

# Viscosity and Density of Aqueous Solutions of Carbon Dioxide at Temperatures From (274 to 449) K and at Pressures up to 100 MPa

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## ABSTRACT

The viscosity and density of aqueous solutions of carbon dioxide having mole fractions of CO<sub>2</sub> of 0.0086, 0.0168 and 0.0271 are reported. The measurements were made in the single-phase compressed liquid region at temperatures between (294 and 449) K at pressures up to 100 MPa; additional density measurements were also made at  $T = 274$  K in the same pressure range. The viscosity was measured with a vibrating-wire viscometer while the density was measured by means of a vibrating U-tube densimeter; both were calibrated with pure water and either vacuum or ambient air.

The density data have an expanded relative uncertainty of 0.07 % with a coverage factor of 2. From the raw data, the partial molar volume of CO<sub>2</sub> in aqueous solution has been determined and correlated as an empirical function of temperature and pressure. When combined with the IAPWS-95 equation of state of pure water, this correlation represents the measured densities of under-saturated solutions of CO<sub>2</sub> in water within  $\pm 0.04\%$ .

The viscosity data have an expanded relative uncertainty of 1.4 % with a coverage factor of 2. A modified Vogel-Fulcher-Tamman equation was used to correlate the viscosity as a function of temperature, pressure and mole fraction of CO<sub>2</sub> with an absolute average relative deviation of 0.4 %.

The viscosity and density of saturated aqueous solutions of CO<sub>2</sub> may be calculated by combining the correlations presented in this work with a suitable model for the mole fraction of CO<sub>2</sub> at saturation.

## Keywords

Carbon dioxide; Density; Vibrating-tube densimeter; Vibrating-wire viscometer; Viscosity; Vogel-Fulcher-Tamman equation; Water

## 1. INTRODUCTION

Carbon dioxide is a fluid commonly used in the chemical and petroleum industries. It plays an important role in the refrigeration industry as a replacement for chlorofluorocarbons (CFCs) which have high global warming potentials (GWP).<sup>1</sup> It is used as a supercritical fluid in extraction and purification processes and, in environmental engineering, for treatment of industrial waste liquids.<sup>2</sup> It is also used in oilfield process engineering as a fluid for enhanced oil recovery (EOR).<sup>3, 4</sup> However, because CO<sub>2</sub> is a greenhouse gas and huge volumes are emitted annually from anthropogenic sources, large-scale capture of CO<sub>2</sub> from fossil fuel combustion processes, and subsequent geological storage, is currently being considered. This process is known as carbon capture and storage (CCS). Deep saline aquifers represent a sink that can potentially store very large amounts of CO<sub>2</sub> on a geological timescale. Consequently, there is interest in the physical and chemical properties of mixtures of CO<sub>2</sub> and water or brine.

Understanding the multiphase flow properties of CO<sub>2</sub> and brines in porous media is essential for successful large-scale geologic CO<sub>2</sub> storage. Optimizing the design and operation of injection projects will depend upon expectations about the distribution of CO<sub>2</sub> in the subsurface, knowledge of injectivity, and estimates of the capacity of permanent trapping processes. It is recognized that the capillarity of the CO<sub>2</sub>-brine system in porous media is important in controlling fluid flow over lengths ranging from sub-core to basin scale.<sup>5</sup> The distribution of CO<sub>2</sub> in the subsurface, including the column height in contact with the caprock and the surface extent of the plume, is dependent upon capillary pressure-saturation relationships, and the relative permeability function.<sup>6</sup> Small variations in relative permeability can strongly influence injectivity and, in turn, the number of wells required to meet an overall injection goal.<sup>7</sup> Lower-than-expected injectivity is a well-known but poorly understood phenomenon in CO<sub>2</sub> EOR processes, and may be due to poorly characterized relative permeability functions<sup>8</sup> and/or inaccurate knowledge of fundamental thermophysical properties.

When CO<sub>2</sub> is injected into an aquifer, some of it dissolves in the brine leading to a solution of higher density than the original brine.<sup>9</sup> Natural convection due to negative buoyancy may then lead to the CO<sub>2</sub>-dense brine sinking towards the bottom of the reservoir formation at a rate that is influenced by, among other factors, viscosity. This process allows undissolved CO<sub>2</sub> to contact fresh brine and so it accelerates the rate of dissolution thereby shortening the time scale for the storage of CO<sub>2</sub> by solubility trapping.<sup>2</sup> Knowledge of the viscosity and density of CO<sub>2</sub>-brine system is therefore essential in reservoir flow simulations used to model the injection and long-term fate of CO<sub>2</sub> in a storage project. Inspection of the literature yields a very limited amount of experimental data for the viscosity and density of solutions of CO<sub>2</sub> in water or brine, especially in relation to high pressure and high temperature conditions. Li *et al.*<sup>10</sup> performed an extensive literature survey considering experimental transport-property data for mixtures with dissolved CO<sub>2</sub>.<sup>2, 10-14</sup> As summarized in Table 1, the data available for viscosity are sparse, derived from only a few sources, and restricted to low temperatures and relatively modest pressures. The situation for density is slightly better but the database is still limited.

In our work, we seek to expand substantially the ranges of temperature, pressures and mole fraction over which the viscosity and density of aqueous solutions of CO<sub>2</sub> are known. We begin in this paper with the (CO<sub>2</sub> + H<sub>2</sub>O) binary system because this system is easier to study than (CO<sub>2</sub> + brine) system and also exhibits the highest solubility of CO<sub>2</sub>, thereby maximizing the effect that we wish to study. The effects upon viscosity of dissolved CO<sub>2</sub> and dissolved salts are probably almost separable so that the results of the present study will be transferrable to (CO<sub>2</sub> + brine) systems. The present study on the (CO<sub>2</sub> + H<sub>2</sub>O) binary system extends in temperature from 274 K (for density) or 296 K (for viscosity) up to 449 K, with mole fractions of CO<sub>2</sub> up to 0.027, and pressures up to 100 MPa. These ranges of temperature and pressure extend beyond typical aquifer conditions but allow for the construction of a more wide-ranging model.

## 2. APPARATUS

There are numerous methods available for viscosity and density determination, each of which has their respective benefits. The techniques used in this work for viscosity and density measurements are the vibrating-wire (VW) viscometer and vibrating U-tube (VT) densimeter, respectively. Thus, the experimental system developed is referred to as the VW-VT apparatus. Figure 1 is a schematic diagram of the VW-VT apparatus.

Since the VW-VT apparatus was designed for work with aqueous solutions, including concentrated brines, a high resistance to corrosion was needed. Consequently, wetted parts of the fluid system were made from Hastelloy-C276 (HC-276) as it provides good resistance to corrosion.<sup>15, 16</sup>

The VW technique has previously been used successfully to study hydrocarbons with dissolved CO<sub>2</sub>.<sup>17</sup> The sensor used in this study was a compact design in which the tensioned vibrating wire is clamped securely at both ends. The absence of a tensioning weight allows the device to be used in any orientation and, like all VW viscometers, it requires no bulk movement the fluid because it is the wire itself that vibrates.

In the VW technique, the tensioned wire becomes a stiff string through which a sinusoidal alternating current of frequency  $f$  is passed thereby generating a transverse force due to the presence of a perpendicular magnetic field. The vibration of the wire induces a voltage proportional to the velocity of the wire in addition to that arising from the passage of the current through the electrical impedance presented by the stationary wire. A lock-in amplifier demodulates, filters and digitizes the signal to yield the in-phase and quadrature components of the combined complex voltage  $V$ . The resonance curve  $V(f)$  is represented by a rigorous theoretically-derived working equation<sup>18</sup> as follows:

$$V = \frac{\Lambda if}{f_0^2 - f^2(1 + \beta) + if^2(\beta' + 2\Delta_0)} + a + bi + cif, \quad (1)$$

Here,  $\Lambda$  is the amplitude, and  $f_0$  and  $\Delta_0$  are the resonance frequency and logarithmic decrement of the wire in vacuum. In equation (1),  $\beta$  and  $\beta'$  are real-valued terms that account for the added mass and damping arising from the fluid around the wire and are given by:

$$(\beta' + i\beta) = \frac{\rho}{\rho_s} \left[ \frac{i + 4_i K_1(\sqrt{i\Omega})}{\sqrt{i\Omega} K_0(\sqrt{i\Omega})} \right], \quad (2)$$

where

$$\Omega = \frac{2\pi f \rho R^2}{\eta}, \quad (3)$$

$\rho$  and  $\eta$  are the density and viscosity of the fluid,  $R$  and  $\rho_s$  are the radius and density of the wire, and  $K_n$  is the modified Bessel functions of the second kind with order  $n$ . The remaining terms in equation (1) arise from the impedance of the stationary wire.

