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23 temperature. The present results are also compared against previously published ones for a  
24 more volatile n-heptane droplet and reveal that fuels with a lower volatility are more prone to  
25 breakup. A 0-D model accounting for the temporal variation of the heat/mass transfer  
26 numbers is proposed, able to predict with sufficient accuracy the thermal behavior of the  
27 deformed droplet.

28 **Keywords:** droplet breakup; VOF; heating; evaporation

29

## 30 **1 Introduction**

31 The efficiency of spray combustion systems is determined by the dispersion of the spray  
32 droplets which increase the surface area and subsequently the rates of heat and mass transfer.  
33 Following the primary jet breakup, the produced droplets are subjected to secondary breakup  
34 which further enhances the heat/mass transfer rates. The coupled problem of secondary  
35 droplet breakup under the influence of heating and evaporation is of major engineering  
36 interest, but due to its complexity has not been yet addressed in detail and the vast majority of  
37 relevant works examine these two phenomena independently.

38 Droplets under the influence of aerodynamic forces are subjected to different breakup modes,  
39 namely the bag breakup, the transitional breakup, the sheet-thinning breakup and the  
40 catastrophic breakup; for details see Guildenbecher et al. [1] among many others. The  
41 outcome of the breakup is determined by the relative strength of the aerodynamic, surface  
42 tension, viscous and external body forces acting on the droplet. These are grouped into  
43 dimensionless numbers, forming the Weber number ( $We$ ), the Reynolds number ( $Re$ ), the  
44 Ohnesorge number ( $Oh$ ), the density ratio ( $\varepsilon$ ) and the viscosity ratio ( $N$ ), as shown in Eq. 1,  
45 while under certain flow conditions other parameters such as the Froude number, the Mach  
46 number and the turbulence levels may become important.

$$We = \frac{\rho_g U_{rel,0}^2 D_0}{\sigma} \quad Re = \frac{\rho_g U_{rel,0} D_0}{\mu_g} \quad Oh = \frac{\mu_l}{\sqrt{\rho_l \sigma D_0}} \quad \varepsilon = \frac{\rho_l}{\rho_g} \quad N = \frac{\mu_l}{\mu_g} \quad (1)$$

47

48 The phenomena observed during droplet breakup have been addressed in review studies such  
 49 as those of [1-5] among others; it is generally considered that the  $We$  number is the most  
 50 influential parameter, while viscous effects become important when  $Oh > 0.1$ . The breakup  
 51 process requires some finite time to be established and the duration of the phenomenon is in  
 52 the order of the shear breakup timescale  $t_{sh}$  proposed by Nicholls and Ranger [6]:

$$t_{sh} = \frac{D_0}{U_{rel,0}} \sqrt{\varepsilon} \quad (2)$$

53

54 Many works have studied either experimentally or numerically the droplet breakup, aiming to  
 55 enlighten the conditions leading to the different breakup regimes and the underlying physics.  
 56 Selective experimental studies on droplet breakup are those of [7-22] but generally, there is a  
 57 scattering of the experimental findings which is probably due to the variety of the  
 58 experimental techniques used and the experimental uncertainties. Numerical works aiming to  
 59 fill the gap in knowledge such as those of [23-32]; they have examined the isothermal droplet  
 60 breakup in 2-D and 3-D computational domains and they have provided useful information  
 61 into the detailed processes inside and in the vicinity of the droplets during droplet breakup,  
 62 which are difficult to be determined with experimental techniques. More specifically, [7-10]  
 63 provided breakup maps in the  $We$ - $Oh$  plane, [11-13, 16] further clarified the boundaries  
 64 between different breakup regimes, [14, 15, 20, 23, 25, 30, 31] clarified the physical  
 65 mechanisms behind the breakup regimes, [13, 18] examined the size distribution of the child  
 66 droplets after the parent droplet disintegration, [22] identified experimentally the gas flow  
 67 structure during droplet breakup, [15, 24, 26, 32] examined the effect of density ratio and [26,

68 27, 29, 31] examined the droplet drag coefficient. For a detailed presentation of the works  
69 referring to droplet breakup, see Strotos et al. [33].

70 Regarding the evaporation studies, in addition to 0-D or 1-D models (see details in the review  
71 articles of [34-37] among others), detailed CFD works solving the complete Navier-Stokes  
72 and heat/mass transfer equations have also been published. Selectively, the works of [38-47]  
73 refer to single component evaporation and [48-53] refer to multicomponent droplet  
74 evaporation, providing detailed information in the transport processes between the liquid and  
75 the gas phase. More specifically, [39, 40] were the first who solved the complete set of the  
76 governing equations, [42, 47] modelled the presence of the suspender, [43] examined the  
77 effect of thermocapillary flow, [44] studied the effect of turbulence and [46] proposed  
78 numerical improvements for the evaporation modelling. Similarly, in multicomponent studies  
79 the first ones were those of [48, 49], followed by [50] who included variable thermophysical  
80 properties and [52, 53] which conducted parametric studies. The aforementioned studies were  
81 restricted to the modelling of isolated spherical droplets and a detailed presentation of the  
82 works referring to droplet evaporation, was given in Strotos et al. [54].

83 Regarding the coupled problem of droplet breakup and evaporation, this has not yet been  
84 studied in detail except in the CFD works of [55-60]. Haywood et al. [55, 56] showed that for  
85 droplets under steady or unsteady (oscillatory) deformation, the quasi-steady correlations for  
86 Nusselt ( $Nu$ ) and Sherwood ( $Sh$ ) numbers are still valid when a volume-equivalent diameter is  
87 used, Mao et al. [57] showed that the mass transfer from deformed droplets is mainly  
88 controlled by the Peclet ( $Pe$ ) number, while the  $We$  number has a small impact only at high  
89  $Pe$  numbers. Hase and Weigand [58] studied the effect of droplet deformation on the heat  
90 transfer enhancement and they found that this increases due to the oscillatory droplet motion  
91 and the increased surface area of the deformed droplets; moreover, the steady-state classical  
92 correlations for the  $Nu$  number, under-predict the heat transfer at the beginning of the  
93 simulation. Later, Schlottke et al. [59] included the evaporation in their model and they found

94 that the droplet heating is affected by the flow field inside the droplet which transfers hotter  
95 fluid from the droplet surface towards inside. Cerqueira et al. [60] studied spherical and  
96 deformed rising bubbles and proposed new correlations for the  $Nu$  and  $Sh$  numbers.

97 The aforementioned studies were restricted to  $We$  number below 10, which limits the results  
98 to small droplet deformation without breakup. Recently, Strotos et al. [61] examined the  
99 effect of heating and evaporation in cases undergoing breakup for  $We=15-90$ . They examined  
100 volatile n-heptane droplets and they showed that the droplet heating becomes increasingly  
101 influential during breakup for lower  $We$  number and higher gas temperature. The present  
102 numerical work is a continuation of this work and examines an n-decane droplet with  
103 substantially lower volatility than the n-heptane; this promotes the higher heating of the  
104 droplet. This work is the first examining the combined effect of heating and breakup solving  
105 the Navier-Stokes, energy and transport of species equations coupled with interface capturing,  
106 for a wide range of  $We$  numbers, gas phase temperatures for this particular fuel while it  
107 compares it with the less volatile one for similar flow conditions. The structure of the paper  
108 includes a brief description of the numerical model and the cases examined, followed by the  
109 results, while the most important conclusions are summarized at the end.

110

## 111 **2 Numerical model and methodology**

112 The continuous field representation of the two-phase flow with the VOF methodology is used  
113 to study the droplet breakup. The problem is assumed to be 2-D axisymmetric and an  
114 automatic local grid refinement technique [62, 63] enhances the accuracy of the computations  
115 at the interface region, while achieving low computational cost compared to a simulation with  
116 a uniform grid of the same density. The droplet heating and evaporation are accounted for by  
117 solving the energy and vapor transport equations, while the local evaporation rate is obtained  
118 by using a model based on Fick's law, which is independent of the droplet shape. The species

119 properties depend on the local temperature [64, 65] and mass averaging rules are used for the  
120 gaseous mixture assuming incompressible ideal gas. For the complete presentation of the  
121 equations solved, the reader is referred to Strotos et al. [54]. The simulations were performed  
122 with the commercial CFD tool ANSYS FLUENT v14.5 [66] and the numerical settings  
123 adopted as also the User Defined Functions (UDFs) are identical to those used in Strotos et al.  
124 [61].

