

Turbulent Transport in Premixed Flames Approaching Extinction

K. H. H. Goh, P. Geipel, R. P. Lindstedt*

Department of Mechanical Engineering, Imperial College, London SW7 2AZ, UK

*Corresponding author.

Fax: +44 20 7594 5696. Email: p.lindstedt@imperial.ac.uk

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Figure 5: 154 (method 2)

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K. H. H. Goh^a, P. Geipel^b, R. P. Lindstedt*

Department of Mechanical Engineering, Imperial College, London, SW7 2AZ, UK

Abstract

The turbulent transport in premixed flames approaching extinction has been characterised in terms of statistical properties using an opposed jet burner featuring fractal grid generated turbulence. The burner was used in a symmetric twin flame configuration featuring pre-vaporised cyclopentane and JP-10 (exotetrahydrodicyclopentadiene) at equivalence ratios of 0.75 and 0.85. The choice of fuels follows from the practical importance of JP-10 as an aviation fuel with cyclic C₅ compounds appearing as breakdown products. The bulk velocity was set to 3.0 m/s resulting in a turbulent Reynolds number of 120. The obtained data includes conditional velocity statistics, flame curvature information and scalar fluxes. The conversion between conventionally and Favre averaged statistics follows the Bray-Moss-Libby theory and the assumption that finite reaction interface thickness effects can be neglected. The impact of deviations from the latter on statistics is explored and results suggest that the effect is modest for interface thicknesses less than 20% of the turbulent flame brush. The experimental data obtained is sufficient to enable terms up to and including triple correlations to be evaluated in closed form. The work also clearly illustrates the rapid transition from non-gradient to gradient turbulent transport as the extinction limit is approached.

Keywords: Fractal grids, Premixed, BML, Opposed jets, Liquid fuels

*Corresponding author. Fax: +44 20 7594 5696.

Email address: p.lindstedt@imperial.ac.uk (R. P. Lindstedt)

Current address: ^aInstitute of Materials Research and Engineering 3, Research Link, Singapore 117602.

^bSiemens Industrial Turbomachinery AB, SE-612 83 Finspong, Sweden.

1. Introduction

Bilger et al. [1] observe that turbulent premixed combustion is commonly agreed to be inherently complex with increasingly wide application in internal combustion engines, modern gas turbines for power generation and jet engine afterburners [2]. The increased use stems from a desire to reduce emissions while obtaining higher efficiencies. Bray, Moss and Libby [3] derived the arguably most successful framework (BML) for analysing turbulent premixed combustion on the basis of a statistical description and Bray [4] presented a recent review of the approach. The current contribution considers statistically stationary flames in the context of this framework through experimental measurements using a twin flame opposed jet geometry featuring fractal grid generated turbulence. The density segregation technique derived by Goh et al. [5] is used to detect flame iso-contours and to obtain conditional statistics. Opposed jet flames have been used extensively in the past (e.g. [6–10]) and recent contributions include those of Geipel et al. [11], Goh et al. [12, 13] and Coriton et al. [14].

The use of fractal grids to generate multiscale turbulence was proposed by Vassilicos and Hunt [15] and subsequently investigated by Hurst and Vassilicos [16] and Stresing et al. [17]. Fractal grids have shown significant promise in generating elevated levels of turbulence while maintaining flows free of bulk instabilities. The ideal grid for the opposed jet configuration was identified by Geipel et al. [11] and found to produce a 100% increase in Reynolds stresses compared to traditional grids with 4 mm holes as used previously by Böhm et al. [18]. Comprehensive statistical information for twin methane and propane flames has also been obtained by Goh et al. [13] using synchro-

26 nised velocity and scalar statistics to provide conditional dissipation and flow
27 field structure information via conditional Proper Orthogonal Decomposition
28 (CPOD). A revised configuration was used by Goh et al. [12] to study the
29 transition from conventional premixed turbulent JP-10 flames to a Homo-
30 geneous Charge Diffusion Ignition (HCIDI) [19] related flameless oxidation
31 mode using single JP-10 flames. It was observed that conventional flames
32 ceased to exist after transition to flameless oxidation, with reaction inter-
33 faces residing on the instantaneous stagnation plane, similar to flames close
34 to extinction as observed by Kostiuk et al. [6]. Furthermore, a shift from
35 non-gradient to gradient turbulent transport was observed for flames beyond
36 the normal extinction point [12] as the combustion mode shifted to flameless
37 oxidation. Under such conditions, reactant conversion must be supported by
38 hot combustion products emerging from one of the nozzles.

