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4 Comparison of Relative Permeability-Saturation-Capillary Pressure
5 Models for Simulation of Reservoir CO₂ Injection
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1 Abstract

2 Constitutive relations between relative permeability (k_r), fluid saturation (S),
3 and capillary pressure (P_c) determine to a large extent the distribution of brine
4 and supercritical CO₂ (scCO₂) during subsurface injection operations. Published
5 numerical multiphase simulations for brine- scCO₂ systems so far have primarily
6 used four $k_r - S - P_c$ models. For the $S - P_c$ relations, either the Brooks-Corey
7 (BC) or Van Genuchten (VG) equations are used. The $k_r - S$ relations are based
8 on the Mualem, Burdine, or Corey equations without the consideration of
9 experimental data. Recently, two additional models have been proposed where
10 the $k_r - S$ relations are obtained by fitting to experimental data using either an
11 endpoint power law or a modified Corey approach. The six models were tested
12 using data from four well-characterized sandstones (Berea, Paaratte, Tuscaloosa,
13 Mt. Simon) for two radial injection test cases. The results show a large variation
14 in plume extent and saturation distribution for each of the sandstones,
15 depending on the used model. The VG-Mualem model predicts plumes that are
16 considerably larger than for the other models due to the overestimation of the
17 gas relative permeability. On the other hand, the predicted plume sizes are the
18 smallest for the VG-Corey model due to the underestimation of the aqueous
19 phase relative permeability. Of the four models that do not use fits to
20 experimental relative permeability data, the hybrid model with Mualem aqueous
21 phase and Corey gas phase relative permeabilities provide the best fits to the
22 experimental data and produce results close to the model with fits to the
23 capillary pressure and relative permeability data. The model with the endpoint
24 power law resulted in very low, uniform gas saturations outside the dry-out
25 zone for the Tuscaloosa sandstone, as the result of a rapidly declining aqueous

1 phase relative permeability. This observed behavior illustrates the need to obtain
2 reliable relative permeability relations for a potential reservoir, beyond
3 permeability and porosity data.

4

5 **Nomenclature**

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7 α : van Genuchten parameter, 1/Pa

8 k_{rj} : phase j relative permeability

9 k_{rj0} : phase j endpoint relative permeability

10 λ : Brooks-Corey pore geometry factor

11 n_v : van Genuchten shape parameter

12 m_v : ($= 1 - 1/n_v$) van Genuchten shape parameter

13 N_{j-vC} : coefficient for variable Corey relative permeability model (phase j)

14 N_{j-EPL} : coefficient for endpoint power law relative permeability model

15 (phase j)

16 P_c : capillary pressure, Pa

17 P_e : Brooks-Corey entry pressure, Pa

18 P_o : ($= 1/\alpha$) strength coefficient, Pa

19 S_j : phase j actual saturation

20 \bar{S}_j : phase j effective saturation

21 S_{li} : aqueous phase irreducible saturation

22 S_{l0} : aqueous phase endpoint saturation

23 *subscripts:*

24 g : gas phase

25 l : aqueous phase

1 1. Introduction

2 The option of carbon sequestration in deep formations (e.g., coalbeds, saline
3 aquifers, and oil and gas reservoirs) is developing rapidly as a promising method
4 to mitigate the adverse impacts of climate change. Of the deep formations, saline
5 aquifers, widely distributed around the globe in sedimentary basins, offer the
6 largest storage potential. Numerical simulation of the injection and redistribution
7 of supercritical CO₂ (scCO₂) is important to determine storage capacity,
8 formation pressure, plume extent and shape, and leakage potential. Ideally,
9 numerical simulators should have the ability to represent the four primary
10 mechanisms identified for CO₂ trapping (Doughty, 2010): stratigraphic or
11 structural, residual, dissolution, and mineral. Given that mineral trapping
12 typically occurs over very long time scales (Pruess et al., 2003), the first three
13 mechanisms, often referred to as hydrodynamic trapping, dominate plume
14 behavior during injection and immediately thereafter over a hundred-year time
15 scale (Doughty, 2010). Given the dominance of the stratigraphic, residual, and
16 dissolution trapping mechanism in the near future, most major simulators with
17 capabilities for CO₂ storage (e.g., TOUGH2 (Pruess et al., 1999; Pruess and
18 Spycher, 2007) and STOMP (White and Oostrom, 2006; White et al., 2010)) focus
19 on these processes.

20 In these simulators, interaction between the reservoir brine (wetting phase)
21 and scCO₂ (nonwetting phase) occurs through constitutive relations between
22 relative permeability (k_r), fluid saturation (S), and capillary pressure (P_c). In
23 reservoir simulators like Eclipse (Schlumberger, 2010) capillary flow at the grid
24 block scale is often considered to negligible and only $k_r - S$ relations are specified
25 (Benisch et al., 2013; Chadwick et al., 2012; Pham et al., 2013). For the simulators

1 requiring both $k_r - S$ and $S - P_c$ relations as inputs, it has been established that
2 these constitutive relations determine to a large extent the plume shape and
3 phase distribution (Class et al., 2009; Juanes, 2006; Pruess and Garcia, 2002).

4 Simulation of hydrodynamic trapping and pore-geometry hysteresis typically
5 requires the consideration of $k_r - S$ and $S - P_c$ hysteresis as these relations are
6 functions of saturation history and the displacement process (drainage or
7 imbibition). However, full hysteretic formulations, including both fluid
8 entrapment and pore geometry hysteresis, are complex and may result in
9 considerable computational demands. Due to the complexity of incorporating
10 hysteresis, models that provide a full hysteretic capability are limited. An
11 exception is the work by Doughty (2007; 2010) who described the
12 implementation of a hysteric model in TOUGH2. Alternatively, simpler models
13 allowing gas entrapment as the only hysteretic mechanism in $S - P_c$ (Krevor et
14 al., 2012; White et al., 2013) or $k_r - S$ relations (Pham et al., 2013; Senel et al., 2015)
15 are more widespread. As stated by Doughty (2007), the use of hysteretic
16 constitutive relations is not important for the simulation of the CO₂ injection
17 stage because the plume is continuously growing and all locations follow the
18 primary drainage branch of the $S - P_c$ curves, which can be replicated using a
19 non-hysteretic formulation. In the analysis presented in this paper, only
20 displacement processes during injection are considered, allowing for the
21 comparison of nonhysteretic constitutive relations.

22 The parameter values for the $k_r - S$ and $S - P_c$ relations are typically
23 obtained for comparable formations from data in the literature (Schnaar and
24 Digiulio, 2009). Alternatively, these values can be obtained by fitting the relations
25 to experimentally obtained datasets. For the $S - P_c$ relations, a common and
26 inexpensive experimental procedure is the mercury injection capillary pressure

1 (MICP) method, using small rock samples. Due to the sample size and potential
2 issues related to the translation of the mercury data into scCO₂-brine fluid pair
3 $S - P_c$ relations, the applicability of the method is not without controversy. Pini
4 et al. (2012) derived $S - P_c$ relationships with scCO₂-brine systems at reservoir
5 conditions using a CT scanner. While the technique used is perhaps too costly
6 and time-consuming for widespread application, it demonstrated the validity of
7 using capillary pressure curves derived from MICP or other analogue water-wet
8 fluid systems. For the $k_r - S$ relations, an inexpensive experimental method
9 (Muller, 2011) does not exist and uncertainty persists around the best
10 measurement techniques and the quality of existing scCO₂-brine $k_r - S$ data sets
11 (Benson et al., 2015). Modelers therefore tend to use relations that minimize the
12 use of fitted parameter values or use relations based on the scarce data sets (e.g.,
13 Bachu and Bennion, 2010; Bennion and Bachu, 2008, 2010). Recently, CT scanners
14 were used by Akbarabadi and Piri (2013), Krevor et al. (2012), Ruprecht et al.,
15 (2014) and Perrin and Benson (2010) to obtain high-quality $k_r - S$ data sets. The
16 increased understanding of the appropriate measurement techniques for CO₂
17 relative permeability suggests there is potential to expand the availability of
18 $k_r - S$ data sets in the near future (Benson et al., 2013, 2015).

19 The two major $S - P_c$ models used for nonhysteretic subsurface scCO₂
20 injection simulations are based on retention relations proposed by van
21 Genuchten (1980) and Brooks-Corey (1964) and are listed in Table 1. In the Van
22 Genuchten (VG) model, α (Pa⁻¹) is roughly the inverse of the gas entry pressure,
23 and n_v and m_v are pore-geometry parameters related by $m_v = 1 - 1/n_v$. A main
24 characteristic of the VG $S - P_c$ relation is that the wetting fluid is displaced by
25 the nonwetting fluid if $P_c > 0$. Based on the assumption that $P_e \approx 1/\alpha$ (Pa), $1/\alpha$ is
26 often represented in the VG $S - P_c$ equation by the strength coefficient P_o (e.g.,

1 Birkholzer et al, 2009; Doughty, 2010; Mathias et al., 2013; Yamamoto et al., 2009).
 2 It is important to realize that although a finite pressure P_o is part of the alternative
 3 VG equation (Table 1), P_o does not constitute an entry pressure: The porous
 4 medium still desaturates with respect to the wetting fluid when $P_c > 0$ (Lenhard
 5 et al., 1989). For the Brooks-Corey (BC) $S - P_c$ relation, values of a $P_e > 0$ and a
 6 pore-geometry parameter λ are prescribed (Table 1). Both the VG and BC
 7 models are easily fitted to experimental retention data and the parameterization
 8 of either one of the relations can be used to find the corresponding other relation
 9 by using a method developed by Lenhard et al. (1989).

10 Most $k_r - S$ relations reported in the subsurface scCO₂ literature use the
 11 empirical model proposed by Corey (1964) or the geometry-based models of
 12 Burdine (1953) and Mualem (1978). Corey's (1964) simple polynomial functions
 13 have been widely used in the petroleum literature. The two geometry-based
 14 models relate relative permeability to the $S - P_c$ curve based on the simple
 15 geometric assumption that the pore space is a bundle of capillary tubes (Dury et
 16 al., 1999). Both the Burdine (1953) and Mualem (1978) relative permeability
 17 models consist of the product of an empirical connectivity/tortuosity term and an
 18 integral term representing the actual capillary theoretical model. Assuming that
 19 in a water-wet porous medium the nonwetting fluid is residing in the largest
 20 pores, the relative permeabilities for both models can be written as

$$21 \quad k_{rl} = \bar{S}_l^a \left[\frac{\int_0^{\bar{S}_l} \frac{dx}{h^b(x)}}{\int_0^1 \frac{dx}{h^b(x)}} \right]^c \quad (1a)$$

$$k_{rg} = (1 - \bar{S}_l)^a \left[\frac{\int_{\bar{S}_l}^1 \frac{dx}{h^b(x)}}{\int_0^1 \frac{dx}{h^b(x)}} \right]^c \quad (1b)$$

2 where x is a dummy integration value, and $h(\bar{S}_l)$ is the inverted $S - P_c$ relation.
 3 For the Burdine (1953) model, $b = 2$, and $c = 1$. For the Mualem (1978) model, $b =$
 4 1 , and $c = 2$. Mualem (1978) suggested a value of 0.5 for the tortuosity coefficient
 5 a , based on wetting fluid permeability data, whereas Burdine (1953) proposed an
 6 empirical value of 2. None of these values were based on theoretical
 7 considerations. When nonhysteretic $k_r - S$ relations are obtained according to
 8 Eq. (1), the resulting $k_r - S - P_c$ model is considered to be coupled through the m_v ,
 9 and λ parameters for the VG and BC relations, respectively. A discussion of the
 10 effects of coupling in constitutive relations is provided by DeHoff et al. (2011).

11 Although combining the VG and BC $S - P_c$ relations with either the Burdine
 12 (1953), Corey (1964), or Mualem (1978) $k_r - S$ relations could lead to a large
 13 number of $k_r - S - P_c$ models, just four of them are primarily used in the
 14 subsurface scCO₂ literature: the VG-Mualem (VG-M), BC-Burdine (BC-B), and
 15 VG-Corey (VG-C) models, and a model combining the VG $S - P_c$ relation with
 16 the Mualem relation for $k_{rl} - S$ and the Corey relation for $k_{rg} - S$. The latter
 17 model is referred to as the VG-hMC model where the h denotes that a hybrid
 18 Mualem-Corey $k_r - S$ model is used. It is noted that other $k_r - S$ relations have
 19 occasionally been used in the modeling literature but not at a level that warrants
 20 inclusion in this analysis. Examples of sparingly used models are cubic Corey-
 21 type expression for relative permeability (Vilarrasa, 2014), or linear interpolation
 22 between experimentally obtained relative permeability data points (Mtiku and
 23 Bauer, 2013).

1 Some of the reasons the empirical and geometry-based $k_r - S$ models have
2 been widely used in subsurface scCO₂ modeling include the relative ease in
3 implementation into numerical simulators and the lack of site-specific data,
4 potentially masking the need to use more appropriate representations. As an
5 alternative to these models, two promising $k_r - S$ models have been recently
6 introduced that are obtained by fitting to experimental data. The VG-EPL model
7 (Mathias et al., 2013) uses endpoint power law (EPL) equations and the BC-vC
8 model (Krevor et al., 2012) uses Corey-type equations with variable exponents to
9 obtain relative permeability relations. Although these two models are relatively
10 recent, it is expected that the use of the proposed approaches will increase in the
11 future when more site-specific data becomes available (Benson et al., 2013).

12 An overview of the $S - P_c$ and $k_r - S$ relations for the six considered models
13 in this analysis (VG-M, BC-B, VG-C, VG-hMC, VG-EPL, and BC-vC) is presented
14 in Table 1 and brief descriptions of each of the models are provided below. The
15 VG-M model has been used by Birkholzer et al. (2009) to investigate pressure
16 responses in stratified deep saline aquifers. Zhang and Agarwal (2013) used this
17 model to simulate optimization of CO₂ sequestration but did not present any
18 parameter values. Gor et al. (2013) did not provide parameter values in their VG-
19 M simulations of thermal stresses on caprock integrity. It should be noted that
20 only the $k_{r,l} - S$ relation was formally derived by van Genuchten (1980) and that
21 $k_{r,g} - S$ relation was first presented by Lenhard and Parker (1987). Hysteretic VG-
22 M models have been used by Doughty et al. (2008) and Doughty (2010) to predict
23 plume behavior during and after injection at the Frio brine pilot in Texas and the
24 Kimberlina site in California, respectively. The full hysteretic VG-M model,
25 based on the model developed by Parker and Lenhard (1987) and Lenhard and
26 Parker (1987) was presented in Doughty et al. (2007). The VG-M model is an

1 example of a coupled $k_r - S - P_c$ model if the same pore-geometry m_v parameter
2 value is used in both the $S - P_c$ and $k_r - S$ relations. Coupling was used in
3 Birkholzer et al. (2009), Doughty (2007) and Doughty et al. (2008). However,
4 Doughty (2010) used different m_v values for the capillary pressure and relative
5 permeability relations.

6 The BC-B model is also mostly used as a coupled $k_r - S - P_c$ model through
7 the pore-geometry λ parameter. The BC-B model has been primarily used in
8 benchmarking simulations (Class et al., 2009; Ebigbo et al., 2007; Kolditz et al.,
9 2012) but also for an analysis coupled wellbore-reservoir flow during injection
10 (Rasmussen et al., 2015). Interestingly, the λ value for the injection benchmark
11 problems discussed by Kolditz et al. (2012) is omitted in their Table 4. Bandilla et
12 al. (2012) mentioned the use of the BC-B model but did not report BC parameter
13 values.

14 The VG-C model is an example of an uncoupled approach as the Corey (1954)
15 $k_r - S$ relation is used where both phase relative permeabilities are only a
16 function of the effective water saturation (Table 1) and is the same for all
17 sediments. Examples of the model use are presented by Alkan et al. (2010),
18 numerically investigating the combined effects of capillary pressure, salinity and
19 in situ thermodynamic conditions on CO₂-brine-rock interactions in a saline
20 aquifer, and by Kim et al. (2012), simulating salt precipitation and associated
21 pressure build up.

22 The VG-hMC is by far the most widely used model for scCO₂ injection with
23 contributions from, among others, Espinet et al. (2013), Giorgis et al. (2007), Liu
24 et al. (2011), Middleton et al. (2012), Oldenburg et al. (2001), Okwen et al. (2011),
25 Pruess and Muller (2009), Rutquist et al. (2007), Yamamoto and Doughty (2011),
26 Yamamoto et al. (2009), Xu et al. (2007), and Zhou et al. (2010). The hybrid

1 approach uses the Mualem $k_{rl} - S$ function, typically coupled via the m_v
2 parameter to the VG $S - P_c$ relation, and the uncoupled $k_{rg} - S$ Corey function.
3 Exceptions are the simulations of Yamamoto and Doughty (2011) and Xu et al.
4 (2010), who have used uncoupled Mualem $k_{rl} - S$ functions. Giorgis et al. (2007)
5 did not list the parameter values for the conducted salt precipitation modeling.
6 All of the listed VG-hMC references were completed with the TOUGH2-ECO2N
7 simulator (Pruess et al. 1999; Pruess and Spycher, 2007). Of interest is the
8 observation that for a large number of the VG-hMC papers, an m_v value of 0.457
9 was used as a generic parameter value (e.g., Espinet et al., 2013; Liu et al., 2011;
10 Rutquist et al., 2007; Okwen et al., 2011; Xu et al., 2007; Yamamoto et al., 2009).
11 This value was also used by Birkholzer et al. (2009) using the VG-M, and by Kim
12 et al. (2012) using the VG-C relations. The origin of this ubiquitous value is not
13 immediately clear, although Birkholzer et al. (2009) state that the value is typical
14 for sedimentary formations suitable for CO₂ storage. Another widely used value
15 for m_v in VG-hMC simulations is 0.412 (e.g., Middleton et al. 2012; Yamamoto
16 and Doughty, 2011; Zhou et al., 2010). This value was also used in the VG-M
17 simulations reported by Doughty (2007; 2010) and Doughty et al. (2008) and
18 originates from Sakurai et al. (2005).

19 The application of the VG-EPL model is explained in detail by Mathias et al.
20 (2013). The endpoint power laws used in the model are common relations used
21 in the petroleum literature (e.g., Orr, 2007). A complication in using the VG-EPL
22 model is that the physical meaning of the endpoint S_{i0} in the relative
23 permeability relations (i.e., the aqueous saturation at the largest experimentally
24 obtained k_{rg}) is not necessarily the same as the irreducible saturation S_{ii} in the
25 VG $S - P_c$ equations (Table 1) because the values typically come from different

1 sources. However, if an EPL relative permeability model is used, the S_{ii} in the
2 associated VG relation has to be equal to S_{i0} so that $\bar{S}_l = (S_l - S_{i0}) / (1 - S_{i0})$. The
3 VG-EPL models reported in the literature (e.g., Mathias et al., 2013) typically
4 employ a generic VG relation with P_e , n_v and m_v parameter values independent
5 of the rock.