The wire material should be of high density, high tensile strength, high melting temperature, sufficient hardness and adequate electrical conductivity. Tungsten, which meets these criteria, has been the material of choice in most previous work. However, we experienced difficulties with tungsten wires in aqueous systems and adopted instead an alloy of platinum and iridium containing 90 mass% Pt. The wire used was 0.15 mm in diameter and the density of the material at  $T = 298.15$  K is  $21560 \text{ kg}\cdot\text{m}^{-3}$ .<sup>19</sup>

The viscometer sensor was similar to that described by Peleties and Trusler<sup>20</sup> and comprised a ceramic flow tube with metallic end pieces between which the wire was clamped. These end pieces were made from Monel K-500 and contained pins which were used for aligning the wire along the center line of the flow tube, and clamping plates to hold the wire securely in place under axial tension. The main body of the sensor, made from Shapal-M ceramic, was 52 mm in length, with an outer diameter 11.5 mm and an inner diameter of 6.0 mm. The end pieces were attached using epoxy resin (Stycast 2850 FT cured with catalyst 9) and, when assembled, the length of wire stretched between the end pieces was 50 mm. M2 screws, also made from Monel K-500, were used to hold down the clamping plates for the wire at each end and also for securing one solder tag at each end for the electrical connections. The outer surface of the ceramic tube was machined to accept a pair of O-rings (Kalrez Spectrum 7090, i.d. 9.5 mm x 1 mm section) in 10.0 mm diameter recesses, thereby centering the sensor within the 12.0 mm bore of the pressure vessel. This effectively prevented the metallic end-pieces from touching the inside wall of the vessel and thereby avoided short circuits.

For assembly, with the sensor orientated vertically, a length of wire was passed through, aligned and secured to the top clamp, and tensioned by attaching a mass of approximately 0.5 kg to its lower end. The wire was left in this condition for a period of typically 24 h before the lower end clamp was tightened and, finally, the excess wire protruding from each end cut

off. Tensioned in this way, the fundamental transverse resonance frequency of the wire in ambient air was approximately 1000 Hz.

Electrical connections, two to each end, were made with PTFE insulated Cu lead wires. The pair from one end passed back through the ceramic tube so that all four wires could pass out through a single electrical feedthru unit. The Monel end pieces were provided with holes so that the copper wires passing through the ceramic tube were kept well away from the vibrating wire, close to the inner diameter. The electrical feedthru (Greene-Tweed, part 5672-4592-002) was fitted in a custom tee-piece attached to the end of the tubular pressure vessel that contained the VW sensor. A junction box on the outside permitted onward connection via coaxial cables to the lock-in amplifier (Stanford Research Systems SR830).

The VW viscometer was housed within a tubular pressure vessel (Sieber-Sitec, part 740.1222) fabricated from HC-276 and rated for a maximum working pressure of 100 MPa at  $T = 473$  K. The ends of the vessel were closed by plugs fitted with 9.53 mm diameter tube extensions and Bridgeman-style seals comprising a glass-filled PTFE sealing ring backed with a Torlon anti-extrusion rings, and a stainless steel trust ring. This assembly was retained by a threaded gland and the tube adapters were connected to the fluid system to allow fluids in and out. In order to regulate the temperature of the VW viscometer, a heat exchanger sleeve, made from aluminum, was fitted over the outside of the pressure vessel and sealed with Viton O-rings. Silicone oil from a circulating thermostatic bath (Huber Petit-Fleur, Tango) was passed through this heat exchanger and insulation was provided by an outer layer of silicone-rubber sponge. The temperature was measured using a platinum resistance thermometer (PRT, Sensing Devices Ltd, Ceramic Capsule PT100/1P Band 5) located in a thermowell in the wall of the pressure vessel.

The VT densimeter was an Anton Paar model DMA HPM rated for operation at temperatures from 263.15 K to 473.15 K at pressures up to 138 MPa. It was connected to an evaluation unit (mPDS 2000V3) that served to excite oscillations of the tube at its fundamental resonance frequency and to digitize the period of oscillation. The densimeter was fitted with an internal heat exchanger through which silicone oil was passed from the circulating thermostatic bath; the densimeter and viscometer heat exchangers being connected in parallel. The temperature of the densimeter was measured using a second PRT located in a thermowell at the center of the instrument.

As shown in Figure 1, the VW and VT instruments were connected in a loop, fitted with a circulation pump, around which the fluids under study could be circulated. The purpose of the circulating pump was to permit *in-situ* homogenization of the fluid mixture under study. The circulating pump was a pneumatically operated reciprocating pump similar in design to that of Peleties *et al.*<sup>21</sup> The pump cylinder was honed to an inside diameter of 5.00 mm and fitted with a piston of diameter 4.97 mm. This piston comprised a soft-iron core encapsulated in a polyphenylene sulfide (PPS) sleeve with end caps sealed in place using epoxy resin (Stycast 2850 FT cured with catalyst 9). The pump incorporated four check valves operated in a vertical orientation such that the ceramic poppets sealed under gravity without the need for a spring. The pump was mounted on a thick aluminum plate, fitted with electrical heaters and a temperature sensor, and the whole assembly was enclosed within an insulated box. Thus,

operating with a process controller, the temperature of the circulation pump could be regulated.

A set of syringe pumps (Quizix Q5000-20k) made from HC-276 were used to inject fluids into the loop. These pumps had a displacement of 5.2 cm<sup>3</sup> and a maximum working pressure of 138 MPa. In the present work, only one pump cylinder was used (to inject water). CO<sub>2</sub> was introduced directly into the system from a gas bottle fitted with a filter and pressure regulator. The pressure of the system was monitored using a pressure transducer (Honeywell model TJE) having a full-scale range of 104 MPa, located in the flow loop between the VW viscometer and VT densimeter. The pressure in the syringe pump was separately monitored using a pressure transducer installed in the head of the pump.

### **3. MATERIALS**

The chemical samples used in this work are detailed in Table 2. The water was thoroughly degassed by agitation under vacuum prior to injection into the system.

## **4. CALIBRATION PROCEDURES AND VALIDATION RESULTS**

### **4.1 Temperature and Pressure**

The Honeywell TJE pressure transducer was calibrated against a hydraulic pressure balance (DH Budenberg Model 580EHX) at pressures of (20, 40, 60, 80 and 100) MPa, using both rising and falling pressure. The pressure was correlated as a linear function of the output voltage with a standard deviation of 0.02 % of reading. Sensor drift was checked by periodically comparing the measured pressure when open to the atmosphere with the reading of a digital barometer in the same laboratory and accounted for by adjusting the zero of the sensor. Taking this factor into account, the standard uncertainty of the pressure was taken to be 0.1 MPa.

The two PRTs used in the system to measure the temperatures were calibrated in a constant-temperature bath by comparison with a standard PRT which was itself calibrated on ITS-90. The calibration was performed in the temperature range (273 to 473) K at 50 K intervals the resistance-temperature data were used to determine the constants in the Callendar-van Dusen equation. The overall standard uncertainty of the measured temperatures was estimated to be 0.025 K.

### **4.2 Densimeter**

The period of oscillation  $\tau$  of the vibrating U-tube densimeter is generally related to the density by

$$\rho(T, p) = A(T, p)r^2 - B(T, p) \quad (4)$$

where  $A$  and  $B$  are functions of temperature and pressure to be determined, in principle, by calibration with two reference fluids. In this work we have followed the simplified calibration procedure developed by Lagourette *et al.*<sup>22</sup> and later modified by Comuñas *et al.*<sup>23</sup> in which a single reference fluid, water, is used together with measurements under vacuum. This amounts to an assumption that  $A$  and  $B$  have the same dependence upon pressure as, applying equation (4) to the cases of water and vacuum measurements and solving for  $A$  and  $B$ , one finds:

$$A(T, p) = \frac{\rho_w(T, p)}{r_w^2(T, p) - r_0^2(T)} \quad (5)$$

and

$$B(T, p) = \frac{\rho_w(T, p)r_0^2(T)}{r_w^2(T, p) - r_0^2(T)} \quad (6)$$

where subscript “w” denotes water and “0” denotes vacuum. It is then sufficient to correlate  $A$  as a function of temperature and pressure and, separately,  $r_0^2$  as a function of temperature. In the present work, calibration measurements were made under vacuum at each nominal experimental temperature and in pure deionized water at each nominal temperature and pressure. The densities of water were obtained from the equation of state of Wagner and Pruss<sup>24</sup> which forms the basis of the 1995 recommendations of the International Association for the Properties of Water and Steam (IAPWS) for the thermodynamic properties of water. The results of these calibration equations were represented by the following empirical equations:

$$r_0^2 = \sum_{i=0}^3 c_i (T/K)^i \quad (7)$$

and

$$A = \sum_{i=0}^3 \sum_{j=0}^1 a_{ij} (T/K)^i [p/(0.1 \text{ MPa})]^j \quad (8)$$

The standard uncertainties of these correlations are 0.003  $\mu\text{s}$  for  $r_0$  and  $1.0 \times 10^{-7} \text{ kg}\cdot\text{m}^{-3}\cdot\mu\text{s}^{-2}$  for  $A$ . The overall uncertainty of  $A$  is also influenced by the uncertainty of the density of the reference fluid. The relative uncertainty given by Pruss and Wagner<sup>24</sup> varies over the range of our measurement up to a maximum of 0.01 %. Interpreting that figure as twice the standard relative uncertainty of  $\rho_w$ , we find the overall standard uncertainty of  $A$  to be  $1.6 \times 10^{-7} \text{ kg}\cdot\text{m}^{-3}\cdot\mu\text{s}^{-2}$ , fractionally  $6 \times 10^{-5}$ . It is likely that the number of parameters in equations (7) and (8) could have been reduced by eliminating terms of low statistical significance. However, since the calibration data set was large, and the correlations for  $r_0$  and  $A$  were used only as a means of interpolation, we believe that the approach adopted is robust.