39 By contrast, the current study considers turbulent transport in flames ap-
40 proaching extinction in a conventional back-to-back twin flame configuration
41 that can more readily be related to conventional premixed turbulent flame
42 theories (e.g. BML). Density segregation methods e.g. [5, 12, 20], used in the
43 current work, result in flame isocontours one pixel in width. For flames with
44 a broader reaction interface, the probability of detecting a burning mixture
45 may become significant. The effect has been assessed experimentally through
46 comparisons with OH-PLIF [12, 21] and the current work provides a further
47 theoretical analysis of the impact on statistics. The approach is based on
48 a stochastic analysis of the impact of the ratio of the flame thickness (δ_f)
49 or, more generally, the instantaneous interface thickness (δ_I) to the turbu-
50 lent reaction zone (flame brush) thickness (δ_t). The analysis supports the

51 conclusion [12] that the impact on reaction progress variable (c) statistics
52 is negligible under the current experimental conditions. The finding allows
53 direct comparisons of experimental results with theoretical investigations of
54 premixed turbulent flames stabilised in evolving multiscale turbulence. Fi-
55 nally, a set of equations [22] that enable the closed form conversion between
56 conventionally and Favre averaged terms, up to and including triple correla-
57 tions, on the basis of presented experimental data are reported.

58 2. Experimental Techniques

59 The turbulent opposed jet configuration corresponds to that of Goh et
60 al. [12] with the exception that the optimal fractal grids identified by Geipel
61 et al. [11] were used in both nozzles in order to produce a twin flame config-
62 uration. Impact plates were placed upstream of the fractal grids in order to
63 isolate upstream conditions from grid generated turbulence [23] and hence
64 to simplify the boundary conditions leading to a reduced size of the physical
65 domain required for computational studies. The nozzle exits were one nozzle
66 diameter D ($= 30$ mm) apart. Twin premixed flames of cyclopentane and
67 JP-10 were investigated using equivalence ratios (ϕ) of 0.75 and 0.85. Flow
68 rates were such that mixtures from each nozzle had a bulk velocity (U_b) of
69 3.0 m/s (at 298 K). Cyclopentane and JP-10 were heated to 353 K and 473 K,
70 respectively, with nozzle exit temperatures of 333 K and 408 K maintained
71 in order to prevent fuel recondensation.

72 The flow control system was the same as used by Goh et al. [12] with
73 uncertainties in flow rates ≤ 0.8 % for each fluid. Flow rates of cyclopentane
74 and JP-10 were metered and vapourised using Bronkhorst CoriFlow M53 and

75 CEM W-303A units with the vapourised fuel stream mixed with air and split
76 equally using two needle valves. Measurements performed using GCMS on
77 the reactant stream using an Agilent 7890A series GC with a 5975C inert
78 MSD/DS Turbo EI Bundle equipped with 60 m DB-1 column have confirmed
79 that no cracking of the fuel takes place. Coflow velocities were set to 0.3 m/s
80 to remove any large scale bulk motion. The reactant streams were mixed
81 further with seeded air within heated hoses, temperature controlled with an
82 accuracy of ± 1 K, for about 3 m before being introduced into the nozzles.
83 A digital camera was used to capture the CH chemiluminescence from both
84 flames and measurements performed only when CH intensities were equal.

85 Particle Image Velocity (PIV) measurements were conducted in 2D using
86 a 120 mJ Solo-New Wave Nd:YAG laser. Both the upper and lower streams
87 were seeded with aluminium oxide particles of about $3 \mu\text{m}$ diameter with
88 correlation between Mie scattered images calculated using decreasing inter-
89 rogation window sizes from 128×128 via 64×64 to 32×32 with a 50%
90 overlap resulting in velocity vectors spaced about 0.4 mm apart. Laser pulses
91 were separated by $40 \mu\text{s}$ to minimise spurious vectors, and 1000 image pairs
92 were obtained at around 5 Hz for each case (e.g. [8, 11, 12]).

