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## **Abstract**

We study the impact of video frame drops in buffer constrained multiprocessor system-on-chip (MPSoC) platforms. Since on-chip buffer memory occupies a significant amount of silicon area, accurate buffer sizing has attracted a lot of research interest lately. However, all previous work studied this problem with the underlying assumption that no video frame drops can be tolerated. In reality, multimedia applications can often tolerate some frame drops without significantly deteriorating their output quality. Although system simulations can be used to perform video quality driven buffer sizing, they are time consuming. In this paper, we first demonstrate a dual-buffer management scheme to drop only the less significant frames. Based on this scheme, we then propose a formal framework to evaluate the buffer size vs. video quality trade-offs, which in turn will help a system designer to perform quality driven buffer sizing. In particular, we mathematically characterize the maximum numbers of frame drops for various buffer sizes and evaluate how they affect the worst-case PSNR value of the decoded video. We evaluate our proposed framework with an MPEG-2 decoder and compare the obtained results with that of a cycle-accurate simulator. Our evaluations show that for an acceptable quality of 30 dB, it is possible to reduce the buffer size by upto 28.6% which amounts to 25.88 megabits.

## **Disciplines**

Computer Sciences | Physical Sciences and Mathematics

## **Comments**

17th IEEE International Conference on Embedded and Real-Time Computing Systems and Applications (RTCSA), Toyama, Japan, Aug 2011.

# Video Quality Driven Buffer Sizing via Frame Drops

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**Abstract**— We study the impact of video frame drops in buffer-constrained multiprocessor system-on-chip (MPSoC) platforms. Since on-chip buffer memory occupies a significant amount of silicon area, accurate buffer sizing has attracted a lot of research interest lately. However, all previous work studied this problem with the underlying assumption that no video frame drops can be tolerated. In reality, multimedia applications can often tolerate some frame drops without significantly deteriorating their output quality. Although system simulations can be used to perform video quality driven buffer sizing, they are time consuming. In this paper, we first demonstrate a dual-buffer management scheme to drop only the less significant frames. Based on this scheme, we then propose a formal framework to evaluate the buffer size vs. video quality trade-offs, which in turn will help a system designer to perform quality driven buffer sizing. In particular, we mathematically characterize the maximum numbers of frame drops for various buffer sizes and evaluate how they affect the worst-case PSNR value of the decoded video. We evaluate our proposed framework with an MPEG-2 decoder and compare the obtained results with that of a cycle-accurate simulator. Our evaluations show that for an acceptable quality of 30 dB, it is possible to reduce the buffer size by upto 28.6% which amounts to 25.88 megabits.

## I. INTRODUCTION

### A. Motivation

Decoding video content on video playback devices requires significant amount of on-chip buffer resources for storing the incoming/partially processed frames. Therefore, accurate buffer sizing in multimedia MPSoC platforms has attracted lot of research attention. All the prior works in buffer sizing (e.g., [11], [9] and [15]) did not tolerate video quality loss at the output, i.e., they did not allow frame drops. On the other hand, there have been works on frame dropping strategies ([7] and [17]) to maximize video quality output in the presence of buffer constraints. However, there has been no work on quality driven buffer sizing using a frame dropping strategy. Such a strategy would be very useful as it is a well known fact that multimedia applications can tolerate some quality loss without deteriorating the video perception.

In this paper, we propose a formal framework to explore the buffer size vs. video quality trade-offs, which can help a system designer to perform quality driven buffer sizing. Although these trade-offs can be explored using system simulations, simulation-based techniques are time consuming. The concepts discussed here, however, can be applied in the context of network- on-chip architectures where buffer size can be traded off against some quality parameter by dropping the less important data. In general, it is applicable to all such scenarios where losing some low priority data helps in saving buffer resources while still maintaining a good content quality. Therefore, it is important to recognize the least important data

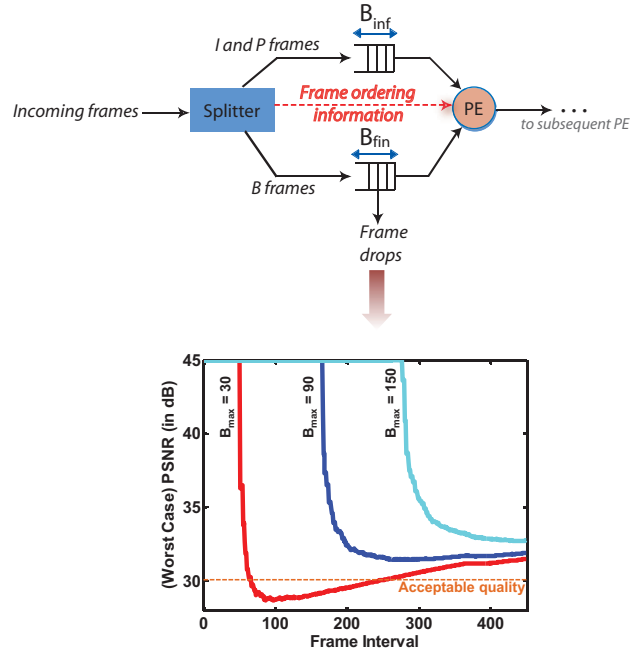


Fig. 1. Dual buffer management scheme with drops in less significant frames and buffer size vs. video quality trade-off results for a benchmark MPEG-2 video *susi\_080* ([12]).

in the target application. As our framework bounds the quality degradation, the video quality does not deteriorate too much.

In MPEG-2/MPEG-4 video streams, there are typically three types of frames, namely, *I frame* (Intra coded), *P frame* (Predicted) and *B frame* (Bidirectionally predicted). I frames are intra coded frames and are not dependent on other frames in the video stream for decoding. Decoding a P frame requires the previous I or P frame as the reference frame. Finally, decoding a B frame requires two reference frames, namely, a forward reference frame (I/P frame) and a backward reference frame (I/P frame). It is clear from this organization of frames that B frame drops result in lesser amount of quality degradation in comparison to the I and P frame drops. Therefore, in MPEG-2/MPEG-4 decoder applications mapped onto MPSoC platforms, B frame drops can be used to trade-off quality for buffer size. This selective dropping of frames requires a special scheme to differentiate among frames.

In our approach, a simple dual buffer management scheme is used in order to drop only the less significant frames (B frames). This scheme is shown in Fig. 1. The incoming multimedia stream is split into two distinct streams: the first consists of the less significant frames (B frames) and the second consists of the more significant ones (I/P frames). These two streams are fed to two distinct buffers. This partitioning

will be explained in detail in Section III. The processing element (PE) needs to be given a side information conveying the order in which the frames are to be processed (shown as the dotted line from the splitter to the PE in Fig. 1). In the setup shown in Fig. 1, drops occur only for B frames and the size of the associated buffer can be traded off with video quality. This trade-off (shown in Fig. 1) is obtained using a well known video benchmark *susi\_080* ([12]). In multimedia literature ([19]), 30 dB is considered to be an acceptable output video quality (shown as the horizontal line in the trade-off graph in Fig. 1). From Fig. 1, it can be observed that we give quality variations for three different buffer sizes over frame intervals. We define frame interval below.

**Definition 1: (Frame Interval).** For a given video clip, a frame interval  $F$  is defined as a window of any  $F$  consecutive frames.

The worst case quality value for a frame interval  $F$  is the minimum quality obtained over any  $F$  consecutive frames across the clip. From Fig. 1, it can be observed that if a maximum buffer size ( $B_{max}$ ) of 30 frames is chosen, then the quality values (in dB) fall below the threshold value of 30 dB for certain frame intervals from 80 to 260. If the target quality constraint is to satisfy the 30 dB value for all frame intervals, then  $B_{max} = 30$  frames will not be sufficient. However, if the target quality constraint is that the threshold value of 30 dB should be satisfied for any frame interval greater than 300, then  $B_{max} = 30$  frames will be a good choice as the buffer size. We denote buffer sizes in number of frames in the rest of the paper because video frames consist of variable number of bits. However, we give an estimate of the minimum buffer savings in megabits (Mbs).

