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Parallelized Incomplete Poisson Preconditioner in Cloth Simulation

Abstract

Efficient cloth simulation is an important problem for interactive applications that involve virtual humans, such as computer games. A common aspect of many methods that have been developed to simulate cloth is a linear system of equations, which is commonly solved using conjugate gradient or multi-grid approaches. In this paper, we introduce to the computer gaming community a recently proposed preconditioner, the incomplete Poisson preconditioner, for conjugate gradient solvers. We show that the parallelized incomplete Poisson preconditioner (PIPP) performs as well as the current state-of-the-art preconditioners, while being much more amenable to standard thread-level parallelism. We demonstrate our results on an 8-core Apple* Mac* Pro and a 32-core code name Emerald Ridge system.

Disciplines

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ABSTRACT:

Efficient cloth simulation is an important problem for interactive applications that involve virtual humans, such as computer games. A common aspect of many methods that have been developed to simulate cloth is a linear system of equations, which is commonly solved using conjugate gradient or multi-grid approaches. In this paper, we introduce to the computer gaming community a recently proposed preconditioner, the incomplete Poisson preconditioner, for conjugate gradient solvers. We show that the parallelized incomplete Poisson preconditioner (PIPP) performs as well as the current state-of-the-art preconditioners, while being much more amenable to standard thread-level parallelism. We demonstrate our results on an 8-core Apple* Mac* Pro and a 32-core code name Emerald Ridge system.

PARALLELIZED INCOMPLETE POISSON PRECONDITIONER IN CLOTH SIMULATION:

Simulating flexible materials, such as cloth, is an important task for applications involving virtual humans such as computer games and visual effects. High quality offline simulations are achieved by using implicit methods for simulating cloth [20–22]. Real-time applications, on the other hand, use explicit or semi-explicit methods for cloth simulation in order to meet time constraints [5, 17]. Despite the decades of research on simulating flexible materials, the efficient simulation of cloth remains an important challenge for computer animation. A large amount of research exists that addresses algorithmic optimizations for speeding up implicit integration methods for simulating cloth. The use of preconditioners [4, 9, 13] has been shown to greatly reduce the number of iterations of the conjugate gradient method in an effort to achieve convergence.

In this paper, we explore the use of a novel preconditioning scheme – the incomplete Poisson preconditioner – that has not been used before in clothing simulation. Using a variety of standard benchmarks, we first demonstrate that this preconditioner is just as good as, if not better, than currently used methods. A major advantage of this method is that it is extremely easy to parallelize and can take advantage of the processing power available in current and next generation multi-core hardware. Current state-of-the-art

preconditioners [13] are not as suitable for parallelization and do not scale well with increase in computational resources. This paper makes the following contributions:

- 1. To our knowledge, we propose for the first time the use of the incomplete Poisson preconditioner for clothing simulation.
- 2. We compare the incomplete Poisson preconditioner to the most commonly used preconditioning methods in terms of efficiency, quality and ease of parallelization.
- 3. We demonstrate that a parallel implementation of the incomplete Poisson preconditioner (PIPP) achieves significant performance improvement on multi-core computers.
- 4. We demonstrate the scalability of the PIPP on a state-of-the-art, 32-core compute server and show that it is ready for the next generation of hardware resources.

The rest of this document is organized as follows. We start by reviewing related work. Subsequently we present an overview of the method we use for simulating cloth. We describe the Jacobi preconditioner, the symmetric successive over-relaxation, and the incomplete Cholesky preconditioner which are commonly used to accelerate convergence. In addition, we propose the use of the incomplete Poisson preconditioner for cloth simulation. We compare the four preconditioning methods on four standard benchmarks and also demonstrate the effectiveness of parallelizing the incomplete Poisson preconditioning scheme. Finally, we conclude with a discussion of future work.

Related Work

Early work by [20–22] has applied techniques from mechanical engineering and finite element communities to cloth simulation. Since then, there has been an extensive amount of work by different research groups [5, 7, 10, 23] that have addressed several aspects of simulating cloth. An extensive overview of cloth simulation techniques can be found in two survey papers [8, 16]. Preconditioners play a very important part in implicit cloth simulation as they can greatly speed up convergence of numerical methods. The work in [3] used a simple diagonal preconditioner for the modified preconditioned conjugate gradient method (MPCG). The work in [9] demonstrated 20% speedup by using a 3×3 block diagonal preconditioner. This work was extended in [4] by proposing an approximation of the filter matrix A of the MPCG. The work in [13] demonstrates the effectiveness of the incomplete Cholesky and successive symmetric over-relaxation (SSOR) preconditioning schemes by reducing the number of iterations by 20%.