6 The other model using fitted $k_r - S$ relations, the BC-vC model, uses variable
7 exponents, with values depending on the fit to the experimental data (Table 1).
8 Krevor et al. (2012) proposed using this modified Corey (1954) approach to allow
9 for the inclusion of fitted gas relative permeability values beyond the
10 experimentally obtained gas saturation endpoint value. A major difference with
11 the VG-EPL model is that the fitted S_{ii} value in the $S - P_c$ model is also used in
12 the $k_r - S$ relations. The BC-vC model has been used by Cameron and Durlovsky
13 (2012).

14 So far, comparisons of the major $k_r - S - P_c$ models for subsurface scCO₂
15 behavior have been limited. Lu et al. (2009) compared numerical simulations
16 using linear, cubic, VG-M, and interpolated $k_r - S$ relations to analytic sharp
17 interface models. They concluded that the analytical models did not perform
18 very well because due to the omission of capillary pressure and relative
19 permeability data. Court et al. (2012) extended the analysis by Lu et al. (2009) to
20 include comparisons with vertical equilibrium models. The authors found
21 satisfactory agreement for a large range of $k_r - S$ relations, representing different
22 rocks, as long as the equilibrium models are applied within the appropriate
23 length and time scales. Both studies did not explicitly compare the performance
24 of the used $k_r - S$ models.

25 The objective of this work is to compare the listed $k_r - S - P_c$ models in Table
26 1 for scCO₂ injection into four homogeneous sandstone reservoirs (Berea,

1 Paaratte, Tuscaloosa, and Mt. Simon). The parameter values for the models are
2 obtained by fitting $S - P_c$ relations (for all models) and $k_r - S$ relations (for the
3 VG-EPL and BC-vC models only) to experimental data provided by Krevor et al.
4 (2012). For the models that use non-fitted $k_r - S$ relations, the used relations are
5 based on empiricism or on capillary pressure data. Although the consensus is
6 that it is vastly better to use models fully fitted to experimental data, it is not
7 known what the performance is of models that only fit capillary pressure. The
8 simulations are conducted for one-dimensional (1-D) and two-dimensional (2-D)
9 configurations, described Mathias et al. (2013). In this comparison, only the main
10 drainage process (aqueous phase displaced by scCO₂) in water-wet porous media
11 is modeled and therefore no scCO₂ entrapment or pore-geometry hysteresis is
12 considered.

13

14 **2. Methods**

15 *Numerical Simulator*

16 The $k_r - S - P_c$ model comparison has been conducted with STOMP-CO₂, a
17 fluid injection and production simulator for multiphase component flow and
18 transport (White and Oostrom, 2006; White et al., 2010). The simulator has been
19 verified against other simulation codes capable of modeling CO₂ flow and
20 transport that were part of the GeoSeq code intercomparison study (Pruess and
21 Garcia, 2002). For isothermal conditions without salt transport, as assumed in
22 this contribution, mass conservation equations for water and CO₂ mass are
23 solved. The conservation equations are converted to algebraic form using the
24 finite volume approach applied to structured orthogonal grids and Euler-
25 backwards time differencing. Each conservation equation is solved for a single
26 unknown, such as fluid pressure, referred to as the primary variable. Because of

1 phase appearances and disappearances, four sets of primary variables are used
2 depending on the phase condition. Constitutive relations, like the $k_r - S - P_c$
3 models, relate primary to secondary variables. Although the STOMP-CO2
4 simulator allows for hydraulic entrapment, the reported simulations describe
5 constant CO₂ injection and, therefore, nonhysteretic $k_r - S - P_c$ relations were
6 used. The CO₂ properties were developed from the CO₂ equations of state
7 presented by Span and Wagner (1996).

8 To simulate formation dry-out, vapor pressure lowering according to Kelvin
9 law's application to porous media (Nitao, 1988) is used in combination with
10 extensions below irreducible aqueous phase saturation for the traditional van
11 Genuchten (1980) and Brooks-Corey (1964) $S - P_c$ relations. The $S - P_c$ models
12 are extended to allow for dry-out using the Webb (2000) procedure, resulting in
13 the use of the existing relations above a computed saturation matching point,
14 and a log-linear $S - P_c$ relation below this saturation, all the way to $S_l = 0$. A
15 newly implemented phase condition allows for a primarily variable switch of the
16 water conservation equation from water pressure to water vapor partial pressure
17 when the aqueous saturation falls below the machine precision.

18

19 *Sandstone Properties and $k_r - S - P_c$ Model Parameter Values*

20 Simulations were conducted for constant-rate injections into four sandstone
21 formations: Berea, Paaratte, Tuscaloosa, and Mt. Simon. The porosity and
22 permeability were determined by Krevor et al. (2012) on rock cores and are listed
23 in Table 2. The Berea and Paaratte rock cores were classified as high, the
24 Tuscaloosa rock as moderate, and the Mt. Simon as low permeability sandstone.
25 For all sandstones, a compressibility of 4.5×10^{-10} 1/Pa was assumed.

26 The $k_r - S - P_c$ parameter values for the six models are shown in Table 3 for

1 all four sandstones. The listed values are based on experimental $S - P_c$ and
2 $k_r - S$ data presented by Krevor et al. (2012). The $S - P_c$ data were obtained
3 using a standard mercury injection method, and were subsequently converted to
4 brine - CO₂ systems assuming a brine-CO₂ interfacial tension of 32 mN/m and a
5 contact angle of 40°. The $k_r - S$ data were obtained by performing a series of
6 steady-state drainage experiments under reservoir conditions with *in situ*
7 saturation monitoring using an X-ray CAT scanner (Krevor et al. 2012; Perrin and
8 Benson 2010).

9 The listed $S - P_c$ parameter values in Table 3, associated with Brooks-Corey
10 curve fits to the Berea, Paaratte, and Mt. Simon data, were obtained by Krevor et
11 al. (2012), and are used in the BC-B and BC-vC models of this analysis (Table 1).
12 As the shape of the Tuscaloosa $S - P_c$ data was somewhat irregular, Krevor et al.
13 (2012) did not present parameter values for that rock. For this analysis, the
14 Tuscaloosa entry pressure was computed with the Leverett-J function, using the
15 Mt. Simon permeability and porosity (Table 1) as reference values. The choice of
16 the Mt. Simon rock core as a reference rock is justified by recognizing, based on
17 the data shown in Krevor et al. (2012), that the Tuscaloosa entry pressure is
18 smaller than that of the other three rock cores, excluding the Berea and Paaratte
19 as possible reference rock candidates.

20 The inverse of a procedure presented by Lenhard et al. (1989) has been used
21 to obtain the equivalent van Genuchten curves from the Brooks-Corey relations,
22 resulting in the parameter values shown in Table 3 for the VG-M, VG-C, and VG-
23 hMC models. The only difference between the van Genuchten relation for the
24 VG-EPL model and the van Genuchten $S - P_c$ relation used in the VG-M, VG-C,
25 and VG-hMC models is the value of the irreducible aqueous phase saturation.
26 For consistency with the EPL $k_r - S$ model, the endpoint aqueous phase

1 saturation, S_{10} , is used as the irreducible aqueous phase saturation in each of the
2 $S - P_c$ relations. This approach was applied by Mathias et al. (2013) in their
3 relative permeability uncertainty analysis on CO₂ injectivity estimation.

4 The Brooks-Corey, the equivalent van Genuchten, and the van Genuchten
5 curves for the EPL models are shown in Fig. 1 for all four sandstones. In this
6 figure, the applied extensions according to Webb (2000) are also presented. The
7 associated matching point saturations and capillary pressures are listed in Table
8 4. The measured $k_r - S$ data for both phases and the associated model relations
9 for the four sandstones are shown in Fig. 2. As intended in the literature, it was
10 assumed that the gas relative permeability reaches a value of 1 at the irreducible
11 aqueous phase saturation in the VG-M, BC-B, VG-C, and VG-hMC models. The
12 fitted gas relative permeability relations for the VG-EPL and BC-vC models
13 assume a linear segment between the endpoint relative permeability at the
14 irreducible water saturation and a relative permeability of 1 at $S_l = 0$, similar to
15 what was used by Mathias et al. (2013) and Krevor et al. (2012).

16

17 *Test Case Description*

18 The Test Case defined by Mathias et al. (2013) was used to simulate 1-D and
19 2-D CO₂ injection in homogeneous reservoirs. The 2-D simulations were included
20 to investigate the effects of buoyancy on the plume development. Test Case
21 details are shown in Table 5. In the horizontal direction of both the 1-D and 2-D
22 cases, a variable grid size was employed ranging from a minimum length of 0.5
23 cm adjacent to injection boundary to a maximum length of 10 m. The small grid
24 cells near the injection boundary were needed to obtain monotonically increasing
25 pressures, as observed by Pickup et al. (2012) and Mathias et al. (2013). For the 2-
26 D simulations, a uniform grid size of 1 m was used in the vertical direction,

1 which is equal to the fine grid size used by Yamamoto and Doughty (2011) in
2 their investigation of gridding effects. The injection was assumed to be uniform
3 over the vertical length of the reservoir.

4 5 **3. Results and Discussion**

6 *Capillary Pressure and Relative Permeability Relations*

7 The BC curves (red lines) in Fig. 1 are the fitted expressions (Krevor et al.,
8 2012) to the experimental $S - P_c$ data. These curves are used in the BC-B and BC-
9 vC models. The curves indicate that the Berea and Paaratte rocks have similar
10 characteristics and that the Mt. Simon sandstone has the largest P_c value. The VG
11 curves used in the VG-M, VG-C, and VG-hMC models (black lines) are very close
12 to the BC curves, except at high aqueous phase saturations. Under these
13 conditions, the differences are the result of the entry pressure value, which is
14 zero for the VG relations but greater than zero for the BC relation. The VG curve
15 used in the VG-EPL model (blue lines) is different than for the other models
16 because the endpoint aqueous phase saturation (S_{i0}) of the $k_r - S$ relation is
17 used as the irreducible saturation (S_{li}). For this model, aqueous phase
18 displacement is harder than for the other VG models as for a given capillary
19 pressure, the aqueous saturations are larger. The effects of the Webb extension
20 are the largest (blue dashed lines) for the VG-EPL model because of the large
21 saturation matching points (Table 4).

22 In general, the fitted VG-EPL and BC-vC relative permeability relations have,
23 as expected, good matches with the experimental data, making the BC-vC model
24 the only model with good fits to both the $S - P_c$ and $k_r - S$ experimental data. For
25 that reason, the simulation results for this model will be used as a reference in
26 the discussions.

1 The $k_{rg} - S$ curves for the models not fitted to experimental data (VG-M, BC-
2 B, VG-C, and VG-hMC) are relatively close for each of the sandstones, with a few
3 notable exceptions. The Mualem $k_{rg} - S$ relation, as used in the VG-M model,
4 overestimates the experimental data for all sandstones. The shape of the curve is
5 convex for all rock types, which is inconsistent with the concave shapes that are
6 typically obtained in the laboratory (e.g., Bennion and Bachu, 2010; Benson et al.,
7 2013; Muller, 2011). The convex shape of the Mualem $k_{rg} - S$ curves is related to
8 the relatively low n_v values, ranging from 1.669 for the Mt. Simon to 2.266 for the
9 Paaratte sandstone (Table 3). Using the VG-M $k_{rg} - S$ equation (Table 1), it can be
10 shown that a concave shape similar to the other $k_{rg} - S$ relations would only be
11 reached for relatively large n_v values (i.e., $n_v > 8$), which are indicative of highly
12 uniform porous media and are much larger than typical n_v values for sandstones
13 (Schroth et al., 1996). This discrepancy suggests that the use of the Mualem
14 $k_{rg} - S$ relation in the VG-M model may not be appropriate to describe scCO₂
15 relative permeability for the considered rocks.

16 Although the differences are less than for the VG-M model, the VG-EPL
17 $k_{rg} - S$ curve deviates from the other models for the Tuscaloosa and Mt. Simon
18 sandstone. The main reason for the differences is that the EPL fit does not
19 include the range below the endpoint saturation, for which a linear relation was
20 assumed. For the Tuscaloosa sandstone, which has a very low endpoint
21 saturation (Fig. 2c), the k_{rg} values are larger than for the other models in that
22 range. The EPL fit for the Mt. Simon (Fig. 2d) deviates from the other models
23 because of the combination of the moderate endpoint saturation for the EPL fit
24 and the relatively high irreducible water saturation used for the other models. As
25 a result the k_{rg} values are larger than for the other models above the endpoint

1 saturation and smaller below.

2 For the $k_{rl} - S$ relations, there is more variation between the models that do
3 not use direct fits to the data (VG-M, BC-B, VG-C, and VG-hMC). The Corey
4 model consistently overestimates the values for all models. Given that the
5 differences with the Corey model and the models directly fitted to the
6 experimental data (VG-EPL and BC-vC) are substantial for all considered
7 sandstones and biased towards larger k_{rl} values, the Corey $k_{rl} - S$ relation may
8 not be a good choice for scCO₂-brine displacement simulations. For the non-fitted
9 models, the Burdine $k_{rl} - S$ curves used in the BC-B also overestimate k_{rl} values
10 for most of the sandstones. The Mualem $k_{rl} - S$ curves, used in the VG-M and
11 VG-hMC model, appear to provide the best matches with experimental data,
12 with the exception of the Berea sandstone. Combining this observation with the
13 previous finding that the Corey $k_{rg} - S$ relation provide good matches with the
14 experimental data, the use of the VG-hMC model appears to be a reasonable
15 approach for the models without fitted relative permeability relationships.

16 For the Berea sandstone (Fig. 2a), it is noted that the $k_{rl} - S$ BC-B and BC-vC
17 relations overlap due the use of $\lambda = 0.67$ in the Burdine and $N_{l-vC} = 6.0$ in the
18 variable Corey relations, respectively (Table 3), yielding almost identical
19 expressions.

20

21 *1-D Simulations*

22 Spatial distributions of gas saturations, relative permeabilities, and pressures
23 at the end of the injection period are shown in Figs. 3, 4, 5, and 6 for the Berea,
24 Paaratte, Tuscaloosa, and Mt. Simon reservoirs, respectively. To a large degree,
25 the results can be explained using the $k_r - S - P_c$ relations shown in Figs. 1 and 2.
26 Using the VG-M model, the injected scCO₂ migrates considerably further into all

1 reservoirs compared to all other models (Figs. 3a, 4a, 5a, and 6a). In addition, the
2 k_{rg} values for the VG-M model at all locations are always larger (Figs. 3b, 4b, 5b,
3 and 6b) and the gas pressures smaller (Figs. 3c, 4c, 5c, and 6c) than for the other
4 models. These results can be primarily attributed to the much larger k_{rg} values,
5 as a function of S_g , for the VG-M model compared to the others (Fig. 2).

6 For each of the sandstones, the horizontal plume extent was the least for the
7 approach using the VG-C model (Figs. 3a, 4a, 5a, and 6a). Consequently, the
8 average scCO₂ saturation over the plume length was the largest for this modeling
9 approach. The main reason for this behavior is the use of the Corey $k_{rl} - S$
10 relation (Table 3), yielding considerable larger k_{rl} values of the pertinent
11 saturation range than the other models. The aqueous phase is therefore easier to
12 be displaced for this model, resulting in larger average gas saturations and a
13 smaller plume extent. The relative results for each sandstone using the VG-C
14 model, compared to the other models, is related to the fact that the Corey $k_{rl} - S$
15 relation is the same for each rock (Table 1) and produces values that are
16 consistently larger than for the other models. Given that the differences with the
17 Corey model and the models directly fitted to the experimental data (VG-EPL
18 and BC-vC) are substantial and biased towards larger k_{rl} values, the Corey
19 $k_{rl} - S$ relation does not appear to be a good choice for scCO₂-brine displacement
20 simulations.

21 The gas saturation figures (Figs. 3a, 4a, 5a, and 6a) indicate that for all
22 $k_r - S - P_c$ models simulations a dry-out zone develops, with a relatively rapid
23 decrease in saturation with distance from the injection location. The shape of the
24 curves is similar to simulation results obtained by Mathias et al. (2013) for the
25 same test case. The dry-out zone for each simulation and rock type is fairly
26 consistent and ranges from approximately 75 to 100 m after 30 years of injection.

1 Away from the dry-out zone, the scCO₂ saturations are relatively low, with the
2 lowest saturations always obtained with the VG-M model and the highest with
3 the VG-C model. For each model, these low saturations in this zone mostly
4 correlate with capillary pressures smaller than the Webb (2000) matching point
5 capillary pressures, even for the VG-EPL with considerably larger S_{li} values.
6 These observations indicate that the extended part of the $S - P_c$ relations, below
7 the matching point saturation, (Fig. 1) was not used for most of each plume
8 except the dry-out zone.

9 The results for the Berea sandstone show relatively small differences in plume
10 extent, saturations, and pressures (Fig. 3) for the BC-B, VG-hMC, VG-EPL, and
11 BC-vC models. The results for the BC-B and BC-vC models are nearly the same
12 because the k_{rl} values are the same and the k_{rg} values are very close (Fig. 2a) for
13 this particular rock. The formation pressures during injection are only up to ~0.5
14 MPa larger than the initial pressure of 10 MPa (Fig. 3c) with differences smaller
15 than ~0.2 MPa between the models. This result is consistent with the high
16 permeability of this sandstone (914 mD) and indicates that the imposed injection
17 rate of 15 kg/s can be easily handled by a reservoir with similar characteristics.
18 Of interest is that the relative position of the pressure plots for the six models
19 (Fig. 3c) is the inverse of the relative positions of the k_{rg} relations (Fig. 3b). This
20 observation is also valid for all other considered sandstone, although the relative
21 position is different for each of them. For the Berea sandstone, the highest
22 pressures are obtained for the VG-hMC model, which has both the lowest k_{rl}
23 and k_{rg} values for the saturation range applicable to most of the plume (Fig. 2a).

