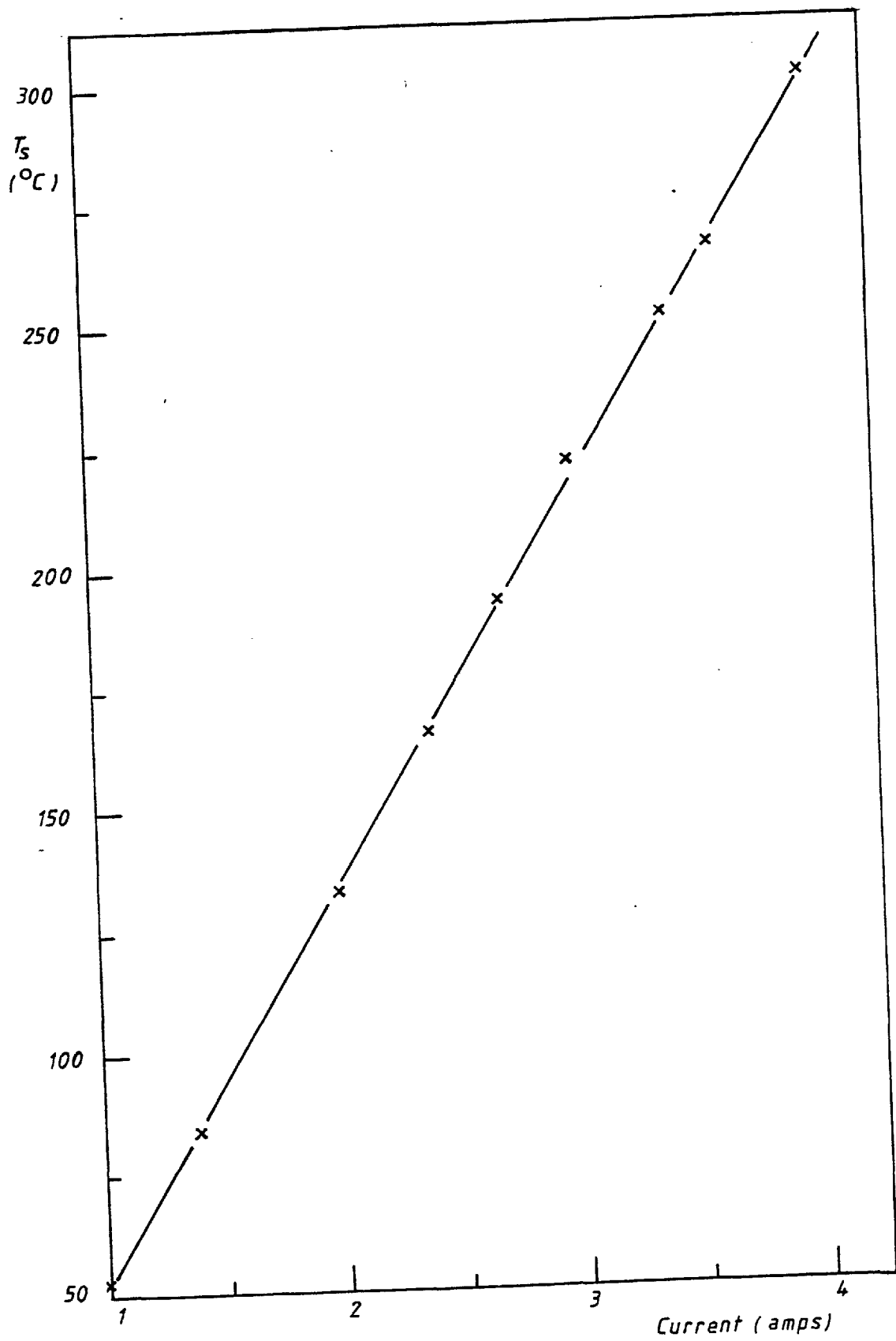


Fig. 2.4 Substrate heater calibration



highly reflective surface. The film surface was pressed against the Fizean plate and by adjusting the contact between the plate and film, interference fringes were produced at right angles to the step. By measuring the fringe spacing,  $s$  and the fringe offset,  $d$ , the thickness of the film can be calculated as follows (B12),

$$t = \frac{\lambda}{2} \frac{d}{s} \quad (2.1)$$

where  $t$  is the thickness of the film. Values of  $d$  and  $s$  for several fringes were usually recorded and an average value of  $t$  was obtained.\* The value of  $t$  ranged from 2000-4000Å for films used in the Hall measurements and the gaseous ambient experiments.

## 2.5 X-RAY DIFFRACTION

Two different x-ray diffraction techniques were used to investigate the source material and the thin films grown from it. Using the Debye-Scherrer powder method (C4), the source material was examined and the cylindrical texture camera (W1) was used to examine the thin films. In both cases, Ni-filtered  $\text{CuK}\alpha$  radiation was used. Fig. 2.6 shows the photograph of x-ray diffraction pattern of the source material using the Debye-Scherrer method. Following the method of Azaroff and Buerger (A4), interplanar spacings were determined and the lines were indexed. Similarly, the

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\* to an accuracy of  $\pm 200\text{Å}$

method described by Wallace and Ward (W1) was used to determine the interplanar distances in the case of the x-ray diffraction pattern of the thin film of PbTe grown on a microscope glass slide at 200°C. The indexed pattern is shown in Fig. 2.7. The interplanar spacings determined by the Debye-Scherrer powder method and the cylindrical texture camera agreed closely with those given by A.S.T.M. Using the method of least squares (C4), the corrected value of the lattice constant,  $a_0$  was determined for the source material. This value was 6.54Å (2 dec. places) compared with 6.50Å given by Ravich et al (R1) and 6.46Å given by Scanlon (S1).

## 2.6 TRANSMISSION ELECTRON MICROSCOPY

The films were grown on air-cleaved muscovite mica to an expected thickness of 600Å. Layer of colloidal graphite was floated off by immersing the film gently in distilled water. Several methods were tried to detach the film from mica. When the film was immersed in HNO<sub>3</sub>, it dissolved either much too quickly or much too slowly depending on the concentration of the acid. Exposure to HF vapour failed to detach the film from mica substrate as well, whereas Band (B2) used this method successively for his films of Pb<sub>x</sub>Sn<sub>1-x</sub>Te grown on mica. Stripping the film off mica using sellotape was also tried, but invariably a thin layer of mica was also peeled off with the film. Diluted HF was used to remove the film from the mica. HF was

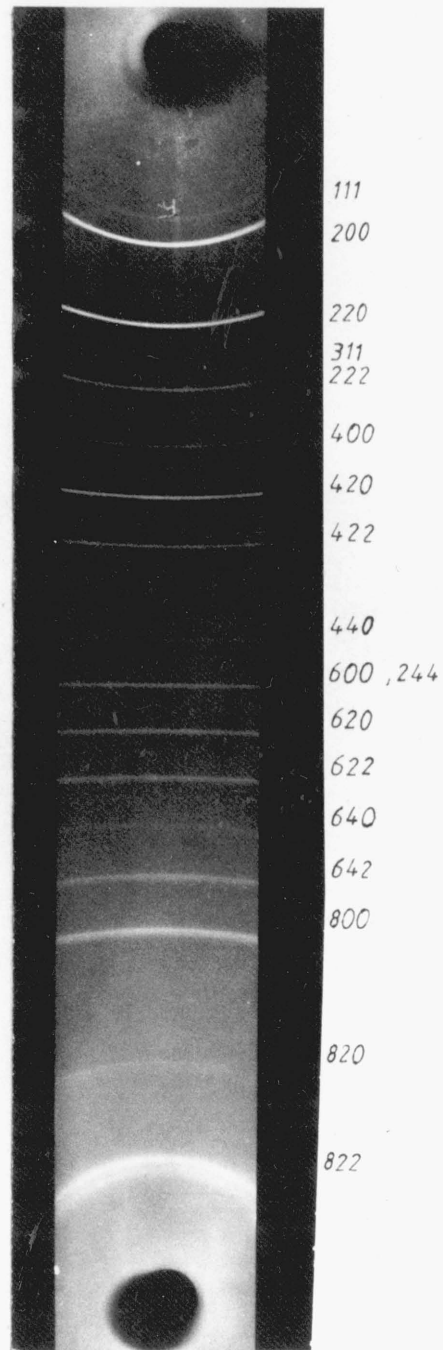


Fig. 2.6 Xray Diffraction Pattern, PbTe (Source Material)

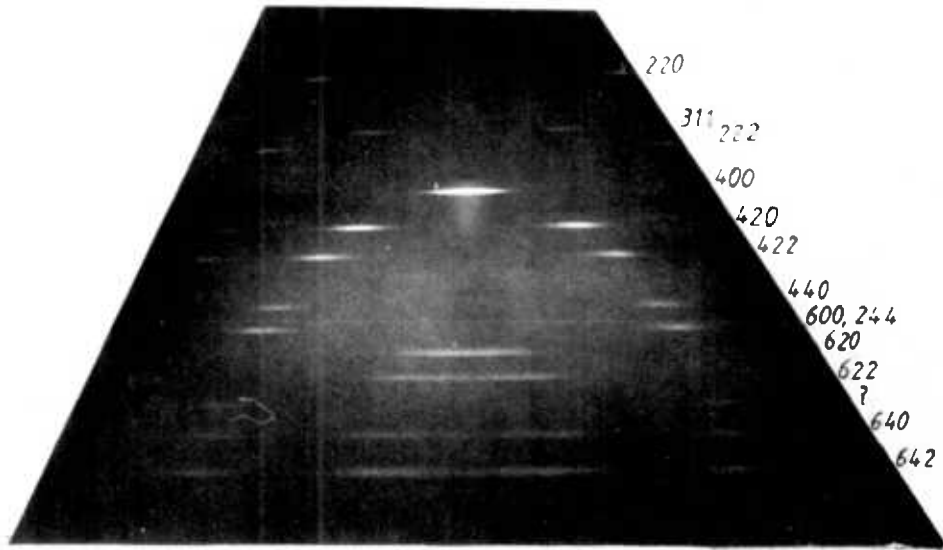


Fig. 27 X-ray Diffraction Pattern  
PbTe Thin Film On Glass Substrate

diluted to 40% by volume with distilled water. The film was first immersed in HF acid for about 20 minutes and then vigorously shaken in a bath of distilled water. Consequently, the film floated off the mica. Copper grids were used to mount the films and the films were then examined using JEM 100B, a 100 kV transmission electron microscope.

Shown in Fig. 2.8 and Fig. 2.9 are the micrographs considered to be representative of this study. These micrographs illustrate some of the common features of structure of a continuous film of PbTe on mica. Fig. 2.8 shows the selected area diffraction pattern and Fig. 2.9 shows the microstructure of a film grown on mica at 225°C. The spot pattern has a six-fold symmetry showing that the deposited material has (111) planes parallel to the substrate surface (E3). In a discontinuous film, triangular nuclei (equilateral) in two orientations are randomly distributed (G1). Coalescence of oppositely oriented triangular nuclei gives rise to double positioning boundaries where the latter become rounded and move out of the (11 $\bar{2}$ ) planes during the film growth (S6). Therefore, a continuous film has a maze-like structure where the like oriented nuclei are bounded in a domain. As the substrate temperature was raised, the domains became larger and the triangular nuclei also grew in size as previously reported (P3, P4).

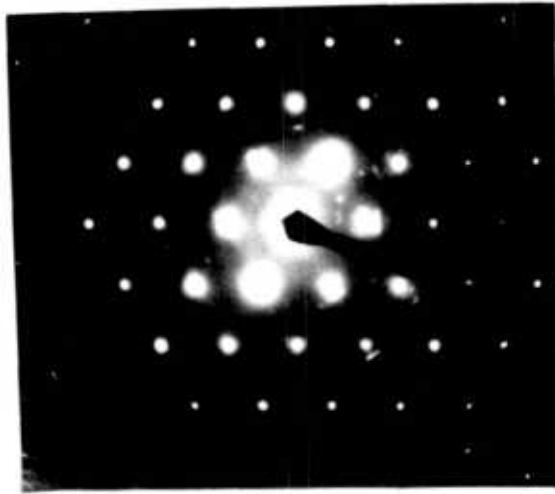
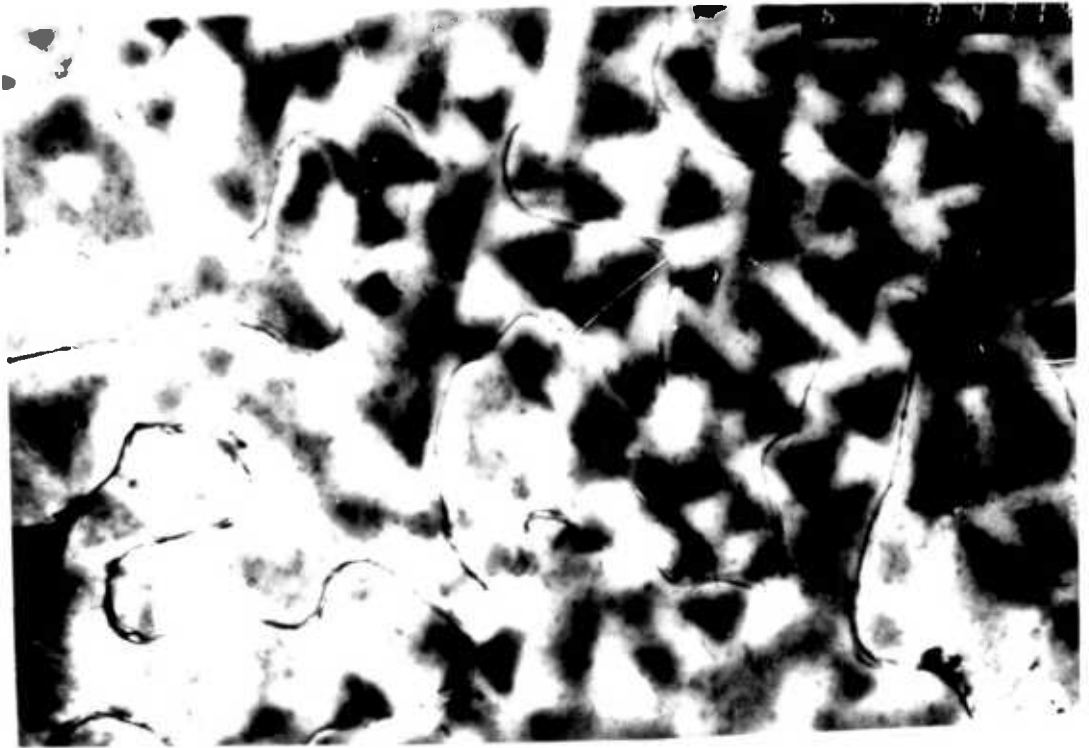


Fig. 2.8 Selected Area Pattern



100 $\mu$ m

Fig.2.9 Microstructure Of PbTe On Mica.

## CHAPTER 3

### HALL EFFECT MEASUREMENTS

#### 3.1 INTRODUCTION

In this chapter, the Hall effect measurements carried out under two different situations are described. In one case, the Hall measurements as a function of temperature were performed for air exposed films. In the second case in situ Hall effect measurements (without breaking the vacuum seal) were carried out at a constant temperature (usually room temperature) as the films were exposed to atomic hydrogen and oxygen. Discussion of results pertaining to the first case will be presented in this chapter, whereas the results for the second case will be discussed in chapters 4 and 5.

#### 3.2 SIMPLE THEORY OF THE HALL EFFECT

Suppose in a p-type semiconductor, current density  $J_x$  is produced by the application of an electric field  $E_x$  in x-direction and a magnetic field of flux density,  $B_z$  is applied in the z-direction. The magnitude of the Lorentz force experienced by holes will be (A5),

$$F_L = ev_{Dx}B_z \quad (3.1)$$

where  $v_{Dx}$  is the average drift velocity. This will create an excess of holes at one face of the semiconductor

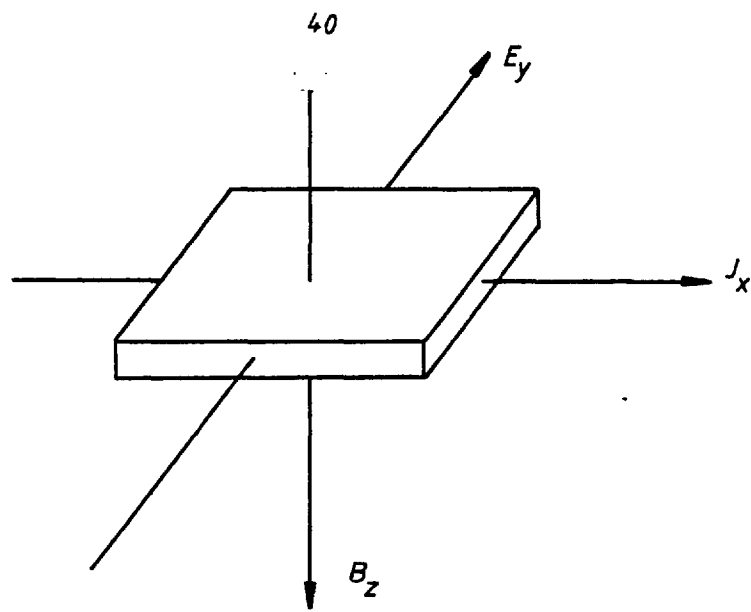


Fig 3.1 The Hall Effect

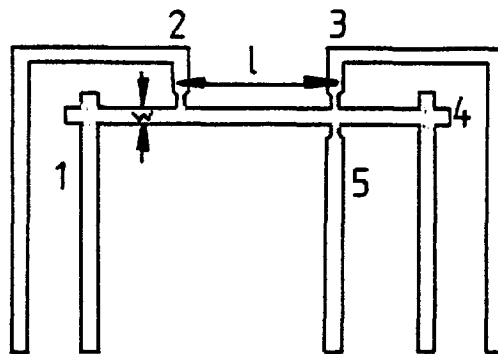


Fig 3.2 Film Mask



and a deficiency of holes at the opposite face giving rise to a transverse electric field,  $E_y$ . In equilibrium, force produced by  $E_y$  on holes will balance the Lorentz force.

$$eE_y = ev_{Dx} B_z \quad (3.2)$$

or

$$\frac{E_y}{B_z J_x} = \frac{1}{pe} \quad (3.3)$$

where  $J_x = ev_{Dx} p$  and the Hall coefficient  $R_H$  is defined by (A5),

$$R_H = \frac{E_y}{B_z J_x} \quad (3.4)$$

When in a semiconductor conduction is due to both electrons and holes,  $R_H$  is generally given by (P5),

$$R_H = \frac{R_e \sigma_e^2 + R_h \sigma_h^2 + B^2 R_e R_h \sigma_e^2 \sigma_h^2 (R_e + R_h)}{(\sigma_e + \sigma_h)^2 + B^2 \sigma_e^2 \sigma_h^2 (R_e + R_h)^2} \quad (3.5)$$

where  $R_e$ ,  $\sigma_e$ ,  $R_h$  and  $\sigma_h$  are the Hall coefficient and conductivity of electrons and holes respectively. In the case of low magnetic fields ( $\mu B \ll 1$ ), equation (3.5) simplifies to the following,

$$R_H = \frac{R_e \sigma_e^2 + R_h \sigma_h^2}{(\sigma_e + \sigma_h)^2} \quad (3.6)$$

Equation (3.6) may also be written in terms of  $\mu_e$  and  $\mu_h$ , the mobilities of electrons and holes respectively.

$$R_H = \frac{A_\tau A_K}{e} \left[ \frac{p\mu_h^2 - n\mu_e^2}{(p\mu_h + n\mu_e)^2} \right] \quad (3.7)$$

where  $p$  and  $n$  are the hole and the electron concentrations respectively and  $e$  is the electronic charge.  $A_K$  is a numerical factor related to the band structure of the semiconductor. For ellipsoidal constant energy surfaces,  $A_K$  is given by the following equation (R1, S7),

$$A_K = \frac{3K(K+2)}{(2K+1)^2} \quad (3.8)$$

where  $K = m_l/m_t$  is the mass anisotropy ratio (see chapter 1). For conduction band of PbTe, Cuff et al (C1) give  $K = 10$  at  $4^\circ\text{K}$ . From equation (3.8),  $A_K \approx 0.82$  for  $K = 10$ .

$A_\tau$  is a statistical factor and is related to the relaxation time as follows (S7),

$$A_\tau = \frac{\langle \tau^2 \rangle}{\langle \tau \rangle^2} \quad (3.9)$$

where  $\langle \tau \rangle$  is the relaxation time averaged over energy and is given by (R1, A7),

$$\langle \tau^\gamma \rangle = \frac{\int_0^\infty \tau^\gamma \frac{\partial f}{\partial \epsilon} \epsilon^{3/2} d\epsilon}{\int_0^\infty \epsilon^{3/2} \frac{\partial f}{\partial \epsilon} d\epsilon} \quad (3.10)$$

where  $f = 1 / (1 + \exp(\epsilon - \epsilon_F))$ , is the Fermi-Dirac function,  $\epsilon = E/kT$  and  $\epsilon_F = E_F/kT$ ,  $k$  being Boltzmann's constant.

In the case of classical statistics, from equations (3.9) and (3.10) one obtains,

$$A_\tau = \frac{\Gamma(2r + 5/2) \Gamma(5/2)}{\Gamma^2(r + 5/2)} \quad (3.11)$$

where  $\Gamma(x)$  is the gamma function defined by (S10),

$$\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt \quad (3.12)$$

The parameter  $r$  in equation (3.11) depends on the scattering mechanism and represents the energy dependence of the relaxation time. In the case of acoustical phonon scattering  $r = -1/2$  (S7) and from equation (3.11),  $A_\tau = \frac{3\pi}{8}$ . For a degenerate semiconductor  $A_\tau = 1$  (R1). A detailed discussion of scattering mechanisms for non-parabolic energy bands and arbitrary magnetic fields and degeneracy has been given by Harman et al (H8) and Ravich et al (R4).

When  $p \gg n$ , equation (3.7) simplifies further to the following,

$$R_H = \frac{A_\tau A_K}{ep} \quad (3.13)$$

$$\text{Similarly, for } n \gg p, \quad R_H = - \frac{A_K A_\tau}{en} \quad (3.14)$$

Under these conditions, corresponding expressions for conductivity become,

$$\sigma_h = ep\mu_h \quad (3.15)$$

and

$$\sigma_e = ne\mu_e \quad (3.16)$$

The Hall mobility  $\mu_H$  is given by  $|R_H|\sigma$ . In the present calculations  $A_K A_T$  has been assumed to be unity. This gives,

$$\mu_H = \mu_e \quad \text{for } n \gg p \quad (3.17)$$

and

$$\mu_H = \mu_h \quad \text{for } p \gg n \quad (3.18)$$

In terms of experimental quantities,  $R_H$  and  $\rho$  are given by the following equations,

$$R_H = \frac{V_H t}{BI} \quad (3.19)$$

and

$$\rho = \sigma^{-1} = \frac{V_c tw}{\ell I} \quad (3.20)$$

where  $V_H$  is the Hall voltage between contacts 3 and 5 (see Fig. 3.2),  $V_c$  is the conductivity voltage between contacts 2 and 3,  $\ell$ ,  $w$  and  $t$  are the length, width and thickness of the sample respectively.

### 3.3 EXPERIMENTAL PROCEDURE

The mask shown in Fig. 3.2 was used to deposit films in a Hall shape and a standard d.c. technique was used to carry out the Hall effect measurements. The width,  $w$  and the length,  $\ell$  of the film were measured using a travelling microscope.

In the case of in situ Hall measurements (i.e. gaseous ambient experiments described in chapter 4), current of typically 300  $\mu\text{A}$  was passed through contacts 1 and 4 (Fig. 3.2) where actual current passing through the sample was determined by measuring the voltage drop across a standard 100 $\Omega$  resistor connected in series with the sample. The electromagnet was energised by a d.c. power supply unit. The magnetic field was measured by the Hall probe fluxmeter and the fluxmeter was also used to test the uniformity of the field. Using a switch-box, it was possible to change the direction of current flow and magnetic field. The Hall voltage,  $V_H$  between contacts 3 and 5 was determined from four readings

Field

Current	+B	-B
+I	$V_{35}^{++}$	$V_{35}^{+-}$
-I	$V_{35}^{-+}$	$V_{35}^{--}$

$$V_H = \frac{1}{4} \left[ V_{35}^{++} - V_{35}^{+-} + V_{35}^{-+} - V_{35}^{--} \right] \quad (3.21)$$

Conductivity voltage  $V_c$  between contacts 2 and 3 is given by,

$$V_c = \frac{1}{2} \left[ V_{23}^+ + V_{23}^- \right]^* \quad (3.22)$$

where  $V_{23}^+$  is the value for positive current, i.e. current flowing from contacts 1 to 4.

In the case of the Hall measurements as a function of temperature, the film was removed from the vacuum chamber and mounted in a sample holder shown in Fig. 3.3. Indium, electrodag 915 high conductivity silver paste and an evaporated thin film of gold, were used to make ohmic contacts to the film. All three gave satisfactory results. The sample holder was enclosed in a tight fitting copper can and placed inside a dewar flask. The dewar was then placed between the poles of a permanent magnet of 0.148 T field strength. The circuit used to do the Hall measurements is shown in Fig. 3.4. The sample was rotated through  $360^\circ$  and maximum and minimum values of  $V_H$  were recorded. The direction of the current flow was reversed and the sample was rotated through  $360^\circ$  and minimum and maximum values of  $V_H$  were recorded again. The two readings were averaged to obtain  $V_H$ .  $V_c$  was determined from equation (3.22). The sample was cooled to  $77^\circ\text{K}$  using liquid nitrogen and when the temperature had stabilised at  $77^\circ\text{K}$ , liquid  $\text{N}_2$  was poured out. This allowed the film to warm up slowly to room temperature ( $300^\circ\text{K}$ )

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\*  $|V_{23}^+|, |V_{23}^-|$  were almost identical

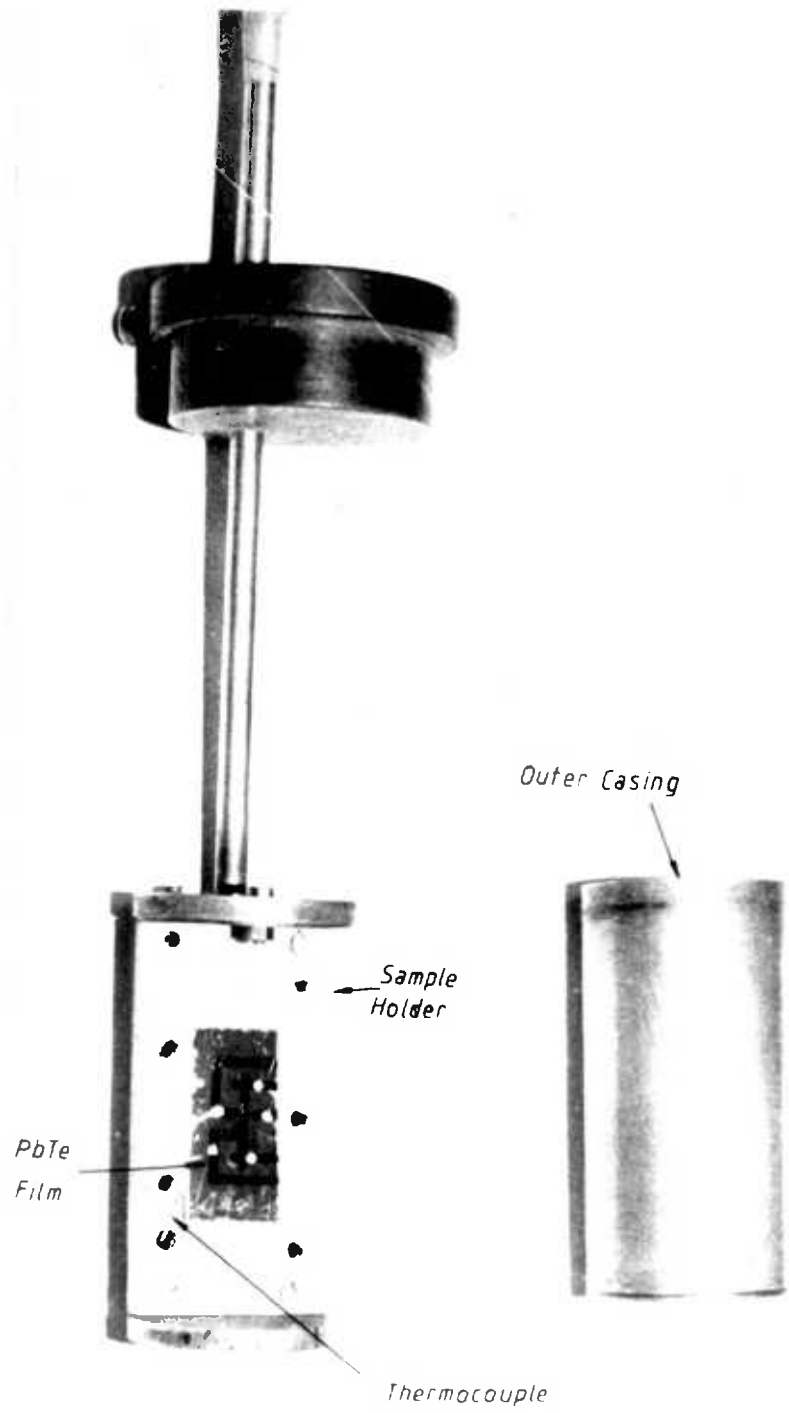


Fig. 3.3

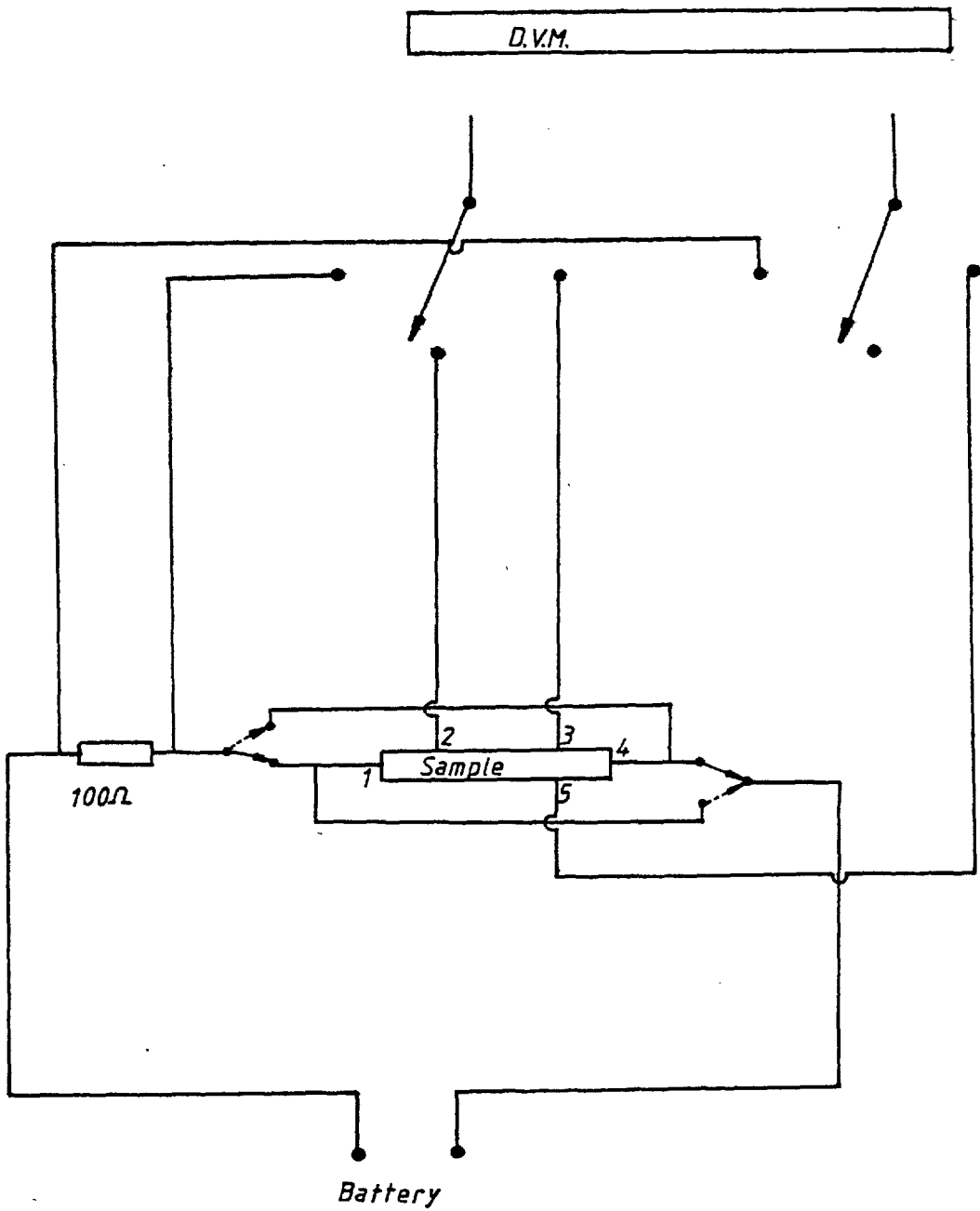


Fig3.4 Circuit diagram for the Hall measurements



and the Hall measurements were performed. The temperature of the film was monitored by iron-constantan thermocouple placed near the film inside the sample holder. A Solartron LM1420 digital voltmeter which had input impedance of  $10^9 \Omega$  was used to measure all the voltages.

### 3.4 RESULTS AND DISCUSSION

The Hall measurements were carried out on eighteen films. Results of four representative films will now be presented. All these films were n-type and grown on mica.

#### 3.4.1 Hall Coefficient, $R_H$ Versus Temperature

Fig. 3.5 shows the temperature dependence of  $R_H$  of films S10, S14, S17 and S66. As it may be noted from the figure,  $R_H$  has a weak temperature dependence and  $|R_H|$  decreases as temperature increases, especially around room temperature. This is in common with other workers (K3, M3, L2, P6) for films grown on mica and NaCl. A change of  $\sim 18\%$  in  $R_H$  may be explained in terms of changing carrier statistics from degenerate to classical when  $A_T$  changes from 1 to  $3\pi/8$ .

#### 3.4.2 Hall Mobility, $\mu_H$ Versus Temperature

Dependence of  $\mu_H = R_H/\rho$  on temperature is shown in Fig. 3.6. Also shown in the figure is  $\mu \propto T^{-2.5}$  dependence. The following points are worth noting.

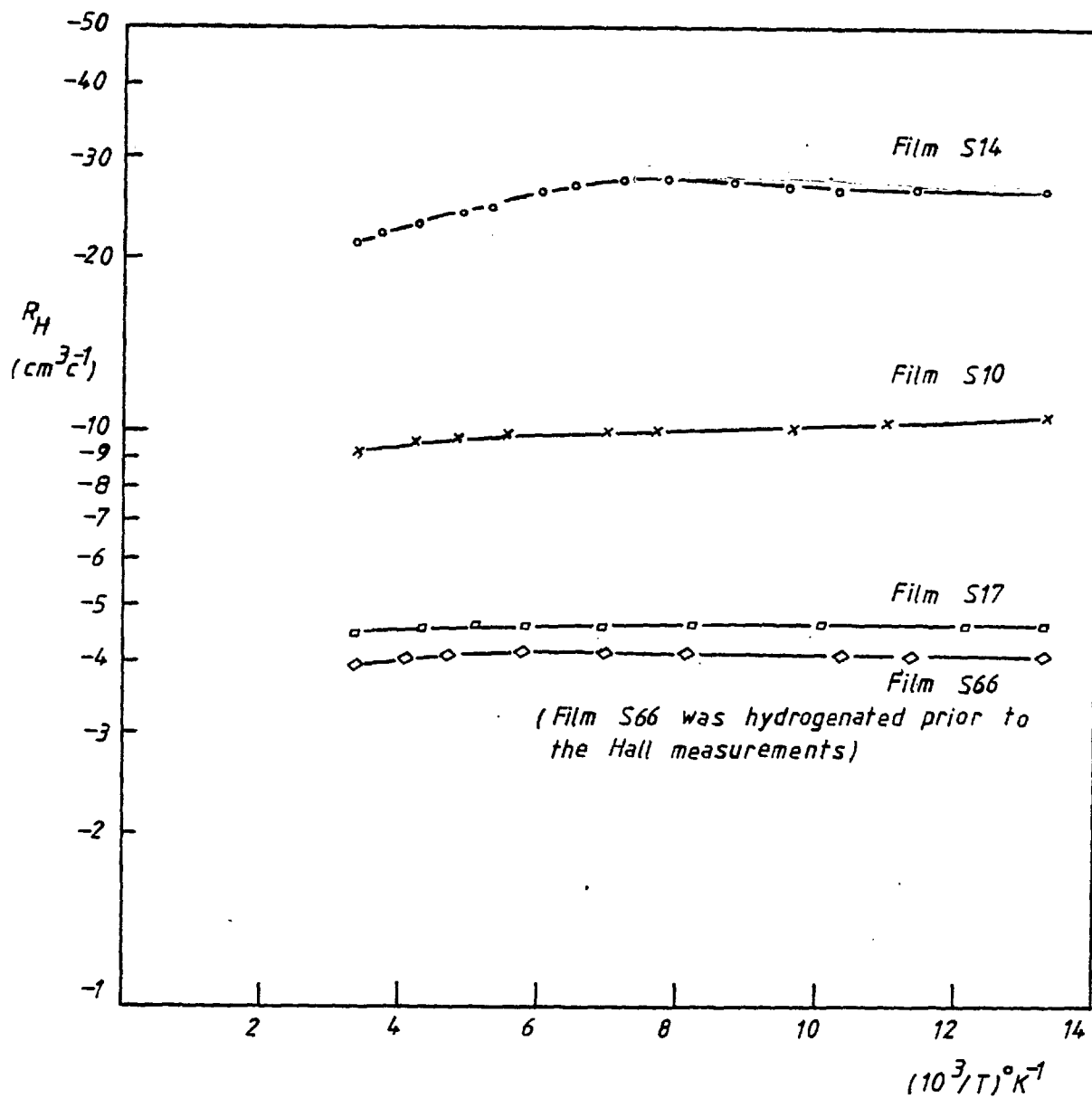


Fig.3.5  $R_H$  versus Temperature

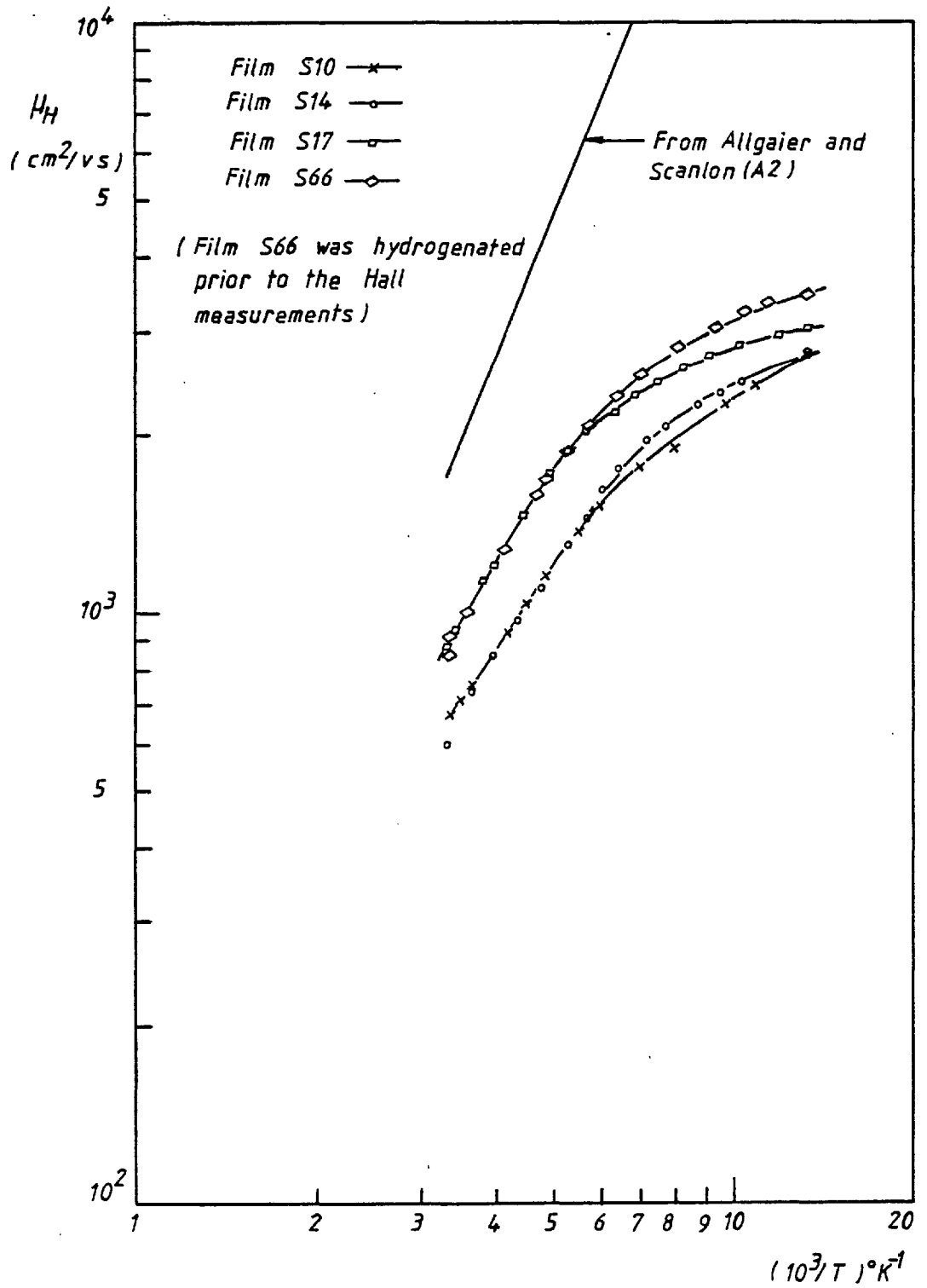


Fig.3.6  $\mu_H$  versus Temperature

- (i)  $\mu_H$  increases with decreasing temperature and the rate of increase tends to level off as liquid  $N_2$  temperature is approached. This was particularly true for films with high carrier concentration ( $\times 10^{18} \text{ cm}^{-3}$ ). This is in common with other workers (K3, G2).
- (ii) The temperature dependence of  $\mu_H$  is weaker than  $T^{-2.5}$  dependence observed for good single crystal PbTe and epitaxial films of PbTe grown on  $BaF_2$  and  $NaCl$  (L2, A2, P1, Z1) where workers in the past have invoked temperature dependence of effective mass in addition to acoustic phonon scattering to account for experimentally observed  $T^{-2.5}$  dependence.

In Table 3.1, a summary of Hall measurements of these films is given. Value of  $s$  in  $\mu_H \propto T^{-s}$  ranged from 1.4 to 1.8 in temperature range 200-300°K for all the films.

In order to assess the contribution of individual scattering mechanisms in case of strong degeneracy (B11, G2), use of Matthiessen's rule can be made, i.e.

Sample	Deposition Temp. (°C)	Film Thickness (Å)	Evap. rate (Å s <sup>-1</sup> )	'Virgin' $\mu_H$ at 300°K (cm <sup>2</sup> v <sup>-1</sup> s <sup>-1</sup> )	$\mu_H$ at 300°K (cm <sup>2</sup> v <sup>-1</sup> s <sup>-1</sup> )	$\mu_H$ at 77°K (cm <sup>2</sup> v <sup>-1</sup> s <sup>-1</sup> )	s in $\mu\alpha T^{-s}$ in temp. range $\sim 200-300^\circ\text{K}$	$n_{300^\circ\text{K}}$ (cm <sup>-3</sup> )	$n_{77^\circ\text{K}}$ (cm <sup>-3</sup> )
S10	175	2900	4.9	882	678	2798	1.45	$6.72 \times 10^{17}$	$6.19 \times 10^{17}$
S14	200	4000	3.1	978	591	2792	1.45	$2.93 \times 10^{17}$	$2.39 \times 10^{17}$
S17	150	3400	3.5	843	883	3016	1.75	$1.4 \times 10^{18}$	$1.36 \times 10^{18}$
S66*	150	3400	2.8	820	845	3483	1.75	$1.6 \times 10^{18}$	$1.55 \times 10^{18}$

\*S66 was H sat. before Hall measurements

Table 3.1

$$\frac{1}{\mu_H} = \frac{1}{\mu_L} + \frac{1}{\mu_s} + \frac{1}{\mu_d} \quad (3.23)$$

where  $\mu_H$  is experimentally determined Hall mobility (assumed equal to  $\mu_e$ ),  $\mu_L$  is mobility limited by lattice scattering,  $\mu_s$  is mobility due to surface scattering and  $\mu_d$  is the defect-scattering mobility. Scattering of carriers due to ionised impurities in the temperature range 77-300<sup>o</sup>K has been considered to be insignificant in PbTe (C9,P1). It is also assumed in equation (3.23) that the above mentioned scattering mechanisms are operating independently of each other. Equation (3.23) was used to evaluate the contribution due to defect scattering for film S17. Assuming completely diffused surface scattering and flat band conditions (J5, M4),

$$\frac{1}{\mu_H} = \frac{1}{\mu_b} \left( 1 + \frac{\lambda}{d} \right) \quad (3.24)$$

where  $\lambda$  is the mean free path of the carriers,  $2d$  is the film thickness and  $\mu_b$  is the mobility due to all other scattering processes except surface scattering.

$$\therefore \mu_b^{-1} = \mu_L^{-1} + \mu_d^{-1} \quad (3.25)$$

From equations (3.23), (3.24) and (3.25),

$$\frac{1}{\mu_s} = \left( \frac{\lambda}{\lambda+d} \right) \frac{1}{\mu_H} \quad (3.26)$$

For degenerate electron gas,  $\lambda$  is given by (O2, R5),

$$\lambda = \frac{\mu_H h}{e} \left(\frac{3n}{8\pi}\right)^{1/3} \quad (3.27)$$

where  $h$  is Plank's constant,  $n$  is the carrier concentration and  $e$  is the electronic charge. Since  $\mu_H$  is known,

$\mu_S$  can be determined from equations (3.26) and (3.27).