125 The model has been successfully validated in [33, 54, 63, 67, 68] for cases including the  
126 motion of a free falling droplet, droplet breakup, droplet evaporation and droplet impact onto  
127 a solid substrate.

128

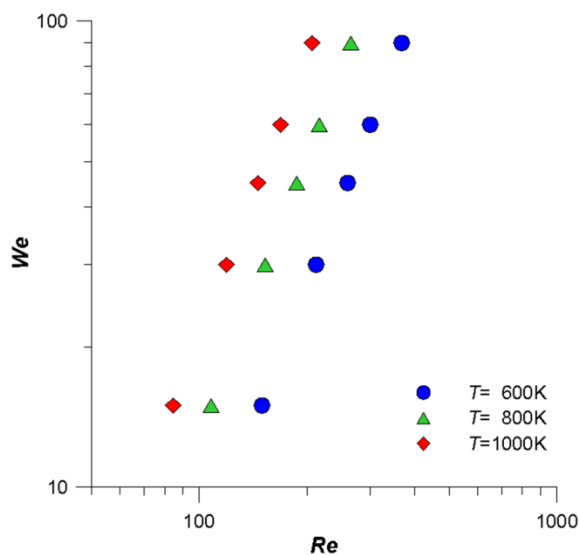
## 129 **3 Results and discussion**

### 130 **3.1 Cases examined and numerical setup**

131 The cases examined are similar to those presented in Strotos et al. [61] for a volatile n-  
132 heptane droplet (C07), but this time an n-decane (C10) droplet is examined which has a much  
133 lower volatility (i.e. vapor pressure) than the n-heptane. The cases examined refer to a small  
134 100 $\mu$ m diameter droplet with an initial temperature of  $T_0=300$ K, corresponding to  $Oh=0.02$   
135 which is low enough to guarantee breakup process almost independent from the  $Oh$  number.  
136 The droplet is assumed to be initially motionless and it is subjected to a step change of the gas  
137 phase velocity leading to  $We$  numbers in the range 15-90. The ambient air has a high  
138 temperature in the range 600-1000K ( $T_{cr,C10}=617.7$ K) which correspond to high density and  
139 viscosity ratios ( $\epsilon>1200$  and  $N>20$  respectively) and thus the breakup outcome is not affected  
140 by them since  $\epsilon>32$  [24]. The aforementioned combination of  $We$  numbers and gas phase  
141 temperatures corresponds to gas phase velocities in the range 77-243m/s; these in turn  
142 correspond to  $Re$  numbers in the range 84-367 which ensures that the flow remains laminar

143 and axisymmetric [69, 70]; the Mach numbers are below 0.38, which implies that the  
 144 compressibility effects can be ignored. For all cases examined, the ambient pressure is  
 145 atmospheric; thus no modifications capturing high pressure effects are required in the  
 146 evaporation model. A graphical representation of the cases examined is shown in Fig. 1 on the  
 147  $We-Re$  map. These cases were examined both for evaporating and isothermal conditions. For  
 148 the latter, the energy equation and the evaporation source terms were not accounted for, while  
 149 the species properties were kept constant at their reference temperature values, i.e. at  
 150  $T_0=300K$  for the liquid droplet and at  $T_\infty$  for the surrounding air; the isothermal runs  
 151 correspond to a parametric study for the effect of  $We$  and  $Re$  numbers.

152



153

154 Fig. 1: Cases examined on the  $We-Re$  plane.

155

156 Regarding the computational domain and the boundary conditions, these are the same as in  
 157 Strotos et al. [33, 61, 68], in which a step change of the gas phase velocity is applied around  
 158 the initially motionless droplet; the 2-D axisymmetric computational domain is moving with  
 159 the average translational droplet velocity. Upwind the droplet, Dirichlet boundary conditions



160 were applied (i.e. fixed velocity and temperature for the non-isothermal cases) and downwind  
 161 Neumann boundary conditions (i.e. zero first gradient for all variables) were used. A locally  
 162 refined grid with 192 cells per radius was used, able to resolve the boundary layers at the  
 163 interface region as explained in Strotos et al. [61]. It has to be noted that the 2D simulations  
 164 performed in this work are considered reliable up to the breakup instant, since after that,  
 165 three-dimensional phenomena appear.

166 In an effort to relate and also distinguish the simulations performed in Strotos et al. [61] for  
 167 the volatile n-heptane droplet, from the present simulations referring to n-decane, the heat and  
 168 mass transfer Spalding numbers ( $B_T$  and  $B_M$  respectively) are considered (Eqs. 3 and 4). These  
 169 are calculated by using the initial surface temperature  $T_{s,0}$  (Eq. 5) which corresponds to the  
 170 contact temperature between semi-infinite solids [71]; this concept was also used in [72-74]  
 171 for droplet impact on hot substrates and agrees well with the CFD predictions at the first time-  
 172 step.

$$B_{T,\infty} = \frac{c_{p,g,\infty}(T_\infty - T_0)}{L(T_{s,0})} \quad (3)$$

$$B_{M,0} = \frac{Y_s(T_{s,0}) - Y_\infty}{1 - Y_s(T_{s,0})} \quad (4)$$

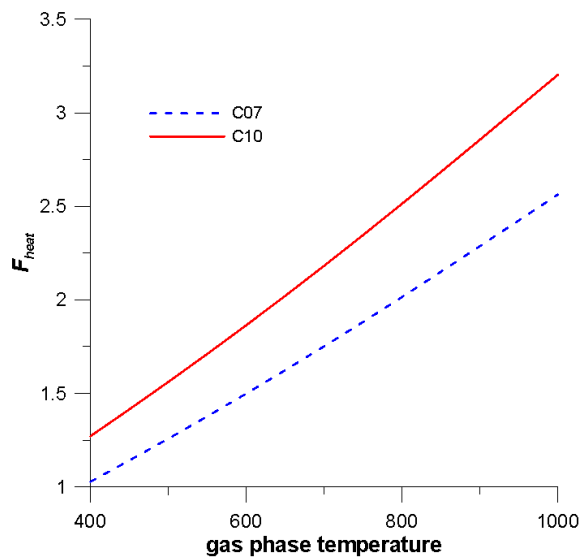
$$T_{s,0} = \frac{\gamma_l T_0 + \gamma_g T_\infty}{\gamma_l + \gamma_g} \quad (5)$$

$$F_{heat} = \frac{1 + B_{T,\infty}}{1 + B_{M,0}} \quad (6)$$

173 The droplet's tendency to increase its temperature is proportional to  $B_T$  and inversely  
 174 proportional to  $B_M$ , since the evaporation absorbs heat and tends to decrease the droplet  
 175 temperature. An indicator of the droplet heat-up is the heating factor  $F_{heat}$  (Eq. 6); large values  
 176 imply a high tendency to increase the temperature. A comparison of the heating factor for the  
 177 n-heptane (C07) and the n-decane (C10) is shown in Fig. 2 as a function of the gas phase

178 temperature for  $T_0=300\text{K}$  (note that this is independent of the flow conditions). It is evident  
179 that the n-decane has a higher possibility to heat-up due to its lower vapor pressure; the  
180 heating factor increases with the gas phase temperature and decreases with increasing initial  
181 fuel temperature (not shown in Fig. 2). It has to be noted that the heating factor has a  
182 qualitative character and for the isothermal cases it was assumed that  $F_{heat}=1$ , which  
183 corresponds to infinite latent heat and zero vapor pressure. Note that the definition of the  
184 heating factor adopted here is suitable for the present conditions, but might not be suitable for  
185 low ambient temperatures close to the droplet temperature in which  $F_{heat}<1$ .

186



187

188 Fig. 2: Heating factor as a function of the gas phase temperature for two different fuels  
189 ( $T_0=300\text{K}$ ).

