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Upscaling of Relative Permeability to Minimise Numerical Dispersion

By

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A report submitted in partial fulfillment of the requirements for the MSc and/or the DIC.

September 2011

DECLARATION OF OWN WORK

I declare that this thesis *upscaling of relative permeability to minimize numerical dispersion* is entirely my own work and that where any material could be construed as the work of others, it is fully cited and referenced, and/ or with appropriate acknowledgement given.

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Abstract

Upscaling in numerical reservoir simulation is required when the computer time requirements to run a fine grid simulation of length scale 10-100m becomes too large. In waterflooding and other multiphase flow situations, it may then be necessary to upscale relative permeabilities. Relative permeability curves obtained from laboratory core analysis (core scale, in cm)) are converted to pseudo-relative permeability to reduce numerical dispersion and describe the effects of reservoir heterogeneity on flow in simulation models.

Numerical dispersion in reservoir modelling can be caused by the effects of discretizing continuous flow properties in discrete gridblocks by commercial simulators using finite difference methods. This phenomenon is seen in the difference between the production rate, recovery and field pressures simulation results of the fine grid model and resulting coarse grid model. Normally pseudos are generated from fine grid simulations. This is in itself a time-consuming process. It would be much quicker if it were possible to derive these pseudos analytically. In addition dynamic pseudo-relative permeability methods tend to predict different pseudos for every grid block in a coarse grid simulation which may result in a very large and unwieldy input data set.

Here we examined an analytic method for deriving pseudofunctions to compensate for numerical dispersion. Three pairs of pseudo-relative permeabilities are required to compensate for numerical dispersion in 1D, 2D homogeneous and heterogeneous systems. One pair for the injector wellblock, one pair for the intermediate wellblock between the wells and one pair for the producer wellblock. The pseudofunctions are well-behaved and maintain the endpoint values of the parent rock curves. The performance of the analytical pseudo-functions does not depend on the gridblock size or number of gridblocks present.

In heterogeneous systems, we propose first homogenisation of the model to develop of effective relative permeability and effective absolute permeability. The effective relative permeability can then be converted analytically to pseudo-relative permeability that compensate for numerical dispersion.

The performance of the new upscaling method shows that in production scenarios, pressure changes, water breakthrough and two phase production profile after breakthrough can be predicted by running only the coarse grid simulation for the 1Dimensional model. Moreover, the watercut development profile can adequately be predicted using the performance of the pseudo-functions in the two phase flow regime.

Although, the results we have obtained are accurate for 1D and approximate for 2D systems further investigation is required to extend the approach to 2D and 3D homogeneous and heterogeneous systems and real field applications with many producers and injectors.

Acknowledgements

I utilize this opportunity to express my utmost high gratitude to my college supervisor, Dr. Ann Muggeridge, for her support guidance and direction throughout the duration of the project.

Also, I wish to profoundly thank my family for their support and love during the course of my Msc Program, and finally thank my fellow Msc, Petroleum Engineering students whose encouragement had helped to see me through this course.

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Upscaling of Relative Permeability to Minimise Numerical Dispersion

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Abstract

Upscaling in numerical reservoir simulation is required when the computer time requirements to run a fine grid simulation of length scale 10-100m becomes too large. In waterflooding and other multiphase flow situations, it may then be necessary to upscale relative permeabilities. Relative permeability curves obtained from laboratory core analysis (core scale, in cm)) are converted to pseudo-relative permeability to reduce numerical dispersion and describe the effects of reservoir heterogeneity on flow in simulation models.

Numerical dispersion in reservoir modelling can be caused by the effects of discretizing continuous flow properties in discrete gridblocks by commercial simulators using finite difference methods. This phenomenon is seen in the difference between the production rate, recovery and field pressures simulation results of the fine grid model and resulting coarse grid model. Normally pseudos are generated from fine grid simulations. This is in itself a time-consuming process. It would be much quicker if it were possible to derive these pseudos analytically. In addition, dynamic pseudo-relative permeability methods tend to predict different pseudos for every grid block in a coarse grid simulation which may result in a very large and unwieldy input data set.

Here we examined an analytic method for deriving pseudofunctions to compensate for numerical dispersion. Three pairs of pseudo-relative permeabilities are required to compensate for numerical dispersion in 1D, 2D homogeneous and heterogeneous systems. One pair for the injector wellblock, one pair for the intermediate wellblock between the wells and one pair for the producer wellblock. The pseudofunctions are well-behaved and maintain the endpoint values of the parent rock curves. The performance of the analytical pseudo-functions does not depend on the gridblock size or number of gridblocks present.

In heterogeneous systems, we propose first homogenisation of the model to develop of effective relative permeability and effective absolute permeability. The effective relative permeability can then be converted analytically to pseudo-relative permeability that compensate for numerical dispersion.

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Although, the results we have obtained are accurate for 1D and approximate for 2D systems further investigation is required to extend the approach to 2D and 3D homogeneous and heterogeneous systems and real field applications with many producers and injectors.

Introduction

Numerical reservoir simulation is an important tool used in the petroleum industry for reservoir fluid flow description and performance prediction. In recent studies, Batycky et al (1997), Vega et al (2004) and Safian and Ramirez (2008) the fine grid geological models used are of the order 10^5 - 10^6 gridblocks. This poses a challenge to meet computational requirements for extremely fine grid geological models. These fine grid models are often coarsened for flow simulation, in which single phase upscaling is required to give suitable average values of absolute permeability and also, input of rock relative permeability to generate flow functions for the coarse gridblocks.

In two phase systems, reservoir fluid flow behaviour cannot be fully characterized by absolute permeability especially when the heterogeneity 'correlation length' is close in size to the gridblock to be scaled up e.g. a high permeability channel in a lower permeability system and as an extensive narrow shale barrier in a high permeability system following the analysis of Muggeridge (1991), Christie (1996) and Barker and Thibeau (1997). The use of rock relative permeability curves in simulation models may produce numerical dispersion in results such as the smearing seen in the saturation – dimensionless distance

profile. Numerical dispersion phenomena can be attributed to the discretization of continuous flow variables in gridblocks combined with the use of coarse grid models. The size of the gridblocks and time steps taken can affect the quantity and level of numerical dispersion in coarse grid models, with larger gridblock sizes having higher levels of dispersion (Lantz, 1971). Pseudo-relative permeability functions can be formulated from laboratory relative permeability curves to scale up multiphase fluid flow property in coarse grid models and reduce numerical dispersion in simulation results. These pseudo-functions can be formulated analytically (Hewitt et al, 1998), and numerically (Barker and Dupouy, 1996).

Numerically formulated or dynamic pseudo-functions are obtained from the results of the simulation of a fine grid model. These dynamic pseudofunctions are generated to reduce numerical dispersion in coarse grid reservoir models. Barker and Thibeau (1997) summarized six dynamic pseudoisation methods. The Kyte and Berry (1975), pore volume weighted and total mobility methods reproduce fine grid results to an extent, however they produce non-single value, negative, and infinite pseudo-relative permeabilities and make severe assumptions about boundaries. These make them difficult to use. Stone's, weighted relative permeability (Eclipse Simulator Pseudo) and quasi-steady state dynamic methods give poor results due to assumptions on total mobility, restrictive conditions such as neglect of coarse grid gravity term, and neglect of time derivative of saturation respectively which make the methods ineffective when these vary or become significant. The main limitations of most dynamic relative permeability upscaling methods are that a different set of pseudofunctions are needed in every grid cell and flow axis, that the pseudo-relative permeabilities are a function of well position and flowrates and the problem of running the fine grid simulation initially which we are trying to avoid (Barker and Thibeau, 1997), (Christie, 1996). These create computational challenges and can present huge and unwieldy input datasets in 3D field simulations.

As a result, there is a significant work investigating the grouping of pseudo-relative permeabilities to reduce the number required. Hewitt et al (1998) analytically investigated this using an approach based on the method of characteristics to define flow variables for grid representations in a waterflood. Their results showed that the changes required to account for discretization effects on a coarse grid depend only on the ratio of the distances from the injection block boundary to the inlet and outlet faces of a particular gridblock i.e. they explained why different pseudo-relative permeabilities are needed in each grid block. They also showed that the required changes on relative permeability are independent of gridblock size and the total number of gridblocks used. However, the method produced increases in oil pseudo relative permeabilities above its endpoint. Christie (1996) used a semi-analytic renormalization technique to deduce effective relative permeability and also suggested in his work that pseudofunctions can be ordered based on flow variables such as minimum of total mobility curve and slope of fractional flow at the shock front height. Barker and Thibeau (1997) suggested that the grouping of pseudo-relative permeability can be based on the different rock types in the coarse grid model. They added that instead of running a full fine grid simulation; a sector model or dual scale simulation models can be used. In the upscaling of heterogeneous fine grid models, Muggeridge (1991) investigated these using multistage simulation methods to show that using pseudo-relative permeability data in homogeneous coarse grid model can illustrate mean properties of flow of the fine grid heterogeneous model.

This study will show, in contrast to the results of Hewitt et al (1998), that only three sets of pseudos are needed to upscale two phase flow in a homogeneous line drive; one pair for the injection well-block, one set for the production well block and another set for other intermediate gridblocks. We will use pseudo relative permeability analytically derived from Buckley Leverett theory to control numerical dispersion for a range of waterfloods. The generated pseudos are tested in a range of homogeneous and heterogeneous, 1D and 2D models. For heterogeneous reservoirs, the pseudoisation method involves two main steps, homogenisation and compensation of numerical dispersion following a method proposed by Muggeridge (1991). The resulting pseudos were input into 1D homogeneous coarse grid models and simulation results of the fine grid and coarse grid models, with and without two phase upscaling were compared. The method was also applied to the control of numerical dispersion in a homogeneous 2D quarter five-spot model. In this case the upscaling was less successful because upscaling needs to include radial flow effects.

Definitions and Concepts of Study

Let us consider an ideal condition of one dimensional continuous water injection into a coarse grid reservoir model in which the water displaces the oil in the pore volume of the model gridblocks. The waterflooding is carried out at high flowrates and the inter-block flow occurs in the horizontal direction (x-direction) in a simplified reservoir model with constant connate water saturation S_{wc} , so we can neglect the effects of capillary pressure and gravity. The continuous flow of oil and water in the reservoir during displacement are described by Darcy's two phase flow equation for water and oil

$$q_w = - \frac{KK_{rw}(S_w)A}{\mu_w} \frac{\partial P}{\partial x} \quad (1)$$

$$q_o = - \frac{KK_{ro}(S_w)A}{\mu_o} \frac{\partial P}{\partial x} \quad (2)$$

where total flow is given by

$$q_T = q_o + q_w \quad (3)$$

where q_t is the total flowrate in the reservoir.

Assuming immiscible incompressible displacement of oil by water, the fractional flow of water developed by Leverett (1941) can be given as a fraction of the total flow.

$$f_w = \frac{q_w}{q_w + q_o} \quad (4)$$

where q_o and q_w are oil and water phase interblock flowrates respectively. We also express fractional flow as a function of relative permeability and viscosity ratio of oil and water. (Leverett, 1941)

$$f_w = \frac{1}{1 + \frac{K_{ro}(S_w)\mu_o}{K_{rw}(S_w)\mu_w}} \quad (5)$$

The mobility of oil and water in the displacement is represented by the ratio of the relative permeability to fluid viscosities of oil and water and are given by

$$\lambda_w = \frac{K_{rw}(S_w)}{\mu_w} \quad (6)$$

$$\lambda_o = \frac{K_{ro}(S_w)}{\mu_o} \quad (7)$$

Therefore the mobility of oil and water at a point can be said to be a function of the water saturation at that point in any gridblock. For the displacement of oil by water in one dimension, the total mobility is

$$\lambda_T = \lambda_w + \lambda_o \quad (8)$$

The displacement of oil by water can be described analytically by Buckley & Leverett (1942) Frontal Advance Theory for one dimensional displacement. The Frontal Advance Equation showing the relationship between change in distance, saturation and fractional flow (Buckley & Leverett, 1942)

$$\frac{\partial x}{\partial t} = \frac{q_t}{A\phi} \frac{\partial f_w}{\partial S_w} \quad (9)$$

This gives rise to a characteristic, dimensionless velocity which is equivalent to the slope of the fractional flow curve at a particular saturation (Welge 1952).

$$v = \frac{df_w}{dS_w} = \frac{\Delta f_w}{\Delta S_w} \quad (10)$$

This shows that each saturation moves through the reservoir with a velocity equivalent to the slope of the fractional flow curve at that saturation. Given a table of relative permeability and water saturation using equation 5, the shock front saturation can be obtained using Welge construction method (Welge, 1952). Inspection of equations 4 and 5, we observe that the fractional flow curve is affected by fluid viscosity ratio for a constant rate horizontal displacement.

Formulation of Pseudo-Relative Permeability Curves

Here we will summarize the analysis of pseudo-relative permeabilities to compensate for numerical diffusion that was originally derived by Muggeridge (private communication). The rock relative permeability is calculated and tabulated. (refer to Appendix B1 for correlations).

Figure 1 shows the non-uniform saturation of the last gridblock and the smearing it caused at its outlet face due to the discretization of continuous flow variable. Numerical diffusion occurs because finite difference reservoir simulators calculate an average saturation and assumes this saturation is uniform within the gridblock and evaluates the flow downstream the gridblock in the next timestep based on this average saturation characterized by a saturation front and its relative permeability. But in reality, the saturation within the gridblock may not be uniform as shown in Figure 1 and may be less than the average saturation. A flowrate which is evaluated based on the average saturation will not be representative and may cause numerical diffusion or smearing seen in a saturation distance profile. The fewer the number of gridblocks between well locations then the higher the numerical diffusion levels (Lantz, 1971).

The Buckley Leverett shock front describes the sudden increase in saturation from immobile connate water saturation to mobile water saturation, therefore the velocity of the shock front should determine the water breakthrough time in a homogeneous reservoir model. The increase in watercut in the produced fluid will depend on the shock front saturation level and the rise behind it to the $1 - S_{or}$ water saturation level (rarefaction) (Buckley & Leverett, 1942).

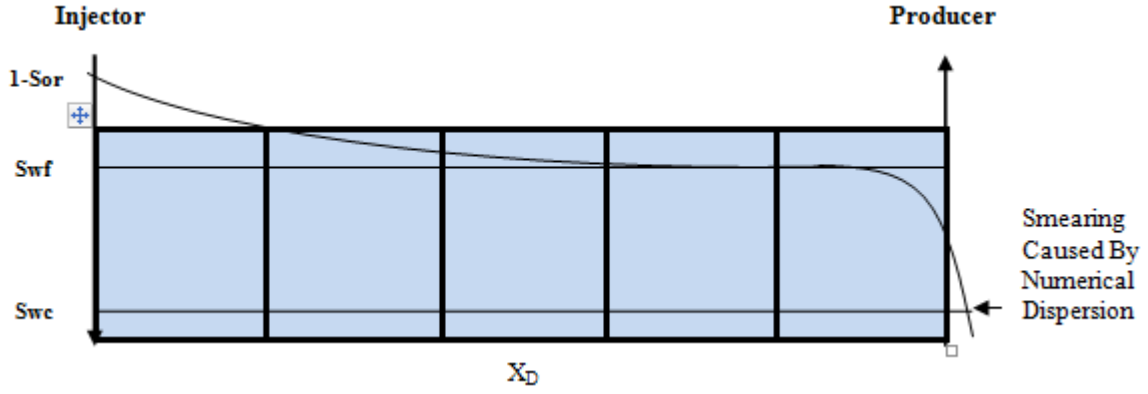


Figure 1 Saturation distance profile showing inter-gridblock saturation distribution and smearing of the last gridblock caused by numerical dispersion.

The accurate prediction of the breakthrough time and watercut profile in field reservoir studies and their effect on production rate, recovery and reservoir pressure depends on the accurate depiction of this saturation distance profile. Moreover, reservoir engineers can predict reservoir decline curve much better, improve field life and economics and surface facilities management. Consequently, this accurate prediction depends on our ability to reduce numerical dispersion observed to as low as possible in our flow simulation models.

We will formulate two pairs of pseudo-relative permeabilities using Buckley Leverett analytical solution (Buckley & Leverett, 1942) and the concept of change in fractional flow with change in saturation (Leverett 1941, Buckley & Leverett 1942). A pair of laboratory rock curves will be input into the inlet gridblock to the injection wellblock and also into the production wellblock. One pair of formulated pseudo-relative permeabilities will be input into the injector wellblock and the second pair of pseudo-relative permeabilities input into intermediate non-well blocks between the injector wellblock and producer wellblock. These pseudos will be tested in homogeneous one dimensional and two dimensional models undergoing linear waterflooding. The pseudo-relative permeabilities will also be tested in three two dimensional heterogeneous models to understand the effect of sub-grid scale heterogeneity on flow and recovery (Muggeridge, 1991) and reduce numerical dispersion.

Injector Wellblock

When the shock front reaches the outlet face of the injector wellblock i , the average saturation in the gridblock is calculated analytically by

$$\bar{S}_w = \frac{1}{\Delta x} \int_{x_{i-\frac{1}{2}}}^{x_{i+\frac{1}{2}}} S_w(x) dx \quad (11)$$

$S_w(x)$ can be obtained from Buckley & Leverett saturation versus distance plot at any distance and Δx is the size of any gridblock. Relative permeability values for saturations less than this average saturation in the rock curve table is equated to zero to depict the Buckley Leverett continuous solution. (Buckley & Leverett, 1942). We call this new value water pseudo-relative permeability which is recorded in the pseudo-rock table as K_{rwp} . This instructs the simulator to equate to zero flowrates and relative permeabilities for water saturations lower than the gridblock average and numerical dispersion can be reduced

$$K_{rwp} = 0 \quad S_{wj} < \bar{S}_{wf} \quad (12)$$

For a rock curve and water saturation table, the discretized solutions to our derived analytic equations (refer to Appendix B for the analytic derivations and equations) to upscale our coarse grid models will be done using 1D finite difference approximation in line with most commercial simulators. Most commercial simulators make use of single point upstream weighting finite difference approximation. Now, consider the shock front saturation moving at a velocity obtained from equation 13, the dimensionless time it requires to reach the outlet face of the gridblock is

$$\tau = \frac{S_{wf} - S_{wc}}{f_{wj}} \quad (13)$$

where f_{wj} and S_{wf} are the fractional flow and water saturation of the shock front in the rock curve table. In addition, individual water saturations higher than the shock front in the rock curve table will move a distance given by when the shock front reaches the gridblock outlet face

$$x_j = \frac{f_{wj} - f_{w(j+1)}}{S_{wj} - S_{w(j+1)}} \times \frac{S_{wf} - S_{wc}}{f_{wj}} \quad (14)$$

We to obtain pseudo-total mobility $\Psi_T(S_{wj})$ required by the shock front water saturation to reach the gridblock outlet face

$$\frac{1}{\Psi_T(S_{wj})} = \frac{S_{wf} - S_{wc}}{f_{wj}} \sum_{j=J}^{j=n} \left[\frac{f_{wj} - f_{w(j+1)}}{S_{wj} - S_{w(j+1)}} - \frac{f_{w(j+1)} - f_{w(j+2)}}{S_{w(j+1)} - S_{w(j+2)}} \right] \frac{1}{\lambda_{Tj}} \quad (15)$$

In the saturation distance profile in Figure 1, due to the discontinuity of the shock front, the average saturation over a distance is calculated with saturations higher than the shock front using the analytical Buckley & Leverett solution. (Buckley & Leverett, 1942). For water saturations in this range and higher than the shock front saturation we can compute their velocities and distance. This velocity is a function of the water pseudo-total mobility $\Psi_T(S_{wj})$ obtained by

$$\frac{1}{\Psi_T(S_{wj})} = \left(\frac{S_{wj} - S_{w(j+1)}}{f_{wj} - f_{w(j+1)}} \right) \sum_{j=J}^{j=n} \left[\frac{f_{wj} - f_{w(j+1)}}{S_{wj} - S_{w(j+1)}} - \frac{f_{w(j+1)} - f_{w(j+2)}}{S_{w(j+1)} - S_{w(j+2)}} \right] \frac{1}{\lambda_{Tj}} \quad (16)$$

where S_{wf} and S_{wj} are shock front saturation and rock table water saturation.

The pseudo-water mobility is obtained by

$$\frac{\lambda_w}{\lambda_T} = \frac{\Psi_w(S_{wj})}{\Psi_T(S_{wj})} \quad (17)$$

where λ_w and λ_T are the rock water and rock total mobilities and $\Psi_T(S_{wj})$ and $\Psi_w(S_{wj})$ are the total and water pseudo-mobility. We calculate water and oil pseudo-relative permeability from the water and total pseudo-mobility by

$$K_{rwp}(S_{wj}) = \Psi_w(S_{wj}) \times \mu_w \quad S_{wj} \geq \overline{S_{wf}} \quad (18)$$

$$K_{rop}(S_{wj}) = \left(\Psi_T(S_{wj}) - \Psi_w(S_{wj}) \right) \times \mu_o \quad S_{wj} \geq \overline{S_{wf}} \quad (19)$$

Water saturations lower than the shock front saturation remains the same on the pseudo-relative permeability table. The oil pseudo-relative permeability is obtained from

$$\frac{1}{\mu_o} = \left(\frac{S_{wj} - S_{wc}}{S_{wf} - S_{wc}} \right) \frac{1}{\Psi_{Tj}} + \left[1 - \left(\frac{S_{wj} - S_{wc}}{S_{wf} - S_{wc}} \right) \right] \frac{1}{\lambda_o(S_{wc})} \quad (20)$$

Now, we can calculate the oil pseudo-relative permeability K_{rop} by

$$K_{rop}(S_{wj}) = \Psi_o(S_{wj}) \times \mu_o \quad S_{wj} < \overline{S_{wf}} \quad (21)$$

Using Welge (1952) formulation for average saturation behind the shock front, we replace the rock table water saturations with average saturations for the saturation range $S_{wj} \geq S_{wf}$ using

$$\overline{S_{wj}} = S_{wj} + \frac{(1-f_{wj})(S_{wj} - S_{w(j+1)})}{(f_{wj} - f_{w(j+1)})} \quad (22)$$

where S_{wj} is the water saturation obtained from the rock relative permeability table.

Non-Injector Gridblock

Immediately after the injector wellblock, the non-injector wellblock flow properties were also modified. For water saturations lower than the shock front saturation, the relative permeability is equated to zero for the same reason as the injector wellblock.

$$K_{rwp} = 0 \quad S_{wj} < S_{wf} \quad (23)$$

We calculate the pseudo oil mobility for water saturations less than the shock front saturation with

$$\frac{1}{\Psi_{oj}} = \frac{1}{\lambda_T(S_{wf})} \left(\frac{S_{wj} - S_{wc}}{S_{wf} - S_{wc}} \right) + \left[1 - \left(\frac{S_{wj} - S_{wc}}{S_{wf} - S_{wc}} \right) \right] \frac{1}{\lambda_o(S_{wc})} \quad S_{wj} < S_{wf} \quad (24)$$

$\lambda_o(S_{wc})$ and $\lambda_T(S_{wf})$ are rock oil mobility at the connate water saturation and rock total mobility at the shock front saturation respectively. The oil pseudo-relative permeability K_{rop} is obtained by

$$K_{rop}(S_{wj}) = \Psi_o(S_{wj}) \times \mu_o \quad S_{wj} < \overline{S_{wf}} \quad (25)$$

For saturations greater than the shock front saturation we use the same saturation and relative permeabilities in the rock table as in the pseudo-relative permeability table. We assume that the saturation in the gridblock is alike at the inlet and outlet and there is no need changing them with average saturations (refer to Appendix B for the explanation).

Methodology

Simulation Study

For the 1D, 2D homogeneous areal models and the 2D heterogeneous cross-sectional models, the steps outlined below were followed to investigate whether the upscaling of relative permeability using our pseudo-relative permeability curve does reduce numerical dispersion in the simulation of waterfloods through homogeneous and heterogeneous reservoirs:

1. Perform 1D and 2D homogeneous and heterogeneous fine grid simulations
2. Development of coarse grid models from fine grid models
3. Upscaling of absolute permeabilities in the resulting coarse grid models using conventional analytical methods (Christie 1996) for homogeneous and heterogeneous systems..
4. Formulation of Pseudo-relative permeabilities using Spreadsheet.
5. Input of rock and pseudo relative permeability curves obtained from a spreadsheet into coarse grid models.
6. Carry out 1D and 2D homogeneous and heterogeneous coarse grid simulations for:
 - A. Models with upscaled relative permeability data
 - B. Models with non-upscaled relative permeability data

A commercial black oil reservoir simulation program [reference] was used in this study.

1D Homogeneous Model

The pseudo-relative permeability functions were tested on 1D Cartesian coarse grid models which were a result of the coarsening process of a fine grid model currently undergoing waterflooding. The 1 Dimensional fine grid model was a $202 \times 1 \times 1$ (x, y, z directions) Cartesian grid undergoing a linear water-drive. The model has one injector well at location (1 1 1) and producer well at gridblock (202 1 1). The initial reservoir pressure was 4000psia and the bubble point is very low compared to reservoir pressure to typify a simple black oil reservoir model. The fluid components of the reservoir are incompressible oil and water. There is no aquifer effect on the reservoir model. The fine grid is homogeneous in permeability in the x, y and z directions and have a net to gross of 1. The fluid viscosity ratio is 4 and the rock relative permeability input is the same as that used in the pseudoisation. The water is injected at a constant rate of 6500bbl/day at a pressure of 8000psia and oil is produced at the same rate, ensuring pore volume injected is equal to pore volume produced. The reservoir is produced such that the pressure remains above the bubble point pressure and gas is not evolved. The waterflooding is carried out for 6000days. The bottom-hole pressure for the producer is set at very low limit and the system is designed for rate control. The fine model was uniformly coarsened (except the injector inlet gridblock) by a factor of 40 and 20 reducing into 5×1 and 10×1 coarse grid models.

We avoided the need for modification of transmissibilities and scale-up of the wellblock during the coarsening process by maintaining the same dimensions for the inlet gridblock to the injector wellblock in the coarse grid models as in the fine grid model. (Ding & Renard 1994, Muggeridge et al 2002). We had two coarse grid models of 7gridblocks and 12gridblocks. In the heterogeneous models the absolute permeability is scaled-up or averaged using the pressure solver steady state technique (Christie, 1996).

Since the fine model is homogeneous, the coarse grid models are also homogeneous in absolute permeability for transmissibilities calculation as the fine grid models. Simulation results of recovery, flowrates and field pressures for fine grid, coarse grid and upscaled coarse grid were compared. The parameters of the model are shown in Table 1.

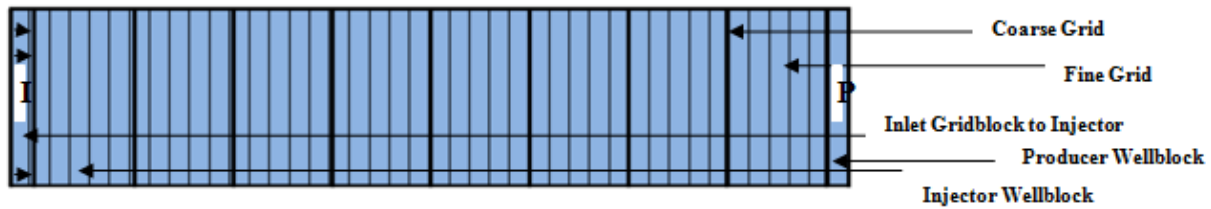


Figure 2. Fine grid and coarse grid showing the injector inlet gridblock.