93 **3. Postprocessing techniques**

94 For every image pair the density segregation method of Goh et al. [5]
95 was used to detect flame isocontours in order to synchronise the instanta-
96 neous reaction progress variable (c) with velocity vectors. The method has
97 been shown to be accurate to the order of the reaction interface thickness
98 (δ_I) [5] and used by Goh et al. [12, 13, 23] to obtain synchronised velocity–

99 scalar statistics. The density segregation method bypasses the need for an
100 additional laser for flame front detection and overcomes problems associated
101 with laser alignment. One drawback is that detected isocontours (reaction
102 interfaces) are one pixel wide (~ 0.026 mm). Reaction interfaces are often
103 thicker, as shown by Goh et al. [12], and care needs to be taken to ensure ap-
104 plicability of the method. The flames investigated here are directly related to
105 the latter study where the use of OH-PLIF via the method of Kerl et al. [21]
106 confirmed the applicability. However, the matter has also been investigated
107 theoretically as outlined below.

108 Goh [22] developed an approach to ascertain the impact of a finite mean
109 reaction layer (flame) thickness (δ_f) on measured flow field statistics using
110 a stochastic mapping method. It was shown that the effects of a finite in-
111 terface thickness on profiles of the mean progress variable were insignificant
112 even when it reached 20% of the turbulent flame brush thickness (δ_t). The
113 simulated flame brush was defined using a Gaussian *pdf* for flame location,
114 such that the distance between the 5th and 95th percentiles of its cumula-
115 tive distribution function (*cdf*) was equal to the measured value. Profiles
116 of instantaneous reaction sheets were also assumed to be in the shape of a
117 Gaussian *cdf* with the distance between the 5th and 95th percentiles equal
118 to the respective measured values of δ_f (or δ_I). A random number genera-
119 tor [24] was used to simulate the locations of instantaneous flame isocontours
120 using the Gaussian *pdf* of the flame location and instantaneous profiles were
121 mapped onto the locations to obtain the first and second moments of the
122 ‘true’ reaction progress variable. The corresponding profiles assuming that
123 flame sheets were infinitesimally thin ($\delta_f \rightarrow 0$) were also obtained. First and

124 second moments of the ‘detected’ reaction progress variable were obtained
 125 using a method accurate to the order of δ_f . The detected isocontours were
 126 assumed to be uniformly distributed between the 0.5th and 99.5th percentiles
 127 of the Gaussian *cdf* for the ‘true’ instantaneous flame. The infinitesimally
 128 thin isocontours were mapped relative to the true signal in order to obtain
 129 ‘detected’ first and second moments of the reaction progress variable. The
 130 same technique was applied here to ascertain the impact on the first and
 131 second moments of progress variable statistics. The former method was used
 132 to show the relative effects on progress variable statistics if the flames were
 133 assumed to be infinitesimally thin, while the latter method included the ad-
 134 ditional effects of uncertainties in the detection of flame isocontours.

135 To measure the instantaneous flame interface thickness a purpose written
 136 algorithm was used with a Savitzky-Golay filter [25] to fit second order poly-
 137 nomials to the detected flame isocontours by using 10 and 15 neighbouring
 138 points (n_{fit}) in each direction, with sample images shown in Fig. 1. The same
 139 fitting algorithm was also used with n_{fit} set to 5 to ascertain the impact on
 140 results. The resulting mean absolute deviations (comparing $n_{fit} = 5$ and 15)
 141 in locations of fitted isocontours ($|\overline{\Delta d}| \sim 0.003$ mm) and direction of normal
 142 vectors to the isocontours ($|\overline{\Delta \theta}| \sim 2.5$ degrees) showed that the location and
 143 orientation of the fitted isocontours were relatively insensitive to the fitting
 144 parameters. Subsequently, bilinear interpolation was used to map profiles of
 145 PIV image intensities normal to the flame for all points on the isocontours
 146 for each set of 1000 image pairs. The profiles for each image were normalised
 147 using the mean intensity in the reference windows used for density segrega-
 148 tion as outlined by Goh et al. [12]. The mean profiles of normalised PIV

149 image intensities were obtained using detected flame isocontours for each set
150 of measurements and the mean flame interface thickness was obtained for
151 each set of measurements by fitting error functions to the profiles. The mag-
152 nitude of δ_f was defined as the distance between the 5th and 95th percentiles
153 of the error functions. The flame brush thickness (δ_t) was also obtained in
154 the manner of Goh et al. [12]. Values of curvature h (positive when concave
155 to product stream) were obtained using the above method.

