

# Determining the slag fraction, water/binder ratio and degree of hydration in hardened cement pastes

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## Abstract

A method for determining the original mix composition of hardened slag-blended cement-based materials based on analysis of backscattered electron images combined with loss on ignition measurements is presented. The method does not require comparison to reference standards or prior knowledge of the composition of the binders used. Therefore, it is well-suited for application to real structures. The method is also able to calculate the degrees of reaction of slag and cement. Results obtained from an experimental study involving sixty samples with a wide range of water/binder (w/b) ratios (0.30 to 0.50), slag/binder ratios (0 to 0.6) and curing ages (3 days to 1 year) show that the method is very promising. The mean absolute errors for the estimated slag, water and cement contents ( $\text{kg/m}^3$ ), w/b and s/b ratios were 9.1%, 1.5%, 2.5%, 4.7% and 8.7%, respectively. 91% of the estimated w/b ratios were within 0.036 of the actual values.

**Keywords:** *Backscattered electron imaging; Image analysis; Slag; Water-binder ratio; Degree of hydration*

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34 **1 Introduction**

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37 Ground-granulated blastfurnace slag (GGBS) is increasingly being used in concrete due to its many benefits. For  
38 example, partial replacement of Portland cement with slag is commonly specified for structures exposed to sea-water  
39 because slag greatly enhances the resistance of concrete to chloride ingress and therefore delays the time until  
40 embedded reinforcement starts to corrode. Slag also reduces the total heat released and peak temperature reached during  
41 the early life of thick concrete elements and therefore is specified to reduce the risk of early-age thermal cracking. The  
42 use of slag in concrete is also motivated by the desire to reduce the environmental impact of Portland cement clinker  
43 and to produce sustainable low-carbon concrete.

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46 To ensure the performance of hardened concrete, minimum and maximum limits of slag replacement of Portland  
47 cement and the mass ratio of water to total cementitious materials (w/b) are usually specified. Occasionally, disputes  
48 have arisen about the actual amount of slag present, or the w/b ratio, in an existing structure, especially when the  
49 structure has not performed to expectations. Knowledge of the slag/binder ratio and the water/binder ratio also greatly  
50 assists in predicting the residual life of concrete structures exposed to environments chemically aggressive to reinforced  
51 concrete such as marine environments. Therefore, there is a need for a reliable and rapid method for estimating the slag  
52 content and w/b ratio in concrete. However, once concrete has hardened, it is often very difficult to determine the exact  
53 amounts of cement, slag and water that were added during batching.

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56 Existing methods for determining the slag content in hardened concrete are reviewed in Table 1. Although several  
57 methods have been used, there is no widely accepted standard method nor is there agreement as to which is best.  
58 Testing of slag content in hardened concrete is known to be prone to errors. All of the prevailing methods require either  
59 the chemical composition of the original cement and slag used in the tested concrete to be known, or comparison with  
60 reference standards made with similar materials, mix proportions and curing conditions as the sample in question. In  
61 practice, the original materials that were used may be unknown or no longer available at the time of the investigation.  
62 Very often, it is the slag content by mass of total cementitious materials (s/b) that was specified and it is this that is  
63 more important with regard to concrete properties including most durability-related properties. If the test method  
64 determines the slag content by weight of concrete, this must be converted to slag content by mass of total cementitious

65 materials. This introduces additional errors since the Portland cement content used is an unknown that must be  
 66 measured separately. None of the methods reviewed in Table 1 are able to determine the s/b ratio or the w/b ratio.

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69 **Table 1: Review of methods for estimating the slag content in cement-based materials**

Method	Description	Accuracy/precision
Sulphide content [BS 1881: Pt 124:1988 [1]]	Slag is usually the only ingredient in concrete containing a significant amount of sulphide. Thus, the amount of slag in concrete can be estimated from its sulphide content provided the composition of the slag is known. However, not all sulphide is recovered so the slag content may be underestimated. The amount of soluble silica and calcium oxide originating from the slag or aggregates is required to determine cement content. Aggregates may contain sulphide and this must be taken into account.	No published precision data is available. A repeatability of 15-20% has been suggested based on experience [2]. Sangha et al. [3] found errors of 8-27% in the slag content for w/b 0.5 pastes containing 20-80% slag cured up to 56 days.
Energy-dispersive X-ray spectroscopy (EDS) [4-6]	The oxide compositions of the unreacted slag, unreacted cement and hydrated cement paste in the unknown sample are measured by SEM-EDS spot analyses. Similar measurements are carried out on reference standards containing known slag amounts. The s/b ratio is then estimated from the ternary plot of MgO, Al <sub>2</sub> O <sub>3</sub> and CaO, or from the plot of the ratio (MgO + Al <sub>2</sub> O <sub>3</sub> ) to binder and slag.	Precision based on repeated analyses of standards has been found to be ~ 2% at a slag replacement level of 25% [5].
X-ray diffraction [7]	The sample is ignited at 950-1050°C to devitrify the unreacted slag, then mixed with 10% CaF <sub>2</sub> (as internal standard) and analysed by XRD. To estimate slag content, the melilite/CaF <sub>2</sub> peak intensity ratio is measured and compared to those from mixtures of ignited slag from the same source as calibration. Note that only the unreacted slag fraction is measured and significant errors could occur if aggregates are not properly separated from the paste.	Hooton and Rogers [7] tested ten mortars with 0-90% slag that were cured for 28 days and found that the slag content could be estimated to ~ 10% of the actual value when the data are properly calibrated.
X-ray fluorescence [8]	Oxide compositions of the unknown concrete and reference cement, slag and aggregates are obtained by XRF. The mix proportions of the concrete are then determined by considering mass balance and solving a set of linear equations. Sisomphon [9] showed a variation of this approach based on the amount of CaO in the hardened paste, reference cement and slag. However, accuracy would be affected if aggregates are not properly removed from the paste. The method is not suitable for concretes containing calcareous aggregates.	Sisomphon [9] tested three concretes with 0.45 w/b ratio, 30-70% slag cured for up to 91 days. Slag content was estimated with an accuracy of ~ 6%.
Electrical conductivity [10]	Xie et al. [10] found an empirical relationship between the electrical conductivity of concrete, aggregate fraction and s/b ratio that may be used to determine slag content in unknown mixtures. However, the relationship would be dependent on other factors that influence conductivity, especially w/b ratio, degree of hydration and degree of saturation.	Unknown
Optical microscopy [7, 11]	A polished thin-section is prepared and observed using polarised light microscopy. The amount of slag as a proportion of the paste is measured by point-counting and compared to a set of reference thin-sections to estimate slag content. However, only particles larger than the thickness of the thin section (25µm) can be detected. Smaller particles can be obscured by overlying hydrates [5].	McIver & Davis [11] found estimates were within 10-20% for samples with 0-90% slag. When properly calibrated, the estimated slag content was ~ 10% of the actual value [7].

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72 BS 1881: Part 124: 1988 [1] describes a physico-chemical method to calculate the original water/cement (w/c) ratio by

73 separate determinations of the cement content from partial chemical analysis of the soluble silica and calcium oxide

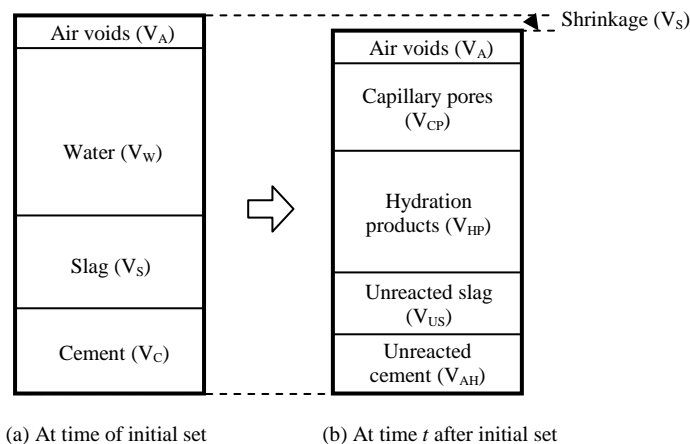
74 content, and original water content from the sum of chemically bound water and volume of capillary pores. However,

75 the method is reported to have a low precision, about 0.1 (w/c ratio) [4] or greater [12, 13]. The Nordtest Build NT 361-

1999 [14] describes a method for estimating w/c ratio using fluorescence microscopy. This method requires comparison to a set of suitable reference thin-sections, which should be made with the same ingredients, mix proportions and degree of hydration, as the concrete being examined [12, 13, 15]. A method based on image analysis of backscattered electron micrographs for estimating the original w/c ratio of hardened pastes [16], mortars and concretes [17] that does not require reference standards has been proposed by two of the authors of this paper. However, it is not known if this method is applicable to systems containing slag.