Finally, the density of the fluid under study was obtained in terms of the measured period  $\tau$  and the calibration equations for  $A(T, \rho)$  and  $\tau_0^2(T)$  as follows:

$$\rho(T, \rho) = A(T, \rho)[\tau^2 - \tau_0^2(T)]. \quad (9)$$

### 4.3 Vibrating-Wire Sensor

In the case of the viscometer, the most important parameter determined by calibration was the mean radius  $R$ . This was obtained at a reference temperature of 296 K and at a pressure of 1 MPa by means of a calibration measurement in pure deionized water. The viscosity of water was obtained from the IAPWS recommended equation for water viscosity<sup>25</sup> while the density was obtained as above from the IAPWS-95 equation of state of Pruss and Wagner.<sup>24</sup> This led to a radius of 73.04  $\mu\text{m}$  at the reference temperature. Considering the standard uncertainty in the reference value of the viscosity of water, which we take to be 0.2 %, and the repeatability of the calibration experiment, the standard relative uncertainty of  $R$  is estimated to be 0.25 %. The radius at other temperatures was calculated making use of a literature value for the mean linear expansivity of the wire material; compressibility effects were negligible. The logarithmic decrement  $\Delta_0$  was also required and was inferred from measurements in ambient air with the result  $\Delta_0 = 35 \times 10^{-6}$ . To validate the viscometer, additional measurements were made in pure water over the whole working range of the instrument. The results of these experiments were found to agree with the IAPWS recommended equation to within  $\pm 1$  %.

### 4.4 System Volume

The system volume was required in the quantitative preparation of the mixtures and was determined by the following procedure. The piston of the syringe pump was fully extended and both the fill and delivery valves were closed. The system was evacuated using vacuum pump at outlet. The temperature was controlled at 298.15 K both in the system and at the syringe pump. A sample of pure deionized water was connected to the delivery line to the syringe pump. It was degassed through agitation under vacuum with until no air bubbles were visible. The delivery tube was lowered to beneath the liquid level and the sample was re-pressurized to ambient pressure by removing the tube to the vacuum pump. The fill valve was then opened and the piston was retracted to around four-fifths to take up the fluid. This valve was closed and the fluid in the barrel was compressed to 1 MPa. The volume of the cylinder was zeroed on the control software. The delivery valve was opened and the piston was driven forward to inject the fluid but stopped just before the end of the stroke. The delivery valve was closed, the cylinder was re-compressed to 1 MPa and the volume injected was recorded. The pressure of barrel was set to 0.1 MPa and the fill valve was opened once this was reached. New fluid was taken up and this process was repeated until the system pressure reached 1 MPa, with the volume injected in each stroke being recorded. On the last stroke, the pump was set to constant pressure mode so as to control the pressure of the system. Once equilibrium was reached, the volume of the final stroke was noted. The volume of the system at 298.15 K found by this method was 44.09  $\text{cm}^3$ . This system volume calibration was performed three times and was found to be repeatable to  $\pm 0.01 \text{ cm}^3$  with an overall standard uncertainty of 0.09  $\text{cm}^3$ , or 0.2%  $\cdot V$ .



## 5. MIXTURE PREPARATION

A sample of pure deionized water was degassed while stirring under vacuum with the delivery valve of the syringe pump closed. Meanwhile, the system was evacuated through valves V2 and V3 (see Figure 1). The temperature of the viscometer and densimeter was controlled to the temperature of the laboratory (294.15 K) to ensure isothermal filling.

CO<sub>2</sub> was admitted through valve V1 to an initial charging pressure of (1, 2 or 3) MPa, based on estimates of the solubility in water obtained the model by Duan *et al.*,<sup>26</sup> originally developed in<sup>27</sup>. Since the VW sensor could only operate correctly in the single phase compressed liquid region, it was important not to introduce an excess of CO<sub>2</sub>.

Water was then injected step-wise following the same procedure outlined in the calibration for the system volume, except it was injected to a pressure of typically 15 MPa. Once this pressure was reached, the mixture was homogenized using the circulating pump. The total volume injected was monitored using the syringe pump control software. It took around 3 h to achieve a homogeneous mixture. At this point, the volume of the syringe pump on the final stroke was noted to allow calculation of the amount of water injected. It was then possible to determine the mole fraction  $x$  of CO<sub>2</sub> in the homogenous mixture. Measurements were performed with the pressure always above the bubble point at the experimental temperature to ensure that the system remained in the homogeneous compressed liquid region.

The standard uncertainty  $u(x)$  of the mole fraction of CO<sub>2</sub> is related to the standard relative uncertainties  $u_r(n_1)$  and  $u_r(n_2)$  of the amounts  $n_1$  and  $n_2$  of CO<sub>2</sub> and water, respectively, as follows:

$$u^2(x) = [x(1-x)]^2 [u_r^2(n_1) + u_r^2(n_2)]. \quad (10)$$

Since the CO<sub>2</sub> filling pressure was low,  $u_r(n_1)$  may be related approximately to the standard relative uncertainties of pressure, temperature and system volume by means of a perfect-gas approximation which gives:

$$u_r^2(n_1) = u_r^2(p) + u_r^2(T) + u_r^2(V). \quad (11)$$

For the water,  $u_r(n_2)$  may be expressed in terms of the standard uncertainties of pressure and temperature and the standard relative uncertainty of the system volume as follows:

$$u_r^2(n_2) = [\beta_T u(p)]^2 + [\alpha_p u(T)]^2 + u_r^2(V), \quad (12)$$

where  $\alpha_p$  is the isobaric expansivity and  $\beta_T$  the isothermal compressibility of water. Since the parts of the system volume other than the viscometer and the densimeter were not temperature controlled, an enlarged temperature uncertainty of 1 K is ascribed to the filling condition. On the other hand, since the CO<sub>2</sub> filling pressure was measured immediately after re-zeroing of the pressure transducer, a reduced uncertainty of 0.05 MPa was ascribed to that pressure. The terms involving  $\alpha_p$  and  $\beta_T$  turn out to be entirely negligible, and the remaining

terms are dominated by the pressure uncertainty in equation (11); recognizing also that  $x \ll 1$ , the following simple approximation for  $u(x)$  suffices for practical calculations:

$$u(x) \approx xu_r(p). \quad (13)$$

This gives  $u(x) = 0.0004$  for all mixtures studied.

## 6. UNCERTAINTY BUDGET FOR DENSITY AND VISCOSITY

The standard uncertainties of the state variables  $T$ ,  $p$  and  $x$  have been detailed above and we now consider the uncertainties of the measured density and viscosity. Since the density is a required input in the determination of the viscosity, we consider first the overall uncertainty of the density. The standard uncertainty in the density  $u(\rho)$  is associated with the standard uncertainties  $u(T)$ ,  $u(p)$ ,  $u(x)$  and  $u(\tau)$  in temperature, pressure, mole fraction and period respectively. Additionally,  $u(\rho)$  is influenced by the uncertainties  $u(\tau_0)$  and  $u(A)$  of the calibration parameters  $\tau_0$  and  $A$ . These terms have been discussed above, except for the  $u(\tau)$  which we take to be  $0.020 \mu\text{s}$  to encompass the observed repeatability uncertainty. The uncertainty budget for density is exemplified in Table 3 for the case of the median temperature, pressure and mole fraction. The uncertainty was found not to vary significantly over the range of conditions investigated and the median-state standard relative uncertainty of 0.033 % was therefore ascribed to all densities.

The standard uncertainty in the viscosity  $u(\eta)$  is associated with the standard uncertainties of temperature, pressure and mole fraction, and also with the standard uncertainties of the density, the wire radius and its thermal expansivity, the vacuum decrement, and finally the repeatability uncertainty. The uncertainty budget for viscosity is exemplified in Table 4 for the case of the median temperature, pressure and mole fraction. The two most significant terms are the uncertainties in the calibrated radius and the repeatability uncertainty. The latter was estimated from repeated check measurements on pure water to be  $0.005 \cdot \eta$ . As with the density, the uncertainty of the viscosity was found to vary little over the range of conditions investigated and the median-state standard relative uncertainty of 0.7 % was therefore ascribed to all viscosities.

## 7. EXPERIMENTAL RESULTS AND CORRELATIONS

Measurements were performed in the temperature range (294 to 449) K for viscosity and (274 to 449) K for density, at nominal pressures of (15, 30, 50, 70 and 100) MPa, and at mole fractions of  $\text{CO}_2$  of approximately (0.009, 0.017 and 0.027). The state points selected for measurements were guided by the solubility model of Duan *et al.*<sup>26, 27</sup> and chosen such that the mixture remained in a single-phase state. As a consequence, some combinations of temperature, pressure and mole fraction implied by the ranges above were avoided. Although the apparatus was designed for simultaneous measurements of density and viscosity, the present results for these two properties were actually obtained in separate experiments.