190

191 Finally, prior to the presentation of the results of the present work, it has to be noted that the  
192 isothermal simulations conducted in Strotos et al. [61] for an n-heptane and the present  
193 simulations for an n-decane are in close agreement between them since they both have low  
194  $Oh$  numbers (0.01 and 0.02 respectively) and similar  $Re$  number ranges (77-337 and 84-367

195 respectively for  $T_\infty=600-1000\text{K}$ ). On the other hand, the evaporating simulations for these two  
196 fuels are exhibiting large variations due to the species thermal properties.

197

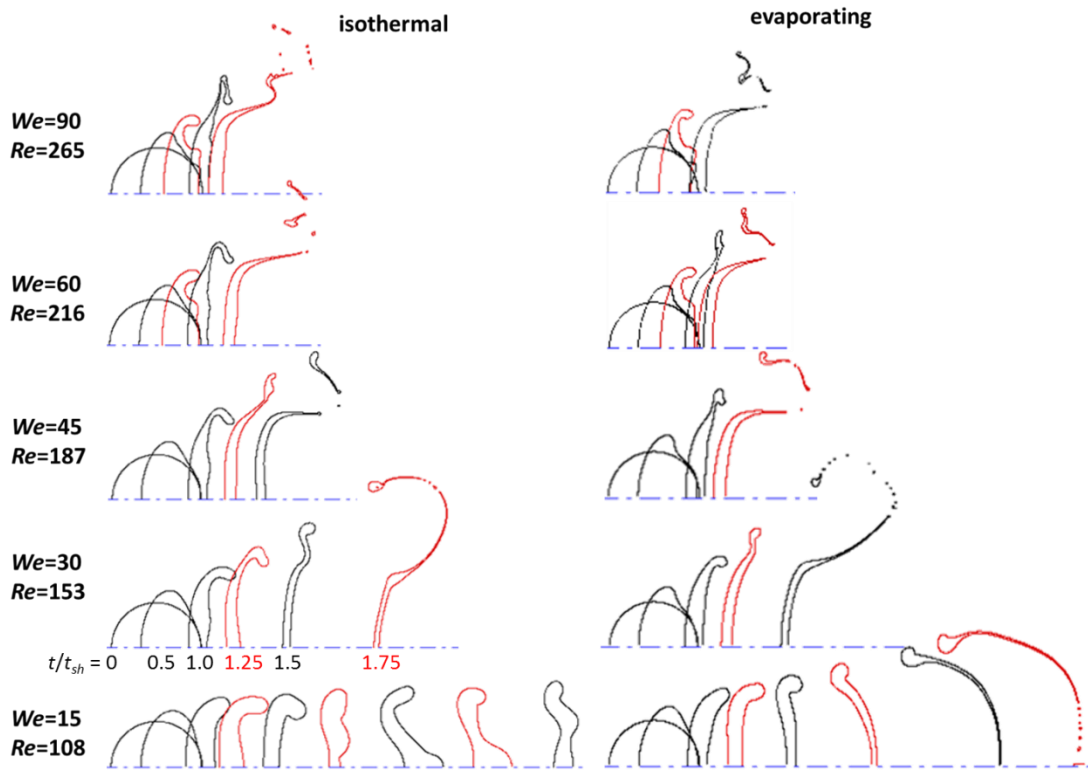
### 198 **3.2 Hydrodynamic effect of heating**

199 The results obtained for the droplet shapes are shown in Fig. 3 and Fig. 4 for the cases with  
200 free stream temperature 800 and 1000K respectively. In these figures the left part corresponds  
201 to the isothermal predictions and the right part to the evaporating simulations; the cases with  
202  $T_\infty=600\text{K}$  are not presented since the differences between isothermal and evaporating  
203 simulations were small. The droplet shapes drawn in black correspond to time intervals of  
204  $0.5t_{sh}$  (i.e. 0.0, 0.5, 1.0, 1.5,  $2.0t_{sh}$ ) and the droplet shapes drawn in red correspond to  
205 intermediate instances i.e. 0.75, 1.25, 1.75,  $2.25t_{sh}$  (the time instant of  $0.25t_{sh}$  has been  
206 omitted); the last droplet shape corresponds to the instant of breakup. From figures Fig. 3 and  
207 Fig. 4 it is evident that the  $We$  number is the most influential parameter leading to different  
208 breakup regimes as the  $We$  number increases, namely the bag breakup for low  $We$  numbers,  
209 the transitional breakup for intermediate  $We$  numbers and the sheet-thinning breakup for the  
210 highest  $We$  number examined. Nevertheless, the sheet-thinning breakup is not clear due to the  
211 low  $Re$  number and the continuous transition between the different breakup regimes; the  
212 effect of  $Re$  number and the existence of a critical  $Re$  number leading to bag breakup at  
213  $We=15$  was in detail discussed in Strotos et al. [61] and similar comments were also made in  
214 Han and Tryggvason [23] and Guildenbecher et al. [1].

215 Apart from the dominant role of  $We$  number, the droplet heating is playing an important role  
216 for the low  $We$  number cases. Under isothermal conditions, droplets with  $We=15$  and  
217  $T_\infty>800\text{K}$  are not breaking up due to the low  $Re$  number. At the same  $We$  number when  
218 heating is accounted for with  $T_\infty=800\text{K}$  (Fig. 3), a clear bag breakup is predicted; this is even  
219 more emphatic for the case of  $T_\infty=1000\text{K}$  (Fig. 4) in which the droplet not only breaks up, but

220 the breakup regime predicted is the transitional breakup. To the authors best knowledge, no  
 221 previous study has reported transitional break-up at such a low  $We$  number; this is purely due  
 222 to the droplet heating which reduces the surface tension coefficient and subsequently the  
 223 forces tending to resist the droplet deformation. Note that the effect of heating was not so  
 224 profound in the high volatility n-heptane examined in Strotos et al. [61].

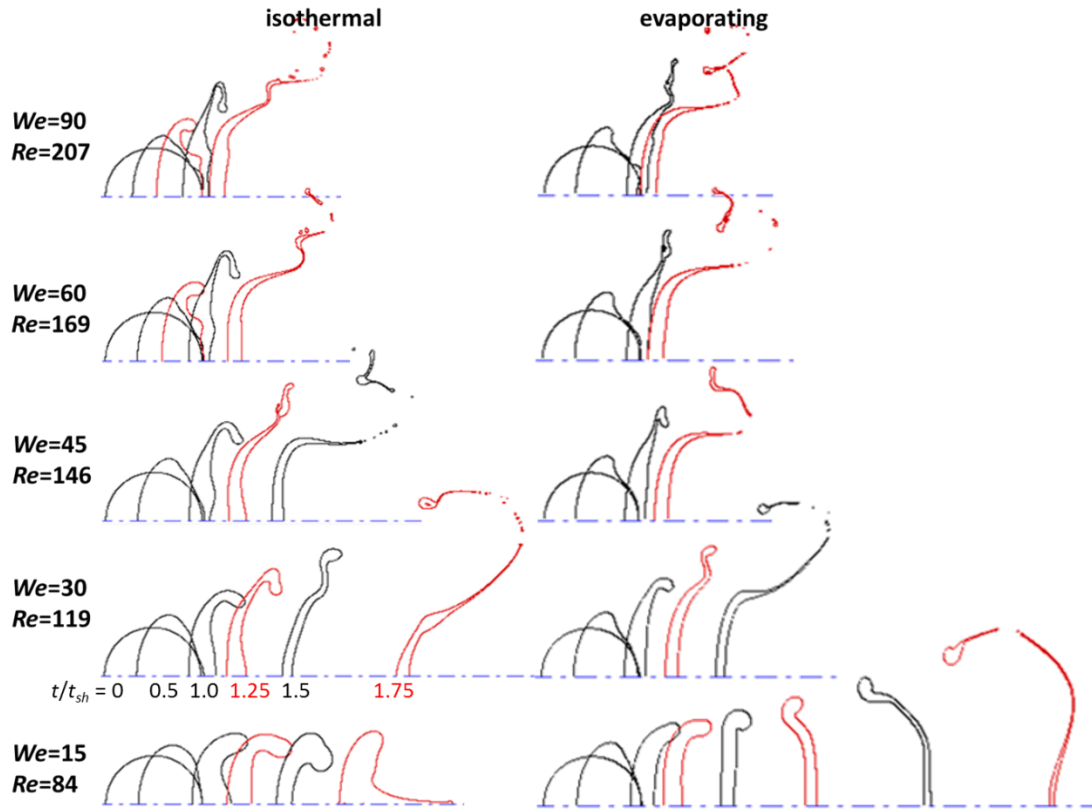
225



226

227 Fig. 3: Droplet shape evolution for the cases with  $T_{\infty}=800K$ . The droplet shapes drawn black  
 228 (see the online version) correspond to time intervals of  $0.5t_{sh}$  and the droplet shapes drawn red  
 229 correspond to representative intermediate instances of  $0.25t_{sh}$ . The last droplet shape  
 230 corresponds to the instant of breakup. Differences are observed at the lower  $We$  number case.