$\mu_d$  can then be isolated as follows,

$$\frac{1}{\mu_d} = \frac{1}{\mu_H} - \left(\frac{1}{\mu_S} + \frac{1}{\mu_L}\right) \quad (3.28)$$

By taking  $\mu_L$  from Allgaier and Scanlon (A2),  $\mu_d$  was determined from equation (3.28) since both  $\mu_S$  and  $\mu_H$  were known.

The result of the above analysis is shown in Fig. 3.7. As it can be seen from Fig. 3.7,  $\mu_S$  has a weak temperature dependence whereas  $\mu_d \propto T^{-1.47}$  in the temperature range 200-300°K. Before pursuing the analysis any further, the validity of the assumptions pertaining to  $\mu_S$  must be questioned.

- (i) It has been assumed in equation (3.24) that energy bands of the film remain flat right up to the surface. This is not necessarily true. Since oxygen (air) has an acceptor like effect on n-type PbTe films (see chapters 4

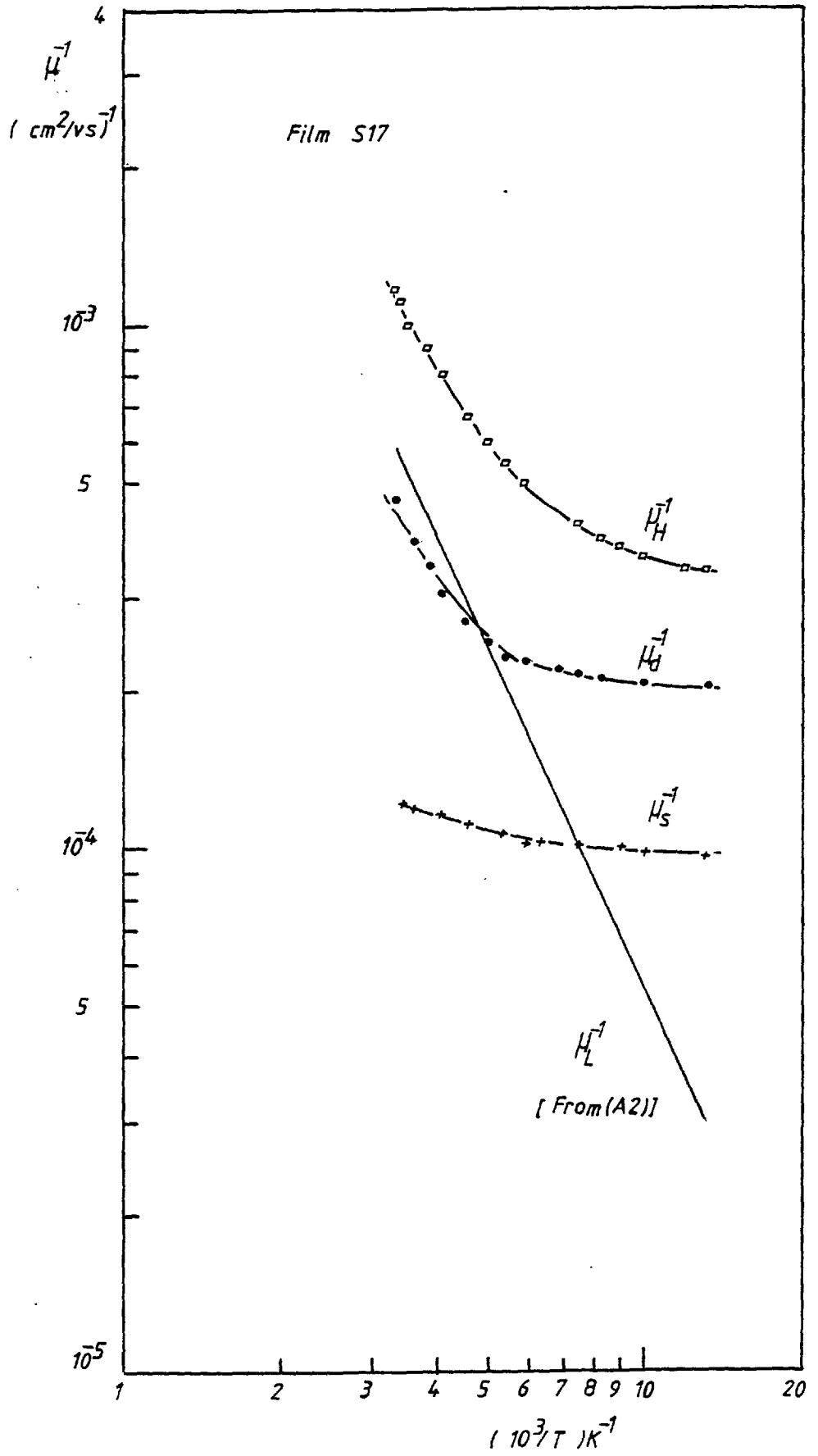


Fig.3.7  $\mu^{-1}$  vs. Temperature



and 5), it is possible that there might be some band bending due to, for instance, depletion of the n-type surface.

- (ii) Completely diffused surface scattering has also been assumed whereas evidence in the literature (P6, B3) suggests that surface scattering in lead chalcogenides is specular.

In view of these assumptions, the above analysis may at best be described as approximate.

It is difficult to associate  $\mu_d \propto T^{-s}$  where  $s = 1.47$  in the case of film S17 (and  $s$  ranged from 1.3-1.5 for films S10, S14 and S66) with defect scattering such as dislocation scattering and grain boundary scattering. Dexter and Seitz (D5) give the following temperature dependence of mobility due to unionised dislocations distributed uniformly within the semiconductor.

$$\mu_{dis} \propto T^{-1} \quad (3.29)$$

Anderson (A6) gives the following expression for grain boundary limited mobility  $\mu_{g.b}$ ,

$$\mu_{g.b} = e\ell \left( \frac{9\pi m_i kT}{8} \right)^{-\frac{1}{2}} \quad (3.30)$$

for classical statistics. For the degenerate case, the expression becomes,

$$\mu_{g.b} = \frac{e\ell}{\hbar} (3\pi^2 n)^{-1/3} \left(\frac{m_d}{m_i}\right)^{1/2} \quad (3.31)$$

where  $\ell$  is the mean free path\*,  $m_d$  is the density of states effective mass,  $m_i$  is the inertial effective mass,  $k$  is Boltzmann's constant,  $T$  is the temperature and  $\hbar = \frac{h}{2\pi}$ ,  $h$  being Plank's constant.

In the case of PbTe, equations (3.30) and (3.31) become (P6),

$$\mu_{g.b} \propto T^{-0.7} \quad (3.32)$$

and

$$\mu_{g.b} \propto T^0 \quad (3.33)$$

Egerton (E1) examined the effect of surface, dislocation and grain boundary scattering on carrier mobility in epitaxial PbTe films. He proposed that the departure from bulk mobility values was due to an additional scattering mechanism. By comparing the theoretical value of  $\ell$  (from equations (3.30) and (3.31) with experimentally determined average spacing,  $D$  between grain boundaries, Egerton put forward that carrier mobility in n-type PbTe films was limited by grain boundary scattering in addition to acoustical phonon scattering. Similar comparison was used by

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\*  $(\approx D/2)$

Parker and Williams (P6) for their n-type PbTe films grown on mica and by Myers et al (M3) for their PbTe films grown on NaCl, to propose that grain boundary scattering was limiting the carrier mobility.

But as mentioned earlier, the value of  $s$  in  $\mu_d \propto T^{-s}$  is incompatible with dislocation and grain boundary scattering in case of present films. Therefore, it seems reasonable to assume that the deviation from  $\mu \propto T^{-2.5}$  dependence in these films is attributable to some other scattering mechanism. For instance, Makino and Hoshina (M5) who carried out in situ Hall effect measurements on n-type PbTe films grown on mica suggested that deviation from  $T^{-2.5}$  dependence was due to scattering of carriers by additional defects formed in the films because of the presence of residual oxygen. In the present case, n-type films are exposed to air prior to the Hall measurements. Therefore, the potential barriers introduced by oxygen at grain boundaries could act as scattering centres. In fact, Green and Miles (G3) have suggested that electrical transport behaviour of air-exposed n-type PbTe films is barrier dominated. Dawar et al (D4) also concluded that carrier mobility of their n-type PbTe films was potential barrier limited.

CHAPTER 4GASEOUS EFFECTS4.1 INTRODUCTION

It is now well established (G4,B3,M2,E1,E4) that the electrical properties of lead salts (PbS, PbSe, PbTe) can be greatly influenced by their interaction with oxygen and atomic hydrogen. For instance as-grown n-type film can be driven p-type by exposing it to oxygen and as-grown p-type film can be turned n-type by exposing it to atomic hydrogen. However, since the important application of these lead salts is in the manufacture of photoconductive infra-red detectors, early work on lead salts was concerned mainly with enhancing the photoconductivity of these salts by oxygenation and mechanism of the gas uptake. Before describing the results of the present study, a brief review of the gaseous effects of lead chalcogenides will be given.

Bode and Levinstein (B1) observed that the resistance of the n-type PbTe film grown on glass substrate increased to a maximum when exposed to oxygen before decreasing again and when the oxygenated film was heated to 650°K it returned to its original resistance. They proposed that oxygen, O<sub>2</sub>, was adsorbed on the surface eventually rendering the surface p-type followed by the diffusion of O<sub>2</sub> via grain boundaries.

This turned parts of the bulk into p-type giving rise to a series of p-n junctions which were responsible for photovoltaic effects. Jones (J1,J2) investigated the reaction of  $O_2$  with PbSe both in powder form and in thin film form. He observed that conductance of n-type film decreased when exposed to  $O_2$ . He also noted that when the oxidised sample was treated with carbon monoxide CO, carbon dioxide  $CO_2$  was evolved. He suggested that  $O_2$  diffuses into the bulk of PbSe to fill Se vacancies. Hillenbrand (H2,H3), studied the reaction of PbS with  $O_2$  and proposed that the adsorbed  $O_2$  exchanged with the lattice to replace S ions and formed PbO phase. The sulphur liberated from the lattice was partially oxidised to  $SO_2$  and slowly desorbed.

Yasuoka et al (Y1) in their study of effects of  $O_2$  on evaporated PbSe films on glass concluded that  $O_2$  was chemisorbed on PbSe at room temperature and diffused into the bulk in the temperature range 100-150°C. Green and Lee (G4) observed that during interaction of  $O_2$  with clean PbTe surfaces in the temperature range 195-303°K, apart from initial rapid reaction a single reaction was operative up to 0.7 monolayer coverage. They further proposed that an adsorption process was consistent with the formation of a peroxide surface complex.

The interaction of  $O_2$  with films of lead salts grown on alkali halides was first studied by Brodsky and Zemel (B3). They noted that the effect of  $O_2$  on epitaxial PbSe films grown on NaCl substrate was reversed by a gas generated by the hot filament of the ionisation gauge whereas other gases like  $N_2$ , He and Ar had no observable effect. They put forward the idea that an appreciable p-type surface layer existed due to exposure to  $O_2$ . However no kinetic studies were carried out to substantiate the proposal. McLane and Zemel (M2) identified the gas generated by the action of hot filament of the ionisation gauge as atomic hydrogen H. They examined the kinetics of the gas uptake on epitaxial films of PbSe grown on NaCl substrate and found that  $O_2$  uptake followed  $\log_e t$  dependence whereas H uptake followed  $t^{\frac{1}{2}}$  dependence.

Egerton et al (E1,E2) investigated the effect of  $O_2$  on epitaxial films of PbS, PbSe and PbTe grown on mica substrate by performing in situ Hall effect measurements. They noted that  $N_2$  and  $H_2$  had no noticeable effect on electrical properties of PbTe and an effect of pure  $O_2$  and air was identical. In order to explain the observed effect of  $O_2$  on PbTe in terms of surface space charge layer, Egerton and Juhasz (E2) found that the surface band-bending in excess of the band gap was necessary and suggested that diffusion was the mechanism of gas uptake. Zemel and Kaplit (Z6) put forward a model based on the oxide with high defect density of ionised

oxygen. According to this model, oxide of about  $20 \text{ \AA}$  in thickness could account for the surface space charge observed by Brodsky and Zemel (B3) and Egerton (E1). The effect of atomic hydrogen, H on PbTe films was investigated by Egerton and Crocker (E4). They noticed that the sheet conductance of n-type film increased with time when exposed to H and the Hall mobility remained constant. They concluded from the kinetics of the reaction that the mechanism for gas uptake was diffusion after the initial fast uptake due to surface adsorption.

Palatnik et al (P7) worked on the effect of  $\text{O}_2$  on single crystal PbS films evaporated onto NaCl substrates. They came to the conclusion that an oxide layer was formed at the surface due to diffusion of lead ions from the bulk to the surface. This loss of cation charge from the bulk made the film less n-type and eventually drove it p-type. Galat et al (G5) measured the work function of PbSe (p-type), PbS (p-type) and PbTe (n-type) in the temperature range  $100\text{--}350^\circ\text{C}$  in oxygen and vacuum and established that oxygen increased the work function of PbSe and PbS and decreased the work function of PbTe. They concluded that initial chemisorption of oxygen at the surface was followed by the formation of heterophase layer where  $\text{PbSO}_4$ ,  $\text{PbSeO}_4$  and  $\text{PbTeO}_4$  (lead sulphate, selenate, tellurate) were the reaction products. In his investigation of oxygen uptake on PbS films evaporated on NaCl substrate in ultra high vacuum, UHV, Lee (L5) carried

out the Hall measurements in situ and suggested a completely new mechanism for the gas uptake. Since the kinetics followed  $\log_e t$  dependence, he suggested that  $O_2$  was chemisorbed on the surface. He further suggested that the chemisorbed  $O_2$  changed the surface stoichiometry and consequently changed the number of free carriers in the bulk of the semiconductor.

Parker and Williams (P8) also carried out in situ Hall effect measurements on PbTe films grown on mica substrate in UHV and concluded that there were two distinct mechanisms of  $O_2$  uptake. During the initial stages of  $O_2$  exposure, the gas reacted at the surface with excess interstitial Pb diffusing outside from the bulk to the surface, whereas during the later stages of the exposure,  $O_2$  atoms were weakly bonded to the outside surface. Hagström and Fahlman (H4) and Sun et al. (S8) used the techniques of x-ray photoelectron spectroscopy (XPS) and ultraviolet photoelectron spectroscopy (UPS) to study the interaction of  $O_2$  with epitaxial films of PbSe and PbTe respectively. Hagström and Fahlman (H4) noted that interaction of  $O_2$  with PbSe was a very slow process with  $O_2$  sticking coefficient of  $10^{-10} - 10^{-11}$ . An oxide layer, a monolayer in thickness, was formed and the continued long exposure led to the diffusion of  $O_2$  into the bulk. Sun et al. (S8) came to the conclusion that  $O_2$  uptake on PbTe occurred in two stages. The first stage was fast and characteristic of the adsorption process and the second stage was characteristic of the oxidation



process where Te and Pb ions break their bonds in favour of affiliating with  $O_2$ .

In summary, it may be noted that the interaction of  $O_2$  with lead salts (PbS, PbSe, PbTe) has been studied under different experimental conditions using different experimental techniques but clear and consistent explanation of mechanism of gas uptake is still lacking. However, based on the above studies two general remarks can be made about this interaction,

- (a) the initial oxygen uptake is rapid and irreversible, and
- (b) prolonged exposure of oxygen is reversible due to removal of  $O_2$  either by pumping or by atomic hydrogen.

In the following sections, results of in situ Hall effect measurements carried out on both n- and p-type PbTe films during their exposure to oxygen and atomic hydrogen will be described and discussed.

#### 4.2 EXPERIMENTAL PROCEDURE

The films used in the gaseous experiments were grown on freshly air-cleaved mica by thermal evaporation as described in Chapter 2. The substrate temperature was in the range  $150-250^{\circ}C$ . The majority of the films grown were n-type (out of about 40 films grown for these experiments only 5 were 'virgin' p-type). When the film had cooled down to room temperature it was placed in

between the poles of an electromagnet using the rotating steel plate. The pressure contacts were then made to the film without breaking the vacuum seal. Since mica substrate (two thou thickness) was not rigid enough to give firm pressure contacts, it was clamped to a clean glass slide. This arrangement gave firm pressure contacts.

The poles of the electromagnet were 1 inch apart and it was energised by passing 3A at 20V through its  $3\Omega$  coil. This produced a uniform magnetic field of 0.22T. The coil of the magnet was placed outside the vacuum chamber to avoid outgassing and the flux was conducted through two steel plates. In order to avoid the heating of the coil, the current through it was switched off as soon as a particular set of readings had been taken. It has been established by other workers (B3, E4, H1) that the effect of  $O_2$  and air on the electrical properties of lead salts is indistinguishable, it was decided to use air instead of  $O_2$  in the present experiments. For H experiments hydrogen gas was conducted into the vacuum system by a flexible steel tubing. The flow of  $H_2$  and  $O_2$  (air) was controlled by two separate needle leak valves.

As an initial experiment, both the needle valves were calibrated in terms of respective gas pressures inside the vacuum chamber where the ionisation gauge was used to measure the gas pressure. As mentioned in Section 4.1, Brodsky and Zemel (B3) believed that the electrical properties of PbSe film changed when the

ionisation gauge was switched on and later McLane and Zemel (M2) identified the gas generated by the action of the hot filament of the ionisation gauge as atomic hydrogen and further noted that H was generated only when the vacuum system was pumped by a diffusion pump filled with Octoil-S oil (a hydrocarbon oil). No H was detected when the diffusion pump oil was replaced by Don Coring 704, a silicone oil (a non-hydrocarbon oil). Therefore the interaction of the residual hydrocarbons from the vacuum system with the hot filament of the ionisation gauge was producing atomic hydrogen (M2). Even though the diffusion pump used in the present case was filled with Silicone MS 704 oil, the use of the ionisation gauge was kept to a minimum during an actual experimental run as a precaution.

A tungsten filament was used to atomise  $H_2$  gas. This has proved to be an effective method of producing H in the past (B4, H5, B2). The tungsten filament used was 8 thou in diameter, 20 cm in length and was placed 15 cm below the film. The filament was heated to about  $1750^{\circ}C$  and the temperature of the filament was measured by an optical pyrometer (Optix No. 10495). An aluminium foil was placed above the tungsten filament to shield the film from the radiative heat. No observable effect on the Hall coefficient  $R_H$  and resistivity  $\rho$  of the film was found when the tungsten filament was switched on in the absence of  $H_2$  gas in contrast to Egerton's and Crocker's (E4) findings.

In the following section, the description of  $R_H$  versus  $\rho$  curves for both n- and p-type will be given where the description has been divided into three sub-sections. The first sub-section will deal with the description of  $R_H$  vs  $\rho$  curves for air-exposed films at room temperature, the second sub-section will deal with the description of unexposed ('virgin') films at room temperature and the third sub-section will deal with the description of air-exposed films not at room temperature. The method of measuring  $R_H$  and  $\rho$  has been detailed in chapter 3.

#### 4.3 RESULTS ( $R_H$ VERSUS $\rho$ CURVES)

##### 4.3.1 Air-exposed Films

During the initial experiments of gaseous effects, some films were grown at 250°C in two different geometric configurations during the same evaporation run. One configuration was the gap configuration achieved by using a molybdenum mask (described in chapter 3) and the other configuration was the sandwich type configuration where the semiconductor film was sandwiched in between two metallic contacts. However, it was necessary to break the vacuum seal to evaporate the contacts for the sandwich configuration and therefore the films grown by this method were all air-exposed prior to carrying out any gaseous effect measurements. All such films remained n-type even after long air-exposure (over one year in some cases). The behaviour of film S6 was typical of these films.

Fig. 4.1 and Fig. 4.2 show the variations of  $R_H$  vs  $\rho$  and resistance  $R_D$  vs time respectively for film S6 during its exposure to atomic hydrogen, H and oxygen  $O_2$ .  $R_H$  and  $\rho$  were monitored for the gap configuration and  $R_D$  vs time were monitored for the sandwich configuration. Prior to H exposure,  $R_H$  was  $-22.1 \text{ cm}^3/\text{C}$  and  $\rho$  was  $0.03 \Omega \text{ cm}$  when the film was exposed to H ( $p_{H_2} = 1 \times 10^{-4} \text{ } \tau$ ),  $R_H$  and  $\rho$  decreased until the film was saturated, i.e. no observable changes occurred in  $R_H$  and  $\rho$ . The saturation values of  $R_H$  and  $\rho$  were  $-2.16 \text{ cm}^3/\text{C}$  and  $0.003 \Omega \text{ cm}$  respectively. Throughout the gas exposure, the Hall mobility  $\mu_n$  given by  $R_H \div \rho$  changed by only 2.3% from  $\sim 737 \text{ cm}^2/\text{V-sec}$  to  $720 \text{ cm}^2/\text{V-sec}$ . The film was then exposed to  $O_2$  ( $p_{O_2} = 1 \times 10^{-4} \text{ } \tau$ ) and the values of  $R_H$  and  $\rho$  increased with very small variations in  $\mu_n$ . Finally when the film was let up to atmospheric pressure,  $R_H$  was  $-5.25 \text{ cm}^3/\text{C}$  and  $\rho$  was  $0.007 \Omega \text{ cm}$ . Resistance  $R_D$  of film S6 in the sandwich configuration decreased from  $49 \Omega$  to  $20.3 \Omega$  during the H exposure and increased from  $20.3 \Omega$  to  $42.7 \Omega$  during the  $O_2$  cycle. As it can be seen from Fig. 4.1, paths traced by  $R_H$  vs  $\rho$  curves during H and  $O_2$  cycles were almost identical and the film showed no tendency to turn p-type.

#### 4.3.2 'Virgin' Films

Since no additional information other than the reversibility of H effect by  $O_2$  effect was obtained using the sandwich configuration, it was decided to grow the films in gap configuration only. This also meant that

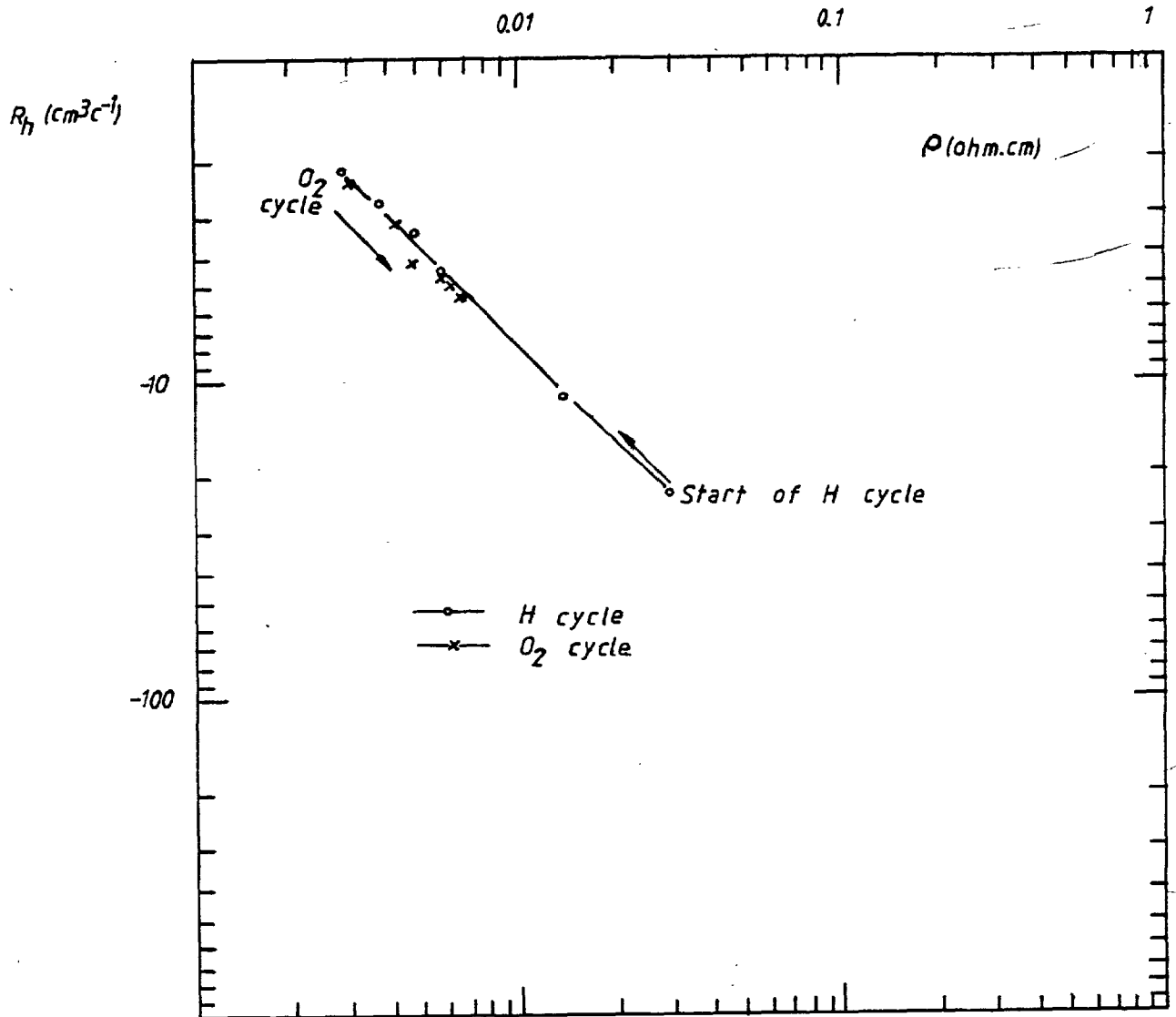


Fig. 4.1  $R_h$  vs.  $\rho$  (Film S6)

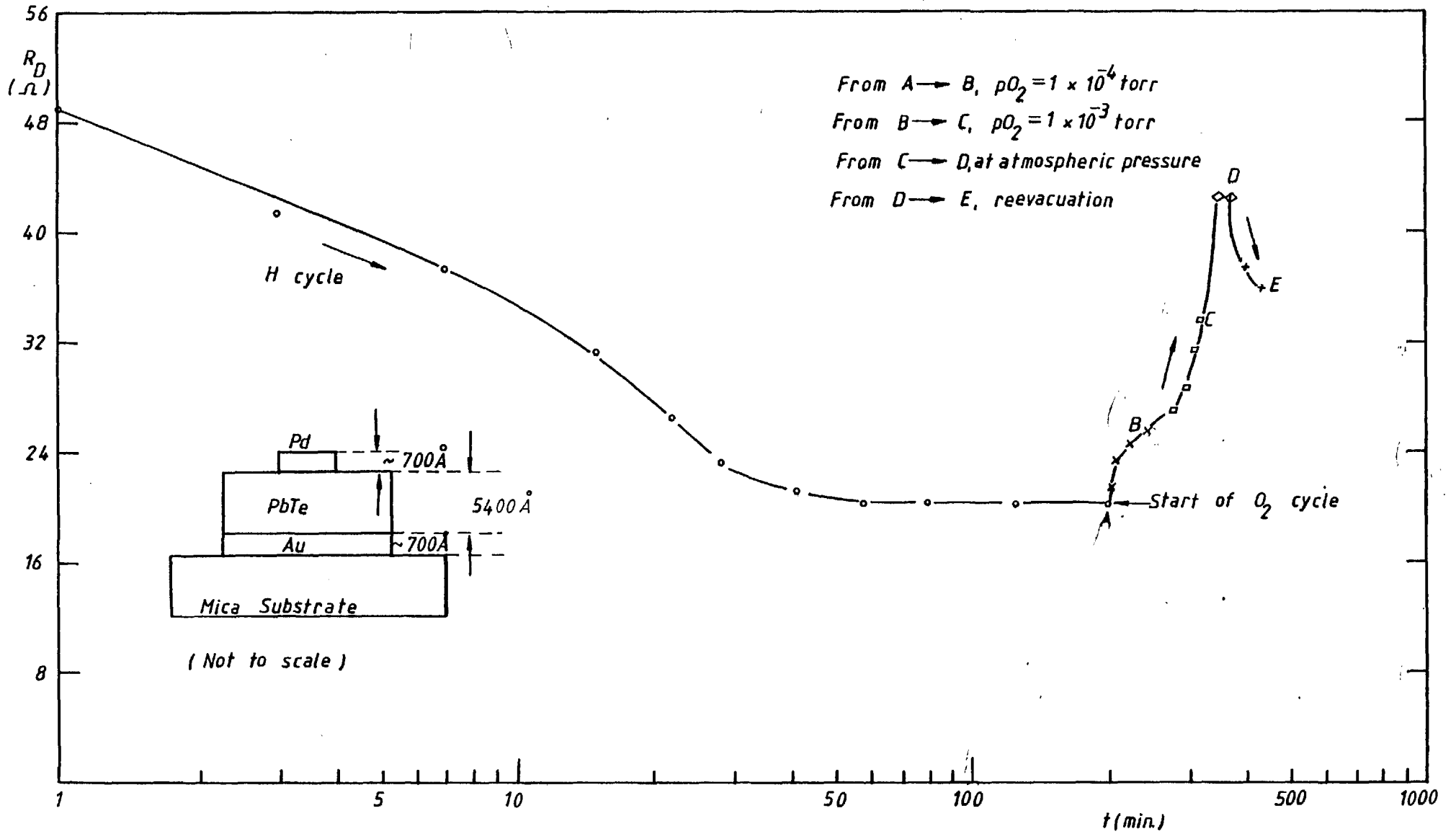


Fig.4.2  $R_D$  versus time for film S6 in sandwich configuration (n-type film)

in situ Hall effect measurements could be carried out as the films were exposed to H and O<sub>2</sub>. Because the films typified by S6 were 'stable' n-type, it was decided to evaporate films at lower substrate temperatures (150-250°C) in an attempt to grow both n- and p-type films.

In the following sections, results will be described for three 'virgin' n-type films and three 'virgin' p-type films considered to be representative of the general<sup>0</sup> behaviour of such films.

#### 4.3.2.1 'Virgin' n-type films

Fig. 4.3 shows the changes in  $R_H$  and  $\rho$  of film S27 grown at 250°C and 2940 Å in thickness. As the film was exposed to H ( $p_{H_2} = 2 \times 10^{-4} \tau$ ),  $R_H$  changed from -139.2 cm<sup>3</sup>/C to -2.32 cm<sup>3</sup>/C and the corresponding change in  $\rho$  was from 0.33 Ω cm to 0.0051 Ω cm while the change in  $\mu_n$  was from 422 cm<sup>2</sup>/V-sec to 455 cm<sup>2</sup>/V-sec. As expected, H drove the film more n-type and the film was saturated in 96 mins. Film S27 was then exposed to O<sub>2</sub> ( $p_{O_2} = 2 \times 10^{-4} \tau$ ) and during the first hour of gas exposure,  $|R_H|$  increased from -2.32 cm<sup>3</sup>/C to -11.25 cm<sup>3</sup>/C and  $\rho$  increased from 0.0051 Ω cm to 0.0215 Ω cm indicating that the film was turning less n-type. The film was left at  $p_{O_2} = 2 \times 10^{-4} \tau$  pressure over night and  $|R_H|$  increased to -15.2 cm<sup>3</sup>/C and when the film was exposed to atmospheric pressure,  $|R_H|$  began to decrease slowly and film S27 turned p-type after three days. Film S27 was kept in air for another two days



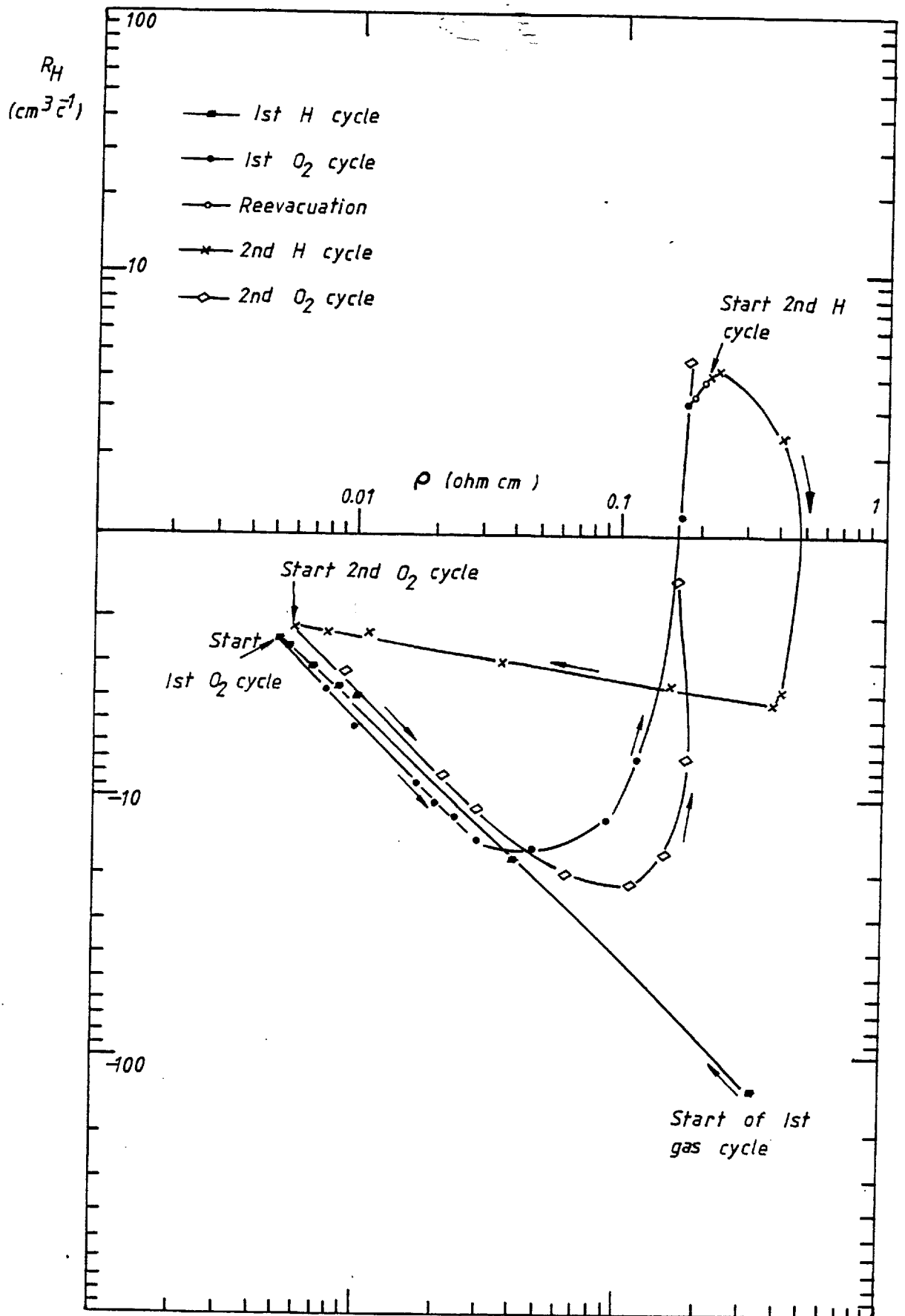


Fig.4.3  $R_H$  versus  $\rho$  for film S27

before re-evacuating the chamber. During re-evacuation, both  $R_H$  and  $\rho$  increased from  $3.2 \text{ cm}^3/\text{C}$  and  $0.183 \text{ } \Omega \text{ cm}$  to  $4.06 \text{ cm}^3/\text{C}$  and  $0.211 \text{ } \Omega \text{ cm}$  respectively, indicating a decrease in surface carrier concentration of  $1.21 \times 10^{13} \text{ cm}^{-2}$ . During the second H cycle ( $p_{\text{H}_2} = 2 \times 10^{-4} \text{ } \tau$ ), the film turned n-type within 10 min. As the film was exposed to  $\text{O}_2$  ( $p_{\text{O}_2} = 2 \times 10^{-4} \text{ } \tau$ ) for the second time,  $|R_H|$  increased from  $-2.2 \text{ cm}^3/\text{C}$  to  $-22.2 \text{ cm}^3/\text{C}$  in about three and a half hours before starting to decrease again and the film turned p-type after two days of air exposure at atmospheric pressure. The paths traversed by  $R_H$  vs  $\rho$  curves during these cycles are shown in Fig. 4.3 where the path traversed during the H cycle is clockwise and the path traversed during  $\text{O}_2$  cycle is counter clockwise.

Film S37 (Fig. 4.4) grown at  $175^\circ\text{C}$  and  $2946 \text{ } \text{\AA}$  in thickness was left in a vacuum of  $\sim 1 \times 10^{-6} \text{ } \tau$  for 20 hours. During this period  $|R_H|$  increased from  $-15.1 \text{ cm}^3/\text{C}$  to  $-22.3 \text{ cm}^3/\text{C}$  showing that the carrier concentration had decreased by  $\sim 3.9 \times 10^{12} \text{ cm}^{-2}$ . When the film was exposed to H ( $p_{\text{H}_2} = 1 \times 10^{-4} \text{ } \tau$ ), it became progressively more n-type and H cycle lasted for 225 mins. When the H saturated film was exposed to  $\text{O}_2$  ( $p_{\text{O}_2} = 2 \times 10^{-4} \text{ } \tau$ ), changes in  $R_H$  and  $\rho$  became slower and slower as time went on. Film S27 turned p-type after six days of air exposure at atmospheric pressure. On re-evacuation,  $R_H$  and  $\rho$  increased and during this period of pump-down carrier concentration decreased by  $3.6 \times 10^{12} \text{ cm}^{-2}$ . The second

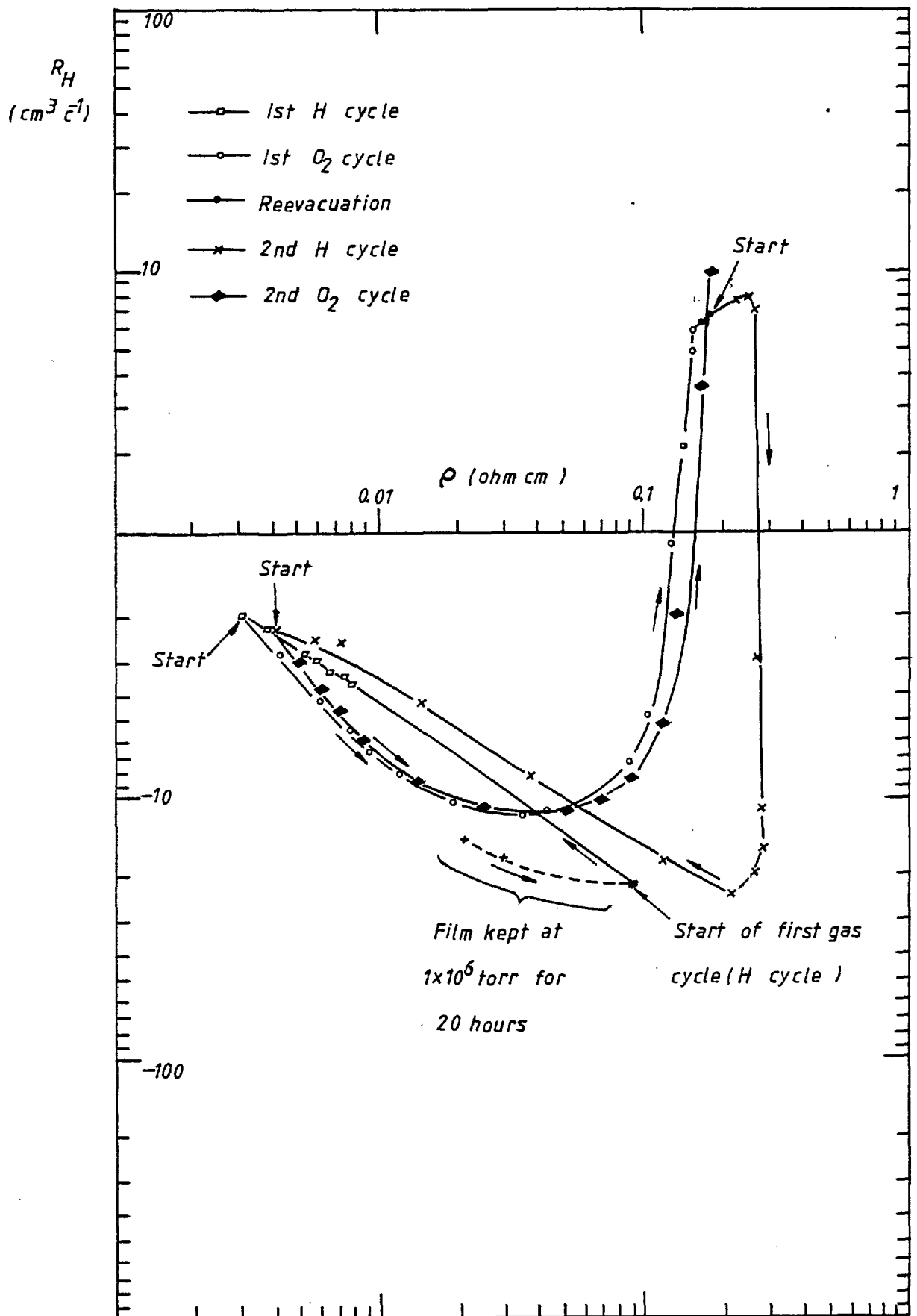


Fig.4.4  $R_H$  versus  $\rho$  for film S37

H cycle drove the film n-type in about  $3\frac{1}{2}$  mins whereas it took another six days to turn the film p-type again. Fig. 4.4 shows the paths traversed as the film was exposed to successive H-O<sub>2</sub> cycles.

Film S47 (Fig. 4.5) represents the behaviour of 'virgin' n-type films exposed to O<sub>2</sub> as the first gas cycle. When the film was exposed to O<sub>2</sub> ( $p_{O_2} = 2 \times 10^{-4} \tau$ ),  $R_H$  changed from  $-1.17 \text{ cm}^3/\text{C}$  to  $+1.48 \text{ cm}^3/\text{C}$  in  $\sim 4$  mins and after a further exposure of three and a half hours  $R_H$  rose to  $9.8 \text{ cm}^3/\text{C}$ . The film was kept at this pressure for 48 hours and as a result  $R_H$  increased to  $73 \text{ cm}^3/\text{C}$  before decreasing again. When the film was let up to atmospheric pressure,  $R_H$  decreased to  $14.8 \text{ cm}^3/\text{C}$  before rising slightly to  $15.1 \text{ cm}^3/\text{C}$ . Corresponding changes in  $\rho$  were from  $0.516 \Omega \text{ cm}$  ('virgin' n-type) to  $0.106 \Omega \text{ cm}$  (p-type). In common with the previous films,  $R_H$  and  $\rho$  rose linearly keeping the Hall mobility almost constant during re-evacuation. During the first H cycle ( $p_{H_2} = 4 \times 10^{-5} \tau$ ),  $R_H$  and  $\rho$  continued to increase linearly keeping the Hall mobility  $\mu_p$  constant at  $\sim 180 \text{ cm}^2/\text{V-sec}$ . As the pressure of H<sub>2</sub> was increased to  $1 \times 10^{-4} \tau$ ,  $R_H$  and  $\rho$  kept on increasing along the same line and reached a maximum where  $R_H$  was  $74.7 \text{ cm}^3/\text{C}$  and  $\rho$  was  $0.46 \Omega \text{ cm}$ . The film was driven n-type in 41 mins. During the second O<sub>2</sub> cycle ( $p_{O_2} = 2 \times 10^{-4} \tau$ )  $|R_H|$  increased rapidly compared with the previous two films from  $-3.68 \text{ cm}^3/\text{C}$  to  $-155 \text{ cm}^3/\text{C}$  within 30 mins and then the uptake slowed down.  $|R_H|$

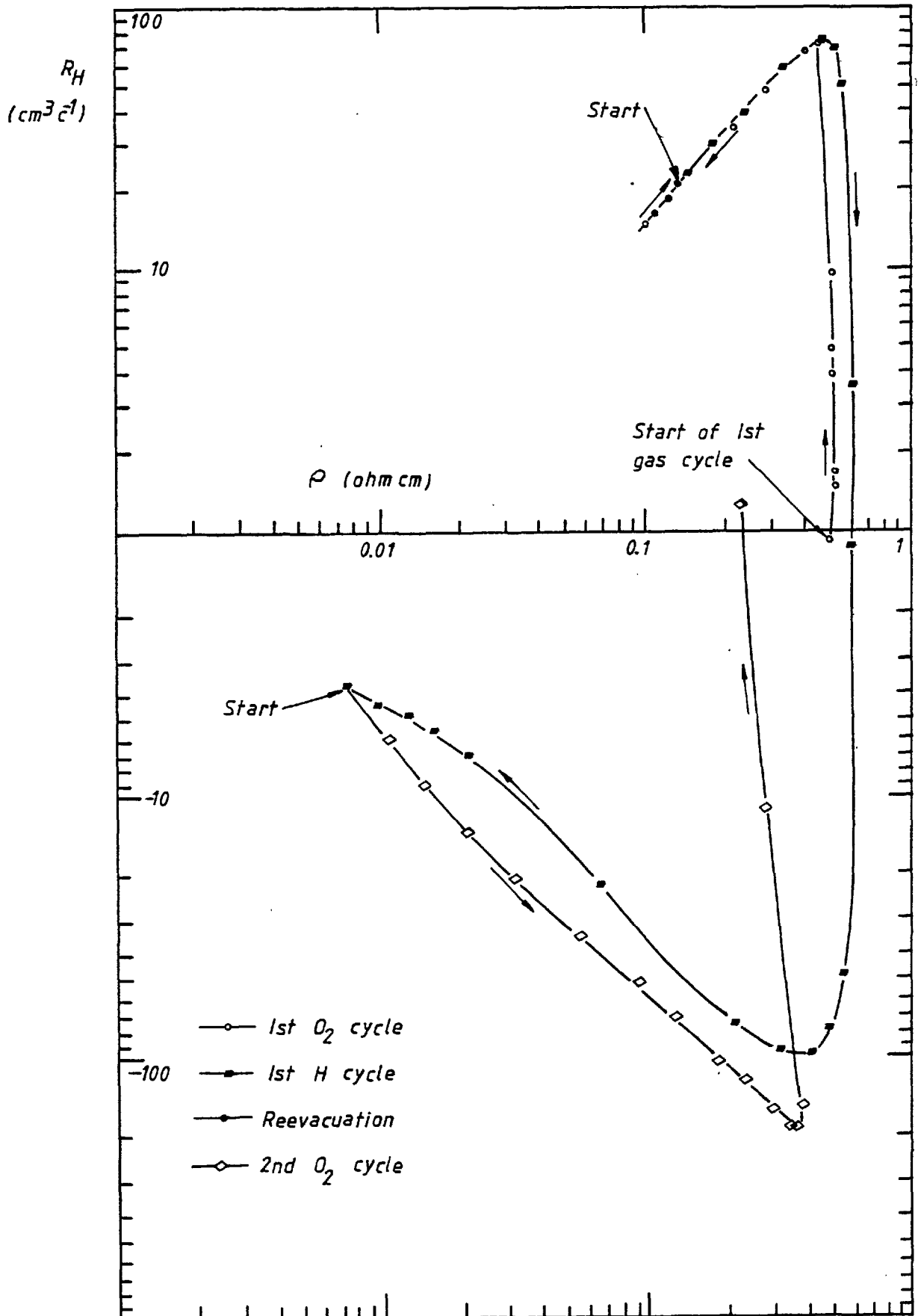


Fig. 4.5  $R_H$  versus  $\rho$  for film S47

Film	Virgin Type	Deposition Temp. °C	Film Thickness (Å)	Cycle No.	Time Elapsed* before Gas Cycle	Effect of Gas Cycle	Time Taken to Reverse Conductivity	Cycle Duration	Carrier Conc. before Gas Cycle (cm <sup>-3</sup> )	Carrier Conc. at End of Gas Cycle (cm <sup>-3</sup> )	Fig. No.
S27	n	250	2940	1st H	194 mins	n + n <sup>+</sup>	Film became more n-type	96 mins	n=4.49 x 10 <sup>16</sup>	n=2.69 x 10 <sup>18</sup>	4.3
				1st O <sub>2</sub>	290 mins	n + p	3 days	5 days	n=2.69 x 10 <sup>18</sup>	p=1.95 x 10 <sup>18</sup>	
				2nd H	~5 days	p + n	10 mins	117 mins	p=1.54 x 10 <sup>18</sup>	n=2.84 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~5½ days	n + p	2 days	3 days	n=2.84 x 10 <sup>18</sup>	p=1.3 x 10 <sup>18</sup>	
S37	n	175	2946	Film left in vacuum of ~1x10 <sup>-6</sup> Torr for 20 hours		n + n <sup>-</sup>	Film became less n-type	20 hours	n=4.14 x 10 <sup>17</sup>	n=2.8 x 10 <sup>17</sup>	4.4
				1st H	20 hours	n + n <sup>+</sup>	Film became more n-type	225 mins	n=2.8 x 10 <sup>17</sup>	n=3 x 10 <sup>18</sup>	
				1st O <sub>2</sub>	~24 hours	n + p	6 days	12 days	n=3 x 10 <sup>18</sup>	p=1 x 10 <sup>18</sup>	
				2nd H	13 days	p + n	3.5 mins	280 mins	p=9.11 x 10 <sup>17</sup>	n=2.5 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~13 days	n + p	6 days	14 days	n=2.5 x 10 <sup>18</sup>	p=6.3 x 10 <sup>17</sup>	
S47	n	175	2900	1st O <sub>2</sub>	19 hours	n + p	4 mins	2 days	n=5.34 x 10 <sup>18</sup>	p=4.14 x 10 <sup>17</sup>	4.5
				1st H	~3 days	p + n	41 mins	204 mins	p=2.68 x 10 <sup>17</sup>	n = 1.7 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~3 days	n + p	~20 hours	24 hours	n=1.7 x 10 <sup>18</sup>	p=4.81 x 10 <sup>18</sup>	

\*Time elapsed was measured from the moment the evaporation of the film was completed to starting a particular gas cycle.