In this paper, a new method for estimating the composition of hardened slag-blended concretes, with the potential to overcome the drawbacks of existing methods, is presented. The method involves measuring the volume fractions of reacted slag, unreacted slag, unreacted cement and air voids by means of image analysis, and measuring the evaporable and non-evaporable water contents based on the mass loss of saturated surface dry samples upon heating and ignition. The results are then used to determine the initial slag, cement and water contents of the cement paste, thus permitting both the w/b and s/b ratios to be calculated. In addition, the method can estimate the degrees of hydration of both cement and slag. Results obtained from slag-blended cement pastes with a wide range of mix compositions and curing ages are presented.

## 2 Proposed method



**Figure 1: Main constituents in the paste fraction of hardened slag-blended concrete at (a) time of initial set and (b) at time  $t$  after initial set. (Not to scale)**

111 Fig. 1 shows a schematic representation of the volumetric proportions of the main constituents in hardened slag-blended  
 112 cement paste. At any moment after setting, the hardened cement paste can be thought to consist of: i) the remaining  
 113 unreacted cement, ii) unreacted slag, iii) hydration products, iv) capillary pores and v) air voids (entrapped or  
 114 entrained). The sum of their volume fractions and any shrinkage must be equal to the sum of volume fractions of the  
 115 original cement, slag, free water and air voids at the time of set. Hydration products are expected to occupy the original  
 116 (time of initial set) water-filled space, thus the volume of air voids is expected to remain unchanged with time.  
 117 Assuming that the total shrinkage is small and negligible for the purpose of this study (See Discussion):

$$V_C + V_S + V_W + V_A = V_{AH} + V_{US} + V_{CP} + V_A = 1 \quad (1)$$

118 The volume fraction of cement,  $V_C$  can be expressed in terms of the volume fractions of slag  $V_S$ , water  $V_W$  and air voids  
 119  $V_A$  as:

$$V_C = 1 - (V_S + V_W + V_A) \quad (2)$$

120 The volume fractions of slag,  $V_S$  (= unreacted,  $V_{US}$  + reacted,  $V_{RS}$ ) and air voids,  $V_A$  can be measured directly using  
 121 backscattered electron microscopy and image analysis (see Section 3.3 for detailed description). The water content,  $V_W$   
 122 can be estimated from loss on heating and ignition from a saturated and surface dry condition as described in Section  
 123 3.4 or alternatively by means of thermal gravimetric analysis (TGA). If the specific gravities of cement, slag and water  
 124 are  $\rho_c$ ,  $\rho_s$  and  $\rho_w$ , respectively, the water-binder ( $w/b$ ) ratio and the slag-binder ( $s/b$ ) ratio can be calculated using Eq. (3)  
 125 and Eq. (4) respectively:

$$\frac{w}{b} = \frac{V_W \rho_w}{V_S \rho_s + V_C \rho_c} = \frac{V_W \rho_w}{V_S \rho_s + [1 - (V_S + V_W + V_A)] \rho_c} \quad (3)$$

$$\frac{s}{b} = \frac{V_S \rho_s}{V_S \rho_s + V_C \rho_c} = \frac{V_S \rho_s}{V_S \rho_s + [1 - (V_S + V_W + V_A)] \rho_c} \quad (4)$$

126 To summarise, the proposed method uses backscattered electron microscopy and image analysis to measure the volume  
 127 fractions of unreacted slag  $V_{US}$ , reacted slag  $V_{RS}$ , and air voids  $V_A$ . The original slag fraction  $V_S$  is then estimated from  
 128 the sum of  $V_{US}$  and  $V_{RS}$ . The original water content  $V_W$  is estimated by measuring the evaporable and non-evaporable  
 129 water content. The original cement fraction  $V_C$  can then be calculated from  $V_S$ ,  $V_W$  and  $V_A$  using Eq. (2), thus allowing  
 130 the  $w/b$  and  $s/b$  ratios to be calculated using Eq. (3) and Eq. (4) respectively. The degree of reaction of slag ( $m_s$ ) can be  
 131 calculated as the ratio of the reacted slag to its initial volume fraction:

$$m_s = \frac{V_{RS}}{V_s} \quad (5)$$

132 Similarly, by measuring the volume fraction of unreacted cement,  $V_{AH}$  using backscattered electron microscopy, the  
 133 degree of hydration of cement ( $m_c$ ) can be calculated from:

$$m_c = 1 - \frac{V_{AH}}{V_c} = 1 - \frac{V_{AH}}{1 - (V_s + V_w + V_A)} \quad (6)$$

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### 136 3 Experimental

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#### 139 3.1 Materials and sample preparation

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142 Twenty slag-blended cement pastes with water/binder ratios in the range of 0.30 to 0.50 and slag contents of 0, 20%,  
 143 40% and 60% by mass of the total cementitious materials were prepared (Table 2). For each mix, three samples were  
 144 prepared, giving a total of sixty samples. The composition of the CEM I cement, obtained from XRD-Rietveld analysis,  
 145 is 64.5% alite, 16.2% belite, 6.7% aluminate and 8.7% ferrite. The oxides composition of the slag, obtained from XRF  
 146 analysis, is 36.5% SiO<sub>2</sub>, 11.6% Al<sub>2</sub>O<sub>3</sub>, 1.4% Fe<sub>2</sub>O<sub>3</sub>, 40.8% CaO, 7.5% MgO, 2.1% SO<sub>3</sub> and 0.5% Na<sub>2</sub>O<sub>equiv</sub>. It is noted  
 147 that the sulphur content in slag exists mainly in the form of sulphide, but it is measured as SO<sub>3</sub> by XRF. The loss-on-  
 148 ignition at 1000°C for the cement and slag were 2.98% and -0.99% respectively. The negative value of LOI for slag was  
 149 due to the oxidation of the sulphide content in slag during ignition [18]. The specific gravities of the slag and cement  
 150 were 2.9 and 3.15 respectively.

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153 The raw materials were mixed with tap water in a bowl mixer and compacted in three equal layers into plastic  
 154 cylindrical moulds (49 mm diameter, 58 mm height) using a vibrating table with adjustable intensity. Samples were  
 155 capped and sealed with tape, taking care to prevent any entrapped air and leakage. Subsequently, they were slowly  
 156 rotated for 24 h to avoid bleeding and segregation effects. One sample from each mix was left to cure in its mould at  
 157 room temperature for 3 days whilst the remaining samples were de-moulded and placed in a curing chamber at 100%  
 158 RH, 20°C until the ages of 28 days and 1 year.

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At the end of each designated curing period, a rectangular block sample ( $45 \times 20 \times 8$  mm) was cut from the centre of each cylinder using a diamond saw. The blocks together with the off-cuts were oven-dried at  $40^\circ\text{C}$  until constant mass in order to facilitate the penetration and polymerisation of epoxy resin. After that, the blocks were encased and impregnated with low viscosity epoxy, which protects the microstructure from damage during preparation and provides contrast for backscattered electron imaging. The epoxy was pre-heated to  $50^\circ\text{C}$  and thinned with toluene. A 2.5 bar pressure was further applied on the impregnated sample to ensure deep penetration [19]. The epoxy-impregnated blocks were cured for several days at room temperature to allow sufficient hardening of the resin. Following that, the blocks were ground and polished with diamonds at successively finer grades to  $0.25 \mu\text{m}$ .

**Table 2: Mix proportions of the slag-blended cement pastes**

No	Designation	Cement (g)	Slag (g)	Water (g)	w/b	Slag (% mass)
1	P 0.3	1000	0	300	0.30	0
2	P 0.3-20	800	200	300	0.30	20
3	P 0.3-40	600	400	300	0.30	40
4	P 0.3-60	400	600	300	0.30	60
5	P 0.35	1000	0	350	0.35	0
6	P 0.35-20	800	200	350	0.35	20
7	P 0.35-40	600	400	350	0.35	40
8	P 0.35-60	400	600	350	0.35	60
9	P 0.4	1000	0	400	0.40	0
10	P 0.4-20	800	200	400	0.40	20
11	P 0.4-40	600	400	400	0.40	40
12	P 0.4-60	400	600	400	0.40	60
13	P 0.45	1000	0	450	0.45	0
14	P 0.45-20	800	200	450	0.45	20
15	P 0.45-40	600	400	450	0.45	40
16	P 0.45-60	400	600	450	0.45	60
17	P 0.5	1000	0	500	0.50	0
18	P 0.5-20	800	200	500	0.50	20
19	P 0.5-40	600	400	500	0.50	40
20	P 0.5-60	400	600	500	0.50	60

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In addition to the paste samples, four epoxy mixes containing dry cement and slag were prepared at epoxy/binder (e/b) mass ratio of 0.5. Their proportions are shown in Table 3. These were prepared to validate the point-counting procedure (Section 3.3) on samples containing only unreacted cement and slag particles. No hydration would occur since water was absent. The epoxy mixes were prepared by first dry mixing the required amount of cement and slag in a cup. Epoxy was then added and stirred rigorously until a uniform mix was obtained. The cup was then placed in a vacuum chamber for 30 minutes to remove all entrapped air. Subsequently, a hardener was added and the mixture was stirred again,

179 before being placed into the vacuum chamber for a further 30 minutes. The mixture was left to harden at room  
 180 temperature for approximately 48 hours. It was unnecessary to continuously rotate the epoxy mixed during hardening  
 181 since segregation is not expected to be significant in a viscous resin. Then a rectangular block ( $45 \times 20 \times 8$  mm) was  
 182 extracted by taking a vertical slice from the centre of the cylinder, then ground and polished in the manner described  
 183 above.

