# Water vapor transport in soils from a pervaporative irrigation system

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## 4 ABSTRACT

A novel method for irrigation with saline water uses a polymer membrane, formed 5 into a tube, to treat and distribute the water simultaneously. The flux of water across 6 the membrane occurs by the process of pervaporation, during which a phase change from 7 liquid to vapor occurs. Thus water arrives in the soil in vapor phase. The experimental 8 results presented in this paper demonstrate that, contrary to previous assumptions, 9 soil vapor flows are a significant transport mechanism during pervaporative irrigation 10 in dry soils. The soil water sorption properties affect the rate of condensation in the 11 soil, which in turn affects both the water distribution in the soil and the loss of water 12 vapor to the atmosphere. The flux from the tube becomes limited by high humidities 13 adjacent to the external surface of the membrane. Thus enhancing condensation in 14 the soil or increasing diffusion through the soil increases flux from the system. These 15 findings highlight the need to consider how plants might interact with water supplied 16

<sup>17</sup> in the vapor phase.

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## 19 Introduction

With growing pressure on the availability of freshwater for agriculture, irriga-20 tors are increasingly exploiting lower quality water sources (Pereira et al., 2002). 21 However irrigating with these waters can, over time, contribute to soil saliniza-22 tion (Penov et al., 2011) or cause other environmental concerns (Beltrán, 1999). 23 The pervaporative irrigation system used in this research is described previously 24 in a series of publications (Quiñones-Bolaños et al., 2005a,b; Quiñones-Bolaños 25 and Zhou, 2006). This system provides in-situ treatment of saline water while 26 simultaneously supplying it to the plant root zone. To irrigate in this way a per-27 vaporative polymer membrane is formed into a tube, buried in the ground and 28 filled with saline water. When the surrounding soil is dry a chemical potential 29 gradient exists across the membrane and draws water into the soil, whilst the 30 transport of salt is limited. The water flux occurs via a membrane transport 31 process called pervaporation. As plants take up water from the root zone the soil 32 moisture content is reduced, decreasing the chemical potential in the soil. This 33 maintains a gradient across the tube, which enables the continued transport of 34 water. The system is intended for use in arid regions, generally deserts, where 35 freshwater is limited but there is an available supply of saline water. 36

Membrane transport processes like reverse osmosis, gas permeation and pervaporation are frequently used in separation technologies (Pabby et al., 2008). Pervaporation is distinct these other membrane transport processes because of the phase change from liquid to vapor that occurs during the process (Feng and Huang, 1997). Conceptually the process of pervaporation is often considered in three steps:

<sup>43</sup> 1. Sorption of the permeate into the membrane

- 2. Diffusion of the permeate across the membrane
- 45

3. Desorption of the permeate in the vapor phase at the external edge

Transport across the membrane used in this research occurs by pervaporation 46 because the membrane polymer is highly hydrophilic. Thus molecules of water 47 are readily adsorbed into the polymer but desorb from it primarily in the vapour 48 phase. Mathematically, the process of pervaporation can be modeled using the 49 solution-diffusion equation (Paul, 2004), which takes into account the sorption of 50 the permeate into the membrane and its subsequent diffusion across the mem-51 brane. The exact location of the phase change from liquid to vapor is unknown, 52 thus diffusion across the membrane may occur in either liquid phase, vapor phase 53 or both. To simplify calculations it is often assumed that transport occurs en-54 tirely in one phase. Thus the driving chemical potential gradient is calculated 55 either using a liquid concentration gradient or, more commonly, a vapor pres-56 sure gradient applied across the membrane (Wijmans and Baker, 1995). Sumesh 57 and Bhattacharya (2006) suggest that transport through the membrane occurs 58 entirely in liquid phase if the gradient across the membrane is below a thresh-59 old value. However as the applied gradient increases the liquid-vapor interface 60 retreats into the membrane, away from the external surface. 61