TABLE 4.1

reached a maximum at  $-188 \text{ cm}^3/\text{C}$  ( $\rho = 0.38 \text{ } \Omega \text{ cm}$ ) and started to decrease again. When the film was exposed to atmospheric pressure, it turned p-type where  $R_H$  was  $1.3 \text{ cm}^3/\text{C}$  and  $\rho$  was  $0.231 \text{ } \Omega \text{ cm}$ . Curves traced by  $R_H$  vs  $\rho$  during H-O<sub>2</sub> cycles are shown in Fig. 4.5.

The main points of the gaseous effects of films S27, S37 and S47 are summarised in Table 4.1.

#### 4.3.2.2 'Virgin' p-type films

The curves for  $R_H$  vs  $\rho$  of film S25 for two H-O<sub>2</sub> cycles are shown in Fig. 4.6. Film S25 had high resistivity ( $\rho = 0.66 \text{ } \Omega \text{ cm}$ ) and low carrier concentration ( $p = 7.4 \times 10^{16} \text{ cm}^{-3}$ ). As the film was exposed to H ( $p_{\text{H}_2} = 1 \times 10^{-4} \text{ } \tau$ ), it drove the film n-type within 90 secs and when the H exposure was stopped,  $R_H$  was  $-1.76 \text{ cm}^3/\text{C}$  and  $\rho = 0.0036 \text{ } \Omega \text{ cm}$ . The film was then exposed to O<sub>2</sub> ( $p_{\text{O}_2} = 2 \times 10^{-4} \text{ } \tau$ ) and  $|R_H|$  increased to  $-14.7 \text{ cm}^3/\text{C}$  within two hours and after that the changes in  $R_H$  and  $\rho$  were much slower. When the vacuum chamber was let up to atmospheric pressure,  $|R_H|$  increased slowly to  $-18 \text{ cm}^3/\text{C}$  and then started to decrease again. The film turned p-type after six days. The film was stored in a dessicator for a period of 20 weeks in the laboratory atmosphere prior to the second H cycle. During the second H cycle, both  $R_H$  and  $\rho$  increased showing that the film was becoming less p-type and the Hall mobility  $\mu_p$  remained constant at  $\sim 120 \text{ cm}^2/\text{V-sec}$ .  $R_H$  reached a maximum and started to decrease and the film turned n-type

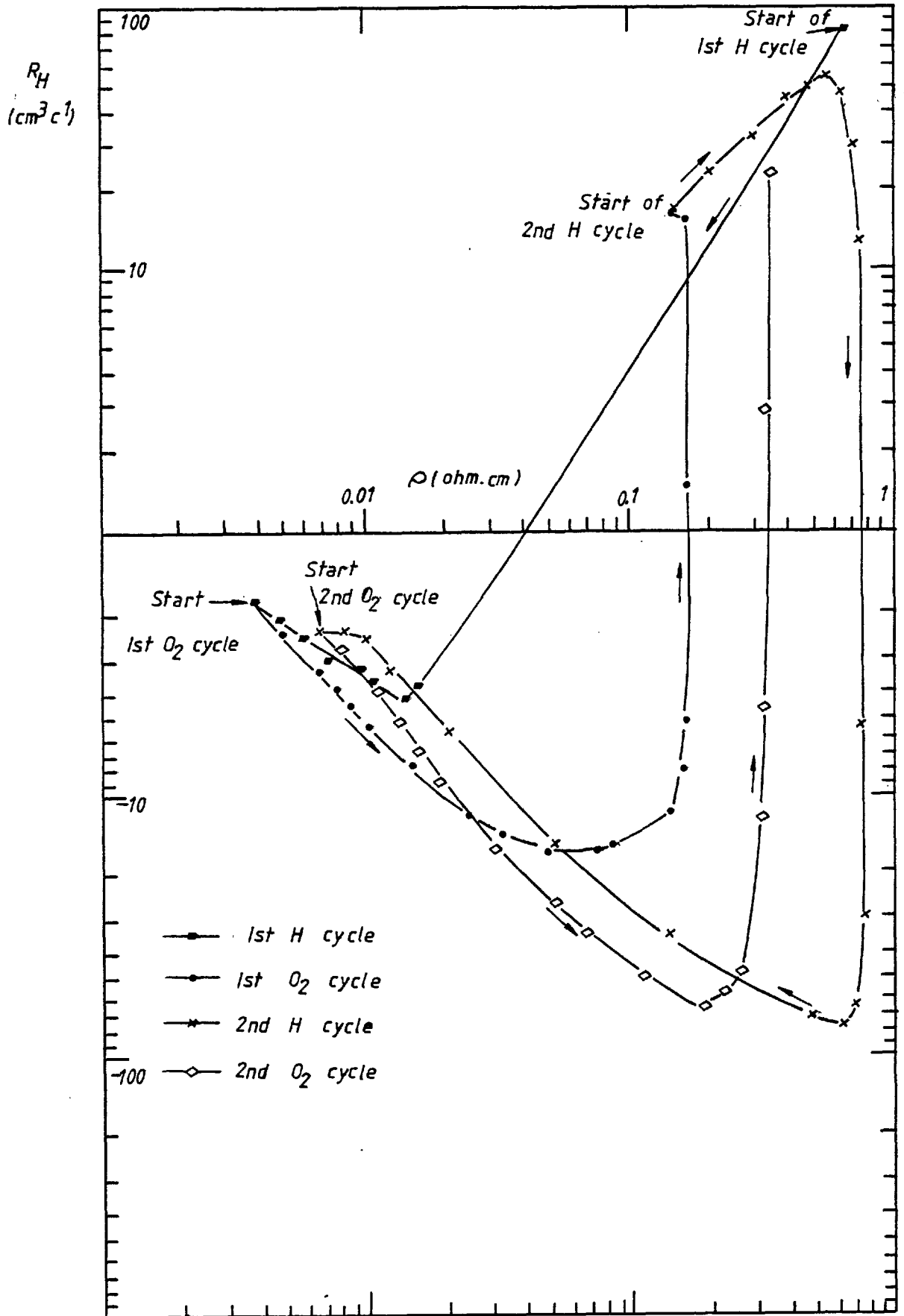


Fig. 4.6  $R_H$  vs.  $\rho$  for film S25



after 47 mins. The effect of H was reversed by  $O_2$  when the film was exposed to the gas at  $p_{O_2} = 2 \times 10^{-4} \tau$  and the film reverted back to its original type of conductivity after three days.

When film S29 (Fig. 4.7) was left in a vacuum of  $\sim 1 \times 10^{-6} \tau$  for 47 hours,  $R_H$  decreased slightly from  $112 \text{ cm}^3/\text{C}$  to  $109 \text{ cm}^3/\text{C}$  indicating that surface carrier concentration had risen by  $6.81 \times 10^{10} \text{ cm}^{-2}$ . As the film was exposed to H ( $p_{H_2} = 1 \times 10^{-4} \tau$ ), it turned n-type as expected. When  $O_2$  was leaked into the vacuum chamber at  $p_{O_2} = 2 \times 10^{-4} \tau$ ,  $|R_H|$  reached a maximum at  $-129 \text{ cm}^3/\text{C}$  ( $\rho \sim 0.5 \Omega \text{ cm}$ ) and started to decrease. Film S29 became p-type after 204 mins. As shown in Fig. 4.7, the paths traversed by  $R_H$  vs  $\rho$  curves during H and  $O_2$  cycles were different.

Fig. 4.8 shows the changes in  $R_H$  and  $\rho$  as film S51 was exposed to  $O_2$  as the initial gas cycle. Prior to the  $O_2$  cycle,  $R_H$  was  $71.3 \text{ cm}^3/\text{C}$  and  $\rho$  was  $0.52 \Omega \text{ cm}$ . During the  $O_2$  cycle, both  $R_H$  and  $\rho$  decreased showing that  $O_2$  was driving the film progressively more p-type as expected. When  $R_H$  reached  $9.6 \text{ cm}^3/\text{C}$ , the film was let up to atmospheric pressure and  $R_H$  increased to  $12.7 \text{ cm}^3/\text{C}$ . During the re-evacuation, like all other films described,  $R_H$  and  $\rho$  increased and during the H cycle  $R_H$  and  $\rho$  continued to increase until  $R_H$  reached a maximum at  $83 \text{ cm}^3/\text{C}$ . After reaching this maximum  $R_H$  decreased and the film became n-type after 28 mins. The  $O_2$  cycle reversed the effect

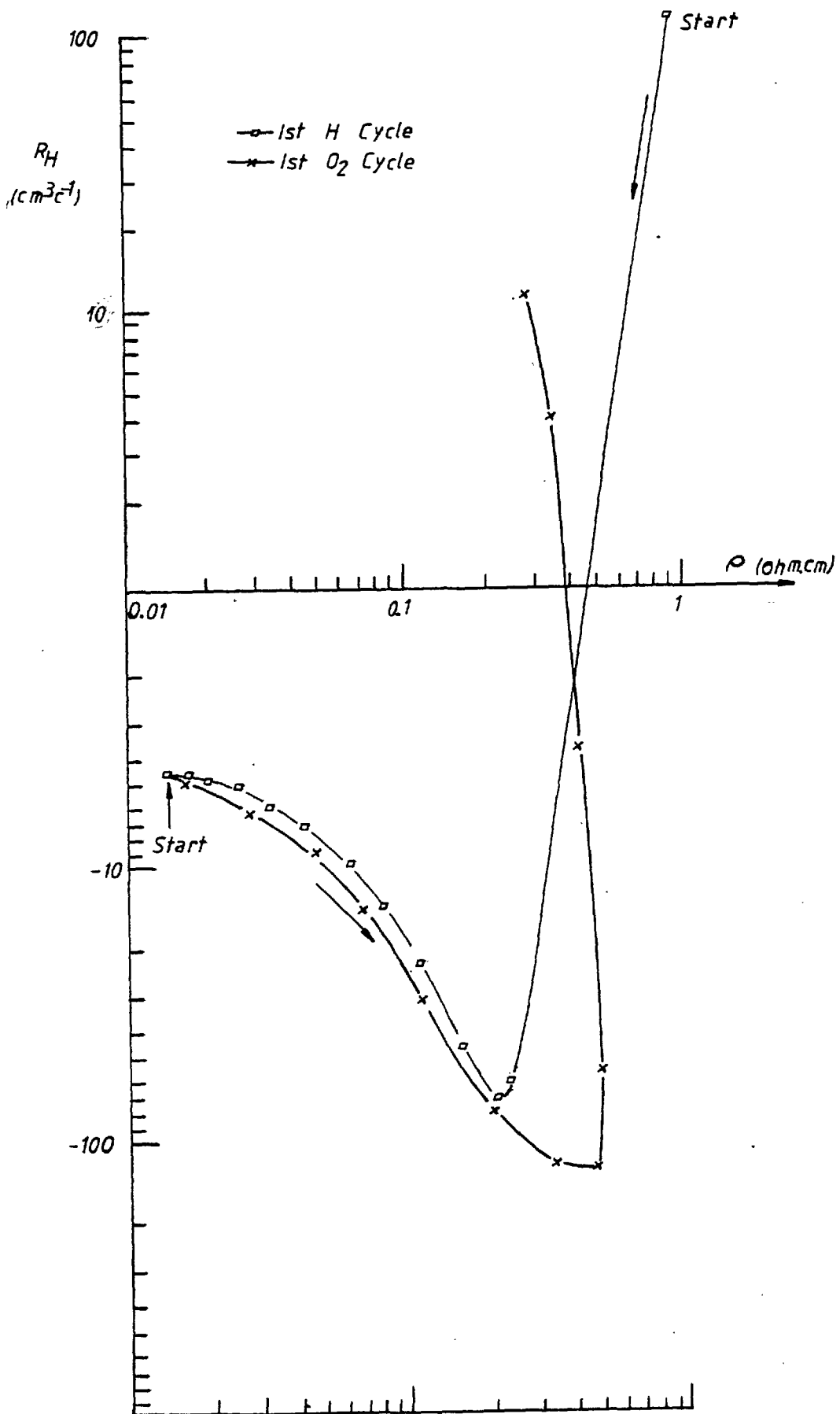


Fig. 4.7  $R_H$  vs.  $\rho$  (Film S29)

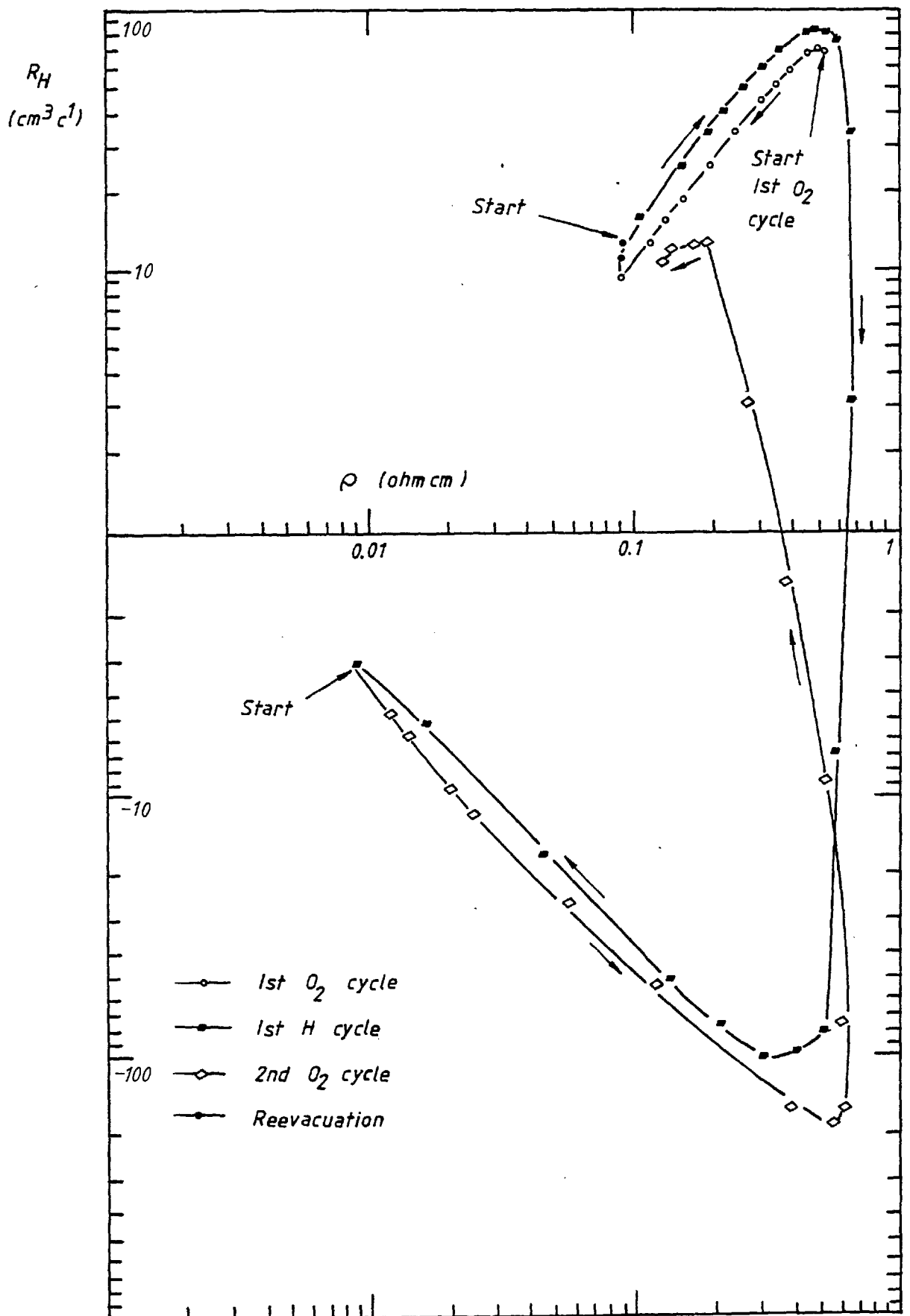


Fig. 4.8  $R_H$  versus  $\rho$  for film S51

Film	Virgin Type	Deposition Temp. °C	Film Thickness (Å)	Cycle No.	Time Elapsed* before Gas Cycle	Effect of Gas Cycle	Time Taken to Reverse Conductivity	Cycle Duration	Carrier Conc. before Gas Cycle (cm <sup>-3</sup> )	Carrier Conc. at End of Gas Cycle (cm <sup>-3</sup> )	Fig.No.
S25	p	170	2038	1st H	138 mins	p + n	~90 secs	159 mins	p=7.4 x 10 <sup>16</sup>	n=3.55 x 10 <sup>18</sup>	4.6
				1st O <sub>2</sub>	297 mins	n + p	6 days	20 weeks	n=3.55 x 10 <sup>18</sup>	p=3.68 x 10 <sup>17</sup>	
				2nd H	20 weeks	p + n	47 mins	230 mins	p=3.7 x 10 <sup>17</sup>	n=2.31 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~20 weeks	n + p	3 days	6 days	n=2.31 x 10 <sup>18</sup>	p=2.6 x 10 <sup>17</sup>	
S29	p	150	4438	Film left in vacuum of 1x10 <sup>-6</sup> r for 47 hours		p + p <sup>+</sup>	Film became more p-type	47 hours	p=5.58 x 10 <sup>16</sup>	p=5.73 x 10 <sup>16</sup>	4.7
				1st H	47 hours	p + n	~90 secs	148 mins	p=5.73 x 10 <sup>16</sup>	n=1.39 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~49 hours	n + p	204 mins	26 hours	n=1.39 x 10 <sup>18</sup>	p=5.21 x 10 <sup>17</sup>	
S51	p	175	2049	1st O <sub>2</sub>	63 mins	p + p <sup>+</sup>	Film became more p-type	81 mins	p=8.77 x 10 <sup>16</sup>	p=4.92 x 10 <sup>17</sup>	4.8
				1st H	~20 hours	p + n	28 mins	156 mins	p=3.93 x 10 <sup>17</sup>	n=2.08 x 10 <sup>18</sup>	
				2nd O <sub>2</sub>	~22 hours	n + p	20 hours	24 hours	n=2.08 x 10 <sup>18</sup>	p=5.95 x 10 <sup>17</sup>	

\*Time elapsed was measured from the moment the evaporation of the film was completed to starting a particular gas cycle.

TABLE 4.2

of the H cycle and restored the film to its original type of conductivity where  $|R_H|$  went through two maxima during the gas cycle.

In Table 4.2, a summary of the H-O<sub>2</sub> cycles is given for films S25, S29 and S51.

#### 4.3.3 Air-exposed Films (not at room temperature)

Up to now, all the results described were for the gas exposures carried out at room temperature. No facility was available to heat the film while it was situated in between the poles of the electromagnet. However, as the film was clamped on the rotating plate therefore by heating the rotating plate radiatively by the substrate heater, the film in turn was heated conductively. This method of heating was inefficient and slow. Seven films were heated to 50-60°C using this method and the changes in  $R_H$  and  $\rho$  were monitored while the films were exposed to H. In Fig. 4.9, results for two air-exposed p-type films are shown. Film S25 has been discussed previously. Film S36 was grown at 175°C and its thickness was 2900 Å.

In the case of film S25, during the initial pump-down,  $R_H$  and  $\rho$  increased along path A → B. At this point, the substrate heater was switched on and the temperature of the film was monitored by an iron-constantan thermocouple. As the film was being heated, path B → C was traced where both  $R_H$  and  $\rho$  decreased. At C, the temperature of the film stabilised at 50°C and the H cycle

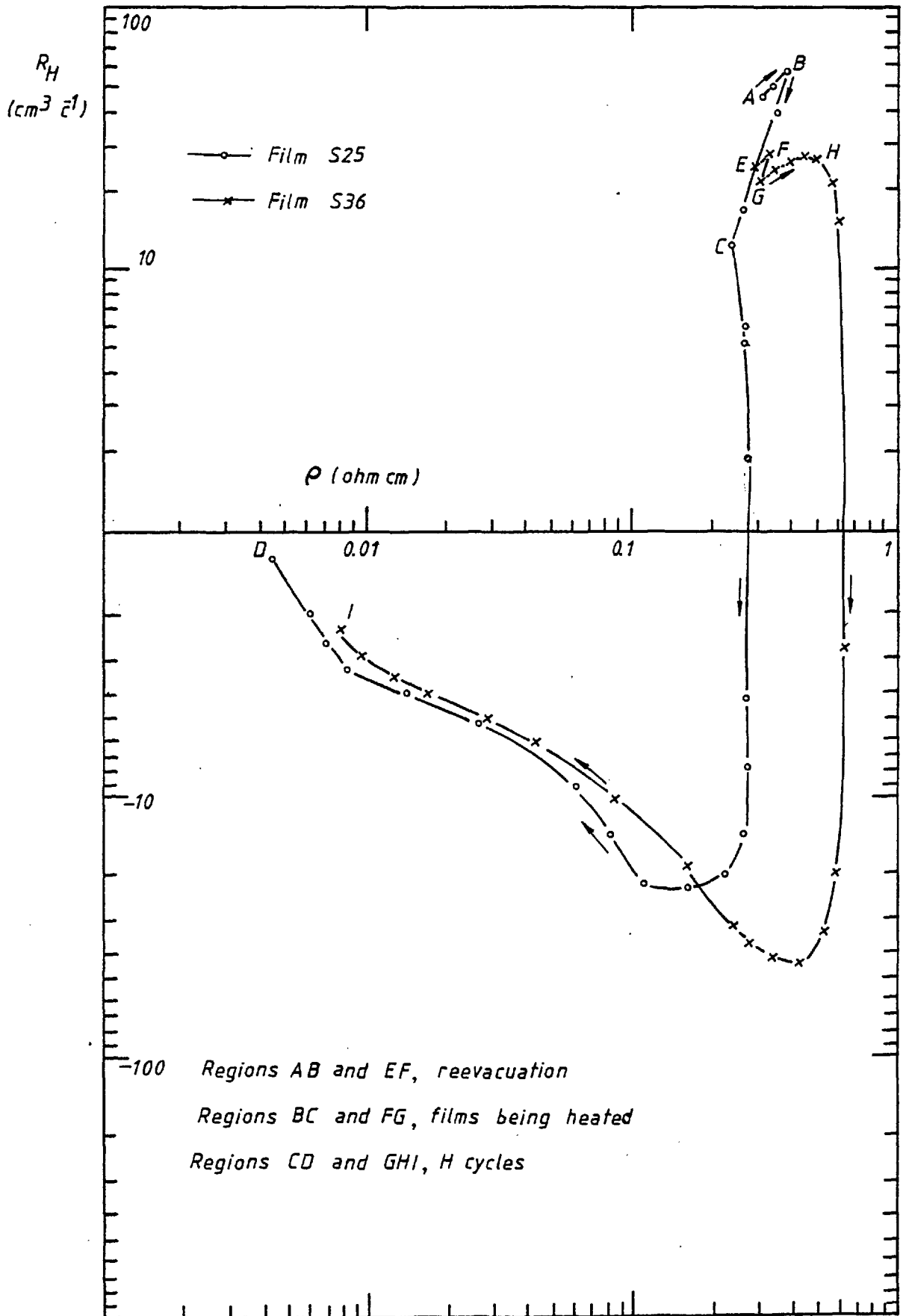


Fig.4.9 H effect at 50°C

was commenced. During the H cycle, the film turned n-type in 9 mins and path C → D was traversed in a clockwise manner. For film S36, path E → F was traced during re-evacuation, path F → G was traced during the period when the film was being heated and path G → H → I was traced during the H exposure. Film S36 was driven n-type in 21 mins.

It may be noted that the curves shown in Figs. 4.1 through to Fig. 4.9 are drawn to be smooth and continuous and are not the best-fit curves.

#### 4.4 THEORETICAL MODELS

In this section, two major theoretical models will be proposed to analyse the results described in the previous section, namely the surface model (planar form and three-dimensional form) and the diffusion model. Both of these models have been used by other workers (E2, H1, B2) with a varying degree of success to explain the gaseous effects of epitaxial films of PbTe and  $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$  alloy.

Brodsky and Zemel (B3), in order to explain the changes in  $R_H$  vs  $\rho$  curves for epitaxial PbSe films deposited on NaCl, initially suggested that the existence of the space charge region on the surface of the semiconductor was influencing the transport properties of such films, i.e. the surface model. This surface model will now be examined in detail.

#### 4.4.1 Surface Model (planar form)

Poisson's equation has been used extensively in the past to relate the variation of the electric field to the charge density especially in the study of p-n junctions (M4), but one can also use this equation to formulate the problem of the surface space charge on a semiconductor. It is intended here to develop expressions for  $R_H$  and  $\rho$  for extrinsic and intrinsic semiconductor-bulks in the presence of surface space charge. For a semi-infinite, homogeneous material under thermal equilibrium the electrostatic potential  $V$  can be expressed by Poisson's equation (M4) as follows,

$$\frac{d^2V}{dx^2} = - \frac{\rho}{\epsilon} \quad (4.1)$$

where

$V$  is a function of  $x$  only

$\rho$  is the charge density

$\epsilon$  is the dielectric constant of the material

$x$  is the distance from the surface of

the semiconductor ( $x = 0$ )

The space charge region shown in Fig. 4.10 can be classified according to the relative values of the carrier concentrations at the surface. If the bulk majority carrier is still in the majority at the surface, the space charge region can either be an accumulation or depletion region depending on whether the concentration of this carrier is being increased or decreased. If



the minority bulk carrier is in the majority at the surface, then it is called the inversion region (F1).

The charge density,  $\rho$  in equation (4.1) consists of static charge (negative and positive) and charge due to mobile electrons and holes. For a fully ionised p-type semiconductor,

$$\rho = q(p(x) - n(x) - N_a) \quad (4.2)$$

where  $p(x)$  and  $n(x)$  are the hole and electron concentrations respectively at distance  $x$  from the surface.  $N_a$  is the fixed acceptor density. Using the reduced potential notation of (M4), equation (4.1) can be rewritten as,

$$\frac{d^2 v}{dx^2} = - \frac{q^2}{\epsilon kT} (p(x) - n(x) - N_a) \quad (4.3)$$

where

$$v = \frac{qV}{kT} \quad (4.4)$$

$k$  is Boltzmann's constant

$q$  is the electronic charge

$T$  is the temperature

Multiplying equation (4.3) by  $dv/dx$  and integrating from the bulk (i.e.  $v = 0$  and  $dv/dx = 0$ ) to the point where the band-bending is  $v$ ,

$$\left(\frac{dv}{dx}\right)^2 = - \frac{2q^2}{\epsilon kT} \int_{v=0}^v (p(v) - n(v) - N_a) dv \quad (4.5)$$

If  $n_b$  and  $p_b$  are the bulk electron and hole concentrations respectively, one can define the effective Debye length as,

$$L_D^2 = \frac{\epsilon kT}{q^2(n_b + p_b)} \quad (4.6)$$

From equations (4.5) and (4.6)

$$\frac{dv}{dx} = \pm \frac{\sqrt{2}}{L_D} \left[ \int_{v=0}^v \frac{(-p(v)+n(v)+Na) dv}{(n_b+p_b)} \right]^{\frac{1}{2}} \quad (4.7)$$

Defining a surface function  $F(v)$  as,

$$F(v) = \sqrt{2} \left[ \int_0^v \frac{(-p(v)+n(v)+Na) dv}{(n_b+p_b)} \right]^{\frac{1}{2}} \quad (4.8)$$

Therefore equation (4.7) becomes,

$$\frac{dv}{dx} = \pm \frac{F(v)}{L_D} \quad (4.9)$$

In equation (4.9), the sign is positive when  $v > 0$ , i.e. band-bending is downwards (as in Fig. 4.10) and the sign is negative when  $v < 0$  (band-bending upwards).

In order to evaluate  $F(v)$ , expressions for  $n(v)$  and  $p(v)$  must be developed. This can be done as follows.

In general, total electron concentration in the bulk of a semiconductor can be written as (B5),

$$n = \int_{-\infty}^{\infty} g_c(E) F(E) dE \quad (4.10)$$

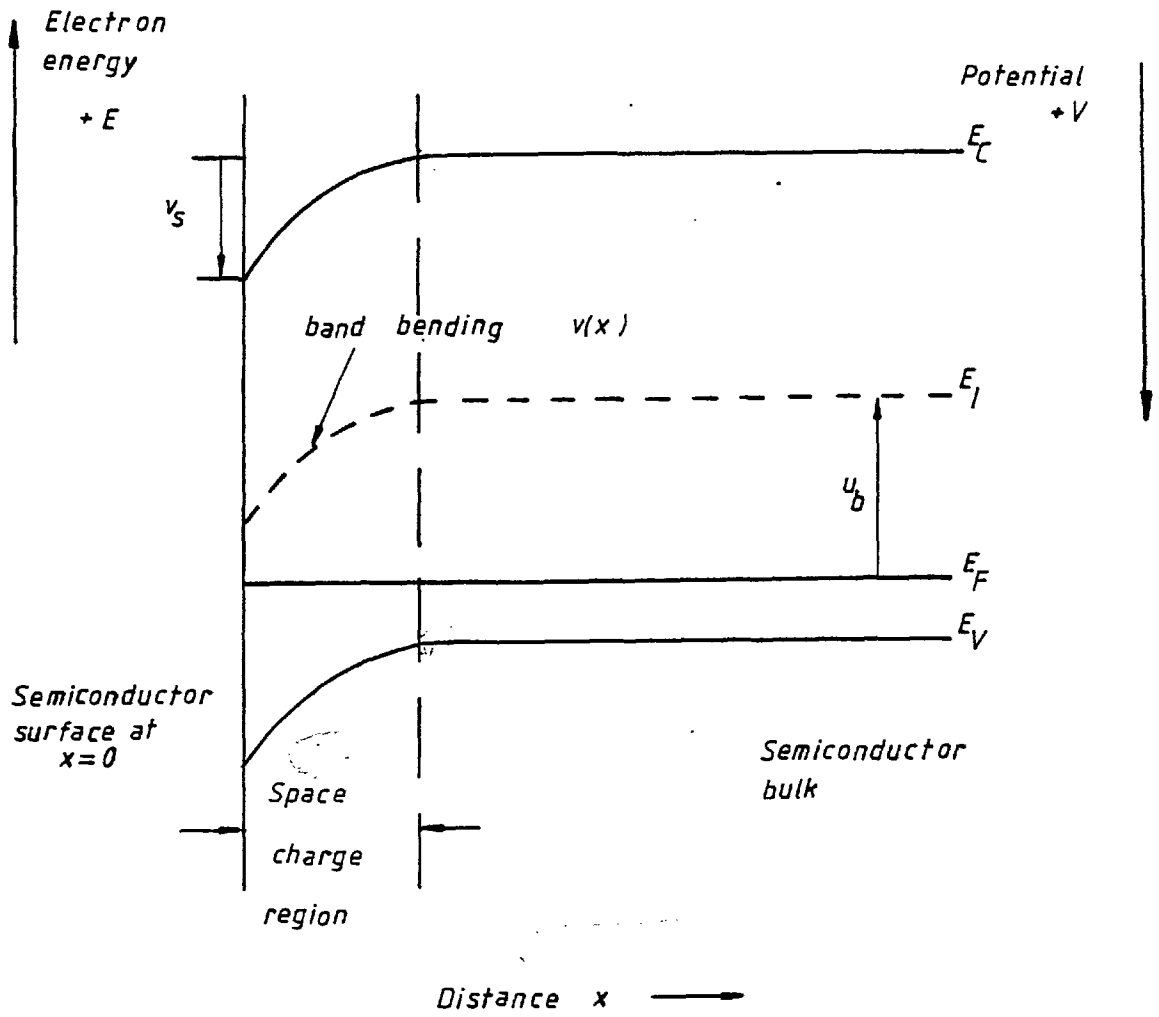


Fig.4.10 Depleted p-type semiconductor

where  $g_c(E)$  is the density of states function for the conduction band and  $F(E)$  is the Fermi-Dirac function expressing the probability of an energy level  $E$  being occupied by an electron under equilibrium.

$$F(E) = \frac{1}{1 + \exp\left(\frac{E-E_F}{kT}\right)} \quad (4.11)$$

Using equations (4.10) and (4.11), electron concentration can be evaluated at a point in a semiconductor where the band-bending is  $v$ .

$$n(v) = \int_0^\infty \frac{g_c(\epsilon) d\epsilon}{1 + G \exp(\epsilon - \epsilon_F - v)} \quad (4.12)$$

where

$$(i) \quad \epsilon - \epsilon_F = \frac{E-E_F}{kT}, \quad d\epsilon = \frac{dE}{kT} \quad (4.13)$$

(ii)  $G$  is the degeneracy factor

(iii) lower limit of integration has been taken at the edge of the conduction band

Similarly for holes,

$$p(v) = \int_0^\infty \frac{g_v(\epsilon) d\epsilon}{1 + G \exp(\epsilon + \epsilon_F + v + \epsilon_g)} \quad (4.14)$$

where  $g_v(\epsilon)$  is the density of states function for the valence band and  $\epsilon_g = E_g/kT$ , the forbidden energy gap. Generally in  $k$ -space density of states per unit volume

(including the two possibilities for electron spin)  
is given by,

$$g(E) dE = \frac{2}{(2\pi)^3} \int d^3 \underline{k} \quad (4.15)$$

The density of states functions for non-parabolic bands and spherical energy surfaces given by Juhasz (J3) were used to evaluate equations (4.12) and (4.14). (These functions have been given in Chapter 1, equations (1.13) and (1.14).) The position of the Fermi level can be determined from the charge neutrality condition in the bulk as follows,

$$p(v) - n(v) - Na = 0 \quad (4.16)$$

In the space charge region, the excess electrons  $\Delta N$  and excess holes  $\Delta P$  with respect to their concentration in the bulk, can be defined as follows,

$$\Delta N = \int_0^\infty (n(x) - n_b) dx \quad (4.17)$$

and

$$\Delta P = \int_0^\infty (p(x) - p_b) dx \quad (4.18)$$

From equations (4.9), (4.17) and (4.18),

$$\Delta N = L_D \int_{v_s}^0 \frac{(n(v) - n_b) dv}{F(v)} \quad (4.19)$$

$$\Delta P = L_D \int_{v_s}^0 \frac{(p(v) - p_b) dv}{F(v)} \quad (4.20)$$

where  $v = v_s$  at  $x = 0$  and at  $x \rightarrow \infty$ ,  $v = 0$  (flat-bands). It may be noted that for  $v_s > 0$ ,  $\Delta N$  is positive and  $\Delta P$  is negative and the converse is true for  $v_s < 0$ . From (Z4), for a semiconductor of thickness  $d$ ,

$$\sigma d = \sigma_b d + q(\mu_{ns} \Delta N + \mu_{ps} \Delta P) \quad (4.21)$$

and

$$R_H \sigma^2 d = R_b \sigma_b^2 d + q(\mu_{ps}^2 \Delta P - \mu_{ns}^2 \Delta N) \quad (4.22)$$

where

- (i)  $\sigma$  is the conductivity =  $\rho^{-1}$
- (ii) subscripts b and s refer to bulk and surface respectively
- (iii)  $\mu_{ns}$  and  $\mu_{ps}$  are the electron and hole mobilities respectively at the surface

A computer program developed by Juhasz (J3) was used to evaluate  $R_H$  and  $\rho$  for various assumed values of the surface potential  $v_s$ . Firstly, the program evaluates the bulk parameters  $n_b$ ,  $p_b$ ,  $\epsilon_F$ ,  $\epsilon_{Fi}$ ,  $\dot{U}_b$  etc. and secondly  $F(v)$  is calculated. Once  $F(v)$  is known  $\Delta N$  and  $\Delta P$  can be calculated from equations (4.19) and (4.20). Using these calculated values of  $\Delta N$  and  $\Delta P$  in equations (4.21) and (4.22),  $\sigma d$  and  $R_H \sigma^2 d$  can be evaluated. Finally,  $\rho$  and  $R_H$  can be determined since the film thickness,  $d$  is known. The program requires  $E_g$ ,  $m_e$ ,  $m_h$ ,  $E_c$ ,  $E_v$ ,  $N_a$ ,  $N_d$ , dielectric (static) constant,  $T$ ,  $\mu_{ns}$ ,  $\mu_{ps}$ ,

film thickness and the limits of the surface potential  $v_s$  as the input data.

Data taken from film S25 (considered to be typical) was used to compare the theoretical  $R_H$  vs  $\rho$  curve predicted by the computer program with the experimental curve for the second H cycle. Brodsky and Zemel (B3) showed that for PbSe films, surface scattering was specular and assuming the same to be true for PbTe films,  $\mu_s = \mu_b$  was used. The values of  $\mu_p$  and  $\mu_n$  were deduced from the slopes of the linear parts of the  $R_H$  vs  $\rho$  curve when the film was considered to be in the single carrier region. Since the film was p-type,  $N_d$  was assumed to be zero and  $N_a$  was given by  $1/R_H e$ . The values of  $E_g$ ,  $m_h$ ,  $m_e$  and static dielectric constant were 0.31 eV, 0.29  $m_0$ , 0.24  $m_0$  and 425 respectively and these values were taken from (E1, B2, Z1). Values of  $\mu_p$  and  $\mu_n$  were 114  $\text{cm}^2/\text{V-sec}$  and 456  $\text{cm}^2/\text{V-sec}$  respectively and  $N_a = 3.7 \times 10^{17} \text{ cm}^{-3}$ . The thickness of the film was 2038  $\text{\AA}$  and T was the room temperature, 300 $^\circ\text{K}$ . Fig. 4.11 shows the two curves.

#### 4.4.1.1 $R_H$ and $\rho$ expressions for intrinsic bulk (planar form)

Since 'virgin' p-type films (typified by S29) and some of the 'virgin' n-type films had carrier concentration at room temperature comparable to the intrinsic bulk, expressions for  $R_H$  and  $\rho$  were developed for intrinsic bulk in the presence of surface space charge region in order to compare the theoretical and experimental data. Unlike the extrinsic bulk case, Poisson's equation for the

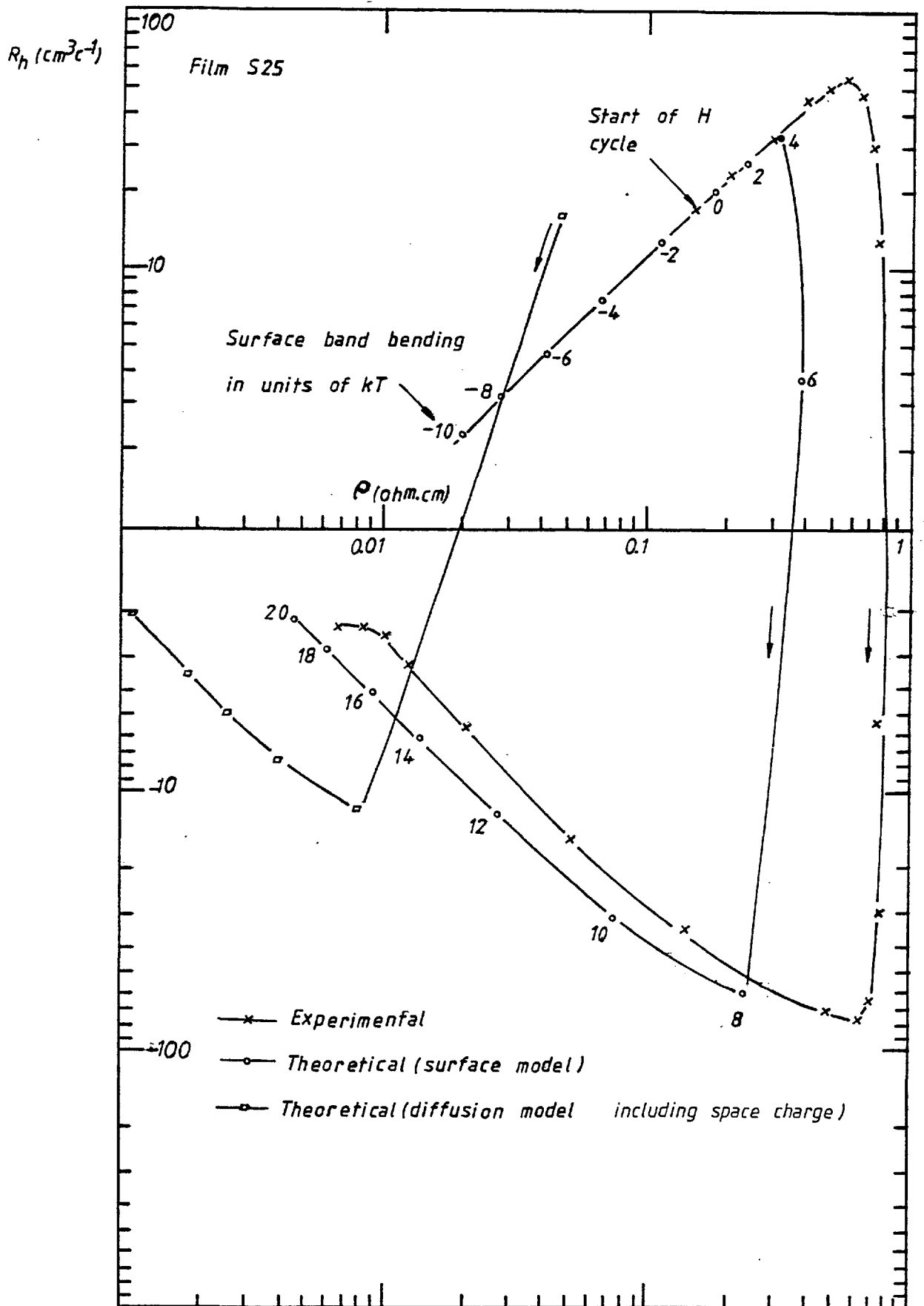


Fig.4.11 H cycle on  $\text{O}_2$  driven p-type film



intrinsic bulk can be solved analytically. This is detailed in Appendix A. From Appendix A,

$$\sigma = \rho^{-1} = \frac{I_1 + I_2}{d} \quad (4.23)$$

and

$$R_H = d \frac{(\mu_p I_2 - \mu_n I_1)}{(I_1 + I_2)} \quad (4.24)$$

where integrals  $I_1$  and  $I_2$  are functions of  $v_s$ , the band-bending at the surface and  $d$  is the thickness of the film. When  $\mu_p I_2 > \mu_n I_1$ , the film is p-type and when  $\mu_p I_2 < \mu_n I_1$  the film is n-type.

For the sake of completeness, expressions for excess electrons and holes are also given where,

$$\Delta N = 2n_b L \left( \exp\left(\frac{v_s}{2}\right) - 1 \right) \quad (4.25)$$

$$\Delta P = 2p_b L \left( \exp\left(-\frac{v_s}{2}\right) - 1 \right) \quad (4.26)$$

where the symbols have their usual meaning. In equation (4.25), when  $v_s > 0$  (i.e. positive band-bending as in Fig. 4.10),  $\exp v_s/2 > 1$  and  $\Delta N$  is positive whereas in equation (4.26)  $\exp -v_s/2 < 1$  for  $v_s > 0$  and  $\Delta P$  is negative. The converse is true when  $v_s < 0$  (upwards band-bending).

The model was tested on film S29 for the first H cycle. Fig. 4.12 shows the  $R_H$  vs  $\rho$  curve predicted by equations (4.23) and (4.24) and the experimental curve.