24 Compared to the Berea simulations (Fig. 3a), the results for the Paaratte
25 reservoir generally show smaller plumes (Fig. 4a), primarily because of its larger
26 porosity (0.283 for Paaratte vs. 0.221 for Berea). The larger porosity yields more

1 compact saturation distributions at pressures that are even lower than for the
2 Berea simulations (Fig. 4c). In contrast to what was observed for the Berea
3 simulations, the BC-B and BC-vC models for the Paaratte sandstone do not
4 produce identical results. For this rock type, the fitted k_{rl} and k_{rg} values for the
5 BC-vC model are considerably smaller than for the non-fitted BC-B model (Fig.
6 2b), leading to a smaller plume extent and larger formation pressures. The two
7 models with relative permeability relations fitted to experimental data, BC-vC
8 and VG-EPL, yielded similar results at slightly higher pressures (Fig. 4c) and at
9 lower k_{rg} values (Fig. 4b) than the other models. The simulated larger resistance
10 to injection for these two models is consistent with the lower relative
11 permeability values for both phases over the predominant saturation range of the
12 scCO₂ plume (Fig. 2b).

13 The results for the Tuscaloosa reservoir, having a moderate permeability of
14 220 mD, show more variability (Fig. 5) than for the highly permeable Berea and
15 Paaratte cases. For this sandstone, especially the VG-EPL results are different
16 than those for the more permeable reservoirs. Fig. 5a shows relative low and
17 almost constant gas saturations beyond the dry-out zone with k_{rg} values less than
18 0.05. In addition, the gas pressures in the formation are considerably larger than
19 those for the other models. The reason for the different VG-EPL results is
20 associated with the low endpoint saturation and relative permeability of the k_{rg}
21 relations and the extremely low fitted k_{rg} values, even at S_l values above 0.8 (Fig.
22 2c). Under these conditions, the aqueous phase is difficult to displace by scCO₂,
23 resulting in relatively large pressures to force the nonwetting fluid into the
24 formation. This observed behavior illustrates the need to obtain reliable relative
25 permeability relations for a potential reservoir, beyond permeability and
26 porosity data. Based only on the measured permeability and porosity

1 information, and using a relative permeability model not fitted to measurement
2 data, predicted gas pressures after 30 years of injection are only ~2 MPa larger
3 than the formation pressure, which are typically acceptable for reservoir
4 injection. However, when using the VG-EPL model, the relative permeability
5 limitations of this sandstone become apparent, leading to much larger formation
6 gas pressures. Interestingly, the other model that uses fitted relative permeability
7 relations, BC-vC, does not produce similarly high pressures or low saturations as
8 the VG-EPL model. The differences between these models result from the $S - P_c$
9 relations shown in Fig. 1c. The very large endpoint saturation ($S_{i0} = 0.7030$) yields
10 a retention relation where the aqueous phase is much harder to replace by scCO₂
11 than for the BC $S - P_c$ relation. For the Berea (Fig. 1a) and Paaratte (Fig. 1b)
12 formations, this effect was much less pronounced because the $S - P_c$ relations are
13 much closer together over the predominant saturation range of the plume
14 beyond the dry-out zone. Given the large differences in results between the BC-
15 vC and VG-EPL models for this sandstone, with a low relative permeability
16 endpoint at a high aqueous phase saturation, additional research is needed to
17 determine if using VG-EPL $S - P_c$ relations according to Mathias et al. (2013) is
18 appropriate.

19 The gas saturations for the Mt. Simon simulations (Fig. 6a) are similar to the
20 Berea and Paaratte results and do not show the larger variability observed for the
21 Tuscaloosa formation. A major difference with the other simulations is that the
22 low permeability of the Mt. Simon (7.5 mD) leads to very large gas pressures, as
23 is shown in Fig. 6c. Although the simulated pressures are obviously too large for
24 actual injection at the imposed rate (15 kg/s), the simulation results are still of
25 interest in this analysis. The gas saturation plots indicate plume extents and
26 saturations comparable to the Paaratte simulations for all models, although the

1 Paaratte has a larger porosity. The reason that similar plume extents are
2 obtained for these different conditions is related to the high gas pressures needed
3 to inject the scCO₂ at the prescribed rate in the Mt. Simon. For these higher
4 pressures, the aqueous phase solubility is considerably larger, yielding less CO₂
5 to migrate in the supercritical phase.

6 The saturation plots in Figs. 3a, 4a, 5a, and 6a show that the VG-hMC results
7 are reasonably close the BC-vC model, consistent with the observation that the
8 non-fitted $k_{rg} - S$ and $k_{rl} - S$ relations in the VG-hMC model have mostly good
9 matches with the experimental data (Fig. 2). Therefore, the use of the VG-hMC
10 model appears to be the most reasonable of the four models that do not have
11 fitted relative permeability relationships.

12

13 *2-D Simulations*

14 In this section, the results of the 2-D radial simulations are presented. First,
15 horizontal plume extents are shown as a function of time. Then, gas saturations
16 of selected simulations at the end the 30-year injection period are discussed.
17 Next, formation pressures distributions are presented, followed by a discussion
18 of the dry-out zone formation.

19 The relative positions of the horizontal plume extents (Fig. 7) are similar as
20 for the 1-D simulations. The plots in Fig. 7 show that the predicted horizontal
21 plume extents of the various models are relatively close, except for the VG-M
22 model. With the exception for the Tuscaloosa sandstone, where the VG-EPL
23 model produced the smallest plume, the application of the VG-M model resulted
24 in the largest and the VG-C model in the smallest plumes. The reasons for the
25 VG-M and VG-C model behavior have been discussed in the previous section.

1 The explanation for the Tuscaloosa exception is given in the description of Fig. 10
2 below.

3 In Figs. 8 through 11, final gas saturation distributions obtained with the BC-
4 vC, VG-M, and VG-EPL models are shown. The BC-vC model uses fitted
5 capillary pressure and relative permeability relations, the VG-M model always
6 produced the largest plumes, and the VG-EPL results typically deviate from the
7 other models. The saturation distributions resulting from the remaining models
8 (i.e., BC-B, VG-hMC, and VG-C) are similar to the VG-M simulations, although
9 the plume extents are smaller. The shape of scCO₂ plumes in Figs. 8, 9, and 10
10 indicate strong buoyancy effects for the injections in the more permeable Berea,
11 Paaratte, and Tuscaloosa sandstones. On the other hand, the vertical migration
12 component was considerably smaller for the injection in the low-permeability
13 Mt. Simon (Fig. 11). In general, due to the buoyancy effects associated with less
14 dense scCO₂ in the reservoirs, the simulated 2-D plume extents (Fig. 7) are larger
15 than for the 1-D simulations (Figs. 3-6), with the exception of the plumes for the
16 Mt. Simon simulations. The differences between 1-D and 2-D plume extents are
17 the largest for the VG-M model, showing 2-D plume extents that are ~1300 and
18 ~1000 m larger than the 1-D plume lengths for Berea and Paaratte sandstone,
19 respectively. For the much tighter Mt. Simon sandstone, the differences are much
20 smaller (only ~200 m for the VG-M model) as its lower permeability leads to
21 reduced vertical transport. For the other Mt. Simon model simulation similar
22 observations can be made except that the differences between the 2-D and 1-D
23 results are less.

24 As can be seen in Figs. 8 – 10, the appearance of the plumes generated with
25 VG-EPL models is much different for all sandstones, except for the Mt. Simon
26 where the plume looks similar to the BC-vC plume. For the Berea and Paaratte
27 VG-EPL simulation, a large portion of the plume has relatively uniform gas

1 saturations, with values less than 0.55 outside the dry-out zones (Figs. 8c and Fig.
2 9c), compared to more gradually changing saturations for the other model
3 simulations (Figs. 8a and 8b for Berea; Figs 9a and 9b for Paaratte). The reason for
4 the more uniform appearance is related to the $S - P_c$ relations used for the VG-
5 EPL simulations (Figs. 1a and 1b). The pressures needed to inject the imposed 15
6 kg/s scCO₂ into these high-permeability sandstones are low (see an example in
7 Fig. 12 for the Berea BC-vC simulation), and therefore the capillary pressures
8 outside of the dry-out zone are relatively small, resulting in gas saturations
9 mostly below 0.5 for both sandstones. For the other models, the range in gas
10 saturations at lower capillary pressures is larger, resulting in values up to 0.8
11 outside the dry-out zones. The pressure distributions for the high-permeable
12 Berea and Paaratte formations are similar for all models with only small
13 deviations from hydrostatic conditions near the injection location (Fig. 12).

14 The VG-EPL model for the Tuscaloosa sandstone produces a relatively
15 uniform plume with gas saturations mostly between 0.2 and 0.25 outside the dry-
16 out zone (Fig. 10c). The figure also shows that although the Tuscaloosa sandstone
17 is considered to be moderately permeable (Krevor et al., 2012), strong capillarity
18 results in multiphase flow effects that minimize buoyancy in the vertical
19 direction. The totally different appearance of the VG-EPL plume (Fig. 10c),
20 compared to the other plumes (Figs. 10a,b), is the result of the combined effects
21 of the rapidly decreasing $k_{r,i}$ during drainage at high aqueous phase saturations
22 (Fig. 2c), and $S - P_c$ relation (Fig. 1c) that is strongly affected by the imposed
23 large irreducible water saturation. The $k_{r,i}$ at high aqueous phase saturations is
24 overestimated by all models except for the BC-vC and VG-EPL models. The
25 models that do not using fitted k_r expressions predict formation pressures (e.g.,
26 Fig. 13b) that are larger than for the Berea and Paaratte injections (Fig. 12) with

1 values almost inversely proportional to the formation permeability. The pressure
2 distribution of the Tuscaloosa VG-EPL simulations shows near-vertical isobars
3 (Fig. 13c) in the first 1500 m at the end of the injection period, with maximum
4 pressures near 13.5 MPa. The larger pressures are needed to overcome the
5 mentioned relative permeability and capillary pressure restrictions. The BC-vC
6 pressures (Fig. 13a) are only slightly larger than the VG-M results shown in Fig.
7 13b. For this model, the $S - P_c$ relation uses a much smaller S_{li} (0.05) than what is
8 used for the VG-EPL model (0.703), resulting in the need of much smaller gas
9 pressures for brine displacement.

10 The gas saturation plots for the Mt. Simon (Fig. 11) are of interest because
11 they depict distributions for hypothetical cases where the injection rate can only
12 be achieved through very large injection pressures, ranging from approximately
13 40 to 55 MPa, depending on the used model (Fig. 14). The low sandstone
14 permeability reduces the potential for vertical flow due to buoyancy and the
15 resulting isobars are nearly vertical for several kilometers from the injection
16 location. Opposed to what was found for the other sandstones, the simulated Mt.
17 Simon gas saturations for the VG-EPL model (Fig. 11c) are close to the BC-vC
18 results (Fig. 11a) because the differences in the $S - P_c$ relations used for these two
19 models are the smallest (Fig. 2c).

20 Dry-out for the more permeable sandstone is comparable among the models,
21 with saturation distributions strongly affected by buoyancy. Examples for Berea
22 formation simulations are shown in Fig. 15. The only exception is observed for
23 the VG-EPL model, where the fully desiccated zone extent only varies by about
24 20 m in the vertical direction after 30 years of injection (Fig. 15c). The occurrence
25 of the sharp interface between the dry-out zone and the rest of the scCO₂ plume
26 for the VG-EPL model is related to the $S - P_c$ curve (Fig. 1a), which has been

1 explained in the discussion of gas distributions in Fig. 8. To relate dry-out for the
2 different sandstones using the same model, the VG-M simulation results shown
3 in Fig. 16 should be compared to Fig. 15a. The four figures (Fig. 15a, 16a, 16b, and
4 16c) show the clear effect of permeability on the shape of the dry-out zone. A
5 reduction of the formation permeability reduces the vertical saturation
6 differences, with the dry-out zone for the low-permeability Mt. Simon to be
7 nearly vertical.

8

9 **4. Summary and Conclusions**

10 The injection behavior of scCO₂ into homogeneous reservoirs was compared
11 for six $k_r - S - P_c$ models using hydraulic property data from four well-
12 characterized sandstones. All models used $S - P_c$ relations fitted to laboratory
13 capillary pressure data, with the exception for the irreducible aqueous phase
14 saturation in the VG-EPL model, which was the same as the endpoint saturation
15 for the associated $k_{rg} - S$ relation. These values for the VG-EPL model were
16 therefore much larger than for the other models. Of the six $k_r - S - P_c$ models,
17 only the VG-EPL and BC-vC models use fitted $k_r - S$ relations to laboratory
18 relative permeability data, making the BC-vC model the only one with fits to
19 both the capillary pressure and relative permeability data. The $k_r - S$ and $S - P_c$
20 relations of the VG-M and BC-B models are coupled through a pore-geometry
21 parameter obtained for the $S - P_c$ fit with the experimental data. The VG-C model
22 uses fully empirical $k_r - S$ relations, while the VG-hMC model uses a hybrid
23 $k_r - S$ formulation with and coupled Mualem-type $k_{rl} - S$ relation and an
24 empirical Corey type $k_{rg} - S$ relation.

25 The simulation results show that, depending on the $k_r - S - P_c$ model, large

1 variations in plume extent and saturation distribution are predicted. The fully
2 fitted BC-vC model yielded intermediate results for all sandstones. In all cases,
3 the VG-M model predicts plumes that are considerably larger than for the other
4 models due to the overestimation of the k_{rg} . For the 2-D simulations, the
5 differences are more enhanced due to buoyancy effects and are related to the
6 shape of the Mualem $k_{rg} - S$ relation, which is different from those of the other
7 models and the experimental data. The discrepancy is an indication that the
8 Mualem $k_{rg} - S$ relations may not be appropriate for scCO₂ injection simulations.
9 The horizontal plume extent was the smallest for most of the VG-C simulations.
10 The main reason for this result is that the empirical Corey $k_{rl} - S$ relation yields
11 much larger k_{rl} values than the other models and the experimental data. As a
12 consequence, the aqueous phase is easier to displace using this model, resulting
13 in larger average scCO₂ saturations and an associated smaller plume. These
14 results illustrate the point that the use of relative permeability models based on
15 capillary pressure data only or on empiricism may result in considerable
16 uncertainty.

17 Although in general it is to be preferred to use a model fitted to quality
18 experimental data, such as the BC-vC model, the VG-hMC model, which only
19 uses fitted $S - P_c$ relations, produced results that relatively close to the BC-vC
20 results for most sandstones. Of the four models that do not use fitted $k_r - S$
21 relations (VG-M, BC-B, VG-C, and VG-hMC), the use of the popular VG-hMC
22 model appears to be the most reasonable, because good matches of both the
23 Mualem $k_{rl} - S$ and the Corey $k_{rg} - S$ relations to the experimental data are
24 obtained.

25 The 2-D plumes generated with the VG-EPL model were always different in
26 shape and saturation distribution than the plumes obtained with the other

1 models. For the more permeable sandstone (Berea and Paaratte), the VG-EPL
2 plumes outside the dry-out zone have uniform gas saturations. The uniformity is
3 related to the relatively small capillary pressures needed to inject the scCO₂ into
4 these reservoirs. Due to the use of relatively high irreducible aqueous phase
5 saturations, the ranges in the gas saturations are therefore smaller. The VG-EPL
6 plume generated for the Tuscaloosa reservoir is characterized by a very low,
7 uniform saturation as a result of the rapidly declining k_{rl} with increasing scCO₂
8 saturation and the very high irreducible aqueous phase. Because of these
9 characteristics, scCO₂ injection requires considerable larger pressures than for the
10 other models because it is much more difficult to displace the aqueous phase.
11 The different results obtained with the VG-EPL model for these sandstones
12 suggest that this model should be used with caution. A different way to assign
13 the irreducible aqueous phase saturation value to the $S - P_c$ relations may be
14 required, maintaining consistency with the endpoint saturation used in the
15 endpoint power law $k_{rg} - S$ relation.

16 The simulations for the Tuscaloosa reservoir demonstrate the need to obtain
17 relative permeability data beyond permeability and porosity. For this particular
18 non-uniform sandstone, the permeability and porosity indicate that there should
19 not be injectivity issues. However, the measured low endpoint k_{rg} and the
20 rapidly declining k_{rl} lead to increased demands on the injection pressure that are
21 not apparent when models are used that do not use fitted relative permeability
22 data.

23 Given the respective over- and under-estimation of the plume extents with
24 the VG-M and VG-C models for these nonhysteretic simulations, the results
25 indicate that development of full hysteretic capabilities (entrapment and pore-
26 geometry hysteresis) should not be based on these models. Current hysteretic

1 capabilities for scCO₂ injection and redistribution appear to have been developed
2 for the VG-M model only (Doughty, 2007; 2010). A hysteretic implementation
3 should ideally be based on a model like the BC-vC, which uses fits to both the
4 capillary pressure and relative permeability data. Alternatively, a hysteretic VG-
5 M model could be relatively easily modified into a VG-hMC model, which
6 produced comparable results with the BC-vC model for most sandstones, by
7 using hysteretic Corey instead of Mualem $k_{rg} - S$ relations.

8 The presented analysis and conclusions are only valid for the four sandstones
9 characterized by Krevor et al. (2013). It is recommended that a similar approach
10 would be conducted for other type rocks when comprehensive $k_r - S - P_c$ data
11 become available.

12

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1 **Table 1.** Overview of the $k_r - S - P_c$ models.