The efficacy of a pervaporative irrigation system to treat saline water has al-62 ready been a subject of some study (Quiñones-Bolaños et al., 2005a,b). From a 63 water treatment perspective a particular benefit of the system is its low energy 64 requirement, as the driving force for the water flux is provided by the environmen-65 tal conditions surrounding the tube. As an irrigation system, another feature of 66 the system also stands out; the inherent feedback between the crop water uptake 67 and the irrigation flux. In recent years techniques such as irrigation scheduling 68 (Jones, 2004) and precision irrigation (Sadler et al., 2005) have been developed to 69

contrive such feedback mechanisms. These methods use sensors to monitor plant 70 water stress (either directly or indirectly). A control system is then implemented 71 to apply water as required, both spatially and temporally. In pervaporative irri-72 gation the system automatically responds to the soil moisture conditions without 73 the need for monitoring. However, once the pervaporative tube is in operation 74 the user has no control over the flux rate. Thus it is important to ensure that 75 sufficient membrane surface area is present in the soil by estimating the likely 76 flux rate from the tube. 77

One model (Quiñones-Bolaños and Zhou, 2006) currently exists to predict the 78 flow rate across the irrigation tube in the soil. In this model the soil moisture 79 conditions are simulated mathematically so that the feedback between the soil 80 moisture conditions and the flux from the tube can be represented. However, 81 it is assumed that the mass transport of water through the soil only occurs in 82 the liquid phase. As the water leaves the membrane in vapor phase it is thus 83 assumed that all of the mass permeating through the tube condenses in the near 84 vicinity. However, it is possible that vapor transport through the soil affects both 85 the distribution of the liquid soil water content and the mass transfer of water to 86 the atmosphere at the soil surface. 87

Diffusive vapor transport through soil occurs due to gradients in the partial 88 pressure of water vapor in the soil pores. Such gradients can occur due to vari-89 ations in temperature, solute concentration and soil water content, all of which 90 affect the equilibrium relativity humidity between the liquid and vapor phases 91 in the soil. Gradients in temperature (Phillip and de Vries, 1957; Bittelli et al., 92 2008) and solute concentration (Kelly and Selker, 2001) are often considered to 93 be significant near to the soil surface under field conditions. However, in this 94 research, no significant gradients in temperature or solute concentration are ex-95 pected due to the experimental methods used. Instead, because of the dry soil 96

<sup>97</sup> conditions, partial pressure gradients that occur due to variations in soil water
<sup>98</sup> content are of particular interest.

In general, vapor flows due to the variation in soil water content are small 99 because the vapor pressure in most soils approaches the saturated vapor pressure 100 at soil water contents above the residual water content of the soil. This can be 101 surmised by observing that, in the absence of osmotic effects, the equilibrium 102 humidity in soil is theoretically greater than 99.5% even at a suction pressure of 103 6 bar (Hillel, 1998, p150). Such high suction pressures correspond to low water 104 contents thus vapor pressure gradients due to soil water content variations are 105 often small. It has been suggested that the residual water content (although often 106 used as a fitting parameter) represents the water content below which water is 107 retained in the soil primarily by adsorptive forces (Lebeau and Konrad, 2010). 108 Hence, at water contents below this residual value, the water is no longer held 109 in the soil by capillarity but by short range adsorptive forces that bind water 110 molecules to the surface of solid particles, forming liquid films (Churaev, 2000, 111 p29-31). In these dry conditions bulk connectivity of water in the liquid phase 112 breaks down and water transport can occur by two mechanisms; liquid film flow 113 along the solid surfaces and vapor flow through the connected air phase (Churaev, 114 2000, p123). Significantly, when water is retained in the soil by adsorptive forces, 115 the equilibrium relative humidity of the vapor phase decreases (Ruiz and Benet, 116 2001) thus vapor pressure gradients can become significant even for tiny varia-117 tions in soil water content and isothermal vapor flow can occur. Although water 118 contents below the residual value are not common in field soils they do occur in 119 arid and semi-arid environments as the atmospheric conditions are very dry and 120 the soil moisture content near the soil surface is often in the adsorptive range 121 (Agam and Berliner, 2006), approaching equilibrium with the dry surrounding 122 air. 123

As this irrigation system is intended for use in arid, desert regions it is there-124 fore likely that vapor flows due to variations in soil water content will occur. 125 The experimental method used in this study was designed to re-examine the as-126 sumption made in previous work (Quiñones-Bolaños and Zhou, 2006) that water 127 transport through soil can be considered entirely in the liquid and to consider 128 its validity in different environmental conditions. The focus is on developing an 129 understanding of the physical processes, specifically the vapor flow, that affect 130 the irrigation flux into the soil and quantifying the flux in various environmen-131 tal conditions. To simplify the analysis this work was carried out in bare soil, 132 without the presence of a crop. 133