## B. Our Contributions

To the best of our knowledge, this is the first attempt at studying the influence of buffer sizing on worst case quality deterioration using a formal framework. There are two interlinked parts constituting our framework. For a given video clip, we perform the following operations.

- 1) Firstly, we derive the maximum number of frame drops (in any frame interval) for any given buffer size using a Network Calculus ([2]) based mathematical framework.
- 2) Secondly, we propose a novel method to compute worst case quality values for video clips. This is further used in conjunction with the maximum number of frame drops derived in the first part to find the worst case quality values for various buffer sizes.

A system designer does buffer sizing for an extensive library (covering all possible scenarios) of video clips, whereby sufficient buffer size is chosen so that a quality constraint is satisfied by all the clips in the library. Our framework can be used in this context. The information obtained from buffer size vs. quality trade-off curves for each clip can be used to determine the optimal buffer size for the entire library.

## C. Related Work

On-chip buffers take up a lot of chip silicon area. This is evident from [6], in which experiments clearly show the

enormous amounts of silicon area increase due to the increase in FIFO size in the router. In [18], this same concern is demonstrated in the context of on-chip network design for multimedia applications. However, the authors do not drop any incoming packet from the buffer thereby giving importance to maximum application quality. A buffer sizing algorithm has been discussed in the context of networks on chip [3], where the authors are concerned about the reduction of buffers in network interfaces. There are various objective functions that are considered while choosing the appropriate buffer size. A buffer allocation strategy is proposed in [6] in order to increase the overall performance in the context of a networks-on-chip router design. In [14], an appropriate buffer size is chosen that gives the best power/performance figure.

Buffer dimensioning is an important aspect of designing media players. In the past, there has been lot of work in this area where several design factors have been taken into consideration while choosing the appropriate buffer size. Most of this work concentrated on studying the playout buffer vs. quality of service (QoS) tradeoffs. In [8], the authors discussed an optimal allocation of playout buffer size such that the playout delay is minimized for a given probability of underflow or a given QoS. Similarly, in [4], the buffer vs. QoS tradeoff is studied for multimedia streaming in a wireless scenario using a dynamic programming framework. A combined optimal transmission bandwidth and optimal buffer capacity is considered to support video-on-demand services [20]. Here, playout buffer overflow and underflow are not tolerated. There are also some other prior works which have not tolerated any loss as a result of buffer overflow and underflow ([10], [11], [9] and [15]). However, none of these works have considered the tradeoff between buffer and video quality by allowing some buffer overflows (i.e., with constrained buffer). Here, video quality is not the end-to-end QoS, but the distortion in the received frames.

There are various frame dropping strategies that have been discussed in literature that try to maximize the video quality ([7] and [17]). Invariably, all these strategies use a prioritization scheme to drop the frames in a quality aware manner such that the quality deterioration is minimized. In [7], frame size is used to prioritize the frames before dropping. In this approach, frames with larger size are dropped later and frames with smaller size are dropped first. A distortion matrix is introduced in [17] to compute the priority of frame dropping based on the distortion that frame suffers if lost. As we drop only the B frames in this paper, we consider the drop oldest policy during a buffer overflow. Similar schemes like *Drop Newest*, *Drop Random* and *Drop All* are also discussed in [16].

## D. Organization of the Paper

In the next section, we give an overview of our analytical framework. Section III discusses the process of partitioning the arrival and service curves in order to analyze the dropping of only certain frames, i.e., B frames. In Section IV, we present the theory behind the calculation of maximum number of frame drops for any frame interval. Section V presents the analytical framework to derive the worst-case quality curve

from frame drop bounds. Section VI discussed a case study of MPEG-2 decoder application. In Section VII, we present the concluding remarks.

## II. FRAMEWORK OVERVIEW

This section presents an overview of our mathematical framework to study the influence of frame drops on the peak signal to noise ratio (PSNR) of the decoded video under buffer constraints. We use the arrival curves and service curves from the Network Calculus to model the data streams and the service given by the resources, respectively, as they can model any arbitrary stream arrival pattern and any arbitrary resource service pattern. In addition, they can easily capture the data size variability and the processing variability exhibited in the multimedia setting we consider here. Before describing our framework, we introduce the underlying MPSoC platform.

**Platform Description:** In this work, we find the buffer size vs. worst case quality trade-off for a video clip on a buffer constrained MPSoC architecture as shown in Fig. 2. The terms explained in the problem definition are marked appropriately alongside the architecture. The architecture consists of two PEs,  $PE_1$  and  $PE_2$ , each with its own offered service curves shown above them. Each PE is mapped with a set of tasks from the target decoder application. The PEs also each have a buffer in front of them, shown as  $B_1$  and  $B_2$ , with maximum capacity of  $B_{1max}$  and  $B_{2max}$  (quantified in number of frames), respectively. As the buffer sizes are not always adequate, frame drops may occur, which are characterized as  $\alpha_{drop1}^u(\Delta)$  and  $\alpha_{drop2}^u(\Delta)$ .  $\alpha_{drop1}^u(\Delta)$  and  $\alpha_{drop2}^u(\Delta)$  give the upper bounds on the number of frames dropped in any time interval of length  $\Delta$ , where  $\Delta \geq 0$ . Although only a single buffer is shown in front of each PE, each buffer internally has two parts - one part where some of the least significant contents (B frames) are dropped and the second part where adequate buffer size is provided and the significant contents (I/P frames) are not dropped. The frame drops occur in the droppable buffer section and its drop bounds are derived by our framework. Before getting into the details of our framework, we first define some terminology.

**Definition 2: (Arrival Curve).** For a video clip, let  $a(t)$  denote the number of frames that arrive in time interval  $[0, t)$ . Then, the video clip is said to be bounded by the arrival curve  $\alpha = [\alpha^u, \alpha^l]$  iff for all arrival patterns  $a(t)$ :

$$\alpha^l(\Delta) \leq a(t + \Delta) - a(t) \leq \alpha^u(\Delta) \quad (1)$$

for all  $\Delta \geq 0$ . In other words,  $\alpha^u(\Delta)$  and  $\alpha^l(\Delta)$  give the maximum and minimum number of frames that can arrive over any interval of length  $\Delta$  across the length of the video clip.

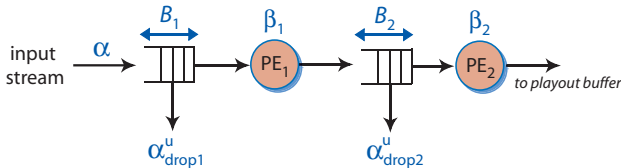


Fig. 2. MPSoC setup with buffer constraints and frame drops

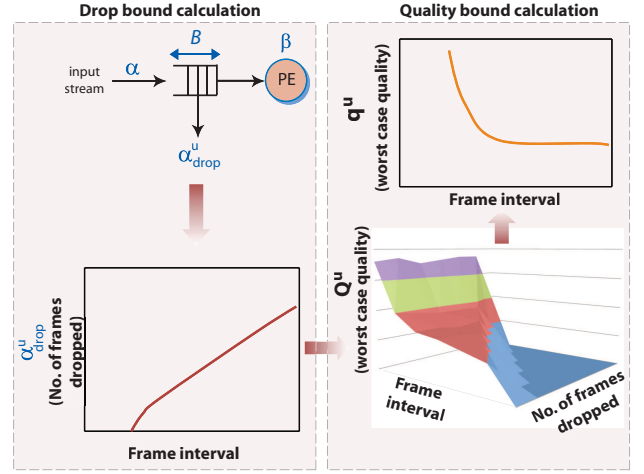


Fig. 3. Overview of the Analytical Framework

**Definition 3: (Service Curve).** Let  $c(t)$  denote the number of frames processed by a task mapped onto a processor in time interval  $[0, t)$ . Then, the service curve  $\beta = [\beta^u, \beta^l]$  is a service curve of the processor iff for all service patterns  $c(t)$ :

$$\beta^l(\Delta) \leq c(t + \Delta) - c(t) \leq \beta^u(\Delta) \quad (2)$$

for all  $\Delta \geq 0$ . In other words,  $\beta^u(\Delta)$  and  $\beta^l(\Delta)$  denote the upper and lower bounds on the number of frames processed over any interval of time  $\Delta$  across the length of the clip.