## 7.1 Density

The density results are given in Table 5. The approximate overall relative standard uncertainty in density across all points is 0.4 kg.m<sup>-3</sup>. The data show a linear dependence upon  $x$  at constant  $T$  and  $p$  as illustrated in Figures 2a and 2b for low and high temperature, respectively. In order to analyze the data further, the molar volume  $V_m$  of the solution is considered and, as shown in Figure 3 (for an example pressure of 70 MPa), this too is a linear function of  $x$ . Similar behavior is observed at each temperature and pressure and we therefore assume that the partial molar volumes of H<sub>2</sub>O ( $V_w$ ) and of CO<sub>2</sub> ( $V_{CO_2}$ ) are independent of  $x$  within the range investigated and we correlated the data at each  $T$  and  $p$  as follows:

$$V_m = Ax + B. \quad (14)$$

In order to constrain the correlation at  $x = 0$ , the experimental data were augmented by values of the molar volume of pure water at each experimental temperature and pressure calculated from the IAPWS-95 equation of state. Thus at the majority of temperatures and pressures, four values of the molar volume were used to determine the two parameters in equation (14) by means of a linear regression.

In terms of the parameters in Equation 14, the partial molar volume of CO<sub>2</sub> is given by:

$$\begin{aligned} V_{CO_2} &= V_m + (1-x)(\partial V_m / \partial x)_{T,p} \\ &= A + B \end{aligned} \quad (15)$$

The standard uncertainty of  $V_{CO_2}$  determined in this way was, on average, 0.15 cm<sup>3</sup>.mol<sup>-1</sup>. Equation 14 also gives the molar volume of the solvent (pure water),  $V_w = B$ . Figure 4 shows  $V_{CO_2}$  as a function of temperature along each isobar and, from this, a six parameter correlation has been established for  $V_{CO_2}(T, p)$  that is linear in pressure and quadratic in temperature as follows:

$$V_{CO_2} / (\text{cm}^3 \cdot \text{mol}^{-1}) = \sum_{i=0}^2 \sum_{j=0}^1 a_{ij} (T/K)^i (p/\text{MPa})^j. \quad (16)$$

The values for the coefficients are given in Table 6 and the standard uncertainty of the correlation is 0.16 cm<sup>3</sup>.mol<sup>-1</sup>. The final model for the density of a mixture  $\rho(T, p, x)$  is based on the IAPWS-95 EOS for the molar volume of pure water<sup>24</sup> and equation (16) for the partial molar volume of CO<sub>2</sub> as follows:

$$\rho = \frac{xM_{CO_2} + (1-x)M_w}{xV_{CO_2} + (1-x)V_w}. \quad (17)$$

Figure 4 shows that  $V_{CO_2}$  increases in magnitude and becomes more dependent upon pressure with increasing temperature. Also shown in Figure 4 are data and models from the literature<sup>28-32</sup> and it can be seen that there is a fair degree of agreement. In particular, the model of Sedlbauer *et al.*<sup>32</sup> is in very close agreement with the present data at temperatures between (323 and 423) K at pressures up to 70 MPa. At other temperatures, and also at the

highest pressure, some deviations are apparent. At 274 K, the model of Sedlbauer *et al.* is about  $1 \text{ cm}^3 \cdot \text{mol}^{-1}$  greater than equation (16).

In Figure 5, we compare our experimental densities, along with data from the literature<sup>10, 13, 33</sup>, with our model (equations 16 and 17) as functions of  $x$ ,  $T$  and  $p$ . The model represents all of the present experimental data within  $\pm 0.04\%$  and the deviations do not depend systematically on any of the three independent variables. The experimental values plotted at  $x = 0$  are derived from the values of  $B$  in equation (14) determined at each experimental temperature and pressure. King *et al.*<sup>33</sup> performed measurements in the temperature range (288 to 313) K at pressures up to around 20 MPa with a claimed uncertainty of 0.5%. From Figure 5, we see that these data agree with the present model to within  $\pm 0.25\%$ . Hebach *et al.*<sup>13</sup> determined densities using a calibrated vibrating tube densimeter with a claimed uncertainty of 0.15% at temperatures from (284 to 332) K and pressures up to 30 MPa; their data agree with the present model mostly to within  $\pm 0.2\%$ . Li *et al.*<sup>10</sup> reports measurements performed with a PVT apparatus coupled to a densimeter in a pressure range of (0.3 to 29) MPa at a single temperature of 332 K, and the maximum uncertainty in density was claimed to be  $0.1 \text{ kg} \cdot \text{m}^{-3}$ , or about 0.01%. However, from Figure 5, we see that there are deviations of up to 0.4% from our correlation.

## 7.2 Viscosity

The viscosity results are given in Table 7. The determination of viscosity with the VW viscometer requires knowledge of the fluid density and the values used were those obtained in the present study. The viscosity data show a linear dependence upon both pressure and the mole fraction  $x$  of dissolved  $\text{CO}_2$ . The dependence of the viscosity upon mole fraction  $x$  at constant  $T$  and  $p$  is illustrated in Figures 6a and 6b for low and high temperature, respectively, and it can be seen that the effect is more pronounced at low temperature. Here, increasing the  $\text{CO}_2$  concentration to near saturation increases the viscosity of the mixture by about 10% from that of pure water. However, at the highest temperature studied the relative effect is just over 1%. The dependence of the viscosity upon pressure at constant  $T$  and  $x$  was also observed to be linear to within the experimental uncertainty.

For practical applications, a correlation of the data is desirable. In order to constrain the correlation at  $x = 0$ , the experimental data were augmented by values of the viscosity of pure liquid water computed from the IAPWS recommended equation for water viscosity<sup>25</sup> at each experimental temperature and pressure. Additionally, calculated data were added at  $T = 274 \text{ K}$  and each experimental pressure.

Motivated by the observed dependence upon  $p$  and  $x$ , a correlation of the form

$$\ln \eta = \ln \eta_0 + f_1 x + f_2 p \quad (18)$$

was tested in which  $\eta_0$  represents the viscosity of the hypothetical pure liquid water at temperature  $T$  and  $p = 0$ , and  $f_1$  and  $f_2$  are functions of temperature only. Figure 7 shows the values of  $\eta_0$ ,  $f_1$  and  $f_2$  obtained from analysis of the data at each temperature. It was found

that  $f_1$  decreased exponentially with increasing temperature, while  $f_2$  could be represented as a linear function of inverse temperature. Accordingly, the following modified Vogel-Fulcher-Tamman (VFT) equation was used to correlate the data:

$$\ln[\eta/(\text{mPa} \cdot \text{s})] = a + b(p/p_0) + \frac{c + d(p/p_0)}{(T/T_0 - 1)} + e_1 \exp[-e_2(T/T_0 - 1)]x. \quad (19)$$

Here,  $p_0 = 1$  MPa, and  $a$ ,  $b$ ,  $c$ ,  $d$ ,  $e_1$ ,  $e_2$  and  $T_0$  are parameters. This form of this equation (without the fourth term) is used extensively for modelling the effects of temperature and pressure on viscosity. Three of the seven parameters ( $a$ ,  $c$  and  $T_0$ ) describe the viscosity of pure liquid water as a function of temperature at  $p = 0$ , two of them ( $b$  and  $d$ ) describe the dependence upon pressure, and the remaining two are required to account for the dissolved  $\text{CO}_2$ . The parameters of the model were fitted to the augmented data set using an objective function based on the absolute average relative deviation, defined by

$$\Delta_{\text{AAD}} = \frac{1}{N} \sum_{i=1}^N \left( \frac{|\eta_i - \eta_{i,\text{fit}}|}{\eta_i} \right). \quad (20)$$

Here,  $\eta_i$  is an experimental datum,  $\eta_{i,\text{fit}}$  is calculated from the correlation applied at the same state point, and  $N$  is the total number of points. This resulted in the parameters reported in Table 8. The absolute average relative deviation for the fit was 0.4 % while the maximum absolute relative deviation was 1.7%.

In Figure 8, we plot the deviations of the present data from the surface-fit correlation. It can be noticed that the present model applied at  $x = 0$  agrees closely with the IAPWS recommended viscosity equation.<sup>25</sup> In fact, except at  $T < 278$  K the agreement is well with  $\pm 1$  %; the absolute relative deviation between equation (19) and the IAPWS formulation increase somewhat near the triple point where it reaches a maximum of 1.7%. Also shown in Figure 8 are the measurements reported by Kumagai *et al.*<sup>11</sup> which agree with the correlation to within  $\pm 2$ %. These data were gathered at temperatures of (273.15 to 278.1) K and the good agreement observed validates the present model for application at temperatures down to 273.15 K. It should be noted that there exists a second literature data set, not shown in Figure 8: that of Uchida *et al.*<sup>12</sup> based on dynamic light scattering experiments on saturated solutions at pressures of (0.7 and 5.0) MPa. Unfortunately, these data have a relative uncertainty of about 6 % which is too large to resolve the effect of dissolved  $\text{CO}_2$  at the lower pressure investigated. Furthermore, the data at the higher pressure were gathered in states at which  $\text{CO}_2$  hydrates are stable; these showed a strong dependence upon time and deviate from the present model by as much as 40 %.