## 134 Experimental methods

The two experimental setups used in this research are shown in Figure ??. 135 The air box setup was designed to quantify the flux from the pervaporative mem-136 brane under different humidity conditions, i.e. under differing vapor pressure 137 gradients, without the complications of transport through the soil. The soil box 138 experiments were designed to explore how the presence of the soil, and various 139 soil conditions (soil depth, soil type, soil salinity, atmospheric humidity), affect 140 the flux, and how moisture is transmitted through and retained in the soil in liq-141 uid and vapor phases. Furthermore, to aid with the interpretation of the soil box 142 experiments, moisture sorption isotherms were determined to quantify the water 143 content of the soils at equilibrium in different humidity conditions. All of the 144 experimental work was carried out in a laboratory maintained at  $21\pm1^{\circ}$ C. The 145 pervaporative membrane used in these experiments was a non-porous hydrophilic 146 polymer composed of a thermoplastic block copolymer of the polyester family 147 synthesised by Du Pont de Nemours (Geneva, Switzerland). The dry thickness of 148 the membrane was 0.75 mm. The polymer was extruded into tubular form and 149



FIG. 1. Diagrams of the experimental setups for a) air box tests in which the tube was enclosed in a humidity chamber with conditions created using a saturated salt solution b) soil box tests in which the tube was buried in soil.

<sup>150</sup> corrugated (Figure ??) to provide structural strength. The inner diameter of the
<sup>151</sup> tube was 19 mm and the outer diameter was 23 mm due to the corrugations.

152 Air box tests

The air box setup (Figure ??a) was constructed to enclose the tube within an air filled chamber so that the flux under different humidity conditions could be observed. The initial conditions in the chamber were established using a saturated salt solution, which maintained the relative humidity at a constant level. Once the pervaporation tube was filled with water the humidity increased as moisture evaporated from the tube, diffused through the air and condensed into the salt solution. A series of saturated salt solutions were used to maintain the humidity at different levels. These saturated salt solutions were; lithium chloride
(11%), calcium chloride (33%), magnesium chloride (37%), calcium nitrate (55%),
sodium chloride (75%) and potassium chloride (85%). The relative humidities
given in brackets indicate the equilibrium condition between a saturated salt
solution and air at 21°C.

The pervaporative tube was stretched across the length of the humidity cham-165 ber and clamped at the entry and exit points by cable glands. Eighty corrugations 166 of tube were within the box corresponding to a dry, un-stretched length of 34cm. 167 The corrugations passing through the length of the cable gland were wrapped in 168 polyfilm to prevent pervaporation from this surface area. Outside of the chamber 169 the tube entered a PVC tube sealed with silicone sealant. One end of this tube 170 was connected to a supply reservoir placed on a load cell, whilst the other end 171 was bunged. Thus the water in the tube was in approximately hydrostatic condi-172 tions, other than the small flow rate due to the pervaporative flux from the tube. 173 The polypropylene box that formed the humidity chamber was sealed around the 174 lid with a foam sealant strip, clamped closed and placed on a load cell. Cables 175 exiting the box were sealed using cable glands. A tray containing a saturated 176 salt solution, and with excess salt, was positioned 4cm below the tube and placed 177 on a load cell to monitor the mass. The load cells were supplied by Applied 178 Measurements Ltd (Aldermaston, UK). The cells for the reservoir and the salt 179 solution had a 3kg maximum load (specification OBUG-3kg), whilst the mass of 180 the chamber was monitored using a cell with a 10kg maximum (OBUG-10kg). 181 All of the cells were fitted with aluminum platforms of appropriate dimensions. 182 The temperature and humidity probe was supplied by Michell Instruments (Ely, 183 UK), specification PC33-3-XX-T3-C (accuracy  $\pm 3$  for 30-80% RH). 184