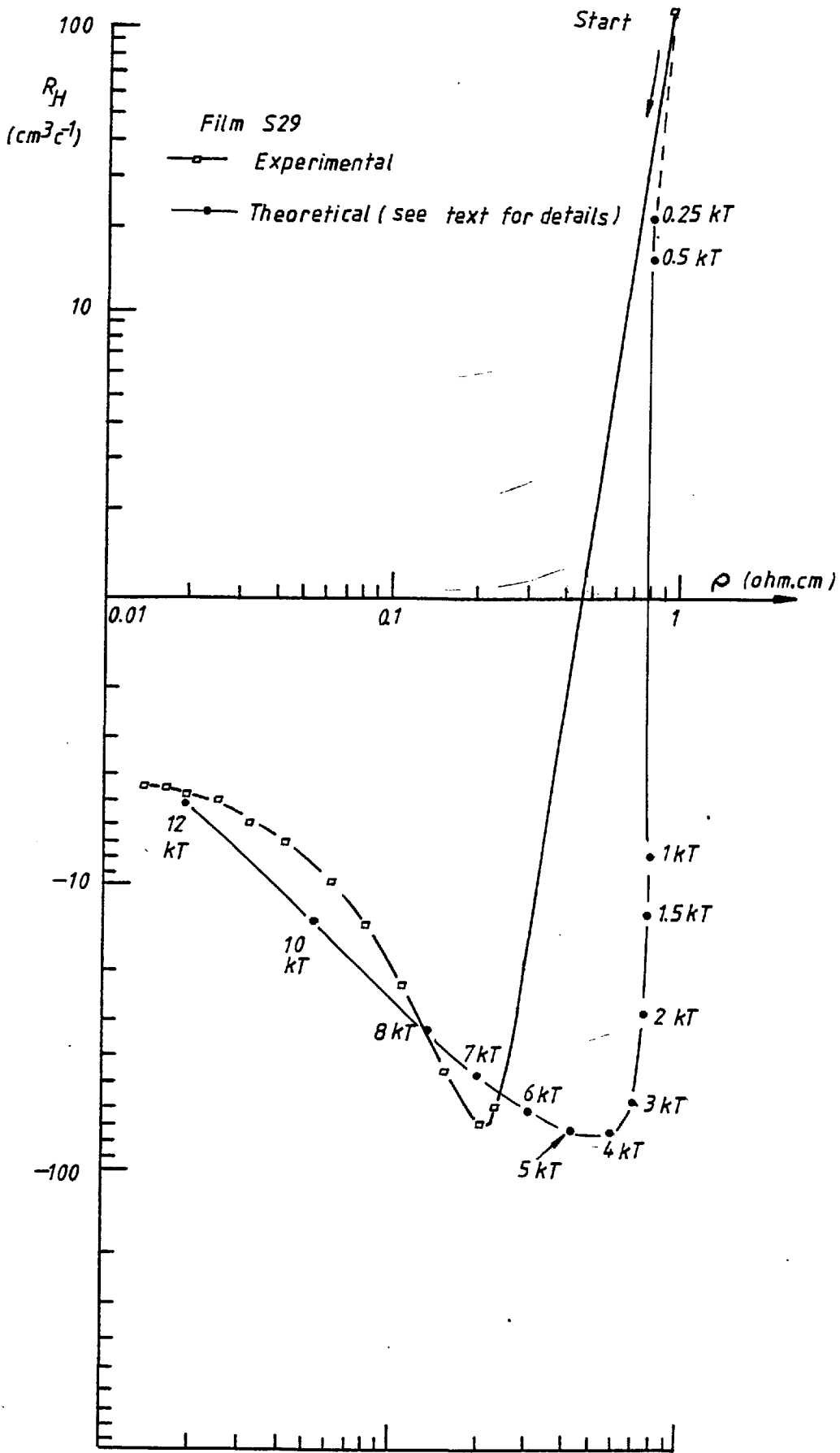


Fig. 4.12 1st H cycle on a 'virgin' p-type film

As seen from Fig. 4.12, the model appears to predict a satisfactory <sup>shape</sup>  $\wedge$  to the experimental curve even though it has the following limitations,

- (i) the model does not predict the flat-band behaviour because  $v_s \neq 0$  when evaluating  $I_1$  and  $I_2$ , although  $v_s$  can be negative or positive,
- (ii) mobility  $\mu$  was assumed to be independent of  $x$ ,
- (iii) in an intrinsic-like film it was assumed that the carrier mobility is given by the Hall mobility.

#### 4.4.1.2 Three-dimensional surface model

Greene et al (G6) point out that when solving Poisson's equation in planar form, the spatial fluctuations in the potential are not taken into account because a uniform sheet charge is used instead of a more realistic array of point charges at the surface. In order to take into account the spatial fluctuations in the potential, they present a three-dimensional formulation of Poisson's equation for a non-degenerate electron gas with an array of localised charges on or near the semiconductor surface. The main points of relevance of their paper are presented below.

If an array of point charges described by delta function on the surface of the semiconductor is giving rise to potential  $V(x,y,z)$  then Poisson's equation can be written as,

$$\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} = \frac{q^2 n_b}{\epsilon kT} (\exp v - 1), \quad z > 0 \quad (4.27)$$

and

$$\frac{\partial^2 v}{\partial x^2} + \frac{\partial^2 v}{\partial y^2} + \frac{\partial^2 v}{\partial z^2} = 0 \quad z < 0 \quad (4.28)$$

where

(i) semiconductor surface is at  $z = 0$

$$(ii) \quad v = q \frac{V(x,y,z)}{kT} \quad (4.29)$$

(iii)  $\epsilon =$  dielectric constant

Defining

$$L^{-2} = \frac{q^2 n_b}{\epsilon kT} \quad (4.30)$$

equations (4.27) and (4.28) can be rewritten as,

$$\nabla^2 v = \frac{1}{L^2} (e^v - 1) \quad z > 0 \quad (4.31)$$

$$\nabla^2 v = 0 \quad z < 0 \quad (4.32)$$

Defining a correction term to the planar band-bending  $v_p$  as

$$\delta v(x,y,z) = v(x,y,z) - v_p \quad (4.33)$$

equation (4.31) can then be rewritten in terms of the correction band-bending and planar band-bending as follows,

$$\nabla^2 \delta v = \frac{1}{L^2} e^{v_p} (e^{\delta v} - 1) \quad (4.34)$$

Greene et al (G6) have shown that the correction term in equation (4.33) is always negative including at the surface ( $z = 0$ ). In other words, for the same space charge density, the band-bending in the three-dimensional case is lower than that for the planar case. Commenting further on the inadequacies of the one-dimensional model, Levine (L6) observed that if the surface state density in an accumulation layer is greater than  $3 \times 10^{11} \text{ cm}^{-2}$  (dielectric constant 5) then the planar potential seriously underestimates the amount of space charge possible. However, one may pose the question that in the context of  $R_H$  vs  $\rho$  curves, how does the choice between planar model and three-dimensional model influence,

- (i) the shape of the  $R_H$  vs  $\rho$  curve, and
- (ii) the magnitudes of  $R_H$  and  $\rho$ ?

Hing (H1) developed an expression for a general function  $F_g(v)$  (similar to the one defined by equation (4.8)) for different geometries of the band-bending and noted that

the shape of the band-bending merely modified the surface function defined by equation (4.8) by a constant of proportionality and since  $F_g(v)$  did not alter the shape of  $R_H$  vs  $\rho$  curve, only the magnitudes of  $R_H$  and  $\rho$  would be affected. In other words, for corresponding values of  $R_H$  and  $\rho$  in the two cases, the band-bending in the case of the three-dimensional model will be smaller than that for the one-dimensional case, although the shape of  $R_H$  vs  $\rho$  curve will be similar for both cases.

#### 4.4.2 Diffusion Model

Egerton and Juhasz (E2) first expressed their dissatisfaction with the surface model when explaining the long-term irreversible effect of  $O_2$  on n-type PbTe films grown on mica and they offered the diffusion model as an alternative. The proposed model for  $O_2$  uptake is schematically shown in Fig. 4.13. However, no mathematical formulation of the model was given by them. The diffusion model will now be examined.

As mentioned in the previous section, in the case of the surface model, the formation of the surface space charge region resulted in band-bending and the gas remained on the surface. In the case of diffusion, a shallow space charge region created during the initial stages of gas uptake penetrates further into the film as time goes on and eventually the gas enters into the bulk of the film where the driving force for diffusion of gas is the concentration gradient. Therefore in both

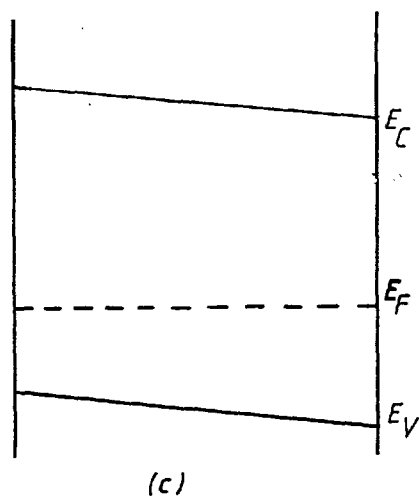
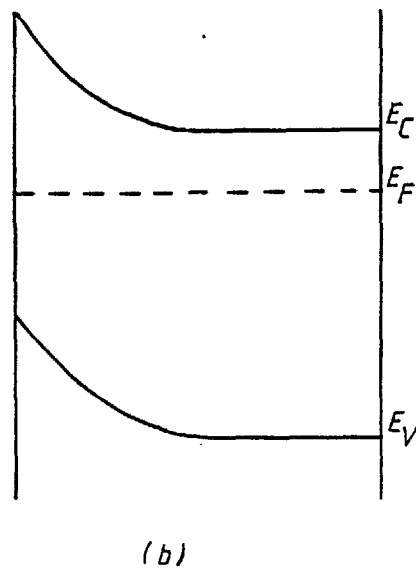
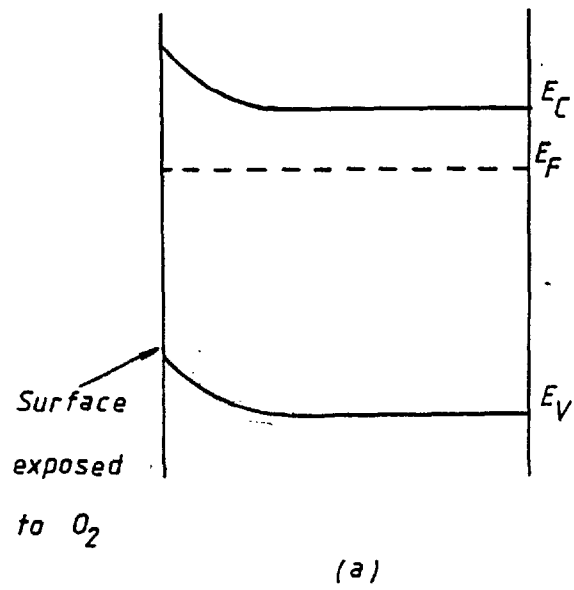


Fig.4.13 Band bending due to  $O_2$  effect on an n-type film after Egerton and Juhasz (E2), Progressive oxidation.

cases, there is band-bending at the surface. The diffusion model will now be described qualitatively taking the H effect on a p-type film as an example.

Due to the concentration gradient, H diffuses into the p-type film and acting as a donor neutralises the charge carriers (holes) near the surface giving rise to band-bending at the surface as shown schematically in Fig. 4.14(a). As the diffusion proceeds, H drives the surface of film n-type and the space charge region moves deeper into the p-type film. As the H exposure is continued, the n-type surface grows and penetrates further into the p-type bulk. In other words, the p-type bulk becomes separated from the n-type region by a space charge region as shown schematically in Fig. 4.14(b). This is effectively an advancing p-n junction within the film (J4). Eventually, the film is driven n-type (Fig. 4.14(c)). Therefore, the film which is initially p-type single carrier (Fig. 4.14(a)) becomes a two carrier film (Fig. 4.14(b)) before becoming a single carrier n-type film (Fig. 4.14(c)).

A quantitative description of the diffusion model will now be detailed below.

One may use Fick's Laws to describe a unidirectional diffusion process, i.e.

$$F = -D \frac{dC}{dx} \quad (4.35)$$

and

$$\frac{dC}{dt} = D \frac{d^2C}{dx^2} \quad (4.36)$$



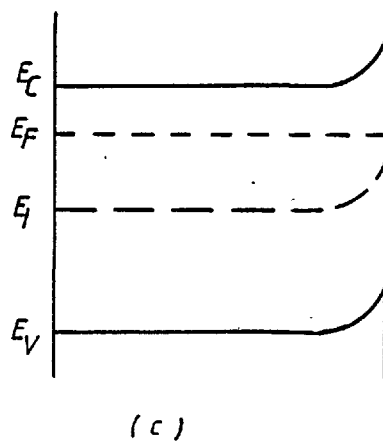
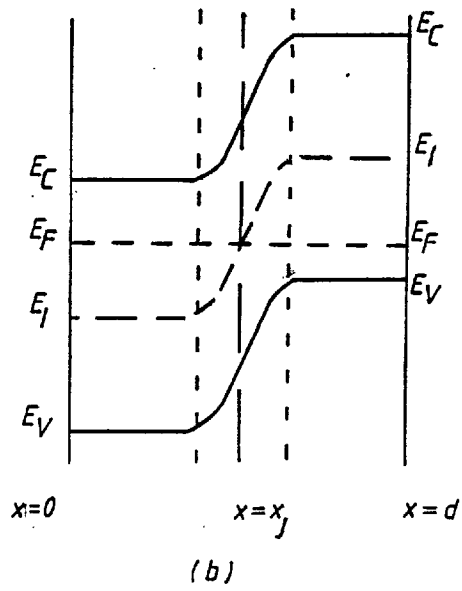
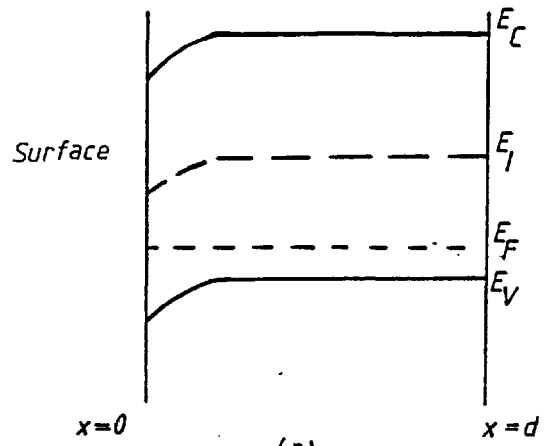


Fig.4.14 H effect on a p-type film (schematic and idealised)

where

- (i) F is the rate of transfer of the diffusant per unit area,
- (ii) C is the concentration of the diffusing species,
- (iii) D is the constant diffusion coefficient of the diffusant,
- (iv) t is the time,
- (v) x is the space coordinates along which diffusion is taking place.

The profiles of the diffusing species can be obtained by solving equation (4.36). Crank (C5) has given solutions of equation (4.36) for various practical situations subject to various boundary conditions. In the present case, shown schematically in Fig. 4.15, a film of thickness d is placed in an ambient with constant concentration  $C_1$ . Assuming that the initial concentration of the diffusant in the film is zero then the concentration C after time t at distance x within the film is given by (C5),

$$\frac{C}{C_1} = 1 - \frac{4}{\pi} \sum_{n=0}^{\infty} \frac{(-1)^n}{(2n+1)} \exp\left[-D \frac{(2n+1)^2 \pi^2 t}{4d^2}\right] \cos \frac{(2n+1)\pi x}{2d} \quad (4.37)$$

where n is an integer. Equation (4.37) is plotted (C5) as a function of x and d for various times in Fig. 4.16. Equation (4.37) is rather awkward to handle when, for

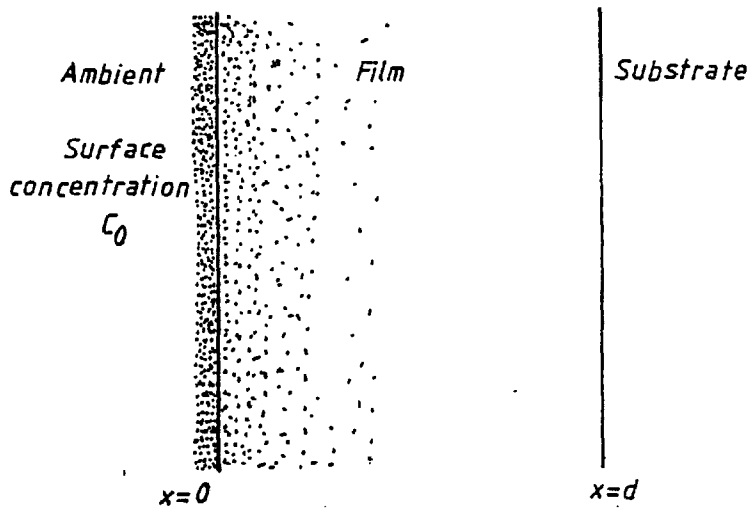


Fig.4.15 Diffusion Model

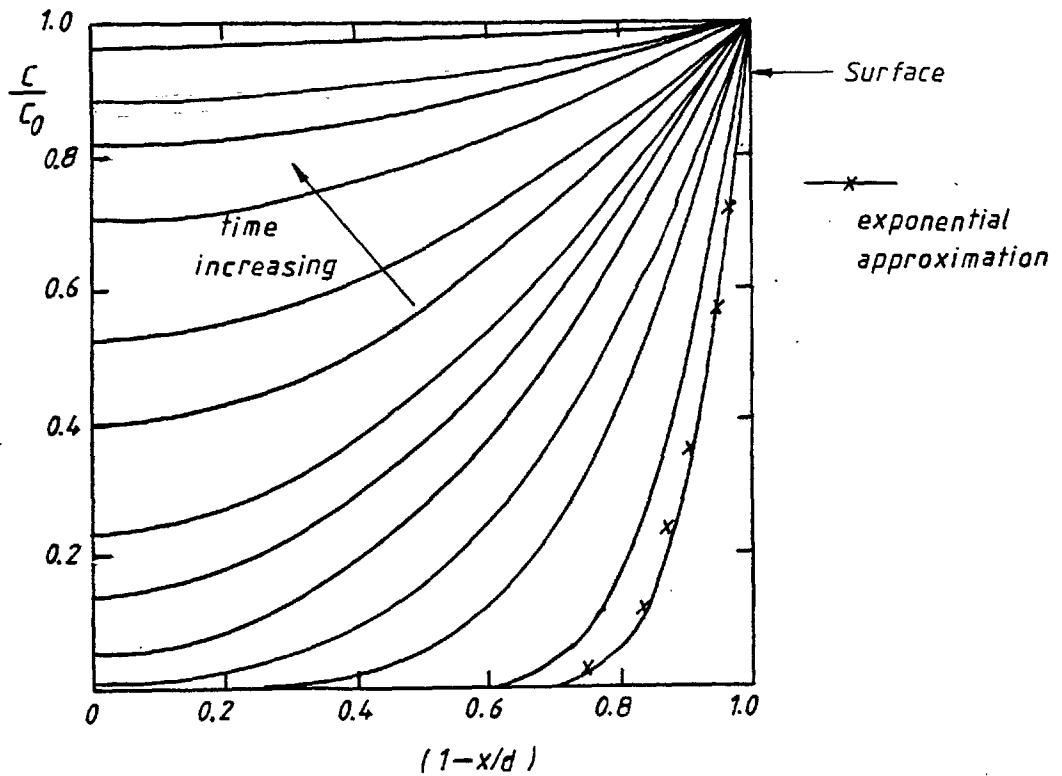


Fig.4.16 Diffusion profile across the film after Crank (C5)

instance, developing expressions for  $R_H$  and  $\rho$ . Therefore it is desirable to simplify this equation or use a simpler approximation to it. An exponential approximation given by equation (4.38) <sup>was found to agree with</sup> equation (4.37)\*.

$$C(x) = C_0 \exp - \frac{x}{\ell} \quad (4.38)$$

where  $\ell = 2\sqrt{Dt}$  and  $C_0$  is the surface concentration. Equation (4.38) is also plotted in Fig. 4.16 for comparison and as it can be seen, the approximation holds good especially for small times. Therefore equation (4.38) was used in the subsequent calculations.

The diffusion model will be considered in two parts. In the first part, single carrier films will be treated and the second part will deal with the two carrier films.

#### 4.4.2.1 Single carrier films

In this sub-section, H effect on a p-type film ( $p \gg n_i$ ) will be considered as an example. Expressions for  $R_H$  and  $\rho$  will be developed. The theoretical curve of  $R_H$  vs  $\rho$  will be compared with the experimental  $R_H$  vs  $\rho$  curve of film S25.

As explained previously, the profile of the diffusing donors can be described by an exponential, i.e.

$$N_d(x) = N_0 \exp - \frac{x}{\ell} \quad (4.39)$$

---

\* Error function approximation is more appropriate.

for a particular value of  $\ell = 2\sqrt{Dt}$  where  $N_0$  is the surface concentration. The following assumptions are made.

- (i) All impurities are fully ionised.
- (ii) The acceptor carrier concentration  $N_a$  is homogeneously distributed throughout the film, i.e.  $N_a(x) = N_a$ .
- (iii) The minority carrier concentration is negligible.

Since, in the present case, donors are diffusing into a p-type film the surface will be depleted of the charge carriers and the band-bending will be positive (i.e. downwards) - see Fig. 4.14(a).

$$\text{Charge density } \rho(x) = q(N_d(x) - N_a(x)) \quad (4.40)$$

or

$$\rho(x) = qN_0 \left[ \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_0} \right] \quad (4.41)$$

In order to develop expressions for  $R_H$  and  $\rho$ , an expression for band-bending  $v(x)$  must be found for a particular value of  $\ell$ . To do this, one may solve Poisson's equation. In the planar form Poisson's equation is,

$$\frac{d^2v}{dx^2} = - \frac{q\rho}{\epsilon kT} \quad (4.42)$$

where all the symbols have their usual meanings. From equations (4.41) and (4.42)

$$\frac{d^2v}{dx^2} = - \frac{1}{L_D^2} \left[ \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_0} \right] \quad (4.43)$$

where

$$L_D = \left( \frac{\epsilon k T}{q^2 N_0} \right)^{\frac{1}{2}} \quad \epsilon = \epsilon_0 \epsilon_r \quad (4.44)$$

Equation (4.43) is solved in Appendix B.

From Appendix B,

$$v(x_j) = v(0) \pm A \left( \frac{x_j}{L_D} \right)^2 \quad (4.45)$$

where sign of A depends on the values of  $N_a$  and  $N_0$ .

Since  $v(0) = v_s =$  surface band-bending

$$\therefore v(x_j) = v_s \pm A \left( \frac{x_j}{L_D} \right)^2 \quad (4.46)$$

For a non-degenerate p-type semiconductor, carrier concentration at any point is given by (M4),

$$p = p_b \exp[-v(x)] \quad (4.47)$$

or

$$p = N_a \exp[-v(x_j)] \quad (4.48)$$

Since the film is considered to be single carrier type,

$$\therefore \rho^{-1} = \sigma = e \mu_p p \quad (4.49)$$

and

$$R_H = \frac{1}{ep} \quad (4.50)$$

for particular values of  $l$  and  $v_s$ .

Therefore, by adjusting  $\ell$  and  $v_s$  a best fit curve of  $R_H$  vs  $\rho$  can be obtained. This has been done for film S25. Reasonable values of  $\ell$  can be estimated provided that H diffusion coefficient,  $D_H$  in PbTe films at room temperature is known. The method adopted to evaluate  $\ell$  will now be described.

Young (Y2) gives the following relationship for H diffusion coefficient,  $D_H$  in PbSe epitaxial films.

$$D_H = D_0 \exp - \frac{E}{kT} \quad (4.51)$$

where

$E$  is the activation energy for diffusion

$D_0$  is a constant (determined experimentally to be  $1.1 \times 10^{-7} \text{ cm}^2 \text{ s}^{-1}$ )

Egerton and Crocker (E4) estimated  $D_H$  in PbTe epitaxial films to be  $\sim 10^{-11} \text{ cm}^2 \text{ s}^{-1}$  at  $170^\circ\text{C}$ . Using  $D_H$  given by (E4) and  $D_0$  given by (Y2),  $E$  was estimated at  $170^\circ\text{C}$ . Using this value of  $E$  and  $D_0$  given by (Y2) in equation (4.51),  $D_H$  was evaluated at room temperature. This was found to be  $\sim 6 \times 10^{-14} \text{ cm}^2 \text{ s}^{-1}$ . The values of  $\ell$  could now be found since both  $D_H$  and  $t$  were known. For each estimated value of  $\ell$ ,  $v_s$  was adjusted to give the best fit curve. However, for a film to remain in the single carrier region,  $v_s < E_g$  (band gap) was used as a constraint on the values of  $v_s$ . The value of  $N_0$ , the surface concentration of H, was determined in the following way.

When the film has been saturated with H, this is equivalent to the diffusion condition for  $t \rightarrow \infty$  and  $N_d(x) = N_o$  (equation (4.39)). But the saturated donor concentration is determined from the measured Hall coefficient which also includes the concentration of donors neutralised by the initial acceptor concentration.

$$\therefore N_o = N_a + N_\infty \quad (4.52)$$

where  $N_\infty$  is the 'saturation' value. The experimental and theoretical curves of  $R_H$  vs  $\rho$  of film S25 for second H cycle are shown in Fig. 4.17. The value of  $N_a$  prior to the H cycle was  $3.7 \times 10^{17} \text{ cm}^{-3}$  and  $N_o$  was equal to  $2.87 \times 10^{18} \text{ cm}^{-3}$ .  $\mu_p$  was determined from the slope of the linear (single carrier regime) region of the experimental curve and was found to be  $114 \text{ cm}^2/\text{V-sec}$ . The values of  $v_s$  for the best fit curve are also shown in Fig. 4.17.

#### 4.4.2.2 Two carrier films

In the present context, the films are considered to be in two carrier region if the carrier concentration determined by the Hall coefficient is low and comparable to the intrinsic carrier concentration.



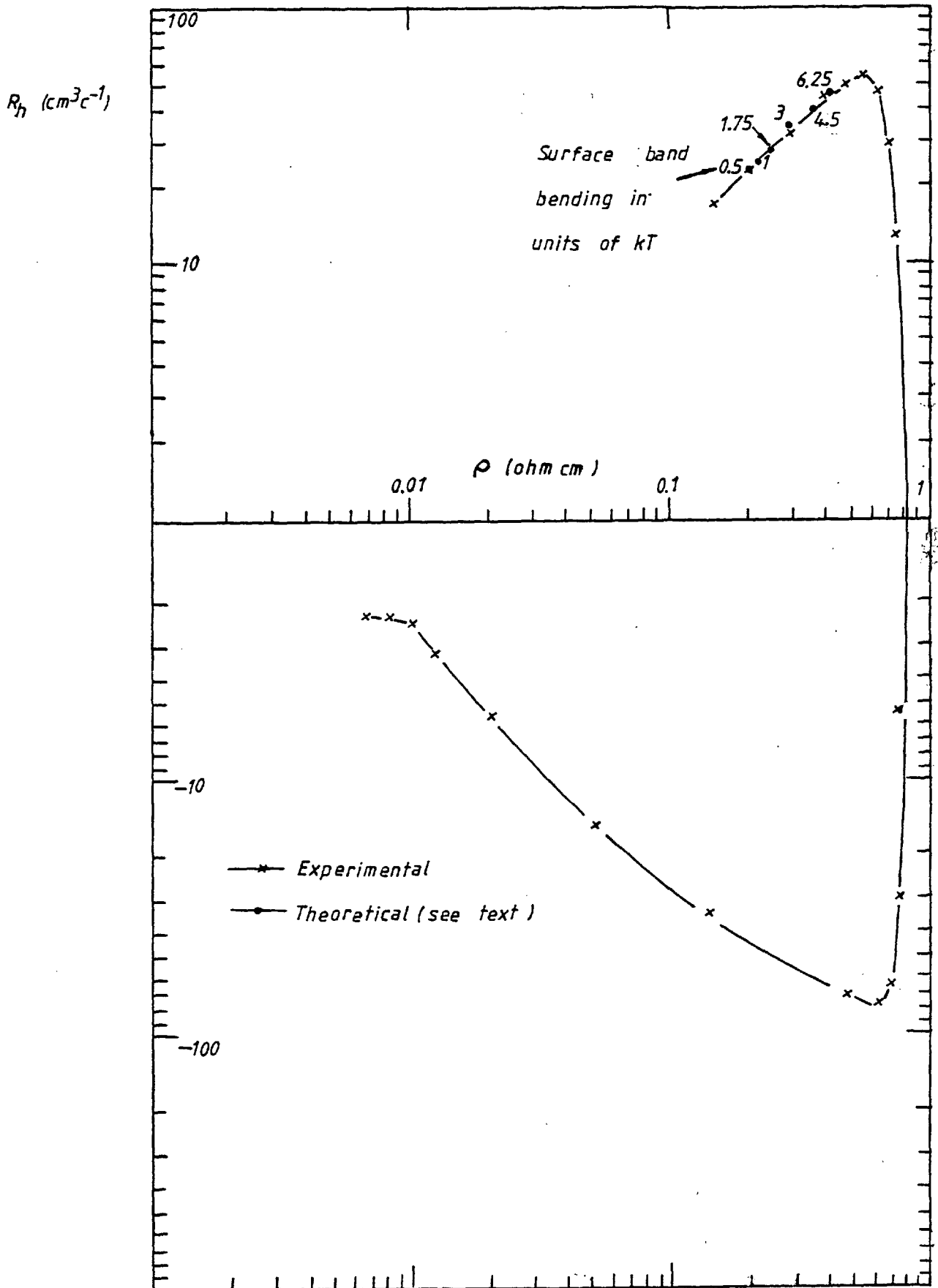


Fig. 4.17 2nd H cycle on film S25

#### 4.4.2.2(a) Two-layer model

This model was proposed by McLane and Zemel (M2) and is shown in Fig. 4.18(a). They proposed that the film consists of a surface layer of thickness  $d_s$  and bulk of thickness  $d_b$  where the surface layer and the bulk are characterised in terms of  $R_H$ ,  $\mu$  and  $\sigma$ . Using Petritz's model (P9),

$$\sigma d = \sigma_b d_b + \sigma_s d_s \quad (4.53)$$

$$= q(C_b \mu_b d_b + C_s \mu_s d_s) \quad (4.54)$$

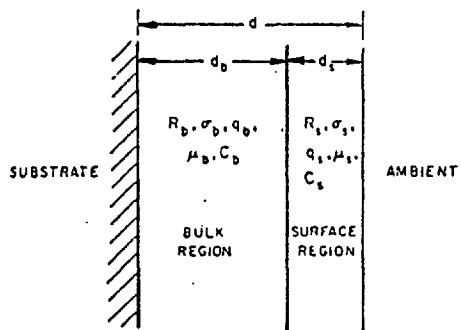
and

$$R_H \sigma^2 d = R_b \sigma_b^2 d_b + R_s \sigma_s^2 d_s \quad (4.55)$$

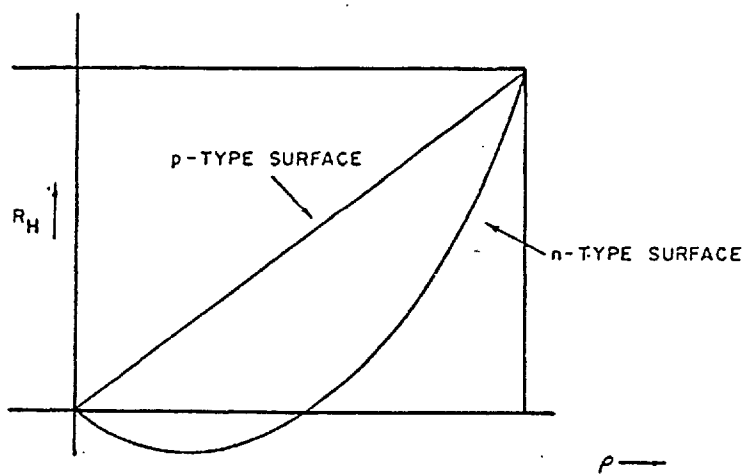
$$= q_b C_b \mu_b^2 d_b + q_s C_s \mu_s^2 d_s \quad (4.56)$$

where

- (i)  $\sigma$  and  $R_H$  are the conductivity and the Hall coefficient of the two-layer (bulk and surface),
- (ii)  $C$  is the carrier concentration,
- (iii)  $d$  is the film thickness,
- (iv)  $q$  is the electronic charge,  $-q$  for electrons and  $+q$  for holes,
- (v) subscripts  $b$  and  $s$  refer to bulk and surface respectively.

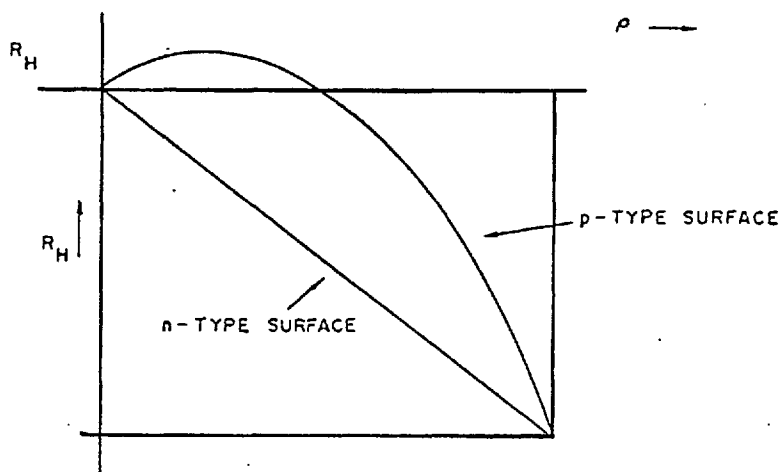


(a)



CASE I p-TYPE BULK

(b)



CASE II n-TYPE BULK

(c)

Fig.4.18 Two layer model after McLane and Zemel (M2)

From equations (4.54) and (4.56)

$$R_H = \frac{q_s \mu_s \rho}{q} + \frac{C_b \mu_b d_b}{d} (q_b \mu_b - q_s \mu_s) \rho^2 \quad (4.57)$$

Equation (4.57) can be examined for two types of bulk.

Case I - p-type bulk:

$$\therefore q_b = e, \mu_b = \mu_p \text{ and } C_b = p_b$$

Therefore for a p-type bulk and p-type surface ( $q_s = e$ ,  $\mu_s = \mu_p$ ) equation (4.57) gives

$$R_H = \mu_p \rho \quad (4.58)$$

which is a straight line with slope  $\mu_p$ . However for p-type bulk and n-type surface ( $q_s = -e$ ,  $\mu_s = \mu_n$ ), equation (4.57) gives,

$$R_H = -\mu_n \rho + \frac{ep_b d_b \mu_p}{d} (\mu_n + \mu_p) \rho^2 \quad (4.59)$$

which is a parabola.

Case II - n-type bulk:

$$\therefore q_b = -e, \mu_b = \mu_n, C_b = n_b$$

for a p-type surface ( $q_s = e$ ,  $\mu_s = \mu_p$ )

$$R_H = \mu_p \rho - \frac{en_b d_b \mu_n}{d} (\mu_n + \mu_p) \rho^2 \quad (4.60)$$

and for n-type surface ( $q_s = -e$ ,  $\mu_s = \mu_n$ )

$$R_H = -\mu_n \rho \quad (4.61)$$

Fig. 4.18(b) and Fig. 4.18(c) show the schematic plots of  $R_H$  vs  $\rho$  for p and n-type bulk.

The model predicts rather idealised  $R_H$  vs  $\rho$  curves because it has the following limitations.

- (i) The model assumes that the gas effect is limited to surface region only and the bulk of the film remains unaffected. Furthermore, surface width is considered to remain constant.
- (ii) The effect of space charge region is neglected.

However, the model predicts some general features of experimental  $R_H$  vs  $\rho$  curves.

#### 4.4.2.2.(b) Diffused layer model

The effect of H on p-type film will be considered here to develop the diffused layer model. As usual, expressions for  $R_H$  and  $\rho$  will be developed so that the experimental and theoretical  $R_H$  vs  $\rho$  curve could be compared. The following assumptions will be made.

- (i) Effect of space charge region is neglected.
- (ii) Effect of compensation is neglected.
- (iii)  $\mu_n$  and  $\mu_p$  are not functions of distance  $x$ .
- (iv) All impurities are ionised.
- (v) All acceptors are homogeneously distributed throughout the film.

The distribution of carriers in the diffused layer is given by,

$$N(x) = N_d(x) - N_a(x) \quad (4.62)$$

and in the p-type bulk,

$$N_a(x) = N_a \quad (4.63)$$

The donor profile is

$$N_d(x) = N_o \exp - \frac{x}{\ell} \quad (4.64)$$

Using Petritz's model (P9),

$$\sigma d = \int_0^{x_j} e \mu_n N(x) dx + \int_{x_j}^d e \mu_p N_a(x) dx \quad (4.65)$$

where it is assumed that the diffused layer extends from  $x = 0$  (surface) to  $x = x_j$  and the p-type bulk from  $x = x_j$  to  $x = d$ , where  $d$  is the film thickness. The value of  $x_j$  is given by,

$$x_j = \ell \ln \frac{N_o}{N_a} \quad (4.66)$$

$$R_H \sigma^2 d = - \int_{x=0}^{x_j} e \mu_n^2 N_a(x) dx + \int_{x_j}^d e \mu_p^2 N_a(x) dx \quad (4.67)$$

Integration of equations (4.65) and (4.67) is carried out in Appendix C.

From Appendix C,

$$R_H = \frac{\frac{e\mu_p N_a}{d} (d + A\ell) - \frac{e\mu_n N_o}{d} (B\ell)}{\left( \frac{e\mu_p N_a}{d} (d + A\ell) + \frac{e\mu_n N_o B\ell}{d} \right)^2} \quad (4.68)$$

and

$$\sigma(\ell) = \rho^{-1} = \frac{e\mu_p N_a}{d} (d + A\ell) + \frac{e\mu_n N_o B\ell}{d} \quad (4.69)$$

where

$$A = \ln N_a/N_o \quad \text{and} \quad B = \left( 1 - N_a/N_o + \frac{N_a}{N_o} \ln \frac{N_a}{N_o} \right) \quad (4.70)$$

All other symbols in equations (4.68) and (4.69) have their usual meanings. From equations (4.68) and (4.69),  $R_H$  and  $\rho$  can be evaluated as functions of  $\ell = 2\sqrt{Dt}$  and  $R_H$  vs  $\rho$  can be plotted. The model was tested for film S29 where  $\mu_p$  was  $121 \text{ cm}^2/\text{V-sec}$ ,  $\mu_n = 274 \text{ cm}^2/\text{V-sec}$ ,  $N_a = 5.69 \times 10^{16} \text{ cm}^{-3}$ ,  $N_o$  was  $1.45 \times 10^{18} \text{ cm}^{-3}$  and  $d = 4438 \text{ \AA}$ . The theoretical and experimental curves of  $R_H$  vs  $\rho$  for film S29 are shown in Fig. 4.19. As it can be seen from Fig. 4.19, there is *satisfactory* agreement between the two curves.

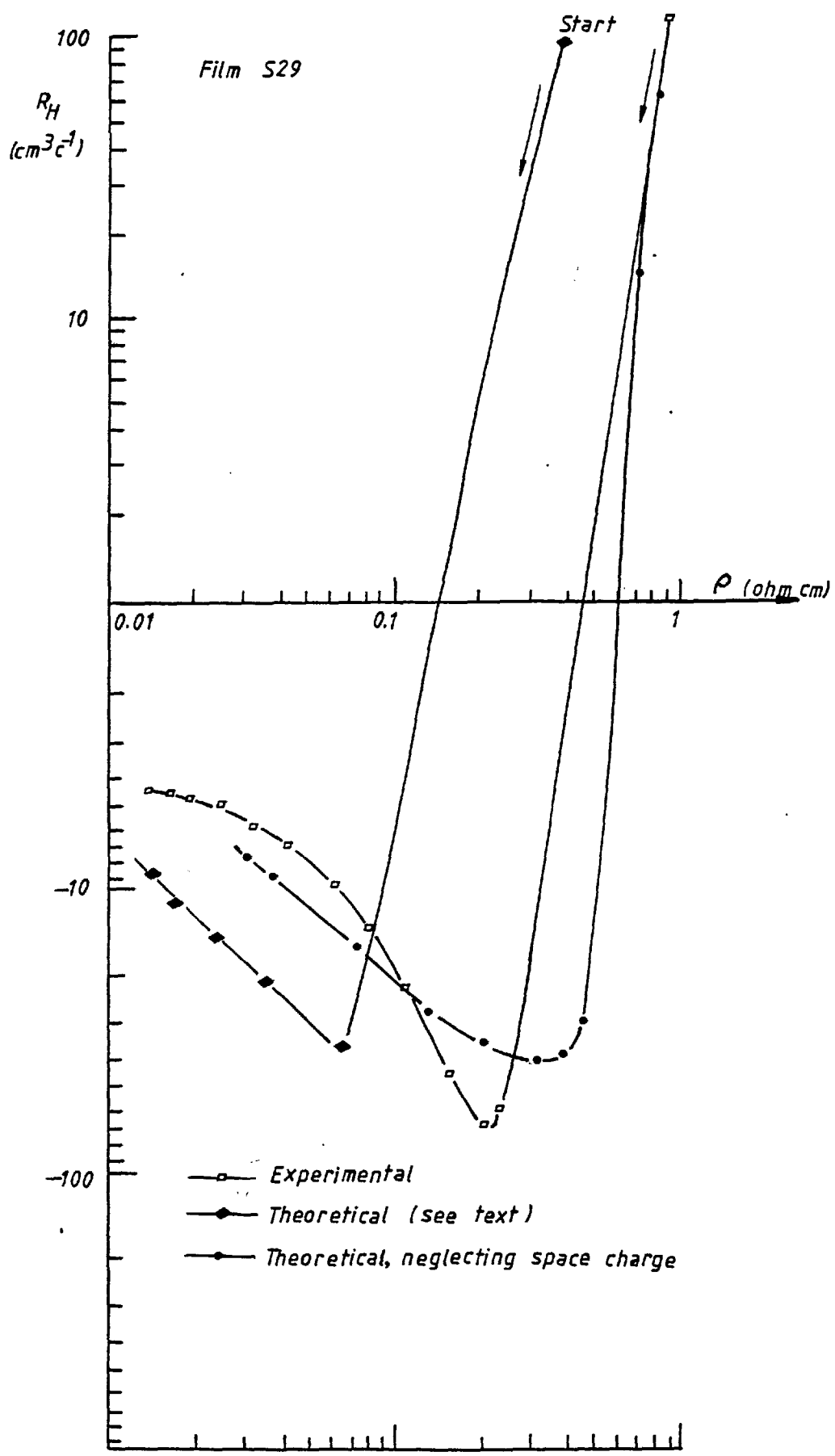


Fig. 4.19 1st H cycle on film S29



#### 4.4.2.2(c) Mobile p-n junction model

The major objection to the two models considered previously is that the space charge region which exists when donors diffuse into a p-type film is not taken into consideration. A model will now be discussed which takes into account the space charge region.

As mentioned in section 4.4.2, for prolonged diffusion of donors into a p-type film, the bulk of the film becomes separated from the n-type surface by a space charge region. This is similar to a moving p-n junction within the film. (See Fig. 4.14.) In common with the other models, expressions for  $R_H$  and  $\rho$  will now be developed for this model. The assumptions made are as follows.

- (i) The diffusion coefficient  $D$  is constant.
- (ii) p-n junction formed due to diffusion is approximated by a linearly graded junction of width  $W$ .
- (iii) Charge neutrality exists on either side of the p-n junction.
- (iv) Non-degeneracy is assumed and at equilibrium  $pn = n_i^2$ .
- (v) All impurities are ionised.
- (vi)  $\mu_n$  and  $\mu_p$  are independent of  $x$ .
- (vii) Homogeneous distribution of all acceptors is assumed.

Consider the effect of H diffusion described by equation (4.39) into a p-type film. For charge neutrality to exist,

$$\rho(x) = 0 \quad (4.71)$$

or

$$p(x) - n(x) + N_d(x) - N_a(x) = 0 \quad (4.72)$$

where  $N_a(x)$  is calculated from the measured Hall coefficient of the p-type film.

$$p(x)n(x) = n_i^2 \quad (4.73)$$

Eliminating  $p(x)$  by means of equations (4.72) and (4.73),

$$n(x) = \frac{1}{2} [N_d(x) - N_a] + \frac{1}{2} [(N_d(x) - N_a)^2 + 4n_i^2]^{\frac{1}{2}} \quad (4.74)$$

Eliminating  $n(x)$ , gives

$$p(x) = \frac{1}{2} [N_a - N_d(x)] + \frac{1}{2} [(N_d(x) - N_a)^2 + 4n_i^2]^{\frac{1}{2}} \quad (4.75)$$

Using Petritz's model (P9) once again,

$$\sigma d' = \int_0^{d'} \sigma(x) dx = q\mu_n \int_0^{d'} n(x) dx + q\mu_p \int_0^{d'} p(x) dx \quad (4.76)$$

and

$$R_H \sigma^2 d' = q\mu_p^2 \int_0^{d'} p(x) dx - q\mu_n^2 \int_0^{d'} n(x) dx \quad (4.77)$$

where  $d'$  is the effective film thickness given by equation (4.78)

$$d' = d - w \quad (4.78)$$

where  $d$  = actual film thickness

$w$  = width of the depletion region

For a linearly graded junction, the depletion width  $w$  is given by (G7),

$$w = \left( \frac{12 \epsilon_r \epsilon_0 \phi}{qa} \right)^{1/3} \quad (4.79)$$

where

- (i)  $\epsilon_0$  is the permittivity of free space
- (ii)  $a$  is the concentration gradient at the junction  $x = x_j$
- (iii)  $\phi$  is the built-in voltage

All the other symbols have their usual meanings. From (G7),

$$\phi = \frac{kT}{q} \ln \frac{N_a N_d}{n_i^2} \quad (4.80)$$

If the donor concentration on the n-side of junction is  $N_{dn}$  then  $a$  is given by,

$$a = \frac{N_{dn} - N_{dp}}{w} \quad (4.81)$$

Since no mobile charge carriers exist in the depletion width, one may account for the effect of the depletion width by subtracting it from the film thickness, i.e.  $d' = d - w$ . Therefore, in order to evaluate equations (4.76) and (4.77), effective thickness,  $d'$  of the film must be found. In other words,  $w$  must be evaluated as a first step. The following procedure was used to evaluate equations (4.76) and (4.77).