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186 **Table 3: Proportions of the epoxy mixes containing cement and slag**

No	Designation	Cement (g)	Slag (g)	Epoxy + hardener (g)	e/b	Slag (% mass)
1	E 0.5	120	0	60	0.50	0
2	E 0.5-20	96	24	60	0.50	20
3	E 0.5-40	72	48	60	0.50	40
4	E 0.5-60	48	72	60	0.50	60

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189 **3.2 SEM-BSE imaging**

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192 A Camscan Apollo 300 field-emission SEM was used for imaging. The SEM was operated in high-vacuum, at 10 kV  
 193 accelerating voltage and working distance of between 10 to 15 mm. Samples were viewed at  $500\times$  magnification, which  
 194 gives a field of view of  $240 \times 192 \mu\text{m}$  per frame. Each frame was digitised to  $2560 \times 2048$  pixels with a pixel spacing of  
 195  $0.094 \mu\text{m}$ . This represents a good compromise for obtaining a decent sampling area and high resolution to discriminate  
 196 the phases of interest. The brightness and contrast settings were adjusted so that the contrast between the unreacted  
 197 cement, unreacted slag, reacted slag and voids were optimised to facilitate the identification of different phases in the  
 198 samples. The same setting was applied for all frames to ensure consistency. To avoid charging artefacts, the polished  
 199 samples were pre-coated with a thin layer ( $\sim 50$  nm) of carbon using an evaporative coater.

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202 **3.3 Image analysis**

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205 The brightness of each pixel in a BSE image increases monotonically with mean atomic number of the underlying  
 206 phase. For a typical slag-blended paste, the unreacted cement will appear brightest, followed by the unreacted slag,  
 207 portlandite, C-S-H, reacted slag and epoxy-filled pores and cracks (Fig. 2). Since some phases share similar mean  
 208 atomic numbers (e.g. unreacted slag and portlandite), pixel brightness alone may not be sufficient to differentiate all



209 phases. Furthermore, using Monte-Carlo simulations, we found that the sampling depth and escape surface radius of  
210 backscattered electrons in cement-based materials can be up to 0.5 and 1.5  $\mu\text{m}$  respectively at 10kV accelerating voltage  
211 [20] so pixels that sample more than one phase will show averaged intensities. These make phase segmentation on the  
212 basis of greyscale alone difficult. Greyscale segmentation can be combined with information from element maps  
213 obtained using energy-dispersive X-ray spectroscopy (EDS) [21, 22]. However, this could be a time consuming  
214 procedure if many frames are required.

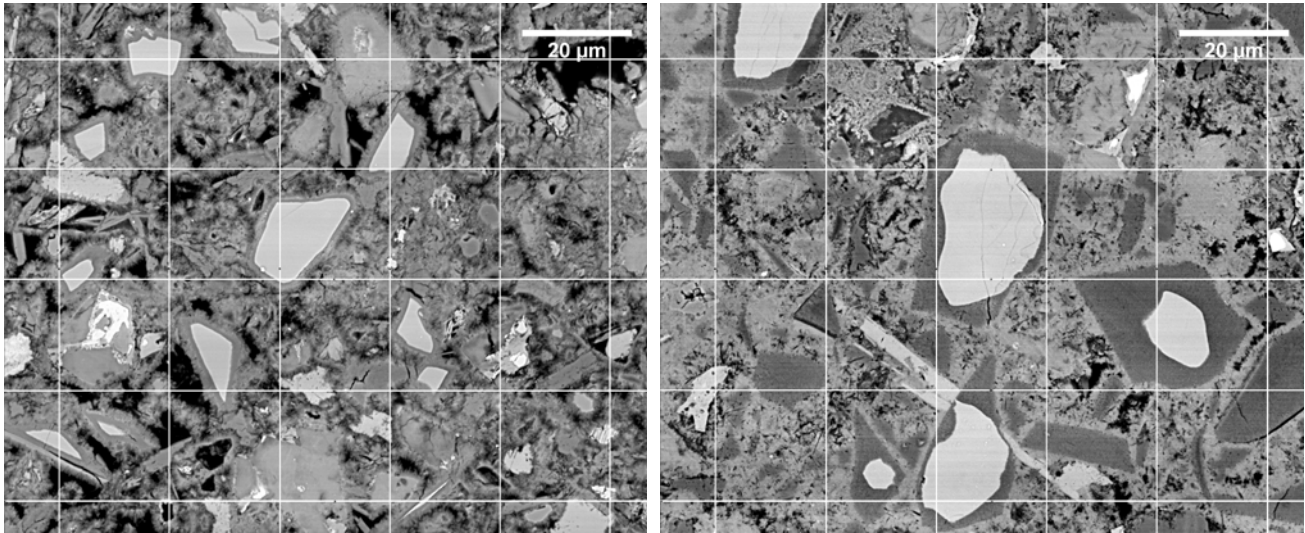
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217 Hence, point counting analysis, which will be further described below, was adopted to measure the volume fractions of  
218 unreacted slag, reacted slag, unreacted cement, air voids and limestone filler in the samples. Pixel brightness along with  
219 visual information such as particle size, shape and texture was used for identifying the phases. This is subjective and  
220 could introduce a source of error. Hence where necessary, the elemental composition was determined via spot analysis  
221 using EDS to confirm the phase present. For example, slag grains are angular, appear smooth and have sharply defined  
222 boundaries (Fig. 2a). In well hydrated samples, dark rims that indicate the extent of slag reaction are clearly visible. An  
223 EDS spot analysis on the slag reaction rims shows that they contain similar elements to the unreacted slag, but  
224 significantly reduced Ca and Si peaks. The Mg peak remains virtually unchanged due to the low mobility of Mg and  
225 does not significantly migrate from the original slag grain [23-25]. As hydration proceeds, the width of the slag reaction  
226 rim increases (Fig. 2b). Small slag particles may appear as fully reacted relicts, hence darker in colour, but their angular  
227 shape and original boundary remain visible. These characteristics allow good discrimination between reacted and  
228 unreacted slag, particularly at later ages. It should also be noted that what appear as small slag particles in the BSE  
229 image may actually be sectioned tips of larger particles.

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232 The point counting analysis was performed by superimposing a 99-point grid on each live image and the phase  
233 intersected at every grid point was identified by a trained operator and tallied using a counting device. However, a grid  
234 point may fall on the boundary of different phases and this might cause ambiguities. In such cases, the phase that lies on  
235 the upper right corner of the grid point was recorded to ensure a systematic and unambiguous point counting procedure.  
236 This process was repeated for 30 frames taken at random locations spanning the sample to obtain a representative  
237 average. Assuming that the counted phases are randomly distributed in the microstructure, the total number of points  
238 that fall on a particular phase divided by the total number of points counted (2970) provides an unbiased estimate of the  
239 volume fraction of that phase (i.e. volume fraction of a phase = number of points falling on that phase / total number of

240 points counted). The time required by a trained operator to complete a point count analysis on each sample was  
 241 approximately 1.5 hours, which seems reasonable considering the amount of information obtained.

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(a) P 0.5-20 at 28 days

(b) P 0.5-20 at 1 year

244 **Figure 2: BSE images of cement pastes at w/b ratio of 0.5 containing 20% slag replacement after curing for (a)**  
 245 **28 days and (b) 1 year. A grid is superimposed on the images for point-counting. Field of view is 120 × 96 µm.**