The chamber was left for 24 hours before the start of the experiment to allow it to reach a pseudo-equilibrium condition. A temperature and humidity probe

positioned below the tube monitored the state of the chamber. To start the test 187 a tap between the supply reservoir and irrigation tube was opened, allowing the 188 tube to fill with water. The bung at the far end of the tube was removed to purge 189 air from the system and replaced when the tube was filled with water. Thus some 190 of the water exiting the supply reservoir at this time did not remain in the tube. 191 At the start of the experiment data were collected for one hour at one minute 192 intervals and for a further three hours at five minute intervals. For ten hours 193 before the irrigation started, and for the rest of the duration of the experiments, 194 the data were collected at fifteen minute intervals. The data were collected using a 195 National Instruments (Newbury, UK) NI USB-6210 data logger connected to the 196 LabVIEW software from the same supplier. A single ended voltage measurement 197 was made for each sensor as they all had a common ground. Each data point was 198 collected by sampling at a frequency of 10kHz for two seconds and recording the 199 mean and standard deviation of the measurement. 200

#### 201 Soil box tests

Figure ??b shows the soil box setup used for experiments to quantify the 202 flux of water from the tube into dry soil. The setup was similar to the air tests 203 described above but the humidity chamber was twice the size and the irrigation 204 tube was buried in soil. The same load cells were used to monitor the reservoir 205 and desiccant mass as for the air tests. The combined humidity and temperature 206 probe was in the air gap between the soil and the desiccant, positioned as in the 207 diagram. This soil box setup was used to conduct three sets of tests; one set with 208 varying depths of sand, one set with different conditions in the humidity chamber 209 and a final set with three different soil types. In the first set the depth of the sand 210 in the box was varied. The minimum depth was 7cm (from the base of the box) 211 and the maximum was 15cm. The tube was consistently buried 5cm from the 212



FIG. 2. Particle size distribution of the sand and top soil. The particle size of the sand was determined by lazer diffraction using a Coulter LS100 (Beckman Coulter, Inc., High Wycombe, UK), as the density of some particles was close to that of water the particle size was determined by sieving.

base of the box. All of these experiments were conducted using sand and 100g 213 of a calcium chloride based desiccant (brand name 'Drysac', Superdry Superior 214 Container Desiccant, Singapore). For comparison, an additional experiment was 215 performed using the same desiccant but without any soil. In the second set of 216 experiments the conditions in the humidity chamber were varied. One experiment 217 was conducted without a desiccant in the box, one with the 'Drysac' desiccant, 218 another with a saturated calcium chloride salt solution (instead of the desiccant) 219 and a final test in which the lid was removed from the box and the surface 220 was exposed to the ambient laboratory conditions. This set of experiments was 221 performed in sand with a depth of 15cm. In the third set of experiments three 222 types of soil were used; marine sand, a garden top soil and a salinized sand. Data 223 on the properties of these soils are provided in Figure ??, Figure ?? and Table ??. 224 The saline sand consisted of marine sand with an added 16g of sodium chloride 225 per kilogram of sand. In this set of experiments there was no desiccant present 226 in the box and the soil was packed to a depth of 10cm. 227



FIG. 3. Soil water retention characteristic of a) sand and b) top soil. These data were collected by placing a sample of the soil (packed at the target density) on a porous plate and applying a suction pressure to the underside of the plate using a hanging column of water (Haines, 1930). The water content of each soil sample was then determined gravimetrically. From this data the residual water content can be estimated as approximately  $0.02m^3/m^3$  in sand and  $0.08m^3/m^3$  in top soil.

Before each experiment the soil was dried in an oven at  $105^{\circ}$ C for 24 hours 228 and stored in an air tight container with silica gel desiccant to cool. Although this 229 procedure reduced the soil water content far beyond the permanent wilting point 230 (generally considered the minimum water content at which plants can grow), this 231 dryness represented possible field conditions in an arid or semi-arid environment. 232 The soil was packed into the boxes 1kg at a time and was compacted with a 233 flat aluminum pestle. The soil surface was then lightly scarified to improve the 234 hydraulic connection with the next layer, following the method reported by Lewis 235 and Sjöstrom (2010) for dry soil packing. After some of the experiments, samples 236 were taken from the soil to determine the liquid soil moisture content. Two 237 samples, each weighing approximately 200g, were taken from each box. These 238 samples were taken from the top 1cm of the soil and from the region immediately 239 surrounding the PV membrane (i.e. less than 1cm from the membrane). The soil 240

water content was determined gravimetrically by weighing the sample, drying it in an oven at 105°C for 24 hours, cooling it in a desiccator and re-weighing the sample. Gravimetric water contents were converted to the equivalent volumetric water content using the packing density of each of the soil types (Table ??).