For an assumed value of the junction depth  $x_j$ ,  $\ell$  was calculated using equation (4.66) and for this value of  $\ell$ ,  $N_{dn}$  and  $N_{dp}$  were evaluated.  $\phi$  and  $a$  were found from equations (4.80) and (4.81). Using these values of  $\phi$  and  $a$  in equation (4.79), the depletion width  $w$  was evaluated for that particular value of the junction depth. Once  $w$  was known,  $d'$  was calculated from equation (4.78). Since  $d'$  was known,  $\sigma d'$  and  $R_H \sigma^2 d'$  could now be determined. This process was repeated for a series of increasing values of  $x_j$ . A computer program written by Hing (H1) was used to evaluate  $R_H$  and  $\rho$ .

The model was tested on film S29 and as it can be seen from Fig. 4.19, there is satisfactory fit between the shape of the theoretical and the experimental curve. To illustrate the inadequacy of the model in the single carrier regime, it was used to predict the theoretical  $R_H$  vs  $\rho$  curve for film S25 during second H cycle when the film was in single carrier region. This is shown in Fig. 4.11. It may be noted from Fig. 4.11 that no fit between the theoretical and the experimental curve exists.

A brief discussion of some of the assumptions made will now be presented.

(a) Ionisation of Impurities

For monovalent donors and acceptors, the degree of ionisation may be expressed as (B5),

$$N_a^- = \frac{N_a}{1 + \frac{1}{2} \exp\left(\frac{E_a - E_F}{kT}\right)} \quad (4.82)$$

and

$$N_d^+ = \frac{N_d}{1 + \frac{1}{2} \exp\left(-\frac{E_d - E_F}{kT}\right)} \quad (4.83)$$

where  $N_a$  and  $N_a^-$  are the densities of acceptors and ionised acceptors with energy level  $E_a$  in the forbidden band gap. Similarly  $N_d$  and  $N_d^+$  are the densities of donors and ionised donors where  $E_d$  is the donor energy level.  $E_F$  is the Fermi level and  $\frac{1}{2}$  is the spin degeneracy factor. Since no carrier freeze-out has been evident from the Hall effect measurements (C6) and the static dielectric constant of PbTe is high anyway, therefore it is reasonable to assume that all impurities are ionised at room temperature

$$\therefore N_a \approx N_a^- \quad N_d \approx N_d^+ \quad (4.84)$$

and charge neutrality gives

$$p + N_d^+ = n + N_a^- \quad (4.85)$$

and

$$\begin{aligned} \therefore \text{ for a p-type film } p &= N_a^- = N_a \text{ ) at } \\ & \text{ room } \\ \text{ for an n-type film } n &= N_d^+ = N_d \text{ ) temperature} \end{aligned} \quad (4.86)$$

(b) Constant Diffusion Coefficient D

The temperature dependence of D has already been mentioned but this dependence is not crucial in the present case since the comparison between the theoretical and the experimental data was carried out at only one temperature (room temperature). However, D can also be dependent on the concentration of the diffusing impurities in addition to being field assisted where the electric field is due to the diffusion of ionised impurities and in the case of non-homogeneous materials, D may also vary with distance x.

When, for example, the diffusing impurities are donors, simultaneous diffusion of ionised donors and electrons must be considered. Since the mobilities of the two diffusing species are different, this will result in a built-in electric field where the field assists the diffusion of the slower species (T1). Lehovec and Slobodskoy (L7) give an expression for effective diffusion coefficient,  $D_{\text{eff}}$  for the diffusion of a singly charged impurity into an intrinsic semiconductor. (In the present context, films in two-carrier regime.)

$$D_{\text{eff}} = D(1 + f) \quad (4.87)$$

where

$$f = \frac{C/n_i}{[(C/n_i)^2 + 4]^{\frac{1}{2}}} \quad (4.88)$$

$D$  = field independent diffusion coefficient  
 $C$  = concentration of the diffusing impurities  
 $n_i$  = intrinsic carrier concentration (at  
diffusing temperature)

If  $C \ll n_i$  ,  $f \rightarrow 0$  and  $D_{\text{eff}} \approx D$

If  $C \gg n_i$  ,  $f \rightarrow 1$  and  $D_{\text{eff}} \approx 2D$

In other words, in the extreme case, the built-in field can effectively double the diffusion coefficient. Since neither  $C$  is known explicitly nor the dependence of  $D$  on the concentration of the diffusing donors ( $H$ ) in the present case, it is difficult to make allowances for these factors affecting  $D$ . However, if  $D$  is known as a function of concentration then equation (4.36) can be written as (for unidirectional diffusion),

$$\frac{dc}{dt} = \frac{d}{dx} \left( D \frac{dc}{dx} \right) \quad (4.89)$$

### (c) Compensation Effect

If a semiconductor contains both donor and acceptor impurities it behaves as if only the difference between the two types of impurities were effective in an otherwise pure crystal. For example, a fully ionised p-type semiconductor,  $N_a$  may be compensated by donors,  $N_d$  giving an effective carrier concentration of  $N_a - N_d$ . It is likely that films may have been doped inadvertently during growth to give compensated films. Hing (H1)

considered the compensation effect for H diffusion into  $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$  thin films. For a p-type film with carrier concentration  $N_a^*$  compensated by donors  $N_{do}$ , the measured carrier concentration ( $N_a$ ) from the Hall coefficient is given by,

$$N_a = N_a^* - N_{do} \quad (4.90)$$

For H diffusion into such a film, total donor concentration at any point  $x$  within the film will be,

$$N_d(x) = N_{do} + N_o^* \exp - \frac{x}{l} \quad (4.91)$$

$$\text{where } N_o^* = N_a^* + N_\infty \quad (4.92)$$

and  $N_\infty$  is the 'saturation' donor concentration.

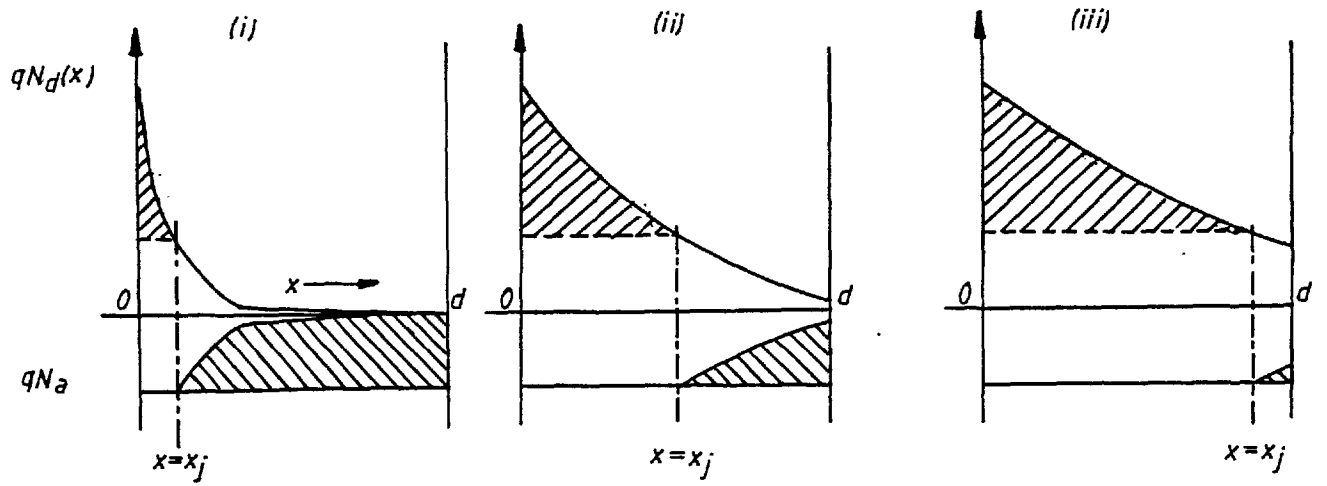
For an assumed donor compensation  $N_{do}$ ,  $N_a^*$  can be calculated from equation (4.90) and then using  $N_a^*$  in equation (4.92),  $N_o^*$  can be determined. Using this value of  $N_o^*$  in equation (4.91),  $N_d(x)$  can be evaluated. Equations (4.74), (4.75), (4.76) and (4.79) can be used to determine  $\sigma$  and  $R_H$ . Hing (H1) found that the theoretical curves were not significantly different from the curves where compensation effect was neglected and furthermore the shape of  $R_H$  vs  $\rho$  curves remained unaltered.



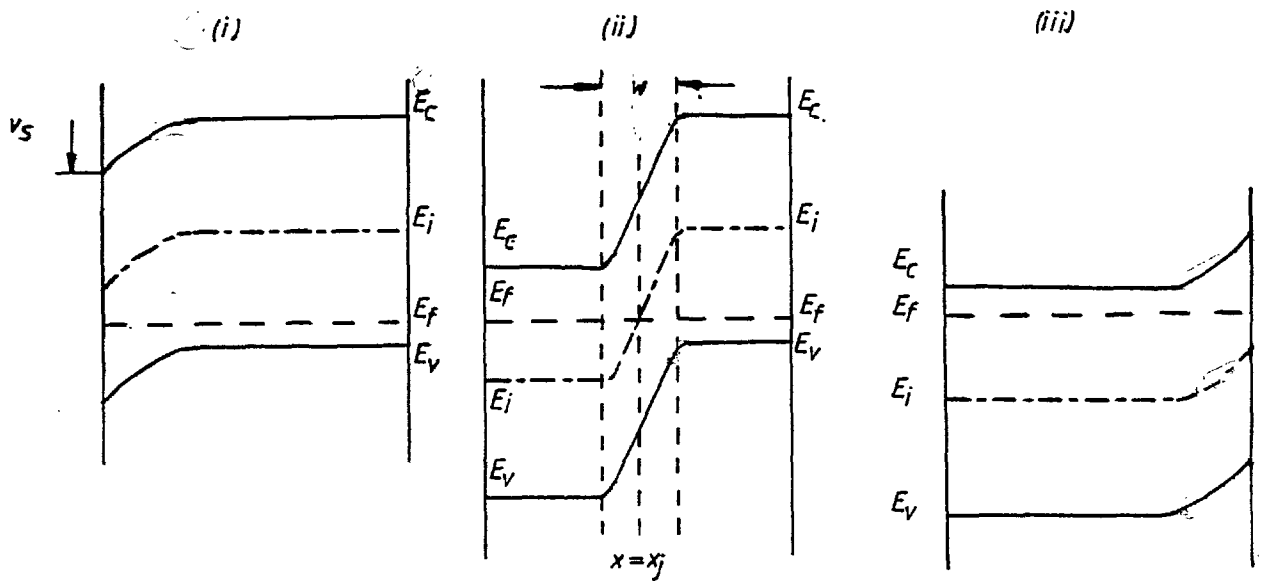
The diffusion model is shown schematically in Fig. 4.20 for different stages of diffusion. Distribution of the charge density is shown in Fig. 4.20(a) and the corresponding energy distribution diagrams and  $R_H$  vs  $\rho$  curves are shown in Fig. 4.20(b) and Fig. 4.20(c) respectively. During the initial stages of diffusion, the charge density distribution was as shown in Fig. 4.20(a,i) and the corresponding energy distribution diagram and  $R_H$  vs  $\rho$  curve was as shown in Fig. 4.20(b,i) and Fig. 4.20(c,i) respectively.

#### 4.5 IONISATION OF H

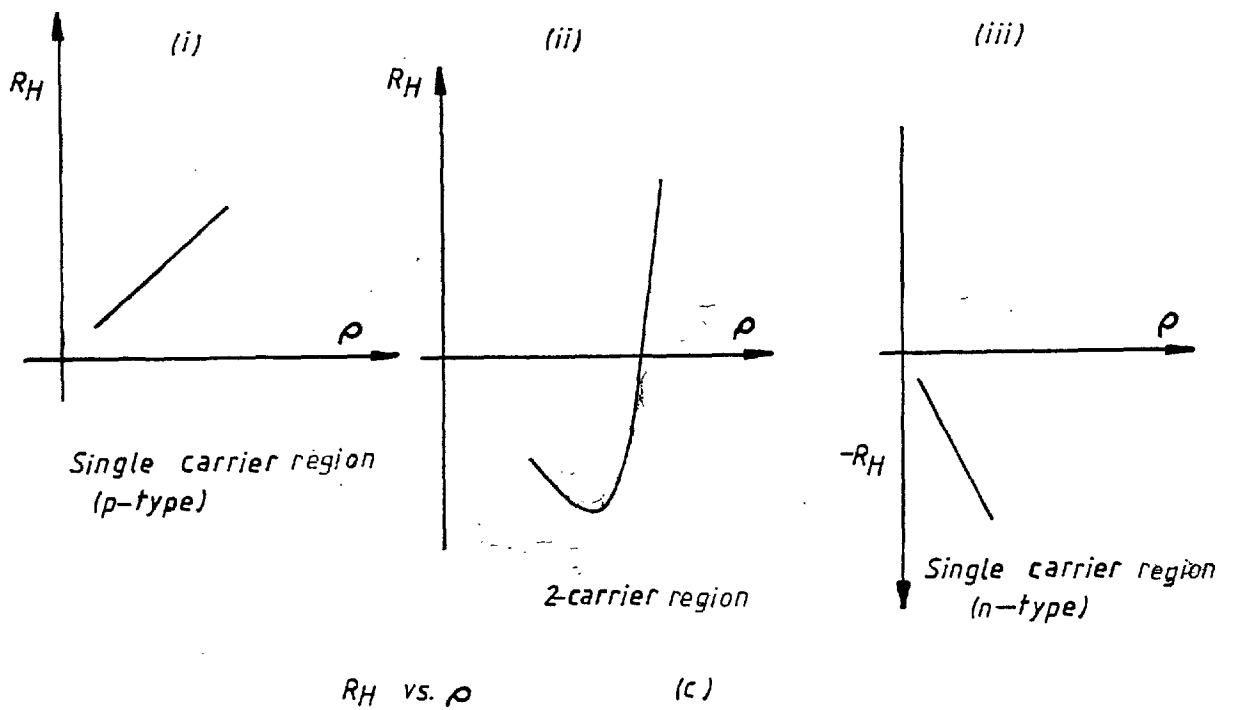
The effect of H entering the PbTe lattice can be examined in terms of Parada-Pratt model (P10) where they considered the effect of introducing Pb and Te vacancies in PbTe. In their model, they consider the perturbing potential due to the vacancy (of Pb and Te) to be approximately the negative of the highly localised potential normally associated with the site. Since Pb has four valence electrons (the outer shell of Pb is  $6s^2 6p^2$ ), it has the perturbing potential corresponding to a charge of -4 electrons. Therefore, introduction of a Pb vacancy into a perfect lattice will result in the loss of four valence electrons and two valence states and production of two holes in the valence band (P10). Similarly, for a Te vacancy ( $5s^2 5p^4$ ), eight valence states



Charge-density distribution (a)



Energy distribution (b)



$R_H$  vs.  $\rho$  (c)

Fig.4.20 Diffusion model (schematic). H effect on p-type film.

and six electrons are lost and two electrons are produced in the conduction band where the ionisation of Pb vacancy  $V_{pb}$ , and that of Te vacancy  $V_{Te}$  can be written as,



where  $Z$  is the level of ionisation (i.e.  $Z = 1, 2$  etc.). Therefore ionised native defects can make PbTe n or p-type.

McLane and Zemel (M2) first considered the Parada-Pratt model to explain the ionisation of H in PbSe epitaxial films. If H atom occupies a  $V_{pb}$ , it produces a perturbing potential of  $-3e$ . This results in the removal of two valence states and three valence electrons and production of one hole. Therefore occupation of  $V_{pb}$  by H has resulted in the reduction of holes due to  $V_{pb}$  from 2 to 1 in the valence band which explains the donor-like effect of H in PbSe. Occupation of  $V_{Te}$  by an oxygen atom can be treated similarly. Since Te and oxygen belong to the same chalcogen family (outer shell of the form  $s^2 p^4$ ), the electrical effect of introducing an oxygen atom on to a Te vacancy is equivalent to reintroducing a Te atom and producing two holes in the valence band. Therefore, the vacancy model assumes that H and  $O_2$  affect the electrical properties of lead salts when H and  $O_2$  occupy  $V_{pb}$  and

$V_{Te}$  respectively.

Re-examination of the vacancy occupation model was done by Zemel (Z4). He also considered the possibility of H entering the interstitial sites but rejected the idea on the basis that the changes introduced in the carrier concentration of lead salts would be far higher than experimentally observed. He concluded that H atom can only influence the carrier concentration when it occupies a  $V_{pb}$ . Further evidence of this model was produced by the mobility-temperature dependence observed for a film before and after the H effect. If H were an ordinary ionised impurity, it would have introduced an additional scattering factor for the H saturated film. However, the temperature dependence of mobility in both cases was identical which was understandable if H was destroying a hole by occupying a  $V_{pb}$  (Z4).

Consider the effect of H entering PbTe film. If the concentration of Pb vacancies is  $V_{pb}$  and  $C_H^+$  is the concentration of ionised H at any point in the film, then the probability of H finding a  $V_{pb}$  is proportional to  $V_{pb}$  (i.e.  $K V_{pb}$ ) and the probability of finding H on  $V_{pb}$  is  $C_H^+/V_{pb}$ . (This treatment is based on McLane-Zemel (M2) formulation.) This gives,

$$C_H^+ = C_H K V_{pb} \left( 1 - \frac{C_H^+}{V_{pb}} \right) \quad (4.95)$$

where  $C_H$  is the total concentration of H (both ionised and unionised) and  $(1 - C_H^+/V_{pb})$  is the probability of  $V_{pb}$

being unoccupied by H. From equation (4.95),

$$\frac{C_H^+}{V_{pb}} = \text{probability of finding H on } V_{pb} = \frac{KC_H}{1 + KC_H} \quad (4.96)$$

where K is a constant

$$\text{when } KC_H \ll 1, \quad \frac{C_H^+}{V_{pb}} \approx KC_H \ll 1 \quad (4.97)$$

i.e. most  $V_{pb}$  are unoccupied by H and  $C_H^+$  is proportional  $C_H$ .

However, for H to turn an extrinsic p-type film n-type, there must be sufficient number of  $V_{pb}$  to compensate the hole concentration. Therefore, for a p-type film,

$$p = \frac{1}{R_H e} = 2 (V_{pb} - V_{Te}) \quad (4.98)$$

where  $Z = 2$  has been assumed in equations (4.93) and (4.94) when H is introduced,

$$\frac{1}{R_H e} = 2V_{pb} - 2V_{Te} - C_H^+ \quad (4.99)$$

when all  $V_{pb}$  are occupied by H, (i.e.  $C_H^+ = V_{pb}$ )

$$\frac{1}{R_H e} = V_{pb} - 2V_{Te} \quad (4.100)$$

Therefore for a film to be n-type,  $R_H$  must be negative.

$$\therefore V_{Te} > \frac{1}{2} V_{pb} \quad (4.101)$$

Since typical hole concentration was  $10^{17}$ - $10^{18}$   $\text{cm}^{-3}$  in the present case and  $V_{pb} \sim 10^{19}$   $\text{cm}^{-3}$ \*, equation (4.101) is easily satisfied.

In summary, the following points may be noted.

- (i) It is reasonable to assume that when H occupies  $V_{pb}$ , it releases one of the two electrons trapped at the vacant site which as a result would increase the concentration of electrons in the conduction band by one or annihilate a hole in the valence band. Furthermore, if the vacancy-impurity interaction model is to be believed then H will affect the electrical properties of lead salts only if H occupies a  $V_{pb}$ .
- (ii) When most  $V_{pb}$  are unoccupied by H (i.e. during the initial period of H exposure),  $C_H^+$  is proportional to  $C_H$ .
- (iii) Based on the above model, H can drive a p-type film n-type if the film is highly compensated.

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\* From (L8), Schottky constant  $K_S = [V_{pb}^{2-}][V_{Te}^{2+}] \approx 10^{38}$   $\text{cm}^{-6}$  at 1023K

#### 4.6 DISCUSSION OF RESULTS

In this section, an attempt will be made to reconcile the experimental results with the theoretical models described in the previous sections.

##### 4.6.1 (a) H Effect on O<sub>2</sub>-driven P-type Films

Before discussing the mechanism of H-uptake, one may note the following general features of H effect on these films.

- (i) H makes p-type film less p-type and drives n-type film more n-type. In other words, H has a donor-like effect on PbTe films.
- (ii) The H effect and the desorption of O<sub>2</sub> from the surface of PbTe films is undistinguishable since  $R_H$  vs  $\rho$  dependence during re-evacuation and H cycle is the same provided the film remains in the single carrier region.

As explained in the previous section, when H occupies a lead vacancy  $V_{pb}$  it releases one of two electrons trapped at the site and H has effectively been ionised. Since H<sub>2</sub> had no effect on the electrical properties of PbTe films, it is reasonable to assume that only one hydrogen atom can occupy  $V_{pb}$  where the energy to dissociate H<sub>2</sub> into H atoms has been provided by the tungsten filament. The interaction between H and

tellurium to form  $H_2Te$  was suggested by Egerton and Crocker (E4).



where  $V_{Te}^{\cdot}$  is a singly charged tellurium vacancy. But they rejected this possibility since the loss of volatile  $H_2Te$  would make the process irreversible and no desorption should be evident.

The surface model for H-uptake was tested on film S25 (Fig. 4.11) and it gave a very good fit for the linear portion of the  $R_H$  vs  $\rho$  curve and the fit became poor as the film moved into the two carrier region. The diffusion model developed in section 4.4.2.1 also gave a very good fit for the linear region (Fig. 4.17). Therefore, during the initial stages of H exposure it is difficult to distinguish between the two models. However, it is more reasonable to believe that the surface model applies during the initial stages of H exposure and the diffusion model during the latter stages.

#### 4.6.1 (b) H Effect on P-Type 'Virgin' Films

Unfortunately, it was not possible to grow single carrier 'virgin' p-type films and all the 'virgin' p-type films had low carrier concentrations comparable to the intrinsic carrier concentration, i.e. the films were two-carrier type. When such films were exposed to H, there was no initial increase in  $R_H$  and  $\rho$  values



(Fig. 4.7) and the films turned n-type rather quickly (see Table 4.2). This is expected since the excess hole concentration to be neutralised by H is much smaller (compared to the single carrier case) due to much smaller difference between the concentrations of ionised  $V_{pb}$  and  $V_{Te}$ . But it is difficult to explain such a quick change-over from p-type to n-type by surface model or even the diffusion of H down short circuit paths such as grain boundaries and dislocations because in the latter case the mechanism of H ionisation remains unclear.

Leaving the kinetics aside for the moment, the diffusion model incorporating the mobile p-n junction does predict the correct shape for the experimental  $R_H$  vs  $\rho$  curve. There is a discrepancy between the theoretical and the experimental values of  $\rho$  where the theoretical values are underestimated.\* This may be so because the width of the depletion region has been subtracted from the actual film thickness to evaluate  $\rho$ , i.e.

$$\rho_c = \rho_e \left( \frac{d-w}{d} \right) = \rho_e \left( 1 - \frac{w}{d} \right) \quad (4.103)$$

where  $\rho_c$  is the calculated value,  $\rho_e$  is the experimental value,  $w$  is the width of the depletion region and  $d$  is the film thickness. Since  $(1-w/d)$  is less than unity,  $\rho_c < \rho_e$ .

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\* Suitable adjustment of parameters like  $w$  should give a better fit.

#### 4.6.1 (c) H Effect on 'Virgin' N-type Films

All such films were driven more n-type when exposed to H where  $R_H$  and  $\rho$  decreased linearly keeping the Hall mobility almost constant. This is consistent with the donor effect of H on PbTe films. Once again, the surface model is expected to apply during the initial stages where an accumulation layer is formed on n-type bulk followed by some in-diffusion of H. Films are considered saturated with H when all the lead vacancies have been occupied.

#### 4.6.1 (d) H Effect on O<sub>2</sub>-driven P-type Films at 50°C

Both films S25 and S36 were put through H-O<sub>2</sub> cycles at room temperature before H cycle at 50°C was carried out. Therefore, it was possible that when these films were heated up to 50°C (prior to H cycle) in a vacuum of  $\sim 10^{-6}$   $\tau$ , some out-diffusion of H previously incorporated into the films had occurred. This made the films more p-type as evidenced by the decrease in values of  $R_H$  and  $\rho$  (regions BC and FG in Fig. 4.9).

#### 4.6.2 (a) O<sub>2</sub> Effect on N-type Films (H Saturated)

Even though the paths traversed by  $R_H$  vs  $\rho$  curves are not the same during the H and O<sub>2</sub> exposures and the duration of the gas exposure to turn a p-type film n-type and vice versa is different, the effect of O<sub>2</sub> on H saturated film can essentially be described as the reversal of H effect especially during the initial stages of

O<sub>2</sub> cycle. When a H saturated film was left in vacuum ( $\sim 10^{-6}$  τ) at room temperature both R<sub>H</sub> and ρ started to increase showing that carrier concentration was decreasing. In other words, some desorption of H was occurring where the desorption of H could take place in the form of either H<sub>2</sub> (Z4) or H<sub>2</sub>O (E4). The possibility of H recombining with O<sub>2</sub> on the surface to form H<sub>2</sub>O which would then be desorbed was confirmed by Young (Y2). Therefore, it is reasonable to suggest that when H saturated films are exposed to O<sub>2</sub>, H is removed from the film in the form H<sub>2</sub>O which is desorbed at the surface. This has the effect of making such films less n-type. During the initial stages the O<sub>2</sub>-uptake is fast and irreversible. During the latter stages of the gas cycle, the rate of O<sub>2</sub> uptake was slower. When the films became p-type on exposure to O<sub>2</sub> at atmospheric pressure, some of the O<sub>2</sub>-uptake was reversible by re-evacuation of the vacuum system.

#### 4.6.2 (b) O<sub>2</sub> Effect on 'Virgin' N-type Films

As it can be seen from Table 4.1, when a 'virgin' n-type film was left in vacuum ( $\sim 10^{-6}$  τ), it became less n-type. This can be explained by the formation of the space charge region on the surface of the film. In this case, the surface region was being depleted of the mobile carriers.

When film S47 (Fig. 4.5) was exposed to  $O_2$ ,  $|R_H|$  began to decrease instantly whereas  $\rho$  was almost constant. Since the film is in two carrier region, it is difficult to say whether changes in  $R_H$  are due to changes in the carrier concentration or carrier mobility. Once the film was driven p-type and into the single carrier region, both  $R_H$  and  $\rho$  decreased linearly to keep the Hall mobility almost constant. When the film was exposed to  $O_2$  at atmospheric pressure and re-evacuated, some desorption of  $O_2$  from the surface occurred as evidenced by the increase in  $R_H$  and  $\rho$  values.

#### 4.6.2 (c) $O_2$ Effect on 'Virgin' P-type Films

Film S51 (Fig. 4.8) illustrates this case. As expected, an originally p-type film became more p-type when exposed to  $O_2$ . In terms of the surface model, an accumulation region was being formed on the surface of the p-type film.

A further discussion of these results will be presented in the next chapter.

## CHAPTER 5

### KINETICS STUDIES

#### 5.1 INTRODUCTION

The variation of the Hall coefficient as a function of resistivity was discussed in the previous chapter. In order to gain further insight into the mechanism of gas-uptake, the changes in the Hall coefficient and resistivity as a function of time were also studied. The results of these kinetic studies will be presented in this chapter. Once again, an attempt will be made to interpret the experimental data in terms of the two models discussed in the previous chapter, namely surface adsorption model and diffusion model.

#### 5.2 RESULTS AND CALCULATIONS

Before describing the results, some general characteristics of the  $R_H$  vs  $\rho$  curve will be discussed first.

Fig. 5.1 shows a schematic  $R_H$  vs  $\rho$  curve. Regions AB and ED are the single carrier regions (p-type and n-type respectively). In these regions, the  $R_H$  vs  $\rho$  dependence is linear and from the slopes of AB and ED the Hall mobility of holes and electrons respectively can be deduced. The measure of gas-uptake in these regions is reflected in the changes of the respective carrier

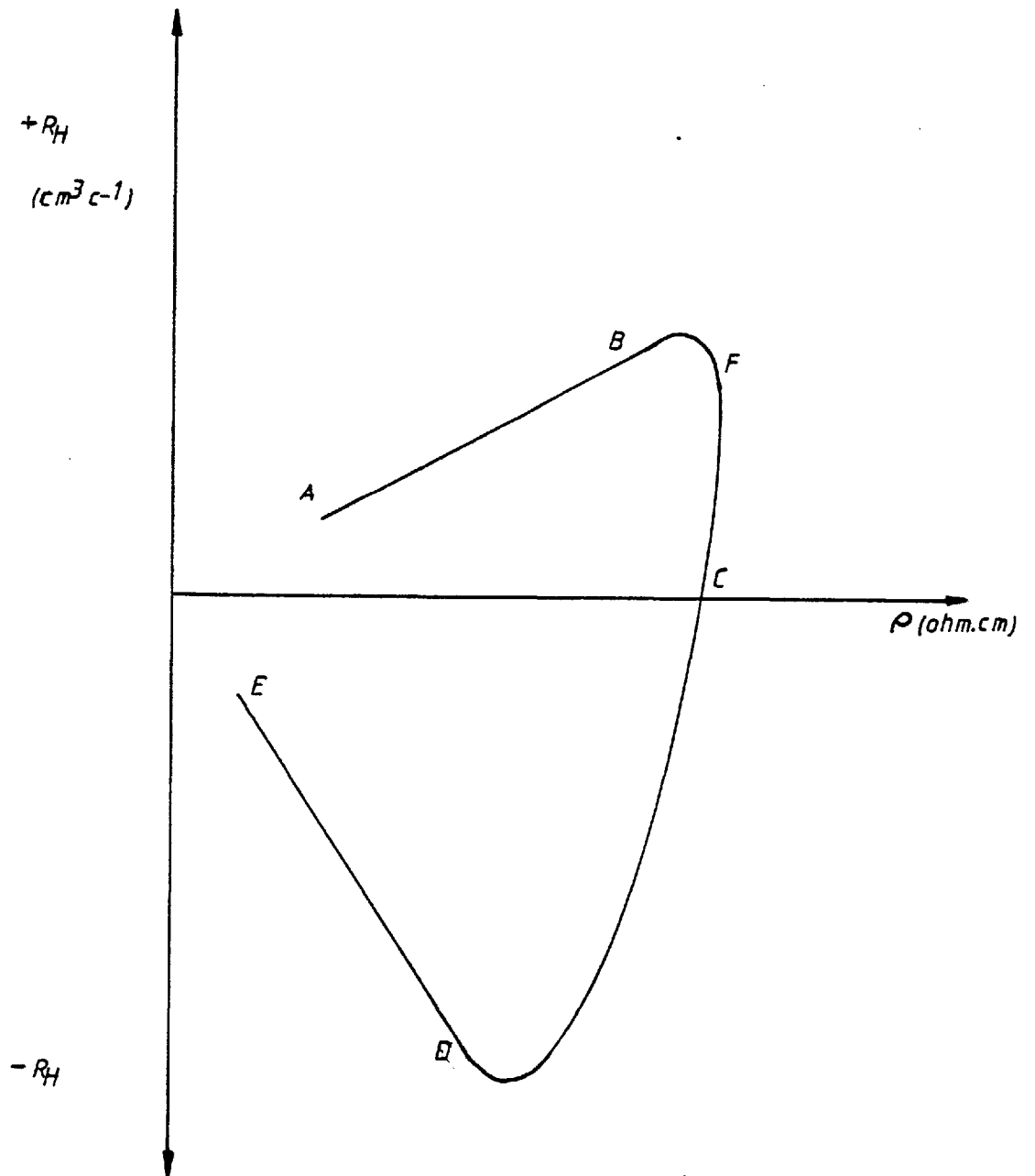


Fig. 5.1 Schematic  $R_H$  vs.  $\rho$  Curve

concentrations. In the regions BC and CD, it is a two carrier film (p-type and n-type respectively) and the measure of gas-uptake can no longer be interpreted in terms of the changes in carrier concentration because the  $R\sigma$  product also varies in these regions. Therefore, the kinetic studies in the present case were restricted to the linear regions of the  $R_H$  vs  $\rho$  curve.

Let us consider the effect of H cycle starting at A (Fig. 5.1). Since H effectively reduces the carrier concentration of a p-type film, both  $R_H$  and  $\rho$  will increase.

$$\therefore \text{ at time } t = t_1, \quad p_1 = \frac{1}{R_{H_1} e} \quad (5.1)$$

$$\text{and at time } t = t_2, \quad p_2 = \frac{1}{R_{H_2} e} \quad \text{where } t_2 > t_1 \quad (5.2)$$

$$\therefore \Delta P = p_2 - p_1 = \frac{1}{e} \left[ \frac{1}{R_{H_2}} - \frac{1}{R_{H_1}} \right] \quad (5.3)$$

Writing  $R_H$  in the planar form,

$$\Delta P = \frac{d}{e} \left[ \frac{R_{H_1} - R_{H_2}}{R_{H_1} R_{H_2}} \right] \text{ cm}^{-2} \quad (5.4)$$

where  $d$  is the film thickness in cm and  $e$  is the electronic charge.

Since  $R_{H_2} > R_{H_1}$ ,  $\Delta P$  is negative. Therefore, for H effect on single carrier p-type films,  $-\Delta P$  vs time will be plotted.

When considering the H effect on 'virgin' n-type films, the relevant part of the  $R_H$  vs  $\rho$  curve is ED. Since H has a donor-like effect, both  $|R_H|$  and  $\rho$  will decrease.

∴ equation (5.4) becomes

$$\Delta N = \frac{d}{e} \left[ \frac{R_{H_1} - R_{H_2}}{R_{H_1} R_{H_2}} \right] \quad (5.5)$$

In this case  $R_{H_2} < R_{H_1}$  ∴  $\Delta N$  is positive.

Therefore, for H effect on 'virgin' films  $\Delta N$  vs time will be plotted.

Let us now consider the effect of  $O_2$  on H saturated n-type films. In this case the cycle will commence at E (Fig. 5.1). As observed in the previous chapter,  $O_2$  makes n-type film less n-type and both  $|R_H|$  and  $\rho$  increase during the initial stages of the gas exposure.

∴ from equation (5.5)

$$\Delta N = \frac{d}{e} \left[ \frac{R_{H_1} - R_{H_2}}{R_{H_1} R_{H_2}} \right]$$

where  $R_{H_2} > R_{H_1}$  and ∴  $\Delta N$  is negative.

Therefore, for  $O_2$  effect on H saturated n-type films  $-\Delta N$  vs time will be plotted. However, for  $O_2$  effect on 'virgin' p-type films,  $\Delta P$  will be positive.

$$\therefore P = \frac{d}{e} \left[ \frac{R_{H_1} - R_{H_2}}{R_{H_1} R_{H_2}} \right]$$



and  $R_{H_2} < R_{H_1}$  in the present case.

For a unidirectional diffusion in the x-direction,

$$\frac{dC}{dt} = D \frac{d^2C}{dx^2} \quad (5.6)$$

where D is the diffusion coefficient (assumed to be concentration independent) of the diffusing species, C is the concentration of the diffusant and t is the time. Solutions of equation (5.6) exist for various practical situations. For diffusion from a constant source into a semi-infinite medium equation (5.6) has the solution (B6),

$$C(x,t) = C_0 \operatorname{erfc} \frac{x}{2\sqrt{Dt}} \quad (5.7)$$

where  $C_0$  is the constant surface concentration and  $\operatorname{erfc}$  is the complementary error function. The area under the curve defined by equation (5.7) gives the amount of the diffused species after time, t.

$$Q(t) = \int_0^\infty C(x,t) dx \quad (5.8)$$

$$\therefore Q(t) = 2C_0 \left(\frac{Dt}{\pi}\right)^{\frac{1}{2}} \quad (5.9)$$

Therefore, amount of diffused impurity is proportional to  $t^{\frac{1}{2}}$ . In order to see whether H uptake was a diffusion limited process, kinetics of the gas-uptake were plotted using  $t^{\frac{1}{2}}$  dependence. Oxygen kinetics were plotted using

a  $\ln(t)$  dependence <sup>(M2,Z4).</sup> H and O<sub>2</sub> kinetics will now be described for both n- and p-type films, including the films discussed in chapter 4.

### 5.2.1 H Kinetics

Fig. 5.2 shows the kinetics of H-uptake when 'virgin' n-type films were exposed to it. As can be seen from the figure,  $t^{\frac{1}{2}}$  dependence is followed by all the films after the initial faster rate of uptake which implies that the mechanism of gas-uptake is diffusion limited. An estimate of the diffusion coefficient can be made as follows.

Rewriting equation (5.9) in the present context,

$$\Delta N = 2N_0 \left(\frac{Dt}{\pi}\right)^{\frac{1}{2}} \quad (5.10)$$

$$\therefore \text{Slope of } \Delta N \text{ vs } t^{\frac{1}{2}} = 2N_0 \left(\frac{D}{\pi}\right)^{\frac{1}{2}} \quad (5.11)$$

$$\text{or } D = \pi \left(\frac{\text{Slope}}{2N_0}\right)^2 \quad (5.12)$$

where  $N_0$  is the value when  $t \rightarrow \infty$ , i.e. the 'saturation' value which can be determined experimentally.

Estimated values of D are shown in Table 5.1.

H-uptake was investigated for some films at temperatures higher than the room temperature. This was not an exhaustive investigation since (as mentioned in chapter 4) no adequate facility was available to heat the films while situated in between the poles of the electromagnet. Fig. 5.3 shows the H-uptake at 50°C

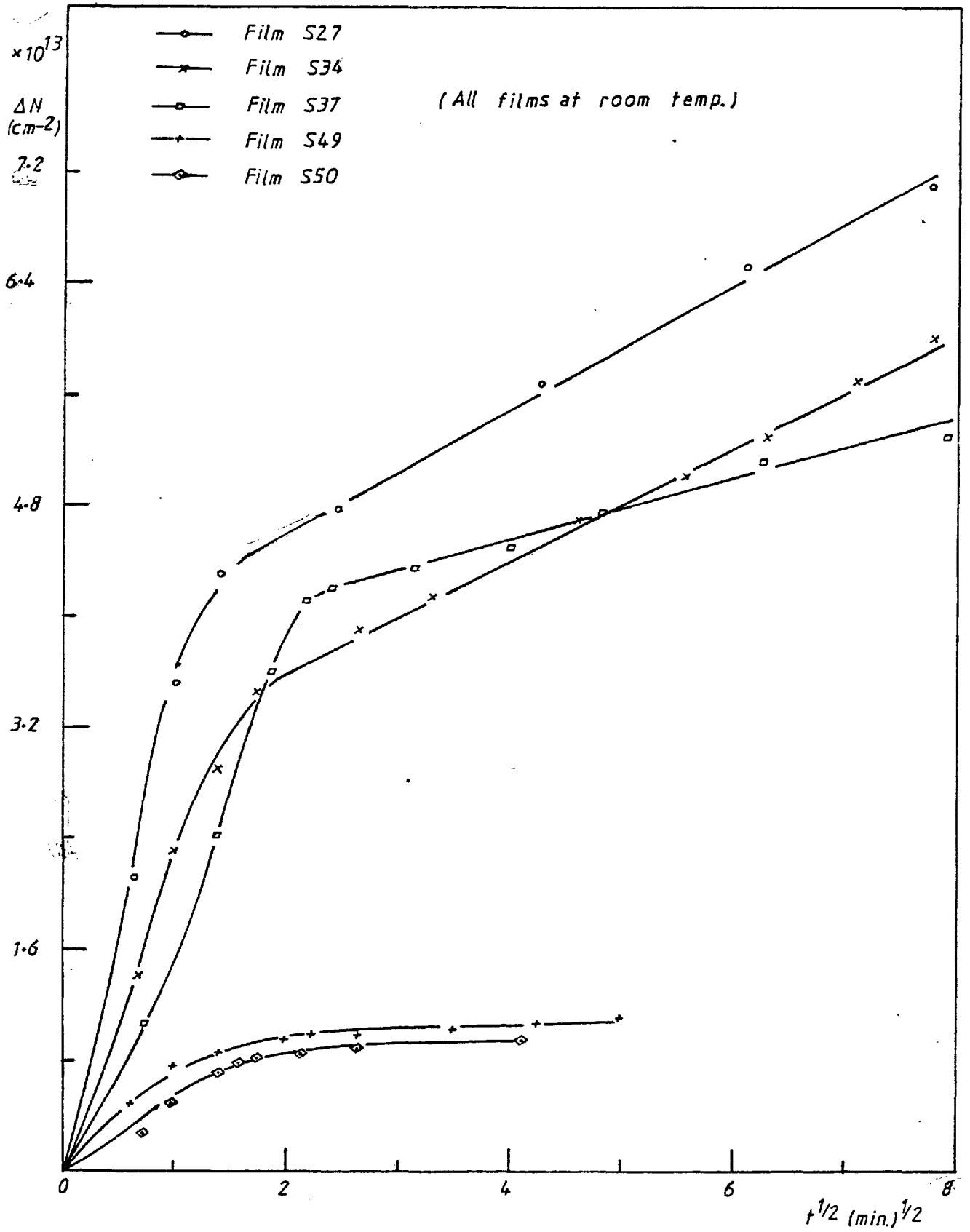


Fig.5.2 H-kinetics of 'virgin' n-type films.

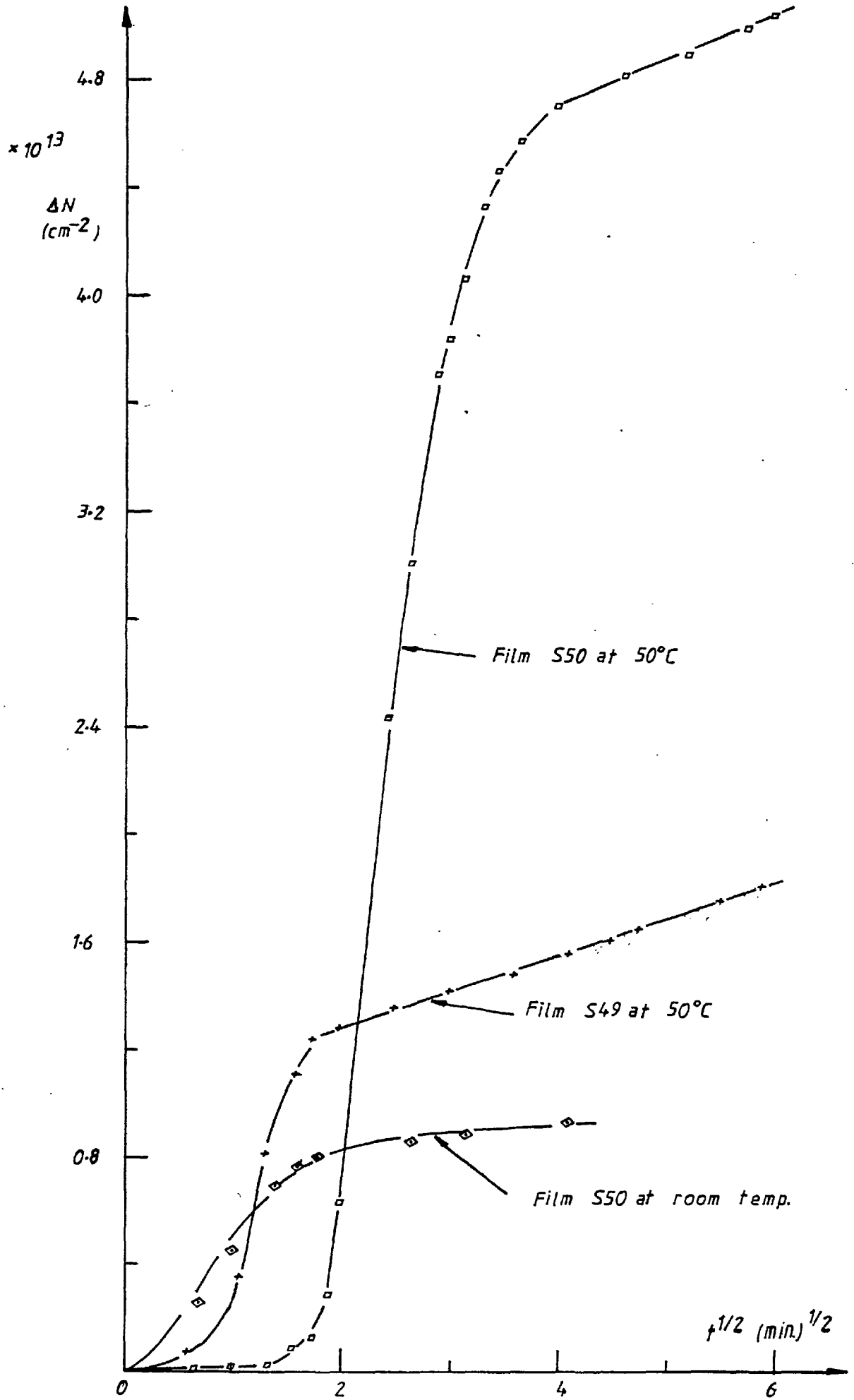


Fig. 5.3 H-kinetics of n-type films

for two n-type films (S49 and S50). Films S49 and S50 were 'virgin' n-type. These films were first exposed to H at room temperature. After 'saturation' had been reached, the films were exposed to O<sub>2</sub> and eventually let up to air at atmospheric pressure. Both films remained n-type. The system was pumped down and the second H exposure was carried out at 50°C. As can be noted from Fig. 5.3, the initial gas-uptake at 50°C is slower but during the latter stages of the gas exposure, both the amount of H-uptake and its rate of uptake is higher than that for room temperature. The estimated values of D at 50°C were  $9.9 \times 10^{-15} \text{ cm}^2 \text{ s}^{-1}$  and  $1.14 \times 10^{-14} \text{ cm}^2 \text{ s}^{-1}$  for S49 and S50 respectively (see Table 5.1 for room temperature values of D). Invoking an exponential temperature dependence of D,

$$D = D_0 \exp - \frac{E_a}{kT} \quad (5.13)$$

value of effective activation energy  $E_a$  can be calculated. In the case of S49,  $E_a$  was 0.34 eV whereas for S50 it was 0.4 eV.