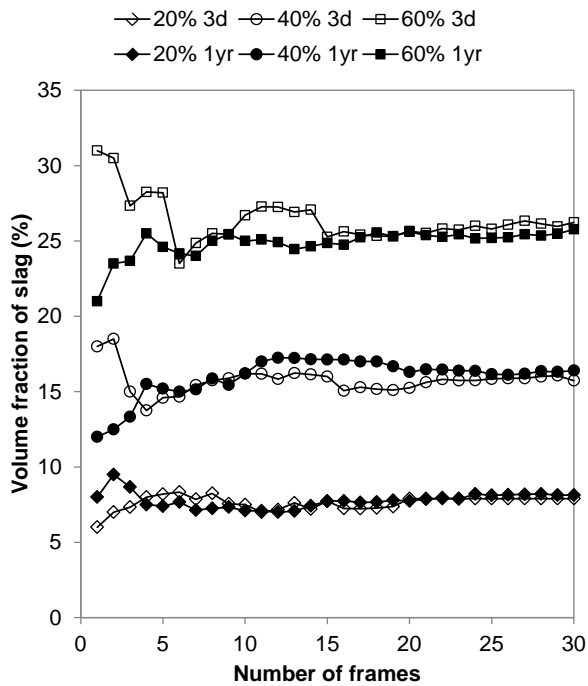
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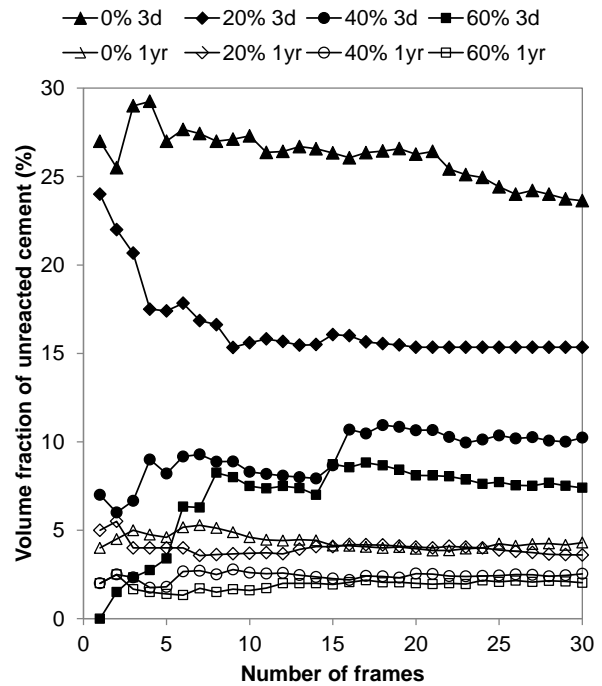
248 Fig. 3 shows plots of moving averages for the measured volume fractions of (a) slag (reacted + unreacted) and (b)  
 249 unreacted cement against number of frames analysed for pastes at 0.45 w/b ratio containing 20, 40 & 60% slag at ages  
 250 of 3 days and 1 year. The results show that as the number of frames analysed increases, the cumulative average  
 251 converges to a relative stable value suggesting that the cumulative average after 30 frames is representative and that  
 252 analysing more frames would not significantly alter the results.

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(a)



(b)

255 **Figure 3: Plot of moving average of the measured volume fractions of (a) slag and (b) unreacted cement against**  
 256 **number of image frames. Samples are pastes at 0.45 w/b ratio containing 20, 40 & 60% slag at an age of 3 days**  
 257 **and 1 year.**

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### 260 3.4 Water content

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263 The original water content was estimated by measuring the sum of the evaporable and non-evaporable water in the off-  
 264 cuts from each mix. The off-cuts measuring about 49 mm in diameter and 25 mm in height were placed in cups, de-  
 265 aired in a vacuum chamber and then immersed in de-aired water without breaking the vacuum. The vacuum is  
 266 subsequently released and an additional 2.5 bars above atmospheric pressure is applied and maintained for about 30  
 267 minutes. The saturated off-cuts were then surface-dried and weighed. To avoid any errors potentially caused by water  
 268 absorbed into large air voids during vacuum saturation, the off-cuts were crushed into small pieces and reweighed. This  
 269 proved to be unnecessary as no significant amount of air voids were found and reweighing the crushed off-cuts did not  
 270 detect any mass difference. The volume of the off-cuts  $V_o$  was measured by applying Archimedes's principle by  
 271 lowering the off-cut into a water-filled beaker until fully submerged and measuring the mass change.

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274 Following that, the off-cuts were placed in a crucible and dried at 105°C until constant mass. The mass difference

275 between the saturated surface-dried and oven-dried (105°C) condition was taken as the mass of evaporable water ( $m_e$ ).

276 The off-cuts were then placed into a furnace and ignited at 1000°C for 4 h. The drying and ignition processes were  
 277 carried out in CO<sub>2</sub>-free conditions. The mass difference between the oven-dried ( $m_{105}$ ) and ignited condition ( $m_{1000}$ ),  
 278 corrected for any mass change of the unreacted cement and slag, was taken as the mass of non-evaporable water ( $m_n$ ).  
 279 Weighing was carried out in an analytical balance with precision of 0.0001g.

$$m_n = m_{105} - m_{1000} + (V_{AH}\rho_c LOI_C + V_{US}\rho_s LOI_S)V_o \quad (7)$$

280 Where  $LOI_C$  and  $LOI_S$  are the loss on ignition of cement and slag respectively, and  $V_{AH}$  and  $V_{US}$  are estimated from point  
 281 counting, and  $V_o$  is the volume of the off-cut. Having determined the masses of evaporable and non-evaporable water,  
 282 the volume fraction of water is calculated as:

$$V_W = \frac{m_e v_e + m_n v_n}{V_o} \quad (8)$$

283 Where  $v_e$  (1.0 cm<sup>3</sup>/g) and  $v_n$  (0.72 cm<sup>3</sup>/g) are the specific volumes of the evaporable and non-evaporable water  
 284 respectively. We assume that the specific volume of evaporable water is equal to that of free water (i.e. 1.0 cm<sup>3</sup>/g). In  
 285 fact, a portion of the evaporable water is water held within the intrinsic gel pores of the hydration products, which may  
 286 have a specific volume of slightly lower than 1.0 cm<sup>3</sup>/g [26].

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289 The specific volume of non-evaporable water  $v_n$  (= 0.72 cm<sup>3</sup>/g) is based on the work of Powers and Brownyard [27]  
 290 because of lack of a better value for slag-blended systems. Here, we have inevitably assumed that  $v_n$  does not depend on  
 291 the binder composition and degree of reaction, and that the physical properties of hydration products of slag-blended  
 292 cement pastes are similar to those in Portland cement pastes. This is an approximation since it is well-established that  
 293 the clinker phases hydrate at different rates to form different amounts of hydrates (mainly C-S-H, portlandite, ettringite  
 294 and AFm phases) containing different amounts of water. Nevertheless, it is often observed that the amount of  
 295 chemically-bound water per mass of reacted material is similar for Portland cements. However, the presence of slag  
 296 changes the reactivity of the clinker phases, hydration kinetics, the type and amount of the hydrates formed [28-30].

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303 **4 Results**

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306 **4.1 Epoxy mixes**

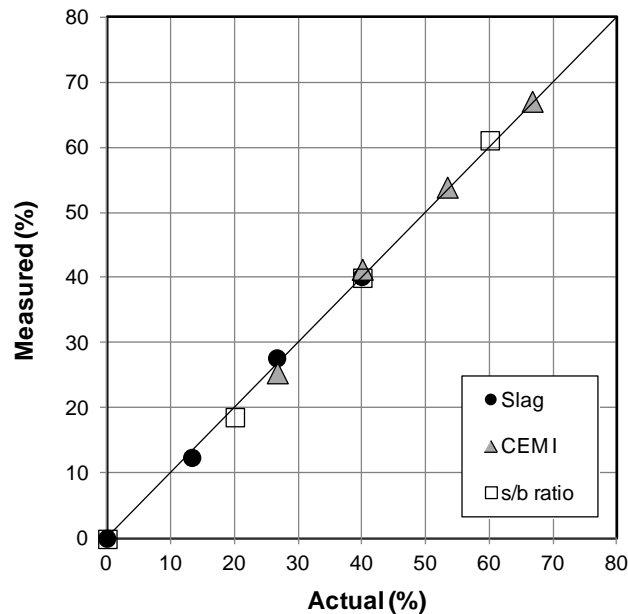
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309 As mentioned in Section 3.1, four epoxy mixes containing dry cement and slag at 20%, 40% and 60% replacement, and  
 310 epoxy/binder mass ratio of 0.5 were prepared to test and validate the point counting procedure. The volume fractions of  
 311 the cement, slag and epoxy were measured by point-counting and the results were converted to mass fractions based on  
 312 known densities of the raw materials. The density of epoxy was taken as  $1.1\text{g/cm}^3$ . The measured mass fractions and  
 313 slag/binder (i.e. slag/(slag + binder)) ratio are compared against the theoretical values in Fig. 4. The results demonstrate  
 314 that the point count measurements were indeed very accurate for the non-hydrated samples. The mean absolute errors  
 315 for mass fractions of cement and slag, and slag/binder ratio were 2.48%, 3.74% and 2.92%, respectively. Absolute error  
 316 is calculated as the absolute difference between the measured and actual value, expressed as a percentage of the actual  
 317 value. Hereafter, mean absolute error refers to the averaged absolute errors for each constituent. No visible sign of  
 318 segregation of cement and slag was observed in the cross-section of the epoxy mixes.