**Problem Definition:** Given the arrival curve  $[\alpha^u, \alpha^l]$  of the video clip that is to be decoded on a decoder application mapped onto a MPSoC platform, the service curve  $[\beta^u, \beta^l]$ , we analytically explore the trade-off between buffer resource  $B_{max}$  (measured in number of frames) and the worst case quality (quantified in terms of PSNR) of the decoded video.

Once this trade-off is explored for all the clips in the library, the system designer can appropriately choose the minimal buffer resource required to satisfy an acceptable quality constraint. The overall analytical framework consists of two stages as shown in Fig. 3, namely the *Drop bound calculation* stage and the *Quality bound calculation* stage. These two stages are described briefly next.

**Drop bound calculation:** The first stage formally derives the worst case frame drop bound  $\alpha_{drop}^u$  for the droppable part of the buffer, with size  $B_{max}$ . This analysis is based on concepts from network calculus. Specifically, it computes the bounds on the number of frames that are processed in an incoming stream when the arrival curves  $[\alpha^u, \alpha^l]$ , service curves  $[\beta^u, \beta^l]$  and buffer size  $B_{max}$  for a single PE are given. Our computation is based on the idea of a virtual processor controlling the admission of frames into the buffer such that the buffer effectively acts as one with no drops, i.e., once an appropriate number of frames are dropped from the stream, the finite and constrained buffer will never overflow, thereby emulating an infinite buffer. We also compute the bounds on the service offered by the virtual processor to the incoming stream. This can be used to compute the worst case bound on the number of frame drops in any interval of time. However, we convert

the time interval based computation of frame drop bounds into frame interval based bounds  $\alpha_{dropF}^u(F)$ , where  $F$  is the frame interval window and  $1 \leq F \leq F_{total}$ . Here,  $\alpha_{dropF}^u(F)$  is the upper bound on the number of frames dropped in a window of  $F$  consecutive frames and  $F_{total}$  is the total number of frames in the clip. The detailed formulation will be shown in Section IV.

The useful feature of this stage is that it allows the analysis of multiple PEs in pipeline with buffer constraints to be done compositionally. In other words, one can compute the bounds on the arrival curve to the next stage. The computed arrival curve can then be used to derive the frame drop bounds in the next stage. These frame drop bounds computed at various stages (with constrained buffer resources) can be finally summed up to obtain the overall bound on the frame drops.

**Quality Bound Calculation:** Once the frame drop bounds are known, we compute a frame interval based worst-case bound on quality in terms of PSNR. Towards this, a parameter called the worst-case quality surface, denoted by  $Q^u$ , is constructed for each video clip.  $Q^u$  is defined as below.

*Definition 4: Worst-case quality surface ( $Q^u$ ).* For any frame interval  $F$ , the worst-case quality surface  $Q^u(f, F)$ , for all  $0 \leq f \leq F$ , is the worst-case quality of the video if  $f$  frames are dropped in any window of  $F$  consecutive frames.

All dropped frames are replaced by immediately preceding and successfully processed frames called *concealment frames*. The amount of quality loss depends on the mean square error (MSE) between the dropped and concealment frames. The resultant quality is measured in terms of PSNR, which in turn depends on the MSE between the dropped and concealment frames. We find all possible concealment frames for a dropped video and analyze which concealment frame results in maximum error or worst quality degradation.

**$B_{max}$  vs. quality trade-off:** The final goal of the framework is to explore the trade-off between the maximum buffer capacity  $B_{max}$  and the quality for each video clip in the library. Once this trade-off is available for all the clips in the library, the system designer can take a well-informed decision on the appropriate buffer size. In order to derive this trade-off, we use the frame drop bound  $\alpha_{dropF}^u$  and map it into the worst case quality surface  $Q^u(f, F)$  where  $f$  is replaced by the value  $\alpha_{dropF}^u$ . Therefore, the quality bound calculation is a mapping from a three dimensional (3D) space to a two dimensional (2D) space shown as

$$q^u(F) = Q^u(\alpha_{dropF}^u, F) \quad (3)$$

where  $q^u(F)$  is the worst-case quality bound for the video clip. This mapping is shown in Fig. 3, where the frame drop bounds are shown at the bottom left hand side and the worst-case quality space is shown on the bottom right hand side. The final worst-case quality bound for a video clip is shown in the top right hand side of Fig. 3.

### III. PARTITIONING ARRIVAL AND SERVICE CURVES

In this paper, we study the effect of frame drops in the context of a video clip being processed by the associated

decoder application. As we are more interested in studying the effect of frame drops on quality degradation, we intend to analyze the drop of those frames that least affect the quality degradation. It has been observed in MPEG-2 or MPEG-4 decoders that B frames are generally the least significant when compared to I and P frames as the loss of B frames results in least quality degradation when compared to I and P frames. Moreover, many video clips are encoded with a IPBBPBBP... frame pattern, where a large percentage of B frames exist. Therefore, we analyze the effect of only the B-frame drops. If there are videos encoded without B frames, then P frames can be dropped. In this case, the framework will remain the same. Consequently, the system model for the platform architecture consists of two kinds of buffers in front of each PE depending on whether B frame drops are allowed or not. This is shown in Fig. 4. If B frame drop is allowed, then we have a finite buffer called the B frame buffer ( $B_{fin}$ ) and another finite buffer called the IP frame buffer ( $B_{inf}$ ) that does not have any drop. The buffer size required for an IP frame buffer can be computed using conventional Network Calculus technique ([2]).

The existence of two buffers makes it necessary to partition the arrival curves and service offered to the two sets of frames. As illustrated in Fig. 4, the original arrival curves of the input stream are partitioned into  $\alpha_{inf} = [\alpha_{inf}^u, \alpha_{inf}^l]$  and  $\alpha_{fin} = [\alpha_{fin}^u, \alpha_{fin}^l]$ , which correspond to the arrival curves of the I and P frames together and of the B frames, respectively. Similarly, the service curves offered by the PE are partitioned into  $\beta_{inf} = [\beta_{inf}^u, \beta_{inf}^l]$  and  $\beta_{fin} = [\beta_{fin}^u, \beta_{fin}^l]$ , which correspond to the service curves offered to the I and P frames and to the B frames, respectively. As the I and P frames share the same buffer  $B_{inf}$  with no frame drops, their buffer size can be computed directly from  $\alpha_{inf}$  and  $\beta_{inf}$  using the technique in [2]. On the other hand, the B frames can be dropped; their drop bound ( $\alpha_{drop}^u$ ) can be computed using  $\alpha_{fin}$ ,  $\beta_{fin}$  and  $B_{fin}$ .

The algorithm to compute the partitioned arrival curve for B frames is shown as Algorithm.1. The arrival curves for I and P frames can also be computed in the same manner. However, due to the existence of partitioned arrival curves and two buffers now, the PE needs to be given information about what is the order in which the frames are processed. This is generally the order in which the frames are encoded and sent out in a video stream.