Fig. 5.4 shows the effect of interrupting H cycle in the case of a 'virgin' n-type film, S66. When the tungsten filament was switched on to atomise H<sub>2</sub>,  $|R_H|$  decreased rapidly initially but more slowly as time progressed. When the filament was switched off,  $|R_H|$  increased. However, the rate of increase of  $|R_H|$  during the 'off' period was slower than the rate of decrease of

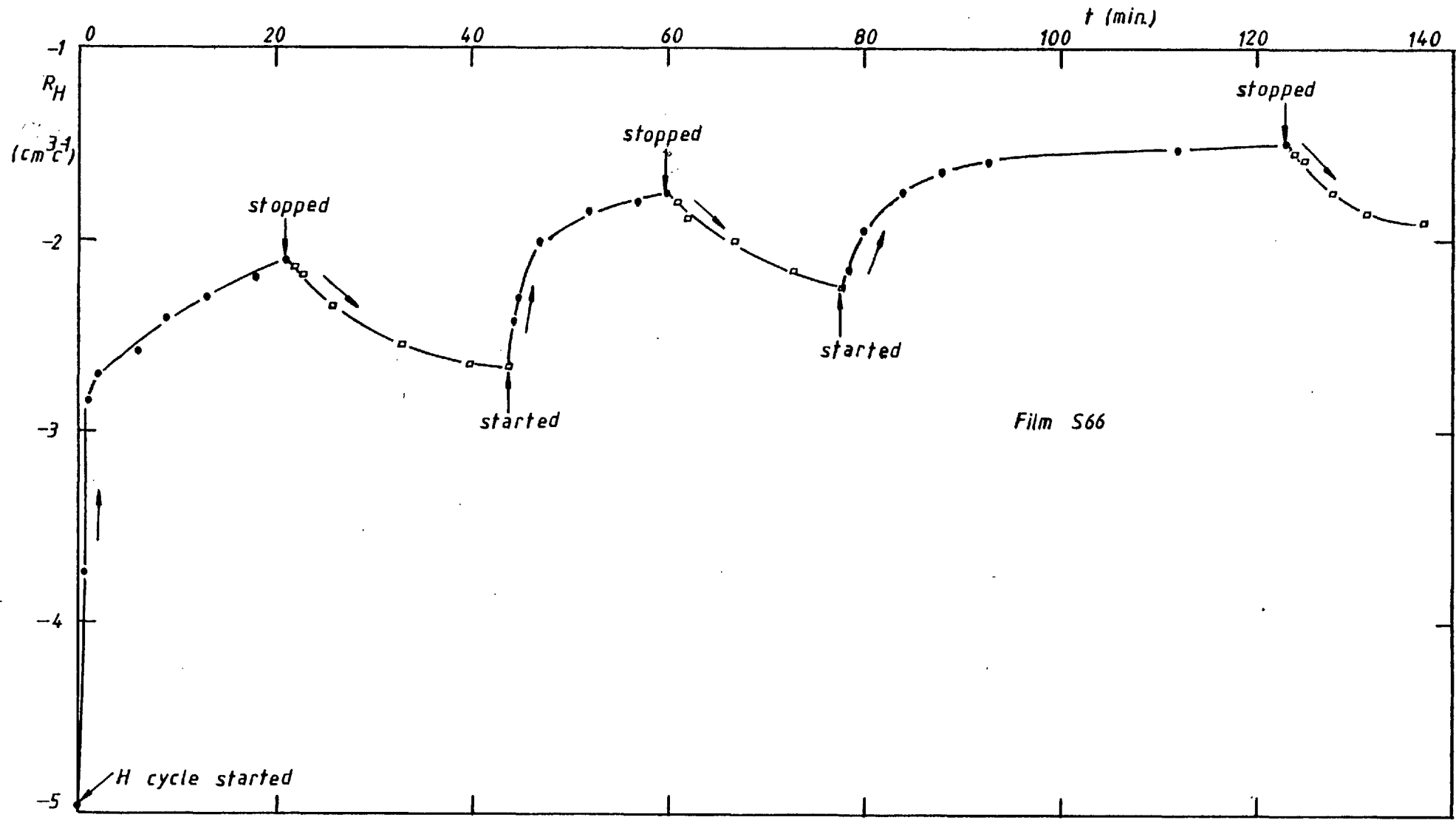


Fig.5.4 Interrupted H cycles on a 'virgin' n-type film

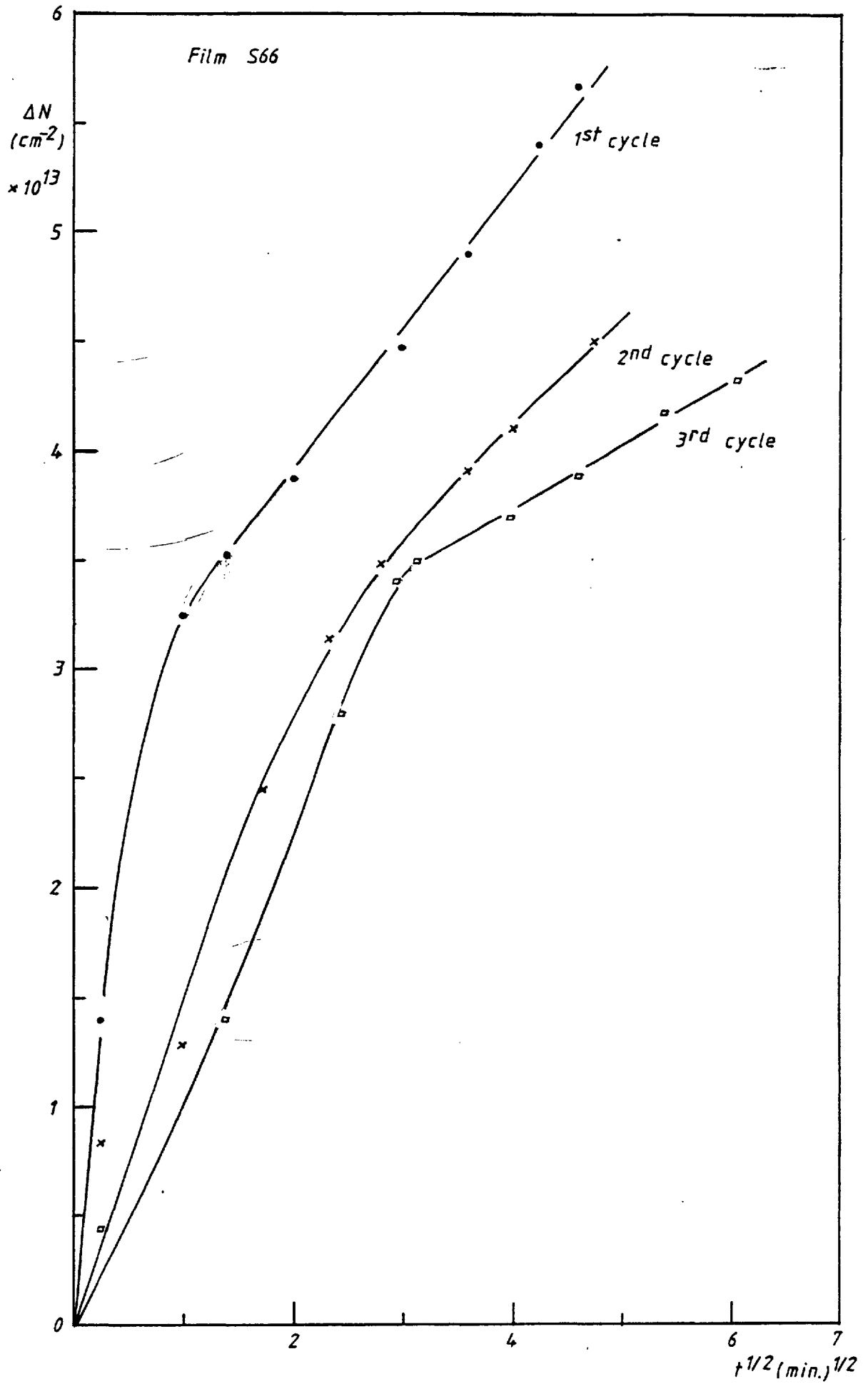


Fig. 5.5 Interrupted H-kinetics of a 'virgin' n-type film

$|R_H|$  during the period the filament was on. A graph of  $\Delta N$  vs  $t^{\frac{1}{2}}$  for these interruptions is shown in Fig. 5.5. The slopes of first, second and third cycle were  $8.3 \times 10^{11} \text{ cm}^{-2} \text{ s}^{-\frac{1}{2}}$ ,  $6.8 \times 10^{11} \text{ cm}^{-2} \text{ s}^{-\frac{1}{2}}$  and  $3.8 \times 10^{11} \text{ cm}^{-2} \text{ s}^{-\frac{1}{2}}$  respectively which meant that the rate of gas-uptake became progressively slower with each cycle.

Shown in Fig. 5.6 are the kinetics of H-uptake for  $O_2$ -driven p-type films. Compared with 'virgin' n-type films, both the rate and amount of gas uptake was smaller. A summary of these results is shown in Table 5.2.

### 5.2.2 $O_2$ Kinetics

The kinetics described first are concerned with H saturated n-type films.

In Fig. 5.7, a graph of  $-\Delta N$  vs  $\ln t$  is shown for two films, S6 and S7. These were air-exposed prior to H cycle and the films remained n-type even after long air exposures at atmospheric pressure. Both of these films followed  $\ln t$  dependence.

Fig. 5.8(a) and Fig. 5.8(b) show the kinetics of  $O_2$ -uptake for films S25 and S33. In both cases, the rate of gas-uptake was higher for the first cycle. As the films were cycled through H- $O_2$  cycles, the amount of gas-uptake decreased and it followed  $\ln t$  dependence more faithfully. The pressure dependence of  $O_2$  kinetics for H saturated n-type film S50 is shown in Fig. 5.9.



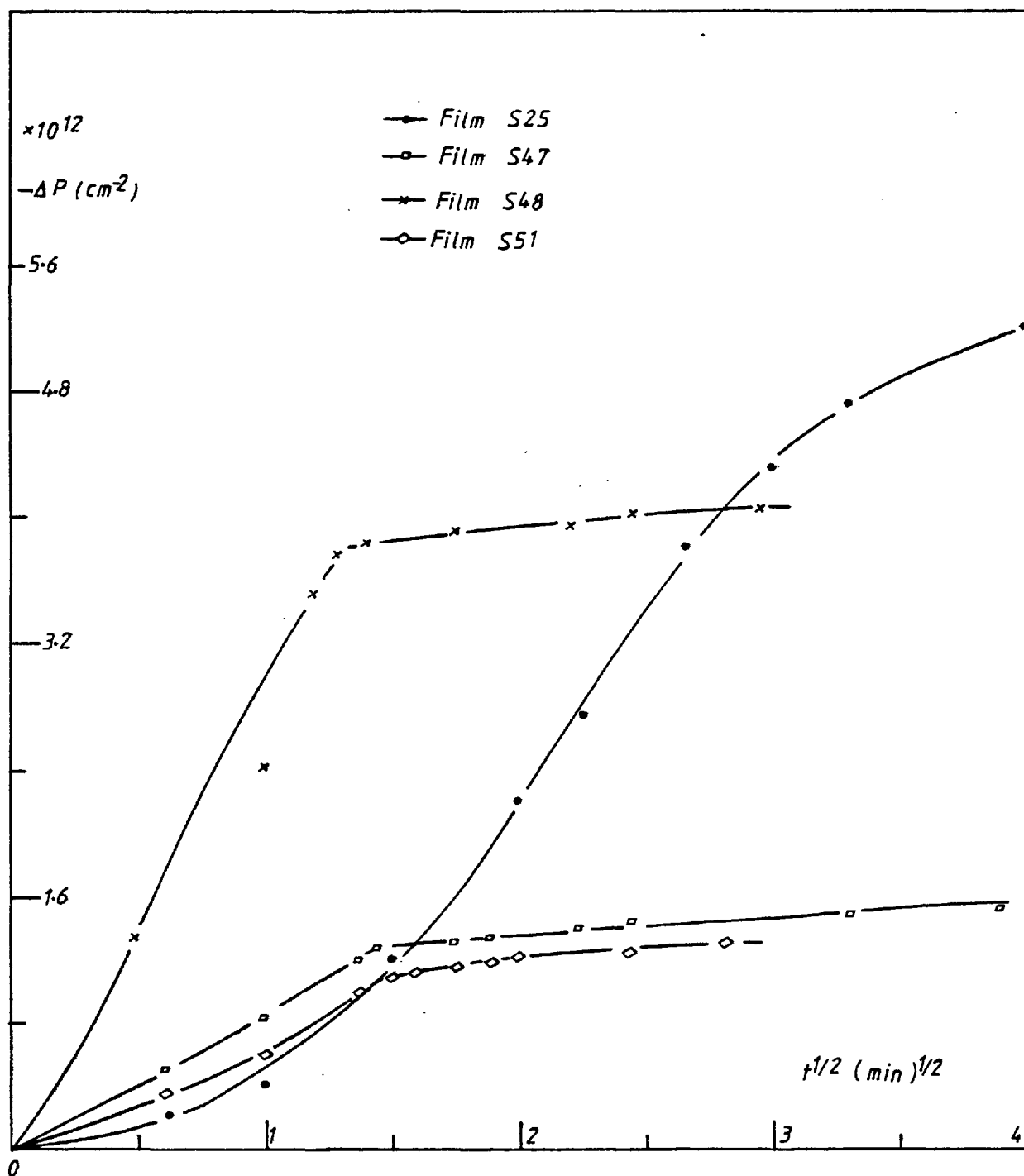


Fig. 5.6  $H$ -kinetics of  $O_2$ -driven  $p$ -type films.

Film	Conductivity type (virgin)	Deposition temperature °C	Film Thickness Å	Slope = $\frac{d\Delta N}{dt^{\frac{1}{2}}}$ cm <sup>-2</sup> sec <sup>-<math>\frac{1}{2}</math></sup>	Diffusion Coefficient, D cm <sup>2</sup> /sec	pH <sub>2</sub> x 10 <sup>-4</sup> torr
S27	n-type	250	2940	5.78 x 10 <sup>11</sup>	3.63 x 10 <sup>-14</sup>	2
S34	n-type	200	4100	5.39 x 10 <sup>11</sup>	7.1 x 10 <sup>-14</sup>	2
S37	n-type	175	2946	2.74 x 10 <sup>11</sup>	0.66 x 10 <sup>-14</sup>	0.5
S49	n-type	175	3400	0.88 x 10 <sup>11</sup>	0.39 x 10 <sup>-14</sup>	0.6
S50	n-type	175	2900	1.17 x 10 <sup>11</sup>	0.33 x 10 <sup>-14</sup>	0.6

Table 5.1

(H-effect on 'virgin' n-type films at room temperature)

Film	Conductivity type prior to gas cycle	Deposition temperature °C	Film thickness Å	Slope = $\frac{d \Delta P }{dt^{\frac{1}{2}}}$ cm <sup>-2</sup> sec <sup>-<math>\frac{1}{2}</math></sup>	pH <sub>2</sub> x 10 <sup>-4</sup> torr
S47	p-type	175	2900	1.3 x 10 <sup>10</sup>	0.4
S48	p-type	175	2000	1.94 x 10 <sup>10</sup>	0.6
S51	p-type	175	2049	1.89 x 10 <sup>10</sup>	0.6

Table 5.2

(H-effect on O<sub>2</sub>-driven p-type films at room temperature)

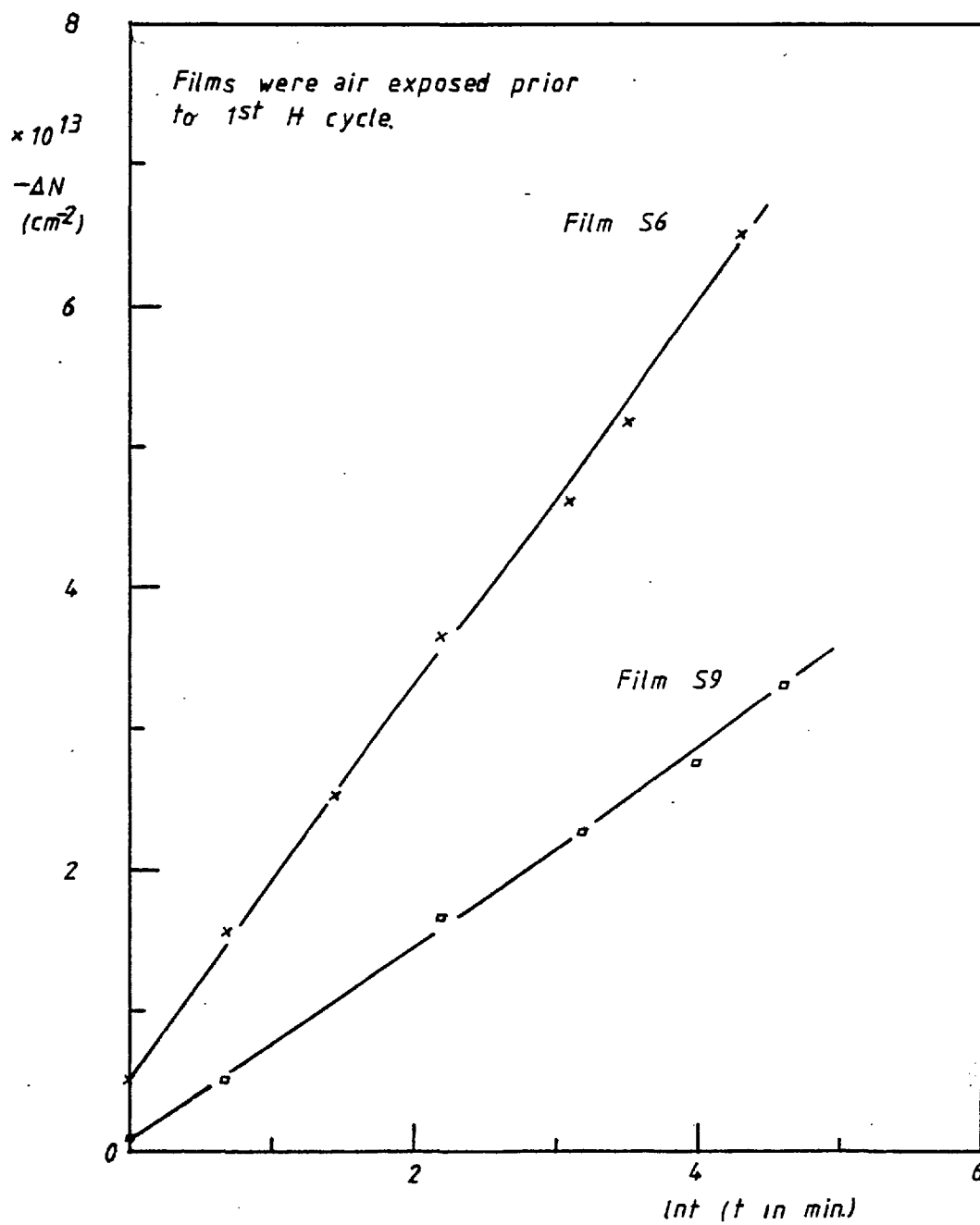
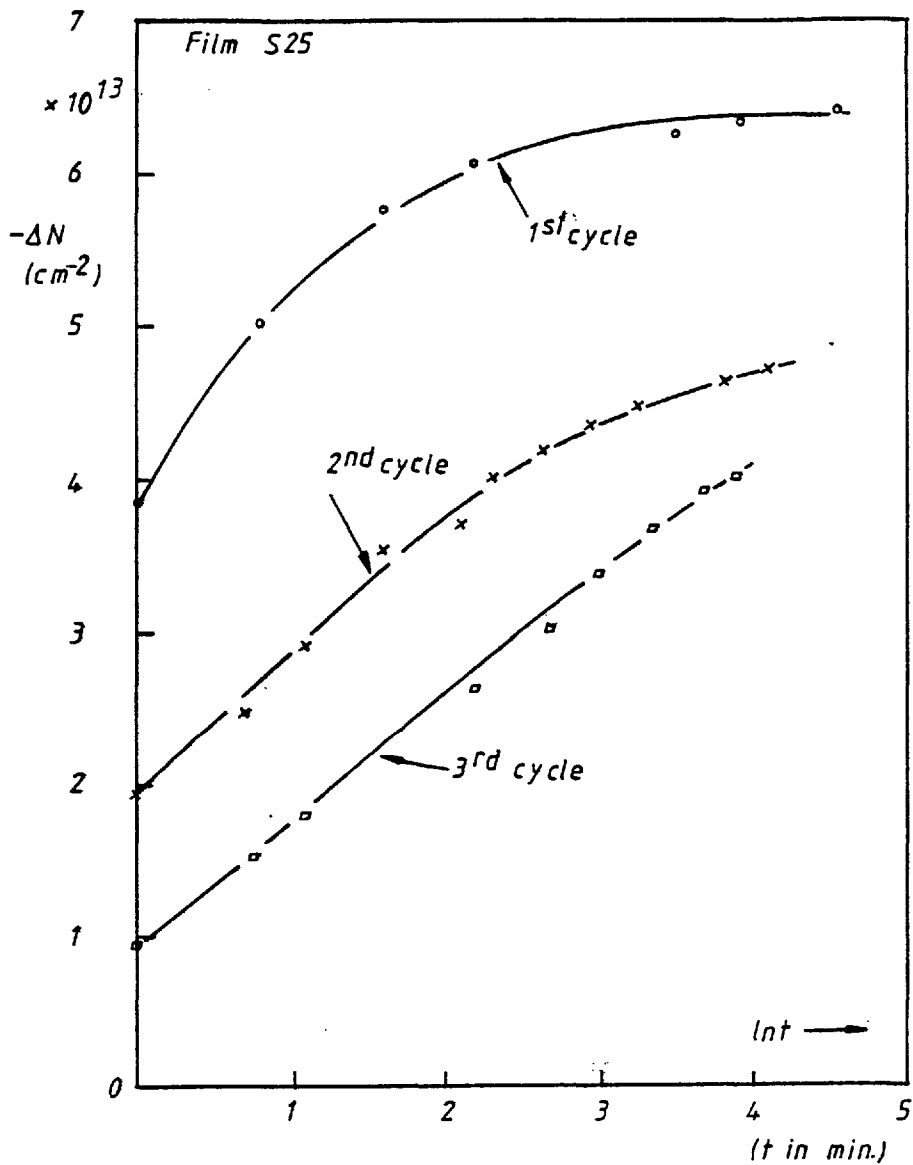
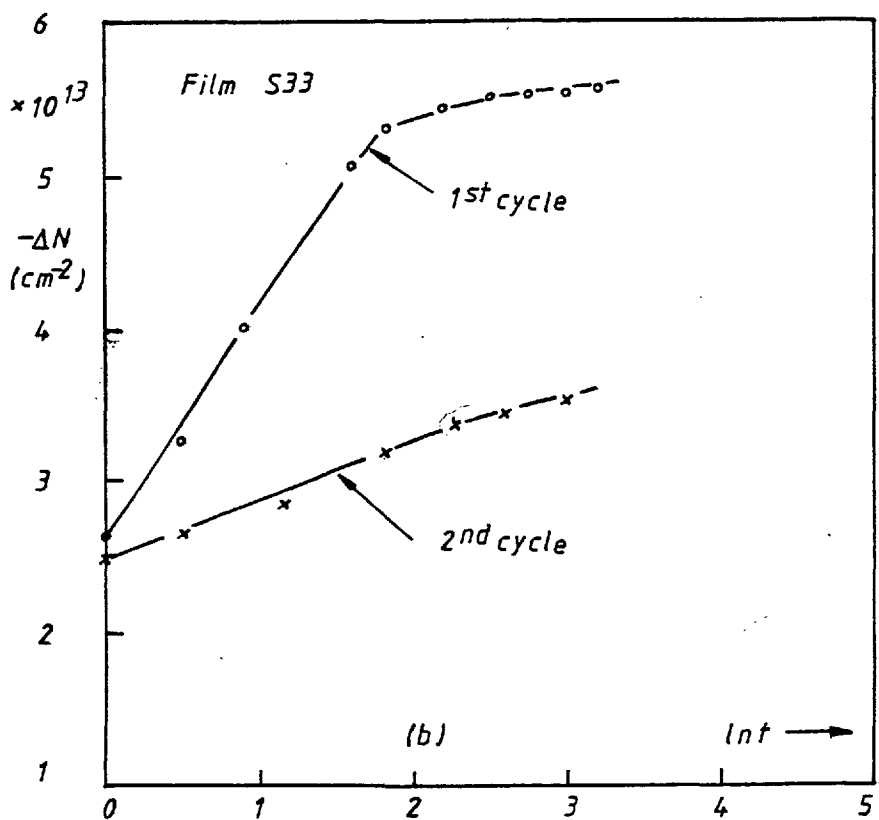


Fig.5.7  $\text{O}_2$  kinetics of hydrogenated films



(a)



(b)

Fig. 5.8  $O_2$ -kinetics of H-saturated films.

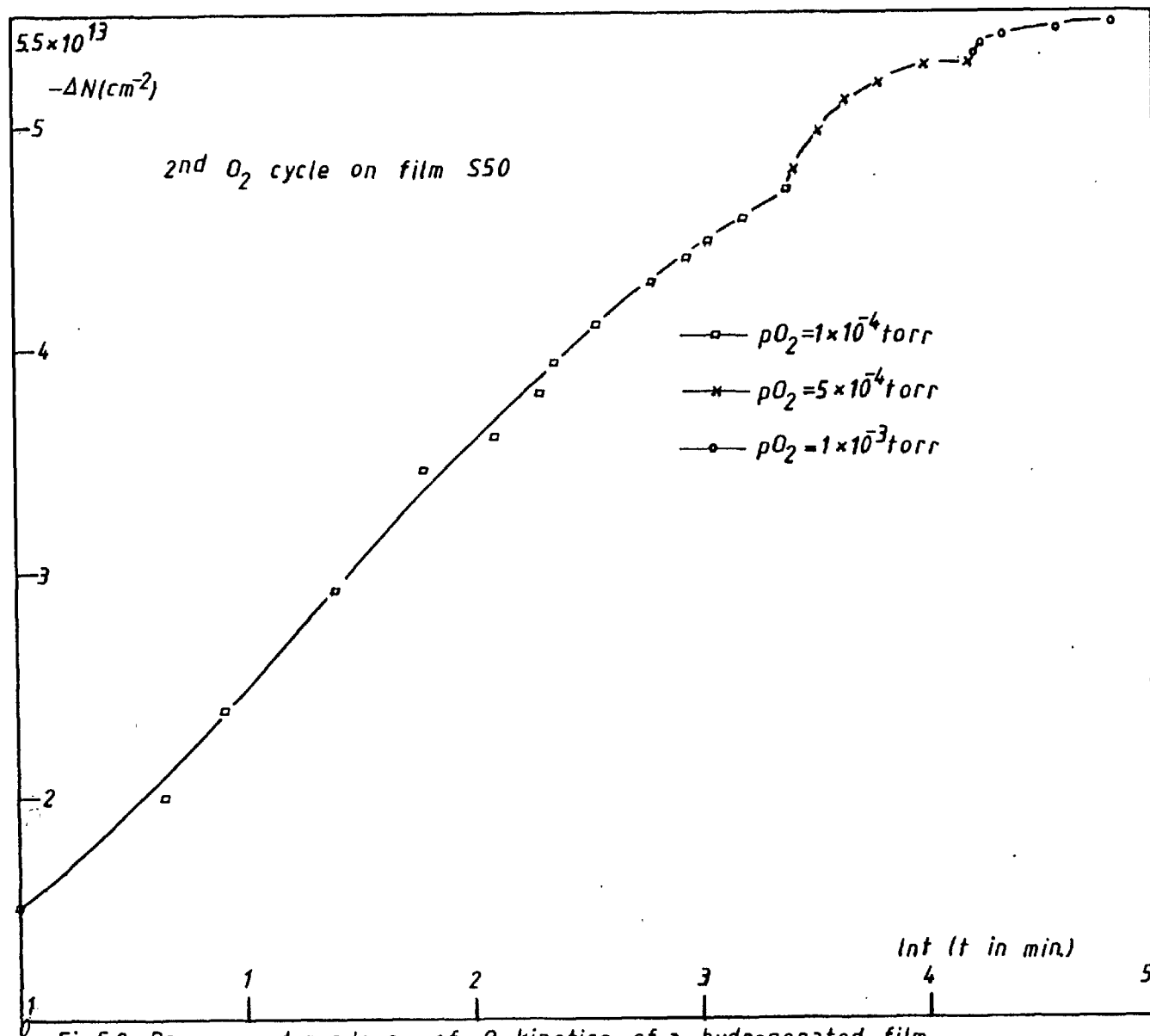


Fig.5.9 Pressure dependence of O<sub>2</sub> kinetics of a hydrogenated film

The changes in  $R_H$  as a function of time,  $t$  are shown in Fig. 5.10 for a 'virgin' n-type film when exposed to  $O_2$  at  $1 \times 10^{-4}$  torr. The film turned p-type after 22 mins and when  $R_H$  reached a value of  $24 \text{ cm}^3/\text{C}$ , the  $O_2$  supply was stopped and film S53 was kept in a vacuum of  $\sim 1 \times 10^{-6}$  torr for 38 mins. During this period, changes in  $R_H$  were small as seen from Fig. 5.10. When the  $O_2$  supply was restored at  $1 \times 10^{-4}$  torr,  $R_H$  started to increase again. The film was left at this pressure overnight and as a result  $R_H$  rose to  $53 \text{ cm}^3/\text{C}$  and when the film was exposed to air at atmospheric pressure,  $R_H$  decreased to  $8.5 \text{ cm}^3/\text{C}$  within 3 mins. Film S53 was driven n-type and 'saturated' with H and exposed to  $O_2$  at  $1 \times 10^{-4}$  torr again. The kinetics of  $O_2$ -uptake are shown in Fig. 5.11(a). The oxygen supply was terminated for 25 mins. During the first 18 mins of this interruption,  $R_H$  changed from  $-23.5 \text{ cm}^3/\text{C}$  to  $-25.4 \text{ cm}^3/\text{C}$  but during the next 7 mins, it rose to  $-43.3 \text{ cm}^3/\text{C}$ . When the  $O_2$  supply was restarted, the kinetics followed by the  $O_2$ -uptake are shown in Fig. 5.11(b). As the two graphs show, the amount of gas-uptake for the first  $O_2$  cycle was higher than that for the second cycle (after 25 mins pause).

Fig. 5.12 shows the effect of exposing 'virgin' p-type film to  $O_2$ . Plots of  $\Delta P$  vs  $\ln t$  and  $\Delta P$  vs  $t^{\frac{1}{2}}$  are shown in this figure.

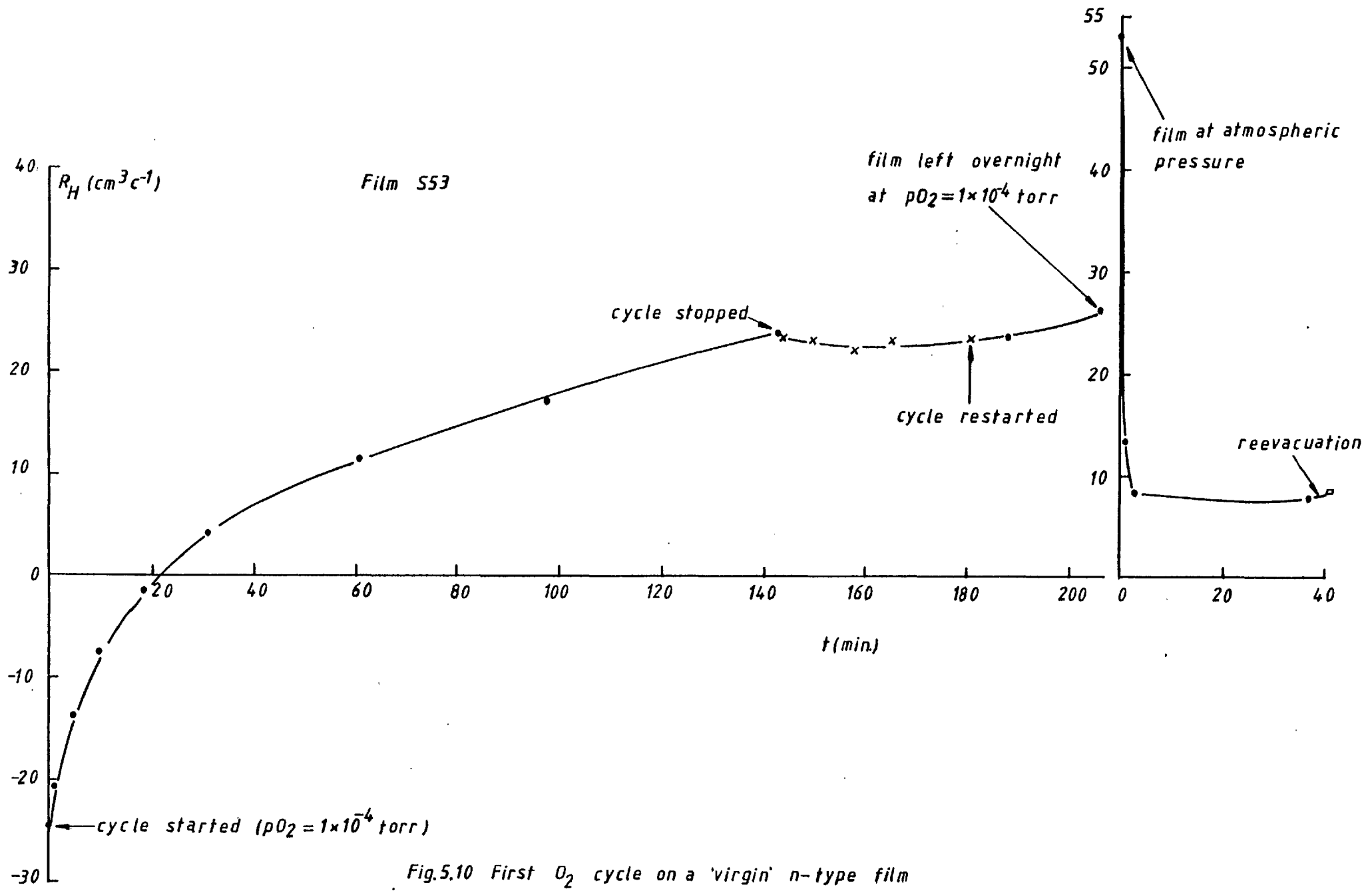


Fig.5.10 First  $O_2$  cycle on a 'virgin' n-type film

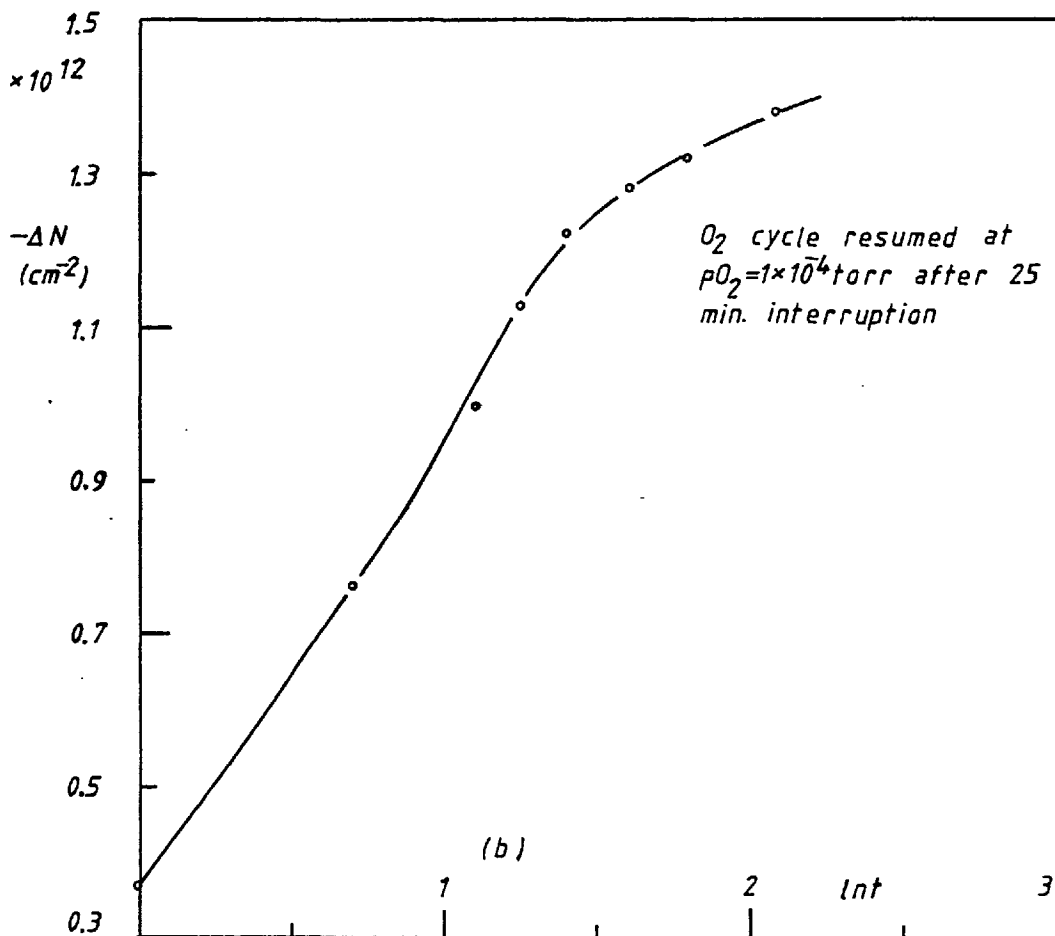
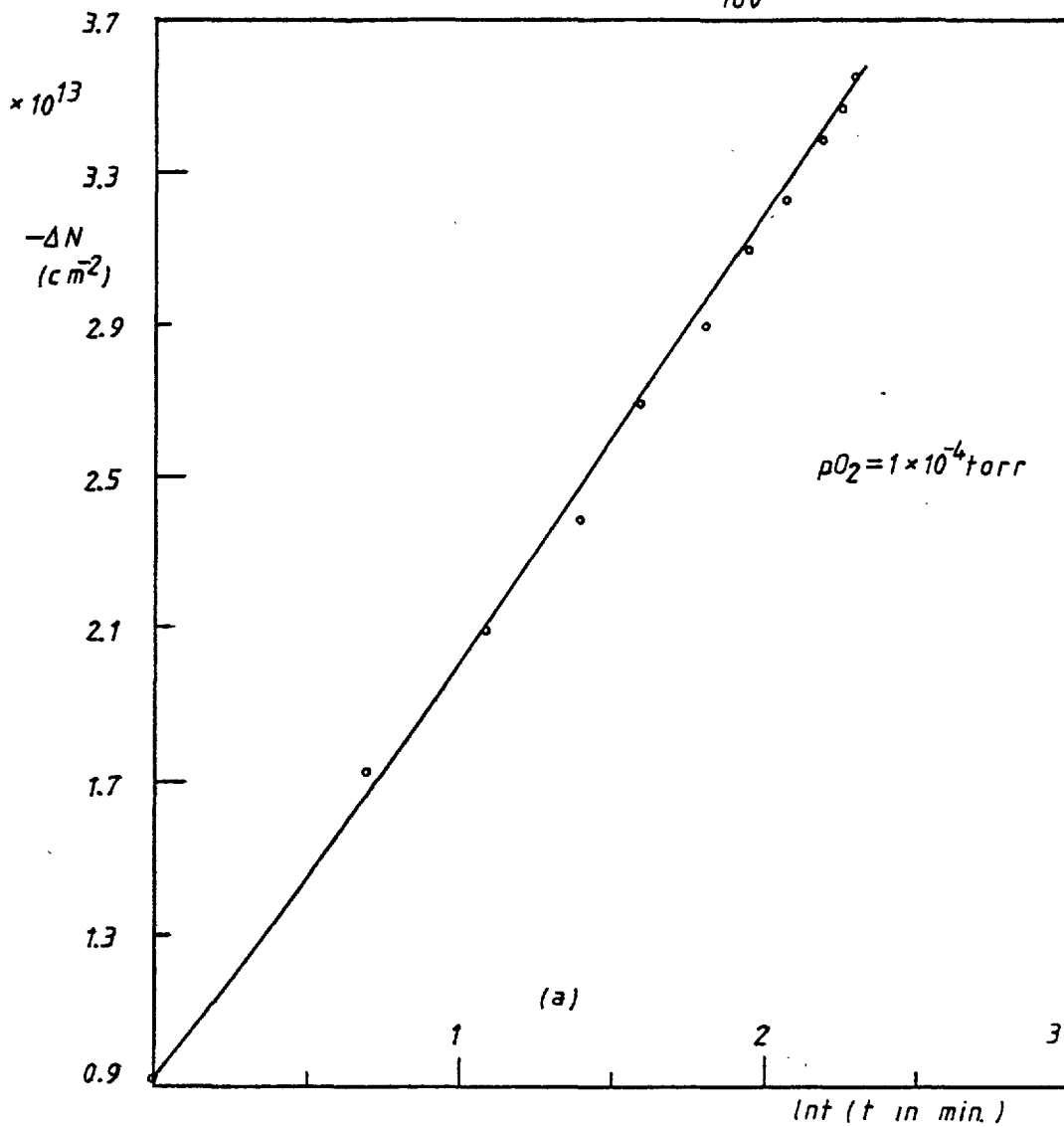


Fig.5.11  $O_2$  kinetics of hydrogenated film S53 (2<sup>nd</sup> cycle)



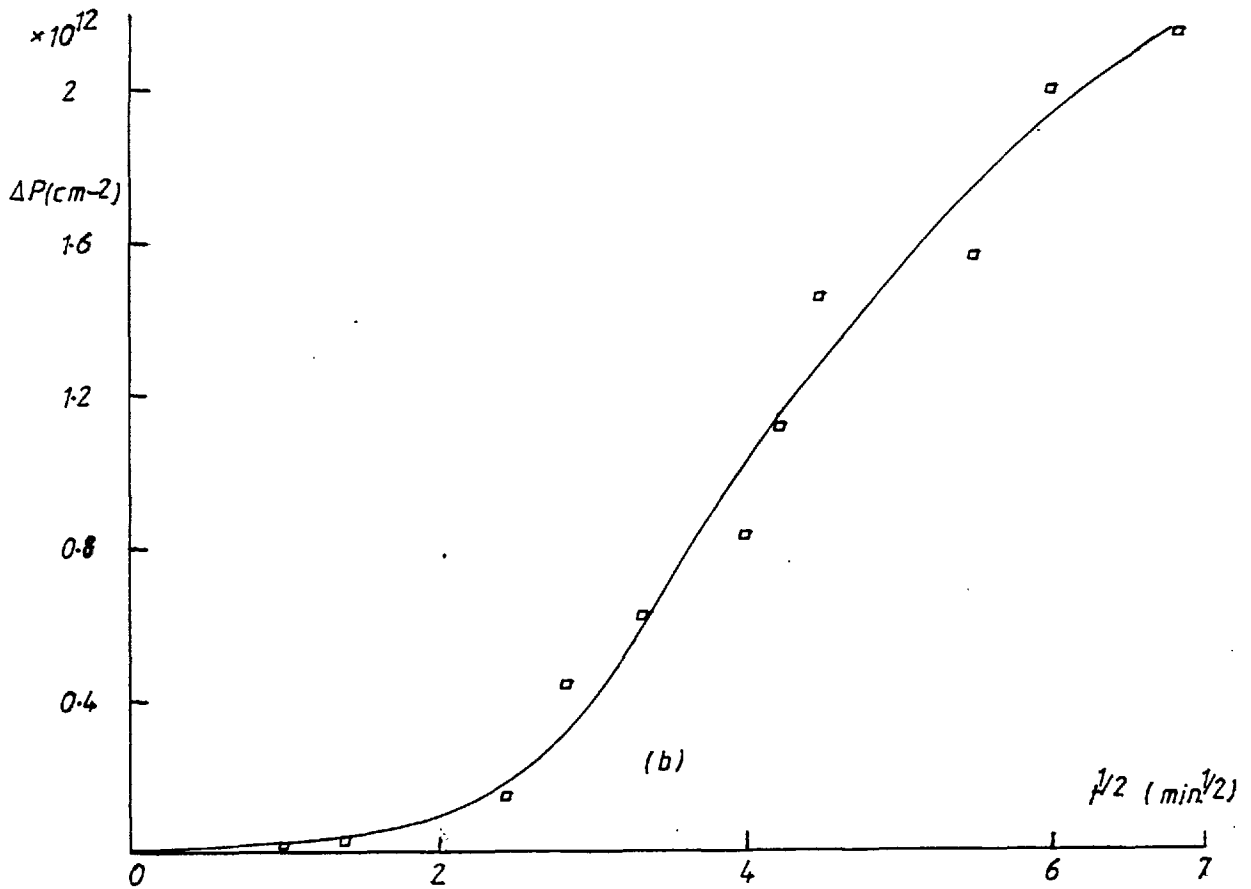
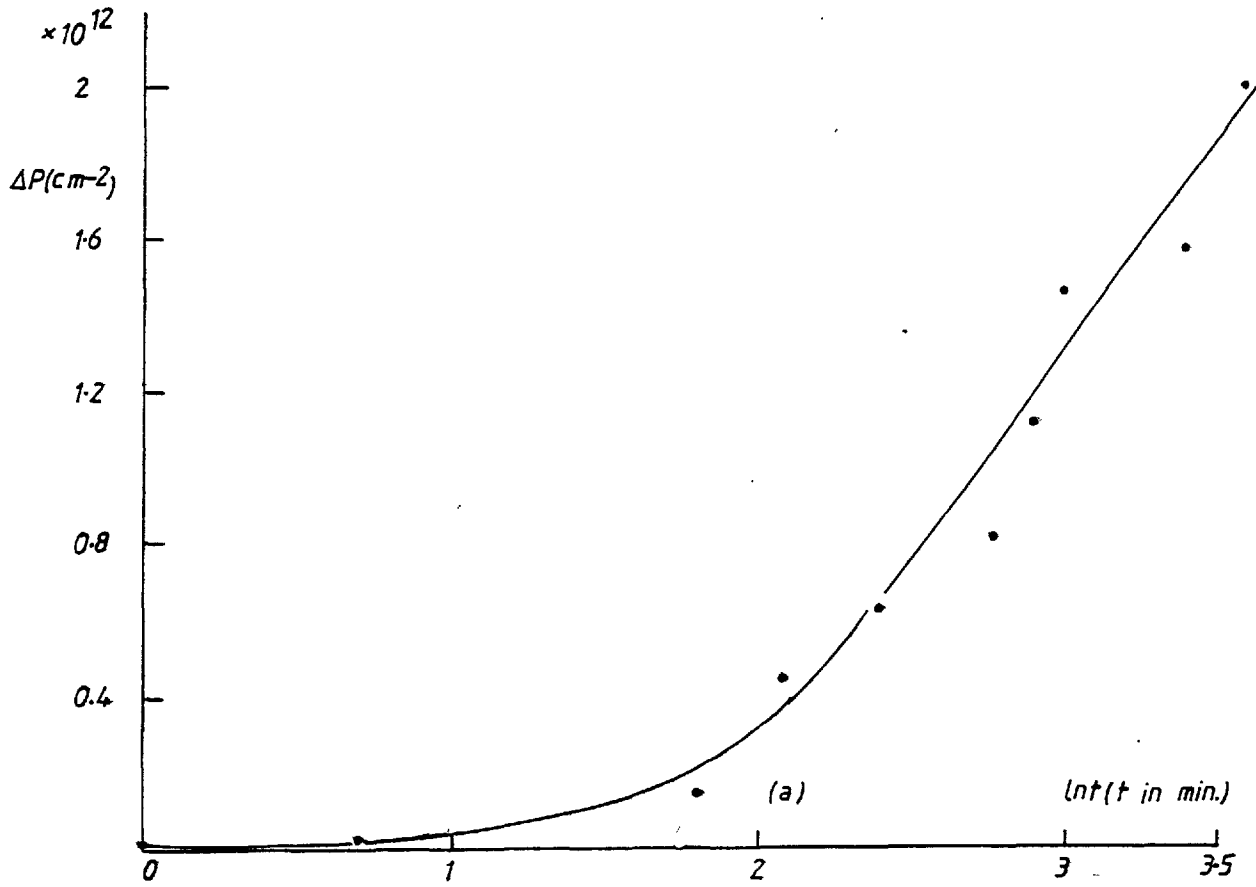


Fig. 5.12  $\text{O}_2$  Kinetics of film S51

### 5.3 DISCUSSION OF RESULTS

#### 5.3.1 H Effect

The following points can be made at the outset.