The moisture sorption isotherms for the different soil types were determined 245 by two methods; desiccator experiments and using a vapour sorption analyzer 246 (VSA). Desiccator experiments were performed by enclosing soil samples in a 247 series of desiccators (Dexter and Richard, 2009). Samples were approximately 248 100g in weight. The relative humidity was maintained in each desiccator by a 249 saturated salt solution. The samples were allowed to reach equilibrium, a process 250 which took between 2-6 weeks. The water content of each sample was then deter-251 mined gravimetrically. VSA experiments were performed by Labcell Ltd (Alton, 252 UK) using a Decagon Devices (Pullman, WA, USA) analyzer. This device has a 253 chamber in which a soil sample is placed. The humidity in the chamber is changed 254 incrementally and the mass of the sample is monitored. The measurement limits 255 are between 10-90% relative humidity and the device monitors the change in mass 256 rather than the absolute mass. Thus the results from the desiccator experiments 257 were used to express the VSA results on an absolute scale. 258

# 259 Results and discussion

## 260 Air box tests

Figure ?? shows a sample of raw data that were collected in the course of these experiments. The initial change in the masses of the reservoir and soil box (observed at t=0hrs) corresponded to the filling of the irrigation tube. Transient conditions were evident for approximately the next eight hours. During this time the relative humidity in the chamber increased, the temperature near to the tube decreased and the measured masses of the reservoir and soil box changed at a



FIG. 4. Results for the air test experiments using a Lithium Chloride salt solution. The change in mass measured by the three load cells is shown relative to the measured value at t=10 hrs. The mass change of the reservoir is plotted as a positive change to allow comparison with the soil box data.

faster rate than that of the salt solution. After this time the system reached a 267 quasi-steady state in which the mass of water pervaporating from the tube was 268 equal to that adsorbed by the salt solution. In this state a humidity gradient 269 between the tube surface and the surface of the salt solution maintained diffusive 270 transport through the air. The system was not strictly at steady state as the 271 excess salt in the salt solution was constantly dissolving, but this effect was small 272 during the test period as excess salt was provided. Thus, a quasi-steady state was 273 maintained in the chamber. Slight variations in temperature (following ambient 274 laboratory conditions) continued to have a small effect on the relative humidity 275 in the chamber. 276

During the transient phase of the experiment the mass of water stored in the air increased and this was seen as an increase in relative humidity in the chamber. However, the mass of water in the air was only of the order of a few grams and did not explain the difference between the change in mass of the reservoir and the desiccant. The additional storage can be explained by membrane swelling, which occurred due to the sorption of water into the tube. This swelling increased the diameter of the tube and thus also increased the storage capacity for liquid water inside the tube. This additional capacity was filled from the reservoir and explains the difference in the mass change rate of the reservoir and the desiccant in the first five hours of the test. The length of the tube also increased due to the swelling; to minimize the effect of this the tube was stretched in its dry state before being clamped in position.

The flux rate from the tube in each experiment was estimated by fitting a 289 linear relationship to the time series of reservoir mass when the system was in 290 a quasi-steady state. This is illustrated in Figure ??. The data from the reser-291 voir mass was selected as this was less sensitive to noise. Linear regression was 292 performed using the MATLAB function 'robustfit', implemented using iteratively 293 reweighted least squares with a bisquare weighting function. This function also 294 provided an estimate of the parameter error. The calculated gradient gave the 295 estimate of the mass flow rate, the error in predicted value of these gradients was 296 small and negligible compared to errors in relative humidity. To convert to a flux 297 rate it was assumed that the tube was equivalent to a cylinder 53cm in length 298 with a diameter of 2.6cm (corresponding to the external diameter of the swollen 299 tube). The mean and standard deviation of the relative humidity measured in 300 the chamber was also calculated. For each of the salt solutions tested two ex-301 periments were conducted. The flux rates for each experiment were calculated 302 individually and are shown in Figure ??. 303

Figure ?? shows that the flux across the pervaporative membrane varied significantly with the surrounding partial vapour pressure as indicated by the relative humidity at  $21^{\circ}$ C. For relative humidities greater than 75% (at the location of the probe) the relationship between the humidity and the flux appeared to vary linearly, however the result for the lithium chloride solution (in which the relative