## 8. CONCLUSION

Experimental and modelling results are reported for the density and viscosity of pure water with known mole fractions of dissolved  $\text{CO}_2$ . The density model is based on the partial molar volume for  $\text{CO}_2$  in aqueous solution. This quantity has been correlated from (274 to 449) K

and from the bubble pressure to  $p = 100$  MPa. When combined with the IAPWS-95 equation of state of pure water, this correlation represents the measured densities of under-saturated solutions of  $\text{CO}_2$  in water within  $\pm 0.04\%$

The modified Vogel-Fulcher-Tamman equation was used to correlate the viscosity as a function of temperature, pressure and mole fraction of  $\text{CO}_2$  with an absolute average relative deviation of 0.4 %. This model is valid from (273 to 449) K and from the bubble pressure to  $p = 100$  MPa. At  $x = 0$ , the model is in good agreement with the IAPWS recommended equation for water viscosity.

Combined with the model of Duan *et al.*<sup>26,27</sup> for  $\text{CO}_2$  solubility, we have a complete model for the density and viscosity of both saturated and under-saturated solutions of  $\text{CO}_2$  in water.

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**Table 1.** Available experimental data for viscosity  $\eta$  and density  $\rho$  of (H<sub>2</sub>O + CO<sub>2</sub>) with relative uncertainty  $U_r$  at temperatures  $T$  and pressures  $p$ .

Reference	Property	Phase	$T/(K)$	$p/(MPa)$	$x_2$	$U_r$
Kumagai <i>et al.</i> <sup>11</sup>	$\eta$	L	273 - 278	0.1 to 30	$\leq 1.59 \times 10^{-2}$	1.5 %
Uchida <i>et al.</i> <sup>12</sup>	$\eta$	L	273 - 282	0.7 to 5	Saturation	2.3 %
Tabasinejad <i>et al.</i> <sup>2</sup>	$\rho$	G & L	382 - 478	3.5 to 129	Saturation	< 0.01 %
Li <i>et al.</i> <sup>10</sup>	$\rho$	L	332	3.3 to 29	Saturation	0.01 %
Hebach <i>et al.</i> <sup>13</sup>	$\rho$	L	284 - 333	1.0 to 30	Saturation	0.15 %
Yaginuma <i>et al.</i> <sup>14</sup>	$\rho$	G & L	304	1.0 to 10	Saturation	0.01 %

**Table 2.** Description of chemical samples

Chemical name	Source	Purity	Additional purification
Carbon dioxide	BOC	0.99995	None
Water	Millipore Direct-Q UV3 apparatus	Electrical resistivity > 18 M $\Omega$ ·cm at $T = 298$ K	Degassed under vacuum

**Table 3.** Uncertainty budget for density at the median state point in terms of standard uncertainty  $u(X)$  of dimensionless parameter  $X$  and arising contribution  $u_r(\rho)$  to the overall standard relative uncertainty of density.

Dimensionless parameter	Value	Standard uncertainty	$10^2 u_r(\rho)$
$T / \text{K}$	373.150	0.025	0.002
$p / \text{MPa}$	50.0	0.1	0.004
$x$	0.0170	0.0004	0.016
$\tau / \mu\text{s}$	2656.18	0.020 <sup>a</sup>	0.027
$\tau_o / \mu\text{s}$	2580.58	0.003	0.004
$A / (\text{kg}\cdot\text{m}^{-3}\cdot\mu\text{s}^{-2})$	$2.4919 \times 10^{-3}$	$1.6 \times 10^{-7}$	0.006
Overall combined standard relative uncertainty			0.033

<sup>a</sup> includes repeatability uncertainty.

**Table 4.** Uncertainty budget for viscosity at the median state point in terms of standard uncertainty  $u(X)$  of dimensionless parameter  $X$  and arising contribution  $u_r(\eta)$  to the overall standard relative uncertainty of viscosity.

Dimensionless parameter $X$	$X$	$u(X)$	$10^2 u_r(\eta)$
$T / \text{K}$	373.150	0.025	0.03
$p / \text{MPa}$	50.0	0.1	0.01
$x$	0.0170	0.0001	0.01
$\rho / (\text{kg}\cdot\text{m}^{-3})$	986.53	0.46	0.04
$R / \mu\text{m}$	73.04	0.18	0.50
$10^6 \Delta_0$	29.9	15	0.03
$\alpha_w / (10^{-6} \text{K}^{-1})$	8.7	0.4	0.01
$\eta / (\text{mPa}\cdot\text{s})$	0.5778	0.0029 <sup>a</sup>	0.50
Overall combined standard relative uncertainty			0.71

<sup>a</sup> repeatability uncertainty.

**Table 5.** Experimental densities  $\rho$  of [(1 - x) H<sub>2</sub>O + x CO<sub>2</sub>] at temperatures  $T$  and pressures  $p$ .<sup>a</sup>

$p$ / MPa	$\rho$ / (kg.m <sup>-3</sup> )	$p$ / MPa	$\rho$ / (kg.m <sup>-3</sup> )	$p$ / MPa	$\rho$ / (kg.m <sup>-3</sup> )
$x = 0.0086$					
$T = 274.73$ K		$T = 296.17$ K		$T = 323.45$ K	
15.01	1012.0	15.10	1008.6	15.02	998.4
30.11	1019.0	30.20	1015.0	30.13	1004.7
50.24	1028.1	50.26	1023.4	50.25	1012.8
70.36	1036.8	70.33	1031.4	70.36	1020.6
100.67	1049.3	100.65	1042.9	100.72	1031.6
$T = 348.32$ K		$T = 373.42$ K		$T = 398.55$ K	
15.05	984.8	15.09	967.8	15.06	948.3
30.15	991.3	30.18	974.6	30.17	955.6
50.27	999.5	50.28	983.2	50.29	964.9
70.37	1007.3	70.39	991.5	70.39	973.7
100.71	1018.6	100.71	1003.2	100.71	986.0
$T = 423.92$ K		$T = 449.20$ K			
15.07	925.9	15.08	900.7		
30.18	934.0	30.19	909.9		
50.30	944.2	50.31	921.3		
70.42	953.8	70.42	931.8		
100.71	967.1	100.71	946.4		
$x = 0.0168$					
$T = 274.77$ K		$T = 296.19$ K		$T = 323.43$ K	
15.08	1017.3	15.07	1013.3	15.06	1002.5
30.19	1024.1	30.17	1019.7	30.18	1008.8
50.31	1033.0	50.30	1027.9	50.30	1016.9
70.43	1041.6	70.41	1035.9	70.42	1024.6
100.71	1053.9	100.73	1047.3	100.72	1035.7
$T = 348.38$ K		$T = 373.46$ K		$T = 398.55$ K	
30.20	994.9	30.19	977.8	30.19	958.2
50.32	1003.2	50.32	986.5	50.33	967.8
70.45	1011.1	70.45	994.9	70.46	976.7
100.74	1022.4	100.74	1006.7	100.73	989.4
$T = 423.93$ K		$T = 449.20$ K			
30.20	935.7	30.21	910.8		
50.34	946.2	50.36	922.6		
70.46	956.0	70.47	933.5		
100.73	969.7	100.74	948.4		

$p / \text{MPa}$	$\rho / (\text{kg}\cdot\text{m}^{-3})$	$p / \text{MPa}$	$\rho / (\text{kg}\cdot\text{m}^{-3})$	$p / \text{MPa}$	$\rho / (\text{kg}\cdot\text{m}^{-3})$
$x = 0.0271$					
$T = 274.72 \text{ K}$		$T = 296.18 \text{ K}$		$T = 323.43 \text{ K}$	
30.29	1030.1	30.25	1025.3	70.46	1029.6
50.41	1038.8	50.36	1033.4	100.78	1040.7
70.53	1047.2	70.44	1041.2		
100.77	1059.2	100.76	1052.6		
$T = 348.33 \text{ K}$		$T = 373.38 \text{ K}$		$T = 398.48 \text{ K}$	
70.58	1015.3	70.59	998.2	50.47	970.0
100.78	1026.8	100.80	1010.3	70.60	979.3
				100.80	992.1
$T = 423.84 \text{ K}$		$T = 449.17 \text{ K}$			
50.46	948.0	50.45	923.6		
70.58	958.1	70.57	934.9		
100.81	972.1	100.80	950.3		

<sup>a</sup> standard uncertainties are  $u(T) = 0.025 \text{ K}$ ,  $u(p) = 0.1 \text{ MPa}$ , and  $u(\rho) = 0.00033 \cdot \rho$ .