- (i) H<sub>2</sub> had no observable effect on PbTe films
- (ii) H had a donor-like effect on PbTe films

An attempt will now be made to resolve the question of mechanism(s) of gas-uptake by considering the results of kinetic studies as well as the theoretical models described in chapter 4.

#### 5.3.1 (a) 'Virgin' n-type Films

If H effect can be described as a surface effect, then H occupies lead vacancies at the surface and donates an electron to the conduction band. This will result in an accumulation layer being formed at the surface. As time progresses, the accumulation layer will grow and so will the band bending. Bearing in mind the values of  $\Delta N$  involved ( $>10^{13}$  cm<sup>-2</sup> - see Fig. 5.2), two questions may be raised regarding the surface model.

- (i) What is the band bending for such values of  $\Delta N$ ?
- (ii) What is the influence of surface quantisation?

Many et al. (M4) give a relationship between the excess surface carrier density  $\Delta N$  and the bulk value,

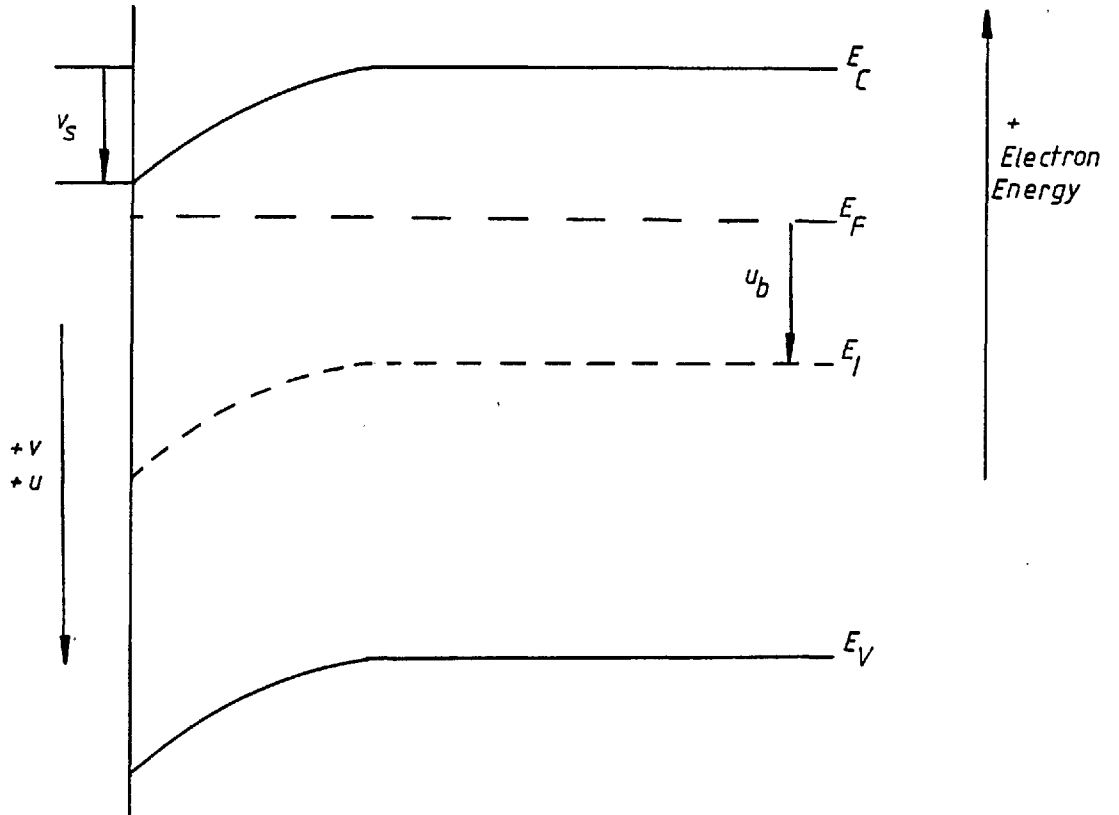
$n_b$ .

$$\Delta N = n_b L G^+(u_b, v_s) \quad (5.14)$$

where  $L$  is the Debye length and graphical representation of the surface function  $G^+(u_b, v_s)$  as a function of  $u_b$  and  $v_s$  is given by Many et al. (M4). In order to evaluate  $v_s$  from equation (5.14), the flat-band ( $v_s=0$ ) condition must be known. If one assumes that the bands are flat prior to the gas cycle, estimates of  $v_s$  can be made for experimentally observed values of  $\Delta N$ . Although there was no experimental justification for this assumption, it was assumed that the bands were flat prior to H cycle in order to estimate the order of magnitude of  $v_s$ . This is shown in Table 5.3. As can be seen from Table 5.3, a charge accumulation in excess of  $10^{13} \text{ cm}^{-2}$  was produced. This raises the possibility of quantisation effects.

In case of strong accumulation

carriers become confined in a deep potential well at the surface and momentum of the carriers in the direction normal to the surface becomes quantised (M6). In the case of quantisation, band bending is larger for a given surface space charge compared with the classical case. Under such conditions, expressions for surface charge given by Many et al. (M4) for a classical case or Seiwatz and Green (S11) for a degenerate case cannot be used since both of these treatments neglect quantum effects. This implies that the surface function requires



(Definition of energy parameters)

Fig. T.1: n-type semiconductor under accumulation

$n_b$ ( $\text{cm}^{-3}$ )	Film	Deposition temp. $^{\circ}\text{C}$	Film thickness $\text{\AA}$	$u_b$ (in kT)	$L$ (in $\text{\AA}$ )	$\Delta N$ $\text{cm}^{-2} \times 10^{13}$	$v_s$ (kT)
$4 \times 10^{16}$	S49	175	3400	1.68	1198	1	5.5
$4.5 \times 10^{16}$	S27	250	2940	1.8	1138	5	8.5
$3.26 \times 10^{17}$	S34	200	4100	3.8	433	4	6
$1.26 \times 10^{18}$	S66	150	3400	5	220	5	5.3

H effect on 'virgin' n-type films

Table 5.3

modification to take quantisation into account.

According to Greene (G8), correction for surface function becomes significant in the case of strong accumulation when the electric field,  $E_s$  due to the space charge region,

$$E_s \geq 6 \times 10^4 \left( \frac{m_d^*}{m_0} \right) \text{ volt cm}^{-1} \quad (5.15)$$

at room temperature where  $m_d^*$  is the density of states effective mass and  $m_0$  is the free electron mass. For PbTe at room temperature  $E_s \sim 1.5 \times 10^4 \text{ V cm}^{-1}$  which give gives a space charge,  $Q_{sc} \sim 3.5 \times 10^{12} \text{ cm}^{-2}$ . As mentioned earlier, a space charge in excess of  $10^{13} \text{ cm}^{-2}$  was encountered suggesting that the quantisation might have occurred. But as Fig. 5.13 shows, quantisation did not have an adverse effect on the Hall mobility of electrons. Using equation (5.16),

$$\% \text{ change in } \mu_H = \left( \frac{\mu_{HO} - \mu_{Ht}}{\mu_{HO}} \right) 100 \quad (5.16)$$

where  $\mu_{HO}$  is the Hall mobility prior to H cycle and  $\mu_{Ht}$  is the Hall mobility after time, t during the gas cycle. Maximum change observed in  $\mu_H$  was 8.2% for S66, 6.9% for S49, 12% for S34 and 13.6% for S27. Zemel and Kaplit (Z6) also found that  $\mu_H$  for p-type PbSe films grown on NaCl was substantially independent of the surface charge ( $\sim 5 \times 10^{13} \text{ cm}^{-2}$ ).

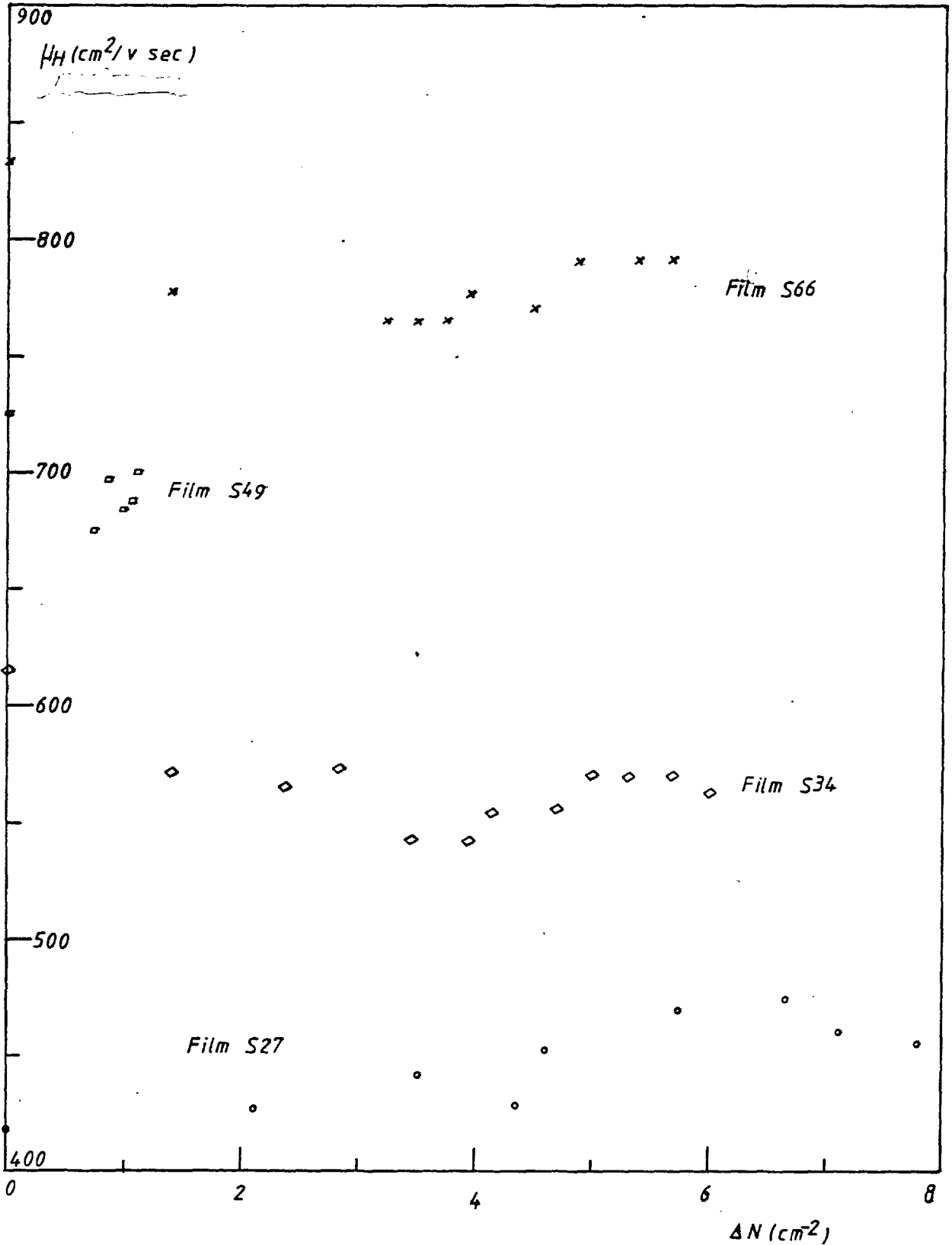


Fig. 5.13  $\mu_H$  vs.  $\Delta N$  for H effect on 'virgin' n-type films

The effect of interrupted H cycles on 'virgin' n-type films is shown in Fig. 5.4 and Fig. 5.5. This was typical behaviour of the three films for which this effect was investigated at room temperature. Two points are worth noting.

- (i) After each interruption, the rate of gas-uptake is slower (Fig. 5.5).
- (ii) Changes in  $|R_H|$  during the period the filament is 'on' are greater compared with changes in  $|R_H|$  during the period the filament is 'off' even though the two periods are approximately of the same duration (Fig. 5.4).

From the above it may be inferred that the mechanism of H uptake is not a unique one. If the mechanism of gas-uptake was just a surface model, then changes in  $|R_H|$  during the 'on' and 'off' periods should be the same. If, on the other hand, the mechanism is a diffusion type process, then there should be no *appreciable* changes in  $|R_H|$  during the 'off' period. Progressively slower rates of gas-uptake after each interruption seems to suggest that some H has permanently been incorporated into the film (even when the 'off' period was extended to 23 hours in vacuum of  $\sim 10^{-6}$  torr,  $R_H$  of film S66 was  $-2.42 \text{ cm}^3/\text{C}$  whereas  $R_H$  was  $-4.95 \text{ cm}^3/\text{C}$  before the gas cycle commenced). Consequently, the concentration

gradient between the gaseous ambient and the film becomes progressively shallower. Relatively fast initial uptake after each interruption also suggests that some out-diffusion of H during the 'off' period may have occurred.

Kinetics of H uptake shown in Fig. 5.2 suggest that after the initial fast rise, the gas-uptake is a diffusion limited mechanism. It was possible to fit  $\ln t$  dependence for kinetics of the initial H uptake. This is shown in Fig. 5.14. This is in common with Egerton and Crocker (E4) who observed similar kinetics for H uptake on PbTe films. A similar  $t^{\frac{1}{2}}$  dependence of H uptake for thin film epitaxial films of PbSe (M7) and  $\text{Pb}_{1-x}\text{Sn}_x\text{Te}$  (H1) has also been observed. However, it must be noted that the films used by McLane (M7) were air exposed prior to H cycle. If the mechanism of H uptake is a diffusion process, one may pose the following questions.

- (i) Is H diffusing into the film? and
- (ii) can the diffusion coefficient of H be associated with the self-diffusion coefficient of lead in PbTe?

The value of the self-diffusion coefficient of lead  $D_{\text{Pb}}$  in PbTe at room temperature can be extrapolated from previously published data. This, unfortunately, can give rise to large discrepancies in  $D_{\text{Pb}}$ . For example,  $D_{\text{Pb}} \sim 2.5 \times 10^{-15} \text{ cm}^2 \text{ s}^{-1}$  in p-type PbTe single crystal with  $p = 10^{17} \text{ cm}^{-3}$  (R1) whereas  $D_{\text{Pb}} \sim 10^{-18} \text{ cm}^2 \text{ s}^{-1}$  for



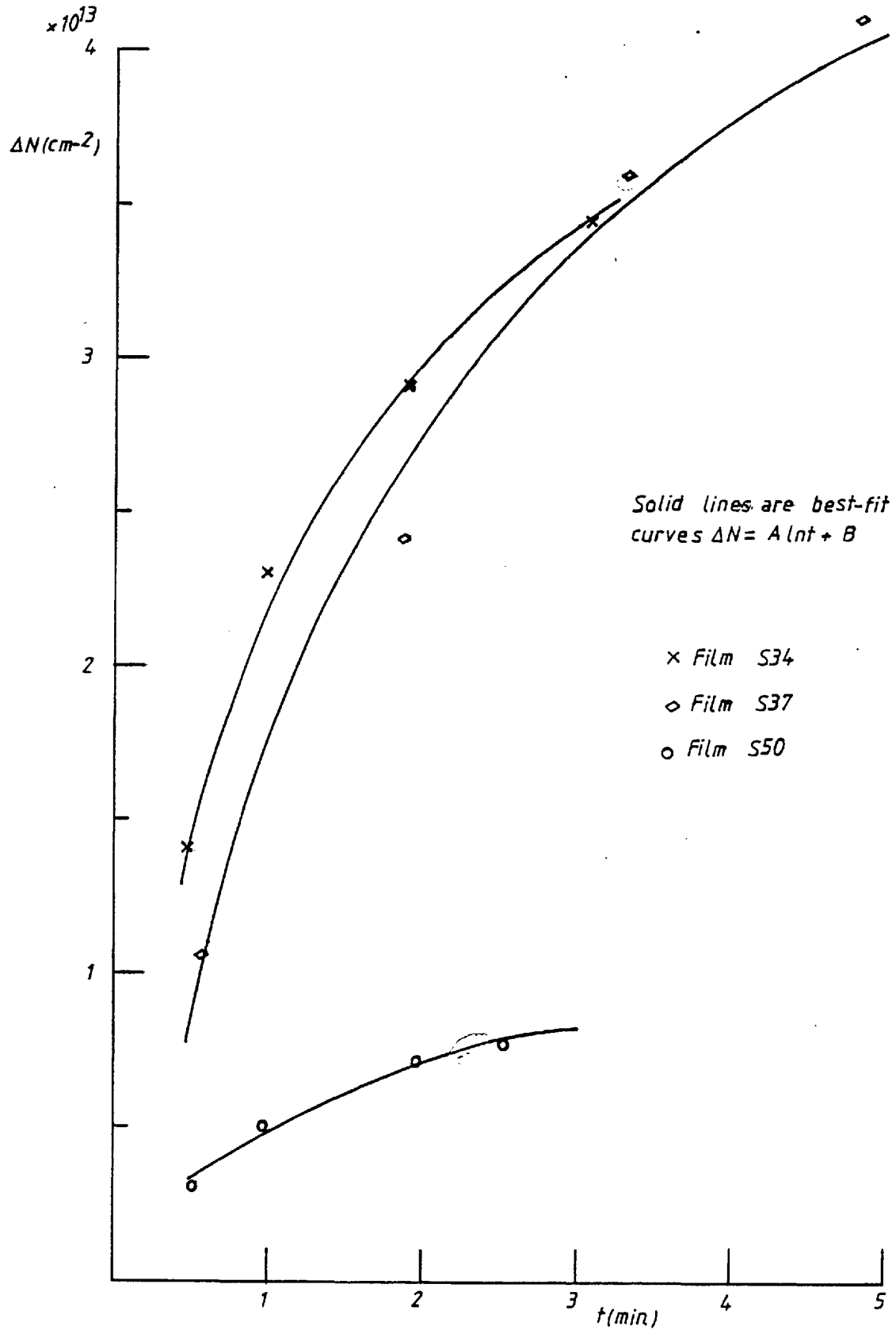


Fig. 5.14  $\Delta N$  vs.  $t$  For Initial Uptake Of H

p-type single crystal PbTe, with  $p = 3 \times 10^{18} \text{ cm}^{-3}$  (G9). Calawa et al (C7) give a value of  $D_{\text{Pb}} \sim 1.9 \times 10^{-21} \text{ cm}^2 \text{ s}^{-1}$  for single p-type PbSe. The values of diffusion coefficient in the present study are in the range  $10^{-14}$ - $10^{-15} \text{ cm}^2 \text{ s}^{-1}$ . Similar values of diffusion coefficient were obtained by Young (Y3) for H effect on epitaxial PbSe films grown on NaCl but his films were air exposed and p-type. Therefore, it is difficult to compare the values of diffusion coefficient obtained during the present study with the values obtained by other workers.

#### 5.3.1(b) H Effect on O<sub>2</sub>-driven p-type Films

Typical examples of H effect on O<sub>2</sub>-driven p-type films are shown in Fig. 4.3 to Fig. 4.6 (chapter 4) where H turns the films less p-type by neutralising the excess hole concentration. In terms of the surface model, H creates a depletion layer on the surface of a p-type bulk. Once again the determination of the resultant band bending is difficult since it is not known whether the bands are flat prior to H exposure. However, a tentative estimation of  $v_s$  may be made as follows.

The range of values of  $v_s$  for the theoretical  $R_H$  vs  $\rho$  curve predicted by the computer program was from -10 kT to 20 kT, i.e. it embraced regions of accumulation and depletion (see Fig. 4.11). By

superimposing the experimental values of  $R_H$  and  $\rho$  prior to H cycle with the theoretical values, the corresponding band bending could be estimated. In cases of films S25 and S51, there was an accumulation layer giving rise to a band bending of  $\sim -1$  kT whereas for films S47 and S48 the bands were flat prior to the H cycle. In Table 5.4, the estimated values of  $v_s$  and other pertinent parameters are shown. Surface functions given by Many et al. (M4) were used to estimate  $v_s$ . As can be seen from Table 5.4,  $v_s > 2 u_b$  in all cases, i.e. inversion has occurred and the majority carriers in the surface region are electrons. This implies that a large electric field would be set up due to the space charge at the surface.

As mentioned in chapter 4, the fit between the theoretical and experimental  $R_H$  vs  $\rho$  curve during the initial stages of H cycle is very good. Fig. 4.11 is a typical example of this. Therefore, it is tempting to infer that the surface adsorption model describes H uptake during the initial stages. Since  $t^{\frac{1}{2}}$  dependence (Fig. 5.6) is followed by H uptake after the initial fast uptake, this further suggests that surface adsorption precedes diffusion.

The mechanism of H uptake in the case of air exposed film is complicated further when one considers the possibility of an oxide growth due to the interaction of the film with air. A recent study by Bettini and

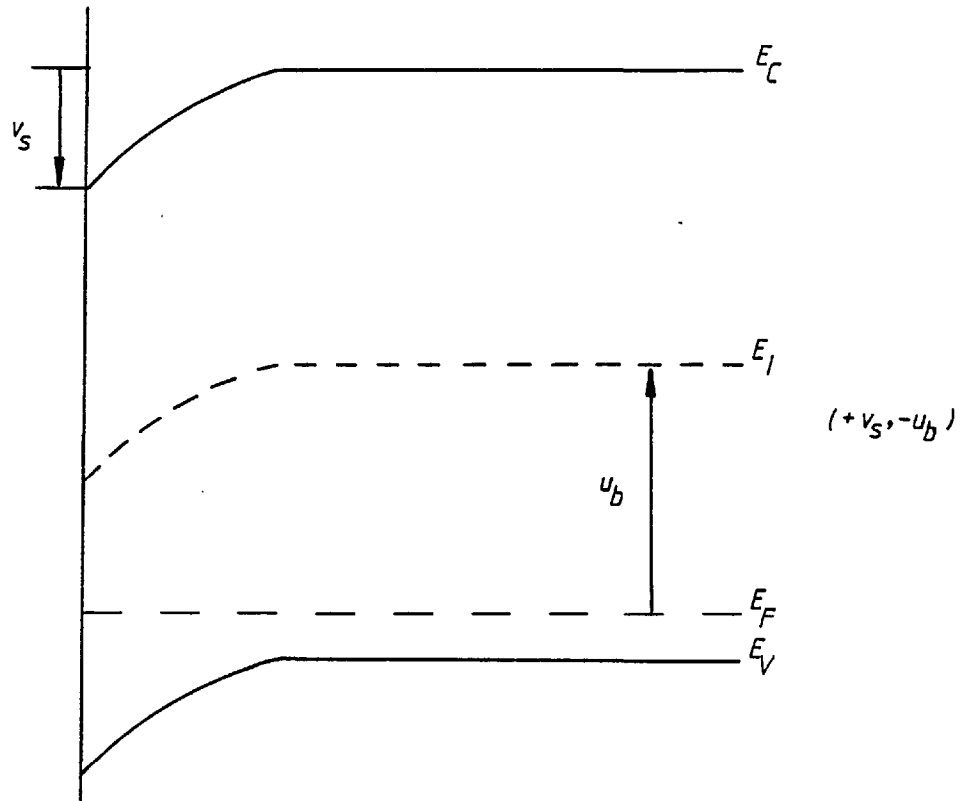


Fig. T.2: p-type semiconductor under depletion

Film	Deposition temp. °C	Film thickness Å	$P_b \text{ cm}^{-3}$ $\times 10^{17}$	$L$ (in Å)	$-u_b$ (kT)	No. of holes neutralised $-(\Delta P) \text{ cm}^{-2}$	$v_s$ (kT)
S47	175	2900	2.68	477	3.3	$1.4 \times 10^{12}$	8
S48	175	2000	2.65	480	3.3	4	9.3
S51	175	2049	3.93	394	3.7	1.2	9.4
S25	170	2038	3.69	407	3.6	4	10.7

H effect on  $O_2$ -driven p-type films

Table 5.4

Richter (B10) has provided evidence for oxide growth on epitaxial films of PbTe when the films were exposed to air. They investigated the oxidation of PbTe films, 5-10  $\mu\text{m}$  in thickness, grown on  $\text{BaF}_2$  with carrier concentration  $\sim 10^{17}$ - $10^{18}$   $\text{cm}^{-3}$  using the techniques of x-ray photo-electron spectroscopy (XPS) and LEED in ultra-high vacuum system. They concluded that the surface became oxidised after a prolonged exposure to air (several days) where  $\text{PbO}$  and  $\text{TeO}_2$  were the oxidation products.

#### 5.3.1(c) H Effect on 'Virgin' p-type Films

Fig. 4.6 and Fig. 4.7 (chapter 4) illustrate the effect of first H cycle on 'virgin' p-type films. This behaviour was typical of all 'virgin' p-type films (four in all). Interpretation of results in this case is difficult because of the following reasons.

- (i) All the 'virgin' p-type films had low carrier concentration (i.e.  $\times 10^{16}$   $\text{cm}^{-3}$ , see Table 4.2) and it was found difficult during the present study to grow p-type films.
- (ii) Almost instantaneous change-over (see Table 4.2) from p-type to n-type is difficult to reconcile with either surface or diffusion model.
- (iii) Since the films not only change over from p- to n-type but also from two carrier type to substantially single

carrier type, the kinetic study of gas-uptake becomes obscure.

However, once the films become n-type (single carrier) H uptake may be plotted as a function of time. This has been done for films S25 and S33 and is shown in Fig. 5.15. Film S33 was grown at 175°C and its thickness was 2600Å.

In order to resolve the question of an instantaneous turnover from p- to n-type, a typical  $R_H$  vs time curve of H effect on an  $O_2$ -driven p-type film (S48) has been plotted in Fig. 5.16. As can be seen from Fig. 5.16, once  $R_H$  starts to decrease after reaching a peak the changeover from p- to n-type is rather fast. For example,  $R_H$  changed from 105.3 cm<sup>3</sup>/C to -173 cm<sup>3</sup>/C in 4 mins. Even though this changeover is slower than that for 'virgin' p-type films (see Table 4.2), it indicates that the value of  $R_H$  of 'virgin' p-type films prior to first H cycle lies in the range FC in Fig. 5.1.

Before concluding the discussion of H effect on PbTe films, possibilities of H incorporation into PbTe film other than through lead vacancy occupation will now be discussed.

As mentioned previously, there exists a large discrepancy in the extrapolated value of self-diffusion coefficient of lead  $D_{Pb}$  (reported in the literature) in PbTe and other lead salts. Furthermore, the value of  $D_{Pb}$  for thin films will be different compared with the

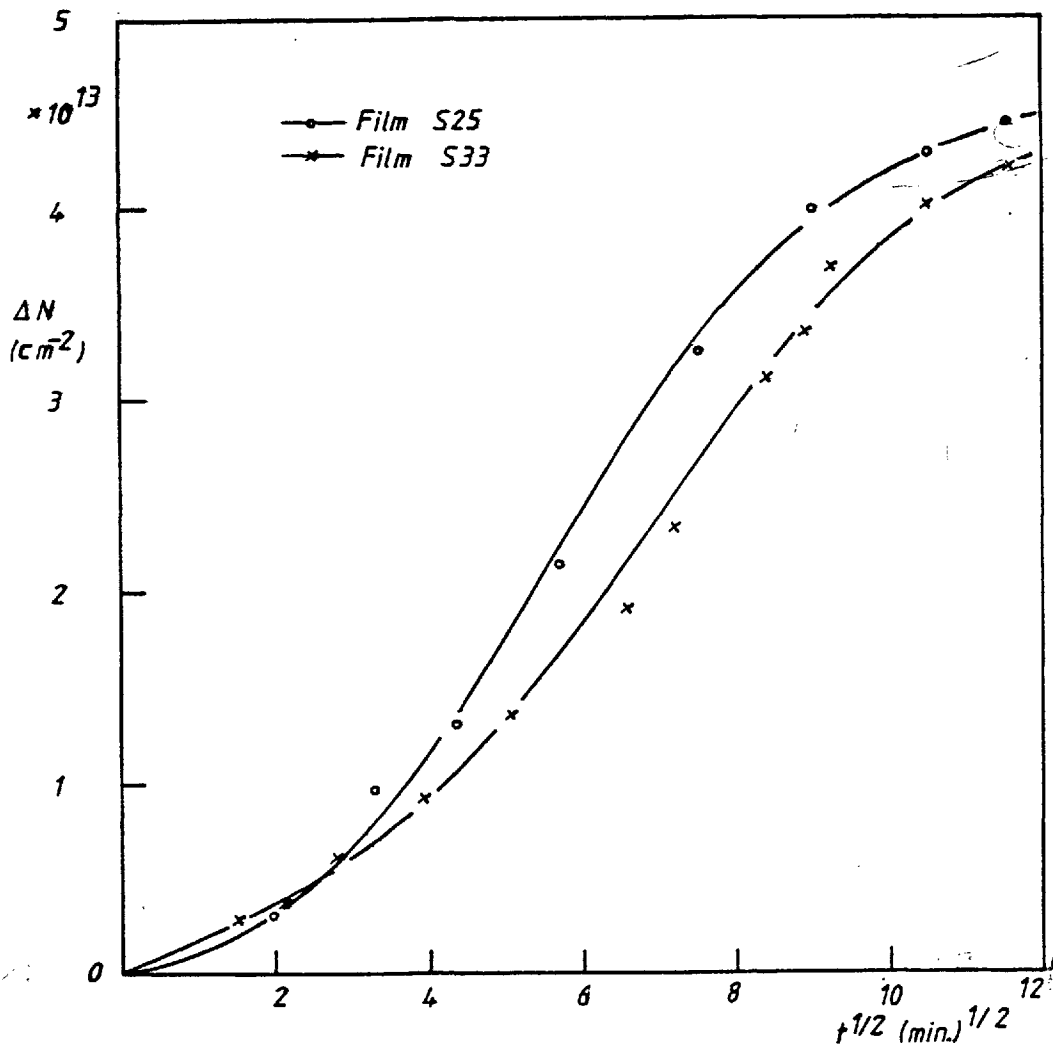


Fig.5.15 1<sup>st</sup> H cycle on 'virgin' p-type films

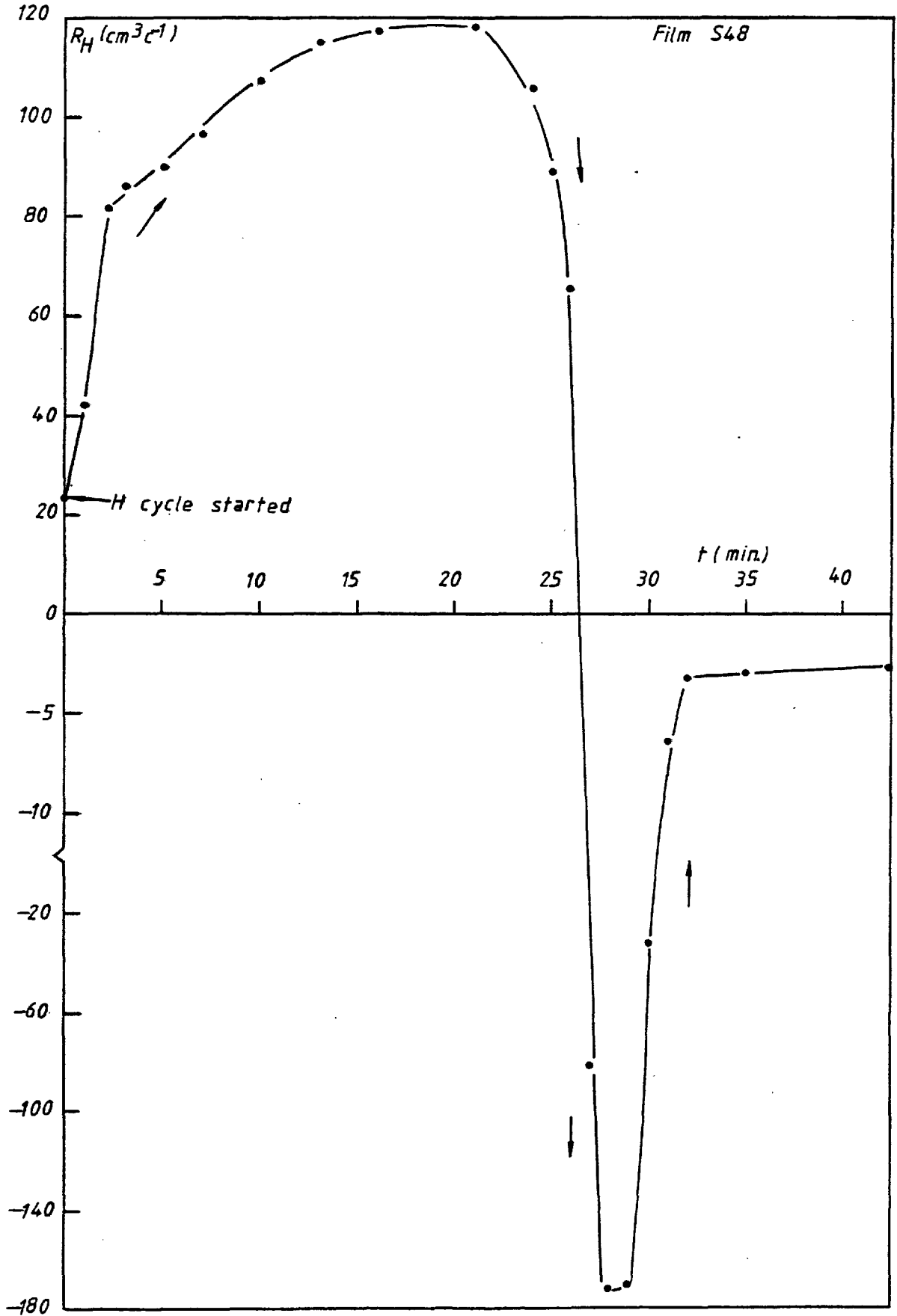


Fig. 5.16 H effect on an  $\text{O}_2$  driven p-type film



single crystal value. For example, Zemel (Z8) estimated  $D_{Pb}$  in PbSe epitaxial films to be  $10^4$  times higher than that for PbSe single crystal. It is, therefore, difficult to correlate  $D_{Pb}$  values for thin film and single crystal and identify the value of diffusion coefficient estimated during the present study with self-diffusion coefficient of lead in PbTe. In any case, for efficient self-diffusion of lead to take place, there must be a high concentration of  $V_{Pb}$ . There is evidence in the literature suggesting that in undoped PbTe ionised lead and tellurium vacancies are the sources of free holes and electrons (B7,H6,B8,K5) and it is normally heavily compensated (Y4). On the other hand, H in-diffusion is also possible via short circuit paths such as dislocations and grain boundaries during the initial stages of the gas cycle followed by diffusion into the crystallites (G10). In general, short circuit diffusion is faster than the lattice diffusion (B13). However, since no data are available (to the best of the author's knowledge) on H diffusion in single crystal PbTe, it is not possible to compare the diffusion coefficients of H for thin film and single crystal PbTe. Therefore, it is difficult to discuss H diffusion along the short circuit paths.

H entering an interstitial site and ionising to act as a donor is another possibility but Zemel (Z4, Z7) has expressed doubts on the compatibility of this model with the experimental data. Ionisation of H once it occupies a lead vacancy seems to be the most

acceptable model (Z4,Z7,Y4). Therefore, a p-type PbTe film is driven n-type because H neutralises the effect of lead vacancies. To establish this model experimentally, PbTe films must be grown with controlled concentration of  $V_{Pb}$  which in the present case was not possible.

### 5.3.2 O<sub>2</sub> Effect

The following points are noteworthy.

- (i) Compared with a 'virgin' n-type film O<sub>2</sub> exposures at higher pressures and for longer periods are required to turn a hydrogenated film p-type. (See section 4.3.2.1, chapter 4.) For instance, film S53 ('virgin' n-type) turned p-type after 22 mins when exposed to O<sub>2</sub> at  $p_{O_2} = 1 \times 10^{-4}$  torr (Fig. 5.10) whereas some H saturated films took days at atmospheric pressure to turn p-type.
- (ii) Reversal of H effect was quicker when O<sub>2</sub> was leaked in at higher pressure (Fig. 5.9).
- (iii) Films like S6 and S9 did not turn p-type at all (S6,S9 were air-exposed prior to H cycle).

Initially it was thought that there might be an oxide growth on the surface of such films as S6 and S9 which prevented O<sub>2</sub> penetration. Cooling films S6 and S9 to liquid N<sub>2</sub> temperature in an attempt to crack the oxide layer, if any, failed to turn the films p-type, although Band (B2) and Hing (H1) had some success using this method with their stable H saturated n-type films. This suggested that the films S6 and S9 were permanently doped n-type.

From the previous argument it may also be inferred that O<sub>2</sub> reverses H effect by removing it probably in the form of H<sub>2</sub>O (E4,Y3) which is desorbed at the surface. But since most H saturated films are eventually turned p-type, a second mechanism in addition to H removal is necessary to explain total O<sub>2</sub> uptake.

Various models of O<sub>2</sub> uptake on lead salts (PbS, PbSe and PbTe) have been proposed in the past where the surfaces of these salts were obtained by epitaxial growth, by crushing or cleaving single crystals. This is partly due to the fact that different workers have used different experimental conditions and techniques (such as change in ambient pressure due to gas-uptake (H2), changes in transport properties in conventional vacuum and ultra-high vacuum (B3,M2,E2,P8), ultra-violet photo-electron spectroscopy (S8)) to study O<sub>2</sub> effect. Based on the evidence presented in the literature, O<sub>2</sub> uptake on lead salts occurs in at least two stages and it is both pressure and temperature dependent.

Initial  $O_2$  uptake for low  $p_{O_2}$  is a surface phenomenon. Green and Lee (G4) proposed that surface adsorption of  $O_2$  was consistent with the formation of a peroxide surface complex whereas Lee (L5) explained  $O_2$  uptake on n-type epitaxial PbS films in terms of surface stoichiometry effect where he suggested that formation of oxide molecules at the surface changed the surface stoichiometry thereby removing more electrons than valence band states. Considering  $O_2$  effect on PbSe films, Hagström and Fahlman (H4) postulated that an oxide growth of monolayer range was formed. Hillenbrand (H3) who studied  $O_2$  uptake on polycrystalline PbS films proposed that total gas-uptake was the sum of three processes operating together which were, (a) the ionisation of oxygen at PbS surface by capturing carrier electrons present in n-type polycrystalline films; (b) adsorption of oxygen atoms by PbS surfaces in amounts that approach one atom of oxygen per lead atom in the surface layer and (c) the incorporation into the PbS lattice by replacement of the sulphur atoms followed by a partial evolution of S as  $SO_2$ .

Other workers such as Egerton and Juhasz (E2) and Parker and Williams (P8) put forward a diffusion model as an alternative mechanism for  $O_2$  uptake on epitaxial PbTe films. By basing their model on the model proposed by Bloem and Kröger (B9) for interstitial diffusion of Cu in PbS single crystal, Egerton and Juhasz (E2) suggested that atomic oxygen diffused interstitially to occupy tellurium vacancies, whereas Parker and Williams postulated that interstitial Pb was diffusing out to

the surface to interact with  $O_2$  during the initial stages of the gas exposure.

A second slower mechanism of oxygen uptake on epitaxial PbTe films at pressure of  $10^{-1}$  torr sec was characteristic of oxidation process according to Sun et al (S8). Galat et al (G5) concluded that oxygen chemisorption was followed by the formation of a heterophase layer of lead tellurate,  $PbTeO_4$ . Bode and Levistein (B1) who measured the effect of  $O_2$  adsorption on conductivity and thermoelectric power of n-type PbTe films suggested that surface adsorption of  $O_2$  was followed by its diffusion along the grain boundaries. Therefore, in the past, total  $O_2$  uptake on lead salts have been discussed in terms of surface adsorption, oxide formation and diffusion.

It is suggested that as far as hydrogenated films were concerned, the first stage of  $O_2$  uptake involves effective removal of H. As far as 'virgin' n-type films are concerned,  $O_2$  chemisorbs on the film surface giving rise to band bending. Direct evidence of this band-bending due to chemisorption of  $O_2$  on PbTe epitaxial films has been provided by Sun et al (S8). The second stage of  $O_2$  uptake for both types of films involves diffusion of the gas into the bulk probably to occupy tellurium vacancies. Low sticking coefficient of  $O_2$  for the latter stage of gas exposure seems to explain why prolonged exposures at higher pressures are necessary to turn films p-type and also why  $O_2$  effect is partially

reversible by evacuating the films to a vacuum of  $\sim 10^{-6}$  torr. A unique interpretation of kinetics of  $O_2$  uptake is difficult since not only Elovich type kinetics ( $\ln(t)$  dependence) and  $t^{1/2}$  dependence are indicative of chemisorption and diffusion mechanism respectively but these kinetics also describe oxidation processes (H7,F2,R2).

## CHAPTER 6

### SUMMARY AND CONCLUSIONS

A summary of experimental results obtained during the present study will be given in this chapter. Conclusions drawn from the study together with some suggestions for future work will also be presented.

#### 6.1 TRANSMISSION ELECTRON MICROSCOPY AND THE HALL MEASUREMENTS

Lead telluride grew epitaxially on air-cleaved muscovite mica in the temperature range 150-225°C. The deposited material had (111) plane parallel to the surface of the substrate as previously reported (E3, G1, S6). The salient feature of the microstructure was the existence of double positioning boundaries enclosing domains of single crystal orientation. The size of the triangular based nuclei and the domain increased as the substrate temperature was increased.

The Hall measurements were carried out in air on 18 films grown on mica substrate. Four films considered to be representative of this work are discussed in chapter 3. These four films (n-type) were grown in the temperature range 150-200°C and thickness of the films was in the range 2900-4100Å. The Hall effect measurements were performed using a standard d.c. technique in the temperature range 77-300°K. Carrier concentration

at room temperature was in the  $10^{17}$ - $10^{18}$   $\text{cm}^{-3}$  range and the Hall mobility at room temperature ranged from 590-883  $\text{cm}^2/\text{V sec}$  compared with the best value of  $\mu_H = 1200$   $\text{cm}^2/\text{V sec}$  obtained by Egerton (E1) at room temperature for his n-type PbTe film grown on mica at  $260^\circ\text{C}$ .

In all cases,  $\mu_H$  decreased as the temperature was increased and the temperature dependence of  $\mu_H$  was described by the power law  $\mu_H \propto T^{-s}$ . Furthermore, the temperature dependence of  $\mu_H$  became weaker in the temperature range  $77$ - $150^\circ\text{K}$ . In the temperature range  $200$ - $300^\circ\text{K}$ , the value of  $s$  was 1.45 for film S10 and 1.75 for film S17 (see Table 3.1, chapter 3). This compares poorly with  $s = 2.5$  for thin films of lead telluride grown on alkali halides (Z1, L1, L2). Matthiessen's rule was used to isolate the contribution of defect scattering such as dislocation and grain boundary scattering often considered to be dominant scattering sources in thin polycrystalline films (A6). The temperature dependence deduced for defect scattering in the case of the present films was incompatible with the known temperature dependence of dislocation and grain boundary scattering. It was proposed that intergrain potential barriers might be responsible for departure from  $\mu_H \propto T^{-2.5}$  dependence. In the past,  $\mu_H \propto T^{-2.5}$  temperature dependence has been interpreted in terms of the combined effect of acoustic phonon scattering and temperature dependent effective mass (A3).



The Hall coefficient was weakly temperature dependent. For instance in the case of film S66,  $R_H$  changed from  $-4.06 \text{ cm}^3/\text{C}$  to  $-3.91 \text{ cm}^3/\text{C}$  in the temperature range  $77\text{-}300^\circ\text{K}$ . A change of about 18% in  $R_H$  may be explained in terms of changing carrier statistics from degenerate to classical.

## 6.2 GASEOUS EXPERIMENTS

Most of the films studied during the present study of gaseous effects were n-type (out of about 40 films grown for these experiments, only 5 were 'virgin' p-type). In spite of this, an attempt was made to perform gas cycles in different sequences and the cycles were repeated to establish reproducibility of the gas interaction with thin films of lead telluride. Changes in  $R_H$  and  $\rho$  were continuously monitored during the gas cycle. The following points can be made at the outset.

- (i) Molecular hydrogen had no observable effect on PbTe thin films.
- (ii) Paths traversed by successive H-O<sub>2</sub> cycles were never the same.
- (iii) Some reversibility of the gas effect was evident when a particular gas cycle was interrupted, for example, re-evacuating an air exposed film. But initial values of  $R_H$  and  $\rho$  were not obtained.