Relation to Prior Work. In this paper, we first examine the fitness of three commonly used preconditioning schemes [3, 13] in comparison to the proposed incomplete Poisson preconditioner. Our simulation method is similar to the implicit simulation method described in [2,3]. We perform collision detection using distance fields [11]. Collision resolution is performed using the techniques described in [6] and [18].

Cloth Simulation Overview

There are many aspects to cloth simulation. A cloth simulator is required to solve a linear system of equations which is used to step the simulator forward by one time step. This system of equations is derived taking into account the specifics of the internal forces and their derivatives. Different soft and hard constraints are imposed on the simulation which must be met. Collision detection and resolution is another area of research that has many contributions. We refer the reader to excellent works in cloth simulation research [3, 12, 14, 15] for more information. In this paper, we focus on the methods of preconditioning that are used to accelerate the preconditioned conjugate gradient solver. In this section, we present an overview of the preconditioning for cloth simulation.

Preconditioned Conjugate Gradient Solver

An overview of the preconditioned conjugate gradient solver is shown in Algorithm 1. A detailed description of the algorithm can be found here [19]. The preconditioned conjugate gradient method takes as input the following: (a) a symmetric positive semi-definite matrix A, (b) a symmetric positive definite preconditioning matrix P of the same dimension as A, and (c) a vector b. The algorithm iteratively solves the linear system of equations, Ax = b and the iterations stop when $|b-Ax| < \epsilon |b|$, where ϵ is a user-defined tolerance value. The preconditioning matrix P, which must be easily invertible, speeds convergence to the extent that P^{-1} approximates A.

Preconditioning Methods

We examine the performance of three commonly used preconditioning methods: (1) diagonal, (2) symmetric successive over-relaxation (SSOR), and (3) incomplete Cholesky against the unconditioned conjugate gradient method. We also examine a new preconditioning scheme, the incomplete Poisson preconditioner, proposed by Ament et al. [1] for the Poisson problem. Their motivation was to find an easily parallelizable preconditioner for simulations on multi-GPU systems. To the best of our knowledge, this is the first time this preconditioning scheme has been applied to cloth simulation. The mathematical formulation of these preconditioners is as follows:

Diagonal (Jacobi) Preconditioner:

$$P = diag\{A\}^{-1} \text{ or } P_{i,i} = \frac{1}{A_{i,i}}$$

This simple preconditioning scheme approximates the inverse of a diagonal matrix. Although lacking in quality, it can be computed quickly and provides increase in performance in many cases. The computation of P^{-1} is relatively simple and this preconditioner can be subsequently applied using SpMV.

```
Procedure Preconditioned Conjugate Gradient Solver(A, x, b,P, \varepsilon)
Input: A: Left hand side of linear system of equations Ax = b.
Input: x: Input constraint.
Input: b: Right hand side of linear system of equations Ax = b.
Input: P: Preconditioner
Input: ε: Maximum tolerance
Output: x: Result.
// Initialization
r = b - Ax; // residual
d = P^{-1} \cdot r;
d_{new} = r \cdot d;
while i < MAX \land d_{new} > \epsilon^2 do
           q = A \cdot d;
           c = \mathbf{d} \cdot \mathbf{q}; // curvature
           if c < 0 then
           return FAIL;
           else if c == 0 then
                       break:
           end
           \alpha = \frac{\text{dnew}}{c};
           \mathbf{x} = \mathbf{x} + \mathbf{\alpha} \cdot \mathbf{d};
           \mathbf{r} = \mathbf{r} - \alpha \cdot \mathbf{q};
           \mathbf{s} = \mathsf{P}^{-1} \cdot \mathbf{r};
           d_{old} = d_{new};
           d_{new} = \mathbf{r} \cdot \mathbf{s};
           if d_{new} < 0 then
                      break;
           end
           \beta = \frac{\text{dold}}{\text{dnew}};
           \mathbf{d} = \mathbf{s} + \boldsymbol{\beta} \cdot \mathbf{d};
           i = i + 1;
end
if d_{new} < 0 \forall i == MAX then
           return FAIL;
else
           return SUCCESS;
```