2

Model	$S - P_c$	$k_r - S$
VG-M (van Genuchten - Mualem)	$\bar{S}_l = \left[1 + \alpha P_c^{n_v}\right]^{-m_v}$ or $\bar{S}_l = \left[1 + \left(\frac{P_c}{P_o}\right)^{n_v}\right]^{-m_v}$	For $S_l > S_{li}$: $k_{rl} = \bar{S}_l^{1/2} \left[1 - \left(1 - \bar{S}_l^{1/m_v}\right)^{m_v}\right]^2$ $k_{rg} = \bar{S}_g^{1/2} \left[1 - \bar{S}_l^{1/m_v}\right]^2$ For $S_l \leq S_{li}$: $k_{rl} = 0$; $k_{rg} = 1$
BC-B (Brooks-Corey - Burdine)	$\bar{S}_l = \left(\frac{P_c}{P_e}\right)^{-\lambda}$	For $S_l > S_{li}$: $k_{rl} = \bar{S}_l^{(3+2/\lambda)}$ $k_{rg} = \bar{S}_g^2 \left[1 - \bar{S}_l^{(1+2/\lambda)}\right]$ For $S_l \leq S_{li}$: $k_{rl} = 0$; $k_{rg} = 1$
VG-C (van Genuchten - Corey)	$\bar{S}_l = \frac{S_l - S_{li}}{1 - S_{li}}$	For $S_l > S_{li}$: $k_{rl} = \bar{S}_l^4$ $k_{rg} = \bar{S}_g^2 \left[1 - \bar{S}_l^2\right]$ For $S_l \leq S_{li}$: $k_{rl} = 0$; $k_{rg} = 1$
VG-hMC (van Genuchten - hybrid Mualem-Corey)	$\bar{S}_l = \left[1 + \alpha P_c^{n_v}\right]^{-m_v}$	For $S_l > S_{li}$: $k_{rl} = \bar{S}_l^{1/2} \left[1 - \left(1 - \bar{S}_l^{1/m_v}\right)^{m_v}\right]^2$ $k_{rg} = \bar{S}_g^2 \left[1 - \bar{S}_l^2\right]$ For $S_l \leq S_{li}$: $k_{rl} = 0$; $k_{rg} = 1$
VG-EPL (van Genuchten - Endpoint Power Law)	$\bar{S}_l = \left[1 + \alpha P_c^{n_v}\right]^{-m_v}$	For $S_l > S_{l0}$: $k_{rl} = k_{rl0-EPL} \left(\frac{S_l - S_{l0}}{1 - S_{l0}}\right)^{N_{l-EPL}}$ $k_{rg} = k_{rg0-EPL} \left(\frac{S_g}{1 - S_{l0}}\right)^{N_{g-EPL}}$ For $S_l \leq S_{l0}$: $k_{rl} = 0$; $k_{rg} = 1 - \left(\frac{1 - k_{rg0-EPL}}{S_{l0}}\right) S_l$

BC-vC (Brooks-Corey – variable Corey)	$\bar{S}_l = \left(\frac{P_c}{P_e} \right)^{-\lambda}$	For $S_l > S_{li}$: $k_{rl} = \bar{S}_l^{N_l - vC}$ $k_{rg} = k_{rg0-vC} \bar{S}_g^2 \left[1 - \bar{S}_l^{N_g - vC} \right]$ For $S_l \leq S_{li}$: $k_{rl} = 0$; $k_{rg} = 1 - \left(\frac{1 - k_{rg0-vC}}{S_{li}} \right) S_l$
---	---	---

1 \bar{S}_l , \bar{S}_g , and P_c are defined as, respectively:

2

3 $\bar{S}_l = \frac{S_l - S_{li}}{1 - S_{li}}$, $\bar{S}_g = \frac{S_g}{1 - S_{li}}$, and $P_c = P_g - P_l$

1 **Table 2.** Rock porosity and permeability (after Krevor et al., 2012)

Name	Porosity (-)	Absolute Permeability (mD)
Berea	0.221	914
Paarete	0.283	1156
Tuscaloosa	0.236	220
Mt. Simon	0.244	7.5

2

1 **Table 3.** Parameter values used for the $k_r - S - P_c$ models simulations.

2

Model	Berea		Paaratte	
	$S - P_c$	$k_r - S$	$S - P_c$	$k_r - S$
VG-M	$\alpha = 2.4 \times 10^{-4} \text{ 1/Pa}$ $n_v = 1.864$ $m_v = 0.464$ $S_{li} = 0.11$	$m_v = 0.464$	$\alpha = 2.9 \times 10^{-4} \text{ 1/Pa}$ $n_v = 2.266$ $m_v = 0.559$ $S_{li} = 0.05$	$m_v = 0.559$
BC-B	$P_e = 2.5 \times 10^3 \text{ Pa}$ $\lambda = 0.67$ $S_{li} = 0.11$	$\lambda = 0.67$	$P_e = 2.1 \times 10^3 \text{ Pa}$ $\lambda = 0.9$ $S_{li} = 0.05$	$\lambda = 0.9$
VG-C	as in VG-M		as in VG-M	
VG-hMC	as in VG-M	k_{rl} : as in VG-M	as in VG-M	k_{rl} : as in VG-M
VG-EPL	$\alpha = 2.4 \times 10^{-4} \text{ 1/Pa}$ $n_v = 1.864$ $m_v = 0.464$ $S_{i0} = 0.4438$	$N_{l-EPL} = 3.2$ $k_{r10-EPL} = 1.0$ $N_{g-EPL} = 2.6$ $k_{rg0-EPL} = 0.3948$ $S_{i0} = 0.4438$	$\alpha = 2.9 \times 10^{-4} \text{ 1/Pa}$ $n_v = 2.266$ $m_v = 0.559$ $S_{i0} = 0.3894$	$N_{l-EPL} = 4.6$ $k_{r10-EPL} = 1.0$ $N_{g-EPL} = 3.0$ $k_{rg0-EPL} = 0.3284$ $S_{i0} = 0.3894$
BC-vC	same as BC-B	$N_{l-vC} = 6.0$ $N_{g-vC} = 5.0$ $k_{rg0-vC} = 0.95$ $S_{li} = 0.11$	same as BC-B	$N_{l-vC} = 8.0$ $N_{g-vC} = 2.0$ $k_{rg0-vC} = 0.95$ $S_{li} = 0.05$

3

4

1 **Table 3.** Continued.

2

	Tuscaloosa		Mt. Simon	
Model	$S - P_c$	$k_r - S$	$S - P_c$	$k_r - S$
VG-M	$\alpha = 7.4 \times 10^{-4}$ 1/Pa $n_v = 1.669$ $m_v = 0.401$ $S_{li} = 0.05$	$m_v = 0.401$	$\alpha = 1.4 \times 10^{-4}$ 1/Pa $n_v = 1.669$ $m_v = 0.401$ $S_{li} = 0.22$	$m_v = 0.401$
BC-B	$P_e = 8.6 \times 10^2$ Pa $\lambda = 0.55$ $S_{li} = 0.05$	$\lambda = 0.55$	$P_e = 4.6 \times 10^3$ Pa $\lambda = 0.55$ $S_{li} = 0.22$	$\lambda = 0.55$
VG-C	as in VG-M		as in VG-M	
VG -hMC	as in VG-M	k_{rl} : as in VG-M	as in VG-M	k_{rl} : as in VG-M
VG-EPL	$\alpha = 7.4 \times 10^{-4}$ 1/Pa $n_v = 1.669$ $m_v = 0.401$ $S_{i0} = 0.7030$	$N_{l-EPL} = 4.7$ $k_{rl0-EPL} = 1.0$ $N_{g-EPL} = 3.2$ $k_{rg0-EPL} = 0.0767$ $S_{i0} = 0.7030$	$\alpha = 1.4 \times 10^{-4}$ 1/Pa $n_v = 1.669$ $m_v = 0.401$ $S_{i0} = 0.4371$	$N_{l-EPL} = 6.0$ $k_{rl0-EPL} = 1.0$ $N_{g-EPL} = 1.6$ $k_{rg0-EPL} = 0.4929$ $S_{i0} = 0.4371$
BC-vC	as in BC-B	$N_{l-vC} = 17.0$ $N_{g-vC} = 4.0$ $k_{rg0-vC} = 0.95$ $S_{li} = 0.05$	as in BC-B	$N_{l-vC} = 9.0$ $N_{g-vC} = 4.0$ $k_{rg0-vC} = 0.95$ $S_{li} = 0.22$

1 **Table 4.** Webb (2000) matching point saturations and capillary pressures for the
 2 Van Genuchten, Brooks-Corey, and Van Genuchten-Endpoint Power
 3 Law (VG-EPL) $S - P_c$ relations.
 4

	Matching Point Saturation (-)	Matching Point Capillary Pressure (Pa)
<i>Berea</i>		
Van Genuchten	0.129	3.61×10^5
Brooks-Corey	0.137	4.79×10^5
Van Genuchten – EPL	0.504	5.46×10^5
<i>Paaratte</i>		
Van Genuchten	0.055	2.12×10^5
Brooks-Corey	0.058	4.14×10^5
Van Genuchten – EPL	0.422	3.48×10^4
<i>Tuscaloosa</i>		
Van Genuchten	0.063	7.99×10^5
Brooks-Corey	0.068	1.13×10^6
Van Genuchten – EPL	0.812	5.68×10^3
<i>Mt. Simon</i>		
Van Genuchten	0.271	4.07×10^5
Brooks-Corey	0.287	4.09×10^5
Van Genuchten – EPL	0.524	1.15×10^5

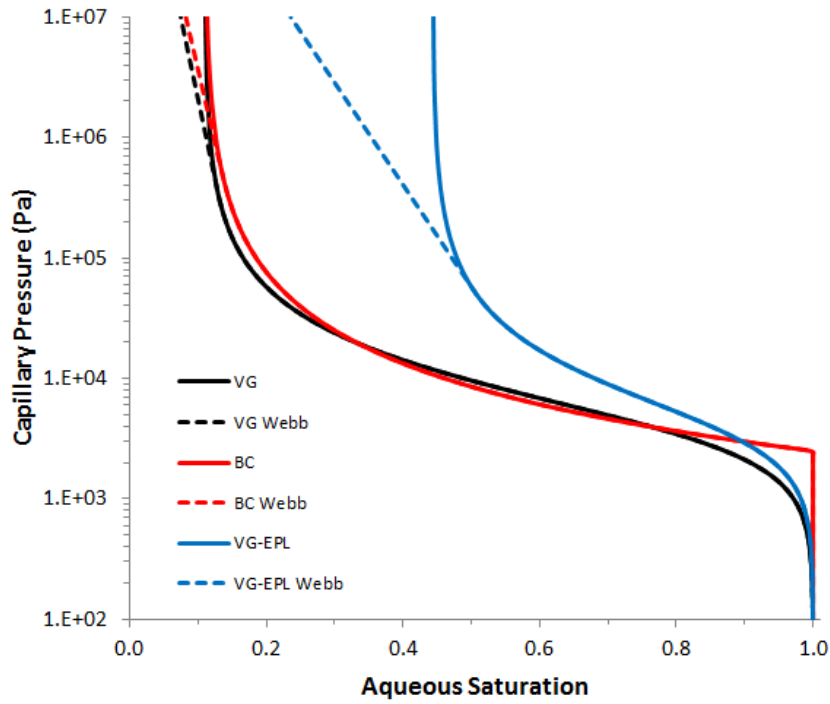
1 **Table 5.** Input parameters for the 1-D and 2-D test cases (after Mathias et al.
2 2013)

3

Parameter	Value
Well radius	0.2 m
Radial extent	20 km
Initial pressure	10 MPa
Temperature	40° C
Salt mass fraction	0
Formation thickness	30 m
Injection duration	30 years
Injection rate	15 kg/s

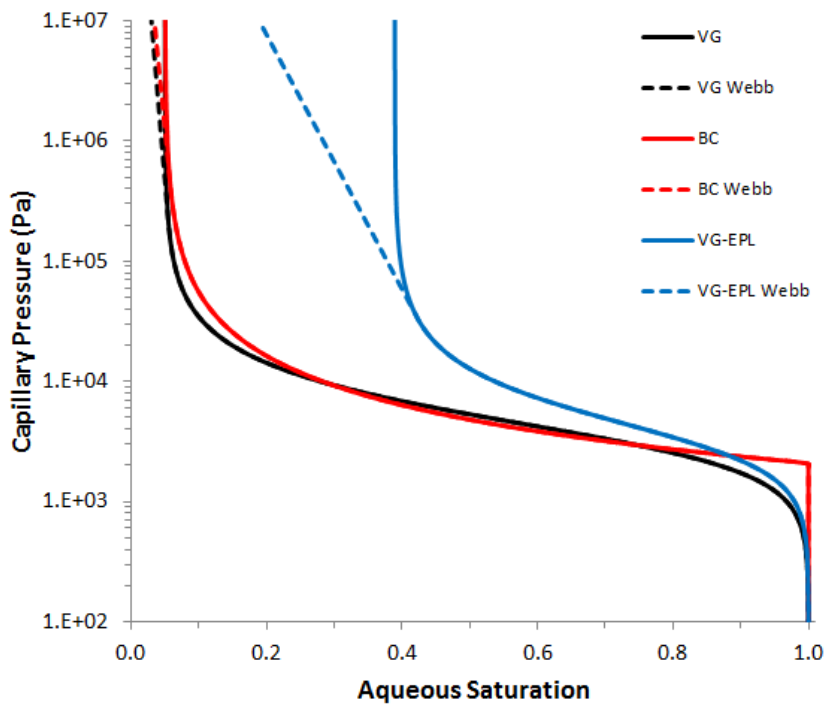
4

1 **Figures**



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(a)

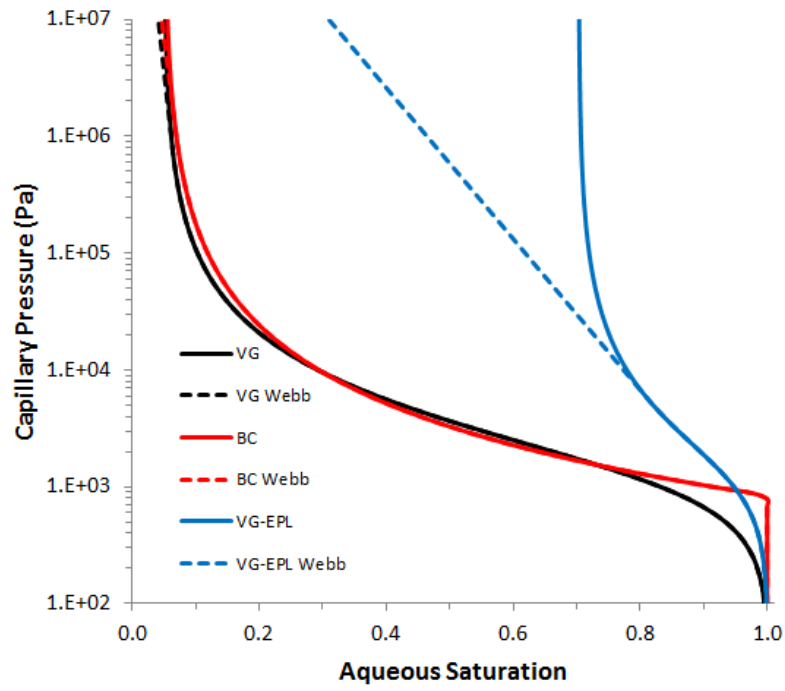


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(b)

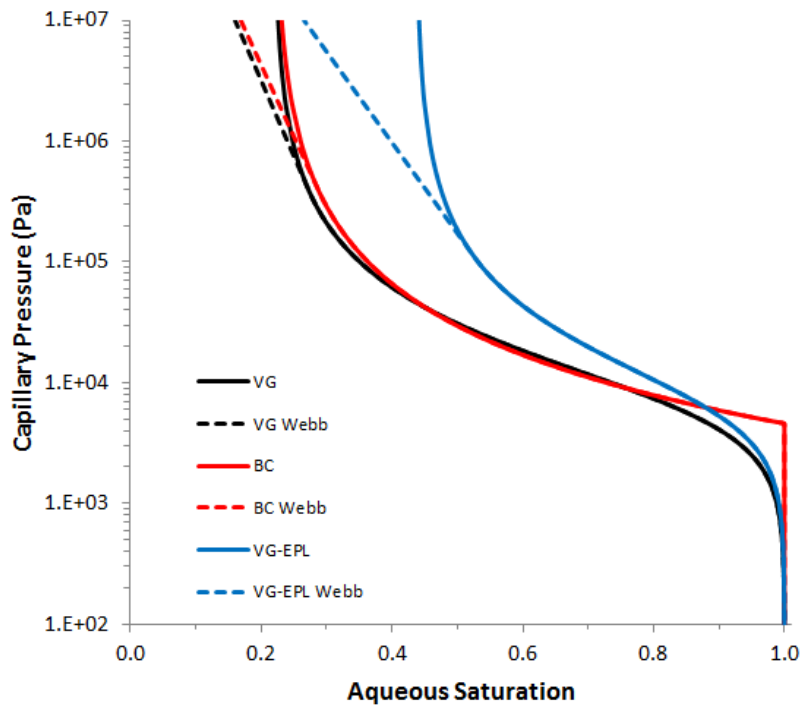
4 **Figure 1.** Capillary pressure-saturation relations, with and without the Webb
5 (2000) extension, for (a) Berea, (b) Paaratte, (c) Tuscaloosa, and (4)
6 Mt.Simon sandstone.

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(c)



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(d)

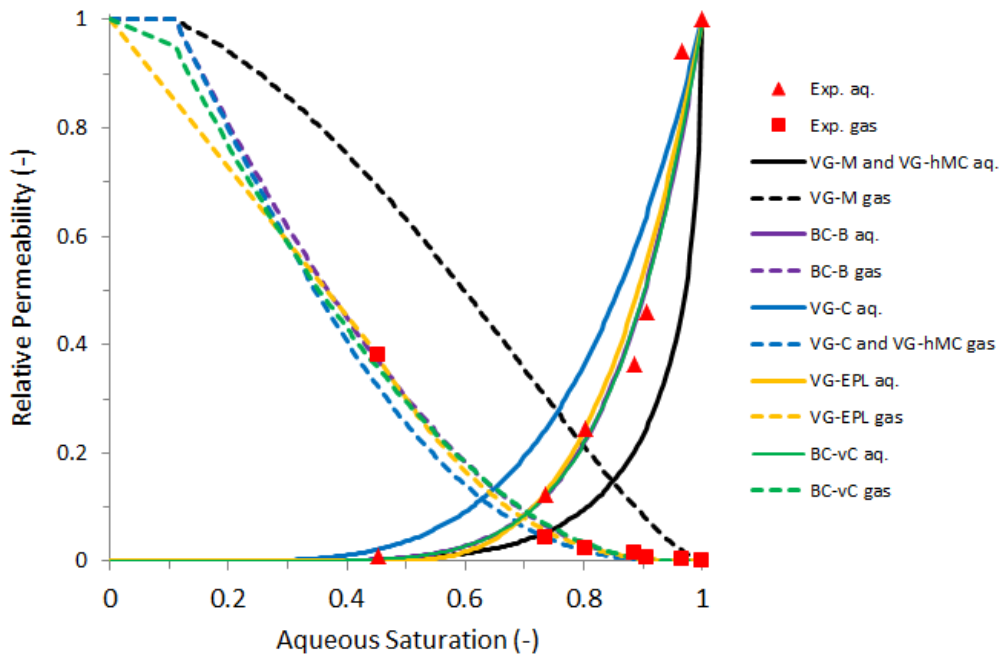
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Figure 1. Continued.