156 4. Results and Discussion

157 The obtained mean interface (δ_f) and flame brush (δ_t) thicknesses are
158 presented in Table 1. The latter were in the range $7.5 \leq \delta_t$ (mm) ≤ 8.5 and
159 hot wire measurements in the corresponding isothermal flow produced inte-
160 gral length scales (L_I) of around 4.0 mm [22]. Accordingly, the flame brush is
161 approximately twice the integral length scale in the reactant flow. Values of
162 the flame (reaction layer) thickness δ_f showed a modest decrease as the equiv-
163 alence ratio was increased from 0.75 to 0.85, similar to the measurements by
164 Goh et al. [12], where the thickness decreased from about 0.78 to 0.58 mm
165 as the equivalence ratio increased from 0.60 to 0.80. The flame thicknesses
166 were similar for both JP-10 flames, probably influenced by a slight asymme-
167 try at the equivalence ratio of 0.75. The error estimation technique outlined
168 above was applied using the determined values of δ_f and δ_t with the detected
169 flame isocontours randomly displaced from the true isocontours. The result-
170 ing normalised errors in the turbulent flame thickness (δ_t), which is directly
171 related to the reaction progress variable (c), were found to be around 0.44
172 - 0.86% ($\Delta\delta_t/\delta_t$). The highest δ_f/δ_t in the current context was around 12%

173 for the JP-10 flame with $\phi = 0.75$. Even when the detection of flame iso-
 174 contours had uncertainties of the order of δ_f , the expected deviations in \bar{c}
 175 were negligible and profiles of $\overline{c'c'}$ showed that true peak values were around
 176 0.22 compared to measured values of 0.25 with minimal deviations in the
 177 profiles as shown in Fig. 2. Hence, the impact of a finite flame (reaction
 178 layer) thickness on statistics is not significant in the current work.

179 It is not possible to present all the obtained statistical information and the
 180 focus is placed on data obtained along the burner centreline, where $\overline{V}, \overline{V}_r, \overline{V}_p,$
 181 and $\overline{v'c'}$ are zero. Measurements presented include unconditional and condi-
 182 tional axial terms $\overline{U}, \overline{U}_r, \overline{U}_p, \overline{u'u'}, \overline{u'_r u'_r}, \overline{u'_p u'_p}$ and $\overline{u'c'}$, the corresponding
 183 radial terms $\overline{v'v'}, \overline{v'_r v'_r}$ and $\overline{v'_p v'_p}$, as well as the first two moments of the
 184 reaction progress variable \bar{c} and $\overline{c'c'}$. (The data enables terms up to and
 185 including triple correlations to be evaluated in closed form [22]). The con-
 186 version between conventionally (e.g. \bar{c}) and Favre (e.g. \tilde{c}) averaged statistics,
 187 more commonly used in model formulations, also follows. The expansion
 188 ratio ($\tau = \frac{\rho_r}{\rho_p} - 1$), readily estimated (e.g. via laminar flame computation), is
 189 the only unclosed term. Equivalent equations have been derived by Bray et
 190 al. [3] for some of the correlations. The Favre averaged axial scalar flux can
 191 be evaluated by re-arranging Eq. (2).

$$\tilde{c} = \frac{\bar{c}}{1 + \tau - \tau\bar{c}} \quad (1)$$

$$\overline{u'c'} = \widetilde{u''c''} \frac{1 + \tau}{(1 + \tau\tilde{c})^2} \quad (2)$$

192 These equations only hold for infinitesimally thin flames. The corresponding
 193 triple correlation can be obtained from Eq. (4),

$$\tilde{U} = (1 - \tilde{c}) \bar{U}_r + \tilde{c} \bar{U}_p \quad (3)$$

$$\begin{aligned} \widetilde{u''u''c''} &= \tilde{c}(1 - \tilde{c}) [\bar{U}_p^2 - \bar{U}_r^2 + 2\tilde{U}(\bar{U}_r - \bar{U}_p)] \\ &\quad + (\overline{u'_p u'_p} - \overline{u'_r u'_r}) \end{aligned} \quad (4)$$

194 and, finally, the axial Reynolds stress follows from a re-arrangement of Eq. (5).
 195 The corresponding equations for radial components follow by similarity and
 196 the general expressions are listed in the Supplemental material.