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322 **Figure 4: Comparison between actual and measured mass fractions of slag, cement and slag/binder ratio in**  
 323 **epoxy mixes**

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## 327 4.2 Cement pastes

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330 Table 4 presents the measured volume fractions of unreacted slag, reacted slag and unreacted cement (from point-  
 331 counting) and water (sum of evaporable and non-evaporable water) for all samples. The measured volume fractions of  
 332 air voids and limestone filler were insignificant and typically less than 0.1%, thus are not shown. The results indicate  
 333 that the amount of unreacted slag and unreacted cement decreases with curing age, while the amount of reacted slag  
 334 increases with curing age, as expected. The sum of reacted and unreacted slag is relatively constant with curing age.  
 335 These trends are consistent throughout the dataset.

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337

338 **Table 4: Measured volume fractions (%) of unreacted slag, reacted slag, unreacted cement and water for all**  
 339 **samples.**

Sample	Unreacted slag ( $V_{US}$ )			Reacted slag ( $V_{RS}$ )			Unreacted cement ( $V_{AH}$ )			Water ( $V_W$ )		
	3d	28d	1yr	3d	28d	1yr	3d	28d	1yr	3d	28d	1yr
P 0.3	0.0	0.0	0.0	0.0	0.0	0.0	23.7	20.4	11.9	46.9	50.6	49.0
P 0.3-20	9.9	7.6	5.0	0.8	1.9	6.1	16.7	14.1	8.4	48.8	48.3	49.8
P 0.3-40	20.0	15.5	11.8	1.0	2.1	8.5	11.8	10.7	7.5	45.9	47.8	49.9
P 0.3-60	27.6	22.2	18.5	0.8	2.6	10.6	7.3	5.9	4.9	46.7	48.6	49.7
P 0.35	0.0	0.0	0.0	0.0	0.0	0.0	23.6	15.4	9.1	51.5	52.8	52.6
P 0.35-20	7.7	6.2	4.3	1.5	2.9	6.4	17.8	12.4	6.5	52.1	54.3	54.2
P 0.35-40	19.0	12.4	10.2	1.3	3.1	8.5	12.0	9.0	3.8	52.6	53.5	54.4
P 0.35-60	26.6	23.5	16.6	2.6	5.1	10.9	6.0	5.2	3.0	51.0	51.2	52.9
P 0.4	0.0	0.0	0.0	0.0	0.0	0.0	21.0	17.3	6.9	57.0	54.8	56.8
P 0.4-20	9.2	6.5	3.1	0.7	2.3	6.0	13.4	9.1	5.8	56.2	57.0	56.6
P 0.4-40	18.1	12.2	8.6	1.2	3.7	8.1	11.1	6.8	3.6	56.0	55.8	55.5
P 0.4-60	27.2	22.0	16.2	3.2	4.3	10.2	6.6	3.6	2.8	55.2	54.2	55.1
P 0.45	0.0	0.0	0.0	0.0	0.0	0.0	25.0	13.1	4.3	57.2	59.4	60.7
P 0.45-20	7.0	6.2	2.2	1.0	2.2	6.0	14.9	9.4	3.6	58.0	57.6	58.3
P 0.45-40	14.8	12.2	7.0	1.1	3.9	9.6	10.3	6.1	2.6	59.0	59.3	57.0
P 0.45-60	25.1	21.7	13.7	1.4	3.4	12.4	7.5	3.0	2.1	57.7	58.5	55.8
P 0.5	0.0	0.0	0.0	0.0	0.0	0.0	19.7	14.0	4.3	60.9	60.4	63.3
P 0.5-20	7.0	5.5	1.3	0.3	2.1	6.5	15.2	8.8	3.0	61.9	61.4	62.1
P 0.5-40	13.0	12.0	6.1	1.3	3.9	8.8	11.6	5.8	2.5	60.9	61.7	58.9
P 0.5-60	19.7	20.8	12.7	2.0	4.7	9.5	8.3	2.5	1.3	61.8	57.9	59.7

340

341

342 The measured volume fractions of slag, cement (Eq. 2) and water are converted to  $\text{kg/m}^3$  and the results are compared  
 343 against the theoretical values, which can easily be deduced from the known masses of the mix constituents and  
 344 densities. Fig. 5 plots the experimentally measured against the actual values. The original w/b ratio is then calculated  
 345 from the slag, cement and water contents, the results are shown in Fig. 6 and Table 5.

346

347

348 The results shown in Fig. 5a suggest that there is a tendency for the slag content to be slightly underestimated. The  
349 mean errors were -4.3%, -11.9% and -6.5% for the 3-day, 28-day and 1-year cured samples, respectively. Here, error is  
350 calculated as the difference between the measured and actual value, expressed as a percentage of the actual value.

351 Hereafter, mean error refers to the averaged error for each constituent. We note that the disagreement between  
352 measured and actual slag content was somewhat higher for the 28-day cured samples. This is attributable to the outliers  
353 in the measurements, for example, two points in Fig. 5a show very large errors of 32.7% and 24.0%. However, we have  
354 not excluded any outliers in the analysis. The reason for the large errors at 28-day is unclear, but probably a result of  
355 experimental errors. Nevertheless, considering the large number of samples tested, the results indicate that the point  
356 counting method is generally quite accurate in determining the original slag content.

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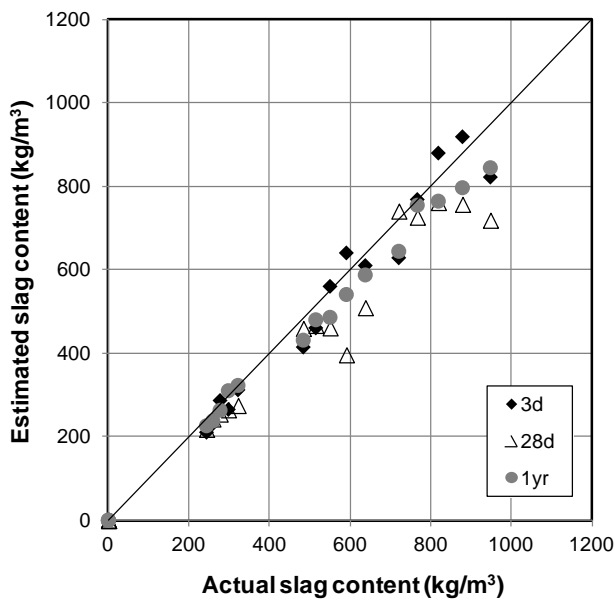
359 The water content (Fig. 5b) was very well estimated with mean errors of only 0.25%, 1.1% and 1.8% for the 3-day, 28-  
360 day and 1-year cured samples, respectively. As for the cement content, the mean errors were 0.1%, 5.4% and 2.2% at  
361 each consecutive curing age. Again, the disagreement between measured and actual cement content was somewhat  
362 higher for the 28-day cured samples. This is primarily due to the tendency to underestimate slag content, given the fact  
363 that the estimated water content was relatively accurate. The mean absolute errors for all samples were 9.1%, 1.5% and  
364 2.5% for slag, water and cement content, respectively.

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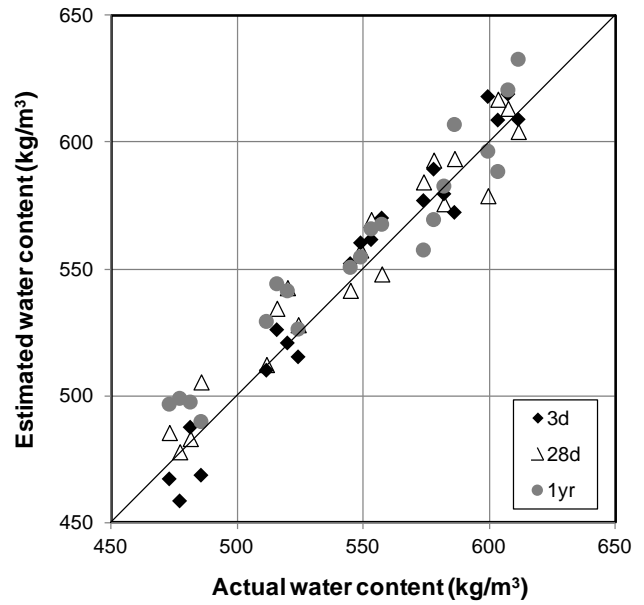
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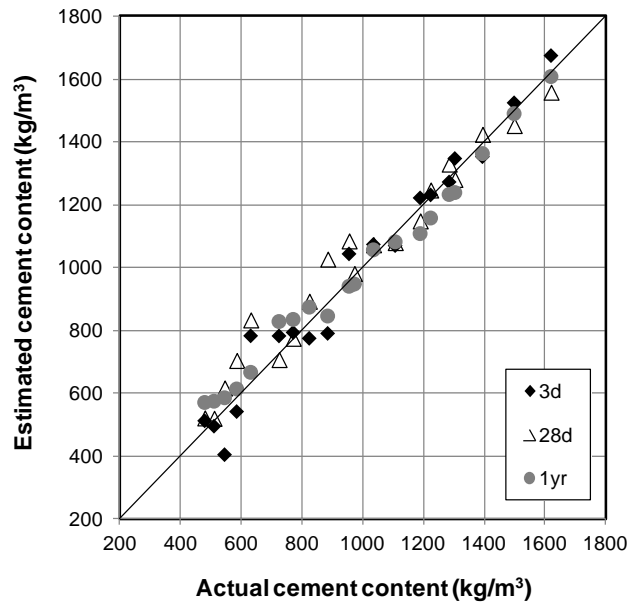
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(a)