Table 1 1D Fine Grid Model Parameters;

Porosity	0.2
Oil Formation Volume Factor	1.0rb/stb
Water Formation Volume Factor	1.0rb/stb
Water Viscosity (cP)	0.5
Oil Viscosity (cP)	2.0
Water Compressibility	3.03E-6/psia
Rock Compressibility	0.30E-05/psi
Uniform Permeability in Homogeneous Model	200md
Water Relative Permeability Endpoint	0.3
Oil Relative Permeability Endpoint	0.9
Residual Oil Saturation	0.1
Connate Water Saturation	0.2
Initial Reservoir Pressure	4000psi
Reservoir Dimension (ft)	3000×2000
Reservoir Thickness (ft)	100
Injector Well Location:	(1 1 1)
Producer Well Location	(202 1 1)

2D Homogeneous Model

The pseudofunctions were also tested on 2D synthetic rectangular areal models undergoing waterflooding. The model is a Cartesian $26 \times 26 \times 1$ (x, y, z) fine grid model equivalent to a quarter-five spot field pattern. The injector wellblock and producer wellblocks occupy extreme opposite corners of the model as shown in Figure 3. The injector wellblock location is $26 \times 1 \times 1$ while the producer wellblock location is $1 \times 26 \times 1$. It has the same reservoir fluid model and rock and fluid properties as the 1D model. Waterflooding was carried out at a constant rate of 7500bbl/day and oil rate maintained at the same constant rate before and at water breakthrough. The secondary recovery was carried out for a period of 4000days. The model is homogeneous in permeability and net to gross is 1. The fine grid was coarsened to three coarse grid models of $6 \times 6 \times 1$, $8 \times 5 \times 1$, and $5 \times 5 \times 1$. The main model parameters are shown in Table 2. The fine grid multiphase flow is represented by rock relative permeability curves used in the pseudoisation.

Two models of each coarse grid were generated and the multiphase flow property of one was upscaled. The 3pairs of rock relative permeability were input into the coarse grids and simulation results compared for compensation of numerical dispersion just as in the case of 1D model.

Table 2 2D Homogeneous Model Parameters

Porosity	0.2
Oil Formation Volume Factor	1.000rb/stb
Water Formation Volume Factor	1.000rb/stb
Water Viscosity (cP)	0.5
Oil Viscosity (cP)	2.0
Water Compressibility	3.03E-6/psi
Rock Compressibility	0.30E-05/psi
Uniform Permeability in Homogeneous Model	400md
Water Relative Permeability Endpoint	0.3
Oil Relative Permeability Endpoint	0.9
Residual Oil Saturation	0.1
Connate Water Saturation	0.2
Initial Reservoir Pressure	4000psi
Reservoir Dimension (ft)	3000 ×1000
Reservoir Thickness (ft)	100
Injector Well Location:	(26 1 1)
Producer Well Location	(1 26 1)

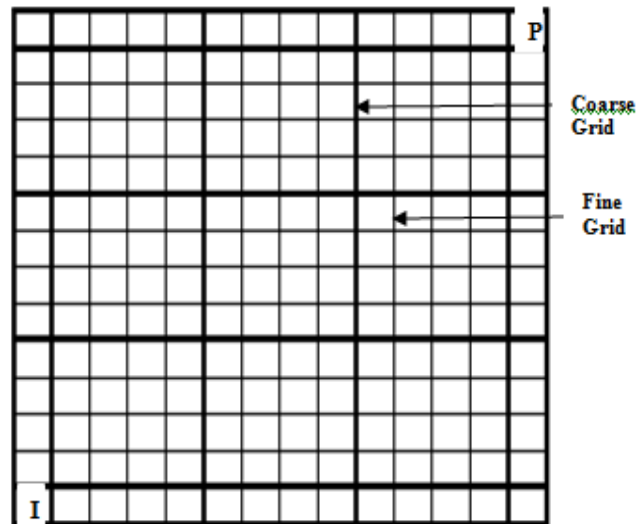


Figure 3 2D Homogeneous Fine Grid and Coarse Grid

2D Heterogeneous Model

We also tested the pseudo-relative permeabilities in three simple heterogeneous vertical cross-section models. The fine grid models were a Cartesian grid of 20×1×10 (x, y, z directions) dimensions. They had absolute permeabilities ranging between 50-150md which were randomly correlated, high-permeability channels in a low permeability system and a layered reservoir system respectively. The fluid model of the 1D and 2D homogeneous and 2D heterogeneous systems were the same. The general parameters of the models are shown in Table 3. In the random-correlated model, the water was injected at constant rate of 2500bbls/d and pressure and the producer had the same oil flowrate till water breakthrough. The permeabilities were generated using a random number generator with normal distribution and standard deviation of 20 and mean of 100md. The secondary recovery was carried out in 6000days.

The layered model had an increasing absolute permeability from the top to the bottom layer. The water injection flowrate was 9800bbl/d and oil rate was equal to the water injection rate before and at water breakthrough. Waterflooding and oil production were carried out in 4000days. In the channel reservoir, the water injection rate and oil production rate before breakthrough was 1450bbl/day. The water injection was carried out at pressure of 8000psia. Waterflooding and production of the reservoir was carried out in 6000days.

The calculated oil and water relative permeabilities were input in each of the models with a viscosity ratio of 4 between the oil and water. Each fine grid model was coarsened by undergoing two steps – homogenization of the heterogeneous fine grid into a 1D 4×1×1 (x,y,z) coarse grid models following an approach used by Muggeridge (1991) and calculation of relative permeability for the coarse grid models from simulation results of the fine grid model using the Johnson, Bossler and Nauman (1957) and the Jones and Roszelle methods (1978). The relative permeabilities calculated are input into one copy of the coarse grid models. The pseudoisation method of section two was carried out on the deduced oil and water relative permeabilities using the JBN method (Jones and Roszelle, 1978). One pair of rock relative permeabilities and two pairs of pseudo-relative permeabilities were input into the second copy of the coarse grid models just as the 1D and 2D homogeneous models and simulation results were compared for effects of heterogeneity representation in the coarse grid and compensation of numerical dispersion.

Table 3 2D Heterogeneous Model Parameter

Porosity	0.2
Oil Formation Volume Factor	1.000rb/stb
Water Formation Volume Factor	1.000rb/stb
Water Viscosity (cP)	0.5
Oil Viscosity (cP)	2.0
Water Compressibility	3.03E-6/psi
Rock Compressibility	0.3E-05/psi
Range of Permeability in Heterogeneous Layer Model	500-50md
Standard Deviation for Random Correlated System	20
Mean Permeability for Random Correlated System	100md
High Permeability Channel Range	49-150md
Water Relative Permeability Endpoint	0.3
Oil Relative Permeability Endpoint	0.9
Residual Oil Saturation	0.1
Connate Water Saturation	0.2
Initial Reservoir Pressure	4000psia
Reservoir Dimension (ft)	3000 ×1000
Reservoir Thickness (ft)	100
Injector Well Location:	(20 1 10)
Producer Well Location	(1 20 10)

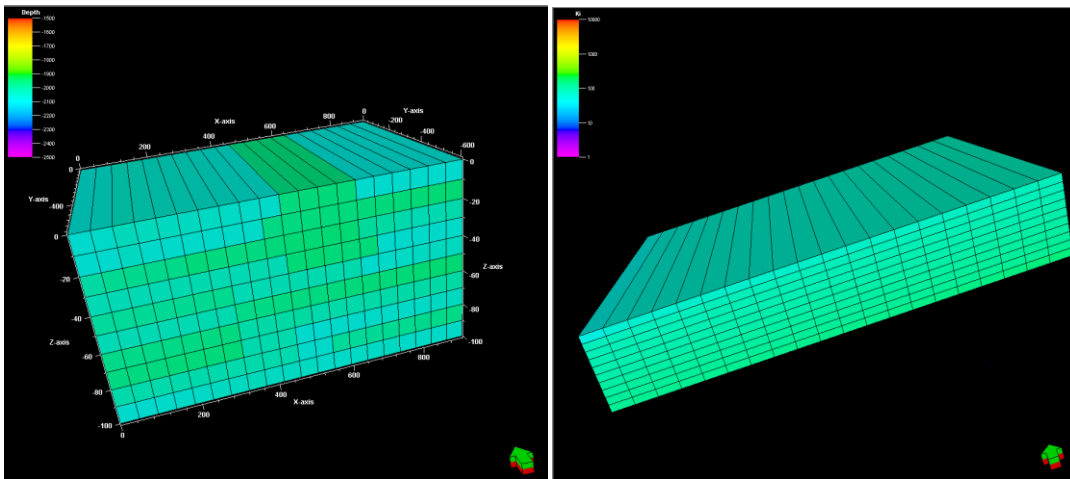
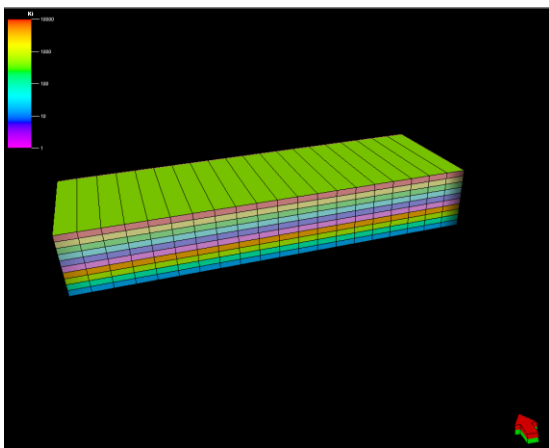


Figure 4(a) 2D Heterogeneous Channel Model; Figure 4(b) 2D Heterogeneous Random Permeability Model
 Figure 4(c) 2D Heterogeneous Layered Model



Pseudoisation Results

1Dimensional Pseudo-Relative Permeability Formulation

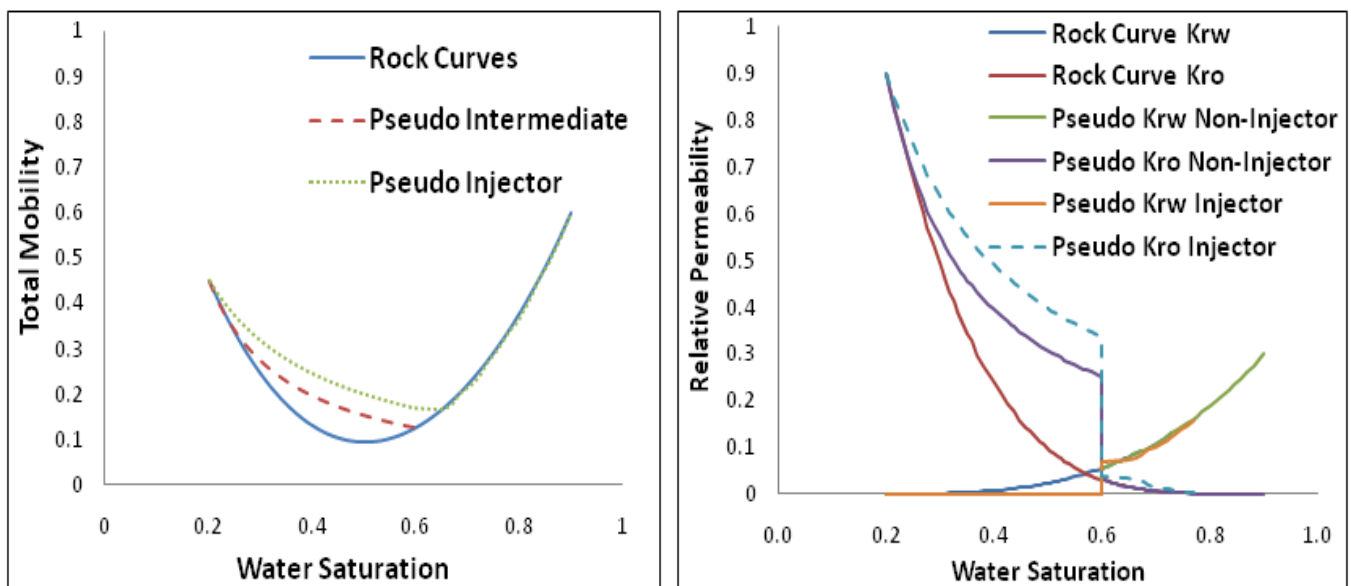


Figure 5(a) Total Mobility Plot for 1D and 2D Homogeneous; (b) Pseudo-relative permeability and relative permeability curve

for the 1D derived Pseudos for 1D and 2D Homogeneous.

Figure 5(b) shows the pseudo-relative permeabilities generated from the rock curves for the 1D and 2D homogeneous case. The oil pseudo-relative permeability curves obtained moved to the right of the rock curves. This shows the classical shape of pseudofunctions required to reduce numerical dispersion as was also seen in the work of Barker and Dupuy (1999). The two oil pseudos start at $1 - S_{or}$ and had similar values as the rock oil relative permeabilities curve then suddenly rise above the rock curves at water saturations equal to 0.75, then increased further at the shock front of 0.598 rising to the same rock oil curve endpoint of 0.9. This is a difference to the outcome of Hewitt et al (1998) analysis in which their oil relative permeability rose above 1.0. The water pseudo obtained are very similar to the water rock curves from the shock front saturation of 0.598 to $1 - S_{or}$ of 0.9. At lower water saturations to the S_{wc} the water pseudos remain at zero.

Figure 5(a) shows the rock curve and pseudo total mobilities calculated in equation 32, 33 and 36 in which at S_{wc} the rock total mobility was 0.45 which reduces to the shock front saturation and then increase to 0.6 at S_w equal to 0.9. The oil mobility for the intermediate gridblock decreased as the water saturation increases. The total mobility for the injector wellblock decreased from S_{wc} and reached a minimum at the average water saturation and then increased to 0.6. Pseudo-relative permeability and total mobility plots (please refer to Appendix B3) for the heterogeneous channel and layered system showed similar classical shape of pseudos that reduce numerical dispersion.

Simulation Study Results

1D Homogeneous Model Results

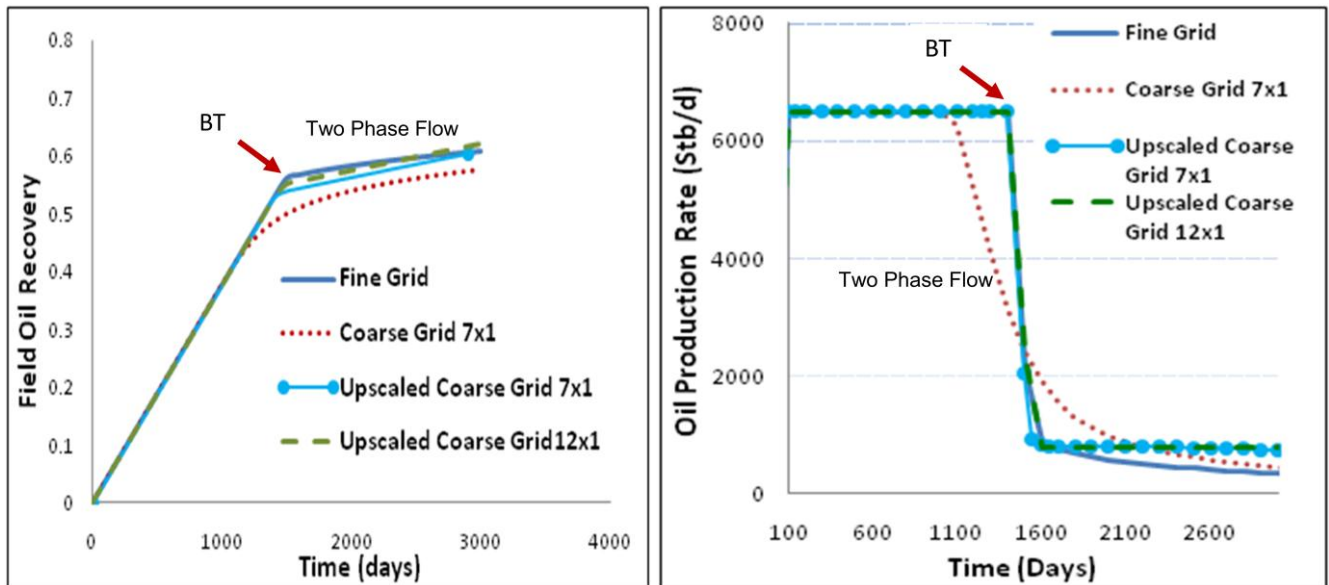


Figure 6(a) Production Rates of 1D Homogeneous Fine Grid and Coarse Grids; 6(b) Field Recoveries of 1D Homogeneous Fine and Coarse Grids

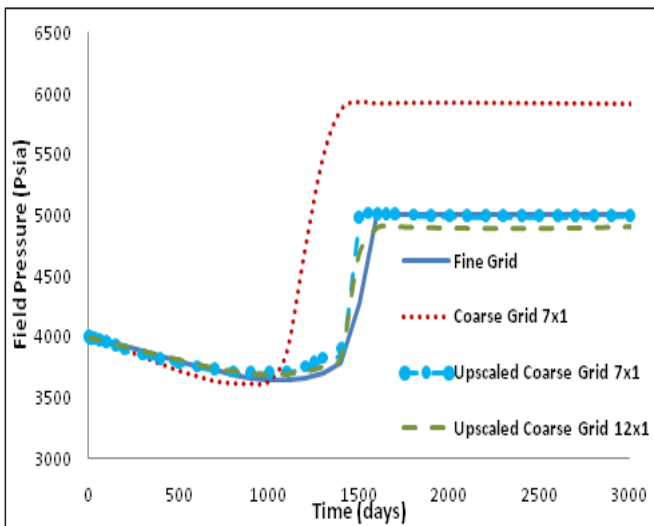


Figure 6(c) Comparison of Field Pressures for the 1D Homogeneous fine grid, upscaled coarse grid and standard coarse grids. The first case study is the 1D homogeneous model with permeability of 200md. The analytically derived pseudo-relative permeabilities was tested in a 1D model. The effect of numerical dispersion was observed in the oil production rates, field recovery and field pressures. The ability of the two upscaled coarse grid models to reproduce the results of the fine grid model was also evaluated. Figure 6(a) shows the comparison of oil production rate for the fine grid, 7×1 coarse grid and upscaled 7×1 and 12×1 coarse grids using the new pseudos. The standard coarse grid produced oil at the rate of 6500bbls/d and had its breakthrough earlier than the fine grid, upscaled coarse grids predicted breakthrough at exactly the same time as the fine grid model. After breakthrough, the fine grid had a similar two phase flow gradient with the upscaled 12×1 coarse grid and 7×1 coarse grid. The upscaled grids have been able to reduce numerical dispersion by 300days at breakthrough and predict similar water cut profile for 12×1 coarse grid and 7×1 coarse grid with the fine grid. Figure 6(b) shows a comparison of the field oil recovery for the fine grid, standard coarse grid and pseudo-upscaled coarse grids. The 12×1 and 7×1 upscaled coarse grids predicted water breakthrough time closer to the breakthrough time of the fine grid model with the 12×1 upscaled coarse grid the closest. The standard coarse grid predicted breakthrough time much earlier than the fine grid, producing the most incorrect prediction. In figure 6(c) the pressures of the fine grid, coarse grid and upscaled coarse grids were compared. The fine grid and upscaled coarse grids had closer pressure profiles during the course of production. The conventional coarse grid had a pressure profile with the lowest pressure coming earlier and then rising and stabilizing higher than the fine grid model. Production rate, recovery and pressures are a function of flow which is average saturation within the gridblock. The effect of numerical dispersion on saturation has caused the disparity between the fine grid results and coarse grid results. The pseudoisation have reduced the effects of numerical dispersion and improved the results of the upscaled coarse grid. Therefore, with the pseudoisation method, we have been able to a very large extent reproduce the results of the fine grid model.

2D Homogeneous Model Results – Quarter-Five Spot Pattern

The pseudos were also tested on three 2Dimensional coarse grid models. The field production rates, oil recoveries and field pressures results were compared on the fine grid, coarse grid and upscaled coarse grid.

Figure 7(a) shows the water breakthrough time of the 2D fine grid model, standard coarse grid and upscaled coarse grids. The upscaled 8×5 coarse grid, upscaled 6×6 coarse grid and upscaled coarse 5×5 grid had their breakthrough times closer to that of the fine grid model. The upscaled 8×5 coarse grid had the closest breakthrough time prediction to that of the fine grid and the upscaled 5×5 had the farthest. This could be attributed to the fact that the assumption of constant saturation may be less valid in one coarse grid than another. The standard coarse grid had the earliest breakthrough time. The use of the pseudo-relative permeabilities have reduced numerical dispersion in breakthrough time for upscaled coarse grids oil rate results. Figure 7(b) shows a similar water breakthrough time of the oil recoveries of the fine grid, and upscaled 8×5, 6×6 and 5×5 coarse grids. The standard coarse grid had an earlier breakthrough time when compared to that of the fine grid. The pseudoisation method has reduced the errors and reproduced similar breakthrough time for the fine and upscaled coarse grid recovery results.

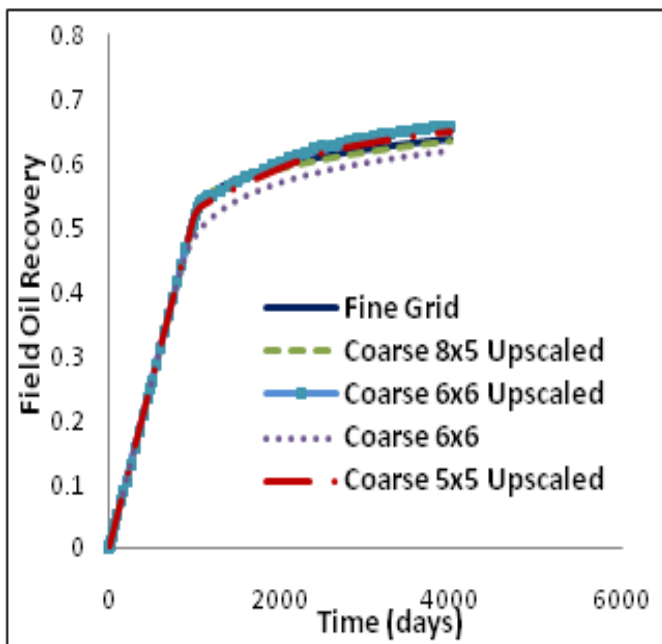


Figure 7 (a) Oil Recovery Comparison for the 2D Homogeneous Models

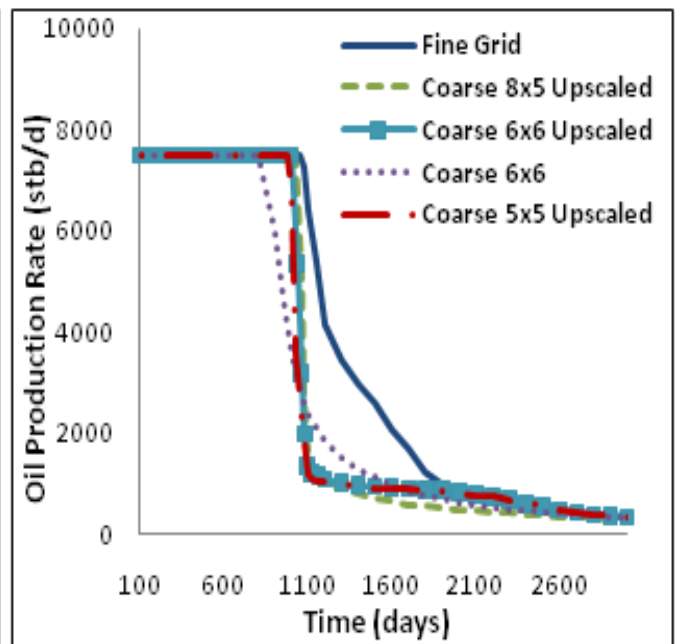


Figure 7(b) Comparison of Oil Production Rate in 2D Homogeneous Models

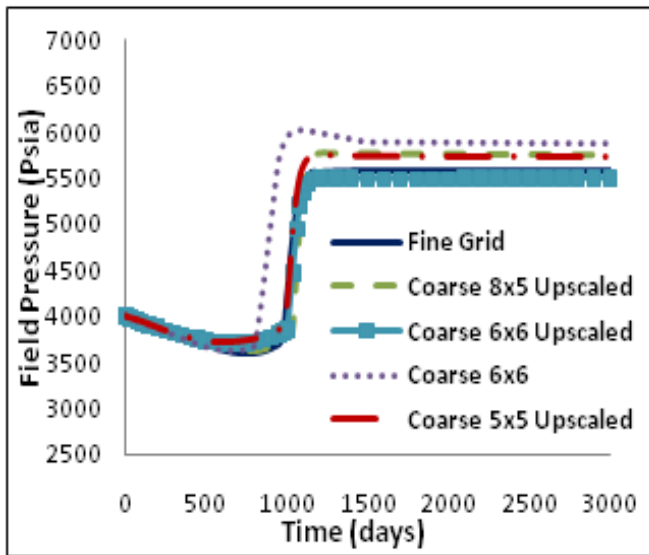


Figure 7(c) Comparison of Pressure Profile in 2D Homogeneous Models

Figure 7(c) showed pressure profiles for the fine grid, upscaled coarse grids and the standard coarse grid. The profiles of the upscaled were closer to the fine grid model with the 8x5 coarse grid having the closest pressure profile. The 5x5 upscaled coarse grid was the furthest of the three. The standard coarse grids predicted earlier pressure decline and rise than the fine grid due to numerical dispersion. The pseudoisation method have given better coarse grid results compared to the fine grid model with the 8x5 model, with largest number of gridblocks between the wellblocks giving the best performance and the 5x5 model with the smallest number of gridblocks giving the worst performance.

2D Heterogeneous Model Results

The pseudos were lastly tested on the two 2D heterogeneous models, a high permeability channel in a low density system and a layered system with increasing permeability. The topmost layer has the lowest permeability. Production rate, recovery and field pressures of the fine grid, homogenized fine grid, homogenized coarse grid and upscaled homogenized coarse grid were compared. In Figure 8(a) and 8(b) the upscaled coarse grid had its breakthrough time closer to the homogenized fine grid and standard fine grid. Also, the production rate showed upscaled coarse grid having closer breakthrough time and profile to the two fin grids compared to the standard coarse grid. Figure 9(b) showed similar trend as error between the two fine grid and upscaled coarse grids were reduced compared with the recoverys and production rates of the standard coarse grid, after the upscaling with the new pseudos that compensate for numerical dispersion. Similar results were obtained for the field pressures. The plot of saturation versus fractional flow curve for the random permeability using its JBN curves gave a characteristic no shock shape (refer to Appendix B4 for the plot).