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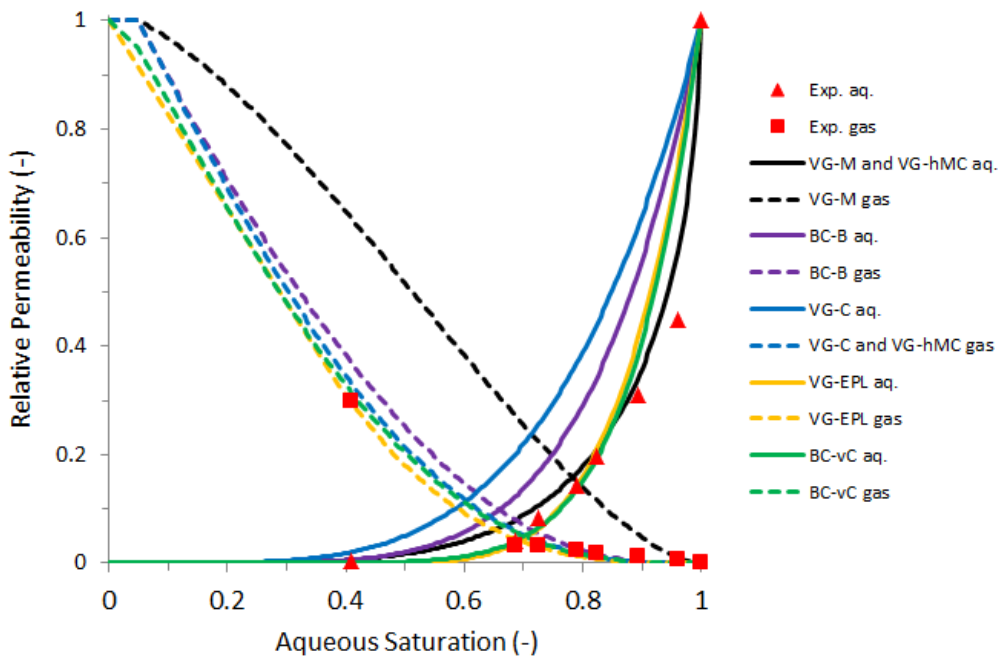
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(a)

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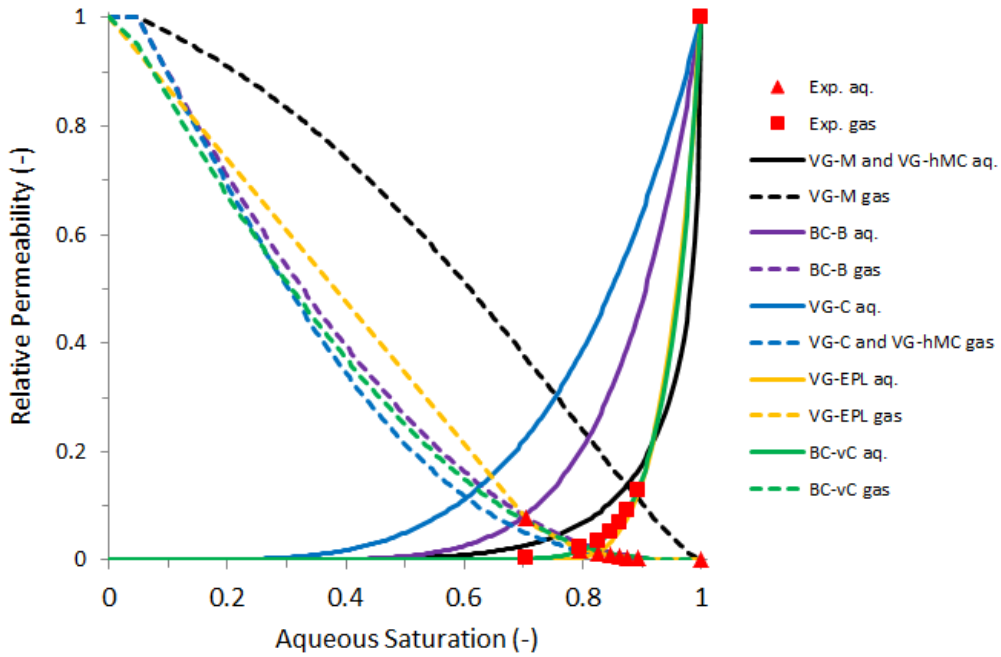
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(b)

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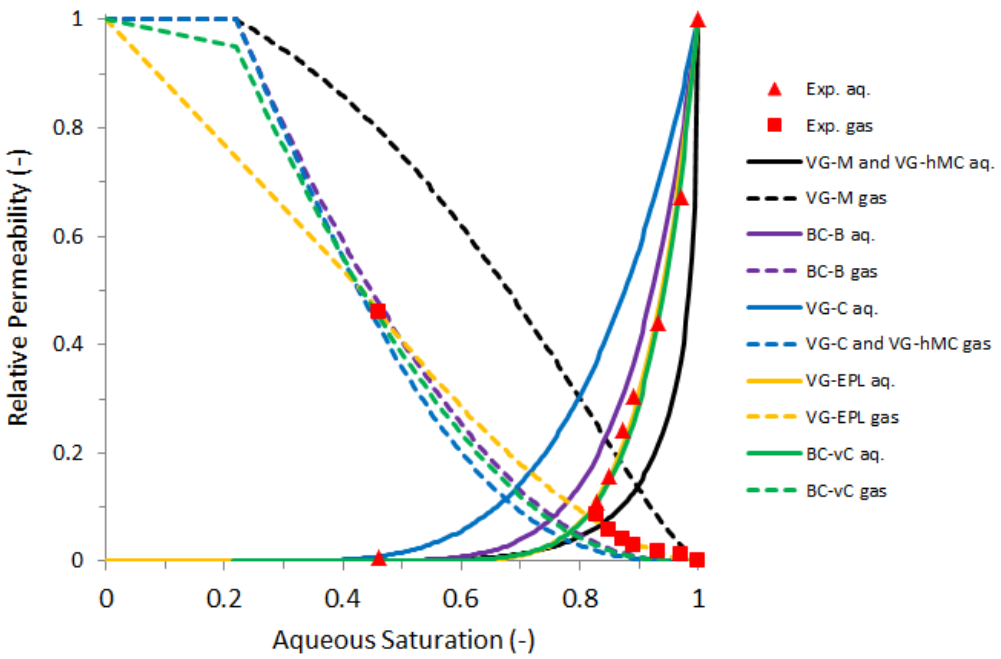
6 **Figure 2.** Experimental (from Krevor et al., 2012) and model relative
7 permeabilities for (a) Berea, (b) Paaratte, (c) Tuscaloosa, and (d) Mt.
8 Simon sandstone.

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(c)

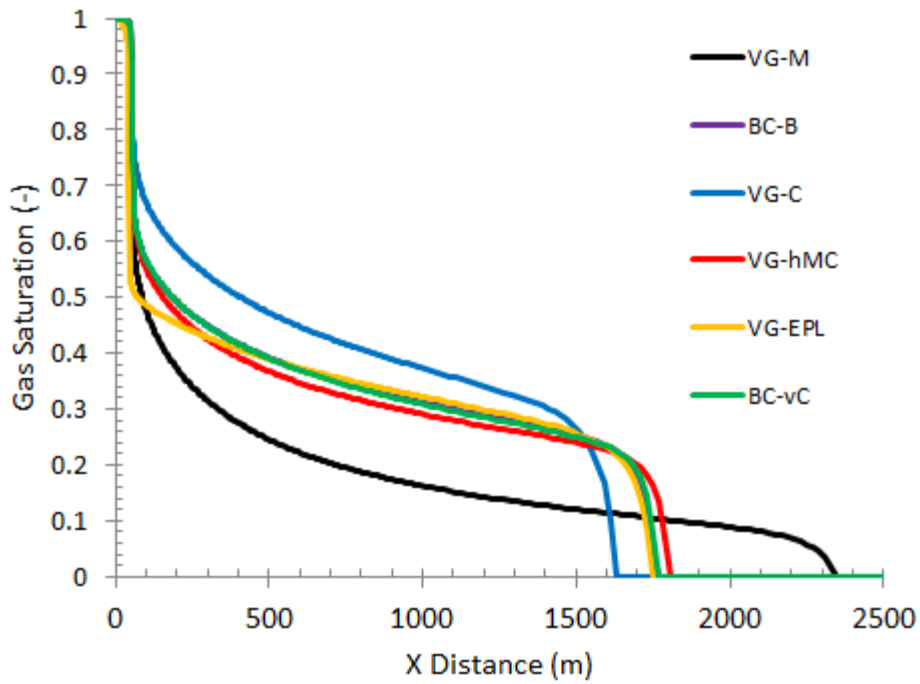
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(d)

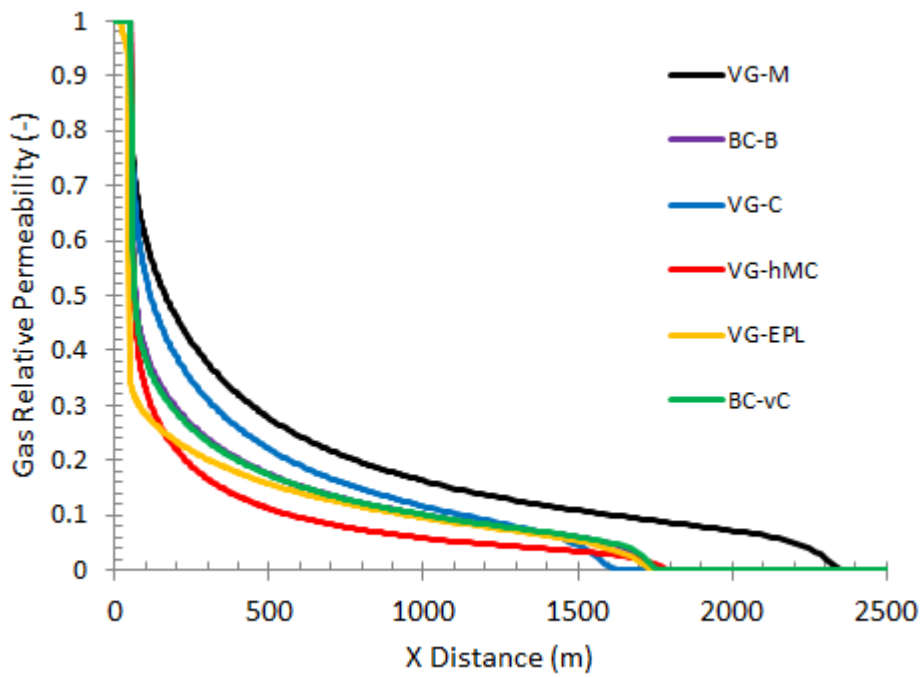
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Figure 2. Continued.



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(a)

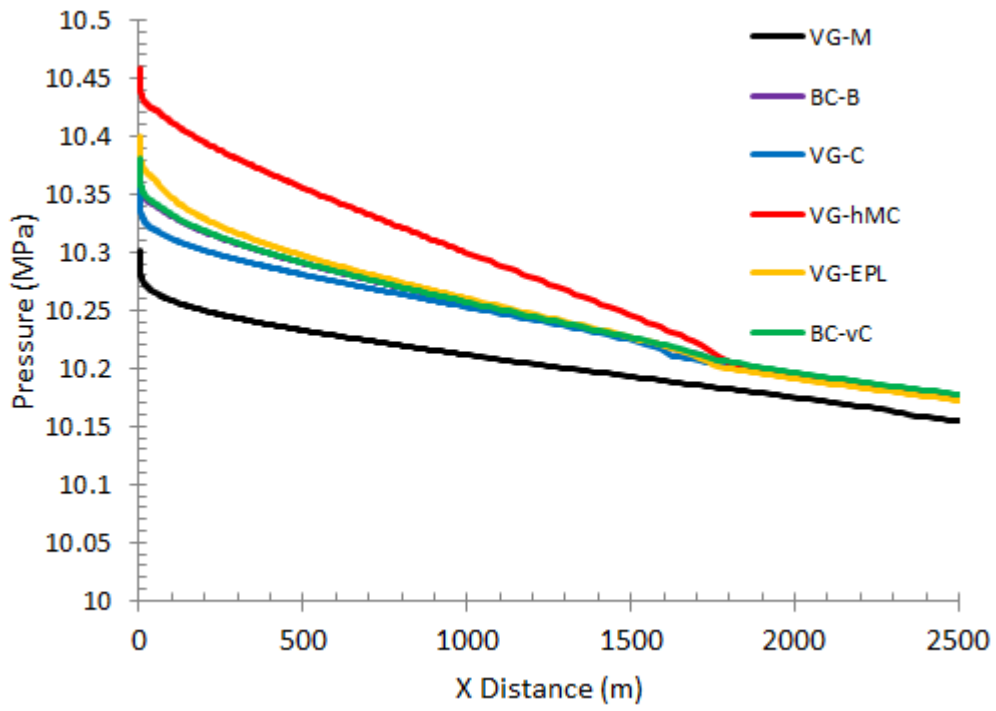


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(b)

3 **Figure 3.** (a) Gas saturation, (b) gas relative permeability, and (c) well
 4 pressure at the end of the injection period for the 1-D Berea
 5 simulations.
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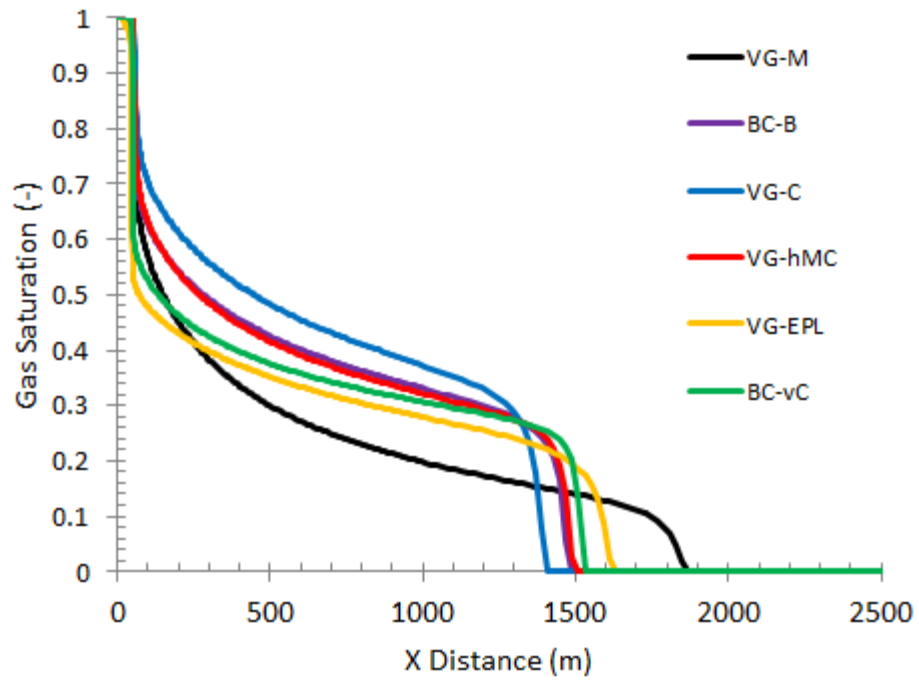
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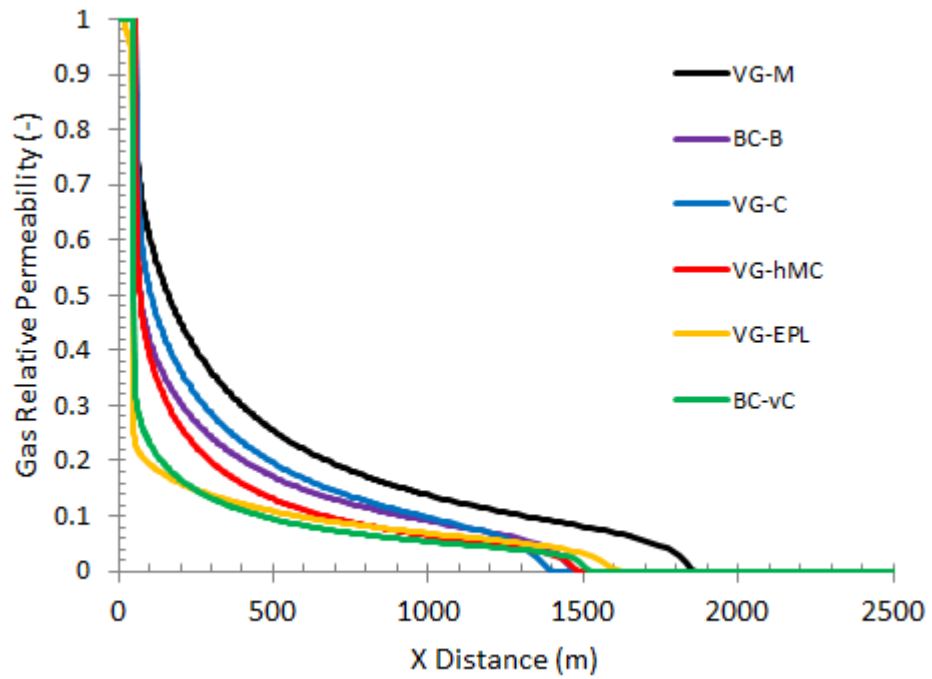
Figure 3. Continued.