231



232

233 Fig. 4: Droplet shapes for the cases with  $T_\infty=1000\text{K}$ . The droplet shapes drawn black (see the  
 234 online version) correspond to time intervals of  $0.5t_{sh}$  and the drawn red correspond to  
 235 representative intermediate instances of  $0.25t_{sh}$ . The last droplet shape corresponds to the  
 236 instant of breakup. Differences are observed at the lower  $We$  number case.

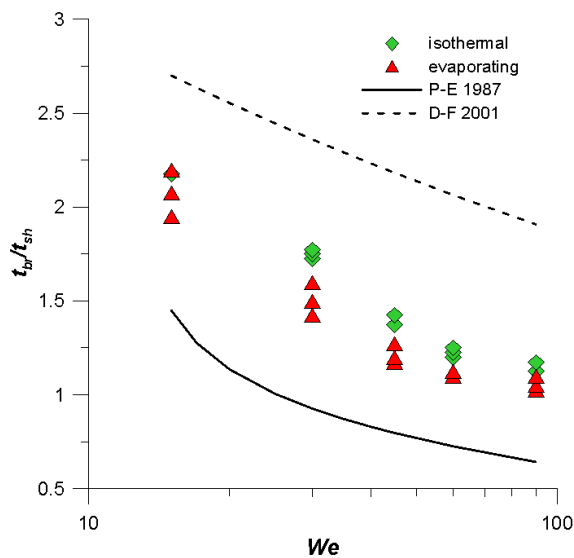
237

238 The predicted onset of breakup  $t_{br}$  (termed also as “initiation time”) for all cases examined is  
 239 shown in Fig. 5, along with the corresponding experimental correlations given by Pilch and  
 240 Erdman [2] and Dai and Faeth [13], abbreviated as “P-E 1987” and “D-F 2001” respectively;  
 241 the present data for the breakup time are subjected to error of the order of  $0.05t_{sh}$  (2.5-5%) due  
 242 to the estimation of the breakup time by examining post-processed images. The experimental  
 243 correlations differ between them due to several experimental uncertainties [25]. The trends  
 244 are correctly captured by predicting faster breakup with increasing  $We$  number. The  
 245 isothermal cases exhibit a weak dependency on  $Re$  number when the  $We$  is kept constant,

246 while in the evaporating cases the reduction of the surface tension coefficient acts as if the  $We$   
 247 number was higher; subsequently the droplet breaks up is faster. A best fit curve of the  
 248 breakup time for both evaporating and isothermal cases is given in Eq. 7 valid for the entire  
 249 range of conditions examined, i.e n-decane fuel,  $Oh=0.02$ ,  $We=15-90$ ,  $Re=84-367$  and  
 250  $T_\infty=600-1000K$ .

$$t_{br}/t_{sh} = 8.628We^{-0.352}Re^{-0.086}F_{heat}^{-0.116} \quad (7)$$

251



252

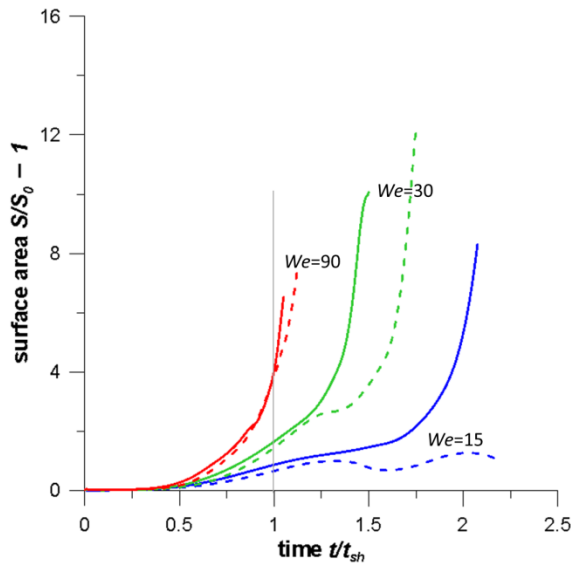
253 Fig. 5: Predicted dimensionless breakup time for the isothermal and the evaporating n-decane  
 254 cases.

255

256 One of the most important magnitudes determining the combustion efficiency is the droplet  
 257 surface area ( $S$ ) which deviates significantly from the corresponding of the initial spherical  
 258 shape ( $S_0$ ) during the droplet deformation and breakup and it is difficult to be measured  
 259 experimentally. The temporal evolution of this quantity is presented in Fig. 6 for selected  
 260 cases ( $T_\infty=800K$  and  $We=15, 30, 90$ ); note that for the isothermal case with  $We=15$ , the

261 droplet is not breaking up. In all cases, after an initial non-deforming period of  $\sim 0.3t_{sh}$ , the  
 262 droplet surface area starts to increase with a fast rate (1.6-5.7 in terms of non-dimensional  
 263 units) proportional to the  $We$  number, which is in accordance with the findings of Han and  
 264 Tryggvason [23]. Up to  $t=t_{sh}$  the variation of the surface area is smooth, but at subsequent  
 265 times the rate of deformation may change due to surface instabilities appearing even in the  
 266 isothermal cases. For that reason, the maximum surface area at the instant of breakup is not  
 267 following a smooth variation as the  $We$  number is changing and a local maximum is observed  
 268 at  $We=30$  (as it was also shown in [61]) reaching values of  $12S_0$ . This point needs further  
 269 investigation by performing 3-D simulations since 3-D phenomena may appear before the  
 270 breakup instant and alter both the rate of deformation as also the breakup instant. Regarding  
 271 the effect of heating (see the solid lines in Fig. 6), it is evident that it is important for low to  
 272 medium  $We$  numbers and  $t>t_{sh}$  by further increasing the rate of deformation.

273



274

275 Fig. 6: Temporal evolution of the dimensionless droplet surface area for selected cases with  
 276  $T_\infty=800K$ . The dashed lines correspond to the isothermal cases and the solid lines to the  
 277 evaporating cases.

278

279 As explained in Strotos et al. [61] it is difficult to find a mathematical expression predicting  
280 the temporal evolution of the surface area for the entire phenomenon up to the breakup instant  
281 and covering the entire range of  $We$  numbers leading to different breakup regimes. This  
282 becomes even more complex when heating is included since the surface area evolution is  
283 implicitly coupled with the variation of the surface tension coefficient due to heating. On the  
284 other hand, the evolution of the surface area can be predicted for  $t < t_{sh}$  with Eq. 8a, which has  
285 been slightly modified relative to the one used in [61] by using in the denominator on the  
286 right hand side of Eq. 8a the term  $\sinh(c_2)$ . Now, the coefficient  $c_1$  expresses the surface area  
287 at  $t=t_{sh}$  and  $c_2$  characterizes the form of the curve connecting the initial and the “final” state at  
288  $t=0$  and  $t=t_{sh}$  respectively; a low  $c_2$  value implies a smoother (closer to the linear) variation.  
289 An important improvement of the present fitting curve relative to the one in [61], is the  
290 inclusion of the effect of heating by using the correction factor  $f_{corr}$  in the adjustable  
291 coefficients  $c_1$  and  $c_2$  (see Eqs. 8b and c). Eq. 8 is valid for the entire range of conditions  
292 examined in the present work, the correlation coefficient for the fitting of the surface area  
293 evolution is above 0.98 and the prediction of the surface area at  $t=t_{sh}$  is within the 15% error  
294 for most of the cases examined; nevertheless this can reach values of 30% for specific cases at  
295 the highest temperature of 1000K.