In Algorithm 1, we compute the arrival curves  $[\alpha_{fin}^u, \alpha_{fin}^l]$  for the B frames. Lines 4-12 compute the arrival times of each B frame (denoted by  $b\_arr$ ) in the video clip.  $F_{total}$  and  $B\_CNT$

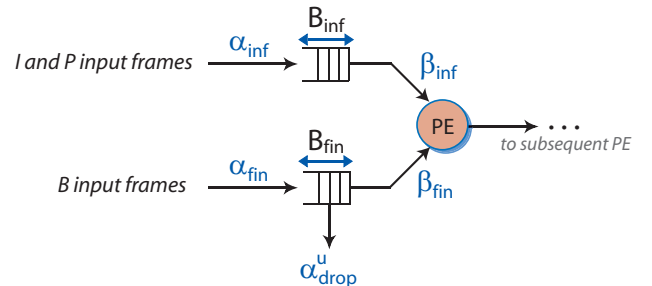


Fig. 4. System model with infinite and finite buffer for a single PE

**Algorithm 1** Computing partitioned arrival curve for B frame**Input:**  $frsize(B\_CNT)$  - Size of each frame in bits;**Output:**  $[\alpha_{fin}^u, \alpha_{fin}^l]$ 

- 1:  $b\_arr(cnt) \leftarrow 0$  for all  $0 \leq cnt \leq B\_CNT$ ,  $ip\_arr \leftarrow 0$ ;
- 2:  $btime\_max(k) \leftarrow 0$ ,  $btime\_min(k) \leftarrow 0$  for all  $1 \leq k \leq B\_CNT$
- 3: —Computing the arrival time of each B frame—
- 4: **for**  $i = 1$  to  $F_{total}$  **do**
- 5:   **if**  $Bframe$  **then**
- 6:      $b\_arr(cnt) = frsize(i)/RATE + ip\_arr$
- 7:      $ip\_arr = 0$
- 8:      $cnt = cnt + 1$
- 9:   **else**
- 10:      $ip\_arr = ip\_arr + frsize(i)/RATE$
- 11:   **end if**
- 12: **end for**
- 13: —Find max and min arrival times for  $k$  consecutive B frames—
- 14:  $btime\_max(k) = \max_{\forall i} \left\{ \sum_{j=1}^k b\_arr(j+i) \right\}$ ,  $0 \leq i \leq B\_CNT - k$
- 15:  $btime\_min(k) = \min_{\forall i} \left\{ \sum_{j=1}^k b\_arr(j+i) \right\}$ ,  $0 \leq i \leq B\_CNT - k$
- 16: —Find upper and lower arrival curves for B frames—
- 17:  $\alpha_{fin}^u(t) = \begin{cases} \max\{k-1\} & : btime\_min(k) < t \\ \min\{k\} & : btime\_min(k) \geq t \end{cases}$
- 18:  $\alpha_{fin}^l(t) = \begin{cases} \max\{k-1\} & : btime\_max(k) < t \\ \min\{k\} & : btime\_max(k) \geq t \end{cases}$

are the total number of frames and B frames, respectively, in the video clip. The input bit rate of the video clip is denoted by  $RATE$ . We then find the maximum and minimum arrival times for  $k$  consecutive B frames. This is shown in lines 14-15. Finally, the arrival curves are computed as in lines 17-18. The upper bound on the B frame arrival curve is obtained from the minimum arrival time required for  $k$  consecutive frames such that they satisfy the condition in line 17. Similarly, the lower bound of B frame arrival curve is determined by the maximum arrival time required for  $k$  consecutive frames.

The service curves  $[\beta_{fin}^u, \beta_{fin}^l]$  for B frames are also computed as the arrival curves have been computed. The only difference here is that instead of the arrival times of B frames, we compute the time required for the execution of the tasks mapped on the PE for each B frame, i.e.,  $b\_arr$  is changed to execution time. Execution time also depends upon the frequency allocated to the PE. Subsequently, we compute the maximum and minimum execution time required for  $k$  consecutive B frames. Finally, we compute the service curves in a similar manner as we did for arrival curves. The arrival and service curves used in the following sections are the partitioned arrival and service curves for B frames presented here.

## IV. BOUNDS ON DROPPED FRAMES

In this section, we present a method for computing bounds on the number of frames that are dropped due to an overflow at a buffer. We first present the modeling idea and the basic concepts, and then present the details of how drop bounds

can be obtained.

**A single buffer case.** Consider an input stream that is processed by a single processing element (PE). Suppose the input buffer that stores the incoming frames of the stream before being processed by the PE, has a finite capacity of  $B$  frames. If the buffer is full when a frame arrives, the oldest frame at the head of the buffer will be dropped and the newly arrived frame will be enqueued at the end of the buffer. We are interested in the maximum bounds on the frames that can be dropped over any interval of a given length. The system architecture is shown in the top part of Figure 5. In the figure,  $a_1(t)$  denotes the input arrival pattern of the frame, i.e.,  $a_1(t)$  gives the number of frames that arrive over the time interval  $(0, t]$ . Similarly,  $a_3(t)$  gives the number of output frames corresponding to  $a_1(t)$ , respectively, over the interval  $(0, t]$ .

To model the buffer refresh at the input buffer, we use a virtual processor  $P_v$  that serves as an admission controller, as shown in the bottom part of Figure 5. The virtual processor  $P_v$  splits the input stream  $a_1(t)$  into two disjoint streams: the former,  $a_2(t)$ , contains the frames that will go through the system, and the latter,  $a'_2(t)$ , contains the frames that will be dropped, such that there are no overflows at the buffer.

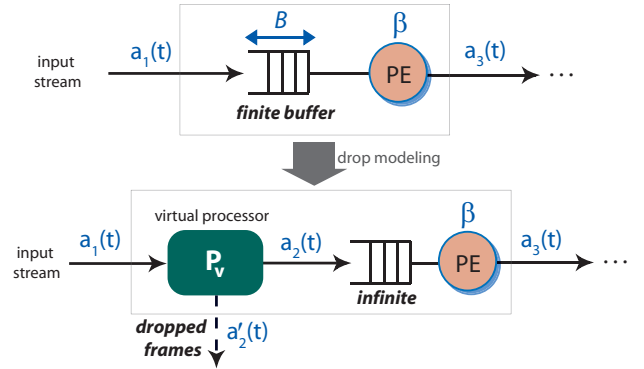


Fig. 5. Modeling systems with drop due to buffer overflow.

Based on this transformed system, we give the relationship between  $a_1(t)$  and  $a_2(t)$ , and the bounds on  $a_3(t)$ , stated by Lemma 4.1 and 4.2. The (min,+) convolution  $\otimes$  and deconvolution  $\oslash$  operators are defined as:

$$\begin{aligned} (f \otimes g)(t) &= \inf\{f(s) + g(t-s) \mid 0 \leq s \leq t\}, \\ (f \oslash g)(t) &= \sup\{f(t+u) - g(u) \mid u \geq 0\}. \end{aligned}$$

Similarly, the (max,+) convolution  $\bar{\otimes}$  and deconvolution  $\bar{\oslash}$  operators are defined as:

$$\begin{aligned} (f \bar{\otimes} g)(t) &= \sup\{f(s) + g(t-s) \mid 0 \leq s \leq t\}, \\ (f \bar{\oslash} g)(t) &= \inf\{f(t+u) - g(u) \mid u \geq 0\}. \end{aligned}$$

In what follows,  $g^*$  denotes the sub-additive closure of  $g$ , defined by  $g^* = \min\{g^n \mid n \geq 0\}$ , where  $g^0(0) = 0$  and  $g^0(t) = +\infty$  for all  $t > 0$ , and  $g^{n+1} = g^n \otimes g$  for all  $n \in \mathbb{N}$ ,  $n \geq 0$ . Further,  $\mathcal{I}$  denotes the linear idempotent operator, i.e.,

$$\mathcal{I}_{a_1}(x)(t) = \inf_{0 \leq s \leq t} \{x(s) + a_1(t) - a_1(s)\}.$$

*Lemma 4.1:* Suppose  $f$  is the mapping from  $a_2(t)$  to  $a_3(t)$ , i.e.,  $a_3 = f(a_2)$ . Then,  $a_2 = (\mathcal{I}_{a_1} \circ (f+B))^*(a_1)$ .

*Lemma 4.2:* Consider the system in Figure 5. Denote  $\alpha$  as the arrival curves of the input stream,  $\beta$  as the service curves of the PE, and  $B$  as the size of the buffer. The output stream of the system is bounded by the arrival curves  $\alpha' = (\alpha^u, \alpha^l)$ , defined by

$$\begin{aligned}\alpha^u &= \min\{(\alpha^u \otimes \beta_{\text{eff}}^u) \otimes \beta_{\text{eff}}^l, \beta_{\text{eff}}^u\}, \\ \alpha^l &= \min\{(\alpha^l \otimes \beta_{\text{eff}}^l) \otimes \beta_{\text{eff}}^u, \beta_{\text{eff}}^l\}.\end{aligned}$$

where

$$\begin{aligned}\beta_{\text{eff}}^u &= (\alpha^u \otimes \beta^u + B)^* \otimes \alpha^u \otimes \beta^u \\ \beta_{\text{eff}}^l &= (\alpha^l \otimes \beta^l + B)^* \otimes \alpha^l \otimes \beta^l.\end{aligned}$$

Based on the above results, Lemma 4.3 gives the bounds on the dropped input frames.