(c)



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(a)



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(b)

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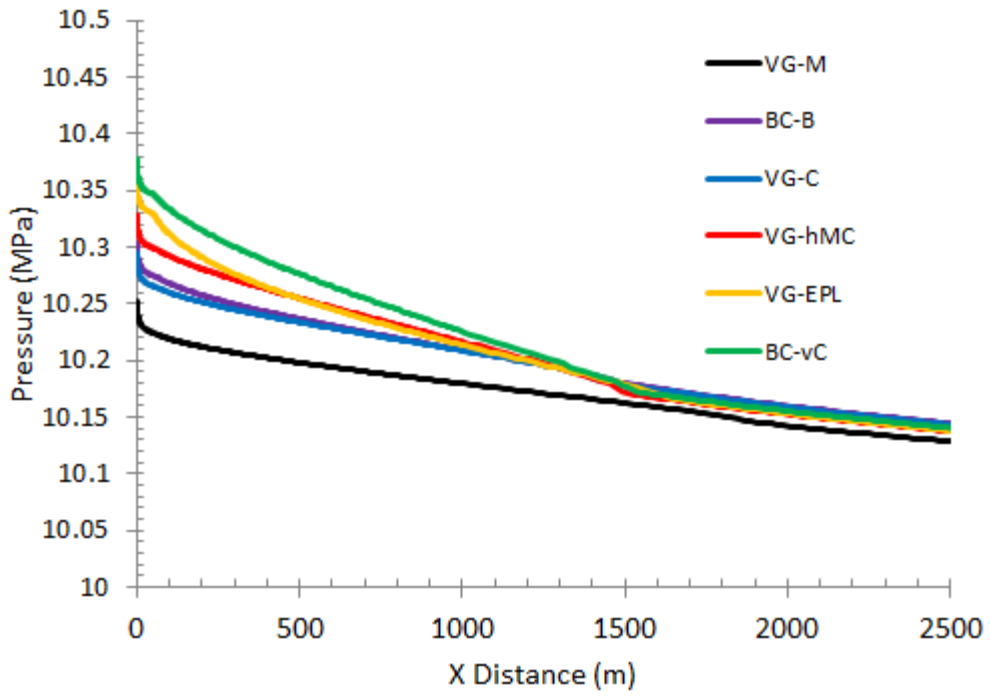
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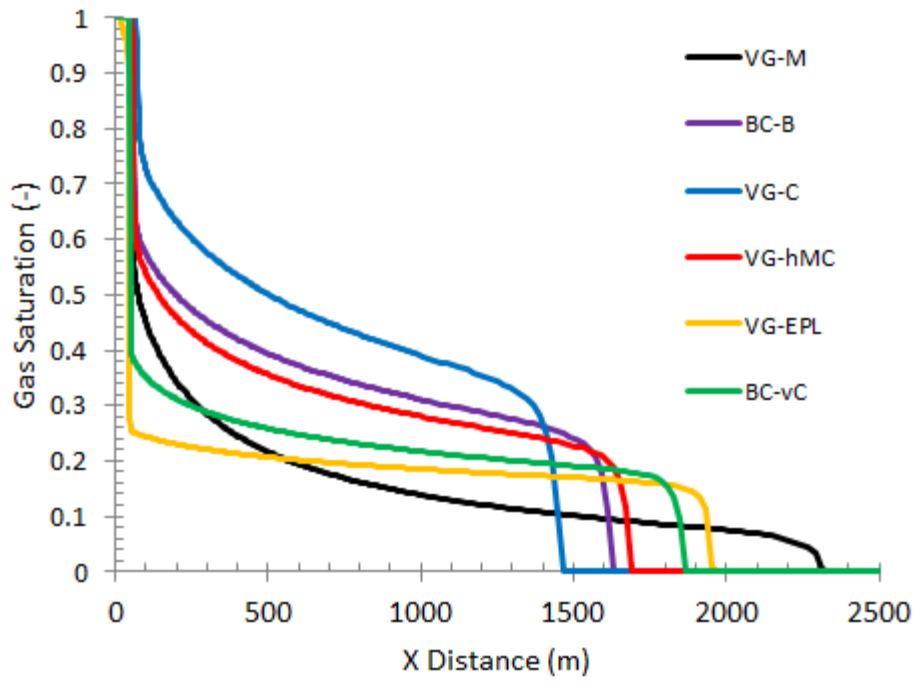
Figure 4. (a) Gas saturation, (b) gas relative permeability, and (c) well pressure at the end of the injection period for the 1-D Paaratte simulations.



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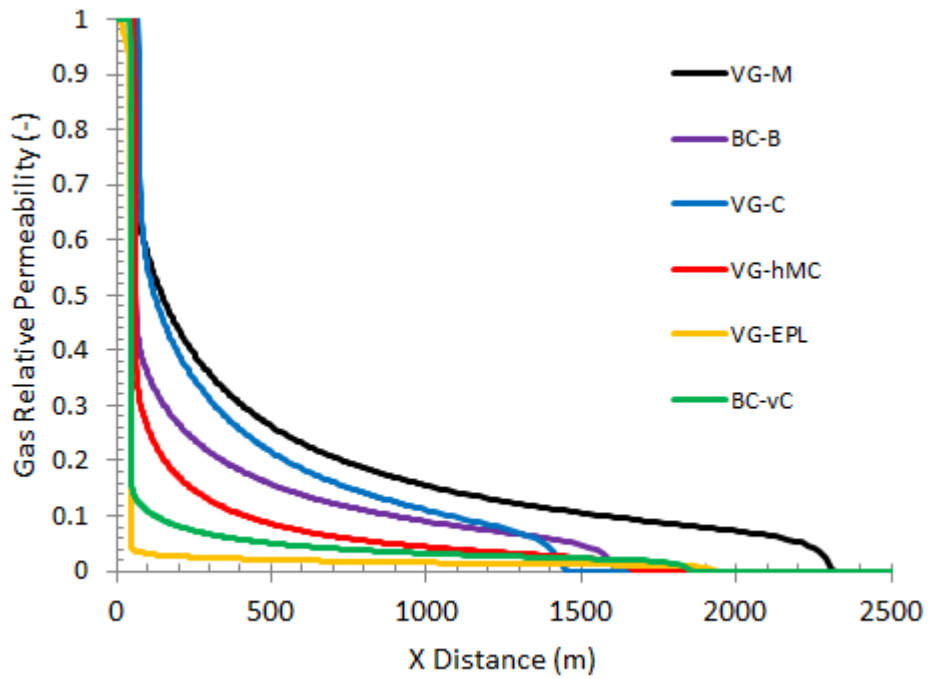
Figure 4. Continued.

(c)



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(a)



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(b)

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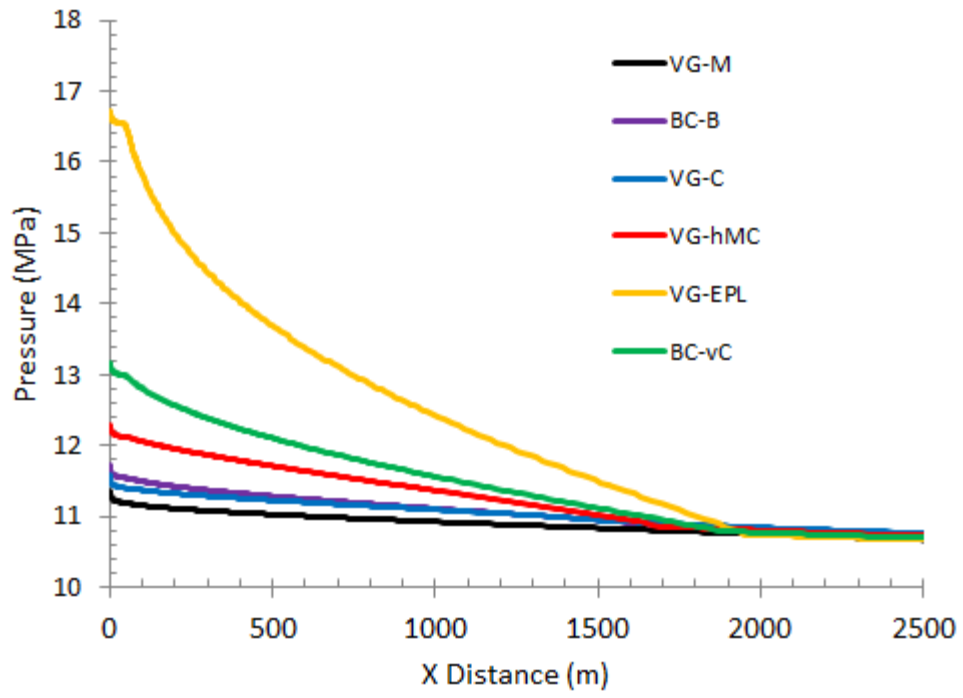
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Figure 5. (a) Gas saturation, (b) gas relative permeability, and (c) well pressure at the end of the injection period for the 1-D Tuscaloosa simulations.

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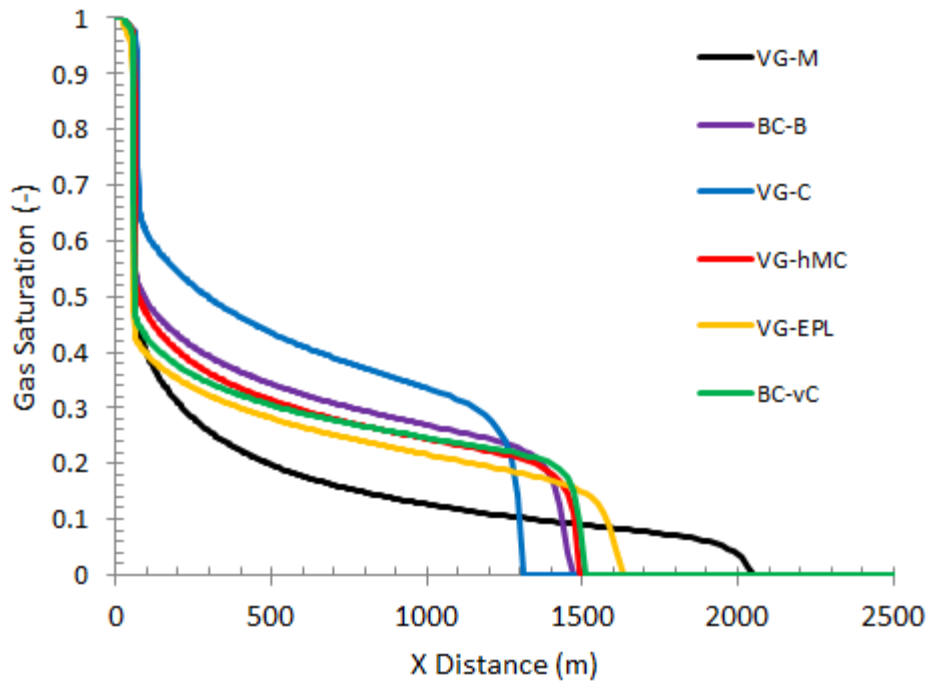
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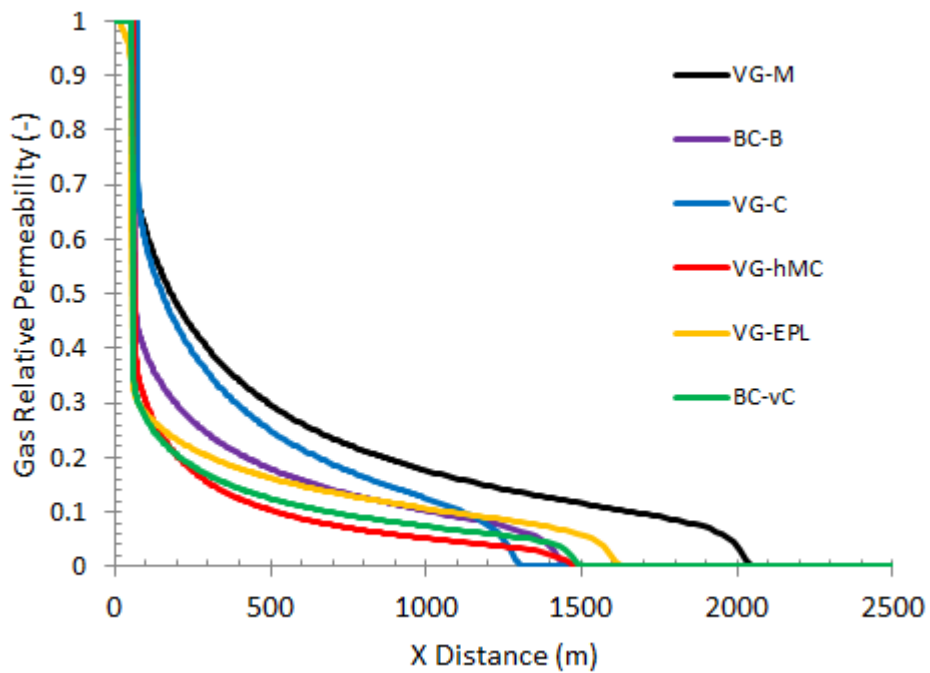
Figure 5. Continued.

(c)



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(a)



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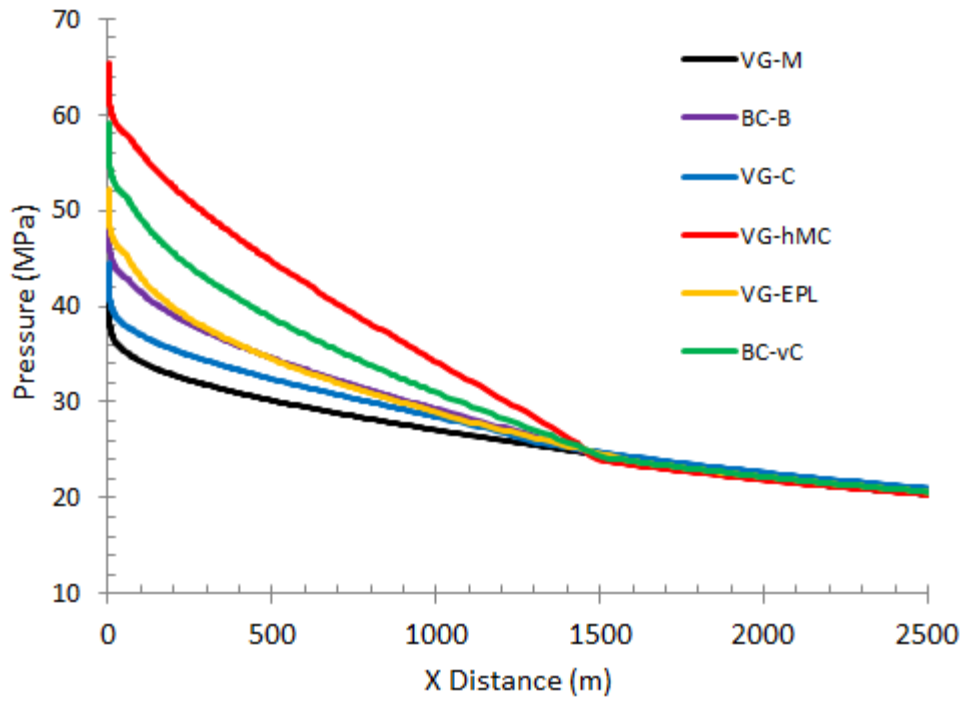
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Figure 6. (a) Gas saturation, (b) gas relative permeability, and (c) well pressure at the end of the injection period for the 1-D Mt. Simon simulations.

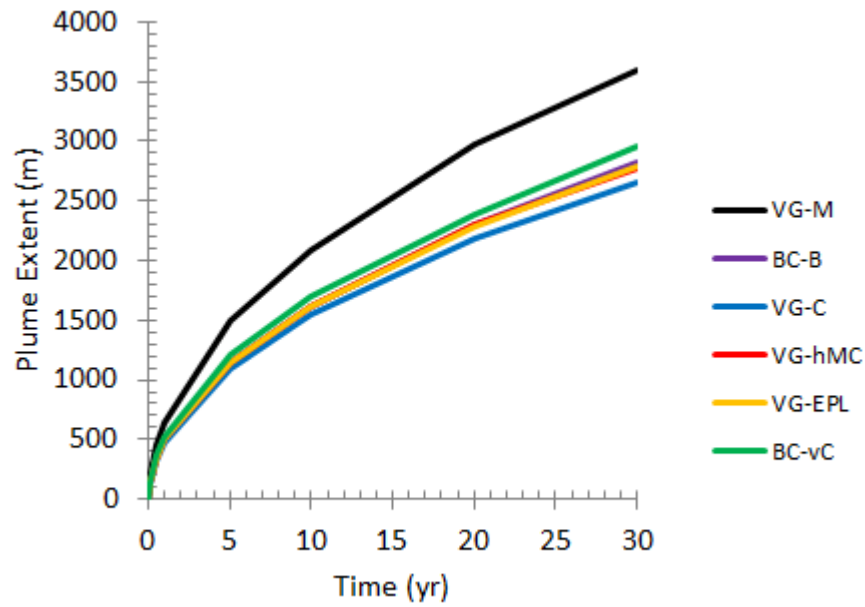


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Figure 6. Continued.

(c)

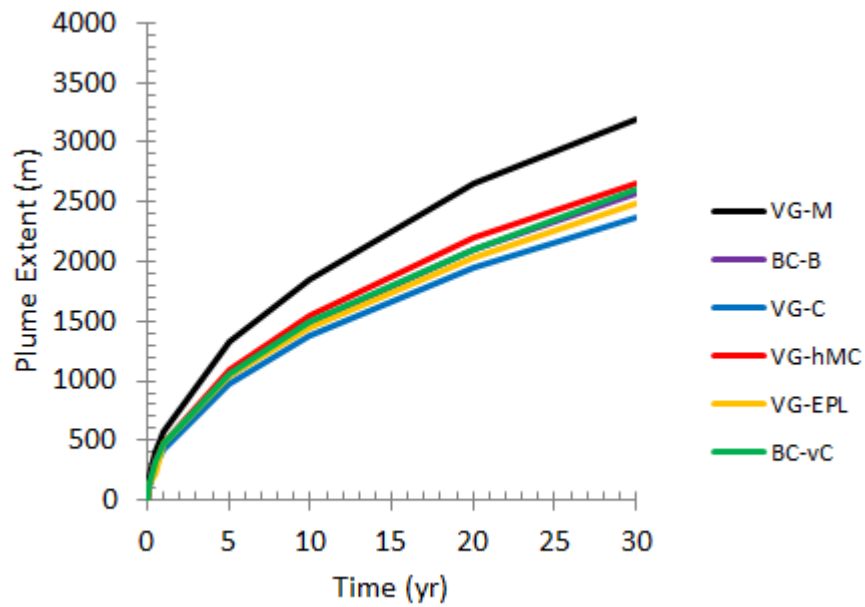
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(a)

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(b)

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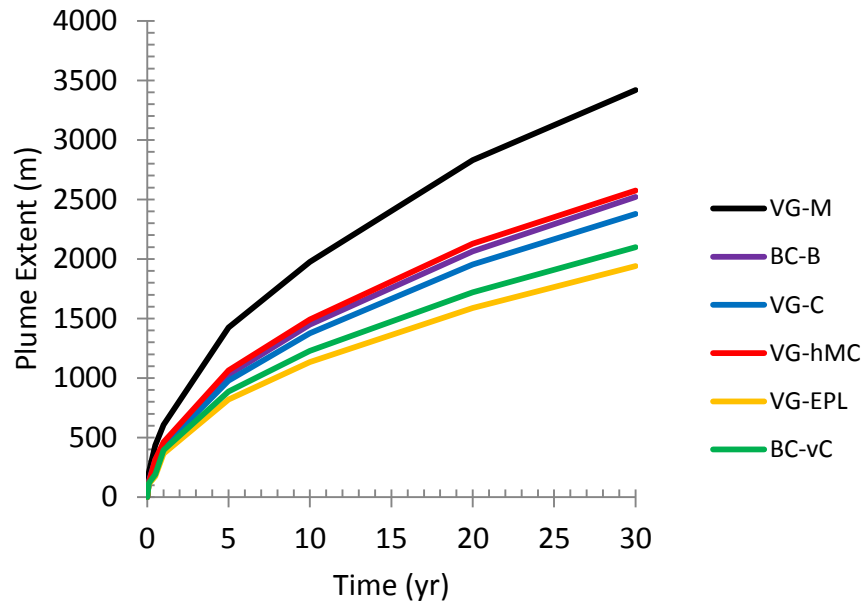
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Figure 7. Plume extent (horizontal distance from injection well) over time for 2-D simulation of injection into (a) Berea, (b) Paaratte, (c) Tuscaloosa, and (d) Mt. Simon sandstone.