$$\overline{u'u'} = \widetilde{u''u''} + \widetilde{u''u''c''} \frac{\tau}{(1 + \tau\tilde{c})} - \left(\frac{\tau \widetilde{u''c''}}{1 + \tau\tilde{c}} \right)^2 \quad (5)$$

197 Boundary conditions in terms of mean velocity components and Reynolds
 198 stresses at a distance of 2 mm from each nozzle exit are included in the Sup-
 199 plemental material in order to aid computational studies. Centreline profiles
 200 of mean axial velocities are shown in Fig. 3, where deviations from straight
 201 line profiles (isothermal) increased with equivalence ratios, similar to previ-
 202 ous findings by Kostiuk et al. [6]. The corresponding unconditional Reynolds
 203 stresses are shown in Fig. 4, where peak radial components at the nominal
 204 stagnation plane increased with equivalence ratio (cf. Goh et al. [13]). Re-
 205 action progress variable statistics, see Fig. 5, show that flames move further
 206 from the nominal stagnation plane as the equivalence ratio is increased (cf.
 207 Goh et al. [12]). Conditional velocities are shown in Fig. 6, where the reactant
 208 velocities decreased slightly and product velocities increased as the equiva-
 209 lence ratio was increased. Conditional axial reactant and product Reynolds

210 stresses are shown in Fig. 7. The corresponding profiles for the radial com-
211 ponents, see Fig. 8, show that the reactant Reynolds stresses were almost
212 constant, while product stresses increased towards the nominal stagnation
213 plane, with slightly higher values as the equivalence ratio increased. For JP-
214 10 flames at an equivalence ratio of 0.75, radial reactant Reynolds stresses
215 showed a peak before the stagnation plane, possibly due to slightly different
216 equivalence ratios between the upper and lower flames. Results for scalar
217 fluxes, see Fig. 9, show large uncertainties for this case. The proximity to
218 global extinction ($\phi_{ext} \sim 0.7$ for both fuels) coupled with the transition in
219 flame propagation mode are likely contributors. However, it can be observed
220 that as the equivalence ratio is increased, there is a transition from gradient
221 to counter gradient transport and that the same trend is obtained for both
222 fuels. It is imperative that computational models reflect such phenomena
223 accurately as the propagation mode impacts flame dynamics and the stabili-
224 sation point. Furthermore, results show that flame extinction in the current
225 twin flame configuration and the transition to flameless oxidation with com-
226 bustion stabilised against a hot product stream [12] are both accompanied
227 by a transition to gradient transport. The mode of transport is affected by
228 a number of factors, including the expansion ratio. Lindstedt and Város [26]
229 derived a relationship based on the balance between mean strain (production
230 term tensor) and mean pressure gradient effects. However, in the turbulent
231 opposed jet configuration the geometry imposed pressure gradient exerts a
232 significant influence on the transition. Efforts have been made to account for
233 such effects [27], though a comprehensive evaluation of the resulting model
234 formulations present difficulties in the current context, while Chen and Bil-

235 ger [28] analysed the transition using Bunsen flames.

236 Curvature statistics for the reaction interfaces was obtained using the
237 Savitzky-Golay filter [25] based technique outlined above and with three val-
238 ues of n_{fit} ($= 5, 10, 15$) to obtain fitted flame isocontours. By using a range
239 of values, it was possible to ascertain the relative sensitivity of derived cur-
240 vatures to the fitting parameter as given in Table 2. It can be noted that dis-
241 crepancies are notably decreased as n_{fit} is raised from 5 to 10. The obtained
242 *pdf* of curvature is shown in Fig. 10 and, again, it can be observed that for
243 the two higher values there is good agreement apart from at zero curvature.
244 The latter discrepancy is very strong when n_{fit} is set to 5 and a plausible ex-
245 planation is that too little local information was available to obtain accurate
246 values for large local radii corresponding to the peak at zero curvature. Also,
247 as the fundamental definition of curvature ($h(s) = (x'y'' - x''y')/(x'^2 + y'^2)^{3/2}$)
248 involves first and second order gradients, the uncertainties are expected to be
249 large. Furthermore, the ‘optimum’ fitting parameter is arguably dependent
250 on the local spectral content as isocontours are a complex superposition of
251 multiple scales. Accordingly, an accurate determination of curvature statis-
252 tics may require prior knowledge of the geometrical nature of the isocontours.
253 Nevertheless, the effects of equivalence ratio on curvature statistics is modest
254 even close to the global extinction limit. The latter is consistent with related
255 experimental studies for stable flames. Bradley et al. [29] analysed a wide
256 range of flames and showed the applicability of a symmetric Gaussian form
257 of the *pdf* of curvature with the peak value at zero curvature linearly related
258 to the Damköhler number as $Da^{1/2}$. Yuen and Gülder [30] also showed a
259 symmetric Gaussian form of the *pdf* for methane and propane flames, while