*Lemma 4.3:* Suppose  $\alpha = (\alpha^u, \alpha^l)$  are the arrival curves of an input stream,  $\beta = (\beta^u, \beta^l)$  are the service curves of the PE, and  $B$  is the size of the input buffer. Then, the number of input frames that can be dropped over any interval of length  $\Delta \geq 0$  is upper bounded by  $\alpha_{\text{drop}}^u(\Delta)$ , defined by

$$\alpha_{\text{drop}}^u = (\alpha^u - \beta^l) \bar{\otimes} 0$$

where  $\beta_v^l \stackrel{\text{def}}{=} (\alpha^l \otimes \beta^l + B)^* \otimes \alpha^u$ .

*Lemma 4.4:* Define  $\alpha$ ,  $\beta$ ,  $B$  and  $\alpha_{\text{drop}}$  as in Lemma 4.3. Denote  $\delta^u(k) = \min\{\Delta \geq 0 \mid \alpha^l(\Delta) \geq k\}$  and  $\delta^l(k) = \min\{\Delta \geq 0 \mid \alpha^u(\Delta) \geq k\}$  for all  $k \in \mathbb{N}$ . Then, for any given non-negative integer  $k$ , the number of frames that can be dropped over any  $k$  consecutive input frames is upper bounded by  $\alpha_{\text{dropF}}^u(k)$ , where

$$\alpha_{\text{dropF}}^u(k) \stackrel{\text{def}}{=} \min\{k, (\alpha_{\text{drop}}^u \circ \delta^u)(k)\}, \quad (4)$$

All the lemmas are proved in [5].

**Multiple buffers case.** Consider a system consisting of  $m$  PEs (as shown in Fig. 6). The input stream that is processed by a sequence of  $m$  PEs,  $PE_1, \dots, PE_m$ , where the input buffer at  $PE_i$  has a finite capacity of  $B_i$  (frames). The arrival curves of the input stream and the service curves of  $PE_i$  are denoted by  $\alpha_1$  and  $\beta_i$ , respectively, as illustrated in Fig. 6. Given such architecture, we would like to compute the maximum bounds on the total number of frames that are dropped within the system.

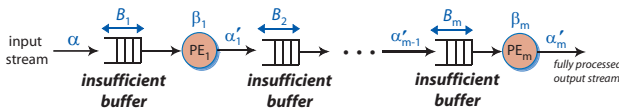


Fig. 6. A sequence of PEs with insufficient buffers.

Since the frames that are dropped at the PEs are disjoint, the number of frames that are dropped in the system is the total number of frames that are dropped at each PE. The maximum number of the frames that are dropped at  $PE_1$  over any interval of a given length  $\Delta$ , denoted by  $N_{\Delta}^1$ , is derived using Lemma 4.4. The maximum number of frames  $N_{\Delta}^i$  that are dropped over any interval of length  $\Delta$  at each subsequent  $PE_i$  for all  $2 \leq i \leq m$ , can be computed in a compositional

manner: first, compute the output arrival curves  $\alpha'_{i-1}$  after being processed by  $PE_{i-1}$  by applying Lemma 4.2; then, compute the drop bounds  $N_{\Delta}^i$  at  $PE_i$  using Lemma 4.4, with  $\alpha'_{i-1}$  as the input arrival curves,  $\beta_i$  as the service curves and  $B_i$  as the input buffer size. We repeat this process until we reach the last PE. The maximum number of input frames that are dropped within the system over any interval of length  $\Delta$  is then the summation of all the computed drop bounds, which is given by  $N_{\Delta}^1 + \dots + N_{\Delta}^m$ .

## V. WORST-CASE BOUND ON QUALITY

In the previous section, we presented how the bounds are computed for dropped frames. In this section, we use this bound to compute the worst-case quality in terms of PSNR. In order to find the worst-case quality for a video clip, we need to construct a worst-case quality 3-D space as shown in Fig.3. This is a surface that maps the frame interval based drop bound from the previous section to a frame interval based quality bound. Let us denote this mapping function as  $Q^u$  and the frame interval based quality bound as  $q^u$ . Then the mapping can be depicted as  $Q^u : \alpha_{\text{dropF}}^u \rightarrow q^u$ . However, in order to perform this mapping, the worst-case quality surfaced  $Q^u$  needs to be constructed. We construct this surface by taking consecutive frame intervals as windows. For each frame interval in the entire video, we find the maximum noise error experienced if any number of frames upto the frame window size is lost. This quantity is architecture independent and depends only on the nature of the clip.

The maximum deviation among the dropped frames and the possible concealment frames are computed in terms of the mean squared error (MSE) given by

$$MSE_{\text{avg}} = \frac{(MSE_{\mathcal{R}} + MSE_{\mathcal{G}} + MSE_{\mathcal{B}})}{(3 \times W \times H)} \quad (5)$$

where  $MSE_{\mathcal{R}/\mathcal{G}/\mathcal{B}} = \sum_{n=0}^{N_{\text{drop}}-1} (MSE_{\mathcal{R}/\mathcal{G}/\mathcal{B}})_n$ .  $MSE_{\mathcal{R}/\mathcal{G}/\mathcal{B}}_n$  is the deviation for red/green/blue pixels due to a dropped frame. The MSE for red pixel is given by

$$(MSE_{\mathcal{R}})_n = \sum_{w=0}^{W-1} \sum_{h=0}^{H-1} (r_d(h, w, n) - r_c(h, w, n))^2 \quad (6)$$

where  $r_d$  is the red pixel intensity of the dropped frame and  $r_c$  is the red pixel intensity of the concealment frame (immediately preceding frame that was successfully processed).  $h$ ,  $w$  and  $n$  are the height, width and frame drop number indices. Similar explanations hold true for  $MSE_{\mathcal{G}}$  and  $MSE_{\mathcal{B}}$ .  $W$  and  $H$  are the horizontal and vertical resolution of each frame in the video.  $N_{\text{drop}}$  is the number of frames dropped in the sequence. Finally, the PSNR value of a video sequence with frame drops is expressed as

$$psnr = 10 \times \log_{10} \frac{(255 \times 255 \times N_{\text{tot}})}{(MSE_{\text{avg}})} \quad (7)$$

where  $N_{\text{tot}}$  is the total number of frames in the video sequence. In our case, we slide the frame interval window from  $1 \rightarrow N_{\text{tot}}$ . Within each frame interval window  $F$ , we find the worst-case PSNR value or the highest MSE value from Equation.5 for



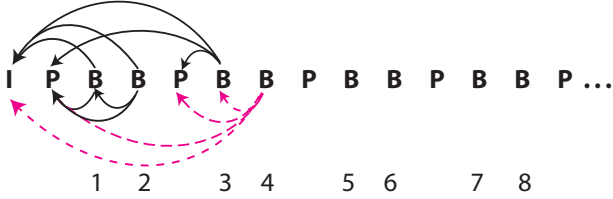


Fig. 7. GOP decoding order with possible replacements for B frames if dropped.

every value  $f$ , such that  $0 \leq f \leq F$ . Here  $f$  is the number of frames that were dropped in the frame interval  $F$ . Therefore, we construct the worst-case quality surface  $Q^u(f, F)$ . This procedure is shown in Algorithm 2.

The  $MSE_{max}$  structure containing the maximum MSE values for B frames is calculated taking all possible concealment frames into consideration. For example, let us take the order of frames in group of pictures (GOP) as shown in Fig. 7. In particular, for the 4th B frame, there are three different possible concealment frames. If the 3rd B frame is not dropped, then it will replace the 4th B frame. If the 3rd B frame is dropped, then the P/I frame will replace 4th B frame in that order. Since P frames are not dropped in our setting, P frame replaces the 4th B-frame if the 3rd B frame is lost. Therefore,  $MSE_{max}$  is constructed taking all such possible concealment frames.