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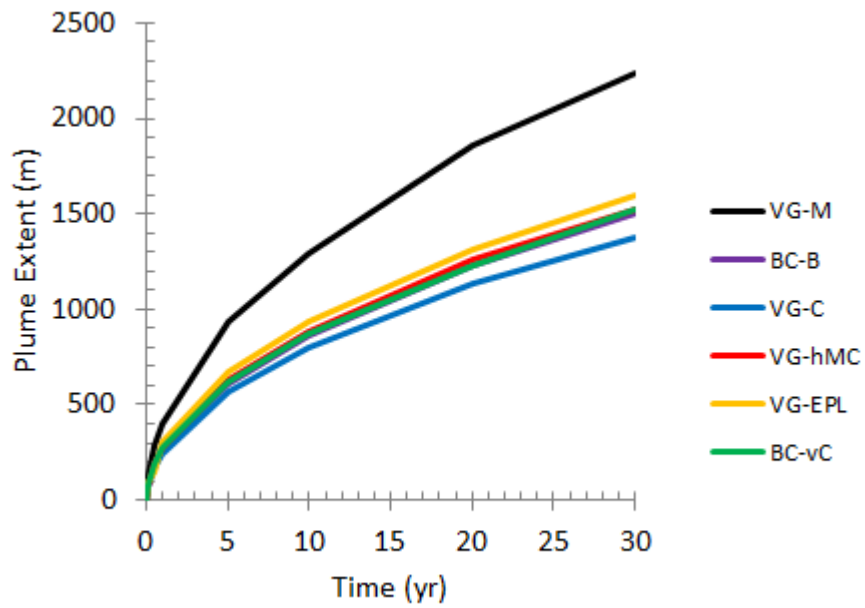
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(c)



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(d)

3 **Figure 7.** Continued.

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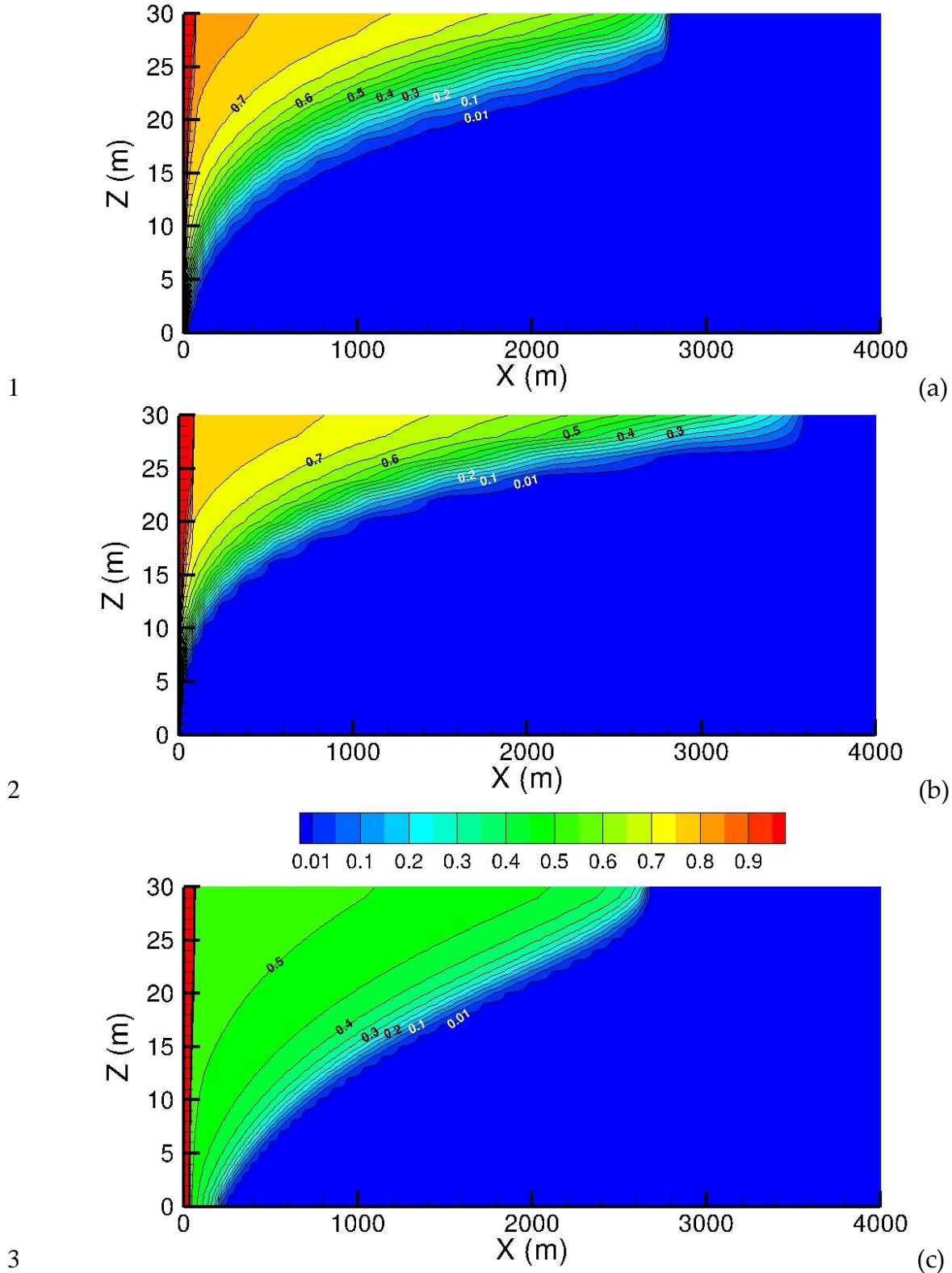


Figure 8. Gas saturation after 30 years of injection into Berea sandstone using the (a) BC-vC, (b) VG-M, and (c) VG-EPL $k_r - S - P_c$ model.

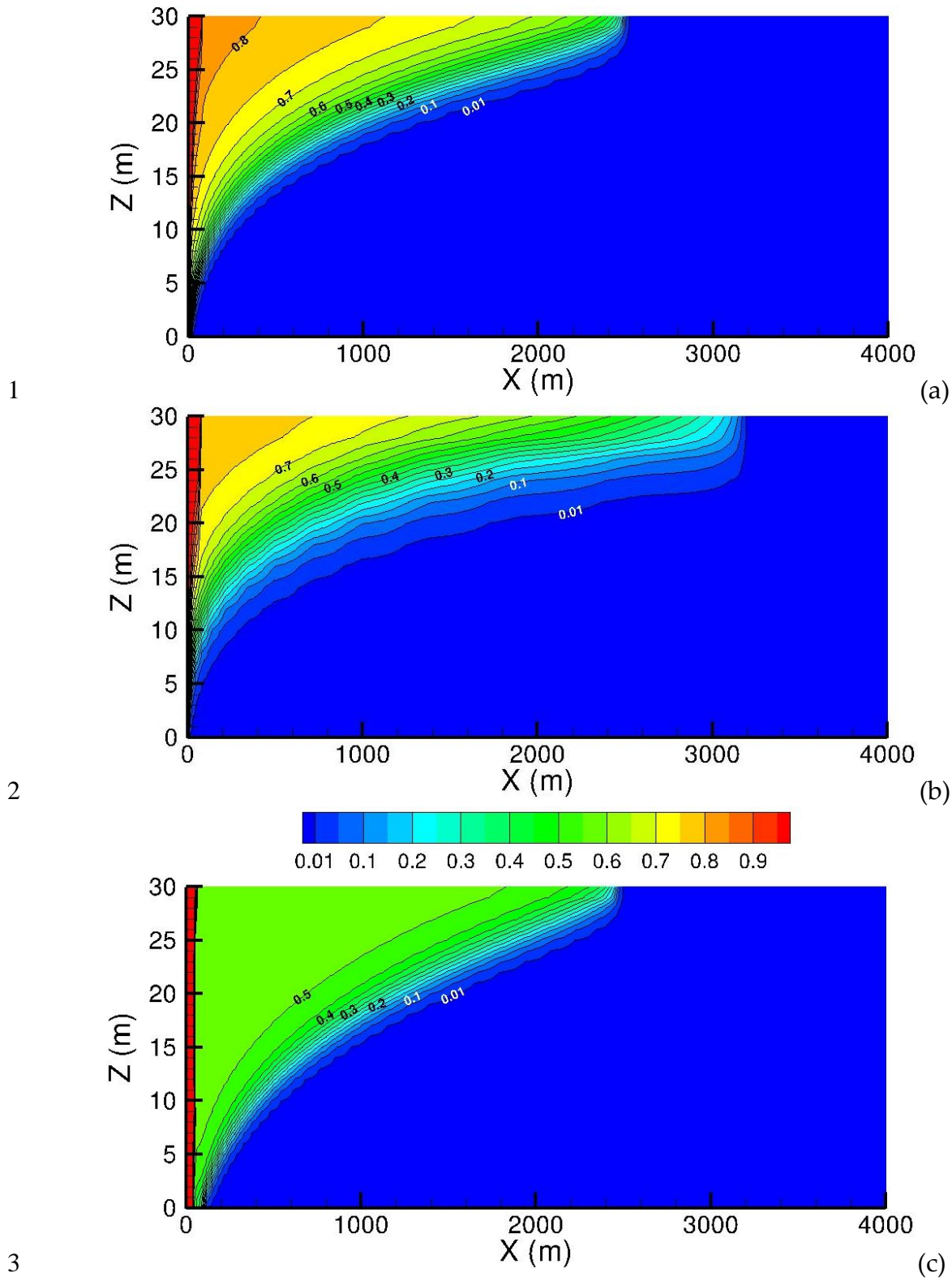


Figure 9. Gas saturation after 30 years of injection into Paaratte sandstone using the (a) BC-vC, (b) VG-M, and (c) VG-EPL $k_r - S - P_c$ model.

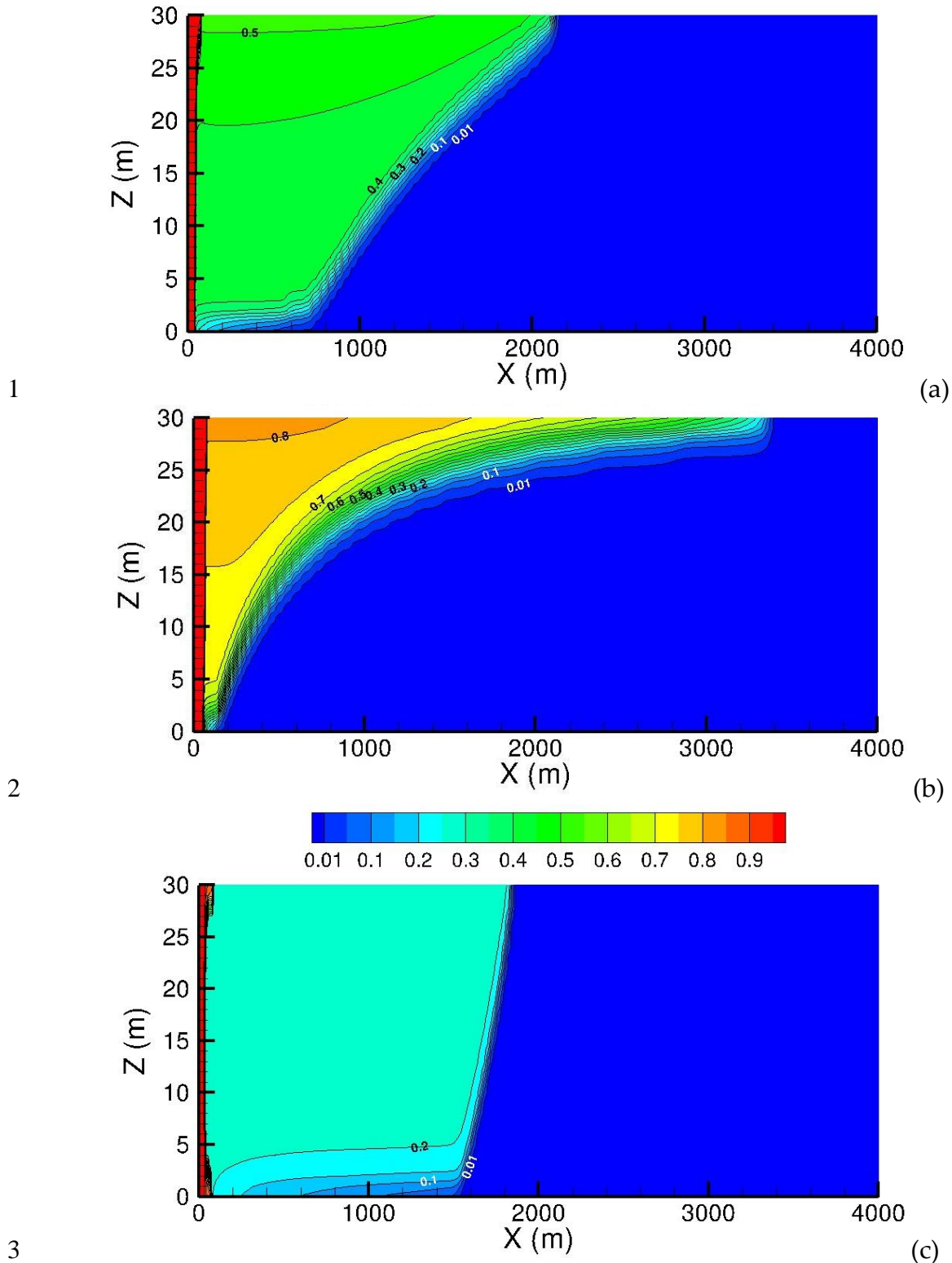


Figure 10. Gas saturation after 30 years of injection into Tuscaloosa sandstone using the (a) BC-vC, (b) VG-M, and (c) VG-EPL $k_r - S - P_c$ model.

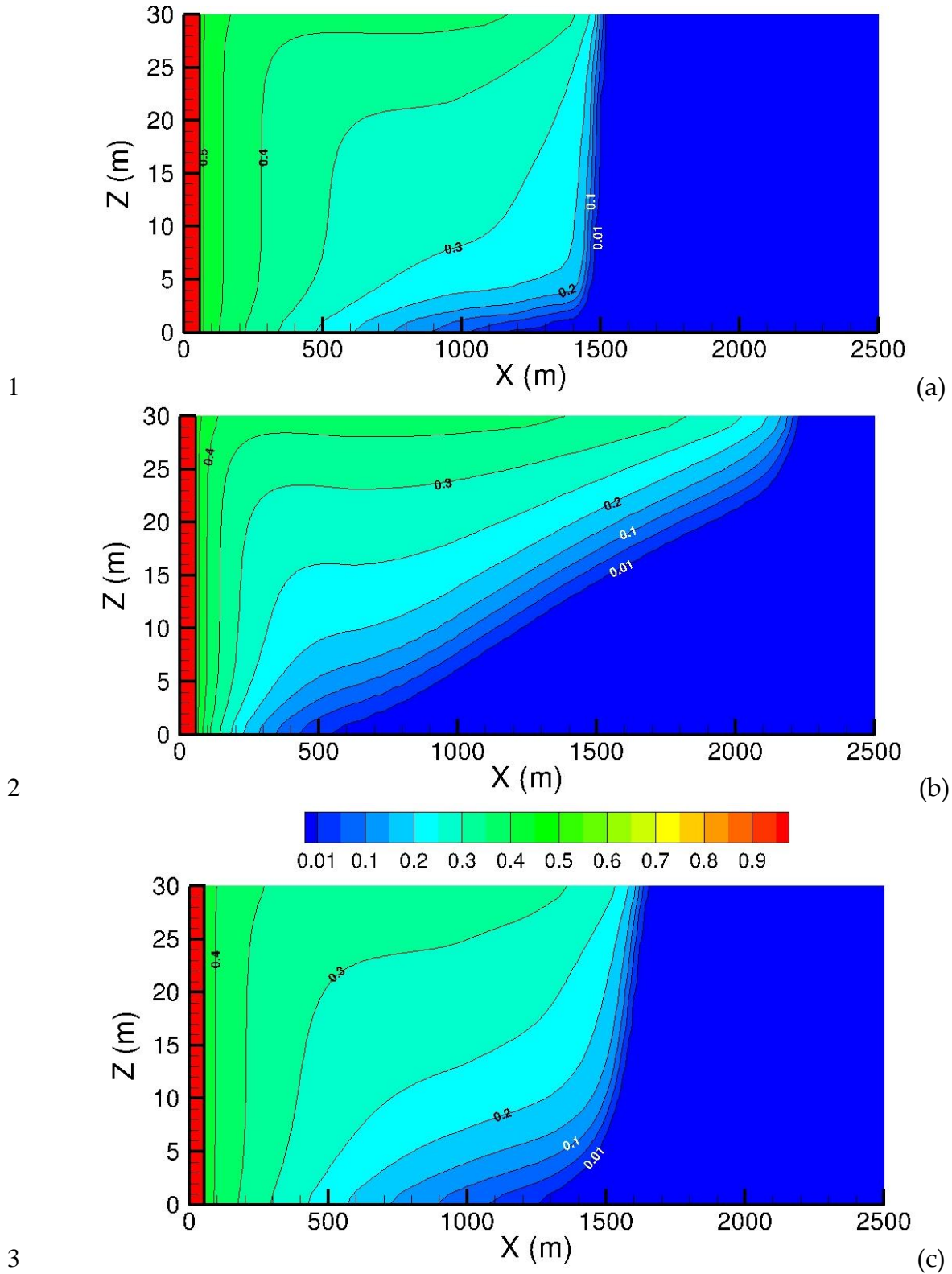
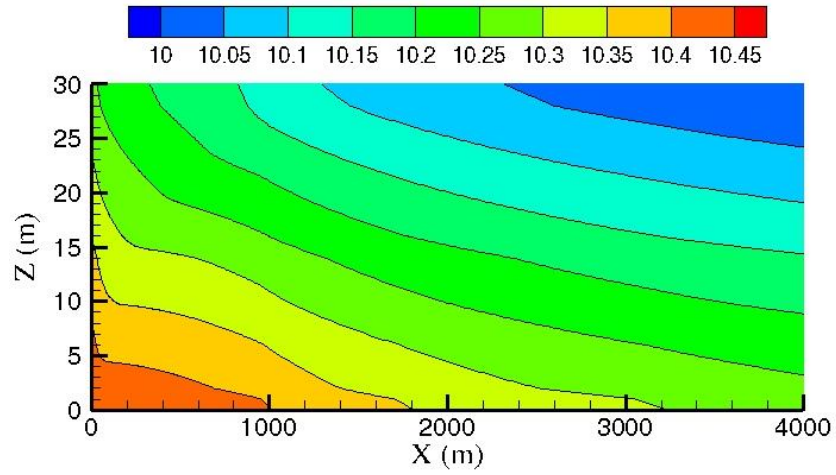
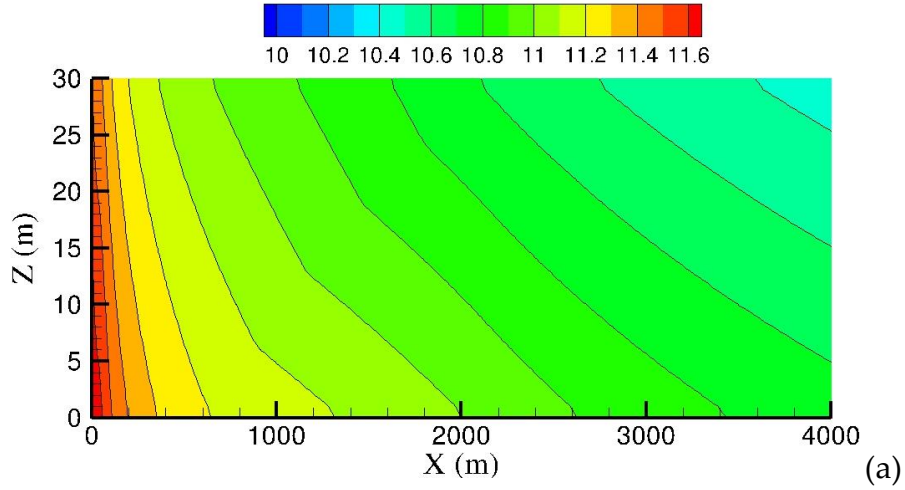


Figure 11. Gas saturation after 30 years of injection into Mt. Simon sandstone using the (a) BC-vC, (b) VG-M, and (c) VG-EPL $k_r - S - P_c$ model.