(b)



(c)

369 **Figure 5: Comparison between the estimated and actual values of the original (a) slag content, (b) water content**  
 370 **and (c) cement content for all samples investigated. Note: results were converted to  $\text{kg/m}^3$  by multiplying the**  
 371 **measured volume fractions of each material by their respective densities.**

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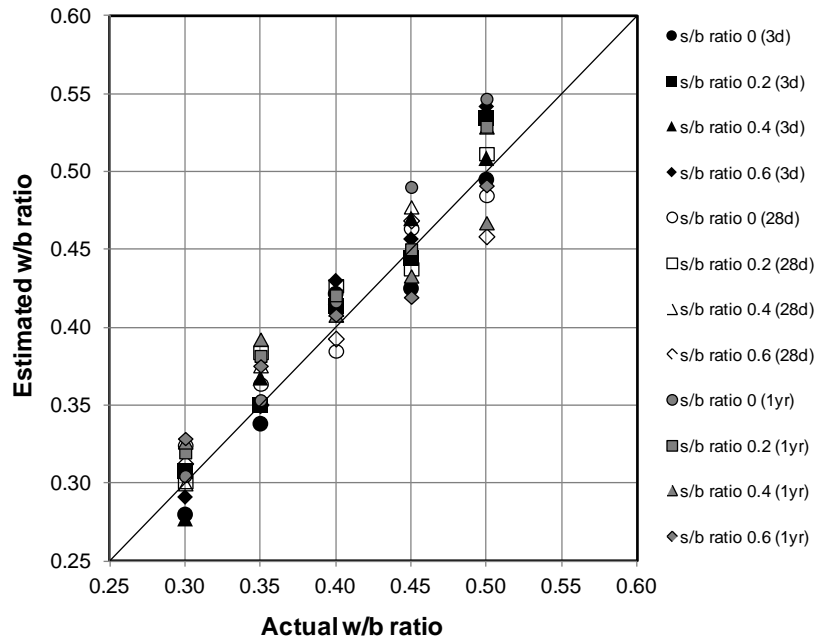
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374 A good agreement between the estimated and actual w/b ratios was observed for all samples, regardless of the slag  
 375 content and curing age. The mean errors of the estimated w/b ratios were 1.2%, 2.3% and 3.8% for the 3-day, 28-day  
 376 and 1-year cured samples, respectively. The mean absolute error for all samples was 4.7%. Of the 60 different samples  
 377 tested, the largest error in the estimated w/b ratio was only 0.046. With the exception of 5 samples, all of the estimated



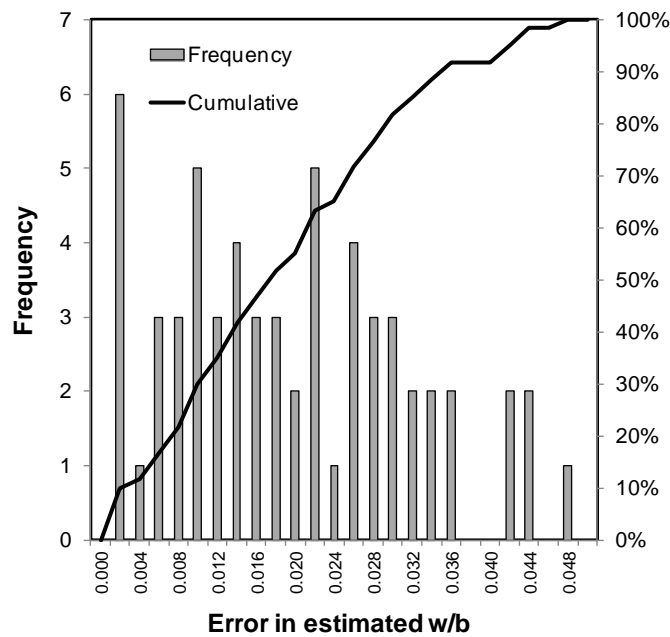
378 w/b ratios were within 0.036 of the actual values (Fig. 7). The estimated s/b ratio shown in Table 5 was also reasonably  
 379 accurate with mean errors of -2.7%, -10.9% and -4.9% for the 3-day, 28-day and 1-year cured samples, respectively.  
 380 The mean absolute error for s/b ratio for all samples was 8.7%.

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Figure 6: Comparison between the estimated and actual w/b ratio for all samples investigated.



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Figure 7: Frequency and cumulative histogram of the absolute error in estimated w/b ratio for all samples.

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**Table 5: Measured w/b ratio, s/b ratio and the degrees of reaction of cement  $m_C$  and slag  $m_S$**

Sample	w/b			s/b			$m_C$			$m_S$		
	3d	28d	1yr	3d	28d	1yr	3d	28d	1yr	3d	28d	1yr
P 0.3	0.28	0.32	0.30	-	-	-	0.55	0.59	0.77	0.00	0.00	0.00
P 0.3-20	0.31	0.30	0.32	0.20	0.17	0.21	0.59	0.66	0.79	0.08	0.20	0.55
P 0.3-40	0.28	0.30	0.33	0.37	0.32	0.38	0.64	0.69	0.75	0.05	0.12	0.42
P 0.3-60	0.29	0.31	0.33	0.51	0.52	0.56	0.71	0.78	0.77	0.03	0.10	0.36
P 0.35	0.34	0.36	0.35	-	-	-	0.51	0.67	0.81	0.00	0.00	0.00
P 0.35-20	0.35	0.38	0.38	0.18	0.19	0.22	0.54	0.66	0.81	0.16	0.32	0.59
P 0.35-40	0.37	0.38	0.39	0.45	0.32	0.39	0.52	0.73	0.86	0.14	0.10	0.45
P 0.35-60	0.35	0.35	0.38	0.63	0.52	0.57	0.65	0.77	0.84	0.16	0.10	0.40
P 0.4	0.42	0.39	0.42	-	-	-	0.51	0.62	0.84	0.00	0.00	0.00
P 0.4-20	0.41	0.43	0.42	0.21	0.19	0.20	0.60	0.73	0.83	0.07	0.26	0.66
P 0.4-40	0.42	0.41	0.41	0.42	0.34	0.36	0.55	0.76	0.87	0.06	0.23	0.49
P 0.4-60	0.43	0.39	0.41	0.69	0.55	0.57	0.48	0.82	0.85	0.10	0.16	0.39
P 0.45	0.43	0.46	0.49	-	-	-	0.41	0.68	0.89	0.00	0.00	0.00
P 0.45-20	0.44	0.44	0.45	0.18	0.18	0.18	0.56	0.72	0.89	0.12	0.27	0.73
P 0.45-40	0.47	0.48	0.43	0.37	0.38	0.37	0.59	0.75	0.90	0.07	0.24	0.58
P 0.45-60	0.46	0.47	0.42	0.61	0.58	0.57	0.52	0.82	0.89	0.05	0.14	0.47
P 0.5	0.50	0.49	0.55	-	-	-	0.49	0.65	0.88	0.00	0.00	0.00
P 0.5-20	0.54	0.51	0.53	0.18	0.18	0.19	0.49	0.72	0.90	0.04	0.28	0.83
P 0.5-40	0.51	0.53	0.47	0.35	0.39	0.34	0.53	0.74	0.90	0.09	0.25	0.59
P 0.5-60	0.54	0.46	0.49	0.55	0.59	0.53	0.49	0.85	0.93	0.09	0.19	0.43

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#### 4.3 Degree of reaction

400 The estimated degrees of reaction of slag (Eq. 5) and cement (Eq. 6) are presented in Table 5. As expected, the degree  
401 of reaction of both binders increased with curing age for all samples. The degree of hydration of cement for the 3-day,  
402 28-day and 1-year samples ranged from 0.41 to 0.71, 0.59 to 0.85 and 0.75 to 0.93, respectively. The presence of slag  
403 had a slight accelerating effect on the hydration of cement at 3 and 28 days, but this became insignificant at 1 year. This  
404 effect has been reported in previous studies, for example Lumley et al. [31] and Escalante-Garcia & Sharp [32].

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The degree of reaction of slag for the 3-day, 28-day and 1-year samples ranged from 0.03 to 0.16, 0.10 to 0.32 and 0.36  
to 0.83, respectively. The degree of reaction of slag at 28 days and 1 year increased with increasing w/b ratio. At a

409 constant w/b ratio, the degree of reaction of slag decreased with increasing s/b ratio. These observations are also in  
410 agreement with those of Lumley et al. [31] and Escalante et al. [33]. The observed trends can be explained by the  
411 dependency of the slag reaction on the amount of available calcium hydroxide and a sustained alkaline-activating  
412 environment. Increasing the w/b ratio increases the amount of water and space available for the formation of hydration  
413 products, thus promoting the hydration of cement and slag. However, these trends were less consistent at 3 days. The  
414 reason for this is unclear, but could be due to experimental errors. In young pastes, the reacted slag rims are very narrow  
415 and this affects the accuracy of the point-counting.