FIG. 5. Relationship between the observed flux and humidity in air tests.

humidity reached approximately 60%) did not continue this trend. It is considered 309 that the humidity measurements greater than 100% were likely to have occurred 310 due to probe error in highly humid conditions. Note that despite the unexpected 311 high humidity, the fluxes were consistent with those in the duplicate experiments. 312 A small flux was observed even at a relative humidity of approximately 100%. In 313 these conditions, under the action of diffusion alone, the partial vapour pressure 314 close to the membrane should be saturated and no flux would be expected across 315 the membrane. It is possible that this flux was observed due to temperature 316 effects, as the temperature at the membrane surface was slightly reduced by the 317 evaporation of water. The slightly cooler, denser air should therefore slowly sink, 318 transporting water vapor with it. 319

When the relative humidity is close to 100% it is likely that the phase change from liquid to vapor occurred at the external surface of the membrane. The flux rate was then limited by the rate of diffusion of water vapor away from the membrane surface. In experiments using salt solutions with lower equilibrium humidities the maximum possible partial pressure gradient was increased, thus



FIG. 6. Humidity change in the chamber after irrigation was commenced in sand of three different depths (from the base of the chamber) and in air. Duplicates of each experiment are shown. Note that in both of the tests with 10cm a sudden increase in laboratory temperature 6.5hrs into the experiments caused a temporary decrease in humidity.

the rate of diffusion increased. However, as the humidity decreased further to below 60%, the location of the phase change may have retreated away from the external edge of the membrane as suggested by Sumesh and Bhattacharya (2006). It is possible that such an effect could have a highly non-linear influence on the flux rate. The observation that the tube was visibly less swollen in the test using lithium chloride compared to the other tests provides qualitative support for this suggestion.

Overall, the results from the air box experiments demonstrated the magnitude of the vapor flux that can be achieved in humid conditions and show, as expected, that there is an inverse relationship between the partial vapor pressure (as indicated by the relative humidity) and the flux rate.

336 Soil box tests

Figure ?? shows the rate of change of the relative humidity in the first set of soil box tests, in which the depth of the sand was varied. For comparison, an additional experiment was performed in air alone. The humidity was 'normalized' compared to the initial and final values in the chamber thus the plotted 'normalized' humidity  $(RH_n)$  can be expressed as

$$RH_n = (RH - RH_0)/(RH_{40} - RH_0)$$
(1)

where  $RH_0$  is the initial relative humidity and  $RH_{40}$  is the relative humidity 40 hours after the start of the test. This was done primarily because the commercial desiccant that was used in the test did not reliably maintain the humidity in the chamber at the same value between repeated tests, but the rate at which the humidity changed between the initial to the steady state conditions was repeatable.

When the experimental system was implemented in air it was clear that all mass transport occurred in the vapor phase. The presence of the sand decreased both the magnitude and speed of the humidity response in the chamber. As the depth of the sand was increased the rate of change of the humidity in the chamber decreased. The form of these breakthrough curves suggests that a diffusive process still dominated mass transport, although with a lower diffusion coefficient.

A time series for the flux rate of water into the soil was estimated by approx-353 imating the rate of change of the mass of the reservoir. To reduce the effect of 354 noise (some of which was diurnal) the rate of change was approximated using the 355 data from a 24 hour period. The flux rates were approximated as before using the 356 MATLAB function 'robustfit'. Due to the chosen measurement window the first 357 approximation could be only made at t=12 hrs. However, as the reservoir mass 358 is affected by the tube swelling, the flux approximated in the initial stages of the 359 test is artificially high, and should be neglected for at least the first 20 hours. 360

Figure ?? shows the results for the second set of soil box experiments in which the conditions at the soil surface were varied. The median, interquartile range and



FIG. 7. The effect of environmental conditions on the irrigation flux. Four experiments are compared; one with no desiccant (nd), another with a calcium chloride salt solution (cd), the third with the commercial desiccant 'Drysac' (sd) and the fourth in a chamber without a lid, left open to the atmosphere (oa). The results for an independent repeat of each experiment are also shown. In the flux plot the flux computed from the change in the reservoir mass is shown in black and that computed from the change in the desiccant mass is shaded in gray.