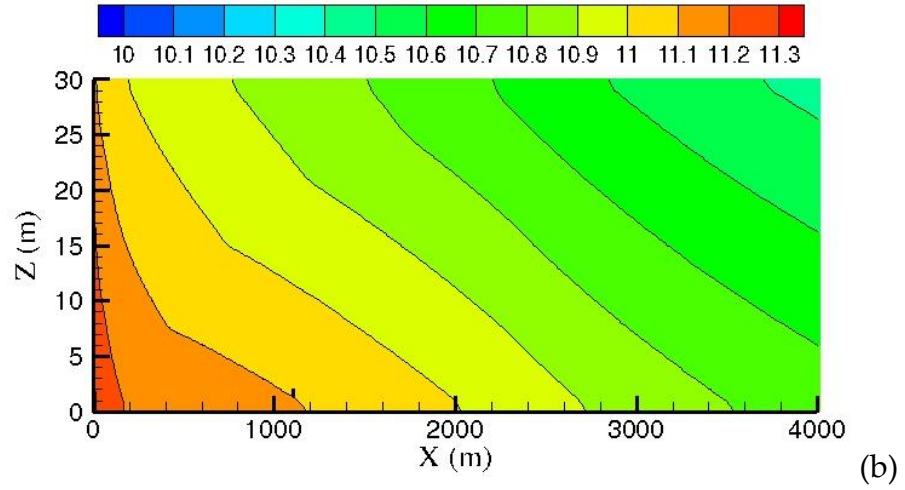


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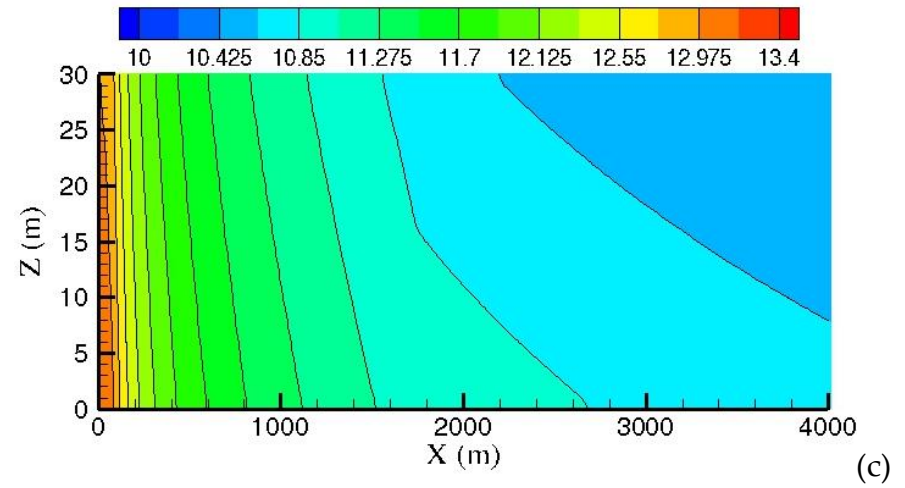
Figure 12. Formation fluid pressures (in MPa) at the end of the injection period for the Berea BC-vC simulation.



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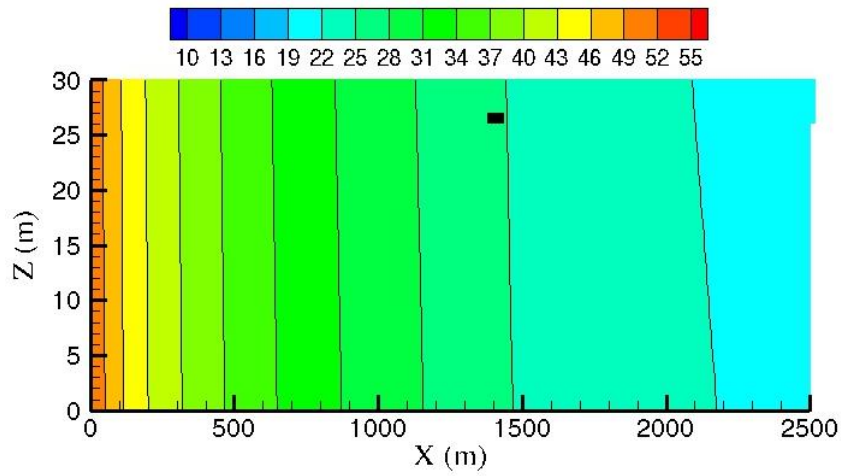
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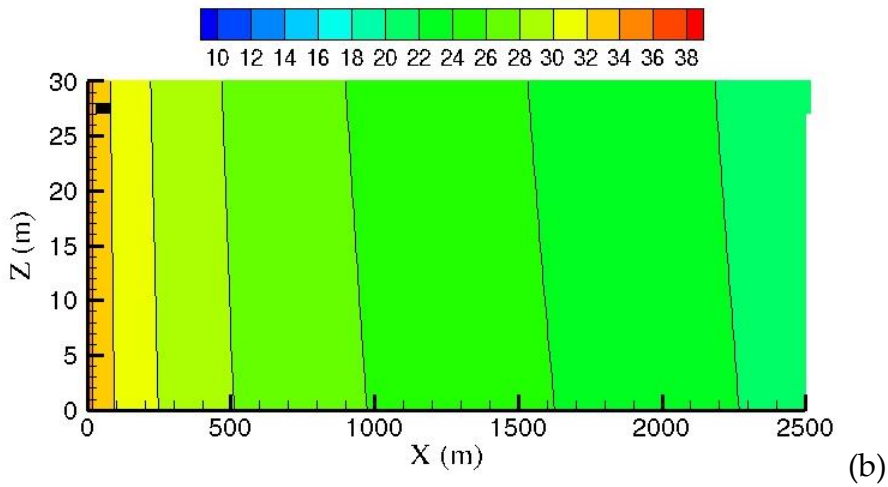
7 **Figure 13.** Formation pressure distribution (in MPa) at the end of the injection
8 period for the Tuscaloosa (a) BC-vC, (b) VG-hMC, and (c) VG-EPL
9 simulations.

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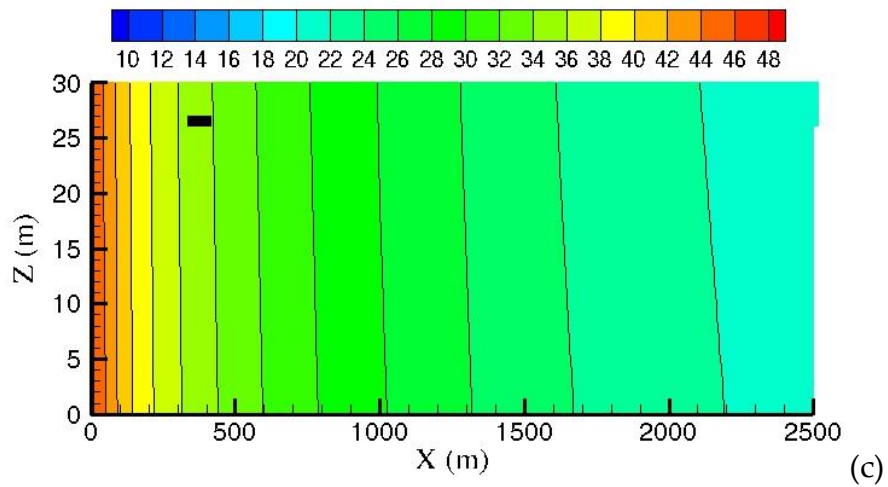
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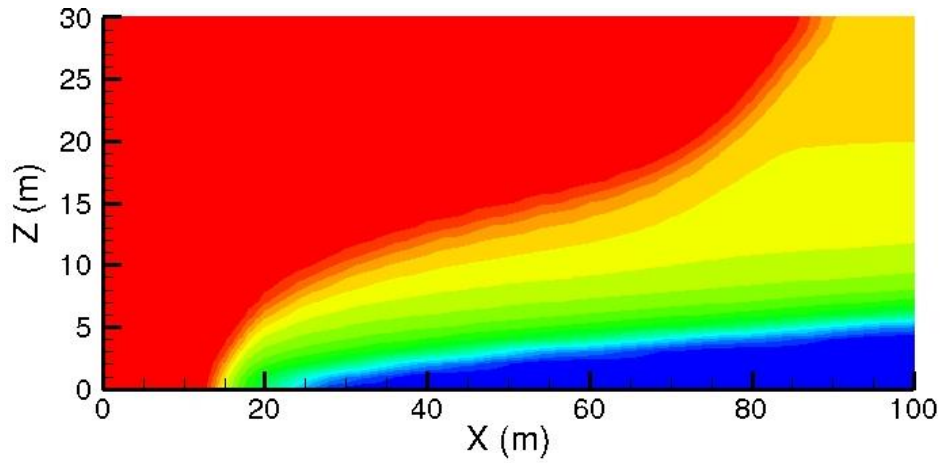
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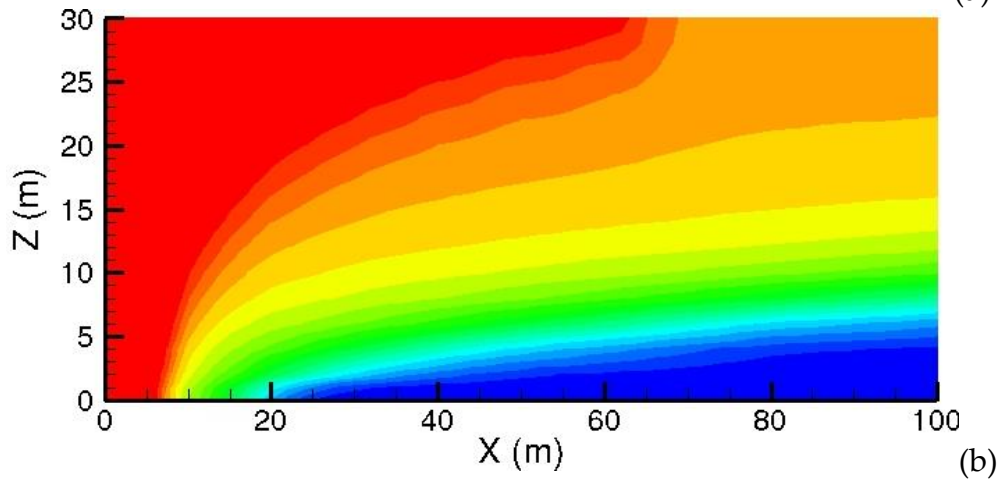
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Figure 14. Formation pressure distribution (in MPa) at the end of the injection period for the Mt.Simon (a) BC-vC, (b) VG-hMC, and (c) VG-EPL simulations.

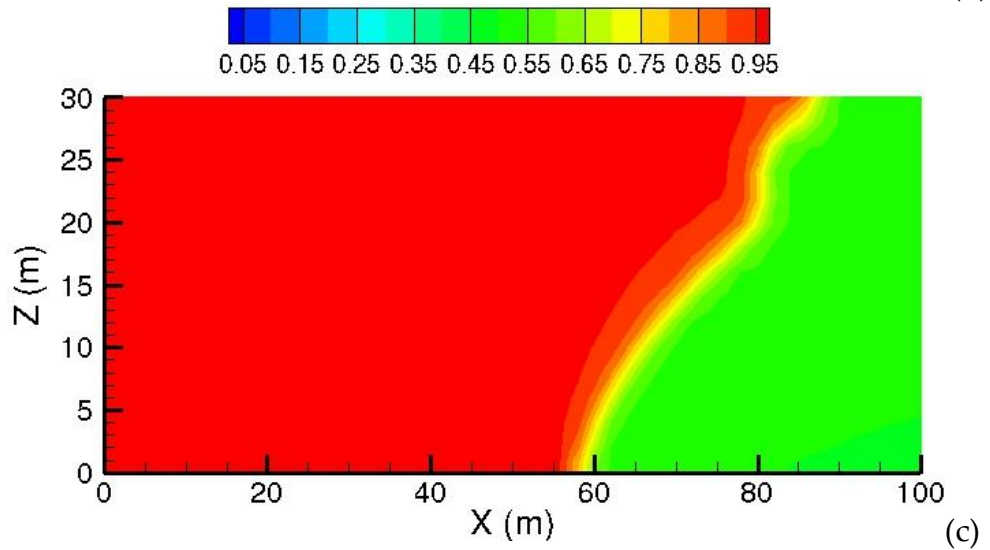
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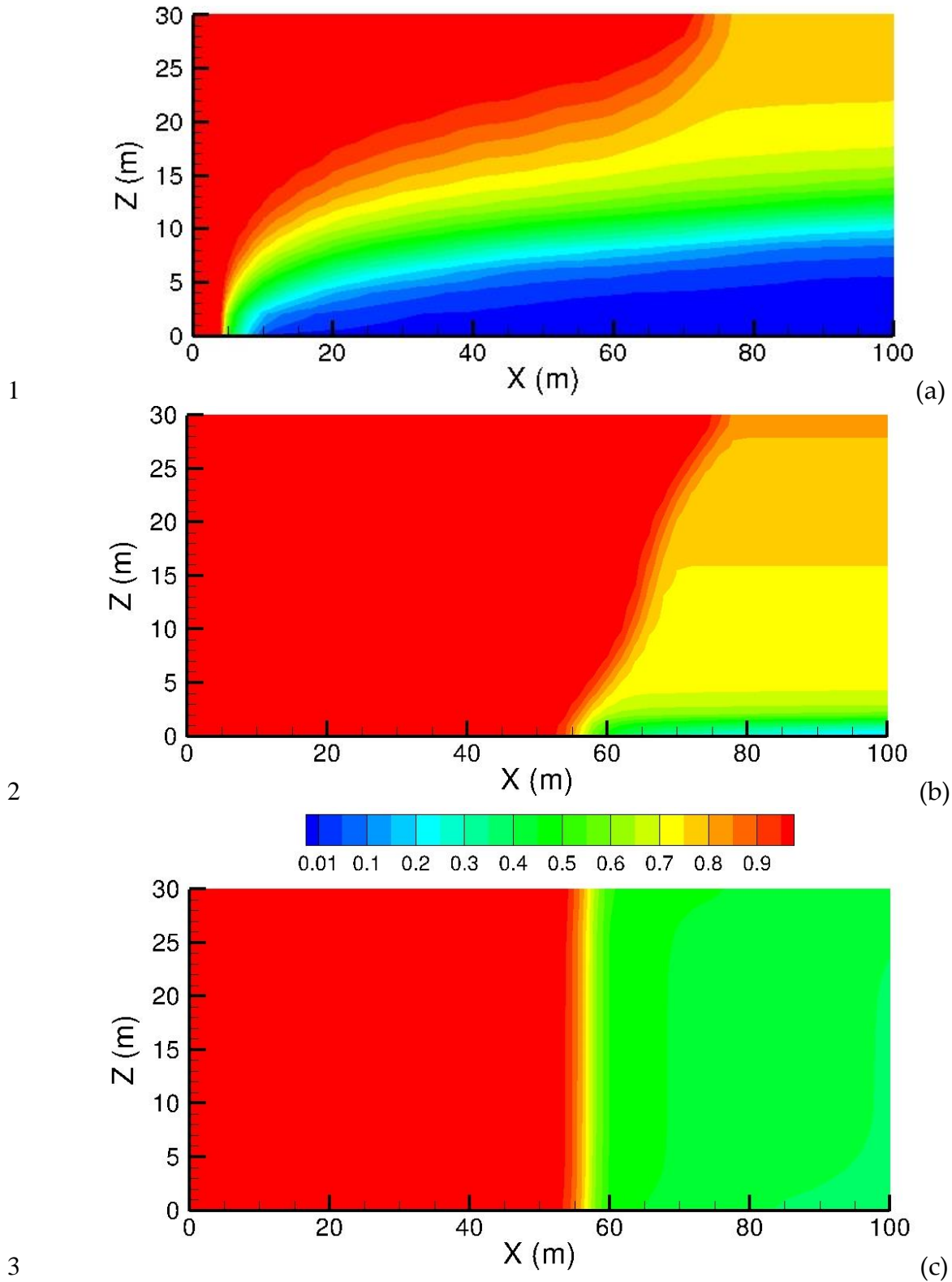
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Figure 15. Near-well gas saturation at the end of the 30-yr injection period into Berea sandstone for the (a) VG-M, (b) VG-C, and (c) VG-EPL $k_r - S - P_c$ models.



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Figure 16. Near-well gas saturation at the end of the 30-yr injection period into (a) Paaratte, (b) Tuscaloosa, and (c) Mt. Simon sandstone for the VG-M $k_r - S - P_c$ model.