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418 The estimated degrees of hydration of cement and slag are compared against measured values from conventional image  
419 analysis using Eq. (5) and Eq. (6) where the original cement and slag content are known beforehand. Results are  
420 displayed in Fig. 8. A good agreement between the estimated and measured values is observed for cement and slag at all  
421 curing ages.

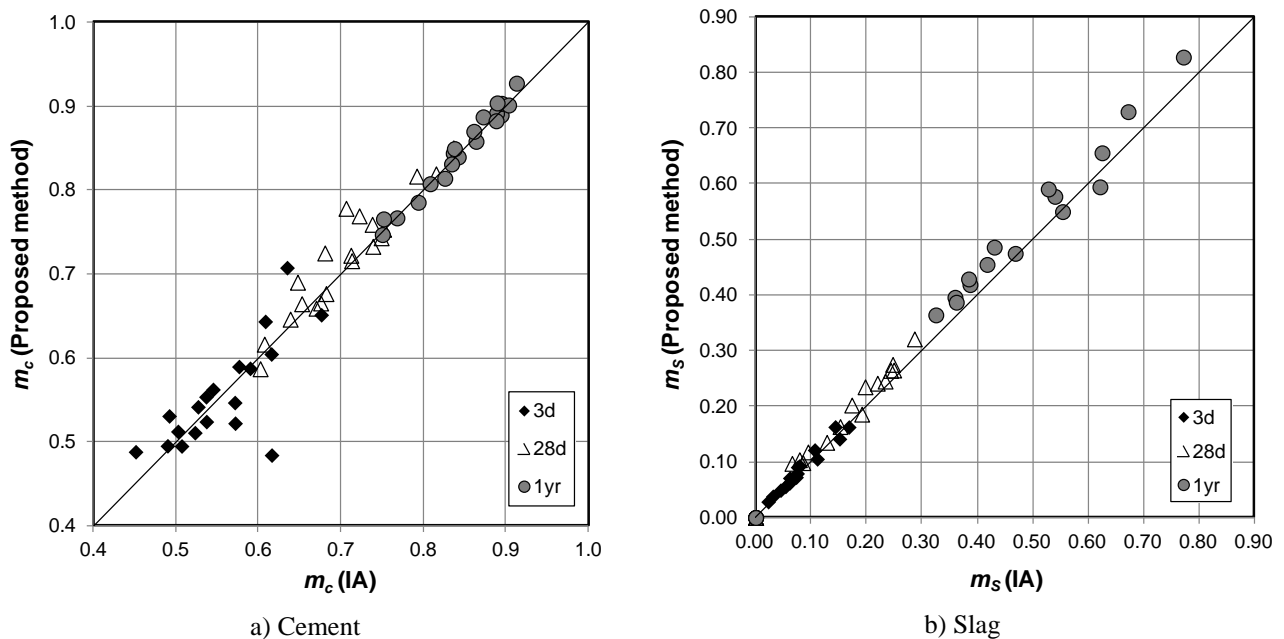
422  
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424 It would be interesting to compare the results from this study to those in the literature, but noting that the binders used  
425 and their intrinsic reactivity, curing conditions and test methods would not be exactly the same. Feng et al. [34]  
426 measured the degree of reaction of slag blended cement pastes with w/b ratio 0.4 and s/b ratio 0.3 using a point-  
427 counting procedure on BSE images. Samples were sealed cured in a 20°C, 100% RH environment. The measured  
428 degrees of hydration for cement in the blended paste at 3 and 28 days were 0.54 and 0.78, and for slag were 0.08 and  
429 0.28 respectively. These values seem to agree well with ours for P 0.4-20 and P 0.4-40 at s/b ratios of 0.2 and 0.4 (Table  
430 5). The averaged degree of hydration of cement for these two pastes at 3 and 28 days were 0.58 and 0.75, and for slag  
431 were 0.07 and 0.25, respectively. The good agreement is probably not surprising since that the oxide composition of the  
432 slag and the point-counting procedure used by Feng et al. [34] are quite similar to ours. However, it should be noted that  
433 our measurements include the reacted slag fraction and the degree of reaction was estimated without requiring prior  
434 knowledge of the w/b ratio or the original slag and cement contents in the sample.

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437 Our results are also consistent with those of Lumley et al. [31], who carried out an extensive study on the degree of  
438 reaction of slag in pastes made with combinations of five cement and seven slag types. The degree of reaction for slag  
439 was measured using selective dissolution (EDTA extraction). They observed that for blended pastes at w/b ratio of  
440 0.40-0.60, s/b ratio of 0.30-0.69 and sealed cured at 20°C, about 30-55% of the slag reacted after 28 days and 38-75%

441 reacted after 1 year. In another study, Kocaba et al. [21] compared five methods for determining the amount of slag  
 442 reacted in blended systems made with two slag types and three cement types at w/b ratio of 0.42 and s/b ratio of 0.4.  
 443 Their results indicated that selective dissolution and differential scanning calorimetry were less reliable compared to  
 444 methods using BSE image analysis combined with EDS mapping of Mg, isothermal calorimetry or chemical shrinkage.  
 445 The two slag types studied had very different reactivity. Using the BSE-EDS method, they reported about 10-40% of  
 446 the slag reacted after 3 days, 30-55% reacted after 28 days and 60-75% reacted after 1 year.

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448



449 **Figure 8: Comparison between the estimated degree of hydration using the proposed method and the measured**  
 450 **degree of hydration from conventional image analysis method**

451

452

## 453 5 Discussion

454

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456 The epoxy mixes containing unreacted cement and slag produced very good results, thus verifying that point counting

457 on backscattered electron images can indeed give accurate estimation of volume fractions. Inevitably, when applied to

458 hydrated cement paste, the observed error increases due to greater complexity in the microstructure of such systems.

459 There are several factors that could contribute to errors and a potential major source lies in counting the reacted slag

460 fraction. This is because the reacted slag shares similar grey level to that of hydration products. In some slag particles,

461 especially at early ages, the reacted slag rims could be too narrow to be accurately identified. This may cause a

462 tendency to underestimate the degree of reaction and the total slag content. Small slag particles may be completely  
463 reacted, but their angular shape and original boundary remain visible and so the operator must be aware of this.

464

465 Because of the finite resolution of the technique, not all of the smallest particles will be counted and some errors will be  
466 associated with this. The smallest dimension of a particle that can be observed and counted meaningfully is about 10  
467 pixels, which is equal to  $0.94\ \mu\text{m}$  ( $10 \times 0.094\ \mu\text{m}/\text{pixel}$ ). The slag used in this study had less than 2% vol. of particles  
468 smaller than  $1\ \mu\text{m}$  while the Portland cement had less than 5% vol. of particles smaller than  $1\ \mu\text{m}$ , as measured with laser  
469 granulometry. The very small particles are expected to have fully reacted by the time the earliest measurement was  
470 made. Thus, the chosen magnification does seem to represent a good compromise between obtaining a good sampling  
471 area and adequate resolution. As a possible improvement to the method, point counting can be carried out at higher  
472 magnification. However, this gives a smaller field of view and so more frames must be measured. It should also be  
473 noted that only one polished sample per mix was imaged in this study, so testing replicates and sampling at different  
474 depths is expected to improve accuracy.

475

476

477 Another probable source of error lies in the determination of the evaporable and non-evaporable water contents using  
478 the adopted temperatures. It is well-established that dehydration of the C-S-H and ettringite phases occurs at  
479 temperatures below  $105^\circ\text{C}$ , thus the measured evaporable water would be over-estimated and correspondingly, the non-  
480 evaporable water content underestimated. An alternative method for measuring the water content is by using thermal  
481 gravimetric analysis (TGA) to monitor continuously the mass change in the sample as a function of increasing  
482 temperature. However, it is very difficult in practice to accurately separate and quantify the various states of water in  
483 hydrated cement paste. Recently, it has been shown that  $^1\text{H}$  NMR is capable of this [35], but it is not yet a widely  
484 available technique, requires specialist interpretation and its application is limited for grey cements and certain SCMs  
485 because of the effects of iron paramagnetic impurities. In contrast, the oven drying followed by ignition approach is  
486 relatively fast, convenient and well-suited for routine application. Although the accuracy of separating the 'evaporable'  
487 and the 'non-evaporable' water content at  $105^\circ\text{C}$  is questionable, this is relatively unimportant for this study since the  
488 data are only used to determine the total water content (evaporable plus non-evaporable). Our results show that the total  
489 water content was just slightly overestimated, with an overall mean error of 1.5%. The maximum error was 5.5%.