Lines 1 and 2 record the indices of the B frame in the GOP decoding order and then sort the frames in decreasing order of the MSE values in  $MSE_{max}$  structure, while retaining the original indices after sorting. For each frame interval window  $F$ , the frame index ranges from  $i$  to  $i + F - 1$  where  $i$  is the variable used for sliding across the video clip. We search for the  $F$  frames within this index range from the sorted MSE structure shown as  $MSE_{maxsort}$  (Line 3). We slide the window across the entire video clip and find the  $F$  frames for each  $i$ . These quantities are stored in the structure  $MSE_{max}(i, n, F)$  where  $0 \leq n \leq F$ . The upper bound on MSE is then computed by searching for the maximum value across all windows of size  $F$  and for every drop count  $f$  which ranges from  $0 \leq f \leq F$  (Line 4). Once the upper bound  $MSE^u(f, F)$  is computed, the worst-case quality surface  $Q^u(f, F)$  can be computed as given

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**Algorithm 2** Computing worst-case quality surface for a video clip

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**Input:**  $MSE_{max}$  - Maximum MSE values for B frames if replaced by possible preceding I/P frames. MSE values for I/P frames are set to 0.

**Output:**  $Q^u(f, F)$  - Worst-case quality surface,  $f$  is the number of frames dropped in a frame interval of  $F$

- 1: Record the frame indices
  - 2: Sort  $MSE_{max}$  structure in descending order preserving the frame indices  $\rightarrow MSE_{maxsort}$
  - 3: Find  $F$  values within frame index range  $i$  to  $(i + F - 1)$  in  $MSE_{maxsort}$ :  $\forall i, \forall F$  and  $1 \leq i \leq N_{tot} - F + 1$  and  $0 \leq F \leq N_{tot} \rightarrow MSE_{maxF}(i, n, F)$  where  $0 \leq n \leq F$
  - 4:  $MSE^u(f, F) = \max_{\forall i} \left\{ \sum_{n=0}^f MSE_{maxF}(i, n, F) \right\}$
  - 5:  $Q^u(f, F) = 10 \times \log_{10} \left( \frac{255 \times 255 \times F}{MSE^u(f, F)} \right)$
- 

in Line 5.

It can be observed from Algorithm 2 that the time complexity of computing worst-case quality surface is  $O(N_{tot}^3)$ .

## VI. CASE STUDY (MPEG-2 DECODER)

In this section, we evaluate our proposed analytical framework using an MPEG-2 decoder application. In this case study, the MPEG-2 decoder tasks are mapped onto the two PEs in the MPSoC architecture shown in Fig. 2. The tasks mapped are Variable Length Decoding (VLD), Inverse Quantization (IQ), Motion Compensation (MC) and Inverse Discrete Cosine Transform (IDCT). VLD and IQ are mapped to PE<sub>1</sub> while MC and IDCT are mapped to PE<sub>2</sub>. According to our setup, each buffer in Fig. 2 is composed of two buffers (as shown in Fig. 4) to separate the B frames from I/P frames. We only analyze the drops for B frames and therefore, we analyze only the B frame buffer. The buffer used for I/P frames is not analyzed here because it can be done using conventional Network Calculus techniques ([2]). PE<sub>1</sub> is allocated a frequency of 40 MHz, whereas PE<sub>2</sub> is allocated a frequency of 100 MHz. The various B frame buffer sizes used in the first stage are set to be 30 frames, 60 frames, 90 frames, 120 frames and 150 frames. The B frame buffer sizes used in the second stage are the same as in the first stage. However, the analysis of drops in the second stage is done by fixing the first stage buffer size to 90.

The cycle requirements for each task on the model of a processor was obtained using the SimpleScalar simulator ([1]). Here, we use a MIPS-like processor model using the Portable instruction set architecture (PISA). We use three MPEG-2 video clips in our experiments, namely, *susi\_080*, *time\_080* and *orion\_2*. The first two videos are taken from [12], where both have a total of 450 frames, i.e.,  $N_{tot} = 450$  with 1320 macroblocks (MBs) in each frame. The first clip is a motion video and the second one is a still video. The third video, taken from [13], is a combination of both motion and still frames. It has a total of 1171 frames, i.e.,  $N_{tot} = 1171$  with 1350 MBs in each frame. All the three video clips have a bit rate of 8 Mbps.

### A. First stage results

The first stage involves computing the drop bounds of the B frame buffer at PE<sub>1</sub> (denoted by  $B_{fin1}$ ), which is of size  $B_{max1}$ . The arrival curves at the input of  $B_{fin1}$  are  $\alpha_{fin1} = [\alpha_{fin1}^u, \alpha_{fin1}^l]$  as computed in Section 3. Similarly, the service curves offered to the frames in  $B_{fin1}$  are  $\beta_{fin1} = [\beta_{fin1}^u, \beta_{fin1}^l]$ .

**Arrival curve, virtual processor service curve and drop bound (in time intervals):** Fig. 8 shows the upper arrival curves of the B frames ( $\alpha_{fin1}^u$ ) and the lower service curve of the virtual processor ( $\beta_{v1}^l$ ) for the three clips (computed using the techniques in Section 4). The worst case drop bound,  $\alpha_{drop1}^u$ , obtained as a result of Lemma 4.3 is also shown in the three plots. In this experiment,  $B_{max1} = 90$ , which is in frames. It can be observed from the plots that, until a certain time interval, the drop bound is zero. After that interval, however, the drop bound increases. This is expected

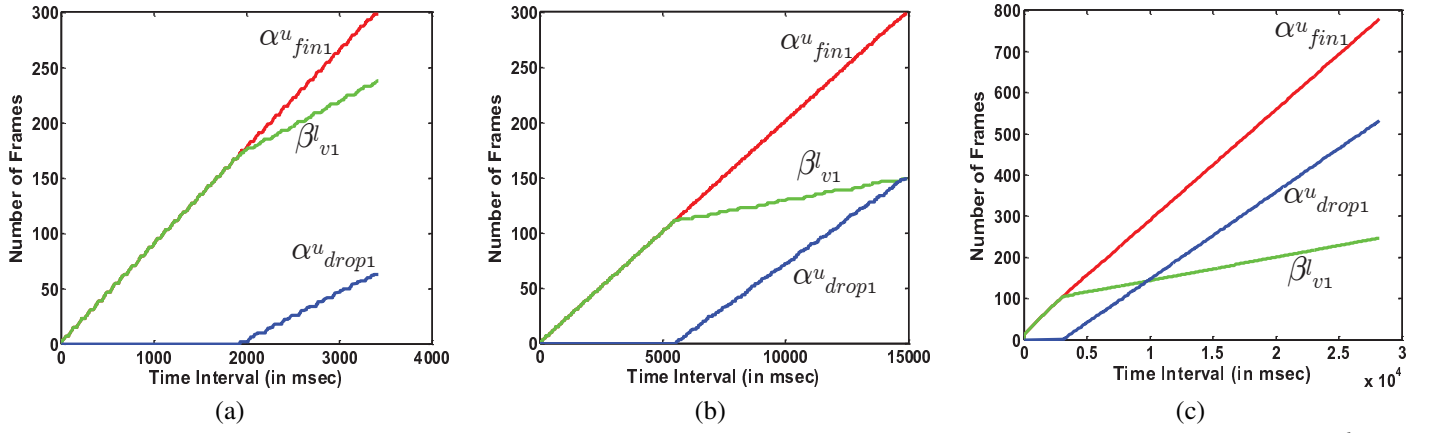


Fig. 8. Generation of time interval based drop bound curves ( $\alpha^u_{drop1}$ ) from the upper arrival ( $\alpha^u$ ) and lower virtual processor service ( $\beta^l_v$ ) curves. Here  $B_{max} = 90$ . The three plots are for clips (a) *time\_080*, (b) *susi\_080* and (c) *orion\_2*.