range of the fluxes and relative humidity are shown, outliers are neglected. All 363 of these experiments are performed in sand of 15cm depth. Without a desiccant 364 the flux across the PV membrane was lower than the flux when a desiccant was 365 present. However, when a desiccant was present, a significant proportion of the 366 water traveled through the sand and was adsorbed into the desiccant. Thus this 367 water was not stored in the soil. This demonstrates that without considering the 368 vapor flow the soil moisture available for plant uptake cannot be predicted. This 369 finding is confirmed in the last test when the lid was removed from the soil box. 370 The flux out of the tube was comparable to that in the tests with a desiccant in 371 the chamber, as was the average relative humidity. It can therefore be surmised 372 that not all of the mass that left the tube remained in the soil and that some was 373 lost to the atmosphere in vapor phase. 374



FIG. 8. Comparison between irrigation flux into sand, top soil and saline sand. Note that the flux calculation for the first 24 hours is affected by the initial filling of the tube and is subsequent calculations may be affected by tube swelling. Duplicates of each experiment are shown.



FIG. 9. Moisture sorption isotherm of a) sand and top soil and b) saline sand at  $21^{\circ}$ C.

The moisture adsorption into sand is low thus it is unsurprising that vapor flow is significant. Figure ?? shows the results of the final set of soil box experiments, which compared the flux rate into marine sand to that into top soil and into

salinized sand. All experiments used a soil depth of 10cm and were conducted 378 without a desiccant in the chamber. The flux rate into the top soil varied with 379 time and decreased over the course of the test but remained higher than the flux 380 into the sand throughout. The relative humidity in the chamber above the top soil 381 began to increase around 50 hours after irrigation started, indicating that mass 382 transfer into the atmosphere began to occur at this time. The flux rate into the 383 salinized sand was higher than into the other two soils. As in the marine sand, 384 the humidity in the chamber above the salinized sand quickly increased when 385 irrigation was started, but stabilized at a lower value of approximately 80%. 386

Figure ?? shows the moisture sorption isotherms calculated from desiccator 387 and VSA experiments, and demonstrates that the differences in the humidity 388 profiles in Figure ?? occurred due to the moisture sorption characteristics of the 389 different soils. At low relative humidities sand adsorbs very little mass (Figure 390 ??), thus the humidity profile in the sand increased quickly (Figure ??). The top 391 soil adsorbs more mass at low humidity and the rate at which the mass increases 392 with humidity is also greater (Figure ??). Consequently in the soil box test the 393 increase in humidity was much slower than in sand as more of the flux out of 394 the irrigation tube was adsorbed in the soil (Figure ??). The sorption isotherm 395 for the saline sand is particularly interesting as the sand suddenly adsorbs more 396 mass at a relative humidity of approximately 75%. Such an increase in moisture 397 adsorption due to the addition of salt is not unexpected as this has also been 398 observed in the isotherms of pure sodium chloride (Foster and Ewing, 2000) and 399 salted food products (Comaposada et al., 2000). Consequently, in the experiment 400 in salinized sand, the humidity profile quickly increased to approximately 80%, 401 but flux from the tube remains high as moisture was being adsorbed into the soil. 402 After one of the tests in top soil and one in saline sand samples were taken 403 from from the soil to determine the soil water content. The initial water content in 404



FIG. 10. Plan view of the wetting front in the saline sand, observable as a change in color and consistency. The hole left after inserting a rod collapsed ahead of the front but retained its shape in the wet sand.

both soils before the experiments started was close to  $0m^3/m^3$  after oven drying. 405 Close to the tube the water content was  $0.037 \text{m}^3/\text{m}^3$  in top soil and  $0.12 \text{m}^3/\text{m}^3$ 406 in the saline sand. In the top 1cm of the soil the water content was  $0.026m^3/m^3$ 407 in top soil and  $0.001 \text{m}^3/\text{m}^3$  in saline sand. Whilst the fluxes into both soils were 408 of the same order of magnitude, the distribution of mass was different. The water 409 content in the top soil was more distributed and remained below the residual water 410 content of the soil (Figure ??) and within the range of water content measured 411 during sorption experiments (Figure ??). However in the saline sand there was 412 clear evidence of a wetting front (Figure ??) and the water content close to the 413 membrane was greater than the residual value of  $0.02 \text{m}^3/\text{m}^3$  (Figure ??). After 414 ten days the wetting front in saline sand extended approximately 4cm either side 415 of the tube, 3cm above the tube and reached the bottom of the enclosing chamber. 416 The absence of this front in the other two experiments is also significant, as it 417 suggests that flow throughout these soils only occurred in the vapor phase. In 418

<sup>419</sup> the saline sand it is probable that some liquid flow occurred.