Algorithm 1: Preconditioned Conjugate Gradient Solver

Incomplete Cholesky Preconditioner:

$$P = (LL^T)^{-1}$$

where L is the Cholesky factorization defined as follows:

$$L_{i,i} = \sqrt{A_{i,i} - \sum_{k=1}^{i-1} L_{i,k}^2}$$

$$L_{i,j} = \frac{1}{L_{i,i}} (A_{i,j} - \sum_{k=1}^{i-1} L_{i,k} L_{j,k}), i > j$$

with the additional constraint to keep the original sparsity pattern of A. The incomplete Cholesky is derived from the Cholesky decomposition method. A symmetric positive-definite matrix can be decomposed into the product of a lower triangular matrix and its conjugate transpose. These triangular matrices can quickly be inverted in order to solve linear systems. In that sense, the incomplete Cholesky preconditioner approximates the full inverse of A without incurring the cost of actually inverting it. It should be noted that P^{-1} is calculated using expensive forward and backward substitutions, which are inherently serial processes because of the triangular structures of L and L^{T} .

Incomplete Poisson Preconditioner:

$$P = HH^T$$

Where

$$H = I - L * diag\{A\} - 1$$

and L is the strictly lower triangular matrix of A. This novel preconditioner has a simple structure and is kind of an approximate inverse. As a result, no substitutions are required and this preconditioner can be applied efficiently with SpMV and thread-level parallelism.

Symmetric Successive Over-Relaxation:

$$P = (M1 * M2)^{-1}$$

Where

$$M1 = \frac{1}{\omega} * D + L$$

$$M2 = \frac{1}{(2-\omega)} * (I + \omega * D^{-1} + U)$$

and L,U,D are the strictly lower triangular, the strictly upper triangular and the diagonal matrix of A respectively. Symmetric successive over-relaxation is a variant of the Gauss-Seidel method but with improved convergence speed. As with incomplete Cholesky, a relatively expensive forward and backward substitution step occurs to calculate P–1. It should also be noted that the choice of ω influences convergence. We use the following ω :

$$\omega = \frac{1}{\max([1, \max(L), \max(U)])}$$

Evaluation Results

In this section we compare the proposed incomplete Poisson preconditioner to the most commonly used preconditioners. First, we describe the test cases we use for the comparison. Second, we evaluate the fitness of each of the preconditioning methods. Third, we provide the results of parallelizing the incomplete Poisson preconditioner on next-generation multi-core hardware. A visual comparison of using each of the preconditioners on the benchmarks can be seen in the accompanying video. All preconditioners seem to produce results of similar quality.

Benchmarks

We use four benchmarks for the purpose of exercising the preconditioners on a variety of challenging scenarios that are frequently encountered in simulating cloth. These four benchmarks are described below.

- **1. Free Fall.** This is more of a baseline case, where a piece of cloth falls under gravity and come to rest on a static sphere with no tangling (Figure 3(a)).
- **2. Curtain.** This case extends the previous benchmark by including fixed point constraints (Figure 3(b)).
- **3. Moving Collider.** Further extending the previous case, a cloth patch hung as a curtain interacts with a moving spherical collider (Figure 3(c)). This benchmark is used to test the behavior of the simulator in a dynamic environment.
- **4. Tangling.** Tangling is one of the toughest cases for cloth simulators to handle because of the complexities introduced by the multiple self-collisions (Figure 3(d)). As far as the conjugate gradient solver is concerned, for tangled states the number of nonzeros (thus the stiffness) of the matrix A(Ax = b) increases significantly. The increased matrix density can significantly affect performance.

Preconditioner Evaluation

We test the performance of the preconditioners by simulating 200 frames for each of the benchmarks described above. The parameters used for the cloth simulator are described in Table 1. The inter-particle forces were shear, bend and stretch. The evaluation results are illustrated in Figure 4. From the results, it is apparent that the incomplete Poisson preconditioner performs on par with incomplete Cholesky for cloth simulation. Table 2 and Figure 1 illustrate the performance results of all preconditioning schemes with increase in number of nodes on cloth patch. Here, we see that PIPP scales well with increase in resolution of cloth patch, but the incomplete Cholesky preconditioner does not. The main advantage of this novel preconditioner is that it can be easily parallelized, whereas incomplete Cholesky is inherently a serial algorithm.

Simulation Parameter	Value			
Grid Resolution	50 x 50			
Spring Constant	1000			
Inter-particle distance	0.005			
Damping Factor	2			
Time Step	0.01			
Error Threshold	10 ⁻¹⁵			
Mass of particle	1			

Table 1: Simulation Parameters.