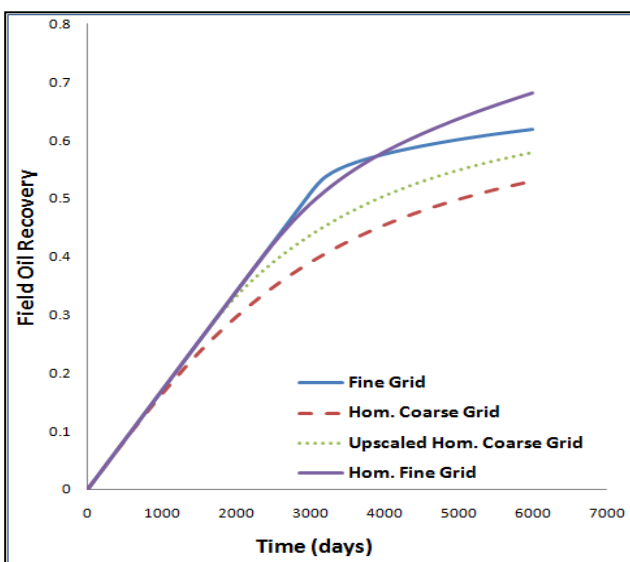


Figure 8(a) Comparison of Recoveries for Channel Model

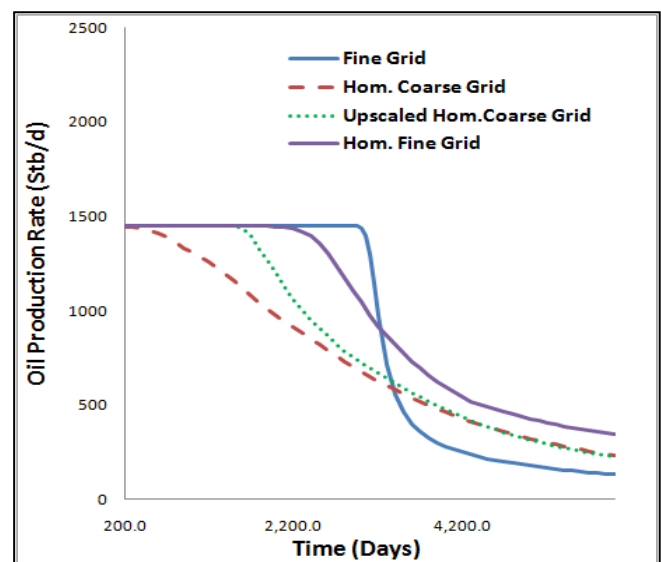


Figure 8(b) Comparison of Production Rate for Channel Model

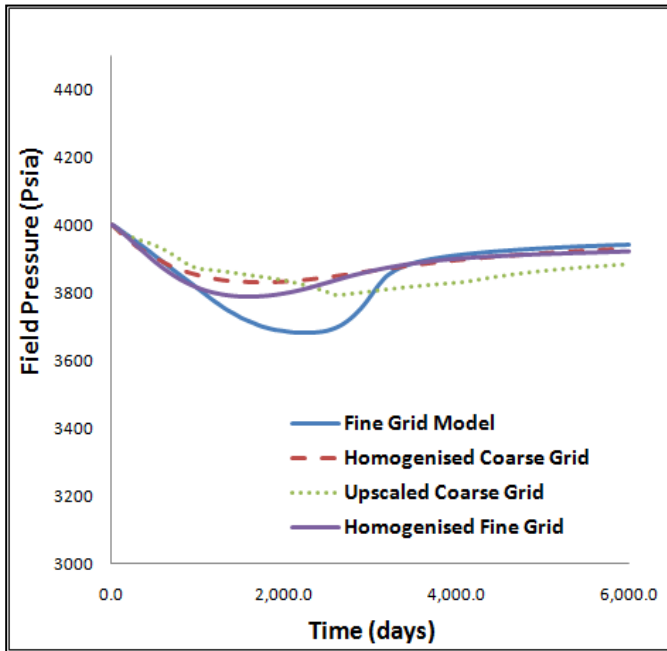


Figure 8(c) Comparison of Pressures of Channel Model

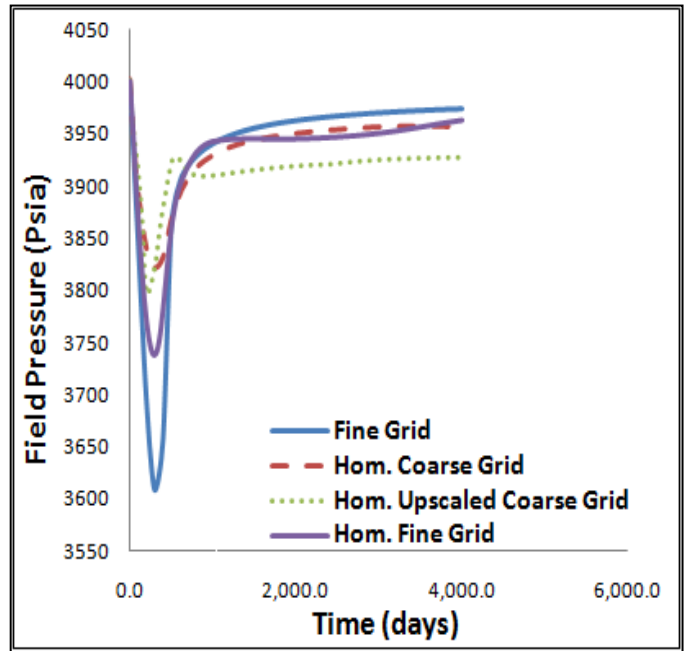


Figure 9(a) Comparison of Pressures for Layered Model

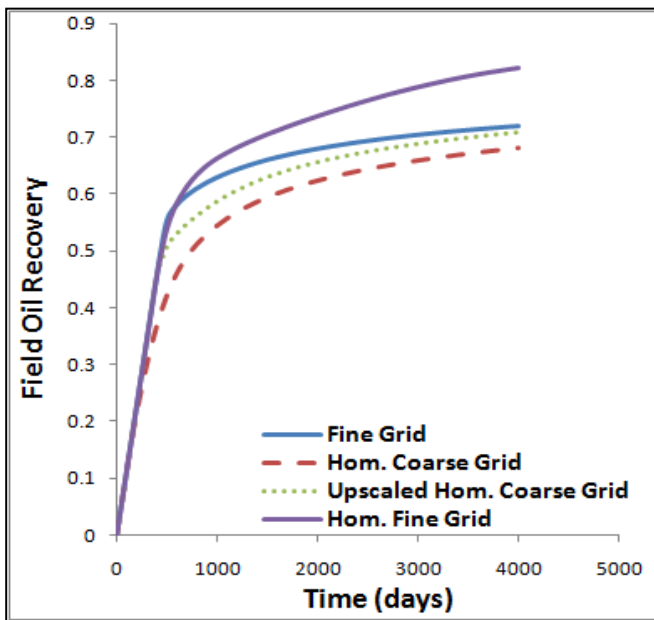


Figure 9(b) Comparison of Recovery for the Layered Model.

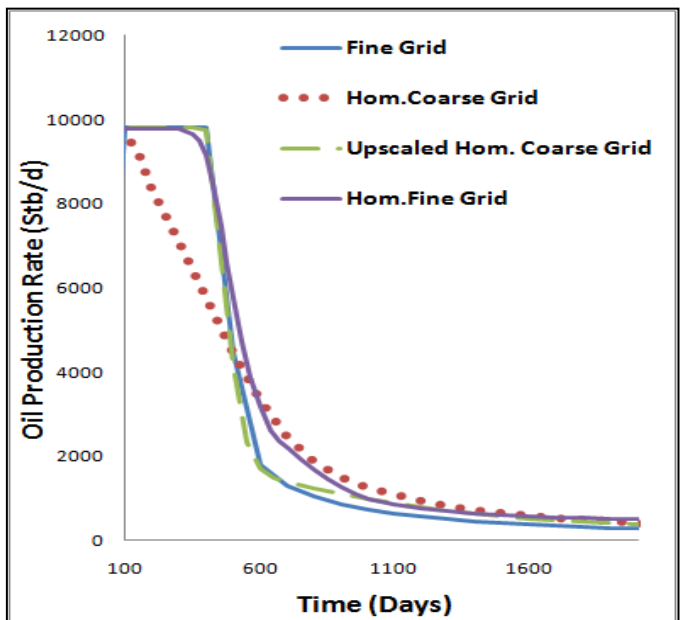


Figure 9(c) Comparison of Production Rate for the Layered Model

Discussion

A new relative permeability upscaling method was introduced and tested in different 1D, 2D homogeneous and 2D heterogeneous models undergoing waterflooding in this project. Unlike in earlier works, the 1D analytically derived pseudo-relative permeability was tested in not just in 1D but in 2D areal and heterogeneous line drive models. The 1D and 2D models tests with the use of the new upscaling technique showed improved results of the coarse grids when compared to the fine grid results. However, we observed reduced performance in 2D homogeneous and 2D heterogeneous models.

The 1D pseudo-relative permeability showed the classic shape for compensating numerical dispersion for the laboratory rock curves and JBN (1957) rock curves. This is a similar result obtained for earlier methods of pseudoisation. But in this study the curves were derived analytically using Buckley Leverett (1942) and Welge (1952) theories of 1Dimensional displacement. They also modified the oil relative permeability for saturations less than the shock front saturation and thus gave a much better prediction of reservoir pressure compared to the traditional methods of truncating of relative permeability curves. The pseudorelative permeabilities formulated worked for smaller and larger coarse gridblocks and for 7 and

12 gridblocks. Moreover, it maintained the parent rock curve endpoint value and the mobilities calculated are between 0 and 1. Therefore any laboratory relative permeability can be easily and quickly converted to pseudos that compensate for numerical dispersion and input into coarse grid models to reproduce fine grid results.

In the 1D test case, the fine grid, coarse grid and upscaled coarse grids predicted the same oil production rate until water breakthrough. Here, the upscaled coarse grid reproduced exactly the fine grid water breakthrough time. The upscaled models also reproduced an improved two phase fine grid profile after breakthrough. The conventional coarse grid had errors in predicting the breakthrough profile. Also with increasing gridblock between the injector and producer wells we are able to have improved prediction of the two phase flow profile of the fine grid after breakthrough. Therefore, the results have shown that for a homogeneous 1D system, we may not need to run the fine grid simulation to obtain accurate results for our waterflooding scheme. That using two pairs of pseudo-relative permeabilities for upscaling can give satisfactory reproduction of fine grid results in 1D. This is in contrast to conventional methods of using one pair pseudo-function for every gridblock. Also, that the performance of the pseudo-functions is independent of the gridblock size in the two phase flow region.

For the 2D homogeneous test case, the single phase flow profile for the the fine grid was reproduced by the standard coarse grid and upscaled coarse grid models. However, the breakthrough time was approximated only by the upscaled coarse grid models in the oil production rate and field recovery. With increasing number of gridblocks in between producer and injector a better match of breakthrough time can be predicted as can be seen by the 8×5 2D model result. But the two phase flow after breakthrough was not accurately predicted by both the upscaled and standard coarse grid models. This discrepancy can be attributed to radial flow effects which is very dominant near well in the producer and the injector and also strong in 2D areal models as the flow spreads from the injector to the producer. The producer wellblock was treated as an intermediate gridblock in this work. For improved flow description around the producer wellblock, pseudo-relative permeability may have to be developed for the wellblock. In addition, the formulation may have to be modified to incorporate radial flow effects for the producer and the injector wellblocks. Furthermore, we deduce that to fully compensate for numerical dispersion in coarse grid models three pairs of pseudo-relative permeabilities are needed to be input into the coarse grid models, one pair for the injector wellblock, one for the producer and one for the intermediate wellblocks.

The use of the JBN method (1957) to derive effective relative permeabilities used to convert a 2D heterogeneous fine grid models to a 2D homogenized fine grid model having constant effective absolute permeability and the conversion of the effective relative permeabilities to analytically derived pseudofunctions that compensate for numerical dispersion in homogenized coarse grid models was successful as seen in the channel model of figure 8(a), (b) and (c); and layered model of figure 9(a), 9(b) and 9(c). The homogenized fine grid gave a close and approximate match to the heterogeneous fine grid models for the oil rates, pressure and recovery plots. In practice it would be faster to homogenize two phase flow using steady state upscaling methods and then apply the analytic method described here to compensate for numerical diffusion. This should be investigated in future work.

The main conclusion of this work is that you do not need to develop pseudofunctions for every gridblock to compensate for numerical dispersion. We have seen that the analytically derived pseudofunctions provide good match to oil production rate, recovery and pressure unlike the traditional methods that simply truncate the rock relative permeabilities at the shock front saturation and setting them to be zero below the shock front.

Conclusions

In our study, we reduced numerical dispersion in coarse grid model results using pseudo-relative permeabilities analytically derived from Buckley & Leverett (1942). This involved creating pseudofunctions for the injector and non-injector gridblocks and inputting these into coarse grid models. From our analysis, the following conclusions can be drawn:

1. We only need three sets of pseudo-relative permeability to compensate for numerical dispersion seen in coarse grid models. These are one for the injector wellblock, one for the intermediate gridblocks between the wells and one for the producer wellblock. The producer wellblock pseudofunctions will serve to account for radial flow effects. The effect of radial flow was seen in the discrepancies of the 2D homogeneous 1 models. However, the nature of the producer wellblock pseudos was not treated by this work and needs further investigation.
2. We will need only one set of pseudo-relative permeabilities in the intermediate gridblocks between the producer wellblock and the injector wellblock. This was seen in the results of the 1D and 2D homogeneous areal model. Important implications of this is that you will only need different pseudo-relative permeabilities for different gridblocks in a heterogeneous model when you want to represent the impact of heterogeneities to flow in individual gridblocks and that grouping of pseudo-relative permeability for heterogeneous systems modeling should be based on similarity in heterogeneity. This is in contrast to the results by Hewitt et al. (1998) that the changes to pseudofunctions depend on the distance between inlet and outlet of gridblock to the injector wellblock.
3. We propose that heterogeneous systems can be homogenized using published JBN method (1957) and then the analytical method described in this work can be used to convert the relative permeability data to pseudofunctions that will compensate for numerical dispersion.
4. The pseudofunctions are easy to precalculate before a simulation which makes them less difficult to use than traditional truncated curves. They also provide better match for pressures than the truncated curves. Moreover, the method provides an easier way of upscaling than the dynamic pseudo-relative permeability methods as we do not need full scale fine grid simulation before computing the pseudos.

Recommendations And Further Work

From the conclusion of the study, recommendations for further work are:

1. Derivation of pseudo-relative permeabilities that will compensate for numerical dispersion for the producer wellblock.
2. Modification of already derived pseudo-relative permeability for the effects of radial flow in wellblocks in 2D and 3D systems
3. Modification of the analytically derived pseudofunctions for the effects of gravity for 2D cross-sectional and 3D systems and capillary pressure in low flowrate systems.
4. Investigate combining the method with the use of steady state pseudo relative permeabilities for homogenization

Nomenclature

i	= notation denoting gridblock position
j	= notation denoting saturation position in the rock curve table.
J	= notation denoting shock front saturation position in the rock curve table.
$K_{rw}(S_w)$	= laboratory or rock relative permeability of water phase
$K_{ro}(S_o)$	= laboratory or rock relative permeability for oil phase
$K_{rwp}(S_w)$	= Pseudo-relative permeability of water phase
$K_{rop}(S_o)$	= Pseudo-relative permeability for oil phase
S_w	= saturation of the water phase
S_{wf}	= shock saturation of the water phase
$\overline{S_{wf}}$	= Average saturation of the water phase behind the shock front
S_{wc}	= Connate Water Saturation
q_o	= oil phase flow
q_w	= water phase flow
q_t	= total flowrate in the reservoir model
f_w	= fractional flow of water phase
μ_w	= viscosity of the water phase
μ_o	= viscosity of the oil phase
λ_o	= rock mobility of the oil phase
λ_w	= rock mobility of the water phase
λ_T	= Total mobility of the water phase
$\Psi_T(S_{wj})$	= Pseudo-total mobility
$\Psi_O(S_{wj})$	= Pseudo-oil mobility
$\Psi_w(S_{wj})$	= Pseudo-water mobility
Δx	= gridblock size
P_{j+1}	= Pressure in the gridblock $j + 1$
ϕ	= Porosity of the reservoir model
A	= cross section of flow within a gridblock
t	= time duration of flow
ζ	= dimensionless time constant
K	= Absolute Permeability
v	= Dimensionless Velocity

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APPENDICES

APPENDIX A

CRITICAL LITERATURE REVIEW

UPSCALING OF RELATIVE PERMEABILITY TO REDUCE NUMERICAL DISPERSION

SPE Paper n°	Year	Title	Authors	Contribution
SPEJ	1998	“Analytical Calculation of Coarse-Grid Corrections for use in Pseudofunctions ”	T. A. Hewitt, K. Suzuki, M.A. Christie	Due to discretization of flow properties on a coarse grid, corrections are required for pseudofunctions. This paper presented an approach to calculate corrections to pseudofunctions.
EAGE	1999	‘An Analysis of Dynamic Pseudo-Relative Permeability Methods for Oil-Water Flows’	J.W. Barker, Philippe Dupouy	Provided the analysis of the properties of six widely used dynamic pseudo-relative permeability methods for incompressible, immiscible, two phase flow
35491	1997	A Critical Review of the Use of Pseudo-Relative Permeabilities for Upscaling	Barker J.W., Thibeau S.	Provides a summary of the practical difficulties encountered in the use of dynamic pseudo-relative permeabilities and highlights need for analytic alternatives.
EAGE	2009	“Vorticity as a measure of heterogeneity for improving coarse grid generation ”	H. Mahani, Ann H. Muggeridge and M. A. Ashjari	1. This paper described sub-grid heterogeneity as a function of vorticity. 2. Provided knowledge on coarse grid generation, numerical dispersion reduction and homogenisation
37324	1996	“ Upscaling for Reservoir Simulation”	M.A. Christie	This paper reviews and summarizes both single and two phase upscaling techniques
SPE R.E.	1994	“A New Representation of Wells in Numerical Reservoir Simulation”	Yu Ding, G. Renard	The paper presents a new analytical solution for near-well pressure is presented for uniform and non-uniform grid-blocks
EAGE	2002	“Scale-up of Well Performance for Reservoir Flow Simulation”	A.H. Muggeridge, M. Cuppers, C. Bacquet and J.W. Barker	1. An example of a method of scale-up of near-well region.
74139	1971	“Quantitative Evaluation of Numerical Diffusion (Truncation Error)”	R.B. Lantz	1. The Paper presents quantification of numerical diffusion caused by finite approximation of flow properties. 2. It shows the interrelationship of gridblock number, size and time to numerical diffusion.
1023-G	1957	Calculation of Relative Permeability from Displacements Experiments	Johnson E.F., Bossler D.P., Naumann V.O.	Provides an analytic method for generating oil and water relative permeabilities from fine grid 2D heterogeneous model for a homogenized coarse grid model.
Reservoir Characterization II 1991	1991	Generation of Effective Relative Permeabilities from Detailed Simulation of Flow in Heterogeneous Porous Media	Ann H. Muggeridge	The paper provided the methodology used in homogenizing the fine grid heterogeneous model and generating pseudo-relative permeabilities.

SPE 51269 (1998)

Analytical Calculation of Coarse-Grid Corrections for Use in Pseudofunctions

Author: Hewitt T.A., Suzuki K., Christie M.A.

Contribution to upscaling of relative permeability for reduction of numerical dispersion:

1. Contributed with his technique of discretizing of saturation, relative permeability curves, fractional flow curves and mobility.
2. Provided the technique used for the determination of average saturation and relative permeability for non-injector well gridblocks.

Objective of the Paper:

1. To show a new method for calculating the corrections for fluid flow variables required to account for discretization of the continuous Buckley Leverett solution on a coarse grid.

Methodology Used:

1. The new approach used a method of characteristic based on the material balance equation describing the displacement of oil by water to yield an expression for gridblock average saturation as a function of outlet face saturation.
2. The method of characteristics was used to develop the right changes to water saturation and flow properties relationships such as relative permeability required for discretization on a coarse grid.
3. Defined water saturations for the discrete representation of the Buckley Leverett continuous solution by averaging them over a volume on the discrete grid.

Conclusions Reached:

1. The differences between discretized relations and local relations used in constructing continuous solution are the result of the different averaging volumes used in their definitions.
2. Interblock fractional flows are associated with upstream gridblock and average total mobility is measured between gridblock centers.
3. The modifications required to account for coarse gridblock effects depend only on the ratio of the distances from the injection boundary to the inlet and outlet faces of a discrete gridblock
4. The changes required for relative permeability for the discrete representation are not dependent of gridblock size and number of gridblocks, but depend on the number of gridblocks only for a uniform discretization, with the first gridblock immediately after the injector outlet face.

Comment

The new approach provides good information for the calculation of discretized water saturation, fractional flow and total mobility in a gridblock. However, the rise of oil pseudo relative permeability above endpoint and presence of non-monotonic relative permeability values is an issue.

EAGE/ Geological Society/ Petroleum Geoscience, Vol 5 (1999) PP 385-394

An Analysis of Dynamic Pseudo-Relative Permeability Methods for Oil-Water Flows

Author: Barker J.W., Dupouy P.

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

Provided knowledge on the of the six main dynamic pseudo-relative permeability methods. Dynamic methods are one approach of creating pseudo-relative permeabilities that reduce numerical dispersion.

Objective of Paper

To analyze the properties of six widely used dynamic pseudo-relative permeability methods for incompressible, immiscible two phase flow.

Methodology Used:

1. Pseudorelative permeabilities from the six dynamic methods are generated from the results of the fine grid simulation on a coarse grid
2. The paper uses simplified Stones example of a dipping vertical cross-section consisting of two non-communicating layers of different permeability undergoing incompressible and immiscible displacement of oil by water in which the oil displacement
3. Analytically derived solution of the simplified Stone's example was obtained using the six methods equations and each were analysed for their properties and limitations.
4. Stones example with Buckley Leverett type of solution in each layer was solved numerically and analytically with the six methods and plots of relative permeability, pressure and water cut were compared for the two approaches using a 50X2 gridblock
5. In the Kyte and Berry method, average pressures from each coarse gridblock and total flowrates of each phase between adjacent coarse gridblocks from fine grid results calculation are input into Coarse grid Darcy flow equation to generate the pseudos.
6. The pore volume method used a similar technique as the Kyte and Berry, but pore volume weighted average pressure over gridblock is used to generate in the coarse grid Darcy flow equation.
7. Stone's and total mobility method uses the concept of total mobility to generate pseudos thereby avoiding problems associated in estimating the coarse grid average pressures.
8. Quasi- steady state method uses upscaled (by solution of Laplace Equation) permeability of each phase divided by the upscaled absolute permeability to calculate oil and water pseudos.
9. Weighted relative permeability calculates pseudos by as an average of the transmissibility weighted fine grid relative permeabilities on the outlet face of the coarse grid block.

Conclusions Reached:

1. Pore volume and Kyte and Berry methods reproduce fine grid results but with problems of infinite and negative pseudo-relative permeabilities, position dependent pseudo-capillary pressure makes them difficult to use.
2. Total mobility, Quasi-steady state, Stone and Weighted Relative permeability (Eclipse Pseudo) methods do not guarantee reproduction of the fine grid results.
3. Numerical dispersion compensation can be seen in the plots of relative permeability and water saturation, field pressure and water cut.

Comments

Kyte and Berry and Pore volume methods are still not very ideal practically as the former is dependent on pseudo-capillary pressure location while the latter produces negative and infinite pseudo-relative permeability values, so there could be a need for investigating alternative semi-analytic and analytic pseudoisation methods. The shape of the pseudo-relative permeability is seen to move towards the right for all the methods are consistent with pseudoisation methods encountered.

SPE 35491 (1996)

A Critical Review of the Use of Pseudorelative Permeabilities Upscaling

Author: Barker J.W., Thibeau S.

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

1. Provided knowledge on grouping pseudo-relative permeabilities in coarse grid

Objective of Paper

1. The paper describes the practicality and limitations of different dynamic pseudo-relative permeability methods.
2. To describe the suitability and reliability of various pseudo-relative permeability methods for use in scaling up from fine grid geological model to coarse grid fluid flow model.

Methodology Used

1. He summarized the individual capabilities and problems of each of the above mentioned six dynamic pseudo-relative permeability methods and came up with generalized practical difficulties with the use of any of the methods.
2. The Pseudorelative permeabilities are obtained using a saturation distribution based on the average saturation of each gridblock.
3. In viscous forces dominated case, the saturation distribution required is obtained from fine grid or dual-scale grid simulation and dynamic pseudo-relative permeabilities are calculated using any of the six main methods.

Conclusions Reached:

1. The limitations of dynamic pseudo relative permeability methods are computing a different set of pseudos for every coarse gridblock or classifying the gridblocks into different rock types, the choice and number of Fine grid models to be used and pseudos dependence on well locations and rates.
2. An alternative method to generating dynamic pseudo-relative permeability is to scale-up relative permeability analytically such as the large scale averaging method.
3. In the geological model, the effects on fluid flow of the correlated heterogeneities can be captured only qualitatively unless assumption of capillary or gravity equilibrium

Comments

The paper highlights the limitations of the six dynamic pseudo-relative permeability models used to reduce numerical dispersion. The problems of infinite and negative pseudo-rel perms, directional and non-zero pseudo capillary pressures and restrictive boundary conditions and assumptions of zero gravity and constant average total mobility limits their practical use. These limitations provide opportunities for analytic and semi-analytic methods of pseudoisation to be investigated. Moreover, we are trying to solve the problem of running the fine grid simulation. The dynamic method requires the fine grid simulation to be run, making them less practical.

EAGE (8) 2002

Scale Up of Well Performance for Reservoir Flow Simulation

Author: Muggeridge A. H., M. Cuypers., C. Bacquet., J.W. Barker

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

The project did not use the technique but it's an example of near-well scale-up methodology.

Objective of Paper

1. To investigate the use of the method of Ding in the scale-up of the near well region in 2D, 3D and partially penetrating problems.

Methodology Used

1. The permeability of the coarse grid can be scaled-up by superimposing the coarse grid on a fine grid heterogeneous model.
2. The method of Alabert & Corre (1991) was used to calculate each flow direction in the coarse grid.
3. Two implementations of Ding method was done, the first is a single flow fine grid simulation for each well and the output pressure and fluxes are read by a post processing program.
4. The second involves solution of pressure equation for single phase flow for each well on a limited region of the fine grid model (reduced computational domain).

Conclusions Reached:

The Ding method gave better results over conventional scale-up methods of well performance and gridblock transmissibility in heterogeneous models.

Comments

This method provides Ding's method of scale-up of well performance in the near well region where the radial flow regime is assumed predominant. The project assumes linear flow in the wellblock and non-wellblocks. The use of small well blocks for the injector wellblock provided sufficiently good results and did not pose convergence problems as informed by the paper. This new method avoids issues arising from scale-up of flow properties in the near-well region and any local grid refinement

SPE 2811 (1971)

Quantitative Evaluation of Numerical Diffusion (Truncation Error)

Author: R.B. Lantz

Contributions to Upscaling of Relative Permeability to Reduce Numerical Dispersion

The paper provided technique in selecting number and size of gridblocks and timesteps to be used in developing coarse grid models.

Objective of Paper

1. To show that numerical diffusion over a wide range of block size and time-step in numerical simulations is quantitative and not just qualitative.
2. To provide guidelines for selecting gridblock sizes and timesteps in order to keep numerical diffusion as small as possible.

Methodology Used:

1. The paper used a backward finite difference approximation for the convective-diffusive equation to represent numerical and physical diffusivity seen in miscible and immiscible displacements.
2. He compared backward difference numerical calculation with Welge analytical solution for a relative mobility curve taken at time of frontal saturation and a quarter of frontal saturation.