296

$$\frac{S}{S_0} - 1 = c_1 \frac{\sinh(c_2 \cdot t/t_{sh})}{\sinh(c_2)}, \quad t < t_{sh} \quad (8a)$$

$$c_1 = 0.1484We^{1.092}Re^{-0.284}f_{corr}, \quad f_{corr} = 1 + 4.152We^{-1.06}(F_{heat} - 1)^{0.84} \quad (8b)$$

$$c_2 = 4.5234We^{0.294}Re^{-0.198}f_{corr}, \quad f_{corr} = 1 - 0.013We^{-0.50}(F_{heat} - 1)^{0.289} \quad (8c)$$

297



298 For the isothermal cases ( $f_{corr}=1$ ) the surface area increases with increasing  $We$  number and  
 299 decreasing  $Re$  number; this is clearly derived from the sign of the exponents of  $c_I$  (Eq. 8b).  
 300 When heating is included, the phenomenon becomes more complicated and the correction  
 301 factor  $f_{corr}$  depends both on the  $We$  number and the heating factor  $F_{heat}$ . The correction factor  
 302 for the coefficient  $c_I$  is always  $f_{corr}>1$  which means that heating tends to increase the surface  
 303 area at  $t=t_{sh}$ . As stated in [61], the extrapolation of this curve up to  $t_{br}$  should be done with  
 304 caution and limit the maximum value not to exceed  $10-12S_0$ , otherwise unphysical values may  
 305 be obtained.

306 The droplet breakup is governed by the relative strength of the forces acting on the droplet,  
 307 which vary dynamically as the droplet shape, dimensions and velocity change during the  
 308 whole process. The instantaneous deforming forces scale with  $\rho_g u_{rel,t}^2 D_{c,t}^2$  where  $u_{rel,t}$  is the  
 309 instantaneous relative drop-gas velocity (obtained by subtracting the average droplet velocity  
 310 from the free-stream velocity) and  $D_{c,t}$  is the instantaneous cross-stream diameter, while the  
 311 instantaneous restorative forces scale with  $\sigma D_{c,t}$  in which the viscous forces have been ignored  
 312 since  $Oh<0.1$ . The ratio of these forces represents an instantaneous  $We$  number (see Eq. 9)  
 313 which changes during the breakup process and includes the effects of heating, deformation  
 314 and velocity change:

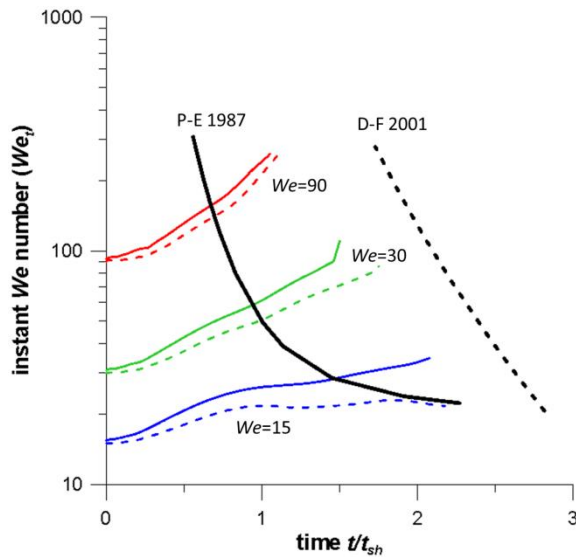
$$We_t = \frac{\rho_g u_{rel,t}^2 D_{c,t}}{\sigma} = We_0 \left(\frac{\sigma_0}{\sigma}\right) \left(\frac{D_{c,t}}{D_0}\right) \left(\frac{u_{rel,t}}{U_0}\right)^2 \quad (9)$$

315 The predicted transient  $We$  number based on Eq. 9 is plotted in Fig. 7 for selected isothermal  
 316 and evaporating cases with  $T_\infty=800K$ . The transient  $We$  number increases in time implying  
 317 that the deforming forces become progressively stronger, except of the isothermal case with  
 318  $We=15$ . In this case the droplet is not breaking up and after reaching a maximum, the  
 319 instantaneous  $We$  number decreases, implying that the restorative forces become stronger.

320 Generally, the instantaneous  $We$  number (as defined in Eq. 9) increases by a factor of 2-3  
 321 relative to the initial  $We$  number which is mainly ought to the increase of the cross sectional

322 diameter; the reduction of the relative drop-gas velocity (no more than 10% for the cases  
 323 examined) and the reduction of the surface tension coefficient play a secondary role. In Fig. 7  
 324 the curves derived from Eq. 9 by using either the experimental breakup time of Dai and Faeth  
 325 [13] or that of Pilch and Erdman [2] for  $Oh=0.02$  are also shown; these were derived by  
 326 processing the experimental data of [13] and more details can be found in [61]. These curves  
 327 represent the critical instantaneous condition for breakup and when crossed, breakup occurs.  
 328 The present simulations qualitatively agree with these curves.

329



330

331 Fig. 7: Predicted instant  $We$  number for selected isothermal (dashed lines) and evaporating  
 332 (solid lines) cases with  $T_{\infty}=800K$ .

333

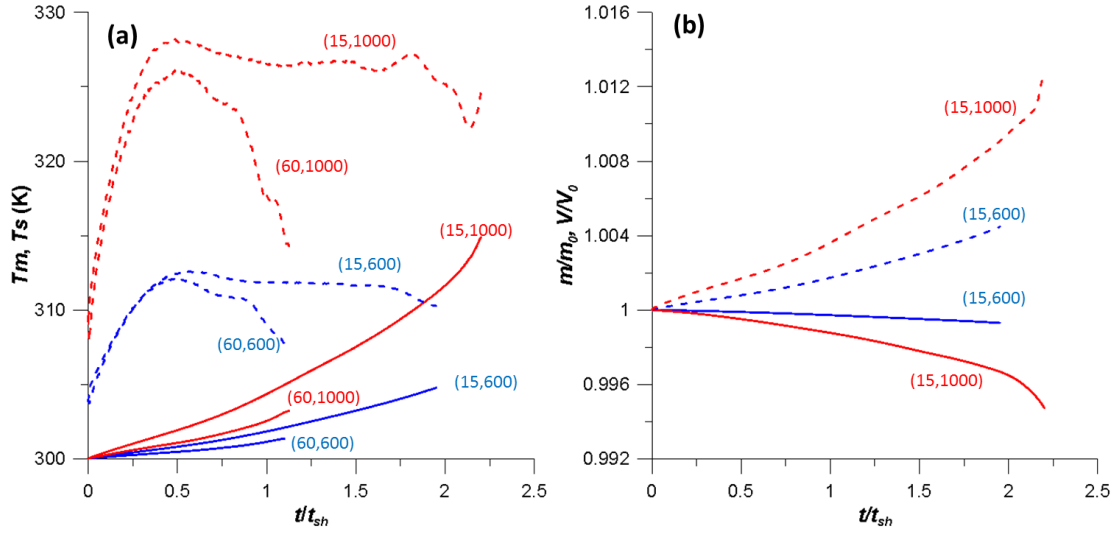
### 334 3.3 Thermal behavior of the droplet

335 The temporal evolution of the mean volume averaged droplet temperature  $T_m$  and the spatially  
 336 averaged surface temperature  $T_s$  are shown in Fig. 8a with the solid and dashed lines  
 337 respectively, for two cases combining different  $We$  numbers and gas phase temperatures;

338 these are indicated inside the parentheses as  $(We, T_\infty)$ . Both the mean droplet temperature and  
339 the surface temperature increase with increasing ambient temperature, as expected. The mean  
340 droplet temperature  $T_m$  increases continuously in time and may reach a heat-up of 15K by the  
341 onset of breakup, while the average surface temperature  $T_s$  exhibits a quite transient behavior;  
342 during the flattening phase ( $t < 0.6-0.8t_{sh}$ ) the surface temperature increases until reaching a  
343 maximum, followed by a decrease until coming closer to the volume averaged temperature.  
344 This behavior is mainly attributed to the flow patterns induced by the shape distortion which  
345 exchange hotter fluid from the droplet surface with the colder fluid from the droplet interior  
346 (see also Schlottke et al [59]). Additional to that, the increased surface temperature results in a  
347 high evaporation rate which tends to further suppress the surface heating.