260 Gashi et al. [31] addressed comparisons between 2D slices obtained exper-
261 imentally and DNS studies. Sadanandan et al. [32] showed that a broadly
262 Gaussian *pdf*, subject to local conditions, was obtained for a range of stable
263 syngas flames operating on a swirl burner at pressures up to 20 bar. Here,
264 the suggestion by Bradley et al. [29], see Supplemental material, results in
265 a peak value of 0.73 and a somewhat narrower distribution (see Fig. 10).
266 The current study thus suggests that a (near) Gaussian distribution extends
267 to flames undergoing a flame propagation mode transition close to global
268 extinction.

269 5. Conclusion

270 The turbulent transport in premixed flames of JP-10 and cyclopentane
271 approaching extinction has been characterised in terms of statistical prop-
272 erties using a twin flame opposed jet burner configuration featuring fractal
273 grid generated turbulence. A comprehensive set of statistical information has
274 been provided along the axis of the burner to support comprehensive com-
275 parisons with computational studies. The obtained data includes conditional
276 velocity statistics, flame curvature information and scalar fluxes and permits
277 the closed form conversion between conventionally and Favre averaged statis-
278 tics on the assumption that finite reaction interface thickness effects can be
279 neglected. It has been shown that the impact of the latter on measured
280 statistics is not significant in the current work. Results also clearly illus-
281 trate the rapid transition from non-gradient to gradient turbulent transport
282 as the extinction limit is approached. The transition in flame propagation
283 mode is important as it affects flame dynamics and the flame stabilisation

284 point. The results also confirm that a (near) Gaussian *pdf* of flame curvature
285 prevails close to global extinction and that the change in flame propagation
286 mode is related to the disappearance of the conventional premixed turbulent
287 flame with a transition to a flameless oxidation mode required to support
288 combustion in leaner mixtures.

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Table 1: Measured turbulent flame brush (δ_t) and mean reaction layer (flame) (δ_f) thicknesses. The uncertainty in the turbulent flame brush thickness ($\Delta\delta_t/\delta_t$) was obtained using the stochastic method of Goh [22]. All uncertainties in presented values illustrate the differences between upper and lower nozzles.

Fuel	ϕ	δ_t [mm]	δ_f [mm]	$\Delta\delta_t/\delta_t$ [%]
C ₅ H ₁₀	0.75	8.13±0.47	0.803±0.026	0.44±0.21
C ₅ H ₁₀	0.85	7.65±0.19	0.751±0.026	0.45±0.05
JP-10	0.75	7.39±0.06	0.829±0.052	0.61±0.20
JP-10	0.85	7.51±0.13	0.829±0.000	0.86±0.05

Table 2: Mean absolute uncertainties in flame front location ($|\overline{\Delta d}|$), orientation in degrees ($|\overline{\Delta\theta}|$) and curvature ($|\overline{\Delta h}|$). Comparison between fitted curves obtained using a Savitzky-Golay filter with $n_{fit} = 5, 10$ and 15 .

Fuel	ϕ	n_{fit} range	$ \overline{\Delta d} $ [mm]	$ \overline{\Delta\theta} $ [°]	$ \overline{\Delta h} $ [mm ⁻¹]
C ₅ H ₁₀	0.75	5 / 15	0.00292	2.42	0.656
C ₅ H ₁₀	0.85	5 / 15	0.00305	2.48	0.673
JP-10	0.75	5 / 15	0.00298	2.55	0.658
JP-10	0.85	5 / 15	0.00312	2.56	0.687
C ₅ H ₁₀	0.75	10 / 15	0.00171	1.18	0.154
C ₅ H ₁₀	0.85	10 / 15	0.00179	1.21	0.161
JP-10	0.75	10 / 15	0.00177	1.28	0.157
JP-10	0.85	10 / 15	0.00184	1.25	0.165