Conclusions Reached:

1. Little or no smearing was observed at time steps taken at Welge frontal saturation compared to significant diffusion at lower time steps
2. Most important numerical diffusion error is assumed to arise from the differential equations that include first-order derivatives
3. With increase in gridblock size, second order numerical diffusivity error could become substantial.
4. Quantitative value of numerical diffusivity in displacements can be affected by a wide range of gridblock size and number and timesteps.
- 5.

Comments

Numerical diffusivity encountered in reservoir simulation of immiscible systems such as the displacement during a waterflood exercise can now be quantified and modeled using this method.

The size and number of cells in a model can determine the level of numerical dispersion seen in the results of a coarse grid model. The input of pseudo-relative permeability reduces levels of numerical dispersion caused by the coarse gridding

Reservoir Characterization II (1991) Academy Press

Generation of Effective Relative Permeabilities from Detailed Simulation of Flow in Heterogeneous Porous Media

Author: Muggeridge A.H.

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

The paper provided the methodology used in homogenizing the fine grid heterogeneous model and generating pseudo-relative permeabilities.

Objective of Paper

To show how well effective relative permeabilities dynamically derived from heterogeneous fine grid model represents the average properties of fluid flow through heterogeneous porous media

Methodology Used

1. Detailed Simulation methods by Christie (1989) were used to derive the effective relative permeabilities from the fine grid heterogeneous models.
2. The oil recovery and effective relative permeability curves obtained for three different heterogeneous media were examined for their behavior and variability.
3. Effective absolute permeabilities were computed on a first stage with the method described by Begg, Carter and Dransfield (1987)
4. Effective relative permeabilities were computed using Jones and Roszelle Method (1978) in the second stage.
5. The absolute permeability and effective permeability were used to represent flow in 1D homogeneous equivalent.
6. KYTE and BERRY method (1975) was used to develop pseudo-relative permeability that will compensate for numerical dispersion and incorporate effects of permeability variations.

Conclusions Reached:

1. Average properties of flow in a heterogeneous fine grid model can be represented by replacing the relative permeability data with pseudo-relative permeability.
2. Each representative volume of the fine grid model used to develop effective relative permeability must contain a representative section of the permeability distribution.
3. Pseudofunctions can perform roles of representing effects of heterogeneity and compensating for numerical dispersion in coarse grid models.

Comments:

The paper combines several established numerical methods suggested by others to develop pseudofunctions and reduced dimensionality of the model from 2Dimensional to 1Dimensional by successive scale-up. The use of the KYTE and BERRY method to reduce numerical dispersion in the coarse grid model creates issues of negative non-single value and infinite pseudo-relative permeability. These can create difficulty in their use.

EAGE (15) 2009 PP 91-102

Vorticity as a measure of heterogeneity for Improving Coarse Grid Generation

Author: Mahani, H., Muggeridge A.H., and Ashjari M.A.,

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

It provided technique to carry out effective gridding from fine grid to coarse grid to capture large scale heterogeneity effects on fluid flow.

Objective of Paper

To show how to generate flow simulation coarse grids from fine grid heterogeneous models with the aim of preserving large scale heterogeneities to flow.

Methodology Used

1. The grid coarsening technique involves fine grid construction, single phase flow simulation, vorticity map generation with finite difference method.
2. The fine grid is homogenized using the method of Li (1995) and lastly compensate for numerical dispersion in the coarse grid using the method of Muggeridge (1991).

Conclusions Reached:

1. Homogenised fine grid using vorticity maps gave a better match to the fine grid oil recovery and oil cut results from waterflooding simulation compared to uniformly homogenized coarse grid
2. Vorticity gives a measure of heterogeneity effects on large scale flow and permeability variation within the fine grid model
3. It can serve as a guide to coarse grid generation from fine grid heterogeneous models.

Comments

To retain some heterogeneity from the fine grid to the coarse grid, an effective gridding technique is required such that with the input of pseudo-relative permeability numerical dispersion would be reduced to a minimal value. The new gridding technique contributes to description of fine grid heterogeneity in coarse grid model

SPE 37324 (1996)

Upscaling for Reservoir Simulation

Author: M.A. Christie

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

1. Provided technique and basis for use of Buckley & Leverret (1942) shock height for grouping pseudo-relative permeability data used for upscaling.
2. Contributed technique on use of pressure solver method and arithmetic harmonic analytical methods for absolute permeability upscaling in the homogenisation of heterogeneous fine grid model.

Objective of Paper

The paper reviews single phase upscaling and introduces multiphase upscaling as a further step to better obtain reservoir heterogeneity description.

Methodology Used

1. He used pressure solver method to show single phase upscaling of absolute permeability, with no flow boundary on the horizontal walls of the model.
2. For two phase upscaling, he used a semi-analytic renormalization technique King (1989), extended by Christie et al (1995) to obtain pseudo-relative permeabilities from.
3. He studied the rate dependency of pseudo-effective permeability by developing a velocity field based on known well locations and rates and pseudos are obtained using the knowledge of expected flowrates.

Conclusions Reached:

1. In two phase upscaling, two limitations are observed, pseudo-relative permeabilities can be rate dependent and may also need some form of grouping to order large number of effective permeabilities into a manageable quantity.
2. A plot of pore volume produced against time showed the pseudos predicted better recovery rates and gave a better match than using the rock curves.
3. For any upscaling algorithm used, other checks should be performed to validate results.

Comments

1. Two phase upscaling can show the effects of reservoir heterogeneity more effectively than single phase upscaling.
2. Single phase upscaling could be insufficient when the correlation size of the permeability system is close in size as upscaled gridblock.
3. Grouping of relative permeability data provides a means reducing computing requirements and difficulties as well as averaging other flow properties in two phase upscaling.
4. Dynamic pseudoisation technique provides pseudo-relative permeability that are rate and well location dependent, limiting its usage and creating computational difficulties.

SPE 1023-G (1957)

Calculation of Relative Permeability from Displacements Experiments

Author: Johnson E.F., Bossler D.P., Naumann V.O.

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

The paper provides an analytic method for generating oil and water relative permeabilities from fine grid 2D heterogeneous model for a homogenized coarse grid model.

Objective of Paper

To show a new method for generating water and oil relative permeabilities from data obtained during a waterflood experiment performed on a linear porous body.

Methodology Used:

1. Very high injection rates was used in the waterflooding experiment to obtain stabilized displacement and constant flow velocity in all cross sections of the porous core sample of about 2-3in in length.
2. High flowrate and high pressure gradient developed across core was used to make the capillary pressure negligible during pressure drops.
3. Used differential equations developed from Welge correlations and Rapoport relative injectivity concept to calculate individual relative permeabilities from data generated from the displacement test.

Conclusions Reached:

1. Method tested and found to yield reliable results which are in agreement with methods using direct measurements of relative permeability in the laboratory.

Comments:

This method is fast and reliable, in agreement with welge fractional flow curve. However use of differential equations could lead to errors and practical difficulty when using tabulated data obtained from the field.

SPE 6045 (1978)

Graphical Techniques for Determining Relative Permeability from Displacement Experiments

Author: Jones S.C., Roszelle W.O.

Contribution to Upscaling of Relative Permeability to Reduce Numerical Dispersion

The paper provided a graphical form of the Johnson Bossler method which can be applied to field tabular rate, water cut and pressure data.

Objective of Paper

To simplify the calculation of relative permeability from displacement data by using graphical constructions.

Methodology Used

1. Carried out unsteady state displacement with successive oil-flooding and water-flooding on a water saturated linear core to irreducible water saturation to determine water injection rates, pressure drop and effluent water.
2. Fractional flow of oil and water was measured in the effluent water from core displacement.
3. Average saturation and effective viscosity was computed using pressure rate and volumetric data from the core displacement.
4. Saturation at outlet and intercept viscosity graphically obtained from average saturation and effective viscosity were used to obtain oil and water relative permeabilities.

Conclusions Reached:

1. Graphical constructions can easily and accurately calculate relative permeabilities from unsteady state displacements using irreducible oil saturation and effective viscosity.
2. Waterflood displacements derived fractional flow curves concave downwards and do not give multiple values saturation.

Comments:

This new method provided is more practical using field data to calculate relative permeability from displacement data than the differential Johnson et al method.

The method involves rigorous and tedious tangent construction methods.

APPENDIX B

B.1 Rock Curves Correlation

We obtained our initial rock curves table of relative permeability of oil and water against water saturation using the power law relationships of relative permeability and water saturation to obtain Corey type correlations.

$$K_{ro} = 0.9 \left[\frac{S_o - 0.1}{1 - S_{wc} - S_{or}} \right]^4 \quad \text{for Oil Relative Permeability}$$

$$K_{rw} = 0.3 \left[\frac{S_w - 0.2}{1 - S_{wc} - S_{or}} \right]^3 \quad \text{for Water Relative Permeability}$$

K_{ro} and K_{rw} are the oil and water relative permeabilities. 0.9 and 0.3 are end point values of the oil and water relative permeabilities used. S_w and S_{wc} are the individual saturations in the rock table and connate water saturation respectively. 4 and 3 are Corey exponents for the oil and water phases. S_{or} is the residual oil saturation. Connate water and residual oil saturations used were 0.2 and 0.1 respectively. Relative permeability data was obtained for a given saturation table. A plot of oil and water relative permeability versus water saturation was done. Using an oil water viscosity ratio of 4 the fractional flow of water is calculated using equation 4. From fig 3 The fractional flow curve was plotted and the saturation at the shock front S_{wsh} of 0.598 was obtained using Welge constructon Method (Welge, 1952). The average saturation behind the shock front S_{wsh} of 0.656 was also obtained when f_w is 1. These data were documented in the rock curve table.

Figure B.1(a) Rock Curve Relative Permeability Plot

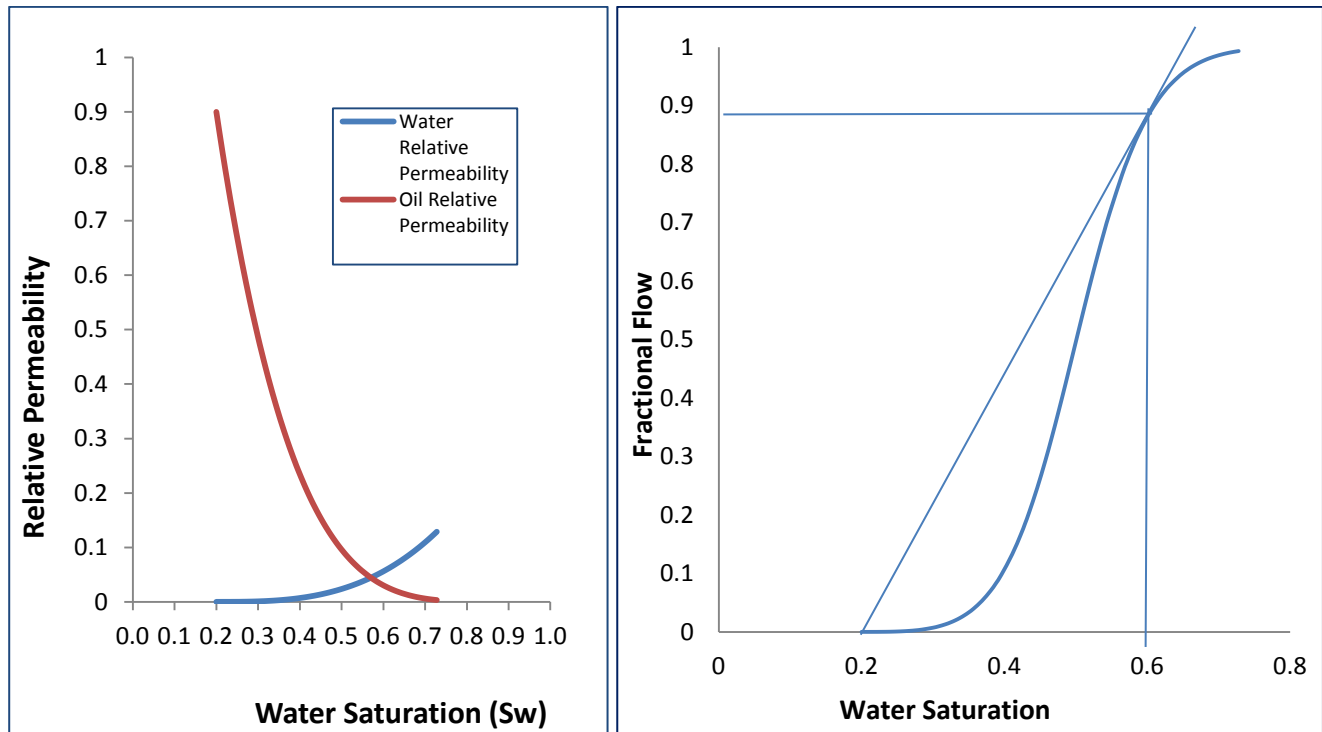


Figure B.1(b) Fractional Flow Plot

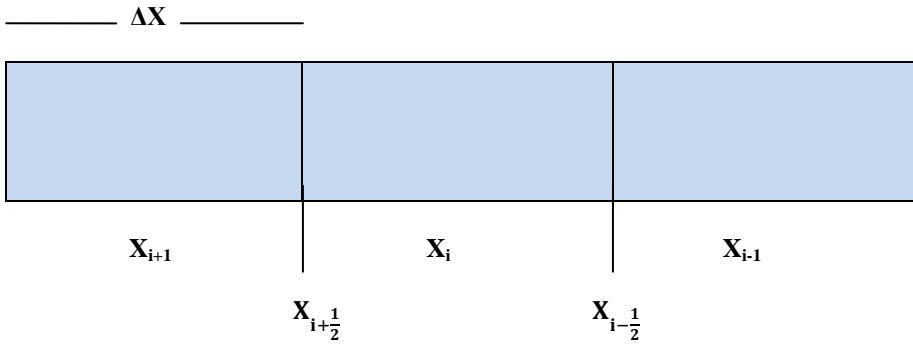
B.2 Analytic Equations For Formulation of Pseudo-relative permeability

Injector Wellblock Pseudos

Following the methodology by Muggerridge (private communication) Our one dimensional coarse grid system having incompressible immiscible displacement of oil by water in the horizontal X direction during a waterflood is defined below.

The notation of the gridblocks is as shown below. The size of each gridblock is given as ΔX .

Figure B.2 Coarse Gridblock System



The system is homogeneous and the oil and rock are assumed to be incompressible. With uniform water saturation distribution with distance and constant cross-sectional area within a gridblock of size Δx . The Darcy total flow through the porous system is following the derivation by Muggeridge (private communication) described the displacement of oil by water; with velocity of displacement $V_{i+1/2}$ through gridblock i is a function of the mobility of water and oil and occurs within the same pressure gradient for both.

$$V_{i+1/2} = -K_{i+1/2} \left(\frac{K_{rw}(S_w)}{\mu_w} + \frac{K_{ro}(S_o)}{\mu_o} \right) \frac{P_{i+1} - P_i}{\Delta x}$$

Where subscript $i + 1/2$ denotes the boundary between upstream block i and downstream block $i + 1$. $K_{i+1/2}$ is the absolute permeability at the gridblock boundary. $K_{rw}(S_w)$ and $K_{ro}(S_w)$ are the relative permeabilities of oil and water respectively. μ_w and μ_o represent the viscosities of water and oil respectively. P_{i+1} and P_i are the pressures between adjacent gridblocks

Now the velocity of flow between gridblock j and $j + 1$ is governed by the pressure gradient between them and a function of the distance averaged water saturation between the inlet face and outlet face of gridblock j . Combining equation 15 and 16 for flow for saturations less than the shock front saturation

$$P_j - P_{j+1} = \frac{V_{j+1/2}}{K_{j+1/2} \left(\frac{K_{rw}(S_w)}{\mu_w} + \frac{K_{ro}(S_w)}{\mu_o} \right)}$$

The size of the gridblock ΔX can be integrated from the inlet to the outlet of the gridblock j

$$\Delta X = \int_{x_{j-1/2}}^{x_{j+1/2}} dx$$

Combining equations 5, 6, 7, and 20 and defining a distance averaged modified oil mobility at the outlet face of the gridblock, equation 19 becomes

$$P_j - P_{j+1} = \frac{V_{j+1/2}}{K_{j+1/2} \Psi_o(S_w)}$$

Where S_{wf} is the shock front saturation and S_{wj} is the individual saturation from the rock curve table. From equation 5, 6 and 7 we maintain total mobility with the increase of the oil mobility for water saturations less than S_{wf} by adding the pseudo-water mobility and pseudo -oil mobility at water saturations less than the mean average saturation in the gridblock. Muggeridge (2007) showed that the pseudo oil mobility in gridblock i is

$$\frac{1}{\Psi_o(S_{wi})} = \frac{1}{\Delta X} \int_{x_{i+1/2}}^{x_{i+1/2}} \frac{dx}{\left(\frac{K_{rw}(S_{wi})}{\mu_w} + \frac{K_{ro}(S_{wi})}{\mu_o} \right)}$$

Similarly the pseudo-total mobility is given as

$$\frac{1}{\Psi_T(\overline{S_{wi}})} = \frac{1}{\Delta X} \int_{x_{i+\frac{1}{2}}}^{x_{i+\frac{1}{2}}} \frac{dx}{\left(\frac{Kr_w(S_{wi})}{\mu_w} + \frac{Kro(S_{wi})}{\mu_o} \right)}$$

Where $Kr_w(\overline{S_{wi}})$ and $Kro(\overline{S_{wi}})$ are water and oil relative permeability as a function of gridblock average saturation; μ_w and μ_o are oil and water viscosities; and ΔX is the gridblock size.

For water saturations higher than gridblock average water saturation in the rock table when the shock front reaches the outlet face of the gridblock the modified total mobility is obtained by equation 23.

She added that pseudo-water mobility is obtained by

$$\frac{\lambda_w}{\lambda_T} = \frac{\Psi_w(S_w)}{\Psi_T(S_w)}$$

Where λ_w and λ_T are the rock water and rock total mobilities and $\Psi_w(S_w)$ is the modified water mobility. We calculate water and oil pseudo-relative permeability by

$$Kr_{wp}(S_{wj}) = \Psi_w(S_{wj}) \times \mu_w \quad S_{wj} \geq \overline{S_{wf}}$$

$$Krop(S_w) = \mu_o \times (\Psi_T(S_w) - \Psi_w(S_w)) \quad S_{wf} \geq \overline{S_{wf}}$$

Approximating the saturation distance profile in fig 1 such that f_w tends to 1 in this gridblock, we replace our rock table water saturations by average water saturations obtained by Welge method. (Welge 1952, Dake 1988)

$$\overline{S_{wj}} = S_{wj} + \frac{1-f_w}{df_w/dS_w} \quad S_{wj} \geq \overline{S_{wf}}$$

where S_{wj} is the individual saturation in the rock curve table.

Non-Injector Wellblock Pseudofunctions

Following the derivation of Muggerridge (private communication) and using Hewitt et al (1998) information that the corrections required for calculating pseudofunctions does not depend on the size of the gridblock but on the ratio between the distance from the inlet face of the gridblock to the injection well and the distance from the injection well block to the outlet face of the gridblock in question and change in fractional flow across gridblock. He used characteristics velocity and distance in his work rather than saturation and fractional flow. (Hewitt et al, 1998). The corrections we usually apply would be to replace the point saturations with mean saturations within a particular gridblock. Now we assume that the average saturation within a gridblock i is calculated by obtaining the difference between average inlet face $\overline{S_{wi}}$ and outlet face $\overline{S_{wo}}$ saturations calculated from the injection wellblock over the simulation model. We refer to the appendix section for a derivation to show this assumption. In the discrete representations of tabulated relative permeability values as a function of tabulated water saturations with relatively constant interval ΔS_w in reservoir simulation models, the change in fractional flow at gridblock outlet face mean saturation S_{wo} is

$$\frac{df_w}{dS_w} = \frac{f_w(S_{wj}) - f_w(S_{wj-1})}{S_{wj} - S_{wj-1}}$$

Where S_{wj} and S_{wj-1} are tabulated saturation values, $S_{wj-1} < S_{wo} \leq S_{wj}$

Also for the mean inlet face gridblock saturation S_{wi}

$$\frac{df_w}{dS_w} = \frac{f_w(S_{wj}) - f_w(S_{wj-1})}{S_{wj} - S_{wj-1}}$$

Where $S_{wj-1} < S_{wi} \leq S_{wj}$

We can say that S_{wi} and S_{wo} are probably similar and infer that the saturation in a gridblock is uniform and we do not need to modify the saturations as in injector wellblock.

B.3

The Pseudo-total mobility and Pseudo-relative permeability plots calculated for the channels and layered reservoir model are presented below

Figure B.3 (a) Pseudo-total mobilites using JBN Rock Curves For Channel Model

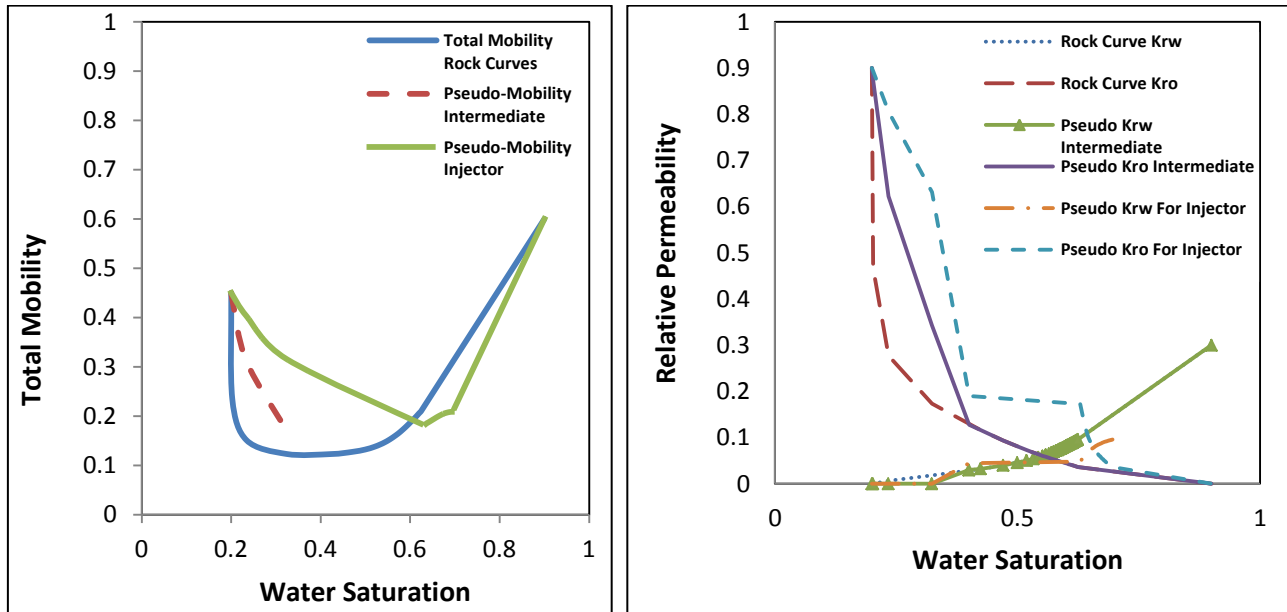


Figure B.3(b) Pseudo-relative Permeability and JBN Rock Curves for the Channel Model

Figure B.3 (c) Pseudo-total mobilites using JBN Rock Curves For Layered Model

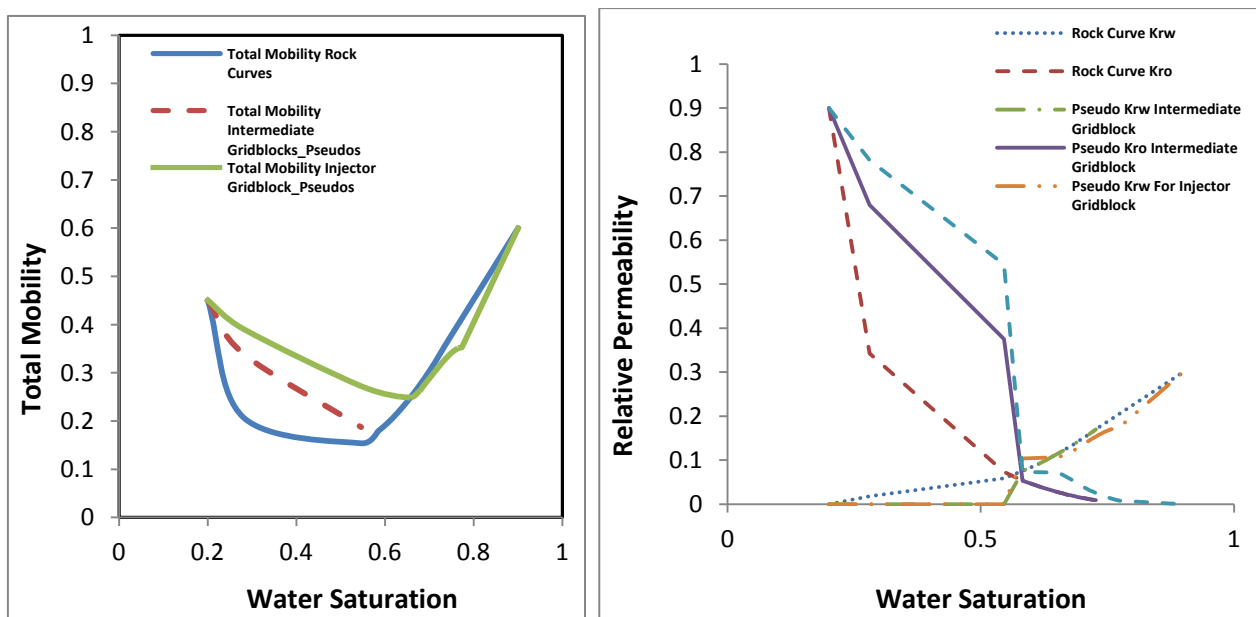
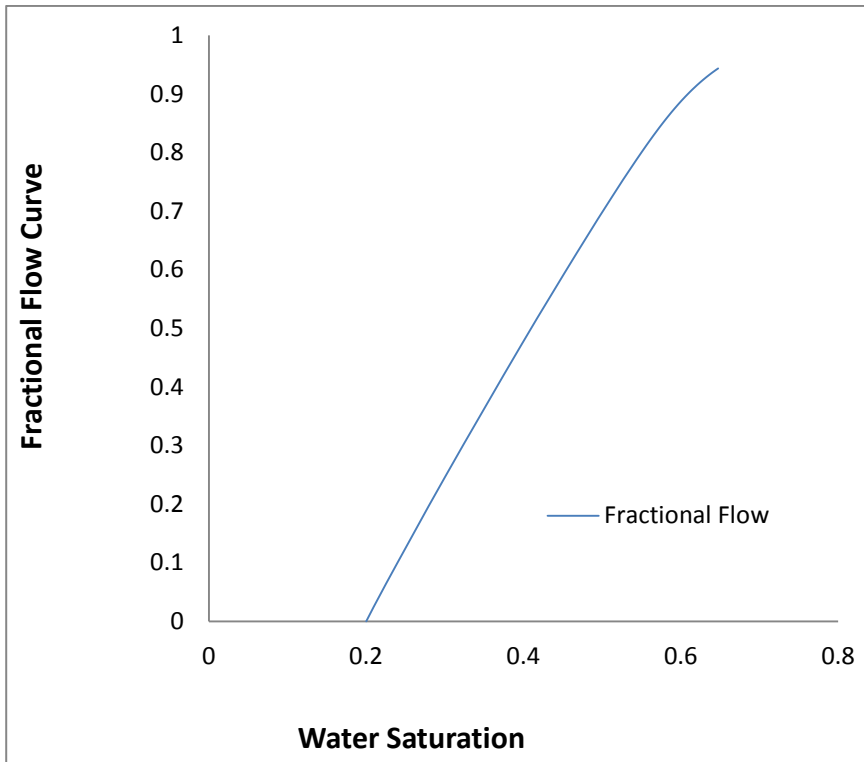


Figure 7(a) Pseudo-relative Permeability and JBN Rock Curves for the Layered Model

B.4

Figure B.4 Fractional flow curve of Effective Relative Permeability obtained using the JBN method. It showed a no shock characteristic shape. It does not give a favourable fractional flow curve.