**Table 6.** Coefficients of equation 16 for the partial molar volume of  $\text{CO}_2$  in aqueous solution.

$a_{0,0}$	$a_{1,0}$	$a_{2,0}$	$a_{0,1}$	$a_{1,1}$	$a_{2,1}$
51.19	-0.15575	$3.2955 \times 10^{-4}$	$-6.0708 \times 10^{-2}$	$5.5026 \times 10^{-4}$	$-1.2114 \times 10^{-6}$

**Table 7.** Experimental viscosities  $\eta$  of [(1 - x) H<sub>2</sub>O + x CO<sub>2</sub>] at temperatures  $T$  and pressures  $p$ .<sup>a</sup>

$p$ / MPa	$\eta$ / (mPa.s)	$p$ / MPa	$\eta$ / (mPa.s)	$p$ / MPa	$\eta$ / (mPa.s)
$x = 0.0086$					
$T = 294.30$ K		$T = 322.93$ K		$T = 373.13$ K	
15.1	1.013	15.0	0.560	15.0	0.286
30.2	1.014	30.1	0.564	30.1	0.291
50.3	1.012	50.2	0.568	50.2	0.297
70.3	1.008	70.2	0.573	70.3	0.302
96.4	1.008	96.3	0.582	96.4	0.308
$T = 397.98$ K		$T = 424.03$ K		$T = 448.93$ K	
30.1	0.231	30.1	0.190	30.0	0.162
50.2	0.236	50.2	0.194	50.1	0.167
70.3	0.242	70.2	0.199	70.2	0.172
96.4	0.248	96.4	0.205	96.3	0.178
$x = 0.0168$					
$T = 294.27$ K		$T = 322.91$ K		$T = 373.03$ K	
15.1	1.049	15.0	0.568	30.1	0.2932
30.2	1.044	30.1	0.573	50.2	0.2989
50.2	1.044	50.2	0.578	70.2	0.3040
70.2	1.041	70.2	0.584	96.2	0.3111
96.3	1.046	96.2	0.592		
$T = 397.88$ K		$T = 422.91$ K		$T = 448.29$ K	
30.1	0.233	30.0	0.192	30.0	0.163
50.2	0.238	50.1	0.196	50.1	0.168
70.2	0.244	70.2	0.202	70.1	0.173
96.3	0.250	96.2	0.208	96.2	0.179
$x = 0.0271$					
$T = 294.31$ K		$T = 323.12$ K		$T = 374.09$ K	
30.3	1.096	70.4	0.606	70.3	0.309
50.3	1.095	96.5	0.615	96.4	0.318
70.4	1.097				
96.5	1.100				
$T = 398.98$ K		$T = 423.82$ K		$T = 448.71$ K	
50.2	0.241	50.2	0.198	50.2	0.169
70.2	0.245	70.3	0.204	70.2	0.173
96.3	0.254	96.5	0.210	96.4	0.179

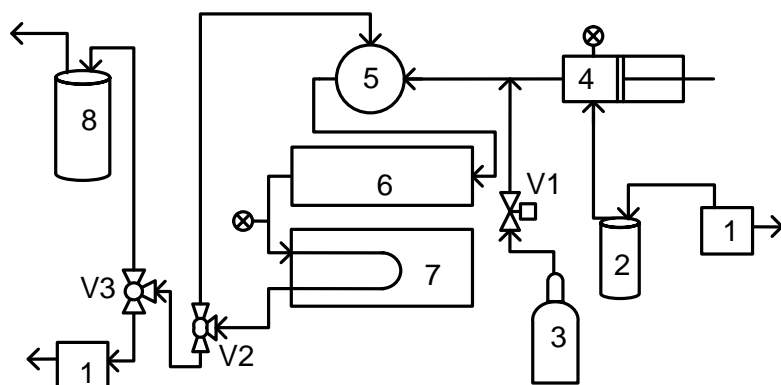
<sup>a</sup> standard uncertainties are  $u(T) = 0.025$  K,  $u(p) = 0.1$  MPa, and  $u(\eta) = 0.007 \cdot \eta$ .

**Table 8.** Parameters in equation 19 for the viscosity of [(1 - x) H<sub>2</sub>O + x CO<sub>2</sub>].

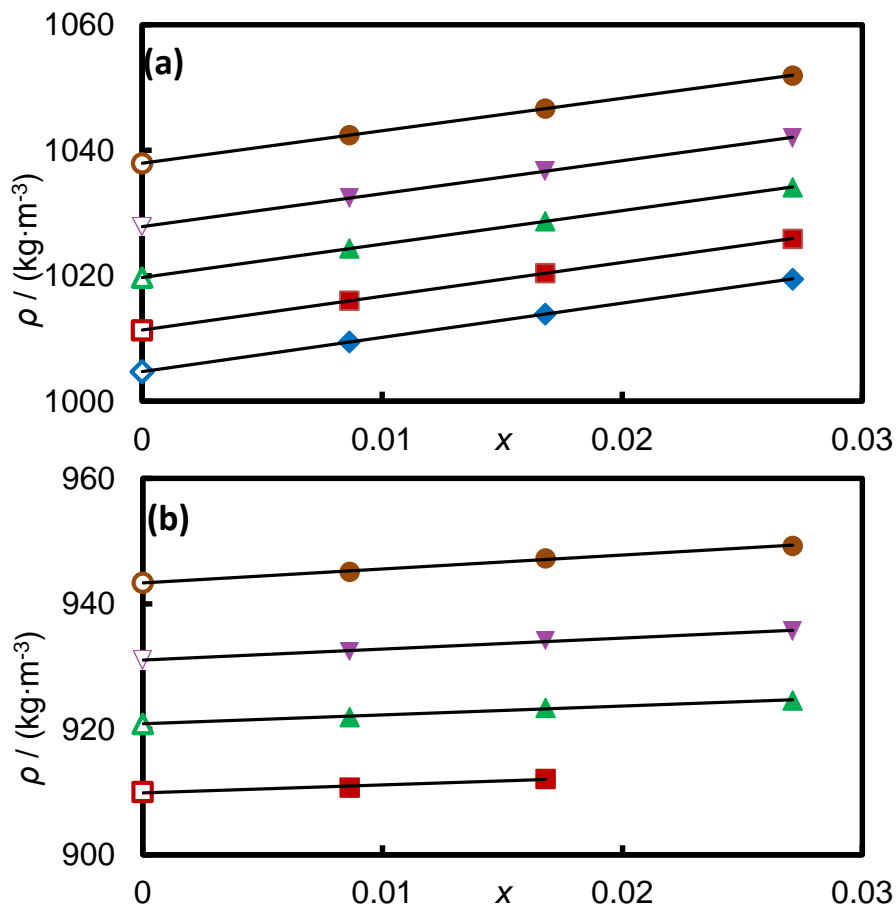
<i>a</i>	<i>c</i>	<i>b</i>	<i>d</i>	<i>e</i> <sub>1</sub>	<i>e</i> <sub>2</sub>	<i>T</i> <sub>0</sub> / K
-3.705013	3.98950	0.00289258	-0.00326	65.55968	2.46811	141.5