348 In Fig. 8b the dimensionless droplet mass and droplet volume (solid and dashed lines,  
349 respectively) are shown for the cases  $(We, T_\infty) = (15, 600)$  and  $(15, 1000)$ . Up to the breakup  
350 instant, the evaporated mass is less than 0.5%, while the droplet volume increases up to 0.1%  
351 due to the thermal expansion effect. Note that in the corresponding cases with n-heptane  
352 presented in [61], the maximum heat-up was 7K, the evaporated mass was reaching 2% and  
353 the thermal expansion effect was absent. The aforementioned differences are mainly affected  
354 by the different volatility between the n-heptane and n-decane.

355



356

357 Fig. 8: (a) Temporal evolution of mean droplet temperature  $T_m$  (solid lines) and spatially  
 358 averaged surface temperature  $T_s$  (dashed lines). In (b) temporal evolution of dimensionless  
 359 droplet mass (solid lines) and dimensionless droplet volume (dashed lines). The cases shown  
 360 in parentheses correspond to  $(We, T_\infty)$ .

361

362 The heat and mass transfer processes are usually characterized by the dimensionless Nusselt  
 363  $(Nu)$  and Sherwood  $(Sh)$  numbers respectively, which express the heat/mass transfer  
 364 enhancement relative to a purely diffusive process. These are defined as the dimensionless  
 365 temperature/concentration gradient at the droplet interface, but their calculation is not  
 366 applicable with the VOF methodology due to the continuous variation of the field magnitudes  
 367 across the interface as explained in [60]. Inspired by Hase and Weigand [58] an indirect  
 368 method is used to estimate them, through the Eqs. 10-12:

$$\rho_l V \frac{d(c_{p,l} T_m)}{dt} = S \left( \frac{Nu \cdot k_{g,\infty}}{D_0} (T_\infty - T_s) - \dot{m}'' L \right) \quad (10)$$

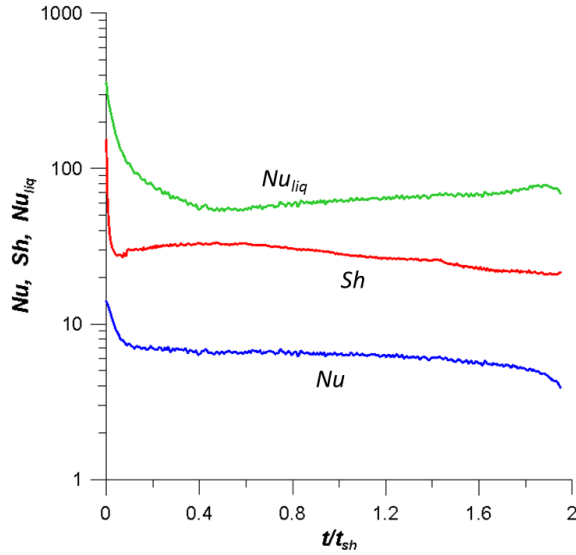
$$\dot{m} = S \frac{Sh \cdot \rho_{g,\infty} D_{AB,\infty}}{D_0} \ln(1 + B_M) \quad (11)$$

$$Nu_l \cdot k_{l,0} \frac{T_s - T_m}{D_0} = Nu \cdot k_{g,\infty} \frac{T_\infty - T_s}{D_0} - \dot{m}'' L \quad (12)$$

369

370 Eq. 10 is the droplet energy balance, Eq. 11 is a widely used relationship for the evaporation  
 371 rate of spherical droplets and Eq. 12 represents the heat flux continuity at the droplet's  
 372 surface, in which  $Nu_l$  is the dimensionless temperature gradient inside the liquid; this equation  
 373 connects the average droplet temperature  $T_m$  with the surface temperature  $T_s$ . The set of Eqs.  
 374 10-12 also forms a variant of the 0-D model for spherical droplet evaporation proposed by  
 375 Rensizbulut et al. [75]. Solving Eqs. 10-12 for  $Nu$ ,  $Sh$  and  $Nu_{liq}$  and using the CFD data for  
 376 the mean droplet temperature  $T_m$ , the space averaged surface temperature  $T_s$  and the  
 377 evaporation rate  $dm/dt$ , the temporal variation of the dimensionless transfer numbers is  
 378 obtained; this is shown in Fig. 9 for the case  $(We, T_\infty)=(15, 600)$ , which can be regarded as  
 379 representative, since the qualitative behavior observed is similar in all cases examined. For  
 380 the  $Nu$  and  $Sh$  numbers, there is a short initial transitional period as the one observed in [39,  
 381 40, 58]; after that, they exhibit small fluctuations in time. The  $Sh$  number seems to oscillate  
 382 around a steady-state value, while the  $Nu$  number decreases continuously in time with a slow  
 383 rate. On the other hand, the  $Nu_{liq}$  number exhibits a more unsteady behavior. The initial  
 384 transitional period is longer compared to the other numbers and its magnitude exhibits almost  
 385 one order of magnitude larger variations with time.

386



387

388 Fig. 9: Temporal variation of  $Nu$ ,  $Sh$  and  $Nu_l$  for the case of  $(We, T_\infty)=(15,600)$ .

389

390 It is of engineering interest to find expressions for the  $Nu$ ,  $Sh$  and  $Nu_{liq}$  numbers and use them  
 391 in 0-D or 1-D models aiming to predict the droplet temperature and the evaporation rate.  
 392 Earlier CFD works on spherical droplets (see [39, 40] among many others) provided such  
 393 expressions as a function of the instantaneous  $Re$ ,  $B_T$  and  $B_M$  numbers. Nevertheless, this is  
 394 not applicable in the case of droplet breakup due to the short duration of the phenomenon and  
 395 more importantly due to shape distortion from the spherical one. In [61] time-averaged  
 396 transfer numbers (being a function of the initial reference conditions) were used and they  
 397 could adequately capture the thermal behavior of droplets undergoing breakup. Following this  
 398 approach, the time-averaged transfer numbers fitting the present data are given in Eqs. 13-15;  
 399 the  $Re_l$  appearing in Eq. 15 ( $Re_l = Re_\infty \varepsilon^{2/3} N^{-4/3}$ ) was taken from [38] and it is derived by  
 400 equating the tangential shear stresses at the droplet surface:

401

$$\overline{Nu} = \frac{2 + 6.83 Re_\infty^{0.07} Pr_{g,\infty}^{1/3}}{(1 + B_{T,\infty})^{0.75}} \quad (13)$$

$$\overline{Sh} = \left(2 + 1.608We_0^{0.591}Sc_{g,\infty}^{1/3}\right)(1 + B_{T,\infty}) \quad (14)$$

$$\overline{Nu}_l = 55.95 + Re_l Pr_l^{1.6}/1429 \quad (15)$$

402

403 The set of Eqs. 10-15 forms a 0-D model which can be used to predict the average droplet  
 404 heating and evaporation, but not the transient variation of the surface temperature, which  
 405 decreases after reaching a maximum (see Fig. 8a). The reason for that discrepancy is that the  
 406 time-averaged expressions ignore the transient behavior of the transfer numbers. In the  
 407 present work, the  $Nu$  and  $Nu_{liq}$  numbers are expressed as a function of the non-dimensional  
 408 time and this is an improvement of the model used in [61]; the correlations used are shown in  
 409 Table 1 and they are valid for the conditions examined in the present work.