Appendix C: SAMPLE SIMULATION DATA FILES

UPSCALING OF RELATIVE PERMEABILITY TO REDUCE NUMERICAL DISPERSION CODE INPUT DATAFILES

C1: 1D CODE INPUT

Fine Grid Model

RUNSPEC

TITLE

'REL PERM UPSCALING TO REDUCE NUMERICAL DISPERSION'

START

1 'AUG' 1975 /

DIMENS

-- nx ny nz

202 1 1 /

CART

NONNC

-- PHASES PRESENT

OIL

WATER

-- UNITS

FIELD

EQLDIMS

-- num num max max max

-- equ depth nodes tab tracer

-- reg nodes VD tab tracer nodes

1 100 1 1 20 /

TABDIMS

-- num num max max max

-- sat pvt sat press fip

-- tab tab nodes nodes regions

```

1 1 100 10 1 1 /

REGDIMS
1 1 0 0 /

WELLDIMS
2 1 1 2 /

EQLOPTS
MOBILE /

NSTACK
50 /

UNIFOUT

UNIFIN

FMTOUT

--
-- <----- PRINT -----> <----- STOP ----->
-- mess comm warn prob err bug mess comm warn prob err b
MESSAGES
2*      1000 5*          100000 2* /
--

GRID =====

EQUALS
DX      15 2 201 1 1 1 1 /
DX      15 1 1 1 1 1 1 /
DX      15 202 202 1 1 1 1 /
DY      2000 1 1 1 1 1 1 /
DY      2000 202 202 1 1 1 1 /
DY      2000 2 201 1 1 1 1 /
DZ      100 2 201 1 1 1 1 /
DZ      100 1 1 1 1 1 1 /
DZ      100 202 202 1 1 1 1 /
PORO    0.2 1 202 1 1 1 1 /
PERMX   200 2 201 1 1 1 1 /
PERMX   200 1 1 1 1 1 1 /
PERMX   200 202 202 1 1 1 1 /
PERMY   200 2 201 1 1 1 1 /
PERMY   200 1 1 1 1 1 1 /
PERMY   200 202 202 1 1 1 1 /
PERMZ   200 2 201 1 1 1 1 /
PERMZ   200 1 1 1 1 1 1 /
PERMZ   200 202 202 1 1 1 1 /
TOPS    0.0 1 202 1 1 1 1 /

```

```

/
RPTGRID
-- Report Levels for Grid Section Data

/
EDIT

PROPS =====
-- SECTION REPORTS DEF. OF REL. PERMEABILITIES, CAPILLARY PRESSRES AND PVT
-- PROPERTIES
-----

INCLUDE
'Fluid_Property_File.DATA' /

/

RPTPROPS
  'PVTW'
/

REGIONS =====
-- SECTION DEFINES HOW RESERVOIR IS SPLIT INTO REGIONS BY SATURATION FUNCTION,
-- PVT FUNCTION, FLUID IN PLACE ETC.

SOLUTION =====
----- SECTION DEFINES INITIAL STATE OF THE SOLUTION VARIABLES - PHASE
----- SATURATIONS AND GAS-OIL RATIO
-----

EQUIL

50.0 4000 2000 0 0 0 0 0 -2 /

RPTSOL
  'PRES' 'SWAT' 'SOIL' /

SUMMARY =====
----- SECTION SPECIFIES DATA TO BE WRITTEN TO SUMMARY FILES AND WHICH MAY
----- LATER BE USED WITH THE ECLIPSE GRAPHICS PACKAGE

FOPR

RPTONLY

WBHP
P /

WBHP

```

I/
 FLPT
 FOPT
 FOE
 FWIR
 FWCT
 FWIR
 FPR
 EXCEL
 RUNSUM

SCHEDULE =====
 ----- SECTION DEFINES THE OPERATIONS TO BE SIMULATED

WELSPECS

-- WELL GROUP LOCATION BHP PHASE
 -- NAME NAME I J DEPTH DEFN
 P 'G' 202 1 0.0 'OIL' /
 I 'G' 1 1 0.0 'WATER' /

/

COMPDAT

-- WELL LOCATION OPEN/ SAT CONN WELL
 -- NAME I J K1 K2 SHUT TABLE FACT ID

P ' 202 1 1 1 'OPEN' 1 1* 0.5 /

I ' 1 1 1 1 'OPEN' 1 1* 0.5 /

/

WCONPROD

P ' 'OPEN' 'LRAT' 3* 6500 1* 1110.0 /

/

WCONINJE

I ' 'WAT' 'OPEN' 'RATE' 6500 1* 8000 /

/

RPTSCHED

```
'PRES' 'SOIL' 'SWAT' 'RESTART= 1' 'CPU=2' 'NEWTON=2' /
```

```
RPTRST  
'BASIC=2' /
```

```
TSTEP  
60*100 /
```

```
END
```

G2: CODE INPUT DATA – 2D**Fine Grid**

```
RUNSPEC
TITLE
'REL PERM UPSCALING TO REDUCE NUMERICAL DISPERSION'

START
1 'AUG' 1975 /

DIMENS

-- nx ny nz

26 26 1 /

CART

NONNC

-- PHASES PRESENT

OIL

WATER

-- UNITS

FIELD

EQLDIMS

-- num num max max max
-- equ depth nodes tab tracer
-- reg nodes VD tab tracer nodes
1 100 1 1 20 /

TABDIMS

-- num num max max max
-- sat pvt sat press fip
-- tab tab nodes nodes regions

1 1 100 10 1 1 /

REGDIMS
1 1 0 0 /

WELLDIMS
2 1 1 2 /

EQLOPTS
MOBILE /

NSTACK
```

50 /

UNIFOUT

UNIFIN

FMTOUT

```
--
-- <----- PRINT -----> <----- STOP ----->
-- mess comm warn prob err bug mess comm warn prob err b
MESSAGES
  2*      1000 5*          100000 2* /
--
```

GRID =====

EQUALS

```
DX    150 1 26 1 26 1 1 /
DY    50 1 26 1 26 1 1 /
DZ    100 1 26 1 26 1 1 /
PORO  0.2 1 26 1 26 1 1 /
PERMX  400 1 26 1 26 1 1 /
PERMY  400 1 26 1 26 1 1 /
PERMZ  400 1 26 1 26 1 1 /
TOPS  0.0 1 26 1 26 1 1 /
```

/

RPTGRID
 -- Report Levels for Grid Section Data

/
 EDIT

PROPS =====
 -- SECTION REPORTS DEF. OF REL. PERMEABILITIES, CAPILLARY PRESSRES AND PVT
 -- PROPERTIES

INCLUDE
 'Fluid_Property_File.DATA' /

/

RPTPROPS
 'PVTW'

/
 REGIONS =====
 -- SECTION DEFINES HOW RESERVOIR IS SPLIT INTO REGIONS BY SATURATION FUNCTION,
 -- PVT FUNCTION, FLUID IN PLACE ETC.

SOLUTION =====
 ----- SECTION DEFINES INITIAL STATE OF THE SOLUTION VARIABLES - PHASE

----- SATURATIONS AND GAS-OIL RATIO

EQUIL

50.0 4000 2000 0 0 0 0 0 -2/

RPTSOL

'PRES' 'SWAT' 'SOIL' /

SUMMARY =====

----- SECTION SPECIFIES DATA TO BE WRITTEN TO SUMMARY FILES AND WHICH MAY
 ----- LATER BE USED WITH THE ECLIPSE GRAPHICS PACKAGE

FOPR

FOE

FWIR

FWCT

FPR

EXCEL

RUNSUM

SCHEDULE =====

----- SECTION DEFINES THE OPERATIONS TO BE SIMULATED

WELSPECS

```
-- WELL  GROUP LOCATION BHP PHASE
-- NAME  NAME  I  J  DEPTH DEFN
  P  'G' 26 1 0.0 'OIL' /
  I  'G' 1 26 0.0 'WATER' /
/
```

COMPDAT

```
-- WELL  LOCATION  OPEN/ SAT CONN WELL
-- NAME  I  J K1 K2 SHUT  TABLE FACT ID

  P  ' 26 1 1 1 'OPEN' 1 1* 0.5 /
  I  ' 1 26 1 1 'OPEN' 1 1* 0.5 /
/
```

WCONPROD

```
  P  ''OPEN' 'LRAT' 3* 7500 1* 1110.0 /
/
```

WCONINJE

```

I      'WAT' 'OPEN' 'RATE' 7500 1* 8000 /
/

RPTSCHED
'PRES' 'SOIL' 'SWAT' 'RESTART= 1' 'CPU=2' 'NEWTON=2' /

RPTRST
'BASIC=2' /

TUNING

1 100 0.1 0.15 3 0.3 0.1 1.25 0.75 /
0.1 0.001 1E-7 0.0001 10 0.01 1E-6 0.001 0.001 /
12 1 1000 1 8 8 4*1E6      /

TSTEP
40*100 /

END

```

C3: Code Input 2D Heterogeneous

Channel Model

```

RUNSPEC
TITLE
'REL PERM UPSCALING TO REDUCE NUMERICAL DISPERSION'

START
1 'AUG' 1975 /

DIMENS

-- nx ny nz

20 1 10 /

CART

NONNC

-- PHASES PRESENT

OIL

WATER

-- UNITS

FIELD

EQLDIMS

-- num num max max max
-- equ depth nodes tab tracer
-- reg nodes VD tab tracer nodes

```

```
1 100 1 1 20 /
```

TABDIMS

```
-- num num max max max
-- sat pvt sat press fip
-- tab tab nodes nodes regions
```

```
1 1 80 10 1 1 /
```

REGDIMS

```
1 1 0 0 /
```

WELLDIMS

```
2 10 1 2 /
```

EQLOPTS

```
MOBILE /
```

NSTACK

```
50 /
```

UNIFOUT

UNIFIN

FMTOUT

```
--
-- <----- PRINT -----> <----- STOP ----->
-- mess comm warn prob err bug mess comm warn prob err b
```

MESSAGES

```
2* 1000 5* 100000 2* /
```

```
GRID =====
```

EQUALS

```
DX 150 1 20 1 1 1 10 /
DY 1000 1 20 1 1 1 10 /
DZ 10 1 20 1 1 1 10 /
PORO 0.2 1 20 1 1 1 10 /
TOPS 0.0 1 20 1 1 1 1 /
```

```
/
```

```
INCLUDE -- Generated : Petrel
```

```
'Channel_Include_File.DATA' /
```

```
/
```

RPTGRID

```
-- Report Levels for Grid Section Data
```

/
EDIT

PROPS =====
-- SECTION REPORTS DEF. OF REL. PERMEABILITIES, CAPILLARY PRESSRES AND PVT
-- PROPERTIES

--
-- OIL WATER GAS
-- (LBS/FT3) (LBS/FT3) (LBS/FT3)
--

DENSITY

52.000 64.000 0.044 /

-- OIL PHASE PRES. OIL FVF OIL VISCOSITY
-- (PSIA) (RB/STB) (CP)
--

PVDO
1100 1.001 2.0
4000 1.000 2.0
8000 0.999 2.0

/
--
-- REF.PRES. FVF-WATER COMPRESSIBILITY VISCOSITY VISCOSIBILITY
-- (PSIA) (RB/STB) (1/PSI) (CP) (1/PSI)
--

PVTW

4000.0 1.0 3.03E-6 0.5000 0.0 /

-- REF.PRES ROCK-COMPRESSIBILITY
-- (PSIA) (1/PSI)
--

ROCK

4000.0 0.30E-05 /

SOF2

0.1000 0
0.1200 5.9975E-07
0.1300 3.03623E-06
0.1430 1.28152E-05
0.1550 3.43006E-05
0.1650 6.6912E-05
0.1880 0.000224792
0.2000 0.000374844
0.2150 0.000655604
0.2250 0.000915146
0.2330 0.001172889
0.2450 0.001656999
0.2600 0.002456576
0.2720 0.003280682
0.2850 0.004390735

0.3000	0.005997501
0.3125	0.007643391
0.3188	0.008583069
0.3250	0.009606837
0.3309	0.010654819
0.3368	0.011786291
0.3432	0.013102297
0.3543	0.015663694
0.3590	0.016867449
0.3685	0.01948173
0.3750	0.021437845
0.3813	0.023454192
0.3875	0.025609538
0.3950	0.028368995
0.4024	0.031345666
0.4122	0.035610818
0.4204	0.039477466
0.4285	0.043650764
0.4350	0.047209519
0.4521	0.057612199
0.4607	0.063415306
0.4692	0.069646151
0.4766	0.075400046
0.4840	0.08150331
0.4905	0.087163468
0.4970	0.093113441
0.5047	0.100550253
0.5098	0.105689583
0.5149	0.111023452
0.5250	0.122294259
0.5339	0.132864498
0.5428	0.14410558
0.5540	0.159247917
0.5652	0.175553371
0.5712	0.184708606
0.5771	0.194217346
0.5890	0.214331393
0.6043	0.242344951
0.6119	0.257339247
0.6195	0.273018802
0.6313	0.298682387
0.6431	0.326114088
0.6494	0.34157338
0.6558	0.357575895
0.6621	0.374134214
0.6684	0.391261059
0.6755	0.41103682
0.6825	0.431552929
0.6925	0.461959357
0.7000	0.485797584
0.7150	0.536229636
0.7250	0.571966271
0.7330	0.601818023
0.7450	0.648767682
0.7600	0.711256243
0.7720	0.764411904
0.7850	0.825301502
0.8000	0.900000000 /

--

-- WATER SAT WATER REL PERM
-- (Sw) (Krw)
--
SWFN

0.2000	0	0.0000
0.2150	2.9519E-06	0.0000
0.2280	0.0000192	0.0000
0.2400	5.59767E-05	0.0000
0.2550	0.000145517	0.0000
0.2670	0.000263058	0.0000
0.2750	0.000368987	0.0000
0.2850	0.000537136	0.0000
0.3000	0.000874636	0.0000
0.3075	0.001086557	0.0000
0.3175	0.001418864	0.0000
0.3246	0.00168989	0.0000
0.3316	0.001993402	0.0000
0.3379	0.00229486	0.0000
0.3443	0.002625274	0.0000
0.3506	0.002985972	0.0000
0.3569	0.003378283	0.0000
0.3687	0.004199256	0.0000
0.3805	0.0051435	0.0000
0.3881	0.005823267	0.0000
0.3958	0.006560432	0.0000
0.4110	0.008216266	0.0000
0.4229	0.009686287	0.0000
0.4289	0.010482862	0.0000
0.4348	0.011321955	0.0000
0.4460	0.013020644	0.0000
0.4572	0.014881271	0.0000
0.4661	0.016480173	0.0000
0.4750	0.018189687	0.0000
0.4852	0.020279034	0.0000
0.4902	0.021381176	0.0000
0.4953	0.022522546	0.0000
0.5030	0.024330723	0.0000
0.5095	0.025930393	0.0000
0.5160	0.027598685	0.0000
0.5234	0.029583338	0.0000
0.5308	0.031660928	0.0000
0.5394	0.034179893	0.0000
0.5479	0.036829042	0.0000
0.5650	0.042531013	0.0000
0.5715	0.044843922	0.0000
0.5797	0.047860513	0.0000
0.5878	0.051009439	0.0000
0.5976	0.05497513	0.0000
0.6051	0.058123672	0.0000
0.6125	0.061390192	0.0000
0.6188	0.064223149	0.0000
0.6250	0.067141946	0.0000
0.6315	0.070269932	0.0000
0.6410	0.0750141	0.0000
0.6458	0.077464227	0.0000
0.6569	0.083396538	0.0000
0.6632	0.086922616	0.0000
0.6691	0.090286628	0.0000
0.6750	0.093736334	0.0000

0.6813	0.097485352	0.0000
0.6875	0.101333022	0.0000
0.7000	0.109329446	0.0000
0.7150	0.119467238	0.0000
0.7280	0.128744564	0.0000
0.7400	0.137723615	0.0000
0.7550	0.14952234	0.0000
0.7670	0.1594323	0.0000
0.7750	0.166276421	0.0000
0.7850	0.175103462	0.0000
0.8000	0.188921283	0.0000
0.8120	0.200484777	0.0000
0.8350	0.223948579	0.0000
0.8450	0.234696319	0.0000
0.8570	0.248040869	0.0000
0.8700	0.263058017	0.0000
0.8800	0.275013411	0.0000
0.9000	0.30000000	0.0000

/

RPTPROPS
'PVTW'

/

REGIONS =====
 -- SECTION DEFINES HOW RESERVOIR IS SPLIT INTO REGIONS BY SATURATION FUNCTION,
 -- PVT FUNCTION, FLUID IN PLACE ETC.

SOLUTION =====
 ----- SECTION DEFINES INITIAL STATE OF THE SOLUTION VARIABLES - PHASE
 ----- SATURATIONS AND GAS-OIL RATIO

EQUIL

50.0 4000 2000 0 0 0 0 0 -2 /

RPTSOL
'PRES' 'SWAT' 'SOIL' /

SUMMARY =====
 ----- SECTION SPECIFIES DATA TO BE WRITTEN TO SUMMARY FILES AND WHICH MAY
 ----- LATER BE USED WITH THE ECLIPSE GRAPHICS PACKAGE

FOPR

FOPT

FOE

WBP

P /

WBP

I /

FWCT

FLPR

FLPT

FWIR

FPR

FVIT

FVPT

EXCEL

RUNSUM

SCHEDULE =====

----- SECTION DEFINES THE OPERATIONS TO BE SIMULATED

WELSPECS

-- WELL GROUP LOCATION BHP PHASE

-- NAME NAME I J DEPTH DEFN

P 'G' 20 1 0.0 'OIL' /

I 'G' 1 1 0.0 'WATER' /

/

COMPDAT

-- WELL LOCATION OPEN/ SAT CONN WELL

-- NAME I J K1 K2 SHUT TABLE FACT ID

P ' 20 1 1 10 'OPEN' 1 1* 0.5 /

I ' 1 1 1 10 'OPEN' 1 1* 0.5 /

/

WCONPROD

P ' 'OPEN' 'LRAT' 3* 1450 1* 1110.0 /

/

WCONINJE

I ' 'WAT' 'OPEN' 'RATE' 1450 1* 8000 /

/

WPAVE

1* 0.0 1* OPEN /

/

RPTSCHED

'PRES' 'SOIL' 'SWAT' 'RESTART= 1' 'CPU=2' 'NEWTON=2' /

RPTRST

'BASIC=2' /

TUNING

1 100 0.1 0.15 3 0.3 0.1 1.25 0.75 /

0.1 0.001 1E-7 0.0001 10 0.01 1E-6 0.001 0.001 /

12 1 1000 1 8 8 4*1E6 /

TSTEP
60*100 /

END

Layer Model

RUNSPEC
TITLE
'REL PERM UPSCALING TO REDUCE NUMERICAL DISPERSION'

START
1 'AUG' 1975 /

DIMENS

-- nx ny nz

20 1 10 /

CART

NONNC

-- PHASES PRESENT

OIL

WATER

-- UNITS

FIELD

EQLDIMS

-- num num max max max

-- equ depth nodes tab tracer

-- reg nodes VD tab tracer nodes

1 100 1 1 20 /

TABDIMS

-- num num max max max

-- sat pvt sat press fip

-- tab tab nodes nodes regions

1 1 80 10 1 1 /

REGDIMS

1 1 0 0 /

WELLDIMS

2 10 1 2 /

EQLOPTS

MOBILE /

NSTACK

50 /

UNIFOUT

UNIFIN

FMTOUT

```

--
-- <----- PRINT -----> <----- STOP ----->
-- mess comm warn prob err bug mess comm warn prob err b
MESSAGES
  2*      1000 5*          100000 2* /
--

```

GRID =====

EQUALS

```

DX      150 1 20 1 1 1 10 /
DY      1000 1 20 1 1 1 10 /
DZ      10 1 20 1 1 1 10 /
PORO    0.2 1 20 1 1 1 10 /
PERMX   50 1 20 1 1 1 1 /
PERMY   50 1 20 1 1 1 1 /
PERMZ   50 1 20 1 1 1 1 /
PERMX   100 1 20 1 1 1 2 /
PERMY   100 1 20 1 1 1 2 /
PERMZ   100 1 20 1 1 1 2 /
PERMX   150 1 20 1 1 1 3 /
PERMY   150 1 20 1 1 1 3 /
PERMZ   150 1 20 1 1 1 3 /
PERMX   200 1 20 1 1 1 4 /
PERMY   200 1 20 1 1 1 4 /
PERMZ   200 1 20 1 1 1 4 /
PERMX   250 1 20 1 1 1 5 /
PERMY   250 1 20 1 1 1 5 /
PERMZ   250 1 20 1 1 1 5 /
PERMX   300 1 20 1 1 1 6 /
PERMY   300 1 20 1 1 1 6 /
PERMZ   300 1 20 1 1 1 6 /
PERMX   350 1 20 1 1 1 7 /
PERMY   350 1 20 1 1 1 7 /
PERMZ   350 1 20 1 1 1 7 /
PERMX   400 1 20 1 1 1 8 /
PERMY   400 1 20 1 1 1 8 /
PERMZ   400 1 20 1 1 1 8 /
PERMX   450 1 20 1 1 1 9 /
PERMY   450 1 20 1 1 1 9 /
PERMZ   450 1 20 1 1 1 9 /
PERMX   500 1 20 1 1 1 10 /
PERMY   500 1 20 1 1 1 10 /
PERMZ   500 1 20 1 1 1 10 /
TOPS    0.0 1 20 1 1 1 1 /

```

/
RPTGRID

-- Report Levels for Grid Section Data

/
EDIT

PROPS =====
-- SECTION REPORTS DEF. OF REL. PERMEABILITIES, CAPILLARY PRESSRES AND PVT
-- PROPERTIES

--
-- OIL WATER GAS
-- (LBS/FT3) (LBS/FT3) (LBS/FT3)

--
DENSITY

52.000 64.000 0.044 /

--
-- OIL PHASE PRES. OIL FVF OIL VISCOSITY
-- (PSIA) (RB/STB) (CP)

--
PVDO

1100.0 1.001 2.0
4000.0 1.000 2.0
8000.0 0.999 2.0

/
--
-- REF.PRES. FVF-WATER COMPRESSIBILITY VISCOSITY VISCOSIBILITY
-- (PSIA) (RB/STB) (1/PSI) (CP) (1/PSI)

--
PVTW

4000.0 1.0 3.03E-6 0.5000 0.0 /

--
-- REF.PRES ROCK-COMPRESSIBILITY
-- (PSIA) (1/PSI)

--
ROCK

4000.0 .30E-05 /

--
SOF2

0.1000 0.00000000
0.1200 5.9975E-07
0.1300 3.03623E-06
0.1430 1.28152E-05
0.1550 3.43006E-05
0.1650 6.6912E-05
0.1880 0.000224792
0.2000 0.000374844
0.2150 0.000655604
0.2250 0.000915146
0.2330 0.001172889
0.2450 0.001656999
0.2600 0.002456576

0.2720	0.003280682
0.2850	0.004390735
0.3000	0.005997501
0.3125	0.007643391
0.3188	0.008583069
0.3250	0.009606837
0.3309	0.010654819
0.3368	0.011786291
0.3432	0.013102297
0.3543	0.015663694
0.3590	0.016867449
0.3685	0.01948173
0.3750	0.021437845
0.3813	0.023454192
0.3875	0.025609538
0.3950	0.028368995
0.4024	0.031345666
0.4122	0.035610818
0.4204	0.039477466
0.4285	0.043650764
0.4350	0.047209519
0.4521	0.057612199
0.4607	0.063415306
0.4692	0.069646151
0.4766	0.075400046
0.4840	0.08150331
0.4905	0.087163468
0.4970	0.093113441
0.5047	0.100550253
0.5098	0.105689583
0.5149	0.111023452
0.5250	0.122294259
0.5339	0.132864498
0.5428	0.14410558
0.5540	0.159247917
0.5652	0.175553371
0.5712	0.184708606
0.5771	0.194217346
0.5890	0.214331393
0.6043	0.242344951
0.6119	0.257339247
0.6195	0.273018802
0.6313	0.298682387
0.6431	0.326114088
0.6494	0.34157338
0.6558	0.357575895
0.6621	0.374134214
0.6684	0.391261059
0.6755	0.41103682
0.6825	0.431552929
0.6925	0.461959357
0.7000	0.485797584
0.7150	0.536229636
0.7250	0.571966271
0.7330	0.601818023
0.7450	0.648767682
0.7600	0.711256243
0.7720	0.764411904
0.7850	0.825301502
0.8000	0.900000000 /

--
-- WATER SAT WATER REL PERM
-- (Sw) (Krw)

--
SWFN

0.2000	0.0000000	0.0000
0.2150	2.9519E-06	0.0000
0.2280	0.0000192	0.0000
0.2400	5.59767E-05	0.0000
0.2550	0.000145517	0.0000
0.2670	0.000263058	0.0000
0.2750	0.000368987	0.0000
0.2850	0.000537136	0.0000
0.3000	0.000874636	0.0000
0.3075	0.001086557	0.0000
0.3175	0.001418864	0.0000
0.3246	0.00168989	0.0000
0.3316	0.001993402	0.0000
0.3379	0.00229486	0.0000
0.3443	0.002625274	0.0000
0.3506	0.002985972	0.0000
0.3569	0.003378283	0.0000
0.3687	0.004199256	0.0000
0.3805	0.0051435	0.0000
0.3881	0.005823267	0.0000
0.3958	0.006560432	0.0000
0.4110	0.008216266	0.0000
0.4229	0.009686287	0.0000
0.4289	0.010482862	0.0000
0.4348	0.011321955	0.0000
0.4460	0.013020644	0.0000
0.4572	0.014881271	0.0000
0.4661	0.016480173	0.0000
0.4750	0.018189687	0.0000
0.4852	0.020279034	0.0000
0.4902	0.021381176	0.0000
0.4953	0.022522546	0.0000
0.5030	0.024330723	0.0000
0.5095	0.025930393	0.0000
0.5160	0.027598685	0.0000
0.5234	0.029583338	0.0000
0.5308	0.031660928	0.0000
0.5394	0.034179893	0.0000
0.5479	0.036829042	0.0000
0.5650	0.042531013	0.0000
0.5715	0.044843922	0.0000
0.5797	0.047860513	0.0000
0.5878	0.051009439	0.0000
0.5976	0.05497513	0.0000
0.6051	0.058123672	0.0000
0.6125	0.061390192	0.0000
0.6188	0.064223149	0.0000
0.6250	0.067141946	0.0000
0.6315	0.070269932	0.0000
0.6410	0.0750141	0.0000
0.6458	0.077464227	0.0000
0.6569	0.083396538	0.0000
0.6632	0.086922616	0.0000

0.6691	0.090286628	0.0000
0.6750	0.093736334	0.0000
0.6813	0.097485352	0.0000
0.6875	0.101333022	0.0000
0.7000	0.109329446	0.0000
0.7150	0.119467238	0.0000
0.7280	0.128744564	0.0000
0.7400	0.137723615	0.0000
0.7550	0.149522234	0.0000
0.7670	0.1594323	0.0000
0.7750	0.166276421	0.0000
0.7850	0.175103462	0.0000
0.8000	0.188921283	0.0000
0.8120	0.200484777	0.0000
0.8350	0.223948579	0.0000
0.8450	0.234696319	0.0000
0.8570	0.248040869	0.0000
0.8700	0.263058017	0.0000
0.8800	0.275013411	0.0000
0.9000	0.30000000	0.0000 /

/
RPTPROPS
'PVTW'

/
REGIONS =====
-- SECTION DEFINES HOW RESERVOIR IS SPLIT INTO REGIONS BY SATURATION FUNCTION,
-- PVT FUNCTION, FLUID IN PLACE ETC.