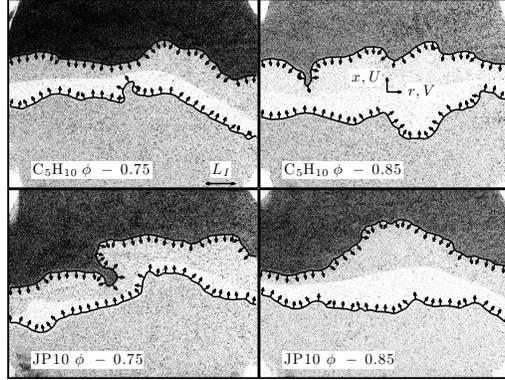


Figure 1: Sample PIV images for all cases, overlaid with detected flame fronts (lines). Mapped local flame normals (arrows) in direction of burnt products are also shown for sample points 50 pixels apart for clarity. The integral length scale (L_I) is also shown.

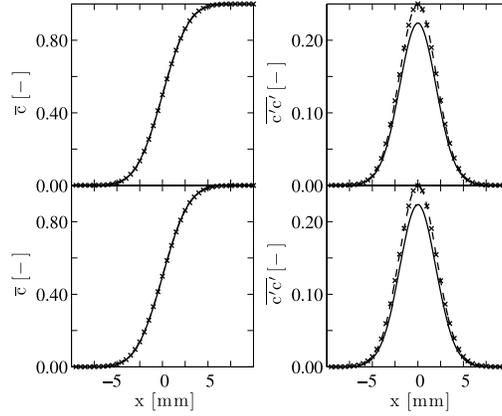


Figure 2: First (left) and second (right) moments of reaction progress variable statistics obtained taking into account finite thickness effects, using the method of Goh [22] for measured values of δ_f and δ_t for JP-10 at equivalence ratio of 0.75. Top row - Actual values (solid) versus values obtained assuming zero interface (flame) thickness ($\delta_f \rightarrow 0$) (\times with dashed lines). Bottom row - Actual values (solid) versus values obtained with randomly displaced infinitesimally thin detected isocontours (\times with dashed lines).

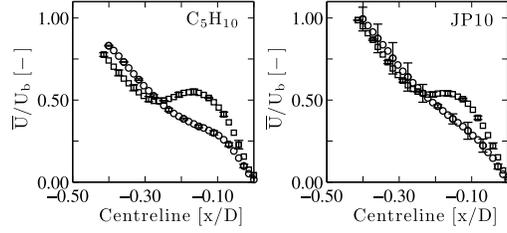


Figure 3: Mean axial velocity along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (\circ) and 0.85 (\square).

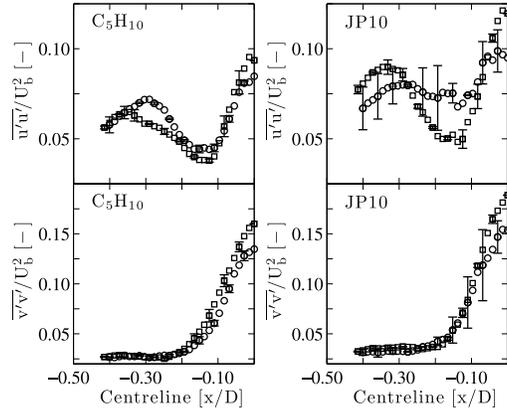


Figure 4: Mean axial (top) and radial (bottom) Reynolds stresses along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (\circ) and 0.85 (\square).

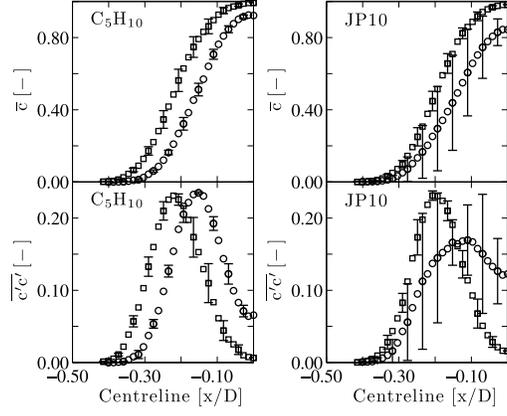


Figure 5: Mean first (top) and second (bottom) moments of reaction progress variable along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (\circ) and 0.85 (\square).