410

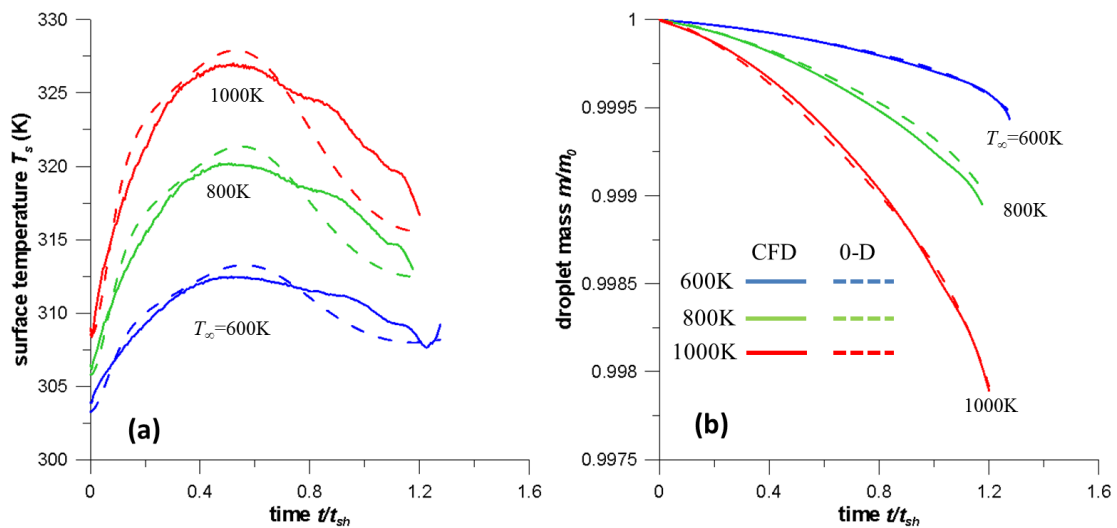
411 Table 1: Transient  $Nu$  and  $Nu_{liq}$  numbers. The time  $t$  corresponds to the dimensionless time  
 412  $t/t_{sh}$ .

	$Nu = c_0 - c_1 t + c_2 \exp(-c_3 t)$	$Nu_l = c_0 + c_1 \exp(-c_2 t) + c_3 \cos(2\pi t/c_4)$
$c_0$	$1.326 Re_\infty^{0.3647} (1 + B_{T,\infty})^{-0.236}$	$56.47 + 7.65 \cdot 10^{-4} Re_l^{1.707} (1 + B_{T,\infty})^{-0.432}$
$c_1$	$3 \cdot 10^{-6} Re_\infty^{2.212} (1 + B_{T,\infty})^{2.226}$	$201 + 1.99 \cdot 10^{-4} Re_l^{2.25} (1 + B_{T,\infty})^{-0.5285}$
$c_2$	3	$15.59 + 1.65 \cdot 10^{-6} Re_l^{2.64} (1 + B_{T,\infty})^{-0.623}$
$c_3$	60	$5.786 \cdot 10^{-5} Re_l^{2.226} (1 + B_{T,\infty})^{-0.825}$
$c_4$	—	1.2

413

414 The results of the 0-D model by using the transient correlations for  $Nu$  and  $Nu_{liq}$  are shown in  
 415 Fig. 10 for the case of  $We=45$  and three different gas phase temperatures; the solid and the  
 416 dashed lines correspond to the CFD and the 0-D model predictions, respectively. As seen, the  
 417 time dependent expressions for the transfer number can adequately predict the transient  
 418 behavior of the surface temperature, with a less than 4K error. The model predictions  
 419 presented in Fig. 10 have assumed that the temporal evolution of the surface area is known  
 420 and this is a limitation of the proposed model. On the other hand, the Eq. 8 for the surface  
 421 area evolution can be used to predict the thermal behavior for  $t < t_{sh}$ ; in this case, the errors are  
 422 mainly determined by the effectiveness of the curve reproducing the surface area evolution.

423



424

425 Fig. 10: Predictions of the 0-D model for (a) the spatially averaged surface temperature and  
 426 (b) the droplet mass for the case of  $We=45$ . The solid lines are the CFD data and the dashed  
 427 lines are the 0-D model predictions.

428

429 In Strotos et al. [61] it was shown that droplet breakup is affected by heating when the  $We$   
 430 number is low and the ambient temperature is high. This conclusion was drawn both by



431 considering the associated timescales (either in a macroscopic or a microscopic level) and by  
432 implementing the aforementioned 0-D model with the time-averaged expressions for the  
433 transfer numbers. These comments are also verified by the present simulations for an n-  
434 decane droplet. Relating the n-heptane CFD simulations performed in [61] and the present  
435 ones for the n-decane, the surface temperature at  $t=t_{sh}$  is well represented by Eq. 16. This  
436 equation clearly demonstrates the effect of  $We$  number, gas phase temperature and species  
437 volatility through the heating factor  $F_{heat}$ :

438

$$T_s(t_{sh}) = T_0(1 + 0.0195We^{-0.2532}F_{heat}^{2.053}) \quad (16)$$

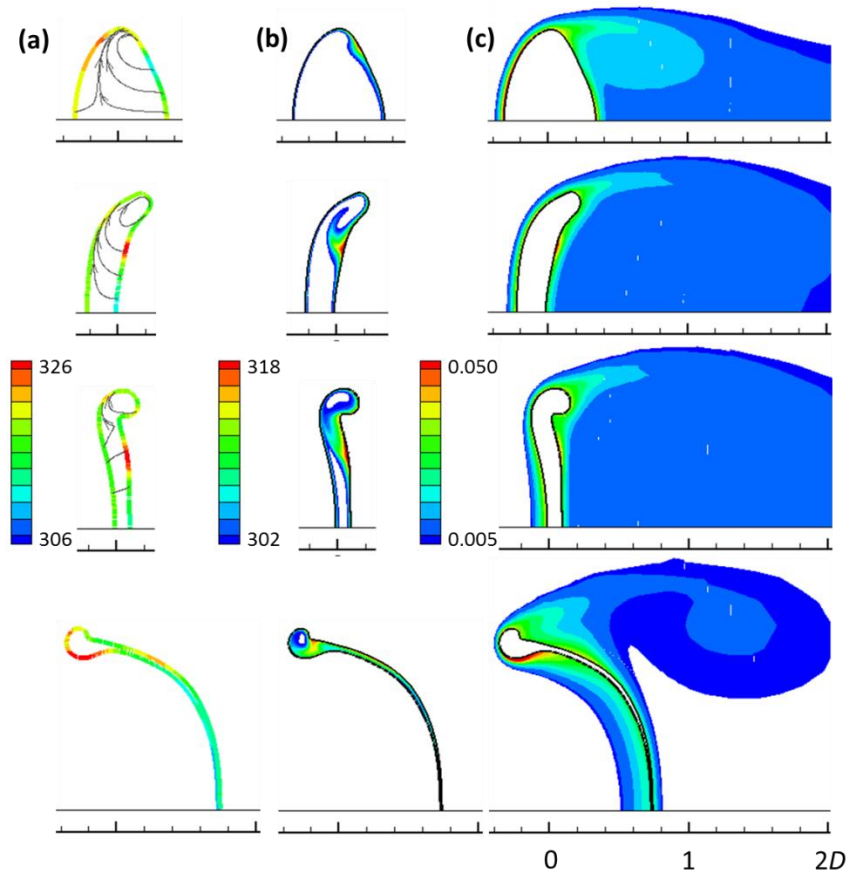
439

### 440 **3.4 Spatial distribution of the flow variables**

441 The spatial distribution of surface temperature, inner droplet temperature and vapor  
442 concentration field are shown in Fig. 11 and Fig. 12 for the cases with  $T_\infty=800K$  and  $We$   
443 number 15 and 30, respectively. The surface temperature (denoted with a thick line colored  
444 with the corresponding temperature values) is not spatially uniform; along the droplet surface  
445 differences of 15K can be observed. In the initial flattening phase, hot spots are observed on  
446 the front side of the droplet in an off-axis location; at subsequent instances hot spots are  
447 observed at the rear of the droplet. In a spherical droplet case these temperature differences  
448 along the surface could induce secondary flow (due to surface tension gradients) and form  
449 cellular vortices. The present work has included the effect of surface tension variation along  
450 the interface through the CSS surface tension model [76]. Nevertheless, no secondary flow  
451 was observed in the present cases (see characteristic streamlines in the left column), since the  
452 flow patterns are determined by the droplet shape. Regarding the inner temperature field and

453 the vapor concentration field in the gas phase, these follow similar patterns to the ones  
454 observed in [61], as affected by the local velocity field and the droplet deformation.