### 6.2.1(a) H. Effect

When a 'virgin' n-type film was exposed to atomic hydrogen, the film turned more n-type. For example, in the case of film S37,  $R_H$  changed from  $-22.3 \text{ cm}^3/\text{C}$  to  $-2.1 \text{ cm}^3/\text{C}$ , whereas in the case of films S27  $R_H$  changed from  $\sim -139 \text{ cm}^3/\text{C}$  to  $-2.3 \text{ cm}^3/\text{C}$ . The corresponding change in  $\rho$  for the latter case was from  $0.33 \Omega \text{ cm}$  to  $0.0051 \Omega \text{ cm}$ . In either case,  $R_H \sigma$  product was almost constant during the gas cycle.

There was a marked difference between the H effect on 'virgin' p-type film and oxygen driven p-type film. As far as the oxygen driven p-type film was concerned, there was an initial increase in the values of  $R_H$  and  $\rho$  such that  $R_H \sigma$  was almost constant, whereas in the case of 'virgin' p-type film there was no initial increase in the value of  $R_H$  and  $\rho$ . Furthermore, 'virgin' p-type film turned n-type much more quickly ( $\sim 90$  secs for film S29) compared with oxygen driven p-type film ( $\sim 47$  mins for film S25).

### 6.2.1(b) Oxygen Effect

Oxygen turned 'virgin' p-type film more p-type. Film S51 was an example of this behaviour. In this case,  $R_H$  decreased from  $71.3 \text{ cm}^3/\text{C}$  to  $12.7 \text{ cm}^3/\text{C}$  during the gas cycle. When films treated with atomic hydrogen were exposed to oxygen, the films became progressively less n-type and the reversal of the H effect was quicker for higher pressures of oxygen. It was also noted that 'virgin' n-type films were driven p-type by oxygen more

quickly compared with hydrogenated films. For example, film S47 ('virgin' n-type) turned p-type in 4 mins. However, once film S47 was treated with atomic hydrogen and then exposed to oxygen, it took  $\sim 20$  hours to turn p-type.

### 6.2.2 Theoretical Models

Two theoretical models were used to interpret the results of gaseous experiments, namely surface adsorption model and diffusion model.

#### 6.2.2(a) Surface Adsorption Model

In this model, it was assumed that the gaseous species was adsorbed onto the surface of the film and the changes produced in  $R_H$  and  $\rho$  of the film were due to the existence of surface space charge region.

Planar form of Poisson's equation was used to formulate the problem mathematically. A computer program using a two-band non-parabolic model and degenerate statistics was used to generate a series of values of  $R_H$  and  $\rho$  for assumed values of surface band bending,  $v_s$ . Accuracy of the fit between the theoretical and the experimental  $R_H$  vs  $\rho$  curve was taken as evidence for the validity of the model. A very good fit was achieved between the two curves in the initial linear region of  $R_H$  vs  $\rho$  curve. In the past (E1, B2), major objection to this model has been the requirement of an excessive amount of band bending ( $\sim 20$  kT) for a p-type film to turn n-type.

Levine (L6) has calculated the three-dimensional electrostatic potential surrounding a square array of fixed charges on an insulator. Using Levine's results, calculation suggests that for a static dielectric constant of 400 planar model and three-dimensional model can be used indiscriminately for a space charge of  $\sim 10^{13} \text{ cm}^{-2}$ . In the present study, inferred value of the space charge density was in  $10^{12} - 10^{13} \text{ cm}^{-2}$  range. Therefore, use of the three-dimensional model of Poisson's equation can remove some of the limitations imposed by the planar form. Greene et al (G6) have given a three-dimensional formulation of Poisson's equation for a non-degenerate electron gas with an array of localised charges on the semiconductor surface. Based on their results, the effective band bending would be lower compared with the one-dimensional model for the same space charge density. Therefore, the objection of excessive band bending required to turn a p-type film n-type in the case of the planar model can be removed to some extent by using the three-dimensional formulation of Poisson's equation. However, the three-dimensional form of Poisson's equation was not used to obtain a theoretical  $R_H$  vs  $\rho$  curve during the present study.

As mentioned earlier, there was a marked difference in H effect on 'virgin' p-type films and oxygen driven p-type films. In addition, the carrier concentration deduced from  $R_H$  in the case of 'virgin' p-type films was comparable to the intrinsic carrier

concentration (see Table 4.2, chapter 4). Therefore, assuming the bulk of the film to be intrinsic and using classical statistics and planar form of Poisson's equation, expressions for  $R_H$  and  $\rho$  were developed in order to compare the theoretical and the experimental  $R_H$  vs  $\rho$  curve for H effect on 'virgin' p-type films. This model correctly predicted the shape of  $R_H$  vs  $\rho$  curve but exact fit with the experimental curve was not possible.

#### 6.2.2(b) Diffusion Model

In this model, it was assumed that gaseous species had diffused into the bulk as a result of concentration gradient between the ambient and the film bulk. This model was considered to account for irreversible changes in  $R_H$  and  $\rho$  of the film.

Fick's laws were used to formulate the problem. The following simplifying assumptions were made.

- (i) Exponential profile of the diffusant was assumed.
- (ii) Surface concentration of the diffusant was constant.
- (iii) Unidirectional diffusion coefficient was independent of concentration.
- (iv) Charge neutrality was assumed.
- (v) All impurities were considered ionised.

Expressions for  $R_H$  and  $\rho$  were developed but the fit between the theoretical and experimental curve was not exact. Expressions for  $R_H$  and  $\rho$  were also developed where condition of charge neutrality was not assumed (i.e. planar form of Poisson's equation was solved for a diffusant with exponential profile).

### 6.2.3 Kinetic Studies

In order to distinguish between surface adsorption and diffusion as being possible mechanisms of gas uptake, kinetic studies were also undertaken. Most of the kinetic studies were carried out at room temperature.

After the initial fast uptake, H effect kinetics followed a  $t^{\frac{1}{2}}$  dependence suggesting that H uptake was a diffusion process. Similar kinetics have been noted for H effect on thin films of PbTe, PbSe and  $Pb_{1-x}Sn_xTe$  (E4, M7, H1). Interrupted kinetics of H effect on 'virgin' n-type film indicated that after each interruption, rate of gas uptake was becoming progressively slower. For example, in the case of film S66, the <sup>slope</sup> of H uptake during first cycle was  $8.32 \times 10^{11} \text{ cm}^{-2} \text{ sec}^{-\frac{1}{2}}$ ,  $6.79 \times 10^{11} \text{ cm}^{-2} \text{ sec}^{-\frac{1}{2}}$  for second cycle and  $3.79 \times 10^{11} \text{ cm}^{-2} \text{ sec}^{-\frac{1}{2}}$  for third cycle.

The value of diffusion coefficient for H effect on 'virgin' n-type films was in  $10^{-14}$ - $10^{-15} \text{ cm}^2 \text{ s}^{-1}$  range at room temperature and in agreement with the value for H effect on PbSe film (Y3). But it was not possible to associate this value of diffusion coefficient with

self diffusion coefficient of lead  $D_{\text{Pb}}$  in PbTe since there were large discrepancies in the values of  $D_{\text{Pb}}$  given in the literature. For example, the value of  $D_{\text{Pb}}$  given by Goldstein (G9) and Ravich et al (R1) is  $10^{-15} \text{ cm}^2 \text{ s}^{-1}$  and  $10^{-18} \text{ cm}^2 \text{ s}^{-1}$  respectively at room temperature. Kinetic study of H effect on oxygen driven p-type films showed that under similar experimental conditions, the rate of gas uptake was slower compared with 'virgin' n-type films. This could be attributable to oxide growth on PbTe film surface due to its exposure to oxygen. Evidence of oxide growth as a result of oxygen interaction with lead chalcogenides has been provided by some recent studies (B10, H4, S8). For instance, Bettini and Richter (B10) studied the oxidation and thermal desorption of PbTe epitaxial layers grown on  $\text{BaF}_2$  (5-10  $\mu\text{m}$  in thickness,  $n = 10^{17}-10^{18} \text{ cm}^{-3}$ ). using XPS and LEED in ultra high vacuum and concluded that prolonged exposure of PbTe at room temperature to air at atmospheric pressure led to the formation of  $\text{PbO}$  and  $\text{TeO}_2$ .

Kinetics of oxygen uptake on hydrogenated films followed  $\ln t$  dependence more faithfully after the first  $\text{H-O}_2$  cycle indicating that atomic hydrogen recombined with oxygen at the surface. Since the reversal of H effect was faster for higher oxygen pressure this further supports the above proposal. Young (Y3) also concluded that atomic hydrogen incorporated into a PbSe film

recombined with oxygen on the surface of the film to form water. The rate of oxygen uptake on a 'virgin' p-type film was plotted using  $t^{\frac{1}{2}}$  and  $\ln t$  time dependence and it was noted that both time dependences were operative over parts of the curve. In any case, since oxygen effect was examined on only one 'virgin' p-type film, no firm conclusions could be drawn.

### 6.3 CONCLUSIONS AND SUGGESTIONS FOR FUTURE WORK

Under appropriate conditions both theoretical models (surface adsorption and diffusion model) predicted the correct shape of  $R_H$  vs  $\rho$  curve but exact fit between the theoretical and the experimental curve in either case was lacking.

As far as H effect is concerned combined evidence of theoretical models and kinetic studies suggest that mechanism of gas uptake is a two stage process, namely in-diffusion of H preceded by its surface adsorption. It is possible for H to be incorporated into PbTe thin film and influence its electrical properties if H diffuses along grain boundaries or occupies interstitial sites or occupies lead vacancies. Although value of the diffusion coefficient for H effect deduced during present study was comparable to those previously reported values of H effect on lead chalcogenides, it could not be identified with the self diffusion coefficient of Pb in PbTe. Since no data are available (to the best of the author's knowledge) for H effect on single crystal



PbTe, it is not possible to compare the two diffusion coefficients and postulate whether H is diffusing along grain boundaries. Occupation of an interstitial site by H was not substantiated experimentally, *since* if H were to occupy every available interstitial site and ionise, the resultant change in carrier concentration, for example, would be incompatible with present experimental data. Therefore, the proposed mechanism of H incorporation into PbTe thin film is through its occupation of lead vacancies.

Oxygen effect is also a two stage process. In the case of hydrogenated films, oxygen reverses the H effect by removing H and reversal of H effect is faster the higher the oxygen pressure. Since unhydrogenated films turned p-type more quickly compared with hydrogenated films under similar experimental conditions, this further supports the above proposal. As far as 'virgin' films are concerned, it is suggested that chemisorption of oxygen is followed by its in-diffusion to occupy tellurium vacancies. This suggestion is based on the evidence given in current literature (H4, S8, Z4). The influence of an oxide growth on PbTe films (due to its interaction with oxygen) on H effect still remains poorly understood.

During present study, it was found difficult to grow p-type films and little control over carrier concentration of 'virgin' films was possible. The latter is expected in view of the experimental technique used

(single and open source evaporation technique, pressure  $\sim 10^{-6}$  torr) to grow thin films. Furthermore, almost entire kinetic studies were limited to room temperature. Removal of these experimental limitations in addition to having a clean surface is essential in furthering the understanding of mechanisms of H uptake on PbTe thin films. Although there have been recent studies of O<sub>2</sub> interaction with PbTe thin films using ultra high vacuum (S8, P6, B10), there has not been an investigation of H effect under similar conditions. For future work, it is proposed that H effect on PbTe thin films should be carried out in UHV system. It is important to have a clearer insight into the mechanisms of gas uptake (H and O<sub>2</sub>) if devices based on PbTe thin films are to have practical applications other than in the field of infra-red detection.

APPENDIX A

$R_H, \sigma$  EXPRESSIONS FOR AN INTRINSIC BULK IN THE PRESENCE  
OF A SURFACE SPACE CHARGE REGION

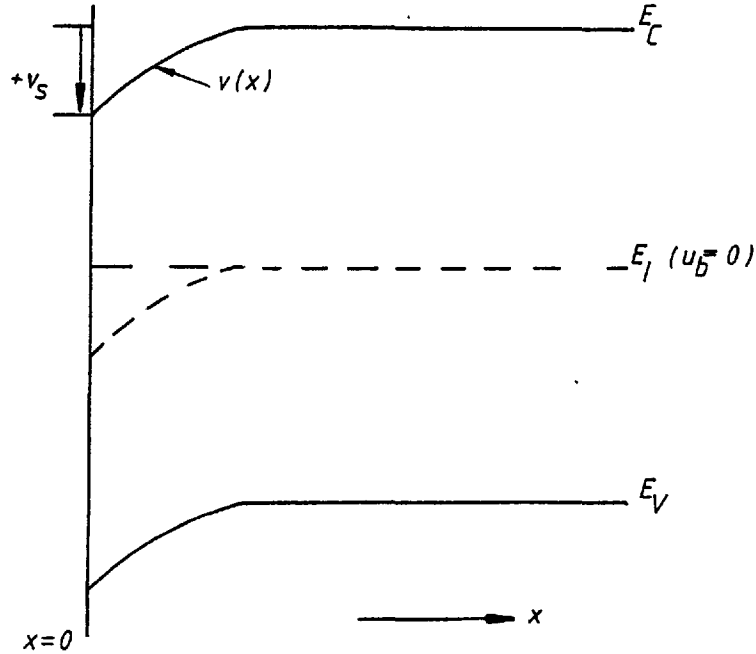


Fig.A1: Intrinsic semiconductor with surface space charge

Using Poisson's equation in the planar form and reduced potential notation,

$$\frac{d^2 v}{dx^2} = - \frac{q\rho}{\epsilon_0 \epsilon_r kT} \quad (\text{A.1})$$

For the case of complete ionisation, uniform impurity concentration and non-degenerate statistics (M4),

$$\frac{d^2 v}{dx^2} = - \frac{q^2}{\epsilon_0 \epsilon_r kT} (n_b - p_b + p_b \exp^{-v} - n_b \exp v) \quad (\text{A.2})$$

Defining 
$$L = \left[ \frac{\epsilon_0 \epsilon_r kT}{q^2 (n_b + p_b)} \right]^{\frac{1}{2}} \quad (A.3)$$

where  $q$  is the electronic charge,  $k$  is the Boltzmann's constant,  $T$  is the temperature,  $\epsilon_0$  is the permittivity of free space,  $n_b$  and  $p_b$  are the electron and hole concentrations in the bulk.

Equation (A.2) becomes,

$$\frac{d^2 v}{dx^2} = \frac{1}{L^2} \left[ \frac{\sinh(u_b + v)}{\cosh u_b} \right] - \tanh u_b \quad (A.4)$$

From Many et al (M4),

$$\frac{x}{L} = \int_{v_s}^v \frac{dv}{\pm F(u_b, v)} \quad (A.5)$$

where

$$F(u_b, v) = \sqrt{2} \left[ \frac{\cosh(u_b + v)}{\cosh u_b} - v \tanh u_b - 1 \right]^{\frac{1}{2}} \quad (A.6)$$

In the case of intrinsic semiconductor  $u_b = 0$

$$\therefore F(0, v) = \pm 2 \sinh (v/2) \quad (A.7)$$

From equations (A.5) and (A.7),

$$\frac{x}{L} = \ln \left[ \frac{\tanh(v_s/4)}{\tanh v/4} \right] \quad (A.8)$$

or 
$$v(x) = 4 \tanh^{-1} \left\{ \tanh(v_s/4) \exp - \frac{x}{L} \right\} \quad (A.9)$$

Expressions for p and n in space charge region can now be written in terms of their respective bulk concentrations as follows:

$$n = n_b \exp\left[4 \tanh^{-1} \left\{ \tanh\left(\frac{V_s}{4}\right) \exp - \frac{x}{L} \right\}\right] \quad (\text{A.10})$$

and

$$p = p_b \exp\left[-4 \tanh^{-1} \left\{ \tanh\left(\frac{V_s}{4}\right) \exp - \frac{x}{L} \right\}\right] \quad (\text{A.11})$$

Assuming that the carrier mobility is independent of x, conductivity can be written as follows:

$$\sigma d = e\mu_n \int_0^d n(x) dx + e\mu_p \int_0^d p(x) dx = I_1 + I_2 \quad (\text{A.12})$$

where d is the thickness of the film.

$$I_1 = e\mu_n \int_0^d n(x) dx \quad (\text{A.13})$$

and

$$I_2 = e\mu_p \int_0^d p(x) dx \quad (\text{A.14})$$

Evaluating  $I_1$  first, from equations (A.9) and (A.13)

$$I_1 = \alpha \int_0^d \exp\left[4 \tanh^{-1} \left\{ \tanh\left(\frac{V_s}{4}\right) \exp - \frac{x}{L} \right\}\right] dx \quad (\text{A.15})$$

$$\text{where } \alpha = e\mu_n n_b \quad (\text{A.16})$$

$$\text{Put } \tanh(V_s/4) = A \quad (\text{A.17})$$

$$\text{and } Y = \tanh(V_s/4) \exp - \frac{X}{L} = A \exp - \frac{X}{L} \quad (\text{A.18})$$

$$\therefore dx = -L \frac{dY}{Y} \quad (\text{A.19})$$

From equations (A.15), (A.17), (A.18) and (A.19),

$$I_1 = -\alpha L \int \frac{\exp(4 \tanh^{-1} Y)}{Y} \quad (\text{A.20})$$

where the limits of integration have been omitted for the time being.

$$\text{Put } P = 4 \tanh^{-1} Y \quad (\text{A.21})$$

$$\therefore dY = \left[ \frac{1}{4} \operatorname{sech}^2(P/4) \right] dP \quad (\text{A.22})$$

From equations (A.20), (A.21) and (A.22),

$$I_1 = -\frac{\alpha L}{2} \int \frac{\exp P}{\sinh(P/2)} dP \quad (\text{A.23})$$

or

$$I_1 = -\alpha L \int \frac{\exp(P/2)}{1 - \exp(-P)} dP \quad (\text{A.24})$$

$$\text{Put } D = \exp P/2 \quad (\text{A.25})$$

$$dP = 2 \frac{dD}{D} \quad (\text{A.26})$$

Substitute equations (A.25) and (A.26) in equation (A.24)

$$I_1 = -2\alpha L \int \frac{D^2}{(D^2-1)} dD \quad (\text{A.27})$$

Equation (A.27) can now be integrated to give,

$$I_1 = -\alpha L \left[ 2D + \ln \left( \frac{D-1}{D+1} \right) \right] \quad \text{iff } D^2 > 1 \quad (\text{A.28})$$

In order to evaluate equation (A.28), limits of integration must be included in the expression. Substitute equation (A.25) in equation (A.28)

$$I_1 = -\alpha L \left[ 2 \exp^{P/2} + \ln \left[ \frac{\exp^{P/2} - 1}{\exp^{P/2} + 1} \right] \right] \quad (\text{A.29})$$

From equations (A.21) and (A.29)

$$I_1 = -\alpha L \left[ 2 \exp(2 \tanh^{-1} Y) + \ln \left[ \frac{\exp(2 \tanh^{-1} Y)}{\exp(2 \tanh^{-1} Y) + 1} \right] \right] \quad (\text{A.30})$$

Substitute equation (A.18) in equation (A.30)

$$I_1 = \alpha L \left[ \ln \left( \frac{\exp 2 \left[ \tanh^{-1} \left\{ \tanh^V s / 4 \exp - \frac{x}{L} \right\} \right] + 1}{\exp \left[ 2 \tanh^{-1} \left\{ \tanh^V s / 4 \exp - \frac{x}{L} \right\} \right] - 1} \right) \right]_0^d - 2 \exp \left[ 2 \tanh^{-1} \left\{ \tanh^V s / 4 \exp - \frac{x}{L} \right\} \right]_0^d$$

$$I_1 = \alpha L \left[ \ln \left[ \left( \frac{\exp 2 \left[ \tanh^{-1} \left( \tanh^V s / 4 \exp - \frac{d}{L} \right) \right] + 1}{\exp 2 \tanh^{-1} \left( \tanh^V s / 4 \exp - \frac{d}{L} \right) - 1} \right) \left( \frac{\exp^V s / 2 - 1}{\exp^V s / 2 + 1} \right) + 2 \exp^V s / 2 \right. \right. \\ \left. \left. - 2 \exp 2 \left[ \tanh^{-1} \left( \tanh^V s / 4 \exp - \frac{d}{L} \right) \right] \right] \quad (\text{A.31})$$

Recalling  $I_2 = e u_p^d \int_0^d p(x) dx$

From equation (A.12),

$$I_2 = \beta \int_0^d \exp - \left[ 4 \tanh^{-1} \left( \tanh^{v_s/4} \exp - \frac{x}{L} \right) \right] dx \quad (\text{A.32})$$

Integral  $I_2$  can be integrated using the substitutions used in the case of  $I_1$ . This finally gives,

$$I_2 = \beta L \left[ \ln \left[ \left( \frac{1 + \exp - 2 \left[ \tanh^{-1} \left( \tanh^{v_s/4} \exp - \frac{d}{L} \right) \right]}{1 - \exp - 2 \left[ \tanh^{-1} \left( \tanh^{v_s/4} \exp - \frac{d}{L} \right) \right]} \right) \left( \frac{1 - \exp - v_s/2}{1 + \exp - \frac{v_s}{2}} \right) + 2 \exp - v_s/2 \right. \right. \\ \left. \left. - 2 \exp - 2 \left[ \tanh^{-1} \left( \tanh^{v_s/4} \exp - \frac{d}{L} \right) \right] \right] \right] \quad (\text{A.33})$$

$$\text{where } \beta = e \mu_p p_b \quad (\text{A.34})$$

$$\text{Recalling } \sigma = \frac{1}{d} [I_1 + I_2]$$

$$\therefore \sigma^2 d = \frac{1}{d} [I_1 + I_2]^2 \quad (\text{A.35})$$

The Hall coefficient can be evaluated as follows,

$$R_H \sigma^2 d = e \mu_p^2 \int_0^d p(x) dx - e \mu_n^2 \int_0^d n(x) dx \quad (\text{A.36})$$

From equations (A.13), (A.14) and (A.36)

$$R_H \sigma^2 d = \mu_p I_2 - \mu_n I_1 \quad (\text{A.37})$$

From equations (A.35) and (A.37) one gets,

$$R_H = d \left[ \frac{\mu_p I_2 - \mu_n I_1}{(I_1 + I_2)^2} \right] \quad (\text{A.38})$$



$$\rho^{-1} = \sigma = \frac{1}{d} \left[ I_1 + I_2 \right] \quad (\text{A.39})$$

Since the bulk is intrinsic  $p_b = n_b = n_i$ .

Integrals  $I_1$  and  $I_2$  can be evaluated as functions of surface band bending  $v_s$  since  $\alpha$ ,  $\beta$ ,  $d$  and  $L$  are known. One major limitation of the model is that it breaks down for  $v_s = 0$ , i.e. it does not predict the flat band values of  $R_H$  and  $\rho$ . However, the model works for  $v_s > 0$  and  $v_s < 0$ .

For the sake of completeness, expressions for  $\Delta N$  and  $\Delta P$  are also given for the case of intrinsic bulk. By definition,

$$\Delta N = \int_0^\infty (n - n_b) dx \quad (\text{A.40})$$

and

$$\Delta P = \int_0^\infty (p - p_b) dx \quad (\text{A.41})$$

Changing the variable to  $v$  (M4),

$$\Delta N = n_b L \int_{v_s}^0 \frac{\exp(v) - 1}{\pm F(u_b, v)} dv \quad (\text{A.42})$$

and

$$\Delta P = \pm p_b L \int_{v_s}^0 \frac{\exp(-v) - 1}{F(u_b, v)} dv \quad (\text{A.43})$$

In the case of intrinsic bulk,

$$\Delta N = \pm \int_{v_s}^0 \frac{\exp(v) - 1}{2 \sinh v/2} dv = \pm 2 n_b L \left[ \exp \frac{v}{2} \right]_{v_s}^0$$

or

$$\Delta N = 2 n_b L \left( \exp \frac{v_s}{2} - 1 \right) \quad (\text{A.44})$$

Similarly,

$$\Delta P = 2 p_b L \left[ \exp\left(-\frac{v_s}{2}\right) - 1 \right] \quad (\text{A.45})$$

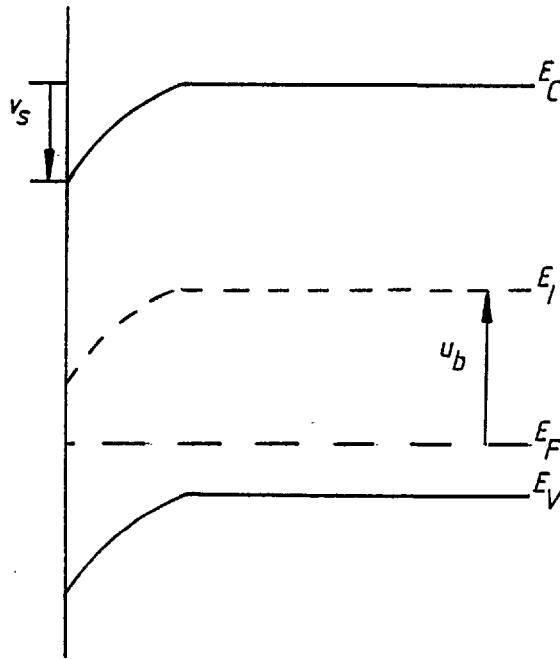
APPENDIX BR<sub>H</sub> AND  $\sigma$  EXPRESSIONS FOR A SINGLE CARRIER FILM IN THE PRESENCE OF A SURFACE SPACE CHARGE DUE TO DONOR DIFFUSION

Fig. B.1: P-type Semiconductor under depletion

For assumptions see chapter 4.

Donors are diffusing into a p-type semiconductor with an exponential profile, i.e.

$$N_d = N_0 \exp - \frac{x}{\ell} \quad (\text{B.1})$$

where  $\ell = 2\sqrt{Dt}$ ,  $D$  = unidirectional diffusion coefficient and  $t$  is the time.

$$\text{Charge density } \rho = e (N_d - N_a) = e N_0 \left( \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_0} \right) \quad (\text{B.2})$$

Using the planar form of Poisson's equation in reduced potential notation,

$$\frac{d^2 v}{dx^2} = - \frac{e^2 N_o}{\epsilon_o \epsilon_r kT} \left[ \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_o} \right] \quad (B.3)$$

Define  $L_D = \left( \frac{\epsilon_o \epsilon_r kT}{e^2 N_o} \right)^{\frac{1}{2}}$  (B.4)

$$\therefore \frac{d^2 v}{dx^2} = - \frac{1}{L_D^2} \left[ \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_o} \right] \quad (B.5)$$

Integrating equation (B.5) with respect to x,

$$\int_{x=0}^{x=x_j} \frac{d^2 v}{dx^2} dx = - \frac{1}{L_D^2} \int_{x=0}^{x=x_j} \left( \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_o} \right) dx \quad (B.6)$$

$$\left. \frac{dv}{dx} \right|_{x=x_j} - \left. \frac{dv}{dx} \right|_{x=0} = - \frac{1}{L_D^2} \left[ -\ell \exp\left(-\frac{x}{\ell}\right) - \frac{N_a}{N_o} x \right]_{x=0}^{x_j} \quad (B.7)$$

where  $x_j$  is the value of x when  $\rho = 0$ .

$$\text{i.e. } x_j = \ell \ln \left( \frac{N_o}{N_a} \right) \quad (B.8)$$

Equation (B.7) becomes,

$$\left. \frac{dv}{dx} \right|_{x=x_j} - \left. \frac{dv}{dx} \right|_{x=0} = \frac{1}{L_D^2} \left[ \ell \exp\left[-\frac{x_j}{\ell}\right] + \frac{N_a}{N_o} x_j - \ell \right] \quad (B.9)$$

Integrating equation (B.9) w.r.t.  $x$  again,

$$v(x_j) - v(0) = \frac{1}{L_D^2} \left[ \ell^2 x_j \exp\left[-\frac{x_j}{\ell}\right] + \frac{N_a}{N_o} x_j^2 - \ell x_j \right] \quad (B.10)$$

From equations (B.8) and (B.10)

$$v(x_j) = v(0) + \left(\frac{\ell}{L_D}\right)^2 \left[ \frac{N_a}{N_o} \ell \ln \frac{N_o}{N_a} + \frac{N_a}{N_o} \left\{ \ell \ln \left(\frac{N_o}{N_a}\right) \right\}^2 - \ell \ln\left(\frac{N_o}{N_a}\right) \right] \quad (B.11)$$

$$\text{Put } A = \left[ \frac{N_a}{N_o} \ell \ln \frac{N_o}{N_a} + \frac{N_a}{N_o} \left\{ \ell \ln\left(\frac{N_o}{N_a}\right) \right\}^2 - \ell \ln\left(\frac{N_o}{N_a}\right) \right] \quad (B.12)$$

$$\therefore v(x_j) = v(0) + A \left(\frac{\ell}{L_D}\right)^2 \quad (B.13)$$

At  $x = 0$ ,  $v(0) = v_s =$  surface band bending.

$$\therefore v(x_j) = v_s + A \left(\frac{\ell}{L_D}\right)^2 \quad (B.14)$$

Since  $A$  is constant,  $v(x_j)$  can be evaluated in terms of  $v_s$  for a given value of  $\ell = 2\sqrt{Dt}$ . Once  $v(x_j)$  is known,  $R_H$  and  $\rho$  can be evaluated as follows.

$$R_H = \frac{1}{ep} \quad (B.15)$$

and

$$\rho = \sigma^{-1} = \frac{1}{e\mu_p p} \quad (B.16)$$

$$\text{where } p = N_a \exp[-v(x_j)] \quad (B.17)$$

Value of  $N_a$  in equation (B.17) is deduced from the Hall coefficient before starting the gas cycle.

APPENDIX CR<sub>H</sub> AND  $\sigma$  EXPRESSIONS USING THE DIFFUSED LAYER MODEL

For assumptions, see chapter 4.

Consider donor diffusion into a p-type semiconductor with bulk hole concentration of  $N_a$ . Assuming the donors have exponential profile, i.e.,

$$N_d = N_o \exp - \frac{x}{\ell} \quad (C.1)$$

where  $\ell = 2\sqrt{Dt}$  as defined in Appendix B and where  $N_o$  is donor concentration for  $t \rightarrow \infty$ . The distribution of carriers in the diffused layer is given by,

$$n(x) = \left[ N_o \exp\left(-\frac{x}{\ell}\right) - N_a \right] \quad (C.2)$$

Using Petritz's model (P9),

$$\sigma d = \int_{x=0}^{x'} e\mu_n n(x) dx + \int_{x'}^d e\mu_p N_a dx \quad (C.3)$$

where  $d$  is the film thickness and  $x'$  is given by the following equations,

$$n(x) = 0$$

or

$$x' = \ell \ln\left(\frac{N_o}{N_a}\right) \quad (C.4)$$

Integrating equation (C.3),

$$\sigma d = \left[ e\mu_n \left\{ -\ell N_o \exp - \frac{x}{\ell} - N_a x \right\}_0^{x'} + e\mu_p N_a (d-x') \right] \quad (C.5)$$

$$\sigma = \frac{1}{d} \left[ e\mu_n \ell N_0 (1 - \exp[-\frac{x}{\ell}] - \frac{N_a}{N_0} \frac{x}{\ell}) + e\mu_p N_a (d - x) \right] \quad (C.6)$$

From equations (C.4) and (C.6),

$$\sigma(\ell) = \frac{e\mu_n \ell N_0}{d} \left( 1 - \frac{N_a}{N_0} + \frac{N_a}{N_0} \ell \ln \frac{N_a}{N_0} \right) + \frac{e\mu_p N_a}{d} \left( d + \ell \ln \frac{N_a}{N_0} \right) \quad (C.7)$$

$$R_H \sigma^2 d = e\mu_p^2 \int_{x'}^d N_a dx - e\mu_n^2 \int_{x=0}^{x'} n(x) dx \quad (C.8)$$

From equations (C.2) and (C.8),

$$R_H \sigma^2 d = e\mu_p^2 N_a (d - x') - e\mu_n^2 N_0 \ell \left( 1 - \exp[-\frac{x'}{\ell}] - \frac{N_a}{N_0} \frac{x'}{\ell} \right) \quad (C.9)$$

Substitute equation (C.4) in equation (C.9)

$$R_H \sigma^2 d = e\mu_p^2 N_a \left( d + \ell \ln \frac{N_a}{N_0} \right) - e\mu_n^2 N_0 \ell \left( 1 - \frac{N_a}{N_0} + \frac{N_a}{N_0} \ell \ln \frac{N_a}{N_0} \right) \quad (C.10)$$

From equations (C.7) and (C.10) one gets,

$$R_H = \frac{\frac{e\mu_p^2 N_a}{d} \left( d + \ell \ln \frac{N_a}{N_0} \right) - \frac{e\mu_n^2 N_0 \ell}{d} \left( 1 - \frac{N_a}{N_0} + \frac{N_a}{N_0} \ell \ln \frac{N_a}{N_0} \right)}{\left[ \frac{e\mu_p N_a}{d} \left( d + \ell \ln \frac{N_a}{N_0} \right) + \frac{e\mu_n N_0 \ell}{d} \left( 1 - \frac{N_a}{N_0} + \frac{N_a}{N_0} \ell \ln \frac{N_a}{N_0} \right) \right]^2} \quad (C.11)$$

Using equations (C.7) and (C.11),  $\sigma = \rho^{-1}$  and  $R_H$  can be evaluated as functions of  $\ell = 2\sqrt{Dt}$  since  $N_a, N_0, \mu_p, \mu_n$  and  $d$  are all known.

When  $t = 0$ ;  $\ell = 0$ ,  $\therefore \sigma = \rho^{-1} = e\mu_p N_a$  from equation (C.7)

and  $R_H = 1/e N_a$  from equation (C.11).

ReferencesA

- A1 Allgaier, R.S., J. Appl. Phys (Suppl), 32 (1961)  
2185
- A2 Allgaier, R.S. and Scanlon, W.W., Phys. Rev., 111  
(1958) 1029
- A3 Allgaier, R.S. and Houston, B.B., Proc. Int. Conf.  
Semicond. Phys., Exeter (1962) (London, Institute  
of Physics and Physical Society) 172
- A4 Azaroff, L.V. and Buerger, M.J., "The Powder Method  
in X-ray Crystallography", McGraw Hill (1958)
- A5 Allison, J., "Electronic Engineering Materials  
and Devices", McGraw Hill, London (1971)
- A6 Anderson, J.C., Advan. Phys., 19 (1970) 311
- A7 Allgaier, R.S., Phys. Rev., 152 (1967) 808

B

- B1 Bode, D.E. and Levinstein, H., Phys. Rev., 96  
(1954) 259
- B2 Band, K.S., Ph.D. Thesis, University of London (1972)
- B3 Brodsky, M.H. and Zemel, J.N., Phys. Rev., 155  
(1967) 780
- B4 Brennan, D. and Fletcher, P.C., Proc. Royal Soc.  
(Lond.) Series A, 250 (1959) 389



B

- B5 Blakemore, J.S., "Semiconductor Statistics", Pergamon Press (1962)
- B6 Boltaks, B.I., "Diffusion in Semiconductors", Infosearch, London (1963)
- B7 Brebrick, R.F. and Gubner, E., J. Chem. Phys., 36 (1962) 1283
- B8 Bauer, G. et al., J. Appl. Phys., 47 (1976) 1721
- B9 Bloem, J. and Kröger, F.A., Philips Res. Rept., 12 (1957) 281
- B10 Bettini, M. and Richter, H.J., Surface Sci., 80 (1979) 334
- B11 Beer, A.C., Solid State Phys. Suppl. 4 (1963)
- B12 Berry, R.W. et al., "Thin Film Technology", D. Van Nostrand Ltd. (1968)
- B13 Balluffi, R.W. and Blakely, J.M., Thin Solid Films, 25 (1975) 363

C

- C1 Cuff, K.F. et al., Proc. 7th Int. Conf. Phys. Semicond., Paris (1964) 677
- C2 Cuff, K.F. et al., J. Appl. Phys., 32 (1961) 2179
- C3 Chernik, I.A. et al., Sovt. Phys. - Semicond., 2 (1968) 645

C

- C4 Cullity, B.D., "Elements of X-ray Diffraction",  
Addision-Wesley Publ. (1956)
- C5 Crank, J., "The Mathematics of Diffusion",  
Oxford (1956)
- C6 Crocker, A.J., J. Phys. Chem. Solids, 28 (1967)  
1903
- C7 Calawa, A.R. et al., Trans. Met. Soc., AIME, 242  
(1968) 374
- C8 Cohen, M.H., Phys. Rev., 121 (1961) 387
- C9 Crocker, A.J. and Rogers, L.M., Brit. J. Appl. Phys.,  
18 (1967) 563

D

- D1 Dalven, R., Infrared Phys., 9 (1969) 141
- D2 Dubrovskaya, I.N. and Ravich, Y.I., Sovt.Phys.-  
Solid State, 8 (1966) 1160
- D3 Dhere, R.G., Private Communication
- D4 Dawar, A.L. et al., Solid State Elec., 22 (1979)  
117
- D5 Dexter, D.L. and Seitz, F., Phys. Rev., 86  
(1952) 964
- D6 Dixon, J.R. and Riedl, H.R., Phys. Rev., 138  
(1965) A873

E

- E1 Egerton, R.F., Ph.D. Thesis, University of London,  
(1968)
- E2 Egerton, R.F. and Juhasz, C., Thin Solid Films,  
4 (1969) 239
- E3 Egerton, R.F., Phil. Mag., 20 (1969) 547
- E4 Egerton, R.F. and Crocker, A.J., Surface Sci.,  
27 (1971) 117

F

- F1 Frankl, D.R., "Electrical Properties of Semiconductor  
Surfaces", Pergamon Press Ltd. (1967)
- F2 Fehlner, F.P. and Mott, N.F., Oxid. Met., 2 (1970)  
59

G

- G1 Green, M., Surface Sci., 26 (1971) 549
- G2 Gudkin, T.S. et al., Sovt. Phys.-Semicond., 8  
(1975) 1453
- G3 Green, M. and Miles, R.E., J. Phys. D: Appl.  
Phys., 6 (1973) L45
- G4 Green, M. and Lee, M.J., J. Phys. Chem. Solids,  
27 (1966) 797

G

- G5 Galat, J. et al., Oxid. Met., 9 (1975) 497
- G6 Greene, R.F. et al., J. Vac. Sci. Techn., 8  
(1971) 75
- G7 Grove, A.S., "Physics and Technology of  
Semiconductor Devices", John Wiley and Sons (1967)
- G8 Greene, R.F., Surface Sci., 2 (1964) 101
- G9 Goldstein, M.L., C.R. Acad. Sci., Paris, 268  
(1969) 686
- G10 Green, M., Private Communication

H

- H1 Hing, L.A., Ph.D. Thesis, University of London  
(1975)
- H2 Hillenbrand, L.J., J. Chem. Phys., 41 (1964) 3971
- H3 Hillenbrand, L.J., J. Chem. Phys., 73 (1969) 2902
- H4 Hagström, A.L. and Fahlman, A., Physica Scripta,  
16 (1977) 432
- H5 Hickmott, T.W., J. Chem. Phys., 32 (1960) 810
- H6 Hemstreet, L.A., Phys. Rev. (B), 12 (1975) 1212
- H7 Hapse, M.G. et al., Surface Sci., 12 (1968) 85
- H8 Harman, T.C. et al., J. Phys.Chem.Solids, 24 (1963)  
835

J

- J1 Jones, R.H., Proc. Phys. Soc. (B), 70 (1957) 704
- J2 Jones, R.H., Proc. Phys. Soc. (B), 70 (1957) 1025
- J3 Juhasz, C., Ph.D. Thesis, University of London  
(1967)
- J4 Juhasz, C., Private Communications
- J5 Jayadevaiah, T.S. and Kirby, R.E., Thin Solid  
Films, 6 (1970) 343

K

- K1 Kolomoets, N.V. et al., Sovt.Phys.-Semicond., 1  
(1968) 1020
- K2 Kanai, Y. and Shohno, K., Jap. J. Appl. Phys., 2  
(1963) 6
- K3 Kondratov, A.V. et al., Sovt. Phys.-Semicond., 7  
(1973) 124
- K4 Kittel, C., "Introduction to Solid State Physics",  
John Wiley (1971)
- K5 Kuchar, F. et al., J. Phys. C: Solid State Phys.,  
10 (1977) 5101
- K6 Kane, E.O., J. Phys. Chem. Solids, 1 (1957) 249

L

- L1 Lopez-otero, A., Thin Solid Films, 49 (1978) 3
- L2 Lopez-otero, A., J. Appl. Phys., 48 (1977) 446
- L3 Lundström, I. et al., Appl. Phys. Lett., 26  
(1975) 55
- L4 Lundström, I. et al., J. Appl. Phys., 46 (1975)  
3876
- L5 Lee, R.N., Jap. J. Appl. Phys. Suppl. 2, pt. 2,  
(1974) 311
- L6 Levine, J.D., Surface Sci., 10 (1968) 313
- L7 Lehovec, K. and Slobodskoy, A., Solid State Elec.,  
3 (1961) 45
- L8 Logothetis, E.M. and Holloway, H., Solid State  
Comm., 8 (1970) 1937

M

- M1 Makino, Y., J. Phys. Soc., Japan; 19 (1964) 580
- M2 McLane, G.F. and Zemel, J.N., Thin Solid Films, 7  
(1971) 229
- M3 Myers, J.H. et al., J. Appl. Phys., 42 (1971) 5578
- M4 Many, A. et al. "Semiconductor Surfaces", North-  
Holland Publ. Co. (1971)

M

- M5 Makino, Y. and Hoshina, T., J. Phys. Soc., Japan,  
19 (1964) 1242
- M6 Many, A., CRC Crit. Rev. in Solid State Sci., 4  
(1974) 515
- M7 McLane, G.F., Ph.D. Thesis, University of  
Pennsylvania (1971)

O

- O1 Ota, T., Proc. 7th Int. Vac. Congr. and 3rd Int.  
Conf. Solid Surfaces, Vienna (1977) 1713
- O2 Okuyama, K., Thin Solid Films, 33 (1976) 165

P

- P1 Putley, E.H., "Materials used in Semiconductor  
Devices", Ed. Hogarth, C.A. (1965) 71
- P2 Piccioli, N. et al., J. Phys. Chem. Solids., 35  
(1974) 971
- P3 Poh, K.J. and Anderson, J.C., Thin Solid Films,  
3 (1969) 139
- P4 Palatnik, L.S. et al., Sovt. Phys.-Solid State,  
11 (1970) 2086
- P5 Putley, E.H., "The Hall Effect and Related  
Phenomena", Butterworths, London (1960)

P

- P6 Parker, E.H.C. and Williams, D., Solid State Elec., 20 (1977) 567
- P7 Palatnik, L.S. et al., Sovt. Phys.-Solid State, 15 (1973) 963
- P8 Parker, E.H.C. and Williams, D., Thin Solid Films, 35 (1976) 373
- P9 Petritz, R.L., Phys. Rev., 110 (1958) 1254
- P10 Parada, N.J. and Pratt, G.W., Phys. Rev. Lett., 22 (1969) 180

R

- R1 Ravich, Y.I. et al., "Semiconducting Lead Chalcogenides", Plenum Press, New York (1970)
- R2 Ritchie, I.M. and Hunt, G.L., Surface Sci., 15 (1969) 524
- R3 Rogers, L.M., Brit. J. Appl. Phys., 18 (1967) 1227
- R4 Ravich, Y.I. et al., Phys. Stat. Sol. (B), 43 (1971) 11, 453
- R5 Rogalski, A., ACTA Physica Polonica, A55 (1979) 45



S

- S1 Scanlon, W.W., Solid State Phys., 9 (1959) 83
- S2 Stavitskaya, T.S. et al., Sovt. Phys.-Semicond.,  
1 (1968) 952
- S3 Silverman, S.J. and Levinstein, H., Phys. Rev.,  
94 (1954) 871
- S4 Shivaraman, M.S., J. Appl. Phys., 47 (1976)  
3592
- S5 Steele, M.C. and MacIver, B.A., Appl. Phys. Lett.,  
28 (1976) 687
- S6 Sealy, B.J. and Crocker, A.J., Thin Solid Films,  
26 (1975) 135
- S7 Smith, R.A., "Semiconductors", Cambridge University  
Press (1968)
- S8 Sun, T.S. et al., J. Vac. Sci. Tech., 15 (1978)  
585
- S9 Schilz, W., J. Phys. Chem. Solids, 30 (1969) 893
- S10 Stephenson, G., "Mathematical Methods for Science  
Students", Longman (1971)
- S11 Seiwatz, R. and Green, M., J. Appl. Phys. 29  
(1958) 1304

T

- T1 Tuck, B., "Introduction to Diffusion in Semiconductors", Peter Peregrinus Ltd. (1974)
- T2 Tauber, R.N. et al., J. Appl. Phys., 37 (1966) 4855

W

- W1 Wallace, C.A. and Ward, R.C.C., J. Appl. Cryst., 8 (1975) 255

Y

- Y1 Yasuoka, Y. et al., Jap. J. Appl. Phys., 7 (1968) 1186
- Y2 Young, J.J. and Zemel, J.N., Thin Solid Films, 31 (1976) 25
- Y3 Young, J.J., Ph.D. Thesis, University of Pennsylvania (1974)
- Y4 Yang, C.Y. and Rabii, S., Int. J. Quantum Chemistry Symp. No. 10, (1976) 313

Z

- Z1 Zemel, J.N. et al., Phys. Rev., 140 (1965) A330
- Z2 Zhitinskaya, M.K. et al., Sovt. Phys.-Solid State, 8 (1966) 246

Z

- Z3 Zemel, J.N., "Solid State Surface Science", Ed. Green, M., vol. 1 (1969) 292
- Z4 Zemel, J.N., "Surface Physics of Phosphors and Semiconductors", Ed. Scott, C.G. and Read, C.E., Academic Press, London (1975) 523
- Z5 Zemel, J.N., Research/Development, 28 (1977) 38
- Z6 Zemel, J.N. and Kaplit, M., Surface Sci., 13 (1969) 17
- Z7 Zemel, J.N. et al., CRC Crit. Rev. in Solid State Sci., 5 (1975) 369
- Z8 Zemel, J.N., "The Use of Thin Films in Physical Investigations", Ed. Anderson, J.C., Academic Press, London (1966) 319