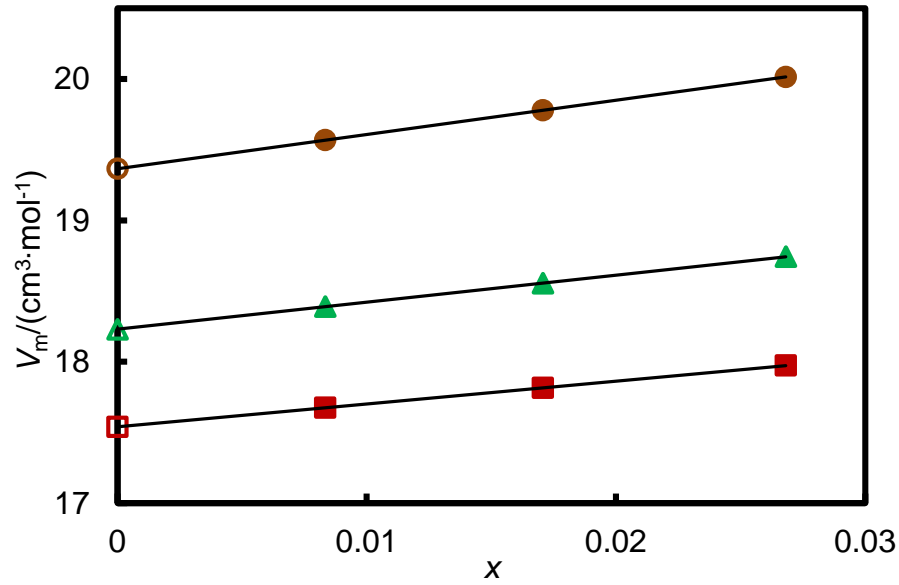
FIGURES



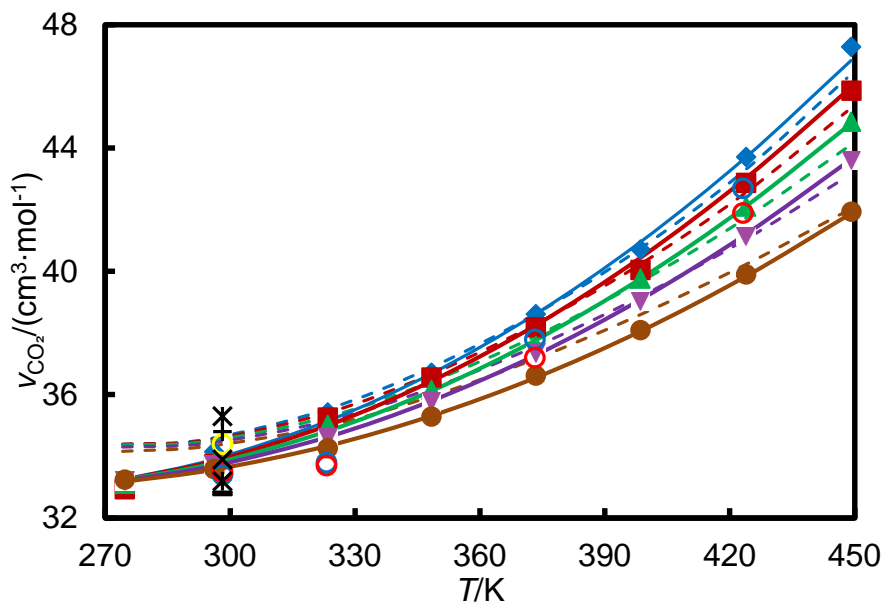
**Figure 1.** Schematic of VW-VT Apparatus: (1) vacuum pump, (2) water reservoir, (3) CO<sub>2</sub> cylinder, (4) syringe pump, (5) circulating pump, (6) vibrating wire viscometer, (7) vibrating tube densimeter, (8) waste, (V1 to V3) valves.



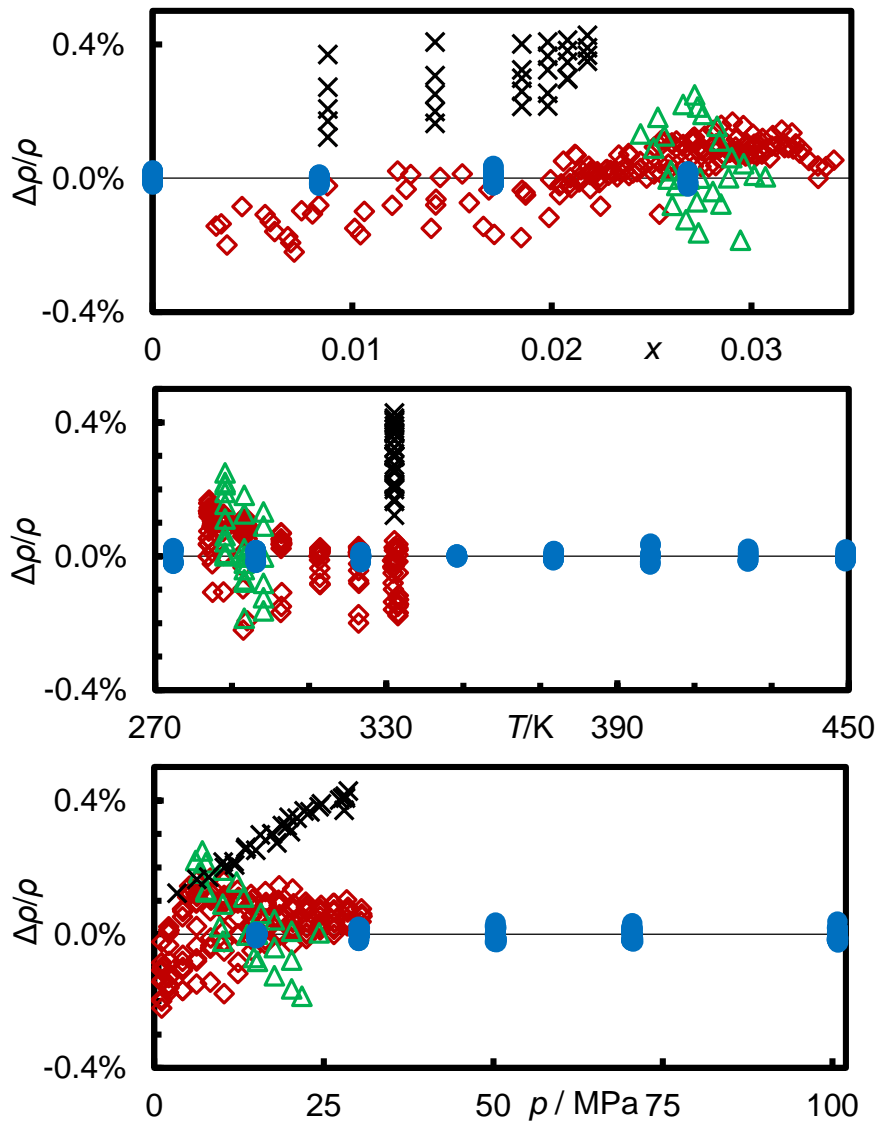
**Figure 2.** Densities  $\rho$  of  $[(1-x)\text{H}_2\text{O} + x\text{CO}_2]$  as a function of  $x$  at (a)  $T = 296 \text{ K}$  and (b)  $T = 449 \text{ K}$ . Experimental data:  $\blacklozenge$ , 15 MPa;  $\blacksquare$ , 30 MPa;  $\blacktriangle$ , 50 MPa;  $\blacktriangledown$ , 70 MPa,  $\bullet$ , 100 MPa. Open symbols at  $x = 0$  are calculated from IAPWS-95 equation of state.<sup>24</sup> Solid lines are linear regression lines.



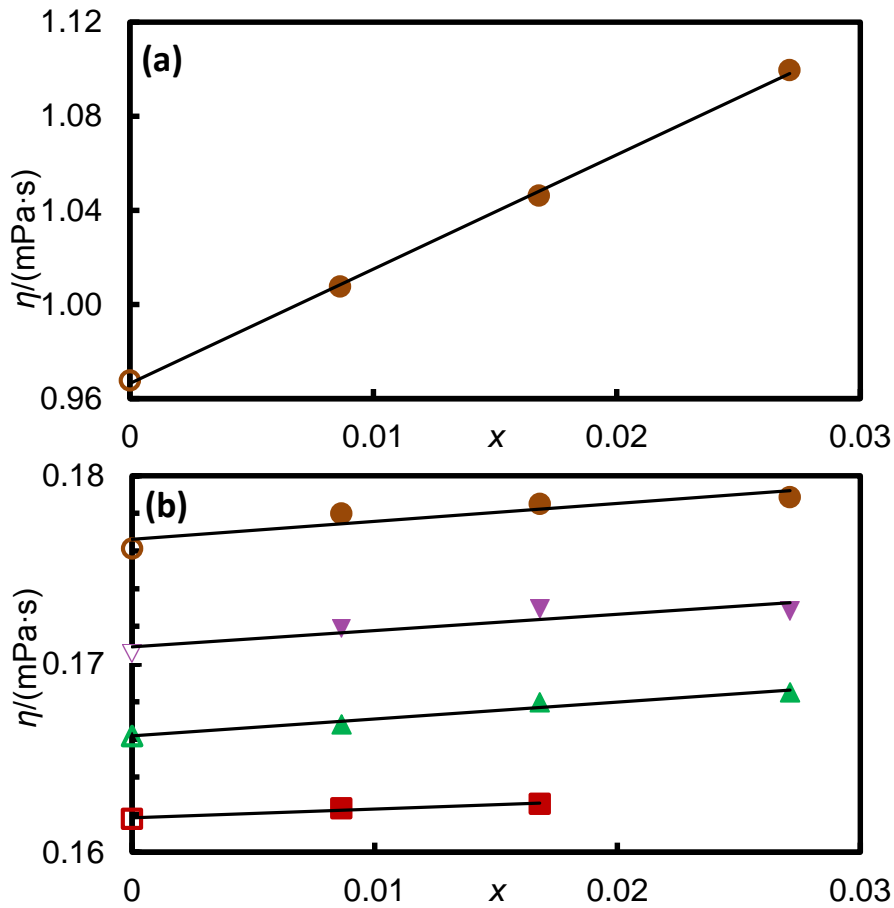
**Figure 3.** Molar volume  $V_m$  of  $[(1 - x) \text{H}_2\text{O} + x \text{CO}_2]$  as a function of  $x$  at  $p = 70$  MPa. Experimental data: ■, 296 K; ▲, 373 K; ●, 449 K. Open symbols at  $x = 0$  are calculated from IAPWS-95 equation of state.<sup>24</sup> Solid lines are linear regression lines.