SOLUTION =====
----- SECTION DEFINES INITIAL STATE OF THE SOLUTION VARIABLES - PHASE
----- SATURATIONS AND GAS-OIL RATIO

EQUIL
50.0 4000 2000 0 0 0 0 0 -2 /

RPTSOL
'PRES' 'SWAT' 'SOIL' /

SUMMARY =====
----- SECTION SPECIFIES DATA TO BE WRITTEN TO SUMMARY FILES AND WHICH MAY
----- LATER BE USED WITH THE ECLIPSE GRAPHICS PACKAGE

RPTONLY

FOPR

FOPT

FOE

WBP

P /

WBP

I/

FWCT

FLPR

FLPT

FWIR

FPR

FVIT

FVPT

EXCEL

RUNSUM

SCHEDULE =====
 ----- SECTION DEFINES THE OPERATIONS TO BE SIMULATED

WELSPECS

-- WELL GROUP LOCATION BHP PHASE

-- NAME NAME I J DEPTH DEFN

P 'G' 20 1 0.0 'OIL' /

I 'G' 1 1 0.0 'WATER' /

/

COMPDAT

-- WELL LOCATION OPEN/ SAT CONN WELL

-- NAME I J K1 K2 SHUT TABLE FACT ID

P ' 20 1 1 10 'OPEN' 1 1* 0.5 /

I ' 1 1 1 10 'OPEN' 1 1* 0.5 /

/

WCONPROD

P ' 'OPEN' 'LRAT' 3* 9800 1* 1110.0 /

/

WCONINJE

I ' 'WAT' 'OPEN' 'RATE' 9800 1* 8000 /

/

WPAVE

1* 0.0 1* OPEN /

/

RPTSCHED

'PRES' 'SOIL' 'SWAT' 'RESTART= 1' 'CPU=2' 'NEWTON=2' /

RPTRST

'BASIC=2' /

TUNING

1 100 0.1 0.15 3 0.3 0.1 1.25 0.75 /
 0.1 0.001 1E-7 0.0001 10 0.01 1E-6 0.001 0.001 /
 12 1 1000 1 8 8 4*1E6 /

TSTEP

40*100 /

Random Permeability Model

RUNSPEC

TITLE

'REL PERM UPSCALING TO REDUCE NUMERICAL DISPERSION'

START

1 'AUG' 1975 /

DIMENS

-- nx ny nz

20 1 10 /

CART

NONNC

-- PHASES PRESENT

OIL

WATER

-- UNITS

FIELD

EQLDIMS

-- num num max max max

-- equ depth nodes tab tracer

-- reg nodes VD tab tracer nodes

1 100 1 1 20 /

TABDIMS

-- num num max max max

-- sat pvt sat press fip

-- tab tab nodes nodes regions

1 1 80 10 1 1 /

REGDIMS

1 1 0 0 /

WELLDIMS

2 10 1 2 /

EQLOPTS

MOBILE /

NSTACK

50 /

UNIFOUT

UNIFIN

FMTOUT

--

-- <----- PRINT -----> <----- STOP ----->

-- mess comm warn prob err bug mess comm warn prob err b

MESSAGES

2* 1000 5* 100000 2* /

--

GRID =====

EQUALS

DX 150 1 20 1 1 1 10 /

DY 1000 1 20 1 1 1 10 /

DZ 10 1 20 1 1 1 10 /

PORO 0.2 1 20 1 1 1 10 /

TOPS 0.0 1 20 1 1 1 1 /

/

INCLUDE

'Incude_Random_Perm.DATA' /

/

RPTGRID

-- Report Levels for Grid Section Data

/

EDIT

PROPS =====

-- SECTION REPORTS DEF. OF REL. PERMEABILITIES, CAPILLARY PRESSRES AND PVT

-- PROPERTIES

-- OIL WATER GAS

-- (LBS/FT3) (LBS/FT3) (LBS/FT3)

--

DENSITY

52.000 64.000 0.044 /

--

-- OIL PHASE PRES. OIL FVF OIL VISCOSITY

-- (PSIA) (RB/STB) (CP)

--

PVDO

1100	1.001	2.0
4000	1.000	2.0
8000	0.999	2.0

/

--

-- REF.PRES. FVF-WATER COMPRESSIBILITY VISCOSITY VISCOSIBILITY

-- (PSIA) (RB/STB) (1/PSI) (CP) (1/PSI)

--

PVTW

4000.0 1.0 3.03E-6 0.5000 0.0 /

--

--

-- REF.PRES ROCK-COMPRESSIBILITY

-- (PSIA) (1/PSI)

--

ROCK

4000.0 .30E-05 /

--

--

SOF2

0.1000 0

0.1200 5.9975E-07

0.1300 3.03623E-06

0.1430 1.28152E-05

0.1550 3.43006E-05

0.1650 6.6912E-05

0.1880 0.000224792

0.2000 0.000374844

0.2150 0.000655604

0.2250 0.000915146

0.2330 0.001172889

0.2450 0.001656999

0.2600 0.002456576

0.2720 0.003280682

0.2850 0.004390735

0.3000 0.005997501

0.3125 0.007643391

0.3188 0.008583069

0.3250 0.009606837

0.3309 0.010654819

0.3368 0.011786291

0.3432 0.013102297

0.3543 0.015663694

0.3590 0.016867449

0.3685 0.01948173

0.3750 0.021437845

0.3813 0.023454192

0.3875 0.025609538

0.3950 0.028368995

0.4024 0.031345666

0.4122 0.035610818

0.4204 0.039477466

0.4285 0.043650764
 0.4350 0.047209519
 0.4521 0.057612199
 0.4607 0.063415306
 0.4692 0.069646151
 0.4766 0.075400046
 0.4840 0.08150331
 0.4905 0.087163468
 0.4970 0.093113441
 0.5047 0.100550253
 0.5098 0.105689583
 0.5149 0.111023452
 0.5250 0.122294259
 0.5339 0.132864498
 0.5428 0.14410558
 0.5540 0.159247917
 0.5652 0.175553371
 0.5712 0.184708606
 0.5771 0.194217346
 0.5890 0.214331393
 0.6043 0.242344951
 0.6119 0.257339247
 0.6195 0.273018802
 0.6313 0.298682387
 0.6431 0.326114088
 0.6494 0.34157338
 0.6558 0.357575895
 0.6621 0.374134214
 0.6684 0.391261059
 0.6755 0.41103682
 0.6825 0.431552929
 0.6925 0.461959357
 0.7000 0.485797584
 0.7150 0.536229636
 0.7250 0.571966271
 0.7330 0.601818023
 0.7450 0.648767682
 0.7600 0.711256243
 0.7720 0.764411904
 0.7850 0.825301502
 0.8000 0.900000000 /

--
 -- WATER SAT WATER REL PERM
 -- (Sw) (Krw)

--
 SWFN

0.2000 0 0.0000
 0.2150 2.9519E-06 0.0000
 0.2280 0.0000192 0.0000
 0.2400 5.59767E-05 0.0000
 0.2550 0.000145517 0.0000
 0.2670 0.000263058 0.0000
 0.2750 0.000368987 0.0000
 0.2850 0.000537136 0.0000
 0.3000 0.000874636 0.0000
 0.3075 0.001086557 0.0000
 0.3175 0.001418864 0.0000
 0.3246 0.00168989 0.0000

0.3316	0.001993402	0.0000
0.3379	0.00229486	0.0000
0.3443	0.002625274	0.0000
0.3506	0.002985972	0.0000
0.3569	0.003378283	0.0000
0.3687	0.004199256	0.0000
0.3805	0.0051435	0.0000
0.3881	0.005823267	0.0000
0.3958	0.006560432	0.0000
0.4110	0.008216266	0.0000
0.4229	0.009686287	0.0000
0.4289	0.010482862	0.0000
0.4348	0.011321955	0.0000
0.4460	0.013020644	0.0000
0.4572	0.014881271	0.0000
0.4661	0.016480173	0.0000
0.4750	0.018189687	0.0000
0.4852	0.020279034	0.0000
0.4902	0.021381176	0.0000
0.4953	0.022522546	0.0000
0.5030	0.024330723	0.0000
0.5095	0.025930393	0.0000
0.5160	0.027598685	0.0000
0.5234	0.029583338	0.0000
0.5308	0.031660928	0.0000
0.5394	0.034179893	0.0000
0.5479	0.036829042	0.0000
0.5650	0.042531013	0.0000
0.5715	0.044843922	0.0000
0.5797	0.047860513	0.0000
0.5878	0.051009439	0.0000
0.5976	0.05497513	0.0000
0.6051	0.058123672	0.0000
0.6125	0.061390192	0.0000
0.6188	0.064223149	0.0000
0.6250	0.067141946	0.0000
0.6315	0.070269932	0.0000
0.6410	0.0750141	0.0000
0.6458	0.077464227	0.0000
0.6569	0.083396538	0.0000
0.6632	0.086922616	0.0000
0.6691	0.090286628	0.0000
0.6750	0.093736334	0.0000
0.6813	0.097485352	0.0000
0.6875	0.101333022	0.0000
0.7000	0.109329446	0.0000
0.7150	0.119467238	0.0000
0.7280	0.128744564	0.0000
0.7400	0.137723615	0.0000
0.7550	0.14952234	0.0000
0.7670	0.1594323	0.0000
0.7750	0.166276421	0.0000
0.7850	0.175103462	0.0000
0.8000	0.188921283	0.0000
0.8120	0.200484777	0.0000
0.8350	0.223948579	0.0000
0.8450	0.234696319	0.0000
0.8570	0.248040869	0.0000
0.8700	0.263058017	0.0000
0.8800	0.275013411	0.0000

0.9000 0.30000000 0.0000 /

/
RPTPROPS
'PVTW'

/
REGIONS =====
-- SECTION DEFINES HOW RESERVOIR IS SPLIT INTO REGIONS BY SATURATION FUNCTION,
-- PVT FUNCTION, FLUID IN PLACE ETC.

SOLUTION =====
----- SECTION DEFINES INITIAL STATE OF THE SOLUTION VARIABLES - PHASE
----- SATURATIONS AND GAS-OIL RATIO

EQUIL

50 4000 2000 0 0 0 0 0 -2/

RPTSOL
'PRES' 'SWAT' 'SOIL' /

SUMMARY =====
----- SECTION SPECIFIES DATA TO BE WRITTEN TO SUMMARY FILES AND WHICH MAY
----- LATER BE USED WITH THE ECLIPSE GRAPHICS PACKAGE

RPTONLY

FOPR

FOPT

FOE

WBP
P /

WBP
I /

FWCT

FLPR

FLPT

FWIR

FPR
FVIT
FVPT

EXCEL

RUNSUM

SCHEDULE =====
 ----- SECTION DEFINES THE OPERATIONS TO BE SIMULATED

WELSPECS

```
-- WELL  GROUP LOCATION BHP PHASE
-- NAME  NAME  I  J  DEPTH DEFN
  P   'G'  20  1  0.0 'OIL' /
  I   'G'   1  1  0.0 'WATER' /
```

COMPDAT

```
-- WELL  LOCATION  OPEN/ SAT  CONN WELL
-- NAME  I  J K1 K2 SHUT  TABLE FACT ID
```

```
  P   '  20  1  1  10 'OPEN' 1  1* 0.5 /
  I   '  1  1  1  10 'OPEN' 1  1* 0.5 /
```

WCONPROD

```
  P   ' 'OPEN' 'LRAT' 3* 2000 1* 1110.0 /
```

WCONINJE

```
  I   ' 'WAT' 'OPEN' 'RATE' 2000 1* 8000 /
```

WPAVE

```
1* 0.0 1* OPEN /
```

RPTSCHED

```
'PRES' 'SOIL' 'SWAT' 'RESTART= 1' 'CPU=2' 'NEWTON=2' /
```

RPTRST

```
'BASIC=2' /
```

TUNING

```
1 100 0.1 0.15 3 0.3 0.1 1.25 0.75 /
0.1 0.001 1E-7 0.0001 10 0.01 1E-6 0.001 0.001 /
12 1 1000 1 8 8 4*1E6 /
```

TSTEP

```
60*100 /
```

END

Appendix D

Table D1 Pseudo-Relative and Pseudo-Mobility Calculation

1D Pseudos

Intermediate Gridblock

Rock Curves Table			Pseudo Relative Permeability Table			Rock Curve Mobility				Pseudo-Mobility	
Sw	Krw	kro	SW	KRW	KRO	λ_o	λ_w	λ_t	λ^{-1}		
0.2	0	0.9	0.2	0	0.9000	0.4500	0.0000	0.4500	2.2222	Loj	1/Loj
0.215	2.95E-06	0.825302	0.215	0	0.8204	0.4127	0.0000	0.4127	2.4233	0.4500	2.2222
0.228	1.92E-05	0.764412	0.228	0	0.7620	0.3822	0.0000	0.3822	2.6161	0.4102	2.4379
0.24	5.6E-05	0.711256	0.24	0	0.7150	0.3556	0.0001	0.3557	2.8110	0.3810	2.6248
0.255	0.000146	0.648768	0.255	0	0.6638	0.3244	0.0003	0.3247	3.0800	0.3575	2.7973
0.267	0.000263	0.601818	0.267	0	0.6278	0.3009	0.0005	0.3014	3.3175	0.3319	3.0130
0.275	0.000369	0.571966	0.275	0	0.6060	0.2860	0.0007	0.2867	3.4877	0.3139	3.1855
0.285	0.000537	0.53623	0.285	0	0.5807	0.2681	0.0011	0.2692	3.7149	0.3030	3.3005
0.3	0.000875	0.485798	0.3	0	0.5464	0.2429	0.0017	0.2446	4.0875	0.2903	3.4443
0.3075	0.001087	0.461959	0.308	0	0.5308	0.2310	0.0022	0.2332	4.2890	0.2732	3.6600
0.3175	0.001419	0.431553	0.318	0	0.5113	0.2158	0.0028	0.2186	4.5743	0.2654	3.7678
0.3246	0.001692	0.410894	0.325	0	0.4983	0.2054	0.0034	0.2088	4.7886	0.2556	3.9116
0.3316	0.001993	0.391261	0.332	0	0.4861	0.1956	0.0040	0.1996	5.0096	0.2491	4.0137
0.3379	0.002294	0.374201	0.338	0	0.4756	0.1871	0.0046	0.1917	5.2168	0.2431	4.1143
0.3443	0.002628	0.357447	0.344	0	0.4654	0.1787	0.0053	0.1840	5.4354	0.2378	4.2049
0.3506	0.002987	0.341511	0.351	0	0.4558	0.1708	0.0060	0.1767	5.6583	0.2327	4.2969
0.3569	0.003378	0.326114	0.357	0	0.4466	0.1631	0.0068	0.1698	5.8888	0.2279	4.3875
0.3687	0.004199	0.298682	0.369	0	0.4303	0.1493	0.0084	0.1577	6.3396	0.2233	4.4781
0.3805	0.005144	0.273019	0.381	0	0.4152	0.1365	0.0103	0.1468	6.8122	0.2152	4.6477
0.3881	0.005821	0.25739	0.388	0	0.4060	0.1287	0.0116	0.1403	7.1257	0.2076	4.8174
0.3958	0.006565	0.242249	0.396	0	0.3970	0.1211	0.0131	0.1343	7.4485	0.2030	4.9267
0.411	0.008216	0.214331	0.411	0	0.3805	0.1072	0.0164	0.1236	8.0907	0.1985	5.0374
0.4229	0.009686	0.194217	0.423	0	0.3685	0.0971	0.0194	0.1165	8.5851	0.1903	5.2559
0.4289	0.01049	0.18463	0.429	0	0.3628	0.0923	0.0210	0.1133	8.8265	0.1843	5.4270
0.4348	0.011322	0.175553	0.435	0	0.3573	0.0878	0.0226	0.1104	9.0563	0.1814	5.5133
0.446	0.013021	0.159248	0.446	0	0.3473	0.0796	0.0260	0.1057	9.4638	0.1786	5.5981
0.4572	0.014881	0.144106	0.457	0	0.3378	0.0721	0.0298	0.1018	9.8217	0.1736	5.7591
0.4661	0.01648	0.132864	0.466	0	0.3307	0.0664	0.0330	0.0994	10.0611	0.1689	5.9202
0.475	0.01819	0.122294	0.475	0	0.3238	0.0611	0.0364	0.0975	10.2536	0.1653	6.0481
0.4852	0.02029	0.11097	0.485	0	0.3163	0.0555	0.0406	0.0961	10.4097	0.1619	6.1761
0.4902	0.021376	0.105715	0.49	0	0.3128	0.0529	0.0428	0.0956	10.4593	0.1582	6.3227
0.4953	0.022523	0.10055	0.495	0	0.3092	0.0503	0.0450	0.0953	10.4910	0.1564	6.3946
0.503	0.024331	0.093113	0.503	0	0.3040	0.0466	0.0487	0.0952	10.5022	0.1546	6.4680
0.5095	0.02593	0.087163	0.51	0	0.2998	0.0436	0.0519	0.0954	10.4775	0.1520	6.5787
0.516	0.027599	0.081503	0.516	0	0.2956	0.0408	0.0552	0.0959	10.4222	0.1499	6.6721

0.5234	0.029583	0.0754	0.523	0	0.2910	0.0377	0.0592	0.0969	10.3235	0.1478	6.7656
0.5308	0.031661	0.069646	0.531	0	0.2866	0.0348	0.0633	0.0981	10.1890	0.1455	6.8720
0.5394	0.034195	0.06338	0.539	0	0.2816	0.0317	0.0684	0.1001	9.9920	0.1433	6.9784
0.5479	0.036829	0.057612	0.548	0	0.2768	0.0288	0.0737	0.1025	9.7595	0.1408	7.1020
0.565	0.042531	0.04721	0.565	0	0.2677	0.0236	0.0851	0.1087	9.2024	0.1384	7.2242
0.5715	0.044844	0.043651	0.572	0	0.2644	0.0218	0.0897	0.1115	8.9675	0.1339	7.4701
0.5797	0.047879	0.039453	0.58	0	0.2604	0.0197	0.0958	0.1155	8.6591	0.1322	7.5635
0.5878	0.051009	0.035611	0.588	0	0.2565	0.0178	0.1020	0.1198	8.3456	0.1302	7.6814
0.5976	0.054975	0.031346	0.598	0	0.2519	0.0157	0.1100	0.1256	7.9603	0.1282	7.7979
0.6051	0.058145	0.02835	0.605	0.058	0.0283	0.0142	0.1163	0.1305	7.6649	0.1260	7.9388
0.6125	0.06139	0.02561	0.613	0.061	0.0256	0.0128	0.1228	0.1356	7.3754	0.1243	8.0466
0.6188	0.064246	0.023438	0.619	0.064	0.0234	0.0117	0.1285	0.1402	7.1321	0.1228	
0.625	0.067142	0.021438	0.625	0.067	0.0214	0.0107	0.1343	0.1450	6.8964	0.1285	
0.6315	0.07027	0.019482	0.632	0.07	0.0195	0.0097	0.1405	0.1503	6.6542	0.1343	
0.6458	0.07749	0.015651	0.646	0.077	0.0157	0.0078	0.1550	0.1628	6.1423	0.1405	
0.6569	0.083424	0.013092	0.657	0.083	0.0131	0.0065	0.1668	0.1734	5.7672	0.1628	
0.6632	0.086923	0.011786	0.663	0.087	0.0118	0.0059	0.1738	0.1797	5.5636	0.1734	
0.6691	0.090287	0.010655	0.669	0.09	0.0107	0.0053	0.1806	0.1859	5.3792	0.1797	
0.675	0.093736	0.009607	0.675	0.094	0.0096	0.0048	0.1875	0.1923	5.2009	0.1859	
0.6813	0.097516	0.008575	0.681	0.098	0.0086	0.0043	0.1950	0.1993	5.0171	0.1923	
0.6875	0.101333	0.007643	0.688	0.101	0.0076	0.0038	0.2027	0.2065	4.8429	0.1993	
0.7	0.109329	0.005998	0.7	0.109	0.0060	0.0030	0.2187	0.2217	4.5115	0.2065	
0.715	0.119467	0.004391	0.715	0.119	0.0044	0.0022	0.2389	0.2411	4.1471	0.2217	
0.728	0.128745	0.003281	0.728	0.129	0.0033	0.0016	0.2575	0.2591	3.8591	0.2411	
0.74	0.137724	0.002457	0.74	0.138	0.0025	0.0012	0.2754	0.2767	3.6143	0.2591	
0.755	0.149522	0.001657	0.755	0.15	0.0017	0.0008	0.2990	0.2999	3.3347	0.2767	
0.767	0.159432	0.001173	0.767	0.159	0.0012	0.0006	0.3189	0.3195	3.1304	0.2999	
0.775	0.166276	0.000915	0.775	0.166	0.0009	0.0005	0.3326	0.3330	3.0029	0.3195	
0.785	0.175103	0.000656	0.785	0.175	0.0007	0.0003	0.3502	0.3505	2.8528	0.3330	
0.8	0.188921	0.000375	0.8	0.189	0.0004	0.0002	0.3778	0.3780	2.6453	0.3505	
0.812	0.200485	0.000225	0.812	0.2	0.0002	0.0001	0.4010	0.4011	2.4933	0.3780	
0.835	0.223949	6.69E-05	0.835	0.224	0.0001	0.0000	0.4479	0.4479	2.2325	0.4011	
0.845	0.234696	3.43E-05	0.845	0.235	0.0000	0.0000	0.4694	0.4694	2.1303	0.4479	
0.857	0.248041	1.28E-05	0.857	0.248	0.0000	0.0000	0.4961	0.4961	2.0158	0.4694	
0.87	0.263058	3.04E-06	0.87	0.263	0.0000	0.0000	0.5261	0.5261	1.9007	0.4961	
0.88	0.275013	6E-07	0.88	0.275	0.0000	0.0000	0.5500	0.5500	1.8181	0.5261	
0.9	0.3	0	0.9	0.3	0.0000	0.0000	0.6000	0.6000	1.6667	0.5500	
0.598	0.055141	0.03118	0.598	0.055	0.0312	0.0156	0.1103	0.1259	7.9445	0.6000	
										0.1259	Swf
0.656	0.082932	0.013286	0.656	0.083	0.0133	0.0066	0.1659	0.1725	5.7969		
										0.1725	Swf(avg)

Injector Gridblock

Pseudo Function Table			Rock Mobility				Pseudo Oil Mobility			
SW	KRW	KRO	λ_o	λ_w	λ_t	$\lambda-1$	Lwj	Loj	1/Loj	LTj
0.2000	0.0000	0.9000	0.4500	0.0000	0.4500	2.2222	0.000000	0.450000	2.2222	0.4500
0.2150	0.0000	0.8465	0.4127	0.0000	0.4127	2.4233	0.000000	0.423239	2.3627	0.4232
0.2280	0.0000	0.8050	0.3822	0.0000	0.3822	2.6161	0.000000	0.402495	2.4845	0.4025
0.2400	0.0000	0.7701	0.3556	0.0001	0.3557	2.8110	0.000000	0.385073	2.5969	0.3851
0.2550	0.0000	0.7306	0.3244	0.0003	0.3247	3.0800	0.000000	0.365308	2.7374	0.3653
0.2670	0.0000	0.7018	0.3009	0.0005	0.3014	3.3175	0.000000	0.350899	2.8498	0.3509
0.2750	0.0000	0.6838	0.2860	0.0007	0.2867	3.4877	0.000000	0.341909	2.9248	0.3419
0.2850	0.0000	0.6626	0.2681	0.0011	0.2692	3.7149	0.000000	0.331298	3.0184	0.3313
0.3000	0.0000	0.6331	0.2429	0.0017	0.2446	4.0875	0.000000	0.316562	3.1589	0.3166
0.3075	0.0000	0.6194	0.2310	0.0022	0.2332	4.2890	0.000000	0.309675	3.2292	0.3097
0.3175	0.0000	0.6019	0.2158	0.0028	0.2186	4.5743	0.000000	0.300946	3.3229	0.3009
0.3246	0.0000	0.5901	0.2054	0.0034	0.2088	4.7886	0.000000	0.295040	3.3894	0.2950
0.3316	0.0000	0.5789	0.1956	0.0040	0.1996	5.0096	0.000000	0.289441	3.4549	0.2894
0.3379	0.0000	0.5692	0.1871	0.0046	0.1917	5.2168	0.000000	0.284580	3.5140	0.2846
0.3443	0.0000	0.5596	0.1787	0.0053	0.1840	5.4354	0.000000	0.279806	3.5739	0.2798
0.3506	0.0000	0.5505	0.1708	0.0060	0.1767	5.6583	0.000000	0.275261	3.6329	0.2753
0.3569	0.0000	0.5417	0.1631	0.0068	0.1698	5.8888	0.000000	0.270861	3.6919	0.2709
0.3687	0.0000	0.5260	0.1493	0.0084	0.1577	6.3396	0.000000	0.262988	3.8025	0.2630
0.3805	0.0000	0.5111	0.1365	0.0103	0.1468	6.8122	0.000000	0.255559	3.9130	0.2556
0.3881	0.0000	0.5020	0.1287	0.0116	0.1403	7.1257	0.000000	0.250993	3.9842	0.2510
0.3958	0.0000	0.4931	0.1211	0.0131	0.1343	7.4485	0.000000	0.246530	4.0563	0.2465
0.4110	0.0000	0.4763	0.1072	0.0164	0.1236	8.0907	0.000000	0.238170	4.1987	0.2382
0.4229	0.0000	0.4640	0.0971	0.0194	0.1165	8.5851	0.000000	0.232010	4.3102	0.2320
0.4289	0.0000	0.4580	0.0923	0.0210	0.1133	8.8265	0.000000	0.229024	4.3664	0.2290
0.4348	0.0000	0.4523	0.0878	0.0226	0.1104	9.0563	0.000000	0.226161	4.4216	0.2262
0.4460	0.0000	0.4418	0.0796	0.0260	0.1057	9.4638	0.000000	0.220919	4.5265	0.2209
0.4572	0.0000	0.4318	0.0721	0.0298	0.1018	9.8217	0.000000	0.215915	4.6314	0.2159
0.4661	0.0000	0.4242	0.0664	0.0330	0.0994	10.0611	0.000000	0.212097	4.7148	0.2121
0.4750	0.0000	0.4168	0.0611	0.0364	0.0975	10.2536	0.000000	0.208412	4.7982	0.2084
0.4852	0.0000	0.4087	0.0555	0.0406	0.0961	10.4097	0.000000	0.204343	4.8937	0.2043
0.4902	0.0000	0.4048	0.0529	0.0428	0.0956	10.4593	0.000000	0.202406	4.9406	0.2024
0.4953	0.0000	0.4009	0.0503	0.0450	0.0953	10.4910	0.000000	0.200468	4.9883	0.2005
0.5030	0.0000	0.3952	0.0466	0.0487	0.0952	10.5022	0.000000	0.197610	5.0605	0.1976
0.5095	0.0000	0.3905	0.0436	0.0519	0.0954	10.4775	0.000000	0.195261	5.1214	0.1953
0.5160	0.0000	0.3859	0.0408	0.0552	0.0959	10.4222	0.000000	0.192967	5.1822	0.1930
0.5234	0.0000	0.3808	0.0377	0.0592	0.0969	10.3235	0.000000	0.190420	5.2516	0.1904
0.5308	0.0000	0.3759	0.0348	0.0633	0.0981	10.1890	0.000000	0.187939	5.3209	0.1879
0.5394	0.0000	0.3703	0.0317	0.0684	0.1001	9.9920	0.000000	0.185136	5.4014	0.1851
0.5479	0.0000	0.3649	0.0288	0.0737	0.1025	9.7595	0.000000	0.182447	5.4810	0.1824
0.5650	0.0000	0.3545	0.0236	0.0851	0.1087	9.2024	0.000000	0.177266	5.6412	0.1773