#Nodes	Cholesky		Poisson		SSOR		Jacobi		None	
	#iter	Time(s)	#iter	Time(s)	#iter	Time(s)	#iter	Time(s)	#iter	Time(s)
2500	10	0.079	11	0.032	11	0.035	18	0.062	13	0.028
3600	10	0.099	11	0.046	11	0.046	18	0.080	13	0.049
4900	10	0.160	11	0.054	11	0.064	18	0.090	13	0.058
6400	10	0.133	11	0.062	11	0.078	18	0.101	13	0.064
8100	9	0.150	11	0.076	11	0.096	18	0.121	13	0.083
10000	9	0.151	11	0.084	11	0.110	18	0.138	13	0.091
19600	9	0.241	11	0.157	11	0.217	18	0.241	13	0.182
30625	9	0.482	12	0.326	11	0.359	18	0.388	13	0.337
40000	9	1.649	12	0.396	11	0.490	18	0.567	14	0.542

Table 2: Performance results (number of iterations and simulation time in seconds) for all preconditioning schemes with increase in number of nodes.

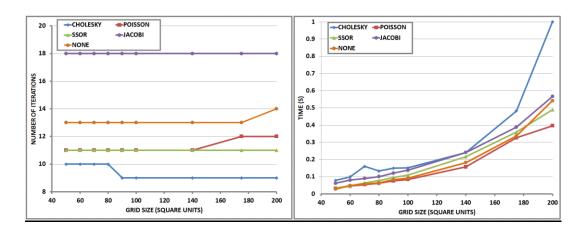


Figure 1: Performance results (number of iterations and simulation time in seconds) for all preconditioning schemes with increase in number of nodes.

Parallelization Results

To evaluate parallelization options for the incomplete Poisson preconditioner, we implemented a parallel version using Pthreads. The columns of matrix A are equally distributed among the available threads, which means that each thread operates on No.Columns / No.threads columns of A. The input of the parallelization function is A and the output $P = H^*H^T$, where $H = I - L^*diag\{A\}^{-1}$. We tested for different numbers of threads and the times we report include construction of the threads as well as thread synchronization. Our tests were performed on an 8-core Apple* Mac* Pro running Mac* OS X* 10.6 with 12GBs of RAM (Figure 2(a)) and a 32-core code name Emerald Ridge server with Intel® Xeon® processors X7560 and 32GB of RAM running OpenSUSE* Linux* 11.3 (Figure 2(b)). Both systems have Intel® Hyper-Threading Technology. To compute execution time, we used system-specific high-resolution timers: mach absolute time() on Mac OS X* and clock gettime() on Linux*. We further refer the reader to [1] for GPU parallel implementations of the incomplete Poisson preconditioner. Figure 2 shows that PIPP scales very well with the number of available cores. For both systems the performance of the PIPP increases significantly and reaches saturation after the number of threads equals the number of available hyper-cores. In the case of the 8-core system the performance of a single thread is about 2 seconds, while the performance of 16 threads is about 0.5 seconds. Similarly, in the case of the 32-core system a single thread takes more than a second, while 64 threads run at about 0.06 seconds.

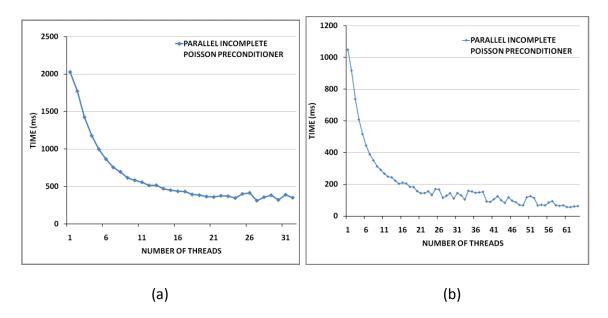


Figure 2: Parallelization results on multi-core hardware. (a) 8-core machine. (b) 32-core machine.