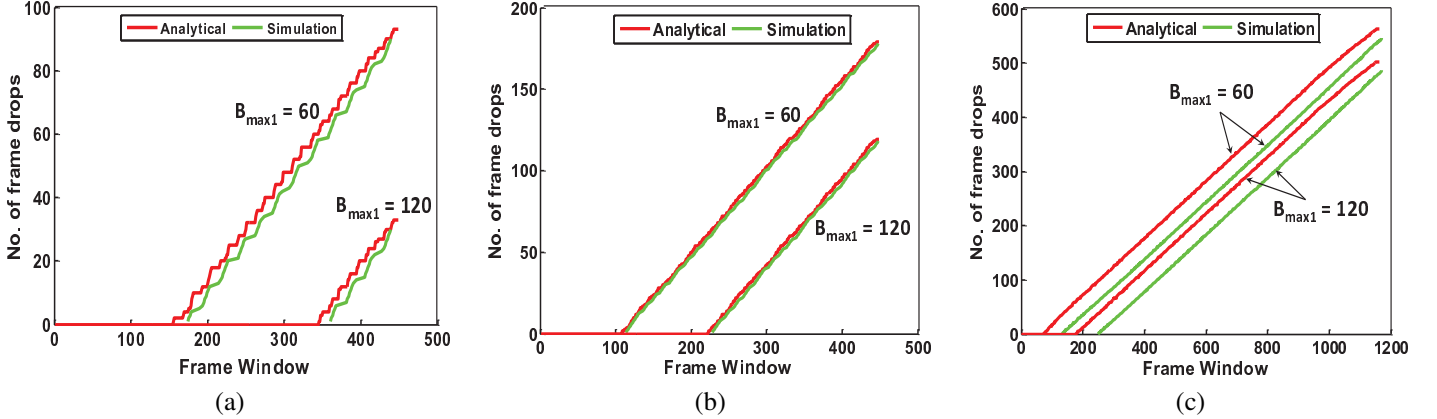


Fig. 9. Comparison of Analytical and Simulation results of worst-case drop bound for two buffer capacities. The three plots are for clips (a) *time\_080*, (b) *susi\_080* and (c) *orion\_2*.

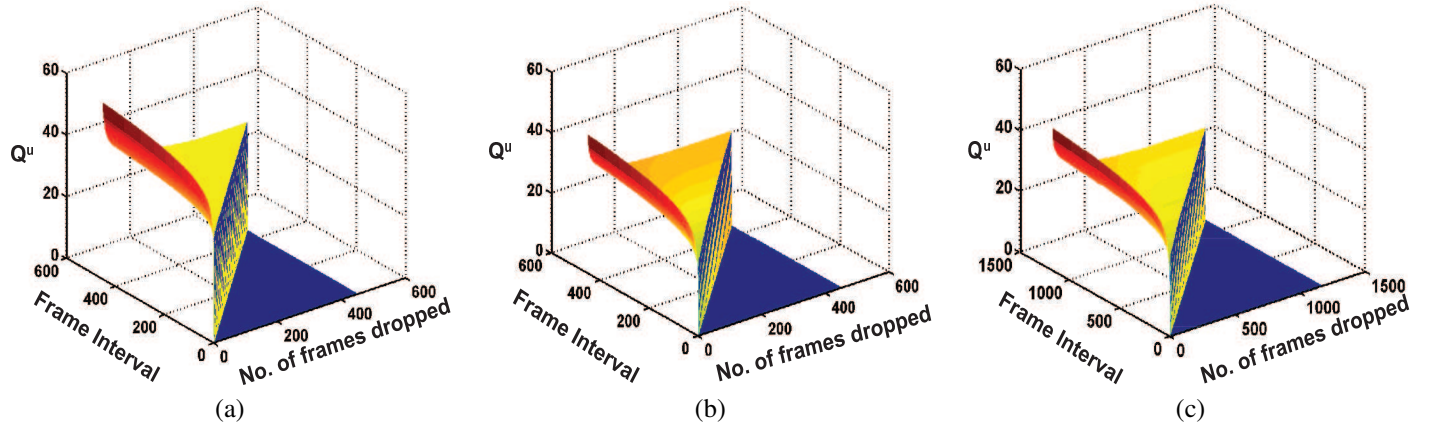


Fig. 10. Worst case quality surface ( $Q^u$  in dB) for the clips (a) *time\_080*, (b) *susi\_080* and (c) *orion\_2*.

because the buffer size of 90 frames is insufficient to avoid buffer overflow. It is also seen that  $\beta^l_{v1}$  follows  $\alpha^u_{fin1}$  until the former rises above the buffer size. From there onwards,  $\beta^l_{v1}$  starts dropping behind  $\alpha^u_{fin1}$  as frames are dropped. Another interesting observation is that for still video *time\_080*,  $\beta^l_{v1}$  is closer to  $\alpha^u_{fin1}$  and hence, the drop bound is lower when compared to clips *susi\_080* and *orion\_2*. However, it is interesting to notice that the video clip *orion\_2* has a higher drop bound value than *susi\_080*. This is because the service required by the frames in *orion\_2* is higher than the the service required by the frames in *susi\_080* as the former has more macroblocks per frame.

**Validation of drop bounds (in frame intervals) with simulation:** We validate the drop bounds  $[\alpha^u_{dropF1}]$  computed using our analytical framework with the ones obtained by simulation. Here, the drop bound is in frame intervals and not time intervals. Once  $\alpha^u_{drop1}$  is computed,  $[\alpha^u_{dropF1}]$  can be computed according to Lemma 4.4. We show the comparison between simulation and analytical results for two buffer sizes,  $B_{max1} = 60$  and  $B_{max1} = 120$ . It is clear from Fig. 9 that the analytical results emulate the simulation results very closely. Our analytical results are a little pessimistic because they consider the worst case in all the frame windows, whereas

the simulation result depicts only one continuous run. It is also seen that  $[\alpha_{dropF1}^u]$  decreases as the buffer size increases, which is expected. It is interesting to note that the difference between simulation and analytical results is greater in *orion\_2* than in the other two videos. The reason for this behaviour is that *orion\_2* is a larger clip and the variability in the required service is larger. In the case of *susi\_080* and *time\_080*, the variability in required service is limited.

**Worst-case quality surface:** The worst-case quality surface computed using Algorithm 2 is presented for the three clips in Fig. 10. It is observed that the worst-case quality surface is an exponential surface as it represents the PSNR value for various frame drops within a frame interval. In all the  $Q^u$  plots shown, the PSNR value is highest when the least number of frames are dropped in the largest frame interval. The PSNR surface keeps falling from that point as the number of frames dropped increases and the frame interval decreases. This surface is an architecture independent feature of the video clips. According to Fig. 10, *time\_080* has the highest  $Q^u$  values among all the video clips.

**Comparison of  $q^u$  with simulation results:** The comparison of frame interval based worst-case quality ( $q^u$ ) is presented in Fig. 11(a), (b) and (c) for the three clips. The immediate observation from the plots is that, for *orion\_2*, there is a considerable deviation of the analytical result from the simulation results in the lower frame intervals. This is because the clip is large and the analytical model considers the worst case across the entire clip. On the other hand, the simulation based result is the outcome of one continuous run. Therefore, if the worst case does not occur in the beginning of the clip, the deviation is large. However, the interesting point is that the curves converge closer towards the higher frame intervals. Hence, it is useful to use the higher frame intervals to explore the quality-buffer design space because they help to reduce the overestimation in buffer size required. However, even if overestimation exists, buffer dimensions can be reduced for a lower tolerable quality if the zero loss constraint need not be strictly adhered to.

**Variation of worst-case quality with buffer size:** The variation of  $q^u$  with buffer size is shown in Fig. 12. As is expected, in Fig. 12(a), (b) and (c),  $q^u$  values increase as the maximum buffer capacity  $B_{max1}$  is increased. We explore the variation for five buffer sizes as shown in Fig. 12. However, it is interesting to note here that, in all the three curves, the  $q^u$  value rises infinitely at some frame interval value. This is because below that frame interval, no frame drop is possible with the corresponding buffer size and therefore, the quality is maximum. As the first drop happens, the worst-case quality reduces and assumes a finite value. Another interesting aspect that this work highlights is shown clearly in Fig. 12. In the higher frame intervals, the worst-case quality values are very close to each other for different buffer sizes. This property could be exploited to reduce buffer dimensions for a small trade-off in  $q^u$ . For example in Fig. 12(a), if 40 – 45dB is an acceptable value for  $q^u$ , in a frame interval of 450, then  $B_{max1} = 90$  can be chosen rather than  $B_{max1} = 120$  in order to reduce the maximum buffer required. For an acceptable  $q^u = 30 - 35dB$ , it is seen in Fig. 12(b) that the least buffer size of 30 can be chosen for a frame interval of 450. Similar

tradeoffs are evident in the third curve as well.