0.5715	0.0000	0.3507	0.0218	0.0897	0.1115	8.9675	0.000000	0.175374	5.7021	0.1754
0.5797	0.0000	0.3461	0.0197	0.0958	0.1155	8.6591	0.000000	0.173043	5.7789	0.1730
0.5878	0.0000	0.3416	0.0178	0.1020	0.1198	8.3456	0.000000	0.170800	5.8548	0.1708
0.5976	0.0000	0.3363	0.0157	0.1100	0.1256	7.9603	0.000000	0.168163	5.9466	0.1682
0.6452	0.0735	0.0358	0.0142	0.1163	0.1305	7.6649	0.147011	0.017919		0.1649
0.6617	0.0770	0.0321	0.0128	0.1228	0.1356	7.3754	0.153977	0.016058		0.1700
0.6673	0.0801	0.0292	0.0117	0.1285	0.1402	7.1321	0.160172	0.014608		0.1748
0.6725	0.0832	0.0266	0.0107	0.1343	0.1450	6.8964	0.166458	0.013287		0.1797
0.6778	0.0882	0.0244	0.0097	0.1405	0.1503	6.6542	0.176368	0.012224		0.1886
0.6868	0.0961	0.0194	0.0078	0.1550	0.1628	6.1423	0.192287	0.009709		0.2020
0.6975	0.1016	0.0159	0.0065	0.1668	0.1734	5.7672	0.203157	0.007970		0.2111
0.7048	0.1050	0.0142	0.0059	0.1738	0.1797	5.5636	0.209939	0.007117		0.2171
0.7100	0.1082	0.0128	0.0053	0.1806	0.1859	5.3792	0.216393	0.006384		0.2228
0.7151	0.1115	0.0114	0.0048	0.1875	0.1923	5.2009	0.222999	0.005714		0.2287
0.7203	0.1149	0.0101	0.0043	0.1950	0.1993	5.0171	0.229770	0.005051		0.2348
0.7257	0.1198	0.0090	0.0038	0.2027	0.2065	4.8429	0.239697	0.004520		0.2442
0.7340	0.1287	0.0071	0.0030	0.2187	0.2217	4.5115	0.257401	0.003530		0.2609
0.7459	0.1387	0.0051	0.0022	0.2389	0.2411	4.1471	0.277330	0.002548		0.2799
0.7577	0.1475	0.0038	0.0016	0.2575	0.2591	3.8591	0.294903	0.001879		0.2968
0.7682	0.1571	0.0028	0.0012	0.2754	0.2767	3.6143	0.314164	0.001401		0.3156
0.7797	0.1679	0.0019	0.0008	0.2990	0.2999	3.3347	0.335783	0.000930		0.3367
0.7908	0.1753	0.0013	0.0006	0.3189	0.3195	3.1304	0.350678	0.000645		0.3513
0.7988	0.1811	0.0010	0.0005	0.3326	0.3330	3.0029	0.362226	0.000498		0.3627
0.8063	0.1896	0.0007	0.0003	0.3502	0.3505	2.8528	0.379252	0.000355		0.3796
0.8169	0.2002	0.0004	0.0002	0.3778	0.3780	2.6453	0.400358	0.000199		0.4006
0.8276	0.2130	0.0002	0.0001	0.4010	0.4011	2.4933	0.426090	0.000119		0.4262
0.8434	0.2327	0.0001	0.0000	0.4479	0.4479	2.2325	0.465304	0.000035		0.4653
0.8546	0.2415	0.0000	0.0000	0.4694	0.4694	2.1303	0.482934	0.000018		0.4830
0.8636	0.2528	0.0000	0.0000	0.4961	0.4961	2.0158	0.505566	0.000007		0.5056
0.8737	0.2644	0.0000	0.0000	0.5261	0.5261	1.9007	0.528794	0.000002		0.5288
0.8823	0.2750	0.0000	0.0000	0.5500	0.5500	1.8181	0.550027	0.000000		0.5500
0.9000	0.3000	0.0000	0.0000	0.6000	0.6000	1.6667	0.600000	0.000000		0.6000

Table D2 Relative Permeability Calculation (JBN Method)

Channels

Total Water Injected	Total Oil	Delta Pressure	Pore Volume of Water Injected	Pore Volume of Oil Produced	Average saturation	Effective Viscosity	Intercept Saturation	Intercept Effective Viscosity	fo	fw	Kro	Krw
0	0	0	0	0	0.2	2	0.2	4				
15000	149999	1126.5	0.0140	0.0140	0.214036	2.250		2.0258		5E-	0.987	1.3E-
0	.9	02	37	36	5	85	0.2	68	1	07	23	07
30000	299999		0.0280	0.0280		2.475		2.1690		6E-	0.922	1.4E-
0	.8	1239.1	73	73	0.228073	83	0.2	3	1	07	07	07
45000	449999	1315.8	0.0421	0.0421	0.242109	2.629		2.2456		4E-	0.890	8.9E-
0	.8	73	1	09	5	23	0.2	95	1	07	59	08
60000	599999	1379.8	0.0561	0.0561		2.757		2.2554		9E-	0.886	1.9E-
0	.7	56	46	46	0.256146	07	0.2	04	1	07	76	07
75000	749999	1442.6	0.0701	0.0701	0.270182	2.882		2.3263		4E-	0.859	8.6E-
0	.6	24	83	82	49	49	0.2	47	1	07	72	08
90000	899999	1498.2	0.0842	0.0842	0.284218	2.993		2.3344		7E-	0.856	1.4E-
0	.5	91	19	19	99	71	0.2	5	1	07	73	07
10500	104999	1553.2	0.0982	0.0982	0.298255	3.103		2.3872		7E-	0.837	1.4E-
00	9	83	56	55	49	59	0.2	33	1	07	79	07
12000	119999		0.1122	0.1122	0.312291	3.205	0.19999	2.4098		2E-	0.829	4.1E-
00	9	1604.5	92	92	98	93	99	29	1	15	93	16
13500	134999	1654.3	0.1263	0.1263	0.326328	3.305	0.20000	2.3151		1E-	0.863	2.9E-
00	9	04	29	28	49	44	01	71	1	06	87	07
15000	149999	1709.3	0.1403	0.1403	0.340364	3.415		2.2680		7E-	0.881	1.5E-
00	9	72	65	65	98	47	0.2	16	1	07	83	07
16500	164999	1766.7	0.1544	0.1544	0.354401	3.530		2.3771		7E-	0.841	1.4E-
00	9	99	02	01	47	22	0.2	48	1	07	34	07
18000	179999	1819.2	0.1684	0.1684	0.368437	3.635		2.4237		7E-	0.825	1.4E-
00	9	62	38	38	97	04	0.2	74	1	07	16	07
19500	194999	1869.7	0.1824	0.1824	0.382474	3.735	0.20000	2.7180		2E-	0.735	3.7E-
00	9	8	75	74	47	98	03	64	1	06	82	07
21000	209999	1908.9	0.1965	0.1965	0.396510	3.814	0.19999	2.6801		2E-	0.746	3.7E-
00	9	68	11	11	95	28	99	91	1	15	22	16
22500	224999	1949.5	0.2105	0.2105	0.410547	3.895	0.20000	2.8631		1E-	0.698	2.3E-
00	9	1	48	47	45	29	01	96	1	06	52	07
24000	239999	1983.9	0.2245	0.2245	0.424583	3.964	0.19999	2.7413			0.729	
00	8	46	84	84	94	09	98	23	1	0	57	0
25500	254999	2022.1	0.2386	0.2386	0.438620	4.040	0.20000	2.9935		2E-	0.668	3.3E-
00	8	94	21	2	45	52	03	21	1	06	11	07
27000	269999	2053.0	0.2526	0.2526	0.452656	4.102	0.20000	3.2018		1E-	0.624	2.1E-
00	8	17	57	57	92	1	01	65	1	06	64	07
28500	284999	2078.0	0.2666	0.2666	0.466693	4.152	0.19999	2.8028			0.713	
00	8	48	94	93	41	12	98	91	1	0	55	0
30000	299999	2113.5	0.2807	0.2807	0.480729	4.223	0.20000	2.8130		2E-	0.710	3.6E-
00	8	88	3	3	92	13	04	85	1	06	96	07
31500	314999	2148.8	0.2947	0.2947	0.494766	4.293	0.20000	2.6100		2E-	0.766	3.8E-
00	8	73	67	66	4	63	04	87	1	06	26	07
33000	329999	2188.9	0.3088	0.3088	0.508802	4.373	0.19999	2.3180			0.862	
00	7	96	03	03	87	8	95	84	1	-0	78	-1E-07

34500	344999	2235.7	0.3228	0.3228	0.522839	4.467	0.20000	1.9448		2E-	1.028	5.1E-
00	7	61	4	39	39	24	04	48	1	06	36	07
36000	359999	2290.6	0.3368	0.3368	0.536875	4.576	0.20000	1.9833		1E-	1.008	3.4E-
00	7	48	76	76	87	91	02	98	1	06	37	07
37500	374999	2344.7	0.3509	0.3509	0.550912	4.684	0.20000	2.0443		2E-	0.978	4.9E-
00	7	32	13	12	35	98	04	75	1	06	29	07
39000	389999	2397.5	0.3649	0.3649	0.564948	4.790	0.20000	2.3112		1E-	0.865	2.9E-
00	7	94	49	49	83	6	02	38	1	06	34	07
40500	404999	2445.3	0.3789	0.3789	0.578985	4.885	0.20001	2.7569		4E-	0.725	6.4E-
00	6	2	86	85	32	96	3	59	1	05	41	06
42000	419999	2484.7	0.3930	0.3930	0.593021	4.964	0.20228	4.2545	0.9	0.00	0.467	0.000
00	1	84	22	21	33	81	92	55	9	6	35	68
43500	434911	2497.4	0.4070	0.4069	0.606976	4.990	0.23396	6.6093	0.9	0.08	0.277	0.006
00	7	79	59	76	05	18	38	32	2	4	29	33
45000	448657	2469.5	0.4210	0.4198	0.619838	4.934	0.32372	8.1215		0.29	0.173	0.018
00	1	36	95	39	54	34	3	99	0.7	7	17	27
46500	459205	2416.3	0.4351	0.4297	0.629709	4.828	0.42350	8.1293	0.4	0.52	0.116	0.032
00	2	64	32	09	06	1	89	66	7	6	58	36
48000	466313	2363.0	0.4491	0.4363	0.636360	4.721	0.47037	7.8497	0.3		0.094	0.040
00	4	67	68	61	68	61	66	3	7	0.63	15	16
49500	471856	2314.1	0.4632	0.4415	0.641547	4.623	0.49952	7.5652	0.3	0.69	0.081	0.045
00	4	43	05	48	68	86	6	39	1	3	06	83
51000	476455	2269.5	0.4772	0.4458	0.645851	4.534	0.51882	7.2808	0.2	0.73	0.073	0.050
00	5	34	41	51	37	72	89	02	7	4	11	4
52500	480447	2229.1	0.4912	0.4495	0.649587	4.453	0.53258	7.0302	0.2	0.76	0.067	0.054
00	9	12	78	87	33	96	79	95	4	2	75	18
54000	484020	2192.2	0.5053	0.4529	0.652930	4.380	0.54310	6.8130	0.2	0.78	0.063	0.057
00	2	72	14	3	17	35	52	06	2	3	8	44
55500	487280	2158.4	0.5193	0.4559	0.655980	4.312	0.55154	6.6190		0.79	0.060	0.060
00	3	52	51	81	86	77	64	16	0.2	9	76	35
57000	490296	2127.2	0.5333	0.4588	0.658803	4.250	0.55858	6.4462	0.1	0.81	0.058	0.062
00	6	57	87	03	42	44	17	51	9	2	3	99
58500	493115	2098.3	0.5474	0.4614	0.661440	4.192	0.56462	6.2932	0.1	0.82	0.056	0.065
00	1	37	24	41	83	66	71	44	8	3	2	4
60000	495767	2071.3	0.5614	0.4639	0.663923	4.138	0.56996	6.1576	0.1	0.83	0.054	0.067
00	9	81	6	23	23	8	66	38	7	3	35	61
61500	498278	2046.1	0.5754	0.4662	0.666272	4.088	0.57475	6.0342	0.1	0.84	0.052	0.069
00	0	21	97	72	15	33	86	65	6	1	7	68
63000	500663	2022.3	0.5895	0.4685	0.668504	4.040	0.57911	5.9162	0.1	0.84	0.051	0.071
00	3	67	33	04	19	86	52	74	5	8	26	7
64500	502937	2000.0	0.6035	0.4706	0.670632	3.996	0.58312	5.8057	0.1	0.85	0.049	0.073
00	7	2	7	32	49	21	49	58	4	5	94	64
66000	505112	1978.9	0.6176	0.4726	0.672667	3.954	0.58683	5.7054	0.1	0.86	0.048	0.075
00	4	58	06	68	55	13	68	72	4	1	72	46
67500	507197	1959.0	0.6316	0.4746	0.674618	3.914	0.59029	5.6119	0.1	0.86	0.047	0.077
00	0	38	43	18	25	33	82	08	3	7	58	2
69000	509199	1940.1	0.6456	0.4764	0.676492	3.876	0.59356	5.5225	0.1	0.87	0.046	0.078
00	4	58	79	92	03	6	1	79	3	2	51	91
70500	511126	1922.2	0.6597	0.4782	0.678294	3.840	0.59665	5.4400	0.1	0.87	0.045	0.080
00	0	49	16	95	88	82	07	69	2	6	5	54
72000	512982	1905.2	0.6737	0.4800	0.680031	3.806	0.59956	5.3618	0.1	0.88	0.044	0.082
00	4	2	52	32	99	79	58	85	2	1	55	11
73500	514773	1889.0	0.6877	0.4817	0.681708	3.774	0.60233	5.2885	0.1	0.88	0.043	0.083
00	8	05	89	08	37	39	3	83	2	5	64	63
75000	516504	1873.5	0.7018	0.4833	0.683328	3.743	0.60497	5.2254	0.1	0.88	0.042	
00	9	4	25	28	28	49	65	23	1	8	73	0.085

76500	518179	1858.7	0.7158	0.4848	0.684895	3.713	0.60751	5.1647	0.1	0.89	0.041	0.086
00	5	06	62	95	32	85	78	5	1	2	86	35
78000	519800	1844.4	0.7298	0.4864	0.686412	3.685	0.60995	5.1072	0.1	0.89	0.041	0.087
00	9	68	98	13	52	41	32	31	5	5	02	65
79500	521372	1830.7	0.7439	0.4878	0.687882	3.658	0.61228	5.0487	0.1	0.89	0.040	0.088
00	2	84	35	83	89	06	42	43	8	8	26	97
81000	522896	1817.6	0.7579	0.4893	0.689309	3.631	0.61453	4.9928	0.1	0.90	0.039	0.090
00	5	51	71	09	28	82	04	96	1	1	52	26
82500	524376	1805.0	0.7720	0.4906	0.690694	3.606	0.61667	4.9397	0.1	0.90	0.038	0.091
00	3	37	08	94	08	62	65	62	4	4	82	51
84000	525814	1792.9	0.7860	0.4920	0.692039	3.582	0.61875	4.8880	0.0	0.90	0.038	0.092
00	5	06	44	4	85	38	17	67	9	7	15	75
85500	527213	1781.2	0.8000	0.4933	0.693348	3.559	0.62077	4.8423	0.0	0.90	0.037	0.093
00	0	37	81	49	57	06	06	29	9	9	47	89
87000	528573	1769.9	0.8141	0.4946	0.694621	3.536	0.62272	4.8020	0.0	0.91	0.036	0.094
00	7	69	17	22	87	55	17	46	9	2	78	93
88500	529898	1759.0	0.8281	0.4958	0.695861	3.514	0.62460	4.7557	0.0	0.91	0.036	0.096
00	5	49	54	62	52	73	16	16	9	4	19	09
90000	531189	1748.5	0.8421	0.4970	0.697069	3.493			0.8	0.17		
00	2	22	9	69	32	7	0	0	3	2	0	0.3

Table D3: Layer Model

Time (days)	Total Water Injected	Total Oil Produced	Delta Pressure	Pore Volume of Water Injected	Pore Volume of Oil Produced	Average saturation	Effective Viscosity	Intercept Saturation	Intercept Effective Viscosity	fo	fw	Kro	Krw
0	0	0	4000	0	0	0.2	6.57	0.2	6.57	##	###	#DIV/0!	#DIV/0!
100	98000	97999	1834.07	0.091705	0.0917	0.29	3.01	0.2	2.42	1	0	0.8252	2E-07
200	196000	195999	2192.95	0.18341	0.1834	0.38	3.6	0.2	2.62	1	0	0.7628	2E-07
300	294000	293999	2491.41	0.275116	0.2751	0.48	4.09	0.2	2.82	1	0	0.7094	2E-07
400	392000	391999	2749.88	0.366821	0.3668	0.57	4.52	0.26	4.82	0.8	0.17	0.3427	0.0181
500	490000	472883	2704.36	0.458526	0.4425	0.64	4.44	0.53	6.5	0.2	0.76	0.0736	0.0586
600	588000	496319	2454.29	0.550231	0.4644	0.66	4.03	0.59	5.56	0.1	0.86	0.0518	0.0769
700	686000	510448	2299.04	0.641936	0.4777	0.68	3.78	0.61	5.03	0.1	0.89	0.0427	0.0887
800	784000	520960	2189.97	0.733641	0.4875	0.69	3.6	0.62	4.74	0.1	0.91	0.0378	0.0961
900	882000	529731	2103.19	0.825347	0.4957	0.7	3.46	0.63	4.51	0.1	0.92	0.0349	0.1024
1000	980000	537235	2031.92	0.917052	0.5027	0.7	3.34	0.64	4.32	0.1	0.93	0.0309	0.1079
1100	1078000	543774	1971.97	1.008757	0.5088	0.71	3.24	0.65	4.17	0.1	0.94	0.0283	0.1129
1200	1176000	549553	1920.69	1.100462	0.5143	0.71	3.16	0.66	4.03	0.1	0.95	0.0261	0.1174

1300	12740 000	55472 16	1876. 12	1.1921 67	0.5191	0.72	3.08	0.66	3.92	0	0.95	0.024 3	0.121 6
1400	13720 000	55938 32	1837. 01	1.2838 72	0.5235	0.72	3.02	0.67	3.82	0	0.96	0.022 6	0.125 4
1500	14700 000	56361 74	1802. 3	1.3755 78	0.5274	0.73	2.96	0.67	3.73	0	0.96	0.021 2	0.128 8
1600	15680 000	56749 01	1771. 21	1.4672 83	0.531	0.73	2.91	0.68	3.65	0	0.96	0.019 9	0.132 2
1700	16660 000	57105 16	1743. 22	1.5589 88	0.5344	0.73	2.86	0.68	3.57	0	0.97	0.018 8	0.135 2
1800	17640 000	57434 09	1717. 8	1.6506 93	0.5374	0.74	2.82	0.69	3.51	0	0.97	0.017 7	0.138
1900	18620 000	57739 30	1694. 55	1.7423 98	0.5403	0.74	2.78	0.69	3.45	0	0.97	0.016 8	0.140 7
2000	19600 000	58023 83	1673. 19	1.8341 03	0.543	0.74	2.75	0.69	3.4	0	0.97	0.016 2	0.143
2100	20580 000	58290 05	1653. 5	1.9258 09	0.5455	0.75	2.72	0.7	3.35	0	0.97	0.015 2	0.145 6
2200	21560 000	58539 80	1635. 26	2.0175 14	0.5478	0.75	2.69	0.7	3.3	0	0.98	0.014 5	0.147 9
2300	22540 000	58774 81	1618. 28	2.1092 19	0.55	0.75	2.66	0.7	3.26	0	0.98	0.013 9	0.15
2400	23520 000	58996 74	1602. 43	2.2009 24	0.5521	0.75	2.63	0.7	3.22	0	0.98	0.013 3	0.152 1
2500	24500 000	59206 77	1587. 61	2.2926 29	0.554	0.75	2.61	0.71	3.18	0	0.98	0.012 8	0.154 1
2600	25480 000	59405 95	1573. 71	2.3843 35	0.5559	0.76	2.59	0.71	3.14	0	0.98	0.012 3	0.155 9
2700	26460 000	59595 22	1560. 62	2.4760 4	0.5577	0.76	2.56	0.71	3.11	0	0.98	0.011 8	0.157 7
2800	27440 000	59775 35	1548. 25	2.5677 45	0.5594	0.76	2.54	0.71	3.08	0	0.98	0.011 4	0.159 4
2900	28420 000	59947 27	1536. 54	2.6594 5	0.561	0.76	2.52	0.72	3.05	0	0.98	0.011 1	0.161 1
3000	29400 000	60111 54	1525. 49	2.7511 55	0.5625	0.76	2.51	0.72	3.02	0	0.98	0.010 6	0.162 8
3100	30380 000	60268 74	1515. 03	2.8428 6	0.564	0.76	2.49	0.72	2.99	0	0.98	0.010 3	0.164 4
3200	31360 000	60419 25	1505. 1	2.9345 66	0.5654	0.77	2.47	0.72	2.97	0	0.99	0.009 9	0.165 9
3300	32340 000	60563 55	1495. 67	3.0262 71	0.5667	0.77	2.46	0.72	2.94	0	0.99	0.009 6	0.167 4
3400	33320 000	60702 00	1486. 67	3.1179 76	0.568	0.77	2.44	0.73	2.92	0	0.99	0.009 3	0.168 8
3500	34300 000	60835 03	1478. 1	3.2096 81	0.5693	0.77	2.43	0.73	2.9	0	0.99	0.009	0.170 1
3600	35280 000	60962 96	1469. 89	3.3013 86	0.5705	0.77	2.41	0.73	2.88	0	0.99	0.008 7	0.171 4
3700	36260 000	61086 21	1462. 01	3.3930 91	0.5716	0.77	2.4	0.73	2.86	0	0.99	0.008 5	0.172 6
3800	37240 000	61205 13	1454. 45	3.4847 97	0.5727	0.77	2.39	0.73	2.84	0	0.99	0.008 2	0.173 9
3900	38220 000	61319 98	1447. 2	3.5765 02	0.5738	0.77	2.38	0.73	2.82	0	0.99	0.008	0.175
4000	39200 000	61431 00	1440. 23	3.6682 07	0.5749	0.77	2.37	0.9	0	-0	1.03	#DIV/ 0!	#DIV/ 0!