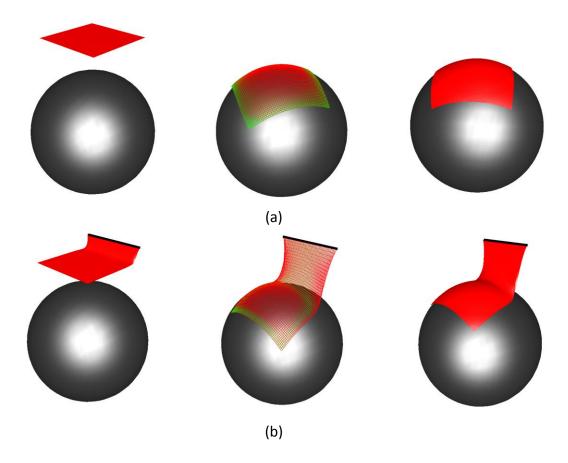
Conclusion and Future Work

We have presented a recently proposed preconditioner, the incomplete Poisson preconditioner, for conjugate gradient solvers. We have analyzed the fitness of the proposed preconditioning scheme on several benchmarks and compared its

performance to commonly used methods. We have showed that PIPP performs as well as the current state-of-the-art preconditioners, while being much more amenable to standard thread-level parallelism. Our experiments on two multi-core systems show that PIPP scales very well with the number of available processing cores.

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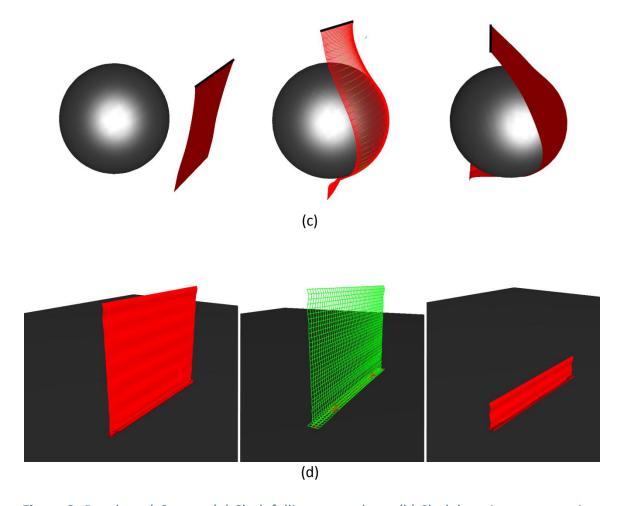
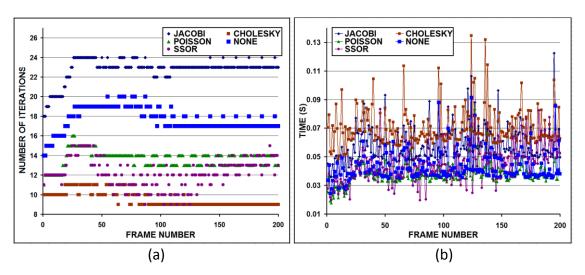


Figure 3: Benchmark Scenes. (a) Cloth falling on a sphere. (b) Cloth hanging as a curtain colliding with sphere. (c) Cloth patch colliding with moving spherical object. (d) Tangling cloth. In the middle frames the red color indicates edges under stress.



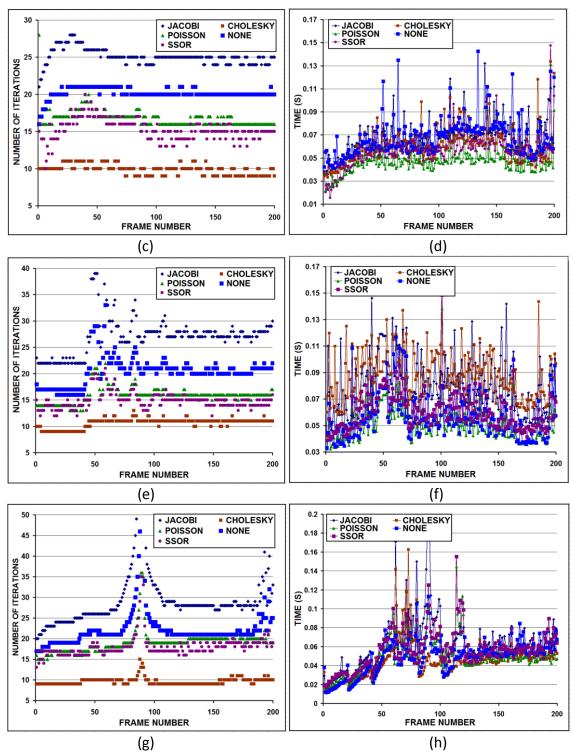


Figure 4: Performance results of different preconditioning schemes on all benchmarks. (a),(b): Number of iterations and simulation time for Free fall benchmark. (c),(d): Curtain benchmark. (e),(f) Tangling benchmark. (g),(h) Moving collider benchmark.

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