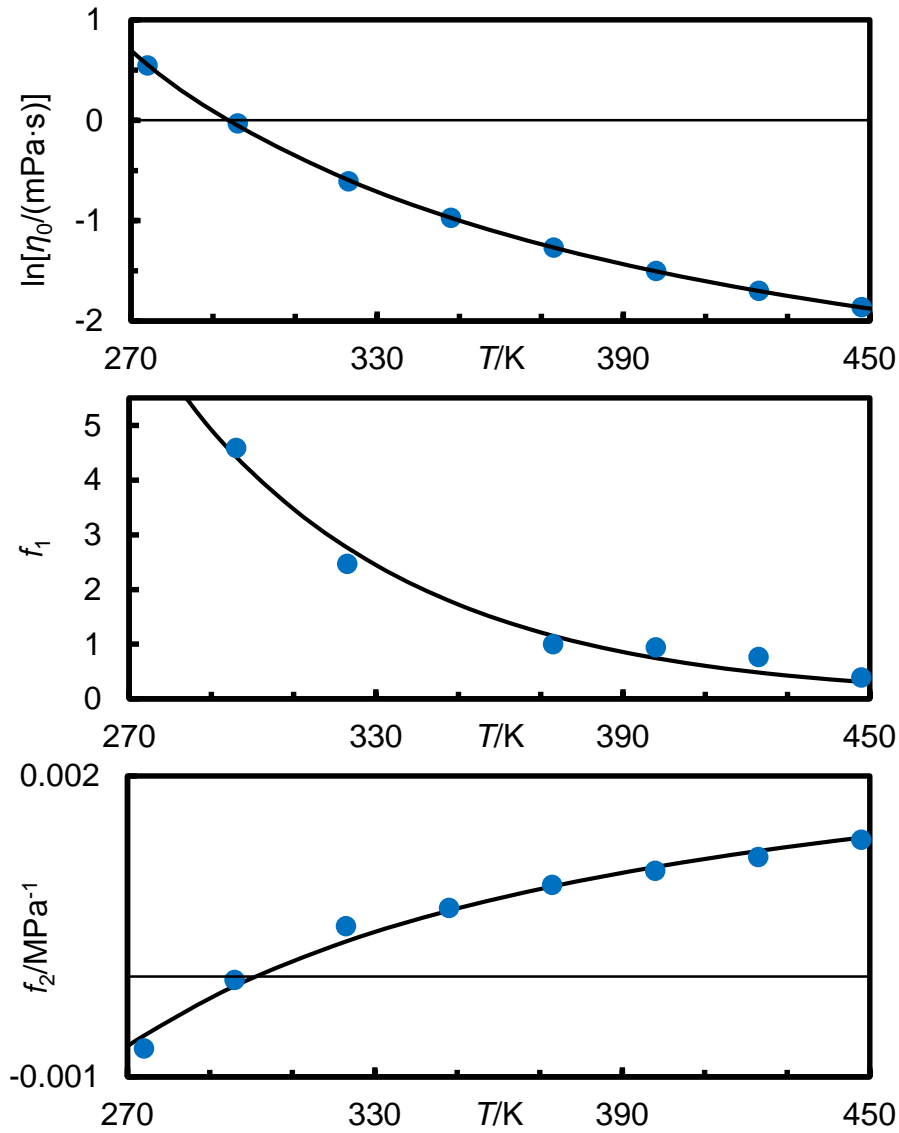
**Figure 4.** Partial molar volume  $V_{\text{CO}_2}$  of  $\text{CO}_2$  in aqueous solution as a function of temperature  $T$ . This work:  $\blacklozenge$ , 15 MPa;  $\blacksquare$ , 30 MPa;  $\blacktriangle$ , 50 MPa;  $\blacktriangledown$ , 70 MPa,  $\bullet$ , 100 MPa. Literature data at  $p > 0.1$  MPa:  $\circ$ , Hněkovský *et al.*<sup>28</sup> at pressures of 1 MPa (yellow), 20 MPa (blue) and 35 MPa (red). Literature data at  $p = 0.1$  MPa:  $\text{—}$ , Barbero *et al.*<sup>31</sup>;  $\times$ , Moore *et al.*<sup>29</sup>;  $+$  Enns *et al.*<sup>30</sup>; and  $\ast$ , Ellis *et al.*<sup>34</sup>. Solid lines and dashed lines represent equation (16) and the model of Sedlbauer *et al.*<sup>32</sup>, respectively, at pressures (from the top down) of (15, 30, 50, 70 and 100) MPa.



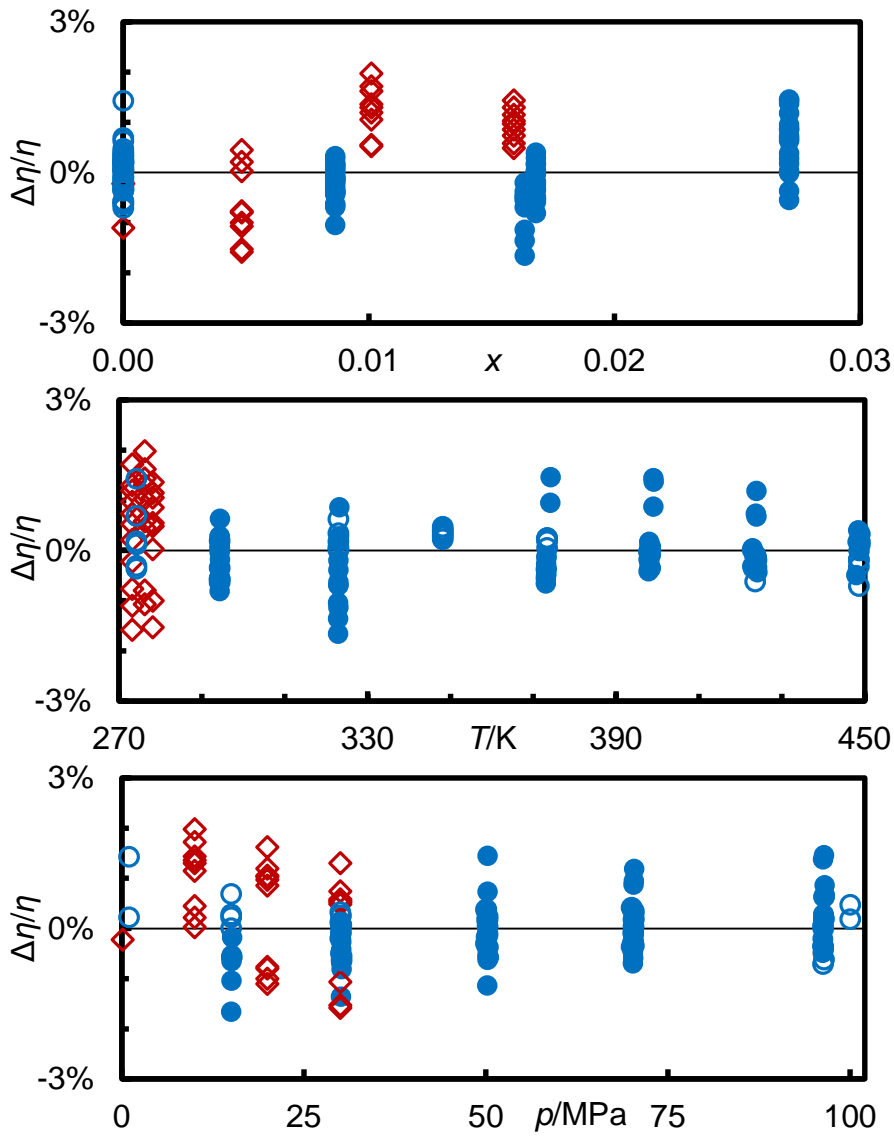
**Figure 5.** Deviations  $\Delta\rho = (\rho_{\text{exp}} - \rho_{\text{calc}})$  between experimental densities  $\rho_{\text{exp}}$  of  $[(1 - x) \text{H}_2\text{O} + x \text{CO}_2]$  and densities  $\rho_{\text{calc}}$  calculated from equations (16) and (17) with the IAPWS-95 equation of state for the density of pure water:<sup>24</sup> ●, this work; ◇ Hebach *et al.*<sup>13</sup>; △ King *et al.*<sup>33</sup>; and ✕ Li *et al.*<sup>10</sup>.



**Figure 6.** Viscosities  $\eta$  of  $[(1 - x) \text{H}_2\text{O} + x \text{CO}_2]$  as a function of  $x$  at (a)  $T = 296$  K and (b)  $T = 449$  K. Experimental data: ■, 30 MPa; ▲, 50 MPa; ▼, 70 MPa, ●, 96 MPa. Open symbols at  $x = 0$  are calculated from the IAPWS-95 equation for water viscosity.<sup>25</sup> Solid lines are linear regression lines.



**Figure 7.** Parameters  $\eta_0$ ,  $f_1$ , and  $f_2$  determined with equation (18) from the experimental viscosities of  $[(1 - x) \text{H}_2\text{O} + x \text{CO}_2]$  at temperatures  $T$ : ●, isothermal fits; —, surface fit.



**Figure 8.** Deviations  $\Delta\eta = (\eta_{\text{exp}} - \eta_{\text{calc}})$  between experimental viscosities  $\eta_{\text{exp}}$  of  $[(1 - x) \text{H}_2\text{O} + x \text{CO}_2]$  and viscosities  $\eta_{\text{calc}}$  calculated from equation (19): ●, this work; ○, pure water from IAPWS equation;<sup>25</sup> ◇, Kumagai *et al.*<sup>11</sup>