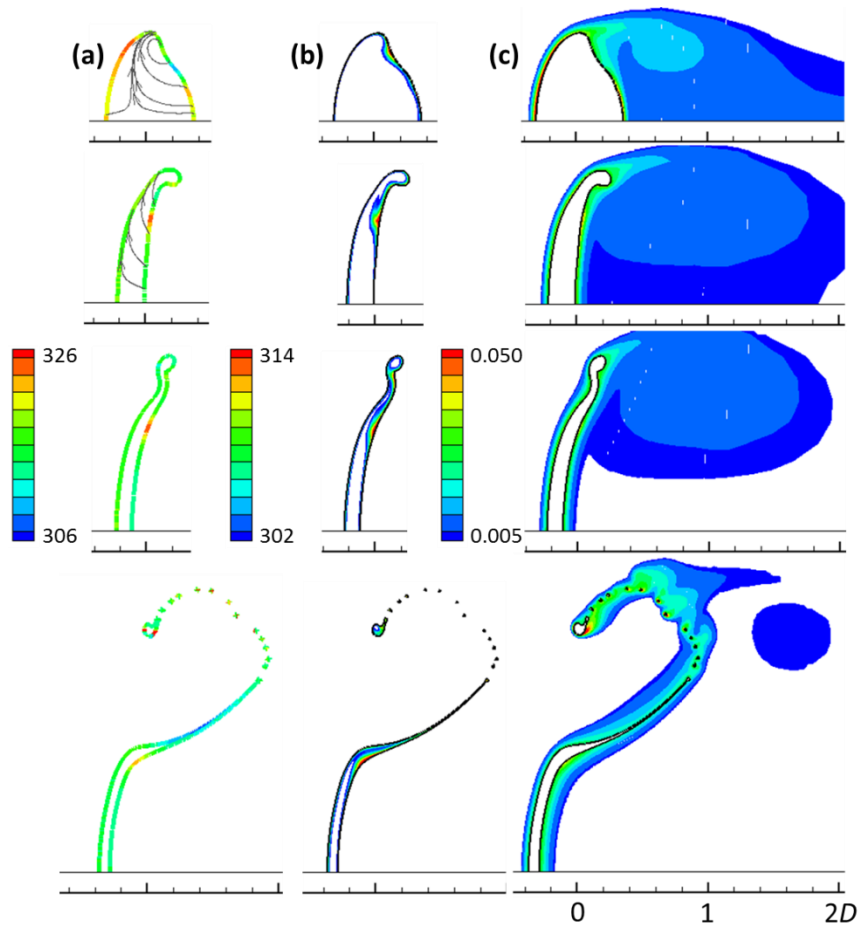
455



456

457 Fig. 11: Spatial distribution of (a) surface temperature, (b) droplet temperature and (c) vapor  
458 concentration for the case  $(We, T_\infty) = (15, 800)$ . The time instances presented are 0.5, 1.0, 1.5  
459 and  $2.0t_{sh}$ . In (a) characteristic streamlines are also shown. For color interpretation, see the  
460 online version.

461



462

463 Fig. 12: Spatial distribution of (a) surface temperature, (b) droplet temperature and (c) vapor  
 464 concentration for the case  $(We, T_\infty) = (30, 800)$ . The time instances presented are 0.5, 1.0, 1.25  
 465 and  $1.5t_{sh}$ . In (a) characteristic streamlines are also shown. For color interpretation, see the  
 466 online version.

467

## 468 4 Conclusions

469 The Navier-Stokes, energy and transport of species conservation equations together with the  
 470 VOF methodology have been utilized to study the coupled problem of aerodynamic droplet  
 471 breakup under the influence of heating and evaporation for  $We$  numbers in the range 15-90  
 472 and gas phase temperatures 600-1000K. To quantify the effect of heating, the same cases

473 were also studied under isothermal conditions assuming constant species properties.  
474 Combining the results obtained from the present work for an n-decane fuel droplet with those  
475 for a more volatile n-heptane droplet presented in Strotos et al. [61], it seems that droplet  
476 heating affects the overall breakup performance for low  $We$  numbers, high gas phase  
477 temperatures and low volatility fuels. For a non-breaking-up case with constant properties,  
478 heating may decrease the surface tension coefficient in such a way, that droplet not only  
479 breaks up in the bag breakup regime, but also in the transitional breakup regime.  
480 Nevertheless, at high  $We$  numbers the surface tension still decreases but without altering the  
481 breakup performance. During droplet breakup, despite the fact that the liquid evaporated mass  
482 is very low (especially for low volatility fuels), one has to consider the evaporation source  
483 terms since they play an important role by suppressing the droplet heat-up; this is evident for  
484 high volatility fuels which seem to be less affected by heating.

485 The concept of “heating factor” was introduced which provides an indication of the droplet  
486 tendency to heat-up by combining the terms tending to increase and decrease the droplet  
487 temperature. Useful correlations were provided for an a-priori estimation of the breakup  
488 instant, surface area evolution and droplet heat-up. Additional to them, an enhanced 0-D  
489 model able to predict the thermal behavior of the droplet is proposed. In relevance to our  
490 previous work [61], it uses time-dependent transfer numbers instead of time-averaged and it is  
491 able to capture the transient behavior of the spatially average surface temperature. The latter  
492 is not spatially uniform and peak values are observed in the front of the droplet in the initial  
493 flattening phase and at the rear of the droplet in the subsequent stages.

494

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499

500 **6 Nomenclature**

501 **Roman symbols**

<b>Symbol</b>	<b>Description</b>	<b>Units</b>
$B_M$	Mass transfer Spalding number	-
$B_T$	Heat transfer Spalding number	-
$c_p$	Heat capacity	J/kgK
$D$	diameter	m
$D_{AB}$	Vapor diffusion coefficient	m <sup>2</sup> /s
$F_{heat}$	heating factor	-
$Oh$	Ohnesorge number $Oh = \mu_l / \sqrt{\rho_l \sigma D_0}$	-
$k$	Thermal conductivity	W/mK
$L$	Latent heat of vaporization	J/kg
$m$	mass	kg
$\dot{m}''$	Evaporation rate per unit area	kg/m <sup>2</sup> s
$Nu$	Nusselt number	-
$Pr$	Prandtl number	-
$R$	radius	m
$Re$	Reynolds number $Re = \rho_g U_{rel,0} D_0 / \mu_g$	-
$S$	surface area	m <sup>2</sup>
$Sc$	Schmidt number	-
$Sh$	Sherwood number	-
$t$	time	s
$t_{sh}$	Shear breakup timescale $t_{sh} = D\sqrt{\varepsilon}/U$	-
$T$	temperature	K
$U$	reference velocity	m/s
$u$	instantaneous droplet velocity	m/s
$V$	volume	m <sup>3</sup>
$We$	Weber number $We = \rho_g U_{rel,0}^2 D_0 / \sigma$	-
$We_t$	instantaneous $We$ number	-
$Y$	vapor concentration	kg/kg

502

503

504 **Greek symbols**

<b>Symbol</b>	<b>Description</b>	<b>Units</b>
$a$	thermal diffusivity	m <sup>2</sup> /s
$\gamma$	thermal effusivity $\gamma = \sqrt{k\rho c_p}$	J/m <sup>2</sup> Ks <sup>0.5</sup>

$\varepsilon$	density ratio $\varepsilon = \rho_l/\rho_g$	-
$\mu$	viscosity	kg/ms
$N$	viscosity ratio $N = \mu_l/\mu_g$	-
$\nu$	kinematic viscosity	m <sup>2</sup> /s
$\rho$	density	kg/m <sup>3</sup>
$\sigma$	surface tension coefficient	N/m

505

### Subscripts

Symbol	Description
0	initial
c	cross-stream
cr	critical
g	gas
l	liquid
rel	relative
s	at surface
t	instantaneous magnitude
x,y,z	coordinates
$\infty$	free-stream conditions

506

### Abbreviations

Symbol	Description
C07	n-heptane C <sub>7</sub> H <sub>16</sub>
C10	n-decane C <sub>10</sub> H <sub>22</sub>
CFD	Computational Fluid Dynamics
cpR	Cells per Radius
CSS	Continuum Surface Stress
UDF	User Defined Function
VOF	Volume of Fluid

507

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509

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