490

491

492 Another issue that needs consideration is that carbonates decompose at temperatures beyond 550°C and this will cause  
 493 an over-estimation of the non-evaporable water content. This error can be reduced by avoiding sampling of areas that  
 494 have been exposed to carbonation or by reducing the maximum ignition temperature to 550°C [36]. Another source of  
 495 error is in the accuracy of the assumed specific volume of non-evaporable water  $v_n$  (0.72 cm<sup>3</sup>/g). If this value changes  
 496 by  $\pm 10\%$  (i.e.  $v_n = 0.65\text{-}0.80$  cm<sup>3</sup>/g), the mean absolute error for the estimated water content, w/b and s/b ratios for all  
 497 samples investigated in this study would range from 2.1 to 4.3%, 4.7 to 10.4% and 7.0 to 10.7%, respectively.

498  
 499  
 500 The proposed method assumes that the sample has not experience macroscopic volume change since initial set (Eq. (1)).  
 501 However, it is known that slag-blended systems can exhibit significantly more drying shrinkage than non-blended  
 502 systems. The error in the obtained result is expected to include a contribution from shrinkage. However, for application  
 503 to concrete in real structures, the shrinkage of an unknown concrete would be difficult to ascertain. Thus, it would be  
 504 instructive to determine the magnitude of error in the estimated w/b and s/b ratios caused by neglecting shrinkage. If  
 505 shrinkage is considered, then the formula for w/b and s/b ratios, derived following the same principle can be written as:

$$\frac{w}{b} = \frac{V_w \rho_w}{V_s \rho_s + V_c \rho_c} = \frac{V_w \rho_w}{V_s \rho_s + [1 - (V_s + V_w + V_A + V_\varepsilon)] \rho_c} \quad (7)$$

$$\frac{s}{b} = \frac{V_s \rho_s}{V_s \rho_s + V_c \rho_c} = \frac{V_s \rho_s}{V_s \rho_s + [1 - (V_s + V_w + V_A + V_\varepsilon)] \rho_c} \quad (8)$$

506 Where  $V_\varepsilon$  is the volume fraction of shrinkage ( $\varepsilon_s$ ). The amount of shrinkage that any concrete experiences is influenced  
 507 by the properties of the concrete (aggregate volume fraction and stiffness, w/b ratio, degree of hydration and slag  
 508 content) and its environment (humidity, temperature). Hooton et al [37] carried out a literature review of the effect of  
 509 GGBS on the drying shrinkage of concrete. Data from 62 concrete mixes containing slag from 16 studies were  
 510 examined, covering concrete mixes with a wide range of w/b ratio (0.26 to 0.60), slag content (20% to 80%), and  
 511 aggregate content (50-73% vol). Curing ranged from 3 to 28 days. The measured shrinkage after drying for up to 365  
 512 days at 50% RH and 20 or 23°C was of the order of  $\sim 750$  microstrain. This is very consistent with a recent study by  
 513 Dellenghausen et al. [38] who measured a total shrinkage of no more than 800 microstrain after 365 days of drying at  
 514 50% RH, 23°C for concretes containing 0-70% of slag in white and grey Portland cements at w/b ratios between 0.3 and  
 515 0.55. However, the shrinkage in neat cement paste containing slag will be much higher. Taking an extreme value of  $\varepsilon_s$   
 516 of 10,000 microstrain ( $V_\varepsilon = 1\%$ ) would change the estimated w/b and s/b ratios by no more than 0.015 and 0.017  
 517 respectively for all the samples investigated in this study. Therefore, neglecting shrinkage is another source of error  
 518 when the method is applied to neat cement pastes.

519

520

521 A major advantage of the proposed method in relation to existing methods is that it is able to make separate estimations  
522 of the original cement, slag and water contents without the need for calibration or reference standards, or requiring the  
523 actual chemical composition of the ingredients or prior knowledge of the mix proportions. In addition, the method can  
524 be used to simultaneously estimate the degree of reaction of both cement and slag in blended pastes. The specific  
525 gravities of slag and Portland cement do not vary significantly and can be taken as 2.90 and 3.15 respectively. The LOI  
526 of the binders has to be known to correct for any mass change for the unreacted slag and cement during ignition to  
527 1000°C. However, this correction is insignificant for mature samples and thus may be omitted without causing large  
528 errors. For example, reanalysing our data for the 3-day, 28-day and 1-year old samples but ignoring LOI corrections for  
529 the unreacted slag and cement produced average differences of 0.7%, 0.4% and 0.2%, respectively for the volume  
530 fraction of water. However, this caused the mean errors of the w/b ratios for the 3-day and 28-day samples to increase  
531 significantly, i.e. from 1.2% to 4.2% and from 2.3% to 4.2%, respectively whilst for the 1-year cured samples, the mean  
532 error increased slightly, i.e. from 3.8% to 4.6%.

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534

535 In practice, concretes with high w/b ratio will be of most interest in the context of resolving disputes due to suspected  
536 non-compliance with mix specification. The presence of aggregates does not influence the method because its volume  
537 fraction is constant with time and is measureable with image analysis. However, aggregates will increase the  
538 heterogeneity of the paste microstructure so that a larger set of image frames must be analysed to obtain representative  
539 results. The volume fraction, specific gravity, water absorption and any loss on ignition of the aggregate will be  
540 required so that the relevant corrections can be made in the calculations. Volume fraction can be measured directly with  
541 image analysis, while the specific gravity, absorption and LOI can be reasonably estimated from the type and  
542 mineralogy of the aggregate, if a sample of the aggregate is not available for direct measurements. Similar corrections  
543 will be required if the Portland cement contains blended limestone fines.

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545

546 In terms of practical application, the method would not yield accurate results if applied to concrete that had experienced  
547 significant mechanical damage or chemical deterioration (carbonation) during the period between initial set and the  
548 time of testing such that the approximation shown in Eq. (1) no longer applies. Therefore, one must ensure that samples  
549 are taken away from the surface zone where these effects may have occurred. This applies to all test methods designed  
550 to assess bulk properties of concrete, for example compressive strength. The method is valid for concretes containing

551 entrained air or excess voidage, since the amount of air voids can be measured with image analysis and corrections can  
552 be made by subtracting the volume fraction of air voids from the measured volume fraction of water to remove any  
553 contribution from the air voids during vacuum saturation. The method is also not affected by bleeding or absorption into  
554 porous aggregates for calculating the free w/b ratio. However, results from our study [17] show that bleeding and  
555 aggregate absorption can significantly reduce the free w/b and so must be accounted for meaningful comparison  
556 between the actual w/b ratio and estimated values. The amount of water absorbed by aggregates can be reasonably  
557 estimated from the type and mineralogy of the aggregate and hence corrections can be made to the measured water  
558 content. Samples that have experienced excessive bleeding will have a more heterogeneous microstructure and show a  
559 larger spread in local w/b ratio therefore requiring more image frames to be averaged to obtain accurate point counting  
560 results. However, any bleed water that is lost to evaporation would result in the measured water content being lower  
561 than expected from the mix proportions. Clearly, more work is needed to test the method on a wider range of samples,  
562 to determine its repeatability and reproducibility, in particular for concretes containing slag.

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564

## 565 **6 Conclusion**

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567

568 There is a practical need for a reliable and rapid method for estimating the slag fraction and water/binder ratio in  
569 hardened concrete. This paper presents a new microscopy-based method for estimating the original mix composition of  
570 hardened slag-blended concretes. The method involves two main measurements: 1) SEM-BSE point counting of the  
571 volume fraction of reacted slag, unreacted slag, unreacted cement and air voids, and 2) heating and igniting the samples  
572 at 105°C and 1000°C, respectively to establish the evaporable and non-evaporable water contents. The results are then  
573 used to calculate the original slag, cement and water contents in the cement paste, thus allowing the w/b and s/b ratios  
574 to be established. The main advantage of the method in relation to existing methods is that it does not require  
575 comparison to reference standards identical to the unknown samples or prior knowledge of the chemical composition of  
576 the binders used. Moreover, the method calculates the degrees of reaction of both cement and slag in blended systems.  
577 The method was tested on 60 different samples with a wide range of w/b ratios (0.30 to 0.50), s/b ratios (0 to 0.6) and  
578 curing ages (3 days to 1 year). The results show that the method is very promising. The mean absolute errors for the  
579 estimation of slag, water and cement contents were 9.1%, 1.5% and 2.5%, respectively. The mean absolute error for the  
580 estimated w/b ratio was 4.7%. Of the 60 samples tested, the largest error in the estimated w/b ratio was 0.046. 91% of  
581 the estimated w/b ratios were within 0.036 of actual values. The results also show that slag had a slight accelerating  
582 effect on the hydration of cement at 3 and 28 days, but this became insignificant at 1 year. The degree of reaction of



583 slag at 28 days and 1 year increased with increasing w/b ratio. At a constant w/b ratio, the degree of reaction of slag  
584 decreased with increasing s/b ratio.

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589

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## 595 **References**

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