Table D5 – Pseudo-Relative Permeability Calculation

Channels Model

Intermediate Gridblock

Rock Curves Table			Pseudo Relative Permeability Table			Rock Curve Mobility				Pseudo Mobility		
Sw	Krw	kro	SW	KRW	KRO	λ_o	λ_w	λ_t	$\lambda-1$	L wj	Loj	1/Loj
0.2	0	0.9	0.2	0	0.9	0.45	0	0.45	2.2222 222	0	0.45	2.2222 222
0.2022 892	0.0006 848	0.4673 454	0.2022 892	0 0	0.8737 088	0.2336 727	0.0013 695	0.2350 422	4.2545 546	0	0.4368 544	2.2890 922
0.2339 638	0.0063 274	0.2772 928	0.2339 638	0 0	0.6222 091	0.1386 464	0.0126 548	0.1513 012	6.6093 316	0	0.3111 045	3.2143 536
0.3237 23	0.0182 721	0.1731 687	0.3237 23	0 0	0.3426 798	0.0865 843	0.0365 441	0.1231 285	8.1215 988	0	0.1713 399	5.8363 53
0.4235 089	0.0323 592	0.1165 847	0.4235 089	0.0323 592	0.1165 847	0.0582 924	0.0647 185	0.1230 108	8.1293 661		0.0582 924	
0.4703 766	0.0401 583	0.0941 527	0.4703 766	0.0401 583	0.0941 527	0.0470 764	0.0803 166	0.1273 929	7.8497 3		0.0470 764	
0.4995 26	0.0458 276	0.0810 567	0.4995 26	0.0458 276	0.0810 567	0.0405 284	0.0916 552	0.1321 835	7.5652 39		0.0405 284	
0.5188 289	0.0503 955	0.0731 128	0.5188 289	0.0503 955	0.0731 128	0.0365 564	0.1007 911	0.1373 475	7.2808 023		0.0365 564	
0.5325 879	0.0541 831	0.0677 506	0.5325 879	0.0541 831	0.0677 506	0.0338 753	0.1083 662	0.1422 415	7.0302 953		0.0338 753	
0.5431 052	0.0574 387	0.0638 015	0.5431 052	0.0574 387	0.0638 015	0.0319 008	0.1148 773	0.1467 781	6.8130 059		0.0319 008	
0.5515 464	0.0603 499	0.0607 603	0.5515 464	0.0603 499	0.0607 603	0.0303 801	0.1206 997	0.1510 799	6.6190 157		0.0303 801	
0.5585 817	0.0629 904	0.0582 964	0.5585 817	0.0629 904	0.0582 964	0.0291 482	0.1259 807	0.1551 289	6.4462 508		0.0291 482	
0.5646 271	0.0653 992	0.0562 042	0.5646 271	0.0653 992	0.0562 042	0.0281 021	0.1307 985	0.1589 006	6.2932 444		0.0281 021	
0.5699 666	0.0676 117	0.0543 531	0.5699 666	0.0676 117	0.0543 531	0.0271 765	0.1352 234	0.1623 999	6.1576 383		0.0271 765	
0.5747 586	0.0696 84	0.0527 046	0.5747 586	0.0696 84	0.0527 046	0.0263 523	0.1393 68	0.1657 203	6.0342 645		0.0263 523	
0.5791 152	0.0716 983	0.0512 575	0.5791 152	0.0716 983	0.0512 575	0.0256 287	0.1433 966	0.1690 253	5.9162 736		0.0256 287	
0.5831 249	0.0736 352	0.0499 447	0.5831 249	0.0736 352	0.0499 447	0.0249 723	0.1472 705	0.1722 428	5.8057 577		0.0249 723	
0.5868 368	0.0754 562	0.0487 158	0.5868 368	0.0754 562	0.0487 158	0.0243 579	0.1509 124	0.1752 703	5.7054 721		0.0243 579	
0.5902 982	0.0772 025	0.0475 75	0.5902 982	0.0772 025	0.0475 75	0.0237 875	0.1544 05	0.1781 925	5.6119 078		0.0237 875	
0.5935 61	0.0789 088	0.0465 145	0.5935 61	0.0789 088	0.0465 145	0.0232 573	0.1578 176	0.1810 748	5.5225 785		0.0232 573	
0.5966 507	0.0805 36	0.0454 982	0.5966 507	0.0805 36	0.0454 982	0.0227 491	0.1610 721	0.1838 212	5.4400 692		0.0227 491	
0.5995	0.0821	0.0445	0.5995	0.0821	0.0445	0.0222	0.1642	0.1865	5.3618		0.0222	

658	138	478	658	138	478	739	277	016	849		739	
0.6023 33	0.0836 324	0.0436 437	0.6023 33	0.0836 324	0.0436 437	0.0218 219	0.1672 647	0.1890 866	5.2885 825		0.0218 219	
0.6049 765	0.0850 036	0.0427 296	0.6049 765	0.0850 036	0.0427 296	0.0213 648	0.1700 073	0.1913 721	5.2254 23		0.0213 648	
0.6075 178	0.0863 459	0.0418 568	0.6075 178	0.0863 459	0.0418 568	0.0209 284	0.1726 918	0.1936 202	5.1647 504		0.0209 284	
0.6099 532	0.0876 45	0.0410 216	0.6099 532	0.0876 45	0.0410 216	0.0205 108	0.1752 9	0.1958 008	5.1072 311		0.0205 108	
0.6122 842	0.0889 707	0.0402 556	0.6122 842	0.0889 707	0.0402 556	0.0201 278	0.1779 413	0.1980 691	5.0487 433		0.0201 278	
0.6145 304	0.0902 626	0.0395 188	0.6145 304	0.0902 626	0.0395 188	0.0197 594	0.1805 252	0.2002 846	4.9928 96		0.0197 594	
0.6166 765	0.0915 149	0.0388 183	0.6166 765	0.0915 149	0.0388 183	0.0194 092	0.1830 297	0.2024 389	4.9397 619		0.0194 092	
0.6187 517	0.0927 527	0.0381 487	0.6187 517	0.0927 527	0.0381 487	0.0190 743	0.1855 055	0.2045 798	4.8880 674		0.0190 743	
0.6207 706	0.0938 894	0.0374 668	0.6207 706	0.0938 894	0.0374 668	0.0187 334	0.1877 788	0.2065 122	4.8423 289		0.0187 334	
0.6227 217	0.0949 266	0.0367 829	0.6227 217	0.0949 266	0.0367 829	0.0183 915	0.1898 531	0.2082 446	4.8020 458		0.0183 915	
0.6246 016	0.0960 9	0.0361 866	0.6246 016	0.0960 9	0.0361 866	0.0180 933	0.1921 8	0.2102 733	4.7557 162		0.0180 933	
0.9	0.3	0	0.9	0.3	0	0	0.6	0.6	1.6666 667		0	
0.4	0.03	0.128	0.4	0.03	0.128	0.064	0.06	0.124	8.0645 161		0.124	
0.62	0.093	0.036	0.62	0.093	0.036	0.018	0.186	0.204	4.9019 608		0.204	

Injector Wellblock

Rock Curve Table		Pseudo Function Table				Rock Mobility				Pseudo Oil Mobility			
Sw	Krw	kro	SW	KRW	KRO	λo	λw	λt	λ-1	Lwj	Loj	1/Loj	LTj
0.2	0	0.9	0.2	0	0.9	0.45	0	0.45	2.222 2222	0	0.45	2.222 2222	0.45
0.202 2892	0.000 6848	0.467 3454	0.202 2892	0 0	0.892 9729	0.233 6727	0.001 3695	0.235 0422	4.254 5546	0	0.446 4865	2.239 7095	0.446 4865
0.233 9638	0.006 3274	0.277 2928	0.233 9638	0 0	0.805 9067	0.138 6464	0.012 6548	0.151 3012	6.609 3316	0	0.402 9534	2.481 6768	0.402 9534
0.323 723	0.018 2721	0.173 1687	0.323 723	0 0	0.631 4403	0.086 5843	0.036 5441	0.123 1285	8.121 5988	0	0.315 7201	3.167 362	0.315 7201
0.423 5089	0.032 3592	0.116 5847	0.629 3547	0.047 9841	0.172 8785	0.058 2924	0.064 7185	0.123 0108	8.129 3661	0.095 9682	0.086 4392		0.182 4074
0.470 3766	0.040 1583	0.094 1527	0.636 3607	0.058 3815	0.136 8779	0.047 0764	0.080 3166	0.127 3929	7.849 73	0.116 7631	0.068 4389		0.185 202
0.499 526	0.045 8276	0.081 0567	0.641 5477	0.065 1042	0.115 1518	0.040 5284	0.091 6552	0.132 1835	7.565 239	0.130 2083	0.057 5759		0.187 7842
0.518 8289	0.050 3955	0.073 1128	0.645 8514	0.069 7649	0.101 2135	0.036 5564	0.100 7911	0.137 3475	7.280 8023	0.139 5298	0.050 6067		0.190 1365
0.532 5879	0.054 1831	0.067 7506	0.649 5873	0.073 2316	0.091 5688	0.033 8753	0.108 3662	0.142 2415	7.030 2953	0.146 4632	0.045 7844		0.192 2476

0.543 1052	0.057 4387	0.063 8015	0.652 9302	0.075 9742	0.084 3903	0.031 9008	0.114 8773	0.146 7781	6.813 0059	0.151 9484	0.042 1952		0.194 1436
0.551 5464	0.060 3499	0.060 7603	0.655 9809	0.078 2343	0.078 7663	0.030 3801	0.120 6997	0.151 0799	6.619 0157	0.156 4685	0.039 3832		0.195 8517
0.558 5817	0.062 9904	0.058 2964	0.658 8034	0.080 151	0.074 1782	0.029 1482	0.125 9807	0.155 1289	6.446 2508	0.160 3019	0.037 0891		0.197 3911
0.564 6271	0.065 3992	0.056 2042	0.661 4408	0.081 8124	0.070 3097	0.028 1021	0.130 7985	0.158 9006	6.293 2444	0.163 6248	0.035 1548		0.198 7796
0.569 9666	0.067 6117	0.054 3531	0.663 9232	0.083 2801	0.066 9489	0.027 1765	0.135 2234	0.162 3999	6.157 6383	0.166 5602	0.033 4745		0.200 0347
0.574 7586	0.069 684	0.052 7046	0.666 2721	0.084 591	0.063 9793	0.026 3523	0.139 368	0.165 7203	6.034 2645	0.169 1821	0.031 9897		0.201 1718
0.579 1152	0.071 6983	0.051 2575	0.668 5042	0.085 7712	0.061 3183	0.025 6287	0.143 3966	0.169 0253	5.916 2736	0.171 5425	0.030 6592		0.202 2017
0.583 1249	0.073 6352	0.049 9447	0.670 6325	0.086 8393	0.058 9006	0.024 9723	0.147 2705	0.172 2428	5.805 7577	0.173 6786	0.029 4503		0.203 1289
0.586 8368	0.075 4562	0.048 7158	0.672 6676	0.087 8075	0.056 69	0.024 3579	0.150 9124	0.175 2703	5.705 4721	0.175 6151	0.028 345		0.203 9601
0.590 2982	0.077 2025	0.047 575	0.674 6183	0.088 689	0.054 6534	0.023 7875	0.154 405	0.178 1925	5.611 9078	0.177 378	0.027 3267		0.204 7047
0.593 561	0.078 9088	0.046 5145	0.676 492	0.089 4957	0.052 7552	0.023 2573	0.157 8176	0.181 0748	5.522 5785	0.178 9914	0.026 3776		0.205 369
0.596 6507	0.080 536	0.045 4982	0.678 2949	0.090 2342	0.050 9771	0.022 7491	0.161 0721	0.183 8212	5.440 0692	0.180 4683	0.025 4885		0.205 9569
0.599 5658	0.082 1138	0.044 5478	0.680 032	0.090 9078	0.049 3186	0.022 2739	0.164 2277	0.186 5016	5.361 8849	0.181 8156	0.024 6593		0.206 4749
0.602 333	0.083 6324	0.043 6437	0.681 7084	0.091 5232	0.047 7615	0.021 8219	0.167 2647	0.189 0866	5.288 5825	0.183 0464	0.023 8808		0.206 9271
0.604 9765	0.085 0036	0.042 7296	0.683 3283	0.092 0867	0.046 29	0.021 3648	0.170 0073	0.191 3721	5.225 423	0.184 1733	0.023 145		0.207 3184
0.607 5178	0.086 3459	0.041 8568	0.684 8953	0.092 606	0.044 8914	0.020 9284	0.172 6918	0.193 6202	5.164 7504	0.185 2119	0.022 4457		0.207 6576
0.609 9532	0.087 645	0.041 0216	0.686 4125	0.093 0822	0.043 5664	0.020 5108	0.175 29	0.195 8008	5.107 2311	0.186 1644	0.021 7832		0.207 9476
0.612 2842	0.088 9707	0.040 2556	0.687 8829	0.093 5174	0.042 3128	0.020 1278	0.177 9413	0.198 0691	5.048 7433	0.187 0349	0.021 1564		0.208 1912
0.614 5304	0.090 2626	0.039 5188	0.689 3093	0.093 9148	0.041 1178	0.019 7594	0.180 5252	0.200 2846	4.992 896	0.187 8295	0.020 5589		0.208 3885
0.616 6765	0.091 5149	0.038 8183	0.690 6941	0.094 2738	0.039 9886	0.019 4092	0.183 0297	0.202 4389	4.939 7619	0.188 5476	0.019 9943		0.208 5419
0.618 7517	0.092 7527	0.038 1487	0.692 0399	0.094 6	0.038 9084	0.019 0743	0.185 5055	0.204 5798	4.888 0674	0.189 2	0.019 4542		0.208 6542
0.620 7706	0.093 8894	0.037 4668	0.693 3486	0.094 8964	0.037 8687	0.018 7334	0.187 7788	0.206 5122	4.842 3289	0.189 7928	0.018 9343		0.208 7271
0.622 7217	0.094 9266	0.036 7829	0.694 6219	0.095 1641	0.036 875	0.018 3915	0.189 8531	0.208 2446	4.802 0458	0.190 3282	0.018 4375		0.208 7657
0.624 6016	0.096 09	0.036 1866	0.695 8615	0.096 09	0.036 1866	0.018 0933	0.192 18	0.210 2733	4.755 7162	0.192 18	0.018 0933		0.210 2733
0.9	0.3	0	0.9	0.3	0	0	0.6	0.6	1.666 6667	0.6	0		0.6
0.4	0.03	0.128	0.4	0.044 5498	0.190 0793	0.064	0.06	0.124	8.064 5161	0.089 0997	0.095 0397		0.184 1394
0.62	0.093	0.036	0.62	0.084 4303	0.032 6827	0.018	0.186	0.204	4.901 9608	0.168 8606	0.016 3414	61.19 4447	0.185 202

Table D6 Layered Model**Intermediate Wellblock**

Rock Curves Table			Pseudo Relative Permeability Table			Rock Curve Mobility				Pseudo Mobility		
Sw	Krw	kro	SW	KRW	KRO	λ_o	λ_w	λ_t	$\lambda-1$	L wj	Loj	1/Loj
0.2	0	0.9	0.2	0	0.9	0.45	0	0.45	2.2222 222	0	0.45	2.2222 222
0.2800 71	0.0181 31	0.3426 895	0.2800 71	0	0.6794 752	0.1713 448	0.0362 62	0.2076 068	4.8167 985	0	0.3397 376	2.9434 48
0.5458 47	0.0585 522	0.0736 201	0.5458 47	0	0.3747 158	0.0368 1	0.1171 043	0.1539 144	6.4971 187	0	0.1873 579	5.3373 781
0.5851 453	0.0769 358	0.0518 166	0.5851 453	0.0769 358	0.0518 166	0.0259 083	0.1538 716	0.1797 799	5.5623 575	0		
0.6087 581	0.0887 116	0.0426 638	0.6087 581	0.0887 116	0.0426 638	0.0213 319	0.1774 233	0.1987 552	5.0313 15	0		
0.6218 371	0.0960 748	0.0377 757	0.6218 371	0.0960 748	0.0377 757	0.0188 878	0.1921 495	0.2110 374	4.7384 975	0		
0.6325 093	0.1023 992	0.0339 631	0.6325 093	0.1023 992	0.0339 631	0.0169 815	0.2047 983	0.2217 799	4.5089 753	0		
0.6415 386	0.1079 387	0.0308 678	0.6415 386	0.1079 387	0.0308 678	0.0154 339	0.2158 773	0.2313 112	4.3231 796	0		
0.6493 43	0.1129 294	0.0283 156	0.6493 43	0.1129 294	0.0283 156	0.0141 578	0.2258 588	0.2400 166	4.1663 779	0		
0.6562 417	0.1174 087	0.0261 36	0.6562 417	0.1174 087	0.0261 36	0.0130 68	0.2348 173	0.2478 853	4.0341 234	0		
0.6623 826	0.1215 627	0.0242 845	0.6623 826	0.1215 627	0.0242 845	0.0121 423	0.2431 254	0.2552 676	3.9174 569	0		
0.6679 805	0.1253 594	0.0226 438	0.6679 805	0.1253 594	0.0226 438	0.0113 219	0.2507 188	0.2620 407	3.8162 008	0		
0.6730 561	0.1288 482	0.0212 046	0.6730 561	0.1288 482	0.0212 046	0.0106 023	0.2576 963	0.2682 986	3.7271 9	0		
0.6777 14	0.1321 68	0.0199 378	0.6777 14	0.1321 68	0.0199 378	0.0099 689	0.2643 361	0.2743 05	3.6455 774	0		
0.6820 45	0.1352 06	0.0187 828	0.6820 45	0.1352 06	0.0187 828	0.0093 914	0.2704 121	0.2798 035	3.5739 372	0		
0.6860 403	0.1380 286	0.0177 477	0.6860 403	0.1380 286	0.0177 477	0.0088 739	0.2760 571	0.2849 31	3.5096 217	0		
0.6897 18	0.1406 926	0.0168 276	0.6897 18	0.1406 926	0.0168 276	0.0084 138	0.2813 853	0.2897 991	3.4506 667	0		
0.6931 439	0.1432 354	0.0159 987	0.6931 439	0.1432 354	0.0159 987	0.0079 994	0.2864 708	0.2944 702	3.3959 295	0		
0.6963 794	0.1456 364	0.0152 346	0.6963 794	0.1456 364	0.0152 346	0.0076 173	0.2912 729	0.2988 901	3.3457 109	0		
0.6994 15	0.1478 691	0.0145 325	0.6994 15	0.1478 691	0.0145 325	0.0072 662	0.2957 381	0.3030 044	3.3002 825	0		
0.7022 312	0.1500 263	0.0139 045	0.7022 312	0.1500 263	0.0139 045	0.0069 522	0.3000 525	0.3070 048	3.2572 782	0		
0.7049 026	0.1520 931	0.0133 24	0.7049 026	0.1520 931	0.0133 24	0.0066 62	0.3041 861	0.3108 481	3.2170 055	0		
0.7074 409	0.1540 719	0.0127 856	0.7074 409	0.1540 719	0.0127 856	0.0063 928	0.3081 437	0.3145 365	3.1792 811	0		

0.7098 52	0.1559 31	0.0122 834	0.7098 52	0.1559 31	0.0122 834	0.0061 417	0.3118 619	0.3180 036	3.1446 181	0		
0.7121 613	0.1576 816	0.0118 102	0.7121 613	0.1576 816	0.0118 102	0.0059 051	0.3153 632	0.3212 683	3.1126 63	0		
0.7143 124	0.1593 935	0.0113 846	0.7143 124	0.1593 935	0.0113 846	0.0056 923	0.3187 87	0.3244 793	3.0818 611	0		
0.7163 884	0.1611 416	0.0109 886	0.7163 884	0.1611 416	0.0109 886	0.0054 943	0.3222 832	0.3277 775	3.0508 501	0		
0.7183 732	0.1628 138	0.0106 17	0.7183 732	0.1628 138	0.0106 17	0.0053 085	0.3256 276	0.3309 361	3.0217 318	0		
0.7203 139	0.1643 992	0.0102 57	0.7203 139	0.1643 992	0.0102 57	0.0051 285	0.3287 983	0.3339 268	2.9946 681	0		
0.7221 734	0.1659 341	0.0099 192	0.7221 734	0.1659 341	0.0099 192	0.0049 596	0.3318 682	0.3368 278	2.9688 764	0		
0.7239 784	0.1674 016	0.0095 958	0.7239 784	0.1674 016	0.0095 958	0.0047 979	0.3348 032	0.3396 011	2.9446 315	0		
0.7257 044	0.1688 172	0.0092 926	0.7257 044	0.1688 172	0.0092 926	0.0046 463	0.3376 344	0.3422 807	2.9215 791	0		
0.7273 747	0.1701 429	0.0090 017	0.7273 747	0.1701 429	0.0090 017	0.0045 009	0.3402 858	0.3447 867	2.9003 441			
0.7289 53	0.1713 849	0.0087 312	0.7289 53	0.1713 849	0.0087 312	0.0043 656	0.3427 698	0.3471 354	2.8807 204			
0.7304 487	0.1726 23	0.0084 822	0.7304 487	0.1726 23	0.0084 822	0.0042 411	0.3452 46	0.3494 871	2.8613 356			
0.7318 978	0.1738 537	0.0082 465	0.7318 978	0.1738 537	0.0082 465	0.0041 232	0.3477 075	0.3518 307	2.8422 76			
0.7332 955	0.1750 316	0.0080 223	0.7332 955	0.1750 316	0.0080 223	0.0040 112	0.3500 632	0.3540 744	2.8242 654			
0.9	0.3	0	0.9	0.3	0	0	0.6	0.6	1.6666 667			
0.5823	0.075	0.053	0.5823	0.075	0.053	0.0265	0.15	0.1765	5.6657 224		0.1765	
0.649	0.112	0.0275	0.649			0.0137 5	0.224	0.2377 5	4.2060 988		0.2377 5	

Injector Wellblock

Rock Curve Table			Pseudo Function Table			Rock Mobility				Pseudo Oil Mobility			
Sw	Krw	kro	SW	KRW	KRO	λ_o	λ_w	λ_t	$\lambda-1$	Lwj	Loj	1/Loj	LTj
0.2	0	0.9	0.2	0	0.9	0.45	0	0.45	2.222 2222	0	0.45	2.222 2222	0.45
0.280 071	0.018 131	0.342 6895	0.280 071		0.781 9346	0.171 3448	0.036 262	0.207 6068	4.816 7985		0.390 9673	2.557 7587	0.390 9673
0.545 847	0.058 5522	0.073 6201	0.545 847		0.544 7382	0.036 81	0.117 1043	0.153 9144	6.497 1187		0.272 3691	3.671 4886	0.272 3691
0.585 1453	0.076 9358	0.051 8166	0.653 1407	0.106 4225	0.071 676	0.025 9083	0.153 8716	0.179 7799	5.562 3575	0.212 8449	0.035 838		0.248 6829
0.608 7581	0.088 7116	0.042 6638	0.677 6555	0.117 4255	0.056 4731	0.021 3319	0.177 4233	0.198 7552	5.031 315	0.234 851	0.028 2365		0.263 0875
0.621 8371	0.096 0748	0.037 7757	0.687 498	0.124 8208	0.049 0783	0.018 8878	0.192 1495	0.211 0374	4.738 4975	0.249 6415	0.024 5392		0.274 1807

0.632 5093	0.102 3992	0.033 9631	0.695 7056	0.130 9467	0.043 4316	0.016 9815	0.204 7983	0.221 7799	4.508 9753	0.261 8935	0.021 7158		0.283 6093
0.641 5386	0.107 9387	0.030 8678	0.702 7274	0.136 1383	0.038 9322	0.015 4339	0.215 8773	0.231 3112	4.323 1796	0.272 2766	0.019 4661		0.291 7427
0.649 343	0.112 9294	0.028 3156	0.708 8463	0.140 6064	0.035 2552	0.014 1578	0.225 8588	0.240 0166	4.166 3779	0.281 2127	0.017 6276		0.298 8403
0.656 2417	0.117 4087	0.026 136	0.714 2557	0.144 4941	0.032 1654	0.013 068	0.234 8173	0.247 8853	4.034 1234	0.288 9882	0.016 0827		0.305 0709
0.662 3826	0.121 5627	0.024 2845	0.719 0902	0.147 9045	0.029 5468	0.012 1423	0.243 1254	0.255 2676	3.917 4569	0.295 809	0.014 7734		0.310 5824
0.667 9805	0.125 3594	0.022 6438	0.723 4523	0.150 9175	0.027 2604	0.011 3219	0.250 7188	0.262 0407	3.816 2008	0.301 835	0.013 6302		0.315 4652
0.673 0561	0.128 8482	0.021 2046	0.727 4146	0.153 5871	0.025 2759	0.010 6023	0.257 6963	0.268 2986	3.727 19	0.307 1741	0.012 638		0.319 8121
0.677 714	0.132 168	0.019 9378	0.731 0385	0.155 9663	0.023 5278	0.009 9689	0.264 3361	0.274 305	3.645 5774	0.311 9326	0.011 7639		0.323 6964
0.682 045	0.135 206	0.018 7828	0.734 3713	0.158 0904	0.021 9619	0.009 3914	0.270 4121	0.279 8035	3.573 9372	0.316 1807	0.010 9809		0.327 1617
0.686 0403	0.138 0286	0.017 7477	0.737 4493	0.159 9907	0.020 5716	0.008 8739	0.276 0571	0.284 931	3.509 6217	0.319 9814	0.010 2858		0.330 2672
0.689 718	0.140 6926	0.016 8276	0.740 3054	0.161 6933	0.019 3394	0.008 4138	0.281 3853	0.289 7991	3.450 6667	0.323 3866	0.009 6697		0.333 0563
0.693 1439	0.143 2354	0.015 9987	0.742 9679	0.163 2226	0.018 2312	0.007 9994	0.286 4708	0.294 4702	3.395 9295	0.326 4451	0.009 1156		0.335 5607
0.696 3794	0.145 6364	0.015 2346	0.745 459	0.164 5982	0.017 2181	0.007 6173	0.291 2729	0.298 8901	3.345 7109	0.329 1963	0.008 609		0.337 8054
0.699 415	0.147 8691	0.014 5325	0.747 7962	0.165 8337	0.016 298	0.007 2662	0.295 7381	0.303 0044	3.300 2825	0.331 6674	0.008 149		0.339 8164
0.702 2312	0.150 0263	0.013 9045	0.749 9953	0.166 9424	0.015 4723	0.006 9522	0.300 0525	0.307 0048	3.257 2782	0.333 8848	0.007 7361		0.341 621
0.704 9026	0.152 0931	0.013 324	0.752 072	0.167 9387	0.014 7121	0.006 662	0.304 1861	0.310 8481	3.217 0055	0.335 8774	0.007 3561		0.343 2335
0.707 4409	0.154 0719	0.012 7856	0.754 0374	0.168 8323	0.014 0105	0.006 3928	0.308 1437	0.314 5365	3.179 2811	0.337 6646	0.007 0052		0.344 6699
0.709 852	0.155 931	0.012 2834	0.755 9013	0.169 6316	0.013 3626	0.006 1417	0.311 8619	0.318 0036	3.144 6181	0.339 2633	0.006 6813		0.345 9446
0.712 1613	0.157 6816	0.011 8102	0.757 6724	0.170 3473	0.012 7589	0.005 9051	0.315 3632	0.321 2683	3.112 663	0.340 6946	0.006 3794		0.347 074
0.714 3124	0.159 3935	0.011 3846	0.759 358	0.170 9832	0.012 2124	0.005 6923	0.318 787	0.324 4793	3.081 8611	0.341 9664	0.006 1062		0.348 0725
0.716 3884	0.161 1416	0.010 9886	0.760 9668	0.171 5492	0.011 6983	0.005 4943	0.322 2832	0.327 7775	3.050 8501	0.343 0983	0.005 8491		0.348 9475
0.718 3732	0.162 8138	0.010 617	0.762 504	0.172 0454	0.011 219	0.005 3085	0.325 6276	0.330 9361	3.021 7318	0.344 0908	0.005 6095		0.349 7003
0.720 3139	0.164 3992	0.010 257	0.763 975	0.172 4803	0.010 7612	0.005 1285	0.328 7983	0.333 9268	2.994 6681	0.344 9605	0.005 3806		0.350 3411
0.722 1734	0.165 9341	0.009 9192	0.765 3834	0.172 8568	0.010 3331	0.004 9596	0.331 8682	0.336 8278	2.968 8764	0.345 7136	0.005 1665		0.350 8801
0.723 9784	0.167 4016	0.009 5958	0.766 7337	0.173 1804	0.009 9271	0.004 7979	0.334 8032	0.339 6011	2.944 6315	0.346 3607	0.004 9635		0.351 3243
0.725 7044	0.168 8172	0.009 2926	0.768 0293	0.173 4537	0.009 5478	0.004 6463	0.337 6344	0.342 2807	2.921 5791	0.346 9074	0.004 7739		0.351 6813
0.727 3747	0.170 1429	0.009 0017	0.769 2742	0.173 6815	0.009 189	0.004 5009	0.340 2858	0.344 7867	2.900 3441	0.347 363	0.004 5945		0.351 9575
0.728 953	0.171 3849	0.008 7312	0.770 4713	0.173 8661	0.008 8576	0.004 3656	0.342 7698	0.347 1354	2.880 7204	0.347 7322	0.004 4288		0.352 161

0.730 4487	0.172 623	0.008 4822	0.771 6246	0.174 0118	0.008 5504	0.004 2411	0.345 246	0.349 4871	2.861 3356	0.348 0236	0.004 2752		0.352 2988
0.731 8978	0.173 8537	0.008 2465	0.772 7375	0.174 1219	0.008 2592	0.004 1232	0.347 7075	0.351 8307	2.842 276	0.348 2438	0.004 1296		0.352 3734
0.733 2955	0.175 0316	0.008 0223	0.773 8122	0.175 0316	0.008 0223	0.004 0112	0.350 0632	0.354 0744	2.824 2654	0.350 0632	0.004 0112		0.354 0744
0.9	0.3	0	0.9	0.3	0	0	0.6	0.6	1.666 6667	0.6	0		0.6
0.582 3	0.075	0.053	0.582 3	0.103 5466	0.073 1729	0.026 5	0.15	0.176 5	5.665 7224	0.207 0931	0.036 5865		0.243 6796
0.649	0.112	0.027 5	0.649	0.123 9361	0.030 4307	0.013 75	0.224	0.237 75	4.206 0988	0.247 8721	0.015 2154		0.263 0875