### B. Second stage

The second stage involves processor PE<sub>2</sub> and again two buffers. The frequency allocated to PE2 is 100 MHz. Again, we do not consider the I/P frame buffer, but analyze drop bounds for the B frame buffer only. Therefore, the resource parameter that we include for the analysis of the second stage is the buffer, labeled by  $B_{fin2}$ , which has size  $B_{max2}$ . The arrival curves at the input of  $B_{fin2}$  are  $\alpha_{fin2} = [\alpha_{fin2}^u, \alpha_{fin2}^l]$  as computed in Section 3. Similarly, the service curves offered to the frames in  $B_{fin2}$  are  $\beta_{fin2} = [\beta_{fin2}^u, \beta_{fin2}^l]$ . The detailed results are presented in [5].

### C. Buffer savings

In this analysis, we highlight the significance of our mathematical framework. The final goal of the framework was to trade-off buffer size with quality. In the earlier results, we have seen that as the maximum buffer capacity is reduced, the quality reduces due to frame drops. However, if the resultant quality after frame drops is within tolerable limits, we can achieve significant savings in buffer. We present this result in Table I. The savings shown consider drops only in the first stage. We find the buffer saving using  $Bit^l(B_{nd}) - Bit^u(B_d)$ . Here,  $B_{nd}$  is the buffer size (in frames) required for no drops and  $B_d$  is the buffer size (in frames) which allows drops within the tolerable quality shown in Table I. Further,  $Bit^l(F)$  and  $Bit^u(F)$  are the maximum and minimum number of bits in  $F$  consecutive frames, respectively. It is known from multimedia literature that a PSNR value of 30-50 dB is an acceptable output quality. Hence, we vary the tolerable quality from 30-40 dB in steps of 5 dB. The  $\times$  symbol against the clip *time\_080* indicates that the quality never drops to 30 dB even if all the B frames are dropped. We can see from Table I that *time\_080* shows more savings in terms of percentage when compared to the other two video clips. This is because *susi\_080* and *orion\_2* require a higher buffer size (in terms of Megabits) without any frame drops. Therefore, their savings (in percentage) is less.

TABLE I  
BUFFER SAVINGS FOR THE THREE VIDEO CLIPS WITH QUALITY VARIATION

Buffer savings	clip	susi_080	time_080	orion_2
	PSNR (in dB)			
In Megabits	30	25.88	×	49
	35	3.53	5.09	6.16
	40	0.15	1.97	1.3
In percentage	30	28.6%	×	29.1%
	35	3.9%	39.4%	3.6%
	40	0.16%	15.5%	0.77%

## VII. CONCLUDING REMARKS

In this paper, we study the effects of frame drops in a multiprocessor system-on-chip platform running video decoder applications. Towards this objective, we propose a novel mathematical model to compute the worst-case drop bound in a MPSoC architecture with finite buffers. This analytical

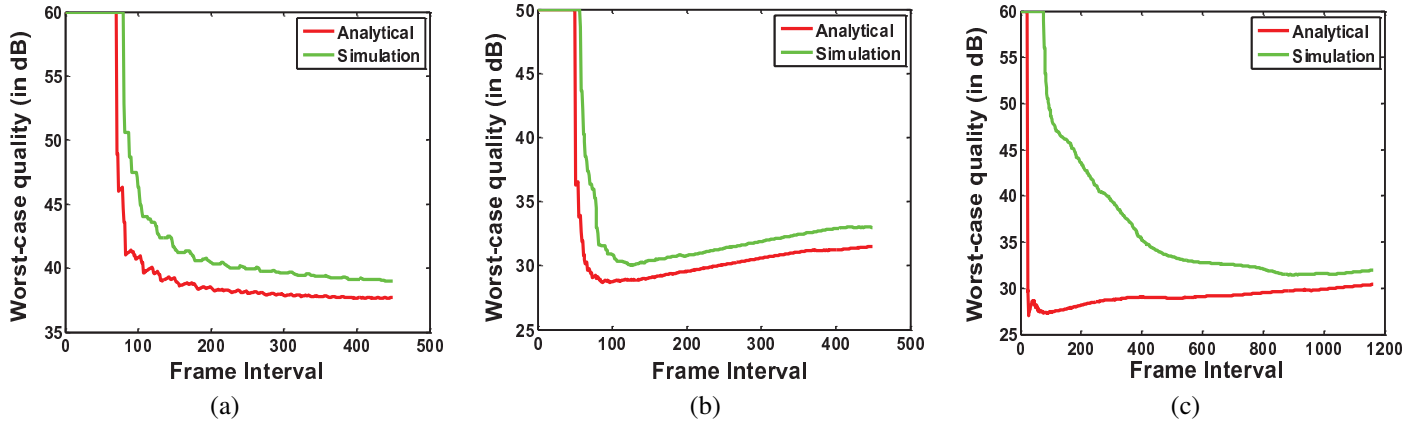


Fig. 11. Comparison of analytical and simulation results of worst-case quality ( $q^w$ ) for  $B_{max1} = 30$  for three clips (a) *time\_080*, (b) *susi\_080* and (c) *orion\_2*.

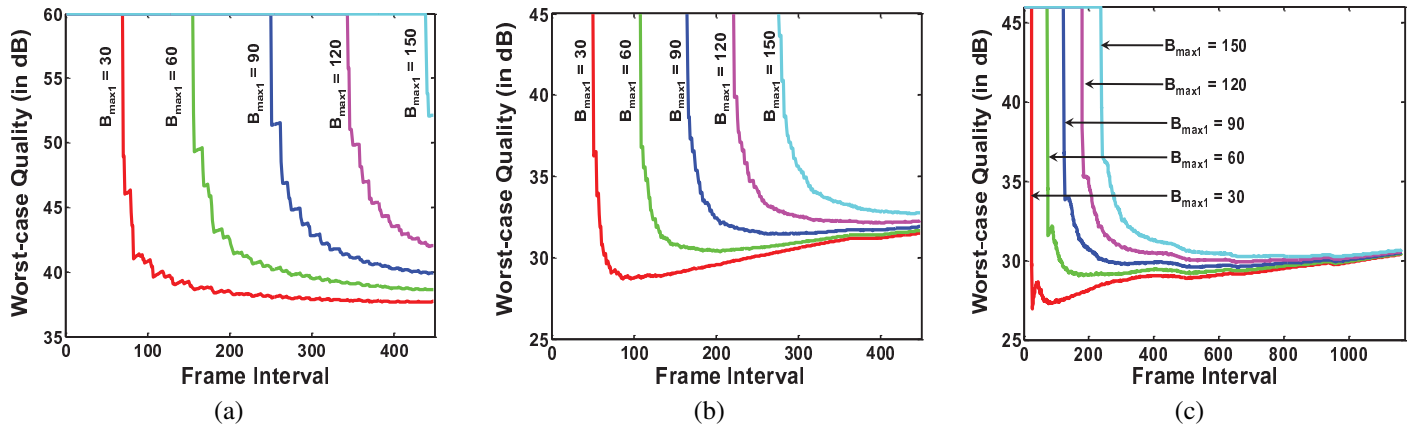


Fig. 12. Variation of worst case quality ( $q^w$ ) with different buffer sizes for the clips (a) *time\_080*, (b) *susi\_080* and (c) *orion\_2*.

model helps in exploring the buffer-quality design space by analyzing the worst-case quality when frames are dropped. One important aspect of this work is that we can explore the buffer-quality design space by trading off a significant buffer area for a tolerable loss in quality. In future, we would like to use our analytical framework to explore trade-offs with other important system parameters like peak temperature.

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