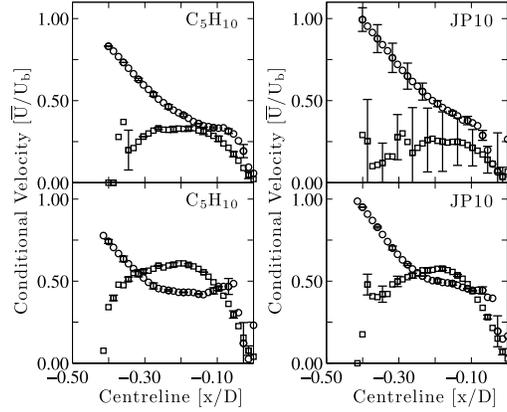


Figure 6: Mean axial reactant ($\circ = \overline{U}_r$) and product ($\square = \overline{U}_p$) velocities along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (top) and 0.85 (bottom).

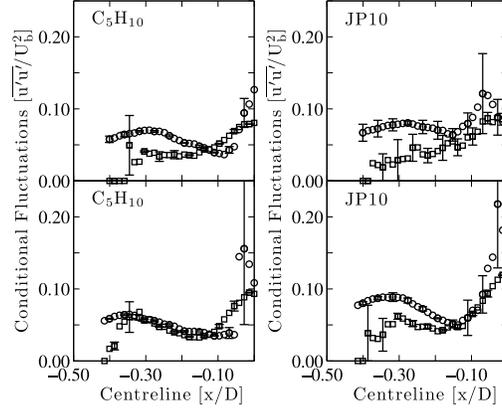


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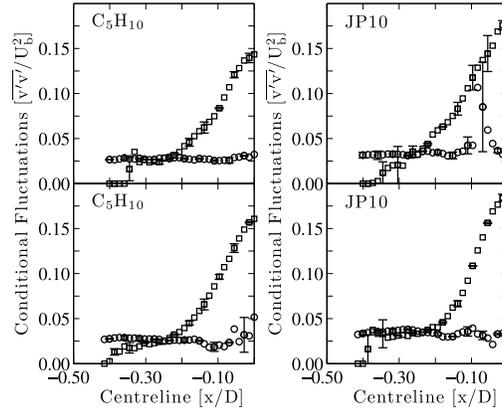


Figure 8: Mean radial reactant ($\circ = \overline{v'_r v'_r}$) and product ($\square = \overline{v'_p v'_p}$) Reynolds stresses along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (top) and 0.85 (bottom).

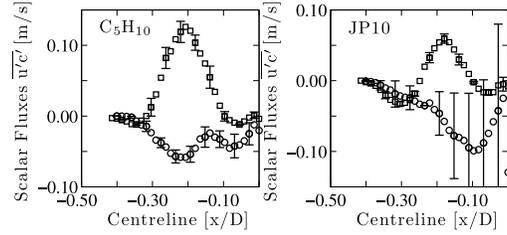


Figure 9: Mean axial scalar fluxes ($\overline{u'c'}$) along axis of burner. Cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (\circ) and 0.85 (\square).

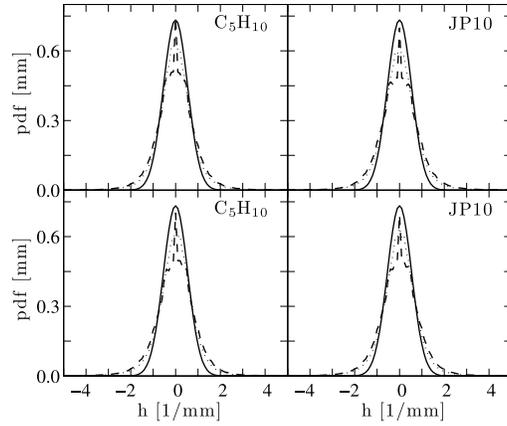


Figure 10: Curvature *pdf* at resolution of 0.1 [1/mm] for cyclopentane (left) and JP-10 (right) flames at equivalence ratios of 0.75 (top) and 0.85 (bottom). Savitzky-Golay filter with $n_{fit} = 10$ (dashed) and 15 (dotted). Empirical Gaussian fit by Bradley et al. [29] is also included for comparison (solid).

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