These results raise a number of further questions regarding how this system 420 performs under field conditions. All of the experiments in soil have highlighted 421 the importance of considering both the transport and condensation of the vapor 422 phase. Thus, under field conditions, it is likely that factors that affect vapor 423 behavior will affect the system performance. Such factors include diurnal tem-424 perature variations, which induce vapor flows (Phillip and de Vries, 1957), and 425 soil heterogeneity, which will affect moisture sorption. It is also not clear how 426 plant roots interact with water vapor. A small amount of work has shown that 427 seeds absorb water vapor in the unsaturated zone (Wuest, 2007), but this work 428 has not been extended to consider developed plants. The presence of plant roots 429 is also likely to increase condensation in the soil. Further study is required to 430 understand how plants interact with water supplied from a vapor source. 431

In some commercial pervaporation systems and in the experiments of Quiñones-432 Bolaños et al. (2005a) air is swept over the surface of the PV membrane to main-433 tain a high pervaporation flux. However, when the PV tube is buried soil (as in 434 the experiments of Quiñones-Bolaños et al. (2005b) and in those presented in this 435 paper) the humidity in the soil pores surrounding the membrane is high, resulting 436 in a low flux across the membrane. Essentially, in these conditions, the flux is 437 limited by the transport through the soil, away from the membrane rather than 438 the membrane characteristics themselves. Thus if a plant roots are present and 439 remove water from the soil the flux from the PV tube should increase. However, 440 a significant increase in flux, would only be expected if the humidity in the soil 441 was very low (e.g. below 50%). Such low humidity corresponds to a soil water 442 content retained by adsorption and well below the permanent wilting of a plant. 443 Further work is required to establish whether such dry conditions continue to 444 prevail when a PV membrane is used in a vegetated environment. 445

## 446 Summary and Conclusions

To apply pervaporative irrigation systems successfully in the field it is important to predict the water that is likely to flow from the tube. The purpose of this study was to observe the flow rate in different controlled conditions so as to understand the fundamental processes that affect the interaction between the irrigation system and the soil. This work has shown that:

In humid air of approximately 100% relative humidity at 21°C, the flux
from the pervaporative tube is small; as the relative humidity decreases to
70% (21°C), the flux from the tube increases linearly. At lower humidities
the flux may become limited by other factors and does not seem to increase
further.

When buried in soil the tube is enclosed in an increasingly humid environment which depends on the soil sorption characteristics. Soil with high water sorption at low relative humidity increases the amount of condensation in the soil which results in an increased flux from the pipe. Hence, the addition of sodium chloride salt to sand (16g/kg) increased the flux rate by an order of magnitude. A moisture sorption isotherm is a useful predictor of this behavior.

3. Previous studies of pervaporative water transfer into soils assumed only 464 liquid transport. This study has shown that vapor flow through dry soil 465 is significant and affects the distribution of liquid water throughout the 466 soil and the flux of water from the system. This vapor flow also leads to 467 a loss of water to the atmosphere, thus failure to account for this process 468 can lead to an over estimation of the soil moisture content. Hence, the 469 availability of water for plant uptake from the soil cannot be predicted 470 without considering vapor flow. 471

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4. As the humidity in the soil increases the flow from the tube decreases, and
473 this increase in humidity occurs at low liquid moisture contents. Thus it
474 is surmised that flux from the tube only occurs in very dry soil conditions.
475 As little liquid water is available for plant uptake this raises an interesting
476 question as to how the plants interact with the vapor flow emanating from
477 this subsurface source. This question should be the subject of further
478 study.

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TABLE 1. Properties of different soil types.	Salinity w	as determined	using
a 1:5 soil:water volume ratio			

	Marine Sand	Saline Sand	Top Soil
Packing Density $(kg/m^3)$	1600	1600	1000
Salinity $(\mu S/cm)$	$1.4 \times 10^1$	$9.0 \times 10^3$	$2.7 \times 10^2$
Organic Matter $(\%)$	0.05	-	8.91
Carbon $(\%)$	0.03	-	5.08